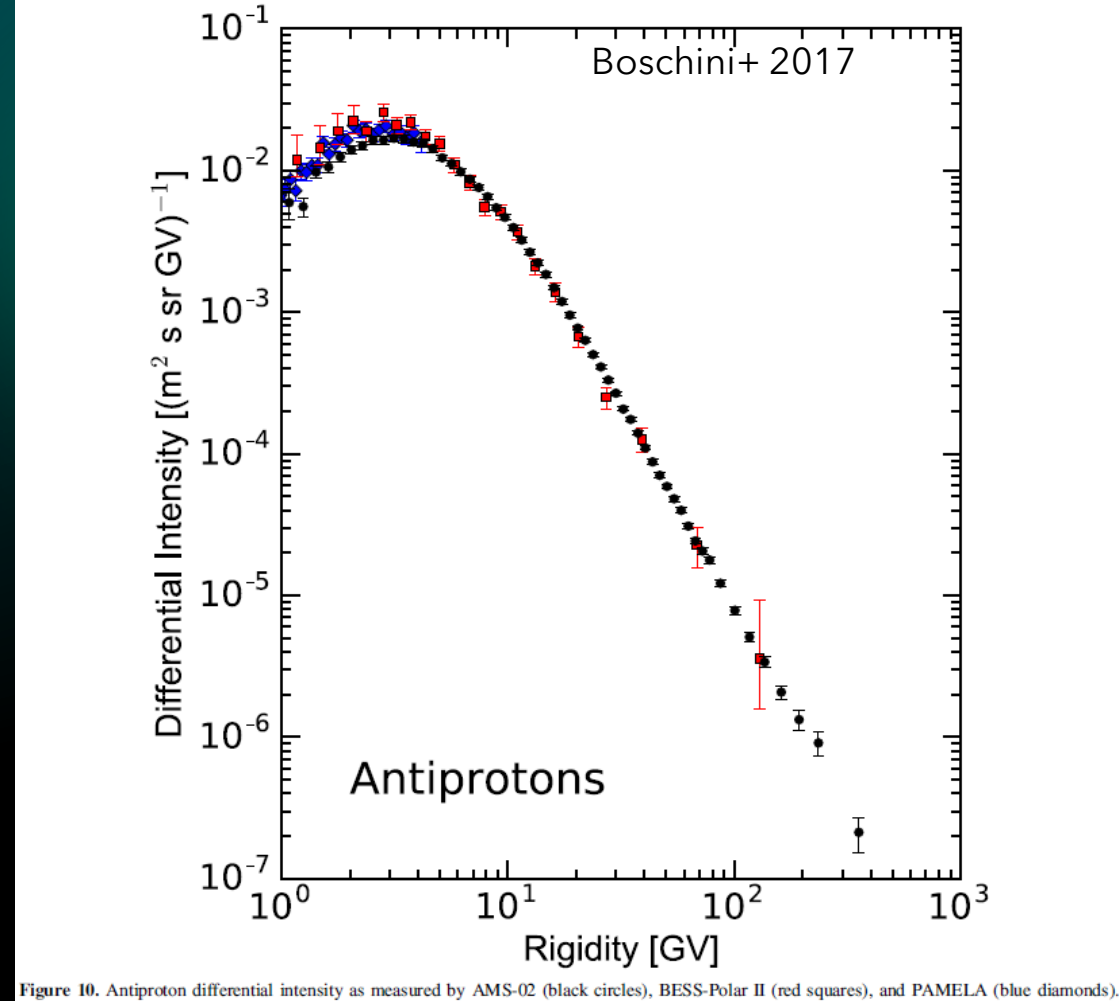
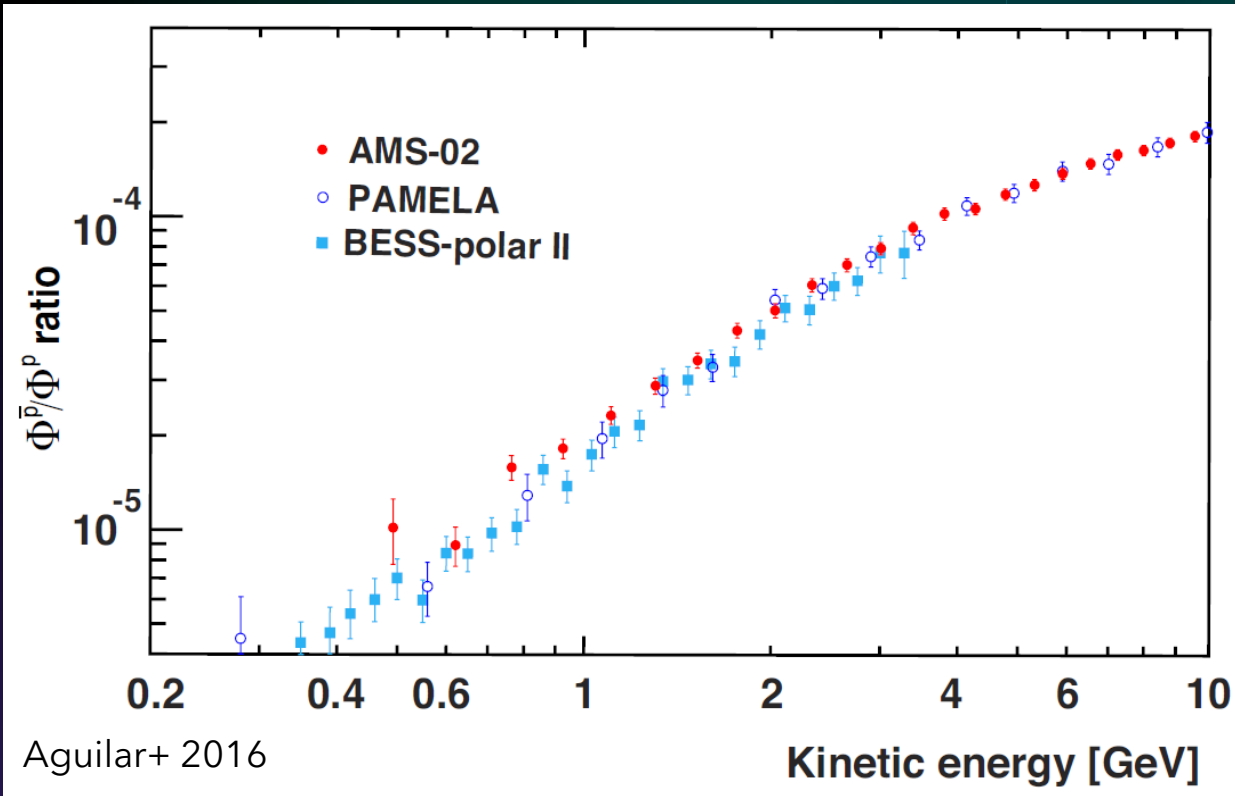


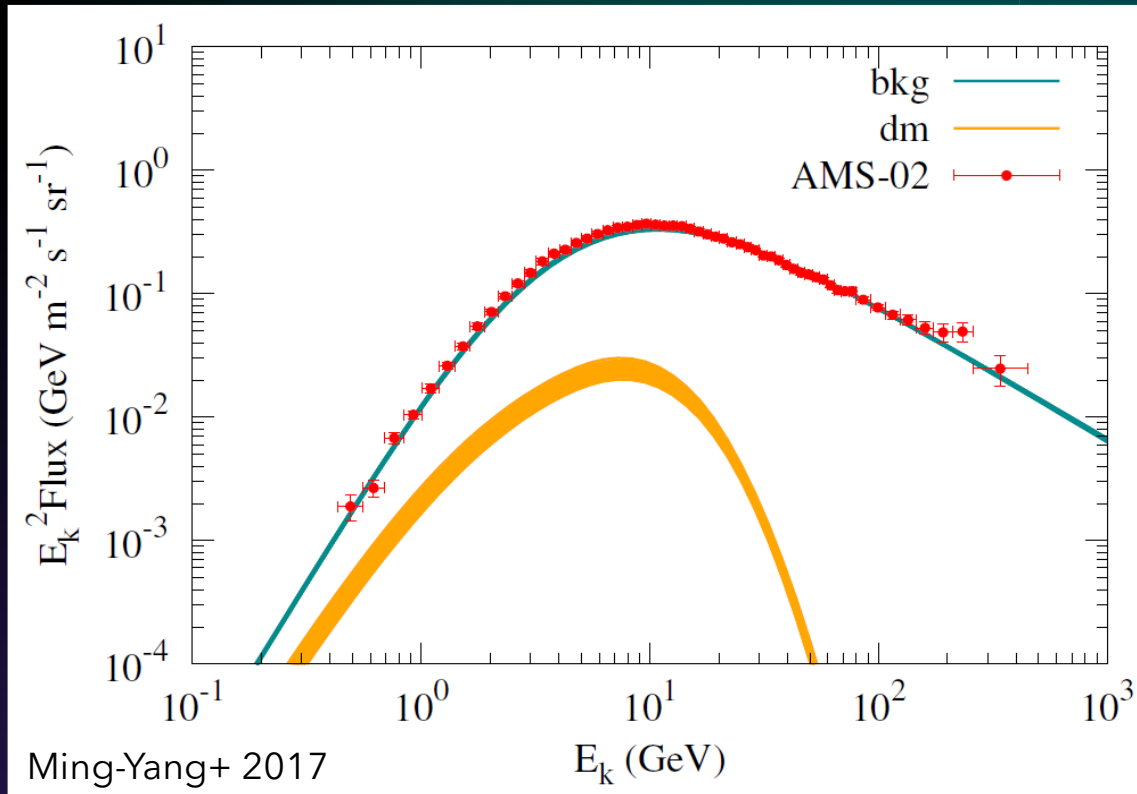
Solar modulation of antiproton GCR for indirect search of dark matter

STEFANO DELLA TORRE
INFN SEZ. MILANO-BICOCCA

Antiproton measurements become extremely precise in the last decade.



Many claims of DM subproducts



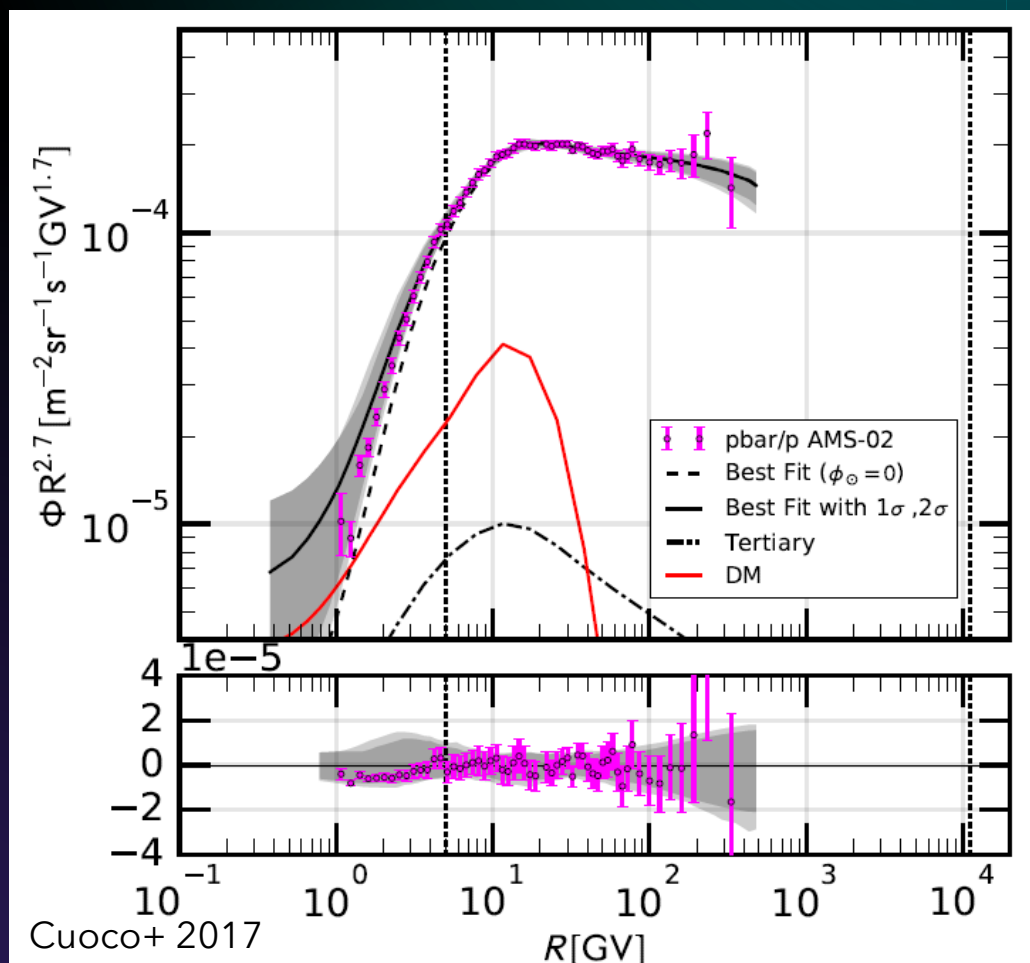
Ming-Yang+ 2017

[...] AMS-02 data favor a DM component with a mass of a few tens GeV and an annihilation cross section of the thermal production level for quark final state [...]

[...] The best fit DM mass is about 40 – 60 GeV, and the annihilation cross section is about $(1 - 3) \times 10^{-26} \text{ cm}^3 \text{s}^{-1}$ for $b\bar{b}$ channel. [...]

[...] The solar modulation model is adopted to be the force-field approximation [...]

Many claims of DM subproducts



Cuoco+ 2017

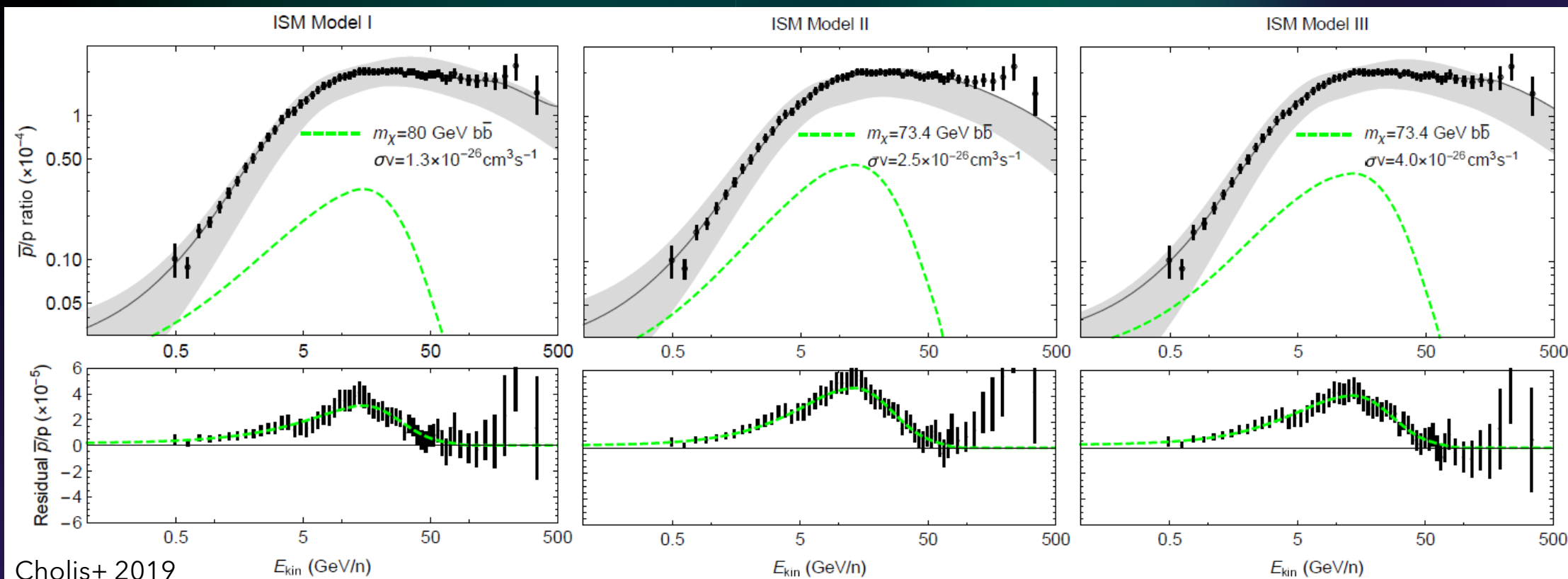
[..] We consider the rigidity range $R \lesssim 5$ GV, for which the force-field approximation should describe solar modulation reliably. Adding DM annihilating into $b\bar{b}$, with $m_{DM} \approx 80$ GeV and $\langle\sigma v\rangle \approx 3 \times 10^{-26} \text{ cm}^3\text{s}^{-1}$, results in a much better fit and provides an intriguing hint for a DM signal in the antiproton flux. [..]

[..] the DM component corresponds to a significance of $\sim 4.5\sigma$, although this does not take into account possible systematics errors. [..]

Many claims of DM subproducts

Cholis+ 2019

[...] We use the standard formula to model the impact of the modulation potential [...]



Is there a Dark Matter signal in Low Energies \bar{p} -GCR?

- What is the impact of using a more complex modulation model?
- How much is reliable an Antiproton LIS?

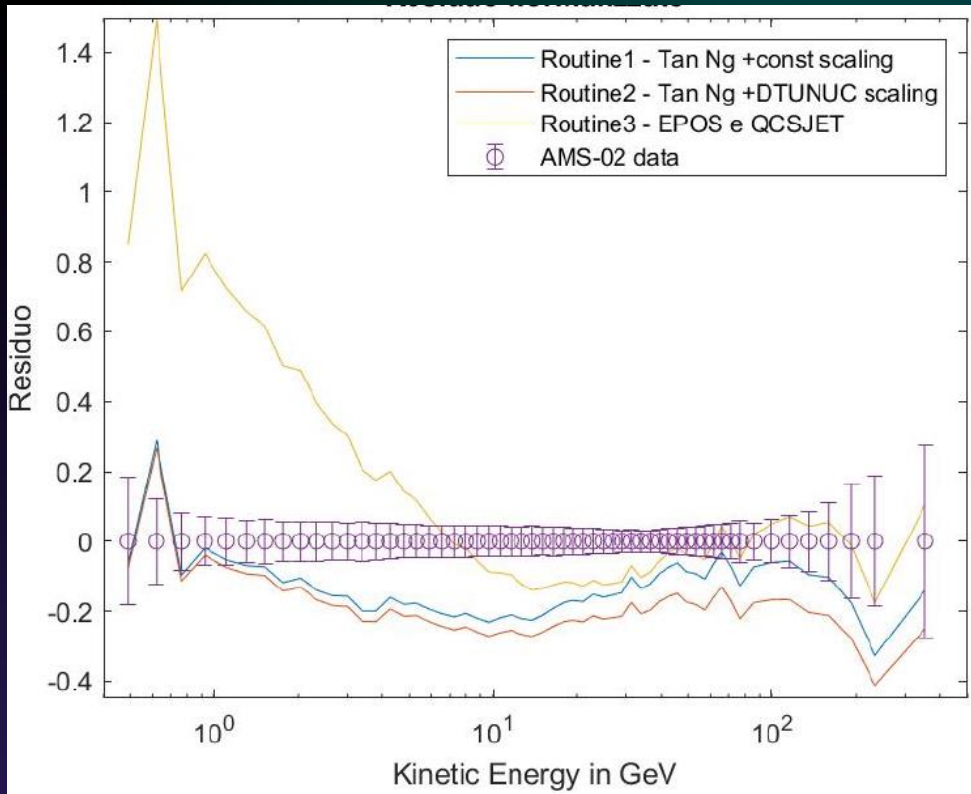
Outline

- General consideration on antiproton production cross section
- Solar Modulation model
- Antiproton LIS

Cross Section

Nuclear uncertainties

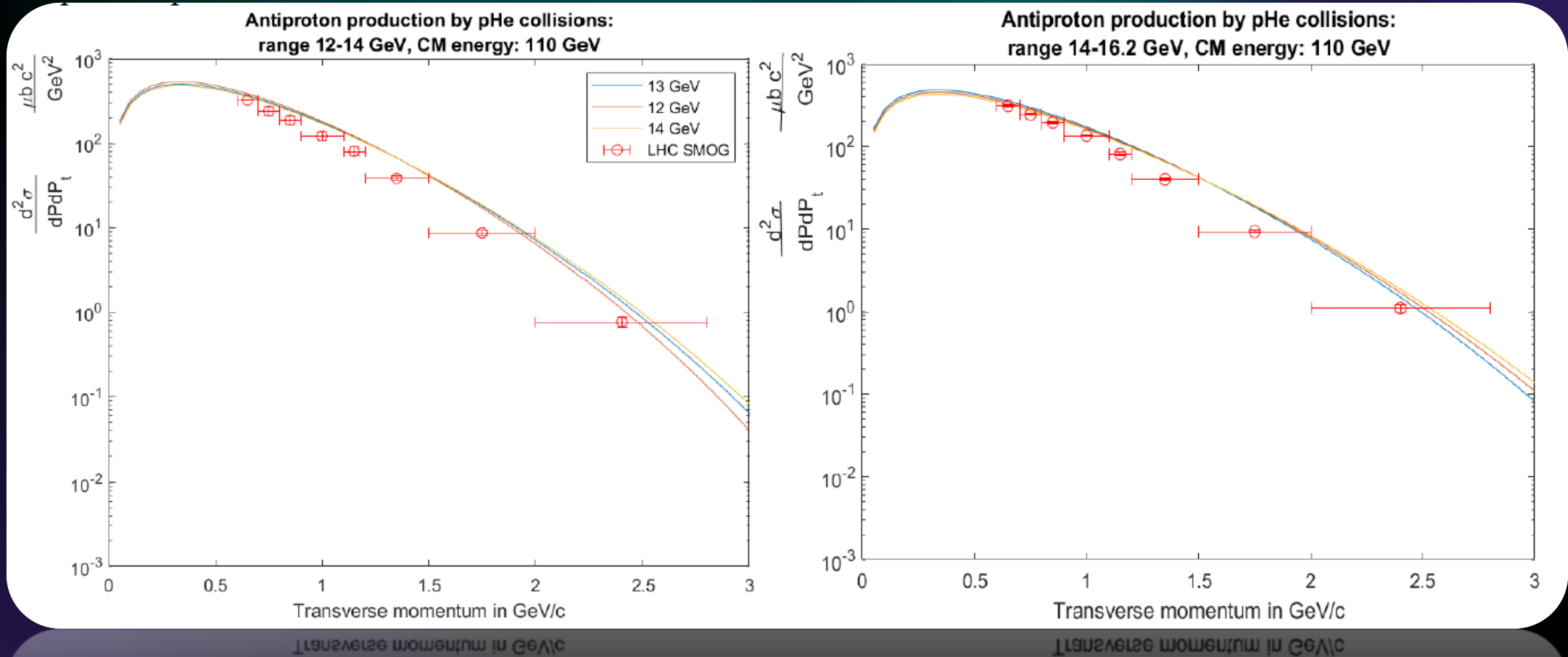
$$p + \text{ISM} \rightarrow \bar{p} \dots \left\{ \begin{array}{ll} p + p_{\text{ISM}} \rightarrow \bar{p} \dots & \text{Fundamental process, poor measurements} \\ p + \text{He}_{\text{ISM}} \rightarrow \bar{p} \dots & \text{No direct measurements} \end{array} \right.$$



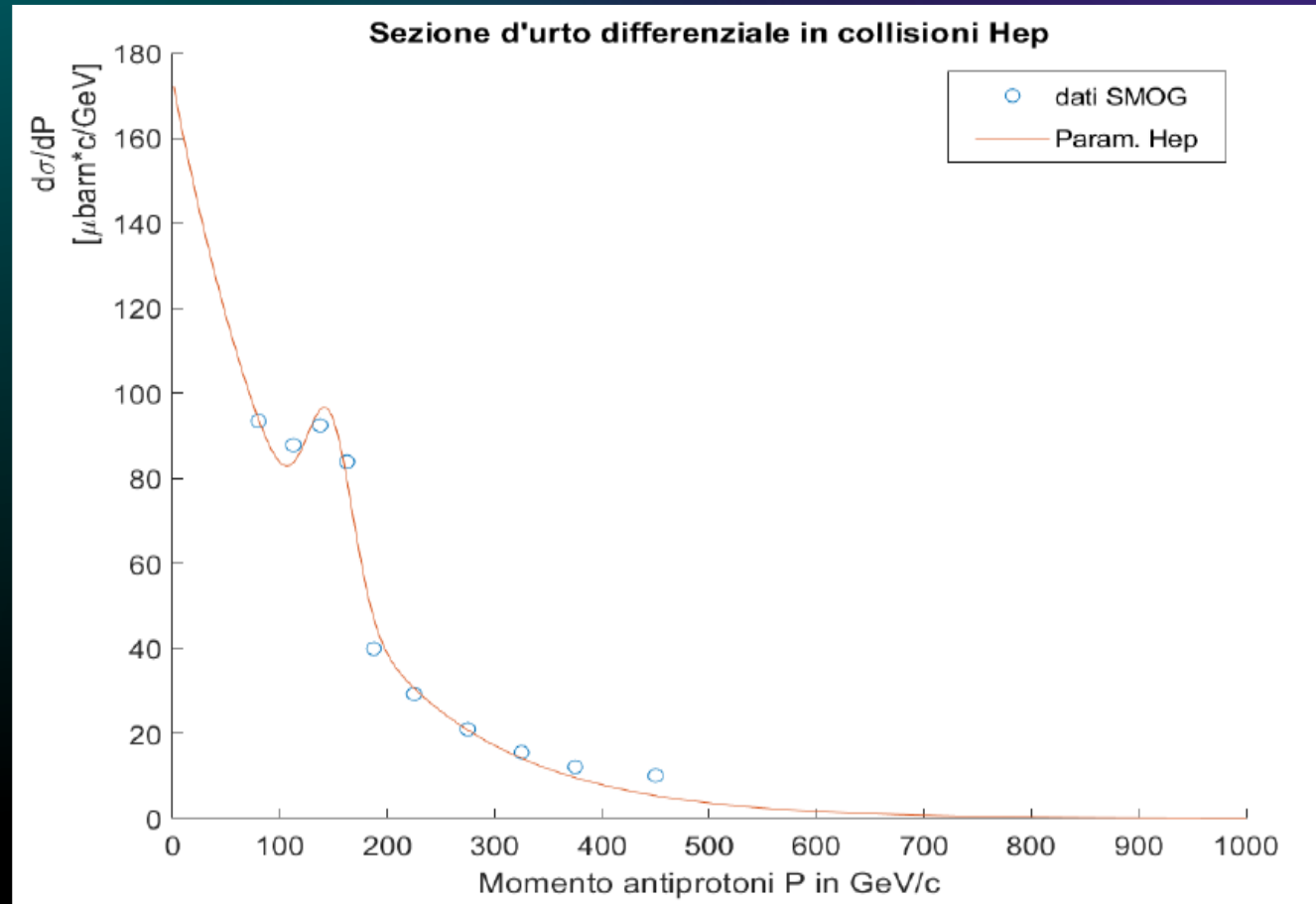
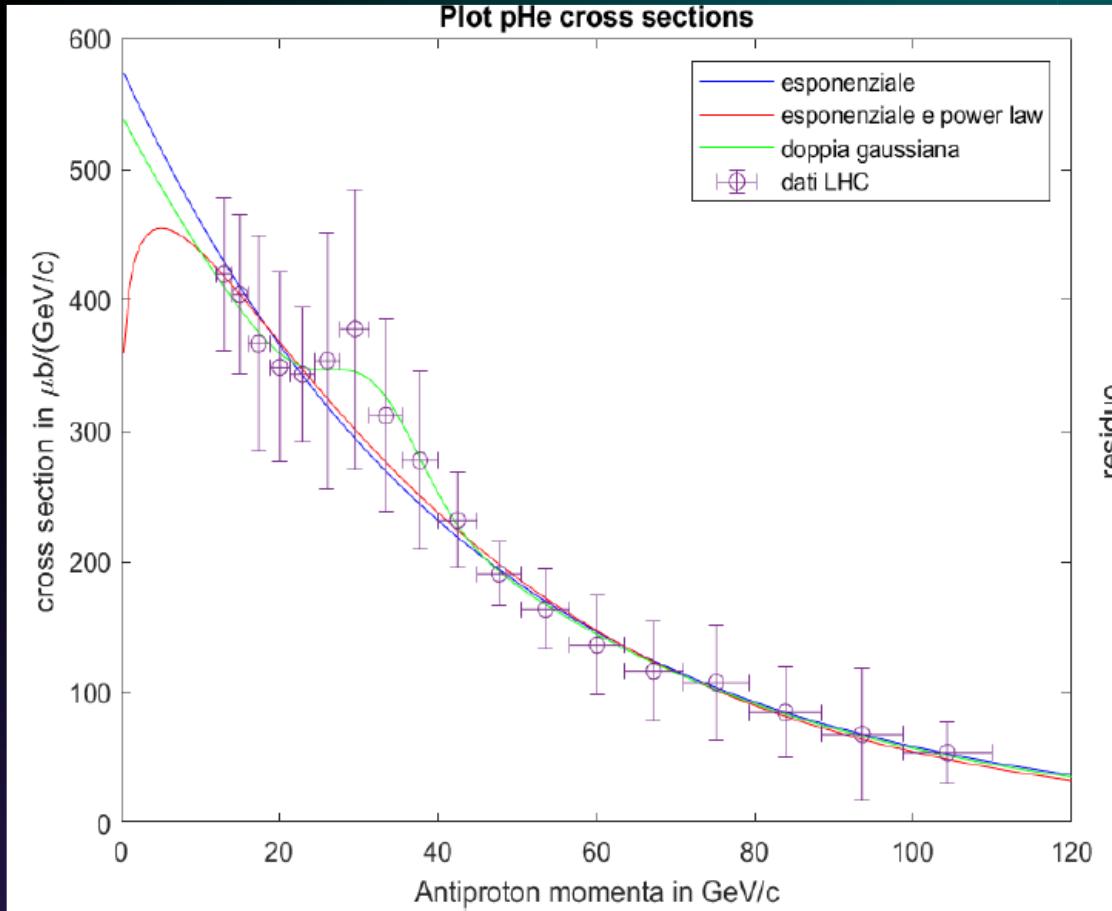
- Uncertainties in the $p\bar{p}$ production spectrum are at least 10%.
- Below 100 GeV the uncertainties for $pp \rightarrow \bar{p}$ are about 10-20%
- Above 100 GeV extrapolations lead to errors larger than 30%
- The antineutron decay contribution is usually not included
- A significant contribution to the cosmic antiproton flux is due to reactions involving He: the relevant cross section have never been measured

N. Masi 2017

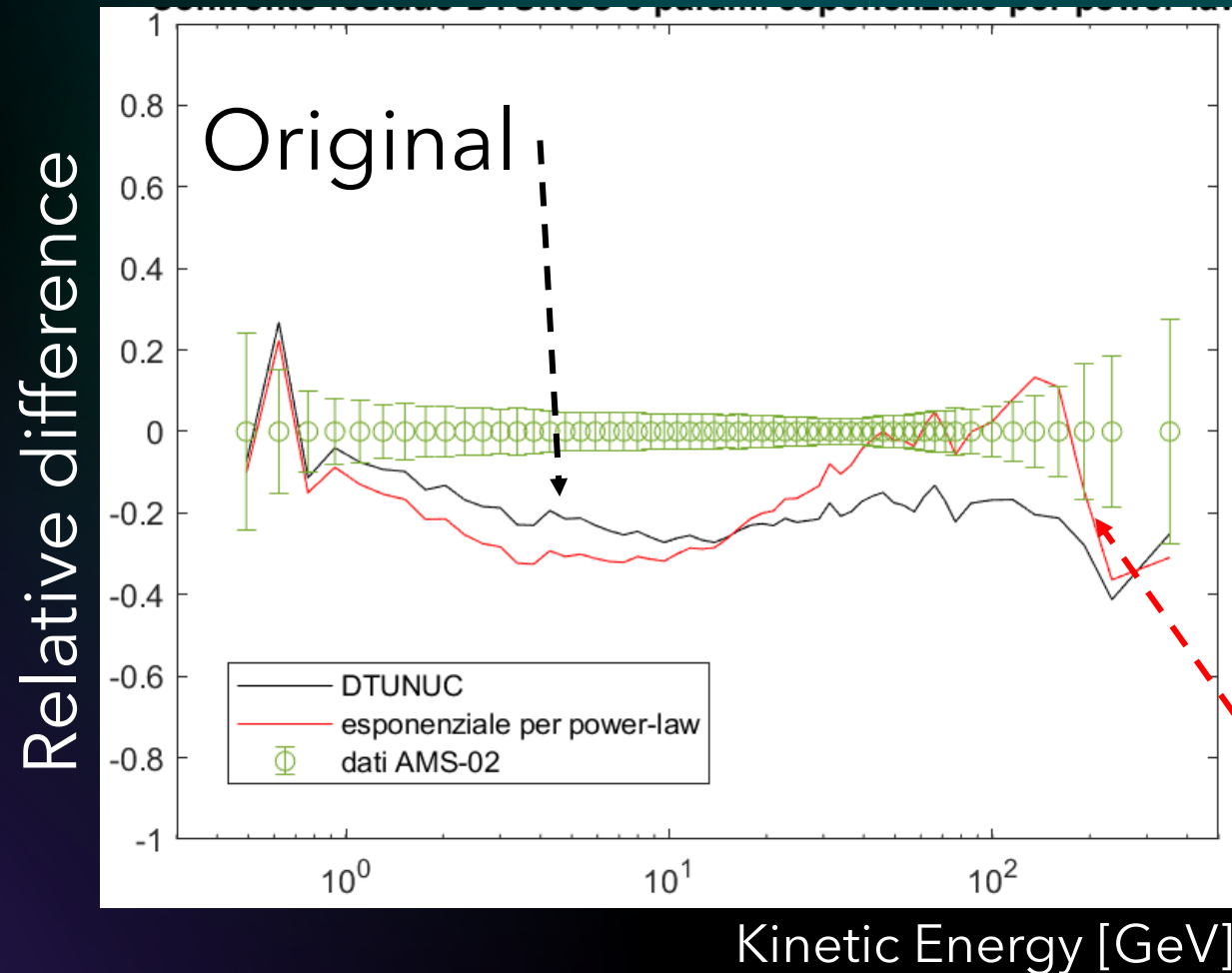
In 2017 LHCb has performed measurement of the **antiproton cross section in p He** collisions at 6.5 TeV using fixed He target @ SMOG. A precision of around 10% is attained



We parametrize p-He, He-p collision cross section from SMOG



Using same propagation parameters in GALPROP but with different cross section



A parallel work on Cross Section is mandatory.

We cannot go much further in reducing astrophysical uncertainties, but we can certainly do it for nuclear ones

Including p-He, He-p collision data

Solar Modulation

THE PASSAGE OF ENERGETIC CHARGED PARTICLES THROUGH INTERPLANETARY SPACE*

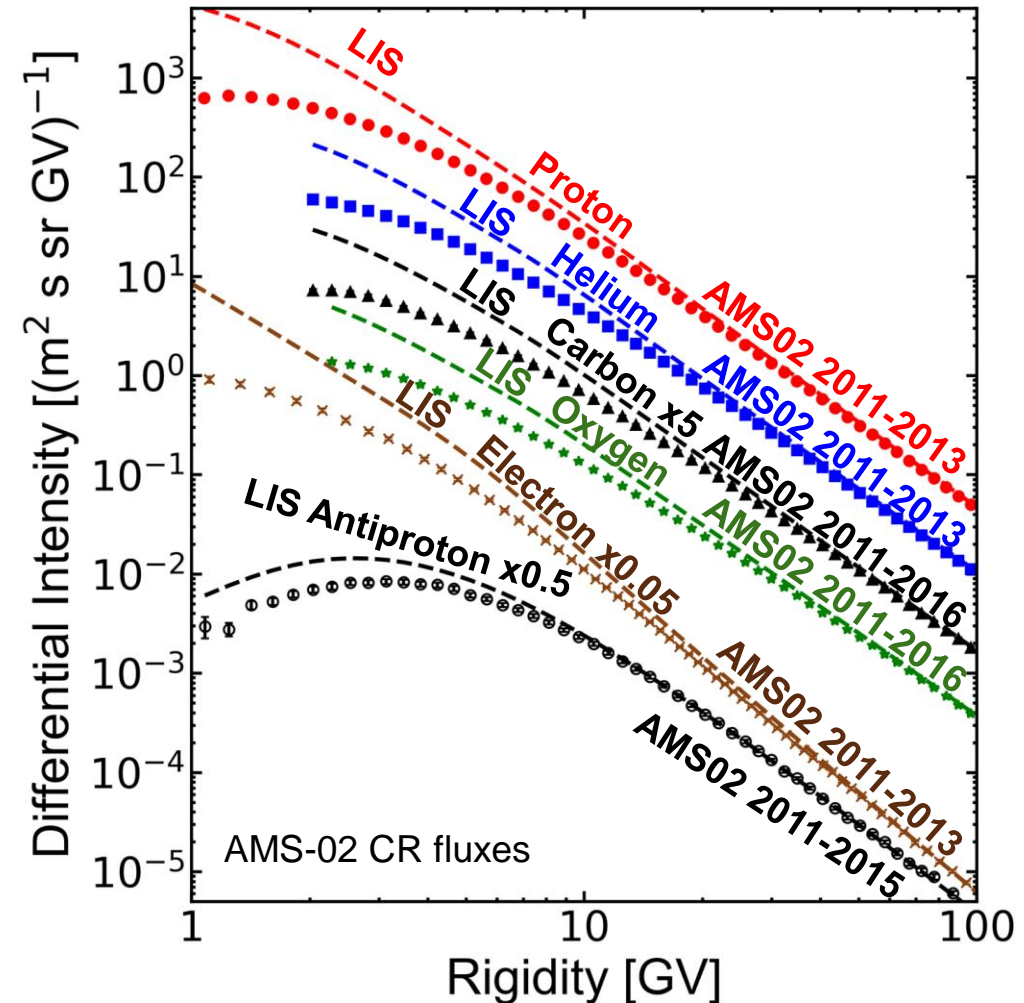
E. N. PARKER

Calculations of the motion of a charged particle in a large-scale field containing smallscale irregularities, shows that a particle is most effectively scattered by irregularities which have a scale comparable to the radius of gyration of the particles

The random walk of the cosmic ray particles is a Markhoff process, describable by a Fokker-Planck equation

Now while the energetic particle is riding along with the fields in the wind, the magnetic fields in which the particle is moving are expanding because of the radial divergence of the wind. The energetic particle is cooled adiabatically and its kinetic energy T decline.

Parker (1965)



$$\frac{\partial U}{\partial t} = \frac{\partial}{\partial x_i} \left(K_{ij}^S \frac{\partial U}{\partial x_j} \right) + \frac{1}{3} \frac{\partial V_{SW,i}}{\partial x_i} \frac{\partial}{\partial T} (\alpha_{rel} T U) - \frac{\partial}{\partial x_i} [(V_{SW,i} + v_{d,i}) U]$$

Solar Modulation

Parker Equation

$$\frac{\partial U}{\partial t} = -\nabla \cdot (U\vec{V}) + \nabla \cdot [\tilde{K} \cdot \nabla U] + \frac{(\nabla \cdot \vec{V})}{3} \frac{\partial}{\partial T} (\alpha_{\text{rel}} T U)$$

Use Kinetic Energy

$$\alpha_{\text{rel}} = \frac{T + 2m_r c^2}{T + m_r c^2}$$

$U \rightarrow$ Cosmic Rays number density per unit interval of kinetic energy

$$\frac{\partial f}{\partial t} = -\nabla \cdot (f\vec{V}) + \nabla \cdot [\tilde{K} \cdot \nabla f] + \frac{(\nabla \cdot \vec{V})}{3p^2} \frac{\partial}{\partial p} (p^3 f)$$

Use particle momentum

$f \rightarrow$ Omnidirectional distribution function

Differential Intensity is measured quantity

$$J = \frac{vU}{4\pi} = p^2 f$$

Diffusion

Convection

Drift

Energetic Loss

Solar Modulation

Computational Complexity



Analytical

- Gleeson & Axford 1968
- Gieseler et al 2017
- Corti et al 2019
- ...

Semi-Analytical

- Kuhlen & Mertsh 2019

Numerical Codes

- Aslam et al 2018
- Engelbrecht and Burger (2013)
- Boschini et al 2019
- Pei et al 2010
- Strauss et al., 2013
- Vos and Potgieter, 2016
- ...

Now GPU technology, in principle,
allows to scaledown computational time
Vogt et al 2020; Solanik et al 2021

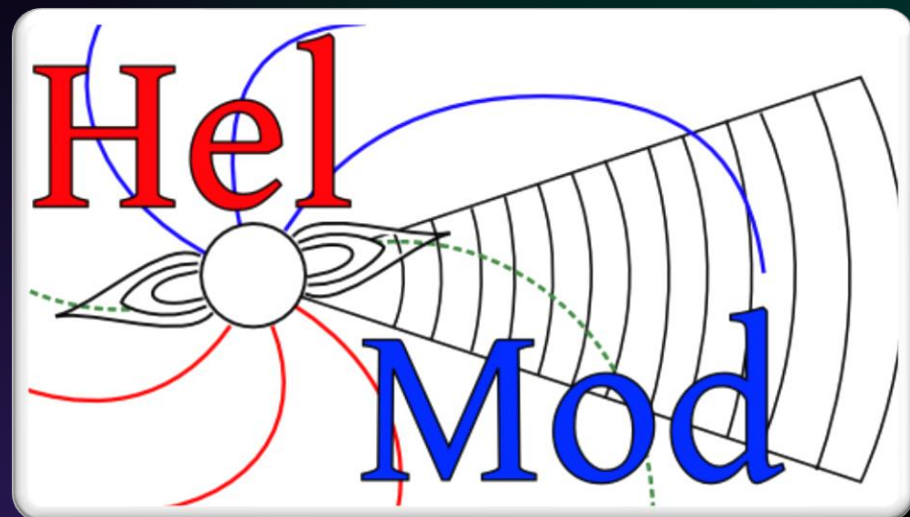
Monte-Carlo approach

Backward-in-time approach. It evolves a probability density in a phase-space

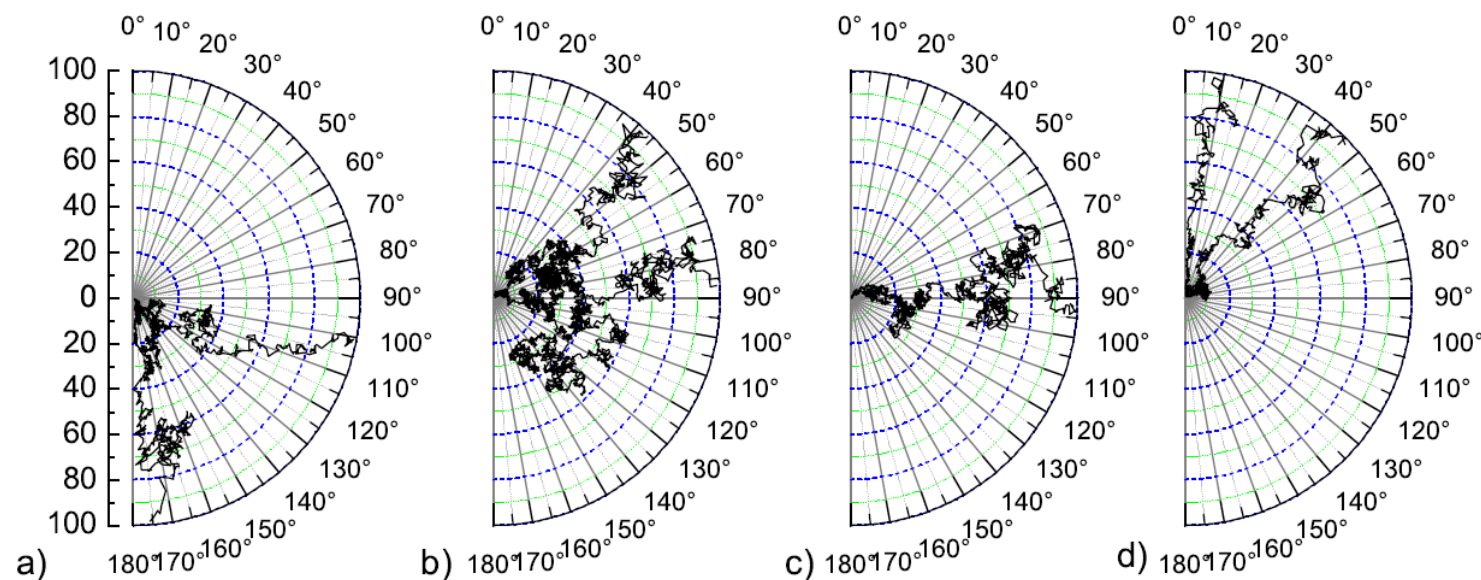
See:

Bobik et al 2016

Strauss&Effemberger SSR 2017



www.helmod.org



$$\partial_t F = - \sum_i \partial_i [A_i(\mathbf{x}, t) F] + \frac{1}{2} \sum_{i,j} \partial_i \partial_j \{ [\tilde{\mathbf{D}}(\mathbf{x}, t)]_{ij} F \}$$

Deterministic

Stochastic

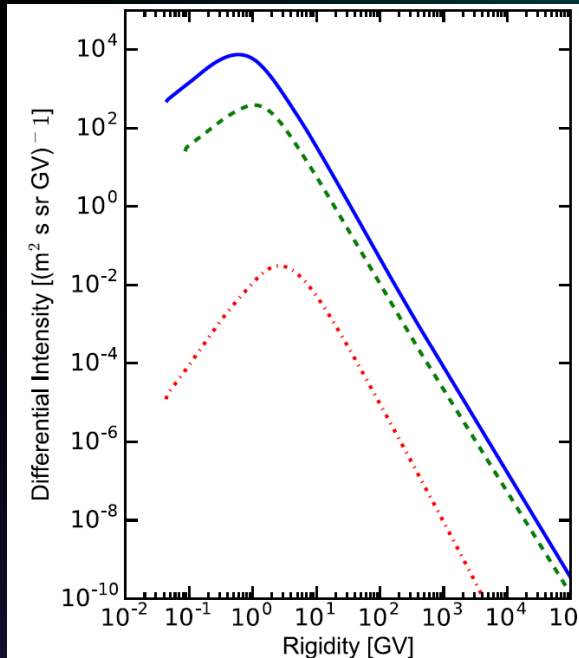
$$dx_i(t) = A_{F,i} dt + B_{F,i,j} dW_j(t)$$

Convection+ Drift

Diffusion

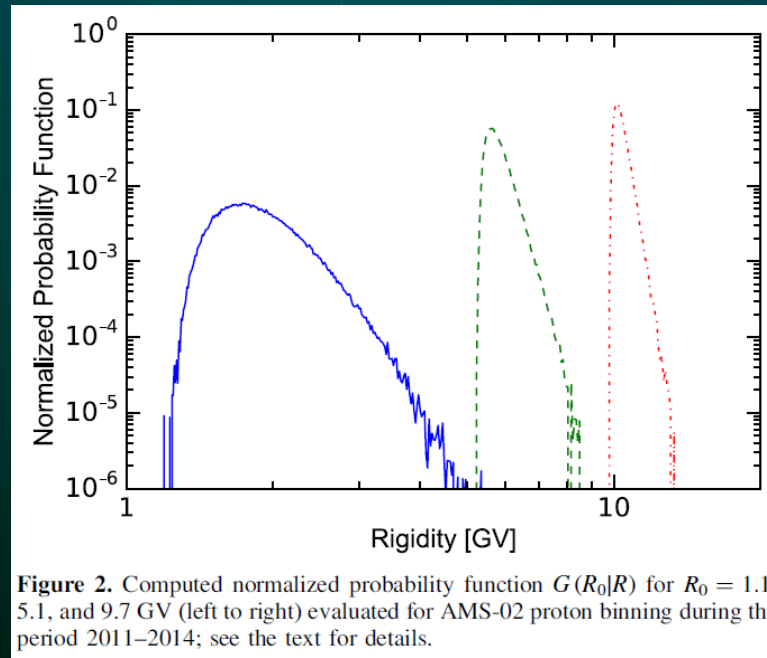
Monte-Carlo approach

Backward-in-time approach. It evolves a probability density in a phase-space



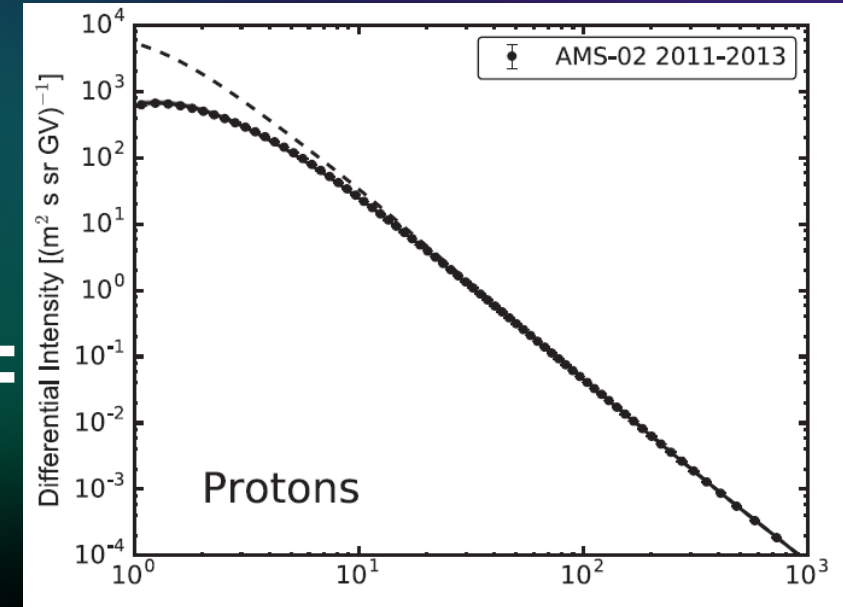
LISs

\times



Monte Carlo Solutions

$=$



Modulated Spectra

Testing Multiple LIS do not require Re-Run Simulations

The diffusion tensor

$$K_{ij} = \begin{bmatrix} K_{\parallel} & 0 & 0 \\ 0 & K_{\perp,2} & K_A \\ 0 & -K_A & K_{\perp,3} \end{bmatrix}$$

$$\frac{K_{\parallel}}{K_0} = \frac{\beta}{3} \left[\frac{P}{1 \text{ GV}} + g_{\text{low}}(t) \right] \left(1 + \frac{r}{1 \text{ AU}} \right)$$

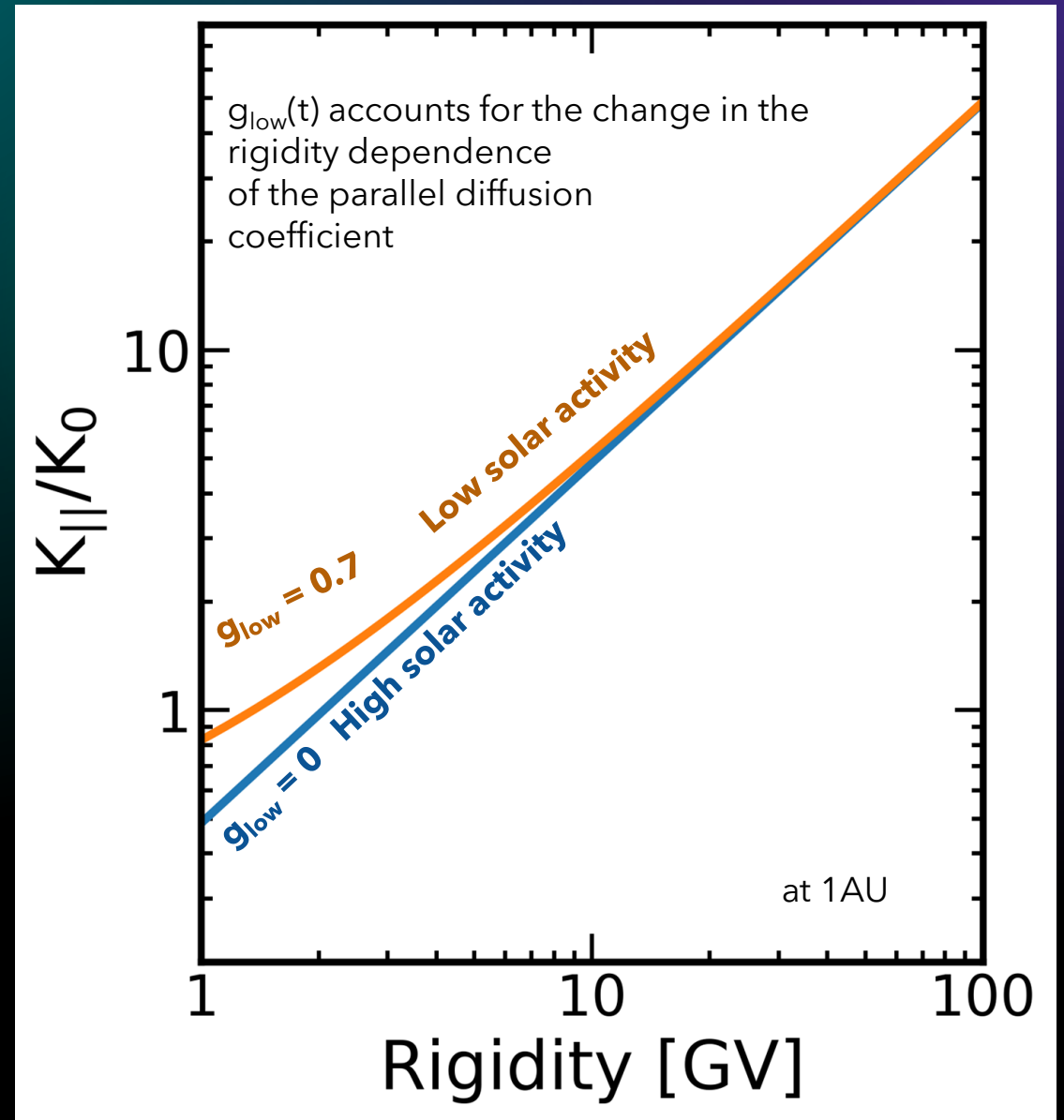
$$K_{\perp,i} / K_{\parallel} = \rho_i$$

see

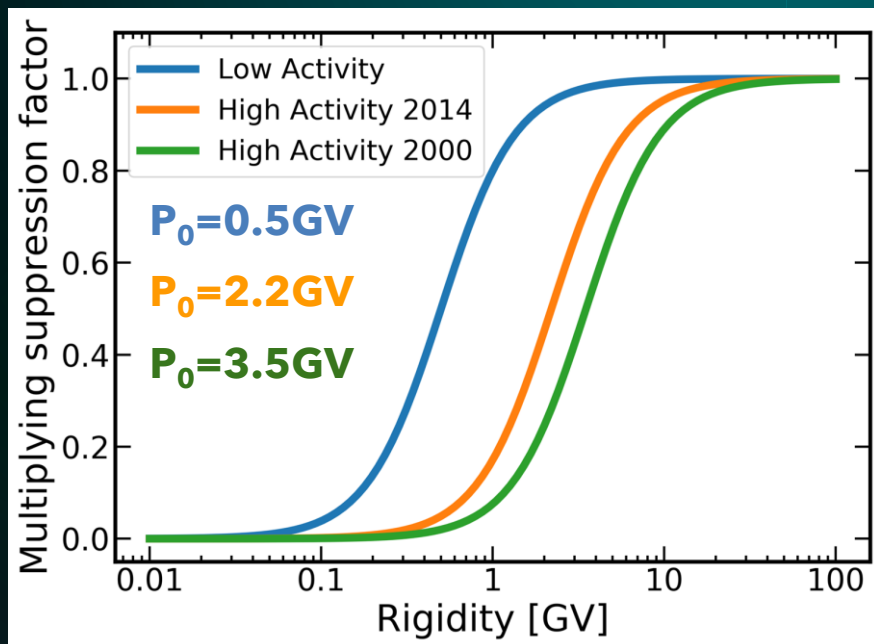
Bobik et al. ApJ 745:132 (2012)

Bobik et al. AdsAst, ID 793072 (2013)

Boschini et al. Adv. S. Res. (2017)



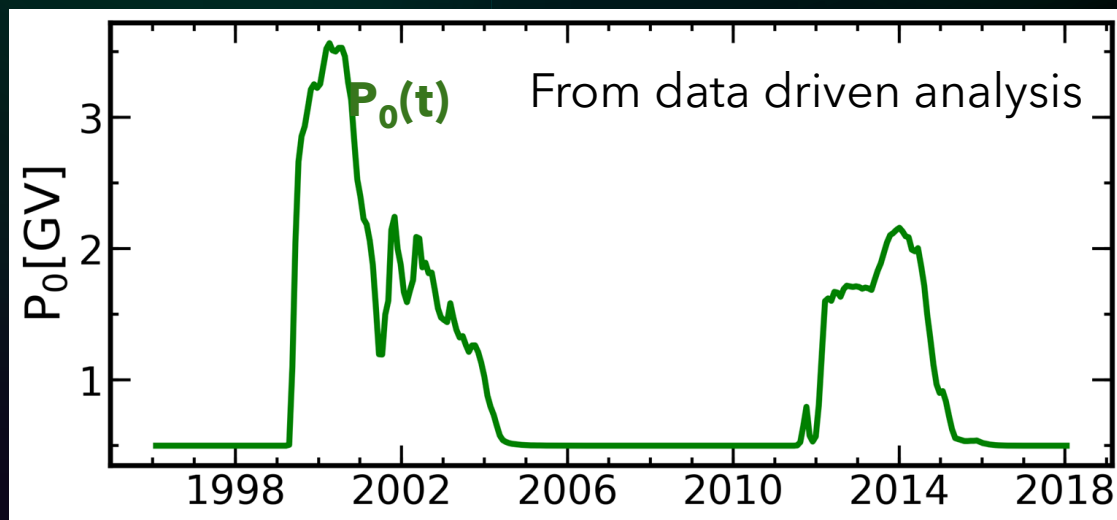
Magnetic Drift



$$K_A = \frac{\beta P}{3 B_0} \frac{P^2}{P_0^2(t) + P^2}$$

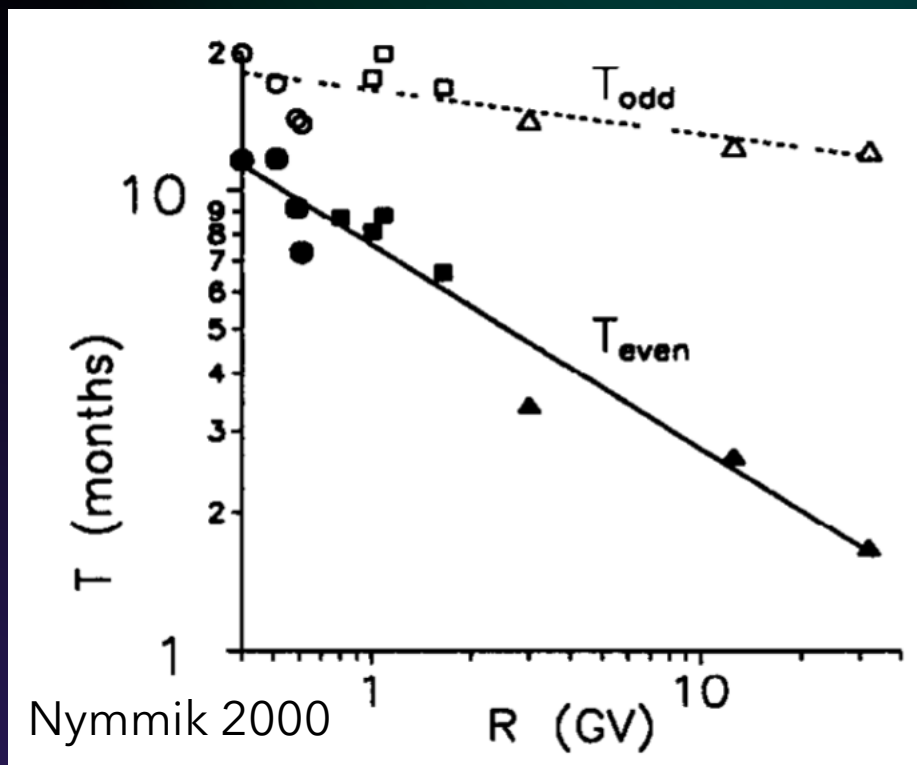
B_0 magnetic field magnitude at Earth

Bieber and Matthaeus (1997)
Burger et al. (2000)
Minnie et al. (2007)
...

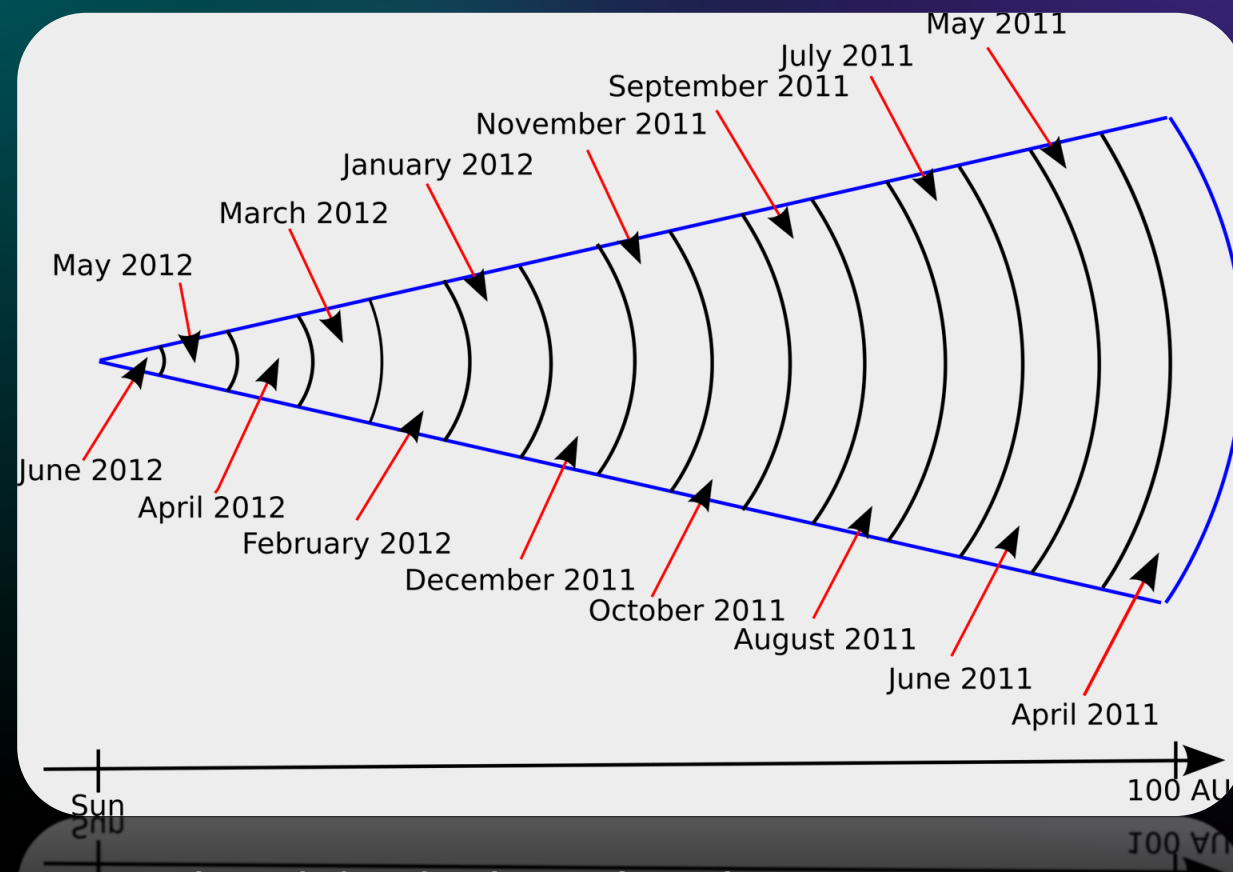


Not same conditions in all Heliosphere

The presence of a time lag between Cosmic Rays intensity and Solar parameters are known since, e.g.,
Mavromichalaki & Petropoulos 1984
Nymmik 2000



Solar perturbations moves along with Solar wind, thus it took a finite time to pass through the heliosphere



HelMod divide the Heliosphere in 15 regions, each one equivalent to the average of solar activity in the periods before the experiment

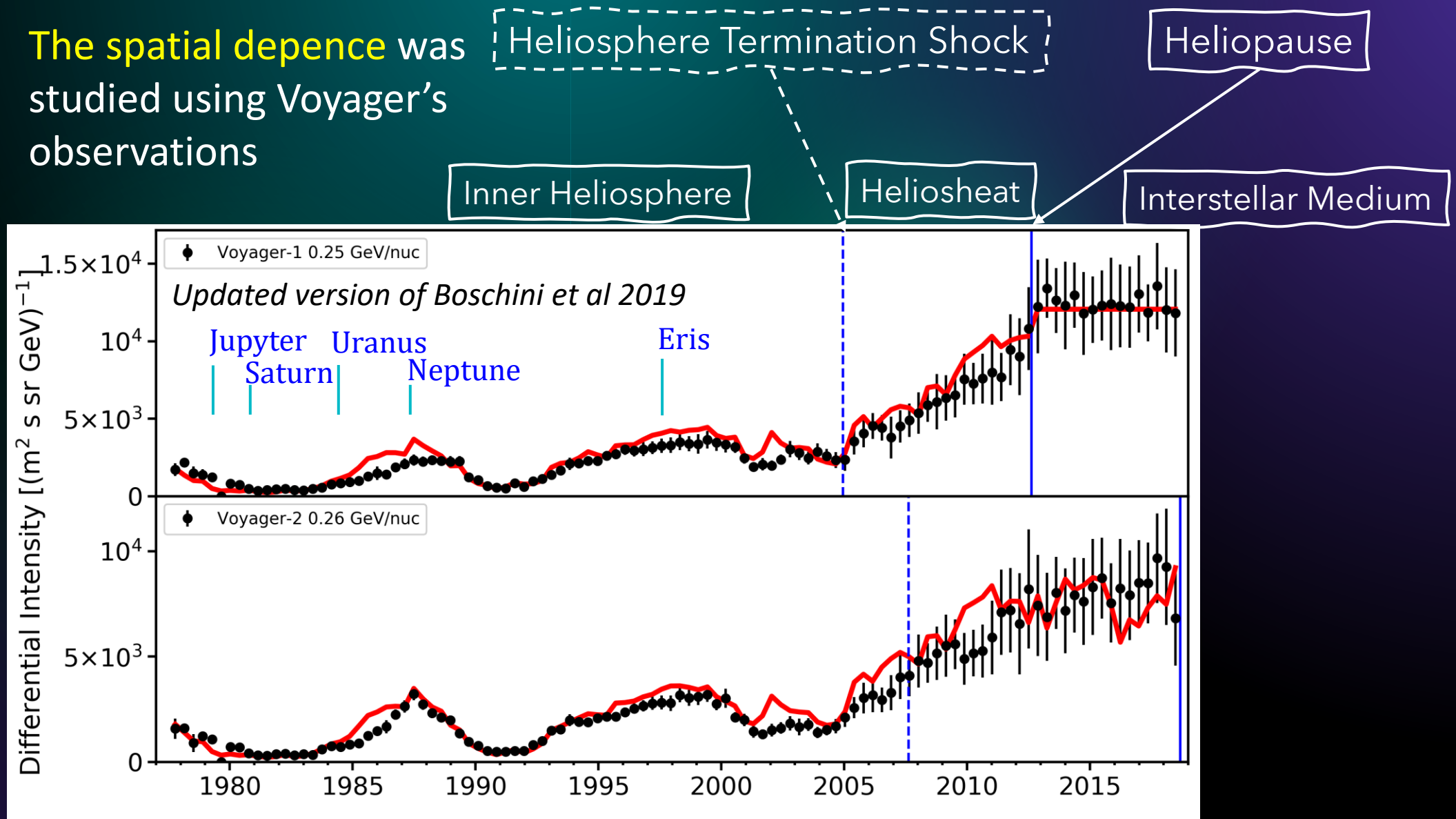
HelMod-4

We provide a web
(and offline) calculator
that allows a fast
calculation of solar
modulation for
selected parameters

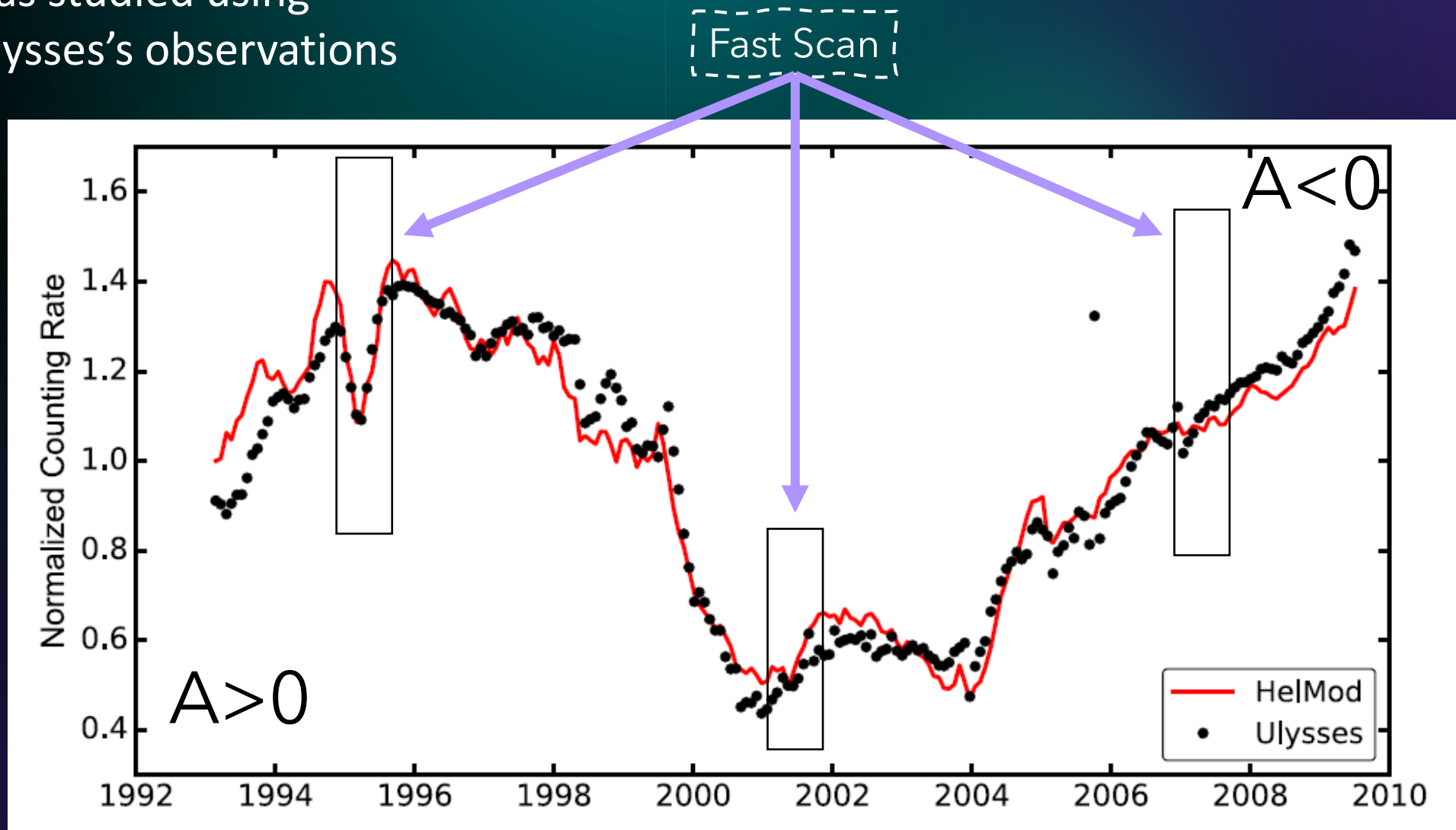
www.helmod.org

Solar Modulation Model	HelMod-4.1
<input type="radio"/> Expected Mission Duration	<input checked="" type="radio"/> Past Mission
Choose a dataset:	Select a Cosmic Rays Species: Select an Experiment: Select the dataset:
Galactic Cosmic Rays	
Local Interstellar Spectra	<input checked="" type="radio"/> LIS from Galprop-HelMod join effort <input type="radio"/> custom LIS - GALPROP Fits File <input type="radio"/> custom LIS - TXT File
Select LIS Version	Choose a GCR species
Display Options	
x-axis value:	<input checked="" type="radio"/> Auto <input type="radio"/> Particle Rigidity [GV] <input type="radio"/> Kinetic Energy/Nuc [GeV/nuc]
Additional modulation models:	<input type="checkbox"/> ISO 15390, DLR version <input type="checkbox"/> ISO 15390
Advanced controls	
Parameters	ρ_i : 0.065 g_{low} : 0.50 k_{hs} : 0.000030
Validate	

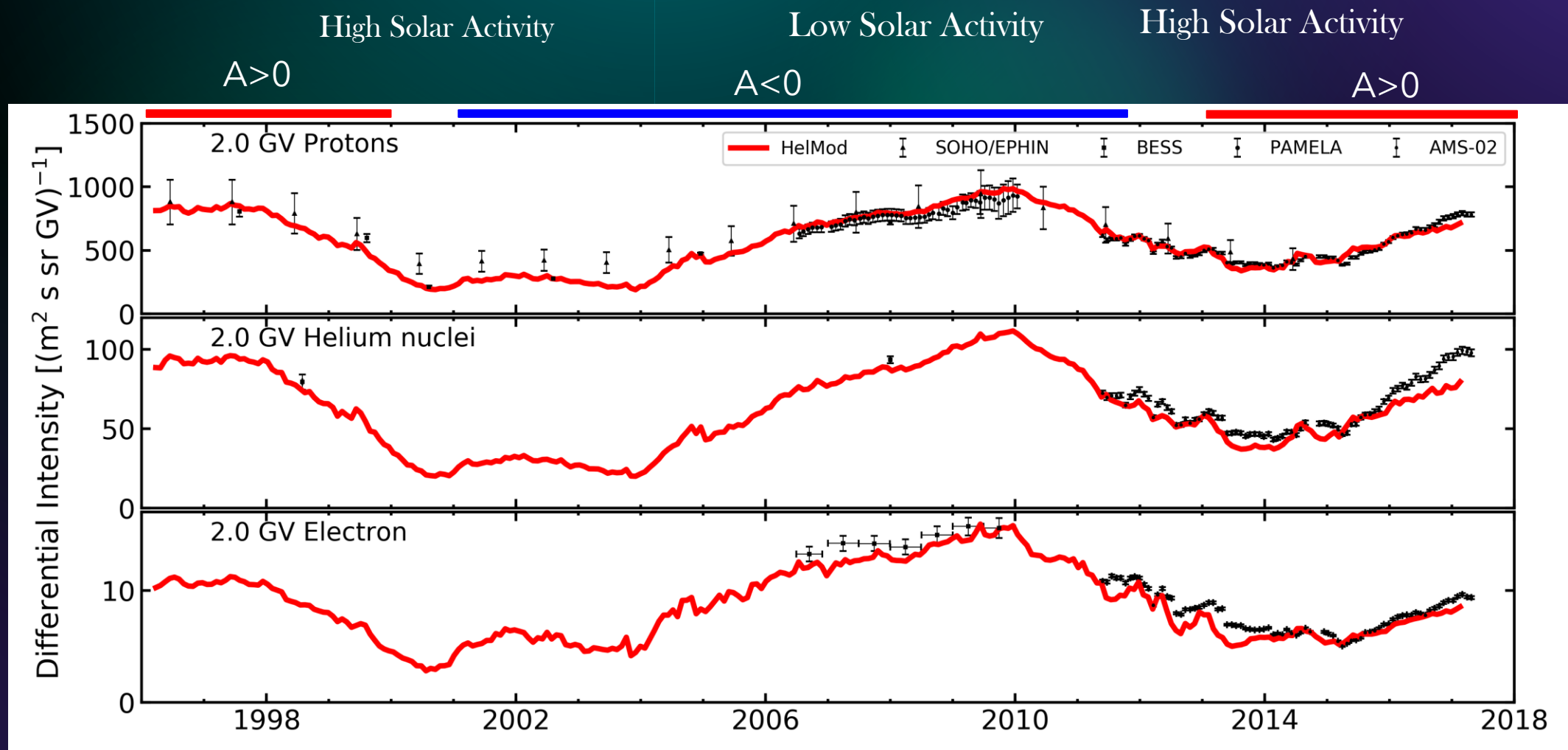
The spatial dependence was studied using Voyager's observations



The **Latitudinal Dependence**
was studied using
Ulysses's observations

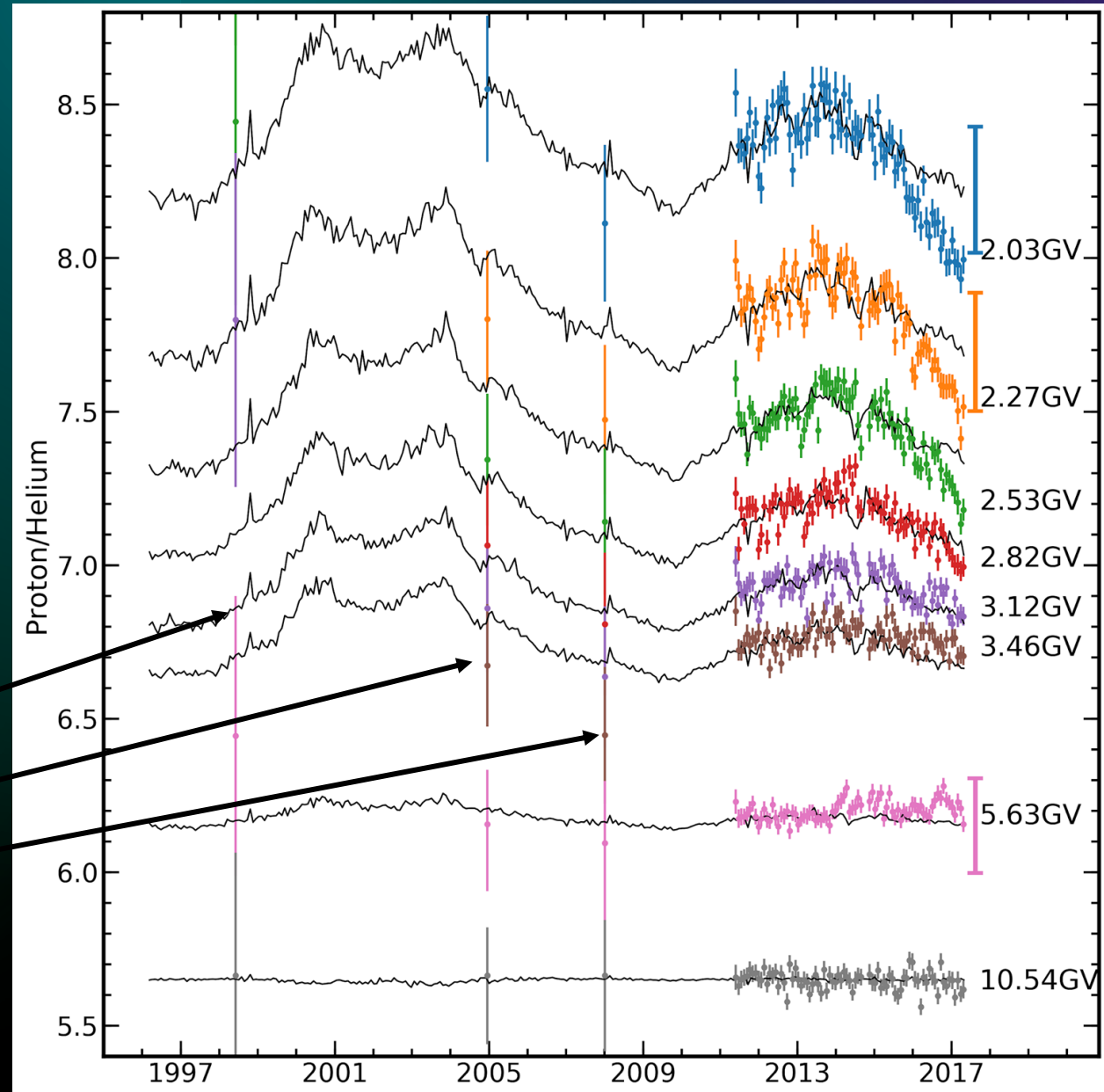


The Model can reproduce the **long-term variation of cosmic rays** along the full 22 years solar cycle.



p/He

AMS-01
BESS Polar I
BESS Polar II

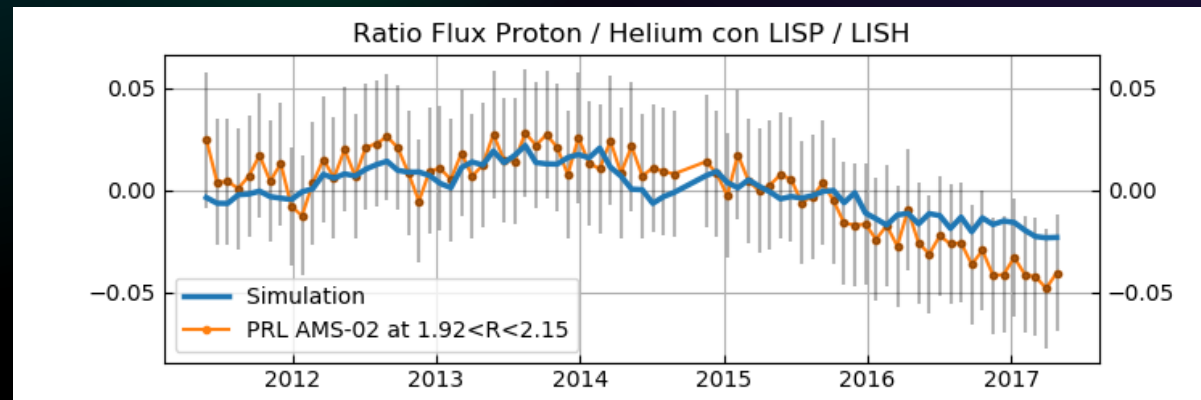
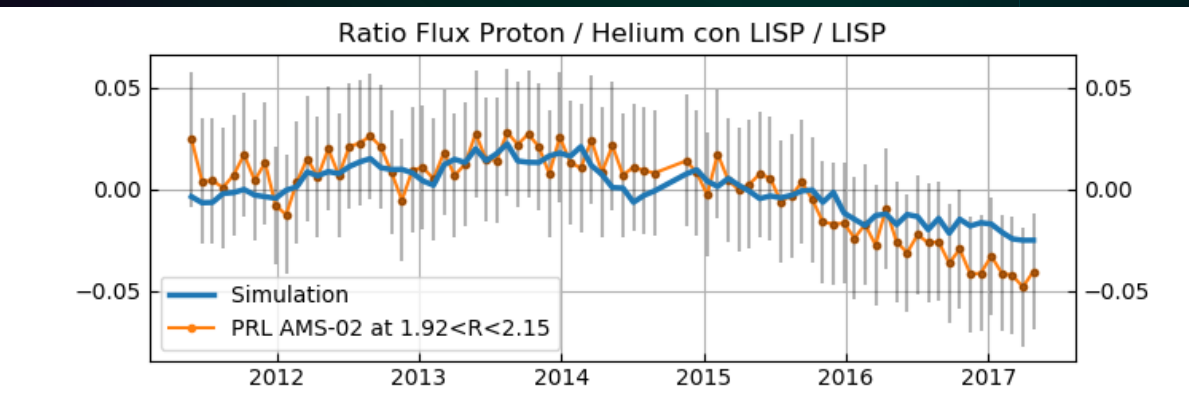
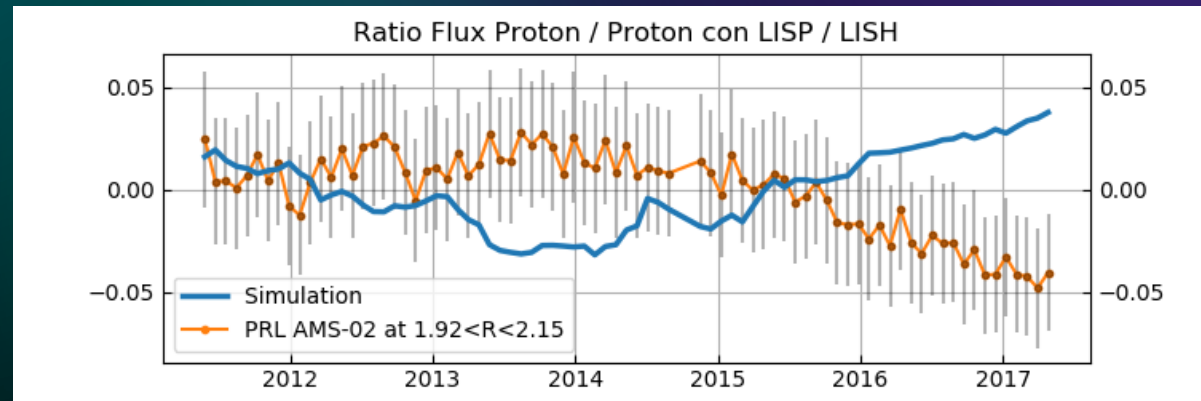
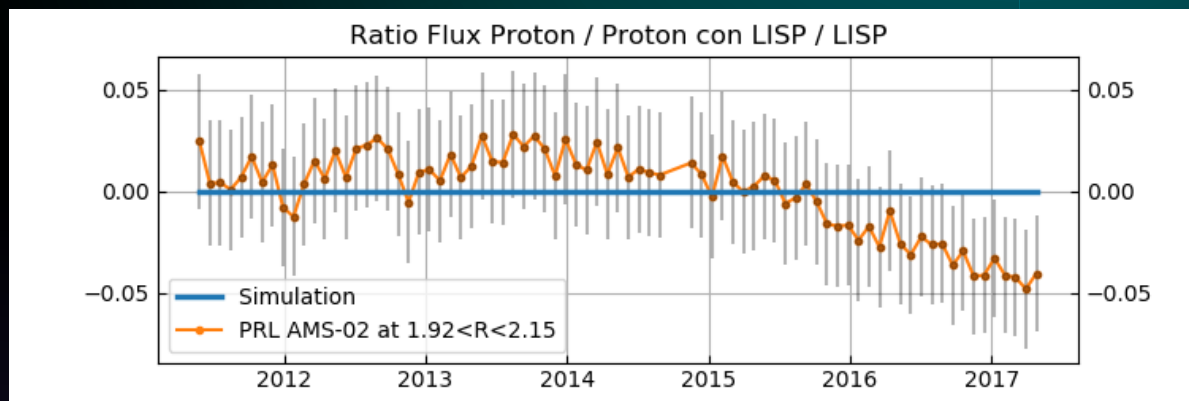


What can cause this time variation?

Proton LIS \rightarrow Helium LIS



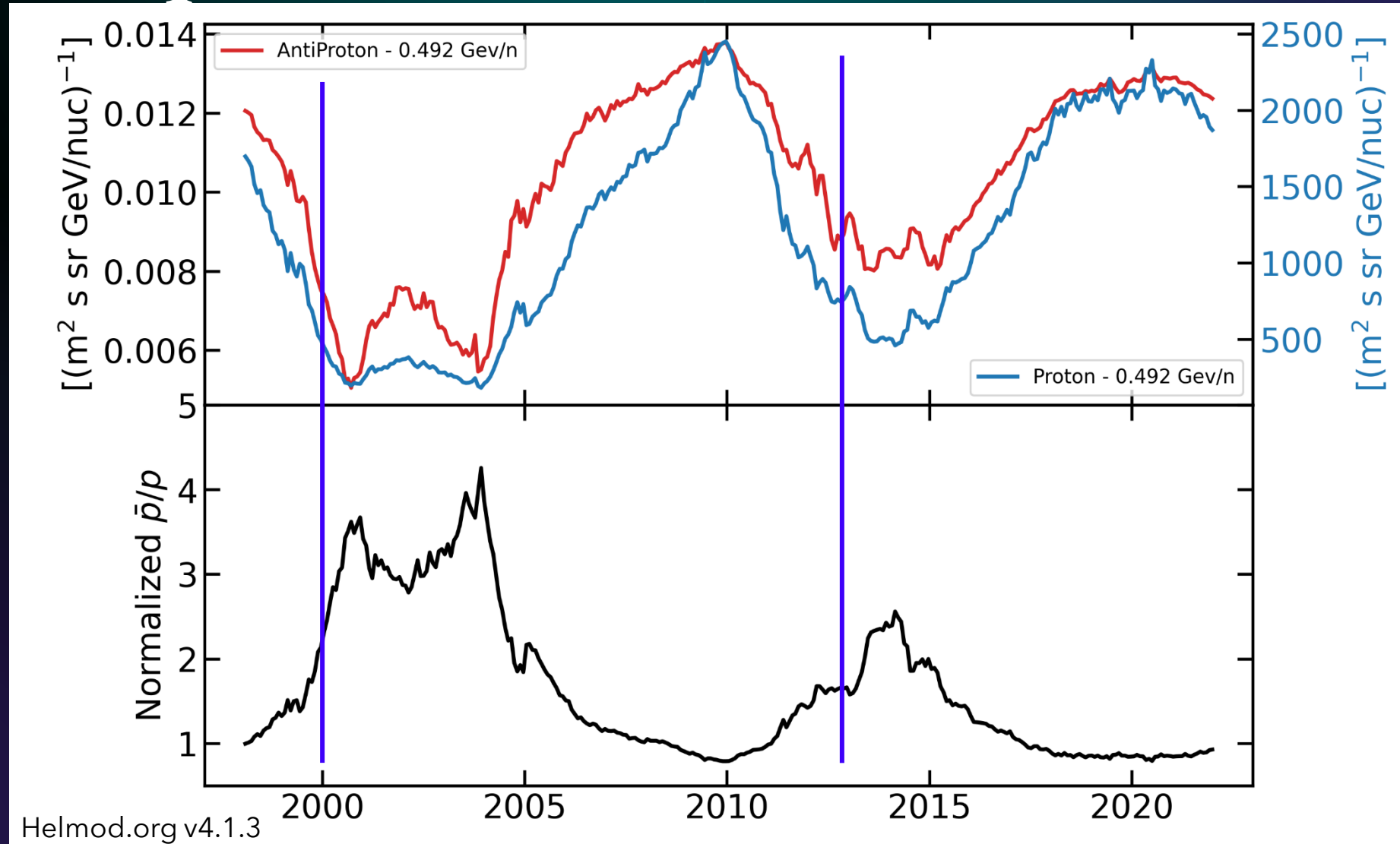
Proton \rightarrow Helium



On p/He the main contribution arise from different Z , but a contribution from LIS spectra cannot be neglected

Colella, Thesis 2019

Antiproton time variation



LIS determination

HelMod Monte Carlo Code and LIS: *GALPROP-HelMod framework*

HelMod is a Monte Carlo Code that evaluate modulated spectrum in the heliosphere for:

- *Protons*
- *Helium Nuclei*
- *Ions (Carbon, Oxygen,...,Nickel)*
- *Antiprotons*
- *Electrons*

The Local Interstellar Spectrum (LIS) were estimated using an iterative procedure involving GALPROP and HelMod

Propagation in
the Galaxy
galprop.stanford.edu



Describes all relevant process in the galaxy. It use as input:

- Injection spectrum
- Gas distribution
- Particle interaction cross section

As Output:

- LIS for all Ions outside heliosphere

Boschini et al. ApJ 840:115, 2017

Boschini et al. ApJ 854:94, 2018

Boschini et al. ApJ 858:61, 2018

Boschini et al. ApJ 889:167, 2020

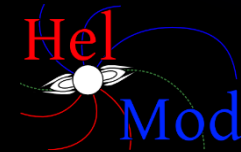
A summary for Ions with $Z \leq 28$

Boschini et al. ApJS 250:2, 2020

Boschini et al. ApJ 913:1, 2021

Boschini et al. accepted on ApJ, 2021

Propagation in the
Heliosphere
www.Helmod.org



Apply solar modulation to LIS as
function of solar activity

Before AMS-02

	Unit	Error (%)
z	kpc	50%
$D_0/10^{28}$	cm^2s^{-1}	100%
δ		60%
V_{Alfven}	km s^{-1}	90%
$V_{0\text{conv}}$	km s^{-1}	100%
dV_C/dz	$\text{km s}^{-1}\text{kpc}^{-1}$	100%

After AMS-02

Error (%)	Improvement factor $\epsilon_{\text{before}}/\epsilon_{\text{after}}$
8%	6
7%	14
6%	10
7%	13
6%	16
5%	20

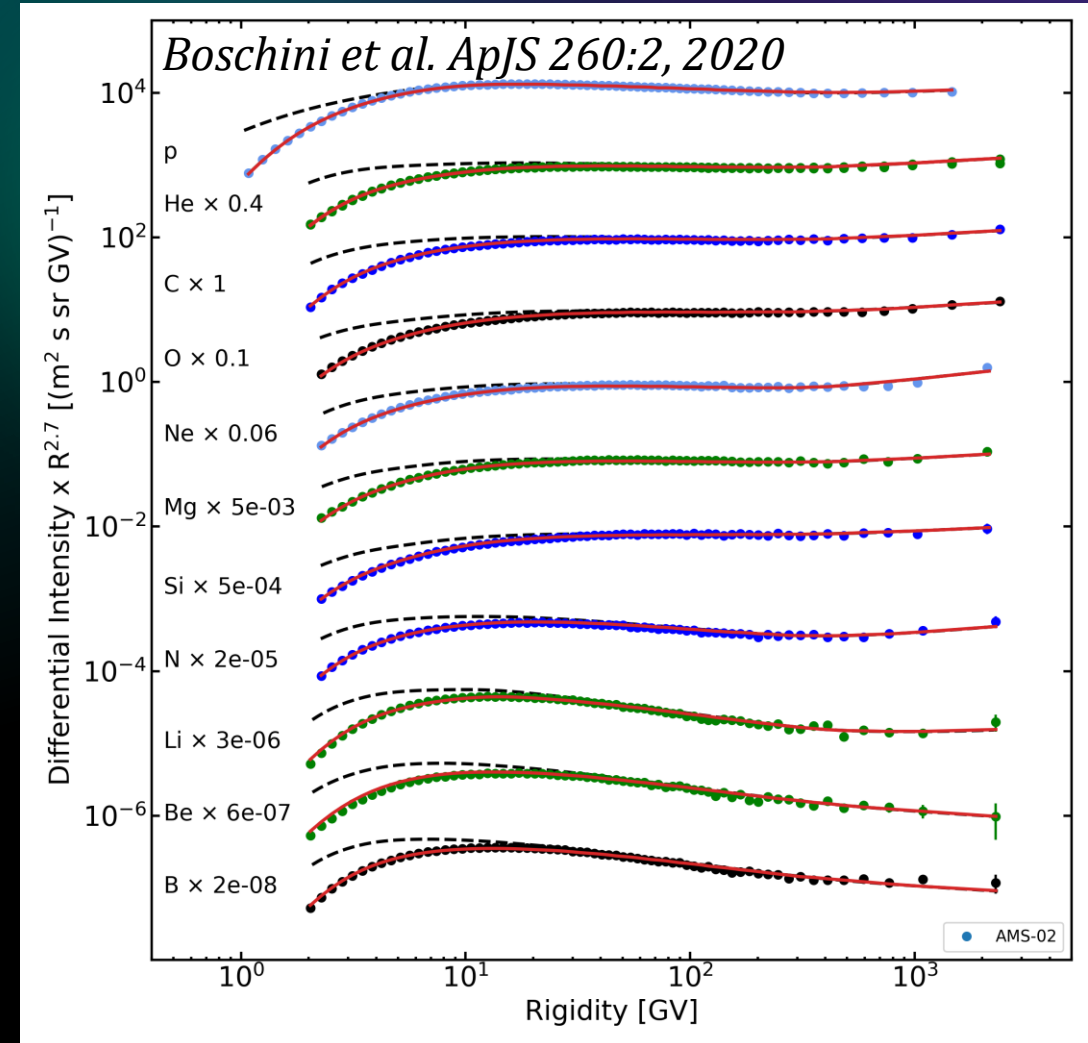
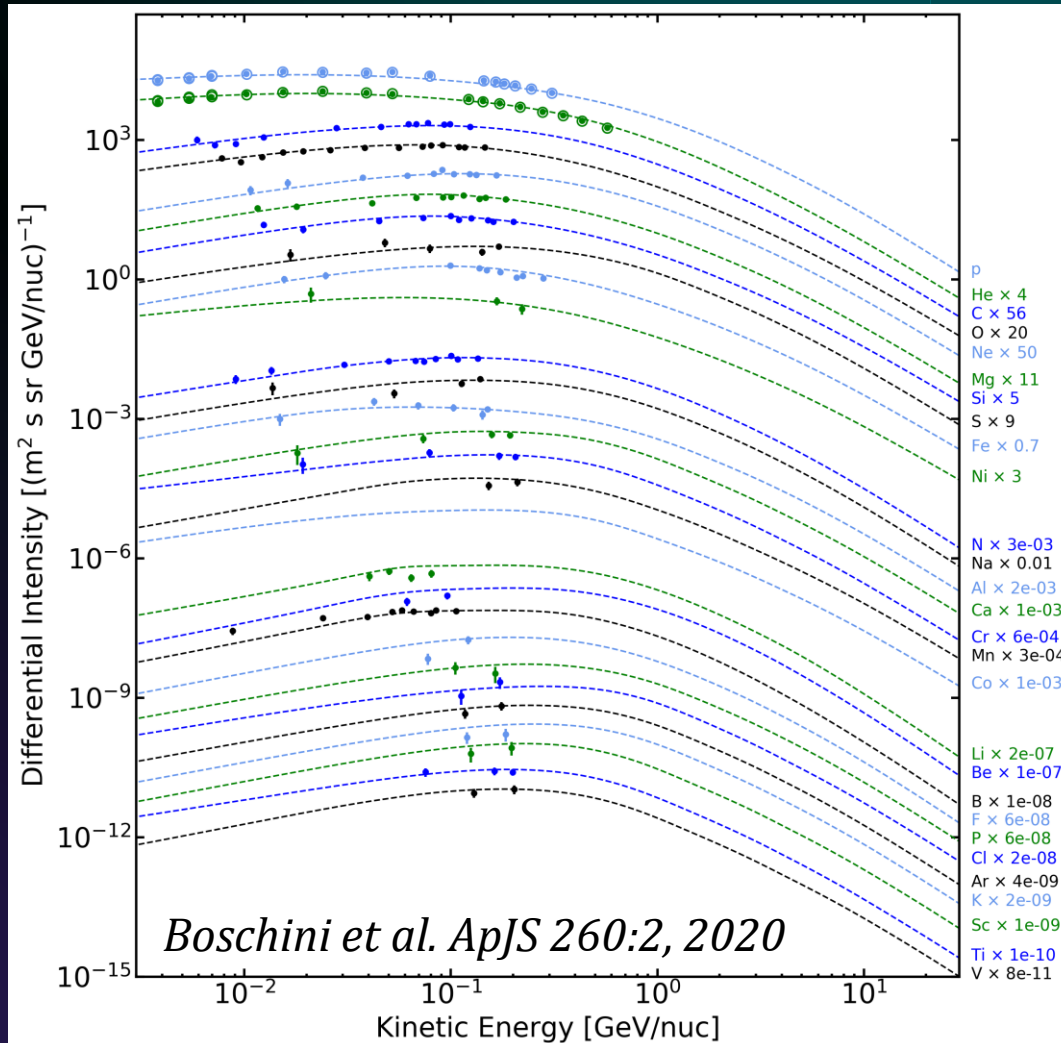
- Before AMS-02 we were not able to fix the CR propagation physics: **the parameters lied in very wide ranges.**
- With AMS-02 data is finally possible to achive a consistent best fit: **the errors associated to the fundamental propagation parameters z , D_{0xx} , $\delta_{1,2}$ are greatly reduced.**
- We still have some degeneracies/uncertainties which afflict secondaries predictions.

A factor 10 of improvement
for fundamental parameters

N. Masi 2017

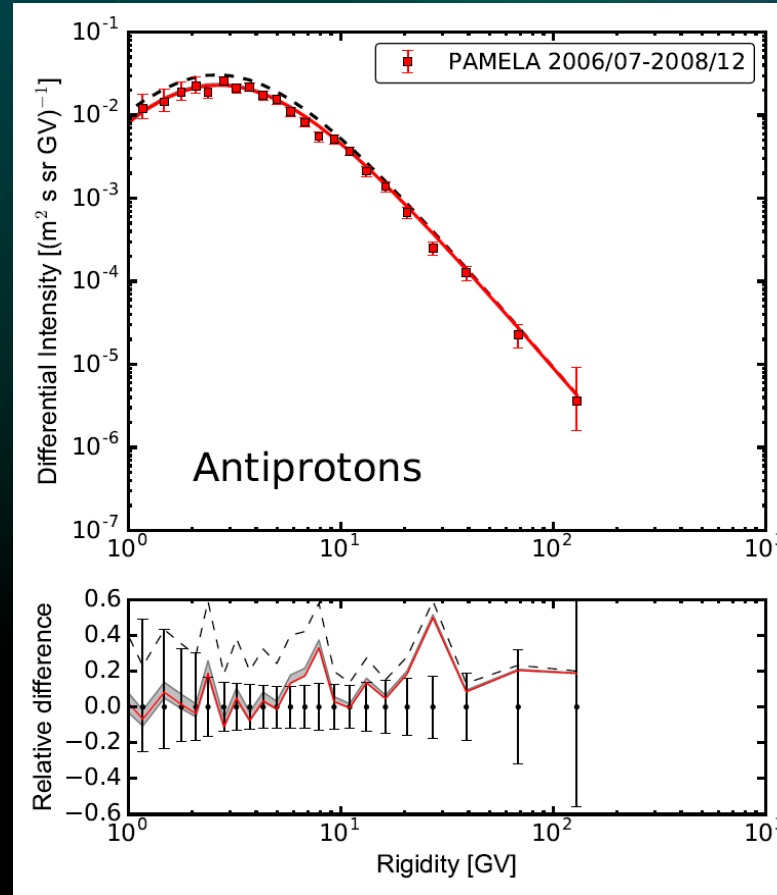
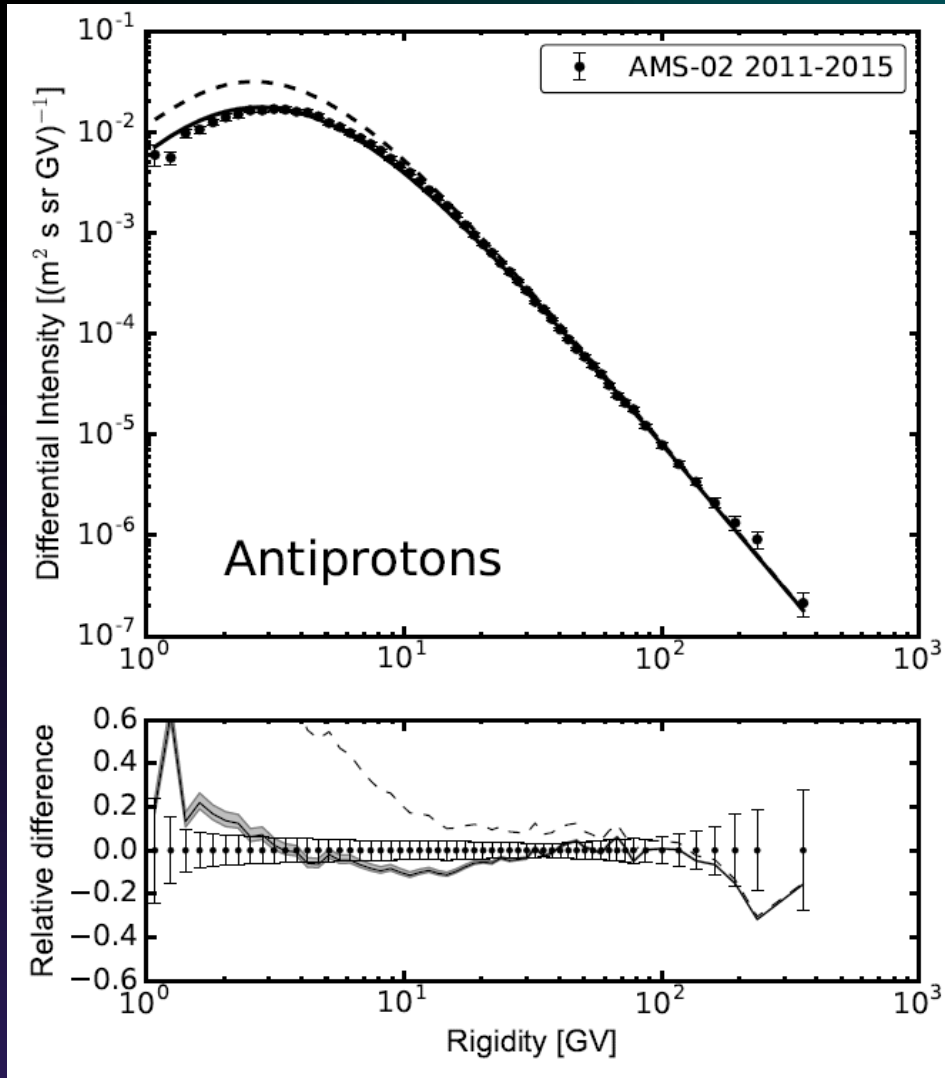


The physically motivated **Local Interstellar Spectra** were inferred from an **iterative procedure** was developed to feed the **GALPROP output into HelMod** to compare with AMS-02 and Voyagers **data as observational constraints**



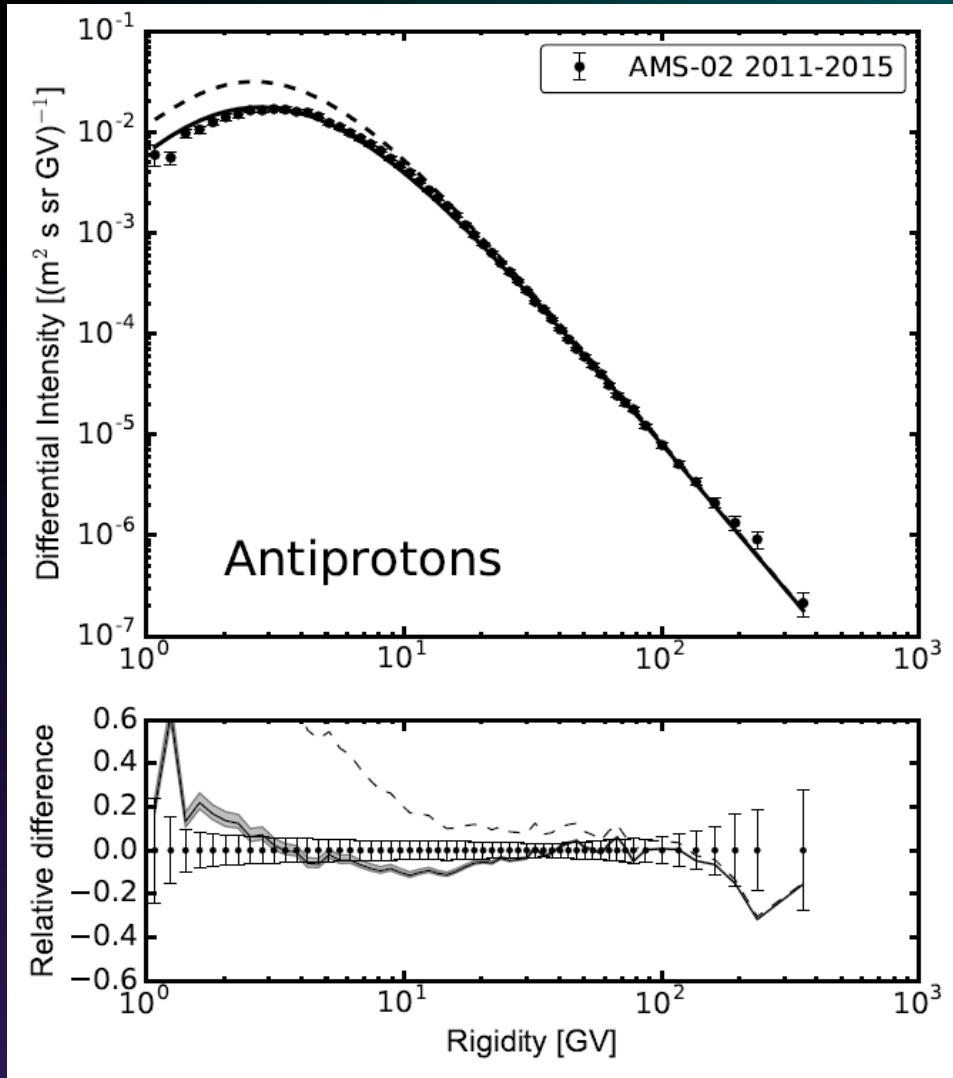
Antiproton

Secondary antiproton production in pp-, pA- and AA-interactions is calculated using the results of QGSJET-II_m (Kachelriess et al. 2015), a dedicated version of the QGSJET-II hadronic interaction model, while inelastically scattered protons and antiprotons are treated as "secondary" protons and "tertiary" antiprotons, respectively.



The obtained Antiproton LIS was NOT constrained with data.

Antiproton

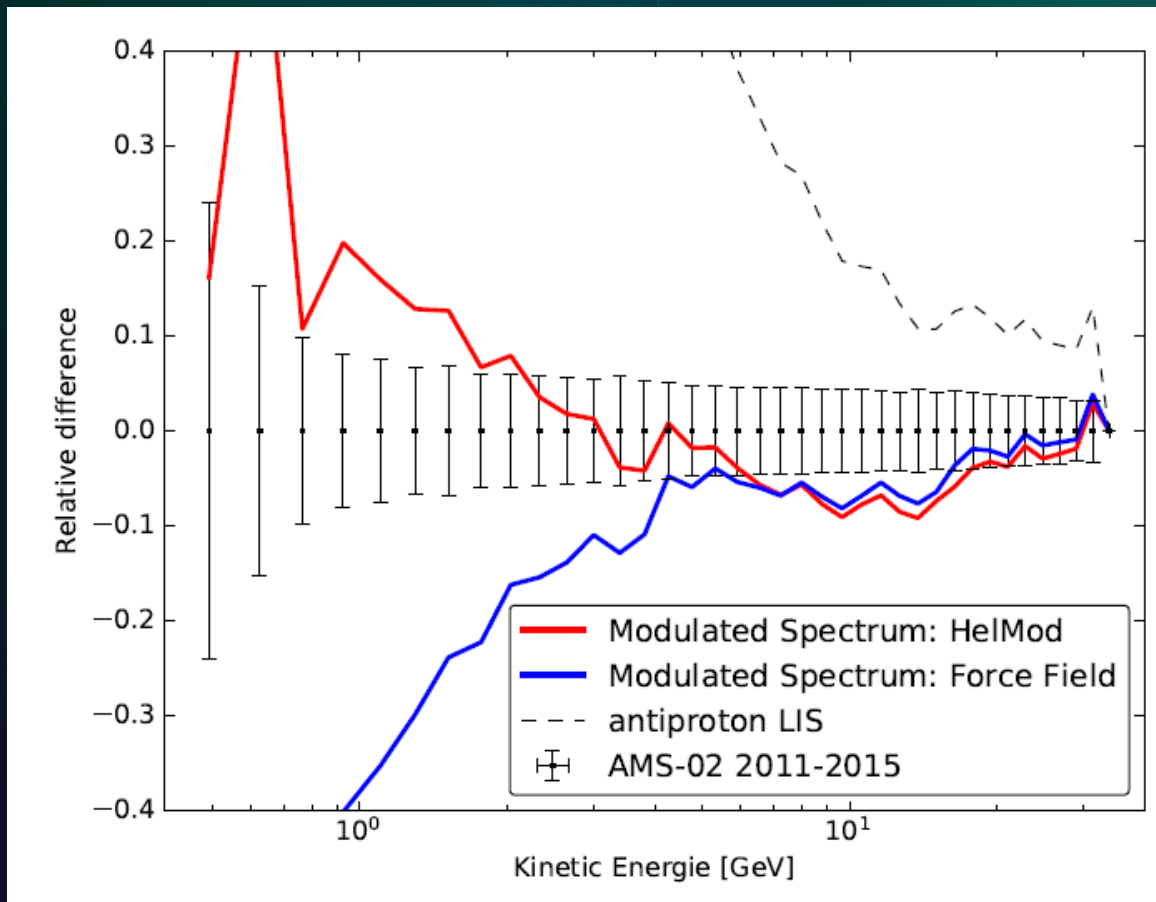


The Antiproton LIS is substantially compatible with AMS-02.

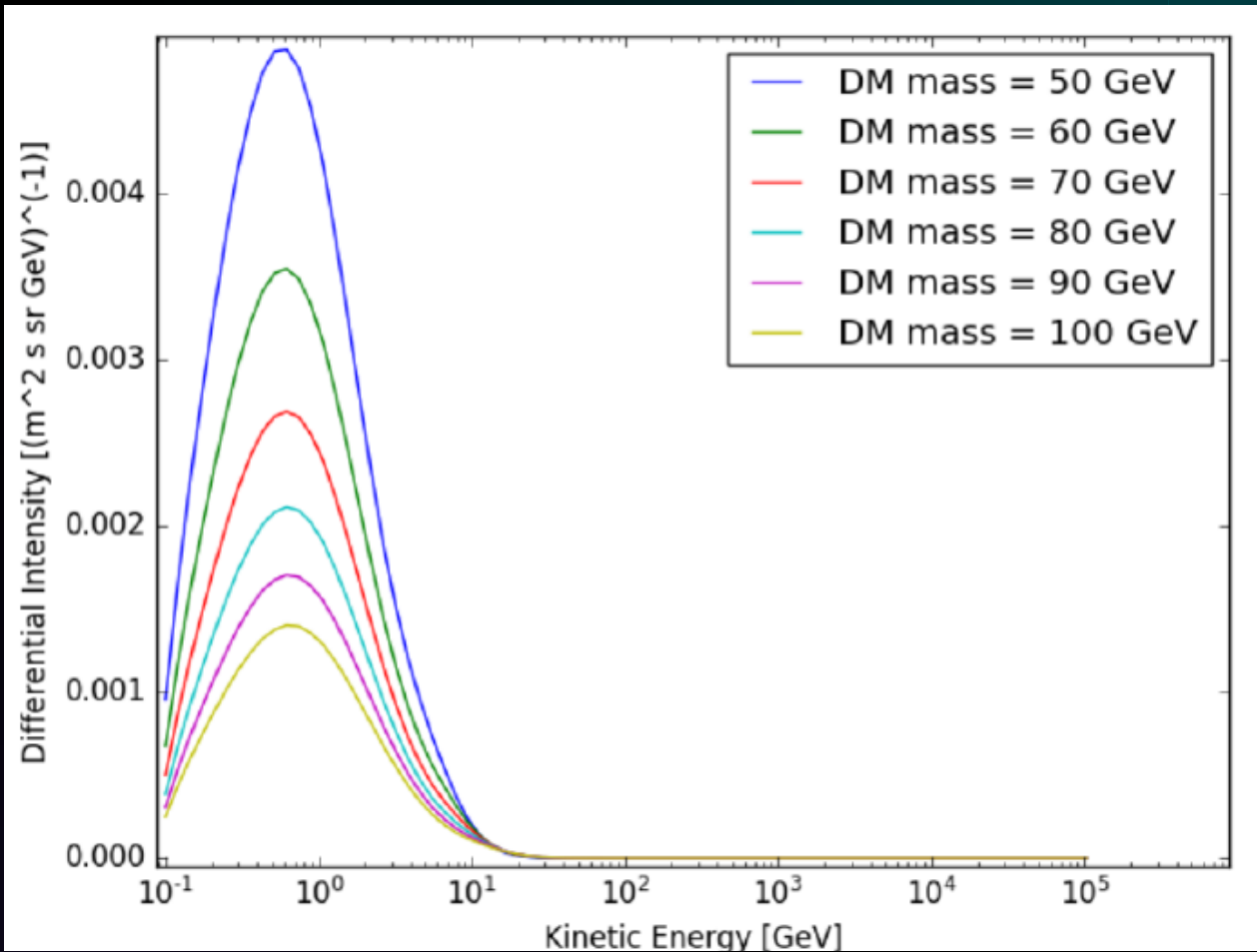
Tiny discrepancies w.r.t. AMS-02 high precision data could be due to:

- Nuclear cross section uncertainties
- Peculiar propagation effects or variation of primary p and He spectra in the Galaxy

Effect on using different Solar modulation model



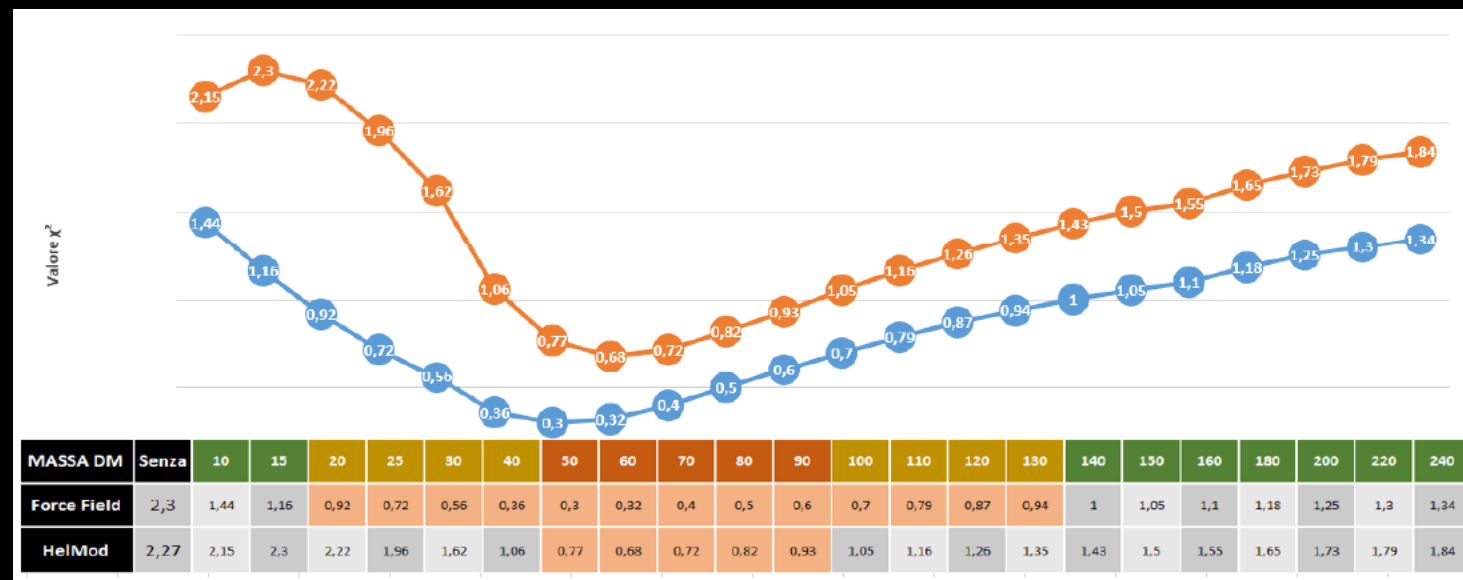
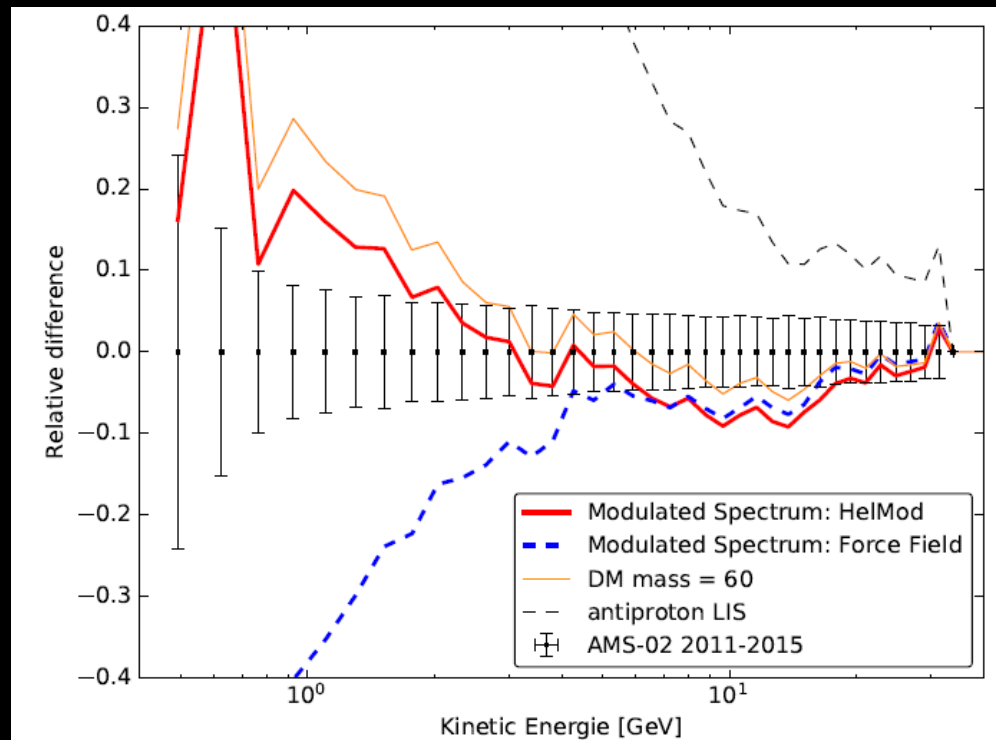
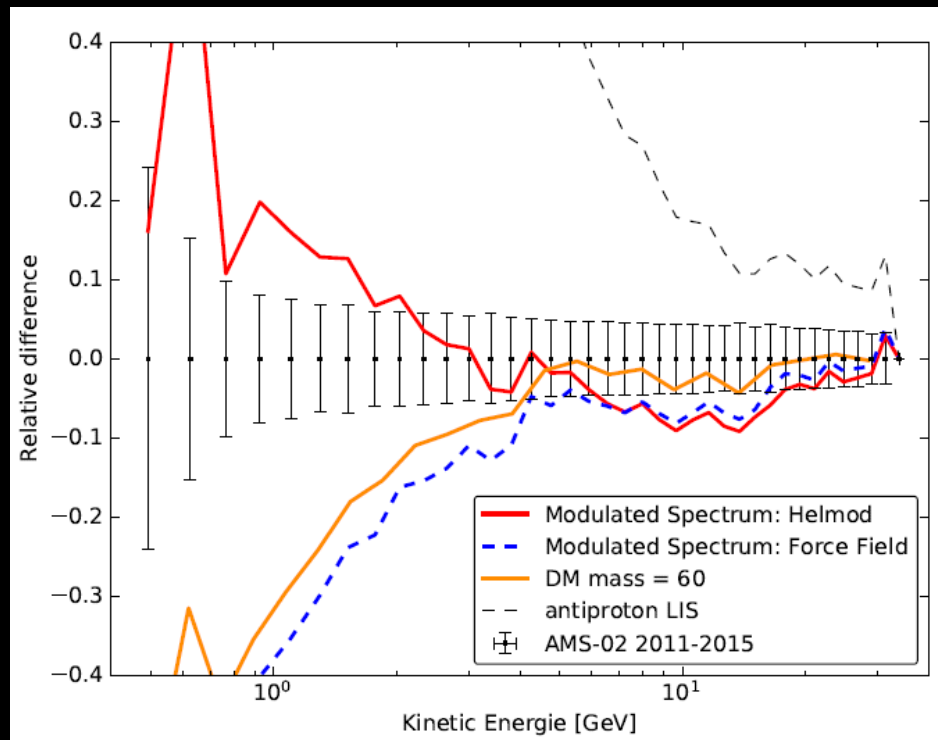
Carella, Thesis 2019



We tested an antiproton produced by $b\bar{b}$ channel similar the one in

- Cuoco et al 2019
- Cholis et al 2019
- ...

Carella, Thesis 2019



The use of HelMod more constrain the mass range for DM candidate

Conclusions

- Dealing with low energy antiproton the major (yet) unsolved issues comes from **Nuclear Uncertainties**.
- The choice of the **solar modulation model is important** in the search of exotic signal.
- As far as new data are available, solar modulation model are constrained and becomes more reliable.