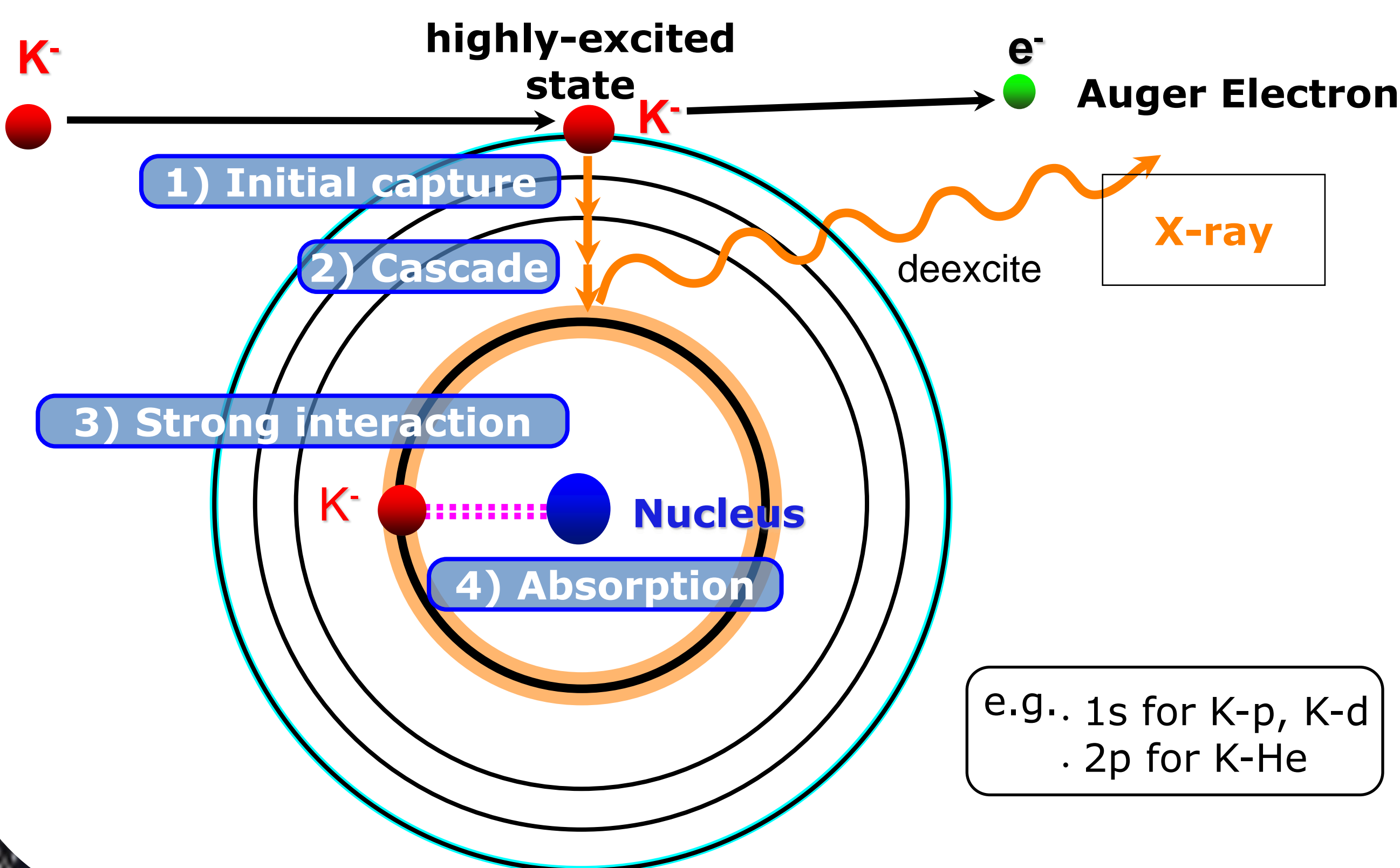


Nuclear Resonance effect in kaonic atoms



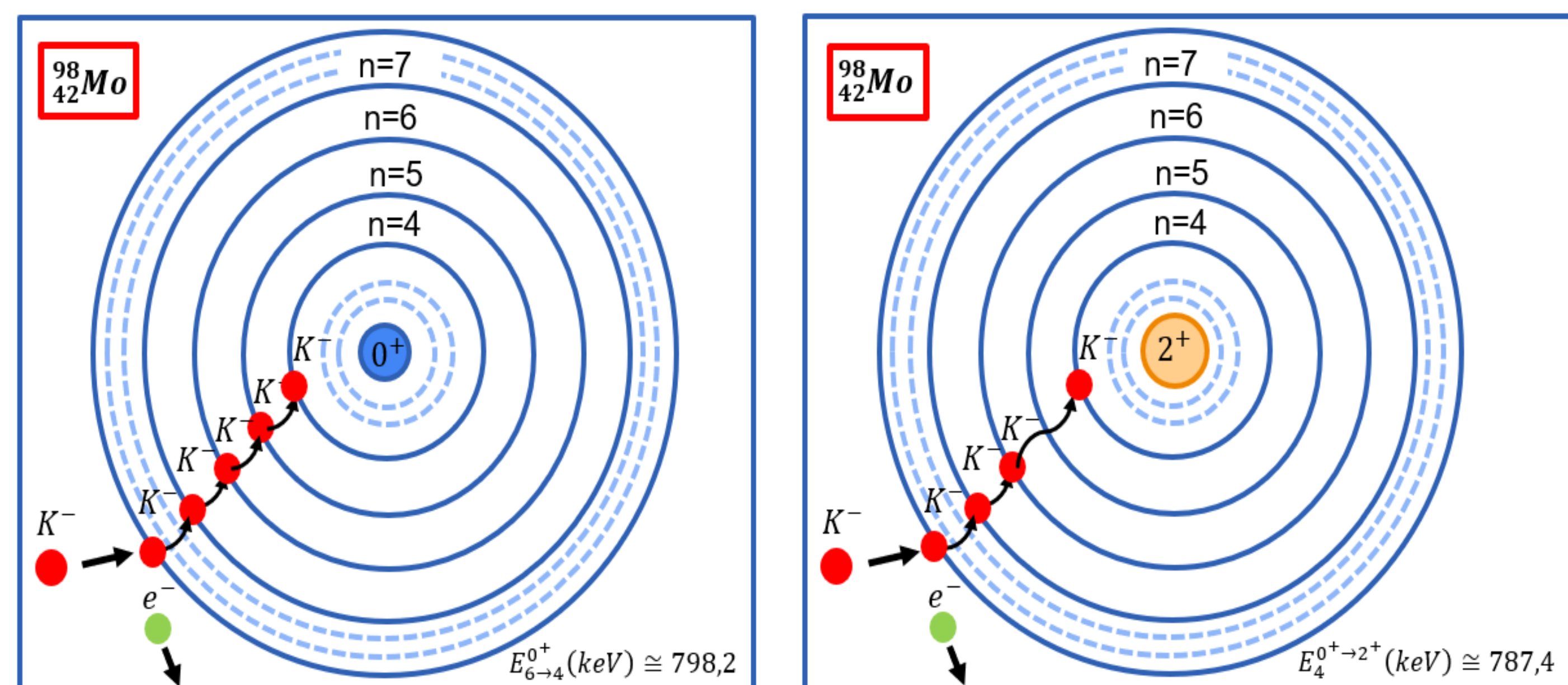
Kaonic atom formation

$n \approx \sqrt{\frac{\mu}{m_e}} \cdot n_e$, where μ is the reduced mass, m_e the electron mass and n_e is the principal quantum number of the outermost electron shell



The E2 Nuclear Resonance Effect

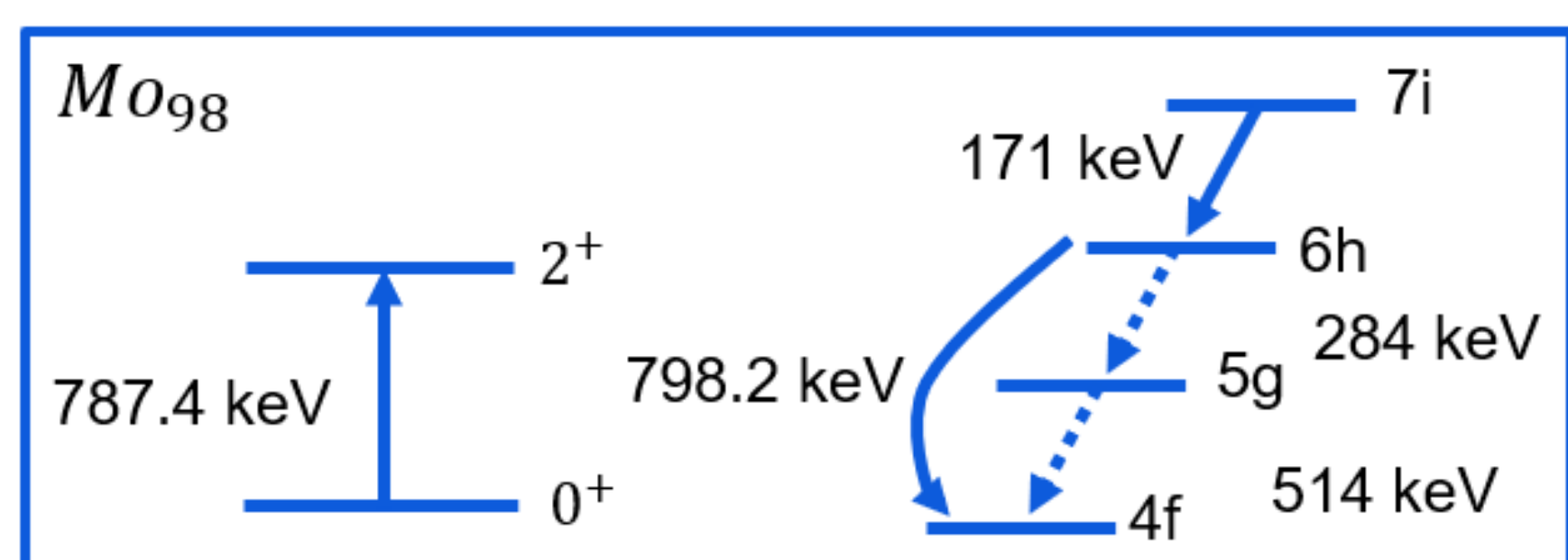
When an atomic de-excitation energy is closely matched by a nuclear excitation energy, a resonance condition occurs, which produces an attenuation of some of the atomic x-ray lines from a resonant versus a normal isotope target.



MOLYBDENUM OFFERS A UNIQUE OPPORTUNITY TO INVESTIGATE THE STRONG $K^- - N$ INTERACTION WITH NUCLEAR RESONANCES

Nucleus	$E_{2^+} - E_{0^+} [keV]$	Levels mixed	$E_{n,l} - E_{n,l-2} [keV]$	$\Gamma_{n,l-2} [keV]$	Atten lines	Energy [keV]	Ref lines	Energy [keV]
$^{94}_{42}\text{Mo}$	871	(6,5)+(4,3)	798.8	24.8	6 → 5	284.3	7 → 6	171.1
$^{96}_{42}\text{Mo}$	778	(6,5)+(4,3)	798.5	25.2	6 → 5	284.3	7 → 6	171.1
$^{98}_{42}\text{Mo}$	787.4	(6,5)+(4,3)	798.2	25.5	6 → 5	284.3	7 → 6	171.1
$^{100}_{42}\text{Mo}$	535.5	(6,5)+(4,3)	797.9	25.8	6 → 5	284.3	7 → 6	171.2
$^{96}_{44}\text{Ru}$	832.3	(6,5)+(4,3)	874.9	29.8	6 → 5	312.1	7 → 6	187.9
$^{122}_{50}\text{Sn}$	1140.2	(6,5)+(4,3)	1105.8	70.4	6 → 5	403.5	7 → 6	243.1
$^{138}_{56}\text{Ba}$	1426.0	(6,5)+(4,3)	1346.3	126.1	6 → 5	505.7	7 → 6	305.4
$^{198}_{80}\text{Hg}$	411.8	(8,7)+(7,5)	406.1	7.8	8 → 7	403.2	9 → 8	276.1

In kaonic $^{98}_{44}\text{Mo}$, the energy difference between 6h and 4f levels, 798.2 keV, is very nearly equal to the nuclear excitation energy of 787.4 keV.



- Isotope of $^{92}_{44}\text{Mo}$, in which the resonance doesn't occur, can be used as reference to measure the attenuations.
- X-rays measurable with **High Purity Ge detectors (HPGe)**

The E2 Nuclear Resonance effect is a mixing of the atomic states due to the electrical quadrupole excitations of nuclear rotational states.

Quanto-mechanically, *the effect mixes* $(n, l, 0^+)$ levels with $(n', l - 2, 2^+)$ levels producing a wave function which contains a small admixture of excited nucleus-deexcited atom wavefunctions:

$$\psi = \sqrt{1 - |\alpha|^2} \phi(n, l, 0^+) + \alpha \phi(n', l - 2, 2^+)$$

where $\alpha = \pm \frac{\langle n, l, 2^+ | H_q | n', l - 2, 0^+ \rangle}{E_{(n, l, 2^+)} - E_{(n, l, 0^+)}}$ and H_q is the *electric quadrupole interaction* between the hadron and the nucleus.

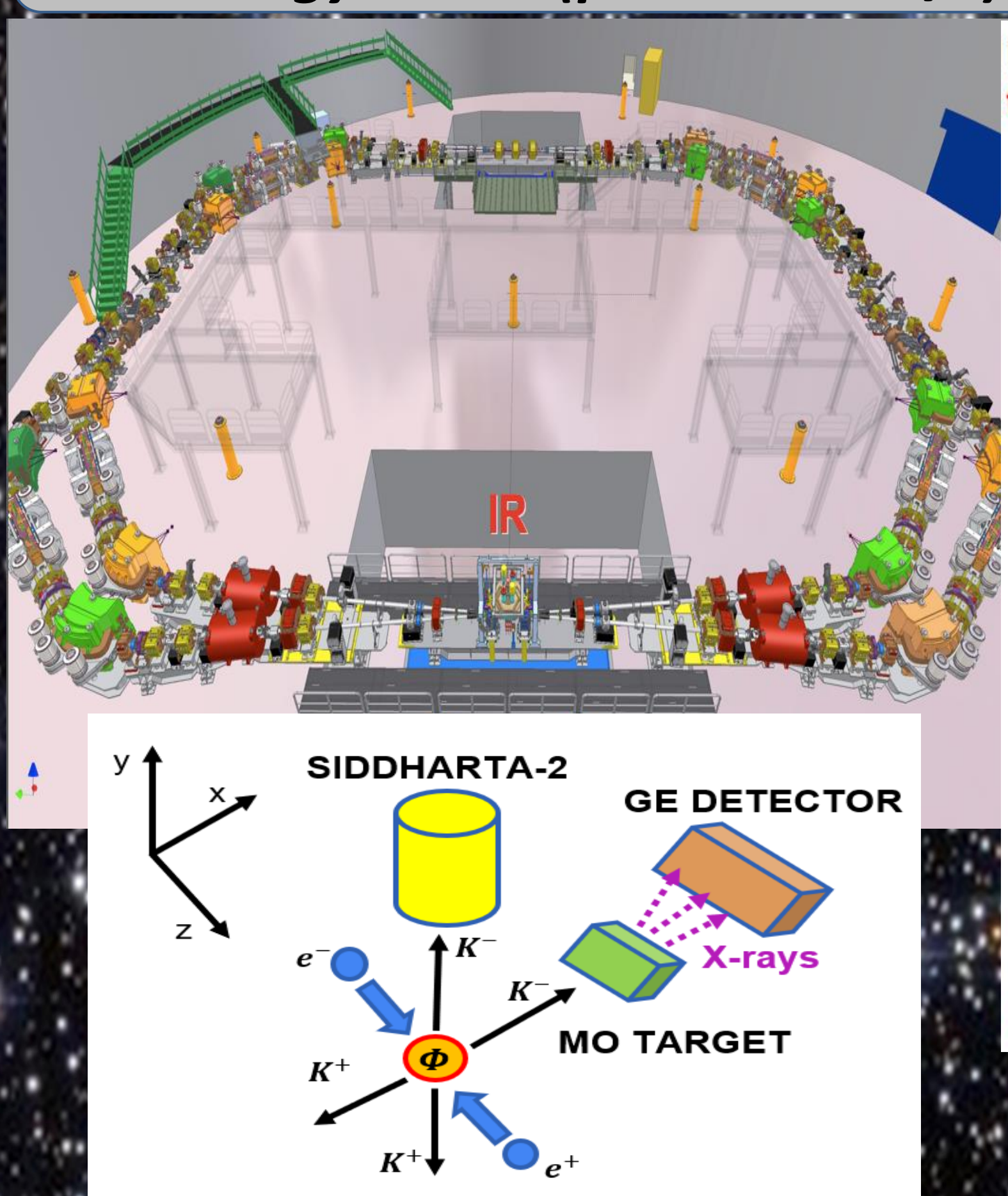
The nuclear absorption rate increases very drastically (by a factor of several hundred) for each unit decrease of orbital angular momentum; thus for a decrease of $\Delta l = 2$, the factor may be around 10^5 .

A very small admixture coefficient α (typically 1%) can mean a significant induced width!

INDUCED WIDTH: $\Gamma_{n,l}^{Ind} = |\alpha|^2 \Gamma_{n',l-2}^0$

A significant weakening/attenuation of corresponding hadronic x-ray line and any lower lines can be observed.

The DAΦNE collider provides low energy kaons ($p \sim 127 \text{ MeV}/c$)



BSI HPGe detector with transistor reset preamplifier (TRP).



Data acquisition:
• analog electronics
• fast pulse digitizer

3.1. Detection unit GCD-30185 characteristics

#	Parameter	Value
1.	Relative efficiency (with respect to 3" x 3" NaI detector and Co-60 source mounted 25 cm above the detector) at 1.33 MeV γ -photon	> 30 %
2.	Energy resolution* at	
	• 122 keV	875 eV
	• 477.6 keV	1400 eV
3.	Peak shape:	
	• FWTM/FWHM	< 1.9
4.	Spectral Broadening of FWHM up to 100,000 counts/sec for 1.33 MeV	< 8 %
5.	Peak position shift	< +/- 0.018 %
6.	Peak to Compton ratio, not worse	58 : 1
7.	Energy range of detector operation	40 keV - 3 MeV
8.	Material of input window	Al
9.	Cooling time	< 8 hours
10.	Liquid nitrogen holding time in Dewar vessel	> 15 days
11.	Dewar volume	30 l
12.	Preamplifier (built - in detector capsule) with cooled FET and transistor reset preamplifier (TRP)	
	• Preamplifier power supply is $\pm 12 \text{ V}$ with 9 pin connector compatible with NIM standards	
	• TTL signal to shut down the HV: - detector warm -0V; - detector cold: +5V	
	• HV INHIBIT - BNC	

WHY INVESTIGATE NUCLEAR RESONANCE EFFECTS IN KAONIC MOLYBDENUM?

- To measure shift and width of the $n = 4$ level, not accessible by kaonic cascade, investigating deeply bound kaonic atoms.
- The measurement of the attenuation α coefficients in $^{94}_{44}\text{Mo}$, $^{96}_{44}\text{Mo}$, $^{98}_{44}\text{Mo}$ and $^{100}_{44}\text{Mo}$ could provide fundamental information on kaon-nucleus strong interaction.
- Isotope effects in the level shift and width would reveal sign of changes in the nuclear periphery when pair of neutrons are added to the lightest isotope ($^{94}_{44}\text{Mo}$)
- To study nuclear distribution in $^{98}_{44}\text{Mo}$, providing important details to investigate neutrinoless double beta ($0\nu\beta\beta$) and two-neutrino double beta decay ($2\nu\beta\beta$)

MEASUREMENT WILL BE PERFORMED IN 2022/2023

References:

- M. Leon, «Hadronic Atoms and Ticklish Nuclei: The E2 Nuclear Resonance Effect», United States: N. p., (1975).
- S. Wycech, Nucl. Phys. A561, 607 (1993)
- Nesterenko, D.A., Jokiniemi, L., Kotila, J. et al., Eur. Phys. J. A 58, 44 (2022)

Contact:
Email to: Luca.DePaolis@Inf.infn.it