

Experimental study of the ^{40,48}Ca + ^{40,48}Ca reactions at 35 MeV/nucleon

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Context and motivations



- a^v and a^s are constants characterizing the **volume** and **surface** symmetry energy [1] ;
- a^s not well constrained by experimental data on g.s nuclear properties ;
- a^s is a fundamental quantity to describe the deformability of n-rich systems (position of the neutron drip-line, border of superheavy region, fusion/fission and rotational properties of n-rich nuclei, r-process, structure of neutron stars)



Ex. of correlations between LDM a^v and a^s coefficients extracted from Skyrme nuclear energy density functionals [2]

[1] P. Danielewicz, J. Lee, Nuc. Phys. A 818 (2009)
[2] N. Nikolov et al., Phys. Rev. C 83, 0343305 (2011)



- Formation of exotic nuclei over a wide range of n/p asymmetry
- Terrestrial way to study transient states of nuclear matter over various ρ, P, T and J
- Relatively high *E*/A* can be reached

Intermediate energies

- *15 AMeV ≤ E_{inc} ≤ 100 AMeV*
- Dissipative collisions
- Sub-saturation density regime (domain expected from model calculations)



INDRA-VAMOS coupling @ GANIL

E503 experiment



^{40,48}Ca+^{40,48}Ca @ 35 AMeV



- Si-wall → Acq. Trigger (peripheral collisions)
- Projectile identification (Z,A)
- Θ_{LAB} ≈ 2.5°- 6.5°
 φ_{LAB} ≈ 220°- 320°
- 12 Bp settings Bp₀ ≈ 0.661 2.220 T.m



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INDRA

- 14 rings (~300 identification modules)
- Identification
- \rightarrow (Z,A) for Light Charge Particles (Z \leq 5)
- \rightarrow Z up to Z~25
- θ_{LAB}≈ 7°-176°
- Event characterization (*b*, *E**, ...)

INDRA-VAMOS coupling @ GANIL

E503 experiment

^{40,48}Ca+^{40,48}Ca @ 35 AMeV



Picture of the experimental setup of the INDRA-VAMOS coupling.

[4] J. Pouthas et al., NIM A 357, 418 (1995)[5] S. Pullanhiotan et al., NIM A 593, 343 (2008)

[6] Q. Fable et al., PRC 106, 024605 (2022)



INDRA-VAMOS : general properties



INDRA-VAMOS : model calculations

- AMD + GEMINI++ calculations
- Triangular input impact parameter distribution : $0 \leq b \lesssim 8.5 \; {
 m fm}$
- Collisions followed up to : $t_{lim}\simeq 300\,\,{
 m fm/c}$
- INDRA-VAMOS experimental filter (KaliVeda)
 - → VAMOS angular acceptance and trigger favorise the detection of semiperipheral collisions



[6] Q. Fable et al., PRC 106, 024605 (2022)[7] KaliVeda HIC analysis toolkit - http://indra.in2p3.fr/kaliveda/



INDRA-VAMOS : LCP multiplicities

- $V_z^{CM} > 0$
- Increasing $\langle M_I \rangle$ with decreasing ${\rm Z_V}$ \rightarrow dissipation/centrality
- Saturation for small Z_v
- Hierarchy according to the system n-richness : $\hat{\geq}_{0.4}^{-0.4}$ $\rightarrow t$, ⁶He (n-rich) $\rightarrow p$, ³He (n-poor)
- « Neutral » behaviour for *d*, ⁴He
- Observations in agreement with published studies of ^{136,124}Xe+^{124,112}Sn [8]



⁴⁰Ca+⁴⁰Ca ⁴⁰Ca+⁴⁸Ca

> Ca+⁴⁰Ca Ca+⁴⁸Ca

> > 20

[6] Q. Fable et al., PRC 106, 024605 (2022)
[8] R. Bougault *et. al*, PRC 97, 024612 (2018)

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Symmetry energy coef. : isoscaling method

• **Isoscaling** is a scaling behaviour observed in a variety of HIC, such as :

$$R_{21}(N,Z) = \frac{Y_{(2)}(N,Z)}{Y_{(1)}(N,Z)} \propto \exp[\alpha N + \beta Z]$$

where $Y_{(i)}$ is the yield of the same isotope (N,Z) measured in two reactions (1) and (2).



• Assuming a thermal & chemical equilibrium is reached, the isoscaling coefficients (a,β) can be linked to the neutron and proton chemical potentials $\mu_{n,p(i)}$:

$$\alpha = \Delta \mu_n / T \qquad \beta = \Delta \mu_p / T$$

• A Gaussian approximation of the fragments yields in the grand-canonical approximation allows to link the isoscaling parameters to C_{sym} and the temperature T of the system (at fixed Z) :

$$\frac{4C_{sym}(Z)}{T} = \frac{\alpha(Z)}{\left(\frac{Z}{\langle A_1(Z)\rangle}\right)^2 - \left(\frac{Z}{\langle A_2(Z)\rangle}\right)^2}$$

[9] M. B. Tsang et al., Phys. Rev. Lett. 86, 5023 (2001) [10] Ad. R. Raduta, F. Gulminelli, Phys. Rev. C 75, 044605 (2007)

Symmetry energy coef. : QP reconstruction

QP reconstruction based on the relative velocities between the reaction products detected with INDRA and :

(i) The PLF identified with VAMOS ;

(ii) The largest fragment identified in charge with INDRA at backward angles (TLF)

Fragment selection :
$$\frac{V_{rel,TLF}/V_{rel,PLF} > 1.35}{V_{rel,TLF}/V_{rel,PLF} > 1.75}$$
, if $Z \ge 2$









No sel.

With sel.

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Symmetry energy coef. : QP reconstruction

QP reconstruction based on the relative velocities between the reaction products detected with INDRA and :

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• Fragment selection : $\frac{V_{rel,TLF}/V_{rel,PLF} > 1.35}{V_{rel,TLF}/V_{rel,PLF} > 1.75}$, if $Z \ge 2$

• Optimized from filtered AMD+GEMINI calculations

Estimation of the evaporated neutrons from the simulations







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Symmetry energy coef. : isoscaling coef.



 $\frac{4C_{sym}}{T} = \frac{\alpha(Z)}{\Delta}$ Isoscaling parameter $\Delta = (Z/\langle A_1 \rangle)^2 - (Z/\langle A_2 \rangle)^2$ Asymmetry of the two sources

• $\alpha vs \Delta plots$:

- → The α parameter is expected to linearly increase with increasing Δ [11,12];
- \rightarrow Not observed for the PLF ;
- → Observed for the reconstructed QP, with a better linearity when neutrons are considered.
- Secondary decays tends to :
 - \rightarrow Lower the values ;
 - \rightarrow Remove the correlations between the two parameters.

[11] S. Wuenschel et. al., PRC 79, 061602 (2009)[12] D. V. Shetty et. al., PRC 70, 011601 (2004)

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Symmetry energy coef. : isoscaling coef.

Rec. QP (with evaporated neutrons) ъ [6] 4848/4040 4848/4048 4840/4040 4840/4048 0 (a) \triangleleft 0.06 0.04 0.02 0 0 0 (b) 0 0 0 $\alpha/4\Delta$ 6.5 5.5 4.5 (C) 3.5 10 12 14 16 18 Z_{QP}

$$\frac{4C_{sym}}{T} = \frac{\alpha(Z)}{\Delta}$$
Isoscaling parameter
$$\Delta = \left(Z/\langle A_1 \rangle\right)^2 - \left(Z/\langle A_2 \rangle\right)^2$$
Asymmetry of the two sources

- Evolution of α and Δ with the size of the QP :
 - \rightarrow Increase of both parameters with the size of the reconstructed QP;
 - \rightarrow Surface dependence [13]?
- Hierarchy depending on the system combination

 → Exp. confirmation that α is a good surrogate for isospin transport study [14].

[13] Ad. R. Raduta, F. Gulminelli, PRC 75, 044605 (2007)
[14] L. W. May *et al.*, PRC 98, 044602 (2018)

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Asymmetry of the two sources

- Evolution of α and Δ with the size of the QP :
 - → Increase of both parameters with the size of the reconstructed QP;
 → Surface dependence [13]?
- Hierarchy depending on the system combination

 → Exp. confirmation that α is a good surrogate for isospin transport study [14].
- Evolution of $\alpha/4\Delta = C_{sym}/T$ with the size of the QP :
 - \rightarrow Increase with the size of the reconstructed QP;
 - \rightarrow The change in temperature with Z_{OP} must nonetheless be understood

to draw conclusion about the symmetry energy term itself

[13] Ad. R. Raduta, F. Gulminelli, PRC 75, 044605 (2007)
[14] L. W. May *et al.*, PRC 98, 044602 (2018)



Symmetry energy coef. : calorimetry

- **QP reconstruction** based on the relative velocities between the reaction products detected with INDRA and :
 - \rightarrow (i) The PLF identified with VAMOS;
 - \rightarrow (ii) The largest fragment identified in charge with INDRA at backward angles (TLF)
- The evaporated neutrons were from AMD+GEMINI (filtered)

$$Z_{QP} = Z_V + \sum_{i}^{M_I} Z_i$$
$$A_{QP} = \tilde{A}_{QP} + M_n^{rdm} \left(\tilde{A}_{QP}, Z_{QP} \right)$$
$$\tilde{A}_{QP} = A_V + \sum_{i}^{M_I} A_i$$



• **Calorimetry :** QP reconstruction allows to estimate E*/A using calorimetry :

$$E^* = \sum_{i}^{M_{CP}} Ek_i + M_n \cdot \langle Ek_n \rangle - Q$$

$$E^* = \sum_{i}^{M_{CP}} Ek_i + M_n \cdot \langle Ek_n \rangle - Q$$

$$Estimated from exp. proton average kinetic energy (corrected from Coulomb repulsion)$$

Symmetry energy coef. : temperatures



Apparent temperatures extracted by fitting the slope of the proton kinetic energy spectra using « **3D Calorimetry** » :

→ Definition of 6 domains in azimutal angle in the reaction plane ;

→ The idea is to keep only LCP emitted in a spatial domain where the QP acts as a **screen to other emission sources**



 T_{app} extracted by fitting the slope of the proton kinetic energy spectra in the forward domains with a Maxwell-Boltzmann distribution





Symmetry energy coef. : temperatures



• Evolution of E*/A :

→ Decreasing average E*/A with increasing charge of the QP (dissipation); → Minimum close to Z_{proi} =20 for all systems;

 \rightarrow Similar evolution of the standard deviation ;

- \rightarrow The overall distribution are wide and overlapping, with a saturation for $Z_{OP}^{}$ < 14
- \rightarrow The sensitivity to the most dissipative collisions is reduced for small QP size

 \rightarrow The selection on Z_{QP}, while necessary for isoscaling, is possibly not restrictive enough for extracting the temperature...

Evolution of apparent temperatures T_{app}:

- \rightarrow For all systems, relatively stable values around 3.7 MeV is reached;
- \rightarrow Compatible with Natowitz et. al compilation (PRC65, 034618 (2002))

→ A « grouping » of the distributions according to the projectile is nonetheless observed (use of proton spectra ?)

Symmetry energy coef. : results



- For all combinations, decreasing values of $\alpha/4\Delta$ with increasing excitation energy.
- This behaviour consistent with various HIC isoscaling data

 → Could be indicative of a decrease in symmetry energy as a
 function of increasing excitation energy.
- Comparisons of isoscaling multifragmentation data with evaporation models have also highlighted that α, C_{sym}, the temperature of the source and the density at break-up are all correlated

→ Thus a drop in $\alpha/4\Delta$ may be related to a decrease in density [19].



Symmetry energy coef. : results

$$\frac{4C_{sym}}{T} = \frac{\alpha(Z)}{\Delta}$$
$$\Delta = \left(\frac{Z}{\langle A_1 \rangle}\right)^2 - \left(\frac{Z}{\langle A_2 \rangle}\right)^2$$



A gradual decrease of the symmetry energy of the hot primary fragments is observed with decreasing charge, from **21** *MeV* for the most peripheral collisions (Z close to the projectile) towards **13** *MeV* for the most dissipative.

These findings highlight the importance of **surface contribution** A fit to the data leads to a surface-to-volume ratio :

$$\rightarrow r_{S/V} = a_a^{S}/a_a^{V} \approx -1.72 + -0.04; \rightarrow a_a^{V} = 41.58 + -0.44 \text{ MeV}; \rightarrow a_a^{S} = -71.63 + -1.38 \text{ MeV}.$$

Nonetheless, high value of a_a^{V} is obtained

→ Temperatures ?

→ Overestimation from isoscaling method ?

 \rightarrow Effect of measuring the hot QP?

Symmetry energy coef. : conclusions

• The **experimental symmetry energy** of the primary fragments formed in HIC peripheral collisions at intermediate energies were extracted using the **isoscaling method** :

→ The Quasi-Projectile reconstruction (based on the relative velocities between the reaction products detected in INDRA and the PLF detected in VAMOS) is mandatory to extract meaningful values from isosacling ;

→ Temperatures around 3.6 *MeV* for all the systems were extracted from Maxwellian fits to the protons kinetic spectra ;

- A gradual decrease of the symmetry energy of the hot primary fragments is observed with decreasing charge, from 21 MeV for the most peripheral collisions (Z close to the projectile) towards 14 MeV for the most dissipated.
- These findings highlight the importance of surface contribution :
 → A fit of Eq.(2) to the data leads to a surface-to-volume ratio r_{s/v} = a^s/a^v ≈ 1.7;
- These results are consistent with the idea that the fragments formed a sub-saturation density and finite temperature behave differently than the bulk nuclear matter.
- The observed isosaling parameters as well as the Z/A ratios (from PLF and reconstructed QP) are of first
 interest to study the isospin transport phenomena.



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Isospin transport



Isospin transport

The Equation of State of a nuclear system

- The EOS of a nuclear system is defined by its energy per nucleon : $\epsilon(\rho, T, \delta)$
- The density dependence of the symmetry energy term $\epsilon_{sym}(\rho,T)$ remains a major issue in modern nuclear physics :
- \rightarrow describes the energetic cost of converting isospin symmetric matter into neutron matter ;
- \rightarrow constraints well established for T=0K and $\rho=\rho_0$ by fitting with nuclear masses ;
- \rightarrow largely unknown as soon as we move away from saturation density.





- Formation of exotic nuclei over a wide range of n/p asymmetry
- Terrestrial way to study transient states of nuclear matter over various ρ, P, T and J
- Relatively high E*/A can be reached

Intermediate energies

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- Dissipative collisions
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Isospin diffusion with INDRA-VAMOS



Evaporative Attractor Line

- ≠ evolution depending on the system:
 1) Projectile
 → number of available neutrons in the
 - entrance channel.
- 2) Target
 → Isospin diffusion
- Initial N-Z not reached
 → Statistical decay

• QP reconstruction :

- \rightarrow Further away from the EAL ;
- \rightarrow For ⁴⁸Ca proj., higher values that the initial n-richness of the mixed systems



Isospin transport ratio with INDRA-VAMOS

Complete eq.

Isospin transport ratio

$$R_x = \frac{2x^M - x^{NR} - x^{ND}}{x^{NR} - x^{ND}}$$



NR : neutron-rich system

ND : neutron-deficient system



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Centrality

- Centrality refers to the classification of events according to their impact parameter **b**.
- In experimental analyses, collisions are instead classified according to a given experimental parameter X, as b is not directly measurable.
- We define the **experimental centrality** (for a variable which increase with collision violence) as :

$$c_x \equiv \int_x^{+\infty} P(X) \, dX$$

[21] J.D. Frankland, PRC 104, 034609 (2021) [22] R. Rogly, PRC 98, 024902 (2018)

"order parameter" (correlated to the centrality)

Isospin transport ratio with INDRA-VAMOS





Isospin transport ratio with INDRA-VAMOS



- Decrease of R_{δ} with the dissipation of the collision \rightarrow from $R_{\delta} = \pm 0.75$ to $R_{\delta} = \pm 0.25$
- This indicates a regular evolution to towards isospin equilibration
- Smoother evolution for the reconstructed QP compared to the PLF

 → The origin could be a non-linear transformation of δ that can't be fully recovered by the isospin transport ratio
- The reconstructed QP asymmetry is an experimental observable relevant for direct comparisons with transport models

 → Direct estimation of the transport coefficients

Isospin migration with INDRA-VAMOS



Conclusions and outlooks

• Symmetry energy term of finite nuclei :

 \rightarrow It is also possible to reformulate the usual relation between the C_{sym} and isoscaling parameter such as :

$$a_a^V - \frac{4}{3}a_a^S \frac{X_{-7/3}}{X_{-2}} = \frac{\alpha(Z)T}{4Z^2 X_{-2}} \quad \text{with} \ X_n = \langle A_1(Z) \rangle^n - \langle A_2(Z) \rangle^n$$

 \rightarrow Ongoing analysis (courtesy of S. Typel)

Isospin transport :

→ INDRA-VAMOS experiment allows to probe the isospin transport phenomena, predicted by transport models, with ^{40,48}Ca+^{40,48}Ca peripheral collisions

- \rightarrow Experimental evidence of isospin diffusion and migration ;
- \rightarrow QP reconstruction allows direct comparisons with dynamical models ;

 \rightarrow Use of the b-centrality.

• INDRA-FAZIA coupling (see C. Ciampi talk) :

- \rightarrow Complementary results ;
- \rightarrow Effect of beam energy (density) ?
- **Extensive comparisons** with different models to link the observations to transport properties :
 - \rightarrow BLOB, QMD, AMD...
 - \rightarrow transport coef.



Thanks for your attention

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Back-up slide : Particle ID





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Back-up slide : Particle ID with VAMOS



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Back-up slide : Particle ID with VAMOS



Back-up slide : Data normalization

- Beam intensity corrections $\rightarrow I_{beam}$
- Dead Time corrections $\rightarrow DT$



• Magnetic rigidity overlaps $\rightarrow \delta$



Weight $W(I_{beam}, DT, \delta, \theta_{LAB})$ applied event-by-event