

Tetraquarks and pentaquarks at LHCb

Quinto Incontro Nazionale di Fisica Nucleare INFN 2022

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9 Maggio 2022 Laboratori Nazionali del Gran Sasso

Outline

PENTAQUARKS

Quick excursus on the experimental discoveries of the pentaquark states

Pentaquarks as compact $5q$ states [1]

Pentaquarks as meson-baryon molecular states in a coupled channel approach [2]

Pentaquarks as core+molecular components in a coupled channel approach [3,4]

TETRAQUARKS

Fully heavy quark tetraquark decay widths in the diquark-antidiquark model [5,6] and the fully-charm tetraquark $X(6900)$ discovered by LHCb (Science Bulletin, Volume 65, Issue 23, 1983 (2020))

[1] E. Santopinto, A. Giachino, Phys. Rev. D 96 (2017) 014014

[2] Y. Yamaguchi, E. Santopinto, Phys. Rev. D Phys.Rev. D 96 (2017) no.1, 014018

[3] Y. Yamaguchi, A. Giachino, A. Hosaka, E. S., S. Tacheuchi, M. Takizawa, Phys .Rev. D96 (2017) no.11, 114031

[4] Y. Yamaguchi, H. Garcia-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa Phys.Rev.D 101 (2020) 091502

[5] C.Becchi, A.Giachino, L.Maiani and E.Santopinto, Phys. Lett. B 806, 135495 (2020).

[6] C.Becchi, J. Ferretti, A. Giachino, L.Maiani and E.Santopinto, Phys.Lett. B 811 135952 (2020).

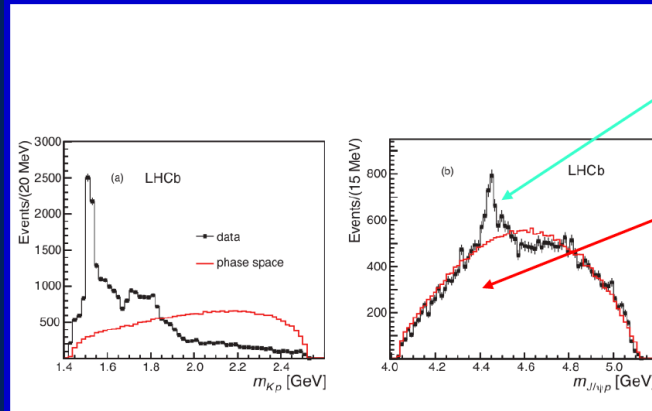
More new valence quark configurations

$$\Lambda_b \rightarrow K^- + J/\psi + P$$

The history of the pentaquark discovery dates back to 2015

LHCb

Phys. Rev. Lett. 115(2015) 072001



$$M_{P_c^+}(4450) = (4449.8 \pm 8 \pm 29) \text{ MeV}$$

$$\Gamma = (39 \pm 5 \pm 19) \text{ MeV}$$

$$M_{P_c^+}(4380) = (4380 \pm 1.7 \pm 2.5) \text{ MeV}$$

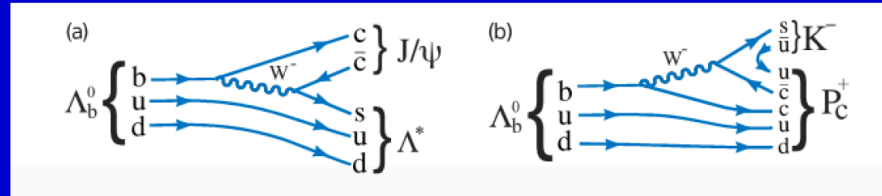
$$\Gamma = (205 \pm 18 \pm 86) \text{ MeV}$$

statistic significance greater than 9 sigma !

$P_c (uudc\bar{c})$

$$\Lambda_b^0 \rightarrow J/\psi + \Lambda^*, \Lambda^* \rightarrow K^- + p$$

$$\Lambda_b^0 \rightarrow P^{0+} + K^-, P^{0+} \rightarrow J/\psi + p$$



The LHCb observation [1] was further supported by another two articles by the same group [2,3]:

[1] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **115** (2015) 072001
 [2] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **117** (2016) no.8, 082002
 [3] R. Aaij *et al.* [LHCb Collaboration], Phys. Rev. Lett. **117** (2016) no.8, 082003

Why pentaquark states?

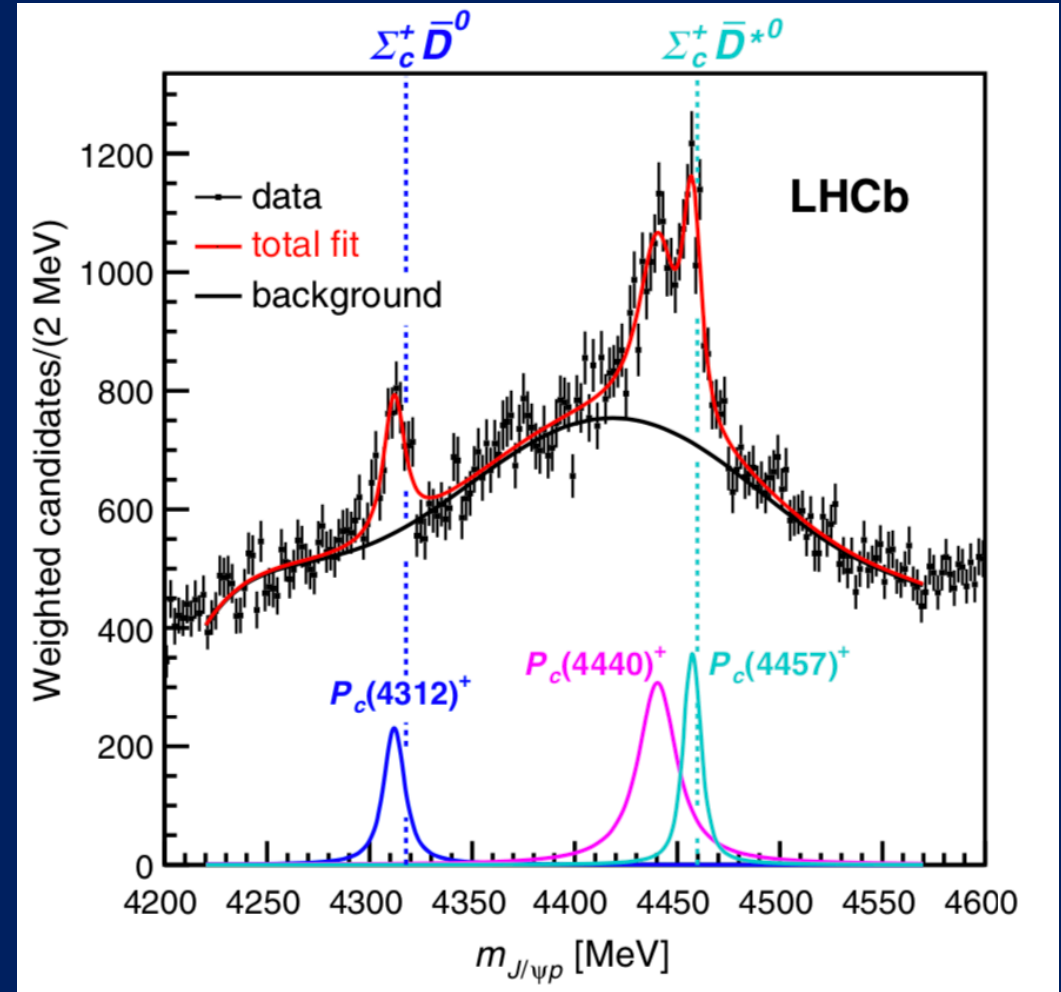
As well as revealing the new $P_c(4312)$ state with 7.3 sigma statistical significance, the LHCb 2019 analysis also uncovered a more complex structure of $P_c(4450)$, consisting of two narrow nearby separate peaks, $P_c(4440)$ and $P_c(4457)$ with the two-peak structure hypothesis having a statistical significance of 5.4 sigma with respect to the single-peak structure hypothesis.

The masses and widths of the three narrow pentaquark states are as follows

State	M [MeV]	Γ [MeV]
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$

[*] R. Aaij et al. (LHCb), Phys. Rev. Lett. 122, 222001 (2019).

$\Lambda_b^0 \rightarrow J/\Psi p K^-$ channel ($P_c \rightarrow J/\Psi p$)



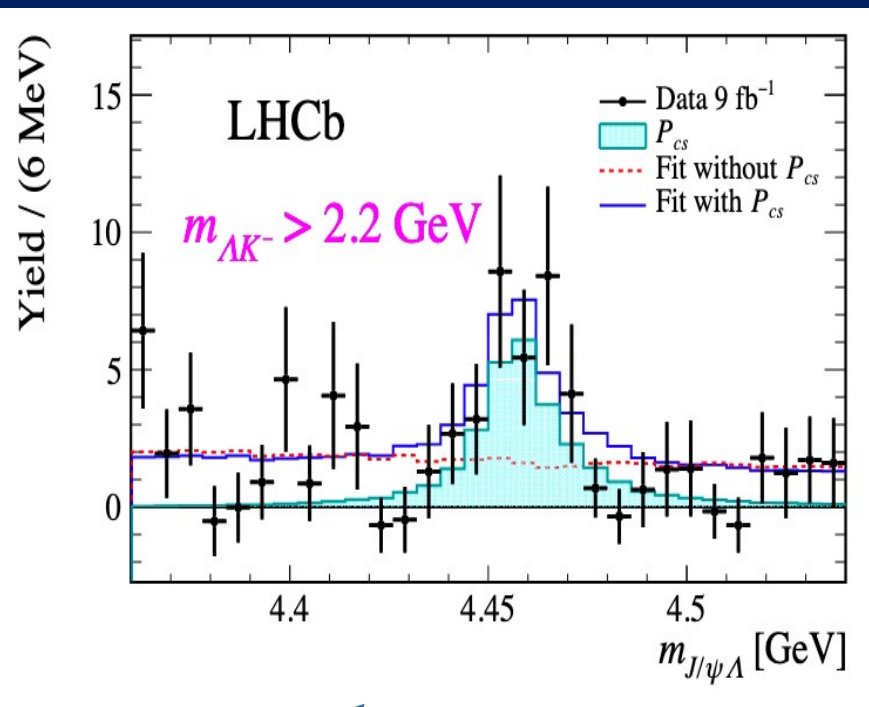
Number of events versus J/Psi p invariant mass [*]. The mass thresholds for the $\Sigma_c \bar{D}$ and $\Sigma_c \bar{D}^*$ final states are superimposed.

2021

P_{cs} ($uds\bar{c}\bar{c}$)

(2021) LHCb, *Sci.Bull.* 66 (2021) 1278-1287

$\Lambda_b^0 \rightarrow J/\Psi \Lambda K^-$ channel ($P_{cs} \rightarrow J/\Psi \Lambda$)

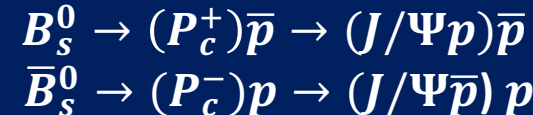


Significance of $P_{cs}^0(4459)$ exceeds 3σ after considering all the systematic uncertainties.

August 2021

Evidence for a new structure in the $J/\psi p$ and $J/\psi \bar{p}$ systems in $B_s^0 \rightarrow J/\psi p \bar{p}$ decays

arXiv:2108.04720v1 [hep-ex] 10 Aug 2021



The $P_c(4437)$ statistical significance is in the range of 3.1 to 3.7 depending on the assigned J^P hypothesis:

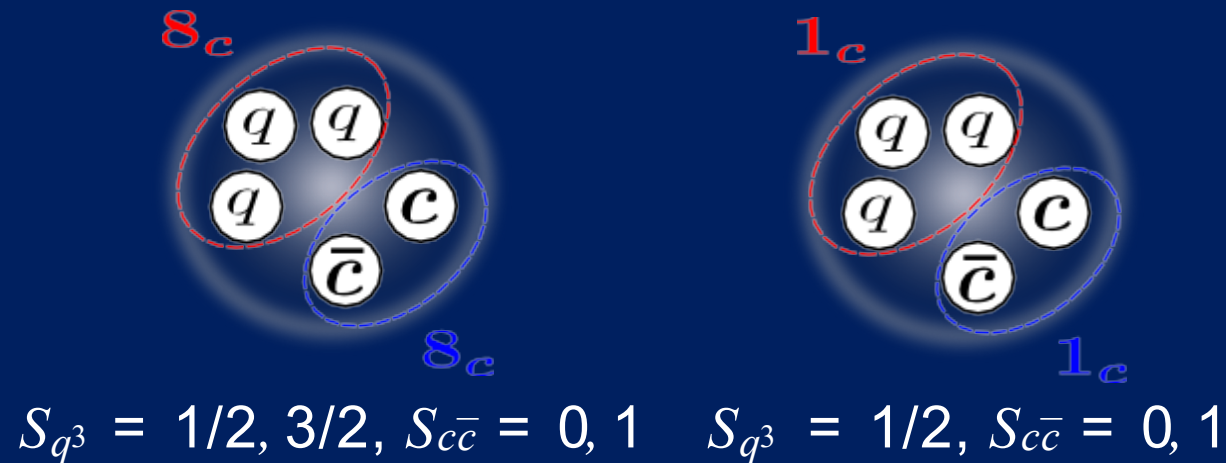
3.1 sigma for $J^P = \frac{1}{2}^+$

3.7 sigma for $J^P = \frac{3}{2}^+$

Mass of $P_{cs}(4459)^0$ 19 MeV below the $\Xi_c^0 \bar{D}^{*0}$ threshold, similar to $P_c(4440)^+$ and $P_c(4457)^+$ pentaquark states.

Pentaquark as compact $5q$ states

- ▶ E. Santopinto, A. Giachino, **Phys. Rev. D96** (2017) 014014.
 P_c states by an algebraic model
- ▶ 5-quark configurations



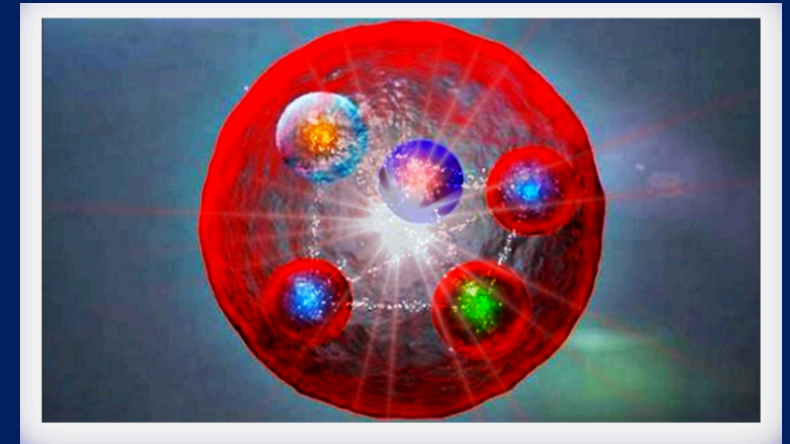
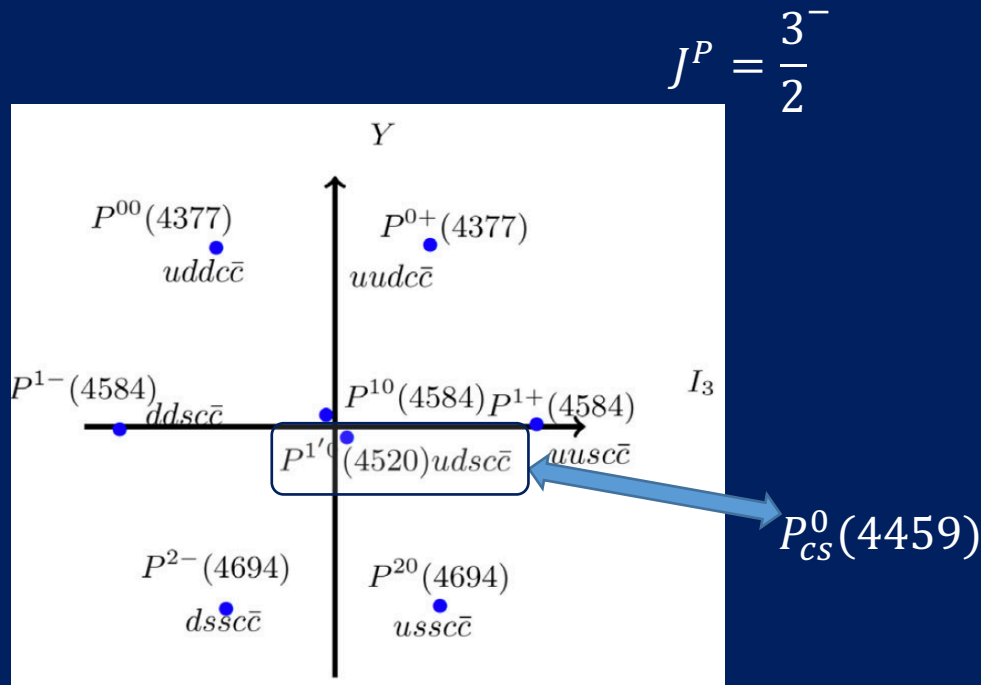
Using only symmetry considerations, and an equal spaced mass formula, we have predicted $P_{cs}(4459)$ 3 years in advance and suggested to look for it in the $\Lambda J/\Psi$ channel. According to our model also $I=1$ P_{cs} should exist (in the $\Sigma J/\Psi$ channel) and $I=1/2$ P_{css} (in $\Xi J/\Psi$ channel)

The discovery paper by LHCb cited our paper

Cited also by PDG2021 (update)!

Pentaquark as compact $5q$ states

We have predicted the strange pentaquark with $I=0$, P_{CS}^0 , for which LHCb reported evidence at $M=4459$ MeV and suggested to look for it in the $\Lambda J/\Psi$ channel. According to our model also $I=1$ P_{CS} should exist (in the $\Sigma J/\Psi$ channel) and $I=1/2$ P_{CSS} (in $\Xi J/\Psi$ channel).



The LHCb Coll. [LHCb, *Sci.Bull.* 66 \(2021\) 1278-1287](#),

Evidence of a $J/\Psi\Lambda$ structure and observation of excited Ξ^- states in the $\Xi_b^- \rightarrow J/\Psi\Lambda K^-$ decay

from E. Santopinto and A. Giachino, [Phys. Rev. D96 \(2017\) 014014](#).

Hidden-charm pentaquarks as a meson-baryon molecule with coupled channels
for $\bar{D}^{(*)}\Lambda_c$ and $\bar{D}^{(*)}\Sigma_c^{(*)}$

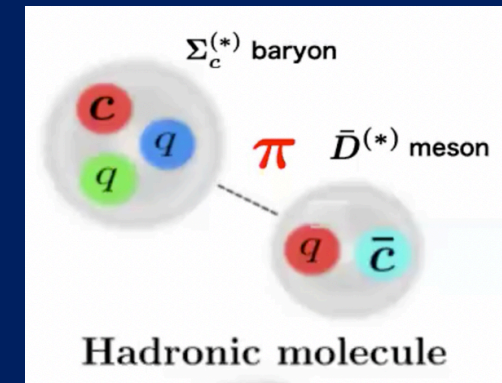
Y. Yamaguchi, E. Santopinto, Phys. Rev. D 96 (2017) no.1, 014018

This description is motivated by the fact that the observed pentaquarks are found to be just below the $\Sigma_c\bar{D}$ threshold ($P_c(4312)$), $\Sigma_c^*\bar{D}$ ($P_c(4380)$) and $\Sigma_c\bar{D}^*$ ($P_c(4440)$ and $P_c(4457)$)

Near the threshold, resonances are expected to have an exotic structure, like the hadronic molecules



In Phys.Rev. D96 (2017) no.1, 014018 E. Santopinto e Y. Yamaguchi considered the coupled channel systems of $\bar{D}\Lambda_c$, $\bar{D}^*\Lambda_c$, $\bar{D}\Sigma_c$, $\bar{D}\Sigma_c^*$, $\bar{D}^*\Sigma_c$ and $\bar{D}^*\Sigma_c^*$ to predict the bound and the resonant states in the hidden-charm sector. **The binding interaction between the meson and the baryon is given by the One Meson Exchange Potential (OMEP).**



This was the first calculation in which a full coupled channel has been performed

**Upgrade of the model:
Coupled channel between the
meson-baryon states and the five
quark states**

- ▶ In the current problem of pentaquark P_c , there are two competing sets of channels: the meson-baryon (MB) channels and the five-quark channels.

**CAN A COUPLE CHANNEL BETWEEN
THE MB CHANNELS AND THE CORE CONTRIBUTION
DESCRIBE IN A MORE REALISTIC WAY THE PENTAQUARK STATES ?**

Coupled channel between the meson-baryon states and the five quark states

Hidden-charm and bottom meson-baryon molecules coupled with five-quark states, Y. Yamaguchi, A. Giachino, A. Hosaka, E. S., S. Tacheuchi, M. Takizawa, Phys .Rev. D96 (2017) no.11, 114031

- ▶ Hidden-charm pentaquarks as $\bar{D} \Lambda_c, \bar{D}^* \Lambda_c, \bar{D} \Sigma_c, \bar{D}^* \Sigma_c, \bar{D} \Sigma_c^*,$ and $\bar{D}^* \Sigma_c^*$, and molecules coupled to the five-quark states



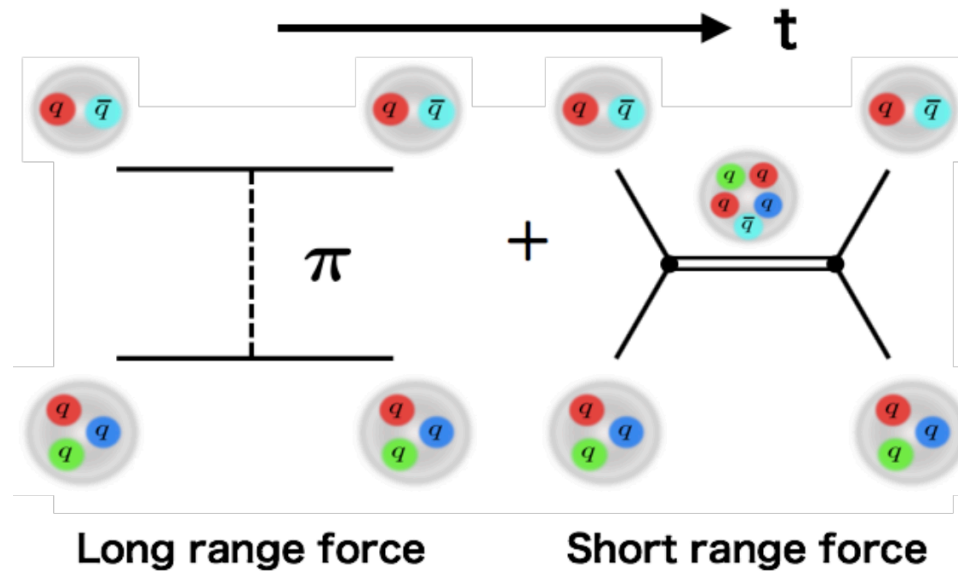
ADDITION OF THE CORE CONTRIBUTION

- ▶ For the first time some predictions for the hidden charm pentaquarks as $\bar{D} \Lambda_c, \bar{D}^* \Lambda_c, \bar{D} \Sigma_c, \bar{D}^* \Sigma_c, \bar{D} \Sigma_c^*$ and $\bar{D}^* \Sigma_c^*$ molecules coupled to the five-quark states are provided.
- ▶ In particular, by solving the coupled channel Schrödinger equation, we study the the bound and resonant hidden-charm

Model setup in this study

- ▶ **Hadronic molecule + Compact state ($5q$)**
⇒ Meson-Baryon couples to $5q$ (Fashbach projection)

Meson-Baryon interactions



- ▶ **Long range** interaction: One pion exchange potential (OPEP)
- ▶ **Short range** interaction: $5q$ potential

Hidden-charm and bottom meson-baryon molecules coupled with five-quark states [3]

- In Refs. [3] we studied the hidden-charm pentaquarks by coupling the $\Lambda_c \bar{D}^{(*)}$ and $\Sigma_c^* \bar{D}^{(*)}$ meson-baryon channels to a $uudc\bar{c}$ compact core with a meson-baryon binding interaction satisfying the heavy quark and chiral symmetries.

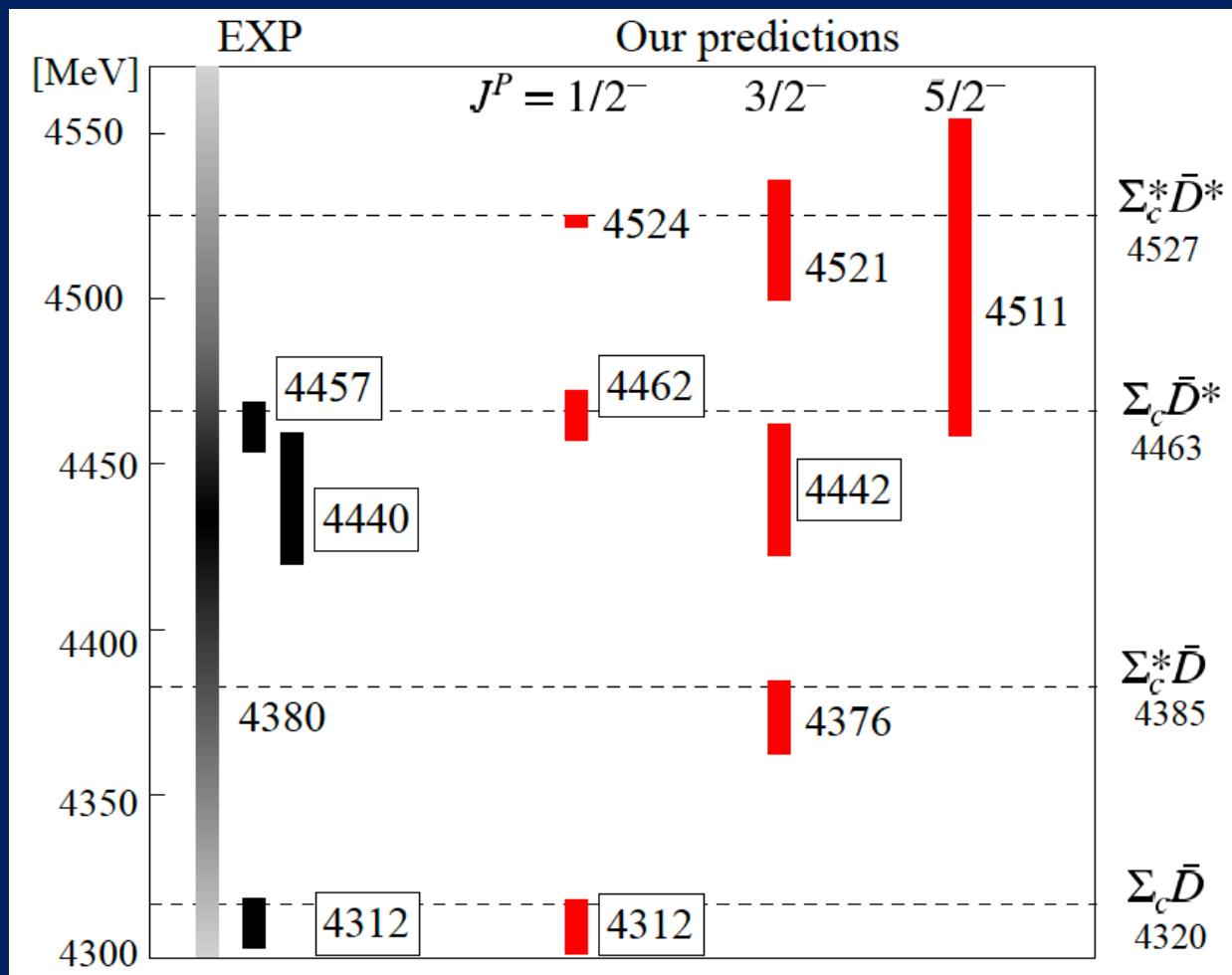
We predicted the three pentaquark states, $P_c(4312)$, $P_c(4440)$ and $P_c(4457)$ two years before the experimental observation by LHCb.

For this reason we wrote a Rapid Communication, Y. Yamaguchi, H. Garcia-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa Phys.Rev.D **101** (2020) 091502 (R)

[3] Y. Yamaguchi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, Phys. Rev. D **96** 114031 (2017)

results

Y. Yamaguchi, H. Garcia-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi and M. Takizawa Phys.Rev.D **101** (2020) 091502 (R)



Cited by PDG2020! Together with Y. Yamaguchi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, PRD **96** (2017) 114031.

Four-Heavy-Quark Tetraquarks

Observation claims of a 4μ on peak in 2Υ spectrum circulated in 2018-2019

- A Genova-Roma collaboration set up to compute lifetime & branching ratios for fully bottom 0^{++} tetraquark, also in view of the luminosity upgrade of LHCb;
- we also included the 2^{++} state (2^{++} has a production cross-section a factor 5 larger than 0^{++} and a larger 4μ Bf !)

C.Becchi, A.Giachino, L.Maiani and E.Santopinto, Phys. Lett. **B 806**, 135495 (2020).

• Very discouraging results were obtained for the 4μ on channel of $4b$ tetraquarks: $\sigma \sim 0.1\text{fb}$ or less, made the positive claims rather unlikely.

- In March 2020, we realised that fully charmed tetraquarks would be more favorable.
- Our paper on fully charmed tetraquarks appeared on ArXiv on June 25.

C.Becchi, J. Ferretti, A. Giachino, L.Maiani and E.Santopinto, arXiv:2006.14388, Phys.Lett. **B 811** (2020) 135952

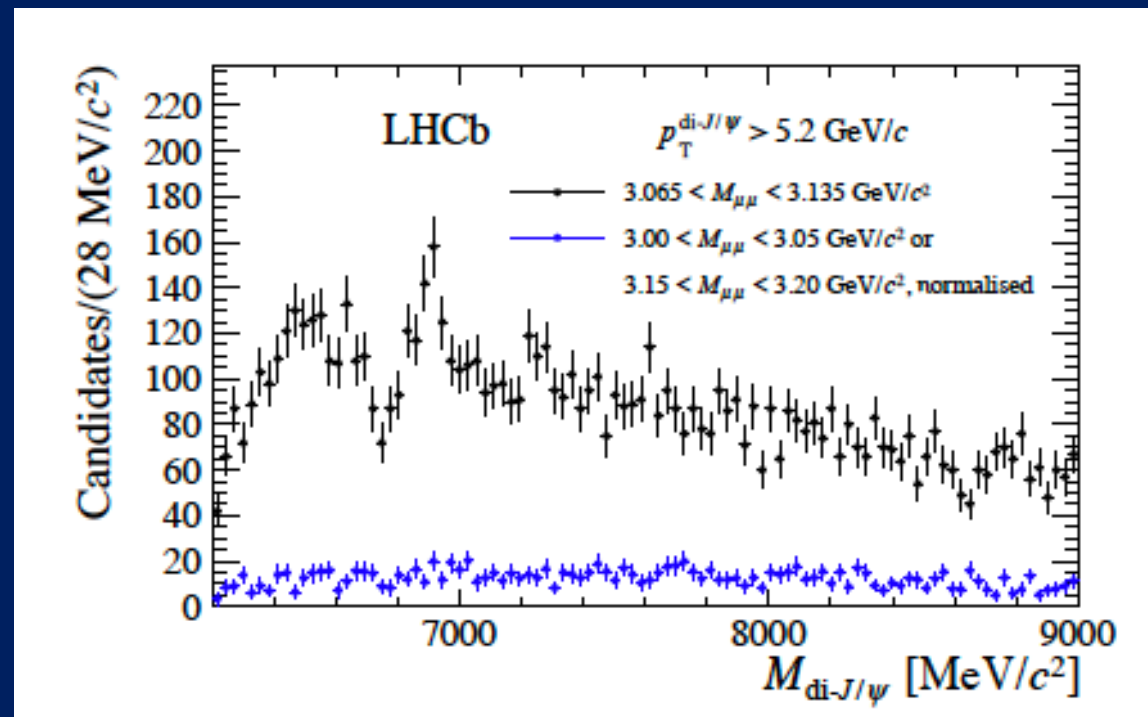
Tetraquark picture of 2 J/Ψ resonances

Describing the X(6900) structure with a Breit Wigner lineshape, its mass and natural width are determined to be ([arXiv:2006.16957](https://arxiv.org/abs/2006.16957), 30 Jun 2020, now Science Bulletin, Volume 65, Issue 23, 1983 (2020)):

$$m[X(6900)] = 6905 \pm 11 \pm 7 \text{ MeV}/c^2$$

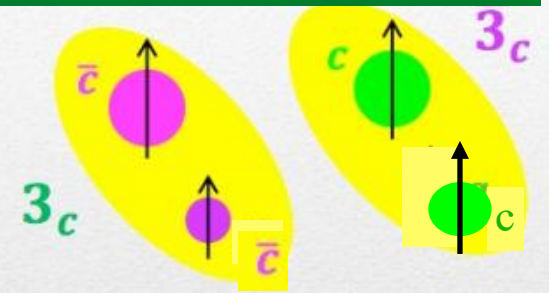
$$\Gamma[X(6900)] = 80 \pm 19 \pm 33 \text{ MeV},$$

The statistical significance of X(6900) is greater than 5.1σ



Tetraquark constituent picture of 2 J/Ψ resonances

$$[cc]_{(S=1)}[c^-c^-]_{(S=1)}$$



- [cc] in color $\mathbf{3}$
- total spin of each diquark, $S=1$ (color antisymmetry and Fermi statistics)
- S-wave: positive parity

S-wave, fully charm tetraquarks

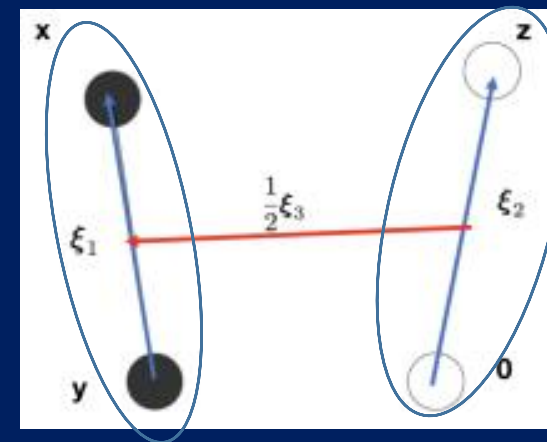
- $C=+1$ states: $J^{PC} = 0^{++}, 2^{++}$, decay in 2 J/Ψ, S-wave
- $C=-1$ states: $J^{PC} = 1^{+-}$, no decay in 2 J/Ψ, S-wave

• masses computed as diquark antidiquark system by Bedolla, Ferretti, Roberts, Santopinto, arXiv:1911.00960, Eur.Phys.J.C80(2020)1004 with an an Hamiltonian introduced in Anwar, Ferretti and Santopinto, PRD 98, 094015 (2018)

$$H = E_0 + \sqrt{q^2 + m_D^2} + \sqrt{q^2 + m_{\bar{D}}^2} + V_{conf} + V_{OGE}$$

- QCD inspired potential (Coulomb+linear potential), h.o. variational method, the diquarks are treated as frozen.
- Authors include computation of the energy levels of radial and orbital excitations.

Jacobi coordinates in the tetraquark



Hamiltonian contains OGE + confining potential. Parameters fitted to XYZ tetra-quark candidate

Decays and branching fractions

- Decays take place via $c\bar{c}$ annihilation. The starting point is to bring the $c\bar{c}$ pairs together

$$\mathcal{F}(J=0^{++}) = \left| \left((cc)_{\bar{3}}^1 (\bar{c}\bar{c})_3^1 \right)_1^0 \right|^2 = -\frac{1}{2} \left(\sqrt{\frac{1}{3}} \left| (c\bar{c})_1^1 (c\bar{c})_1^1 \right>_1^0 - \sqrt{\frac{2}{3}} \left| (c\bar{c})_8^1 (c\bar{c})_8^1 \right>_1^0 \right) + \frac{\sqrt{3}}{2} \left(\sqrt{\frac{1}{3}} \left| (c\bar{c})_1^0 (c\bar{c})_1^0 \right>_1^0 - \sqrt{\frac{2}{3}} \left| (c\bar{c})_8^0 (c\bar{c})_8^0 \right>_1^0 \right)$$

- Four possible annihilations:

- 1 a color singlet pair of spin 1 (0) annihilates into a J/Ψ (η_c), the other pair rearranges into the available states (near threshold: J/Ψ or η_c again);
- 2 a color octet, spin 1 pair annihilates into a pair of light quark flavours, $q=u,d,s$ and the latter recombine with the spectator pair to produce a pair of lower-lying, open-charm mesons. A similar process from color octet spin 0 pair is higher order in α_s and neglected.

- Rates are computed with the formula (well known in atomic physics):

$$\bullet \Gamma = |\Psi_T(0)|^2 \cdot |\mathbf{v}| \cdot \sigma(cc^- \rightarrow f)$$

- Branching fractions are independent from $|\Psi_T(0)|^2$
- Total rates: see later.

2J/Ψ and 4μ cross sections

- We give the upper bound: $\sigma_{theo.}(\mathcal{T} \rightarrow 4\mu) \leq \sigma(pp \rightarrow 2 J/\Psi)[B(J/\Psi \rightarrow 2 \mu)]^2$
- With: $\sigma(pp \rightarrow 2 J/\Psi) \simeq 15.2 \text{ nb}$ (LHCb @ 13 TeV, Aaij : 2016bqq)

The limiting cross sections (in fb) are shown in the table

[cc][c̄c̄]	Decay channel	BF in \mathcal{T} decay	Cross section upper limit (fb)
$J = 0^{++}$	$\mathcal{T} \rightarrow D^{(*)+} D^{(*)-} \rightarrow e + \mu + \dots$	$2.3 \cdot 10^{-3}$	$3.6 \cdot 10^4$ (36 pb)
	$\mathcal{T} \rightarrow D^{(*)0} \bar{D}^{(*)0} \rightarrow e + \mu + \dots$	$0.36 \cdot 10^{-3}$	$0.55 \cdot 10^4$ (6 pb)
	$\mathcal{T} \rightarrow 4\mu$	$2.6 \cdot 10^{-6}$	39
$J = 2^{++}$	$\mathcal{T} \rightarrow D^{*+} \bar{D}^{*-} \rightarrow e + \mu + \dots$	$7.0 \cdot 10^{-3}$	$53 \cdot 10^4$ (532 pb)
	$\mathcal{T} \rightarrow D^{*0} \bar{D}^{*0} \rightarrow e + \mu + \dots$	$1.1 \cdot 10^{-3}$	$8.3 \cdot 10^4$ (83 pb)
	$\mathcal{T} \rightarrow 4\mu$	$1.0 \cdot 10^{-5}$	780

780:39=20 !!

$$B_{4\mu}(2^{++}) : B_{4\mu}(0^{++}) \sim 4:1; \quad \sigma(2^{++}) : \sigma(0^{++}) = 5 : 1$$

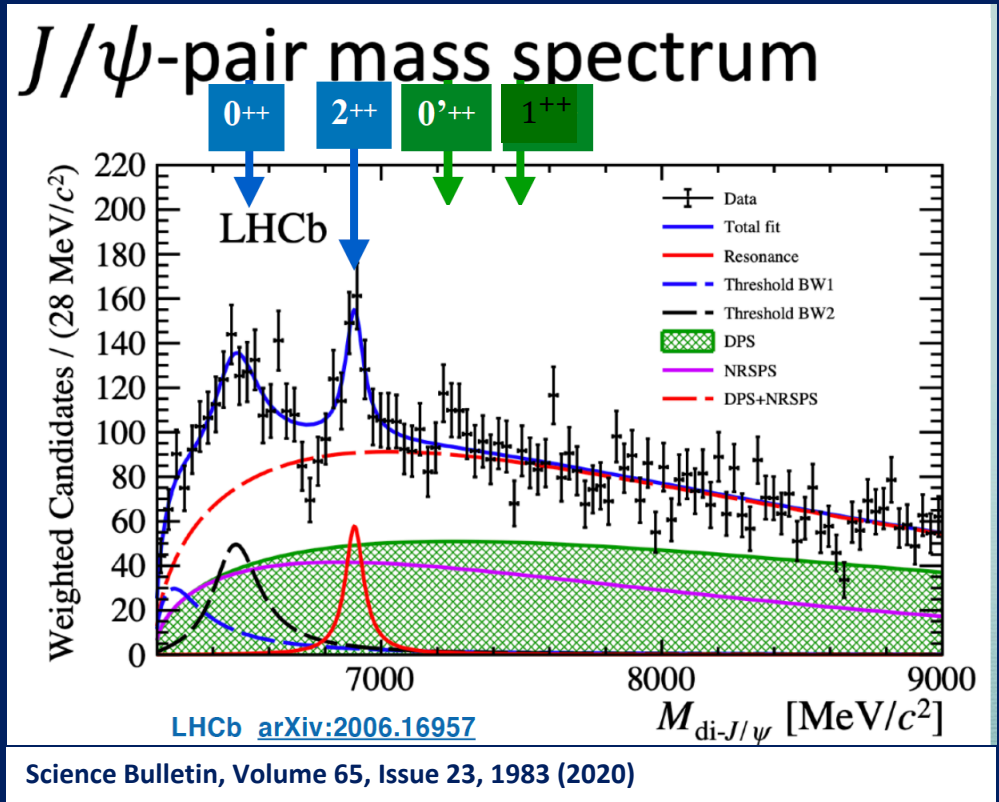
A visibility ratio 20:1 !!

- Branching ratios in 4 muons are more favorable in 4 c than in 4 b tetraquarks
- Among 4 c, the Branching Ratio is more favorable for the 2^{++} (a factor 4)
- In addition 2^{++} is produced in pp collision with a statistical factor $2J+1=5$

Total widths and mass spectrum

- Total widths are proportional to the ratio: $\xi = |\Psi_T(0)|^2 / |\Psi_{J/\psi}(0)|^2$
- we determine ξ from models

$$\xi = 4.6 \pm 1.4$$
$$\Gamma(2^{++}) = (97 \pm 30) \text{ MeV}$$



C.Becchi, J. Ferretti, A.Giachino, L.Maiani and E.Santopinto,
arXiv:2006.14388, Phys.Lett. **B 811** (2020) 135952

Conclusions:

The field of exotic is a hot topic - new discoveries each two-three months

One of my article has predicted the P_{cs} pentaquark before the LHCb observation and in fact it has been cited by LHCb

The same for the fully charm tetraquark: we predicted the fully-charm tetraquark before its experimental discovery

Three of my articles have been cited by the Particle Data Group (PDG2021 update)

**Thanks for your
attention!**

