

Heavy Flavour Physics Workshop

Sapienza, Università di Roma, 17 Feb 2020

Semileptonic Decays: recent results and opportunities

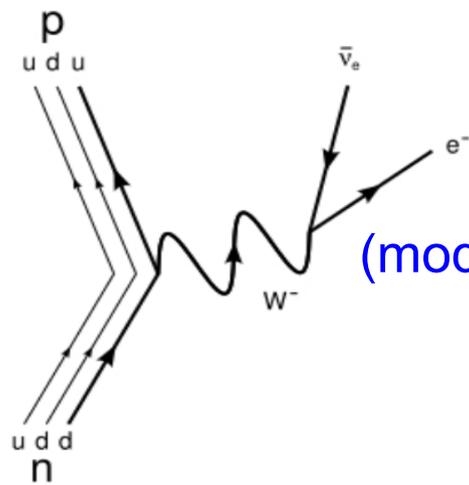
Marcello Rotondo

Laboratori Nazionali di Frascati



Semileptonic decays

Nucleon β -decays



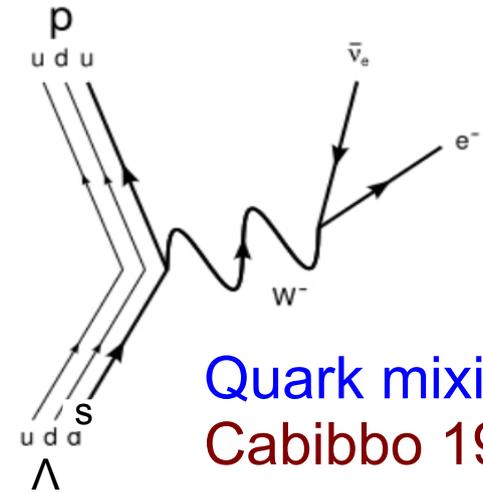
Fermi 4-body interaction

$$G_F \approx 1.17 \times 10^{-5} \text{GeV}^{-2}$$

(modern language) W-boson exchange

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8m_W^2}$$

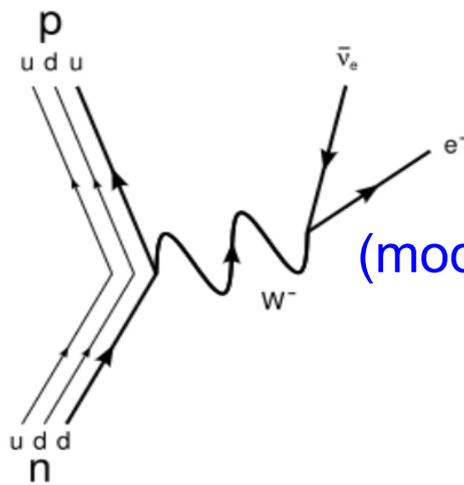
Hyperon semileptonic decays



Quark mixing:
Cabibbo 1961

Semileptonic decays

Nucleon β -decays



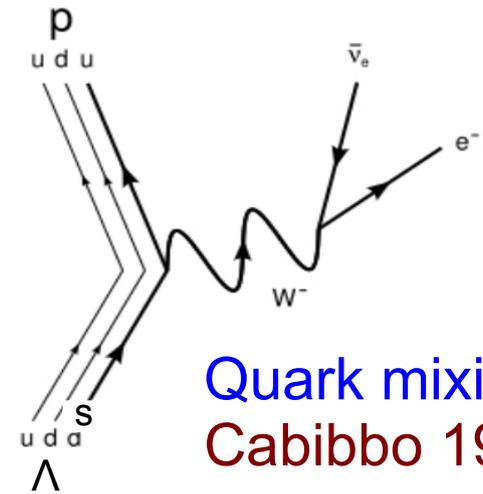
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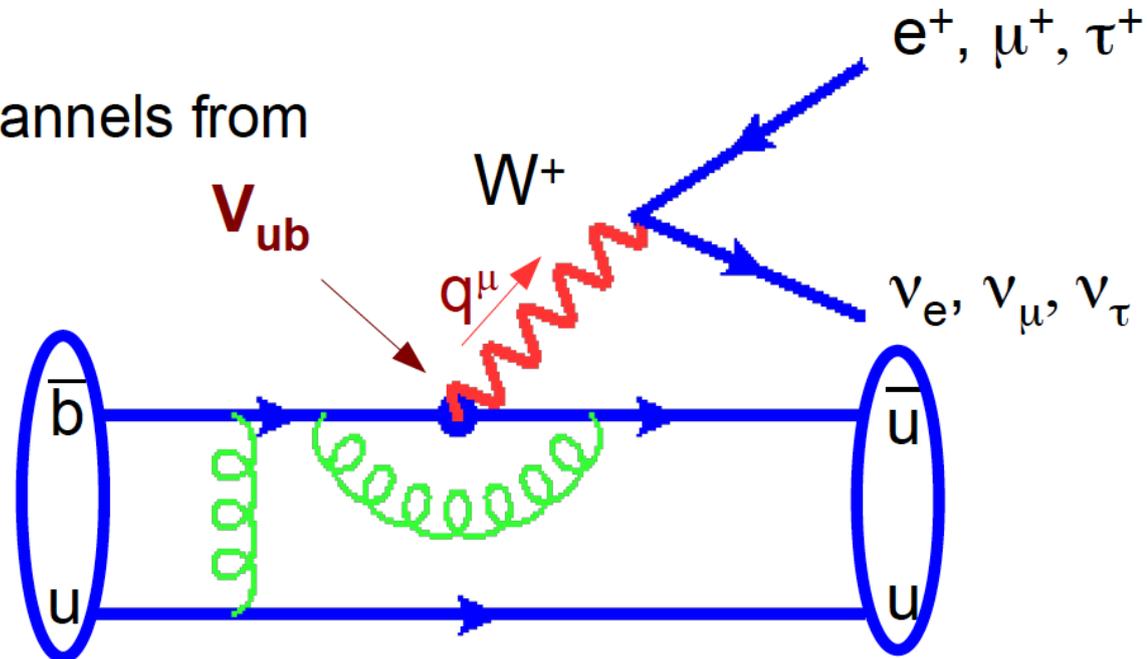


Quark mixing:
Cabibbo 1961

- Semileptonic decays are clean channels from theoretical point of view:

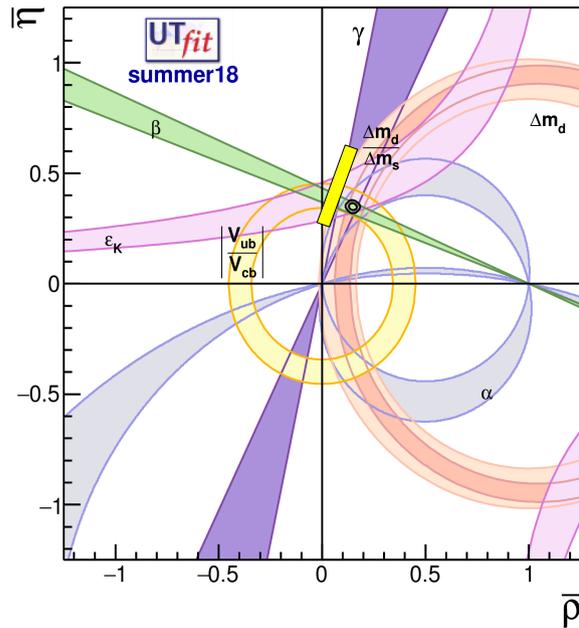
$$\mathcal{M}(B \rightarrow \pi \ell^- \bar{\nu}) = -i \frac{G_F}{\sqrt{2}} \cdot V_{ub} \cdot L^\mu H_\mu$$

- Factorization of the hadronic and leptonic current: no final state interactions

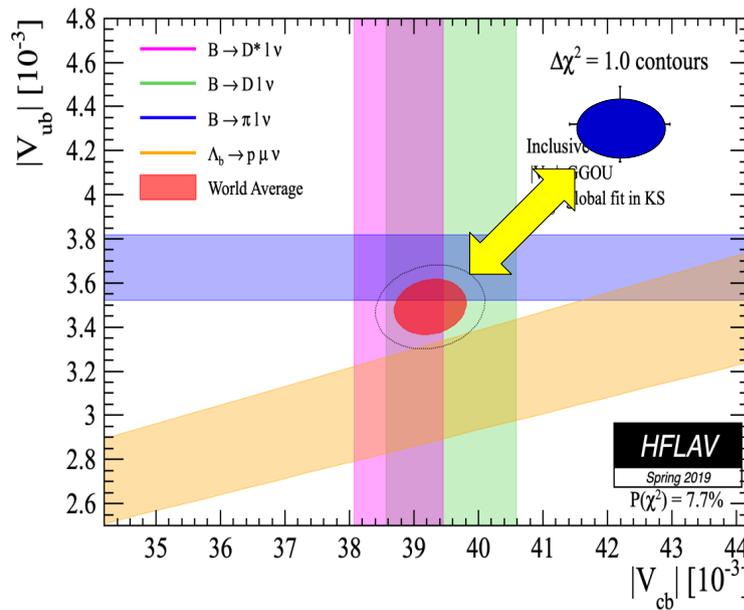


Why semileptonic B decays ?

... at least three reasons:

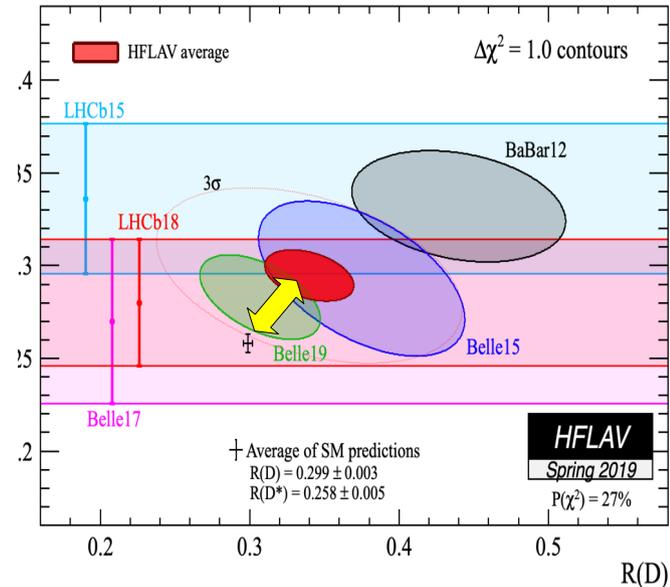


$|V_{xb}|$ provide crucial inputs for indirect search of New Physics



$|V_{ub}|$ and $|V_{cb}|$ discrepancies between different determinations: 3σ effect

$$\frac{\Gamma(B \rightarrow D^{(*)} \tau \nu_\tau)}{\Gamma(B \rightarrow D^{(*)} \ell \nu_\ell)}$$

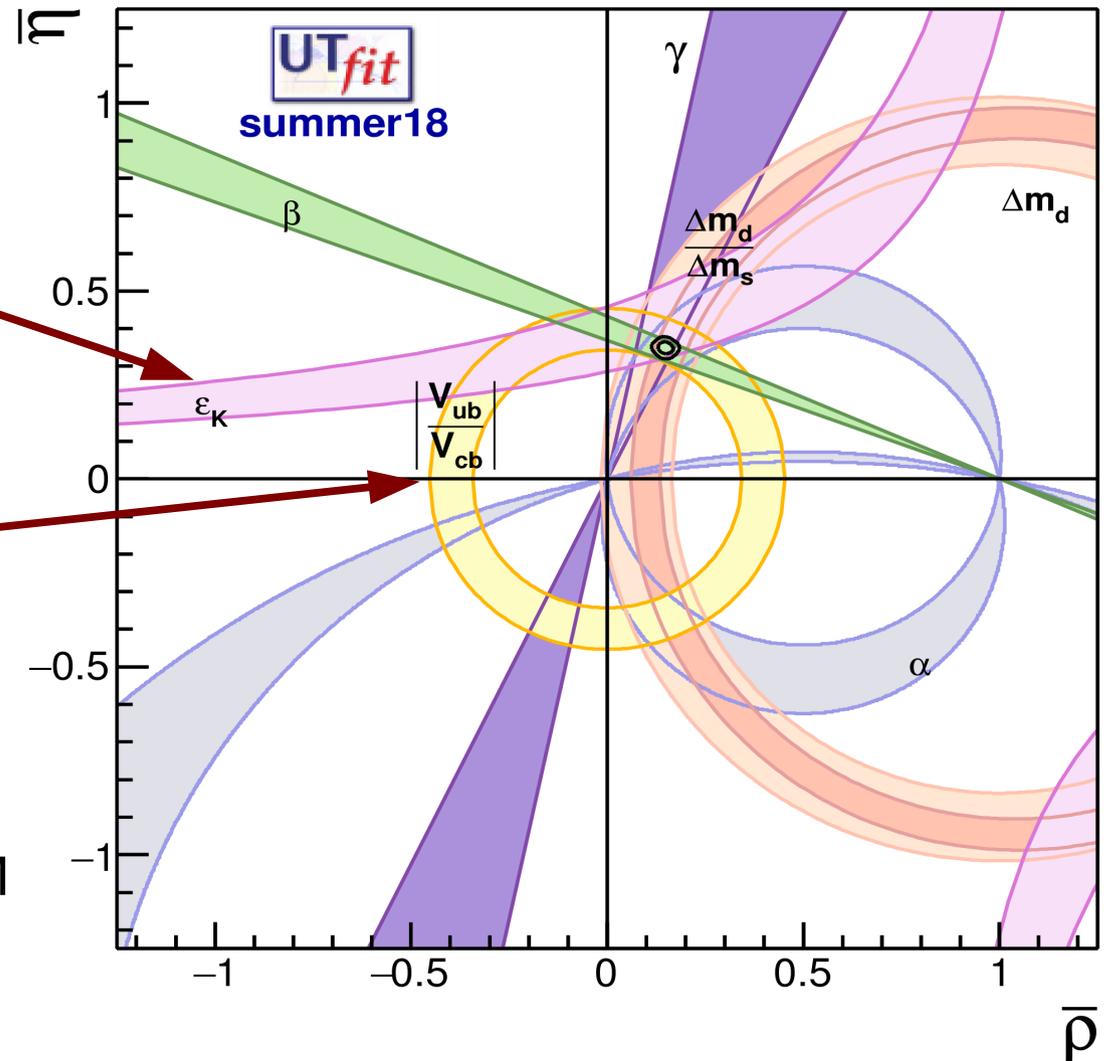


Difference with expectations @ about 3σ

UT Status (Summer 2018)

- Prediction of FCNC processes $\propto |V_{tb}V_{ts}|^2 \approx |V_{cb}|^2[1 + O(\lambda^2)]$

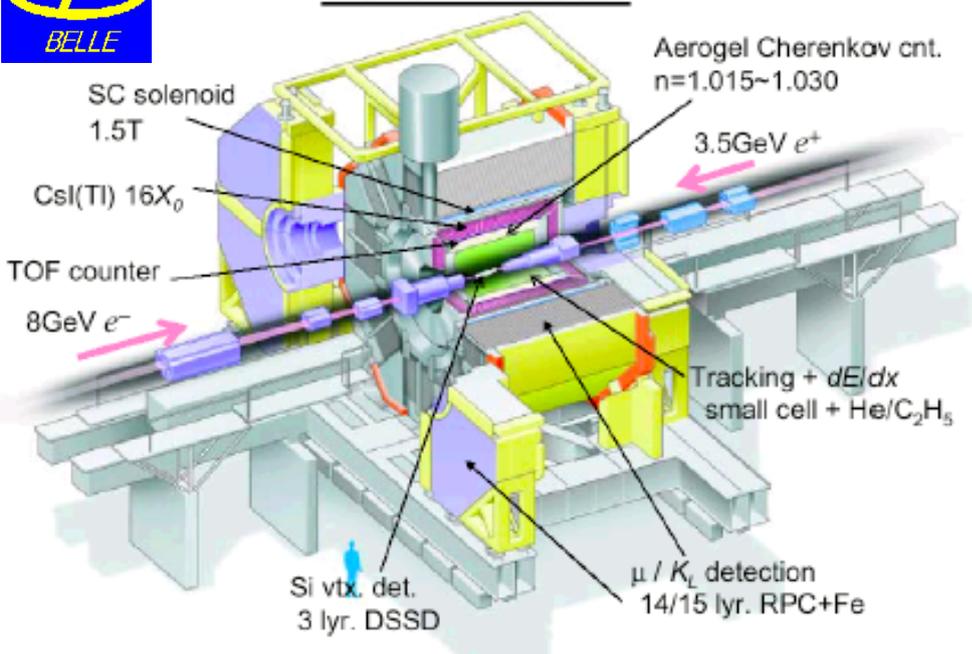
- $|V_{cb}|$ plays an important role in the determination of UT
 - $\epsilon_K \approx x|V_{cb}|^4 + \dots$
- $|V_{ub}|$ is the side opposite to angle β
 - Tree level .vs. loops
- It is the smallest CKM matrix element:
 - It could be more sensitive to any small violation of the CKM paradigm



Experiments: B-Factories



Belle Detector

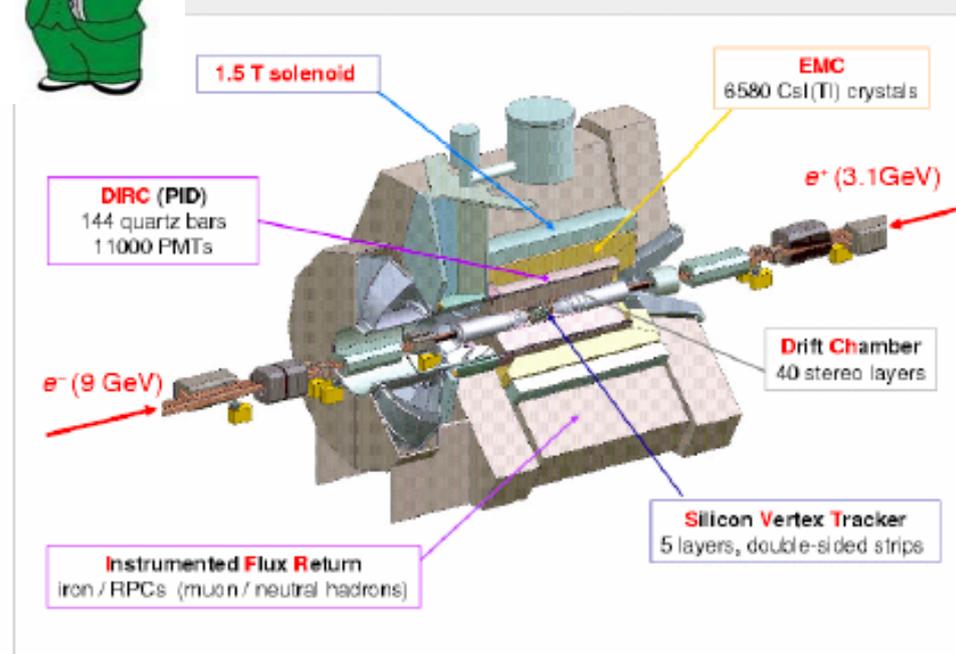


@ KEK Japan: 1999-2009



The BABAR Detector

BABAR, NIMA479.1 (2002.1)



@ SLAC: 1999-2008

B-Factories: hermetic detectors, low background, access (mainly) at $B^{0/+}$

About $(771 + 467) \times 10^6$
 $e^+e^- \rightarrow$ BB events in
 the Belle+BaBar data

Belle and KEK is being upgraded

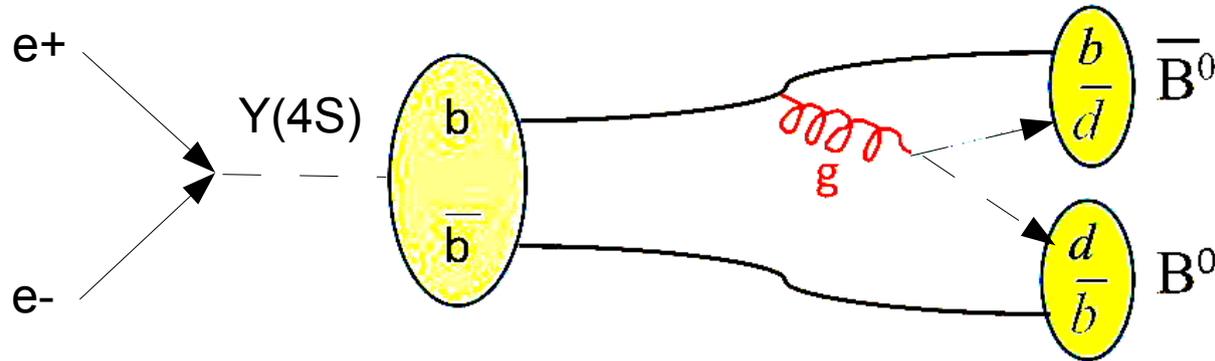


Belle-II will collect
 50 ab^{-1} by ~2026

B-hadron production

$$\mathcal{N} \propto \mathcal{L} \cdot \sigma$$

- B-Factories: e^+e^- running at $\sqrt{s} \sim 10.58$ GeV



$$\sigma(e^+e^- \rightarrow \Upsilon(4S)) = 1.06 \text{ nb}$$

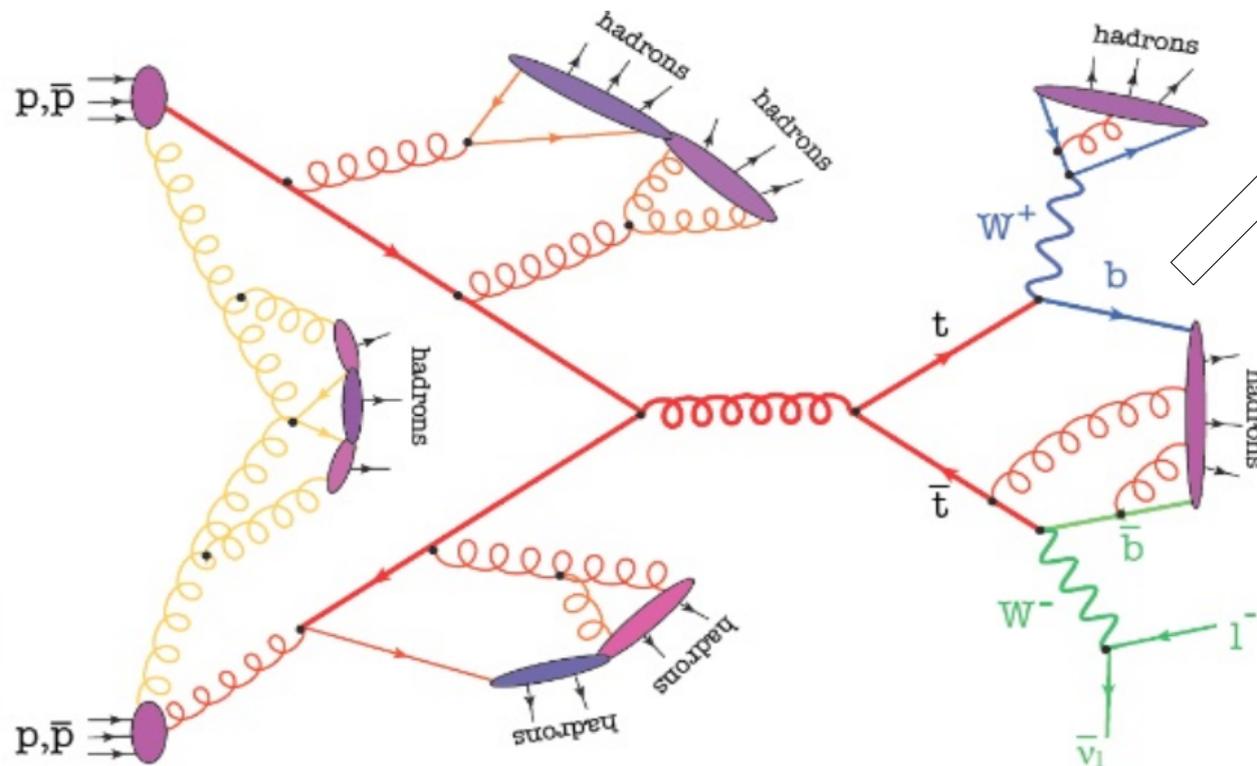
$$BF(\Upsilon(4S) \rightarrow B\bar{B}) \approx 100\%$$

BaBar: 430 fb^{-1}

Belle: 640 fb^{-1}

Belle-II expected 50 ab^{-1}

- Hadron machines: high energy pp (or $p\bar{p}$) collision



b-hadrons

$$\sigma(pp \rightarrow b\bar{b})_{7 \text{ TeV}} \approx 295 \cdot 10^3 \text{ nb}$$

$$\sigma(pp \rightarrow b\bar{b})_{13 \text{ TeV}} \approx 600 \cdot 10^3 \text{ nb}$$

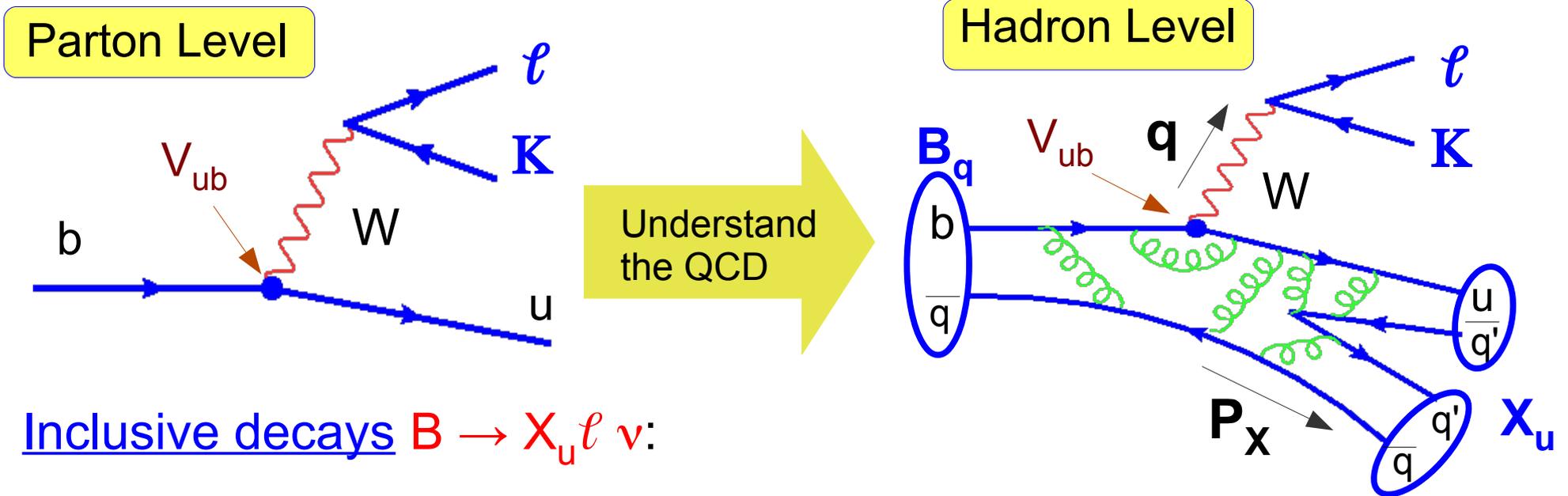
The b-quarks can hadronize in any kind of b-hadron

$B_d, B_u, \Lambda_b, B_s, \Xi_b, \Sigma_b, \Omega_b, B_c \dots$

LHCb: $3 \text{ fb}^{-1} + 6 \text{ fb}^{-1}$

IV_{ub}l

Measurements of $|V_{ub}|$



- Inclusive decays $B \rightarrow X_u \ell \nu$:
 - Need to know QCD corrections to parton level decay rate
 - Operator Product Expansion predicts the total rate Γ_u
- Exclusive decays $B \rightarrow \pi \ell \nu / \rho \ell \nu$
 - QCD effects are embedded in the form factors

$$\frac{d\mathcal{B}(B \rightarrow \pi \ell \nu)}{dq^2} = |V_{ub}|^2 \frac{G_F^2 \tau_B}{24\pi^3} p_\pi^3 |f_+^{B\pi}(q^2)|^2$$

Leptons are considered massless: only one FF $B \rightarrow \pi$

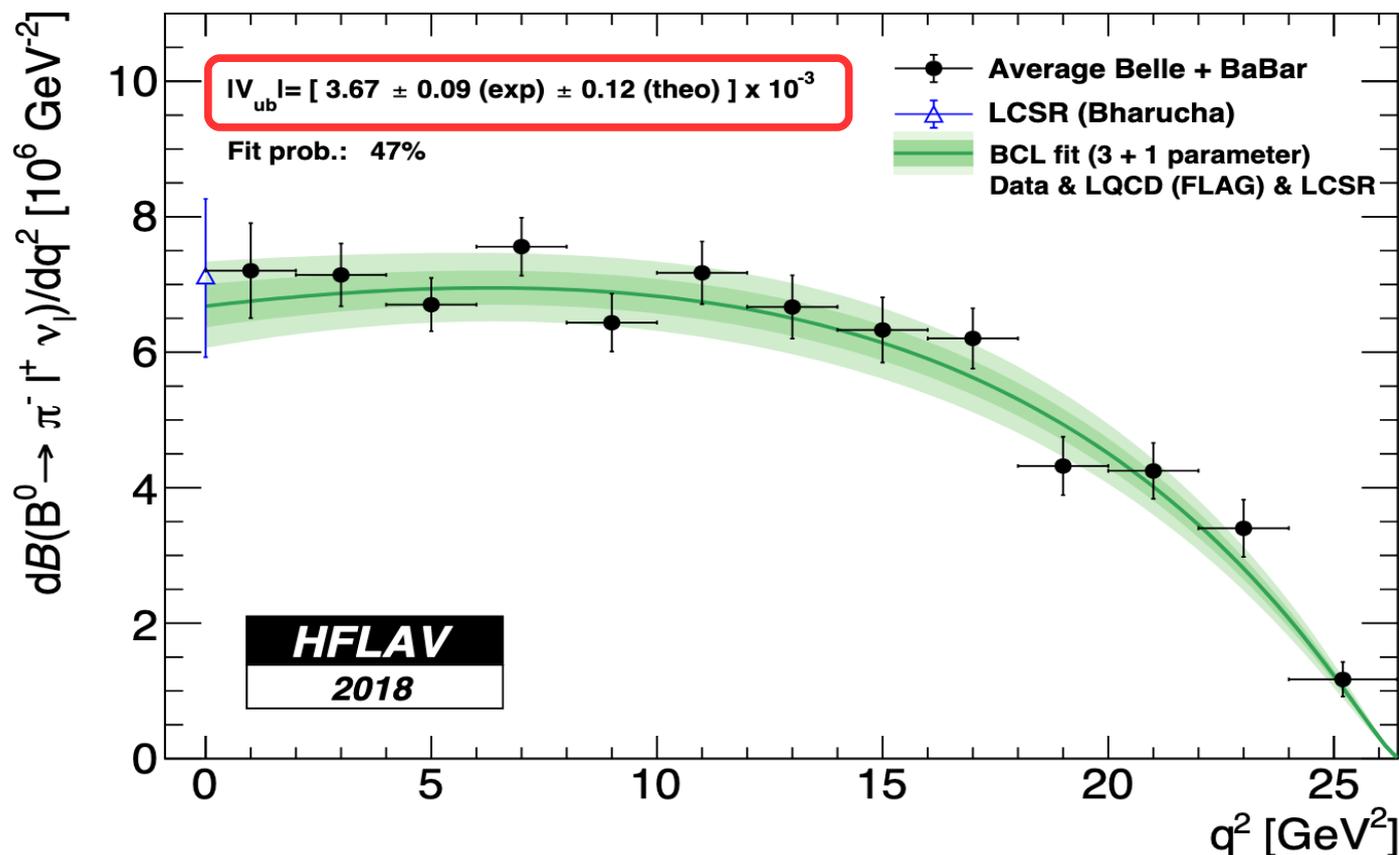
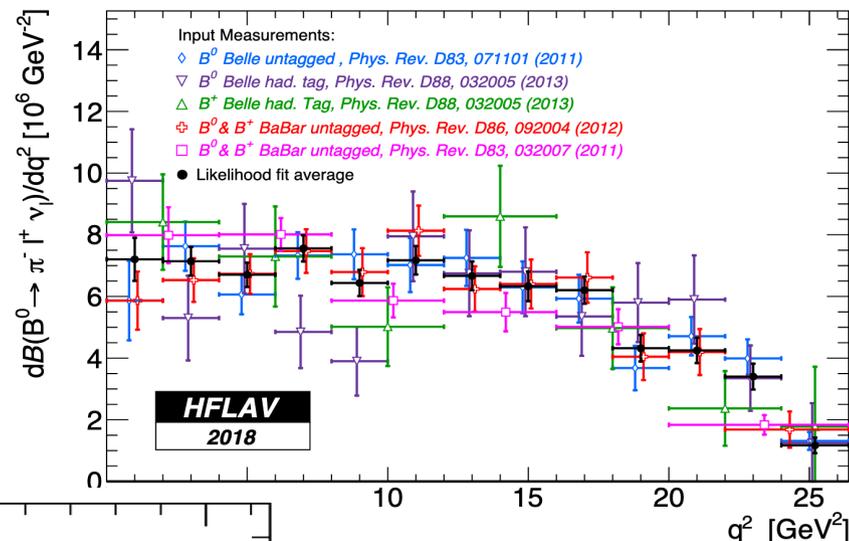
The state of the art at the B-Factories

$$B^0 \rightarrow \pi^+ \ell^- \bar{\nu}$$

$$B^- \rightarrow \pi^0 \ell^- \bar{\nu}$$



- 1) Many different experimental measurements:
Tagged and untagged
- 2) Signal extracted in bins of q^2

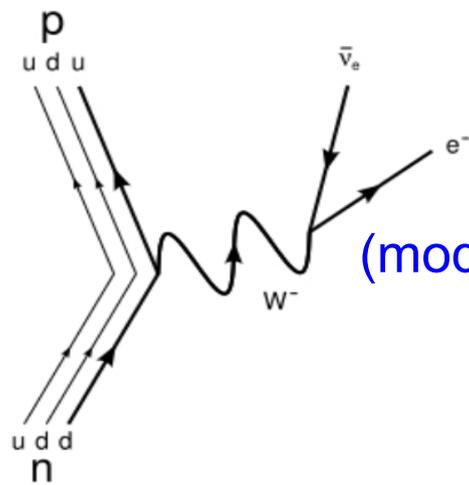


Results of the HFLAV combined fit of the experimental data and theoretical inputs:

- Lattice QCD (HPQCD, FNAL,...) at high q^2
- light Cone Sum Rules at low q^2

Semileptonic decays

Nucleon β -decays



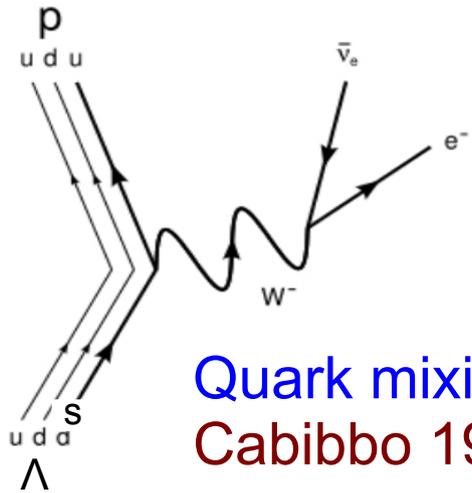
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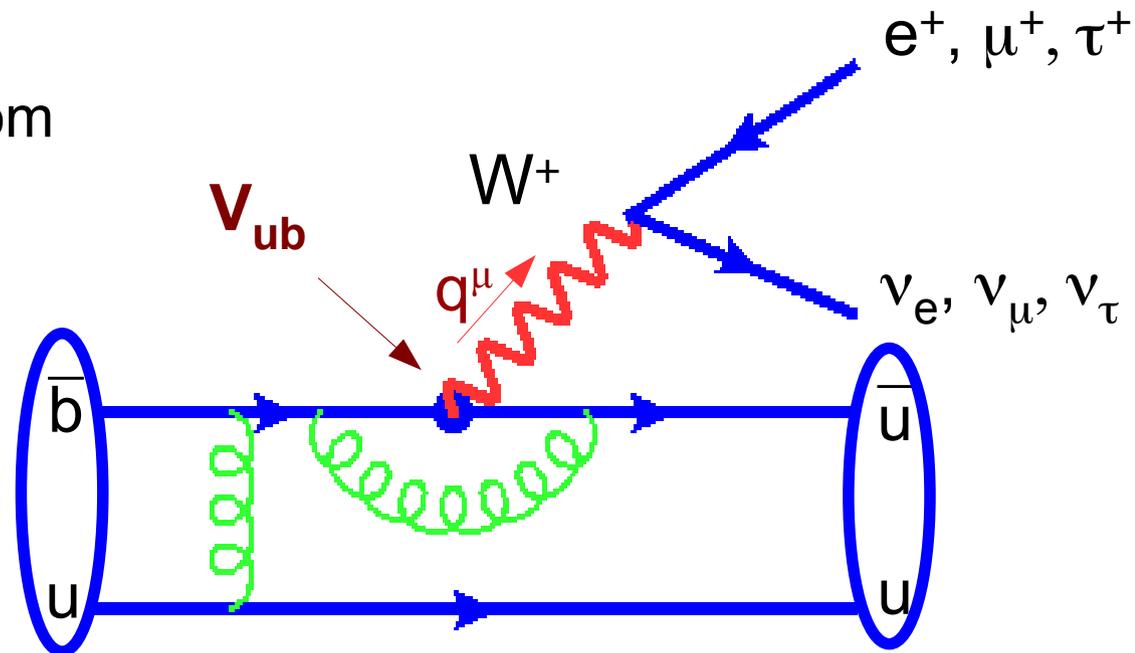


Quark mixing:
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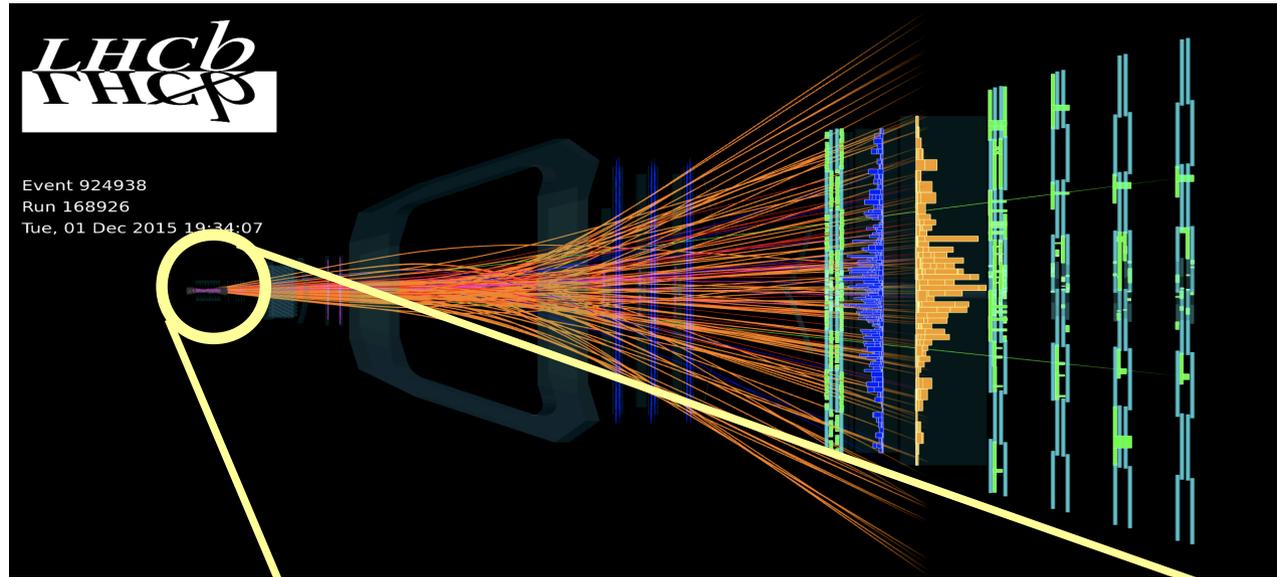
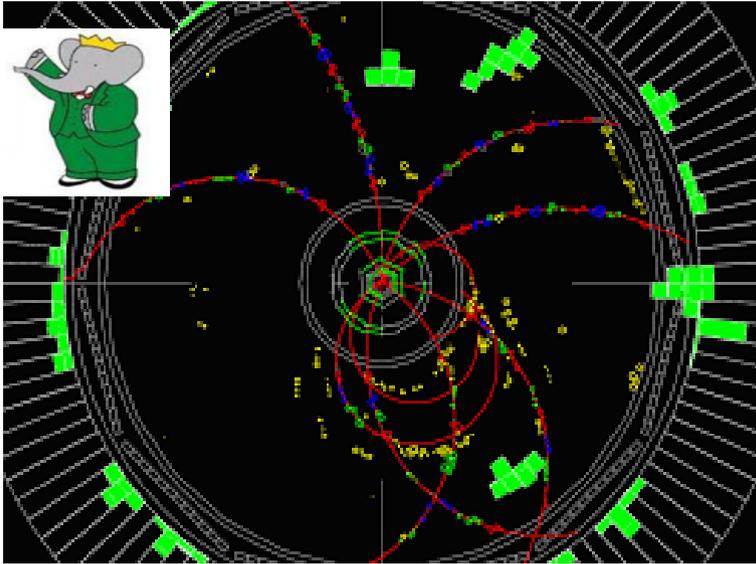
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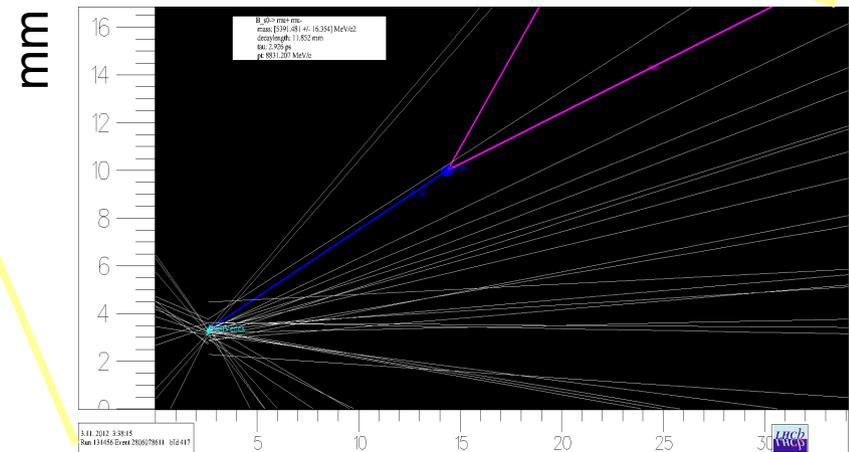


Semileptonics at LHCb!

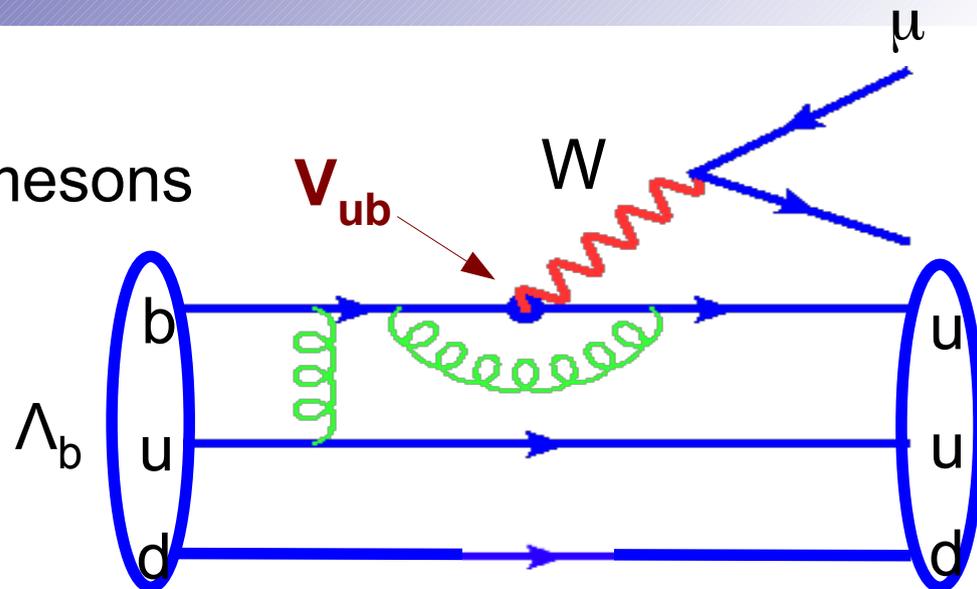
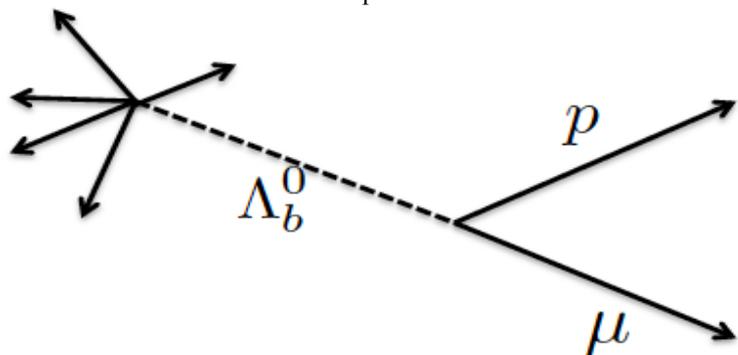
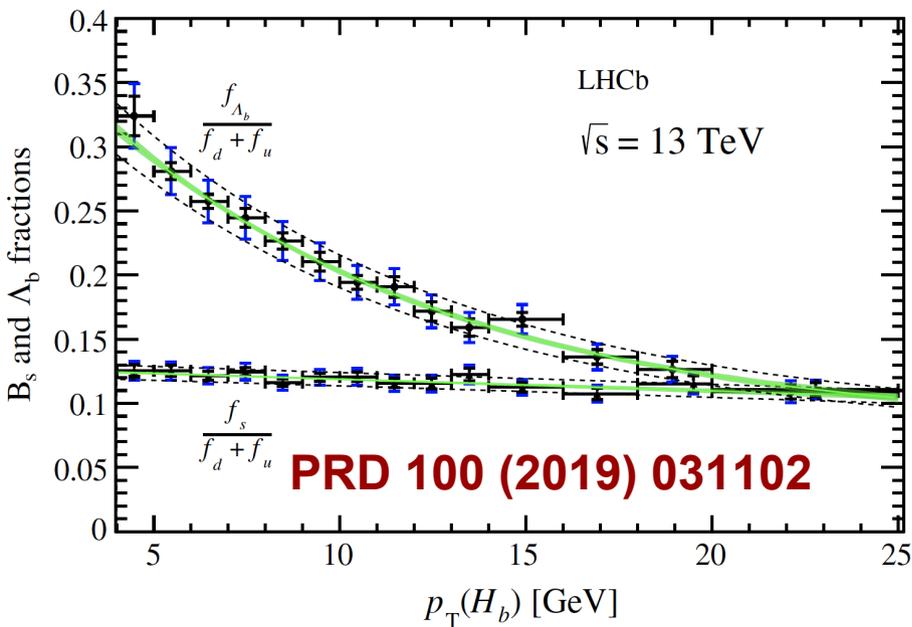


- At LHCb the key ingredients are:

- Lepton identification
- Trigger threshold to low-pT
- Decay vertex separation from the primary vertex to identify the b-hadron decays: b-hadron flight length is $\sim 1\text{cm}$



- The b-baryon decays provided complementary information to B mesons
- Λ_b Produced copiously



- Kinematic constraints allow the determination of the p_{Λ_b} (modulo 2-fold ambiguity)
- Large background from $\Lambda_b \rightarrow \Lambda_c \mu \nu$
- LHCb determines (in the high q^2 region) the ratio

$$R_{exp} = \frac{\mathcal{B}(\Lambda_b \rightarrow p\mu\nu)}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c\mu\nu)}$$

← Signal
 ← Normalization

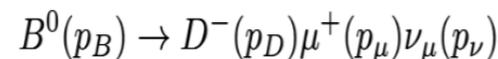
Reconstruction of the q^2

arXiv:1912.09562

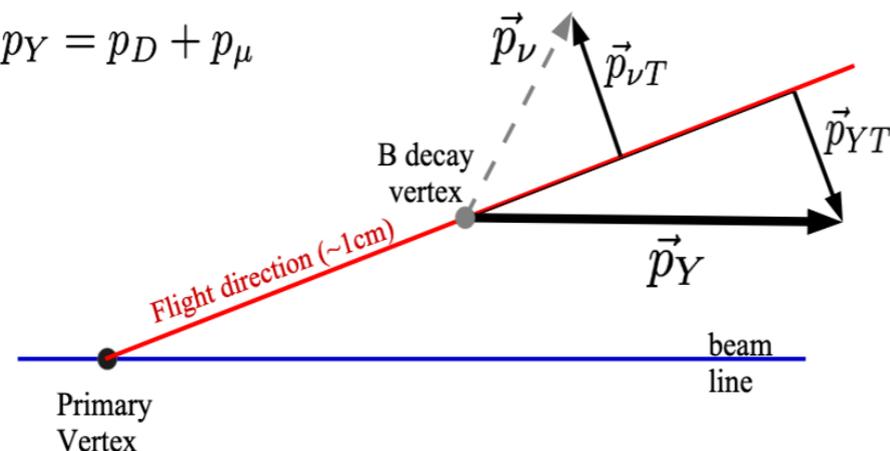
The knowledge of the Λ_b momentum P_{Λ_b} is needed to measure $q^2 = (P_{\Lambda_b} - P_p)^2$

$$m_\nu^2 = (P_{\Lambda_b} - P_p - P_\mu)^2 = (P_{\Lambda_b} - P_Y)^2 = 0$$

$$E_{\Lambda_b}^2 = m_{\Lambda_b}^2 + |\vec{P}_{\Lambda_b}|^2$$



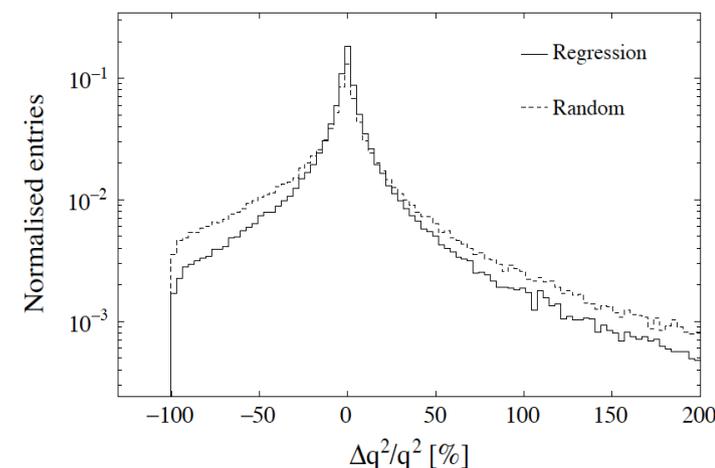
$$p_Y = p_D + p_\mu$$

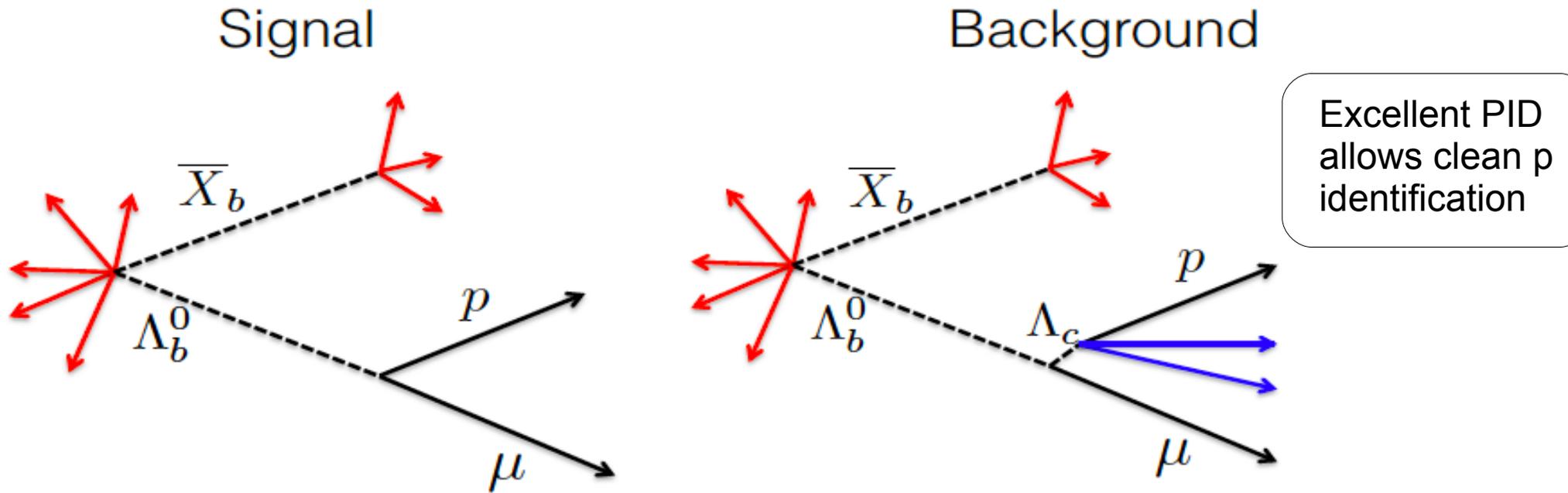


Hypothesis of just 1-neutrino missing, known masses of the particles, and the well-measured Λ_b flight direction gives the momentum with a 2-fold ambiguity

- Ciezarek et al. [JHEP02\(2017\)021](#)

- The q^2 resolution can be improved exploiting other information as decay length and angle with respect to the beam line
- Important when angular variables will be considered
- Improvements foreseen exploiting Machine Learning

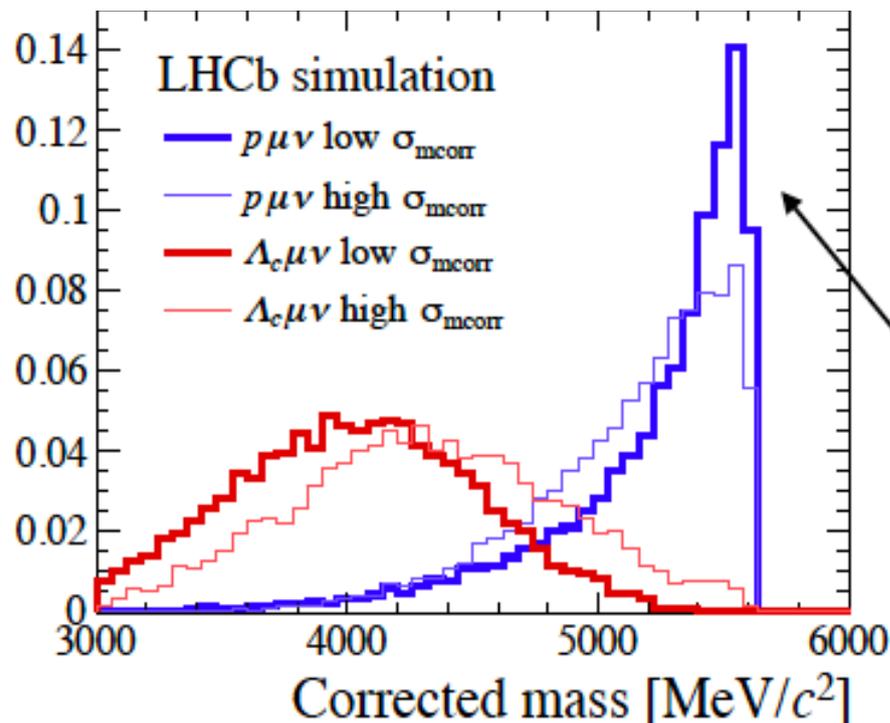
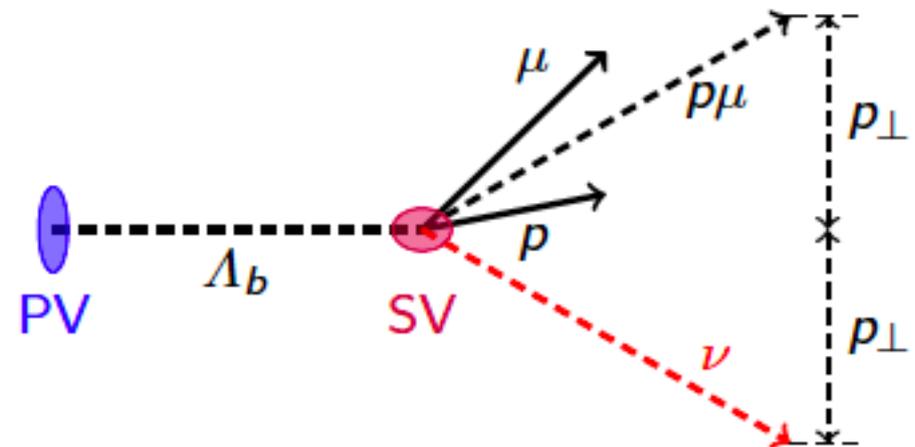




- Require isolated proton-muon vertex
 - A multivariate classifier to distinguish between these two configurations
- Powerful tool to reduce background from other b-hadrons: 90% rejection & 80% efficiency
 - very difficult to isolate against neutral particles: main backgrounds

- Use the corrected mass to discriminate signal from the remaining background

$$M_{corr} = \sqrt{p_{\perp}^2 + M_{p\mu}^2 + p_{\perp}}$$

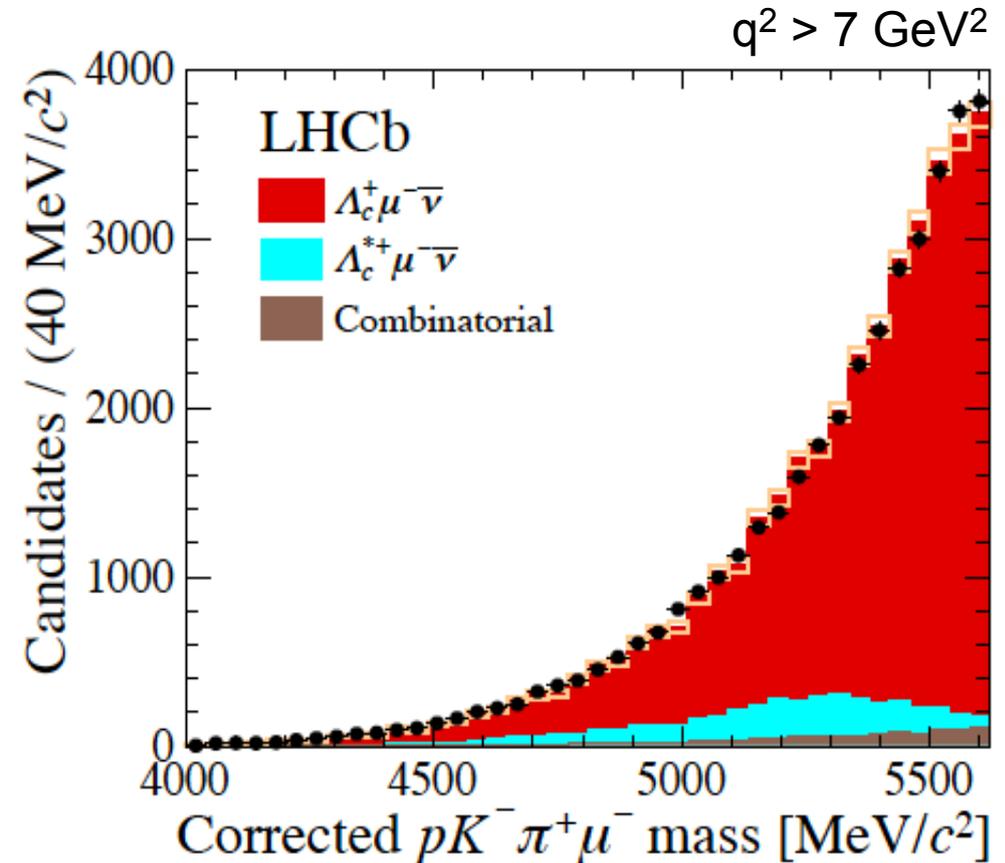
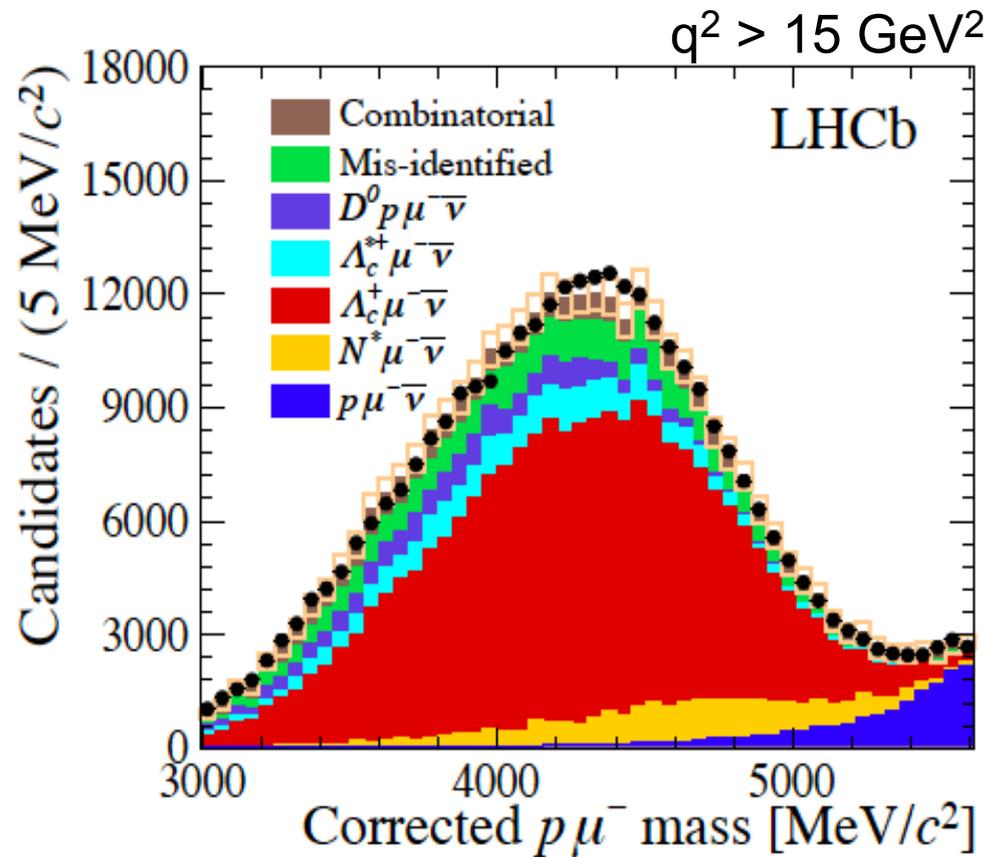


Calculate uncertainty for each event and reject candidates with M_{corr} uncertainty greater than 100MeV only (~23% survive).

The signal peaks even with a missing particle!

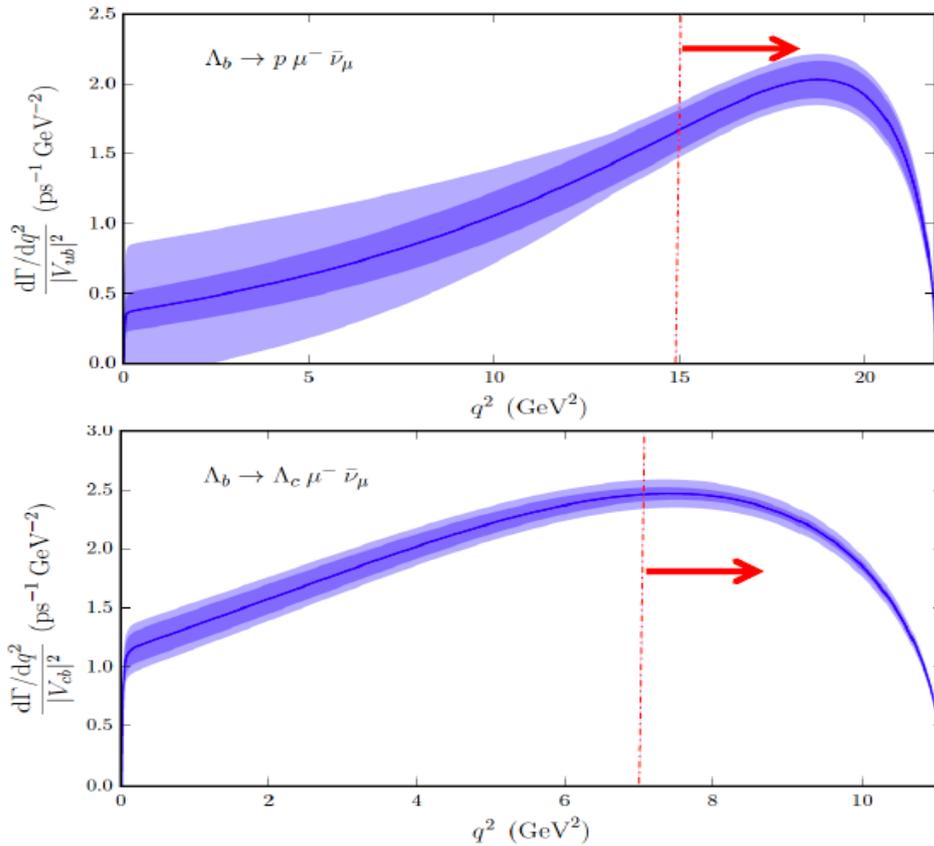
Signal $N=17687 \pm 733$

Normalization $N=34255 \pm 571$



$$R_{\text{exp}} = 0.92 \pm 0.04(\text{stat}) \pm 0.07(\text{syst}) \times 10^{-2}$$

Systematics dominated by $\text{BF}(\Lambda_c \rightarrow pK\pi)$, trigger and tracking efficiency



- Most recent calculation based on 2-1 L-QCD calculation using RBC & UKQCD configurations
- The most reliable theory predictions of the ratio of FF are obtained for:
 - $\Lambda_b \rightarrow \Lambda_c \mu \nu$ $q^2 > 7 \text{ GeV}^2$
 - $\Lambda_b \rightarrow p \mu \nu$ $q^2 > 15 \text{ GeV}^2$

$$\frac{V_{ub}}{V_{cb}} = \sqrt{\frac{R_{exp}}{R_{TH}}}$$

Nature Phys.11(2015)743



First measurement of $\Lambda_b \rightarrow p \mu \nu$



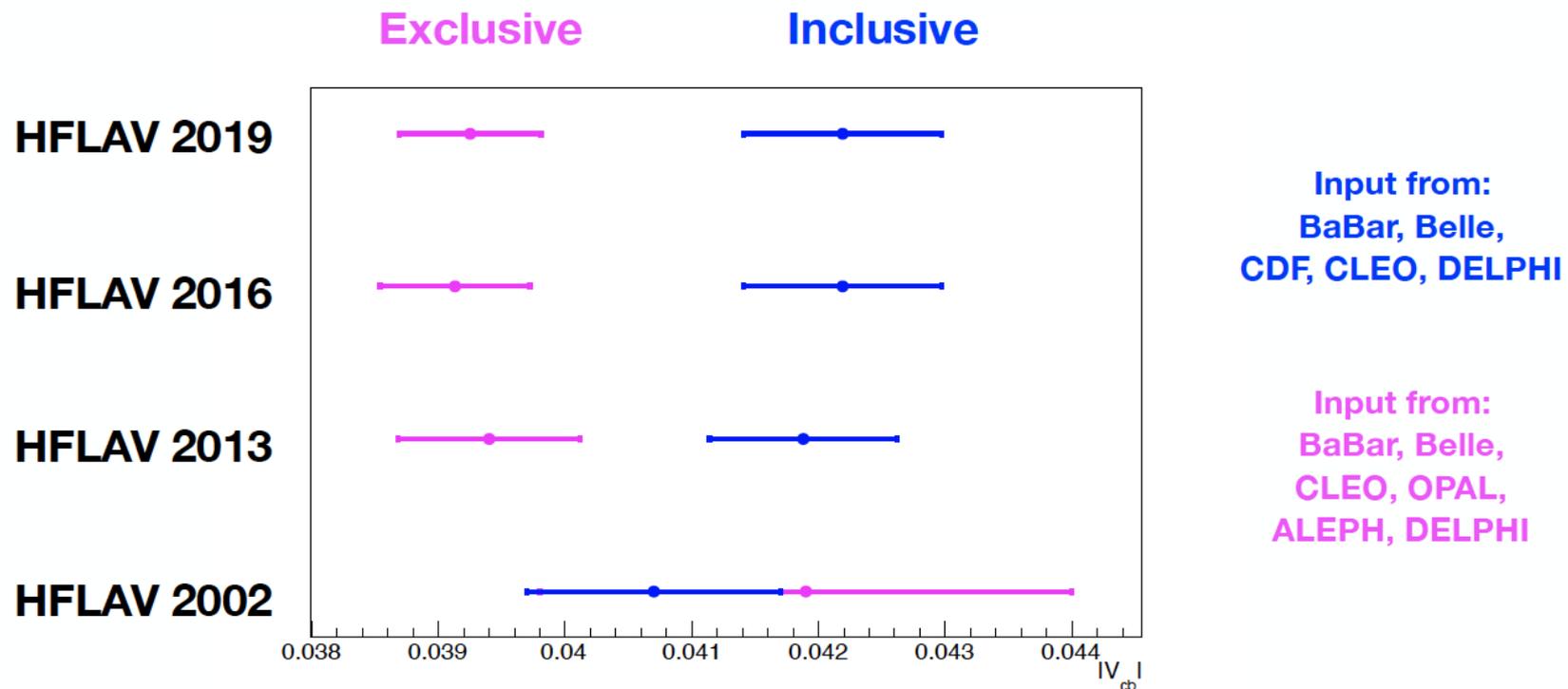
First $|V_{ub}|$ in hadronic environments

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.079 \pm 0.004_{Exp.} \pm 0.004_{F.F.}$$

IV_{cb}l

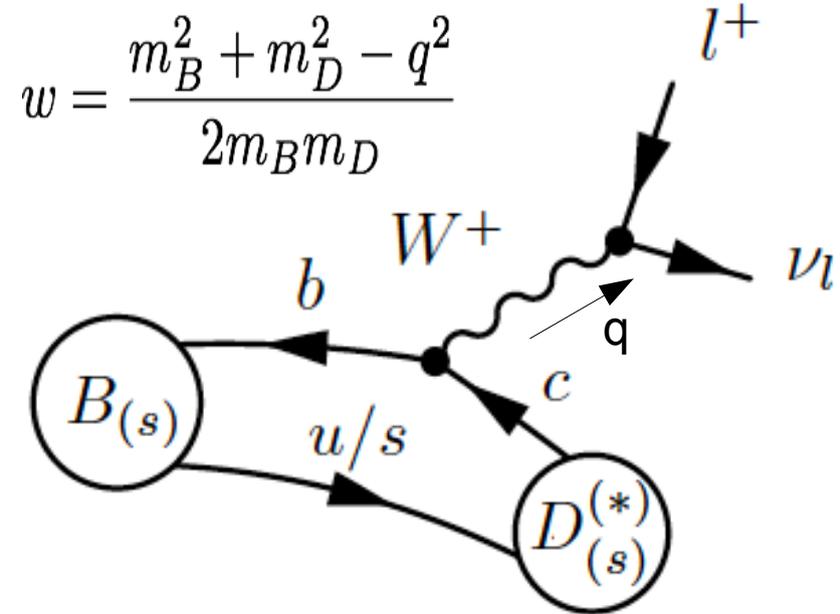
Measurements of $|V_{cb}|$

- Inclusive decays $B \rightarrow X_c \ell \nu$:
 - HQE is the successful tool to include perturbative and non-perturbative QCD corrections
- Exclusive decays $B \rightarrow D \ell \nu / D^* \ell \nu$
 - QCD effects are embedded in the form factors



Exclusive $|V_{cb}|$

- $B \rightarrow D\ell\nu$ and $B \rightarrow D^*\ell\nu$ provide clean way to extract $|V_{cb}|$



$$\frac{d\Gamma(B \rightarrow D\ell\nu)}{dq^2} = \frac{G_F^2 |V_{cb}|^2}{24\pi^3} \frac{(q^2 - m_\ell^2)^2 \sqrt{E_D^2 - m_D^2}}{q^4 m_B^2} \times$$

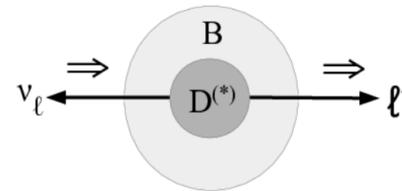
$$\left[\left(1 + \frac{m_\ell^2}{2q^2}\right) m_B^2 (E_D^2 - m_D^2) |f_+(q^2)|^2 + \frac{3m_\ell^2}{8q^2} (m_B^2 - m_D^2)^2 |f_0(q^2)|^2 \right]$$

$B \rightarrow D$: for $\ell=e$ and $\ell=\mu$, only $f_+(q^2)$ plays a role

$B \rightarrow D^*$: three form factors

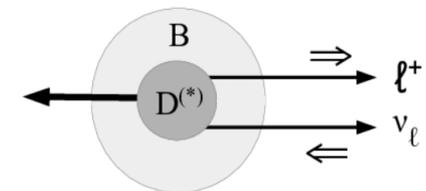
- FF computed from Lattice-QCD

- Lattice-QCD reliable close to zero-recoil regime



$$q^2 = q_{max}^2$$

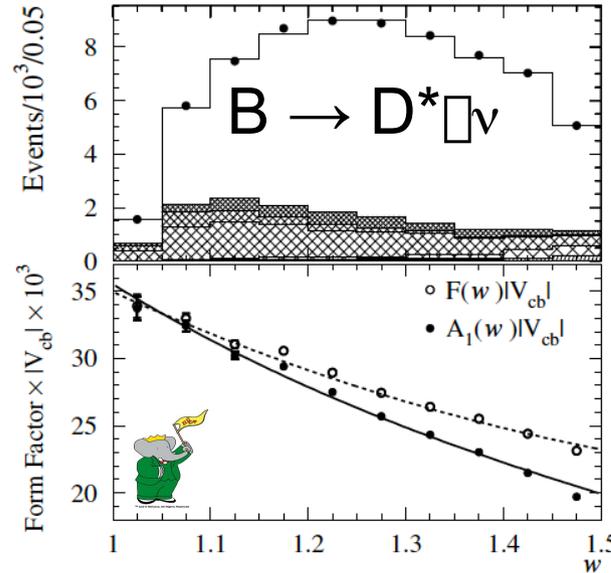
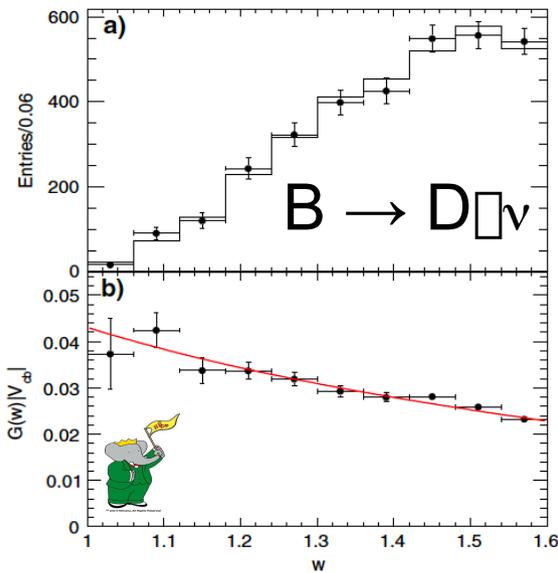
$$w = 1$$



$$q^2 = q_{min}^2 = m_\ell^2 \approx 0$$

$$w \approx 1.5$$

$|V_{cb}|$ and Form Factors parameterizations



- Phase space is reduced to 0 in the zero-recoil region
- Need an extrapolation to $w=1$ which has to rely on a form factor parameterization

- BGL Boyd, Grinstein, Lebed Phys.Rev.Lett 74, 4603 (1995)

$$f_i(z) = \frac{1}{P_i(z)\phi_i(z)} \sum_{n=0}^N a_{i,n} z^n, \quad z(w) = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}}$$

Coefficient $a_{i,n}$ free parameters
The unitarity and analyticity of the FF assure bounds on the sum of the $a_{i,n}^2$

- CLN Caprini, Lellouch, Neubert Nucl.Phys.B530, 153 (1998)

$$B \rightarrow D \ell \nu$$

$$\mathcal{G}(z) = \mathcal{G}(1)(1 - 8\rho^2 z + (51\rho^2 - 10)z^2 - (252\rho^2 - 84)z^3)$$

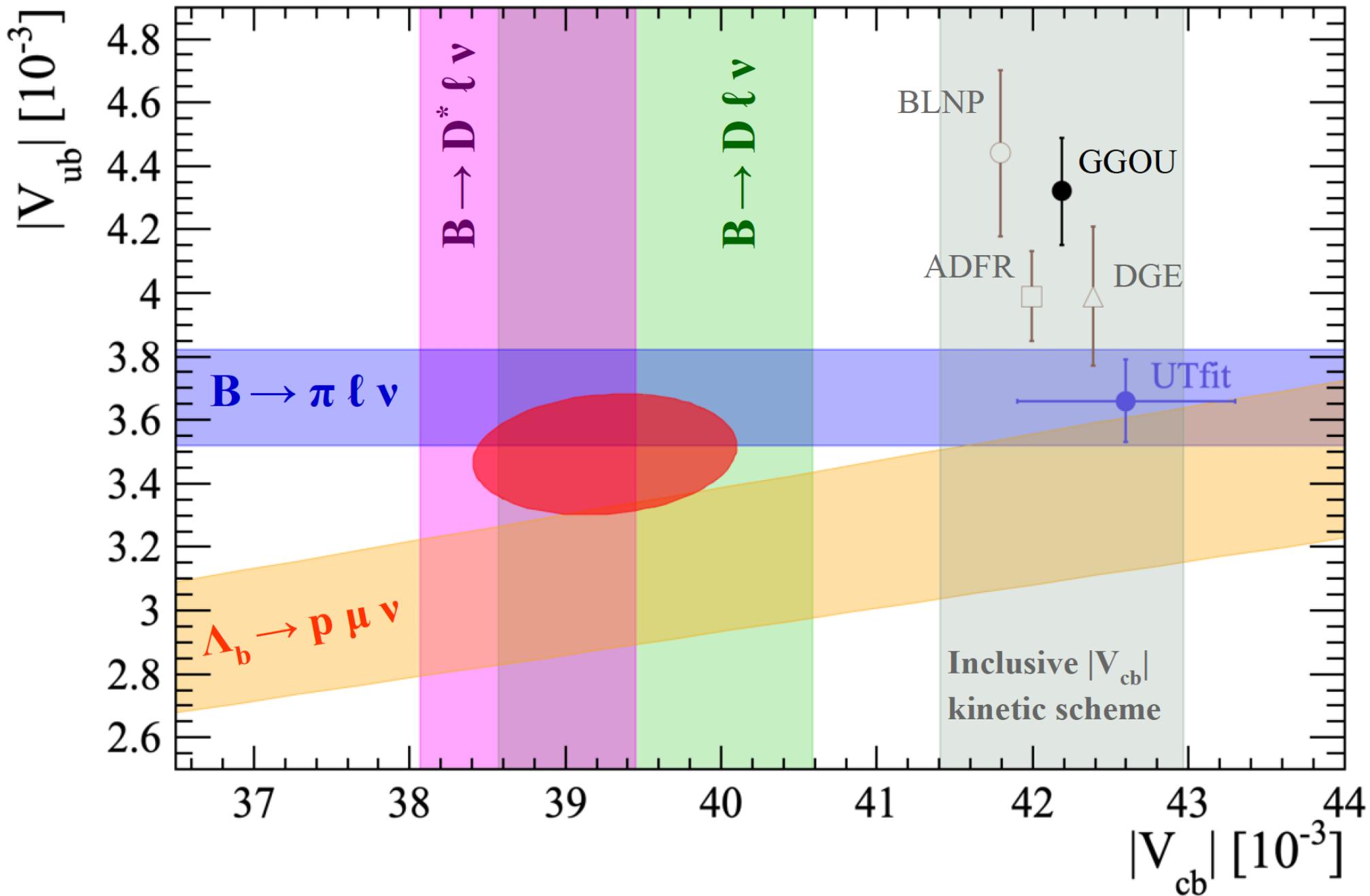
Higher order coefficient connected with the slope ρ^2

$$B \rightarrow D^* \ell \nu$$

$$h_{A_1}(w) = h_{A_1}(1)[1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3],$$

$$R_1(w) = R_1(1) - 0.12(w-1) + 0.05(w-1)^2$$

$$R_2(w) = R_2(1) + 0.11(w-1) - 0.06(w-1)^2$$



B_s semileptonic decays

- Complementary measurements to those from B^0 and B^+



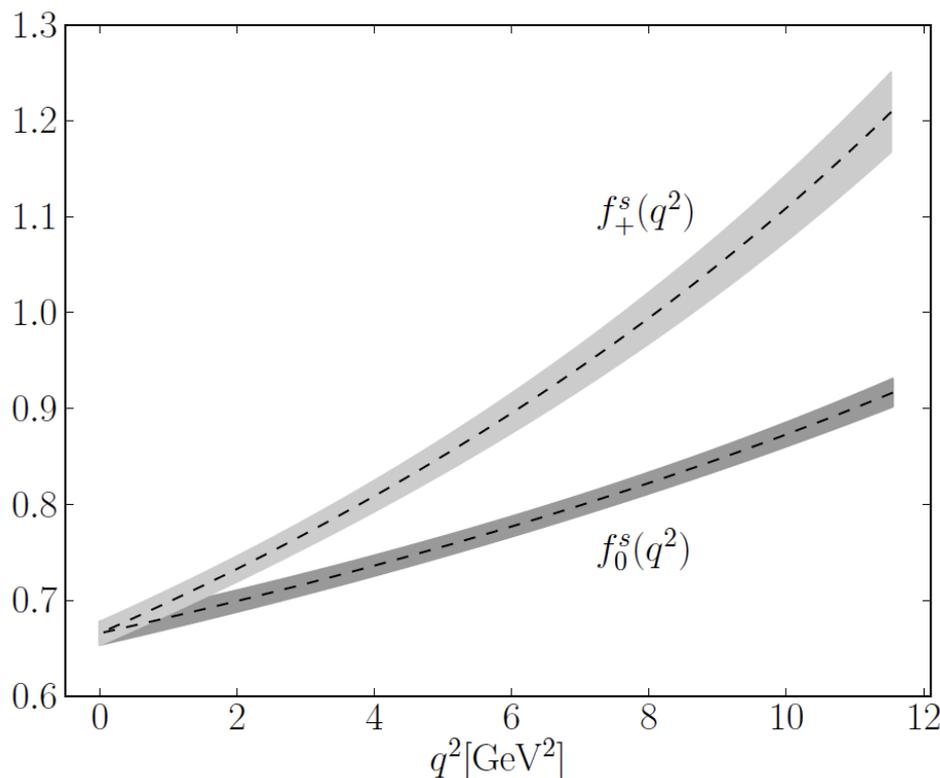
Golden modes
for Lattice-QCD

- Advantages:

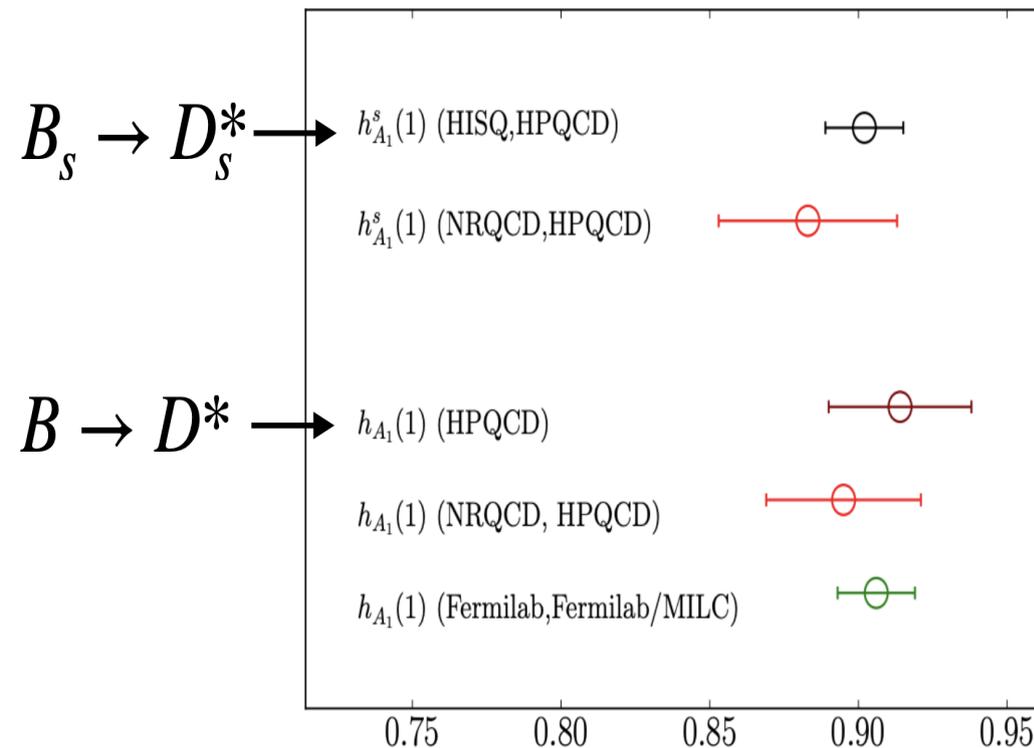
- Lattice calculations easier due to heavier spectator quark, so predictions are more precise
- For the $B_s \rightarrow D_s^*$: the *zero-width* approximation of the D_s^* should work better than the B case (no $D\pi$ pollution)

HPQCD, arXiv 1906.00701

FF in the full q^2 range



HPQCD, PRD 99 (2019) 114512



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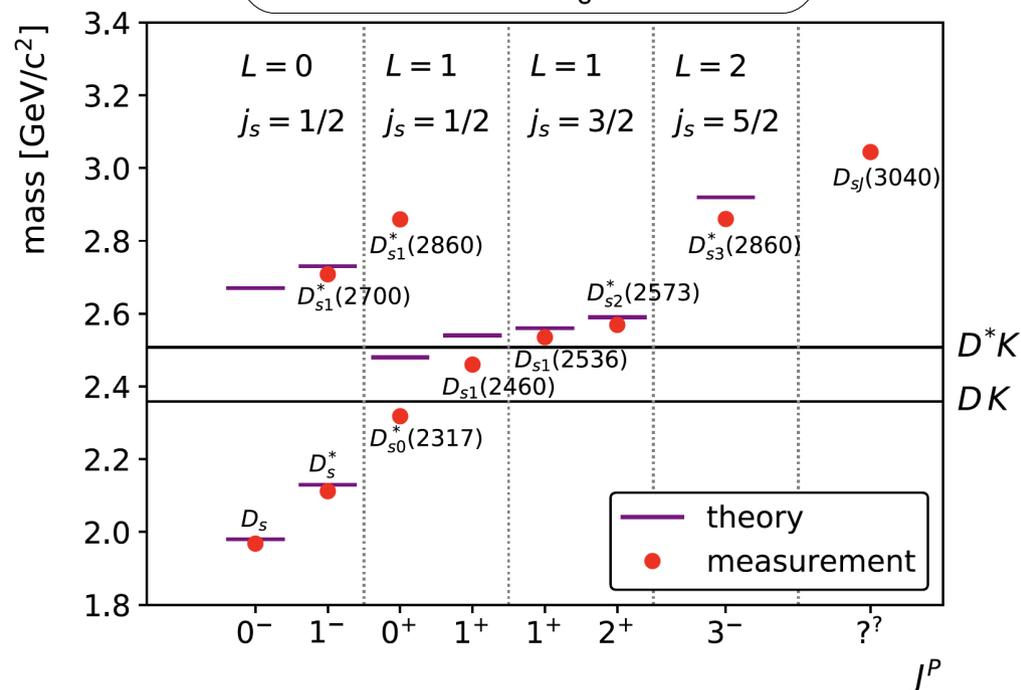
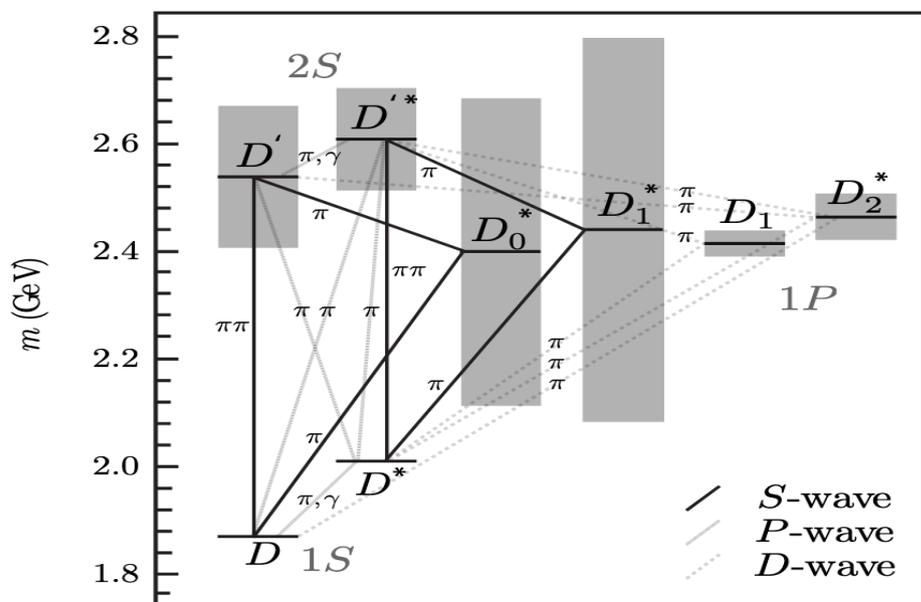
- Advantages:

- Lattice calculations easier due to heavier spectator quark, so predictions are more precise
- For the $B_s \rightarrow D_s^*$: the *zero-width* approximation of the D_s^* is more valid than the B case (no $D\pi$ pollution)
- Experimental point: different background composition from excited D_s states than in the $B \rightarrow D^*$ case

$D_s(2317) \rightarrow D_s \pi^0 > 90\%$

$D_{s1}(2460) \rightarrow D_s^* \pi^0 \sim 50\%$

$D_s X \sim 50\%$



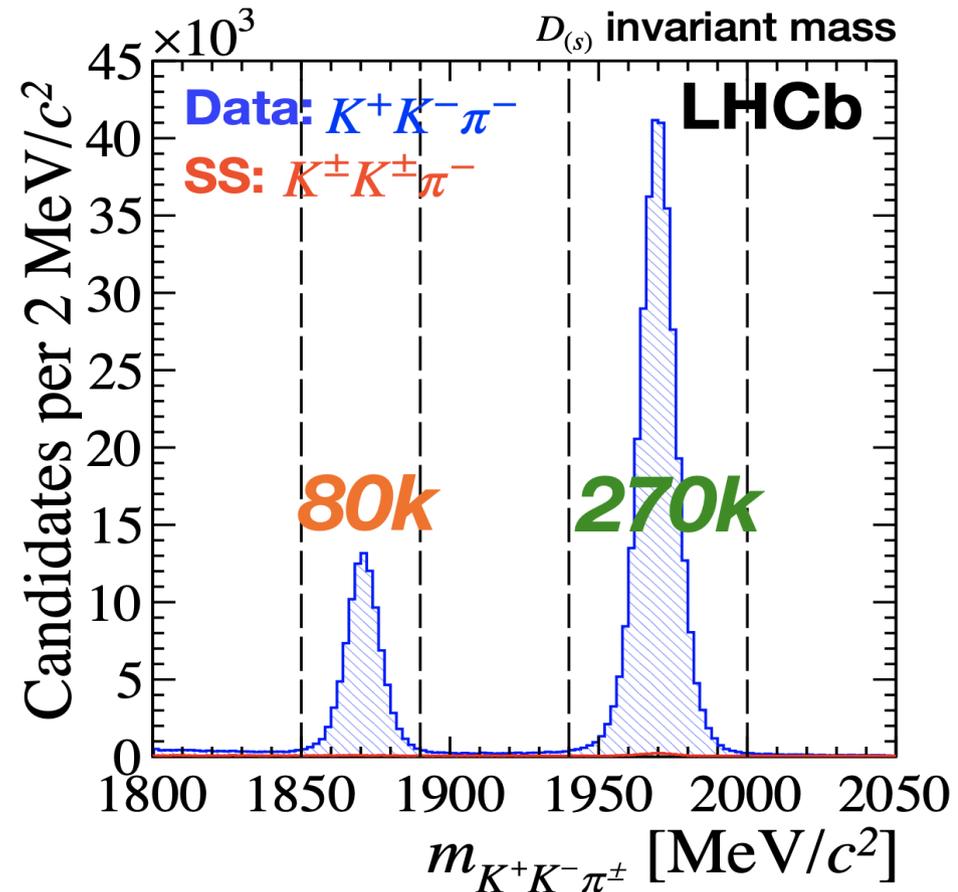
LHCb Measurement of $|V_{cb}|$

ArXiv:2001.03225

- Extract $|V_{cb}|$ from B_s decays $B_s \rightarrow D_s \mu \nu$ and $B_s \rightarrow D_s^* \mu \nu$
- Normalized to $B^0 \rightarrow D^- \mu \nu$ and $B^0 \rightarrow D^{*-} \mu \nu$
 - The $\text{BF}(B^0 \rightarrow D^{(*)-} \mu \nu)$ are known well from B-Factories

$$\mathcal{R} \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^- \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^- \mu^+ \nu_\mu)},$$
$$\mathcal{R}^* \equiv \frac{\mathcal{B}(B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}$$

- The D^- and the D_s are reconstructed in the same final state $D_{(s)}^- \rightarrow KK\pi^-$
- Decrease the systematic uncertainties: same particles and similar kinematic in the final state
- Only the D^- and the D_s are constructed
- The D_s and the D_s^* (and D^- and D^{*-}) are separated kinematically (with m_{corr})



$$\mathcal{R} \equiv \frac{\mathcal{B}(B_s \rightarrow D_s \mu \nu)}{\mathcal{B}(B^0 \rightarrow D^- \mu \nu)} = \frac{N_s \cdot \epsilon_d}{N_d \cdot \epsilon_s} \cdot \frac{f_d \cdot \mathcal{B}(D^- \rightarrow KK\pi)}{f_s \cdot \mathcal{B}(D_s \rightarrow KK\pi)}$$

External inputs
fs/fd from
PRD(2019) 031102
BFs from PDG

Signal yields and normalization yields from fit
Efficiencies evaluated from simulation, adjusted for
Data/MC differences based on control samples

Analogous expression
for R^* (additional BF of the D^*)

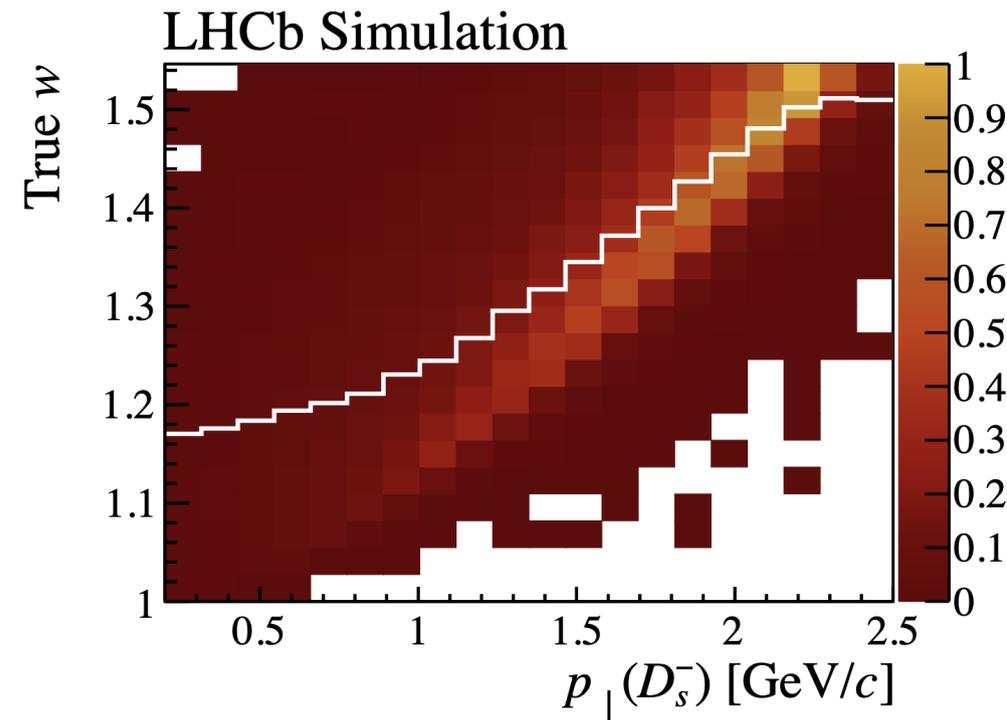
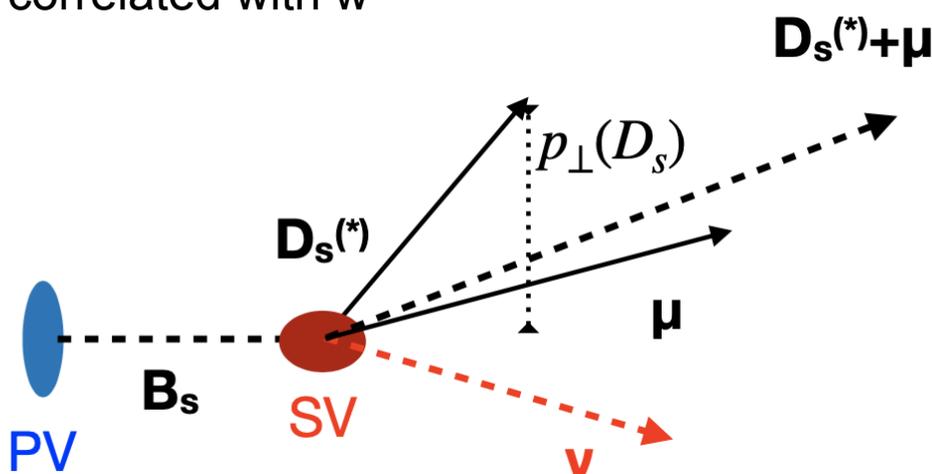
$$\mathcal{R} \equiv \frac{\mathcal{B}(B_s \rightarrow D_s \mu \nu)}{\mathcal{B}(B^0 \rightarrow D^- \mu \nu)} = \frac{N_s \cdot \epsilon_d}{N_d \cdot \epsilon_s} \cdot \frac{f_d \cdot \mathcal{B}(D^- \rightarrow KK\pi)}{f_s \cdot \mathcal{B}(D_s \rightarrow KK\pi)}$$

External inputs
 f_s/f_d from
 PRD(2019) 031102
 BFs from PDG

Signal yields and normalization yields from fit
 Efficiencies evaluated from simulation, adjusted for
 Data/MC differences based on control samples

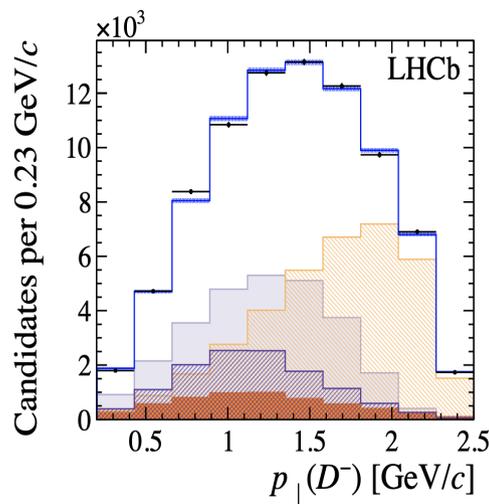
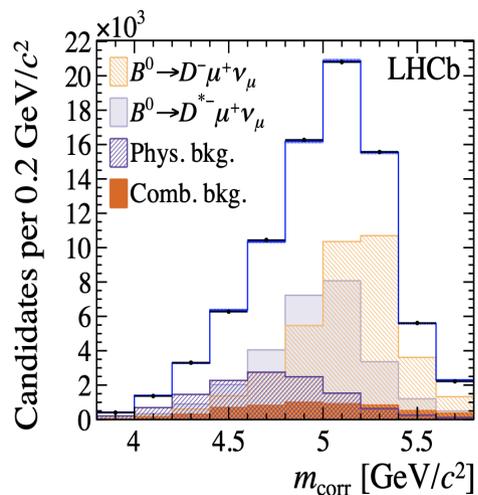
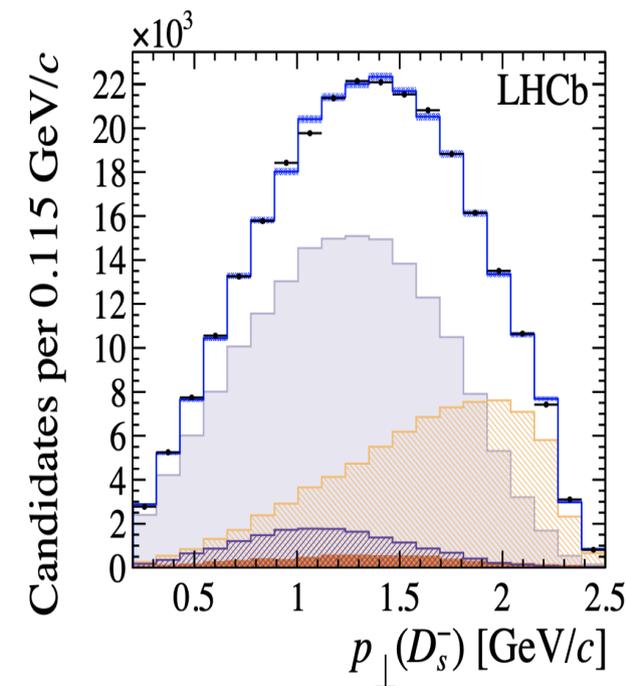
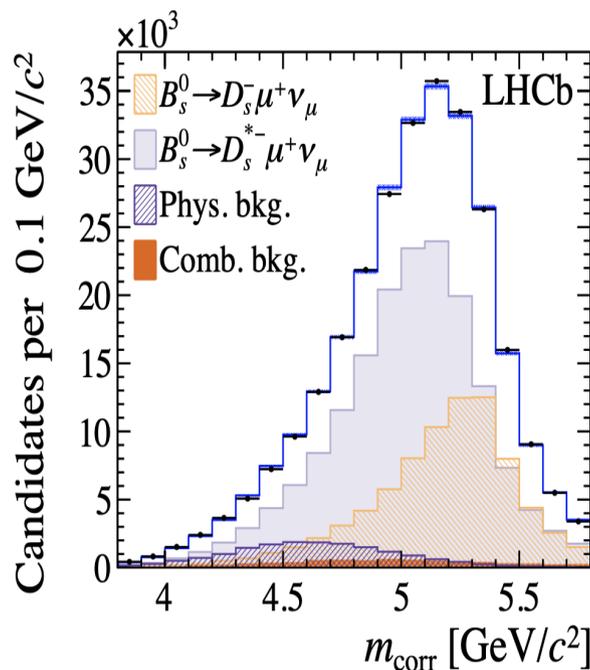
Analogous expression
 for \mathcal{R}^* (additional BF of the D^*)

- N_s can be written in terms of $|V_{cb}|$ and the form factors: also the form factors can be determined by a proper fit of the signal candidates
- The transverse momentum of the D_s is correlated with w



- Template fit to m_{corr} and $p_{\perp}(D_s)$ identify the signal yields and provides a simultaneous measurement of the ratios \mathcal{R}^* and the form factors

	\mathcal{R} [10^{-1}]	\mathcal{R}^* [10^{-1}]
$f_s/f_d \times \mathcal{B}(D_s^- \rightarrow K^+ K^- \pi^-) (\times \tau)$	0.4	0.4
$\mathcal{B}(D^- \rightarrow K^- K^+ \pi^-)$	0.3	0.3
$\mathcal{B}(D^{*-} \rightarrow D^- X)$	-	0.2
$\mathcal{B}(B^0 \rightarrow D^- \mu^+ \nu_\mu)$	-	-
$\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)$	-	-
$m(B_s^0), m(D^{*-})$	-	-
η_{EW}	-	-
$h_{A_1}(1)$	-	-
External inputs (ext)	0.5	0.5
$D_{(s)}^- \rightarrow K^+ K^- \pi^-$ model	0.5	0.4
Background	0.4	0.6
Fit bias	0.0	0.0
Corrections to simulation	0.0	0.0
Form-factor parametrization	0.0	0.1
Experimental (syst)	0.6	0.7
Statistical (stat)	0.5	0.5



$$\mathcal{R} = 1.09 \pm 0.05_{stat} \pm 0.06_{syst} \pm 0.05_{ext}$$

$$\mathcal{R}^* = 1.06 \pm 0.05_{stat} \pm 0.07_{syst} \pm 0.05_{ext}$$

First measurements of these SL branching ratios

Results on $|V_{cb}|$

ArXiv:2001.03225

$$|V_{cb}|_{\text{CLN}} = (41.4 \pm 0.6(\text{stat}) \pm 0.9(\text{syst}) \pm 1.2(\text{ext})) \times 10^{-3}$$

$$|V_{cb}|_{\text{BGL}} = (42.3 \pm 0.8(\text{stat}) \pm 0.9(\text{syst}) \pm 1.2(\text{ext})) \times 10^{-3}$$



- First measurement of $|V_{cb}|$ using B_s

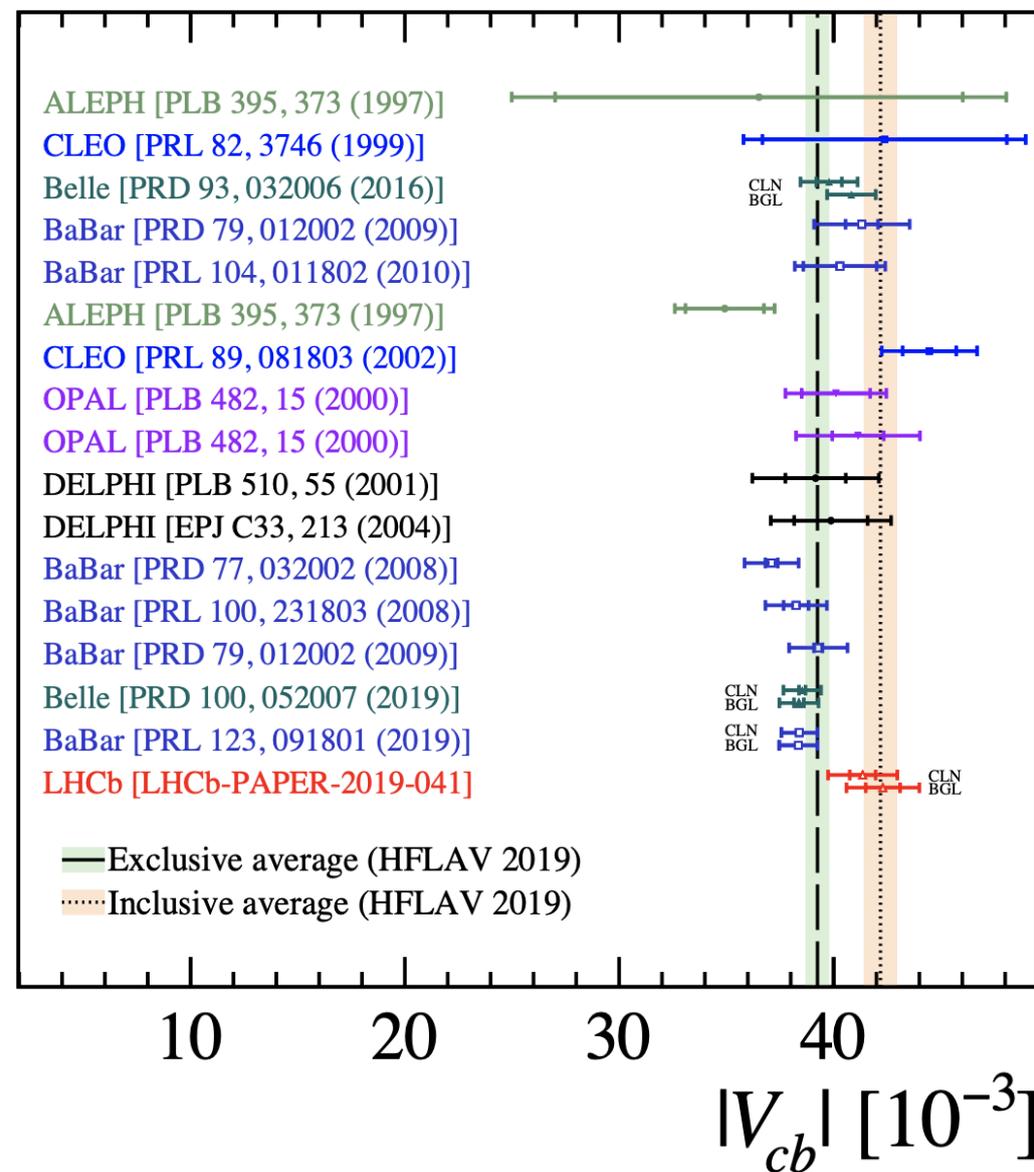


- First measurement of $|V_{cb}|$ in an hadronic environment

- The results are consistent between CLN and BGL
- Results compatible with world average for both inclusive and exclusive determinations
- Uncertainty not competitive with b-factories: limited by knowledge of fs/fd



The approach can be applied also to B^0 decays!



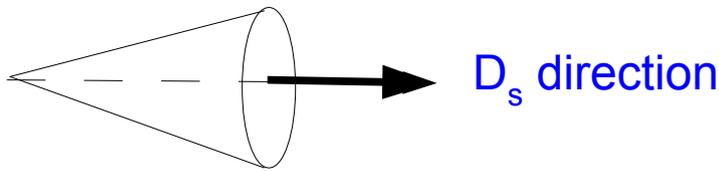
- Determination of the differential decay rate $d\Gamma/dq^2$
- Measure more precisely the form factors in the CLN and BGL parametrisations

$$\frac{d\Gamma(B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu)}{dq^2} = \frac{G_F^2 |V_{cb}|^2 |\eta_{EW}|^2 |\vec{p}| q^2}{96 \pi^3 m_{B_s^0}^2} \left(1 - \frac{m_\mu^2}{q^2}\right)^2 \times \left[(|H_+|^2 + |H_-|^2 + |H_0|^2) \left(1 + \frac{m_\mu^2}{2q^2}\right) + \frac{3m_\mu^2}{2q^2} |H_t|^2 \right]$$

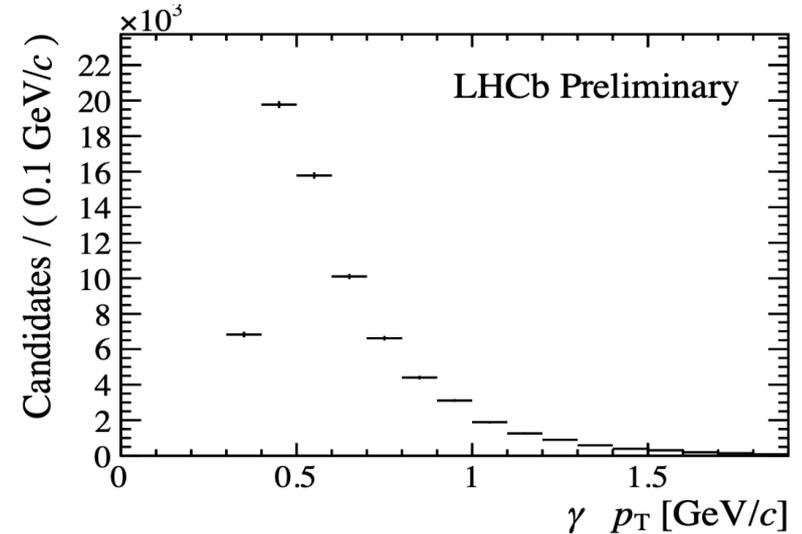
Analysis Strategy

- Extract the production rate of $B_s \rightarrow D_s^* \mu \nu$ as a function of w (2016 data)
 - Fully reconstruct $D_s^* \rightarrow D_s \gamma$
 - Use templates from simulation, properly corrected for data/MC differences from control samples
- Corrected the raw yields for detector resolution (unfolding) and selection/reconstructed efficiencies
- Fit the unfolded and efficiency corrected spectrum with different parameterisations
 - CLN: fit only $h_{A1}(w)$ and slope the single parameter
 - BGL: fit the leading form factor $f(w)$ with two parameters
 - In both cases: the other functions taken from external sources

- Fully reconstruct the $D_s^* \rightarrow D_s \gamma$
 - Requires the selection of soft photons within a cone around the D_s direction



$D_s^+ \gamma$	$(93.5 \pm 0.7)\%$
$D_s^+ \pi^0$	$(5.8 \pm 0.7)\%$
$D_s^+ e^+ e^-$	$(6.7 \pm 1.6) \times 10^{-3}$



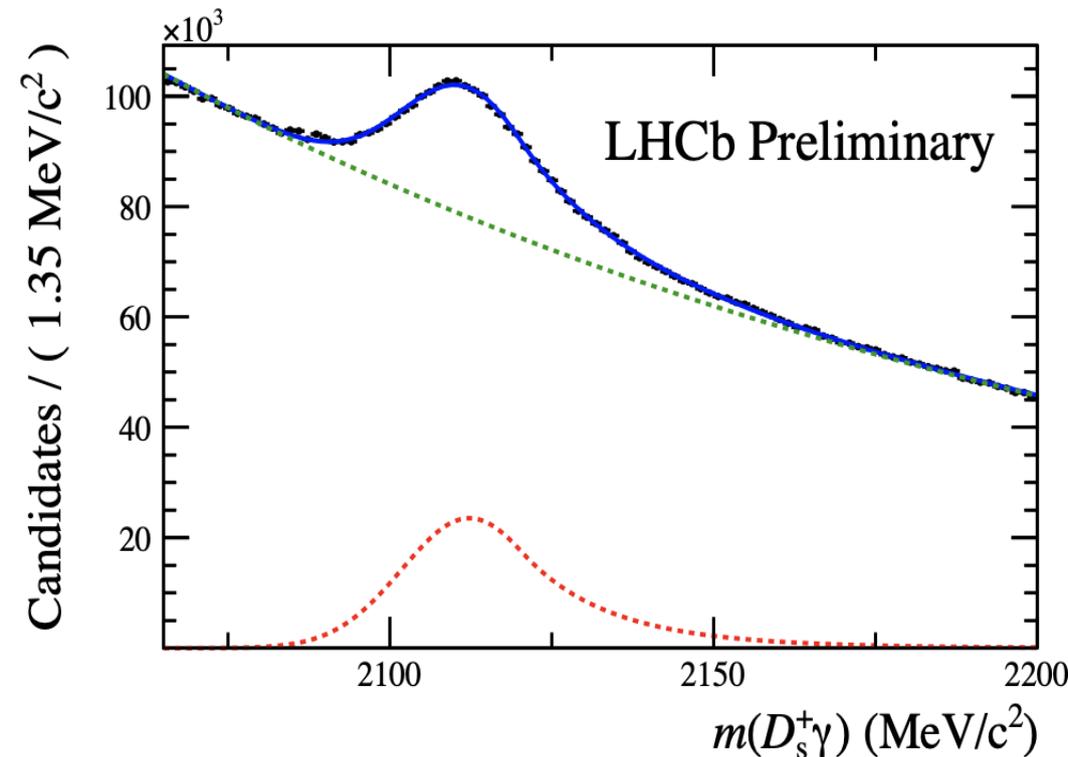
- Most important backgrounds

$$B_s \rightarrow D_s \tau \nu \quad (\tau \rightarrow \mu)$$

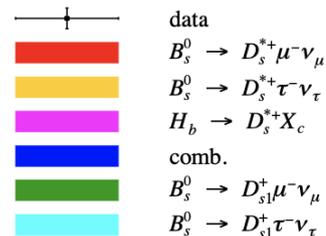
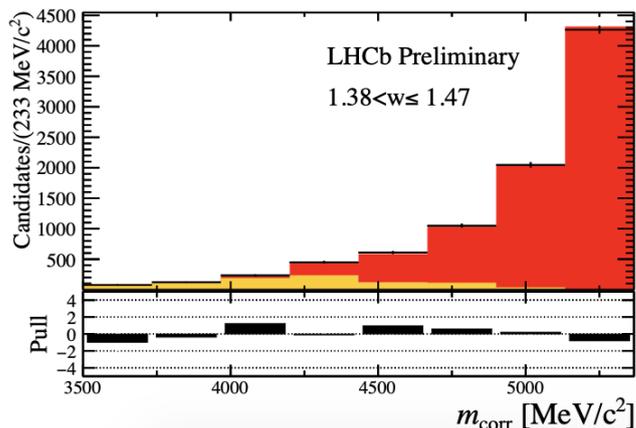
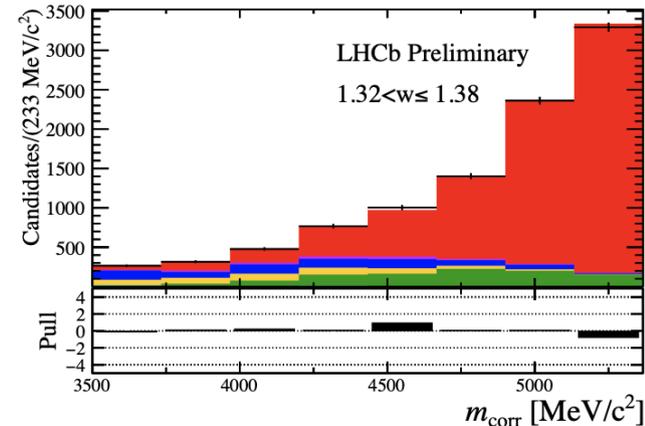
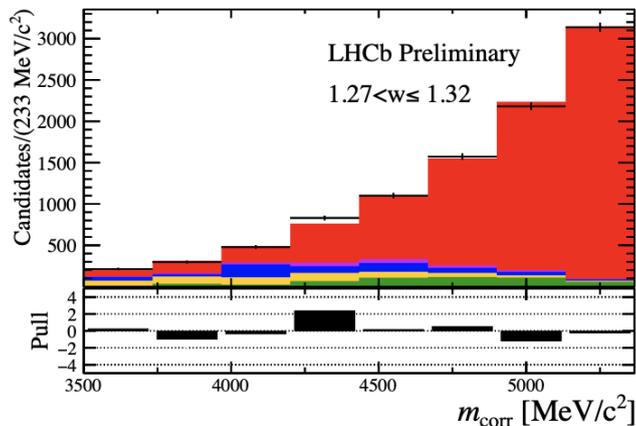
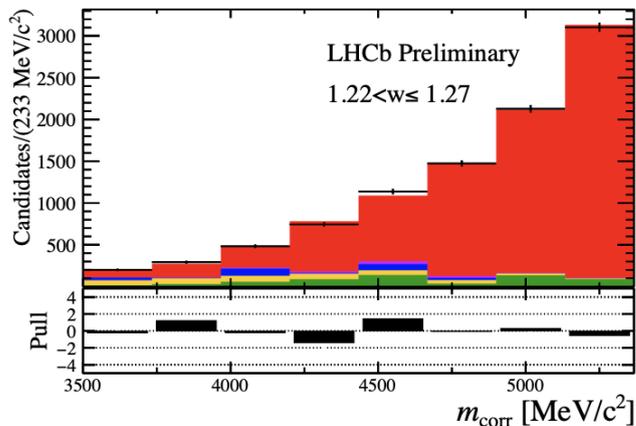
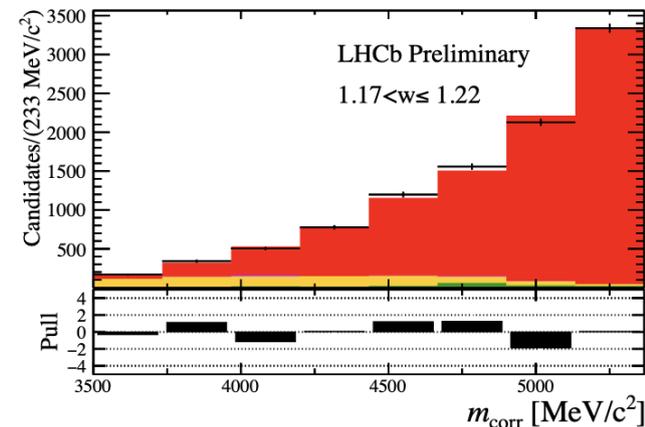
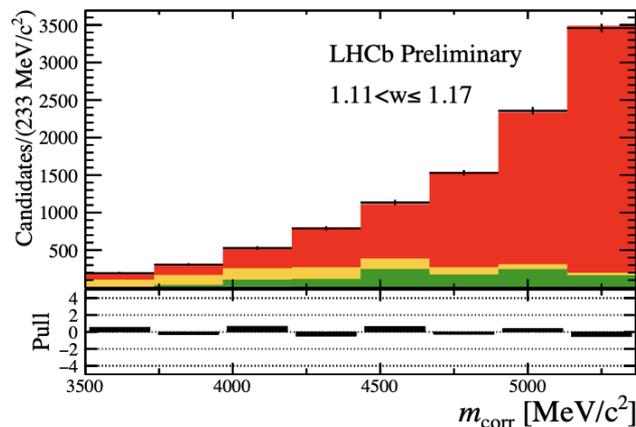
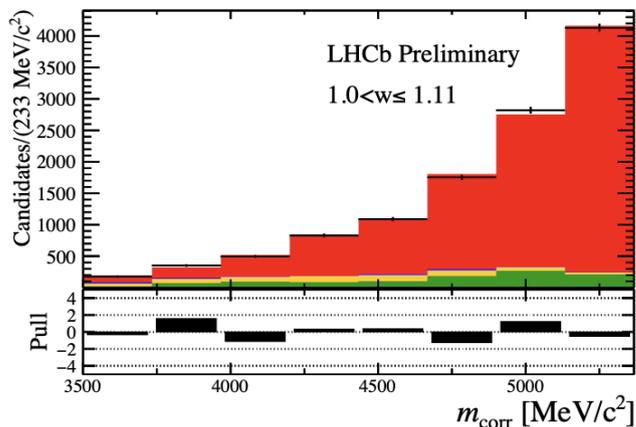
$$B_s \rightarrow D_{s1} \mu \nu \quad (D_{s1} \rightarrow D_s^* X)$$

$$H_b \rightarrow D_s^* X_c \quad (X_c \rightarrow \mu)$$

- Isolation of the muon candidate
- Required a minimum muon p_T



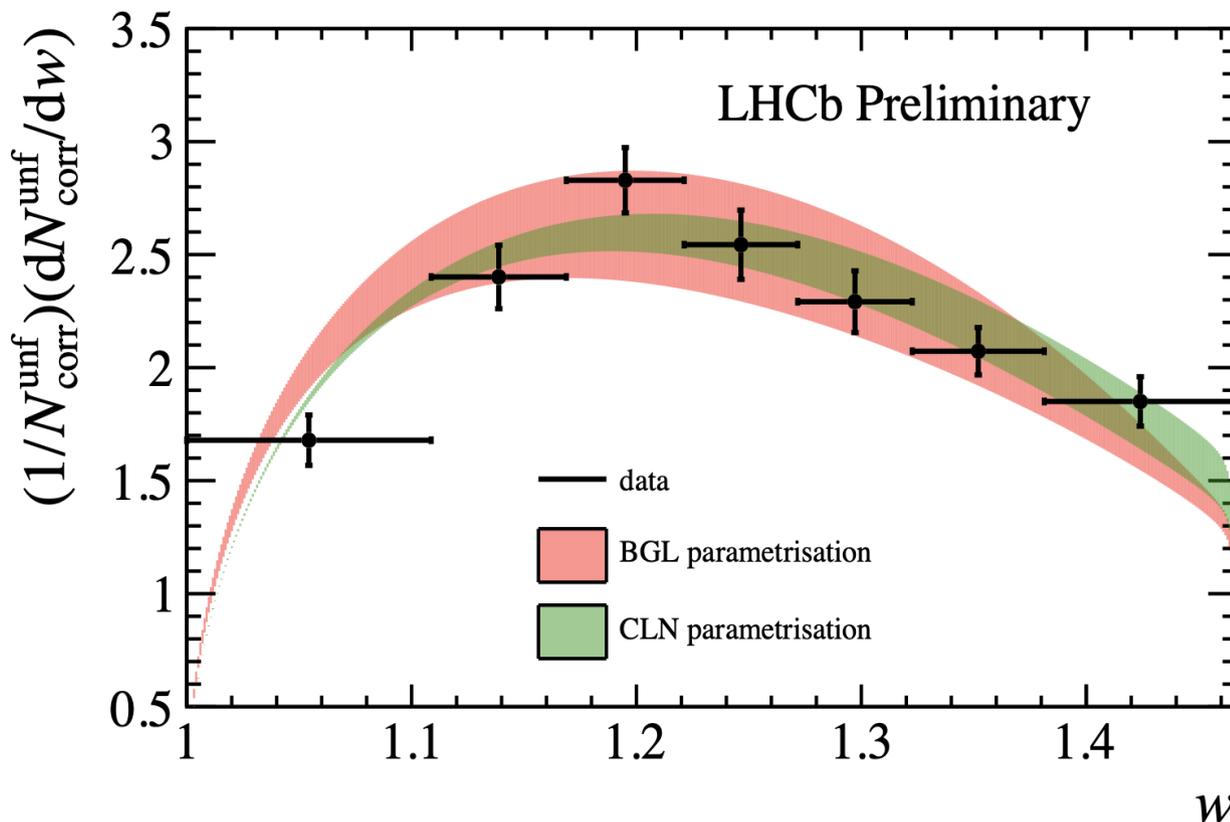
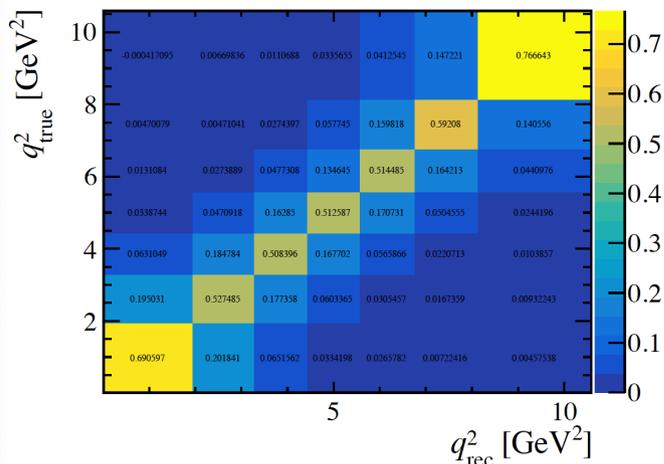
Signal yields



Extremely pure signal samples

$B_s \rightarrow D_s^* \mu \nu$ spectrum

Migration matrix needed for the unfolding



- For CLN parametrisation

$$\rho^2 = 1.16 \pm 0.05(\text{stat}) \pm 0.07(\text{syst})$$

massive leptons

$$\rho^2 = 1.17 \pm 0.05(\text{stat}) \pm 0.07(\text{syst})$$

massless leptons

- For BGL parametrisation

$$a_1^f = -0.002 \pm 0.034(\text{stat}) \pm 0.046(\text{syst})$$

$$a_2^f = 0.93_{-0.20}^{+0.05}(\text{stat})_{-0.38}^{+0.04}(\text{syst})$$

Parameters in agreement with the results on $B \rightarrow D^* \ell \nu$ from b-Factories
No significant SU(3) breaking!

These results and techniques are paving the road for ongoing tests of LFU in the B_s sector

$B \rightarrow D^{(*)} \tau \nu$

Lepton Universality

- Lepton Universality is a key feature of the Standard Model
- The only difference between electrons, muons and taus is the mass
 - Once corrected for the lepton masses, the decays with electrons, muons and taus should be identical!
 - LFU Violation would be a clear signature of BSM Physics
- 1) Deviations with expectations observed in $b \rightarrow s$ transitions

$$R(K) = \frac{\mathcal{B}(B \rightarrow K \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K e^+ e^-)} \qquad R(K^*) = \frac{\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^* e^+ e^-)}$$

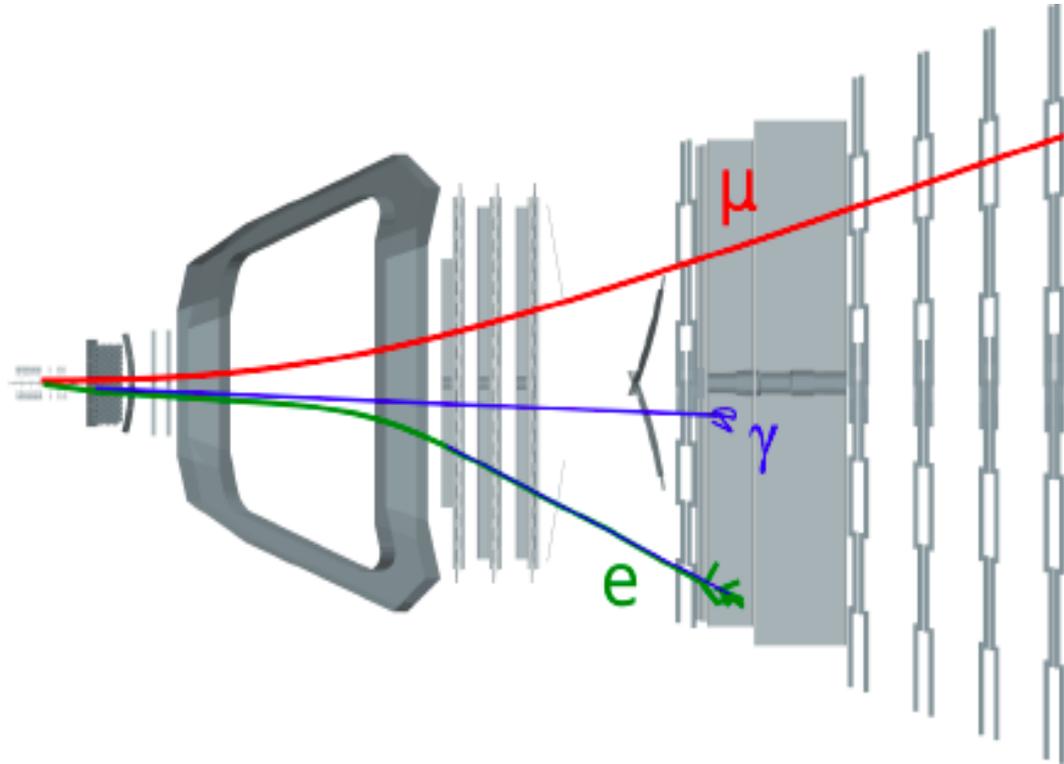
- 2) Deviations with expectations observed in $b \rightarrow c$ transitions

$$R(D) = \frac{\mathcal{B}(B \rightarrow D \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D \ell \nu_\ell)} \qquad R(D^*) = \frac{\mathcal{B}(B \rightarrow D^* \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^* \ell \nu_\ell)}$$

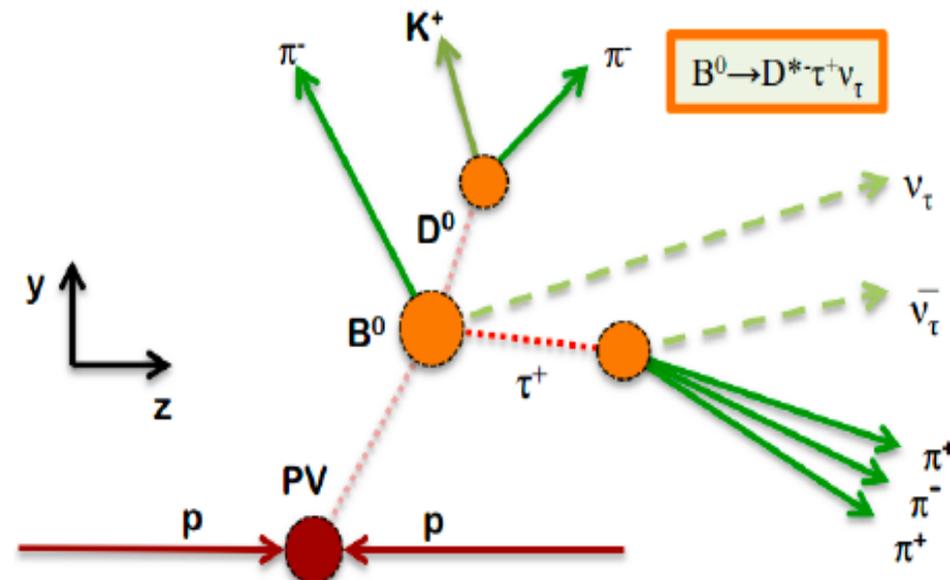
- The SM predictions have reduced unknown hadronic contributions!

Lepton Identification is Not Universal

- **Muons:**
 - Stable within LHCb
 - No radiation
- **Electrons:**
 - Bremsstrahlung emission in the detector: partially recovered from a detected γ
 - Contamination from γ conversions



- **Taus:**
 - Short lifetime: we see only the products
 - Neutrinos in the final state: $\tau \rightarrow \mu\nu\nu$, $\tau \rightarrow \pi\nu$, $\tau \rightarrow \pi\pi\pi\nu$
 - Large contamination from other heavy meson decays



$B \rightarrow D^{(*)} \tau \nu$: measurements

- Experiment can access directly $R(D)$ and $R(D^*)$ ratios

$$\mathcal{R}(D) = \frac{\Gamma(B \rightarrow D \tau \nu_\tau)}{\Gamma(B \rightarrow D \ell \nu_\ell)_{\ell = e, \mu}}$$

$$\mathcal{R}(D^*) = \frac{\Gamma(B \rightarrow D^* \tau \nu_\tau)}{\Gamma(B \rightarrow D^* \ell \nu_\ell)_{\ell = e, \mu}}$$

Signal

$$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$$

Normalization

(largest background)

$$\mathcal{R}(D^{(*)}) = \frac{N_{sig}}{N_{norm}} \times \frac{\epsilon_{norm}}{\epsilon_{sig}}$$

Several experimental and theoretical uncertainties cancel in ratio

- $D^{(*)}$ reconstruction / Particle ID /tracking eff.
- $|V_{cb}|$ & Form Factors (partially)

Very precise

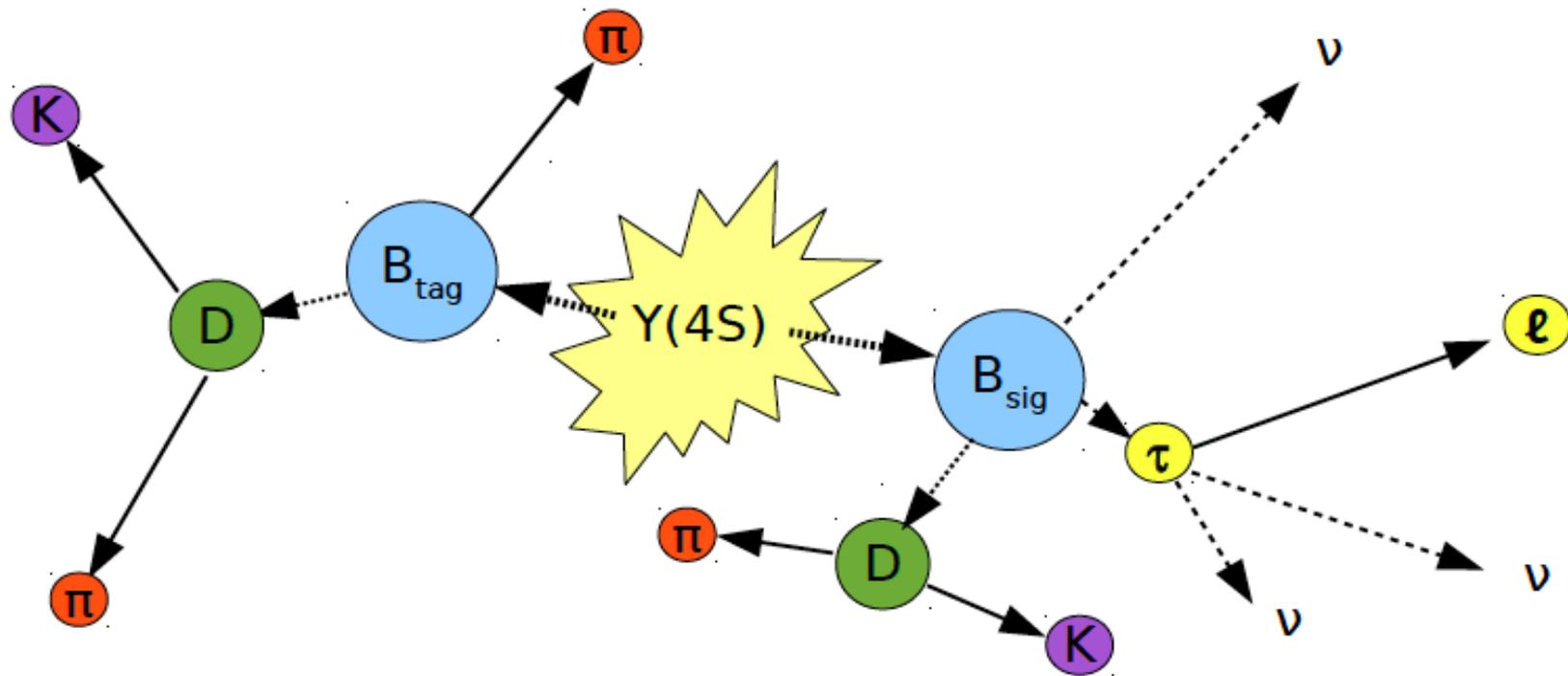
SM prediction

$$R(D) = 0.299 \pm 0.004 \quad \sigma = 1.0\%$$

$$R(D^*) = 0.258 \pm 0.005 \quad \sigma = 2.0\%$$

Weak signal signature

- Many neutrinos in the final state
- Lack of kinematics constraints in the final state



- Tag B determines charge and momentum of signal B
- All remaining particles must come from signal B: Little activity in the Calorimeter

Results of Fit $B \rightarrow D^{(*)}\tau\nu$

PRL 109, 101802 (2012)
PRD 88, 072012 (2013)

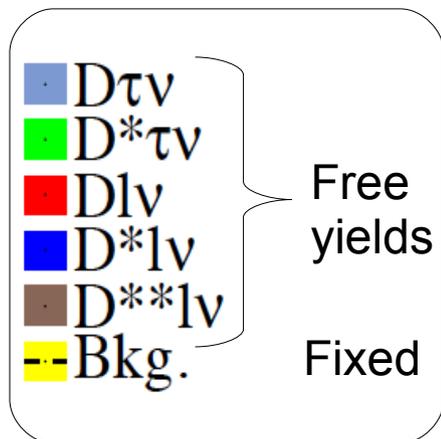
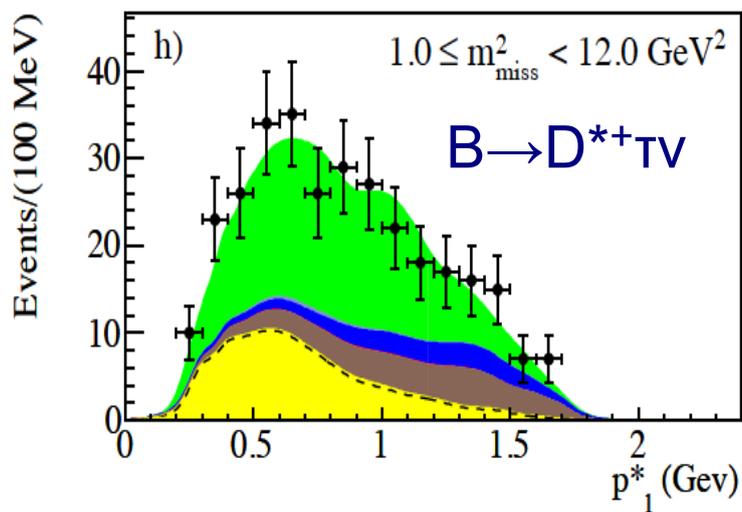
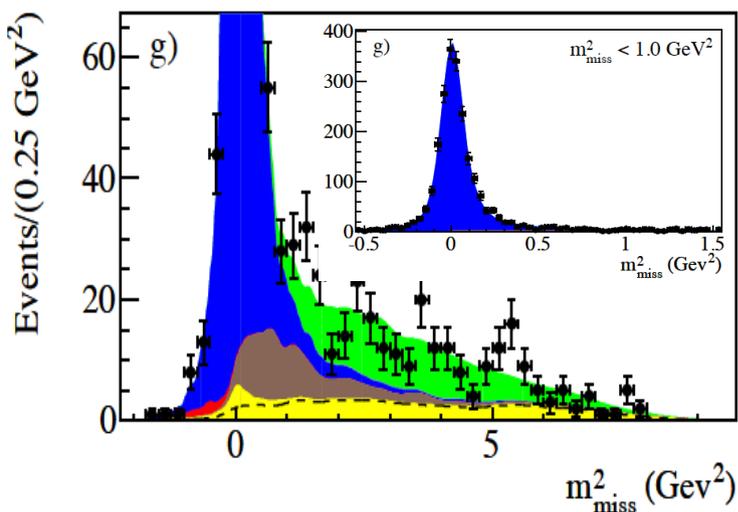
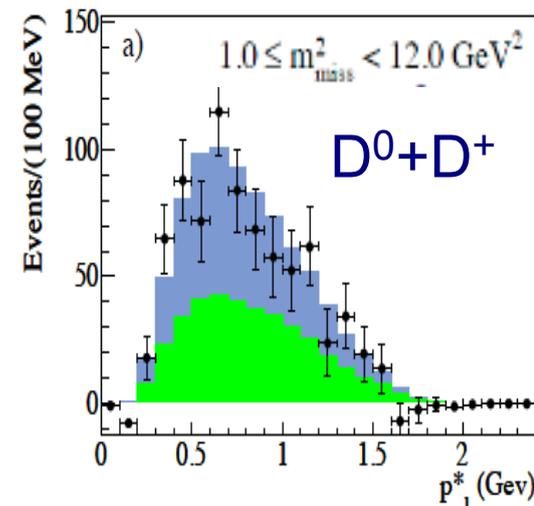
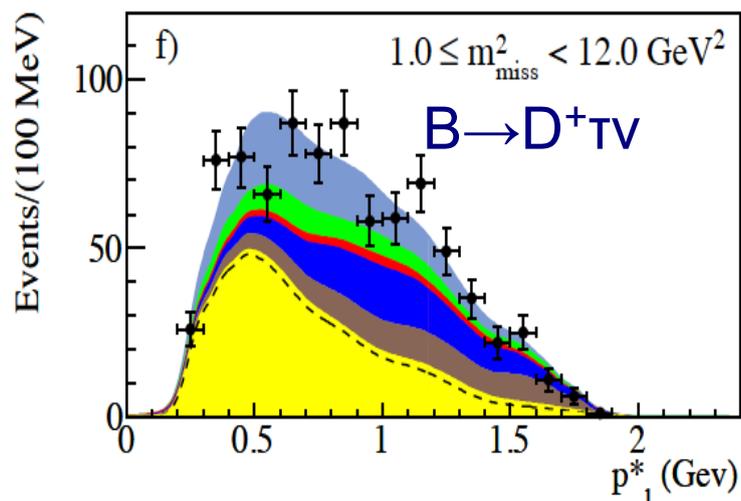
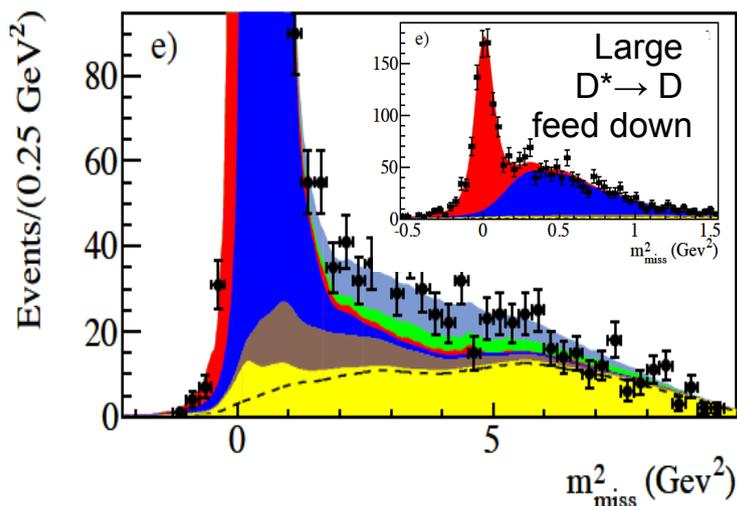


Signal signature:

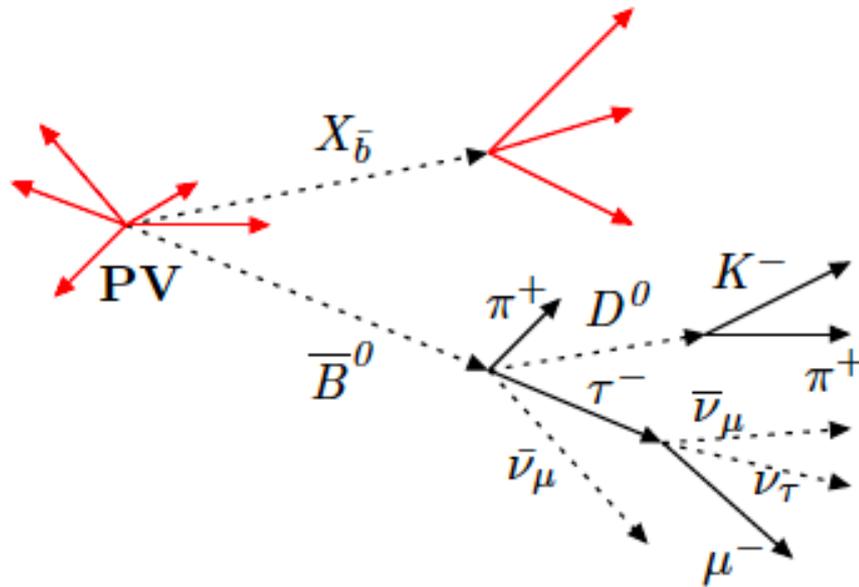
- Large missing momentum
- Softer muon from Tau decays

$$m_{\text{miss}}^2 = (p_{e^+e^-} - p_{\text{tag}} - p_{D^{(*)}} - p_{\ell})^2$$

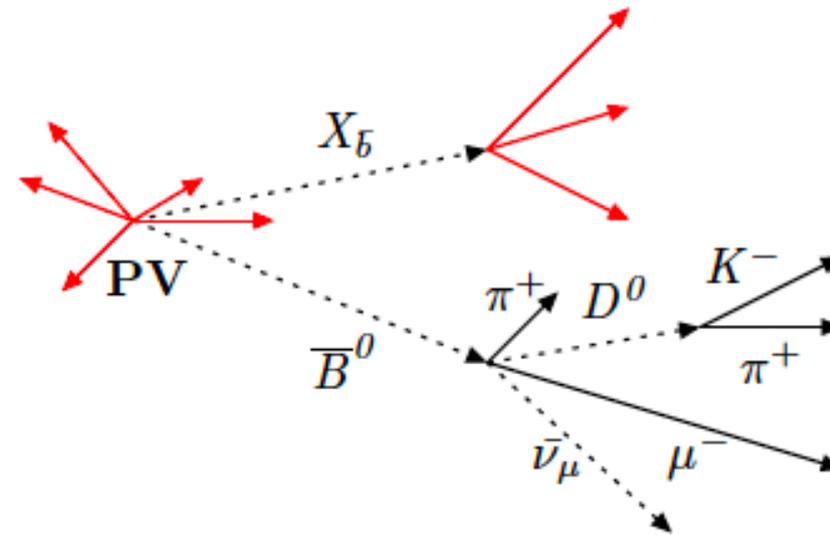
p_{ℓ}^* in the B_{sig} rest-frame



Signal ($B^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$)



Normalisation ($B^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu$)

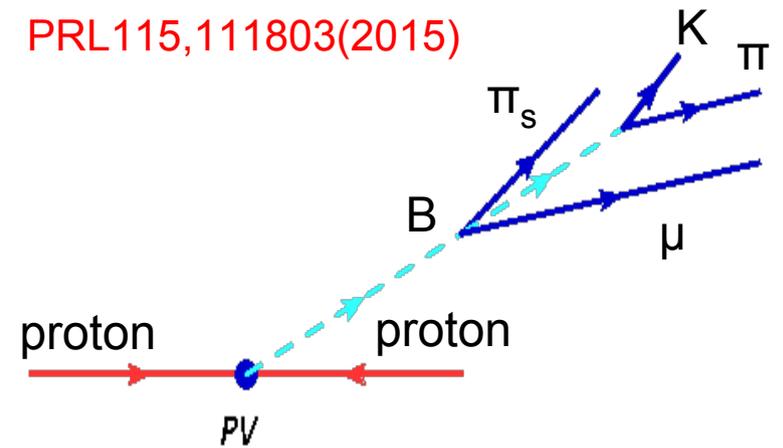


- Trigger on the charm component (to not bias the signal extraction)
- Selection exploiting excellent LHCb performances of the VELO and the particle identification
- Full selection efficiency ratio $\varepsilon_\tau / \varepsilon_\mu = (77.6 \pm 1.4) \%$
 - Lower p_τ and worst vertex in the tau decay

B rest-frame determination

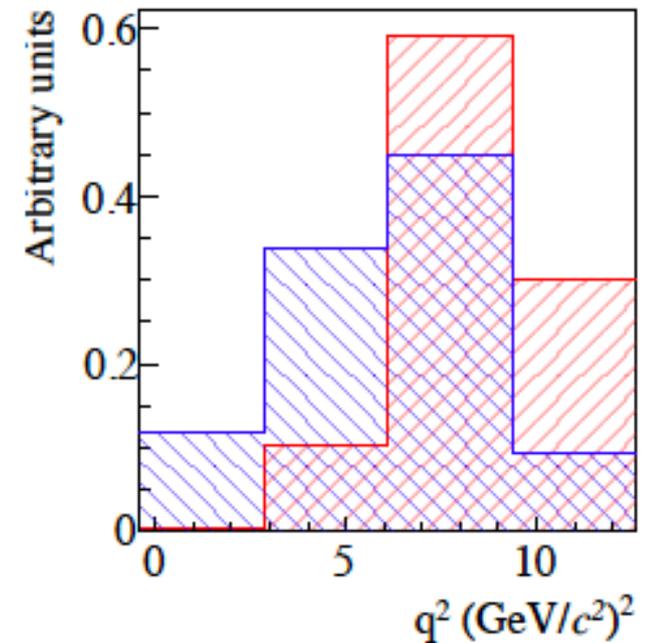
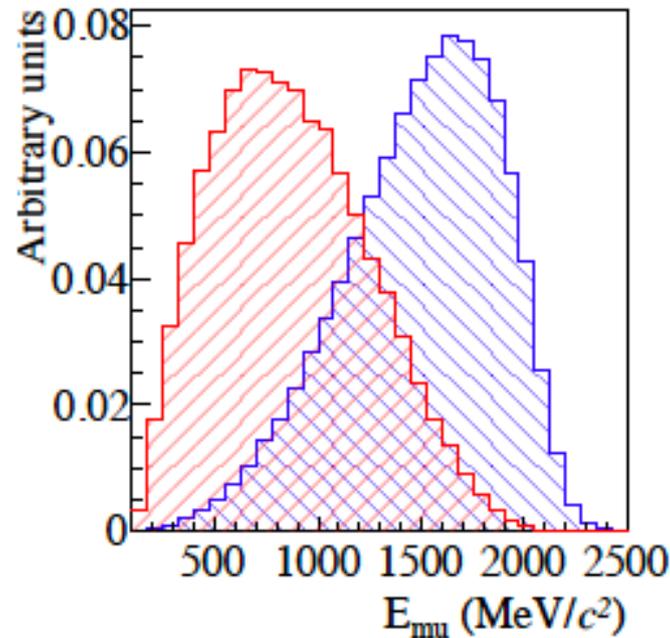
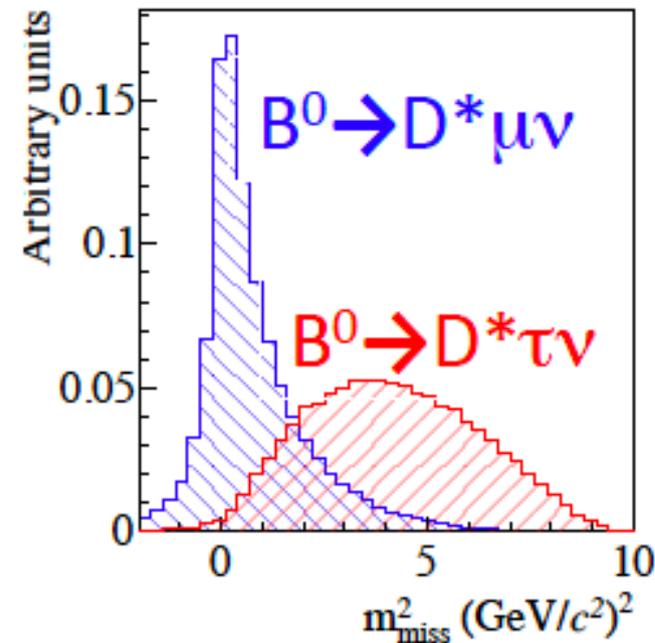
PRL115,111803(2015)

- B momentum unknown in production from pp collision in LHCb
 - B mainly from $gg \rightarrow b\bar{b}$
- Transverse missing momentum is known but no way of measuring longitudinal component
 - B boost \gg energy released in the decay
 - $\sim 18\%$ resolution on p_B



boost-approximation

$$p_z(B^0) = \frac{m_{B^0}}{m(D^* \mu)} p_z(D^* \mu)$$



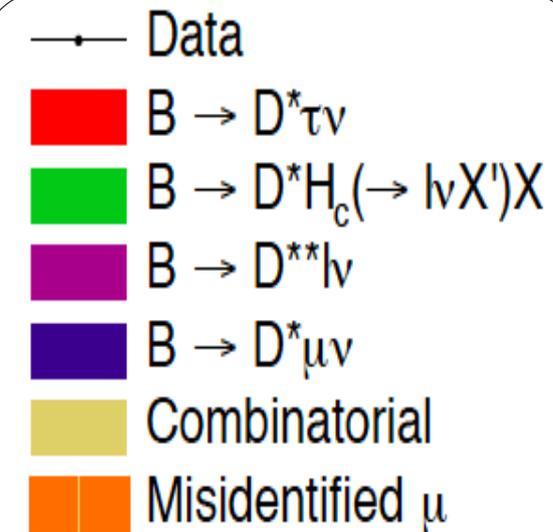
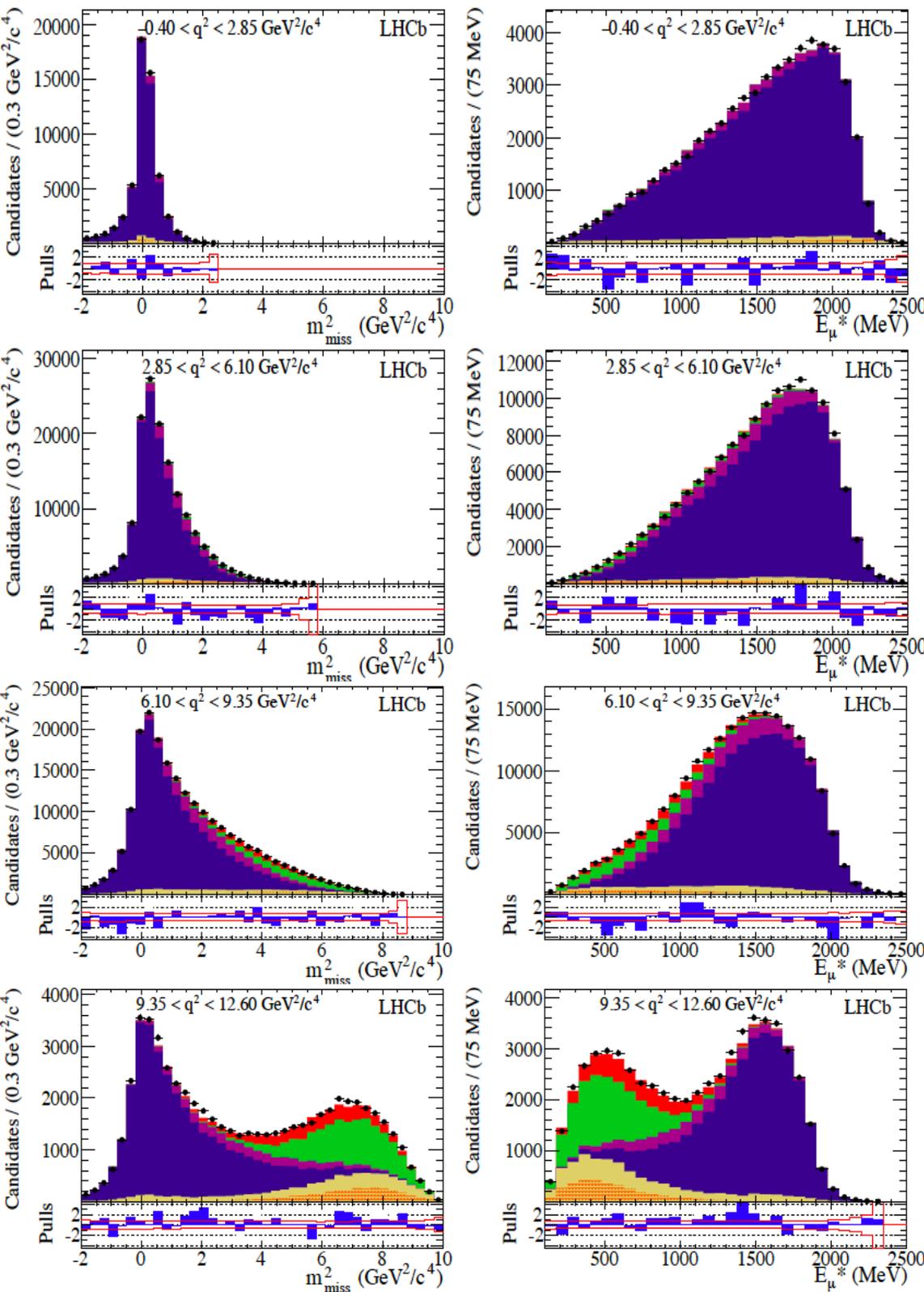
Results (4 q^2 bins)



- Binned 3-D fit in m_{miss}^2 , E_μ and q^2 (40 x 30 x 4 bins)

$$R(D^*) = 0.336 \pm 0.027 \pm 0.030$$

- In agreement with BaBar and Belle measurements
- 2.1 σ higher than SM



- Compared to leptonic τ decay, the largest source of contamination comes from $B \rightarrow D^* 3\pi X$ decays: completely different backgrounds, and new opportunities to control them!
- Signal normalized to $B \rightarrow D^* 3\pi$

$$K(D^*) \equiv \frac{Br(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau)}{Br(B^0 \rightarrow D^{*-} 3\pi)} = \frac{N_{D^* \tau \nu_\tau}}{N_{D^* 3\pi}} \times \frac{\epsilon_{D^* 3\pi}}{\epsilon_{D^* \tau \nu_\tau}} \times \frac{1}{Br(\tau^+ \rightarrow 3\pi(\pi^0) \bar{\nu}_\tau)}$$

- Signal and normalization share the same visible final state
 - Cancel most of the systematics: PID, trigger, tracking efficiency

$$R(D^*) = K(D^*) \times \frac{Br(B^0 \rightarrow D^{*-} 3\pi)}{Br(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}$$

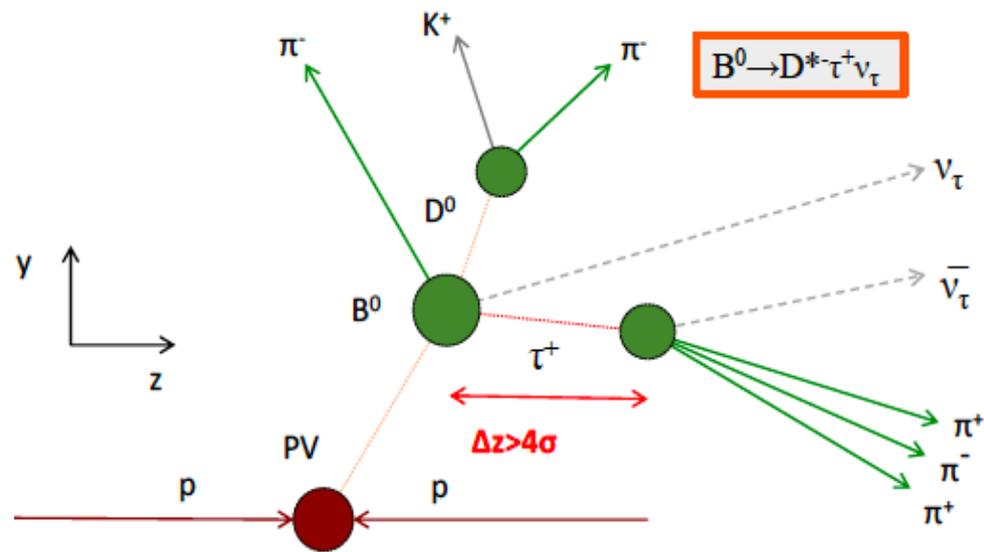
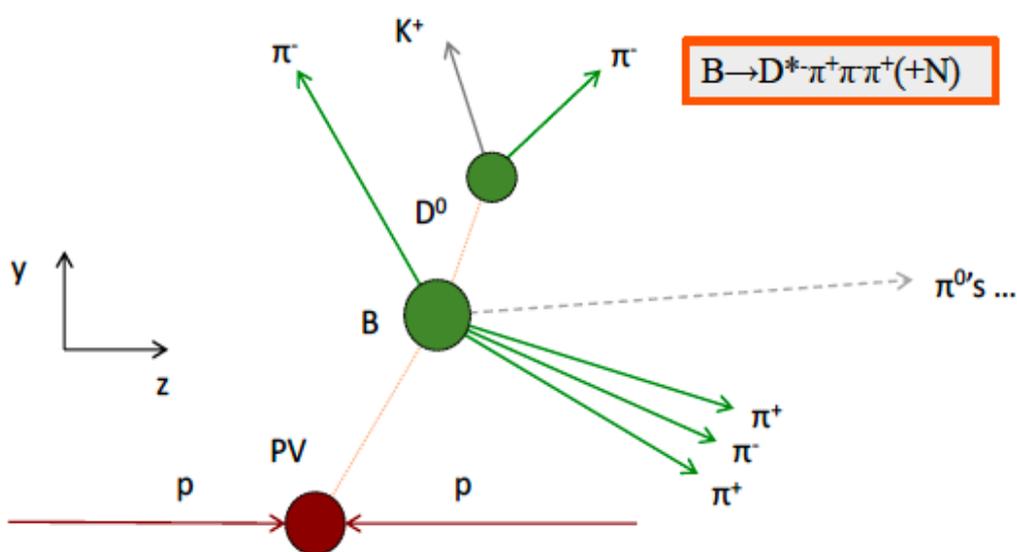
4% precision from PDG2017 

2% precision from HFLAV2018 

B \rightarrow D* $\tau\nu$: background reduction

PRL120(2018)171802
PRD97(2018)072013

- Decay topology exploited to suppress the abundant background from $H_b \rightarrow D^*3\pi X$ (BR $\sim 100 \times$ Signal)

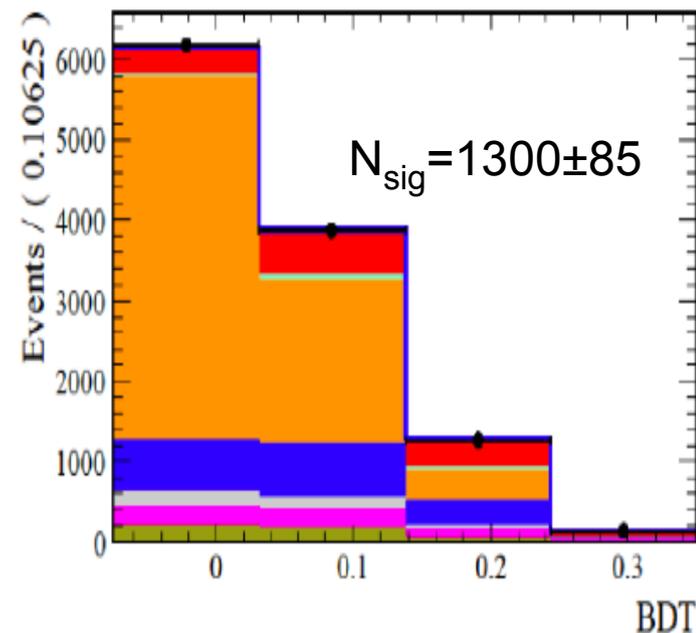
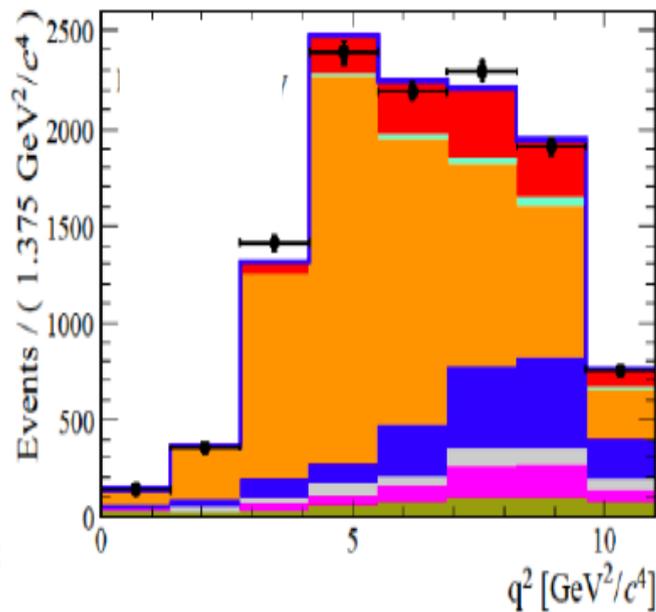
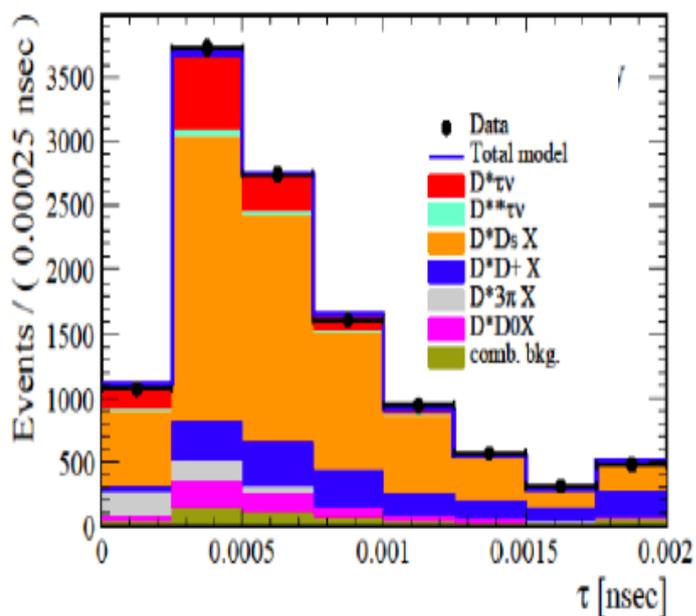
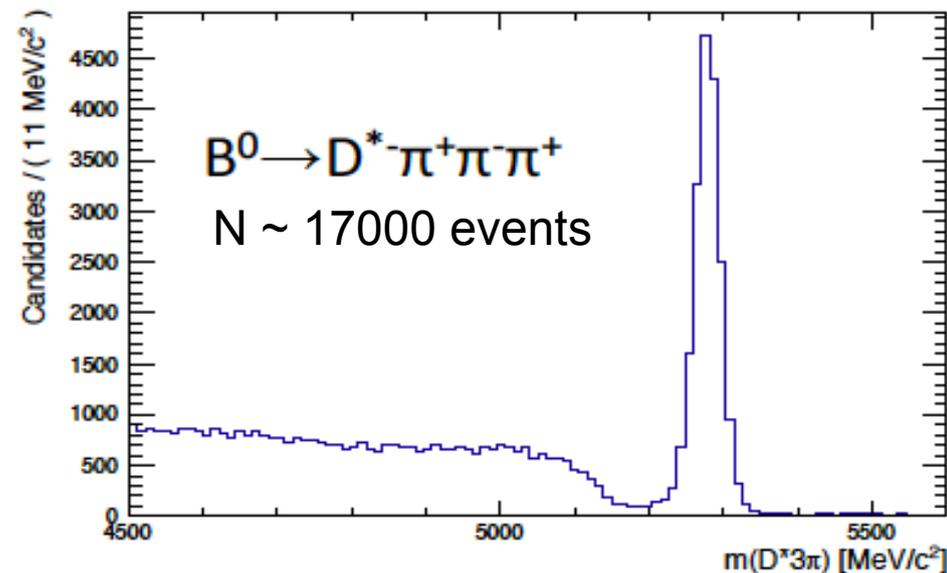


- Minimum distance between H_b and τ required: reduce these background by a factor 1000
 - Remaining backgrounds contains two charm hadrons:
 - uses informations from additional energy around the t direction, and the resonant structure in the $D^*3\pi$ system (BDT)
- $X_b \rightarrow D^{*-} D_s^+ X$: $\sim 10 \times$ signal
 - $X_b \rightarrow D^{*-} D^+ X$: $\sim 1 \times$ signal
 - $X_b \rightarrow D^{*-} D^0 X$: $\sim 0.2 \times$ signal

Fit results

PRL120(2018)171802
PRD97(2018)072013

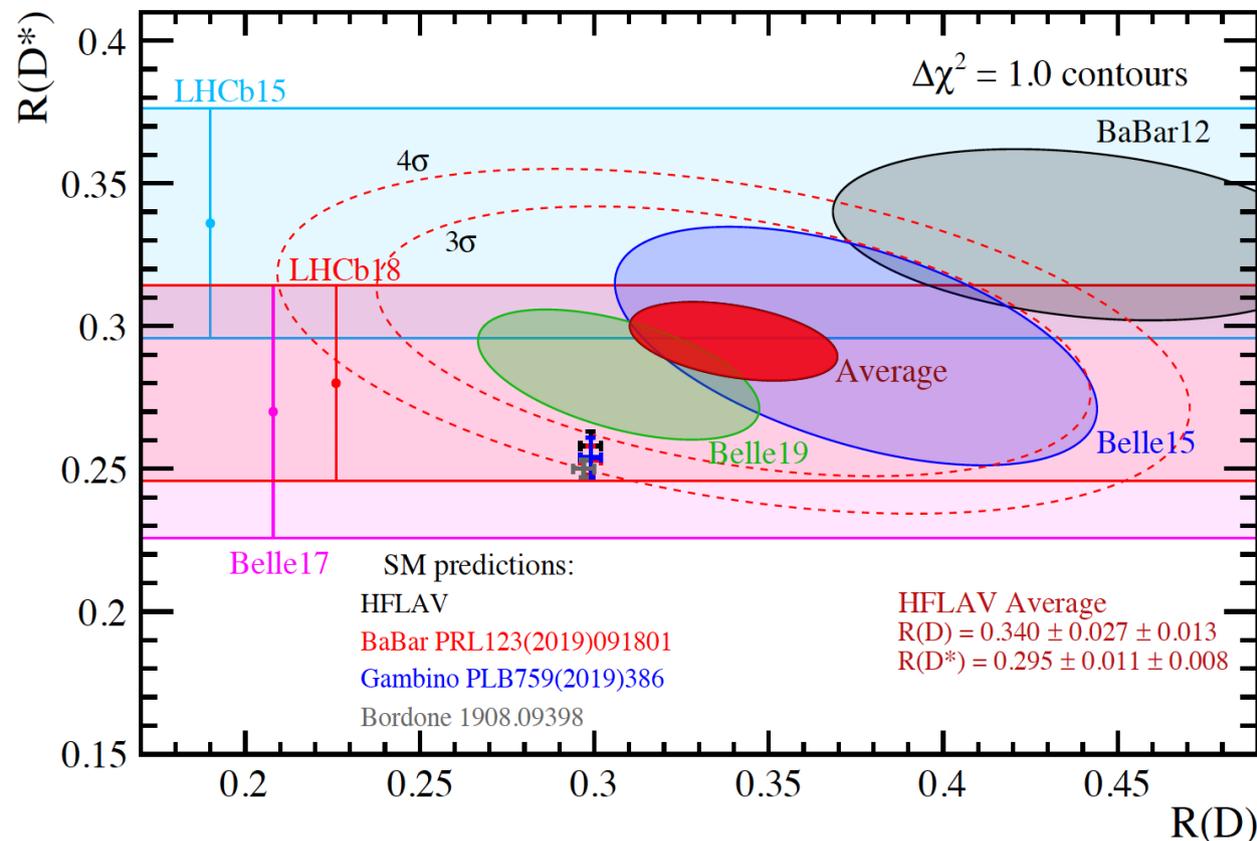
- Normalization mode 
- Signal extracted from 3D fit on
 - q^2 (8 bins)
 - 3π decay time (8 bins)
 - BDT (4 bins)



$$R(D^*) = 0.283 \pm 0.019 \pm 0.025 \pm 0.013 \text{ (from external inputs)}$$

Status of R(D)-R(D*)

Isospin breaking due to QED
PRL120(2018)261804



$$R(D^*) = 0.295 \pm 0.011 \pm 0.008$$

$$R(D) = 0.340 \pm 0.027 \pm 0.013$$

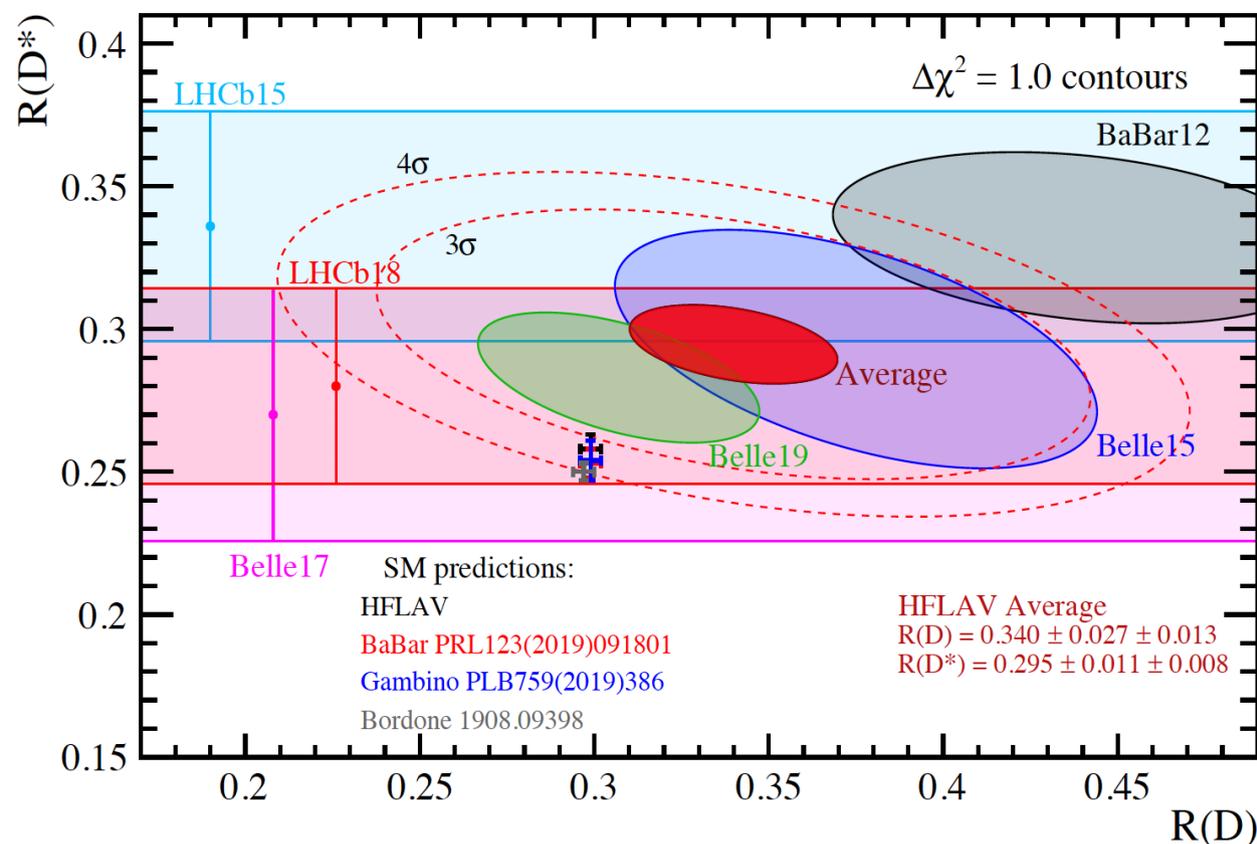
- The uncertainty on the additional form factors needed for massive leptons (Ht) is the dominant source of uncertainty

- How reliable are these predictions?

- QED corrections?
- Form-Factors from Lattice?

	R(D)	R(D*)	RD-RD* # σ from SM	RD* only # σ from SM
Bernlochner et al. PRD95(2017)115008	0.299 \pm 0.003	0.257 \pm 0.003		
Bigi et al. JHEP1711(2017)061		0.260 \pm 0.008		
Jaiswal et al. JHEP1712(2017)060	0.299 \pm 0.004	0.257 \pm 0.005		
HFLAV	0.299\pm0.004	0.258 \pm 0.005	3.08	2.5
BaBar PRL123(2019),091801		0.253 \pm 0.005	3.43	2.8
Gambino et al. PLB795(2019)386		0.254 \pm 0.007	3.16	2.6
Bordone et al. ArXiv:1908.09398 (no exp.)	0.298 \pm 0.003	0.247 \pm 0.006	3.77	3.2
Bordone et al. ArXiv:1908.09398	0.297 \pm 0.003	0.250 \pm 0.003	3.87	3.2

Status of R(D)-R(D*)



$$R(D^*) = 0.295 \pm 0.011 \pm 0.008$$

$$R(D) = 0.340 \pm 0.027 \pm 0.013$$

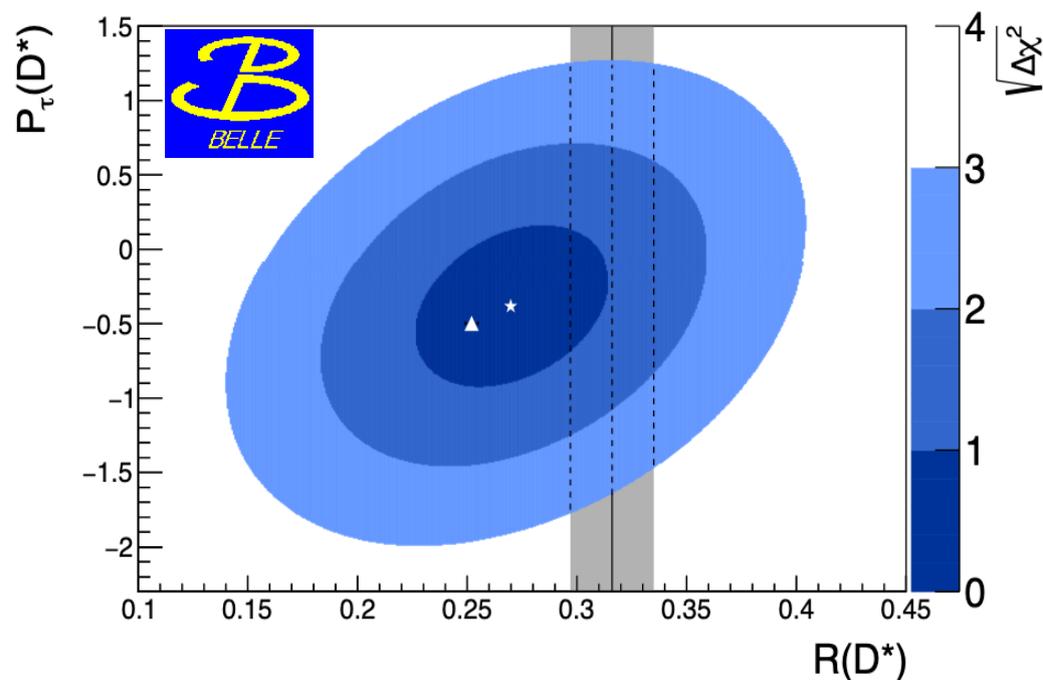
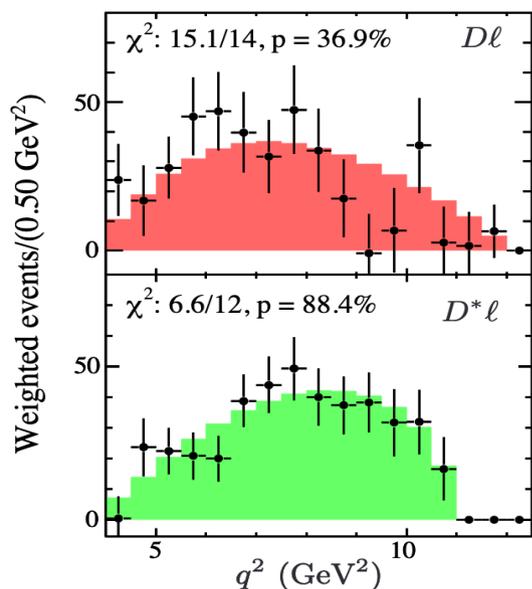
- The uncertainty on the additional form factors needed for massive leptons (Ht) is the dominant source of uncertainty

- Common systematics:

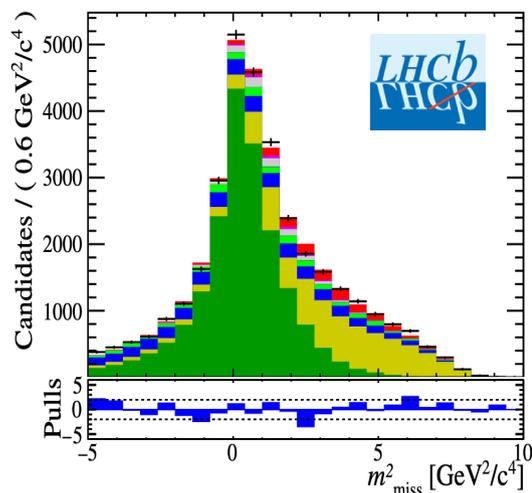
- $B \rightarrow D^{**} / B \rightarrow D^* X_c$
- QED correction: PHOTOS

	R(D)	R(D*)	RD-RD* # σ from SM	RD* only # σ from SM
Bernlochner et al. PRD95(2017)115008	0.299 ± 0.003	0.257 ± 0.003		
Bigi et al. JHEP1711(2017)061		0.260 ± 0.008		
Jaiswal et al. JHEP1712(2017)060	0.299 ± 0.004	0.257 ± 0.005		
HFLAV	0.299 ± 0.004	0.258 ± 0.005	3.08	2.5
BaBar PRL123(2019),091801		0.253 ± 0.005	3.43	2.8
Gambino et al. PLB795(2019)386		0.254 ± 0.007	3.16	2.6
Bordone et al. ArXiv:1908.09398 (no exp.)	0.298 ± 0.003	0.247 ± 0.006	3.77	3.2
Bordone et al. ArXiv:1908.09398	0.297 ± 0.003	0.250 ± 0.003	3.87	3.2

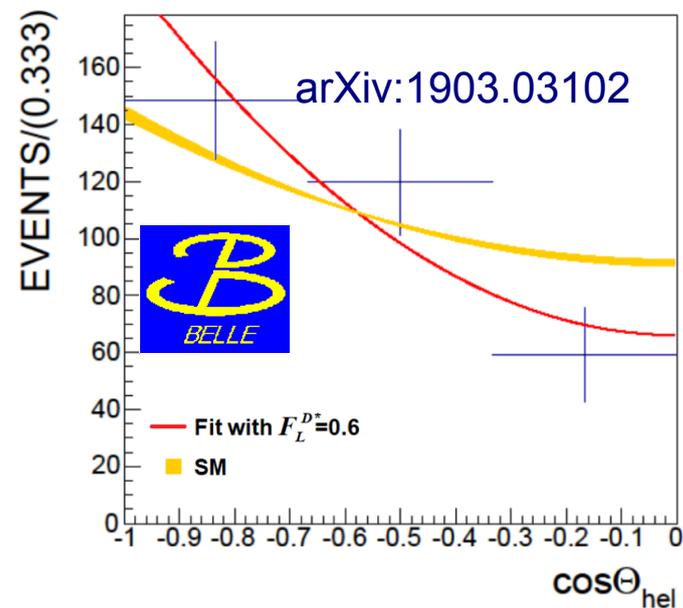
Beyond R(D)-R(D*) observables



$$R(J/\Psi) = \frac{\mathcal{B}(B_c \rightarrow J/\Psi \tau \nu)}{\mathcal{B}(B_c \rightarrow J/\Psi \mu \nu)}$$

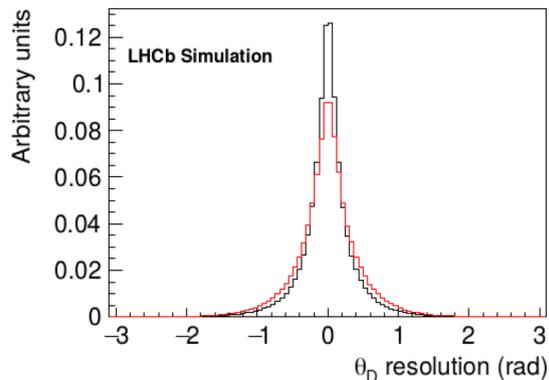
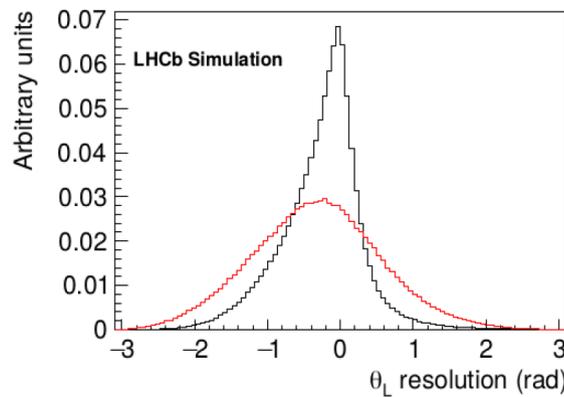
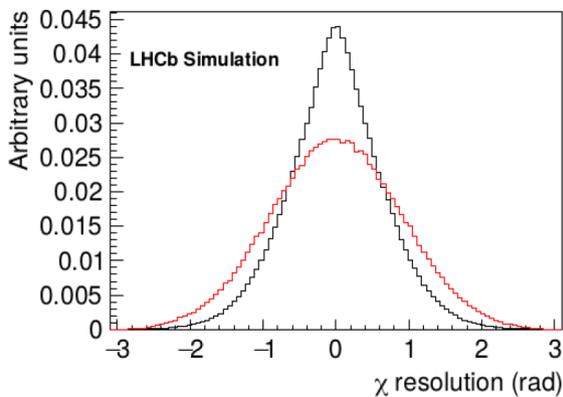


$R(J/\Psi) = 0.71 \pm 0.17 \pm 0.18$
 2 σ higher than the SM

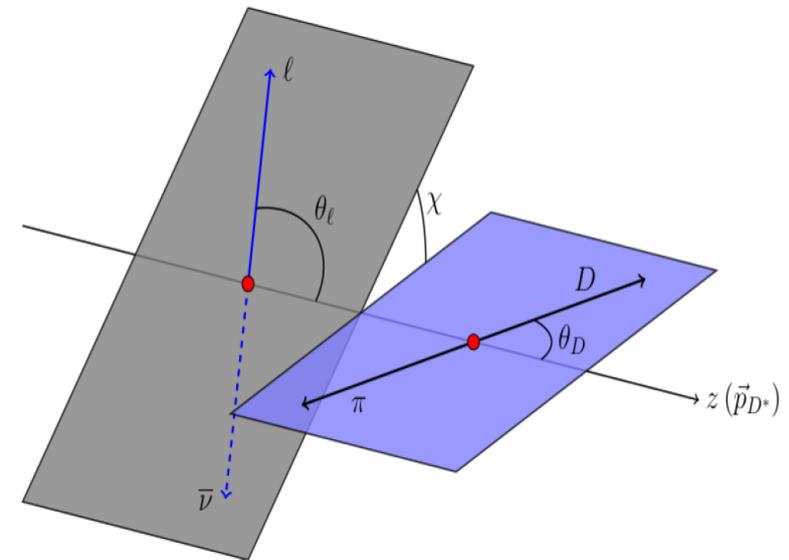


Angular analyses

- $B \rightarrow D^*$ and $B_s \rightarrow D_s^*$: rich angular structure can be exploited:
 - Strong sensitivity to NP Wilson coefficients (for example in arXiv:1602.03030)
 - Belle-II will further analyses these decays
 - With the very high statistics collected in LHCb it is possible to perform angular analysis even with a quite poor resolution on the angular observables

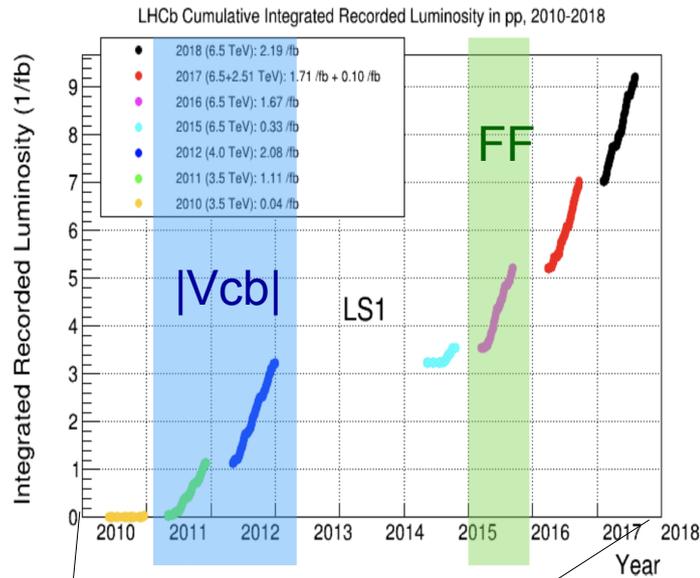


- $B \rightarrow D^* \tau \nu$, $\tau \rightarrow \mu \nu \nu$
- $B \rightarrow D^* \mu \nu$

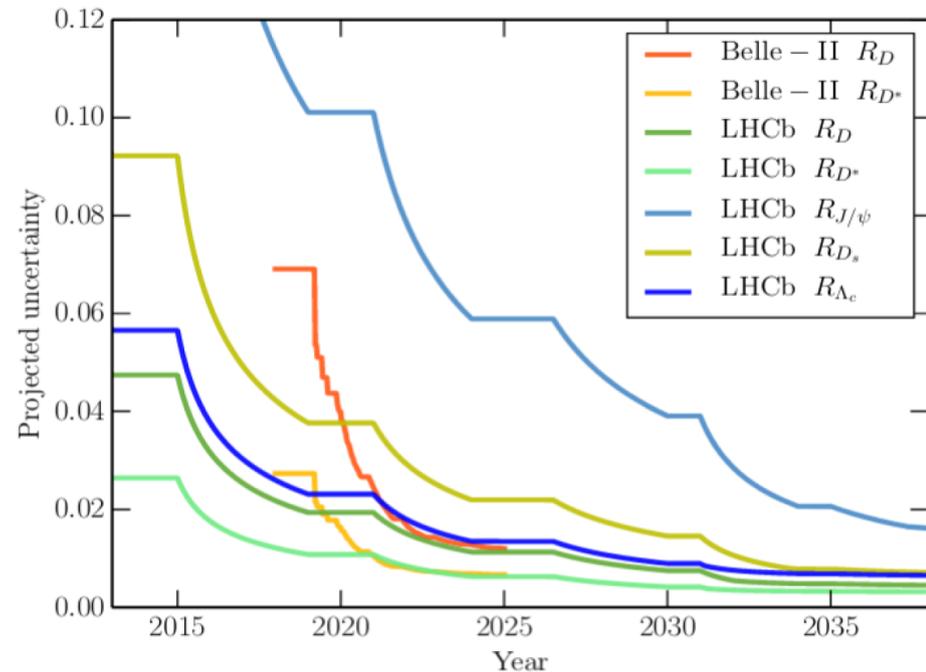
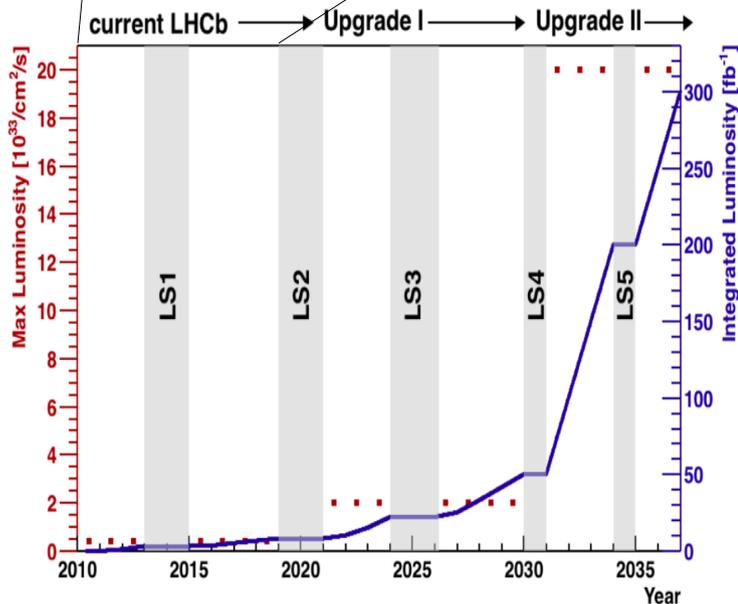


- For $B \rightarrow D^*$ with hadronic tau, a novel approach has been proposed in D. Hill et al. JHEP11(2019)133

Future steps: larger data samples



- In the coming years of data taking the integrated luminosity will greatly increase
- The higher statistics in the control regions will help in constraining the background model
- MC statistics is the limiting systematic in the present measurements
 - Fast simulations already developed arXiv:1810.10362



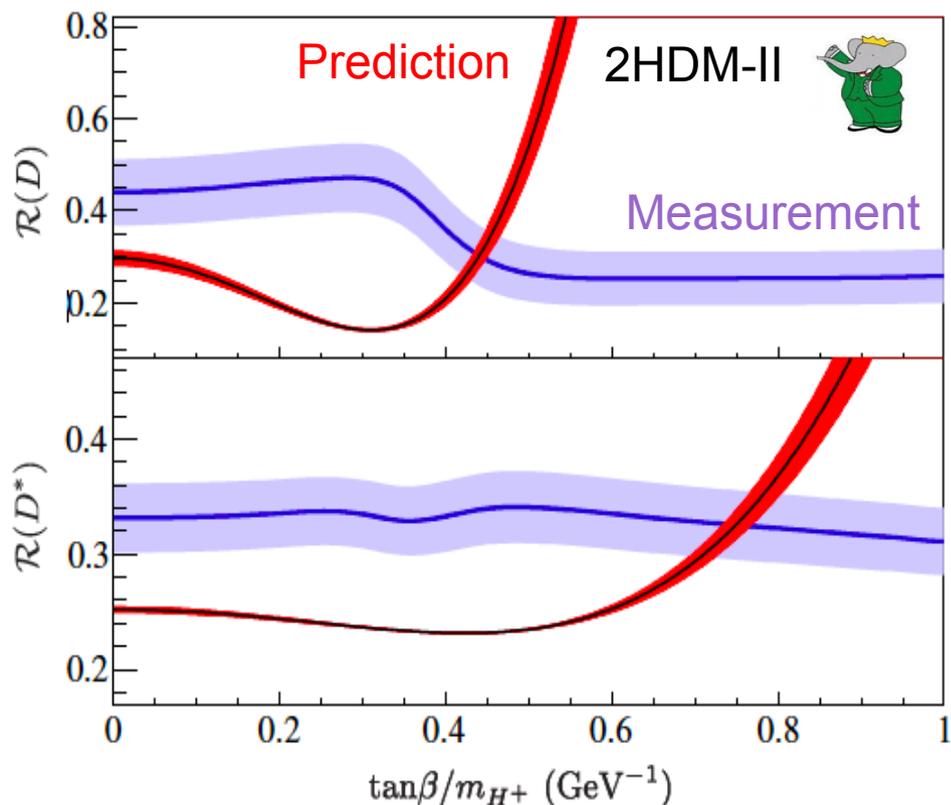
ArXiv:1809.06229

Conclusions

- Semileptonic decays of the B-hadrons are a rich mine of good physics
- They requires close interplay between theorists and experimentalist
- CKM elements: the Inclusive-Exclusive puzzle have to be understood!
 - Inclusive measurements will be dominated by Belle-II in the near future!
 - On exclusive measurements LHCb has shown un-expected great capabilities
- The $R(D)$ - $R(D^*)$ anomalies requires further checks
 - Studies in different hadrons are ongoing: $R(D_s)$, $R(D_s^*)$, $R(\Lambda_c)$, $R(J/\Psi)$
 - Exploit $b \rightarrow u$ transitions: $R(\pi)$, $R(\rho)$, $R(p)$
 - With the increasing in precision, it is crucial to consider effects not considered so far: QED corrections
 - If these anomalies are due to fluctuations, limited QCD understanding, systematics, we will know soon!
 - Crucial to **exploit all the data we already have in LHCb**
 - **Belle-II could confirm/disprove** (Confirmations are important as first measurements!)

Backup

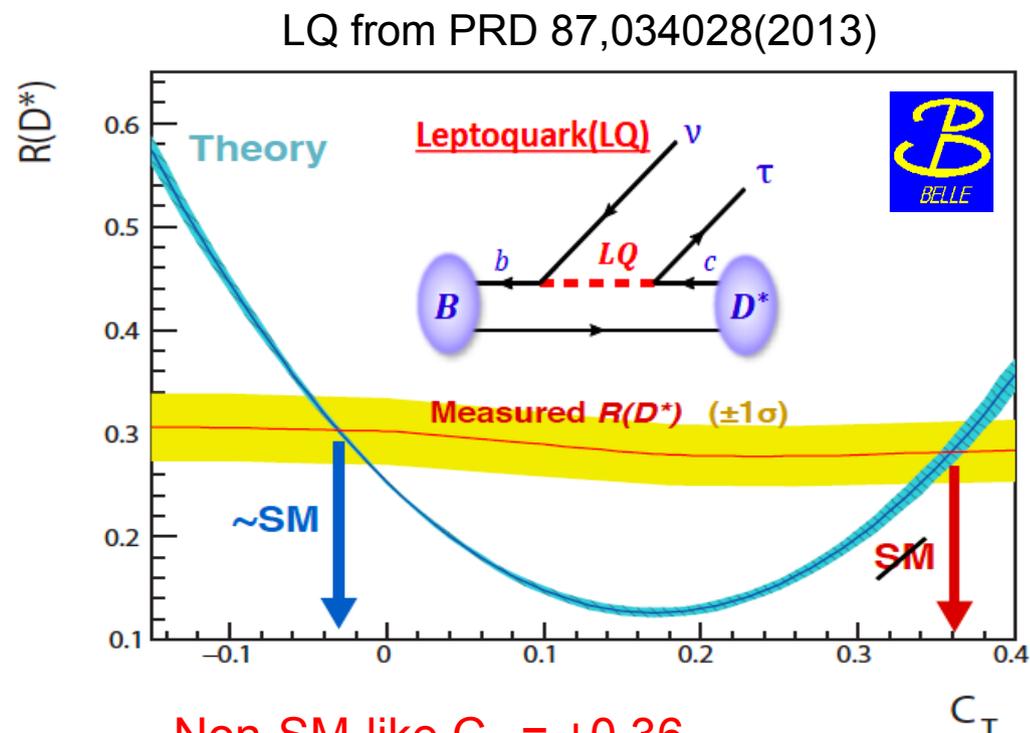
Large New Physics Effect! $H^2, LQ, ?$



$$\mathcal{R}(D) \implies \tan\beta/m_H = 0.44 \pm 0.02$$

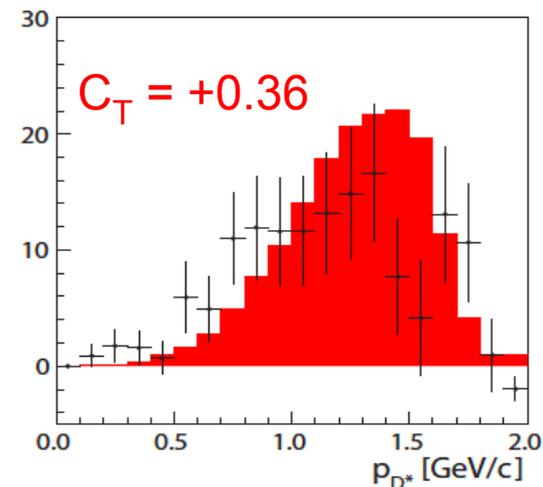
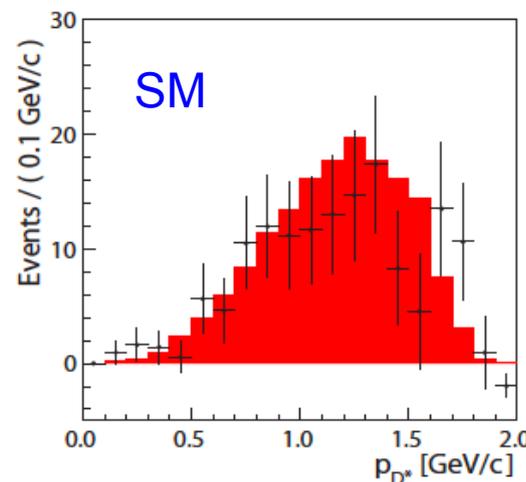
$$\mathcal{R}(D^*) \implies \tan\beta/m_H = 0.75 \pm 0.04$$

- The combination of $\mathcal{R}(D)$ and $\mathcal{R}(D^*)$ excludes the 2HDM-II
- More general 2HDM-III can explain the data (more parameters)



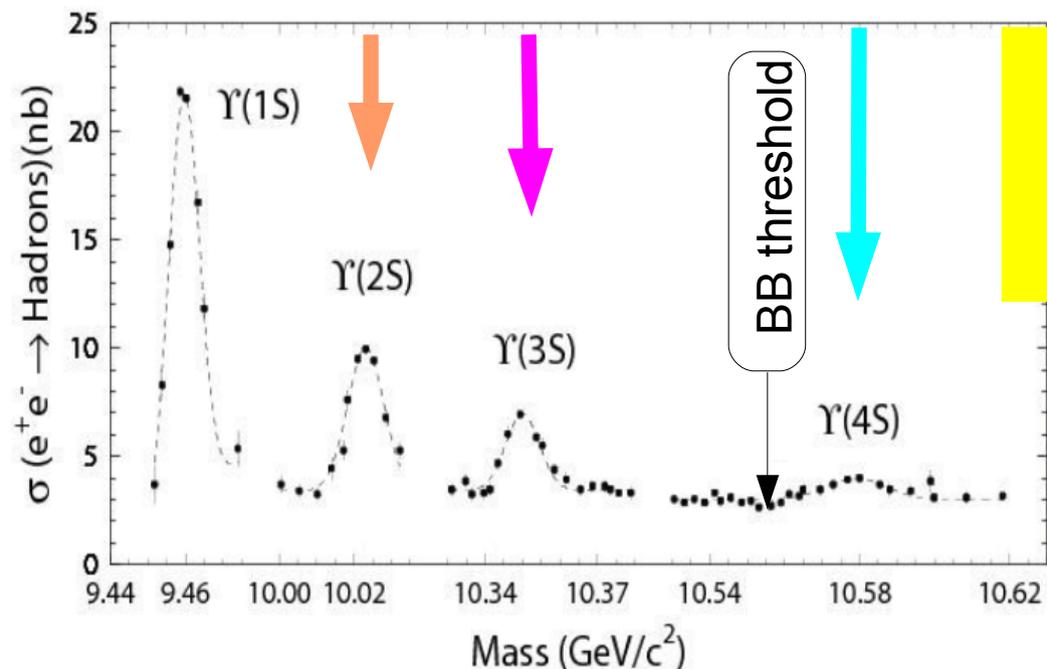
Non-SM-like $C_T = +0.36$

But disagreement in D^* momentum

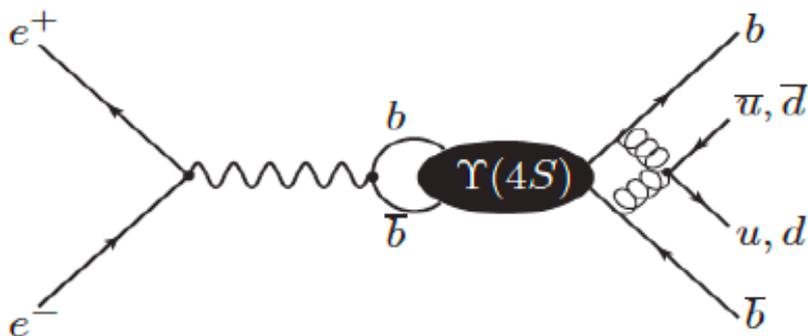


B-Factories BaBar and Belle

- CM energy of the $\Upsilon(4S) = 10.58 \text{ GeV}$ most of the time
 - Large production of B meson from Υ decays
 - $\sigma_{10.58\text{GeV}}(e^+e^- \rightarrow b\bar{b}) = 1.06\text{nb}$
 - Run at $\Upsilon(5S)$ allows to access the B_s mesons



$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

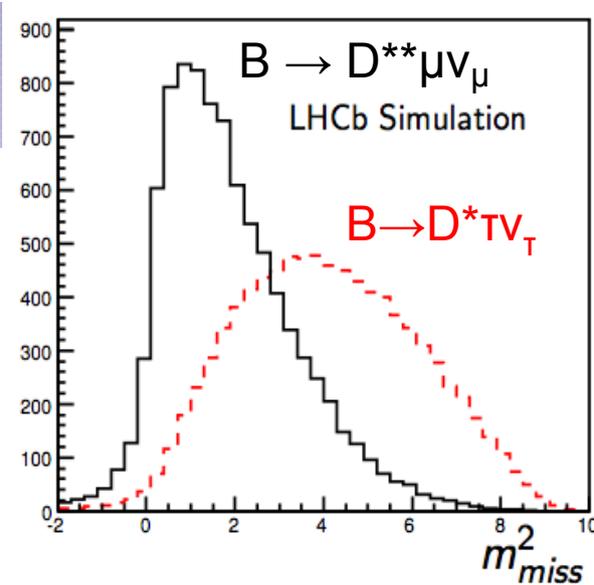


B-Factories: hermetic detectors, low background, Excellent PID, access (mainly) at $B^{0/+}$

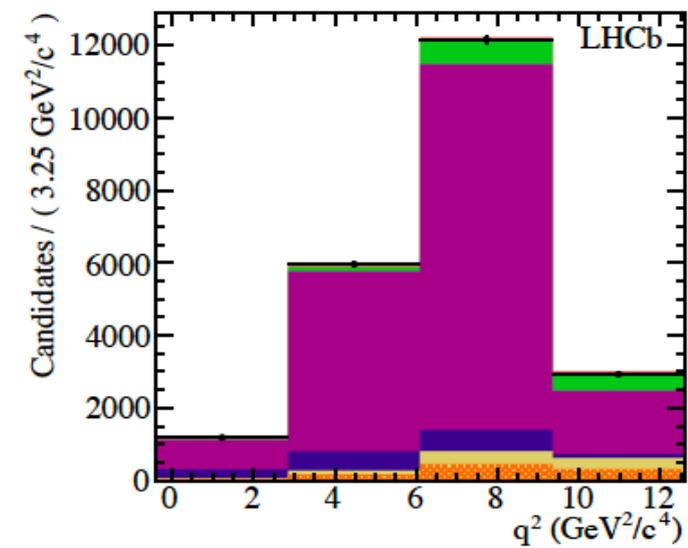
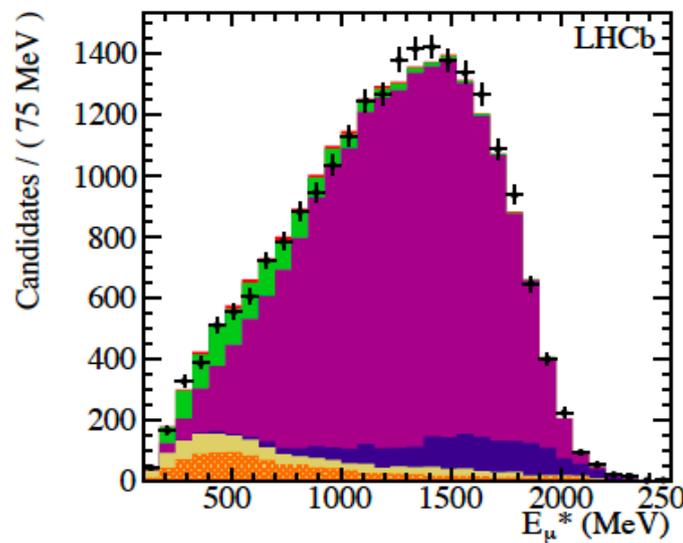
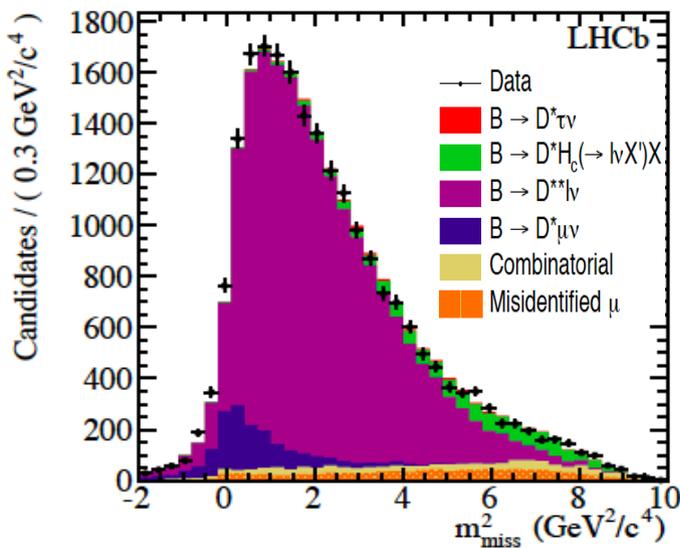
About $(771 + 467) \times 10^6$
 $e^+e^- \rightarrow BB$ events in
 the Belle+BaBar data

D** backgrounds

- $B \rightarrow D^{**} \mu \nu_\mu$ where D^{**} refers to any resonant or non resonant excited charm state
 - Separate templates for narrow resonances $D_1(2420)$, $D_2^*(2460)$, $D_1'(2430)$
 - Form Factor from LLSW model with slope of IW function floated



D* mu pi control sample



- $B \rightarrow D^* \pi \pi \mu \nu_\mu$ recently measured by BaBar
 - Modelled using ISGW2 parameterization
 - q^2 distribution tuned on data with $D^* \mu \pi \pi$ control sample

D^{**} Background is
~12% of the normalization
mode