#### Strings, Particle Physics and the Swampland

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From Home, June 4 2020

# Particle Physics after LHC runs

#### 1) The Higgs is an amazing success

#### 2) No sign so far of SUSY....

#### 3) .....nor any other new Physics

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Small metric plage manual jets are drawning by the tetter (3).

#### ...which direction should we take? SUSY (non-minimal) **SUSY** (be patient) **RPV** Relaxion Technicolor Composite LED Clockwork Twin H Conformal LST Agravity RS



Naturality has been at the forefront of (almost) all our attempts to understand hierarchies in the last decades

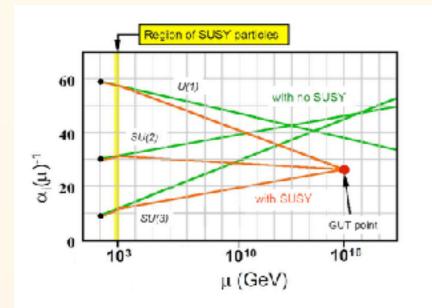
Has the naturality criterium guided us in the right direction?

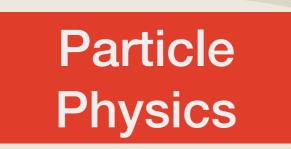
Perhaps we have to abandon some of our most cherised ideas:

- \*\* UV-IR independence
- \*\* Does Quantum Gravity really decouple?

#### Wilsonian view

#### Quantum Gravity





- We normally assume that the SM is unified with quantum gravity at the Planck scale
- Also asume that no trace of such quantum gravity embedding, other than boundary conditions, e.g. coupling unification, or irrelevant operators remain

irrelevant operators 
$$\frac{\phi^{n+4}}{M_p^n}$$

• So we can ignore quantum gravity effects at low energies

• The tacit assumption is the belief that any field theory you can think of can consistently be coupled to quantum gravity.

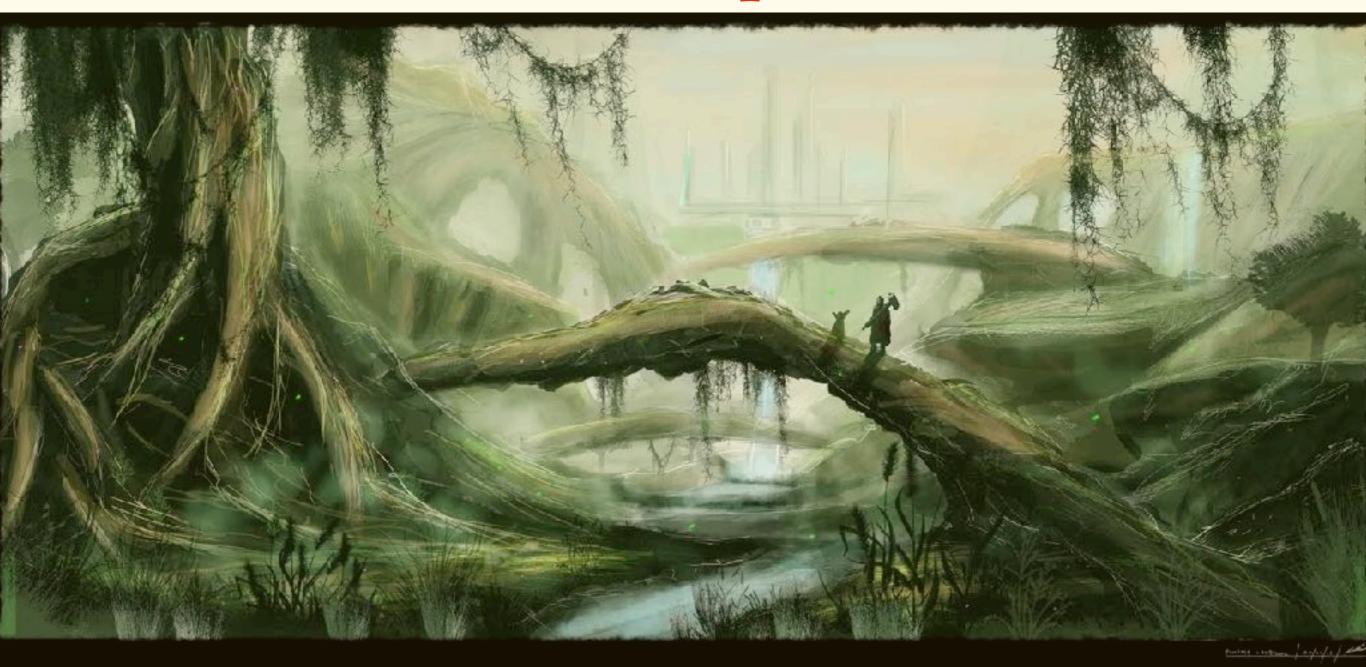
• It has been realized in the last decade that this is NOT TRUE, e.g

$$\int dx^4 \sqrt{g} \ g_{\mu\nu} \partial^{\mu} \phi \partial^{\nu} \phi^* \neq \int dx^4 \ \delta_{\mu\nu} \partial^{\mu} \phi \partial^{\nu} \phi^*$$

 Most field theories cannot be consistently coupled to quantum gravity, they belong to the

SWAMPLAND

# The Swampland



The space of field theories which cannot be embedded into a consistent theory of quantum<sub>7</sub> gravity

# Some Swampland Criteria

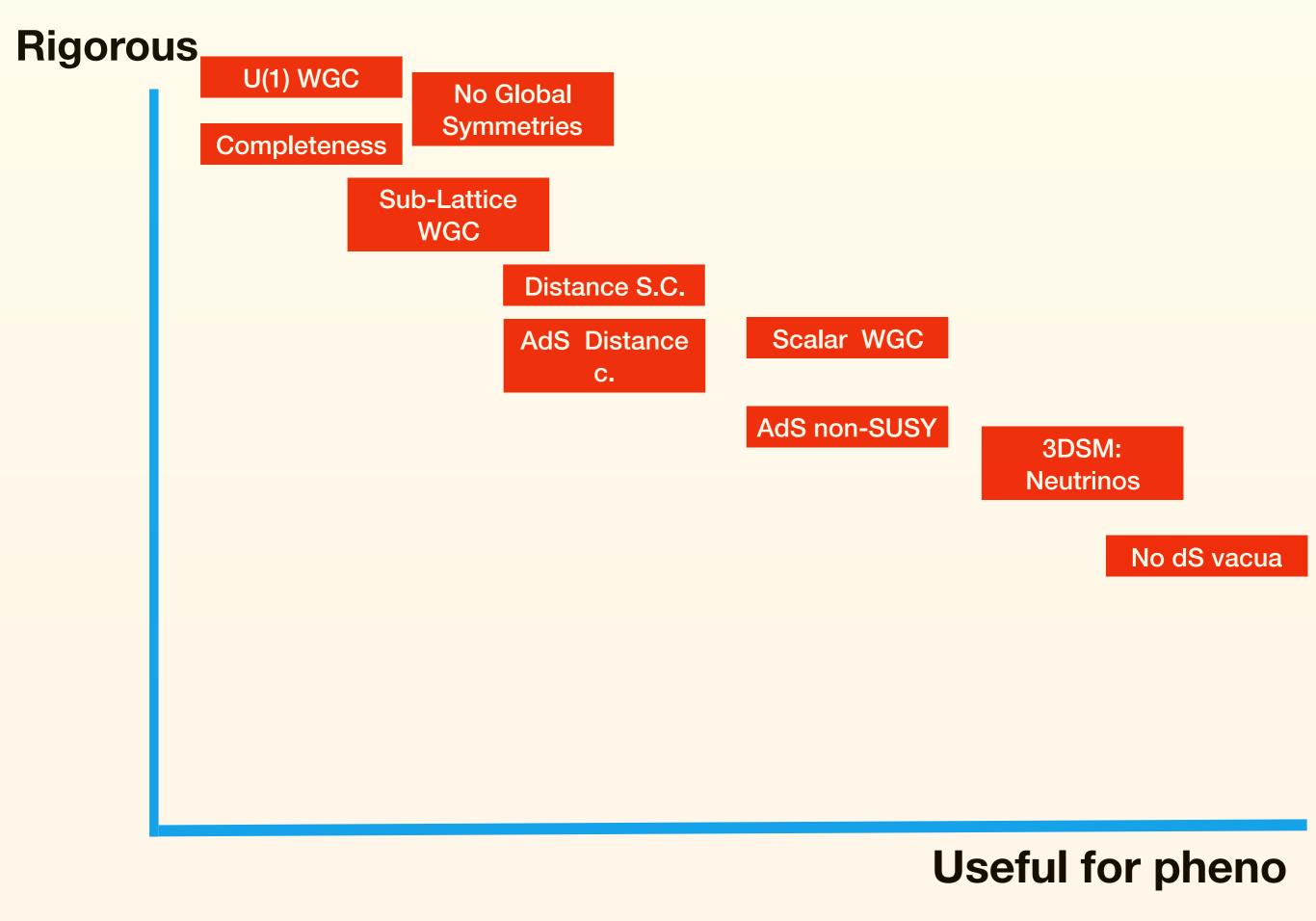
- These are conjectures, many of them suggested by black-hole quantum physics
- Other tested against string theory results

• We are thus assuming that string theory is a consistent theory of quantum gravity

Review: Pa

Palti, arXiv:1903.06239

Brennan, Carta, Vafa . arXiv:1711.00864



# Rigorous U(1) WGC No Global Symmetries Completeness Sub-Lattice WGC Distance S.C. AdS Distance C. AdS non-SUSY No dS vacua

#### **Useful for pheno**

# Rigorous U(1) WGC No Global Symmetries Completeness Sub-Lattice WGC Distance S.C. AdS Distance C. AdS non-SUSY No dS vacua

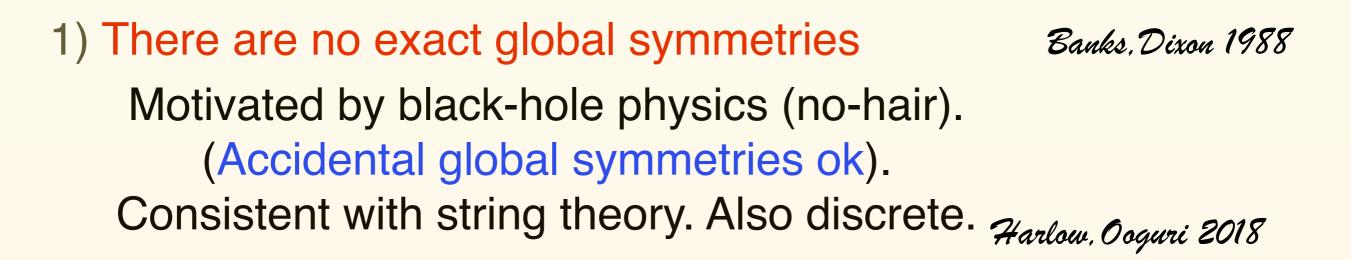


#### **Useful for pheno**

#### 1) Overview of Swampland constraints

#### 2) Some possible applications to Particle Physics

#### Some Swampland Conjectures



2) Existence of gauge bosons implies existence of charged p.

Polchinski 2003

Inconsistent !

$$\frac{1}{4g^2} \int \sqrt{G} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2\kappa} \int \sqrt{G} R$$

Motivated by black-hole physics: Charged BH solutions exist

3) Completeness conjecture:



Particles of all possible charges must exist (not necessarily light!!)

Motivated also by black-hole physics and string theory

4) No free parameters in the theory

All couplings are scalar fields (including masses, kinetic terms)

A fact in String theory

# 5) The Weak Gravity Conjecture

Arkani-hamed, Motl, Nicolis, Vafa 2006; Ooguri, Vafa 2007

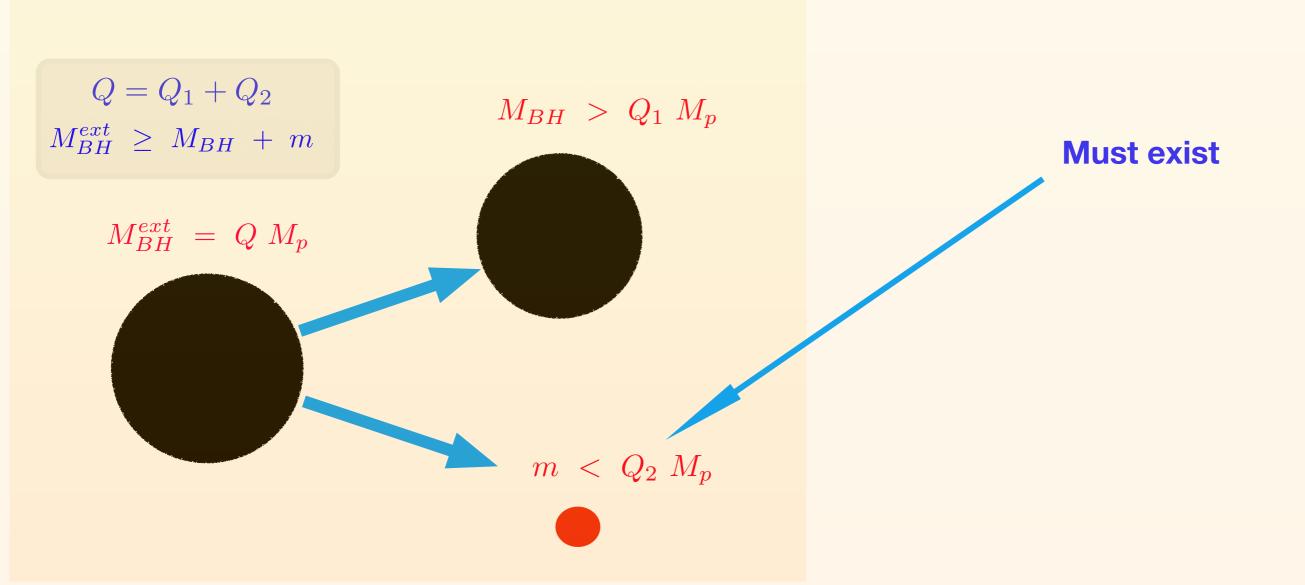
### WGC for a U(I):

• In any UV complete U(1) gauge theory there must exist at least one charged particle with mass m such that:

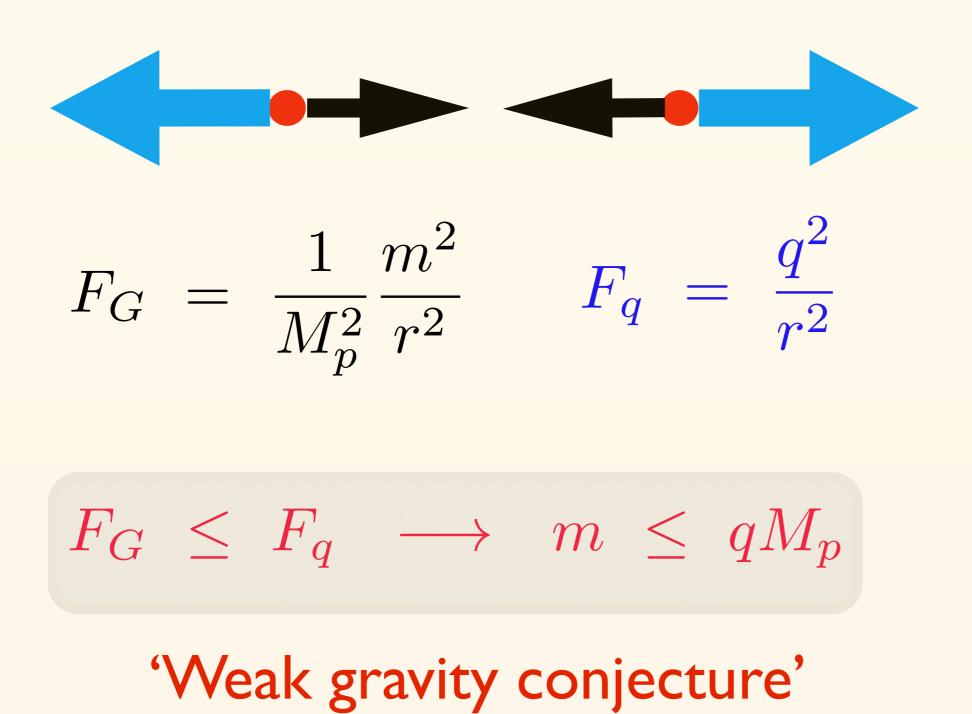
$$m \leq Q M_p$$

### Motivated by Black-hole physics

- Extremal charged blackholes:  $M_{BH}^{ext} = Q M_p$
- BH lore: extremal blackholes must decay. Otherwise there would be an infinite number of 'remants' looking like particles in the theory



#### Gravity is the weakest force

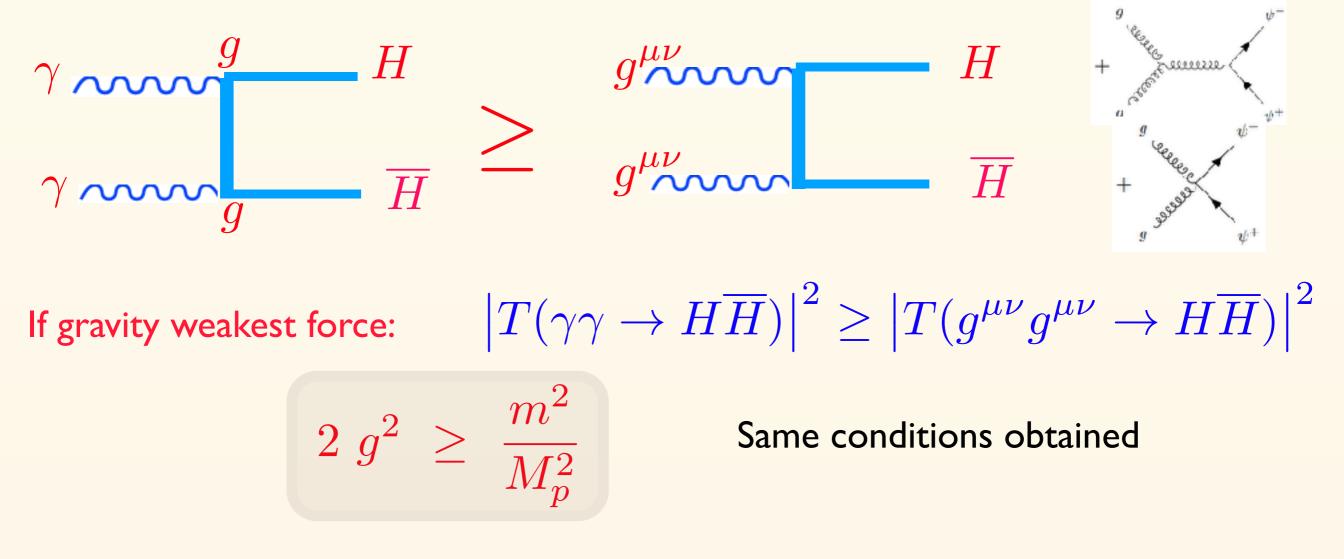


### Alternative formulation: Pair production WGC

H = Heavy charged particle

L. 9., E. Gonzalo 2020

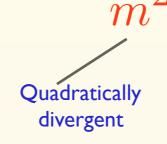
• Particle physicist formulation: production at threshold



- This approach turns out to be useful for a 'scalar WGC' later
- Same results from pair annihilation at rest

# Clash with naturality in field theory?

First observation, scalars:



 $m^2 < g^2 M_p^2$ Logarithmically divergent

U(I) with a scalar:

if

Cheung, Remmen 2014

$$\delta m^2 \simeq \frac{\Lambda^2}{(4\pi)^2} \left(a \ g^2 \ + \ b \ \lambda\right) \ < \ g^2 \ M_p^2$$
$$g^2/\lambda \ \to \ 0 \quad \longrightarrow \ \Lambda^2 \ < \ (4\pi)^2 \left(\frac{g^2}{b\lambda}\right) \ M_p^2$$

Can lower the cut-off arbitrarily ! Address hierarchy problem...

Things are a bit more complex:  $g^2 \longrightarrow 0$  limit is singular ! (Also expected, since as  $g^2 \rightarrow 0$  one recovers a global symmetry!!)

# Magnetic WGC for a U(I)

Arkani-hamed, Motl, Nicolis, Vafa 2006;

• Identical argument for the dual U(1) coupled to a monopole with mass  $M_m$ 

$$M_m < g_{mag} M_p = \frac{1}{g} M_p$$
  
 $M_m \simeq \frac{\Lambda}{g^2}$   $\Lambda \leq g M_p$ 

If there is a small gauge coupling, new thresholds must appear below the Planck scale

- In string theory the thresholds are either KK or string thresholds
- E.g. in the Heterotic string:

$$M_{string} = g M_p$$

# Generalization to NU(I)'s

- Cheung, Remmen 2014
- Slightly non-trivial: not enough to obey it for each U(1)
- For extremal blackholes to decay the BH zone should be contained
- inside the 'convex hull' spanned by the

 $m_i \leq \sqrt{2} \frac{q_i}{\sqrt{N}} M_p$ 

$$\vec{z_i} \equiv \frac{\vec{q_i}}{m_i}$$

• e.g. for 2 U(1)'s

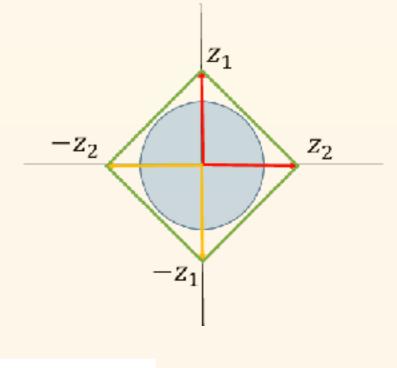
No Black Hole Discharge

 $Z_1$ 

 $-Z_2$ 

Black Hole Discharge

 $|Q_{BH}| \le M_{BH}/\sqrt{2}$ 



 $\sqrt{N}$ 

Condition stronger by

 $Z_2$ 



• Slightly non-trivial: not enough to obey it for each U(1)

 $m_i \leq \sqrt{2}q_i M_n$ 

 $|Q_{BH}| \le M_{BH}/\sqrt{2}$ 

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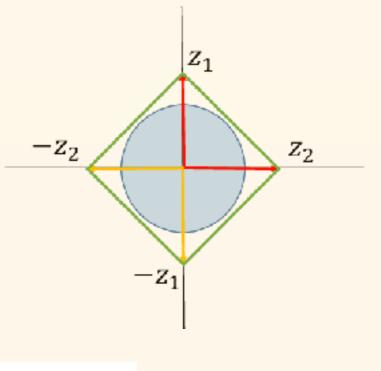
• e.g. for 2 U(1)'s No Black Hole

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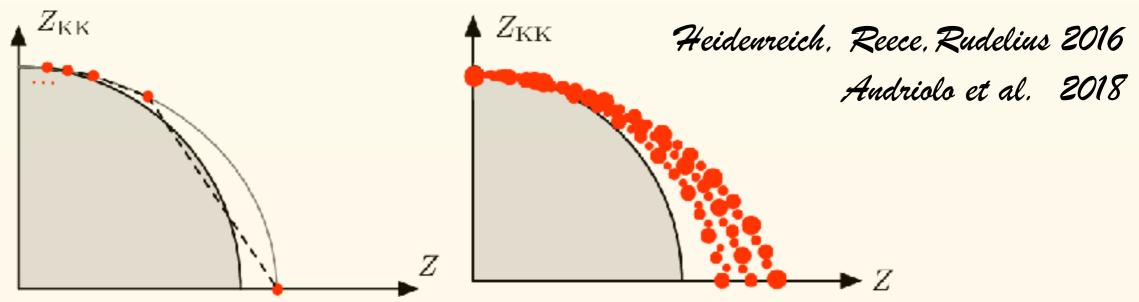
 $\sqrt{N}$ 

Condition stronger by

 $Z_2$ 

# 6) The sublattice WGC

- Simplest WGC is not what seems realised in string theory
- Upon dimensional reduction the KK U(1)'s break the WGC

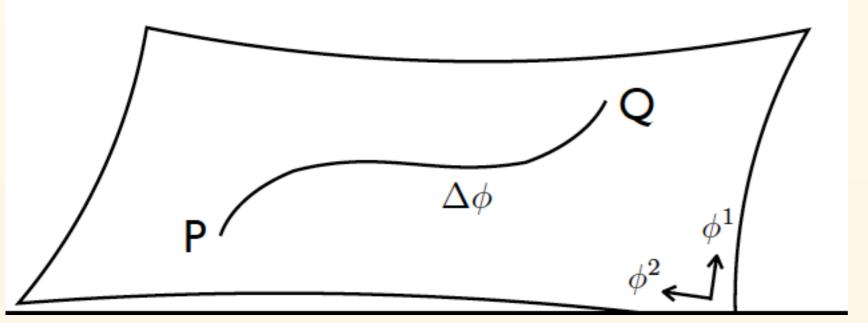


- May be overcome if there are an infinite number of charged states
- Sublattice conjecture: for any point in the gauge lattice there is a superextremal charged particle
- Consistent with 'completeness conjecture'

 $g^2 \longrightarrow 0 \longrightarrow A full tower of charged states becomes massless$ 

• Towers of massless fields as  $g^2 \rightarrow 0$  is an example of a more general phenomenon: Organi, Vafa 2006

Moduli space of scalars: as we move In moduli space by  $\Delta\phi$  a tower of states becomes exponentially massless



 $m(Q) \simeq m(P)e^{-\lambda\Delta\phi}$ 

The effective field theory becomes inconsistent

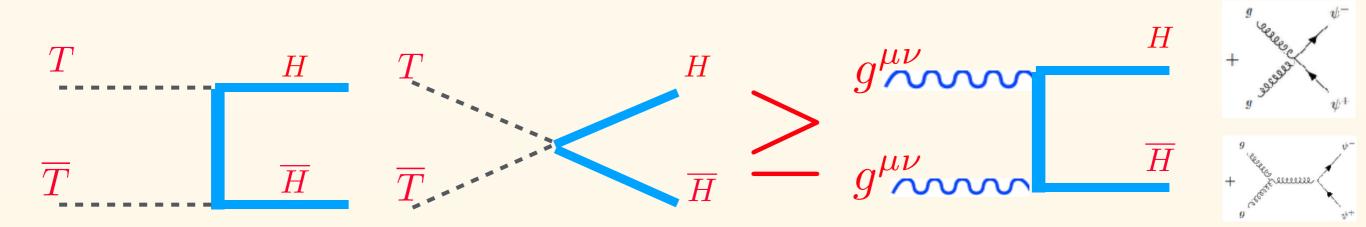
Has been checked in many string theory examples

#### 8) The Scalar WGC Conjecture

- WGC originally formulated for U(1)'s and charged particles
- Is there an analogue for moduli scalars T?
- There must exist heavy states H such that:

L. 7. , E. Gonzalo 2019, 2020

Palti 2017



 $\mathcal{L}_T = \partial_{\mu} H \partial^{\mu} \overline{H} + \partial_{\mu} T \partial^{\mu} \overline{T} - m^2(T, \overline{T}) |H|^2 + \dots$ 

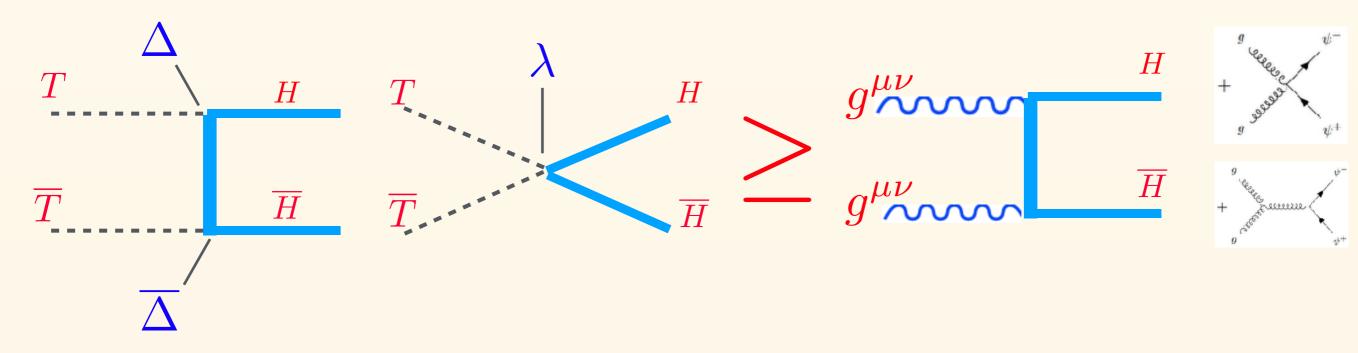
 $m^2 \simeq m_0^2 + (\partial_T m^2)T + (\partial_{\overline{T}} m^2)\overline{T} + (\partial_{\overline{T}} \partial_T)m^2)|T|^2 + \dots$ 

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 $\mathcal{L}_T = \partial_{\mu} H \partial^{\mu} \overline{H} + \partial_{\mu} T \partial^{\mu} \overline{T} - m^2 (T, \overline{T}) |H|^2 + \dots$ 

 $m^2 \simeq m_0^2 + (\partial_T m^2)T + (\partial_{\overline{T}} m^2)\overline{T} + (\partial_{\overline{T}} \partial_T)m^2)|T|^2 + \dots$ 

$$\Delta = \partial_T m^2 \ , \ \overline{\Delta} = \partial_{\overline{T}} m^2 \ , \ \lambda \ = \ \partial_T \partial_{\overline{T}} m^2$$

Scalar T coupled to gravity requires existence massive states with mass

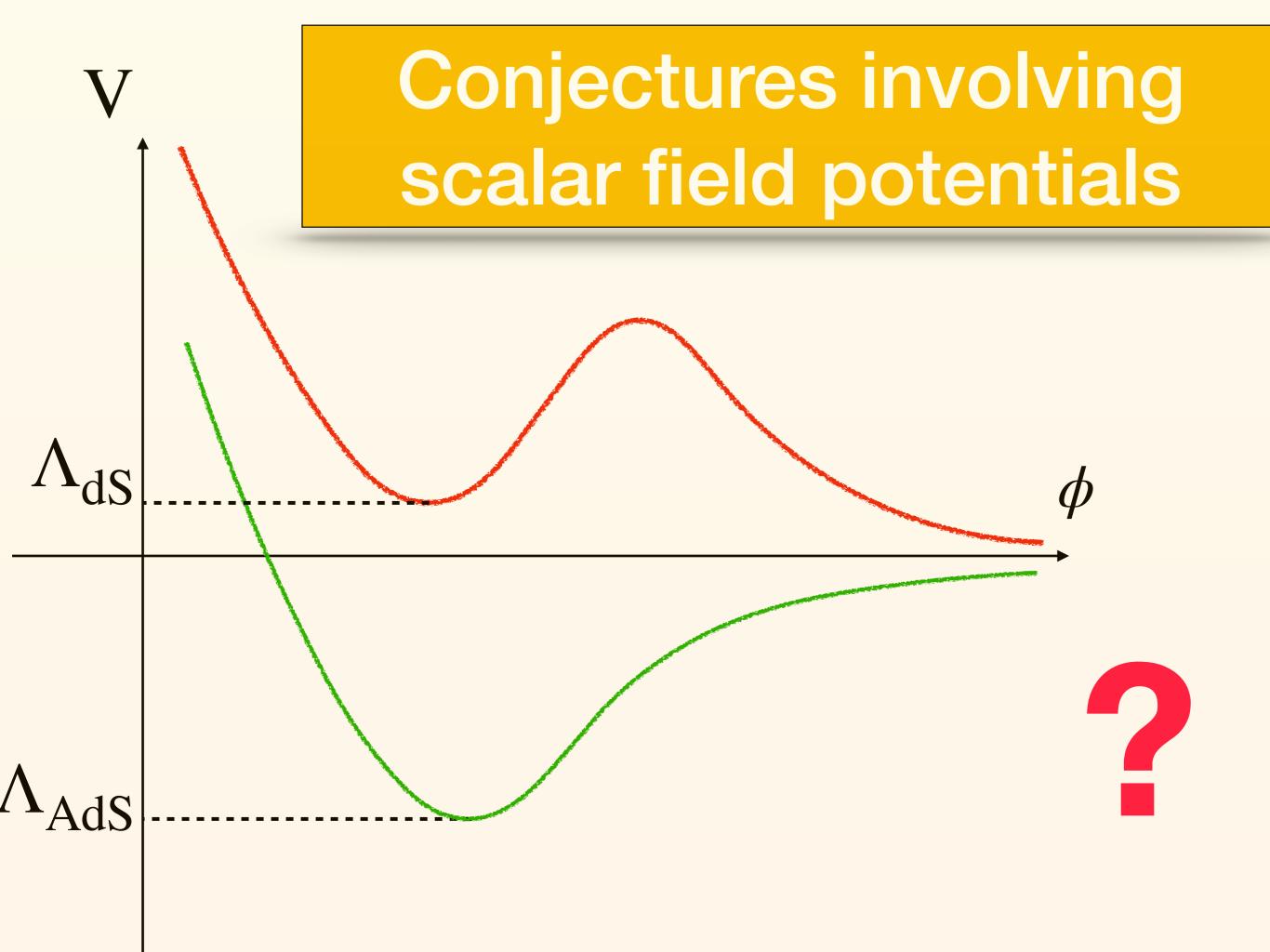
$$g^{T\overline{T}} \left| (\partial_T m^2) (\partial_{\overline{T}} m^2) - m^2 (\partial_T \partial_{\overline{T}} m^2) \right| \geq \frac{m^4}{M_p^2}$$

L. I. , E. Gonzalo, 2020

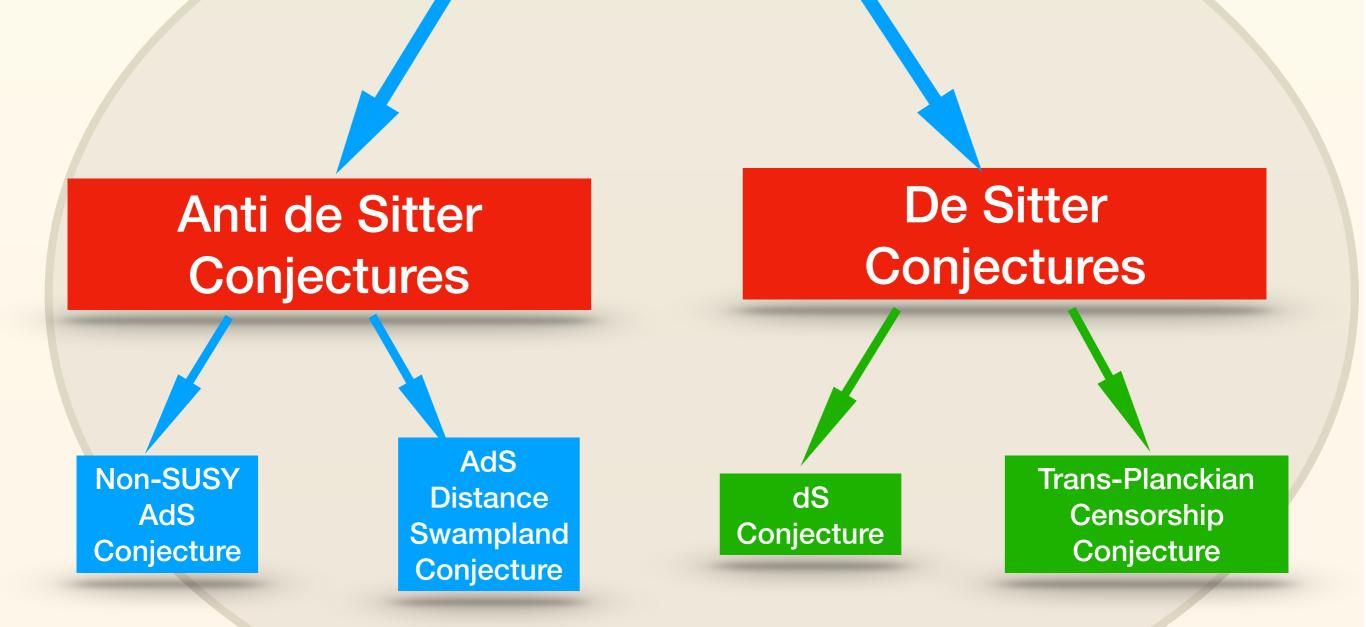
- Consider e.g. a no scale metric  $g_{T\overline{T}} = \frac{1}{(T+\overline{T})^2}$
- There are solutions which saturate the SWGC, in particular:

$$m_{KK}^2 = \frac{1}{(T+\overline{T})} , \ m_w^2 = (T+\overline{T})$$

- Look like KK and winding states in a torus compactification !!
- Emergence of extra dimensions and string states to saturate the bound!
- Although we started just with a massless scalar with a no-scale metric
- Tested in CY Type II string compactifications (Dp-branes wrapping cycles)
- May lead to some pheno constraints, see below



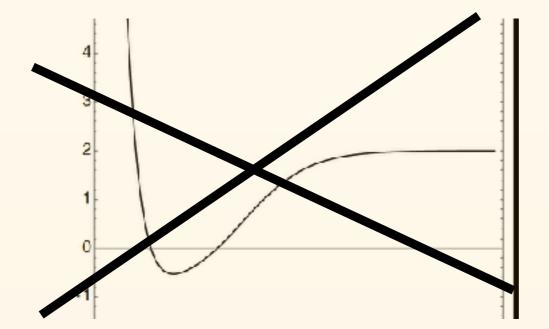
# Conjectures involving scalar field potentials



Non–SUSY AdS conjecture

There cannot be stable non-SUSY AdS vacua in quantum gravity

Non-SUSY AdS flux vacua are unstable and cannot have CFT dual



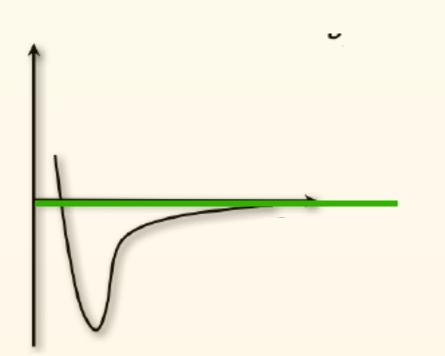
Ooguri,Vafa 2016

(If you find one in your theory, then it is inconsistent with quantum gravity)

• True within known flux string vacua. No counterexample found.

Lust, Palti, Vafa 2019

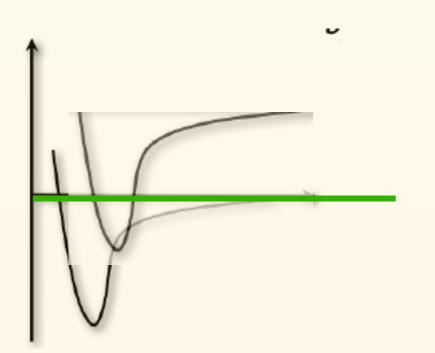
• One cannot go smoothly from AdS to Minkowski:



Consider family of AdS vacua with  $\Lambda_{c.c.} \rightarrow 0$ 

Lust, Palti, Vafa 2019

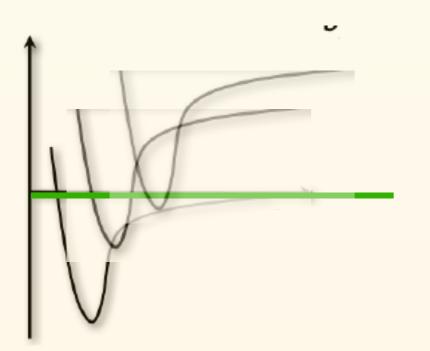
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Lust, Palti, Vafa 2019

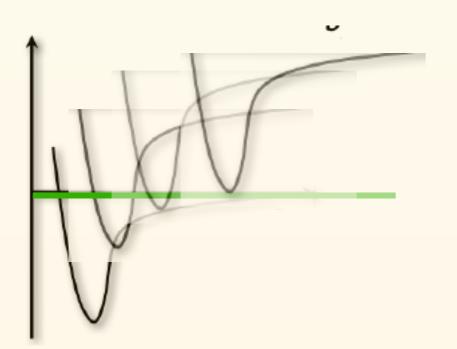
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Lust, Palti, Vafa 2019

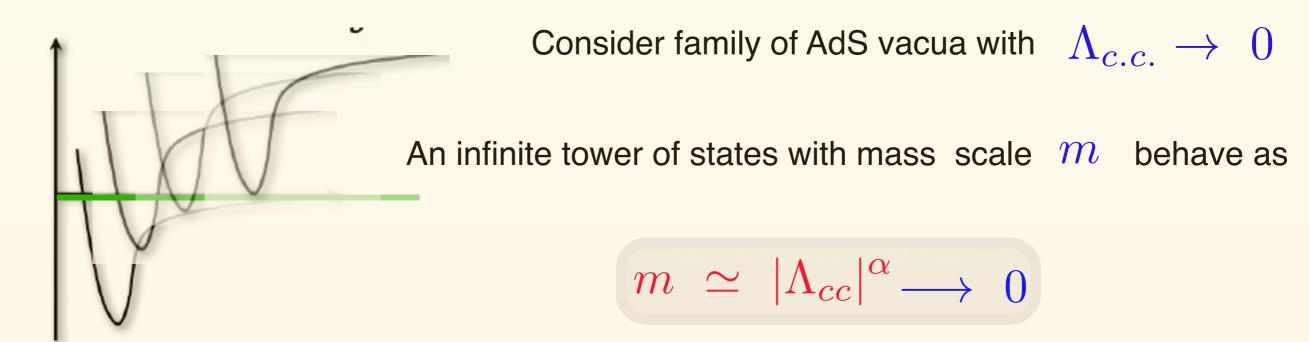
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Consider family of AdS vacua with  $\Lambda_{c.c.} 
ightarrow 0$ 

#### AdS Distance Swampland Conjecture Lust, Palti, Vafa 2019

• One cannot go smoothly from AdS to Minkowski:



Implies no separation between AdS and KK scales Van Riet et al. 2018

This separation of scales is crucial e.g. for the KKLT construction of dS vacua

(there is a possible counterexample still under discussion...)

De Wolfe et al., Camara et al . 2005

### 7) dS Swampland Conjecture

Obied, Ooguri, Spodyneiko, Vafa 2018

Any scalar potential  $V(\phi)$  in a consistent theory of quantum gravity must obey

$$|\nabla V(\phi)| \ge \frac{\mathcal{O}(1)}{M_p} V(\phi)$$

# 7) dS Swampland Conjecture

Any scalar potential  $V(\phi)$  in a consistent theory of quantum gravity must obey

$$|\nabla V(\phi)| \geq \frac{\mathcal{O}(1)}{M_p} V(\phi)$$

or else.....

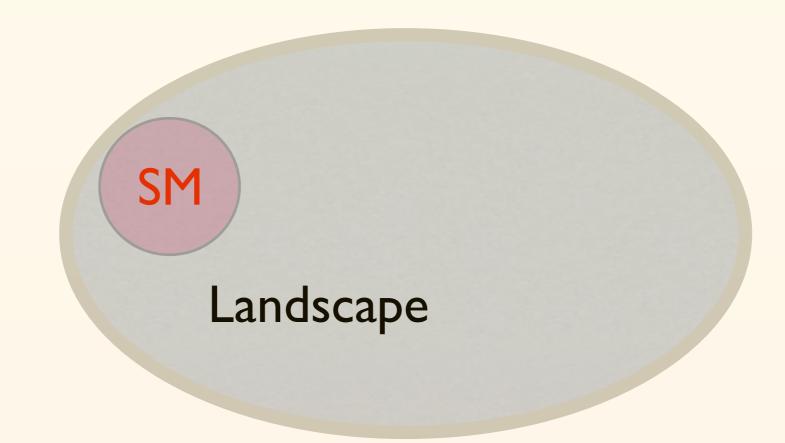
Ooguri, Palti, Shiu, Vafa 2018

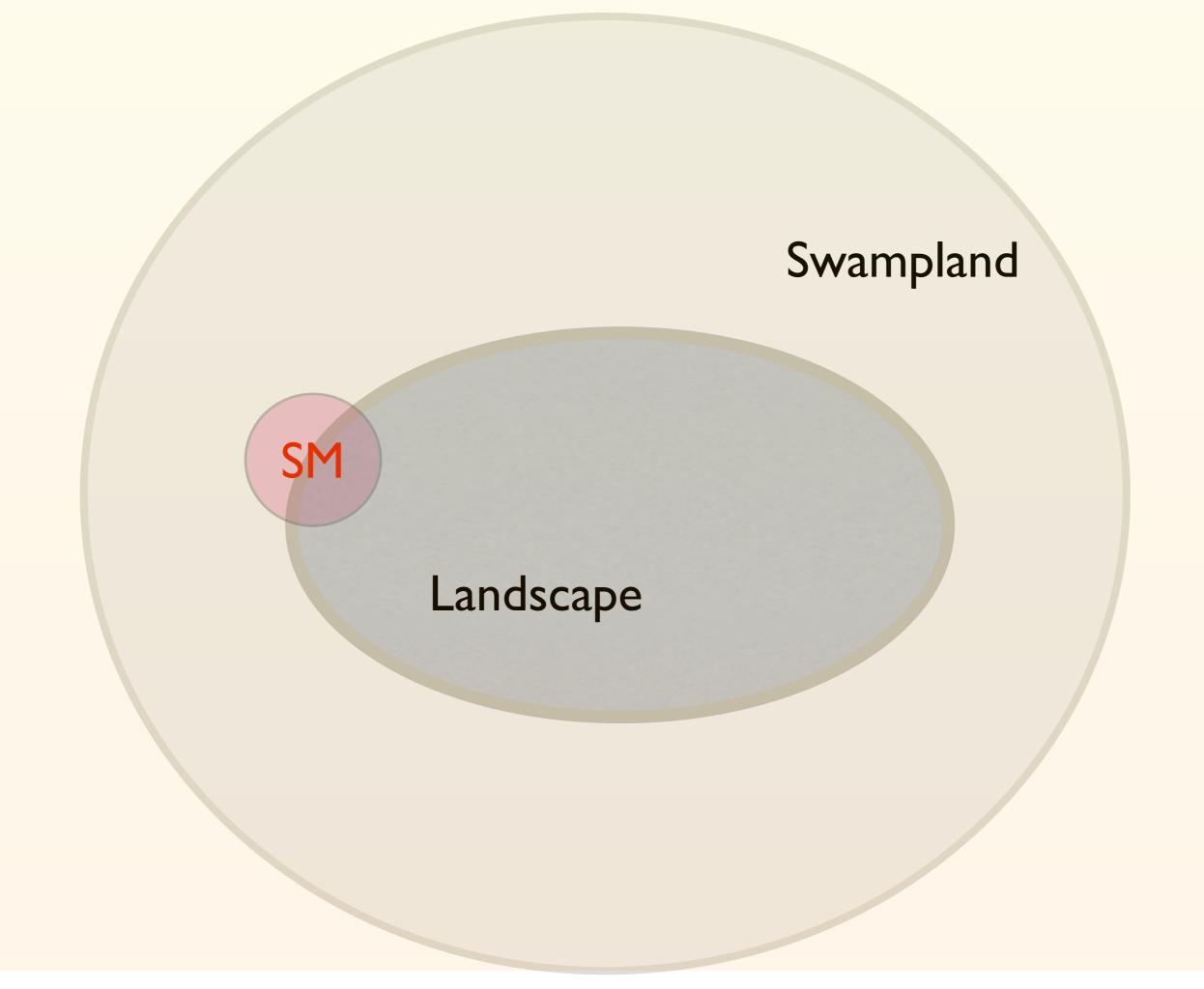
$$\min(\nabla_i \nabla_j V(\phi)) \le -\frac{\mathcal{O}(1)}{M_p^2} V(\phi)$$
  
Forbids dS vacually

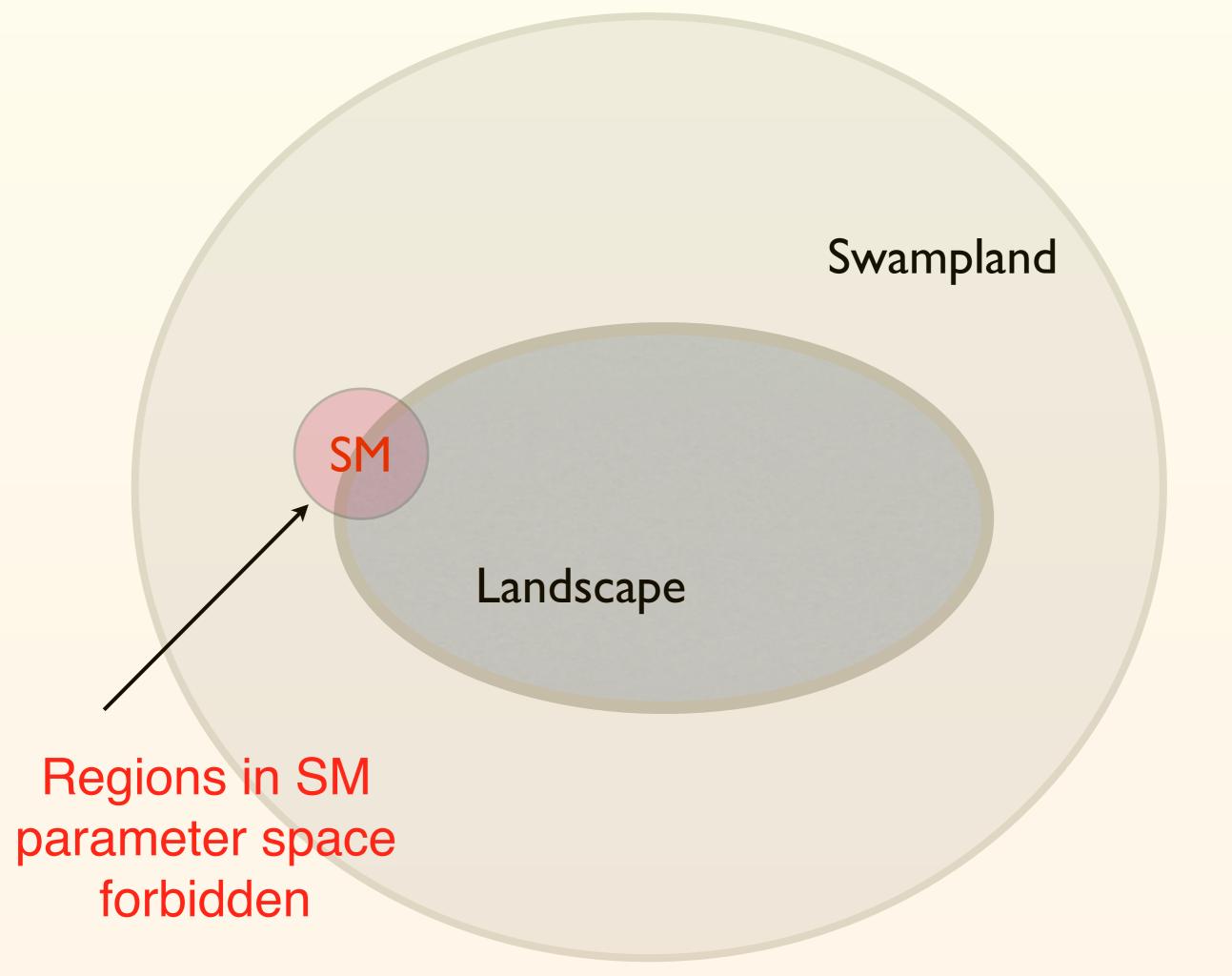
nus us vacua

Suggests runaway dS potential rather than minima.....

Applications To Particle Physics







# I) The Standard Model and 3D AdS

We seem to live in a dS space with  $\Lambda = (2.4 \times 10^{-3} eV)^4$ 

However compactifying the SM on a circle of radius R one may get AdS 3D vacua with

Arkani-Hamed, Dubovsky, Nicolis, Villadoro, 2007

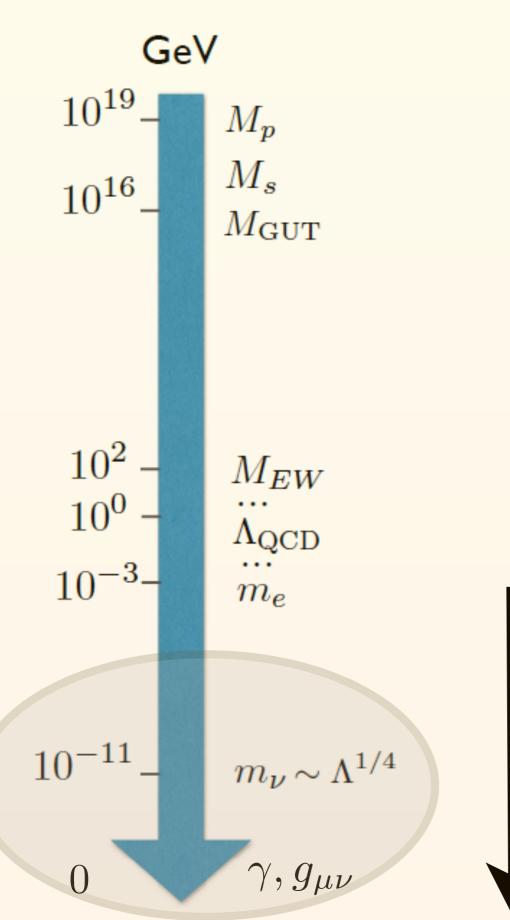
 $m_{KK} \simeq m_{\nu}$ 

non-SUSY AdS stable vacua are in the Swampland
 AdS Distance conjecture

Conjectures forbid these vacua

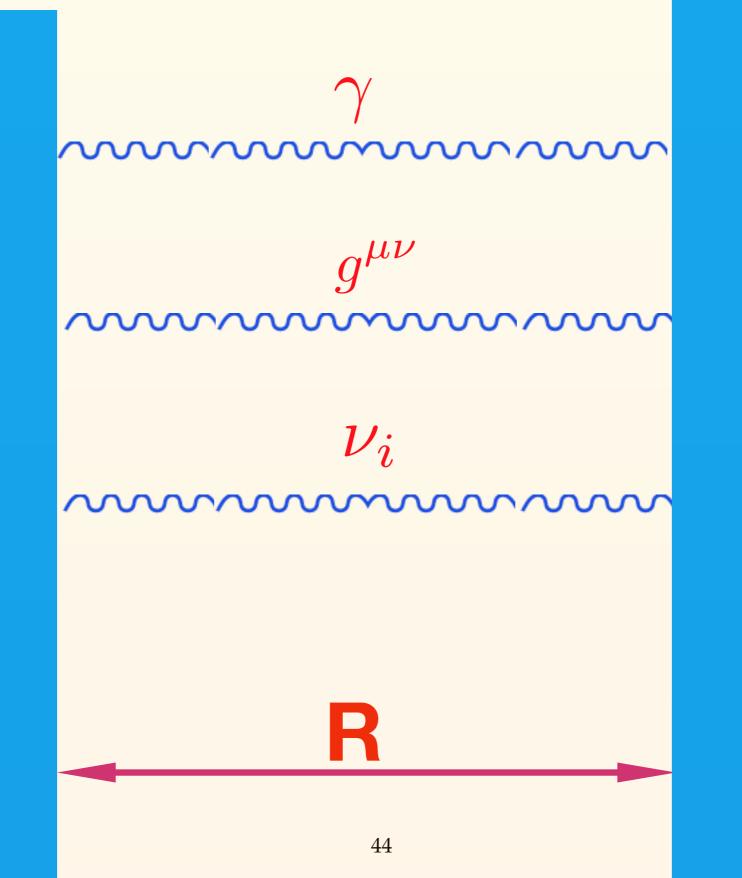
Constraints on SM physics

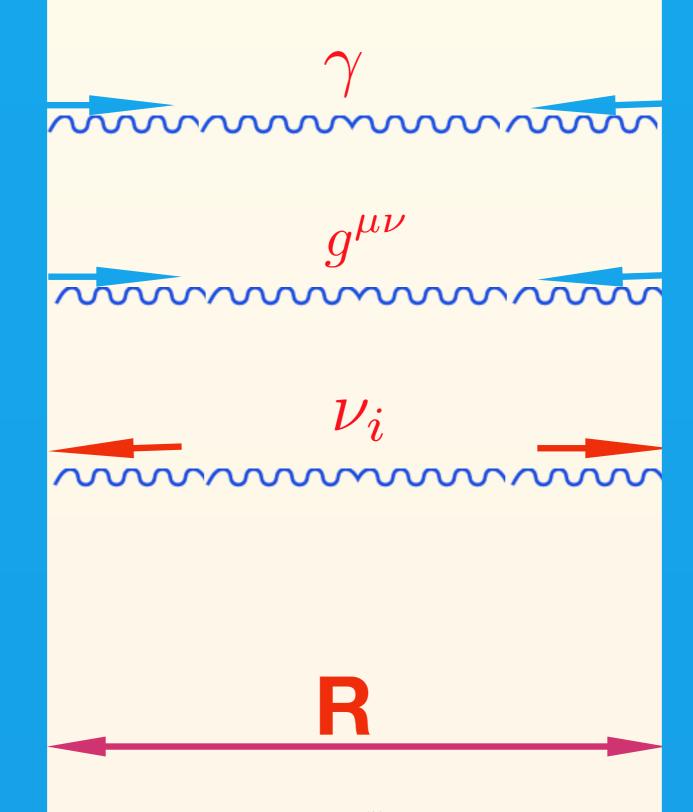
# Scales in Fundamental Physics



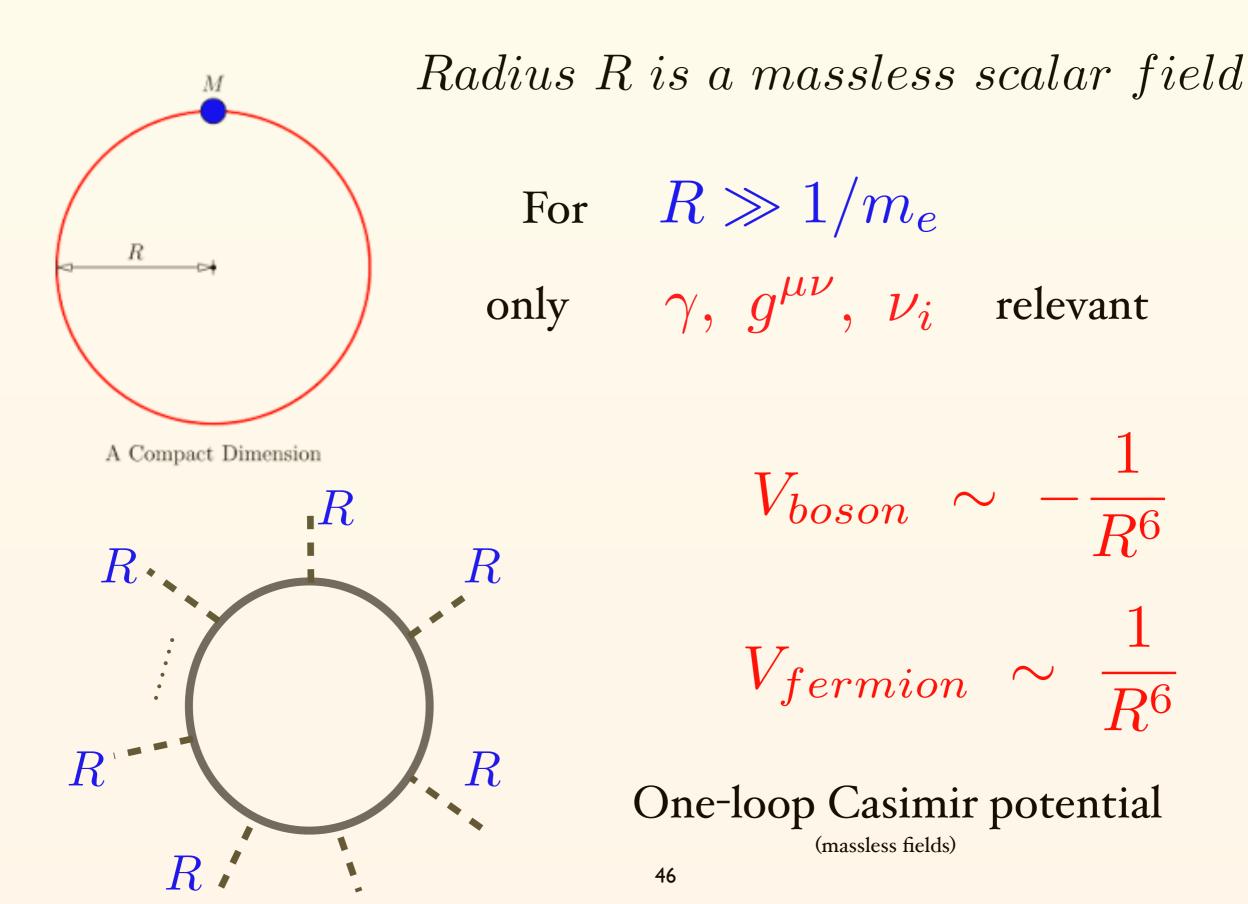
#### Will focus first in lightest SM sector

 $\frac{Below \ electron \ threshold}{m_e/m_{\nu}} \simeq 10^8 : large \ region \ of \ energies \ with \ only \ \gamma, g^{\mu\nu}, \nu_i$ 





# SM compactified to 3D on a circle



# The SM + gravity on a circle $S^1$

Consider the lightest sector:  $\gamma, g_{\mu\nu}, \nu_{1,2,3}$ Arkani-Hamed, Dubovsky, Nicolis, Villadoro, 2007 One - loop Casimir energy

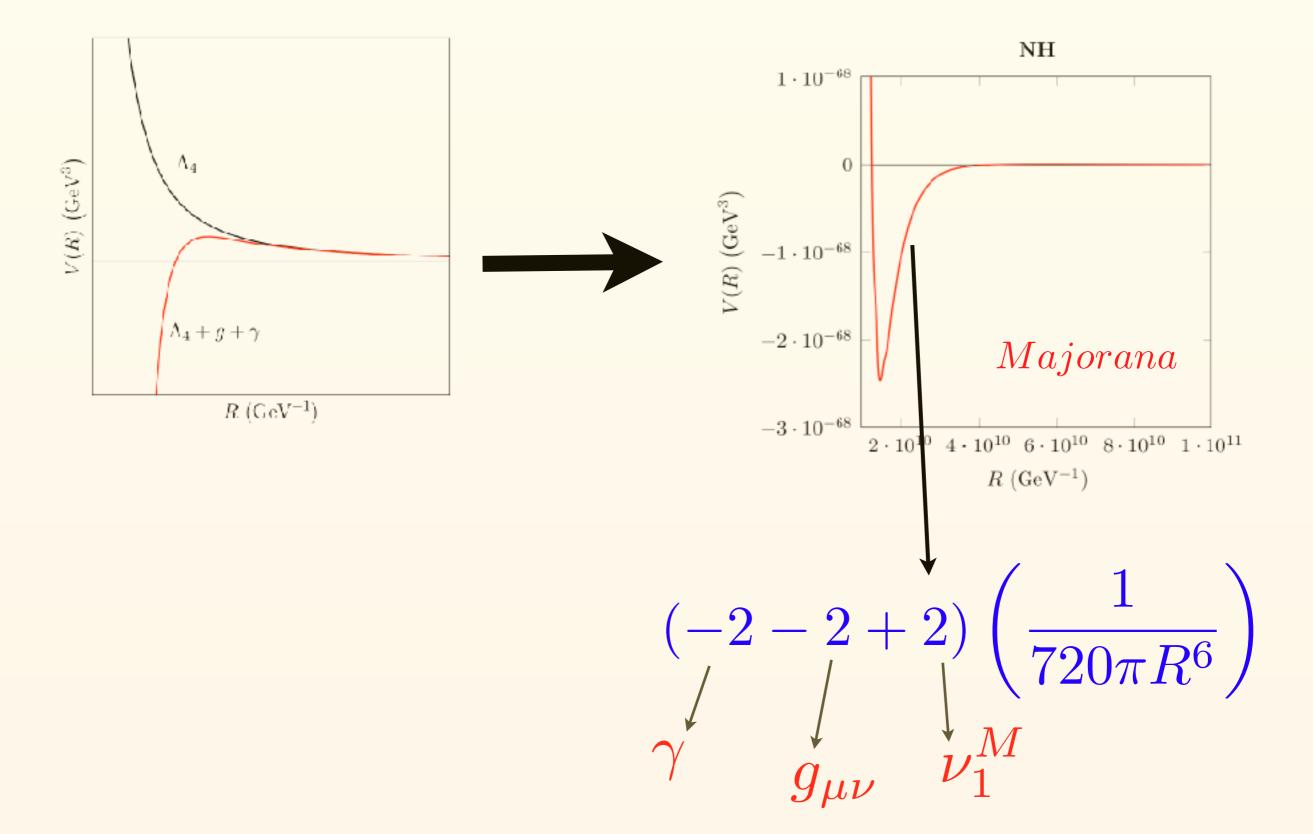
The radius potential :

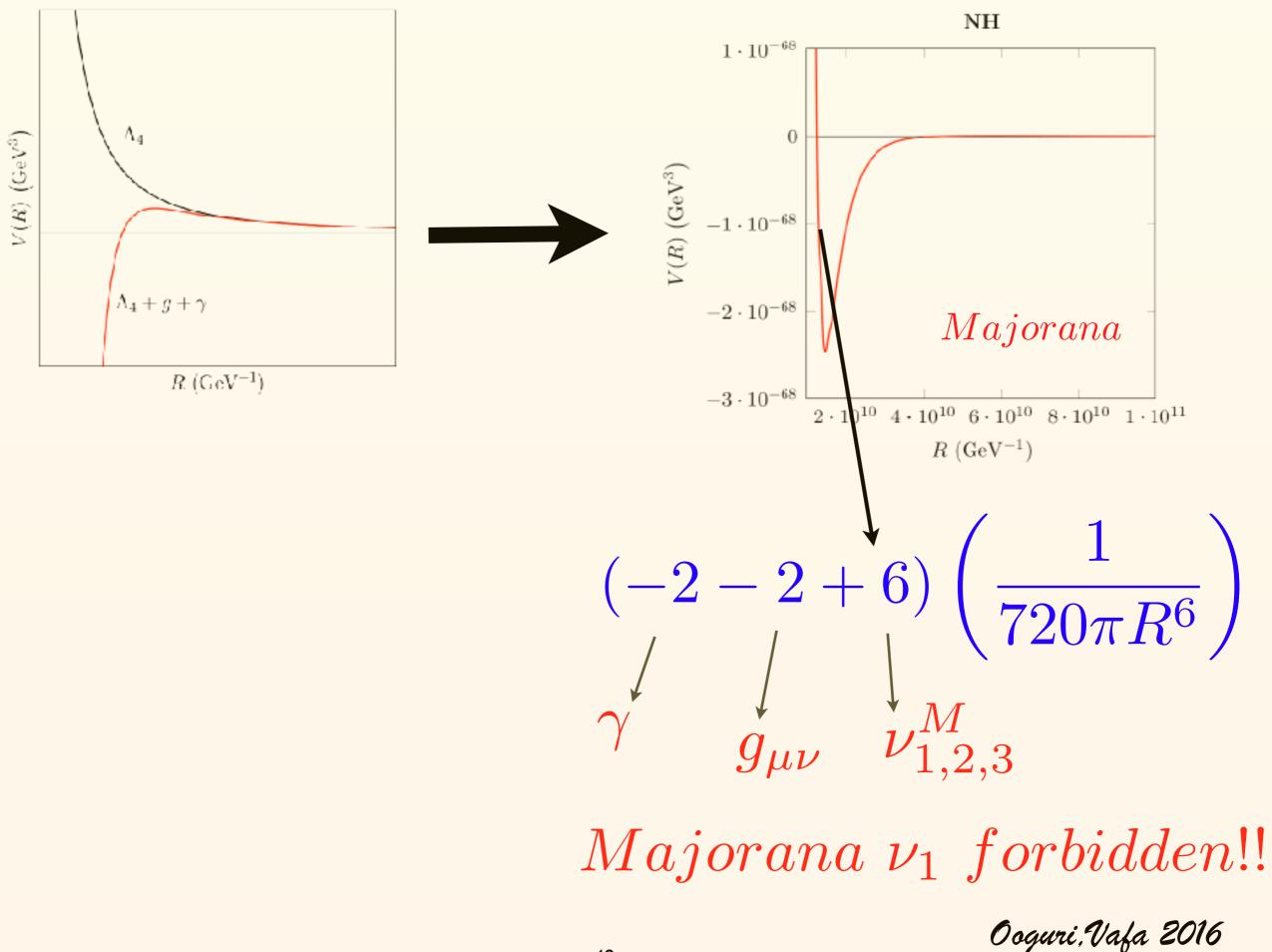
 $V(R) \simeq \frac{2\pi\Lambda_4}{R^2} - 4\left(\frac{1}{720\pi R^6}\right) + \sum_i (2\pi R)n_i\rho_i(R)$   $\int \rho(R) = \sum_{n=1}^{\infty} \frac{2m^4}{(2\pi)^2} \frac{K_2(2\pi Rmn)}{(2\pi Rmn)^2}$ 

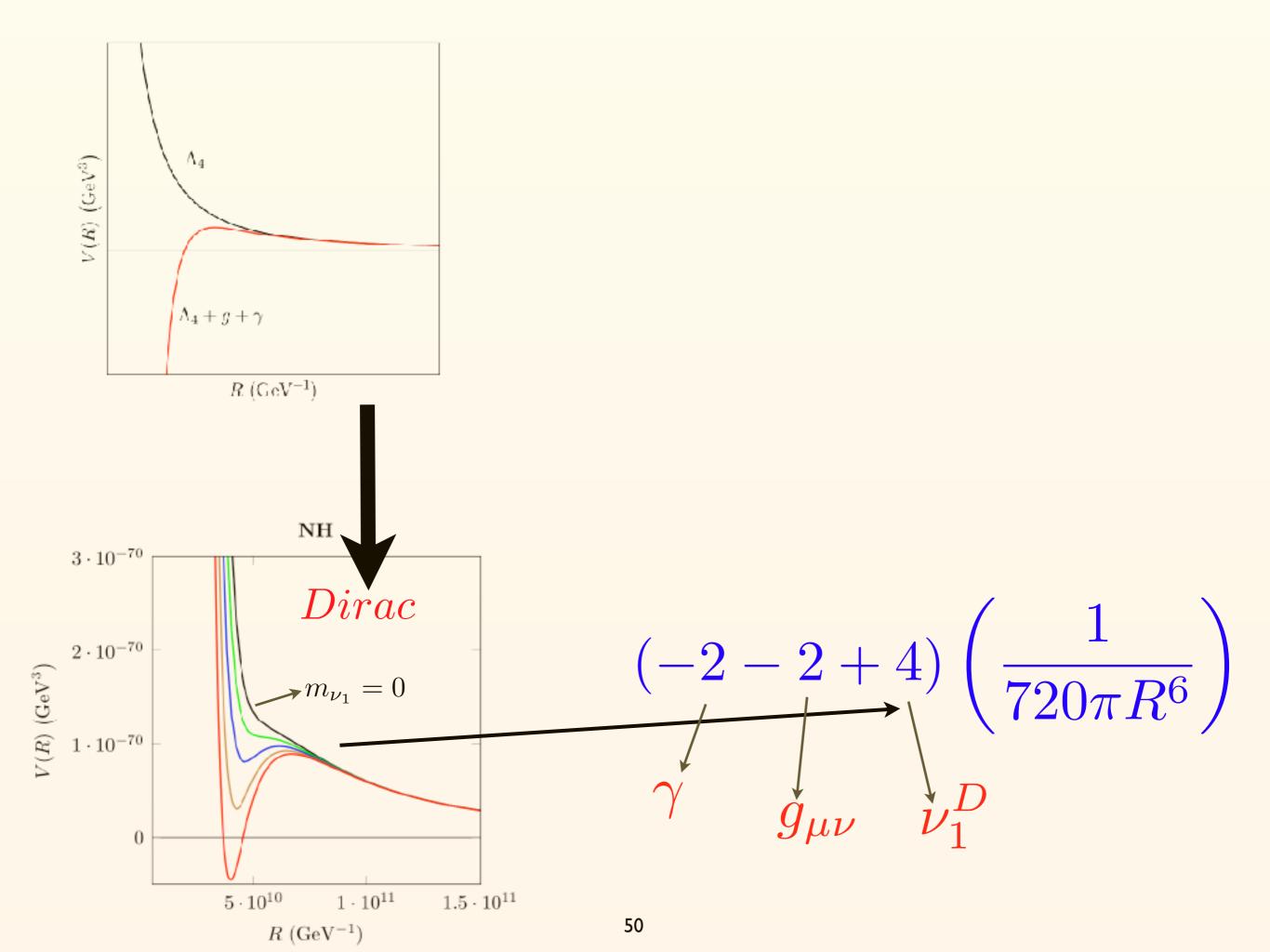
 $\nu_i$  with periodic b.c. contributes positively!!

 $e^{-(m_f/m_{\nu})}$ 

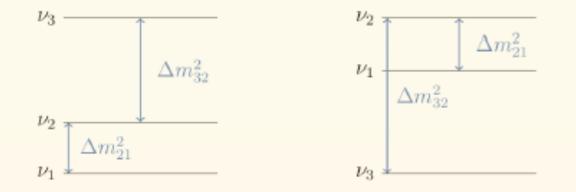
Important: Effect of heavier particles\_suppressed like







### Constraints on neutrino masses



$$\begin{split} \Delta m^2_{21} &= (7.53\pm0.18)\times10^{-5}~{\rm eV}^2,\\ \Delta m^2_{32} &= (2.44\,\pm0.06)\times10^{-3}~{\rm eV}^2~({\rm NH}),\\ \Delta m^2_{32} &= (2.51\pm0.06)\times10^{-3}~{\rm eV}^2~({\rm IH}). \end{split}$$

Majorana: ruled out!! There is always an AdS vacuum for any  $m_{\nu_1}$ Dirac:

	NH	IH
No vacuum	$m_{\nu_1} < 6.7 \mathrm{meV}$	$m_{\nu_3} < 2.1 \text{ meV}$
$dS_3$ vacuum	$6.7 \text{ meV} < m_{\nu_1} < 7.7 \text{ meV}$	$2.1 \text{ meV} < m_{\nu_3} < 2.56 \text{ meV}$
$AdS_3$ vacuum	$m_{\nu_1} > 7.7 \text{ meV}$	$m_{\nu_3} > 2.56 \text{ meV}$

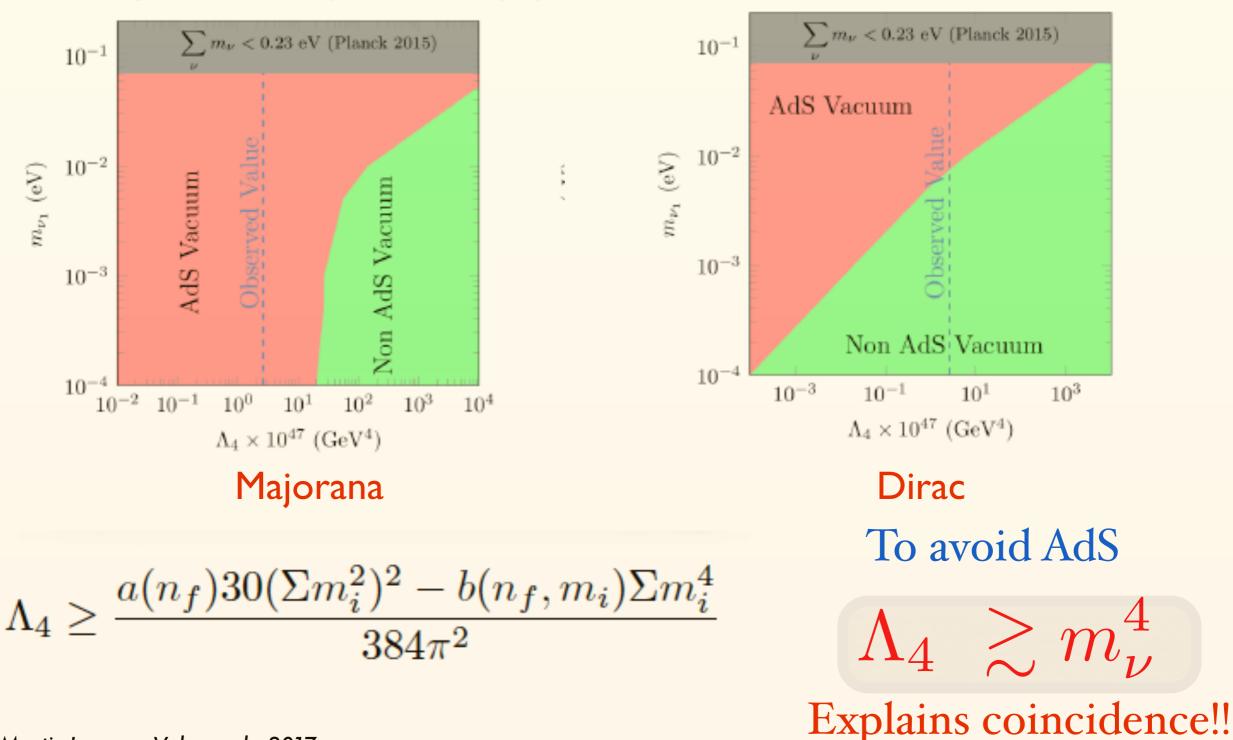
 $m_{\nu_1} < 7.7 \text{ meV (NH)}$  $m_{\nu_3} < 2.1 \text{ meV (IH)}$ 

L.I, Martin-Lozano, Valenzuela 2017 Hamada, Shiu 2017

### Lower bound on the cosmological constant

Cosmological Constant + Dirac Neutrinos (NH)

Cosmological Constant + Majorana Neutrinos (NH)



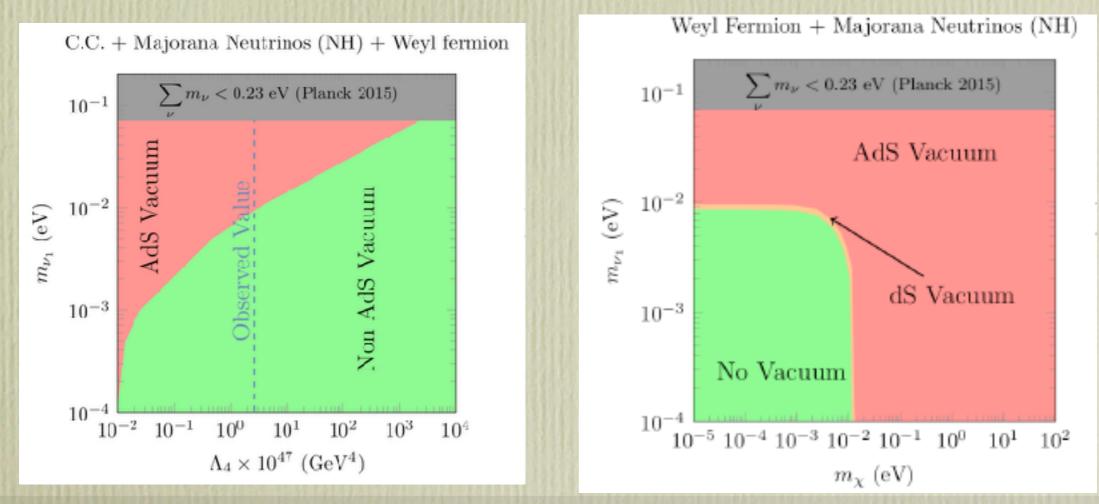
L.I, Martin-Lozano, Valenzuela 2017

First particle physics argument for a non-vanishing c.c. (independent<sup>5</sup>of cosmology)

Constraints with BSM physics: One additional very light Weyl spinor Possitive contribution to Casimir energy

(e.g. axino, hidden sector fermion,...)

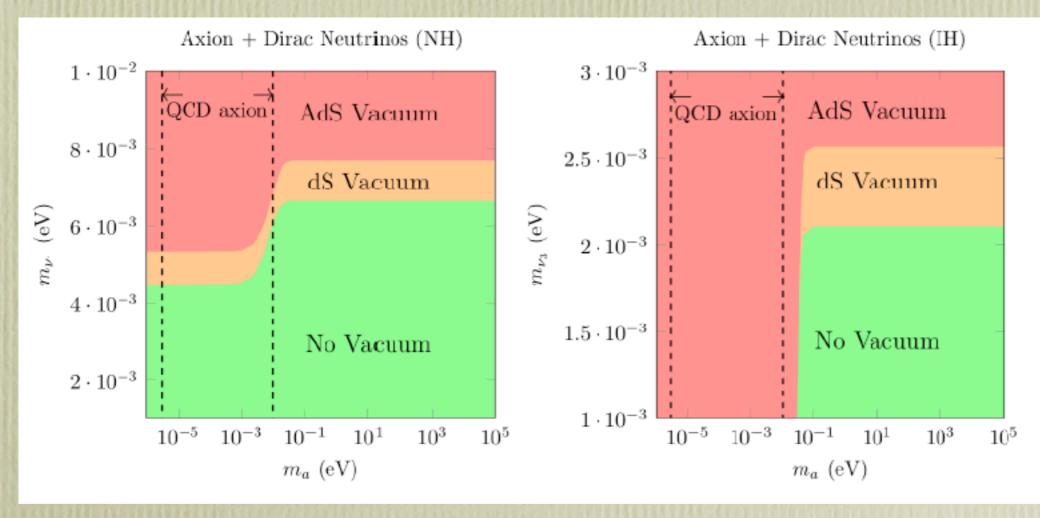
e.g. Majorana, NH



Majorana neutrinos possible for  $m_{\psi}, m_{\nu_1} \leq 10^{-2} eV$ 

L.I, Martin-Lozano, Valenzuela 2017

# 2) One additional very light scalar (e.g. axion) Negative contribution to Casimir energy Majorana : AdS minima deeper Ruled out Dirac:



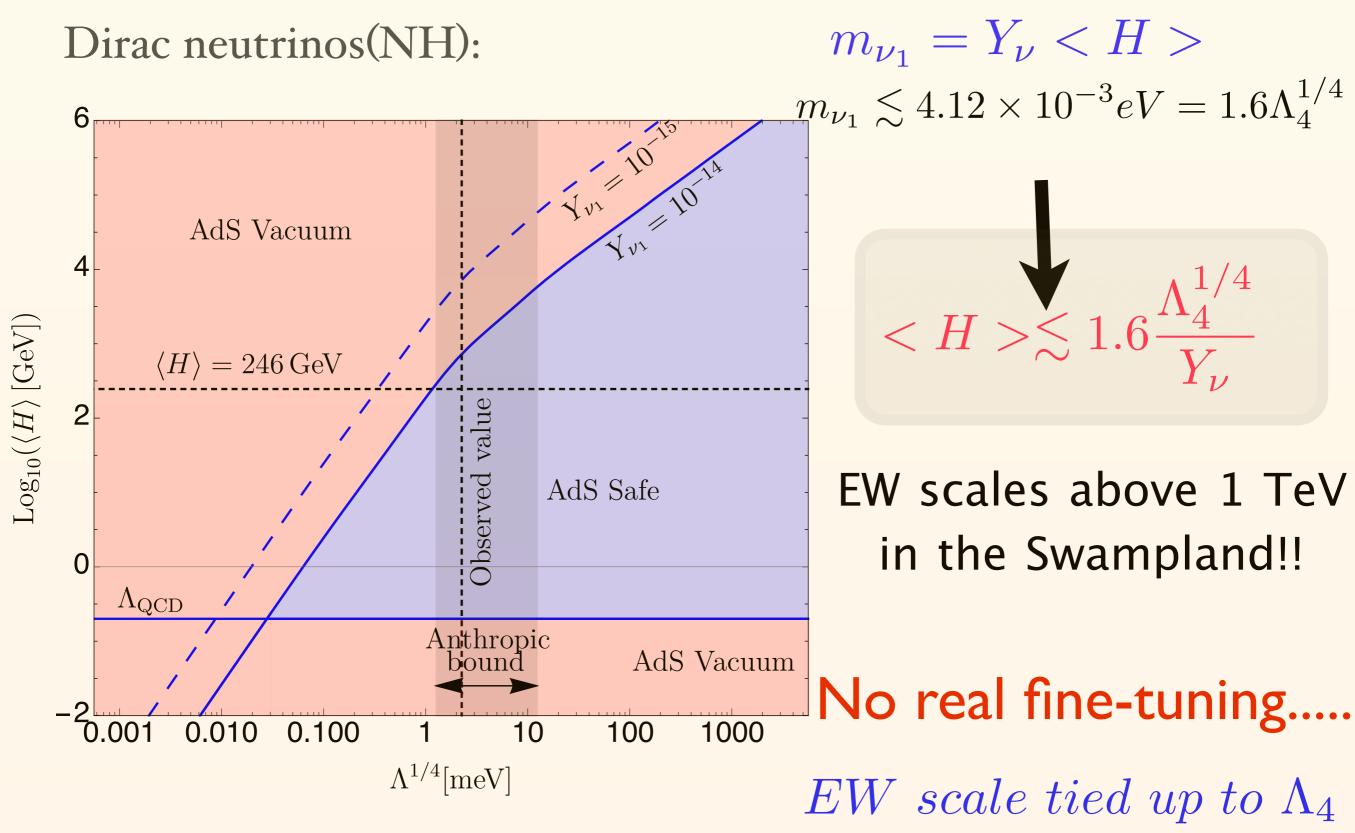
IH Dirac neutrinos incompatible with QCD axion

# Hierarchy problem and the swampland

Dirac neutrinos(NH):

 $m_{\nu_1} = Y_{\nu} < H >$  $m_{\nu_1} \lesssim 4.12 \times 10^{-3} eV = 1.6 \Lambda_4^{1/4}$ 

# Hierarchy problem and the swampland



L.I., Martin-Lozano, Valenzuela 2017; E.Gonzalo, L.I. 2018

# 2) Constraints on axions

$$A^{\mu} \longrightarrow a(x) \ axion$$
  
 $m \leq g \ M_p$   
 $\int \int \frac{1}{f} M_p$   
 $S_{inst} \leq \frac{1}{f} M_p$ 

Axions are 0-forms

Potential under control  $S_{inst} > 1$   $\longrightarrow$   $f \lesssim M_p$ 

Axion inflation:  $V(\phi) = \Lambda^4 (1 - \cos \frac{\phi}{f}) + \dots$ 

Natural inflation, N - flation, ...inconsistent with WGC

Heidenreich, Reece, Rudelius 2015 Montero, Uranga, Valenzuela 2015

# 3) Constraints from the scalar WGC

L. 9., E. Gonzalo 2019, 2020

• Scalar WGC for a single massive scalar H (canonical kinetic term)

$$\left| (\partial_{\phi} m^2)^2 - m^2 (\partial_{\phi}^2 m^2) \right| \ge \frac{m^4}{M_p^2}$$

• You may conjecture that it also applies to the 'modulus' scalar  $\phi$  itself

$$m^2 \longrightarrow \partial_{\phi}^2 V(\phi)$$
$$|(V''')^2 - V''V''''| \ge \frac{(V'')^2}{M_p^2}$$

• The idea is that scalar interactions should be stronger than gravity

 $|(V''')^2 - V''V''''| \ge \frac{(V'')^2}{M^2}$ 

- If this applies for any scalar, a very strong constraint !
- Note a linear potential  $V = a\phi$  is always a solution
- Pure quadratic, with no other interaction is not a solution
- Some tests:  $V = -cos(\phi/f)$
- Axion potential:

$$\frac{1}{f^6} \left| \sin^2(\phi/f) + \cos^2(\phi/f) \right| \ge$$

 $f \leq M_p$ 

$$\frac{\cos^2(\phi/f)}{f^4m_p^2}$$

 Consistent with other Swampland results

• Quartic real scalar coupling:  $V = \frac{m_0^2}{2}\phi^2 + \frac{\lambda}{4!}\phi^4$ 

- For  $\phi \to 0 \longrightarrow |\lambda| \ge (m_0^2/M_p^2)$  consistent with WGC intuition
  - It must be  $m^2(\phi) \neq \lambda \phi^2 for \ all \ \phi$

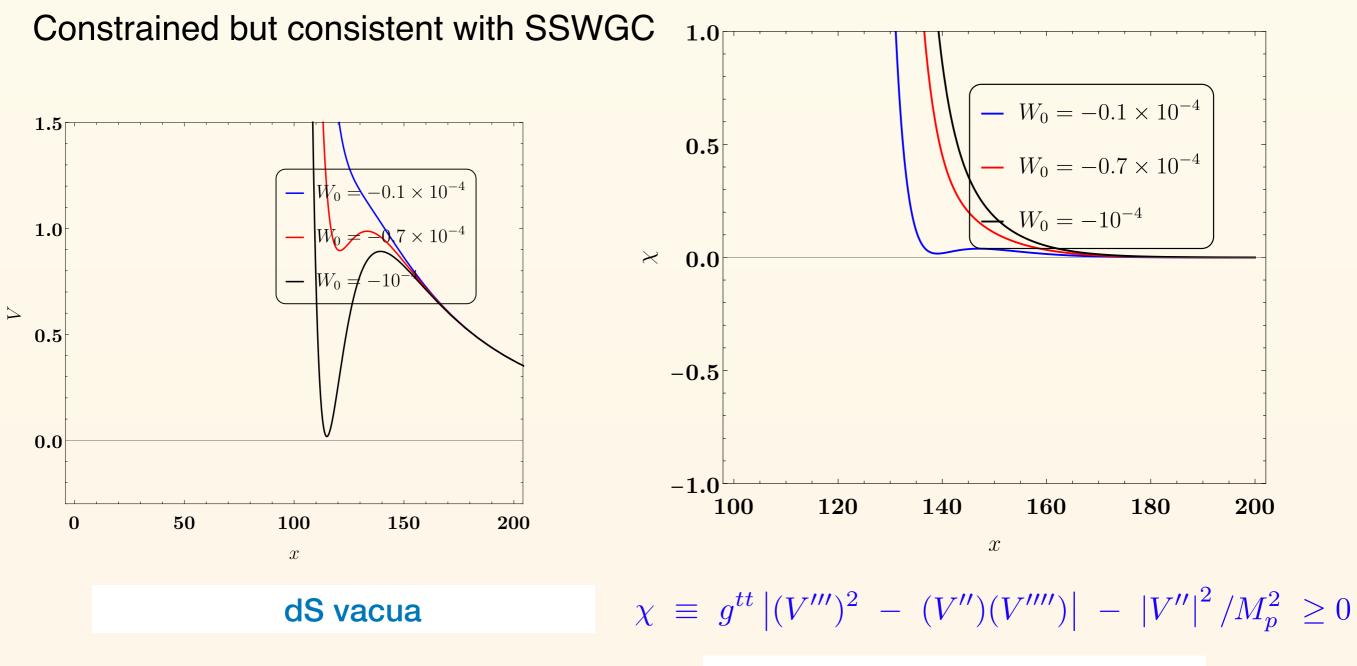
• It would be very interesting to generalize to more realistic case of the SM (gauge couplings, top Yukawa, running.....)

• In particular, the fact that  $\lambda(h) \rightarrow 0$  at  $\sim 10^{11} GeV$  in the SM perhaps would imply interaction becomes weaker than gravity there ?

**New Physics** (like SUSY) at (or before) an intermediate scale

Another application:

#### Moduli fixing in string vacua : E.g. KKLT



Violated if  $W_0$  made too small....

SUSY broken at a large scale

#### It may violate the dS conjecture but not the SSWGC

# 4) Constraints from dS Swampland conjecture

dS Swampland conjecture

Ooguri, Palti, Shiu, Vafa 2018

$$|
abla V(\phi)| \geq rac{\mathcal{O}(1)}{M_p} V(\phi)$$
 or else

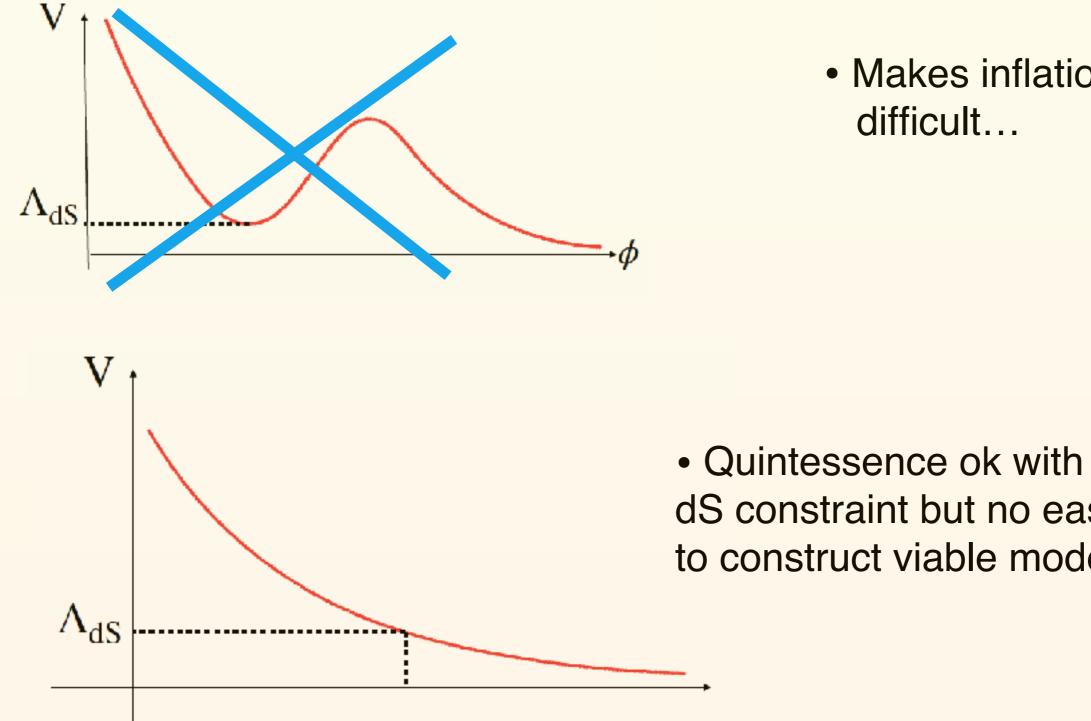
$$\min(\nabla_i \nabla_j V(\phi)) \le -\frac{\mathcal{O}(1)}{M_p^2} V(\phi)$$

Sufficiently unstable maxima

• Minima should have  $\nabla V(\phi) = 0$ ,  $min(\nabla_i \nabla_j V(\phi)) > 0$ Forbids dS vacua

 It is true that (unlike AdS) finding dS minima in string theory has shown to be very difficult (some people claim impossible)

• The canonical example of KKLT is being scrutinised in detail now..... So far, it is fair to say it is alive.....



Makes inflation very

• Quintessence ok with the dS constraint but no easy to construct viable models...

- The Trans-Planckian Censorhip Conjecture (TCC) Bedroya, Vafa 2019
- In cosmological expansion 'no length scales which exit the Hubble horizon could ever had a wavelength smaller than the Planck length'

$$a_i > a_f \frac{H_f}{M_p}$$

- Limits inflation strongly:  $V^{1/4} \leq 10^9 GeV$  ,  $r < 10^{-30}$ 
  - For large field predicts

$$|V'| \ge \frac{2}{\sqrt{((d-1)(d-2))}}V$$

This particular constraint tested in many string compactifications

# 5) Other systems constrained by WGC

Bounds on (Stuckelberg) mass of the photon

M. Reece, 2018

Constraints on clock-work mechanism

L. I., M. Montero, 2017

• Relaxions: constraints on the UV scale

L. I. Montero, Uranga, Valenzuela 2015



1) Quantum gravity constraints effective field theories and may affect SM physics and cosmology in ways not previously foreseen

2) It is important to advance along two parallel lines:

Better understand the origin and structure of the WGC/Swampland ideas

Apply them to address pending issues in BSM physics and Cosmology



#### Swamp





#### land