



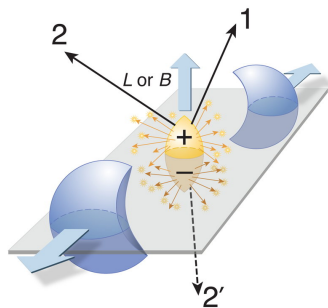
Magnetic-Field-Induced
insulator-conductor transition in
quenched lattice gauge theory

ArXiv:[0907.0494](#), [1003.2180](#)

Pavel Buividovich

Lattice 2010

Magnetic phenomena in hadronic matter



Magnetic field comparable with nuclear scale!!! [Kharzeev,
McLerran '98]

Very strong magnetic fields

- Noncentral heavy-ion collisions:

$$B \sim 10^{15} \text{ Tl}, \quad \sqrt{eB} \sim 10 \text{ MeV} \dots 500 \text{ MeV}$$

- Early Universe after electroweak phase transition:

$$B \sim 10^{16} \text{ Tl}, \quad \sqrt{eB} \sim 1 \text{ GeV}$$

- Magnetars:

$$B \sim 10^{10} \text{ Tl}, \quad \sqrt{eB} \sim 1 \text{ MeV}$$

- Strong laser pulses in PHELIX:

$$B \sim 10^7 \text{ T}, \quad \sqrt{eB} \sim 0.01 \text{ MeV}, \quad I \sim 10^{23} \text{ W/cm}^2$$

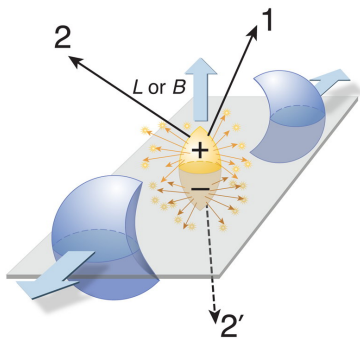
Magnetic phenomena in hadronic matter

- Quarks are charged particles with spin 1/2
- \Rightarrow Paramagnetism, Diamagnetism
- Strong dependence of plasma parameters on the magnetic field
- Masses of particles, heat capacity, viscosity change ...

Chiral magnetic effect

- CME: in systems with nonzero chirality magnetic field \vec{B} induces charge separation $\parallel \vec{B}$ [Kharzeev, McLerran, Warringa]
- charge separation \Rightarrow Electric current,
Electric dipole moment
- Nonzero chirality: created due to topology?
Atyah-Singer theorem

Chiral magnetic effect



Chiral magnetic effect: STAR@RHIC

PRL 103, 251601 (2009)

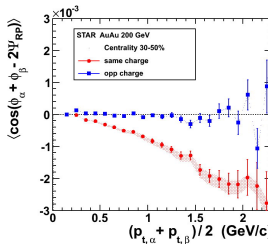
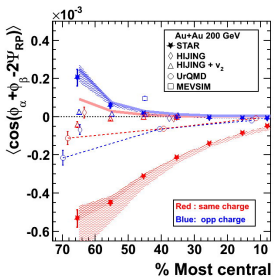
Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending

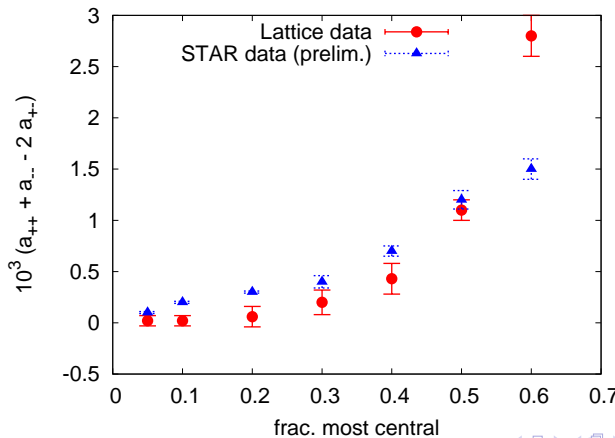
18 DECEMBER 2009

<http://link.aps.org/viewpoint-for/10.1103/PhysRevLett.103.251601>Azimuthal Charged-Particle Correlations and Possible Local Strong Parity Violation

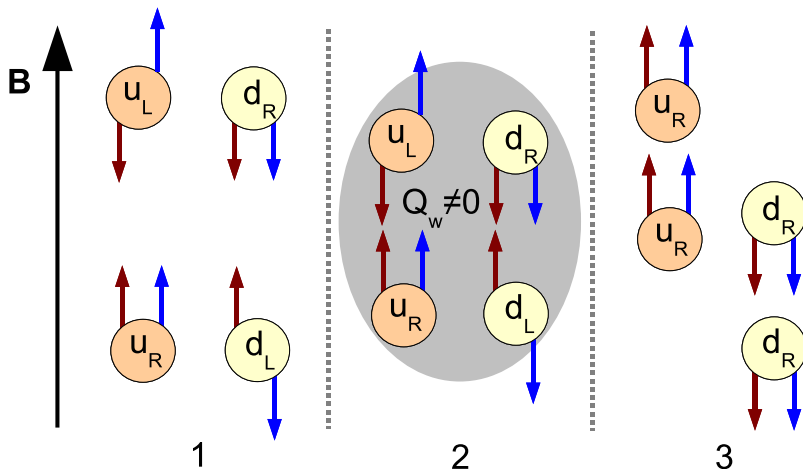
B. I. Abelev,⁸ M. M. Aggarwal,²⁹ Z. Ahammed,⁴⁶ A. V. Alakhverdyants,¹⁶ B. D. Anderson,¹⁷ D. Arkhipkin,³
 G. S. Averichev,¹⁶ J. Balewski,²¹ O. Barannikova,⁸ L. S. Barnby,² S. Baumgart,⁵¹ D. R. Beavis,³ R. Bellwied,⁴⁹
 F. Benedosso,²⁶ M. J. Betancourt,²¹ R. R. Betts,⁸ A. Bhasin,¹⁵ A. K. Bhati,²⁹ H. Bichsel,⁴⁸ J. Bielcik,¹⁰ J. Bielcikova,¹¹



Chiral magnetic effect:

STAR@RHIC vs. ITEP Lattice

Chiral magnetic effect: mechanism [Kharzeev, McLerran '98]

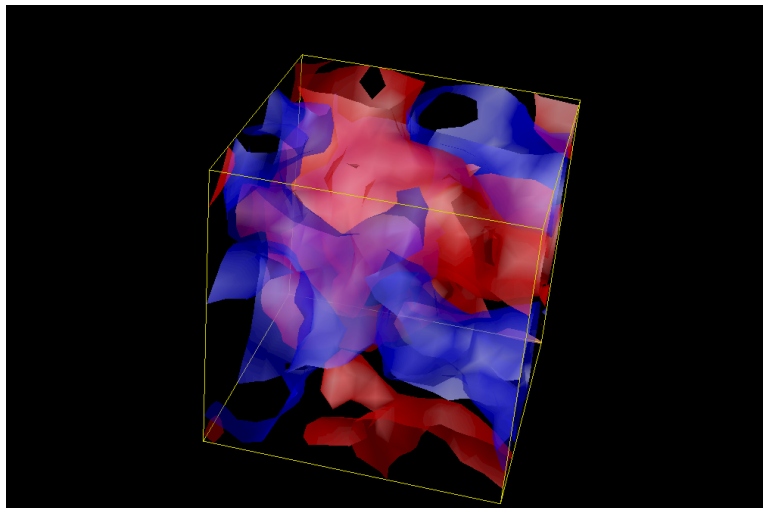


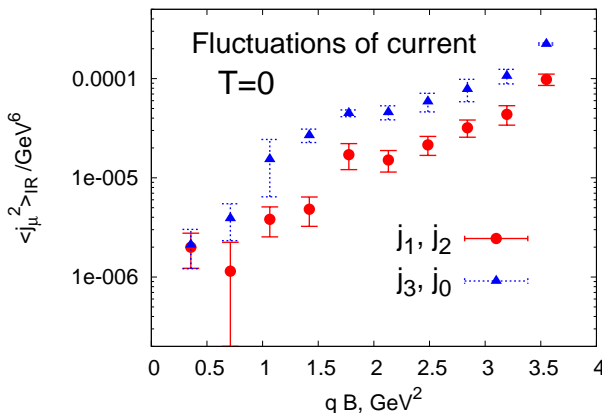
Chiral magnetic effect: mechanism [Kharzeev, McLerran '98]

- In a strong magnetic field \Rightarrow magnetic moment is conserved
- \Rightarrow Tunneling transitions between different topological vacua change the momentum
- \Rightarrow Electric current!
- Separated charge in a very strong field:

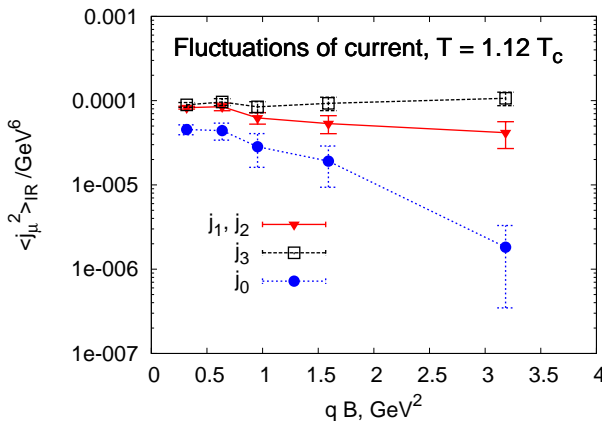
$$\Delta q = 2Q$$

Real vacuum of non-Abelian gauge theories



Chiral magnetic effect: Numerical results, $T = 0$ 

Chiral magnetic effect: Numerical results, $T > T_c$

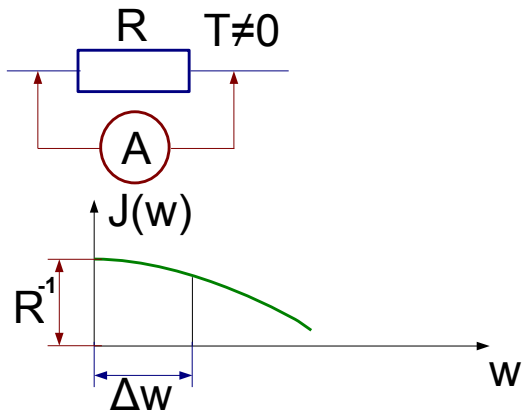


Fluctuations of current and conductivity

- Nyquist formula:

$$R^{-1} = \frac{\langle J^2 \rangle}{4kT \Delta w}$$

Fluctuations of current and conductivity



Green-Kubo formulas

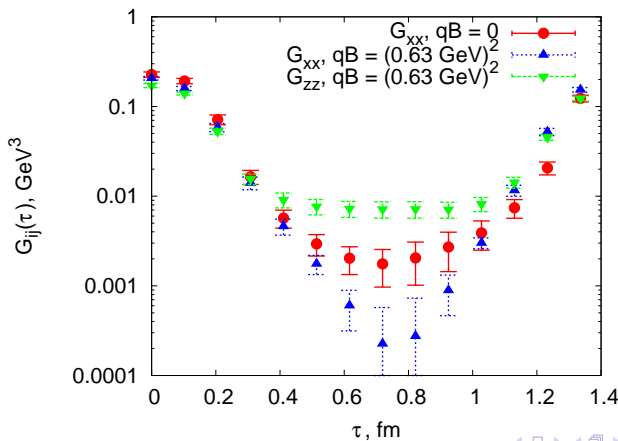
$$G_{ij}(\tau) = \int d^3\vec{x} \langle j_i(\vec{0}, 0) j_j(\vec{x}, \tau) \rangle,$$

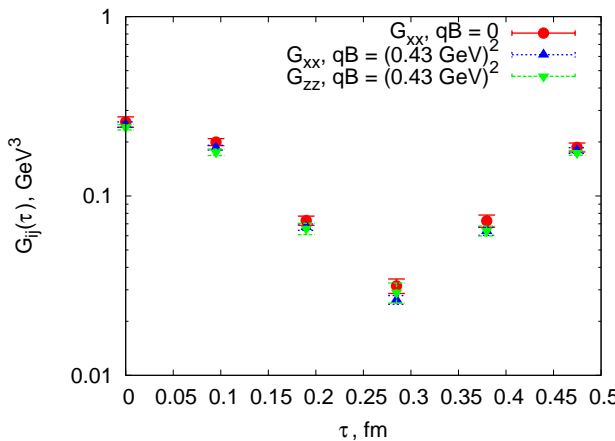
$$G_{ij}(\tau) = \int_0^{+\infty} \frac{d\omega}{2\pi} K(\omega, \tau) \rho_{ij}(\omega),$$

$$K(\omega, \tau) = \frac{\omega}{2T} \frac{\cosh\left(\omega\left(\tau - \frac{1}{2T}\right)\right)}{\sinh\left(\frac{\omega}{2T}\right)},$$

$$\sigma_{ij} = \lim_{\omega \rightarrow 0} \frac{\rho_{ij}(\omega)}{4T}$$

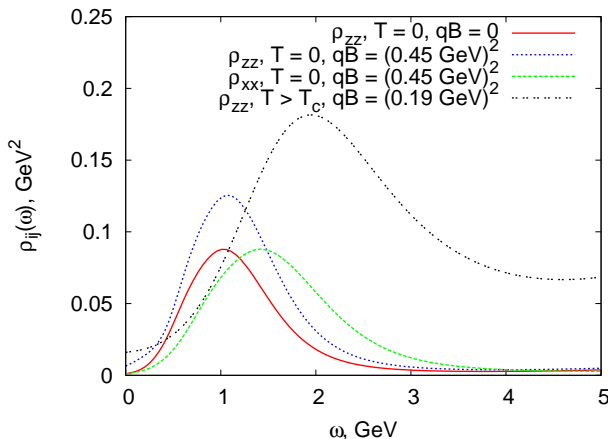
Current-current correlators at small temperatures



Current-current correlators: QGP

└ Fluctuations of current and conductivity

Spectral functions (Max. Entropy Method)

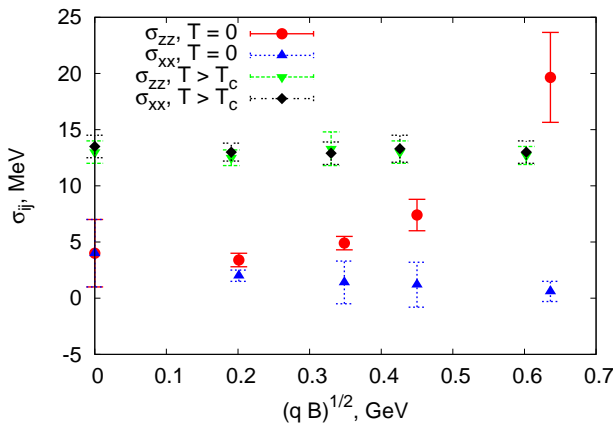


Anisotropic conductivity in magnetic field

- Confining vacuum of non-Abelian gauge theory - electric insulator!
- Magnetic field induces conductivity along its direction
- Quark-gluon plasma - isotropic conductor
- Magnetic field practically does not affect the conductivity of plasma

└ Fluctuations of current and conductivity

Conductivity vs. magnetic field

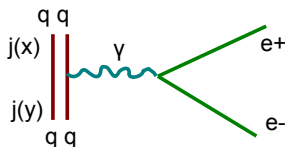


Theoretical explanation?

- Plausible assumption: vacuum is an insulator due to “something like” Anderson localization
- Strong magnetic field changes dimensionality
 $D = 4 \Rightarrow D = 2$ (localization at the Landau levels)
- Localization properties can change with dimensionality (counter-intuitive for Anderson)...
- Chiral magnetic spiral? [Kharzeev, Basar, Dunne'2010]

Experimental consequences

- Anisotropic fluctuations of the number of produced charged particles w.r.t. the reaction plane (existing STAR RHIC data)
- V.E.V. $\langle j_\mu(x) j_\nu(y) \rangle$ is related to the polarization of soft photons
- Polarization of soft virtual photons \Leftrightarrow Angular correlations of soft dileptons



Conclusions

- Chiral magnetic effect: enhanced fluctuations of electric current along the magnetic field
- Fluctuations of electric current \Rightarrow electric conductivity
- Magnetic field induces anisotropic conductivity of cold hadronic matter
- In experiment:
 - Additional anisotropy of charged reaction products
 - Angular correlations of soft dileptons

Thank you for your attention!!!

Basic references:

- K. Fukushima, D. E. Kharzeev, H. J. Warringa, The Chiral Magnetic Effect, Phys.Rev. D 78 (2008) 074033, [ArXiv:0808.3382](#)
- STAR Collaboration @ RHIC, Azimuthal Charged-Particle Correlations and Possible Local Strong Parity Violation, PRL 103, 251601 (2009), [ArXiv:0909.1739](#)
- P. V. Buividovich et al., Magnetic-Field-Induced insulator-conductor transition in SU(2) quenched lattice gauge theory (2010), [ArXiv:1003.2180](#)