

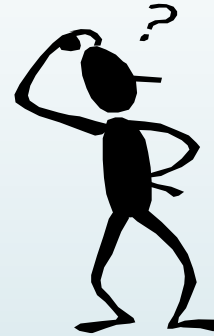
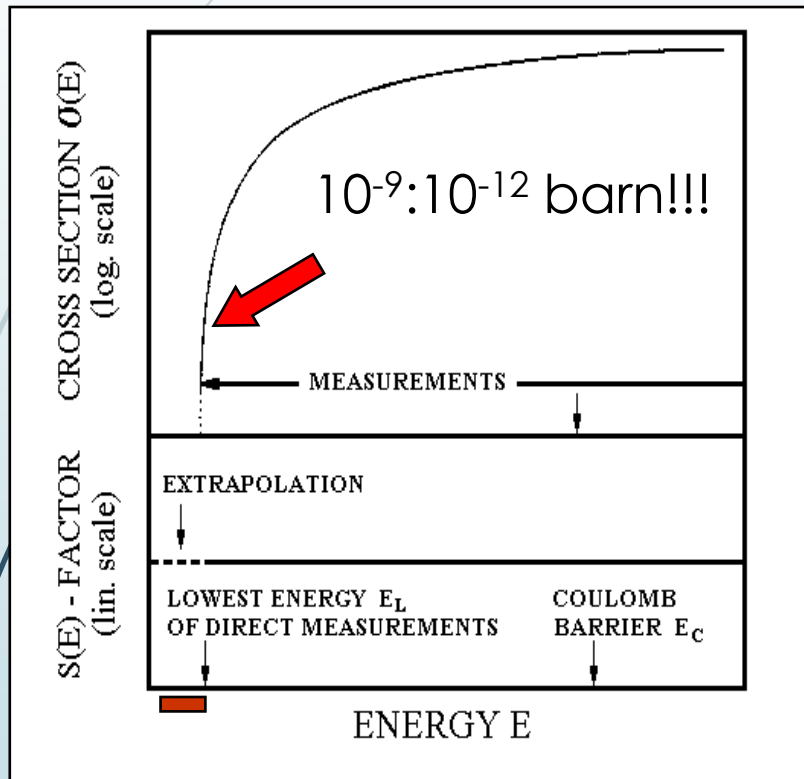
Shedding light on $^{17}\text{O}(n,\alpha)^{14}\text{C}$ reaction at astrophysical energies with Trojan Horse Method and Asymptotic Normalization Coefficient



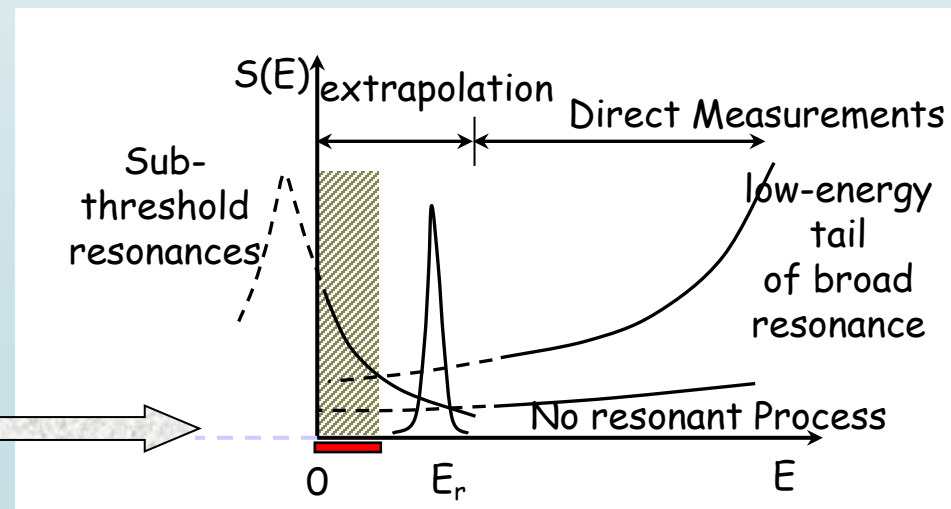
Giovanni Luca Guardo
on behalf of the AsFiN group



Direct measurement in nuclear astrophysics



- Very small cross section values reflect in a faint statistic;
- Very low signal-to-noise ratio makes hard the investigation at astrophysical energies;
- Instead of the cross section, the S(E)-factor is introduced



$$S(E) = E\sigma(E)\exp(2\pi\eta)$$



Neutron induced reactions in nuclear astrophysics

- No accelerator (no charge)
- No target available (half-life 885.7 ± 0.8 sec)

NEUTRON BEAM FACILITY

- ${}^9\text{Be}$ photodissociation or a absorption
 - *Monoenergetic spectra*
- Nuclear reactors
- (γ, n) reactions (bremsstrahlung)
- (p, n) reactions
 - *Energy distributions → TAGGING (ToF, angles,...)*

INVERSE REACTIONS

- Low detection efficiency (<30%)



Indirect methods in nuclear astrophysics

Beyond the extrapolation procedure, **indirect methods** are highly demanded to address missing or incomplete aspects led by the complexity of nuclear reactions in stars



$^{17}\text{O}(n,\alpha)^{14}\text{C}$ reaction: a case study



Astrophysical Scenario

Weak component s-process

$^{17}\text{O}(n,\alpha)^{14}\text{C}$ and $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$ since they act as a neutron poison and a recycle channel during s-process nucleosynthesis in massive stars ($M > 8M_{\text{SUN}}$)



Astrophysical Scenario

Weak component s-process

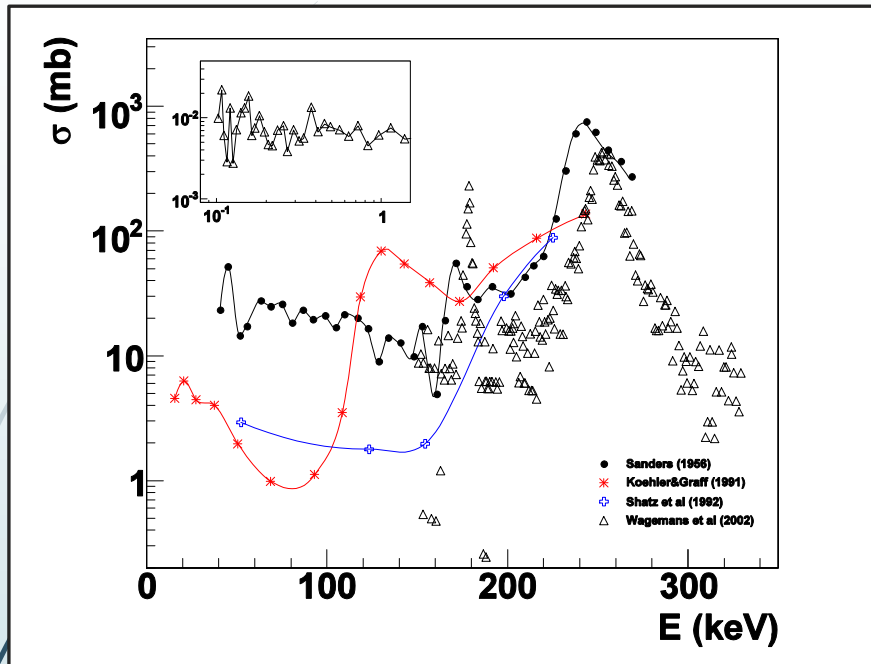
$^{17}\text{O}(n,\alpha)^{14}\text{C}$ and $^{17}\text{O}(\alpha,n)^{20}\text{Ne}$ since they act as a neutron poison and a recycle channel during s-process nucleosynthesis in massive stars ($M > 8M_{\text{SUN}}$)



Temperature $\rightarrow 0.8 < T_8 < 11$ K
Energy range $\rightarrow \sim 0\text{-}100$ keV



Status of the art



• R. M. Sanders, Phys. Rev., 104, 1434 (1956)
 INVERSE REACTION $^{14}\text{C}(\alpha,n)^{17}\text{O}$

* P.E.Koehler & S.M.Graff, Phys. Rev., C44(6),
 2788 (1991)

○ H. Schatz et al., Astroph. J., 413, 750
 (1993)

△ J. Wagemans et al., Phys. Rev., C65(3),
 34614 (2002)

Subthreshold Level
 Suppressed due to the centrifugal
 barrier
 Available in literature

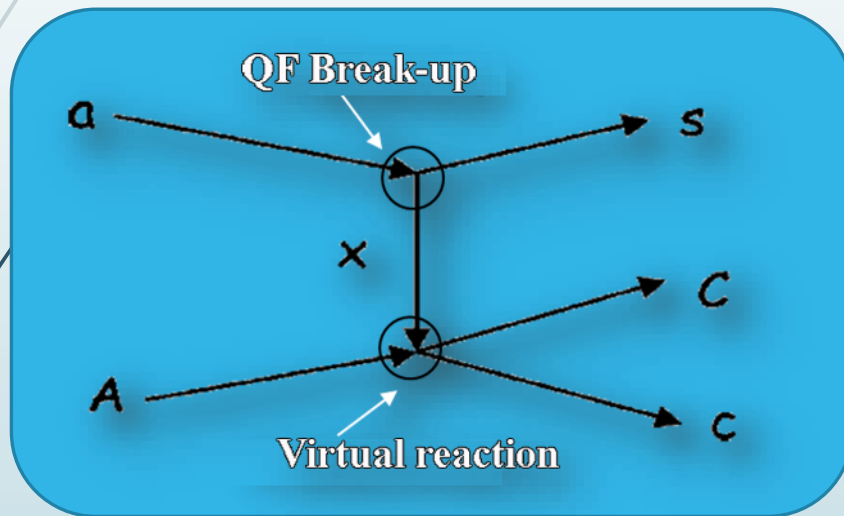
| $E_{c.m.}$ (keV) | $^{18}\text{O}^*$ (MeV) | J^π |
|---------------------|----------------------------|---------|
| -7 | 8.039 | 1^- |
| 75 | 8.125 | 5^- |
| 166 | 8.213 | 2^+ |
| 236 | 8.282 | 3^- |



The Trojan Horse Method



The idea of the **THM** is to extract the cross section of an astrophysically relevant two-body reaction $A+x \rightarrow c+C$ at low energies from a suitable three-body reaction $a+A \rightarrow c+C+s$



Quasi free kinematics is selected

- ✓ only $x - A$ interaction
- ✓ $s = \text{spectator}$ ($p_s \sim 0$)

$$E_A > E_{\text{Coul}} \rightarrow$$

- NO coulomb suppression
- NO electron screening
- NO centrifugal barrier

- THM Review papers \rightarrow Spitaleri C. et al., PAN, 2011
Tribble R. et al., Rep. Prog. Phys. 2014
Spitaleri C. et al., EpJ A, 2019



Theoretical approach

The TH-nucleus is chosen because of:

- its large amplitude in the $\alpha=x\oplus s$ cluster configuration;
- its relatively low-binding energy;
- Its known x-s momentum distribution $|\Phi(p_s)|^2$ in α .

$$E_{Ax} = \frac{m_x}{m_x + m_A} E_A - B_{xs}$$

B_{x-s} plays a key role in compensating for the beam energy thanks to the *x-s intercluster motion* inside α , it is possible to span an energy range of several hundreds of keV with only one beam energy

In the Plane Wave Impulse Approximation (PWIA) the cross section of the three body reaction can be factorized as:

Three body measured cross section

$$\frac{d^3\sigma}{d\Omega_c d\Omega_C dE_c} \propto KF \cdot |\Phi(p_s)|^2 \cdot \frac{d\sigma_{Ax}}{d\Omega}$$

Calculated kinematical factor

Fourier transform for the x-s intercluster motion

Astrophysically relevant two body cross section



THM resonant cross section

Virtual nature of x particle → A+x interaction is off-energy shell

Cross section of the bare nucleus but NO absolute value → normalization to direct data available at higher energies

Standard R-Matrix approach cannot be applied to extract the resonance parameters → Modified R-Matrix is introduced instead

$$\frac{d^2\sigma}{dE_{xA}d\Omega_s} = NF \sum_i (2J_i + 1) \times \left| \frac{\sqrt{\frac{k_f(E_{xA})}{\mu_{cC}}} \sqrt{2P_i(k_{cC}R_{cC})} M_i(p_{xA}R_{xA}) \gamma_{cC}^i \gamma_{xA}^i}{D_i(E_{xA})} \right|^2$$

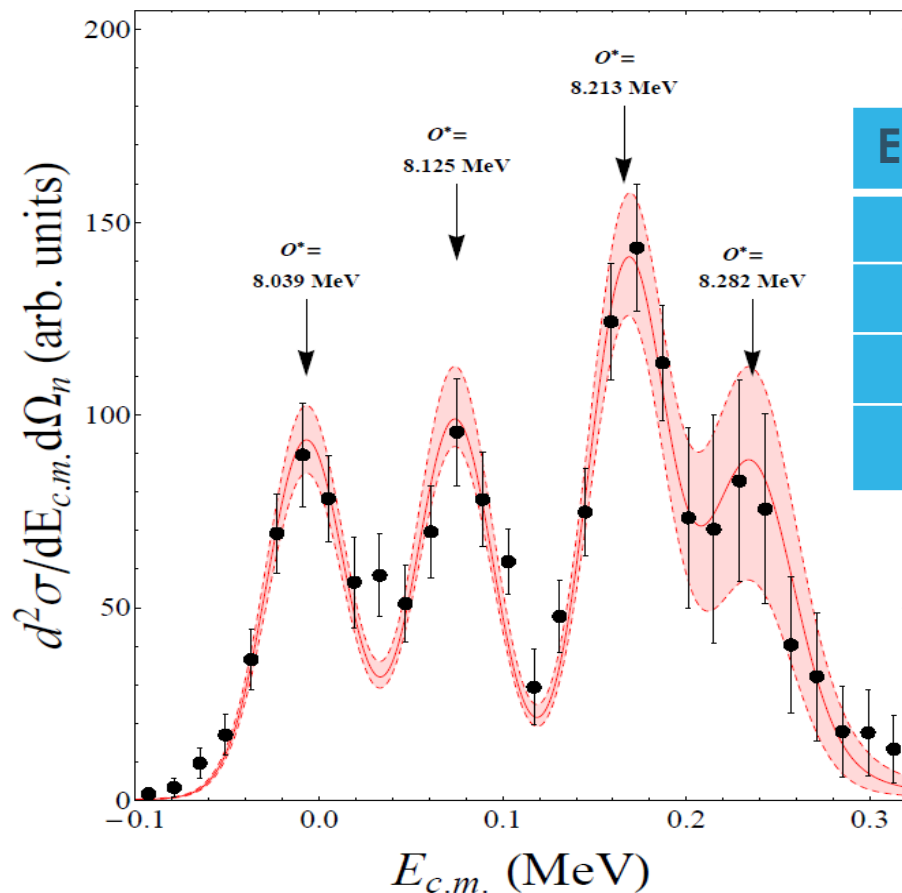
where:

- $M_i(p_{xA}R_{xA})$ describes the transfer amplitude for the QF-process;
- γ_{xA} and γ_{cC} represents the reduced partial widths for the resonant excited states that are the same of the direct measurements

La Cognata et al., ApJ, 777, 143, 2013



Modified R-Matrix approach to the $^{17}\text{O}(n,\alpha)^{14}\text{C}$ reaction



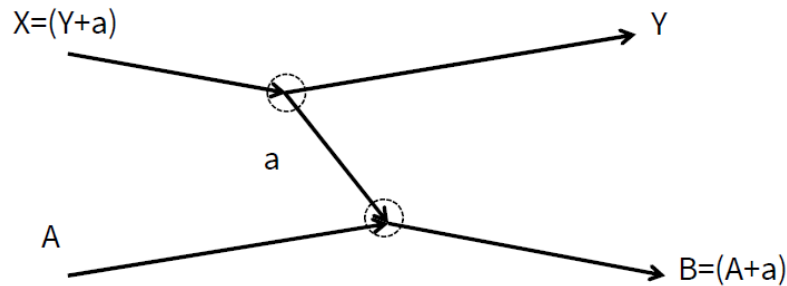
| E_{cm} (keV) | Γ_n (eV) | Γ_α (eV) | Γ_{TOT} (eV) | $\Gamma_{\text{wag.}}$ (eV) |
|-----------------------|------------------|----------------------|----------------------------|-----------------------------|
| -7 | $0,01 \pm 0,001$ | 2362 ± 307 | 2362 ± 307 | 2400 |
| 75 | $0,05 \pm 0,006$ | 36 ± 5 | 36 ± 5 | - |
| 166 | 86 ± 11 | 2171 ± 282 | 2257 ± 293 | 2258 ± 135 |
| 236 | 1714 ± 446 | 13021 ± 3386 | 14735 ± 3832 | 14739 ± 590 |

Guardo et al., Phys. Rev. C, 95, 025807, 2017



The Asymptotic Normalization Coefficient Method

Studies performed by means of «simple» transfer reactions



In Distorted Wave Born Approximation, the transition amplitude between the states before and after the reactions can be written as:

$$M(E_i, \vartheta_{c.m.}) = \sum_{M_a} \langle \chi_f^{(-)} \mathbf{I}_{Aa}^B | \Delta V | \mathbf{I}_{Ya}^X \chi_i^{(+)} \rangle$$

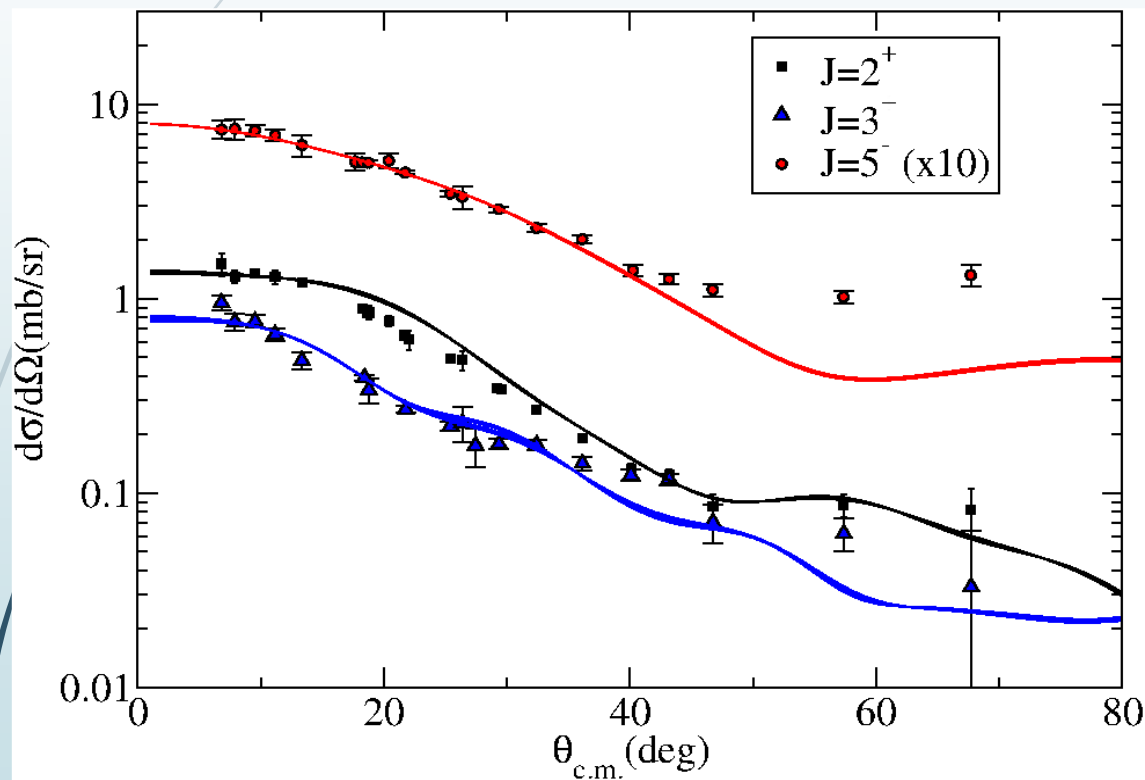
Using DWBA we were able to find the ANC's coefficients from the spectroscopic factors. This gives us some advantages:

- For peripheral reactions, ANCs have small dependence from the potential
- R_{l_B, j_B, l_x, j_x} is nearly independent from b^2
- ANCs are defined in the nuclear «exterior», so are «observable»

$$\begin{aligned} \frac{d\sigma}{d\Omega} &= \sum_{j_B, j_x} (C_{Aa, l_B, j_B}^B)^2 (C_{Ya, l_x, j_x}^X)^2 \frac{\sigma_{l_B, j_B, l_x, j_x}^{DWBA}}{b_{Aa, l_B, j_B}^2 b_{Ya, l_x, j_x}^2} = \\ &= \sum_{j_B, j_x} (C_{Aa, l_B, j_B}^B)^2 (C_{Ya, l_x, j_x}^X)^2 R_{l_B, j_B, l_x, j_x} \end{aligned}$$



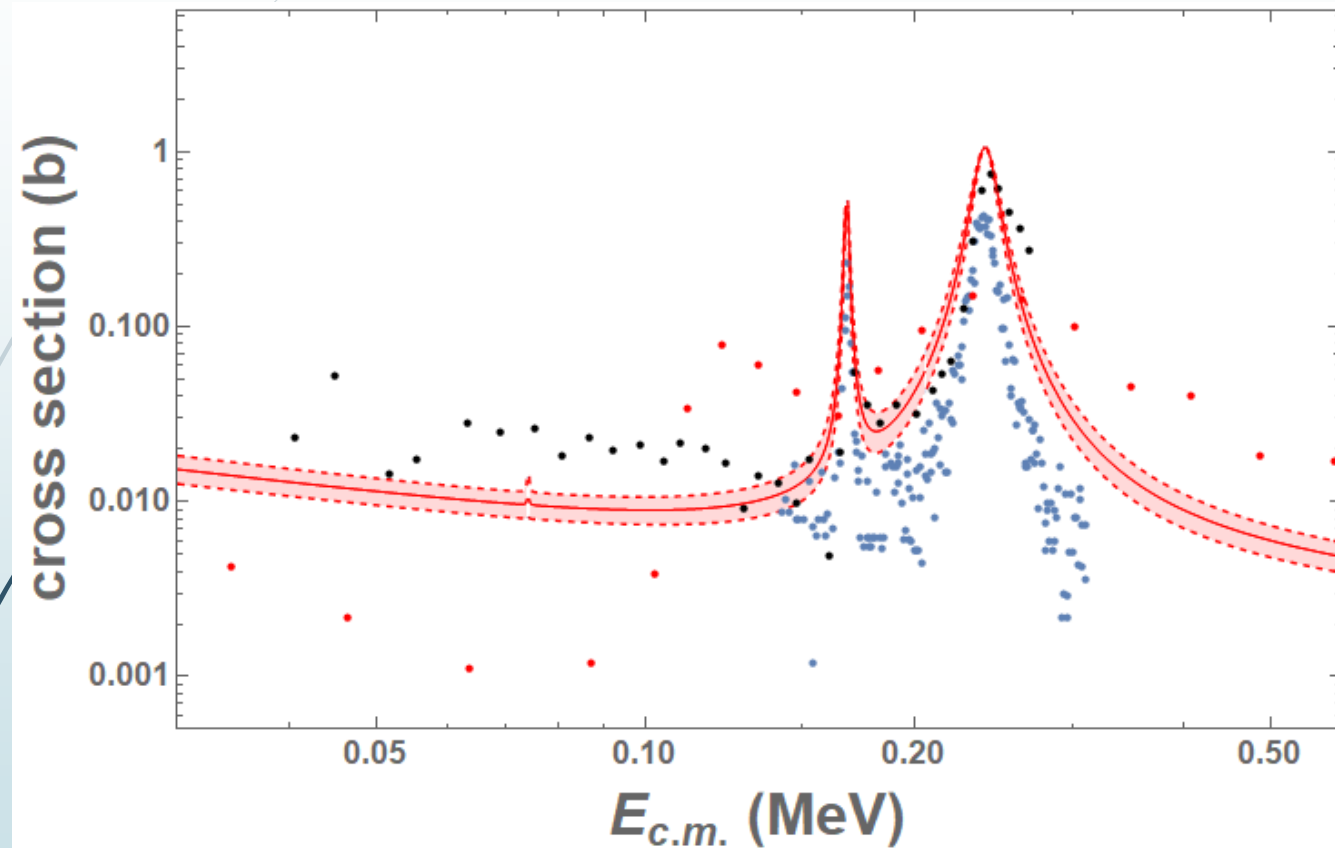
ANC extrapolation from $^{17}\text{O}(d,p)^{18}\text{O}$ transfer reaction



| $E_{18\text{O}}$ (MeV) | J^π | l | $ C ^2$ (fm^{-1}) | Orbital |
|------------------------|---------|---|-------------------------------|---------|
| 8.125 | 5^- | 3 | $3.06 \pm 0.46 \cdot 10^{-8}$ | 1f5/2 |
| | | | $2.53 \pm 0.38 \cdot 10^{-8}$ | 1f7/2 |
| 8.213 | 2^+ | 2 | $2.85 \pm 0.43 \cdot 10^{-5}$ | 2d3/2 |
| | | | $2.87 \pm 0.43 \cdot 10^{-5}$ | 2d5/2 |
| 8.282 | 3^- | 1 | $3.20 \pm 0.48 \cdot 10^{-4}$ | 2p3/2 |
| | | | $3.17 \pm 0.47 \cdot 10^{-4}$ | 2p1/2 |



Direct data comparison

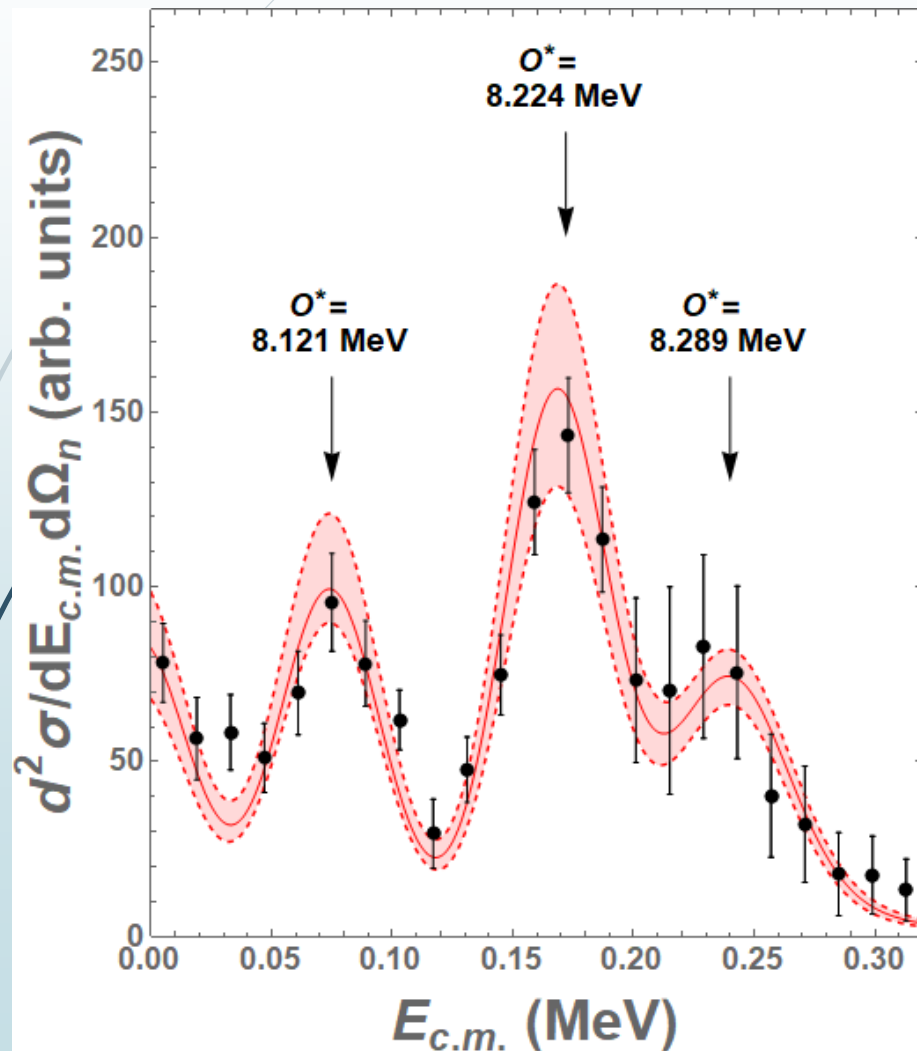


- J. Wagemans et al., Phys. Rev., C65(3), 34614 (2002)
- R. M. Sanders, Phys. Rev., 104, 1434 (1956)
INVERSE REACTION $^{14}\text{C}(\alpha, n)^{17}\text{O}$
- * P.E.Koehler & S.M.Graff, Phys. Rev., C44(6), 2788 (1991)

Figure 8. Comparison of the cross section of the neutron capture $^{17}\text{O}(n, \alpha)^{14}\text{C}$ reaction determined by ANC method (red line) with experimental data taken from Wagemans et al. (2002) (blue points), Koehler & Graff (1991) (red points) and Sanders (1956) (black points). The red band takes into account the error on the ANC calculation.



THM data comparison

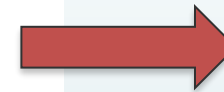
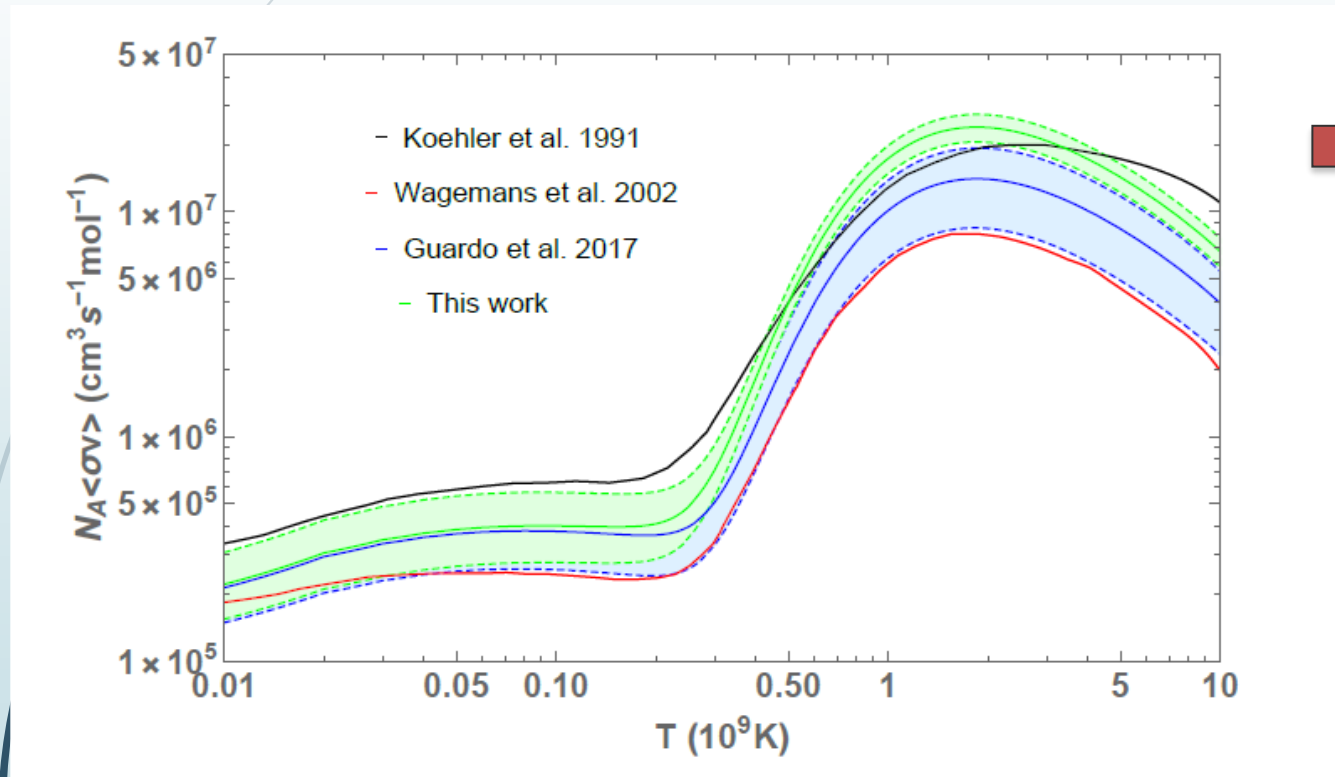


| E_{cm} (keV) | Koehler & Graff (1991) | Wagemans et al. (2002) |
|----------------|------------------------|------------------------|
| 75 | – | – |
| 178 | 1280 ± 1000 eV | 2258 ± 235 eV |
| 244 | 8000 ± 1000 eV | 14739 ± 590 eV |

| E_{cm} (keV) | Guardo et al. (2017) | This Work |
|----------------|----------------------|---------------------|
| 75 | 36 ± 5 eV | 33 ± 5 eV |
| 178 | 2260 ± 300 eV | 2150 ± 323 eV |
| 244 | 14700 ± 3800 eV | 16670 ± 2500 eV |



Astrophysical rate



Possible impact
on stellar
nucleosynthesis?



Conclusions

- A - It is possible measure the bare nucleus cross section s_b (or the bare nucleus Astrophysical Factor $S_b(E)$) at Gamow energy for reactions involving charged particles and neutron.
- B - One of the few ways to measure the electron screening effect; comparison with direct data;
- C - Measurements of radiative capture reaction cross section at Gamow energy;
- D - Application to the radioactive beam measurements;

Method complementary to direct measurements (Multi Diagnostic Experiments)



The ASFIN collaboration

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*Thank you for your
attention*



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