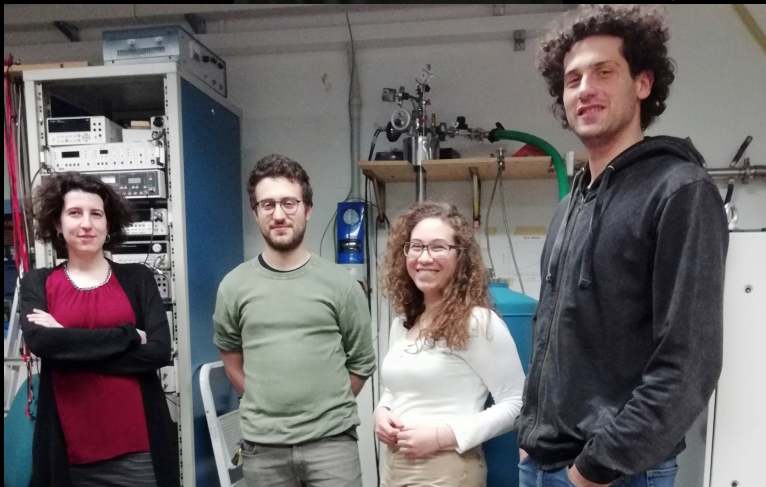


# The Josephson effect for (superconducting) hybrids solutions for quantum technologies



*Halima Ahmad, Roberta Caruso, Davide Massarotti, Alessandro Miano, Domenico Montemurro, Loredana Parlato, Giampiero Pepe, Roberta Satariano, Daniela Stornaiuolo & Francesco Tafuri*

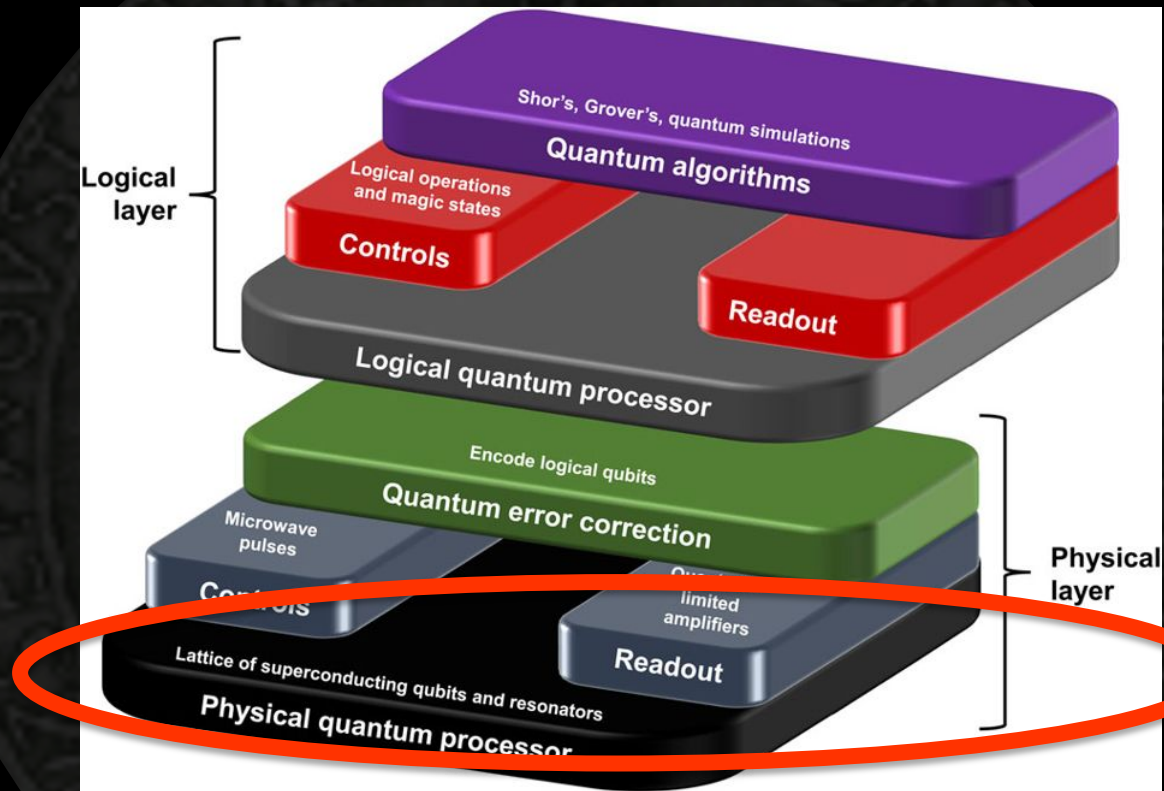
*Università di Napoli "Federico II" Italy*



*Oleg Mukanhov, Marco Arzeo,  
Matthew Hutchings*



# Rewinding the tape to touch the macroscopic quantum world



Jay M. Gambetta, Jerry M. Chow & Matthias Steffen

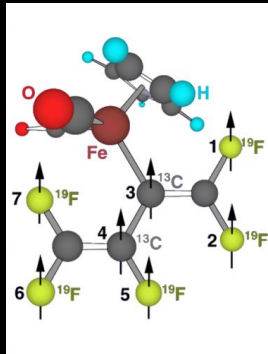
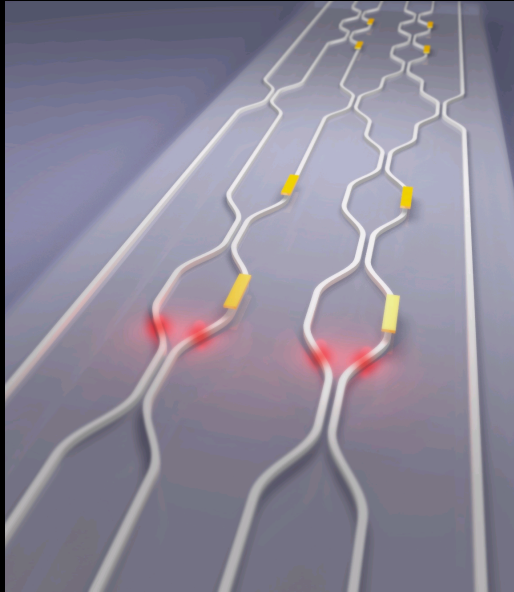
*npj Quantum Information* **3**, Article number: 2 (2017)

# Physical implementations ?

## NMR



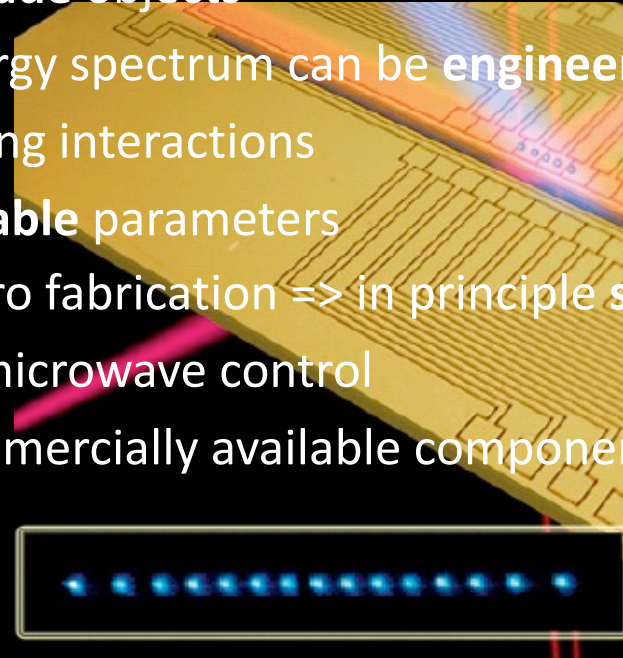
## Photons



## Trapped ions (or atoms)

### manmade objects

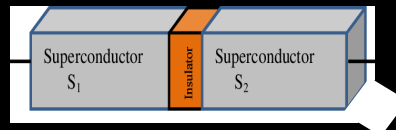
- energy spectrum can be engineered
- strong interactions
- **tunable** parameters
- micro fabrication => in principle **scalable**
- all **microwave** control
- **commercially available** components



## Electrical circuits ?

**usually not quantum !**

**A quantum component  
The Josephson junction**



Quantum Mechanics of a Macroscopic Variable:  
The Phase Difference of a **Josephson Junction**





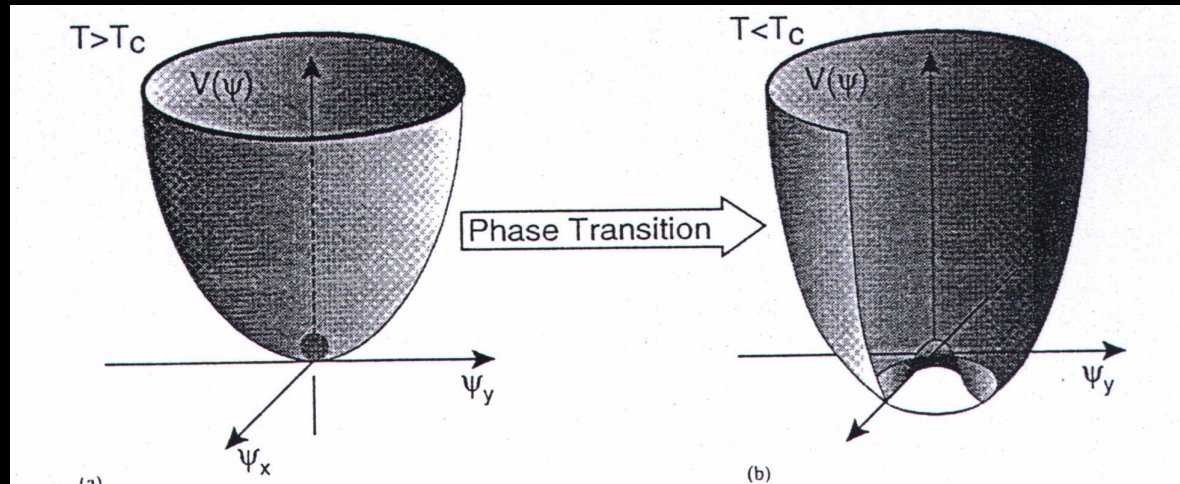
## Superconducting phase qubits

John M. Martinis

Superconducting qubit research began in the 1980s motivated by the question, posed by Anthony Leggett, whether macroscopic variables would behave in a quantum mechanical fashion [23]. Initial experiments verified quantum behavior via the phenomenon of tunneling out of the zero-voltage state of a current-biased Josephson junction [7]. At UC Berkeley, quantum mechanical behavior was also demonstrated by the existence of quantized energy levels [28]. This observation provided stronger proof of quantum behavior, and established at an early stage (before the ideas of qubits were even widely established) that superconducting circuits could be used as general quantum systems [3].

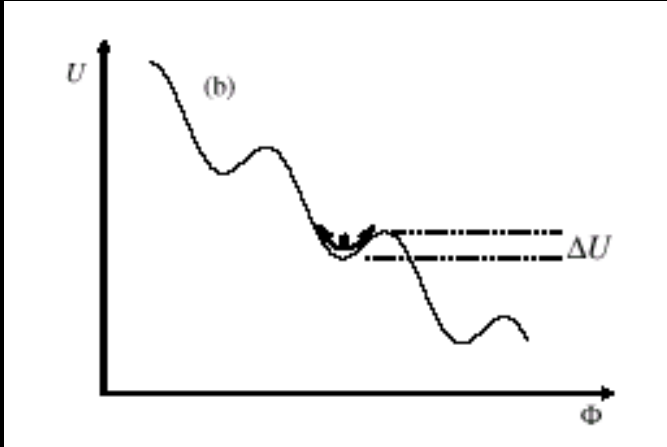


# Superconductivity as a Macroscopic Quantum Phenomenon



$$\psi = n_s e^{i\Phi}$$

*Quantum behavior displayed by a single macroscopic degree of freedom (the phase difference across a current-biased Josephson tunnel junctions): whether or not macroscopic systems like this exhibit quantum mechanical behavior, for example zero point motion, macroscopic quantum tunneling, or quantization of energy.*



**news and views**

# Schrödinger's cat is now fat

Gianni Blatter

Schrödinger's dead-and-alive cat was a thought experiment applying the physics of electrons and atoms to our macroscopic world. New experiments with superconductors narrow the gap between theoretical ideas and reality.

## PHYSICAL REVIEW LETTERS

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NUMBER 4

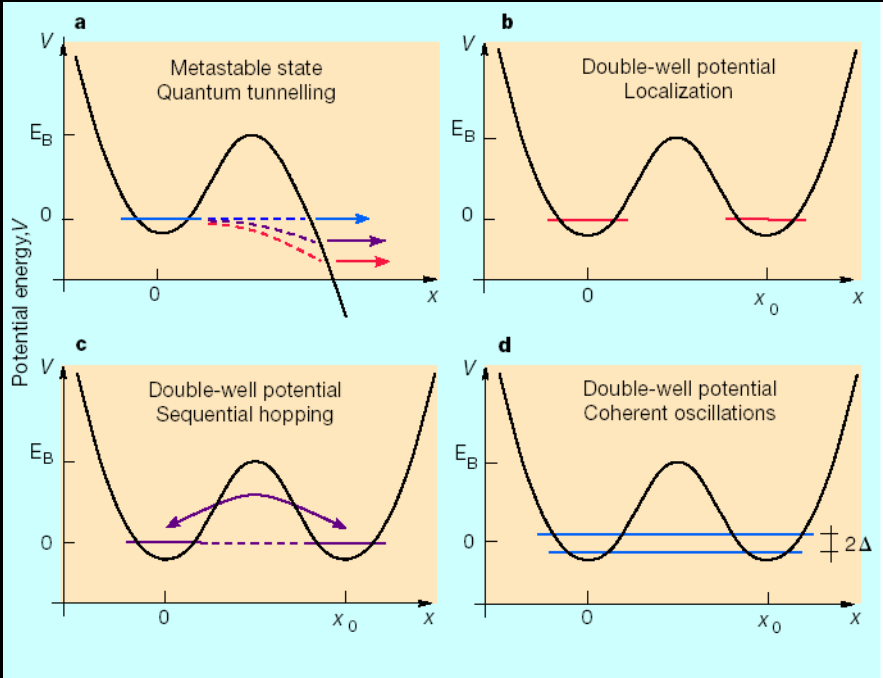
### Influence of Dissipation on Quantum Tunneling in Macroscopic Systems

A. O. Caldeira and A. J. Leggett

School of Mathematical and Physical Sciences, University of Sussex, Brighton BN1 9QH, Sussex, United Kingdom

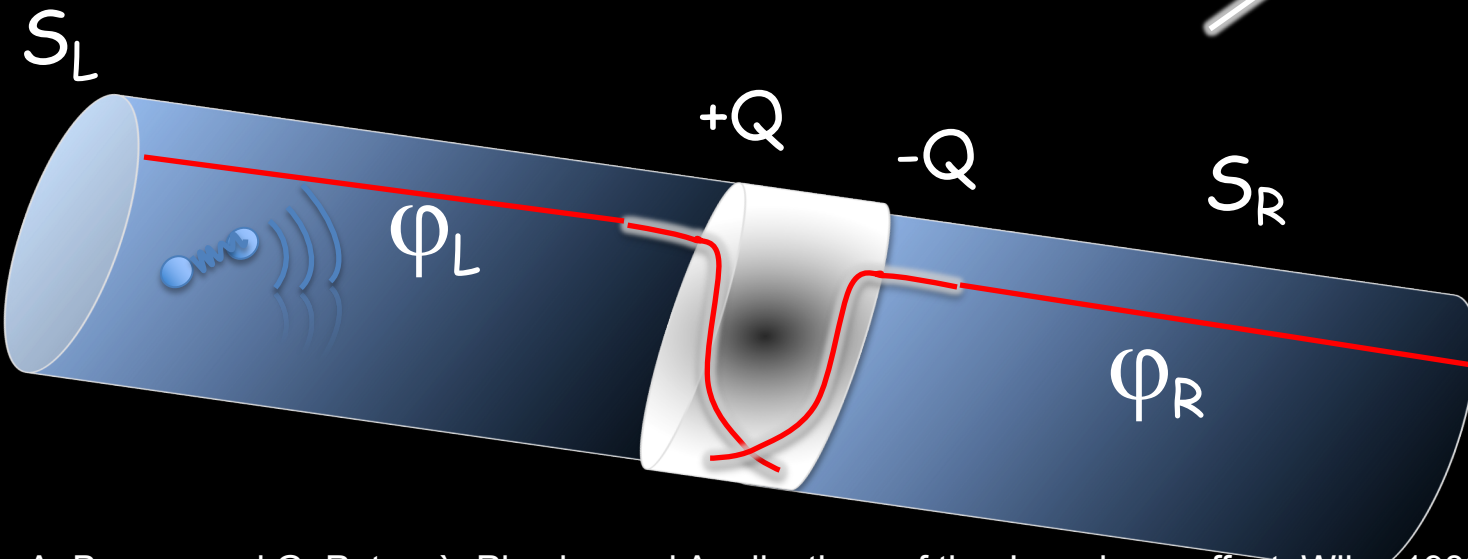
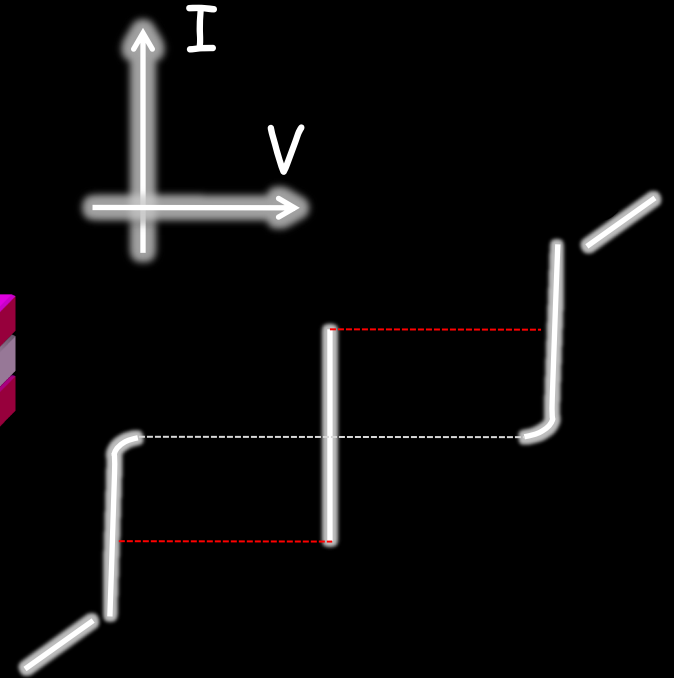
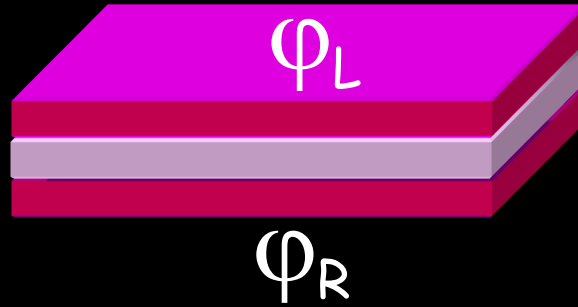
(Received 28 July 1980)

A quantum system which can tunnel, at  $T=0$ , out of a metastable state and whose in-



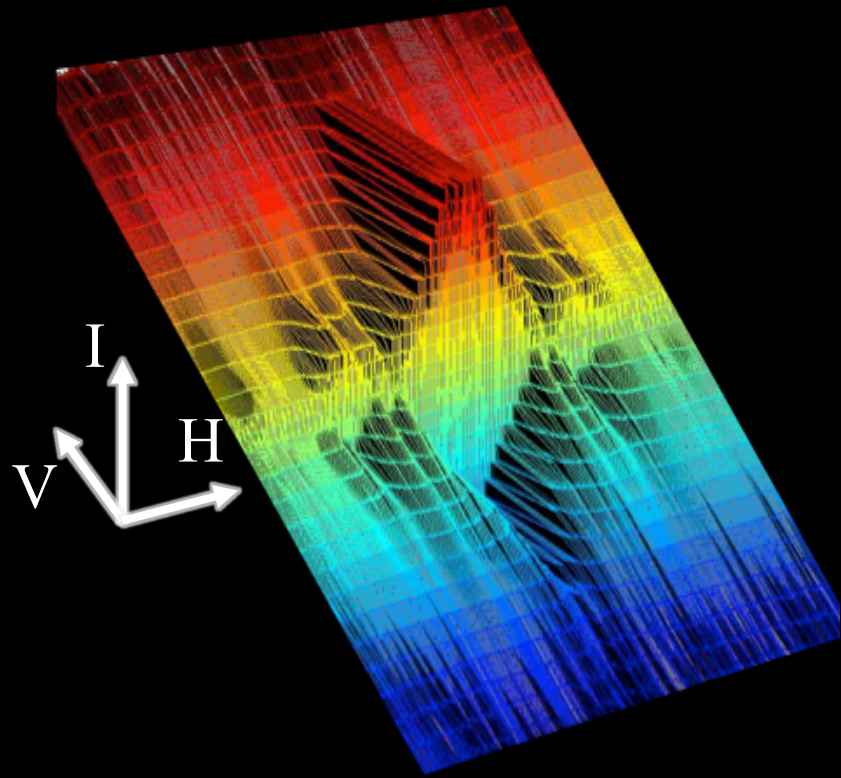
# The Josephson effect

$$\begin{cases} I_S(\varphi) = I_C \sin \varphi \\ \frac{\partial \varphi}{\partial t} = \frac{2eV}{\hbar} \end{cases}$$
$$\varphi = \varphi_L - \varphi_R$$





# The Josephson effect



$$H = Q^2 / (2C) - E_J \cos \varphi$$

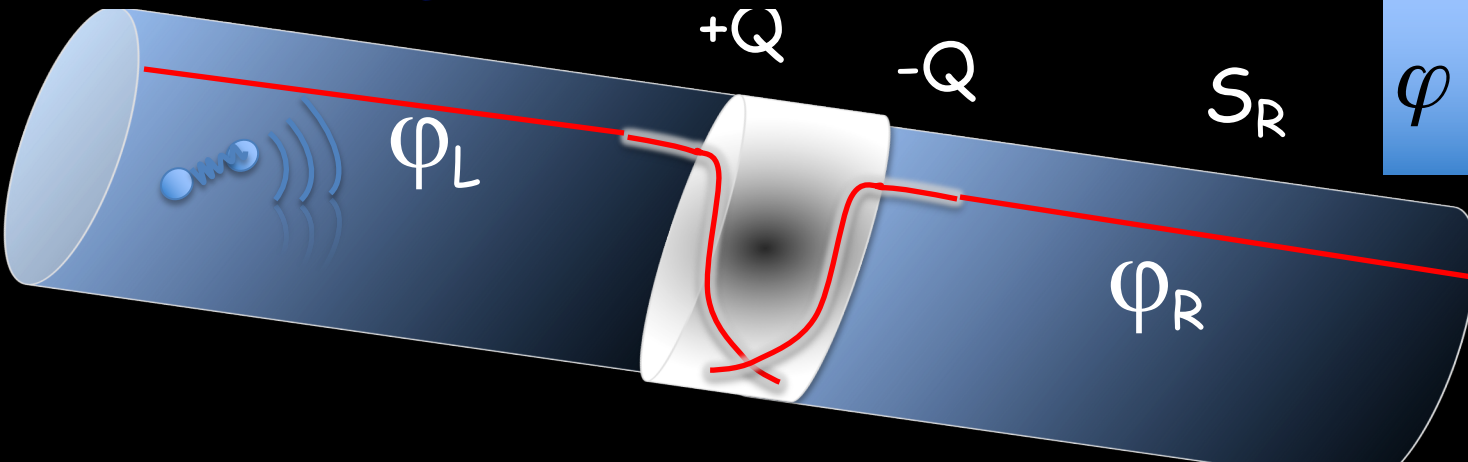
$$[\varphi, Q] = 2i\hbar \quad E_J \ll E_C$$

$$2eN = Q = CV$$

$$N \rightarrow E_C = \frac{(2eN)^2}{2C}$$

$$\varphi \rightarrow E_J = \frac{I_c \Phi_0}{2\pi}$$

$$E_J \gg E_C$$



# Josephson junction: the only non-linear and non-dissipative component

$$I_S(\varphi) = I_c \sin \varphi$$

$$L_{J0} = \frac{\Phi_0}{2\pi I_c}$$

$$L_J(\Phi_J) = \frac{L_{J0}}{\cos \varphi}$$

$$E_c = \frac{e^2}{2C}$$



CAPACITANCE

$$E_L = \frac{\hbar^2}{4e^2 L}$$

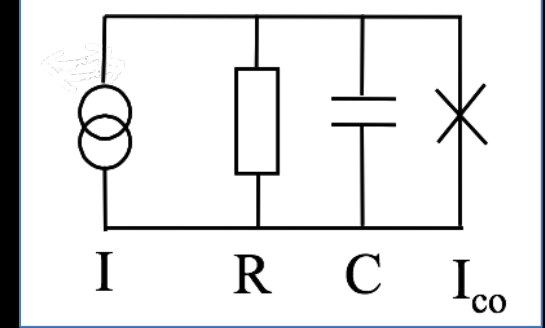


INDUCTANCE

$$E_J = \frac{\hbar^2}{4e^2 L_J}$$



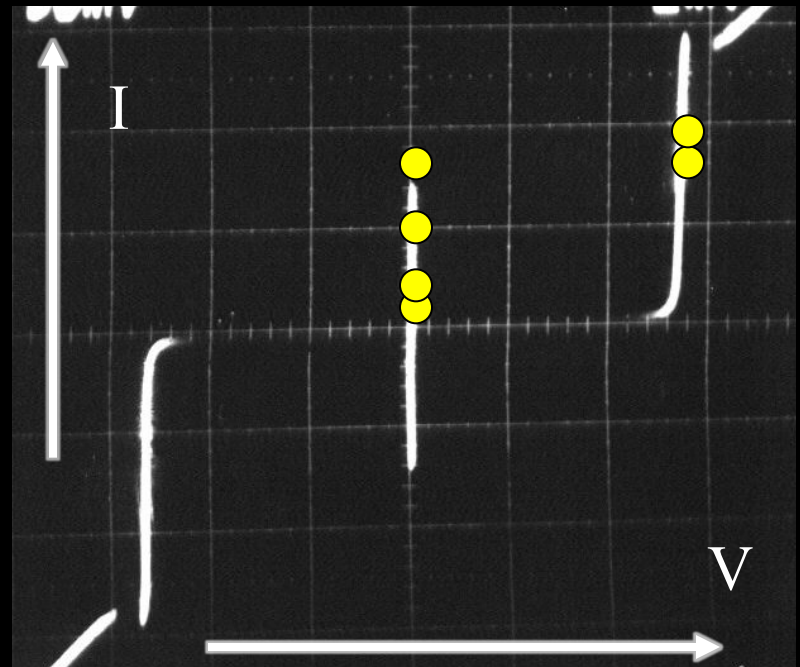
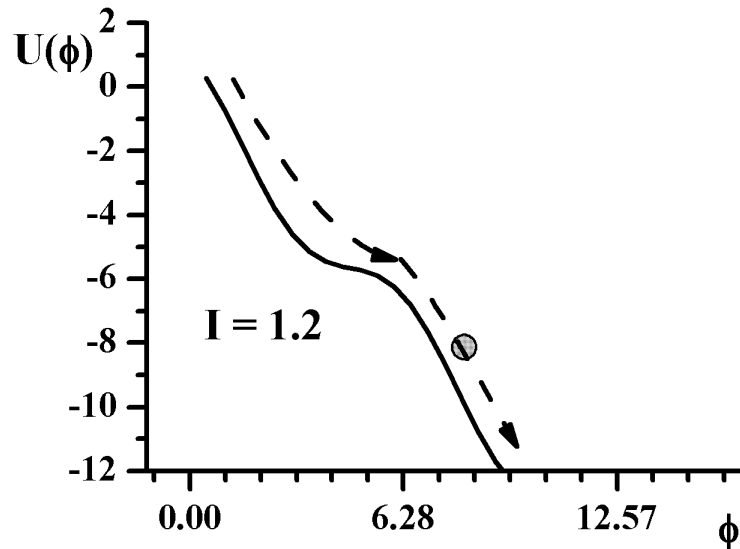
# Phase dynamics



$$I = C \frac{dV(t)}{dt} + GV(t) + I_c \sin \varphi(t)$$

$$\left(\frac{\phi_0}{2\pi}\right)^2 C \frac{\partial^2 \varphi}{\partial t^2} + \left(\frac{\phi_0}{2\pi}\right)^2 \frac{1}{R} \frac{\partial \varphi}{\partial t} + \frac{\partial U(\varphi, I)}{\partial \varphi} = 0$$

$$U(\varphi, I) = E_J \left( -\frac{I}{I_c} \varphi - \cos(\varphi) \right)$$





## QUANTUM OPTICS



## QUANTUM CIRCUITS

FIBERS, BEAMS			TRANSM. LINES, WIRES
BEAM-SPLITTERS			COUPLERS
MIRRORS			CAPACITORS
LASERS			GENERATORS
PHOTODETECTORS			AMPLIFIERS
<u>ELECTRONS IN ATOMS</u>			<u>JOSEPHSON JUNCTIONS</u>

**ADVANTAGES OF CIRCUITS:**

- PARALLEL FABRICATION METHODS
- MECHANICAL STABILITY
- LEGO BLOCK CONSTRUCTION OF HAMILTONIAN
- ARBITRARILY LARGE ATOM-FIELD COUPLING

**DRAWBACKS OF CIRCUITS:** ARTIFICIAL ATOMS PRONE TO VARIATIONS

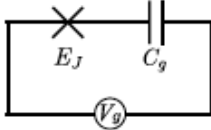
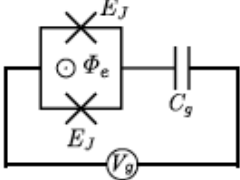
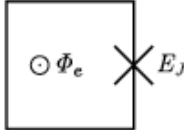

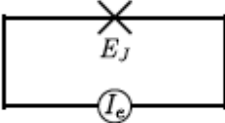
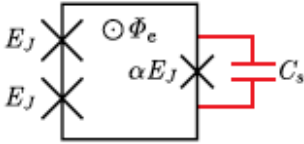
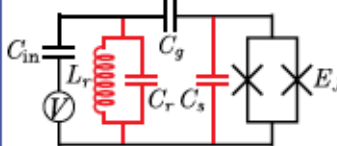
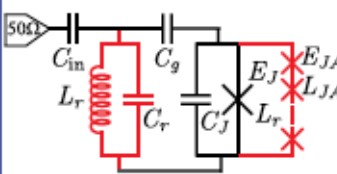
### Hybrid quantum circuits: Superconducting circuits interacting with other quantum systems

Ze-Liang Xiang\*

Sahel Ashhab†

J.Q. You‡

Franco Nori§

	Circuit	Properties	Dominant noise
Charge qubit		$E_J/E_C < 1$ Controlled by $V_g$ .	Charge fluctuations; mainly $1/f$ noise.
		$E_J/E_C < 1$ Controlled by both $V_g$ and $\Phi_e$ .	
Flux qubit		$E_J/E_C > 1$ Controlled by $\Phi_e$ .	Flux fluctuations; mainly $1/f$ noise.
		$E_J/E_C > 1$ $0.5 < \alpha < 1$ Controlled by $\Phi_e$ .	
Phase qubit		$E_J/E_C \gg 1$ Controlled by $I_e$ .	Flux fluctuations; mainly $1/f$ noise.
Low-decoherence qubit		Shunt capacitance $C_s$ . $E_J/E_C > 1$ Controlled by $\Phi_e$ flux qubit: $0.5 < \alpha < 1$ phase qubit: $\alpha < 0.5$	Both charge noise and flux noise can be suppressed.
Transmon		Shunt capacitance $C_s$ . $E_J/E_C > 1$	Behaves like a phase qubit Charge noise can be suppressed.
Fluxonium		Needs an array of larger-area tunnel junctions. $E_J/E_C > 1$	Behaves like a phase qubit Charge noise can be suppressed with appropriate parameters.

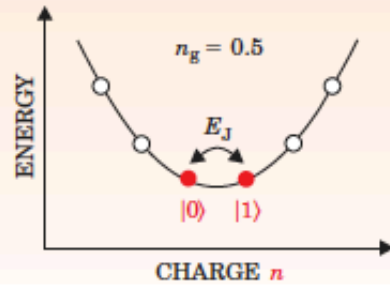
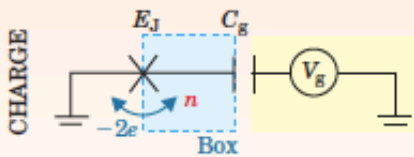
# Superconducting Circuits and Quantum Information

Superconducting circuits can behave like atoms making transitions between two levels. Such circuits can test quantum mechanics at macroscopic scales and be used to conduct atomic-physics experiments on a silicon chip.

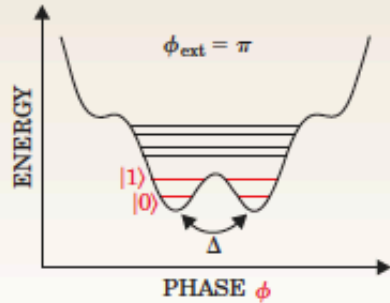
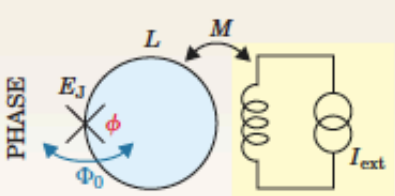
J. Q. You and Franco Nori

2005 Physics Today

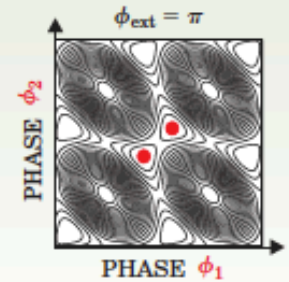
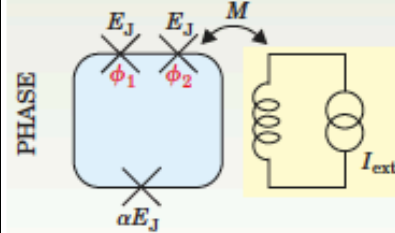
a Cooper-pair box



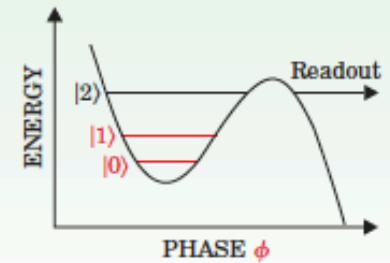
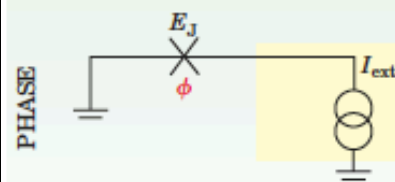
b Magnetic-flux box (RF-SQUID)



c Three-junction magnetic-flux box



d Current-biased junction

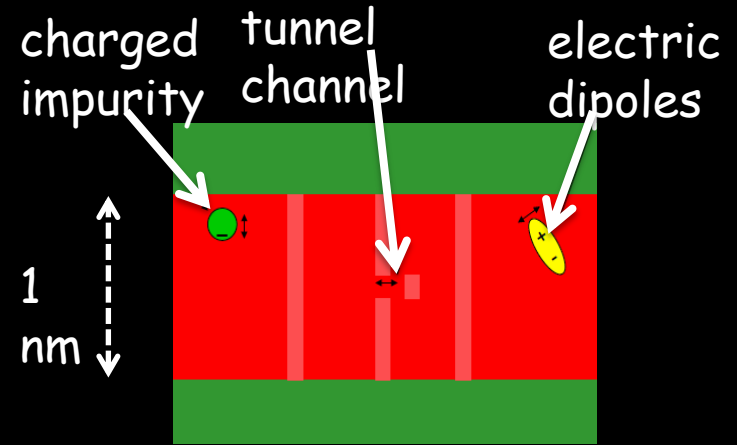




# Junction parameter fluctuations

$$Q_r, E_J, E_C$$

get rid of randomness of static offset charge



possible solutions

possible solutions

1-Control offset charge with a gate



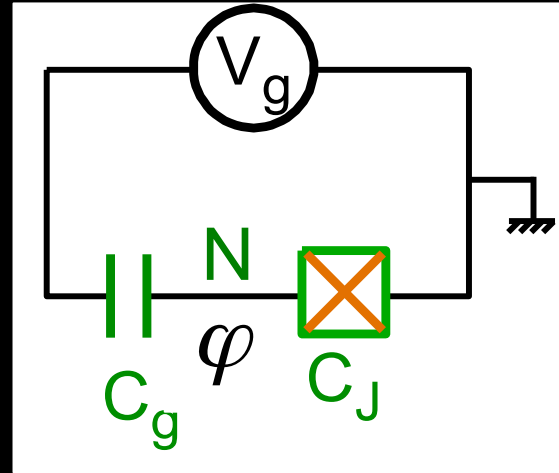
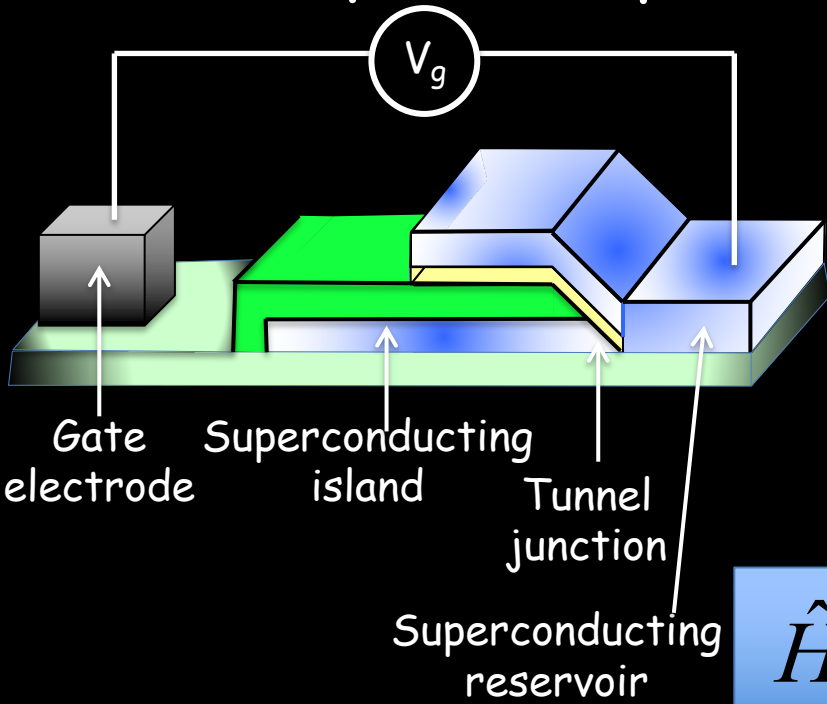
Cooper pair box (charge qubit)

2-make  $E_J/E_C$  very large



RF SQUID (flux qubit)  
Current biased Junction (phase qubit)

# The quantum path, the single Cooper pair box



$$[\hat{\varphi}, \hat{N}] = i$$

Hamiltonian

$$\hat{H} = E_c (\hat{N} - N_g)^2 - E_J \cos(\hat{\varphi})$$

Strategy: compensate static offset charge with gate

$$N_g = \frac{C_g V_g}{2e}$$

$$E_J = \frac{h\Delta}{8e^2 R_t}$$

$$E_c = \frac{(2e)^2}{2(C_g + C_J)}$$

