

Macroscopic Dark Matter: models and detections

Yang Bai

University of Wisconsin-Madison

On-line “Newton 1665” seminars, May 28, 2020

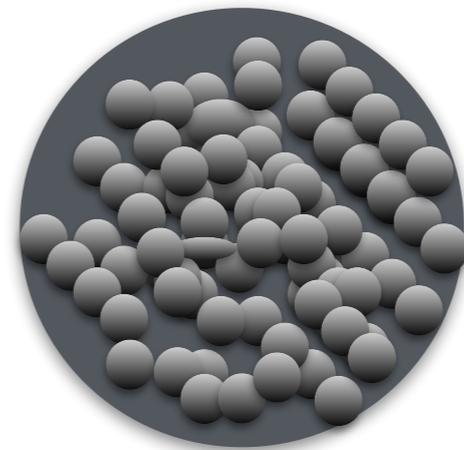
Macroscopic Ordinary Matter

- ❖ For ordinary matter, there are so many different types



Macroscopic Dark Matter (MDM)

- ❖ **Dark matter could be one type of matter made of dark particles**



- ❖ **Macroscopic dark matter is a composite state and may contain many dark matter particles**
- ❖ **Its mass could be much heavier than the Planck mass scale**
- ❖ **Its detections could be dramatically different from ordinary WIMP searches**

Macroscopic Dark Matter

- ❖ **Some recent interests (incomplete):**
 - * **“Big Bang Darkleosynthesis”, Krnjaic and Sigurdson, 1406.1171**
 - * **“Dark Nuclei”, Detmold, McCullough and Pochinsky, 1406.2276**
 - * **“Yukawa Bound States of a Large Number of Fermions”, Wise and Zhang, 1407.4121**
 - * **“Big Bang Synthesis of Nuclear Dark Matter”, Hardy et. al, 1411.3739**
 - * **“Macro Dark Matter”, Jacob, Starkman and Lynn, 1410.2236**
 - * **“Early Universe synthesis of asymmetric dark matter nuggets”, Gresham, Lou and Zurek, 1707.02316**
 - * **“Detecting Dark Blobs”, Grabowska, Melia and Rajendran, 1807.03788**
 - * **“Signatures of Mirror Stars”, Curtin and Setford, 1909.04072**
 - * **“N-MACHOs”, Dvali, Koutsangelas and Kuhnel, 1911.13281**
 - * **“Gravitational microlensing by dark matter in extended structures”, Croon, McKeen and Raj, 2002.08962**

Formations

❖ Non-thermal production

- ✱ parametric resonance: see [Nicholas Orlofsky's talk for dark magnetic monopole, 2005.00503](#)
- ✱ misalignment: QCD axion stars

❖ Thermal production: first-order phase transition

- ✱ Quark nuggets, Dark quark nuggets ([YB, Long, Lu, 1810.04360](#))
- ✱ Non-topological soliton state

a later phase transition produces a bigger object

❖ Late-time coagulation: grow the size of dark matter states

Interactions with SM

- ❖ **Higgs-portal interaction: simple and renormalizable**
 - ✱ interesting interplay with electroweak symmetry breaking
- ❖ **Only gravitational interaction**
 - ✱ similar to primordial black hole (PBH), but with a larger geometric size
- ❖ **Constituents of MDM charged under SM gauge groups (not covered in this talk)**

Higgs-portal Dark Matter

- ❖ The simplest extension of the SM is the Higgs-portal dark matter:

$$\mathcal{L} = \partial_\mu \Phi^\dagger \partial^\mu \Phi + \partial_\mu H^\dagger \partial^\mu H - \lambda_h \left(H^\dagger H - \frac{v^2}{2} \right)^2 - \lambda_{\phi h} \Phi^\dagger \Phi H^\dagger H$$

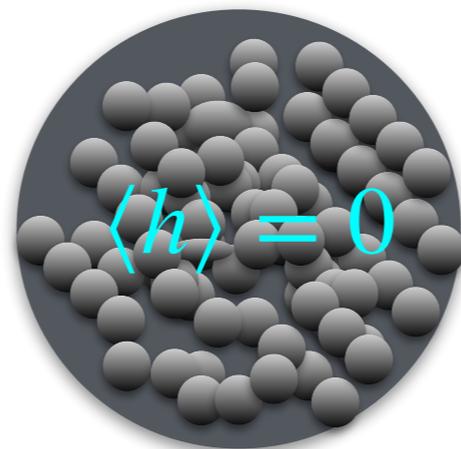
with all dark matter mass from the Higgs VEV: $M_\Phi = \sqrt{\frac{\lambda_{\phi h}}{2}} v$

- ❖ For dark matter as a particle state, there are severe experimental bounds from direct detection experiments
- ❖ There exists a macroscopic dark matter state for this simple model

Non-topological soliton state or Q-ball

Non-topological Soliton

- ❖ For a complex scalar field with an unbroken global symmetry, there exist nondissipative solutions of the classical field equations that are absolute minima of the energy for a fixed (sufficiently large) Q .



$$\langle h \rangle = v$$

the vacuum pressure is balanced by the quantum or self-interaction-generated pressure

Equations of Motion

$$\mathcal{L} = \partial_\mu \Phi^\dagger \partial^\mu \Phi + \partial_\mu H^\dagger \partial^\mu H - \lambda_h \left(H^\dagger H - \frac{v^2}{2} \right)^2 - \lambda_{\phi h} \Phi^\dagger \Phi H^\dagger H$$

- ❖ **The classical equations of motion** $\Phi(x_\mu) = e^{i\omega t} \phi(r) / \sqrt{2}$ $H(x_\mu) = h(r) / \sqrt{2}$

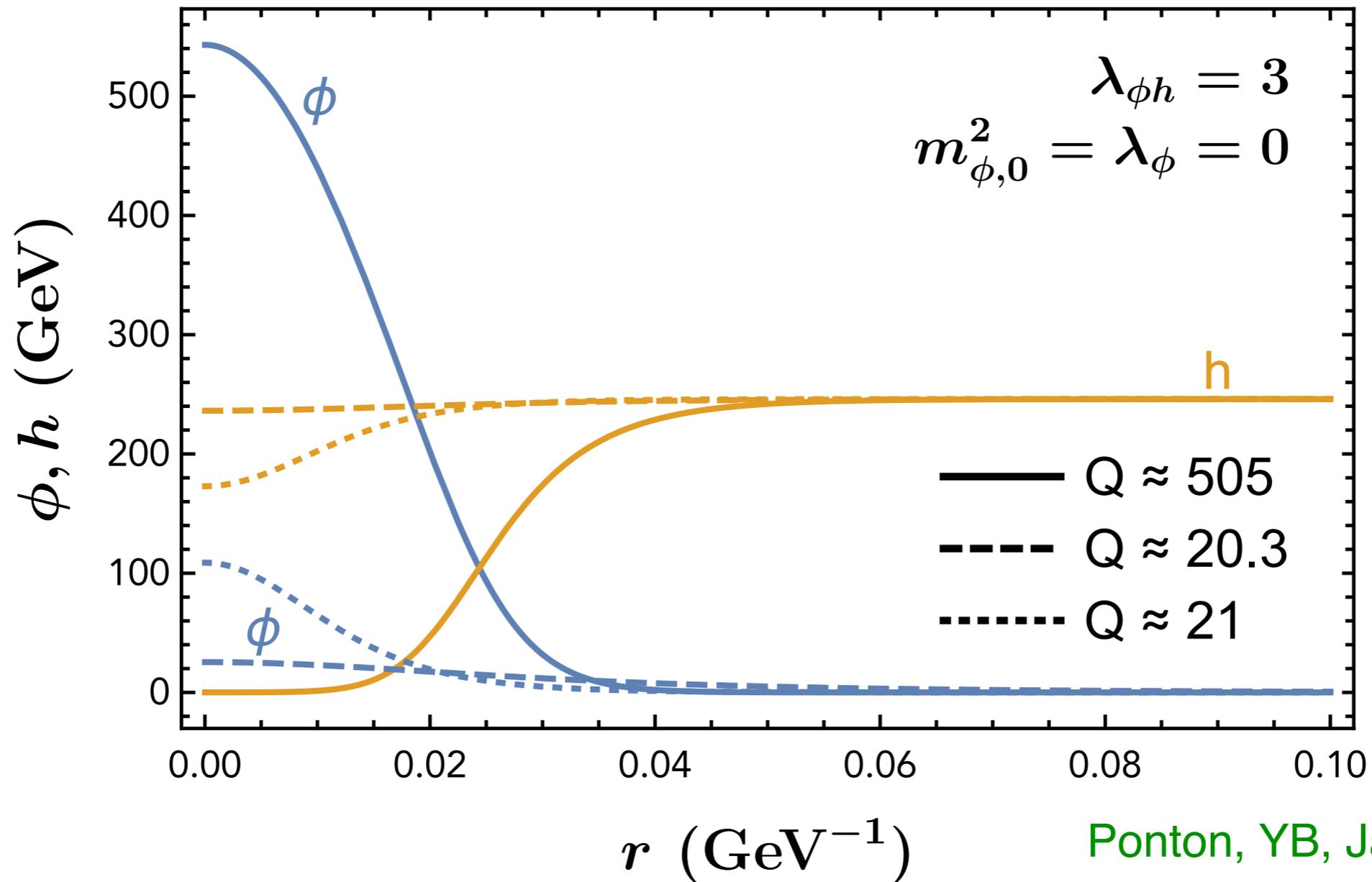
$$\phi''(r) + \frac{2}{r} \phi'(r) + \left[\omega^2 - \frac{1}{2} \lambda_{\phi h} h(r)^2 \right] \phi(r) = 0,$$

$$h''(r) + \frac{2}{r} h'(r) + \left[\frac{m_h^2}{2} - \lambda_h h(r)^2 - \frac{1}{2} \lambda_{\phi h} \phi(r)^2 \right] h(r) = 0,$$

- ❖ **Four boundary conditions:** $\phi'(0) = h'(0) = 0$ $\phi(\infty) = 0$ $h(\infty) = v$

- ❖ **Need to double-shooting on $\phi(0)$ and $h(0)$ for a fixed value of ω**

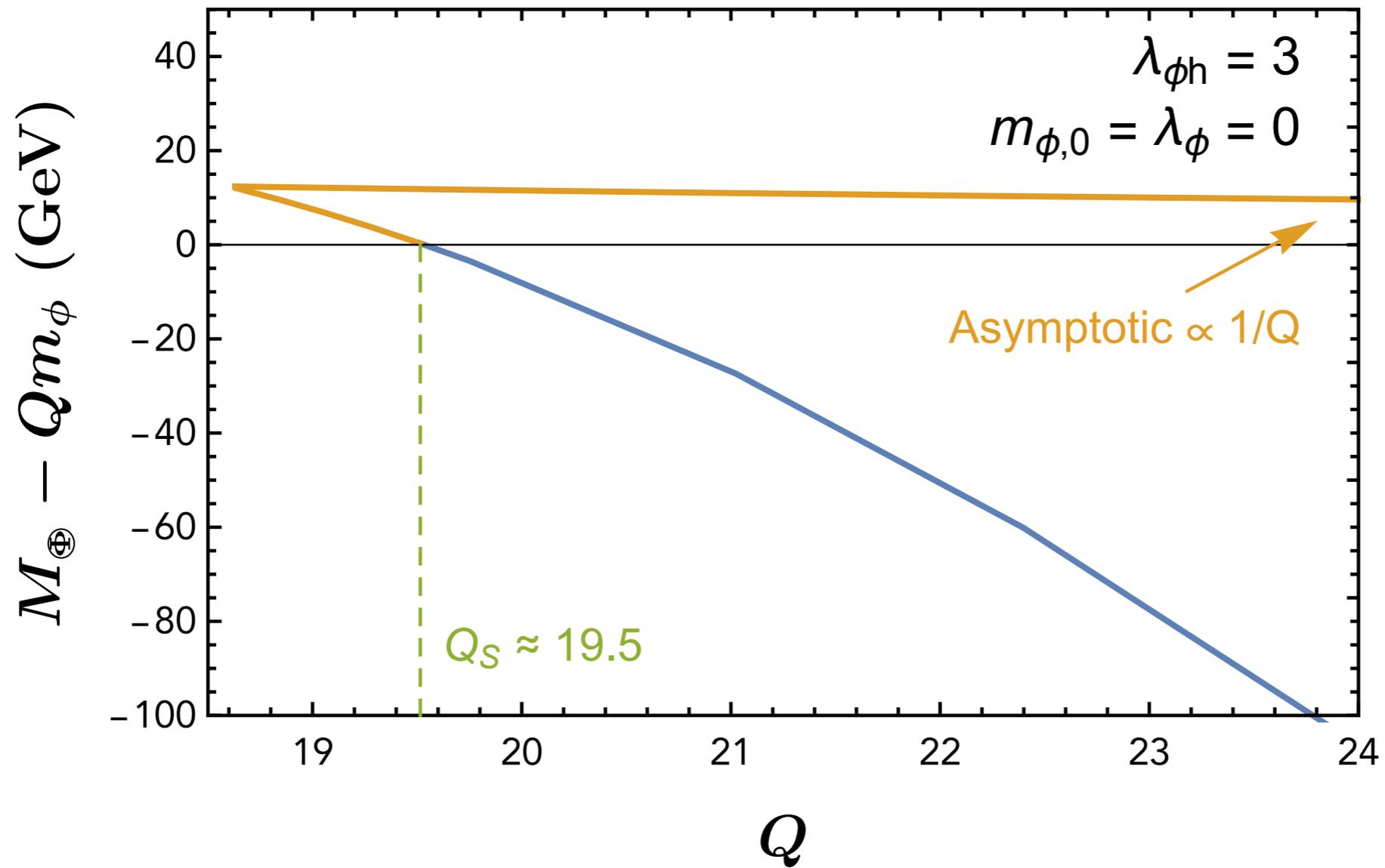
Example Solutions ($\lambda_\phi = 0$)



Ponton, YB, Jain, 1906.10739

for a large Q : Electroweak Symmetric Dark Matter Ball

Dark Matter Ball Mass vs. Q



❖ In the large Q limit, one has a simple relation

$$Q \sim R_{\oplus}^4, \quad M_{\oplus} \sim Q^{3/4} \sim R_{\oplus}^3$$

Add Φ Self-Interaction

$$\mathcal{L} = \partial_\mu \Phi^\dagger \partial^\mu \Phi + \partial_\mu H^\dagger \partial^\mu H - \lambda_h \left(H^\dagger H - \frac{v^2}{2} \right)^2 - \lambda_{\phi h} \Phi^\dagger \Phi H^\dagger H - m_{\phi,0}^2 \Phi^\dagger \Phi - \lambda_\phi (\Phi^\dagger \Phi)^2$$

- ❖ **The existence of the self-quartic interaction changes the dark matter ball properties significantly**

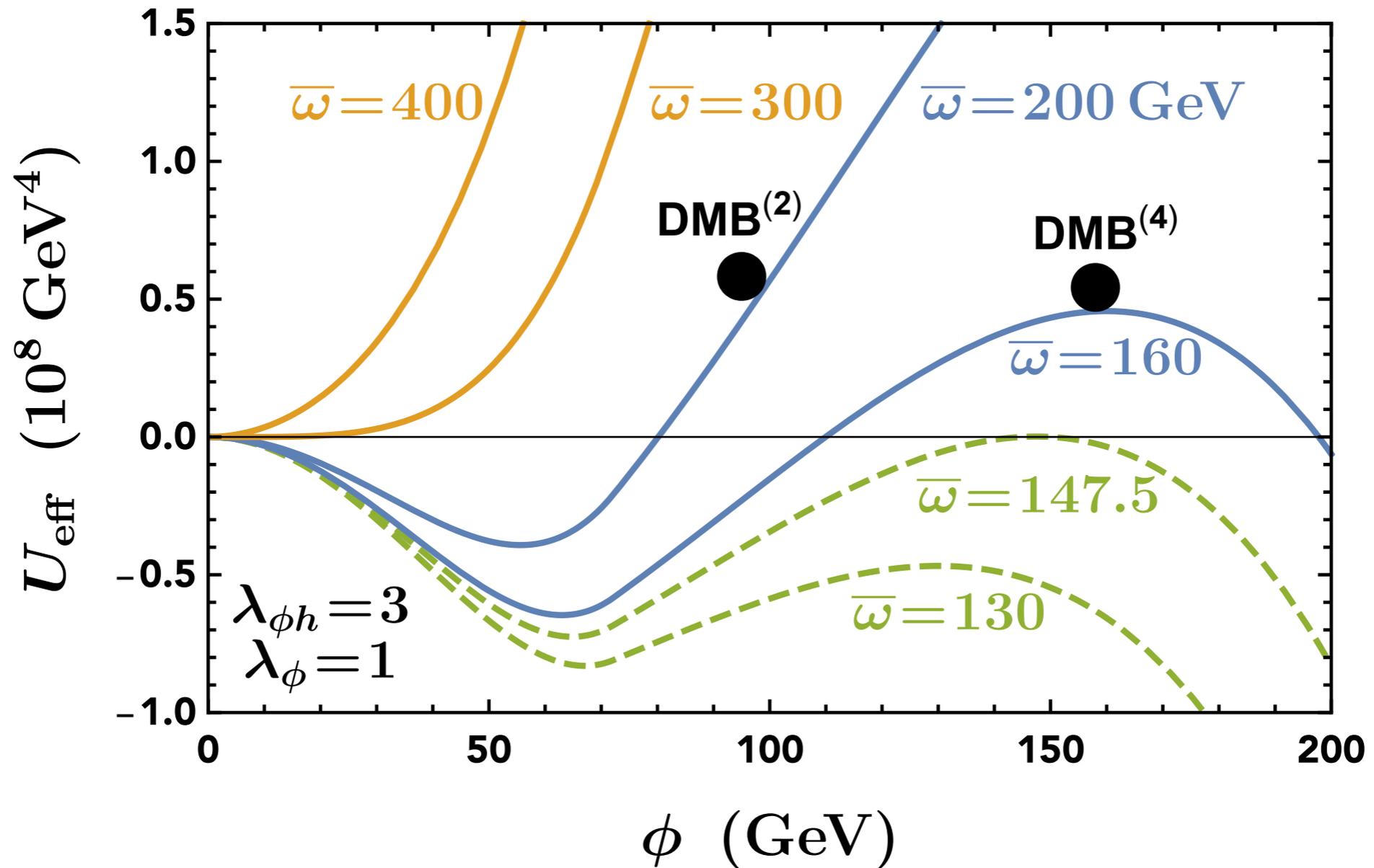
$$h^2 \approx \begin{cases} \frac{m_h^2}{2\lambda_h} - \frac{\lambda_{\phi h}}{2\lambda_h} \phi^2 & \text{for } \lambda_{\phi h} \phi^2 < m_h^2, \\ 0 & \text{for } \lambda_{\phi h} \phi^2 > m_h^2. \end{cases}$$

$$U_{\text{eff}}(\phi) = -V_\Phi(\phi) + \begin{cases} \frac{1}{2} \left(\omega^2 - \frac{\lambda_{\phi h} m_h^2}{4\lambda_h} \right) \phi^2 + \frac{\lambda_{\phi h}^2}{16\lambda_h} \phi^4 & \text{for } \lambda_{\phi h} \phi^2 < m_h^2, \\ \frac{1}{2} \omega^2 \phi^2 - \frac{m_h^4}{16\lambda_h} & \text{for } \lambda_{\phi h} \phi^2 > m_h^2. \end{cases}$$

$$\phi'' + \frac{2}{r} \phi' + U'_{\text{eff}}(\phi) \approx 0$$

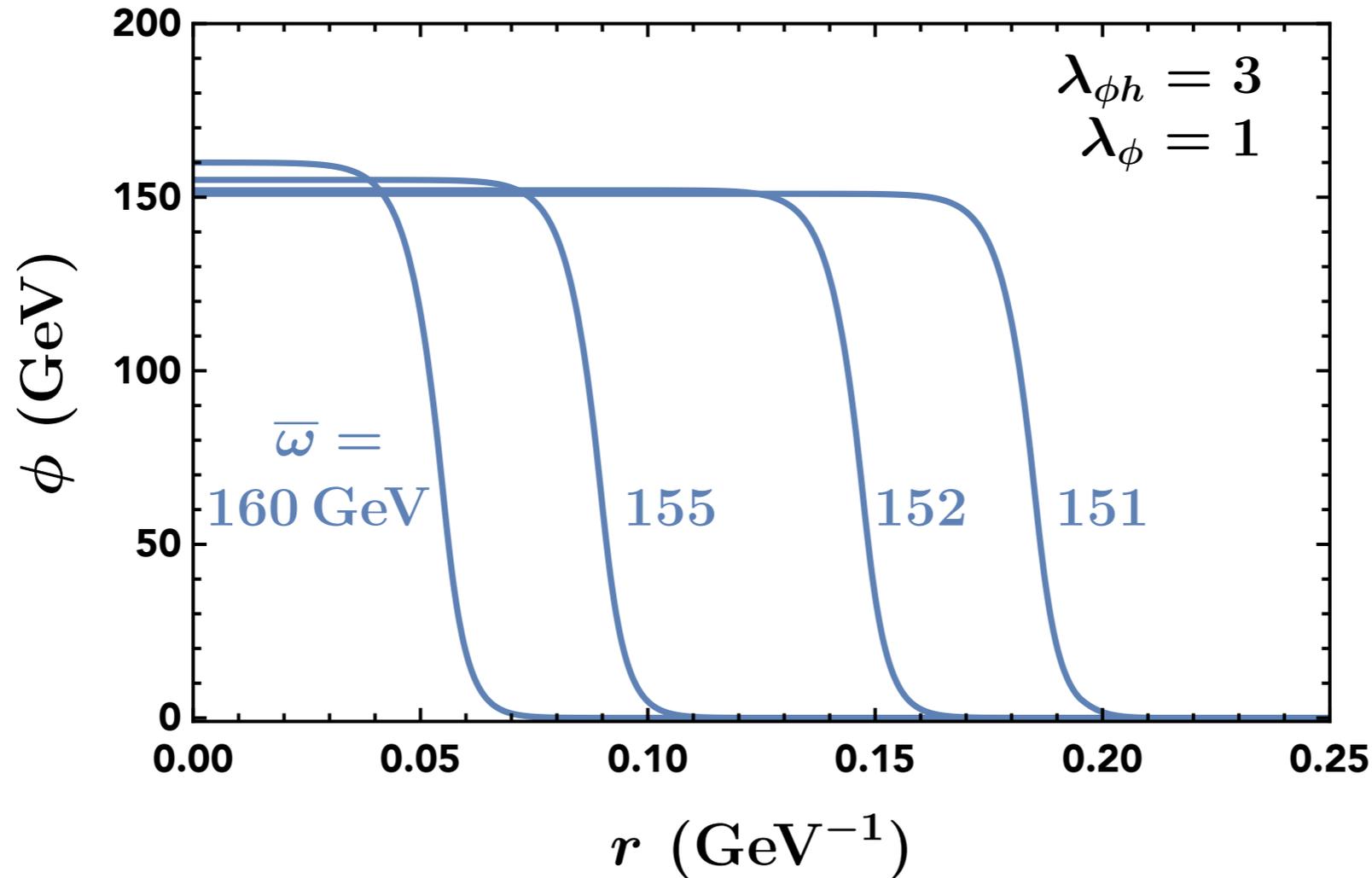
- ❖ **Via Coleman, we can use 1D particle description to understand it**

Add Φ Self-Interaction



$$\bar{\omega}^2 = \omega^2 - m_{\phi,0}^2 \qquad \bar{\omega}_c = \left(\frac{\lambda_{\phi}}{4\lambda_h} \right)^{1/4} m_h$$

Add Φ Self-Interaction



❖ As a $\bar{\omega} \rightarrow \bar{\omega}_c$, the radius increases as $R \approx \frac{0.66}{\bar{\omega} - \bar{\omega}_c}$

$$Q \sim R_{\oplus}^3, \quad M_{\oplus} \sim Q \sim R_{\oplus}^3 \quad \rho = \frac{M_{\oplus}}{(4\pi/3)R_{\oplus}^3} \sim (100 \text{ GeV})^4$$

Two Types of BEC

- ❖ When the Φ self-interaction is not important ($\lambda_\phi \ll 1$), the **core density could be arbitrarily high (BEC)**

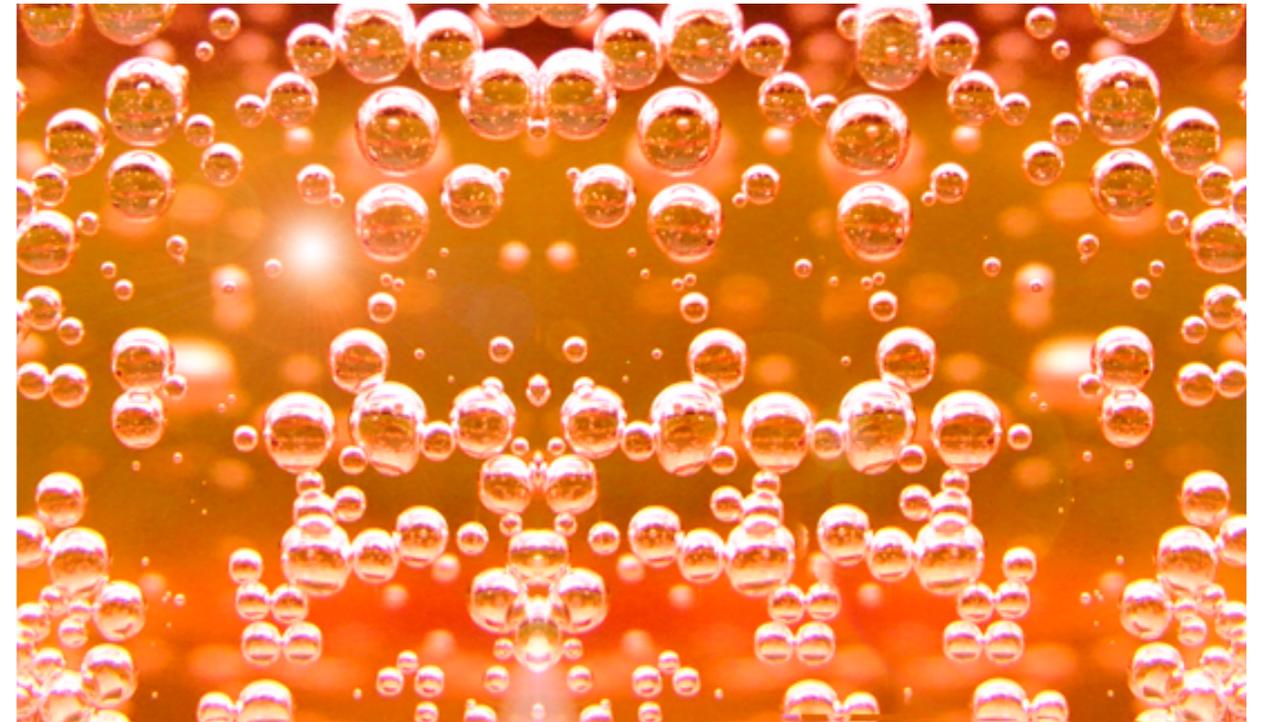
$$Q \sim R_\oplus^4, \quad M_\oplus \sim Q^{3/4} \sim R_\oplus^3$$

- ❖ When the Φ self-interaction is important ($\lambda_\phi \sim 1$), the **energy density is flat** in the inner region

$$Q \sim R_\oplus^3, \quad M_\oplus \sim Q \sim R_\oplus^3$$

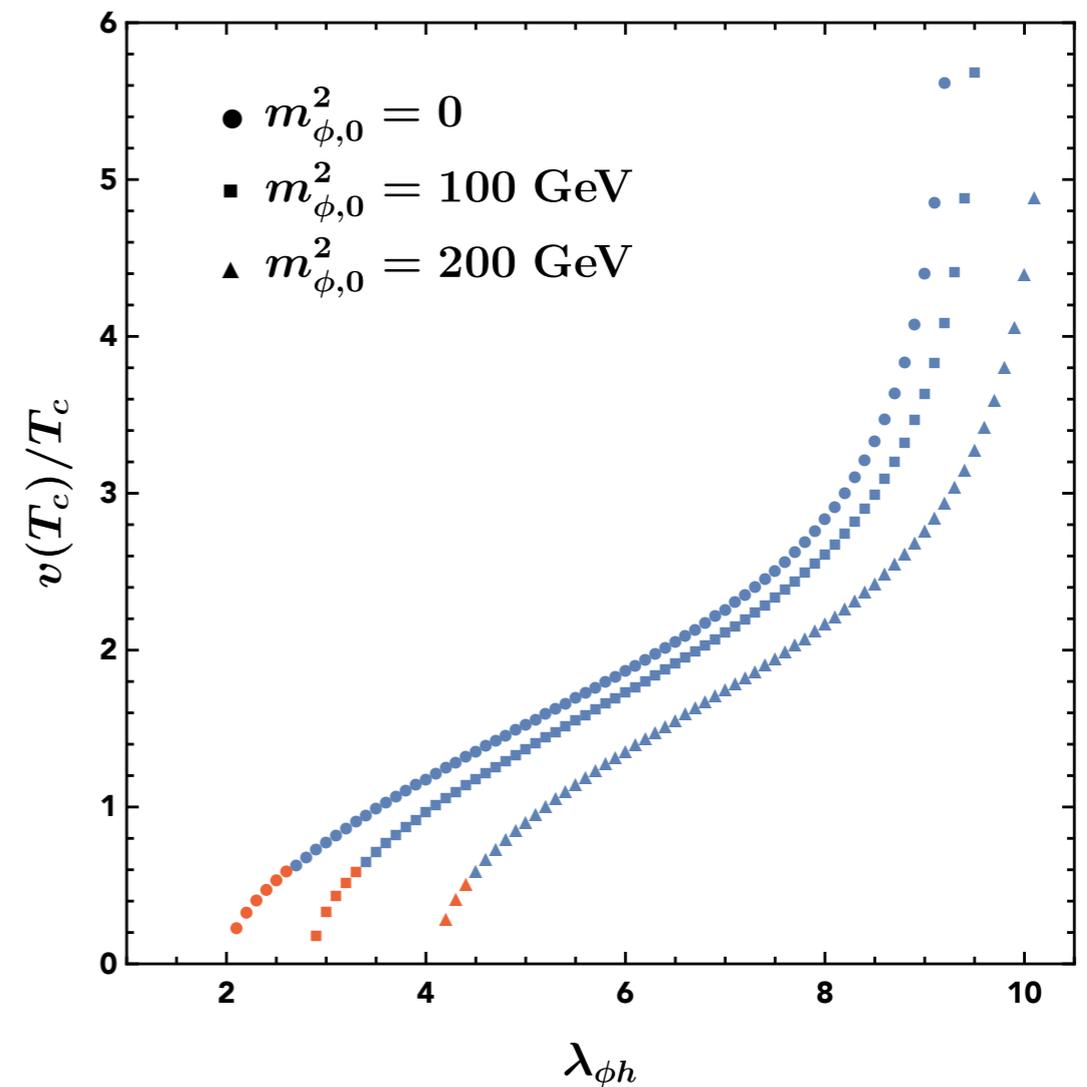
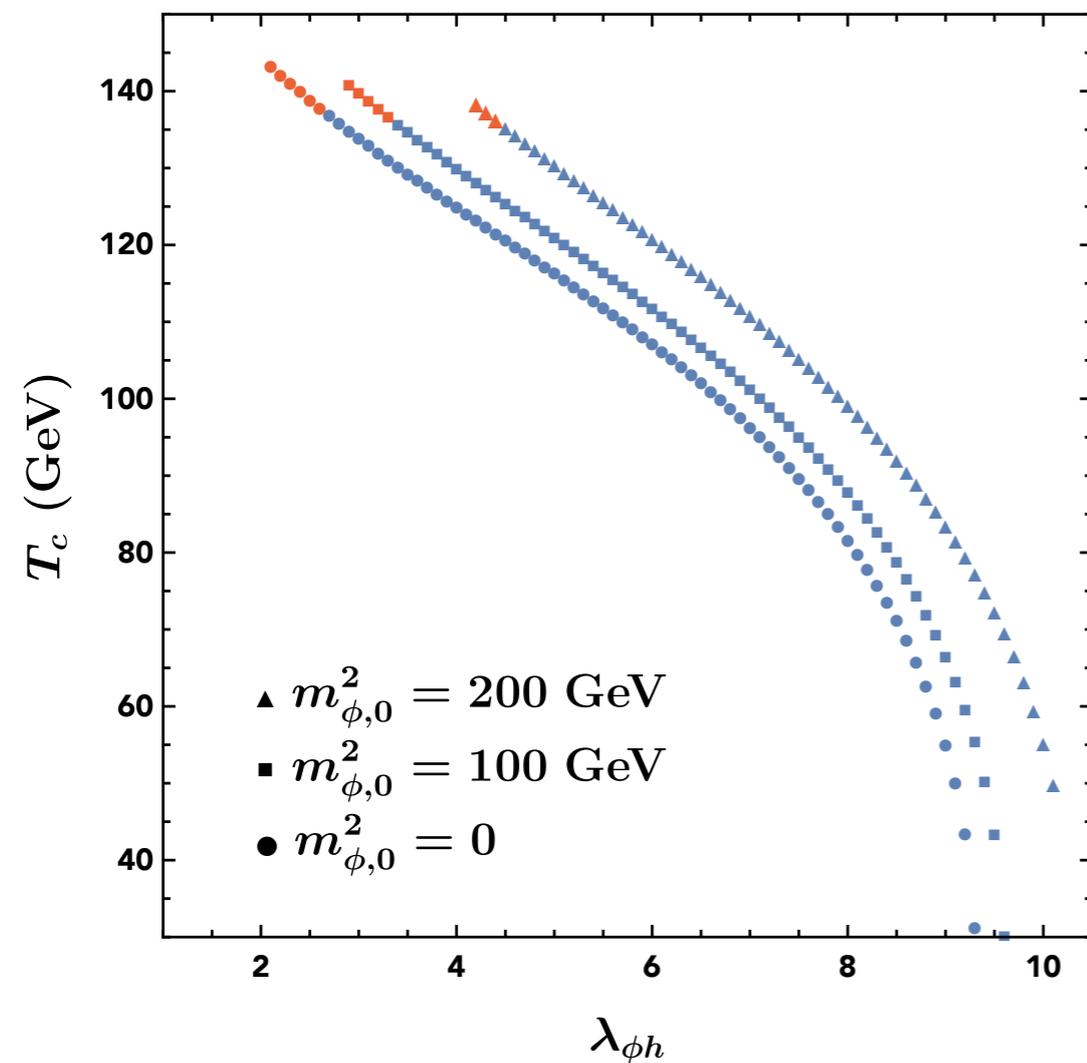
- ❖ Both of them have $\rho^{1/4} \sim v_{\text{EW}}$ and **unbroken electroweak symmetry** in the inner region

Formation from First-Order Phase Transition



Formation from 1'st Phase Transition

- ❖ It is known that the Higgs-portal dark matter can also trigger strong first-order phase transition



Abundance of Dark Matter Balls

- ❖ Use **initial DM number asymmetry** Y_Φ to match DM abundance
- ❖ **The total number of dark matter within one Hubble patch is**

$$N_\Phi^{\text{Hubble}} \approx Y_\Phi s d_H^3 \simeq (7.8 \times 10^{37}) \left(\frac{Y_\Phi}{10^{-11}} \right) \left(\frac{134 \text{ GeV}}{T_c} \right)^3$$

- ❖ **The number of nucleation sites within one Hubble volume has**

$$N_{\text{DMB}}^{\text{Hubble}} \sim 1.0 \times 10^{13} \times \left(\frac{\lambda_{\phi h}}{3} \right)^{-14}$$

$$Q \sim (7.8 \times 10^{24}) \left(\frac{Y_\Phi}{10^{-11}} \right) \left(\frac{134 \text{ GeV}}{T_c} \right)^3 \left(\frac{\lambda_{\phi h}}{3} \right)^{14}$$

$$M_\oplus \sim (3.9 \times 10^{26} \text{ GeV}) \left(\frac{\omega_c Y_\Phi}{5 \times 10^{-10} \text{ GeV}} \right) \left(\frac{134 \text{ GeV}}{T_c} \right)^3 \left(\frac{\lambda_{\phi h}}{3} \right)^{14} \quad 10^{26} \text{ GeV} \sim 100 \text{ g}$$

$$R_\oplus \approx (5.8 \times 10^5 \text{ GeV}^{-1}) \left(\frac{\lambda_\phi}{0.013} \right)^{1/12} \left(\frac{Y_\Phi}{10^{-11}} \right)^{1/3} \left(\frac{134 \text{ GeV}}{T_c} \right) \left(\frac{\lambda_{\phi h}}{3} \right)^{4.7} \quad 10^5 \text{ GeV}^{-1} \sim \text{\AA}$$

Direct Detection

- ❖ The masses of dark matter balls are heavy, above the Planck mass. So, its flux is small. One needs a **large volume detector** to search for it.

$$1 \sim \frac{\rho_{\text{DM}}}{m_{\text{DM}}} v A_{\text{det}} t_{\text{exp}} \sim \frac{10^{21} \text{ GeV}}{m_{\text{DM}}} \frac{A_{\text{det}}}{5 \times 10^5 \text{ cm}^2} \frac{t_{\text{exp}}}{10 \text{ yr}}$$

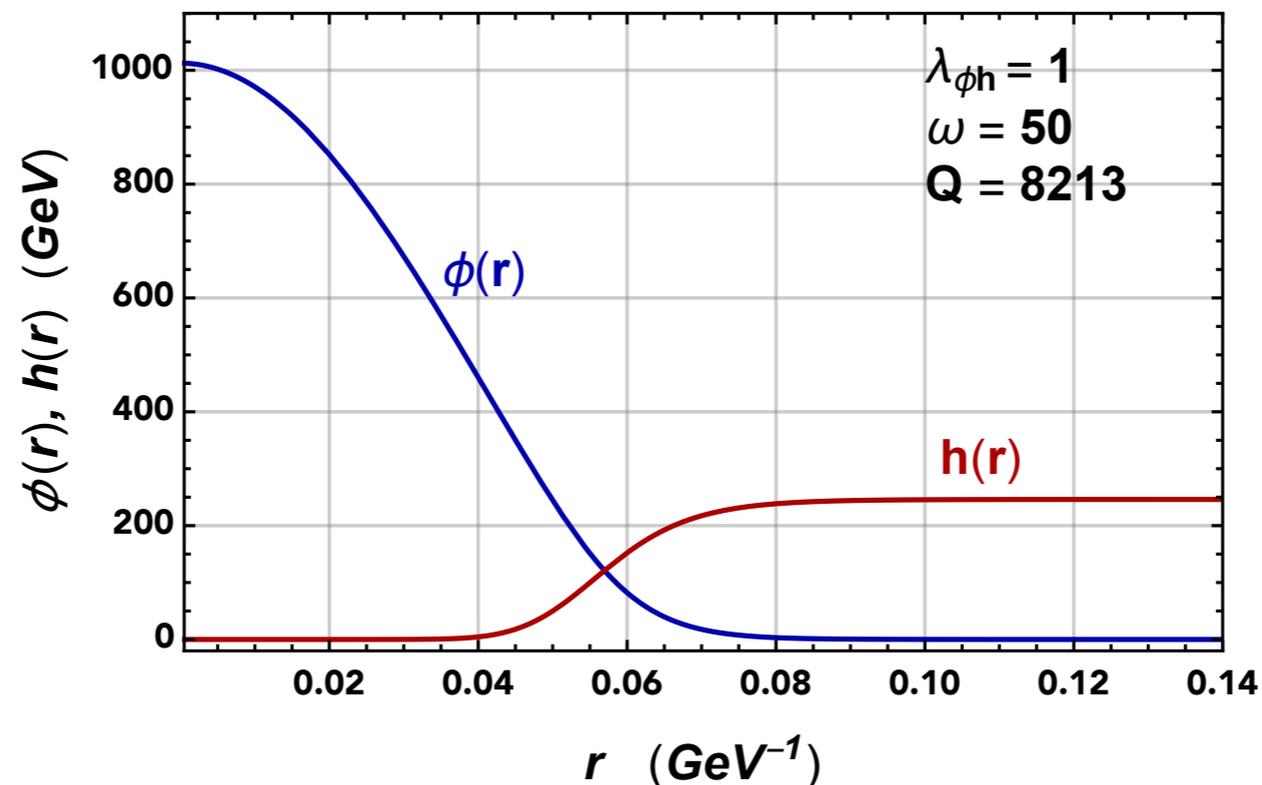
- ❖ Because the cross section is large, it may have **multiple scattering** with the material in a detector

$$\Gamma = n_A \sigma_{\text{DM-ball}} \bar{v}_{\text{rel}}$$

$$E_{\text{sum}} \sim \Gamma \times t_{\text{select}} \times \langle E_R \rangle \times \kappa \sim N_{\text{scattering}} \times 10 \text{ keV} \times \kappa$$

Direct Detection of EWS-DMB

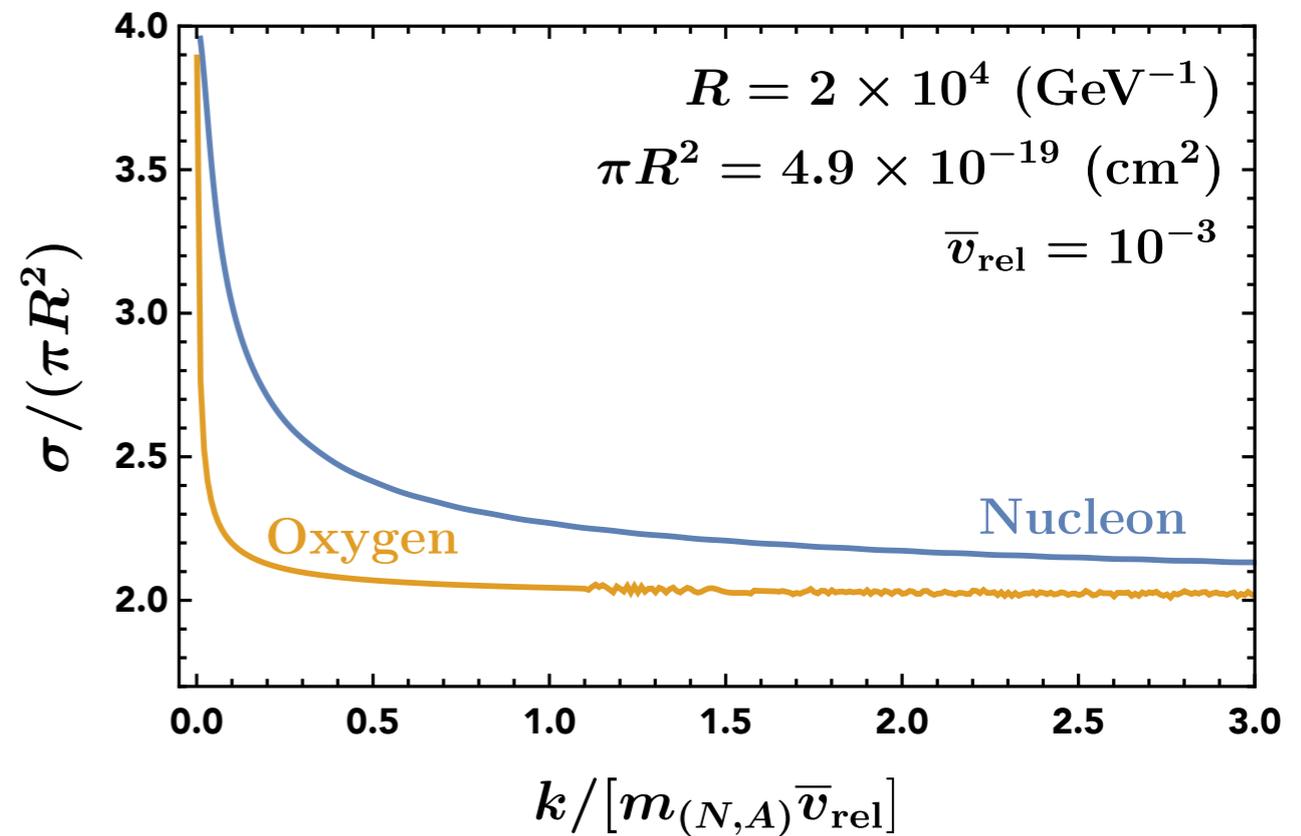
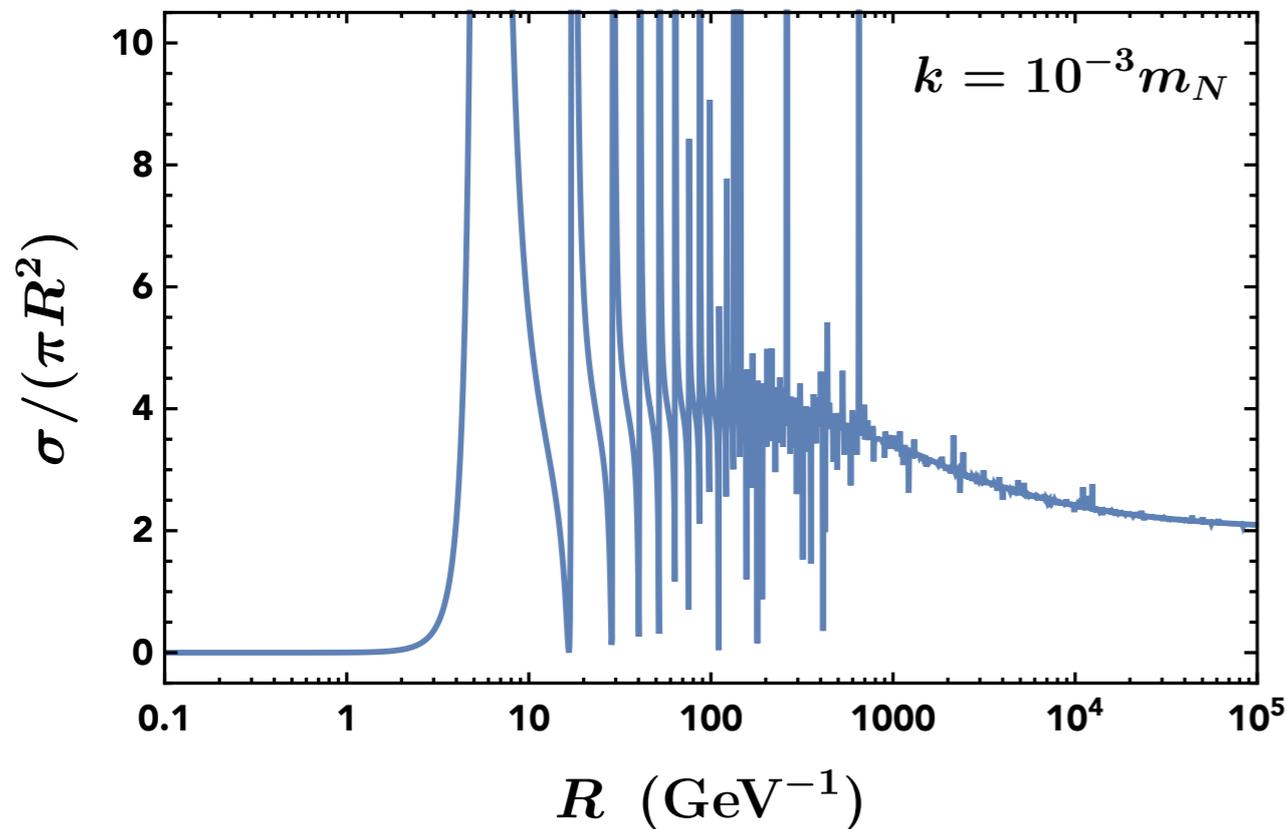
- ❖ The energy density of electroweak symmetric dark matter ball has $\rho \sim (100 \text{ GeV})^4$, and very dense



- ❖ When SM particle (nucleon) scattering off the DMB, it will feel a different mass from the zero Higgs VEV inside DMB

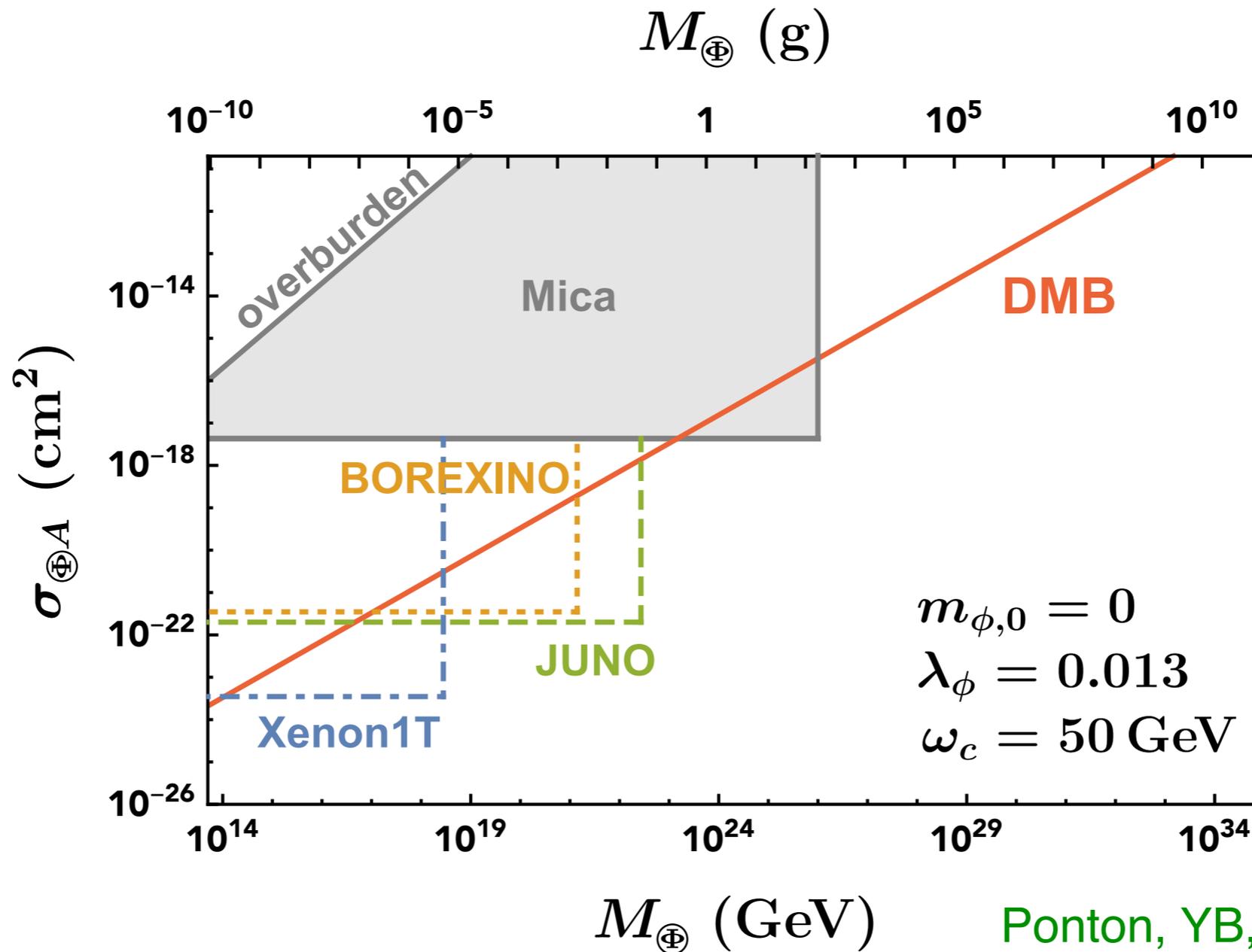
$$\mathcal{L} \supset -m_N \bar{N}N - y_{hNN}(h - v) \bar{N}N \quad y_{hNN} \approx 0.0011$$

Scattering Cross Sections



- ❖ **The cross sections change from a hard sphere $4\pi R^2$ to $2\pi R^2$**
- ❖ **They are insensitive to the target nucleon or nucleus masses**

Direct Detection



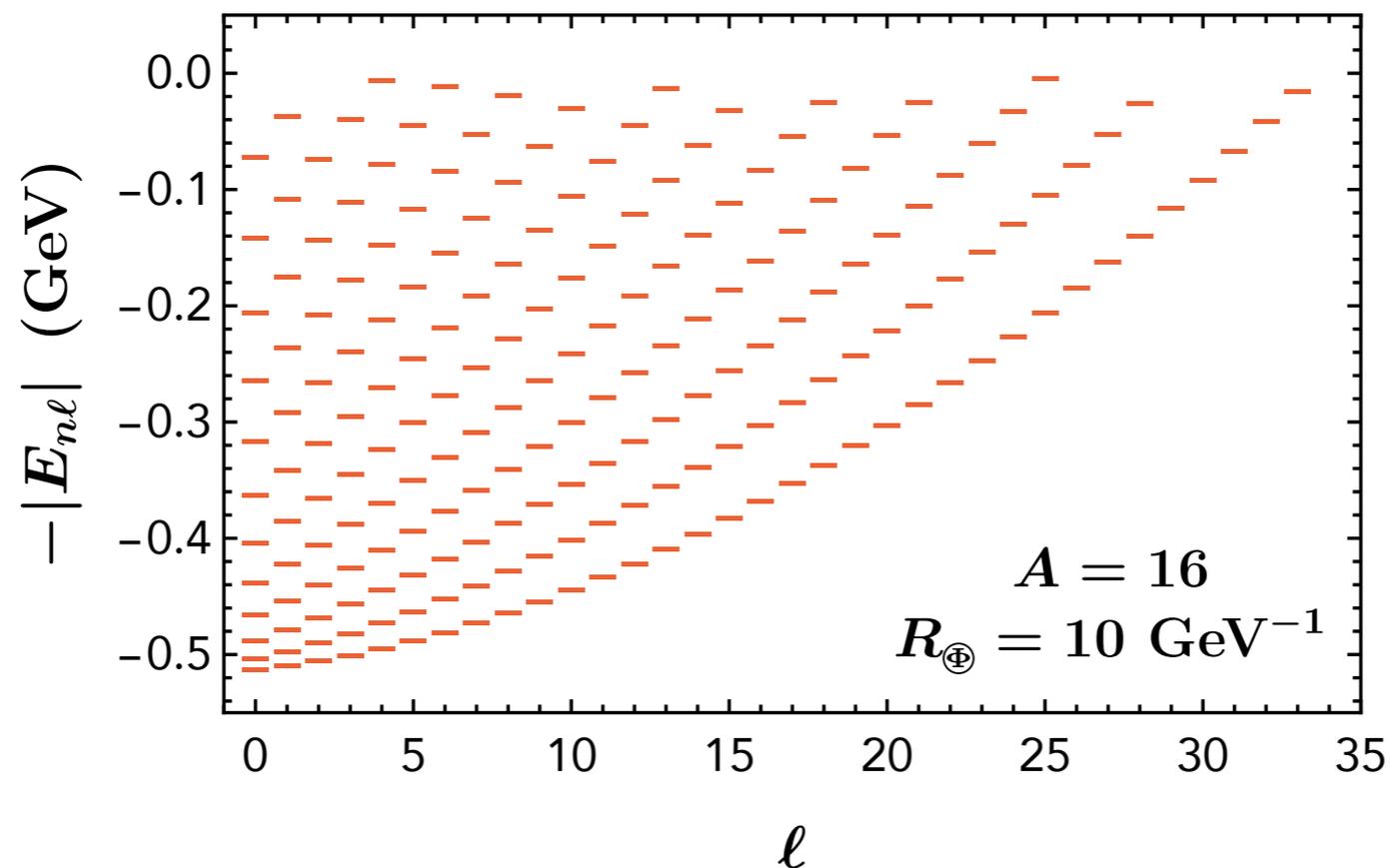
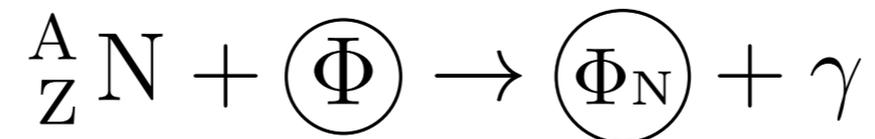
Ponton, YB, Jain, 1906.10739

- ❖ Experiments with an energy threshold lower than ~ 1 MeV have chance to detect elastic scattering of DMB

see also Bramante, et.al., 1812.09325

Radiative Capture of Nucleus by Dark Matter

- ❖ Just like hydrogen formation from electron and proton



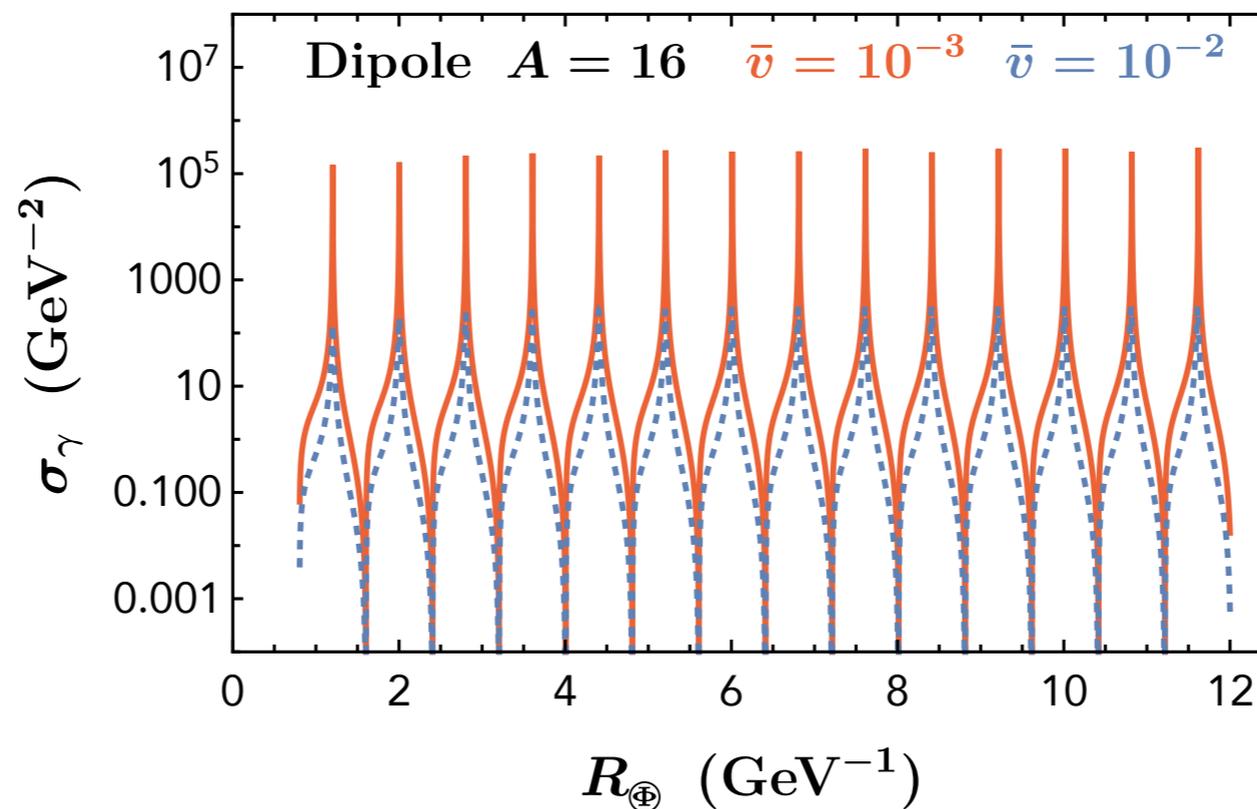
- ❖ Except that one needs to go beyond the dipole approximation

Radiative Capture Cross Section

$$\mathcal{M}_{nlm} = \frac{1}{2\mu} Z e \boldsymbol{\epsilon}^* \cdot \int d^3x e^{-i\mathbf{q}\cdot\mathbf{x}} [\nabla \psi_{nlm}^*(\mathbf{x}) \psi_{\mathbf{k}}(\mathbf{x}) - \psi_{nlm}^*(\mathbf{x}) \nabla \psi_{\mathbf{k}}(\mathbf{x})]$$

$$\sigma_{\gamma,nl} = \frac{1}{v} \int d\Omega \frac{|E_{nl}|}{8\pi^2} \sum_m |\mathcal{M}_{nlm}|^2$$

❖ **Dipole limit:** $qR_{\oplus} \ll 1$

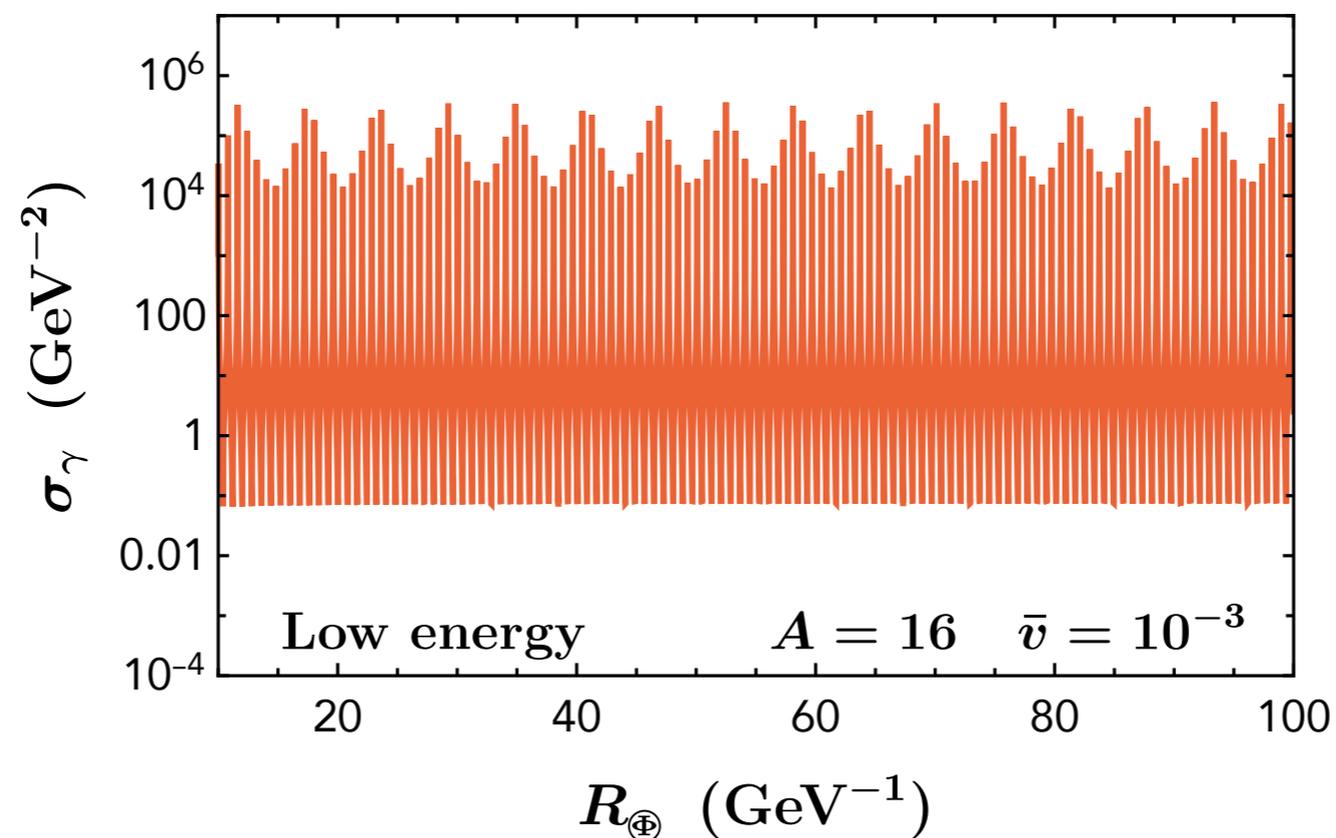


Radiative Capture Cross Section

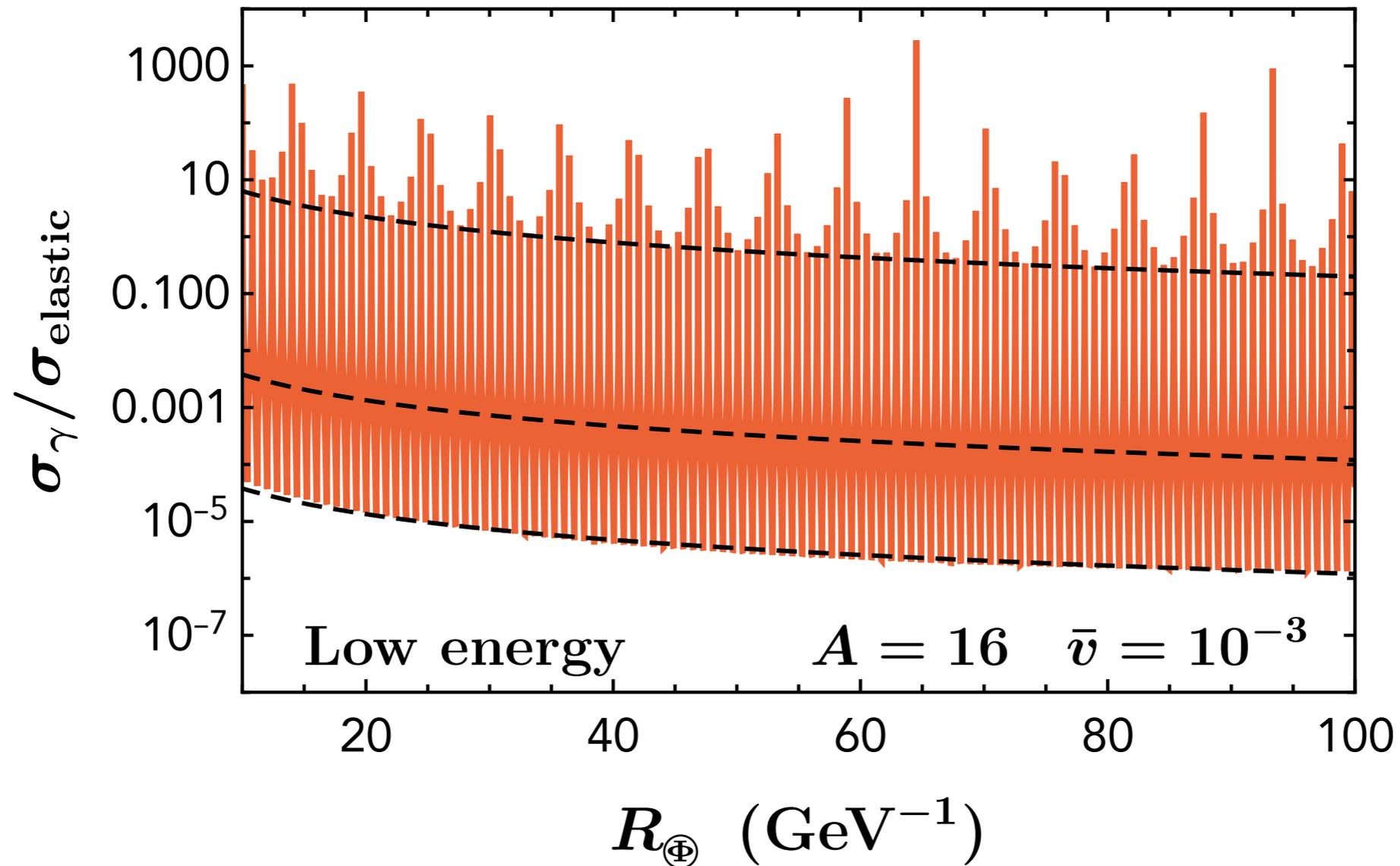
$$\mathcal{M}_{nlm} = \frac{1}{2\mu} Z e \boldsymbol{\epsilon}^* \cdot \int d^3x e^{-i\mathbf{q}\cdot\mathbf{x}} [\nabla \psi_{nlm}^*(\mathbf{x}) \psi_{\mathbf{k}}(\mathbf{x}) - \psi_{nlm}^*(\mathbf{x}) \nabla \psi_{\mathbf{k}}(\mathbf{x})]$$

$$\sigma_{\gamma,nl} = \frac{1}{v} \int d\Omega \frac{|E_{nl}|}{8\pi^2} \sum_m |\mathcal{M}_{nlm}|^2$$

❖ **Lower-energy limit:** $kR_{\oplus} \ll 1$

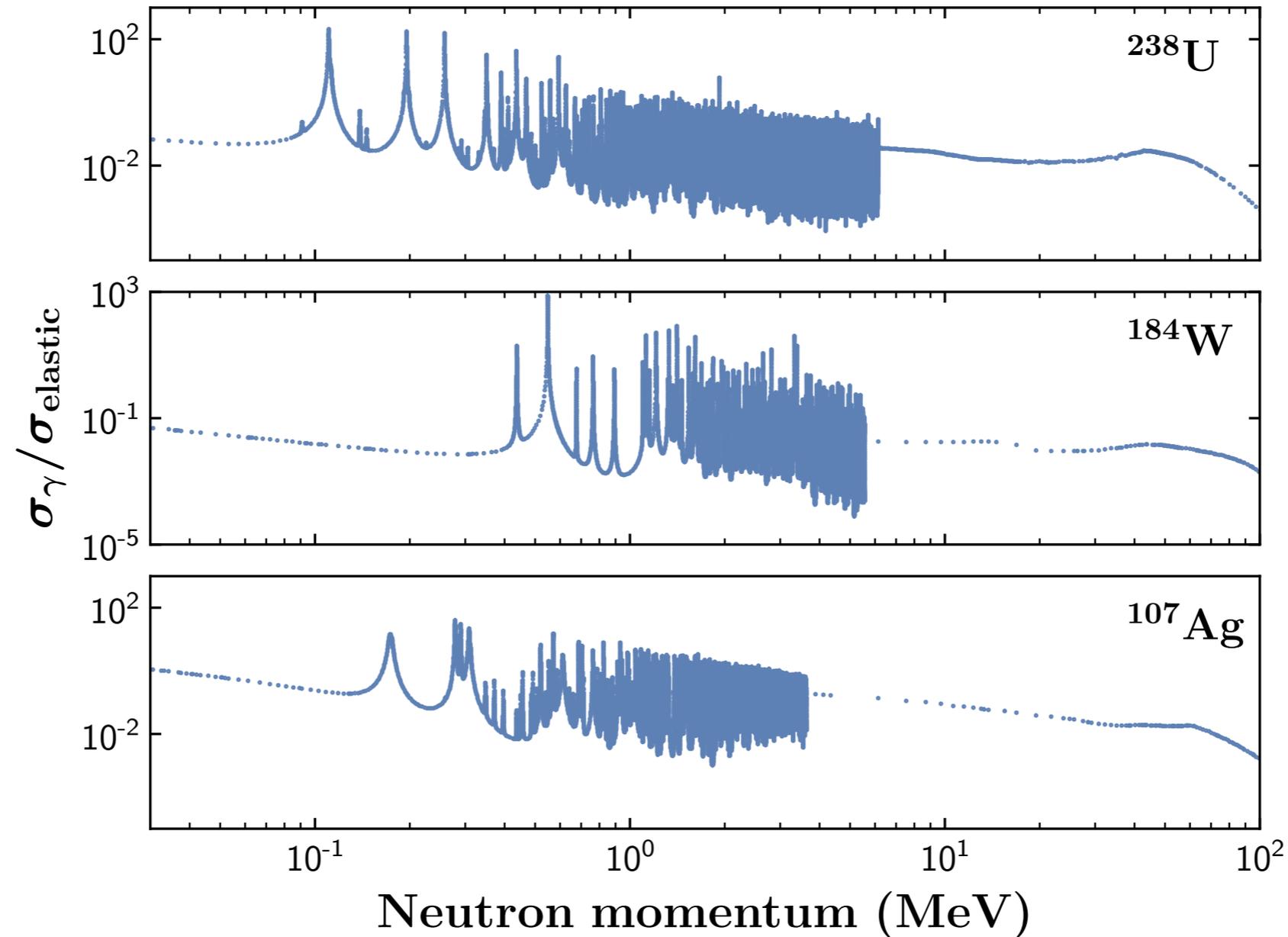


Radiative Capture Cross Section



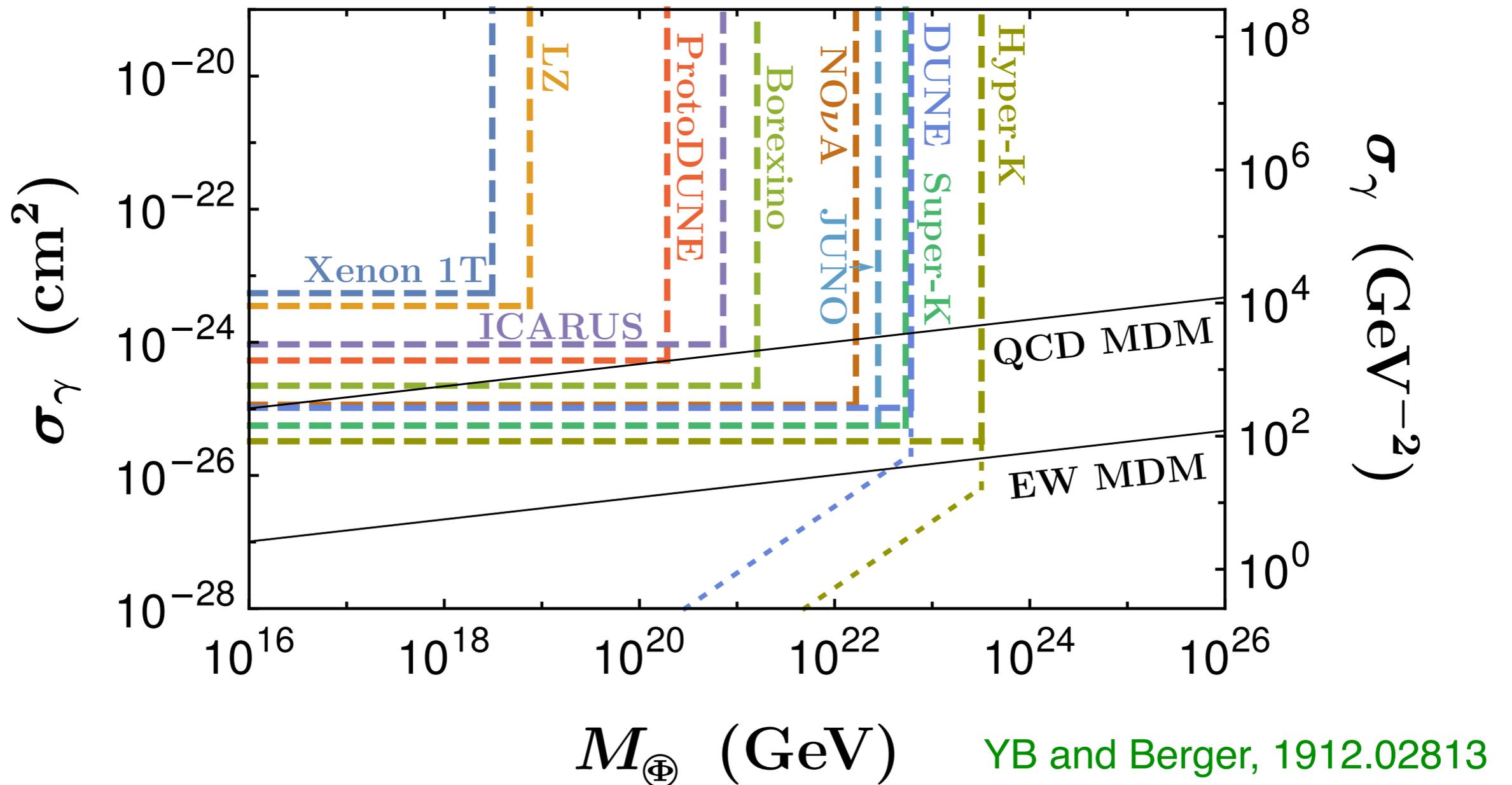
YB and Berger, 1912.02813

Radiative Capture Cross Section



- ❖ Obtain the similar behaviors as neutron capture by a large nucleus

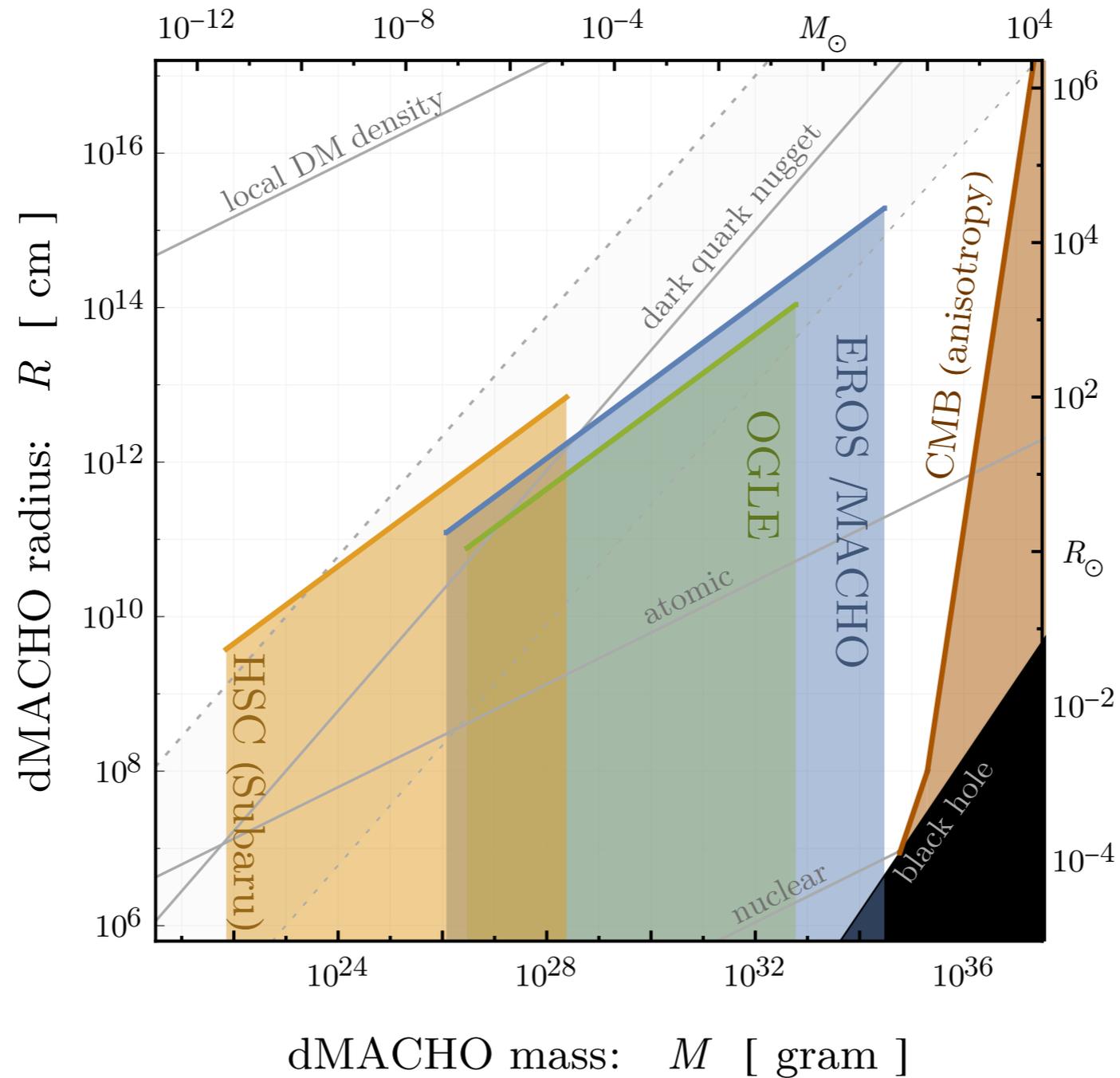
Detection Sensitivity



- ❖ Working in progress with experimentalists to apply the actual data to search for MDM

Only Gravitational Interaction

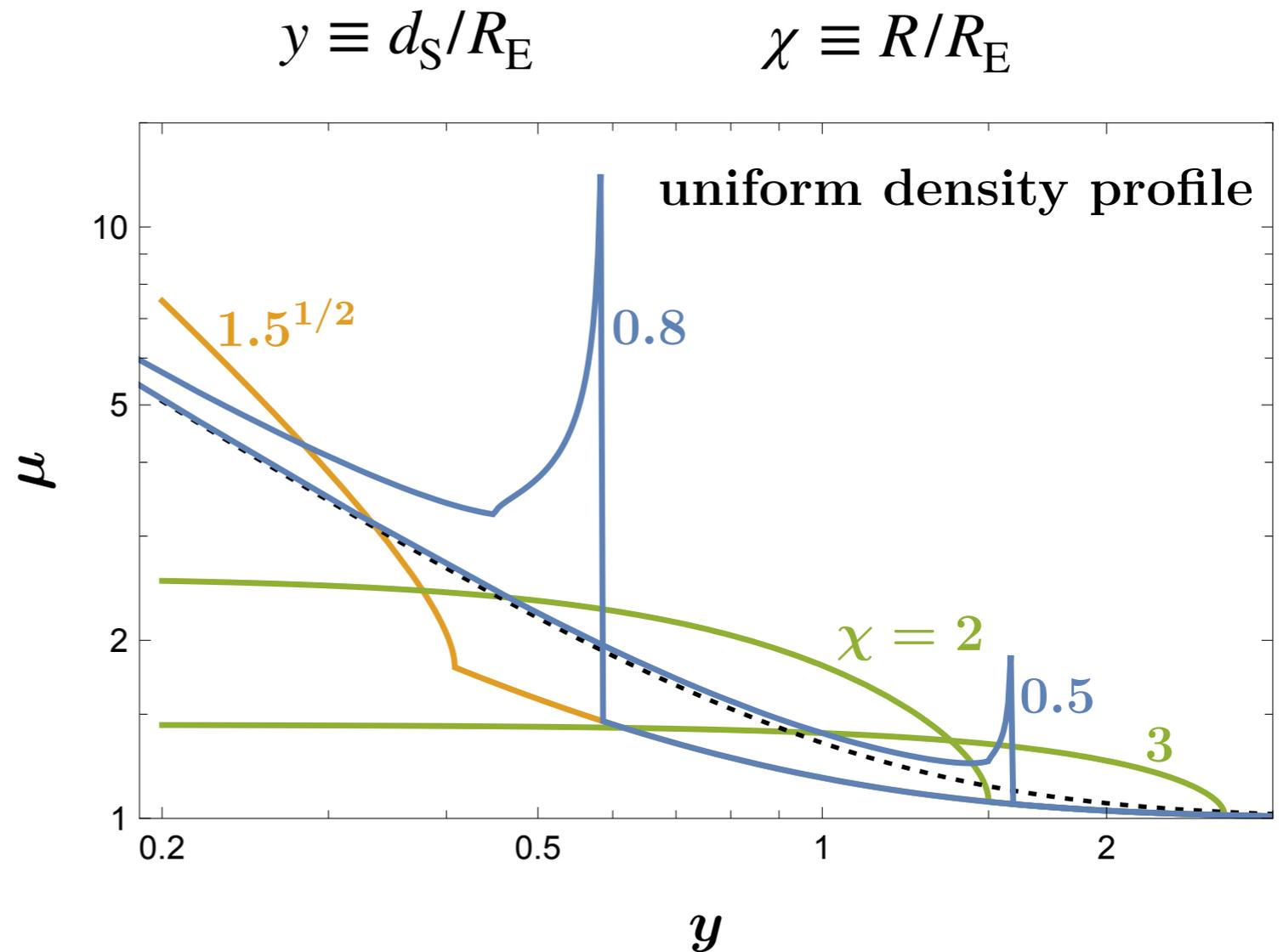
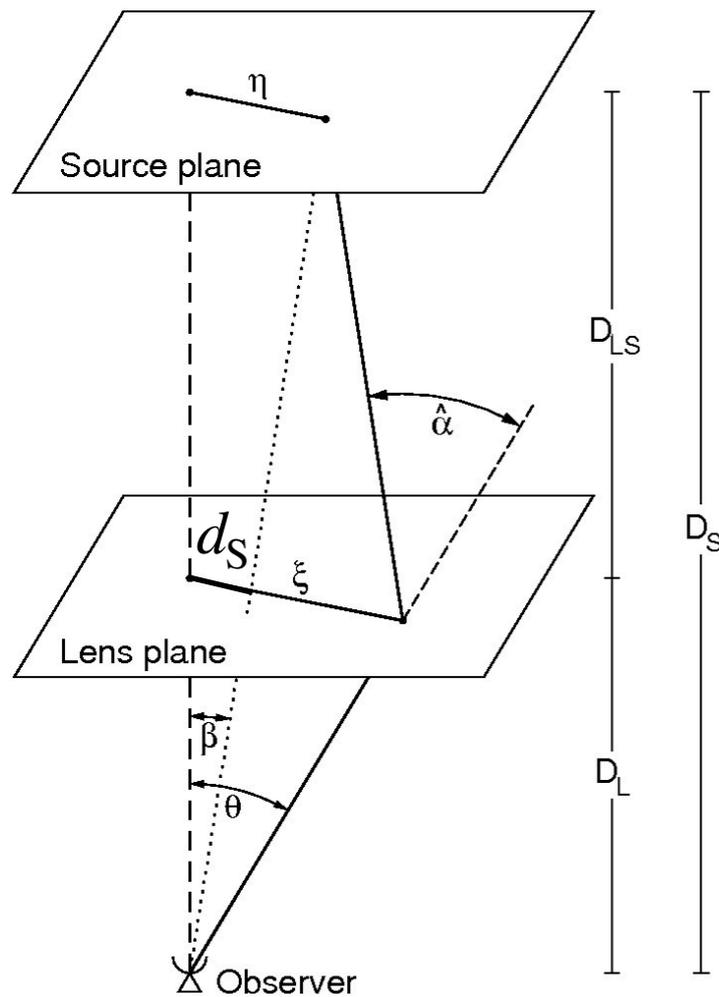
- ❖ Phenomenological model parameter space at a heavy mass



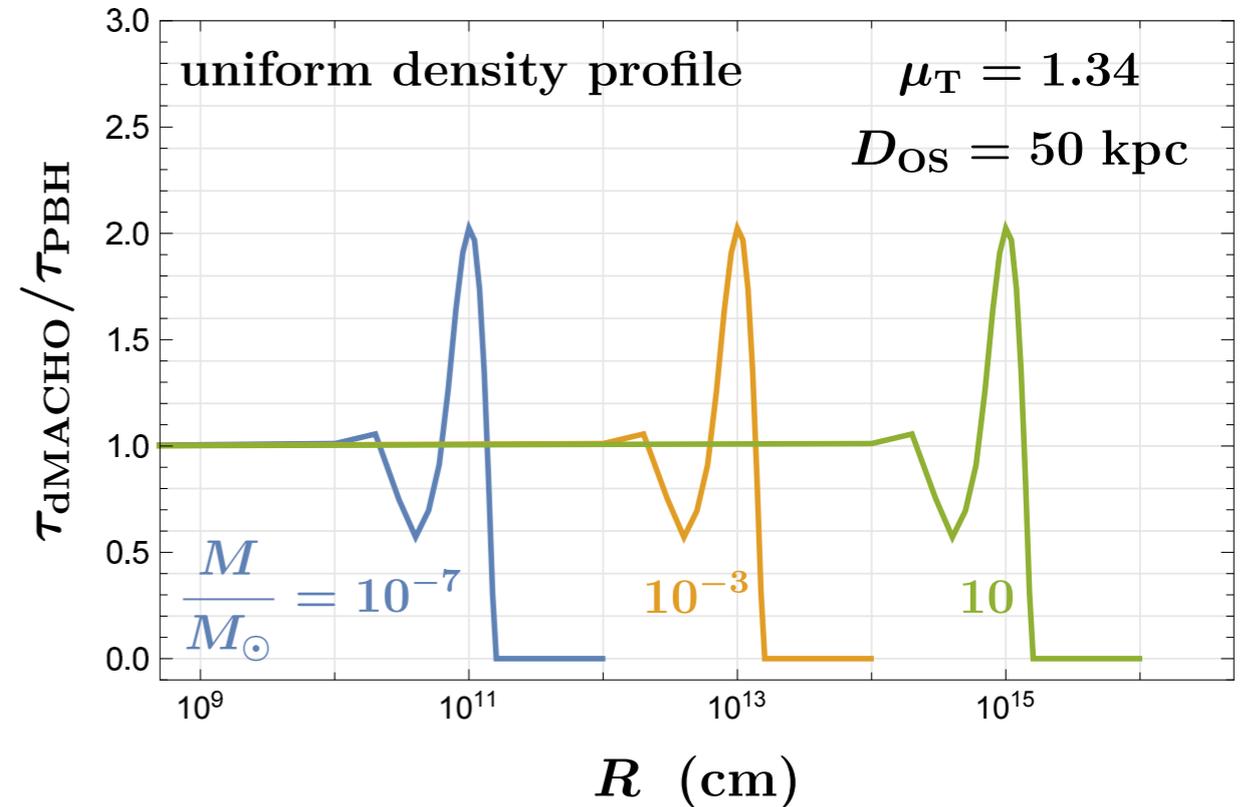
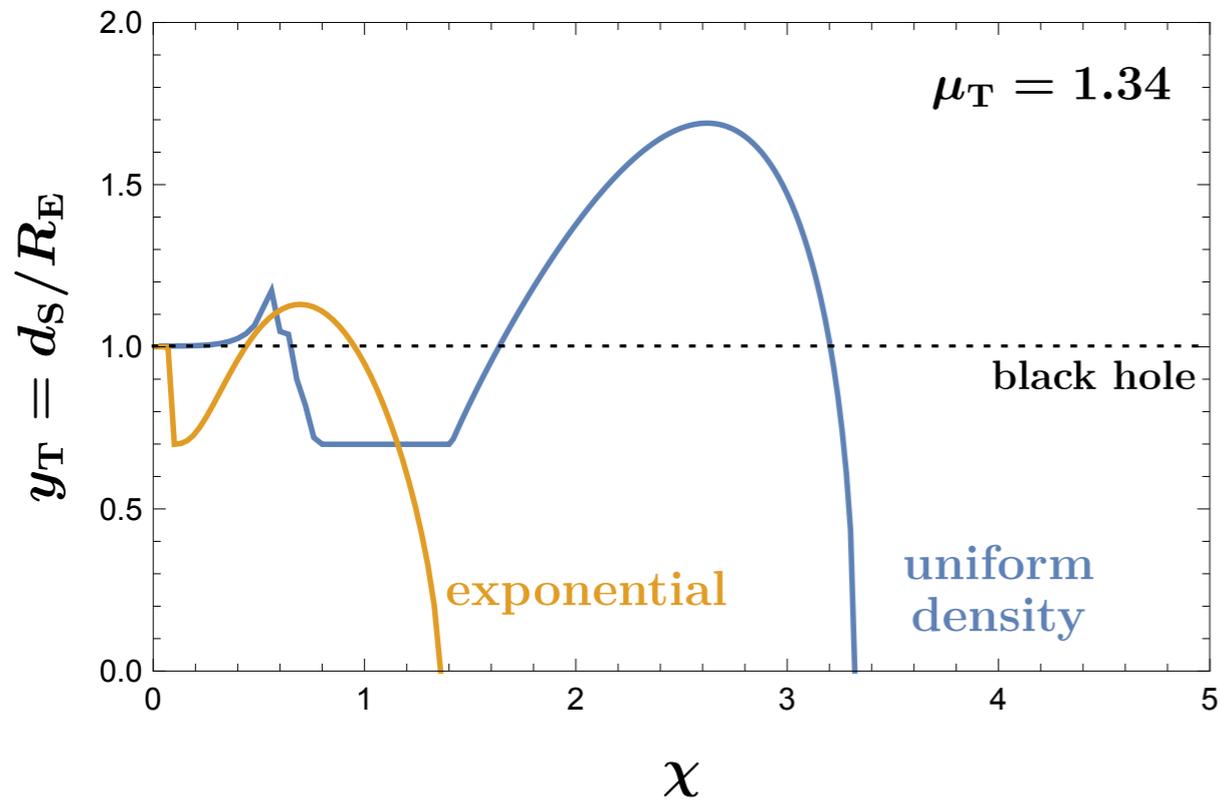
Gravitational Lensing

❖ Einstein radius:

$$R_E = \sqrt{4 G_N M \kappa (1 - \kappa) D_S} \approx (1.51 \times 10^{14} \text{ cm}) \times \left(\frac{\sqrt{\kappa(1 - \kappa)}}{1/2} \right) \left(\frac{D_S}{50 \text{ kpc}} \right)^{1/2} \left(\frac{M}{M_\odot} \right)^{1/2}$$



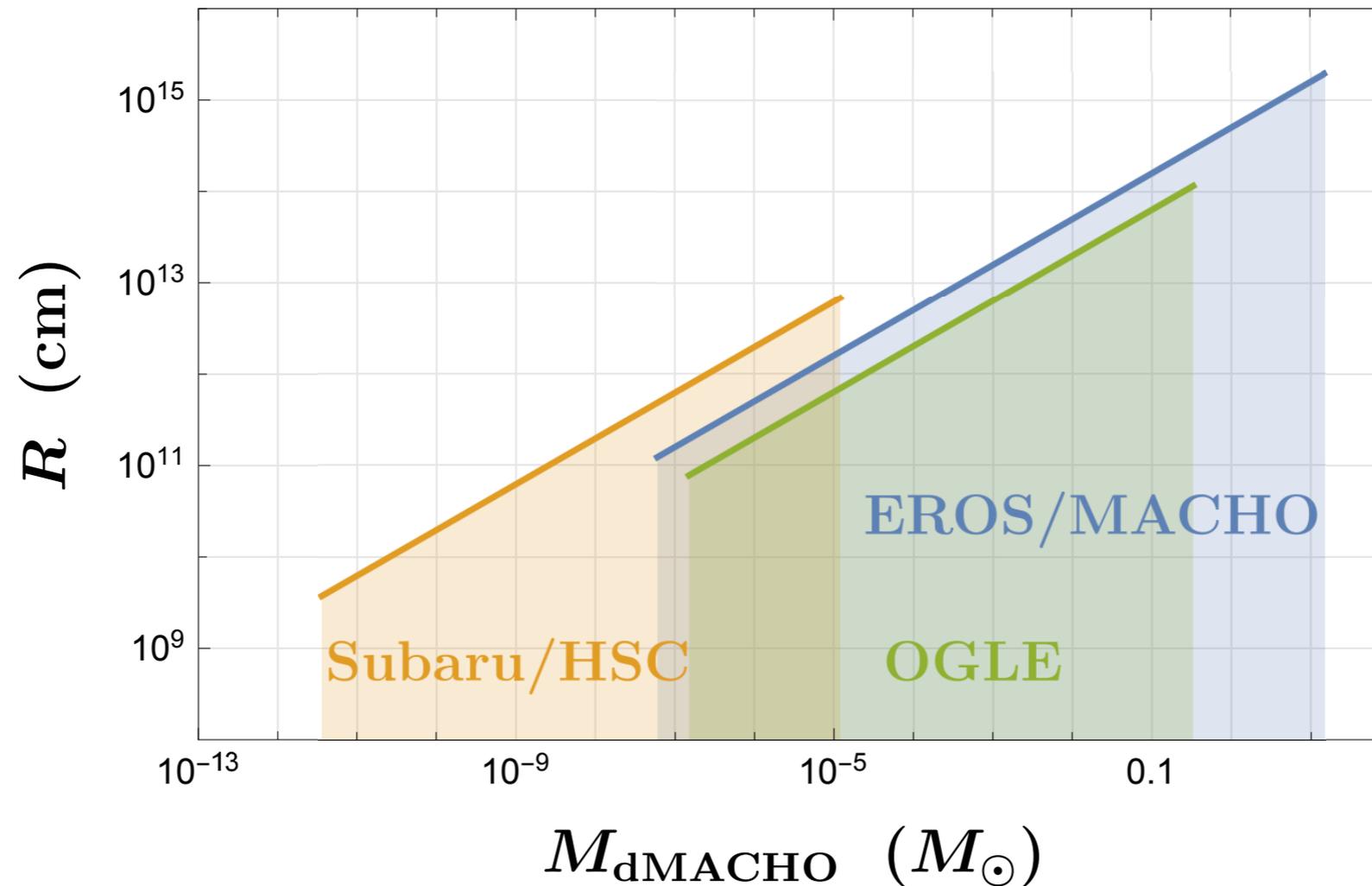
Gravitational Lensing



$$\tau = D_{\text{OS}} \int_0^1 d\kappa n_{\text{lens}}(\vec{r}_O + \kappa D_{\text{OS}} \hat{n}_L) \pi y_T^2 \left(R/R_E(\kappa), \mu_T \right) R_E^2(\kappa)$$

❖ **Optical depths drop dramatically as $R \geq \mathcal{O}(R_E)$**

Gravitational Lensing



- ❖ **Below $\sim 10^{-11} M_{\odot}$, there is no lensing constraint**
- ❖ **Other lensing systems to improve the limits in the future**

Dai, Venumadhav, et. al, 1804.03149

Dror, Ramani, et. al, 1901.04490

Accretion of Baryonic Matter

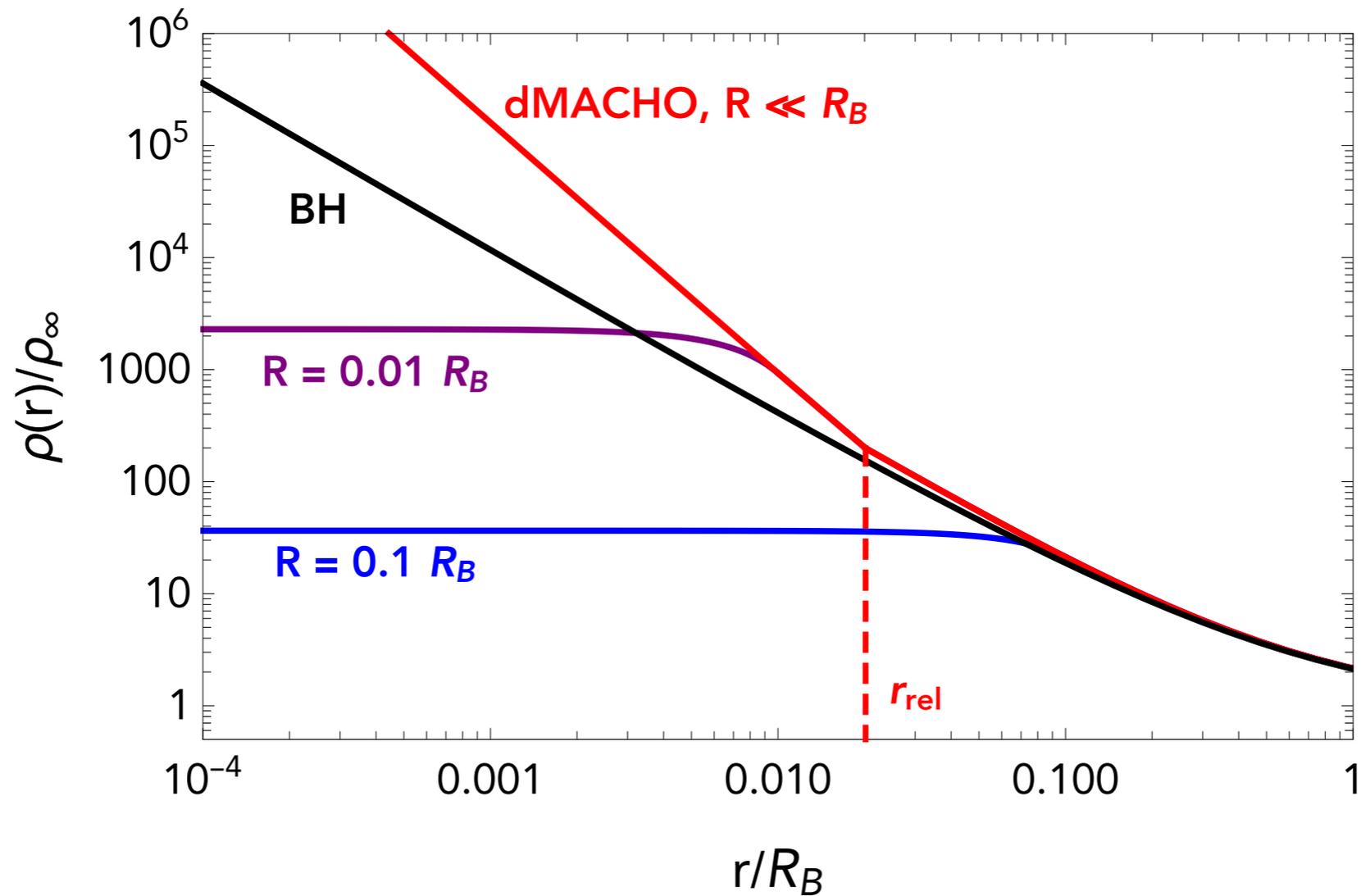
- ❖ Large and localized gravitational potential by MDM can accrete ordinary baryons, which are hot and can radiate photons to change the electron recombination history
- ❖ For PBH, there are many studies along this direction with either spherical or non-spherical accretion. In our study, we take spherical accretion for simplicity
- ❖ For PBH, Bondi accretions have been used (see [Ali-Haimoud and Kamionkowski, 1612.05644](#)). To obtain stationary solutions, we implement the *hydrostatic approximation*

$$\dot{\rho} + \frac{1}{r^2} (r^2 \rho v)' = 0$$

$$\rho \dot{v} + \rho v v' + P' = \rho g \quad \xrightarrow{v \rightarrow 0} \quad \frac{G_N \tilde{M}(r)}{r^2} + \gamma K \rho(r)^{\gamma-2} \frac{d\rho}{dr} = 0$$

$$\rho (\epsilon/\rho)^\cdot + \rho v (\epsilon/\rho)' + P \frac{1}{r^2} (r^2 v)' = \dot{q}$$

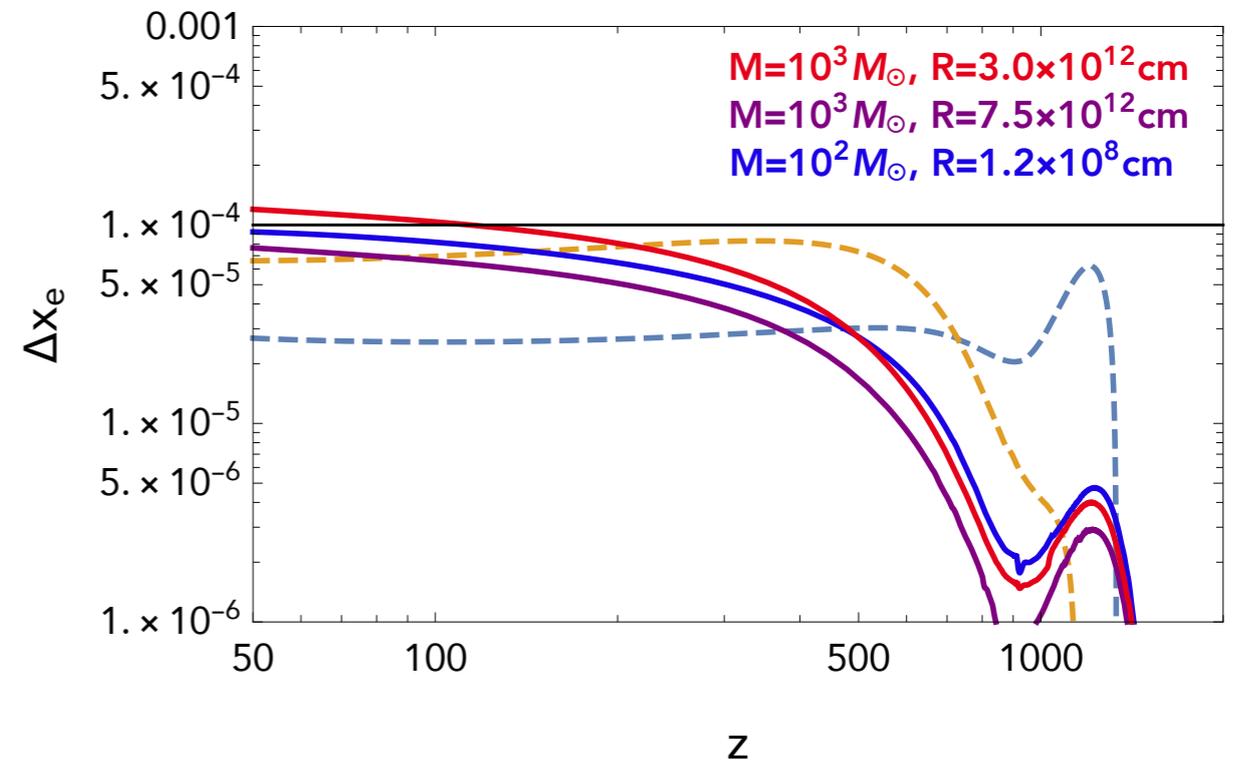
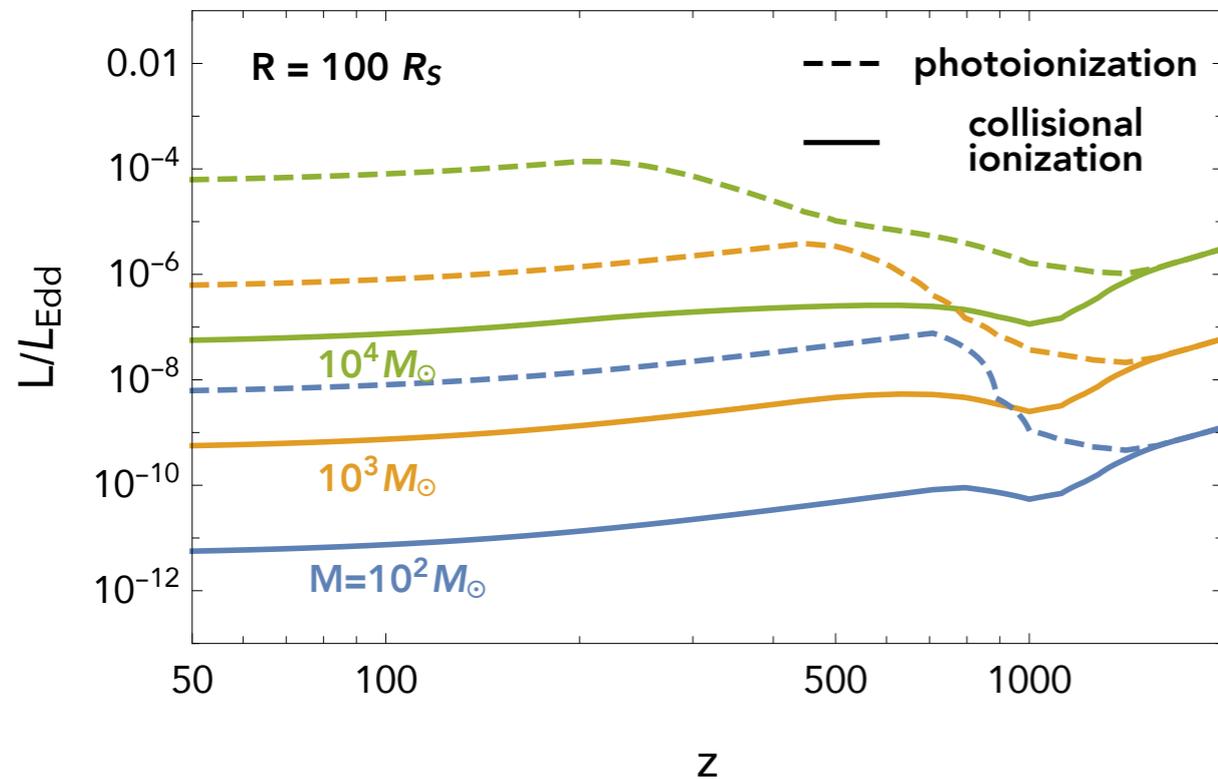
Bondi vs. Hydrostatic



- ❖ **Bondi radius: $R_B = G_N M / c_\infty^2$ with the sound speed**

$$c_\infty = \sqrt{5P_\infty / 3\rho_\infty}$$

Luminosity and Ionization



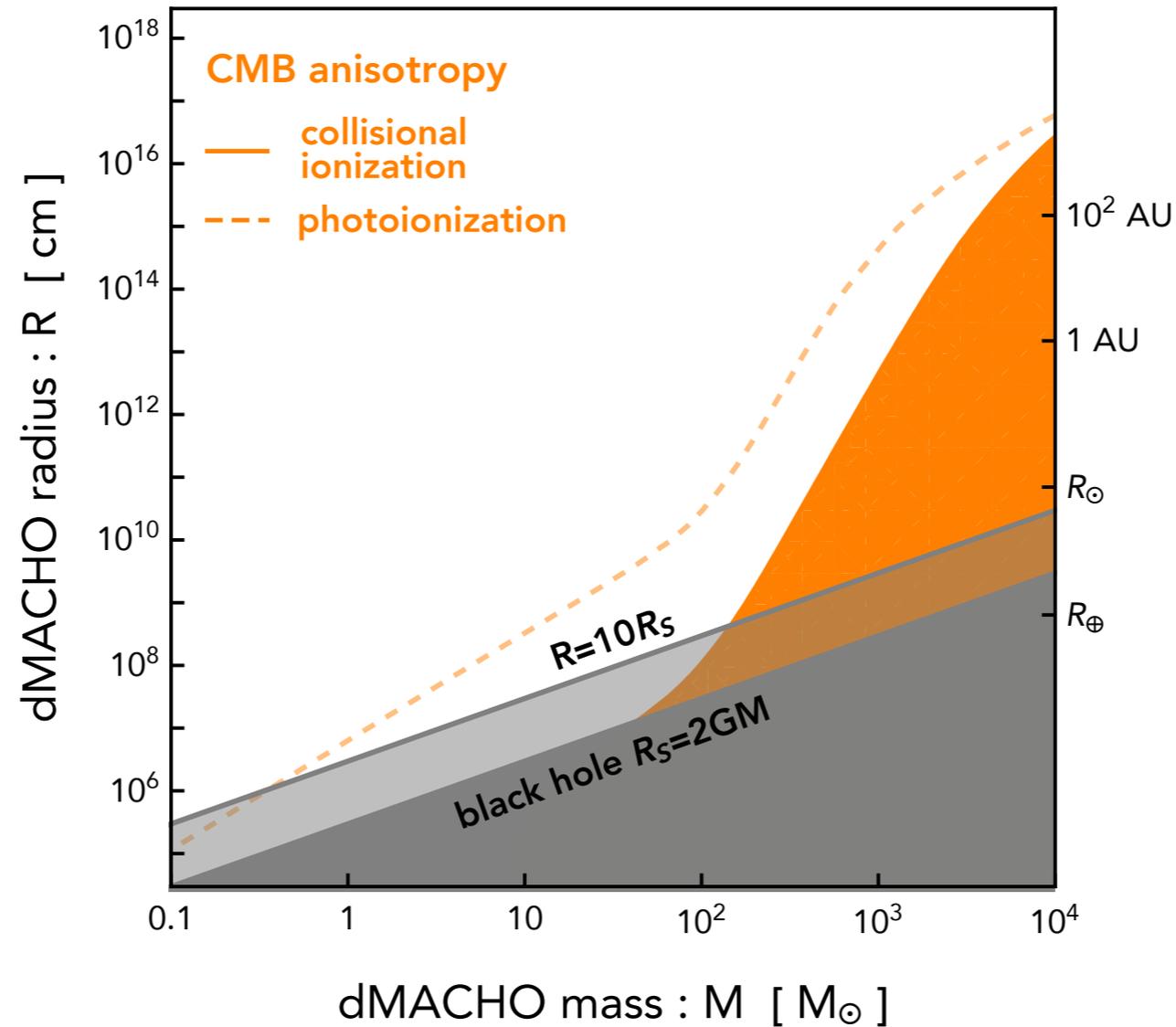
$$L_{\text{Edd}} = 4\pi G_N M m_p / \sigma_T$$

$$L \approx 4.1 \times 10^{-6} \times \frac{\rho_\infty^2 m_p^{3/2} (G_N M)^{7/2}}{T_\infty^3 m_e^{3/2} R^{1/2}}$$

dashed blue: $M = 10^2 M_\odot, f_{\text{PBH}} = 1$

dashed yellow: $M = 10^3 M_\odot, f_{\text{PBH}} = 0.01$

Constraints from CMB anisotropy



- ❖ **Assume dMACHO account for 100% dark matter**
- ❖ **We require $\Delta x_e(z = 50) < 10^{-4}$**

Conclusions

- ❖ **Macroscopic dark matter appears in several simple models**
- ❖ **Non-trivial phase transitions in the early universe generate dark matter in a state different from zero-temperature vacua**
- ❖ **For Higgs-portal dark matter, the non-topological soliton dark matter is in the electroweak symmetric phase**
- ❖ **An experiment with a large volume and a long-exposure time would be ideal to search for dark matter balls with multi-scattering events up to mass of one gram**
- ❖ **Gravitational lensing and CMB experiments probe the parameter space from the heavy side till 10^{22} grams**

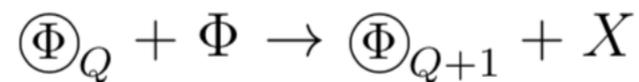
Thanks!

Abundance of Free Dark Particles

- ❖ During the chemical equilibrium, the ratio of dark matter energy density in the low-temperature phase over the high-temperature phase has

$$r \equiv \frac{n_{\Phi}^{(l)}}{n_{\Phi}^{(h)}} \approx 6 \left(\frac{m_{\phi}(T)}{2\pi T} \right)^{3/2} e^{-m_{\phi}(T)/T}$$

- ❖ The freeze-out temperature is controlled by the process



$$\Gamma_{Q+\Phi \rightarrow Q+1} = \langle \sigma v \rangle n_{\textcircled{\Phi}} \simeq 4\pi R_{\textcircled{\Phi}}^2(T) \frac{Y_{\Phi} s}{Q} = 4\pi R_{\textcircled{\Phi}}^2(T) \frac{Y_{\Phi}}{Q} \frac{2\pi^2}{45} g_{*s} T^3$$

- ❖ The freeze-out temperature is low and below ~ 1 GeV
- ❖ So, the dark matter fraction in the free particle state is dramatically suppressed and negligible