06 April 2020

Newton 1665 seminars

Physics beyond the standard model from Higgs Parity

Keisuke Harigaya

(Institute for Advanced Study)

Hall and KH :1803.08119, 1905.12722

Dunsky, Hall and KH :1902.07726, 1908.02756

Standard Model

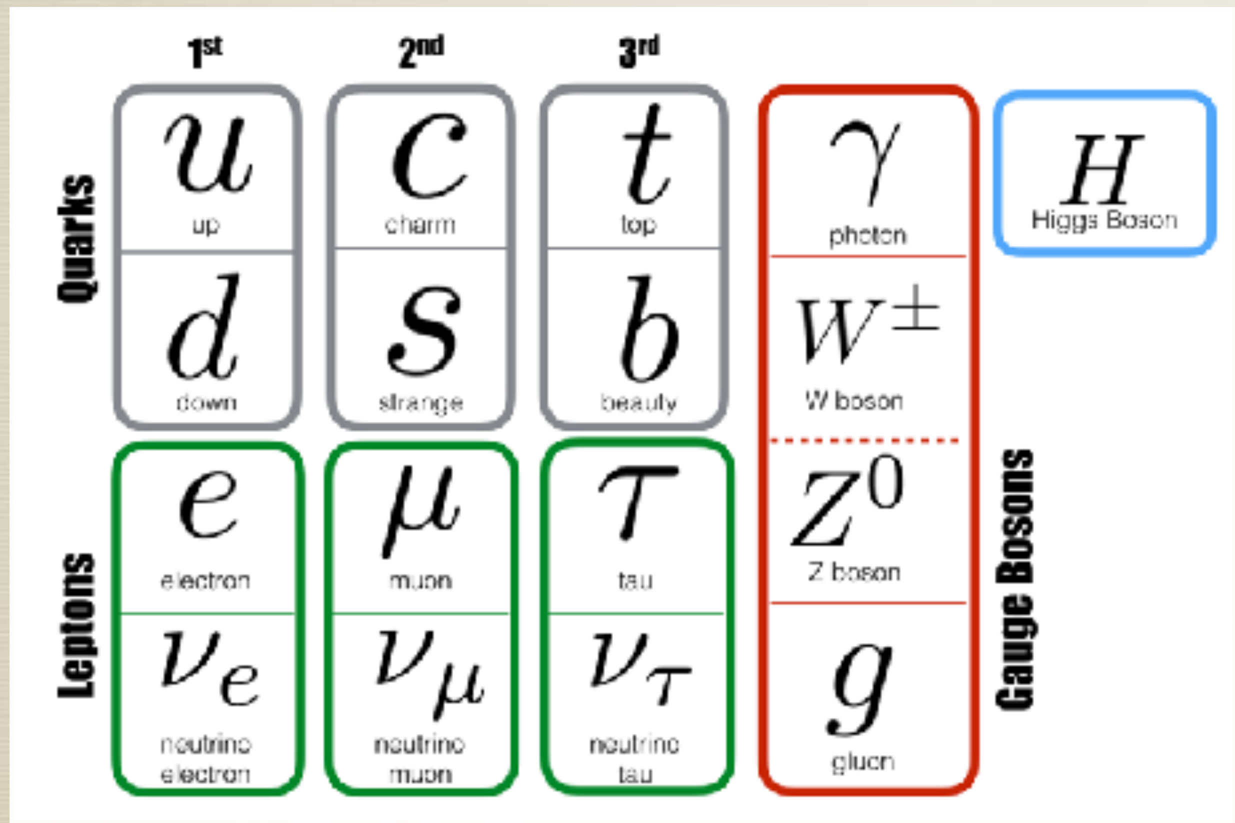
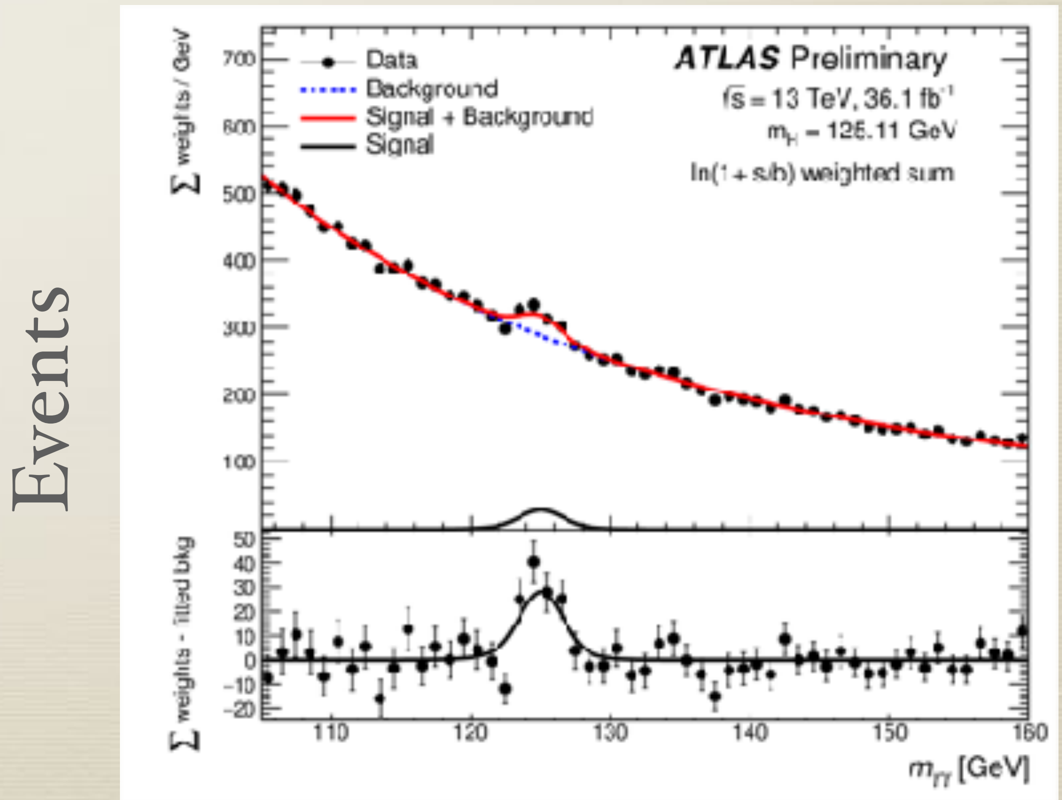


figure from www.physik.uzh.ch



Invariant mass

Precise measurements

* Higgs mass $m_h = 125.18 \pm 0.16$ GeV
* Top quark mass $m_t = 173.1 \pm 0.4$ GeV
* Strong coupling constant $\alpha_s(m_Z) = 0.1184 \pm 0.0011$
* ...

Can we learn something beyond the Standard Model ?

nature of dark matter, mass of new particles, rare decays, etc.

Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

New symmetry
Higgs Parity

* is part of a grand unified gauge symmetry
* solves the strong CP problem
* (gives a dark matter candidate)

Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

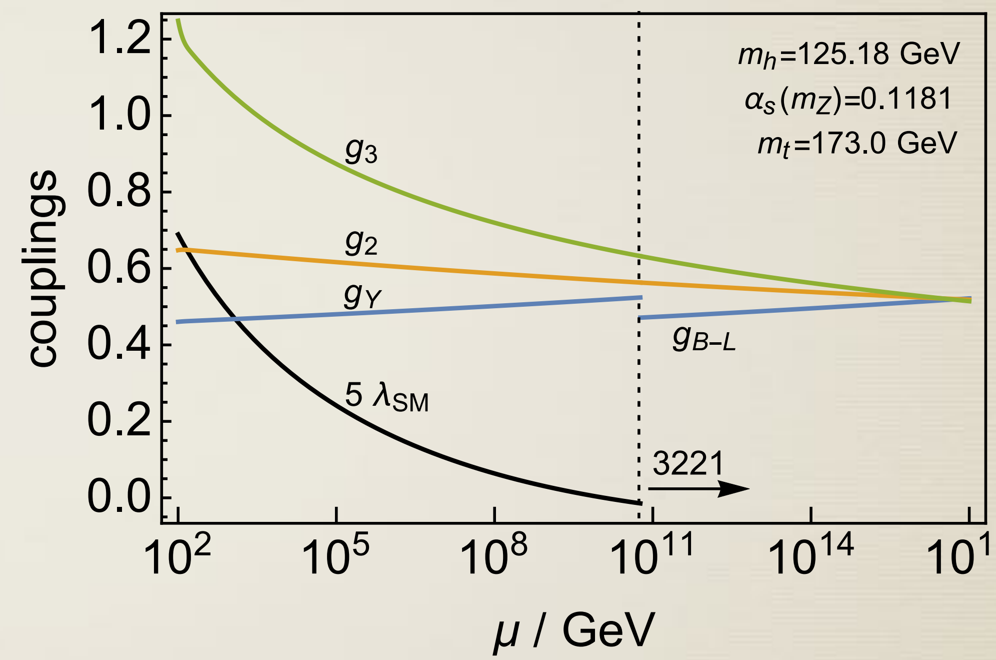
top quark mass
Higgs mass
strong coupling constant

Higgs Parity
symmetry
breaking scale

Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



Higgs Parity
symmetry
breaking scale

UV physics,
experimental signatures

Grand unification, proton decay

Dark matter detection rate, neutron EDM,
gravitational waves, dark radiation, warm dark matter, ...

Outline

* Introduction (continued)
* Higgs Parity
* Grand unification and proton decay
* Summary and outlook

Introduction

Standard Model

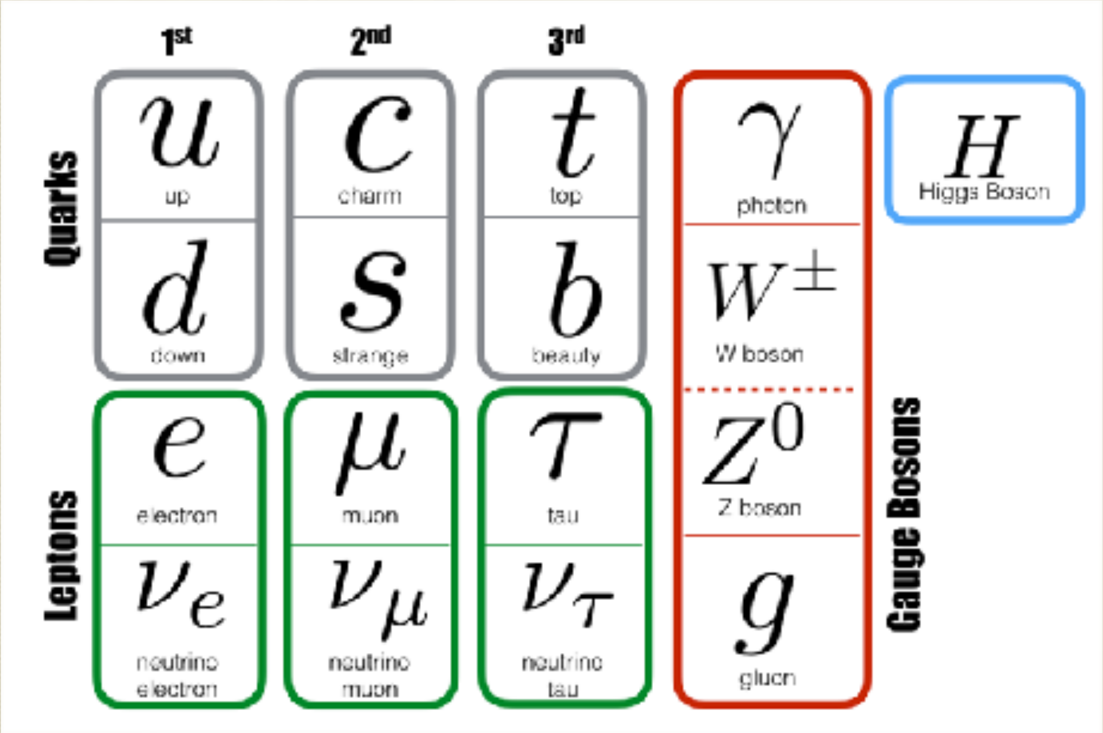
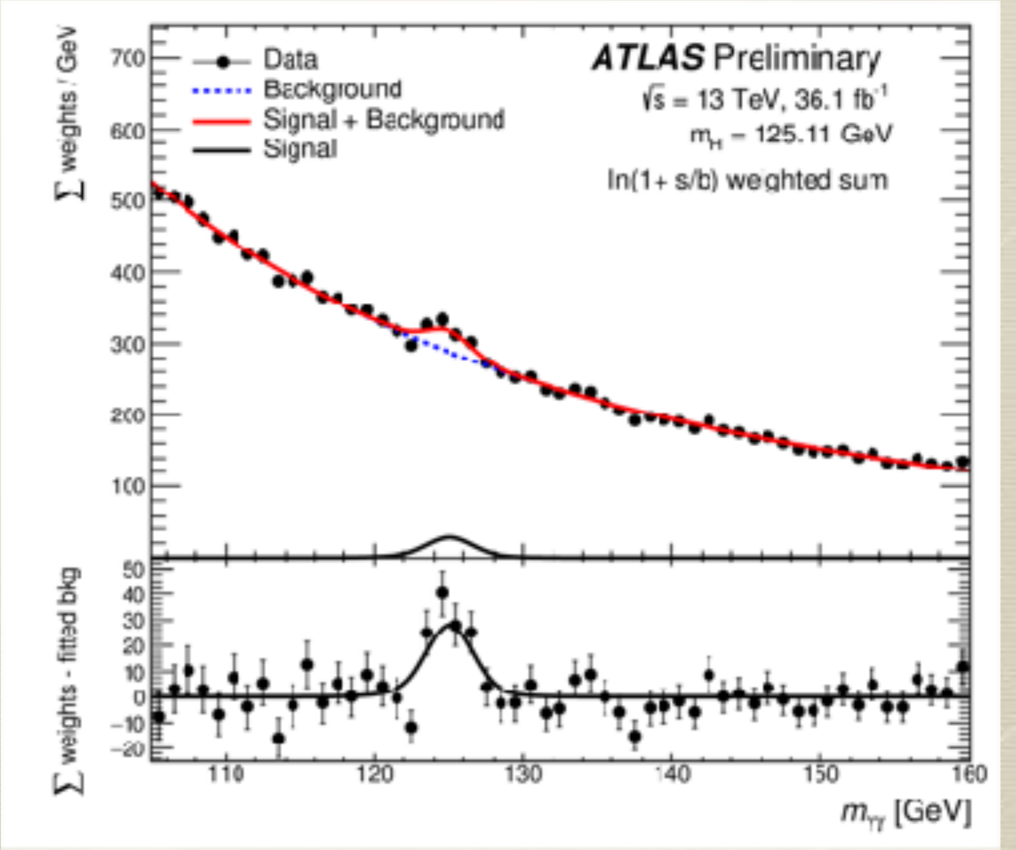


figure from www.physik.uzh.ch



CERN, 2013

Picture from Recondito.org

CERN, 2013

Picture from Recondito.org

We are far away from the goal

* What is dark matter?
* How was the baryon asymmetry of the universe created?
* Why does QCD preserve CP symmetry?
* What sets the Higgs potential parameters?
* ...

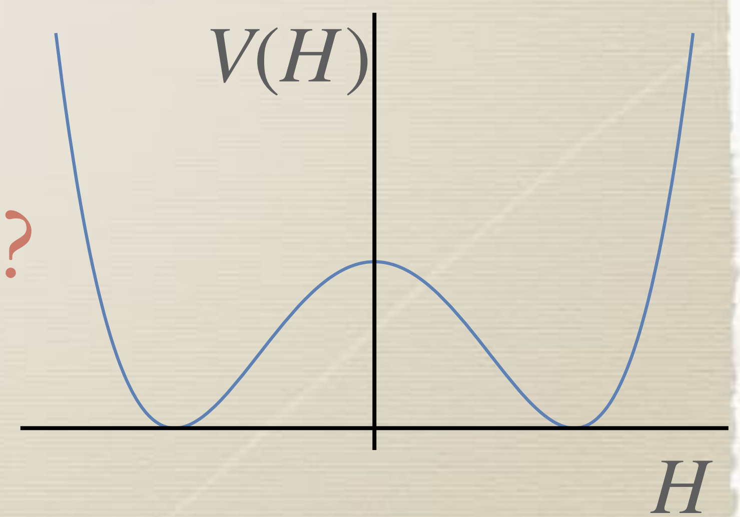
We are far away from the goal

Raymond Co's talk

* What is dark matter?
* How was the baryon asymmetry of the universe created?
* Why does QCD preserve CP symmetry?
* What sets the Higgs potential parameters?
* ...

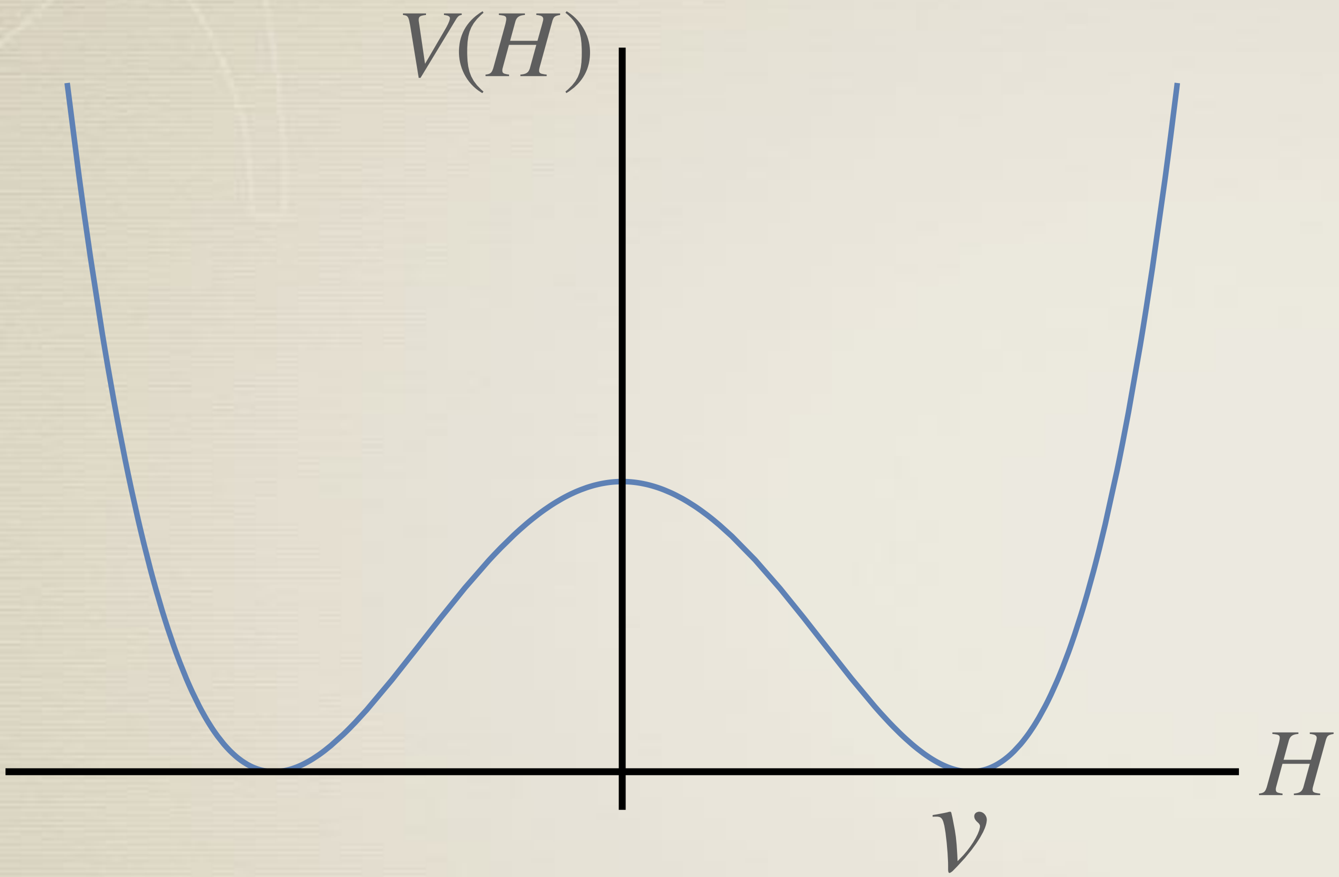
We are far away from the goal

* What is dark matter?
* How was the baryon asymmetry of the universe created?
* Why does QCD preserve CP symmetry?
* What sets the Higgs potential parameters?
* ...



$$V(H) = \lambda_{\rm SM} \left(|H|^2 - v^2 \right)^2$$

Higgs potential



$$V(H) = \lambda_{\rm SM}\left(|H|^2 - v^2\right)^2$$

A question of few decades:
What sets the mass scale of Higgs?

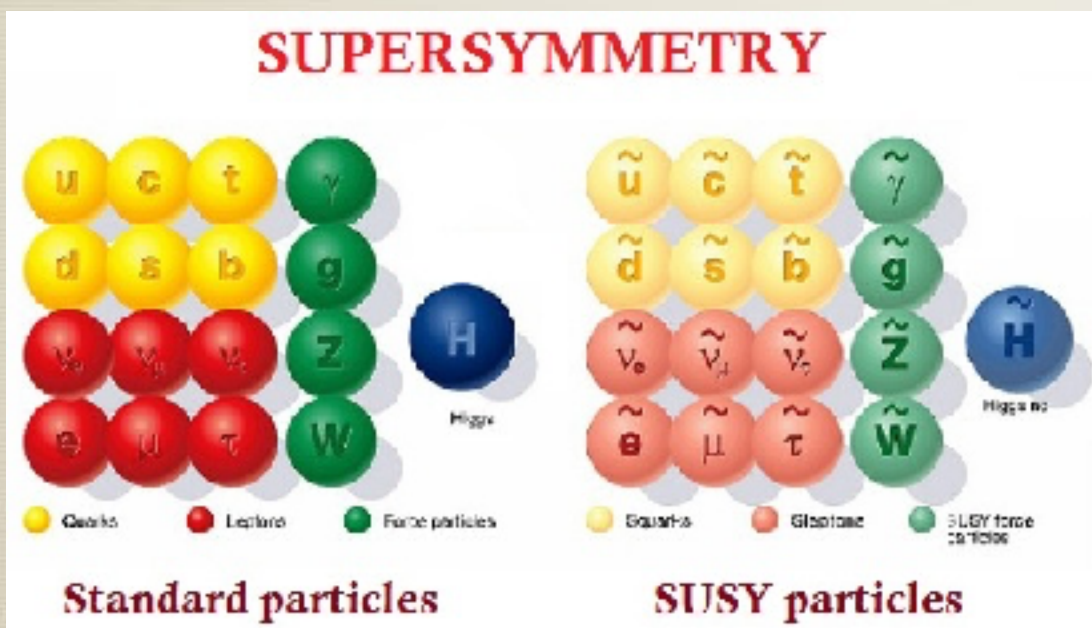
$v = 173$ GeV $\ll$ (Planck scale, GUT scale)

Hierarchy problem

Higgs potential

What sets the small mass scale of Higgs?

Ex. Supersymmetry, composite Higgs



CERN & IES de SAR

Higgs mass scale is naturally much smaller than the Planck scale

Maiani (1979), Veltman (1979), Witten (1981), Kaul (1982), Kaplan and Georgi (1984) Kaplan, Georgi and Dimopoulos (1984)

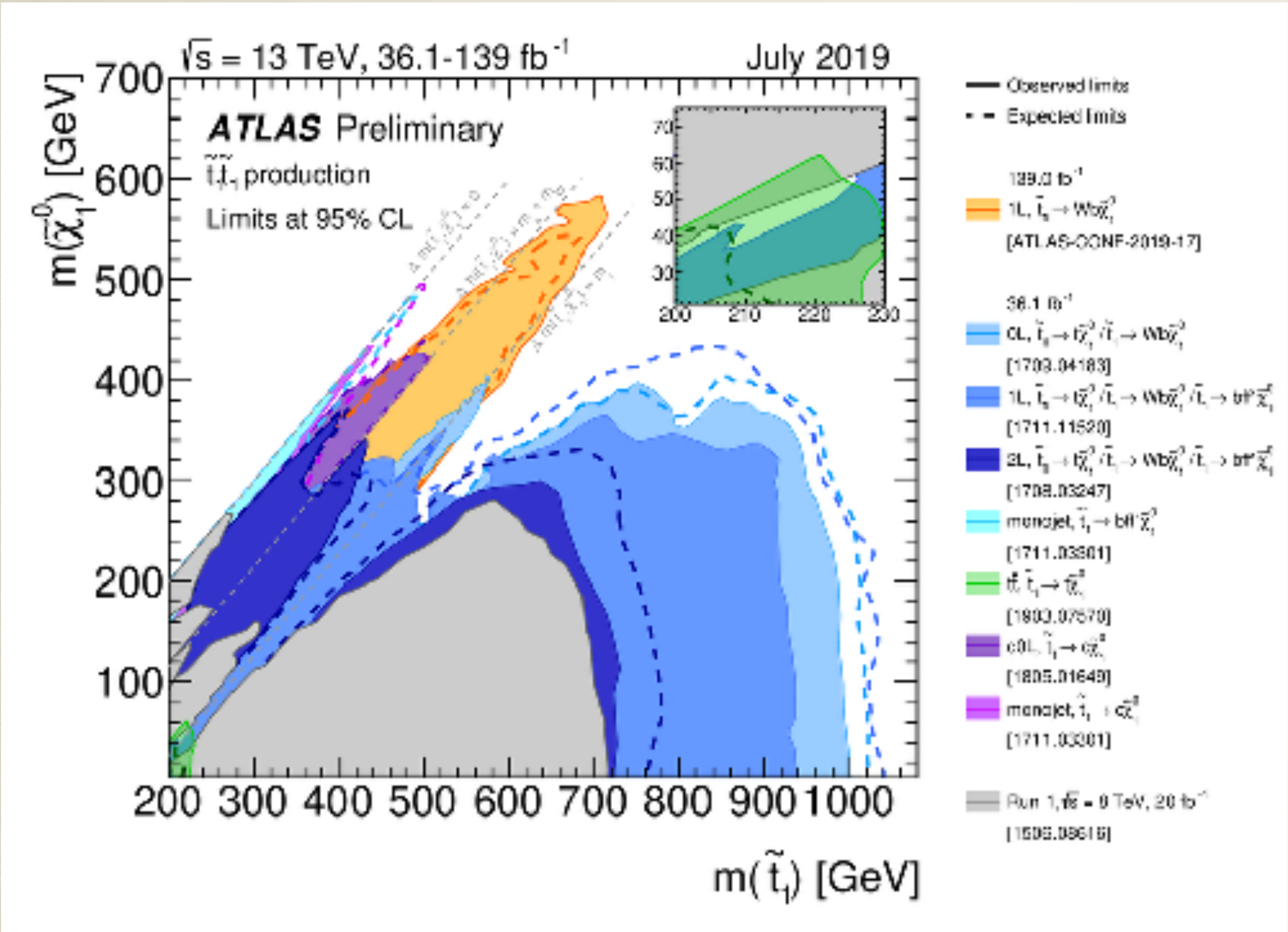
$$m_{\text{SUSY}}, m_{\text{composite}} \propto \exp\left(-\frac{8\pi^2}{g^2}\right)$$

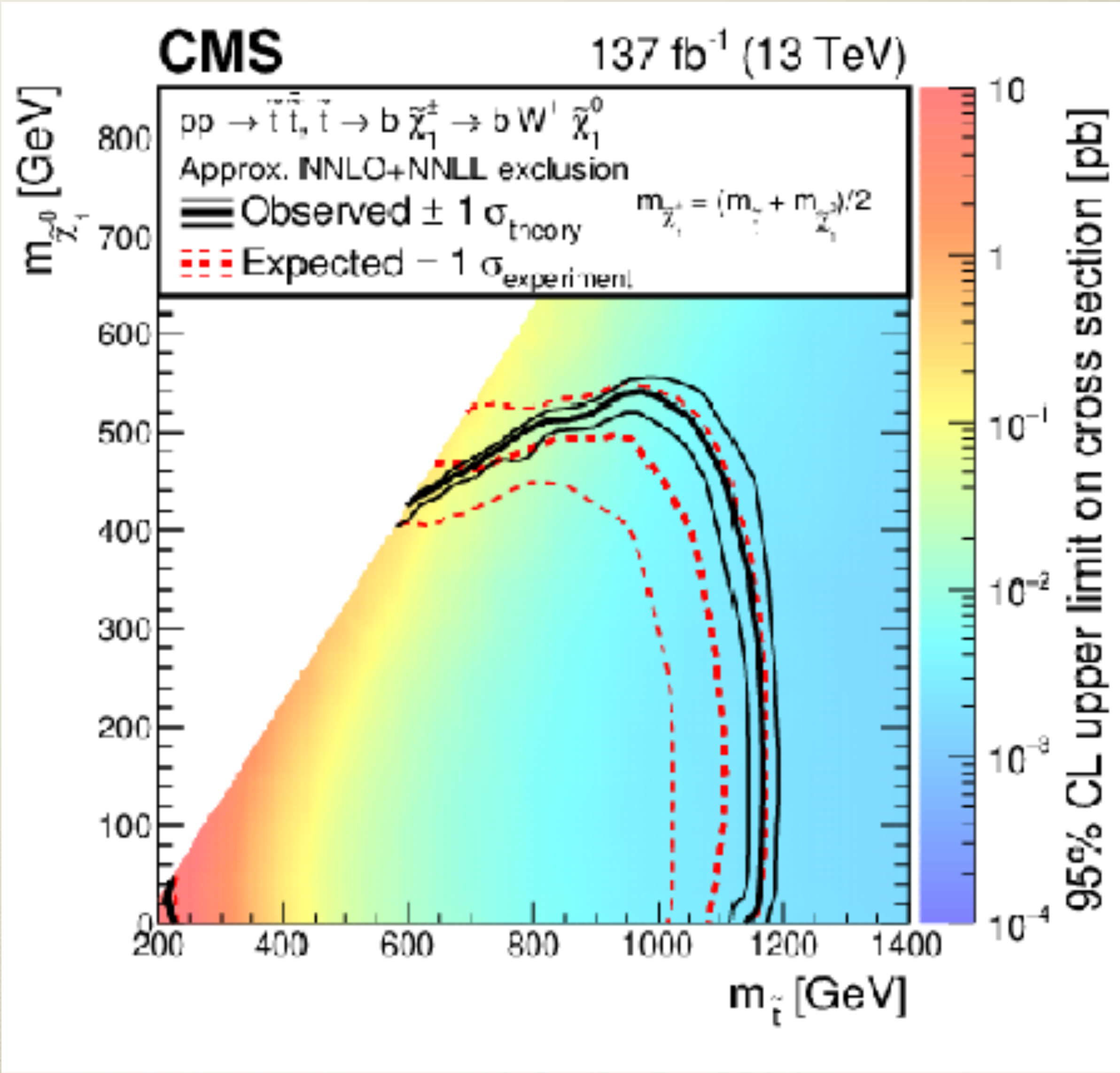
predict new particles with masses around 100 GeV

100 GeV scale new physics

New particles have not yet been found so far

Ex. Constraints on stop and neutralino masses in MSSM





Fine-tuned Higgs mass?

$$V(H) = \lambda_{\mathrm{SM}} \left(|H|^2 - v^2 \right)^2$$

We are not sure if the small Higgs mass is a guiding principle to look for new physics

The small Higgs mass may be explained by theoretical ideas which are difficult to probe experimentally

Ex. Multiverse and anthropic selection

Weinberg (1987), Susskind (2003), Agrawal, Barr, Donoghue and Seckel (1998), Clavelli and White (2006), Hall, Pinner and Ruderman (2014), D'Amico, Strumia, Urbano and Xue (2019), …

Fine-tuned Higgs mass?

$$V(H) = \lambda_{\rm SM} \left(|H|^2 - v^2 \right)^2$$

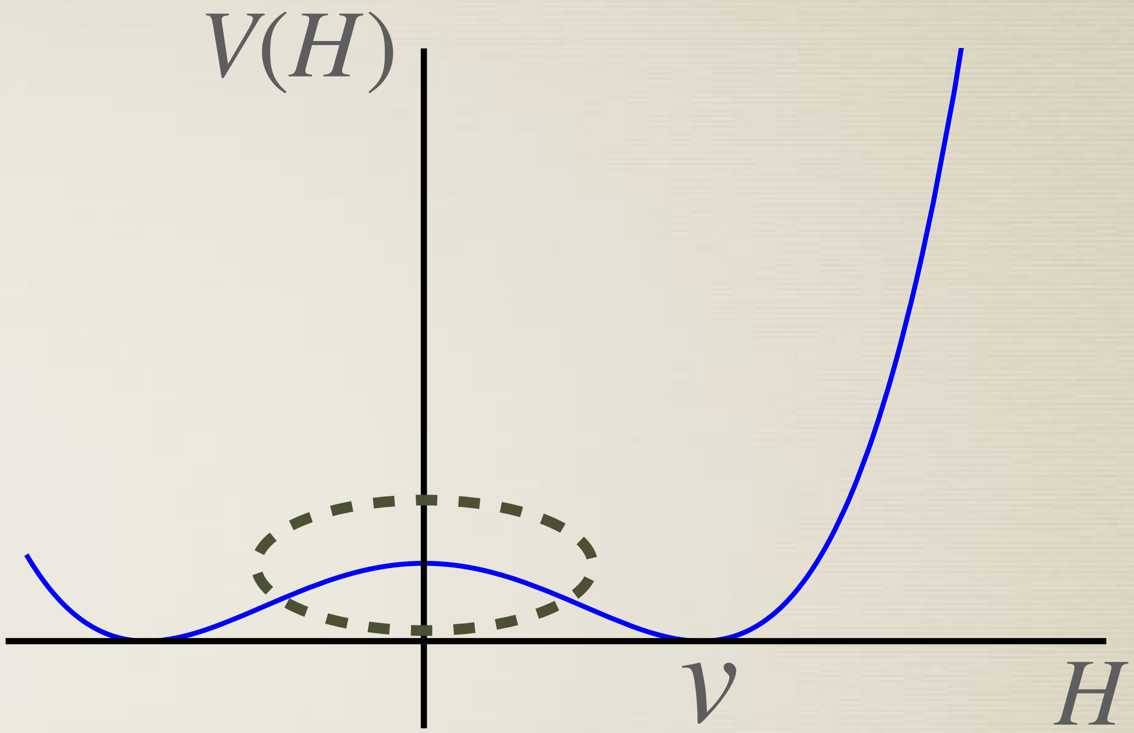
We are not sure if the small Higgs mass is
a guiding principle to look for new physics

I will postulate fine-tuned Higgs mass and look for another clue

Higgs mass

$$V(H) = \lambda_{\rm SM}\left(|H|^2 - v^2\right)^2$$

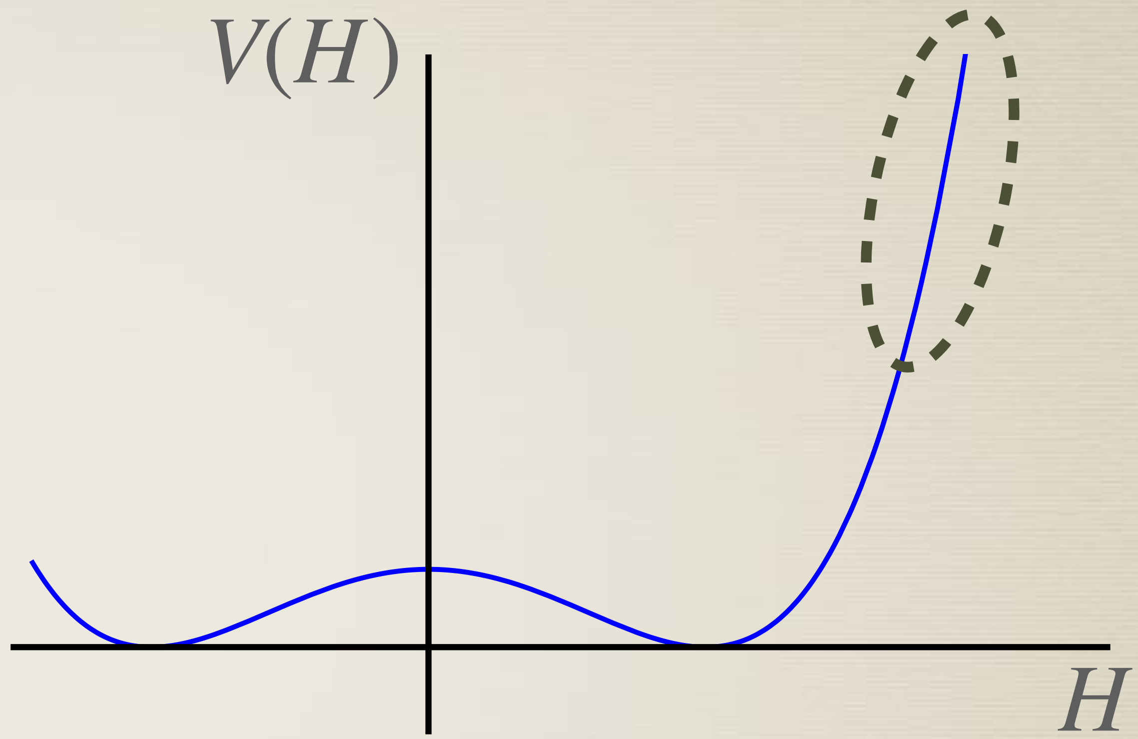
$(173\mathrm{GeV})^2$



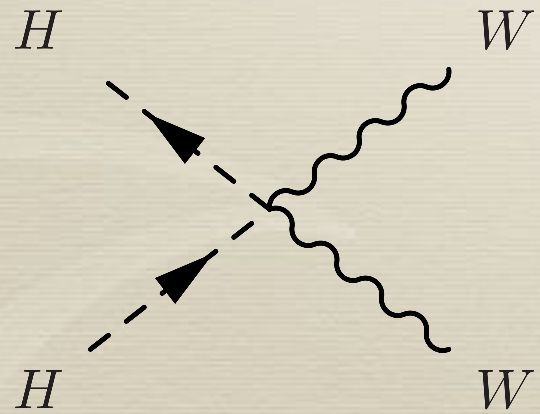
Higgs self-interaction?

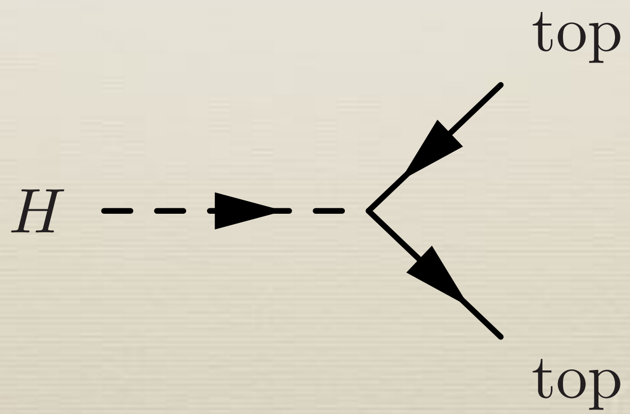
$$V(H) = \lambda_{\rm SM}\left(|H|^2 - v^2\right)^2$$

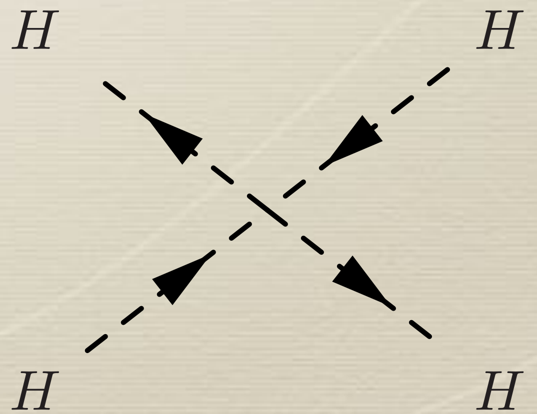
$m_h^2/(4v^2) \simeq 0.13$



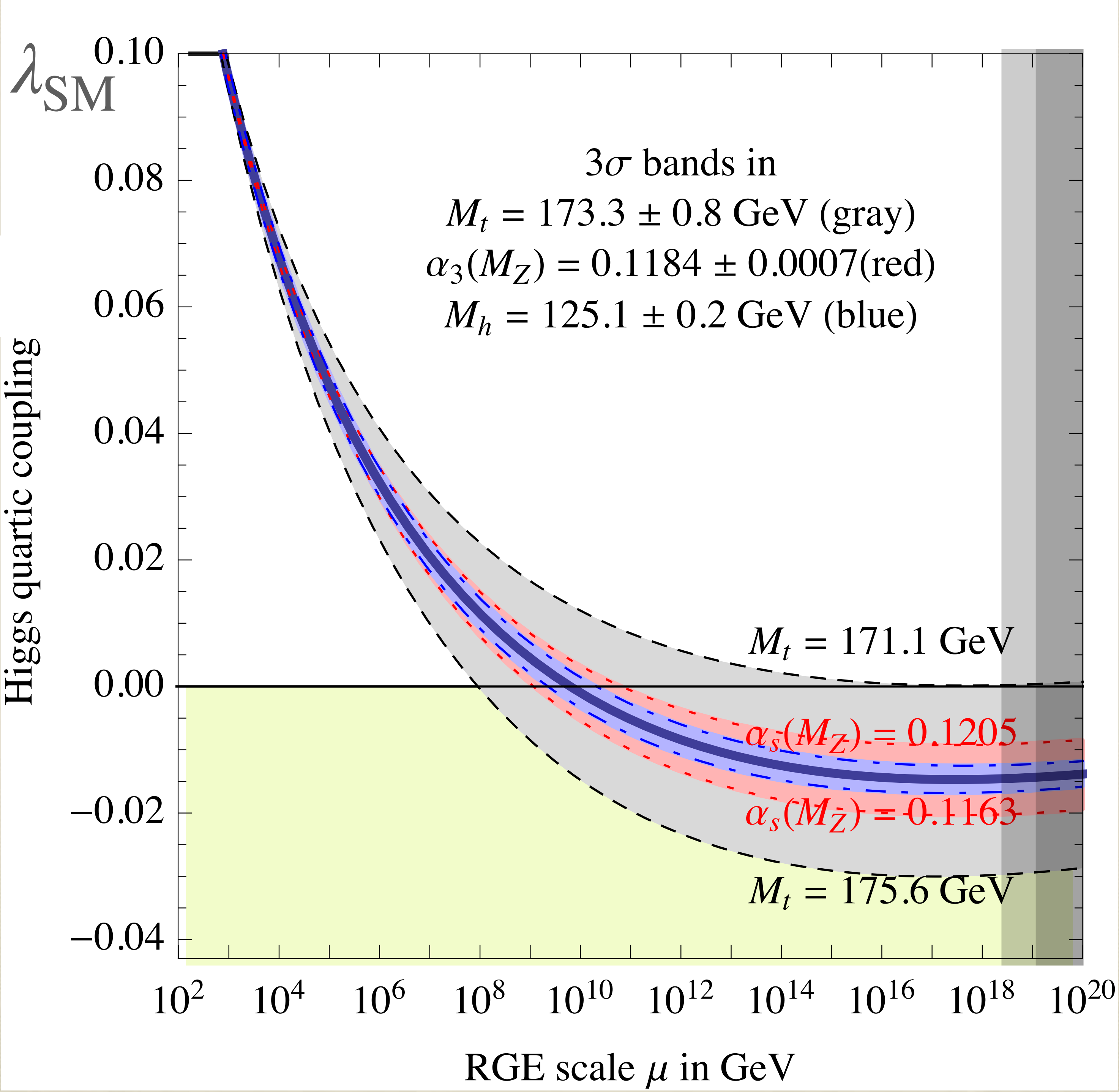
Let us examine the quartic coupling,
assuming that the standard model is valid up to high energy scales,
including quantum corrections





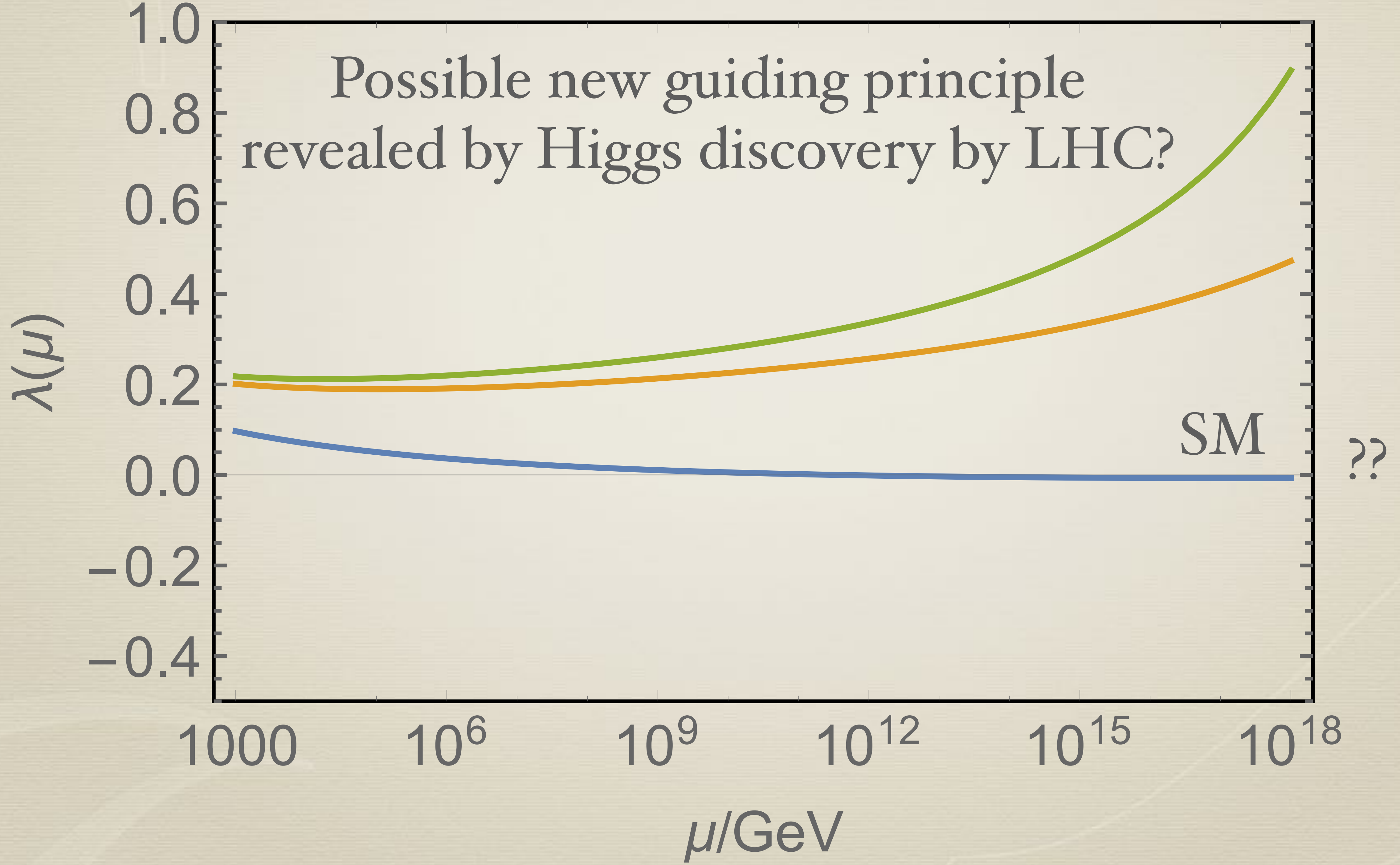


Small quartic coupling



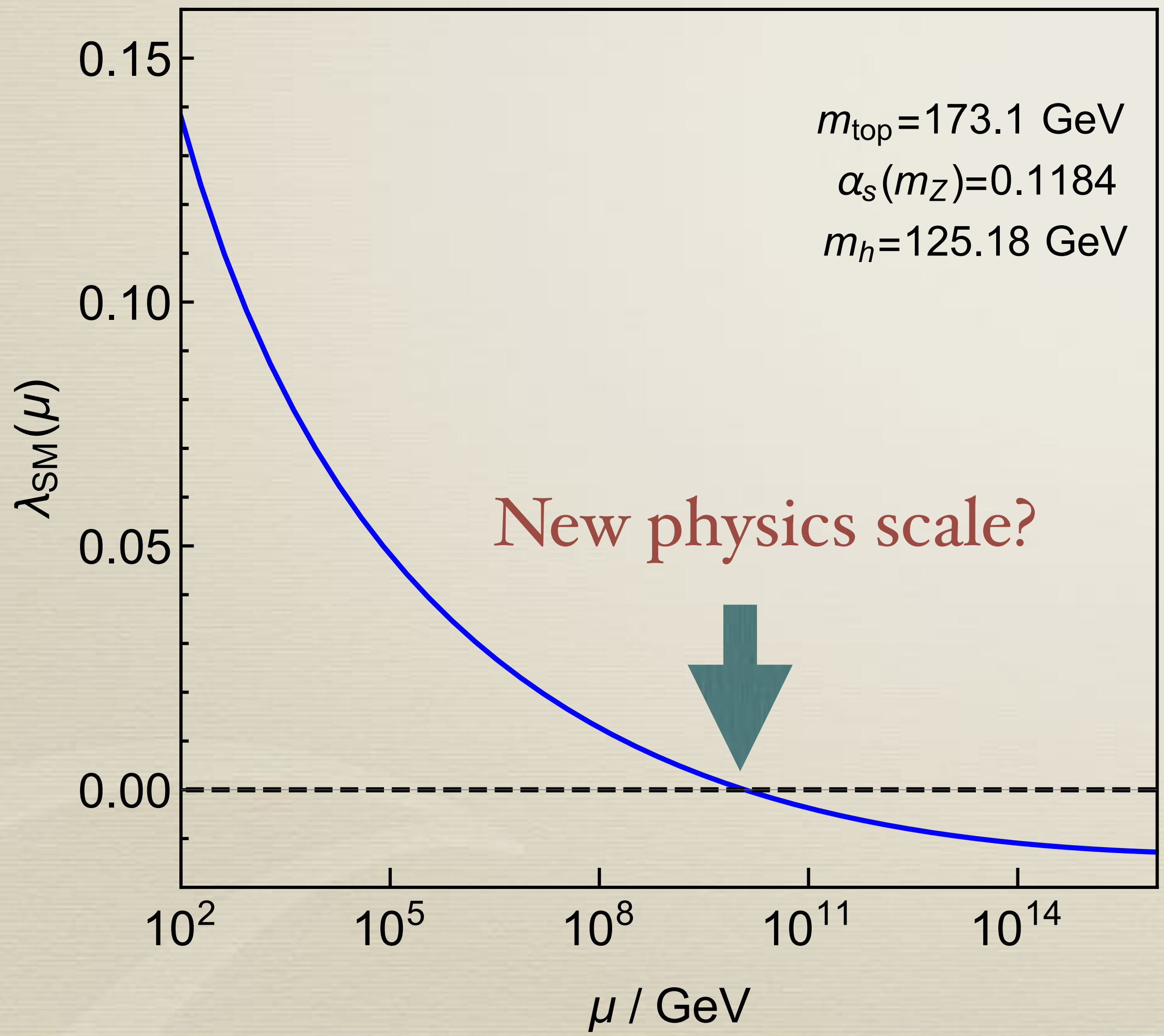
Buttazzo, Degrassi, Giardino, Giudice, Sala, Salvio and Strumia (2013)

Small quartic coupling



New physics?

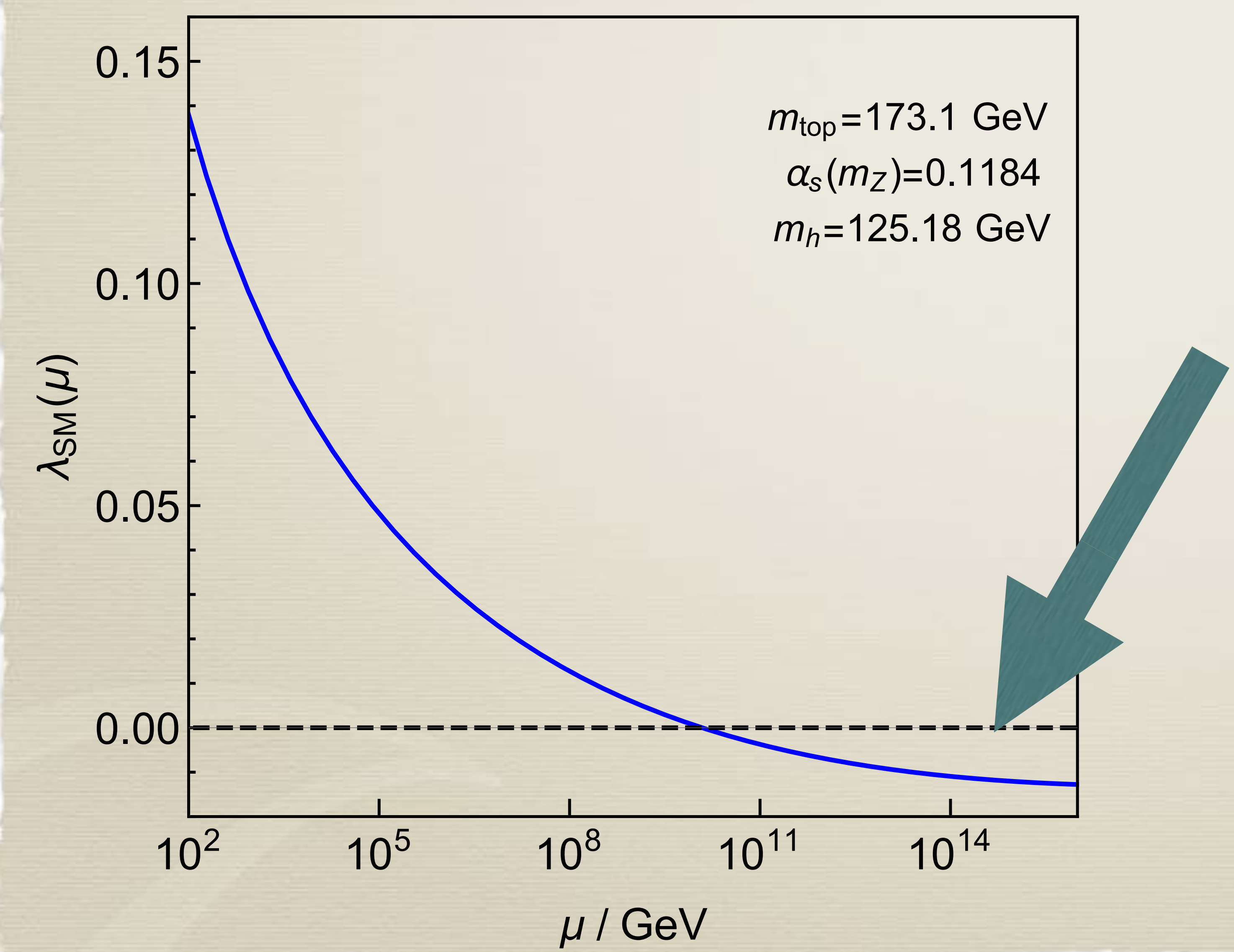
Conjecture : some new physics which couples to Higgs sets $\lambda_{SM} \simeq 0$ at a high energy scale



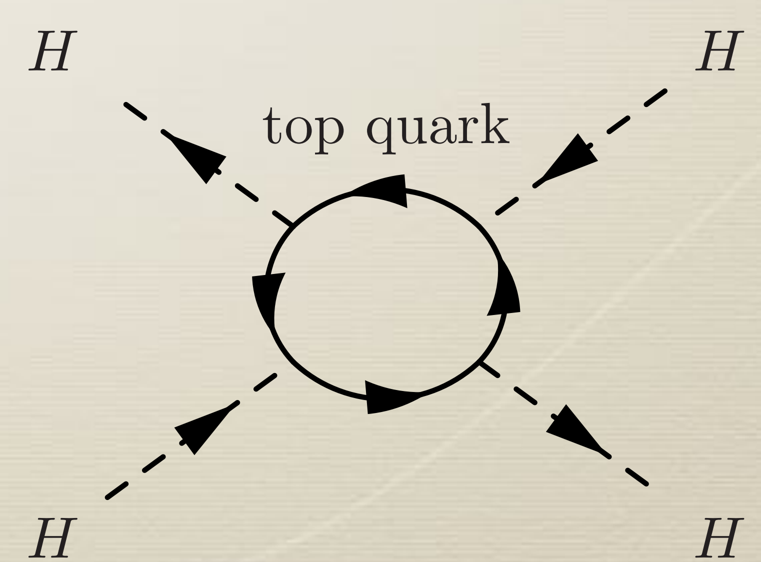
PQ symmetry? Redi and Strumia (2012)
Supersymmetry? Hall and Nomura (2013), Ibe, Matsumoto and Yanagida (2013)

New physics?

Conjecture : some new physics which couples to Higgs sets $\lambda_{\rm SM} \simeq 0$ at a high energy scale

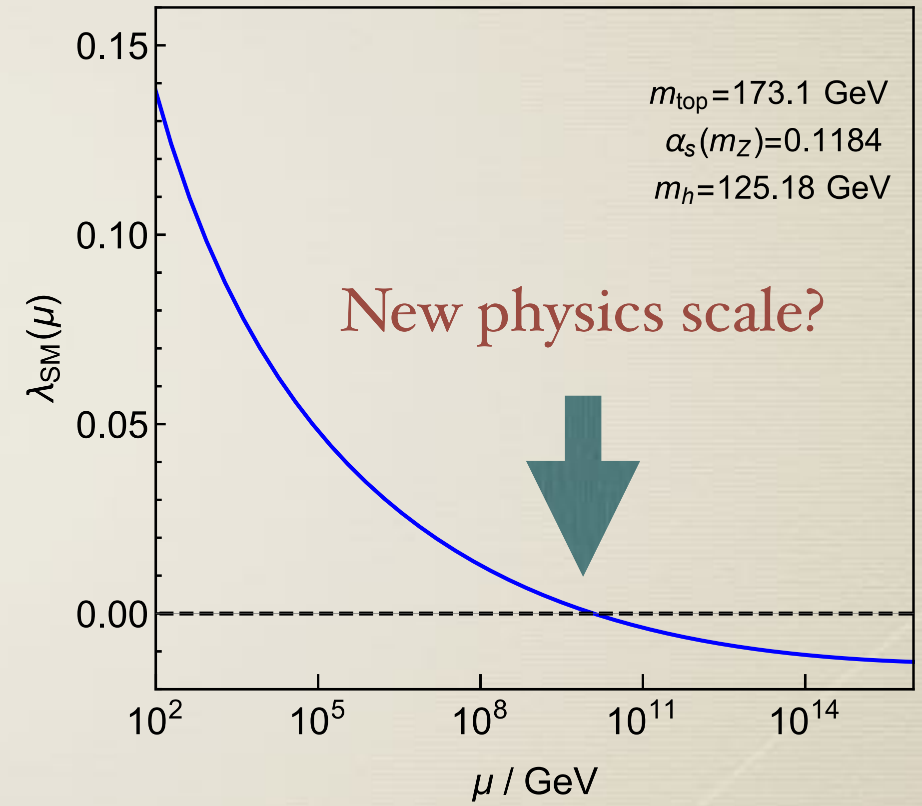


Quartic coupling assuming Standard Model would remain small due to small yukawa coupling at high energy



Precise measurement and new physics?

top quark mass
Higgs mass
strong coupling constant

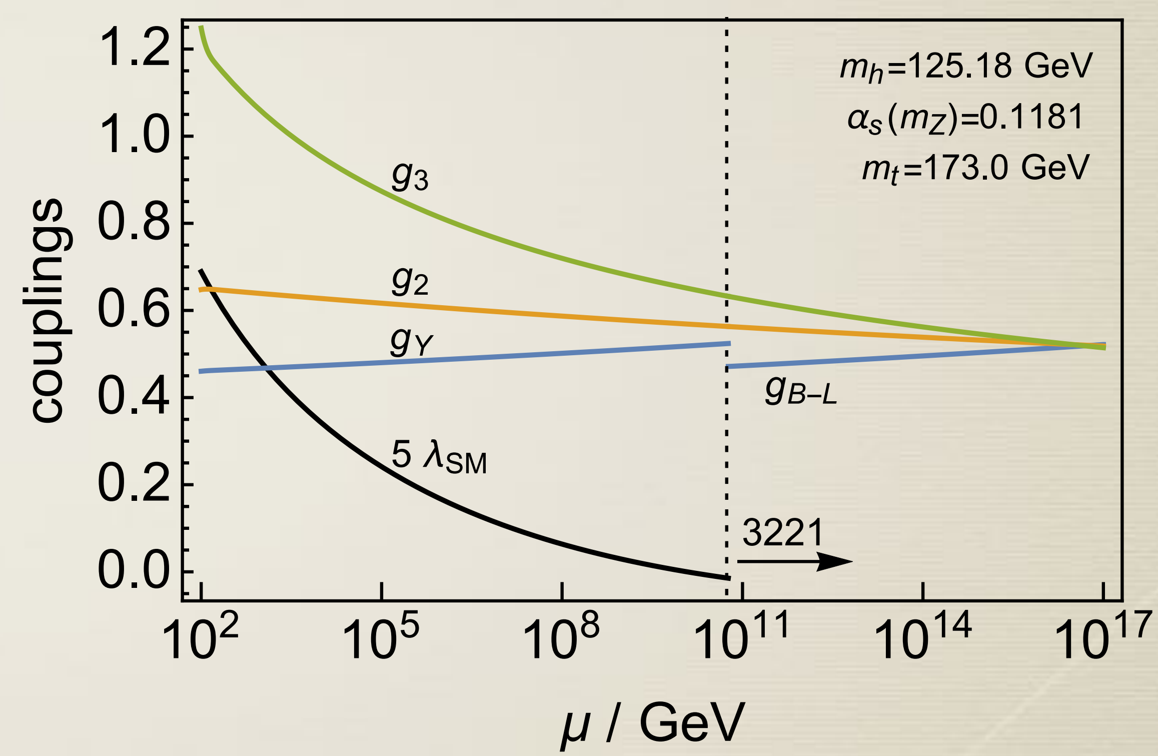


scale of the new physics ⟷ further UV physics, experimental signals?

Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



New symmetry
(Higgs Parity)
breaking scale

Grand unification
proton decay

Dark matter detection rate, neutron EDM, gravitational waves, dark radiation, warm dark matter, ...

Outline

* Introduction
* Higgs Parity
* Grand unification and proton decay
* Summary and outlook

Z_2 symmetry

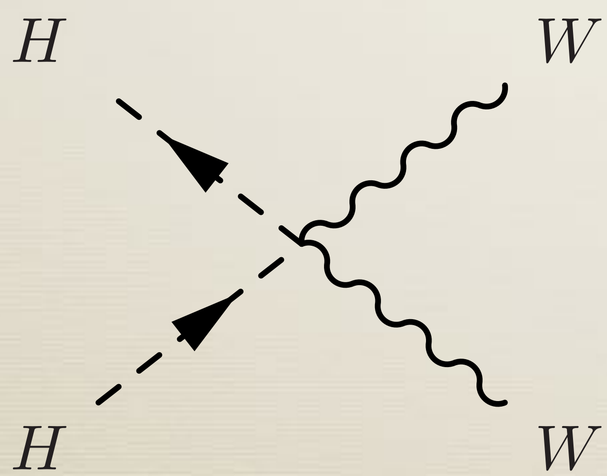
Higgs $\longleftrightarrow$ Higgs'

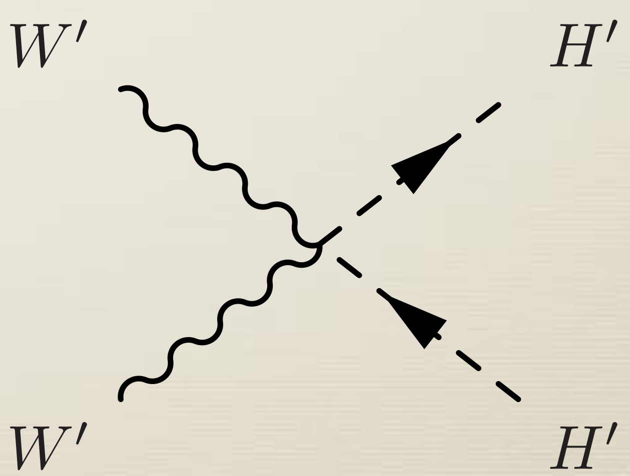
H $\longleftrightarrow$ H'

Weak gauge boson $\longleftrightarrow$ Weak gauge boson'

W $\longleftrightarrow$ W'

$SU(2)$ $\longleftrightarrow$ $SU(2)'$





Z_2 symmetry

Higgs H	⟷	Higgs' H'
Weak gauge boson W $SU(2)$	⟷	Weak gauge boson' W' $SU(2)'$
quark, lepton q, L	⟷	quark', lepton' q', L'

(photon, gluon : several options)

* is part of a grand unified gauge symmetry
* solves the strong CP problem
* (gives a dark matter candidate)

Z_2 symmetry

Higgs H	⟷	Higgs' H'
Weak gauge boson W $SU(2)$	⟷	Weak gauge boson' W' $SU(2)'$
quark, lepton q, L	⟷	quark', lepton' q', L'

Higgs Parity (HP)

Spontaneously broken Higgs Parity

	H		H'	
mass $\propto < H >$ $= v$	W q, L	$\longleftrightarrow$	W' q', L'	mass $\propto < H' >$ $= v'$

In well-motivated theories (explained later),
W', q' or L' interact with Standard Model particles with
$O(1)$ couplings

unbroken Z2 $\langle H \rangle = \langle H' \rangle$ is experimentally excluded

symmetry breaking $\langle H \rangle \ll \langle H' \rangle$ is required

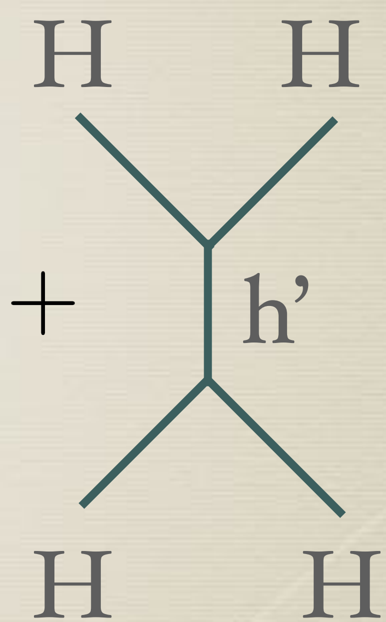
Small quartic

Hall, KH (2018)

$$V(H, H') = \lambda(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2 - m^2(|H|^2 + |H'|^2)$$

$$\langle H' \rangle^2 = \frac{m^2}{2\lambda} \equiv v'^2$$

$\lambda|H|^4 +$



Integrate out heavy d.o.f.

$$V_{\rm eff} \simeq \lambda' v'^2 |H|^2 - \lambda'(1 + \frac{\lambda'}{4\lambda})|H|^4$$

$|\lambda'| \ll 1$

$\lambda_{\rm SM}(v') = 0$

Threshold correction: $\lambda_{\rm SM}(v') \sim -\frac{y_t^4}{16\pi^2} \sim -10^{-3}$

pseudo-NGB Higgs

Hall, KH (2018)

$$V(H,H') = \lambda(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2 - m^2(|H|^2 + |H'|^2)$$

Accidentally U(4) symmetric $4 = (H, H')$

U(4) -> U(3) by H'

$$16 - 9 = 7 = 4 + 3$$

W', Z'

SM Higgs is a pseudo Nambu-Goldstone boson

$$\lambda_{\rm SM}(v') = 0$$

Prediction on symmetry breaking scale

Hall, KH (2018)

Higgs Parity

$$H \longleftrightarrow H'$$

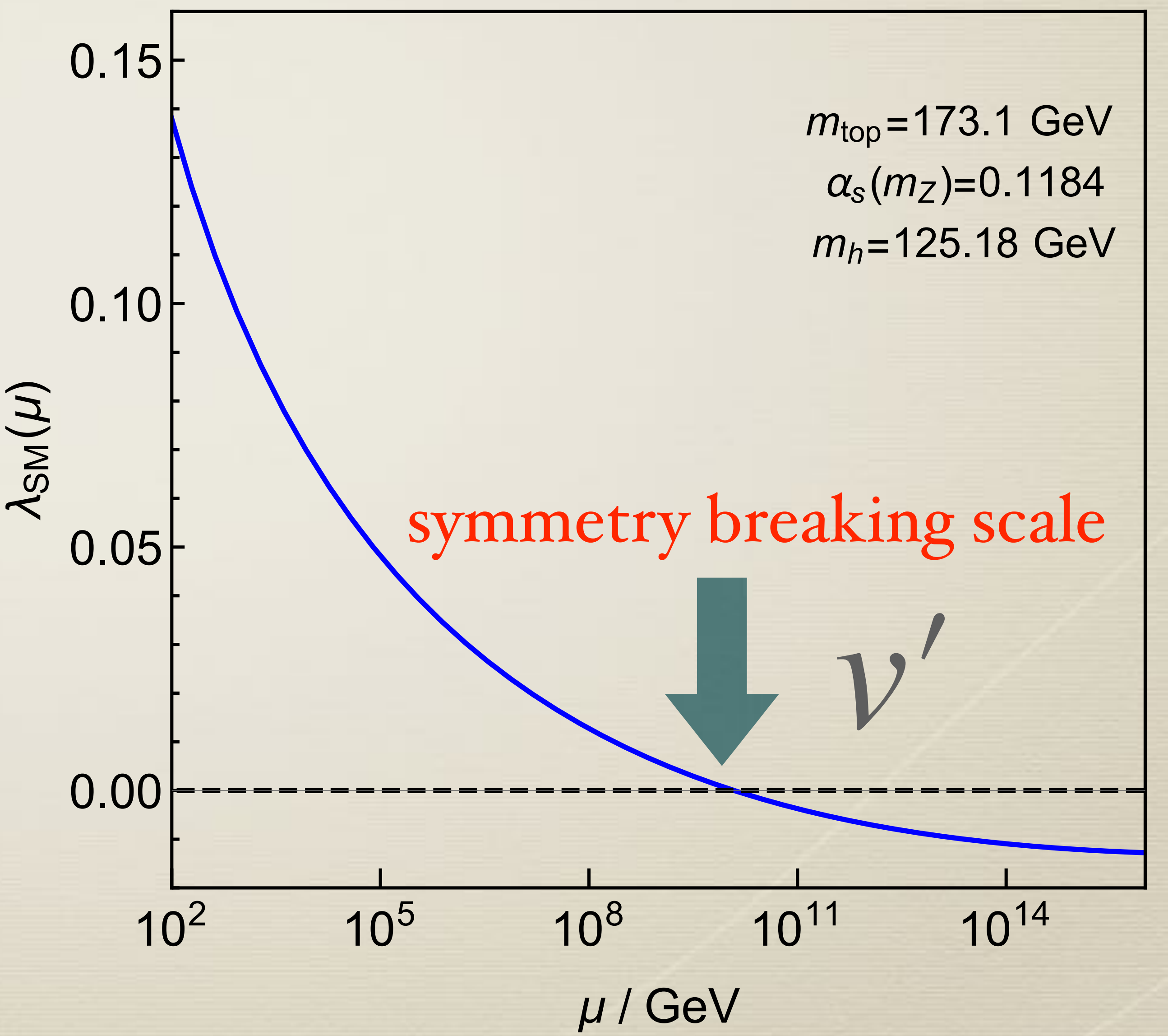
is broken by

$$\langle H \rangle \ll \langle H' \rangle$$

$$v \ll v'$$

$$\Downarrow$$

$$\lambda_{SM}(v') \simeq 0$$



Fine-tuning

$$V(H,H') = \lambda(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2 - m^2(|H|^2 + |H'|^2)$$

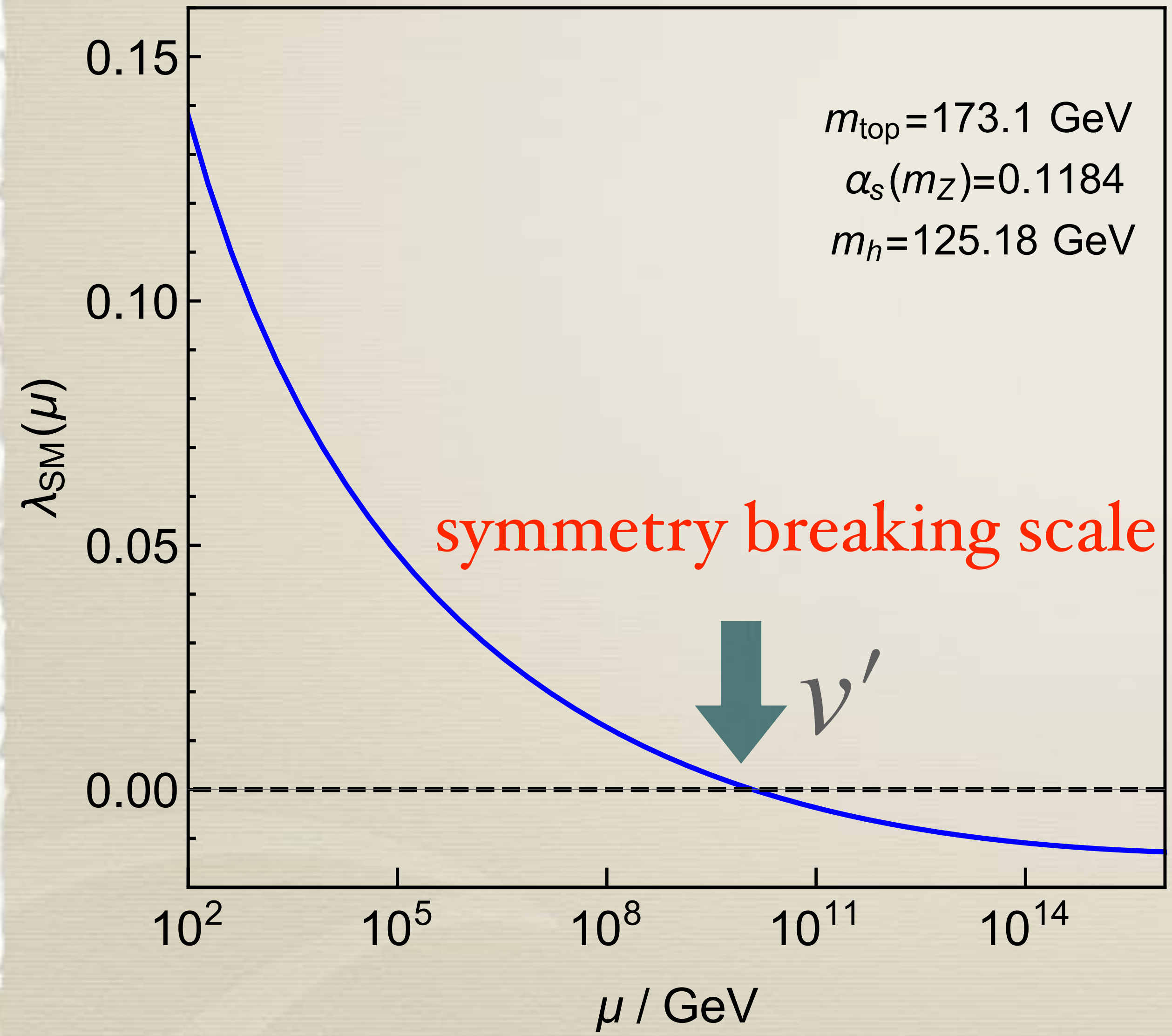
$$\frac{v^2}{v'^2} \times \frac{v'^2}{\Lambda_{\rm cut}^2} = \frac{v^2}{\Lambda_{\rm cut}^2}$$

Despite the intermediate scale v',

same as that of standard model

Quiz 1

If the Higgs mass is larger, v' is



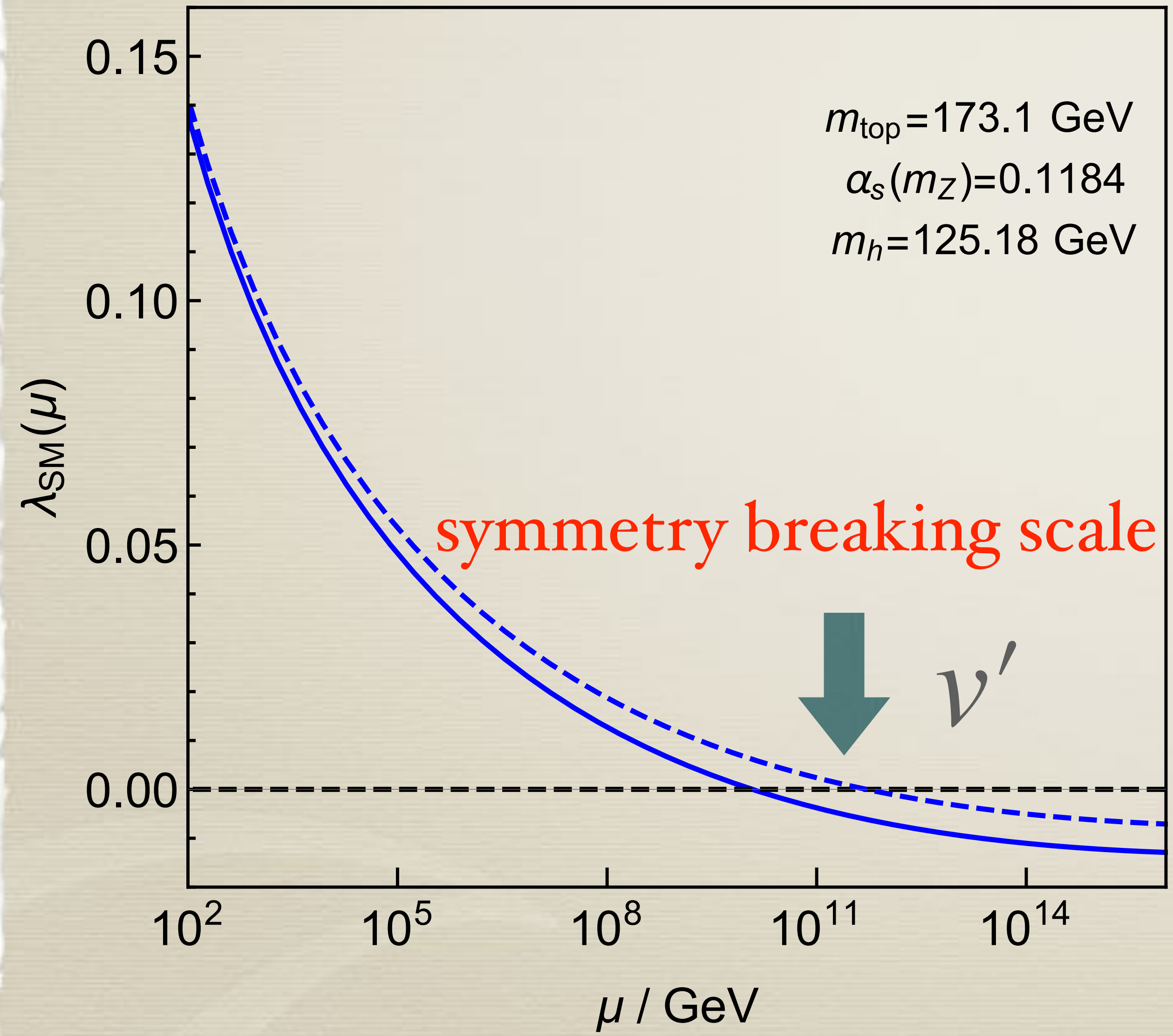
A : Larger
B : Smaller

Hint: Higgs mass

$$m_h \propto \lambda_{SM}^{1/2}(\mu = \text{EW scale})$$

Quiz 1

If the Higgs mass is larger, v' is



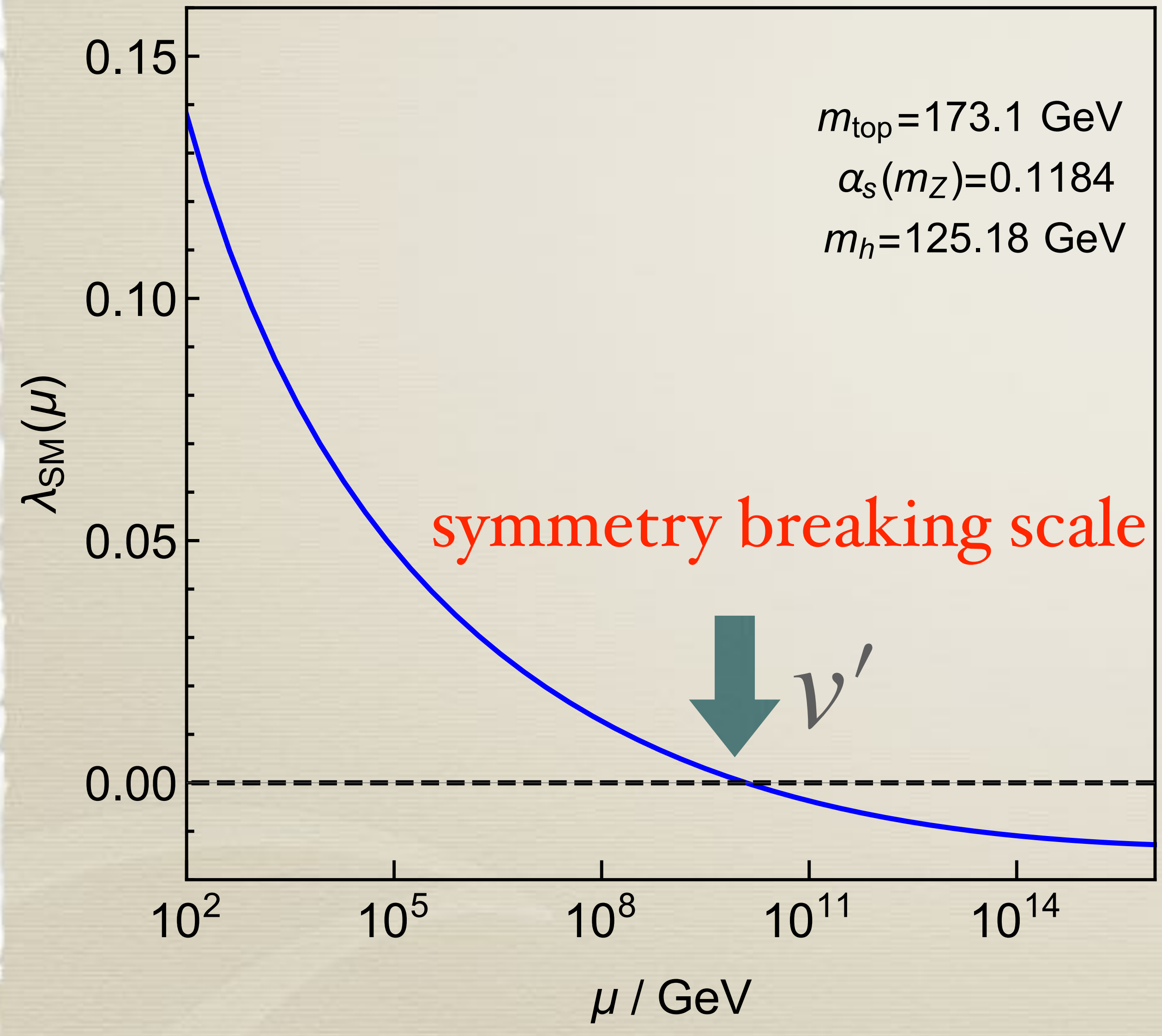
A : Larger
B : Smaller

Hint: Higgs mass

$$m_h \propto \lambda_{SM}^{1/2}(\mu = \text{EW scale})$$

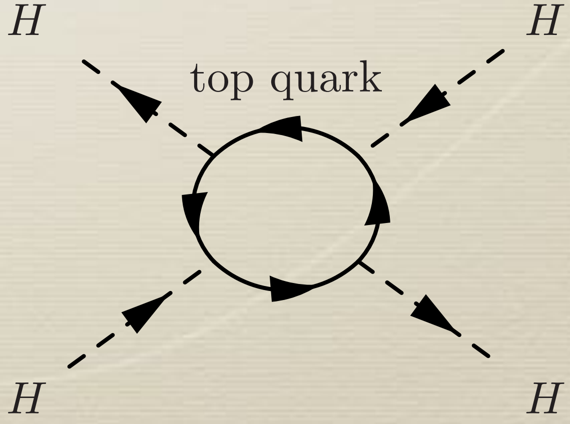
Quiz 2

If the top quark mass is larger, v' is



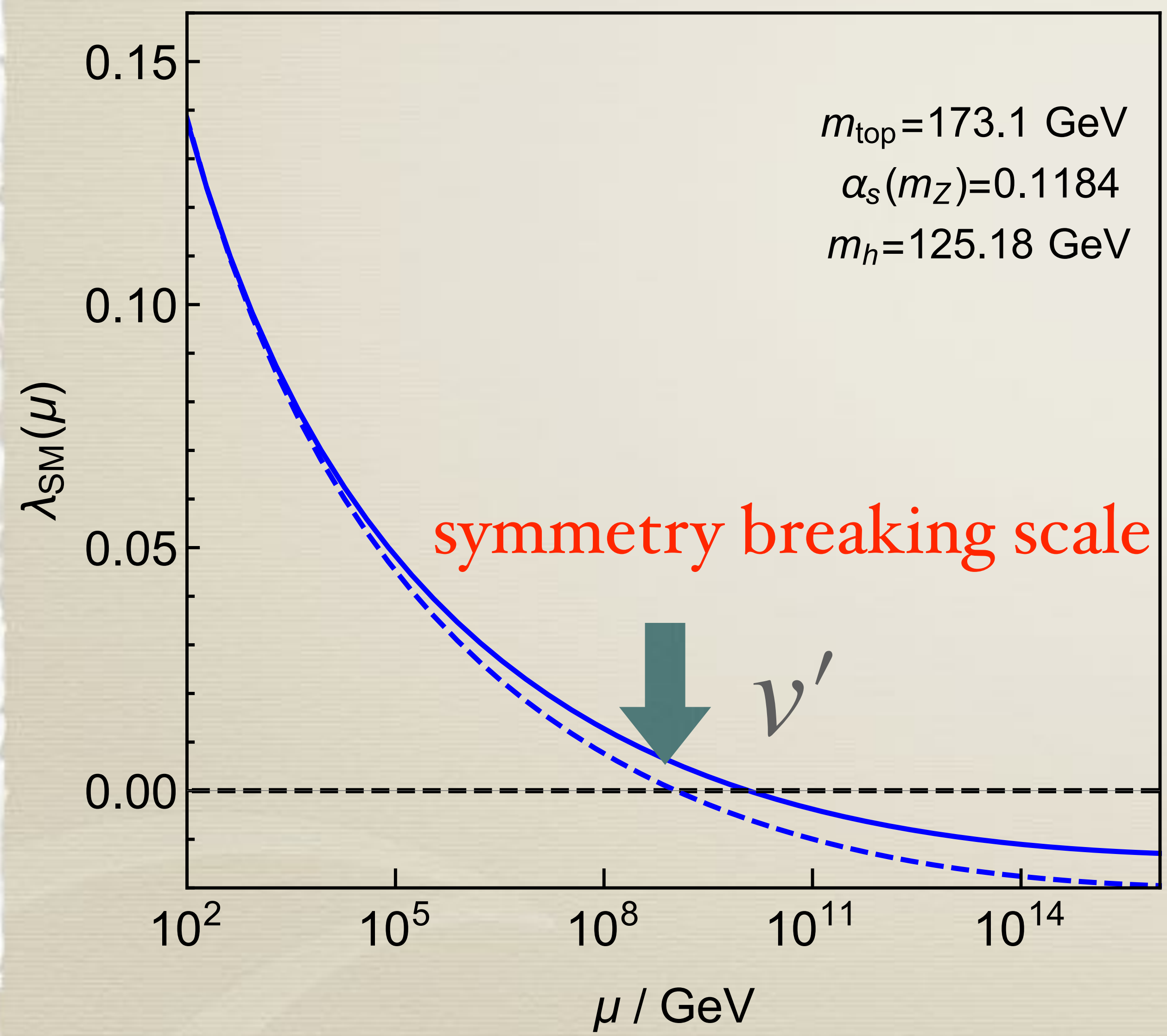
A : Larger
B : Smaller

Hint: the quartic coupling becomes smaller because of the top quark yukawa



Quiz 2

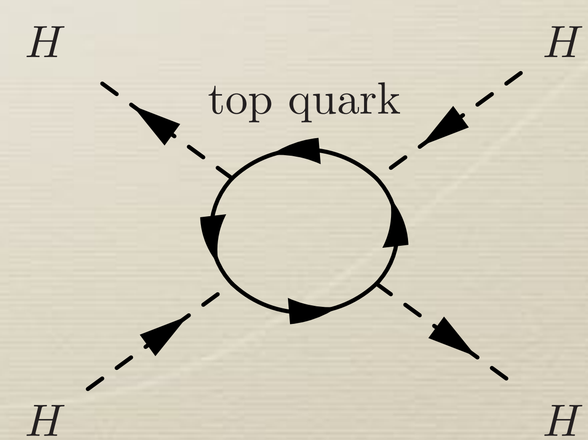
If the top quark mass is larger, v' is



A : Larger

B : Smaller

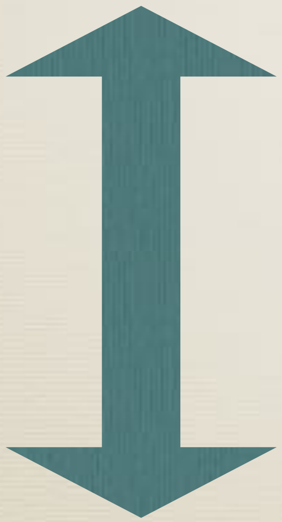
Hint: the quartic coupling becomes smaller because of the top quark yukawa

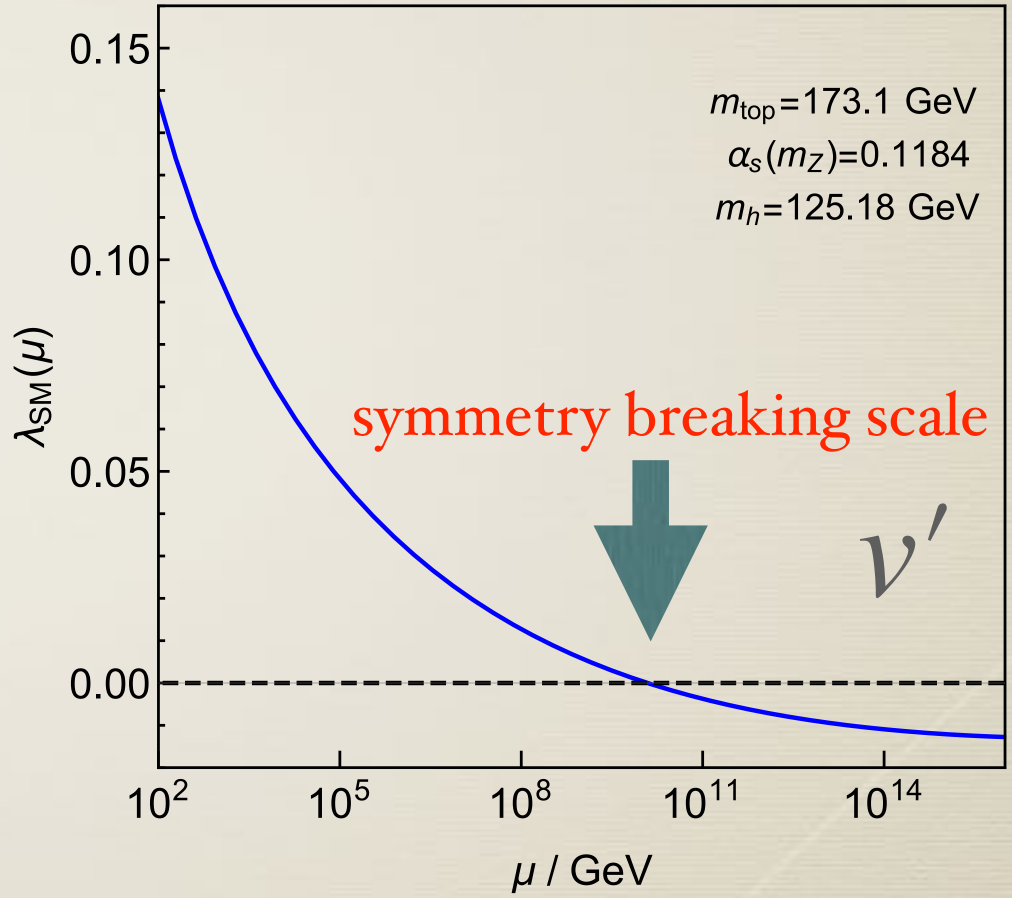


Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



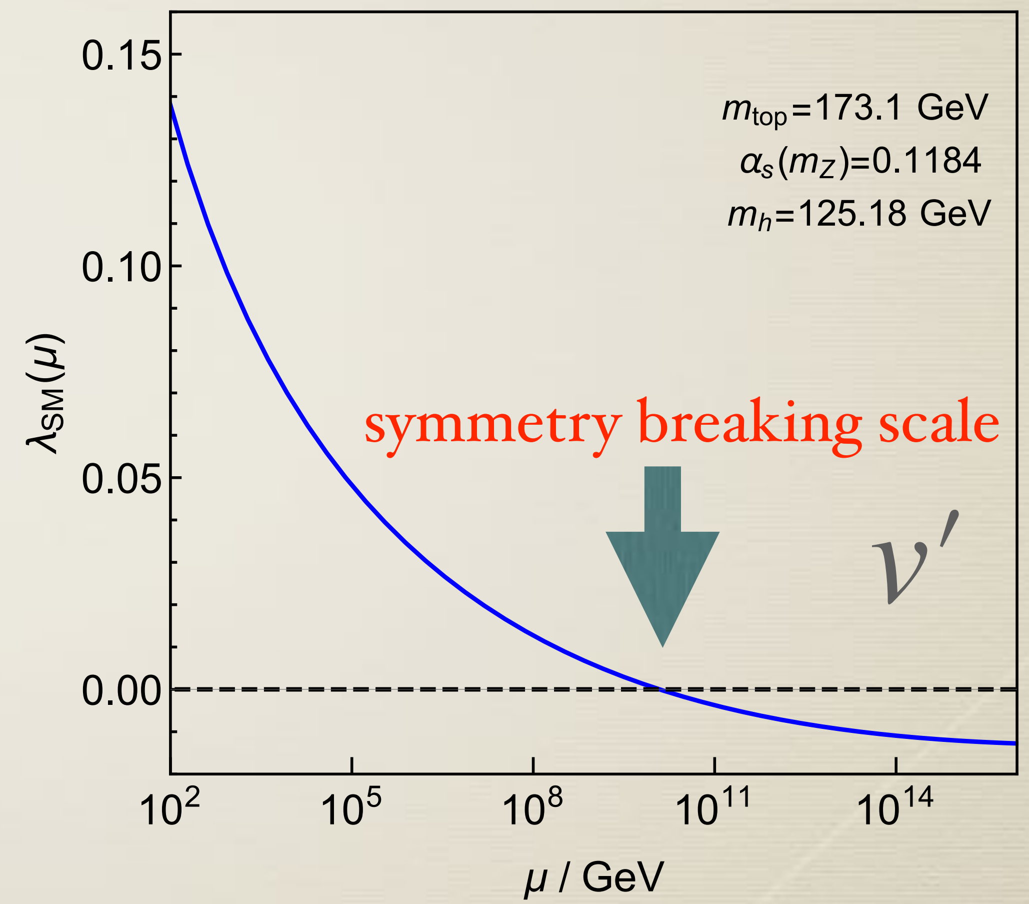


Higgs Parity (HP)
symmetry breaking scale

Precise measurement and new physics

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



Higgs Parity (HP)
symmetry breaking scale

further UV physics,
experimental signatures

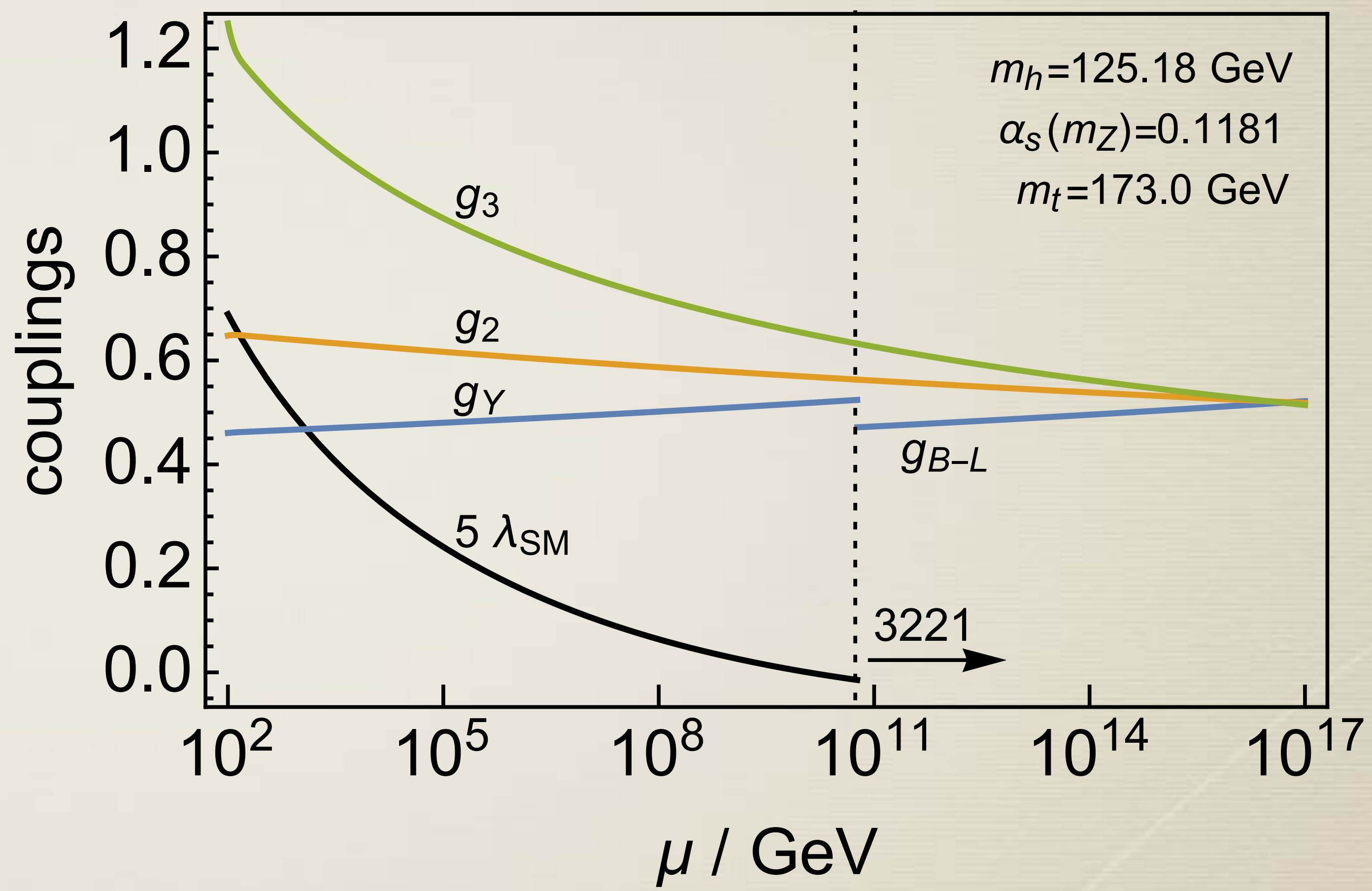
Outline

* Introduction
* Higgs Parity
* Grand unification and proton decay
* Summary and outlook

Precise measurement and Grand Unification

Hall and KH (2018, 2019)

top quark mass
Higgs mass
strong coupling constant



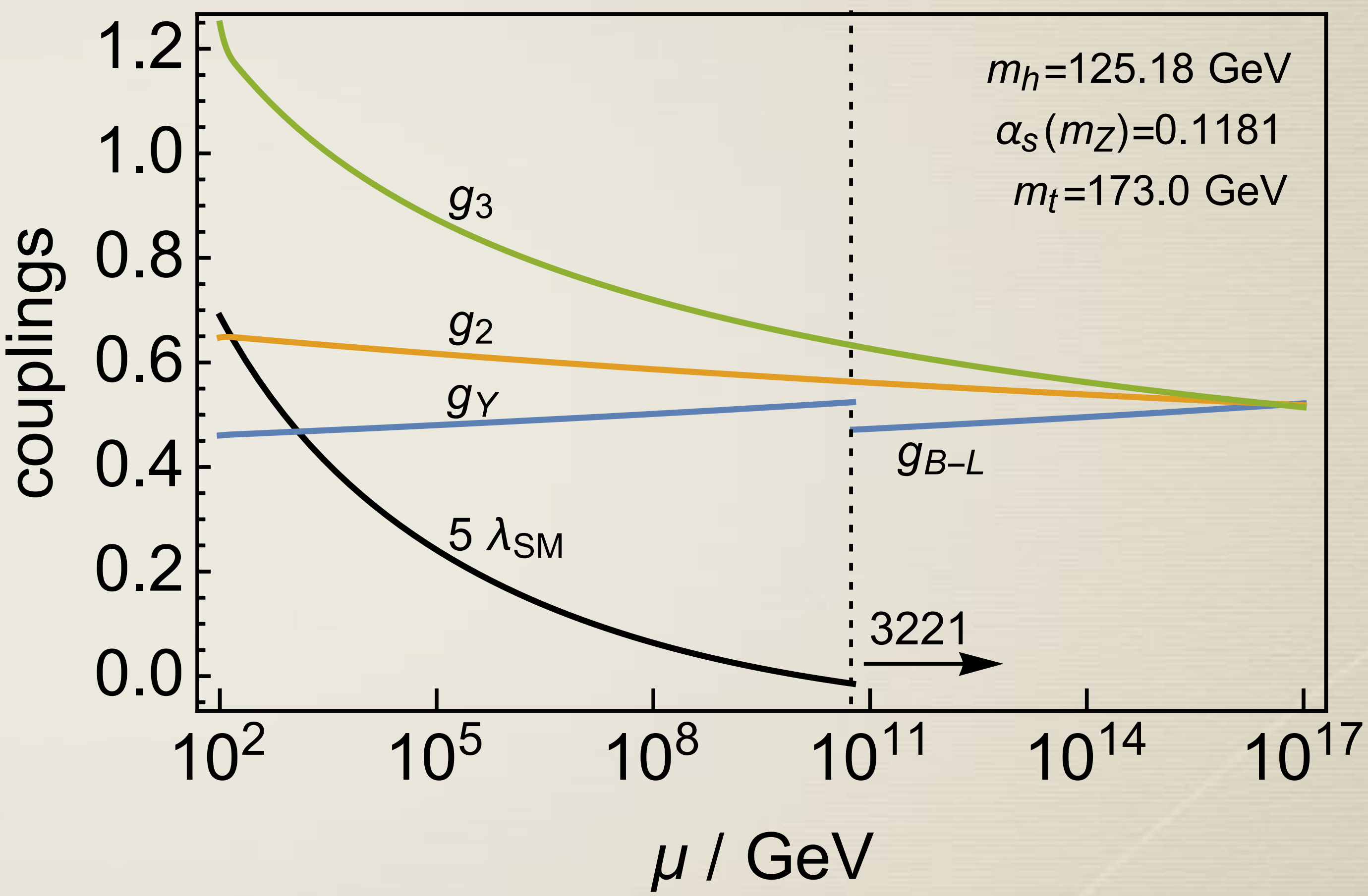
Higgs Parity
symmetry breaking scale

Grand Unification
Proton decay

Precise measurement and Grand Unification

Hall and KH (2018, 2019)

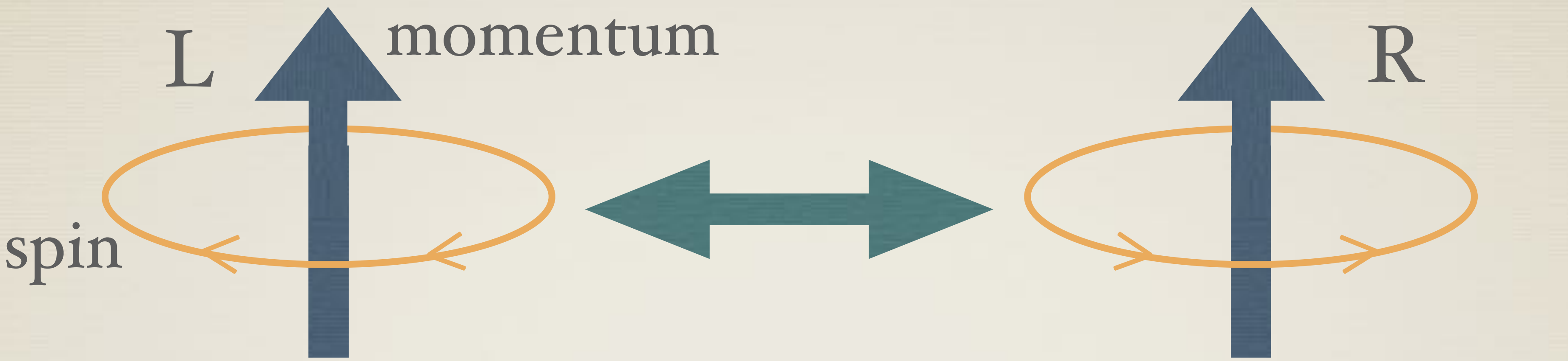
top quark mass
Higgs mass
strong coupling constant

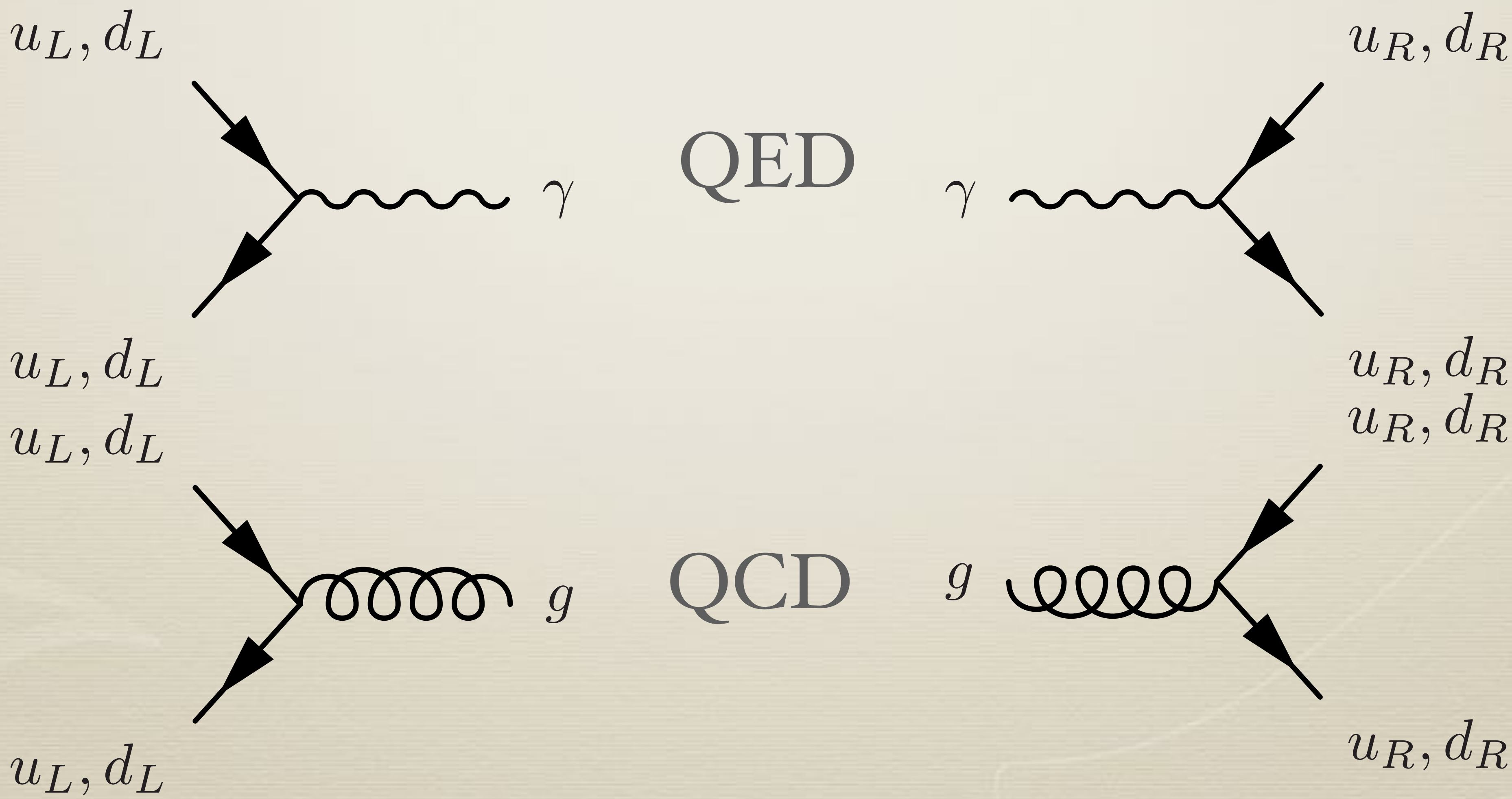


Left-Right
Higgs Parity
symmetry breaking scale

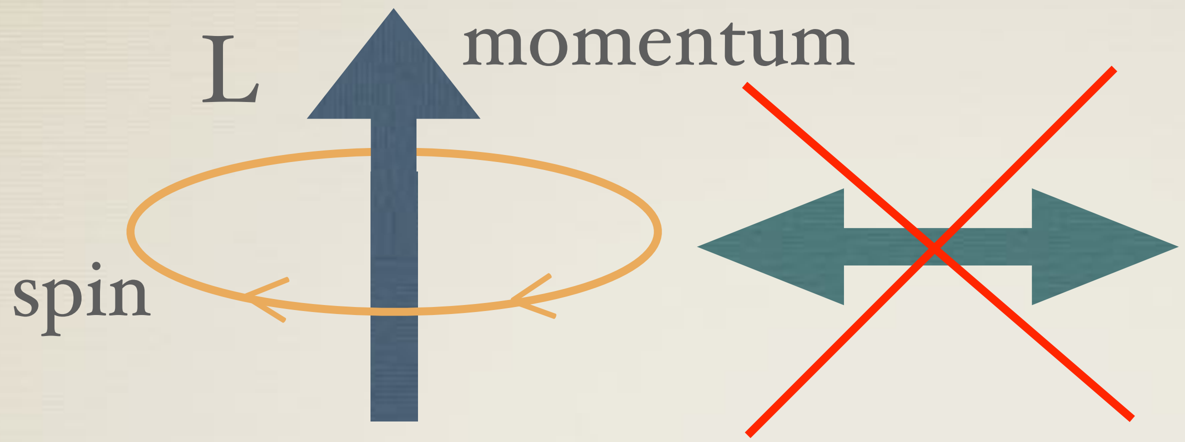
Grand Unification
Proton decay

Left-Right symmetry

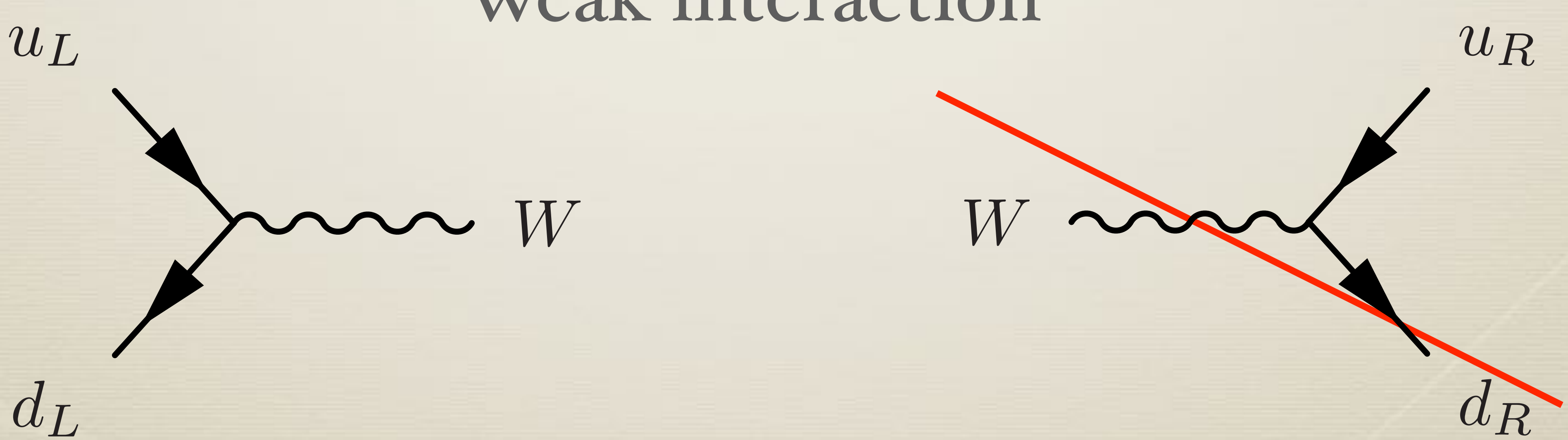




Left-Right symmetry

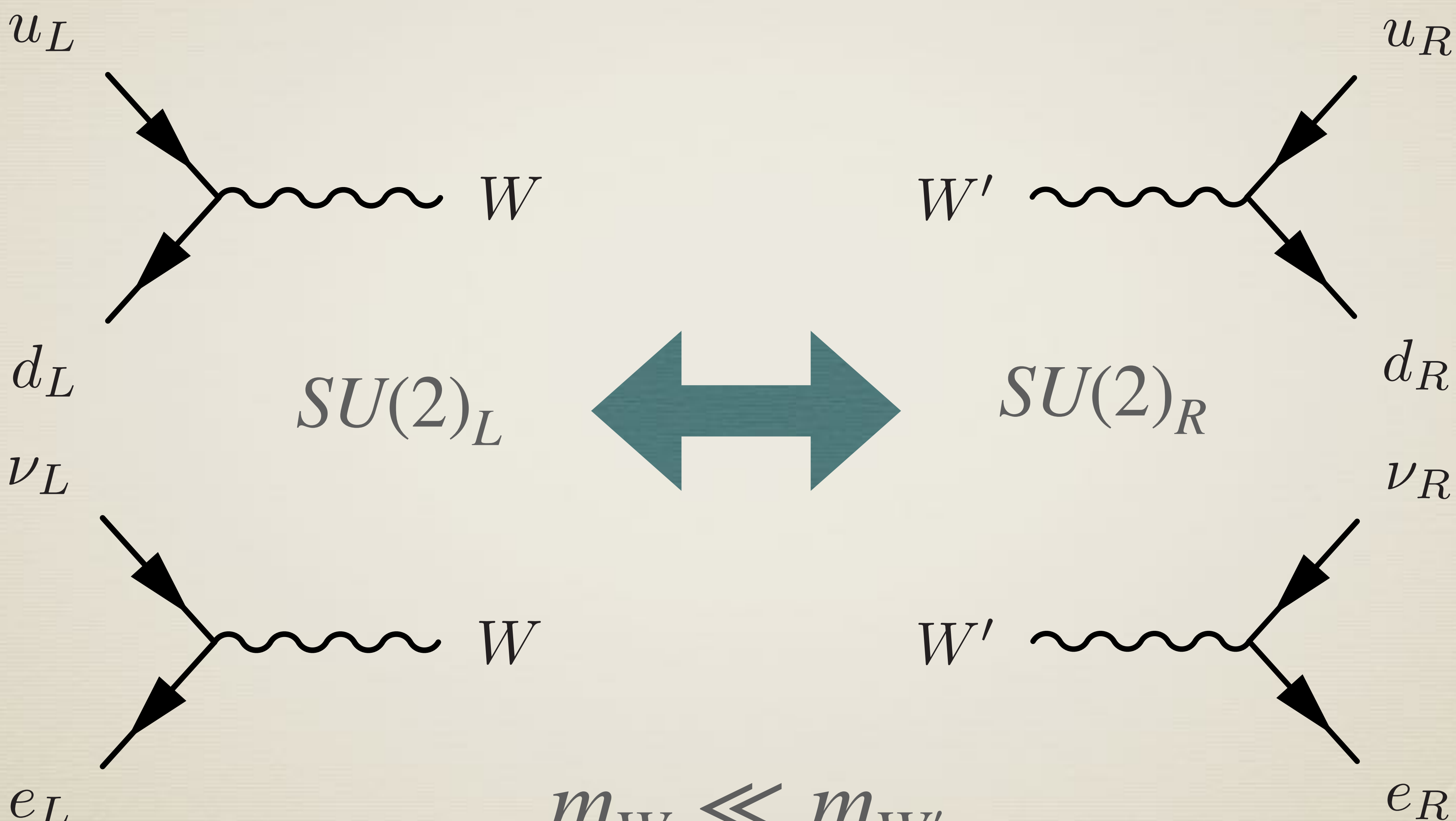


Weak interaction



Lee and Yang (1956), Wu (1957)

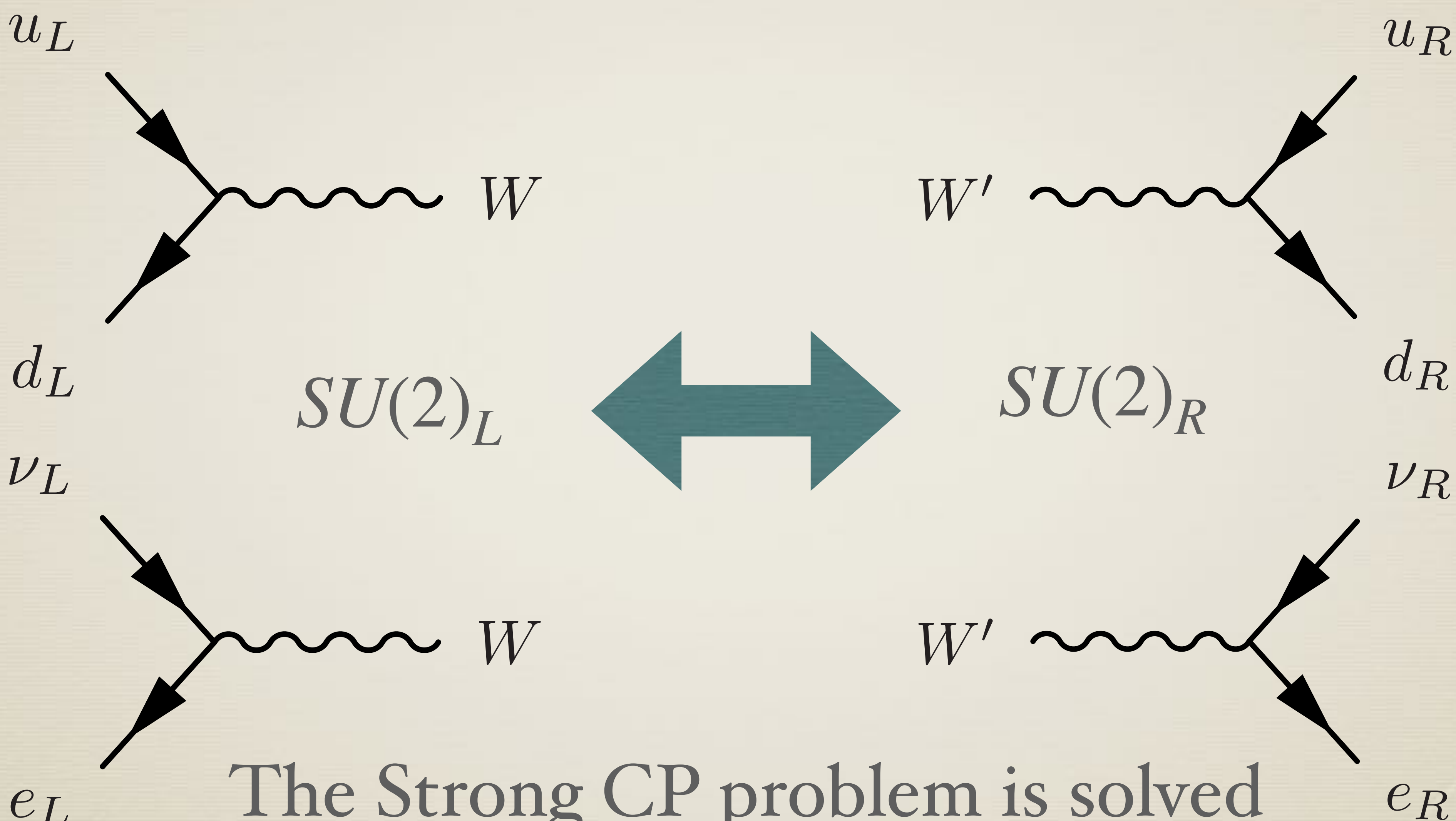
Spontaneously broken Left-Right symmetry



$$m_W \ll m_{W'}$$

Lee (1973), Pati and Salam (1975),
Moahapatra and Pati (1975), Senjanovic and Mohapatra (1975)

Spontaneously broken Left-Right symmetry



The Strong CP problem is solved
via space-time parity

~~$H = d_n \vec{E} \cdot \vec{S}$~~

Mohapatra and Senjanovic (1978), Beg and Tsao (1978),
Babu and Mohapatra (1989), Hall and KH (2018)

Left-Right Higgs Parity

Higgs ↔ Higgs’

H ↔ H'

Weak gauge boson ↔ Weak gauge boson’

W ↔ W'

$SU(2)_L$ ↔ $SU(2)_R$

left-handed quark, lepton ↔ right-handed quark, lepton

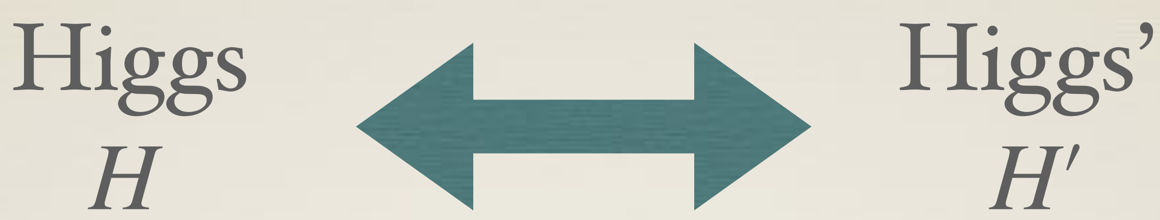
q_L, L_L ↔ $q', L' = q_R, L_R$

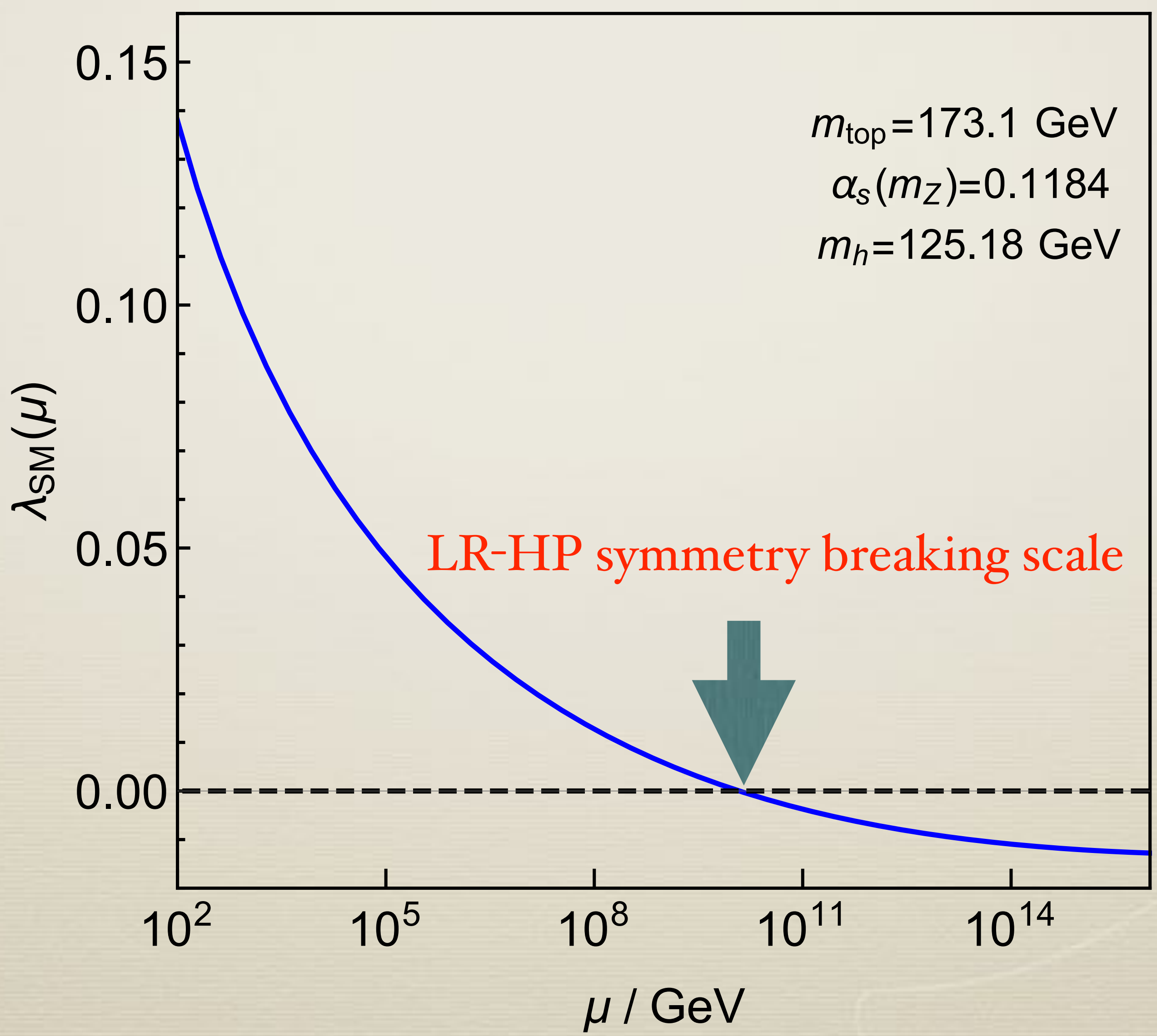
$$SU(3)_c \times SU(2)_L \times \underline{SU(2)_R \times U(1)}$$

$$\downarrow \langle H' \rangle$$

$$U(1)_Y$$

Left-Right Higgs Parity





Left-Right symmetry and Grand Unified Theory

Single gauge group, single type of fermions

Fritzsch and Minkowski (1975), Georgi (1975)

Grand Unification

$SO(10)$

↓

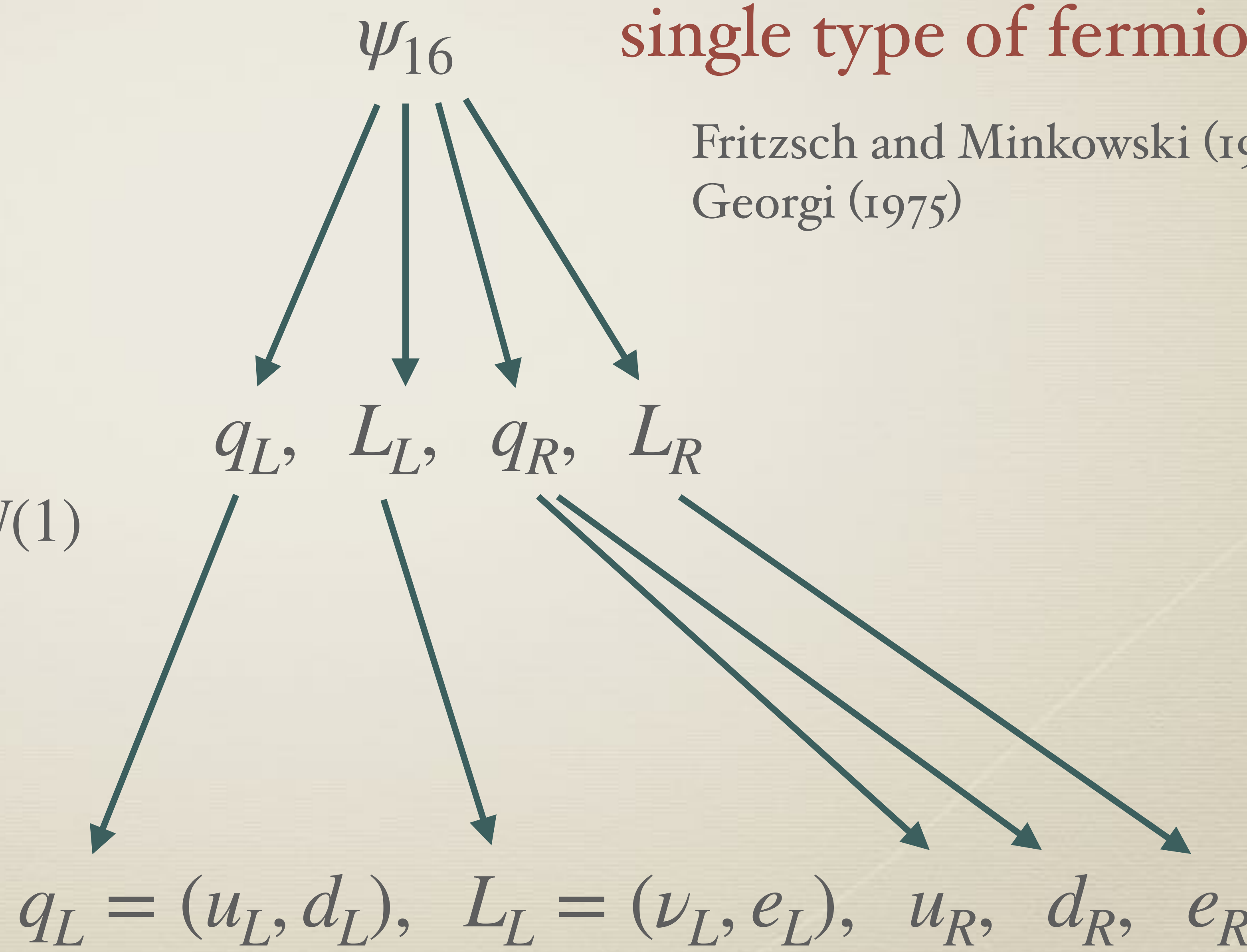
Left-Right Symmetry

$SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)$

↓ $\langle H' \rangle \neq 0$

Standard Model

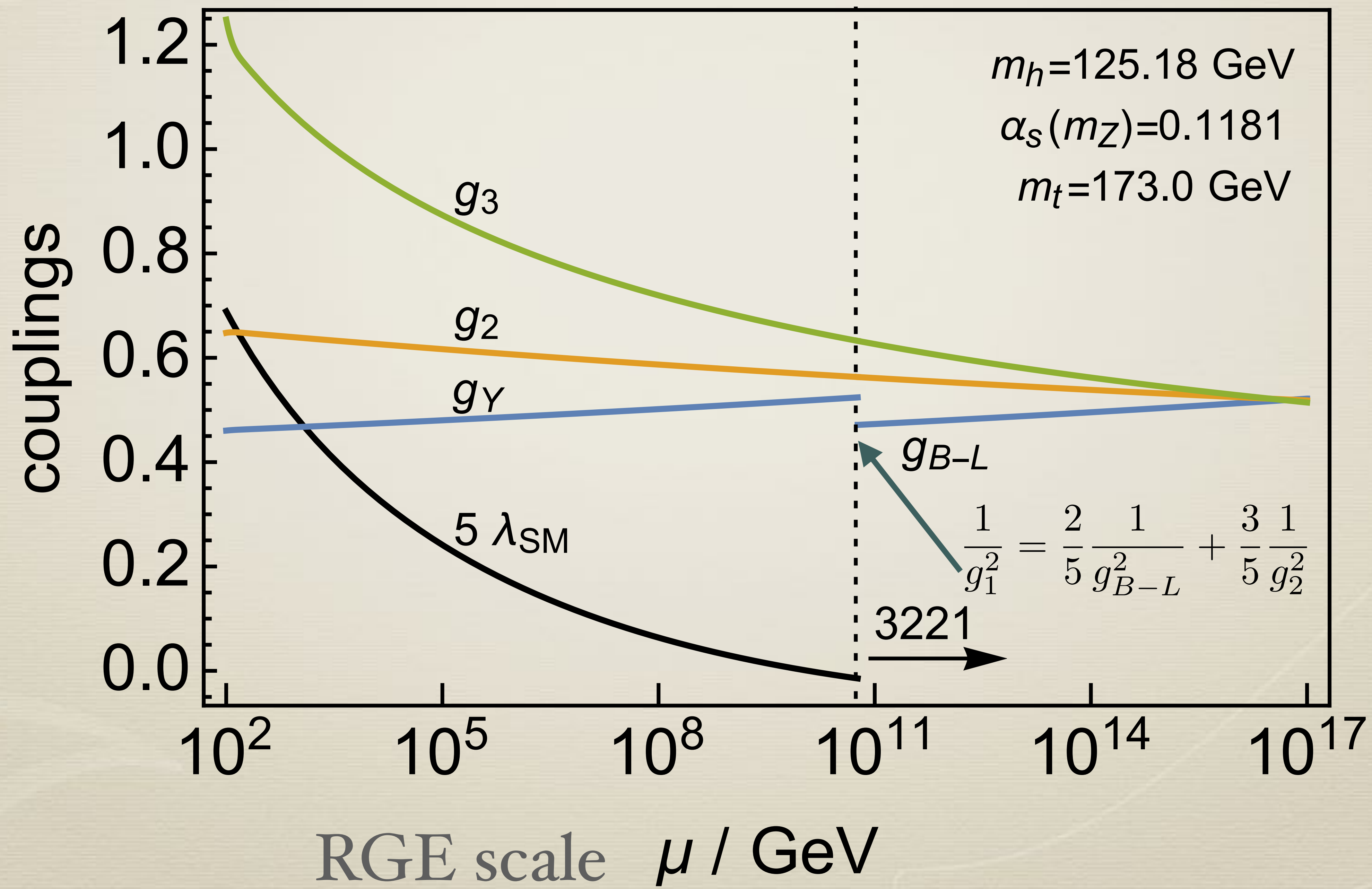
$SU(3)_c \times SU(2)_L \times U(1)_Y$



Coupling unification

Hall, KH (2018, 2019)

energy-dependent couplings

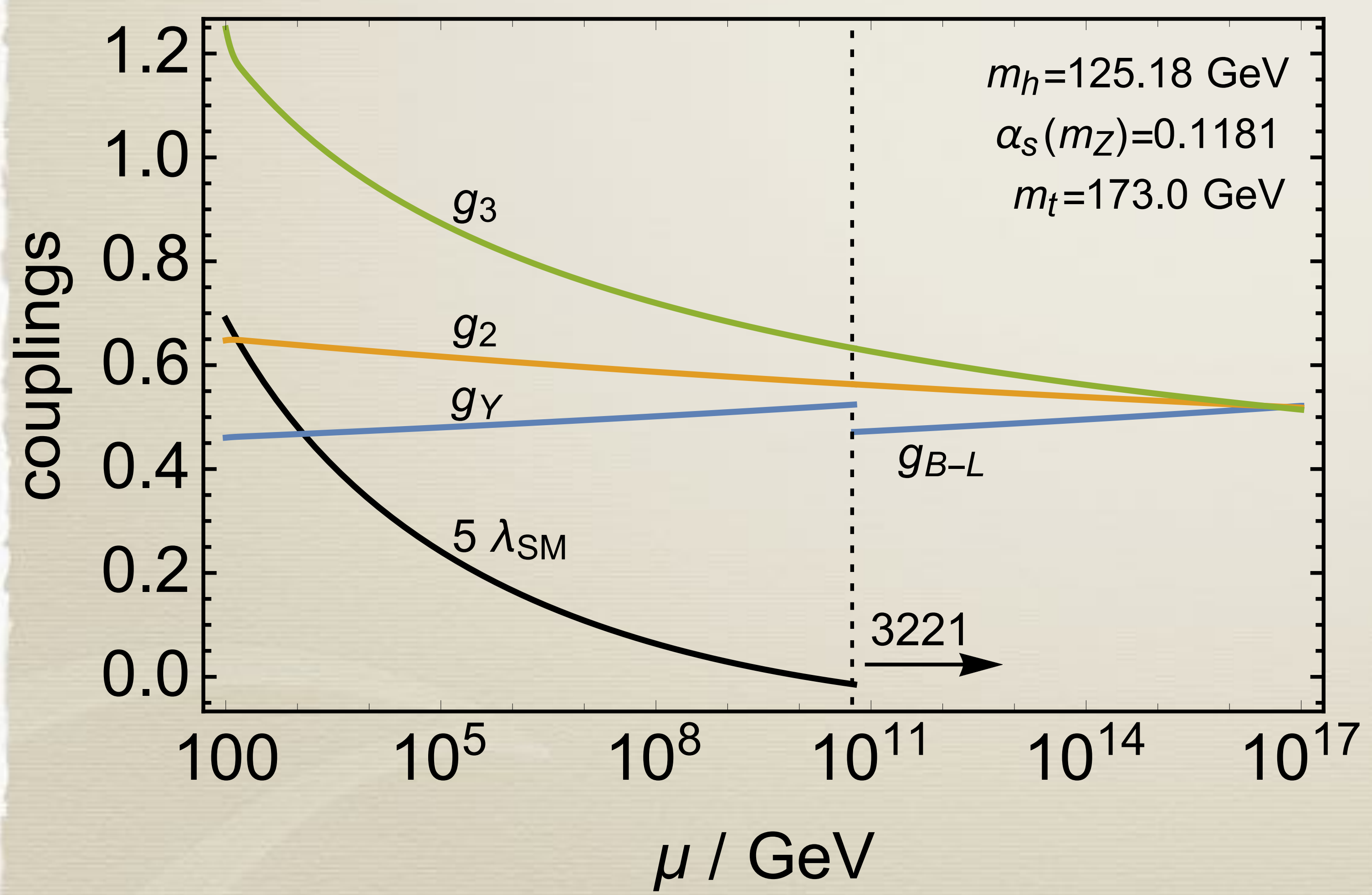


RGE scale

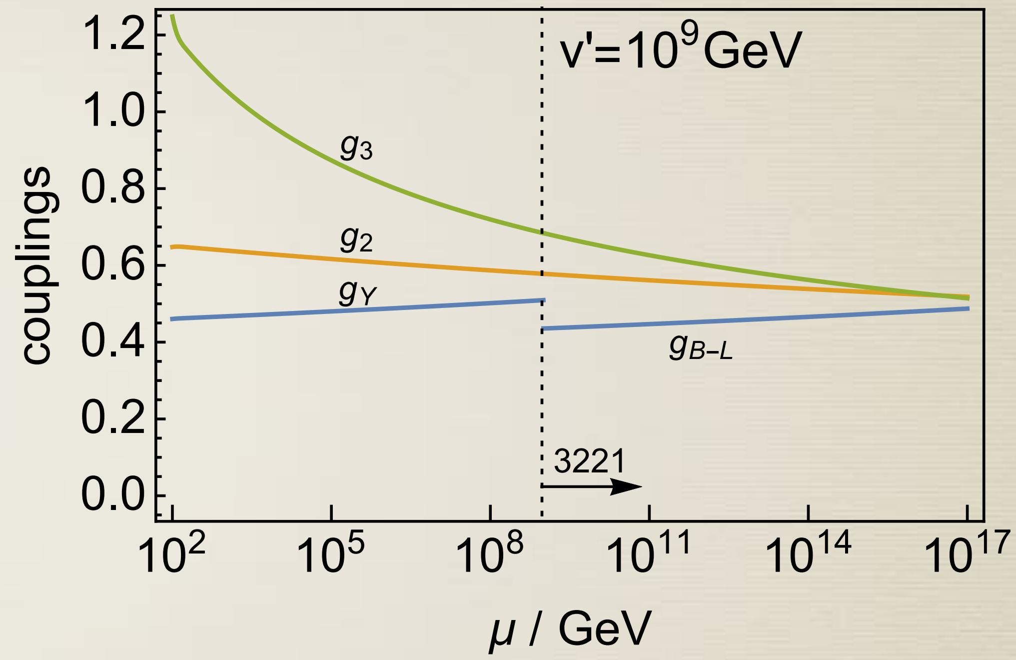
Coupling unification

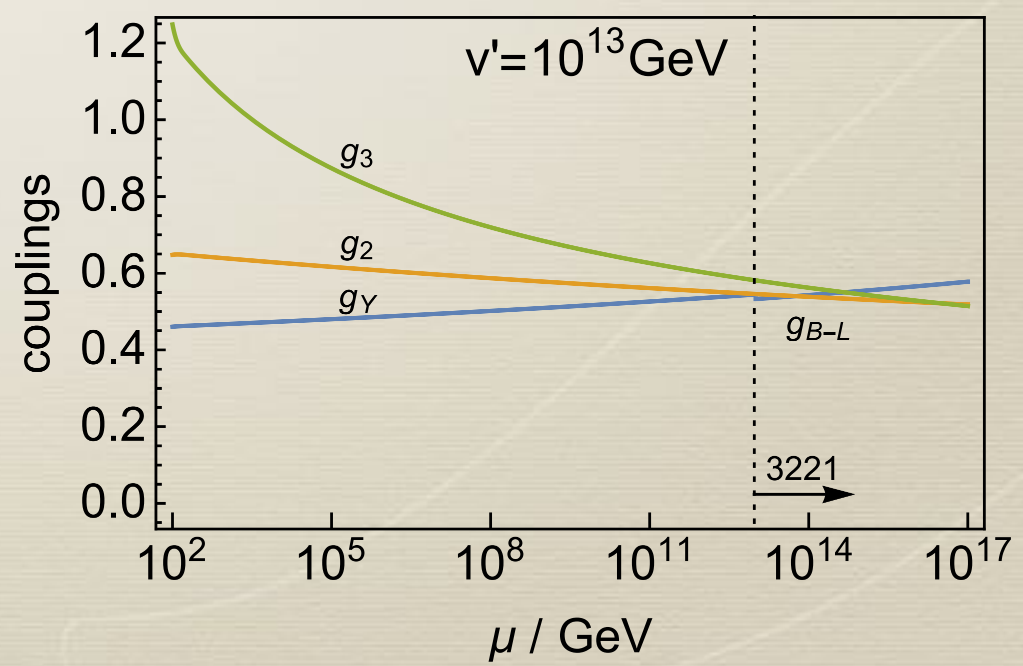
Hall, KH (2018, 2019)

v' determined by Higgs Parity



Other v'

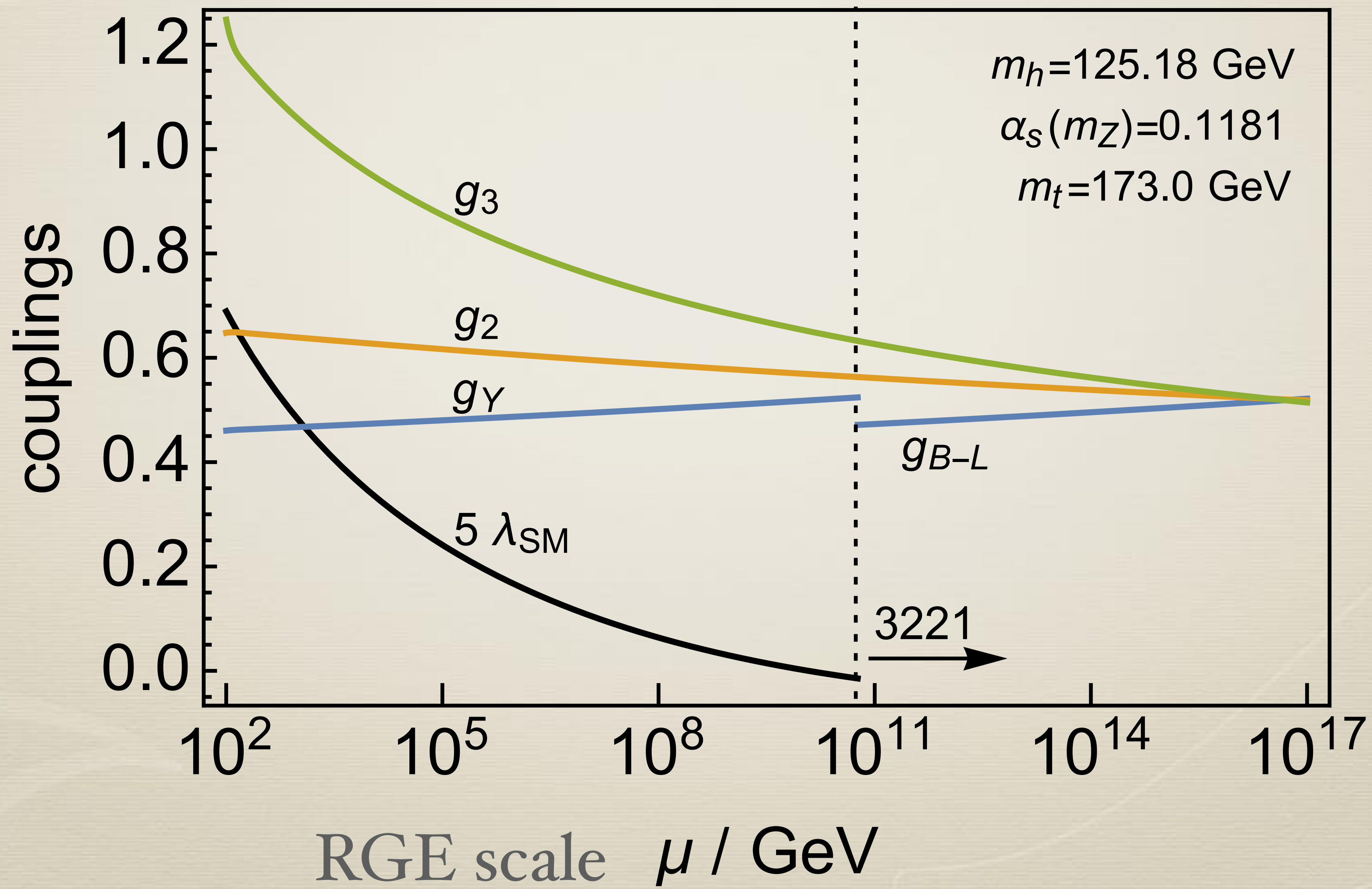




Higgs Parity GUT

Hall, KH (2018, 2019)

energy-dependent couplings



RGE scale

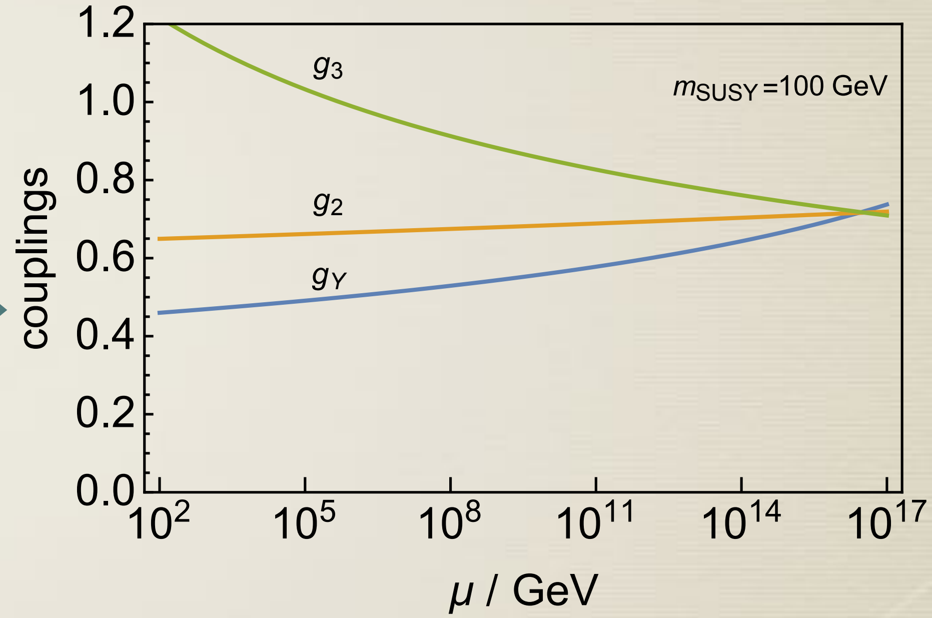
Higgs Parity GUT

Hall, KH (2018, 2019)

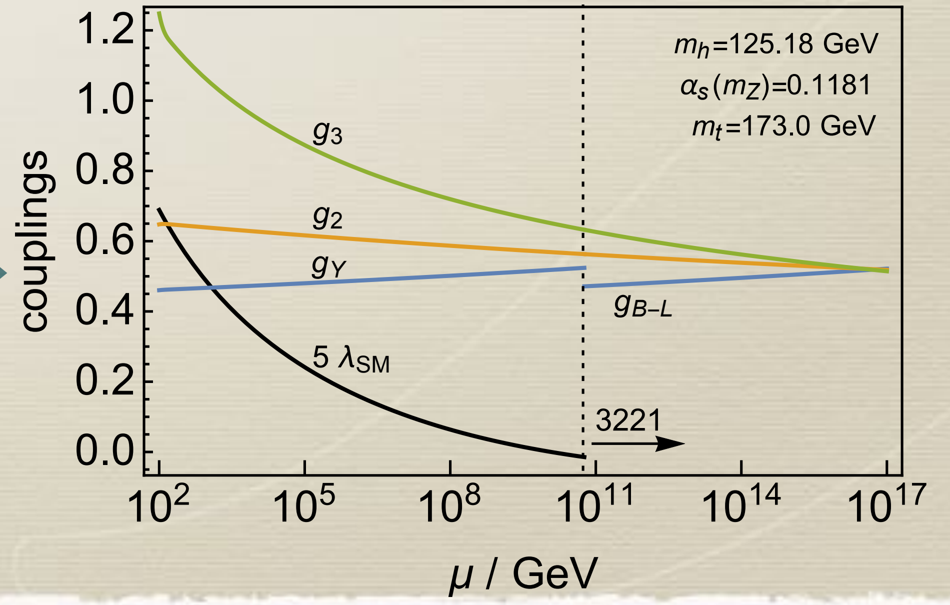
weak scale 10^2 GeV

GUT scale 10^{16} GeV

gauge coupling constants
(LEP, ...)



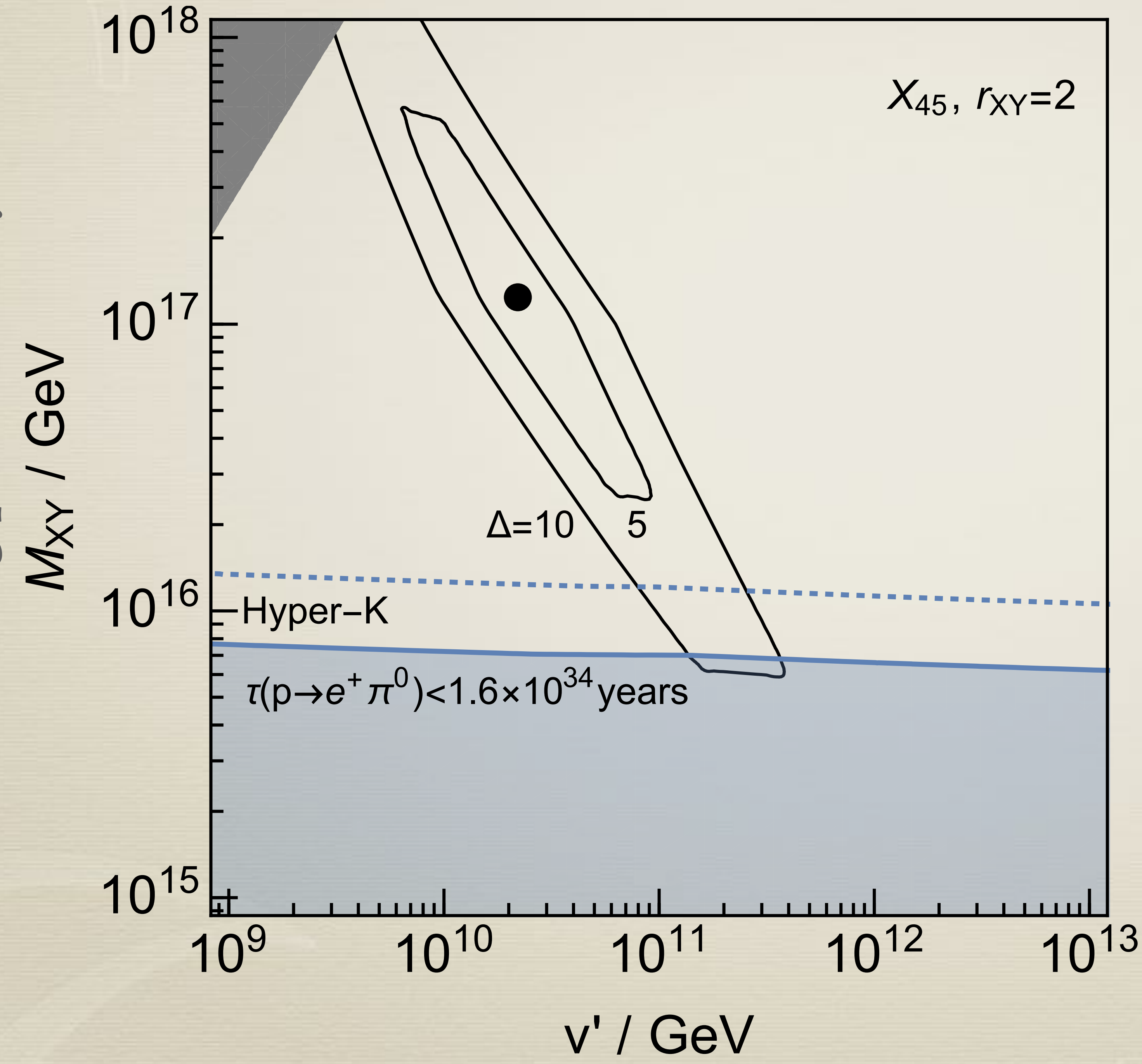
gauge coupling constants
top quark mass
Higgs mass
(LHC, lattice, future colliders, ...)



Quantify unification

Hall, KH (2019)

mass of new gauge boson mediating proton decay



There can be quantum corrections from heavy particles around the GUT scale

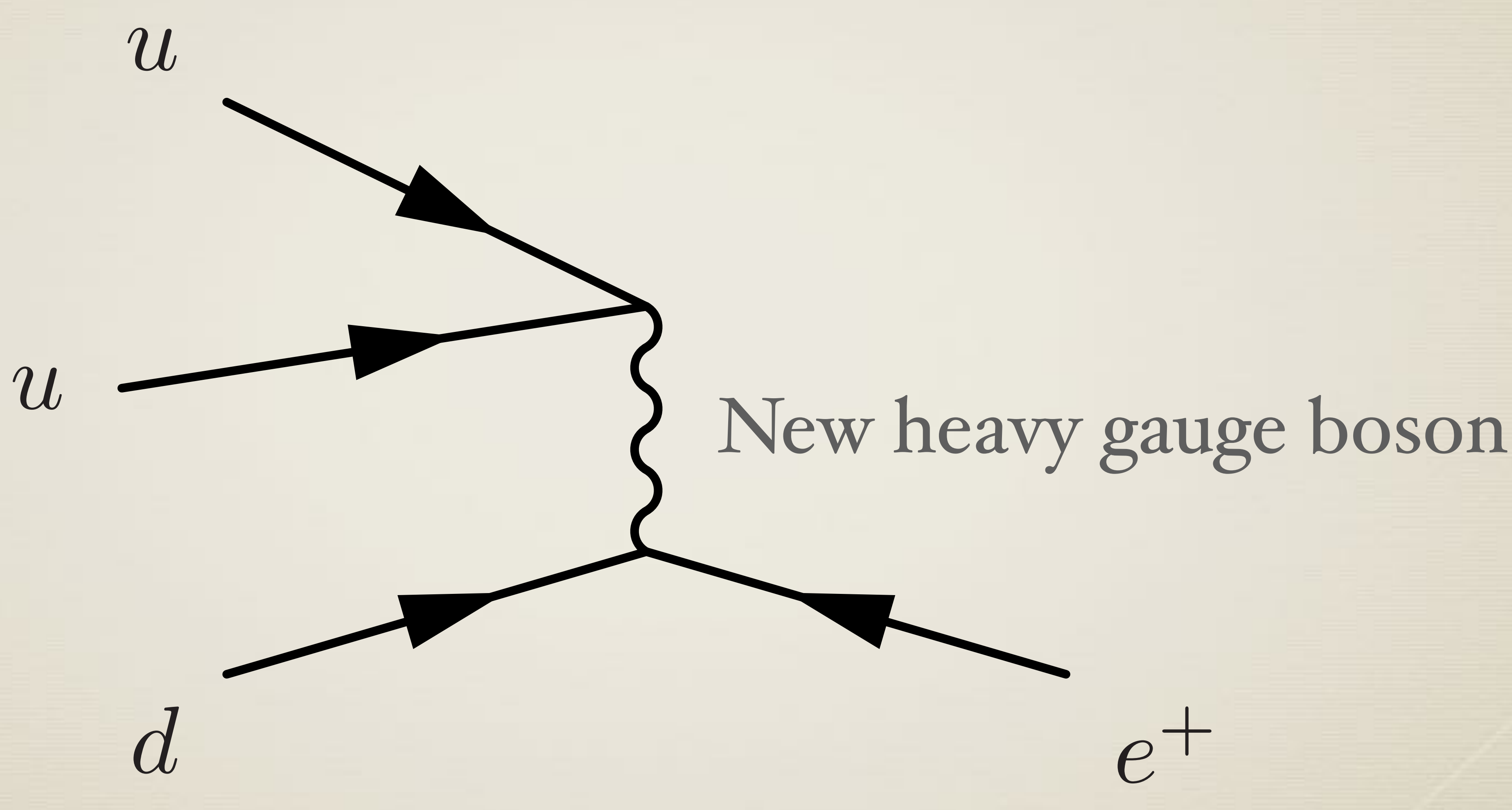
$$\Delta = \max_{i,j}\left|\frac{8\pi^2}{g_i^2} - \frac{8\pi^2}{g_j^2}\right|$$

typically

$$\Delta = \text{few} - 10$$

(smaller than SUSY GUT)

Proton decay

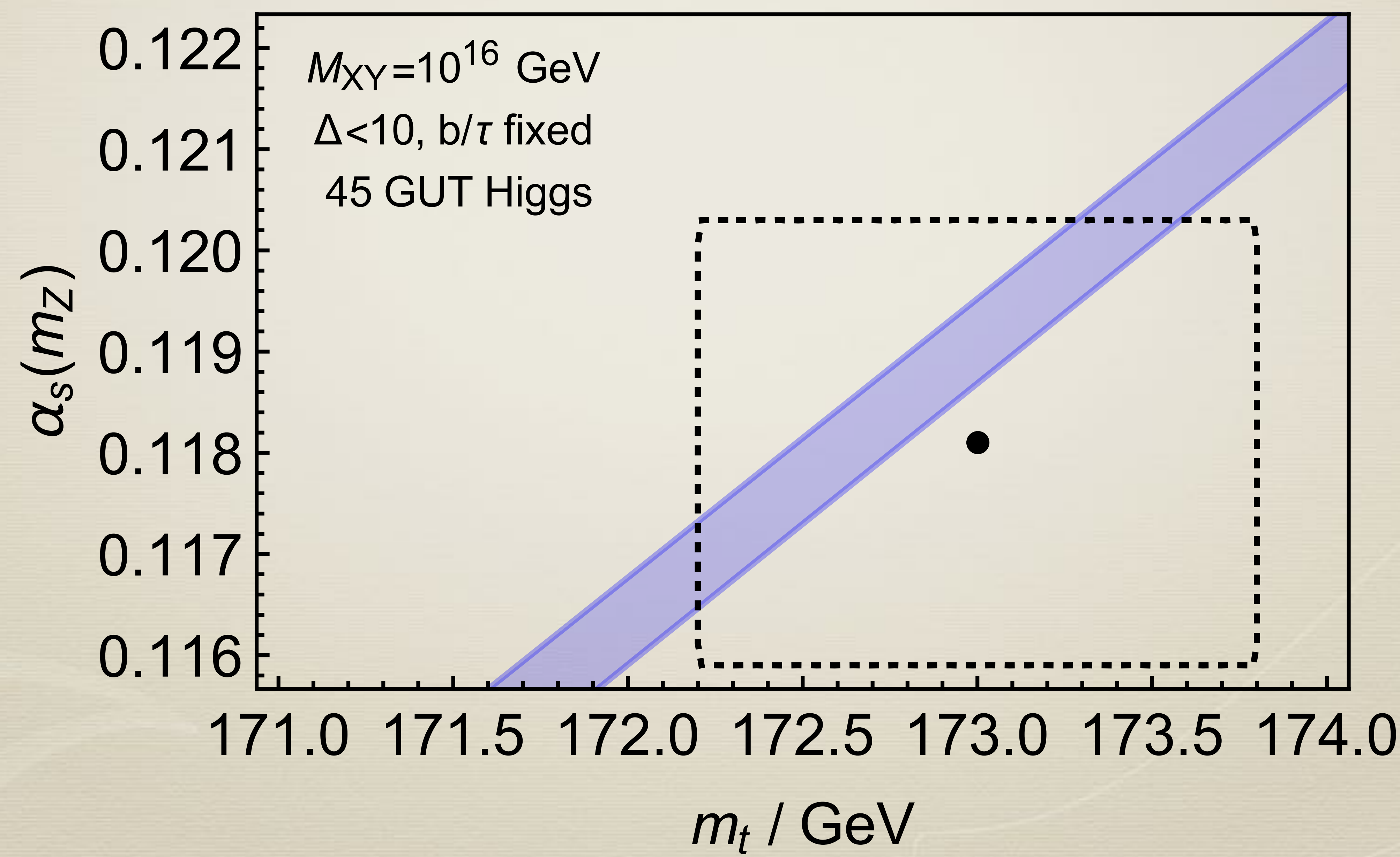


$$p \to e^+\pi^0$$

Proton decay

Hall, KH (2019)

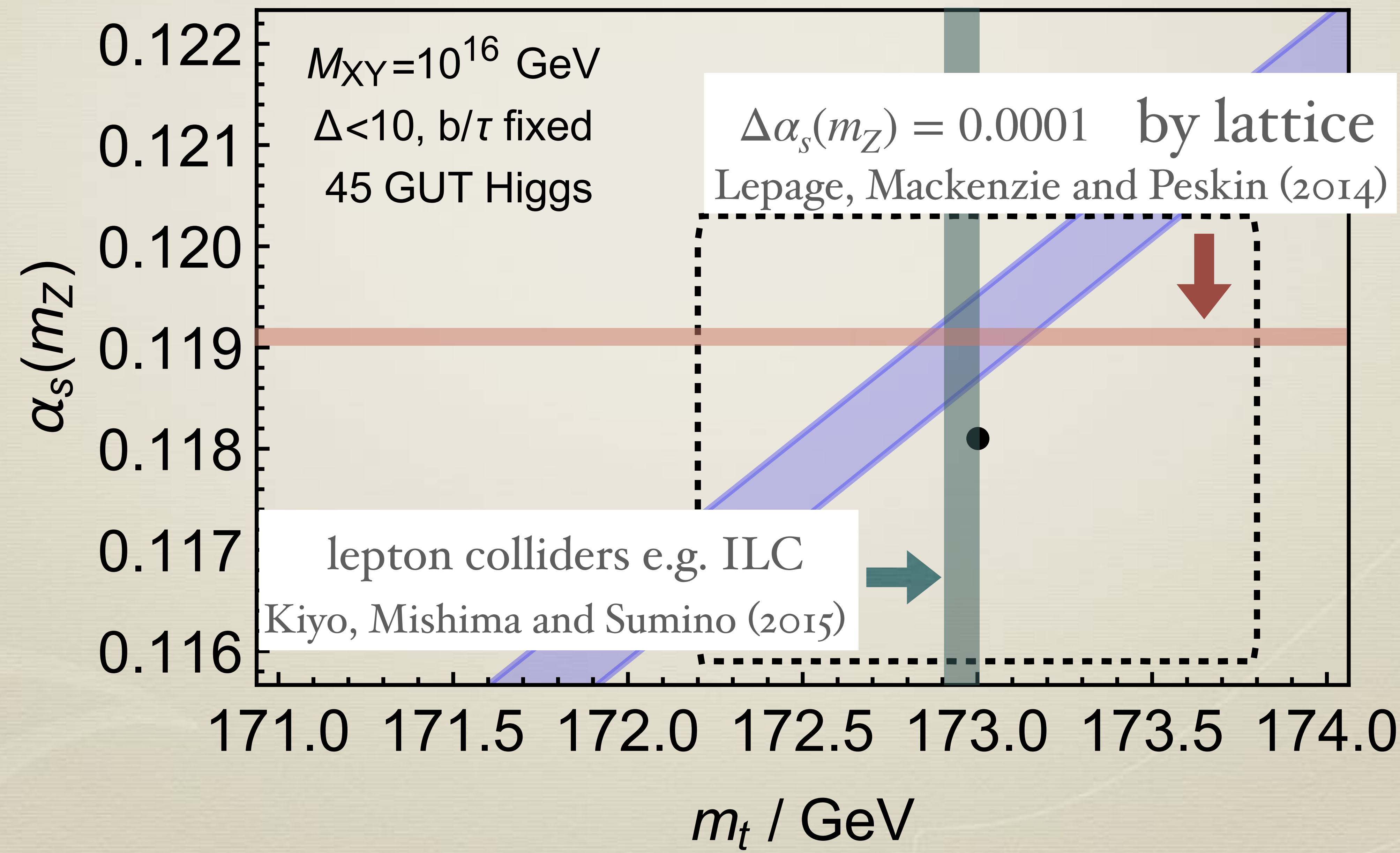
Suppose proton decay is observed at Hyper-K (2027-)



Proton decay

Hall, KH (2019)

Suppose proton decay is observed at Hyper-K (2027-)

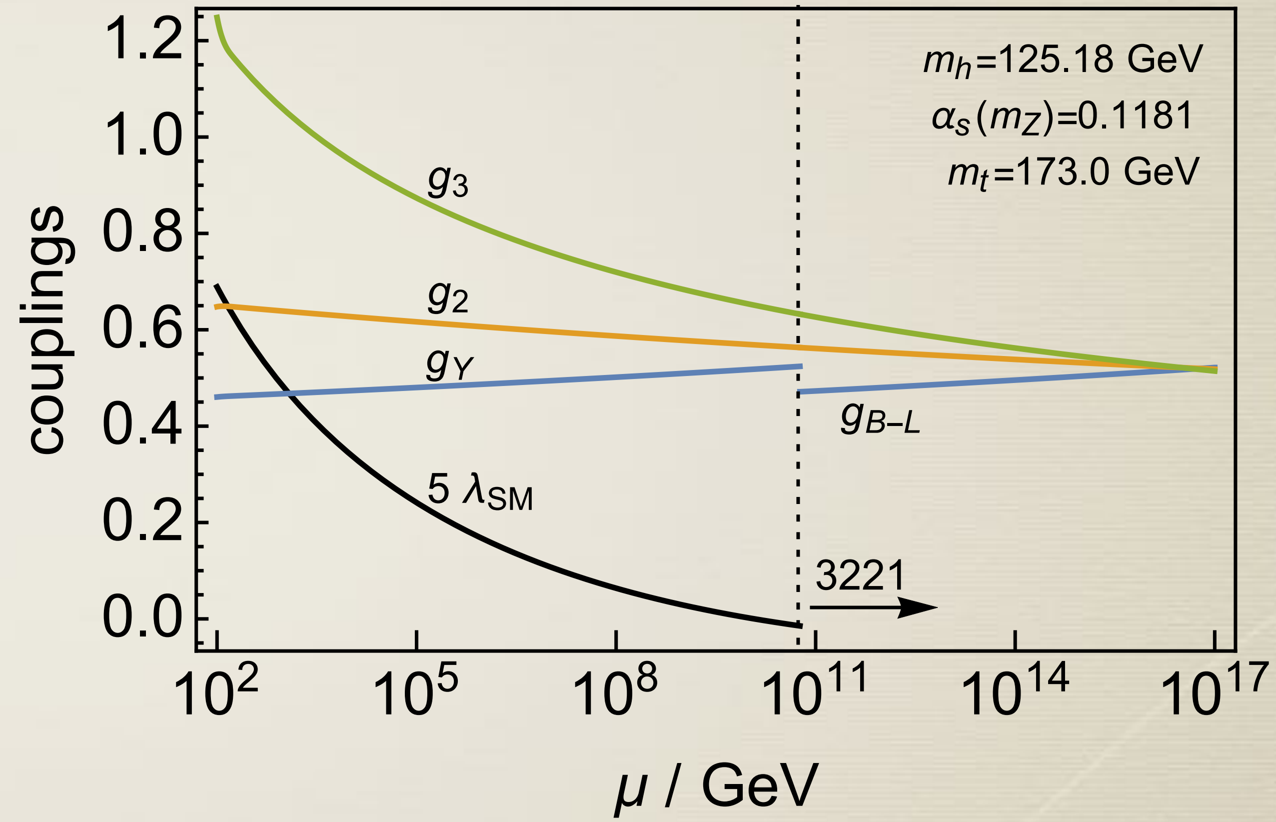


Summary and outlook

Higgs Parity

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



Higgs Parity
symmetry breaking scale

GUT, proton decay

(dark matter direct detection, gravitational waves, dark radiation, warm dark matter, neutron EDM, axion, ...)

Other models with Higgs Parity

* A model with dark matter

  Dunsky, Hall and KH, 1902.07726

  Back up slides, section "Dark Matter"

  Dark matter direct detection rate is predicted from SM parameters

* A model with a mirror copy of the SM

  Dunsky, Hall and KH, 1908.02756

  Dark radiation and gravitational wave abundance are predicted from SM parameters

* ...

Future of colliders

We should maximize the impact of future colliders

* Searches for new particles

* Searches for deviation from the standard model predictions

$$N_{\text{events}} = N_{\text{SM prediction}} \ ?$$

* Precise measurement of the standard model parameters

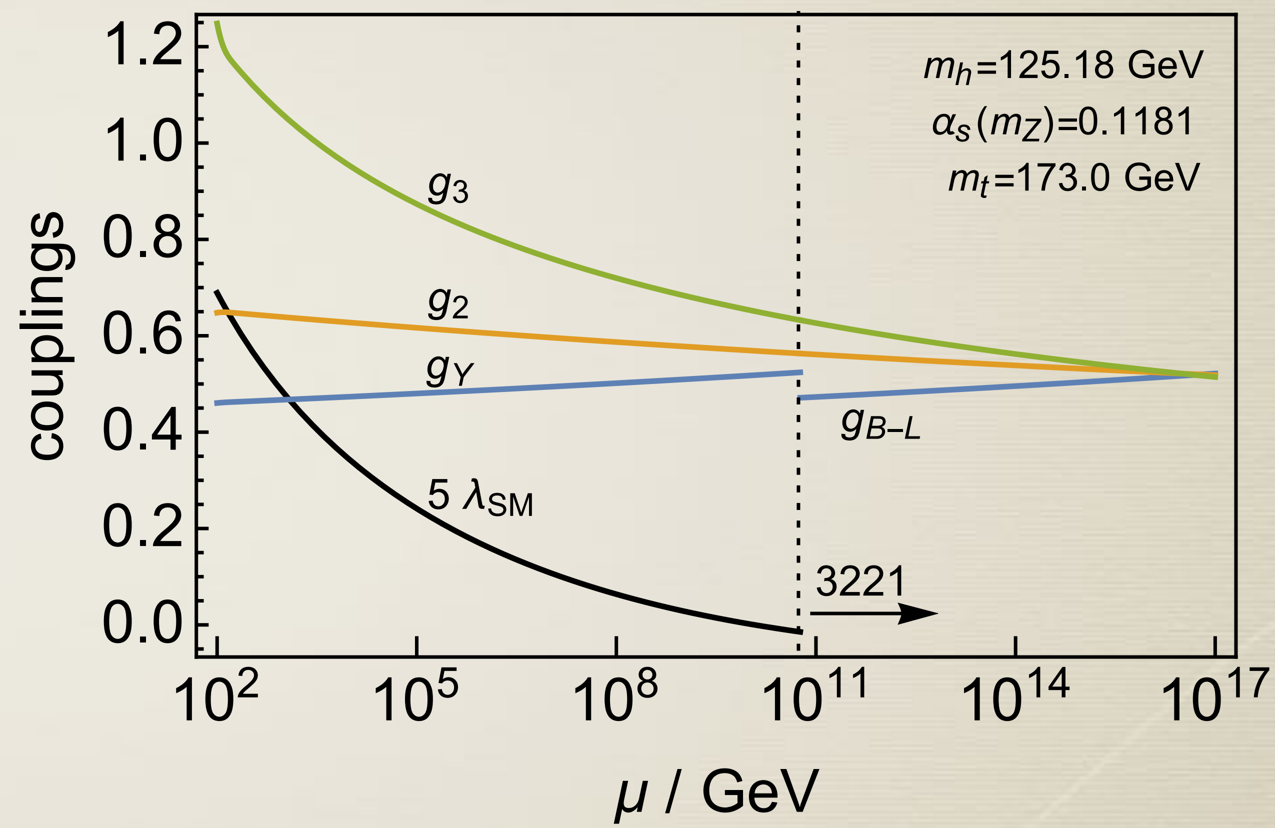
top quark mass,
strong coupling constant,
Higgs mass, etc.

Any other new physics models
impacted by precise measurements?

Higgs Parity

Hall and KH (2018, 2019)
Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



Higgs Parity
symmetry breaking scale

GUT, proton decay

(dark matter direct detection, gravitational waves, dark radiation, warm dark matter, neutron EDM, axion, ...)

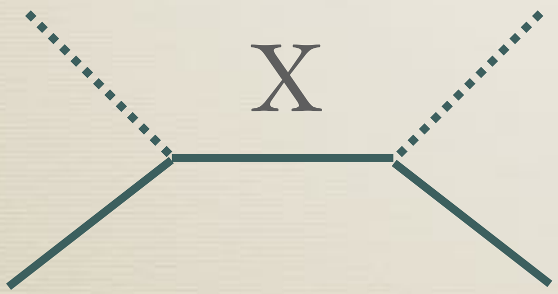
Back up

GUT

Yukawa interaction

No gauge invariant renormalizable coupling

$$\frac{c_{ij}}{M} H H' q_L \bar{q}_R$$

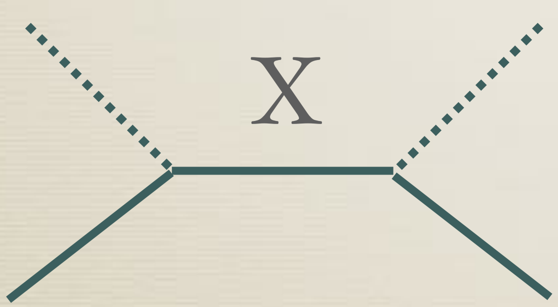


Strong CP problem solved

Babu and Mohapatra (1989)
Hall and KH (2018)

No gauge invariant renormalizable coupling

$$\frac{c_{ij}}{M} H H' q_L \bar{q}_R$$

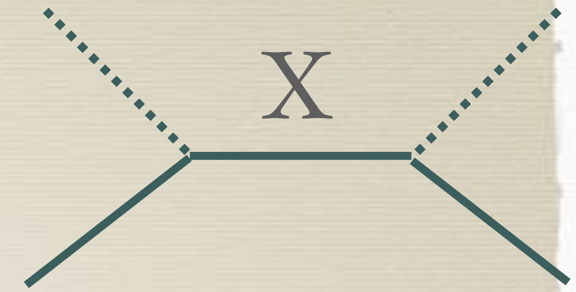


$$q_L(t,x) \overset{\text{HP}}{\leftrightarrow} q_R(t,-x)$$

$$\Downarrow$$

$$c = c^\dagger, \arg(\det[c]) = 0$$

Yukawa couplings



Small enough not to blow up the gauge coupling

	$SU(3)_c$	$SU(2)_L$	$SU(2)_R$	$U(1)$	$SU(4)$	$SO(10)$	coupling
up	**3**	**1**	**1**	2/3	**15**	**45**	$\bar{X}qH^\dagger + Xq'H'^\dagger$
	3	**2**	**2**	−1/3	**6**/**10**	**45**, **54**, **210**/**210**	$\bar{X}qH'^\dagger + Xq'H^\dagger$
down	**3**	**1**	**1**	−1/3	**6**/**10**	**10**, **126**/**120**	$\bar{X}qH + Xq'H'$
	3	**2**	**2**	2/3	**15**	**120**, **126**	$\bar{X}qH' + Xq'H$
electron	**1**	**1**	**1**	−1	**10**	**120**	$\bar{X}\ell H + X\ell'H'$
	1	**2**	**2**	0	**1**/**15**	**10**, **120**/**120**, **126**	$X\ell H' + X\ell'H$
neutrino	**1**	**1**	**1**	0	**1**/**15**	**1**, **54**, **210**/**45**, **210**	$X(\ell H^\dagger + \ell'H'^\dagger)$
	1	**2**	**2**	−1	**10**	**210**	$\bar{X}\ell H'^\dagger + X\ell'H^\dagger$
	1	**3**	**1**	0	**1**	**45**	$X\ell H^\dagger$
	1	**1**	**3**	0	**1**	**45**	$X\ell'H'^\dagger$

SO(10) embedding

Hall, KH (2018)

$$q, \ell, q', \ell' = 16$$

$$H, H' \subset 16_H$$

$$q(t,x) \leftrightarrow \bar{q}'(t,x)$$

C: Part of SO(10)

$$q(t,x) \leftrightarrow i\sigma_2 q^*(t,-x)$$

CP

$$q(t,x) \leftrightarrow i\sigma_2 \bar{q}'^*(t,-x)$$

$$SO(10) \times CP \xrightarrow{\phi_{45}^{-}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

CKM phase

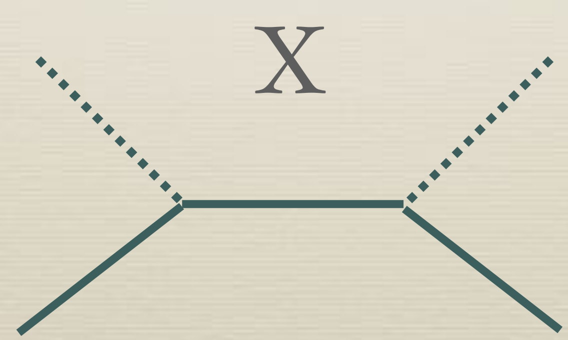
$$SO(10) \times CP \xrightarrow{\phi_{45}^{-}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

Real yukawas, without CP symmetry breaking...

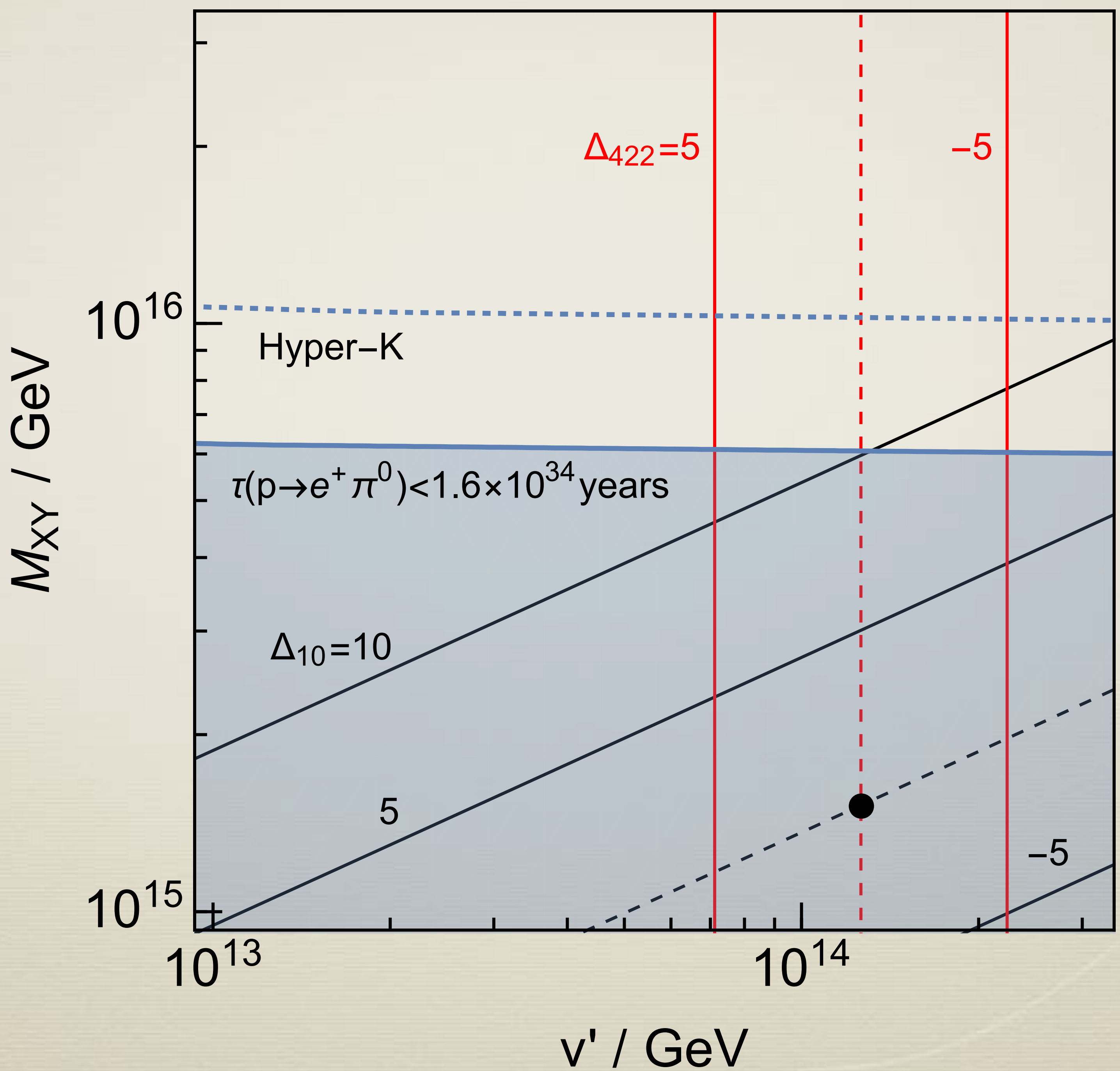
A simple renormalizable example to obtain CP phases

$$\mathcal{L} = \left(M^{ij} + i\lambda^{ij}\phi_{45}\right) X_{10,i} X_{10,j}$$

$$\frac{c_{ij}}{M} H H' q_i q'_j$$

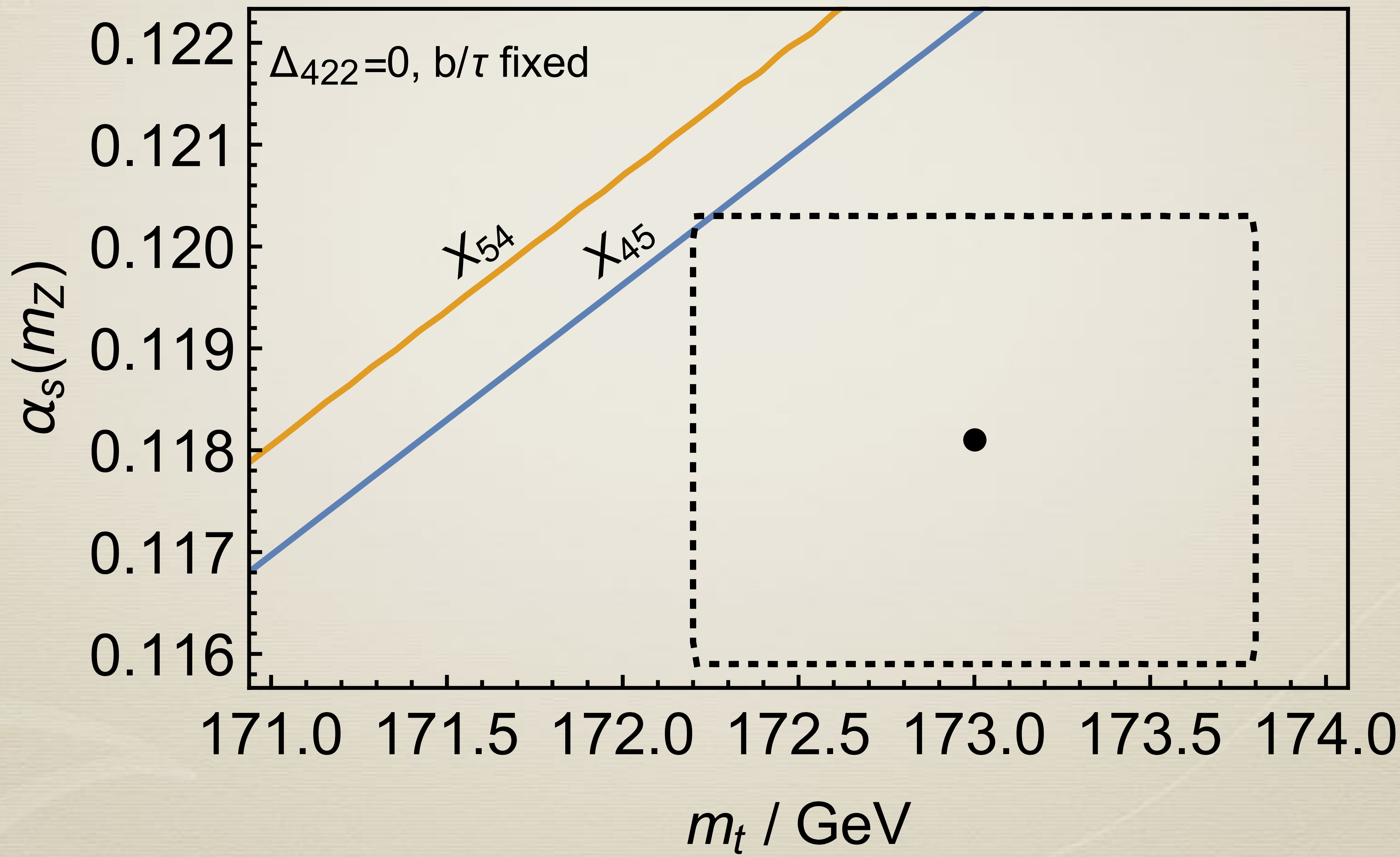


Pati-Salam



Δ422=5
−5
10^16
10^15
Hyper−K
τ(p→e+π0)<1.6×10^34 years
Δ10=10
5
−5
10^13
10^14
M_XY / GeV
v' / GeV

Pati-Salam



0.122
0.121
0.120
0.119
0.118
0.117
0.116
$\alpha_s(m_Z)$
Δ_{422}=0, b/τ fixed
X_{54}
X_{45}
171.0
171.5
172.0
172.5
173.0
173.5
174.0
m_t / GeV

Top-down perspective

SUSY GUT

3 parameters → 4 parameters

$g_{\mathrm{GUT}},\ M_{\mathrm{GUT}},\ m_{\mathrm{SUSY}}$ → $g_1,\ g_2,\ g_3,\ v_{\mathrm{EW}}$

(or more, e.g. Ω_{DM})

Similar structures

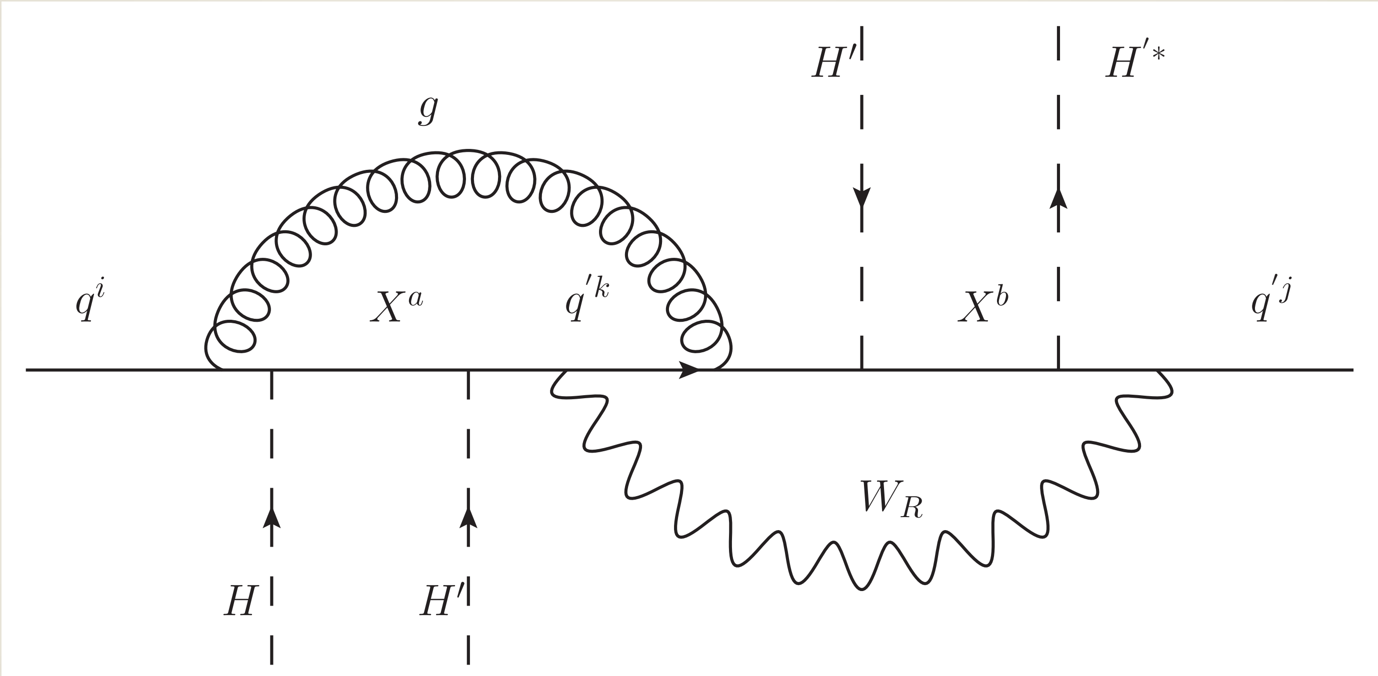
Parity GUT

4 parameters → 5 parameters

$g_{\mathrm{GUT}},\ M_{\mathrm{GUT}},\ v',\ y_t$ → $g_1,\ g_2,\ g_3,\ y_t,\ \lambda_{\mathrm{higgs}}$

Non-zero CPV

Hall, KH (2018)



$$\delta\theta \sim 10^{-11} \frac{\theta^u_{23}\theta^d_{23}}{V^2_{cb}}$$

Suppressed by loop factors, flavor mixing

Correction to the gauge coupling unification by high dimensional operator

$$SO(10) \xrightarrow{\phi_{210}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times C_{LR}$$

$$\frac{210^{abcd}}{M_*} F_{10}^{ab} F_{10}^{cd} \qquad \Delta\left(\frac{2\pi}{\alpha}\right) \lesssim 10$$

$$SO(10) \times CP \xrightarrow{\phi_{45}} SU(3) \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \times P_{LR}$$

$$\frac{45^{ac}}{M_*} \frac{45^{bd}}{M_*} F_{10}^{ab} F_{10}^{cd} \qquad \Delta\left(\frac{2\pi}{\alpha}\right) \lesssim 1$$

Correction to the gauge coupling unification by high dimensional operator

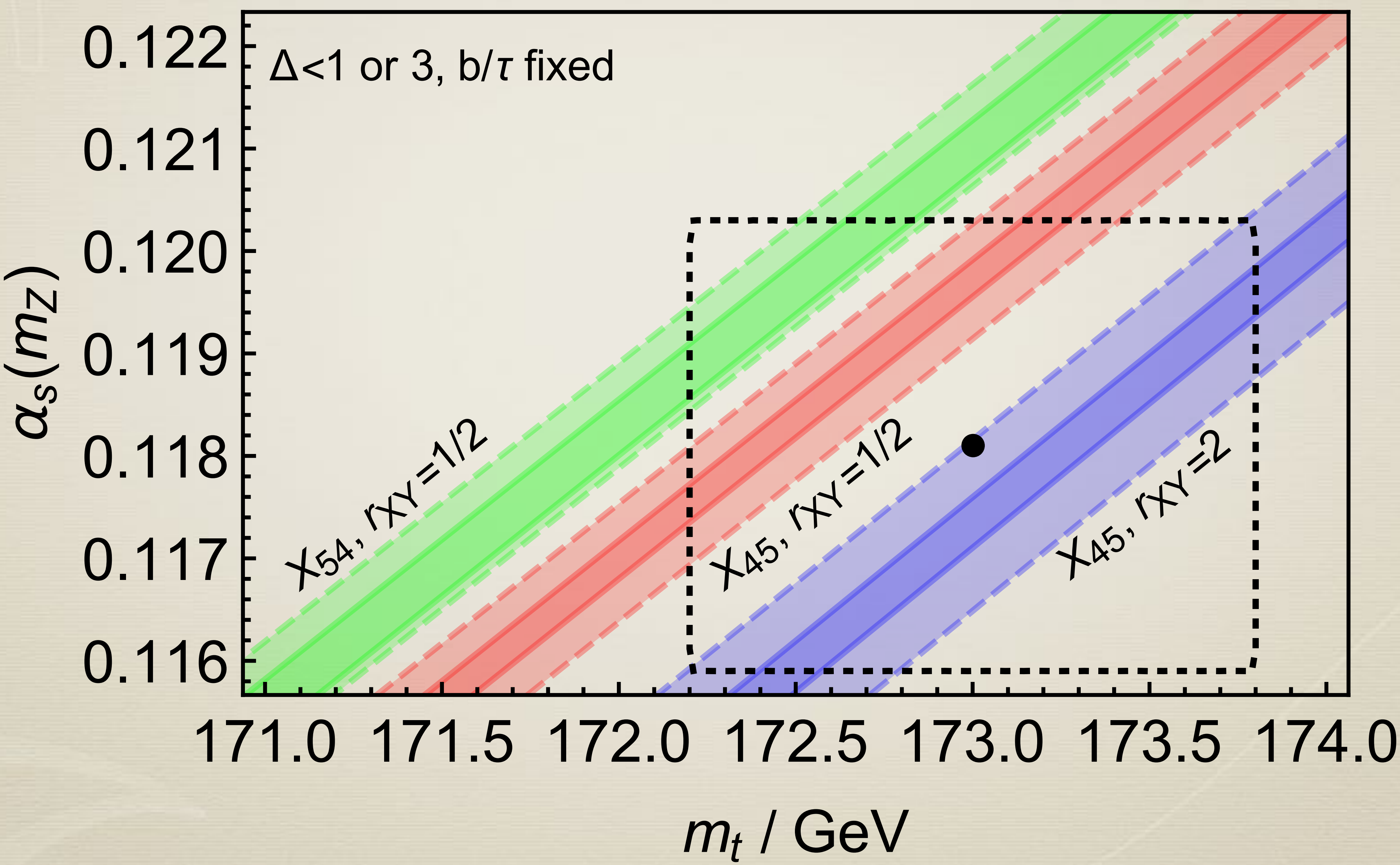
$$SO(10) \xrightarrow{\phi_{54}} SU(4) \times SU(2)_L \times SU(2)_R \times C_{LR}$$

$$\frac{54^{ab}}{M_*} F_{10}^{ac} F_{10}^{bc} \qquad \Delta\left(\frac{2\pi}{\alpha}\right) \lesssim 1$$

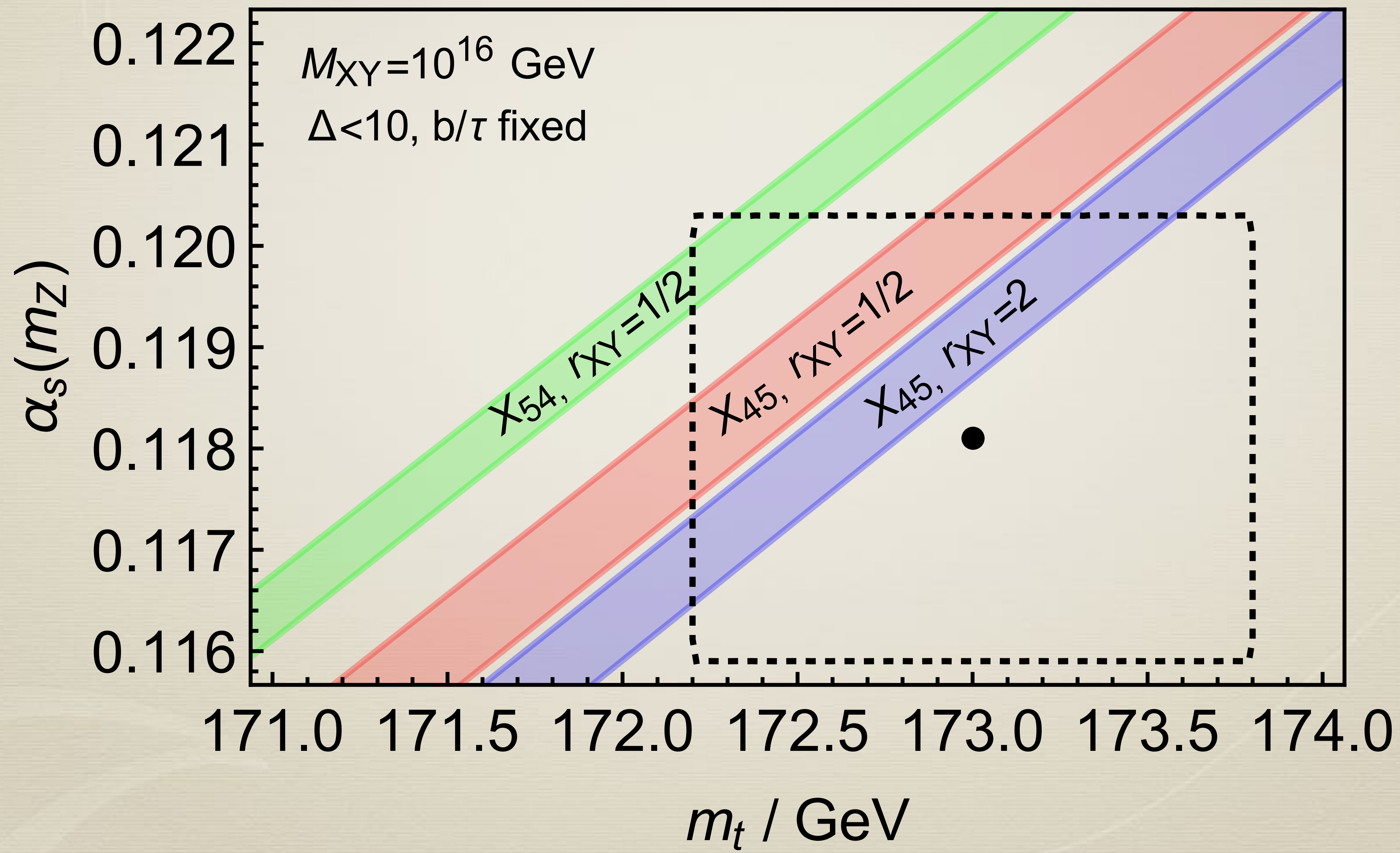
$$SO(10) \times CP \xrightarrow{\phi_{210}} SU(4) \times SU(2)_L \times SU(2)_R \times P_{LR}$$

$$\frac{210}{M_*} \frac{210}{M_*} F_{10} F_{10} \qquad \Delta\left(\frac{2\pi}{\alpha}\right) \ll 1$$

Small threshold corrections



Proton decay observed



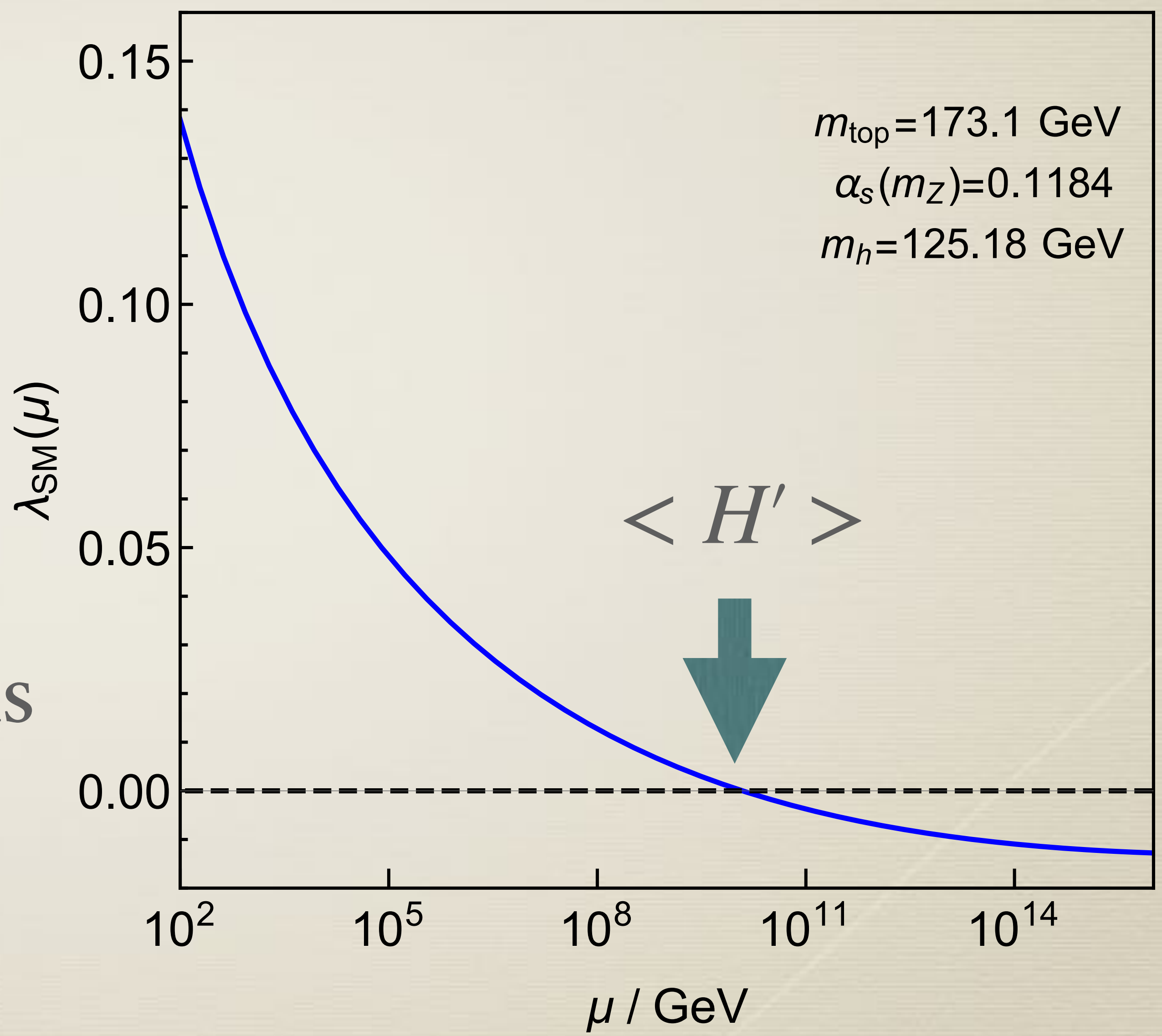
More on small quartic

HP symmetry breaking scale

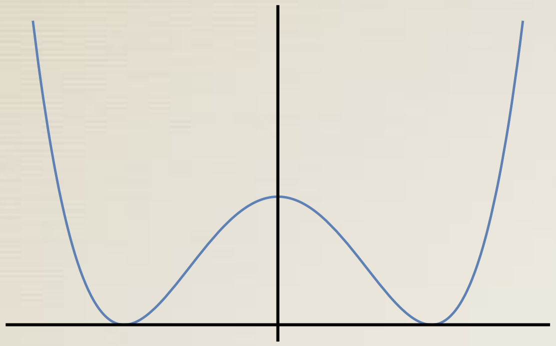
I will show that

$$\lambda_{SM}(< H' >) \simeq 0$$

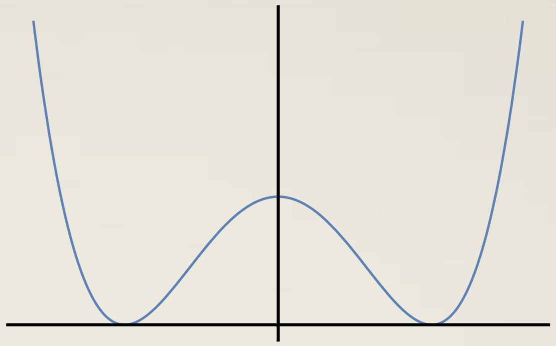
because Higgs Parity constrains the potential of H and H'



Higgs potential



HP

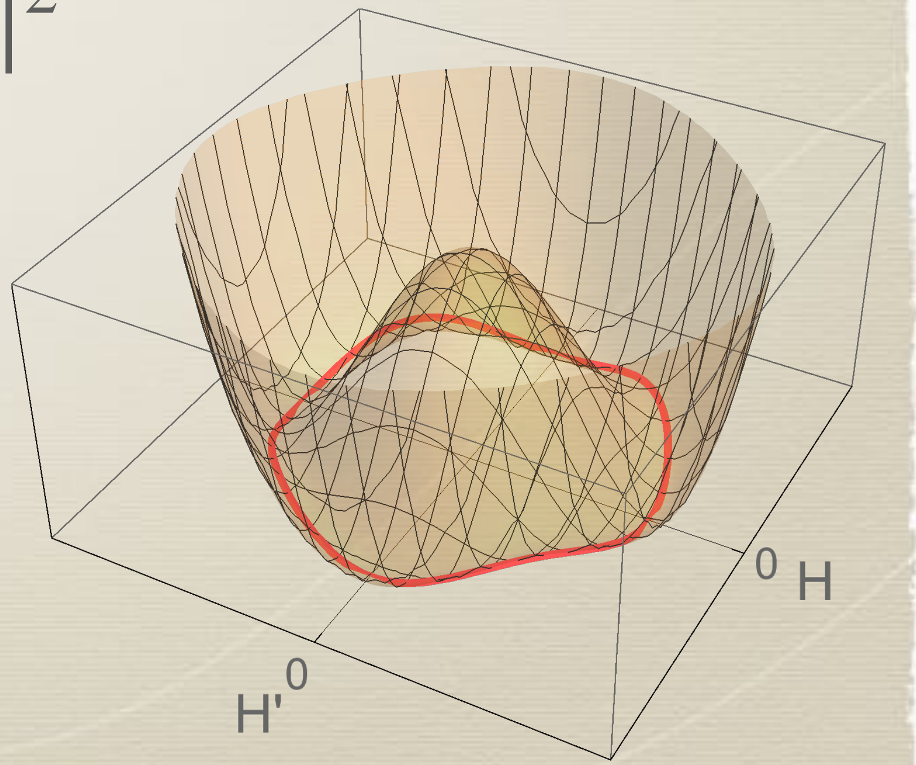


$$V = \left(\lambda|H|^4 - m^2|H|^2\right) + \left(\lambda|H'|^4 - m^2|H'|^2\right) + \tilde{y}\,|H|^2|H'|^2$$

$$= \lambda\left(|H|^2 + |H'|^2 - v'^2\right)^2 + y|H|^2|H'|^2$$

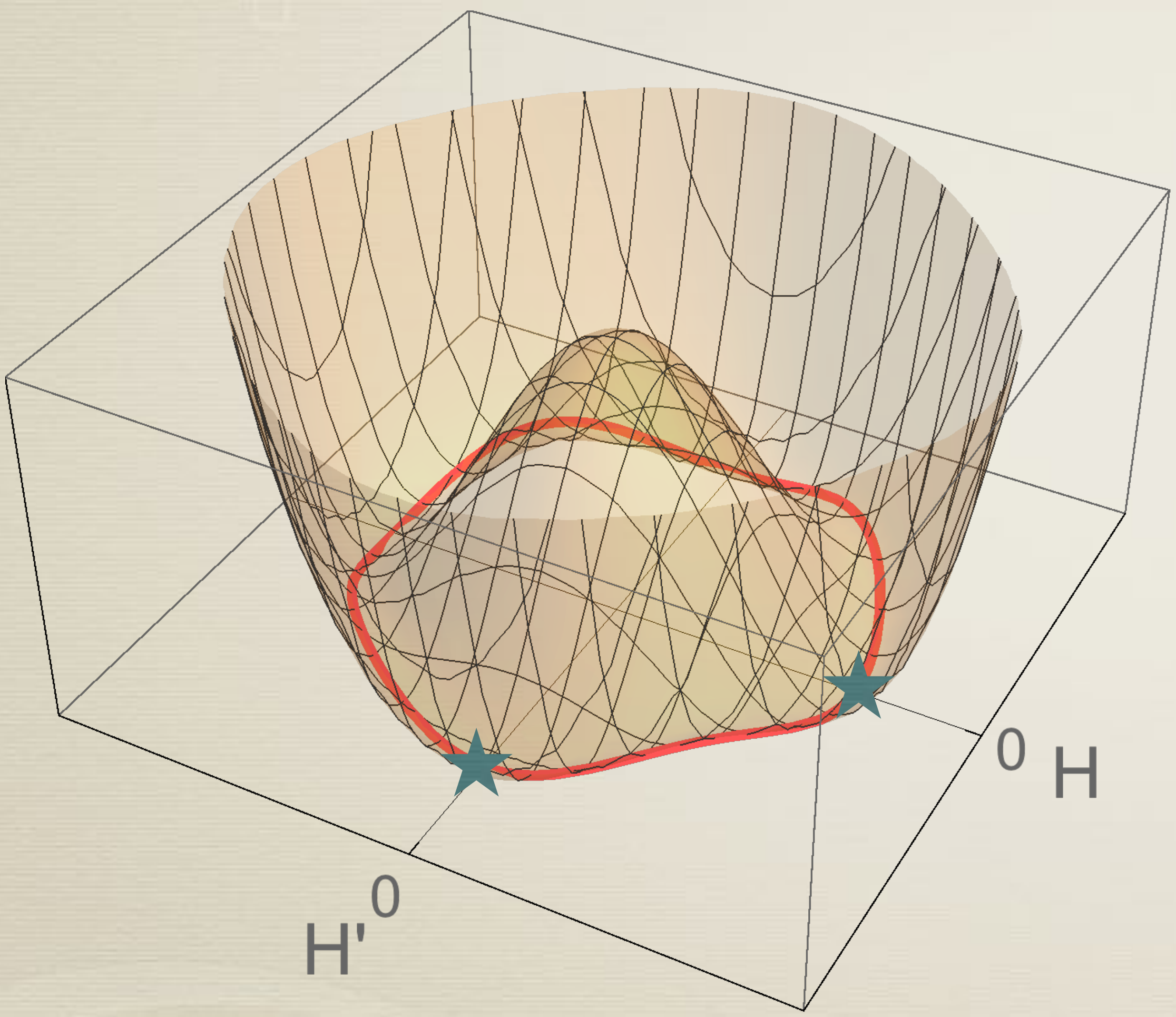
Can we find the minimum with

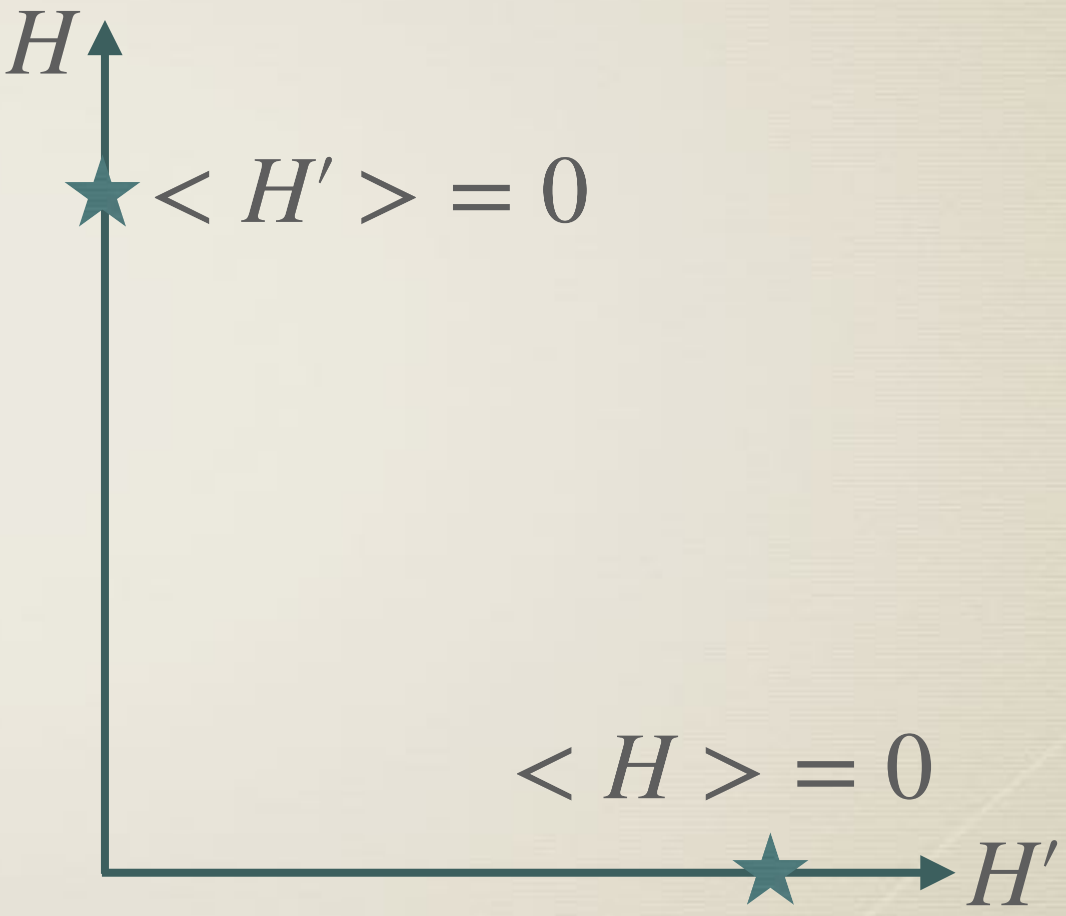
$$\langle H\rangle \ll \langle H'\rangle \,?$$



$y > 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$

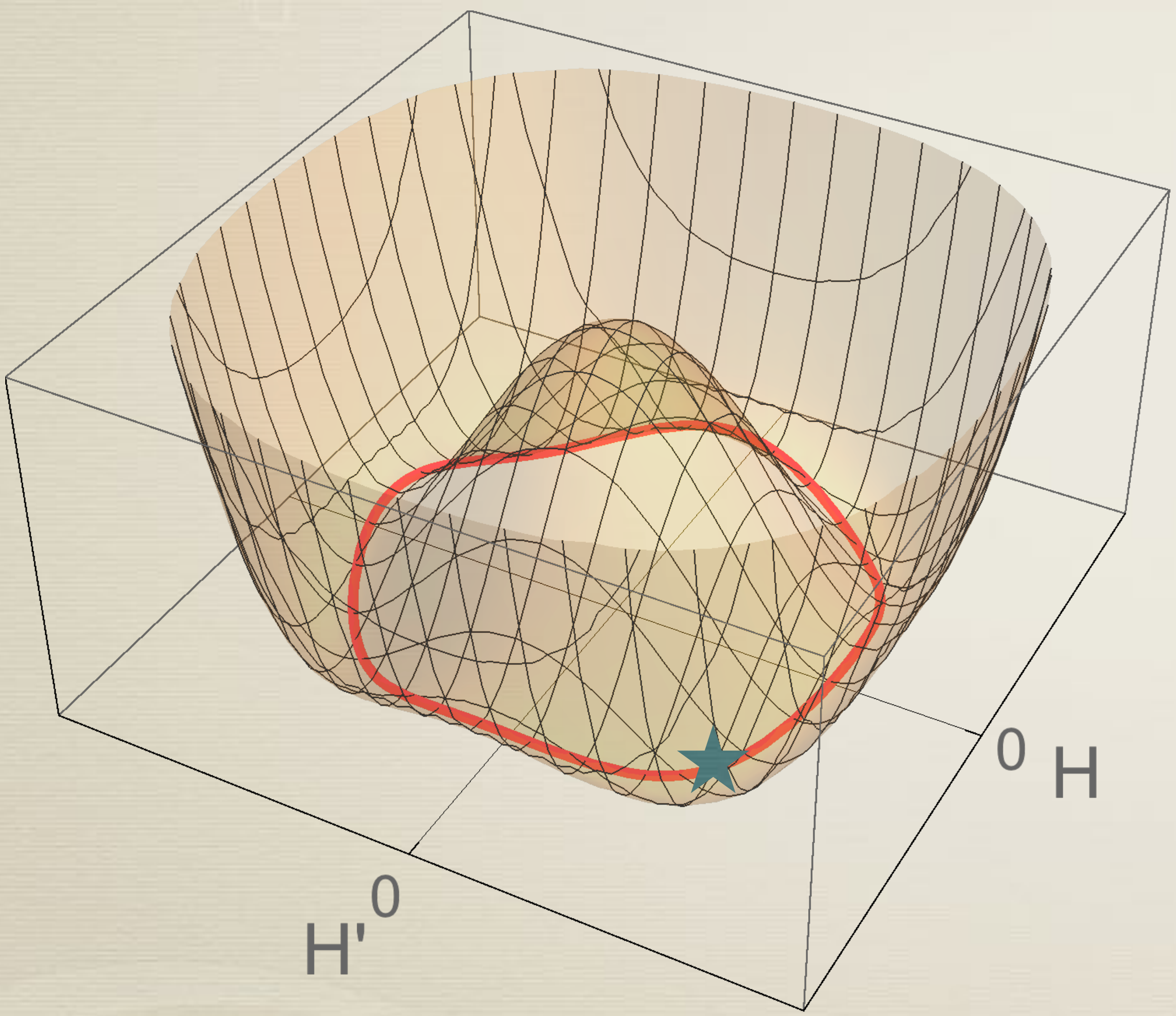


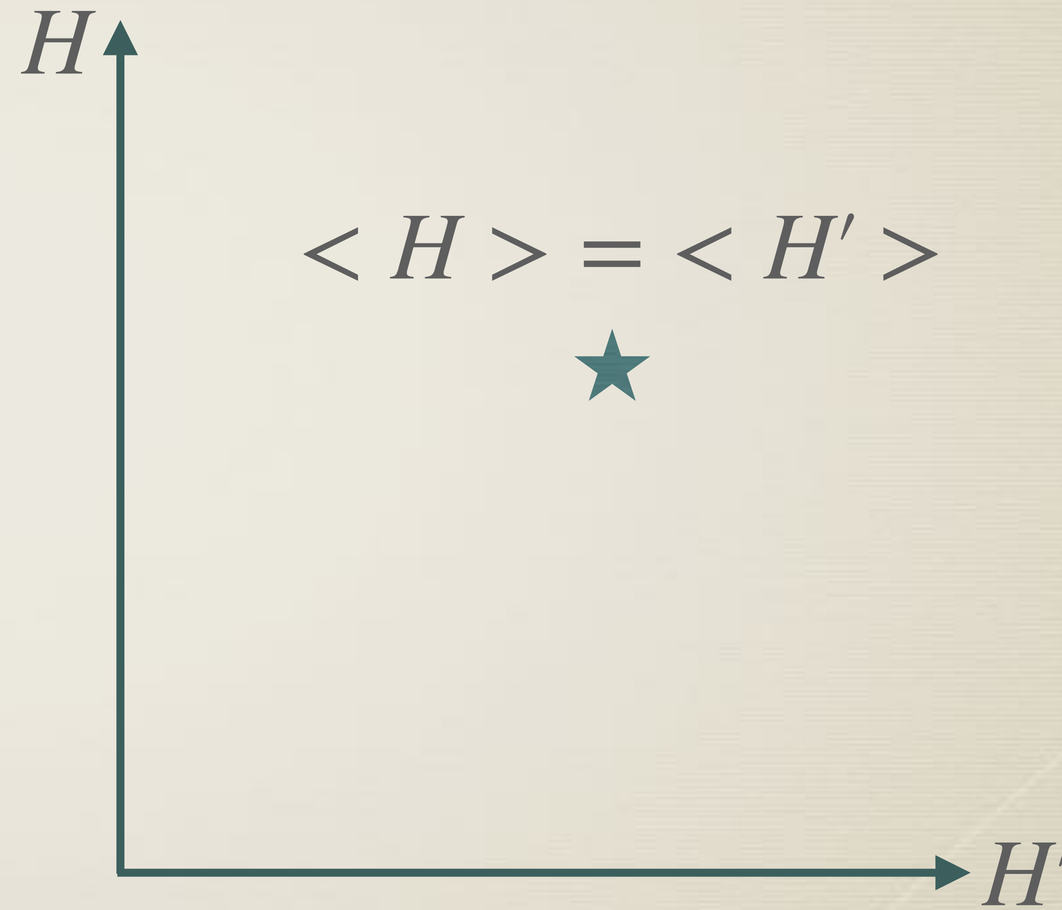


$$0 \neq \langle H \rangle \ll \langle H' \rangle$$

$y < 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$

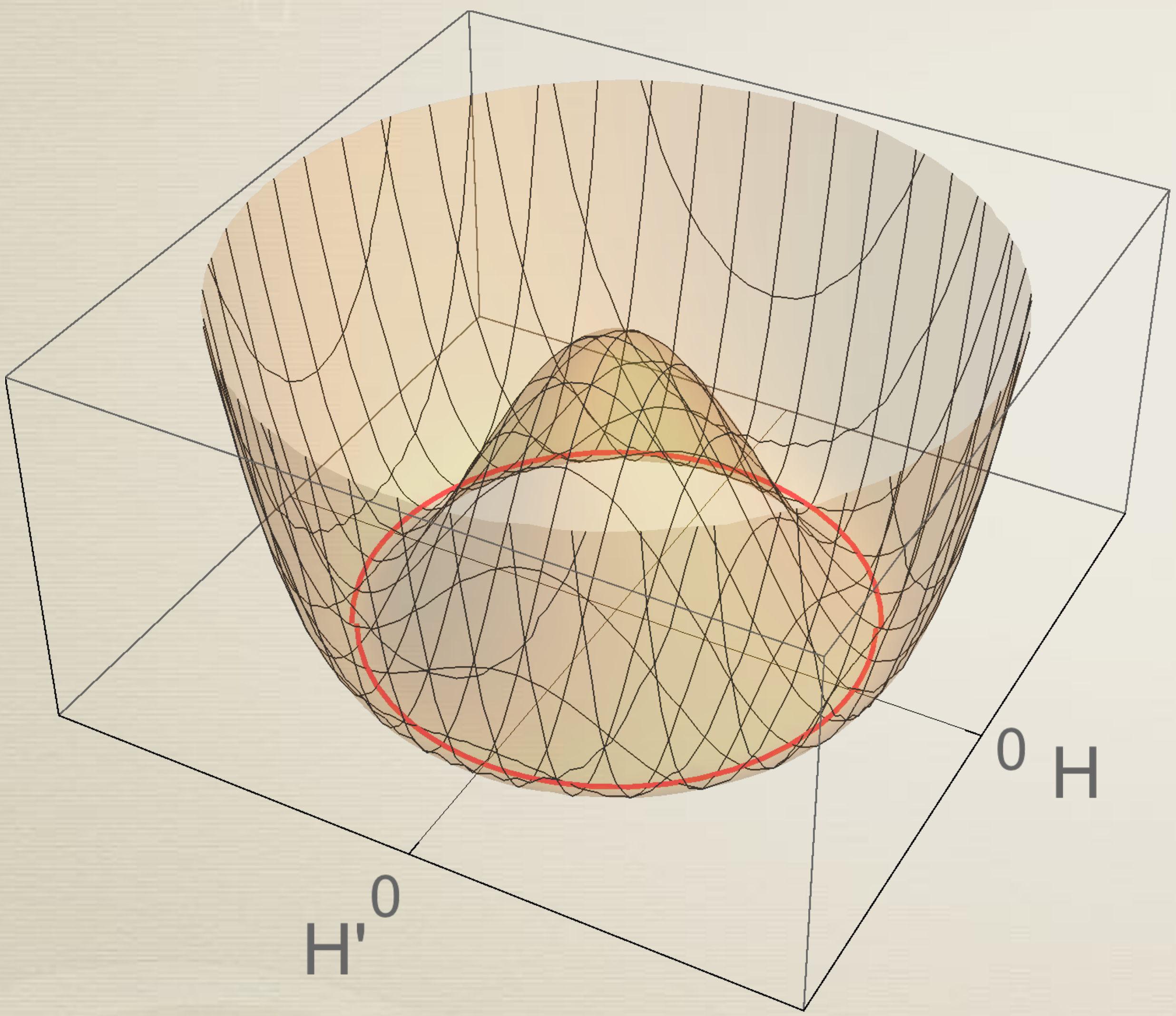


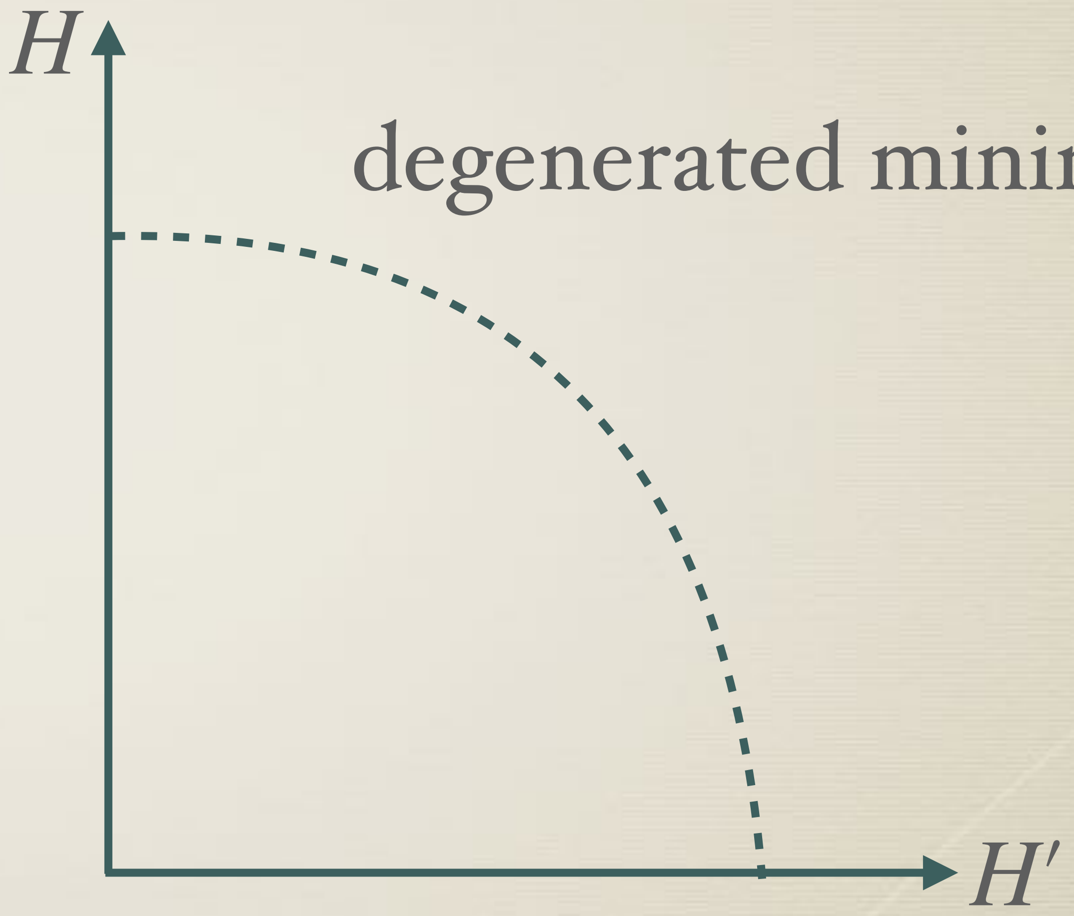


~~$\langle H \rangle \ll \langle H' \rangle$~~

$y \simeq 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$



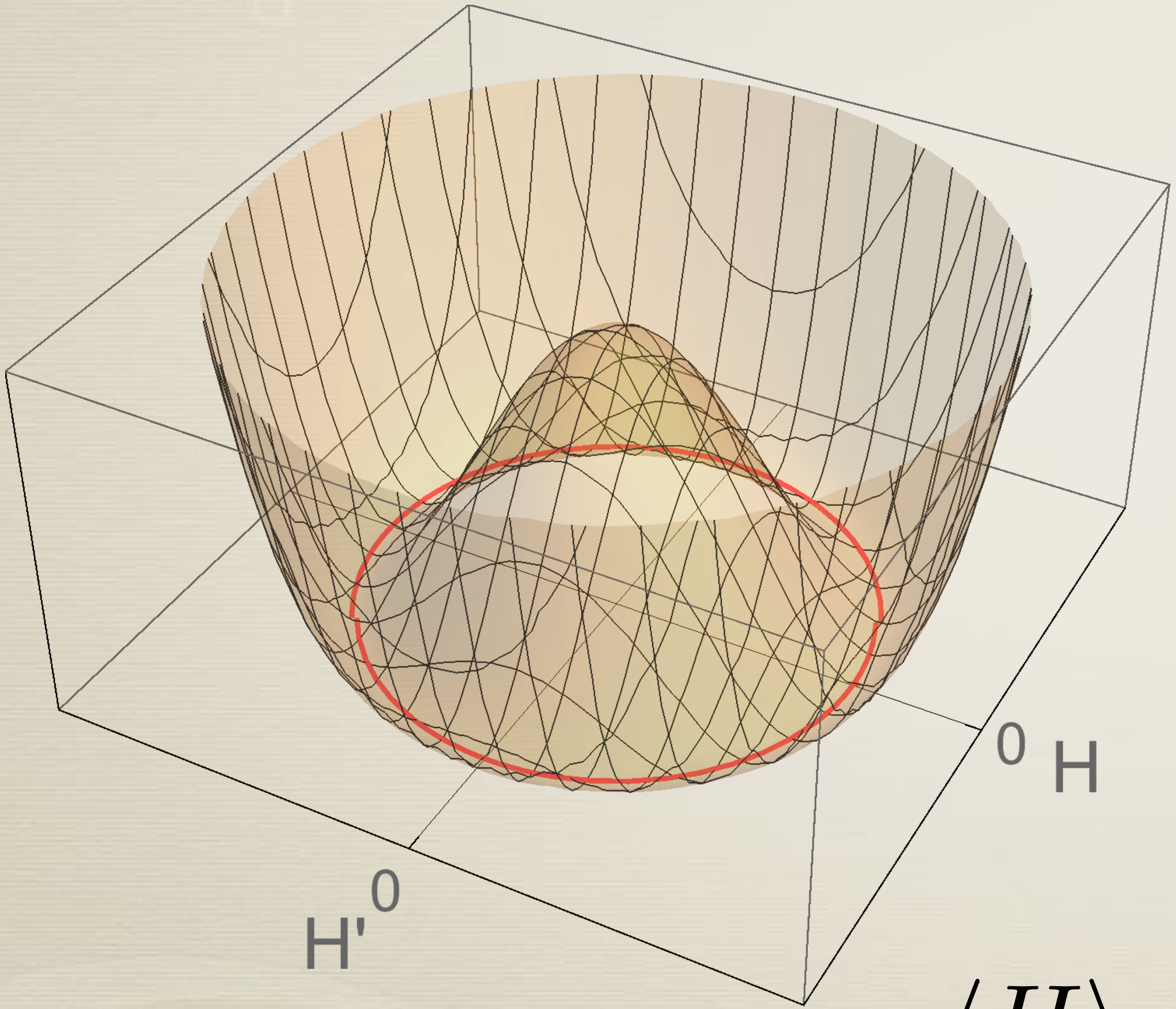


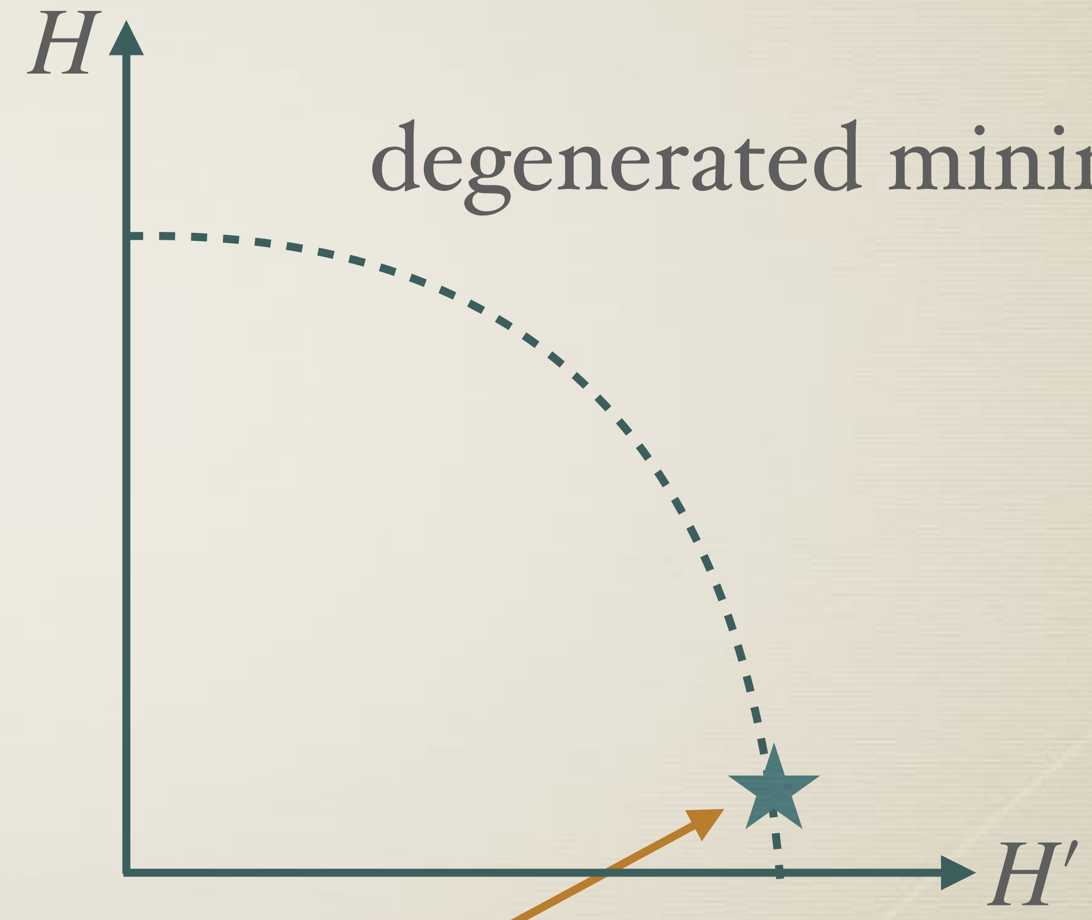
symmetry rotating the vector

(H, H')

$y \simeq 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + y|H|^2|H'|^2$$



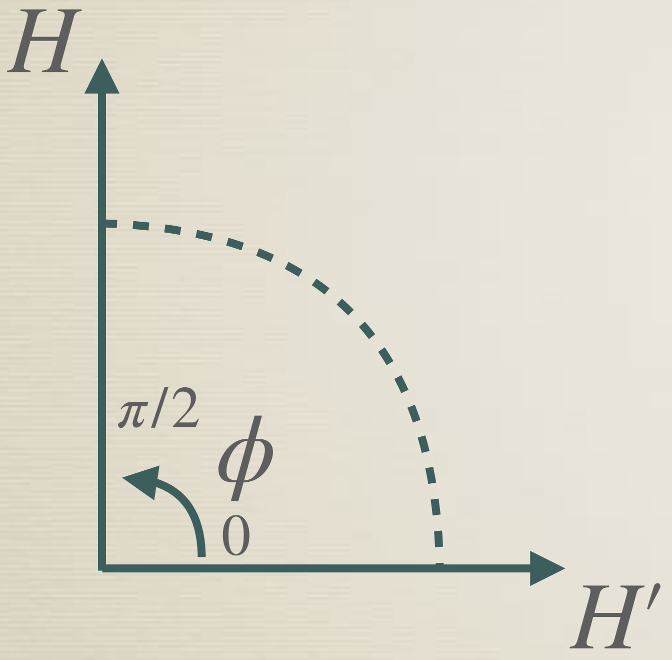


$\langle H \rangle \ll \langle H' \rangle$?

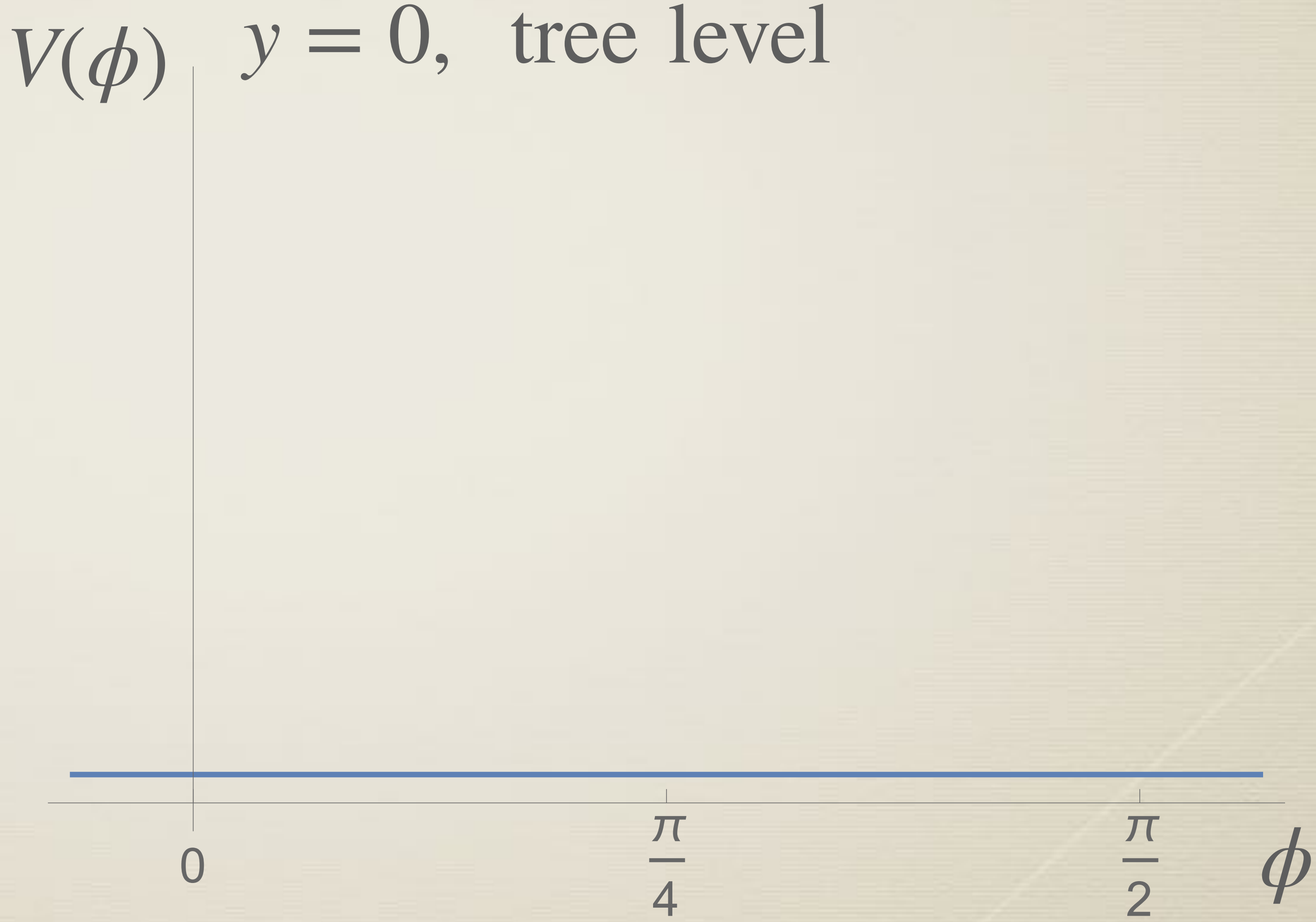
Degeneracy is resolved by quantum corrections

$y \simeq 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2$$



angular direction ϕ

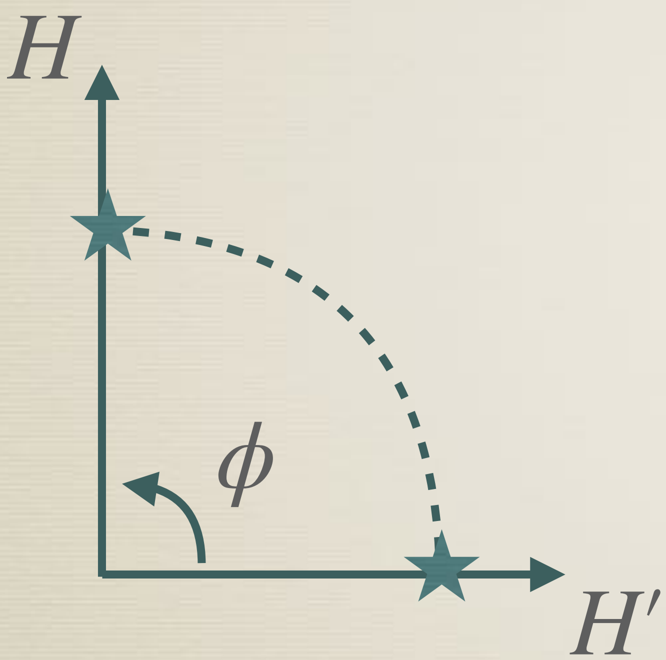


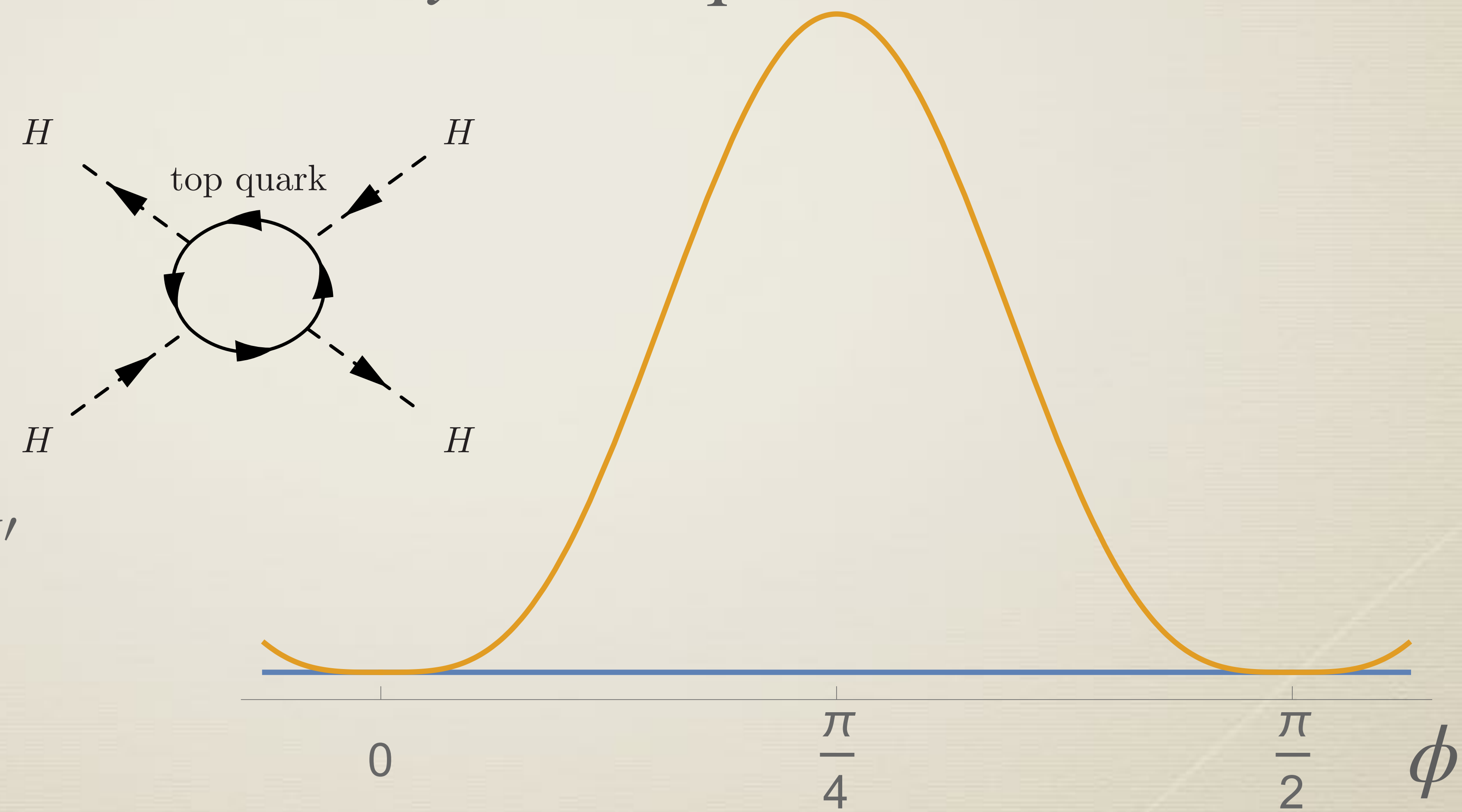
$$y \simeq 0$$

Colemann-Weinberg potential

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + V_{\text{quantum}}(H, H')$$

$y = 0$, quantum correction



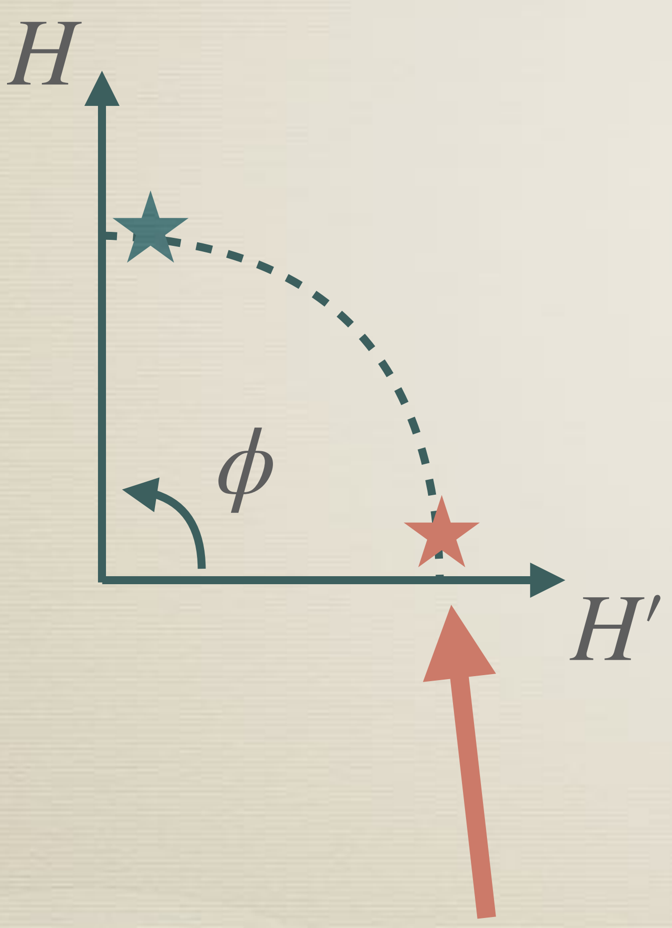


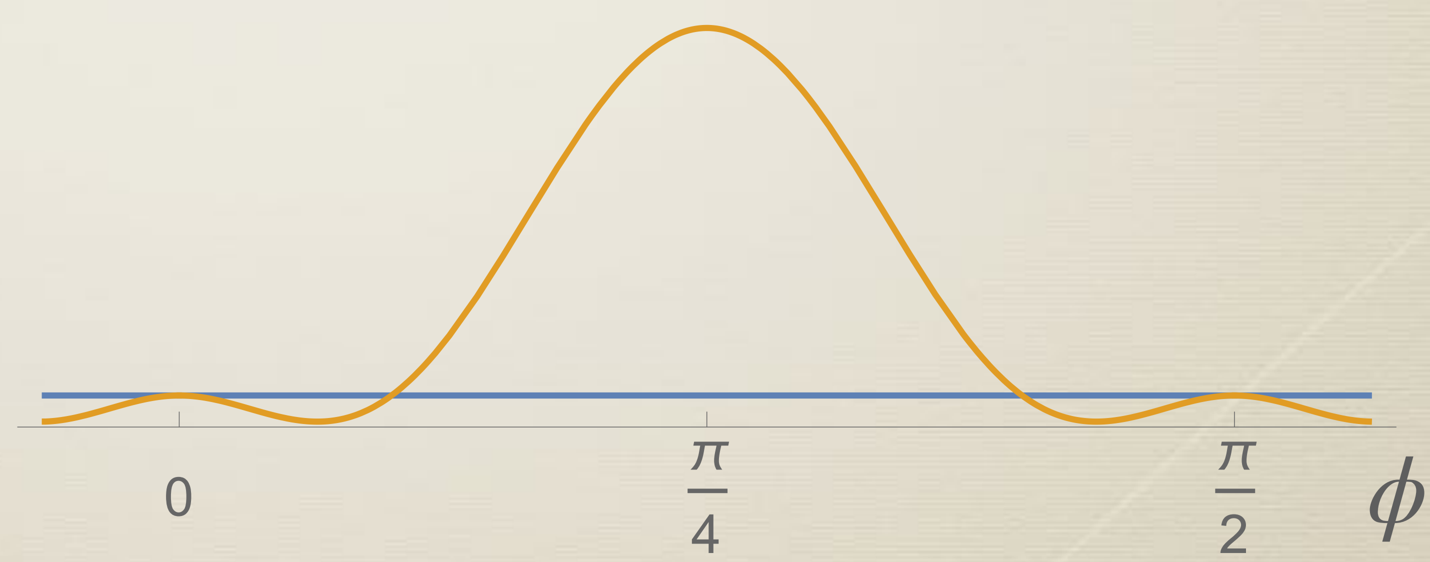
$y \simeq 0$

$$V = \lambda(|H|^2 + |H'|^2 - v'^2)^2 + V_{\text{quantum}}(H, H') + y|H|^2|H'|^2$$

$$y \simeq -\frac{v^2}{v'^2}, \quad \text{quantum correction}$$

(fine-tuned Higgs mass)





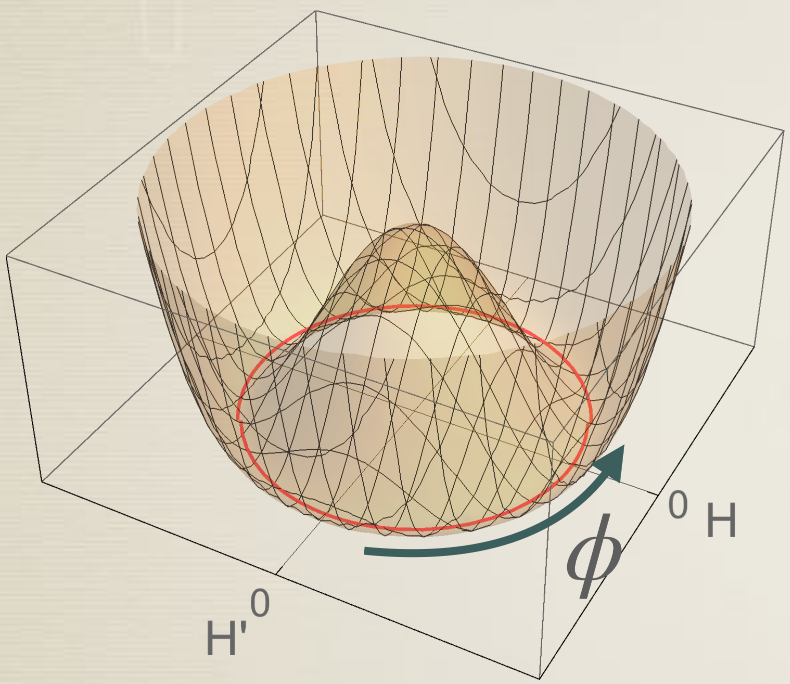
$\langle H \rangle \ll \langle H' \rangle$ is achieved !

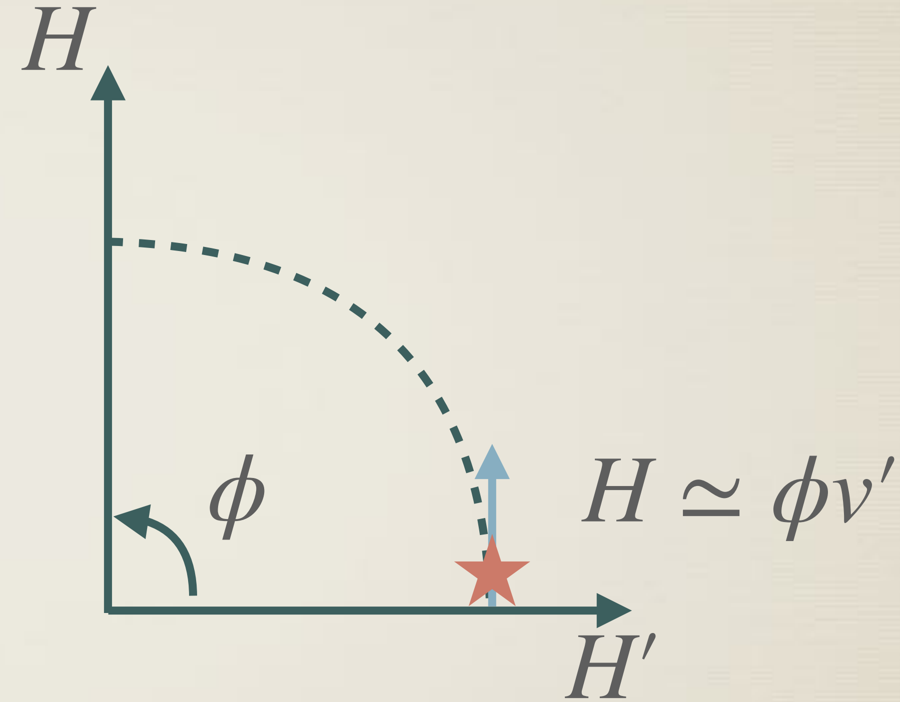
Hall, KH (2018)

Prediction on the quartic coupling

Hall, KH (2018)

$V \simeq \lambda(|H|^2 + |H'|^2 - v'^2)^2$ + small corrections





symmetry rotating the vector (H, H')

Standard Model Higgs is a (pseudo) Nambu-Goldstone boson associated with symmetry breaking by $\langle H' \rangle = v'$

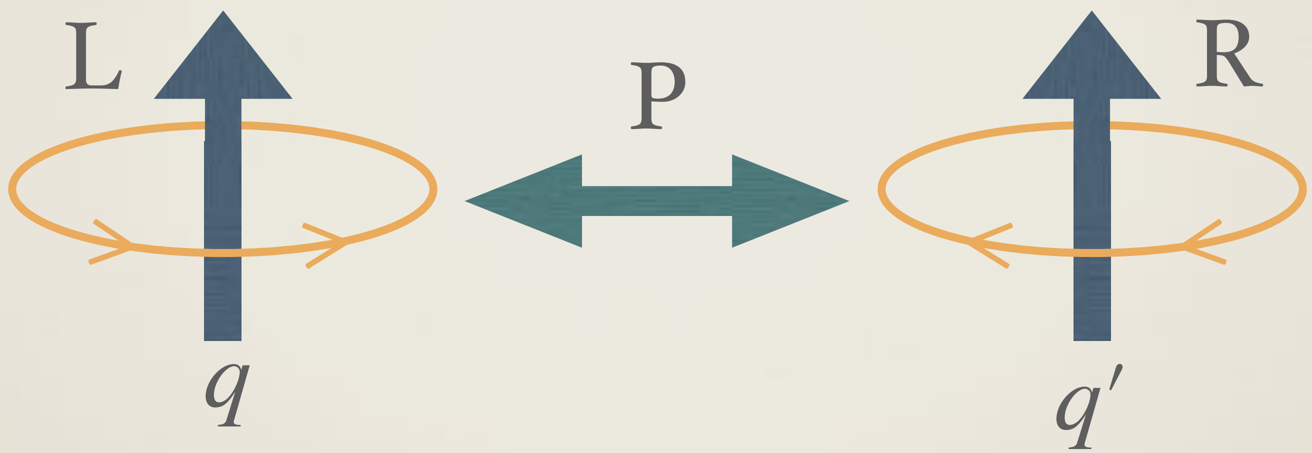
$$\lambda_{\rm SM}(v') \simeq 0$$

(up to calculable threshold correction)

Higgs Parity can solve Strong CP problem

Parity solution

Mohapatra and Senjanovic (1978)
Beg and Tsao (1978)
Babu and Mohapatra (1989)
Barr, Chang and Senjanovic (1991)



How the strong CP problem is solved depends on what q' is.

(q' = antiparticle of q : P is CP)

Mirrored electroweak theory

SM particles | New particles

strong interaction

$SU(3)_c$

SM particles		New particles
q		q’
u		u’
d		d'
L	HP	L’
e	⟷	e’
H		H’

electroweak

$W, Z \quad SU(2)_L \times U(1)_Y$

$\downarrow$

$\gamma \quad U(1)_{\rm EM}$

electroweak’

$SU(2)_L' \times U(1)_Y' \quad W', Z'$

$\downarrow$

$U(1)_{\rm EM}' \quad \gamma'$

Strong CP problem solved

Barr, Chang and Senjanovic (1991)

HP

$$\mathscr{L} = yq\bar{u}H^{\dagger} + yq'^{\dagger}\bar{u}'^{\dagger}H' + y^{*}q^{\dagger}\bar{u}^{\dagger}H + y^{*}q'\bar{u}'H'^{\dagger}$$

HP

~~$+\frac{\theta_{\mathrm{QCD}}}{8\pi^2}\mathbf{E}^a \cdot \mathbf{B}^a$~~

$\Delta\bar{\theta}_q$

$\Delta\bar{\theta}_{q'} = -\Delta\bar{\theta}_q$

$\bar{\theta} = \Delta\bar{\theta}_q + (-\Delta\bar{\theta}_q) = 0$

cancel with each other

Non-zero CP violation

$$\frac{C}{M_{\rm pl}^2}\left(|H|^2 - |H'|^2\right)\mathbf{E}\cdot\mathbf{B}$$

Electric and magnetic fields of gluon

$$d_n \simeq 10^{-26}\ e\ \mathrm{cm} \times C\left(\frac{v'}{10^{12}\ \mathrm{GeV}}\right)^2$$

* Present limit $d_n < 2.9 \times 10^{-26} e\ \mathrm{cm}$ Baker et.al (2006)
* PSI $d_n < 5 \times 10^{-27} e\ \mathrm{cm}$ Baker et.al (2011)
* SNS $d_n < 3 \times 10^{-28} e\ \mathrm{cm}$ Tsentalovich (2014)

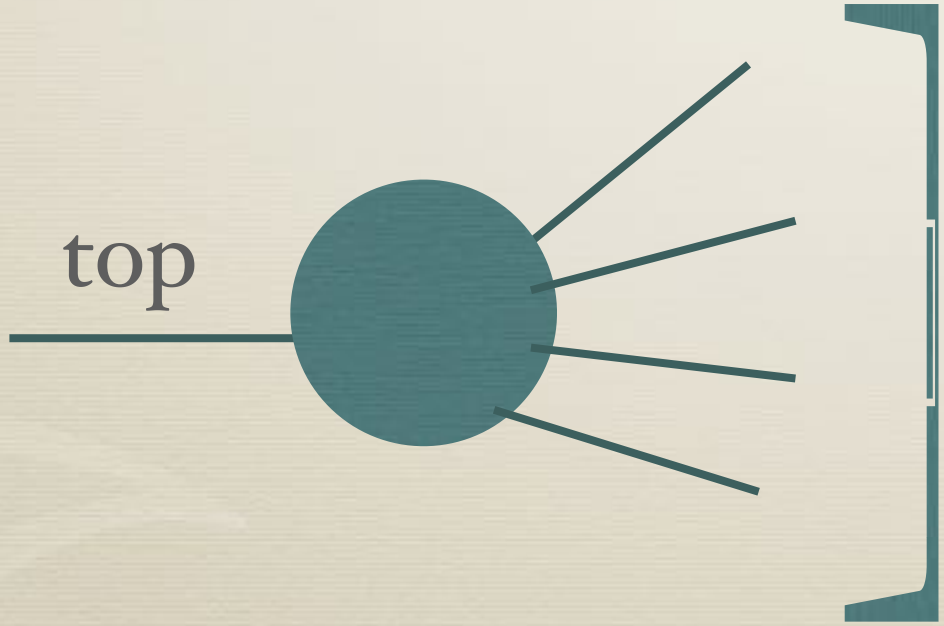
SM parameters

“top quark mass”

pole mass 172.9 ± 0.4 GeV

Particle Data Group

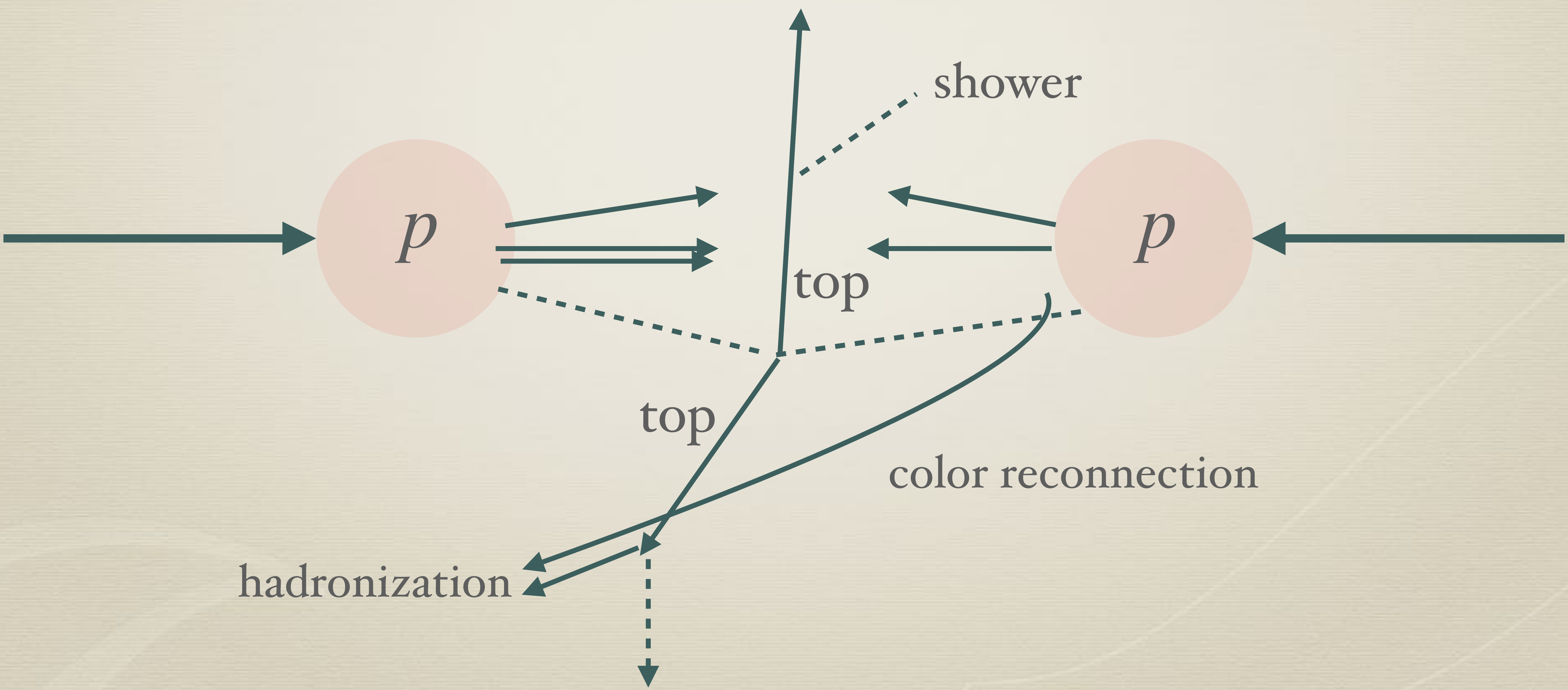
if top were colorless, isolated objects



measure momentum and energy,
take invariant mass

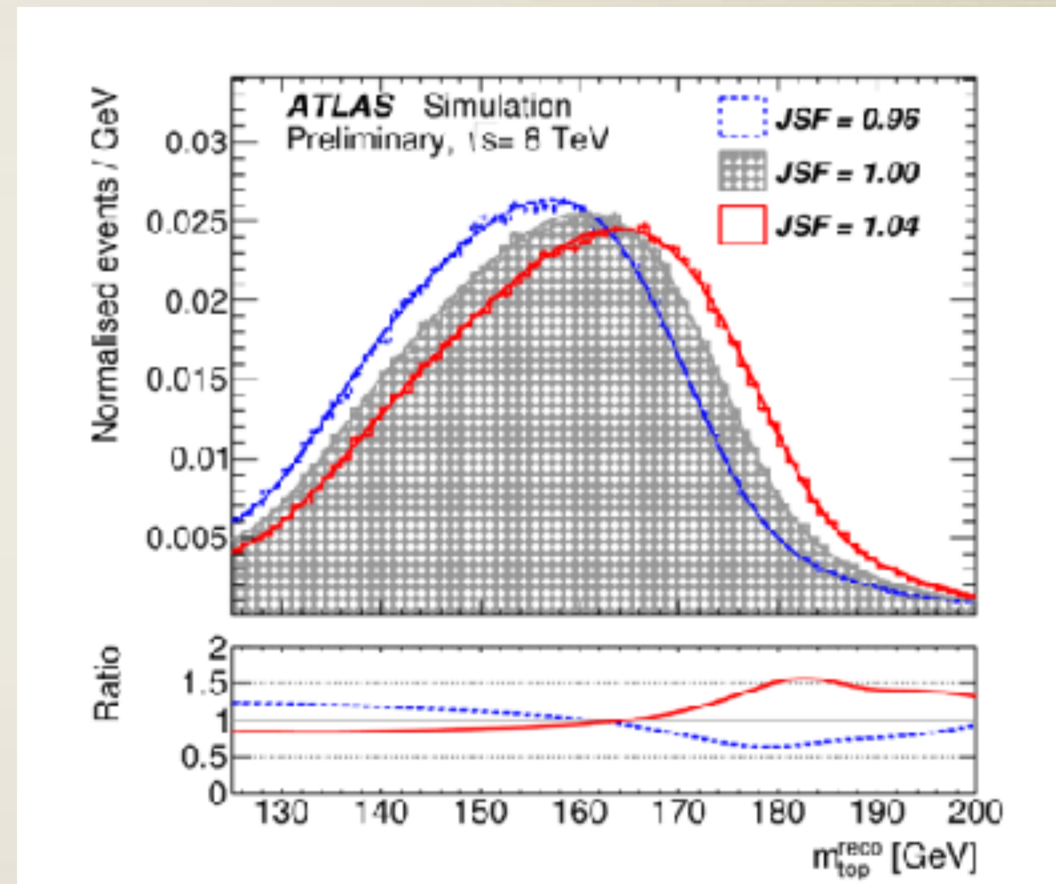
“top quark mass”

but of course top is colored and is not isolated



“top quark mass”

mass parameter → Monte-Carlo Simulation → templates of distribution of kinematical observables



fitting the templates, combining results,

$$172.9 \pm 0.4 \text{ GeV}$$

Uncertainty from non-perturbative QCD $\Delta m_t \gtrsim \Lambda_{QCD}$

MSbar quantity

pole mass

$$y_{t,\overline{MS}}(m_t) = 0.93690 + 0.00556(\frac{m_t}{\text{GeV}} - 173.34) - 0.00042\frac{\alpha_s(m_Z) - 0.1184}{0.0007}$$

Buttazzo et.al. (2013)

* NNNLO QCD corrections included

* Uncertainty from non-perturbative nature of QCD

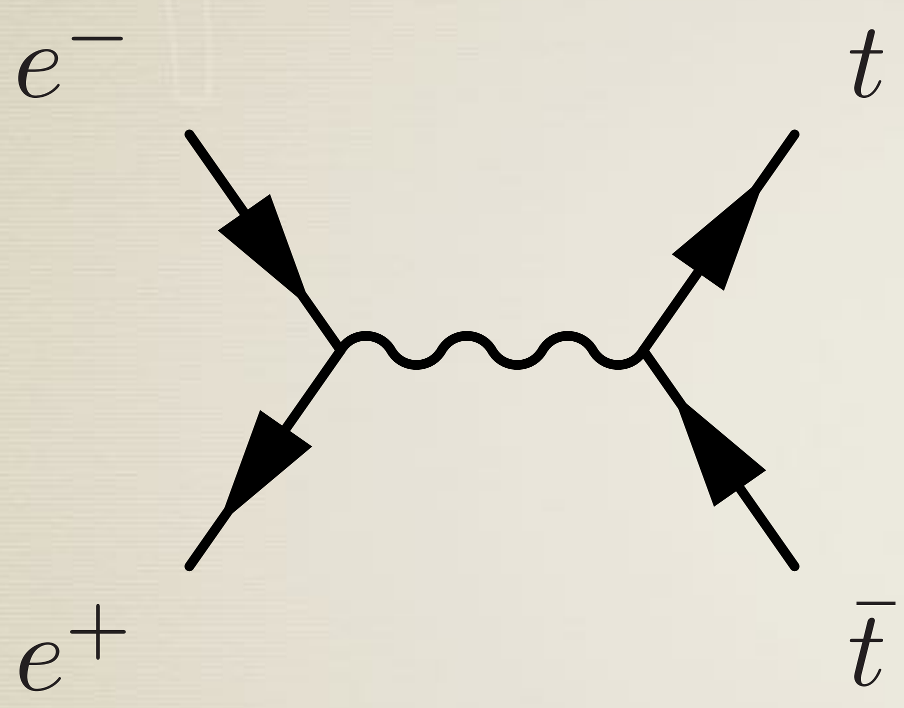
$\Delta m_t \sim \Lambda_{\rm QCD}$

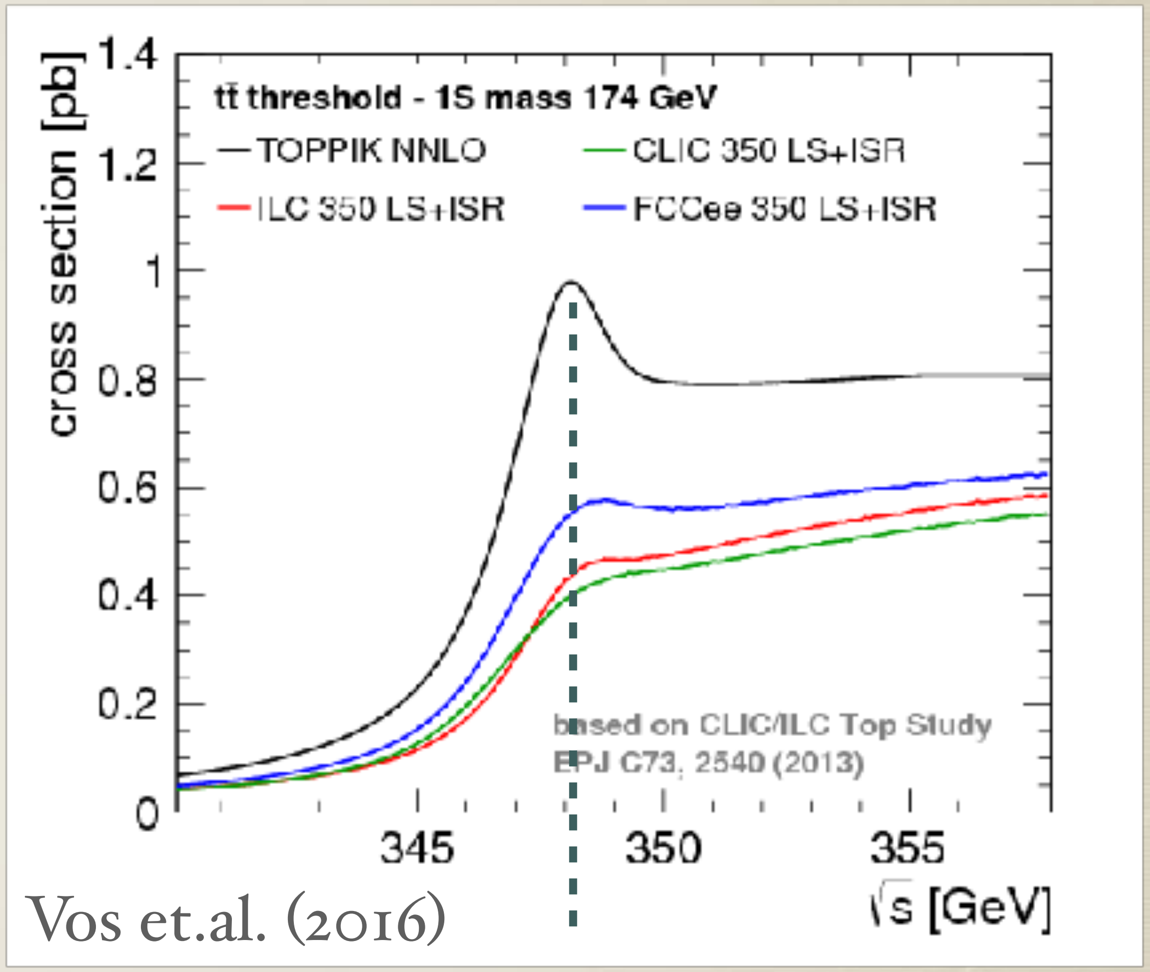
Bigi, Shifman, Uraltsev and Vainshtein (1994)
Benek and Braun (1994)

Eventually, we should directly determine MSbar quantity by

MSbar quantity ⟷ observables

Lepton colliders





$M_{t\bar{t}}(1S)$

$$M_{t\bar{t}}(1S) = 2(165 + 7.20 + 1.20 + 0.216 + 0.0077 + \cdots)\ \text{GeV}$$

Kiyo, Mishima and Sumino (2015)

$$\Delta m_{t,\overline{MS}} \simeq \text{few tens MeV}$$

Strong coupling constant

e.g. HPQCD collaboration (2008)

tune

Lattice ← mass spectrum

↓

Physical quantity

↑

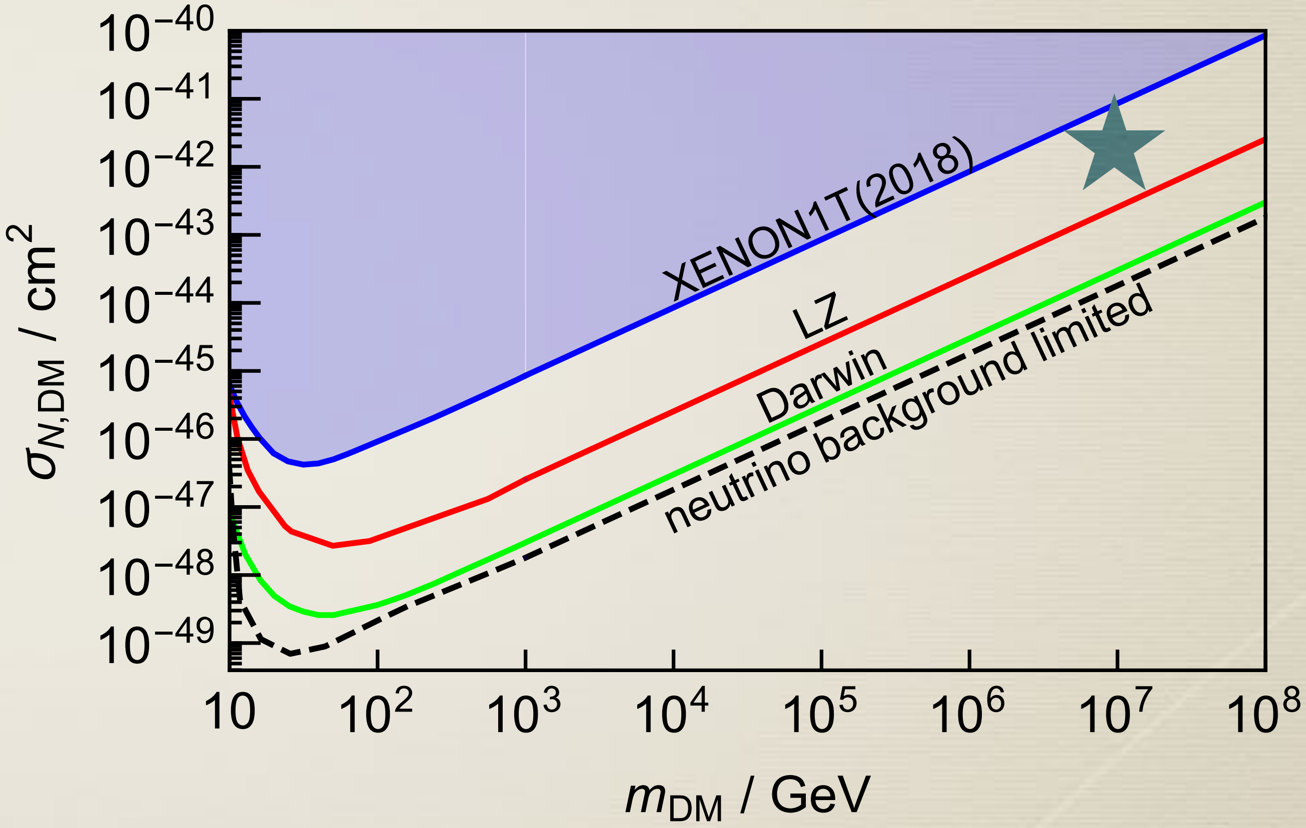
Perturbation theory $\alpha_s(\mu), m_{b,c}(\mu)$

Dark Matter

Precise measurement and dark matter

Dunsky, Hall and KH (2019)

top quark mass
Higgs mass
strong coupling constant



Higgs Parity
symmetry breaking scale

Dark matter direct
detection rate

Mirrored electroweak theory

	SM particles		New particles
quark	q, u, d	strong interaction $SU(3)_c$ g	q', u', d'
lepton	L, e		L', e'
Higgs	H	HP ⟷	H'
gauge bosons	W, Z γ		W', Z' γ'

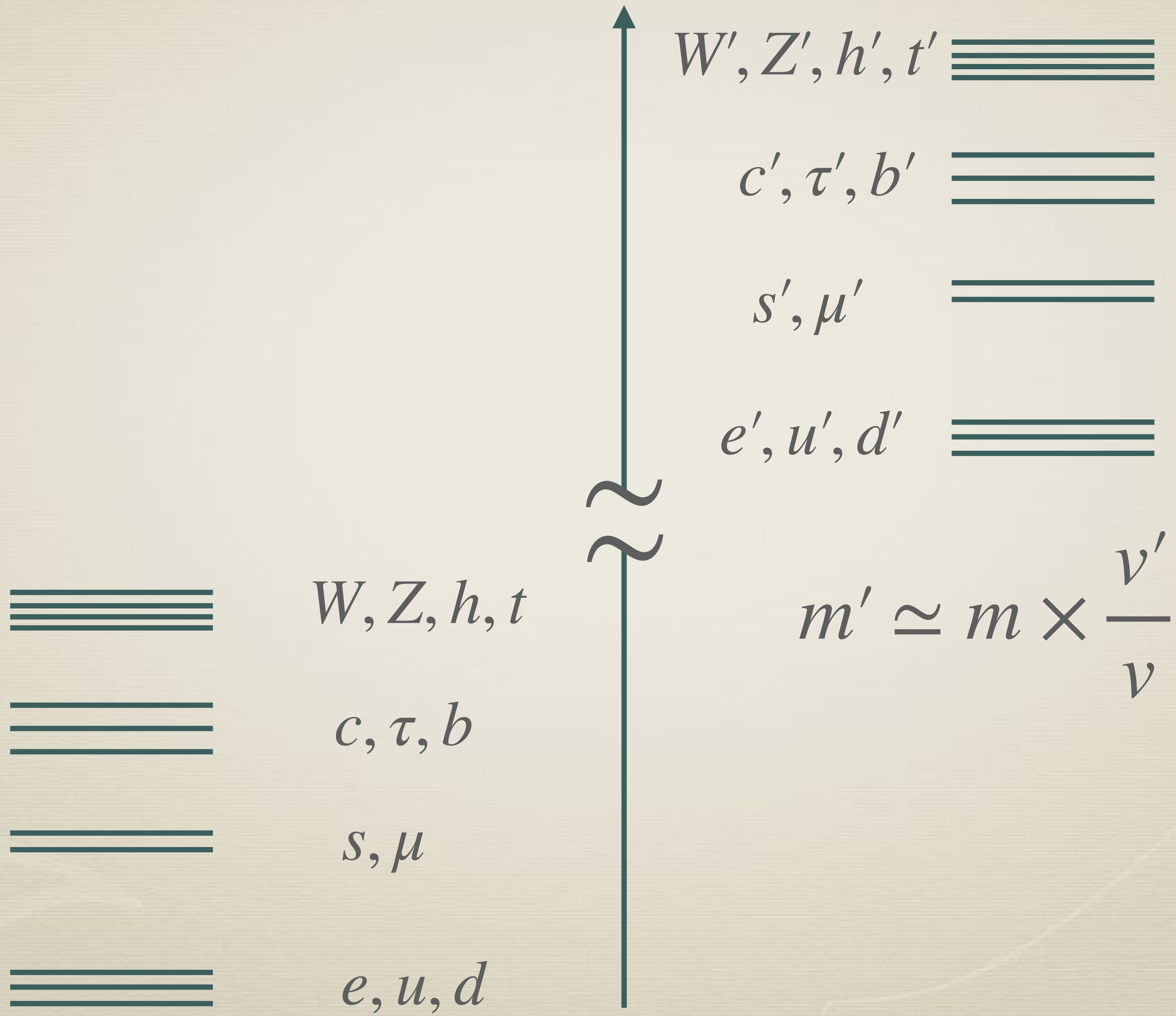
HP with space-time parity forbids solves the strong CP problem

$$\cancel{H = d_n \vec{E} \cdot \vec{S}}$$

Mohapatra and Senjanovic (1978), Beg and Tsao (1978), Babu and Mohapatra (1989), Barr, Chang and Senjanovic (1991) Dunsky, Hall and KH (2019)

(a quick explanation for experts: q and q' have masses with opposite phases)

Mass spectrum



$$m' \simeq m \times \frac{v'}{v}$$

Mirror dark matter

Dunsky, Hall, KH (2019)

New particles

q', u', d'
L', e'
H'

electroweak'

$SU(2)'_L \times U(1)'_Y$ W', Z'

$\downarrow$

$U(1)'_{\mathrm{EM}}$ γ'

The mirror electron and the lightest mirror baryon are stable

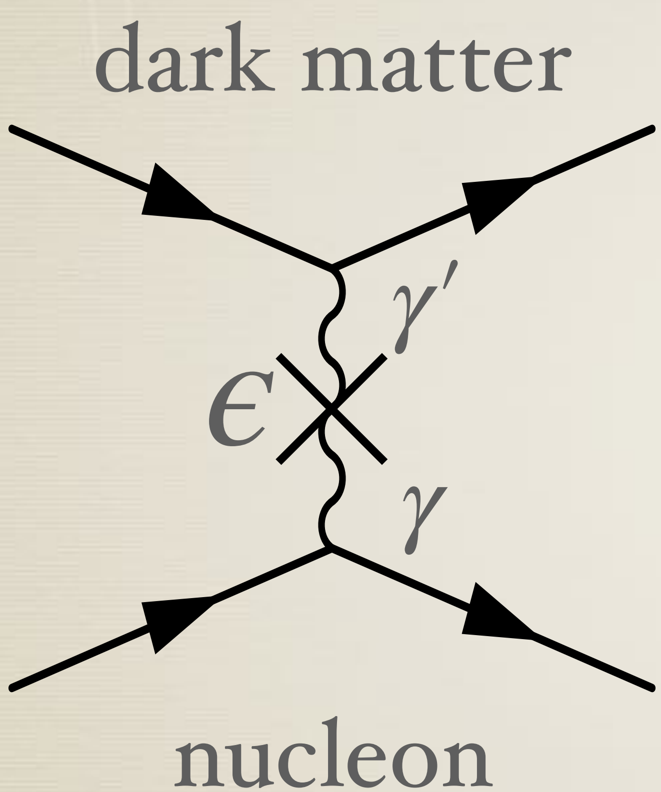
e'

u'
u' u'

I assume that they comprise all of dark matter

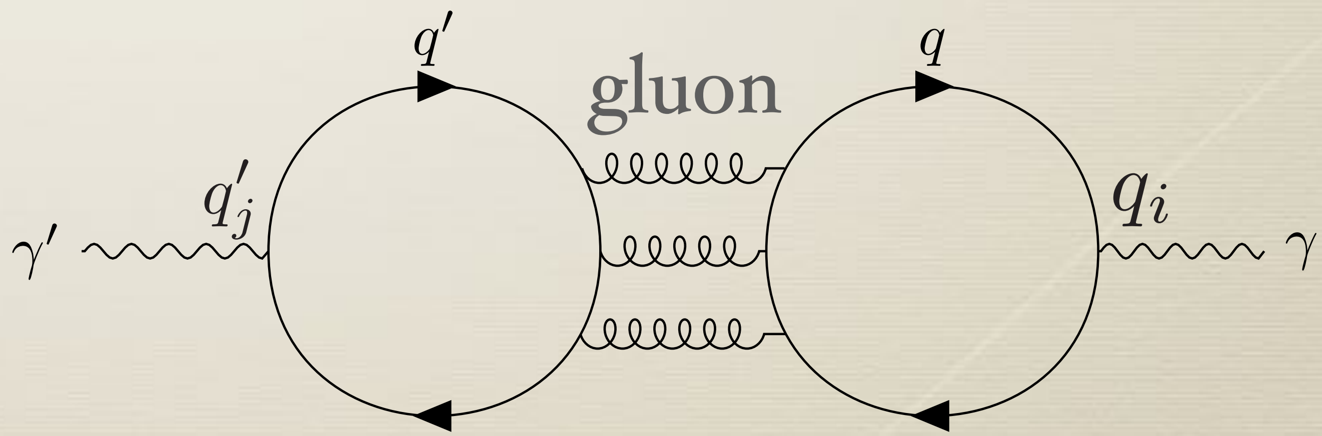
Prediction on interaction

Dunsky, Hall, KH (2019)

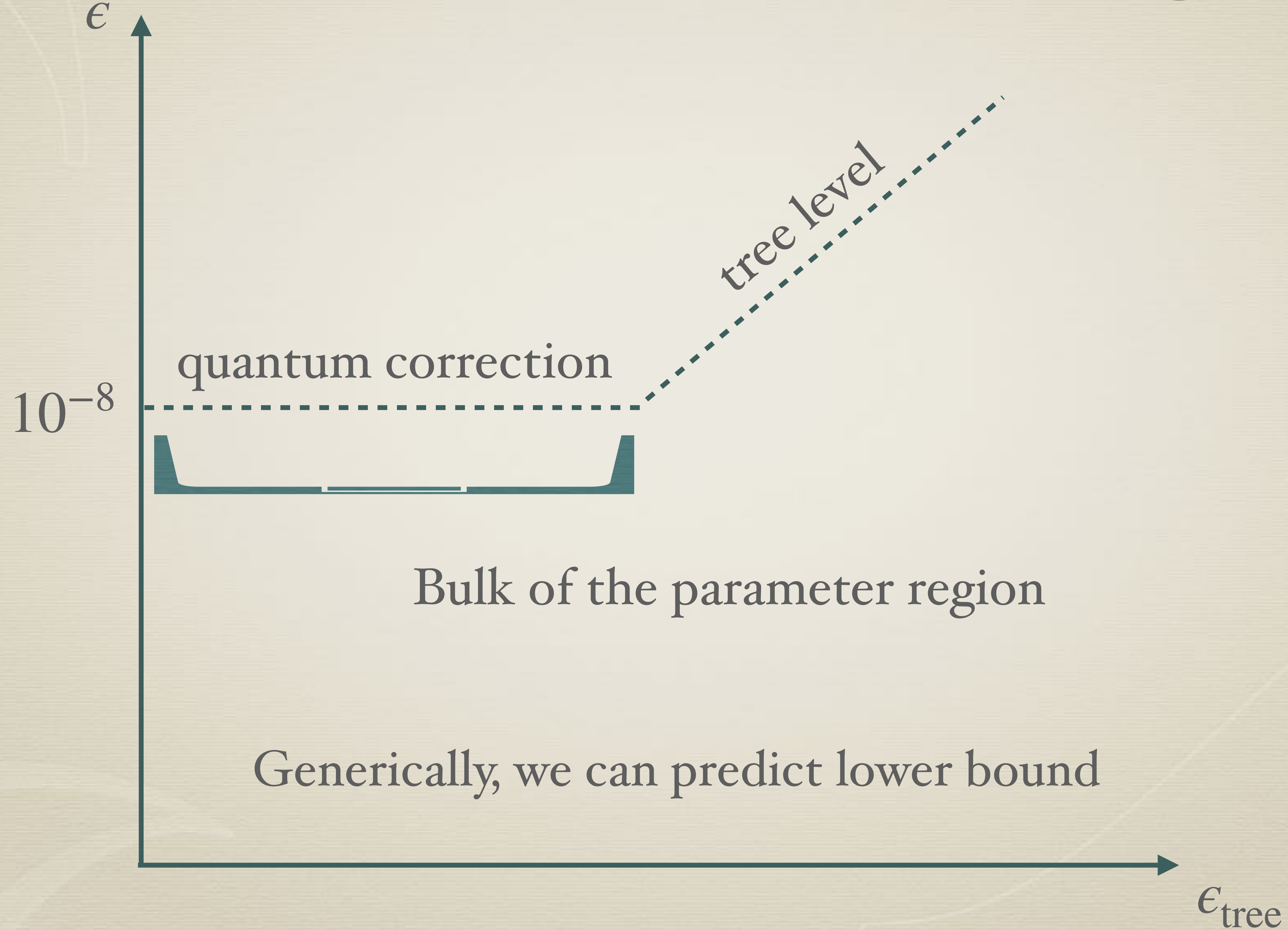


photon-mirror photon mixing

$$\epsilon = \epsilon_{\text{tree}} + \epsilon_{\text{quantum correction}}$$



Prediction on mixing



Composition of DM

e'

u'
$u'\ u'$

$$m_{u'u'u'} \simeq 4m_{e'}$$

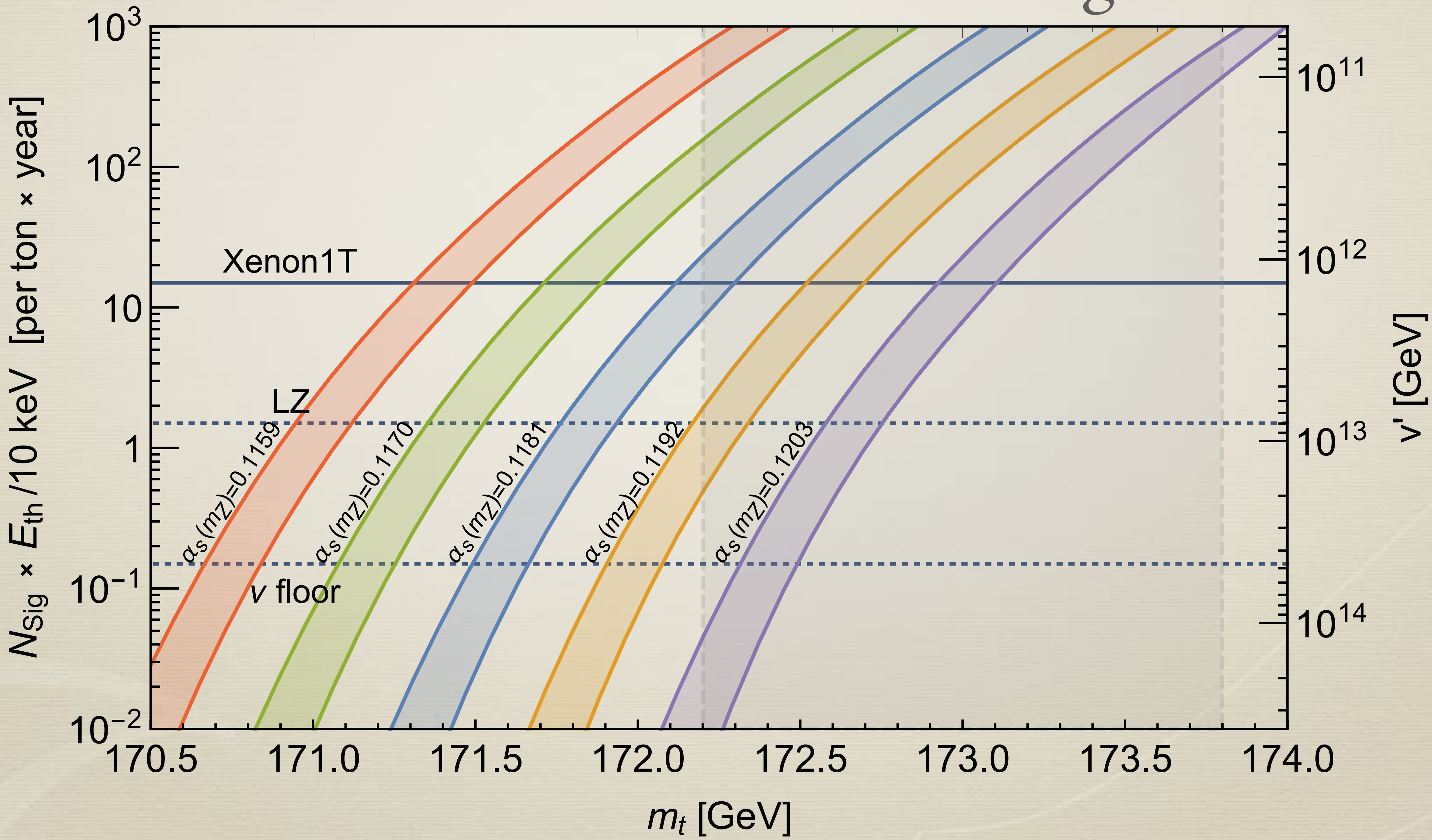
$$Q^2_{u'u'u'} = 2^2 = 4Q^2_{e'}$$

$\Rightarrow$ Signal rates are independent of relative fractions

SM parameters and DM

Dunsky, Hall, KH (2019)

Direct detection rate for Xe targets



SM parameters and DM

Dunsky, Hall, KH (2019)

Direct detection rate for Xe targets