

# Improved Lattice Spectroscopy of Minimal Walking Technicolor

Eoin Kerrane

University of Edinburgh

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Work with: Luigi Del Debbio, Claudio Pica, Biagio Lucini,  
Francis Bursa, Agostino Patella, Antonio Rago, Thomas Pickup

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# Outline

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# Motivation

- Electroweak symmetry breaking in nature about to be probed
- Dynamical EWSB remains a possible mechanism
- Requires new gauge sector with low  $N_c$  and  $N_f$  which is near-conformal → Chivukula, Sat
- Non-perturbative question, requires lattice input → Del Debbio, Thurs

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# Minimal Walking Technicolor

- $SU(2)$  theory with two (Dirac) flavours of adjoint fermion
- Attracted significant phenomenological and lattice attention
- Candidate model for new gauge sector of near-conformal technicolor theory
- Previous simulations have provided some evidence for existence of IR fixed point
  - Renormalisation flow analysis  
[HRT09, BDDK<sup>+</sup>09, BDDK<sup>+</sup>10]
  - Spectroscopic evidence  
[CS07, DDPP08, HRRT09]
- Systematics largely unexplored

# Simulation

- Simulation details found in [DDL<sup>+</sup>10b, DDL<sup>+</sup>10a],  
→ Pica & Patella, Tues
- Wilson fermions  $\Rightarrow am \neq 0$
- Configs from *HiRep* code for arbitrary  $N_c$ ,  $N_f$  and fermion representation
- Fixed lattice spacing  $\beta = 2.25, (2.10)$ , range of bare masses and volumes

# Spectroscopy

- Original analysis involved local correlators

$$C_{\Gamma}^I(t) = a^6 \sum_{\vec{x}} \langle \bar{\psi}(\vec{x}, t) \Gamma \psi(\vec{x}, t) \bar{\psi}(\vec{0}, 0) \Gamma \psi(\vec{0}, 0) \rangle$$

- Generalised *chroma* package to general  $N_c$ ,  $N_f$ , fermion representation
- Made use of *chroma* quark smearing routines
  - Gaussian Shell Smearing
  - Wall Smearing
  - Stochastic  $\mathbb{Z}_2$  Smearing



## Improved Plateaux

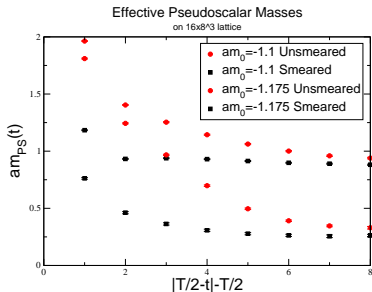
- Wall smearing expected to have lower overlap with excited states

$$C_{\Gamma}^s(t) = a^6 \sum_{\vec{x}} \langle \bar{\psi}(\vec{x}, t) \Gamma \psi(\vec{x}, t) \sum_{\vec{y}, \vec{z}} \bar{\psi}(\vec{y}, 0) \Gamma \psi(\vec{z}, 0) \rangle$$

# Improved Plateaux

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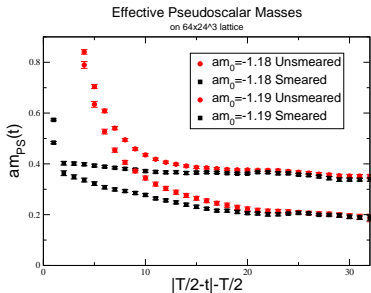
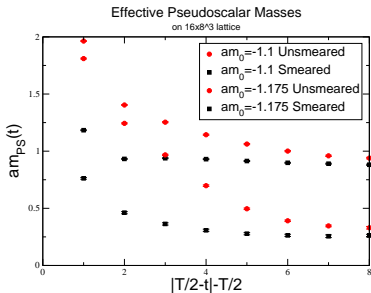
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# Dealing with systematics

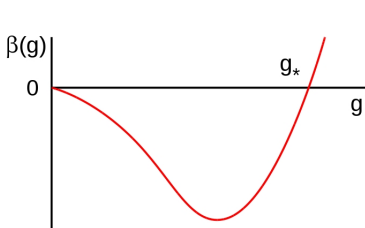
- Results show lower uncertainties due to smaller contribution from excited states
- Discrepancies are apparent at small volume
- Systematically combine two data sets (c.f. Addendum)
  
- Also explored effective mass definitions
  - Settle on one mass *Prony* method [FCLP09]
- And varying definition of effective observables
  - Limited impact

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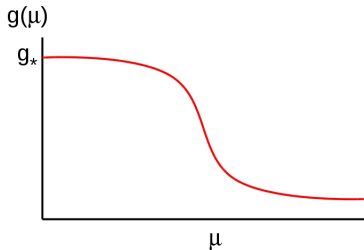
# IR Conformal

- We are interested in IR conformal theories



$$\beta(g_*) = 0$$

$$\rho = \frac{1}{1+\gamma_*}$$



$$\gamma_{\langle\bar{\psi}\psi\rangle}(g_*) = \gamma_*$$

# Conformal Comparison

## QCD

- $m_{\text{PS}} \sim m^{\frac{1}{2}}$
- $\frac{m_{\text{PS}}}{m_{\text{V}}} \xrightarrow{m \rightarrow 0} 0$
- Volume effects  $\sim e^{-m_{\text{PS}} L_s}$

## IR Conformal

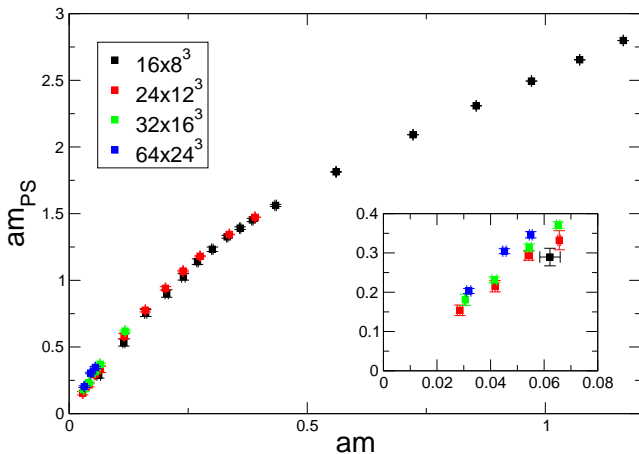
- $m_{\text{PS}} \sim M \sim m^\rho$
- $\frac{m_{\text{PS}}}{m_{\text{V}}} \sim 1$
- $LM = f(x) \quad x = (Lm)^\rho$

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# Pseudoscalar Meson

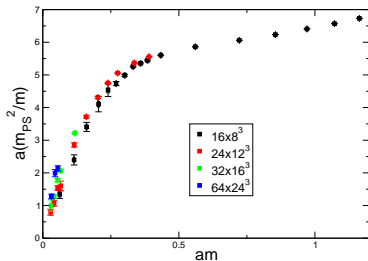


# Pseudoscalar Mass Scaling

$$\text{QCD: } \frac{m_{PS}^2}{m} \stackrel{m \rightarrow 0}{\sim} 1$$

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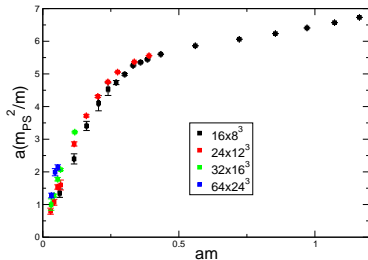
$$\text{QCD: } \frac{m_{PS}^2}{m} \xrightarrow{m \rightarrow 0} 1$$



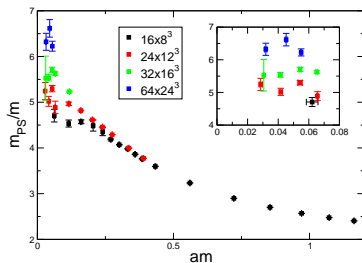
$$\frac{m_{PS}^2}{m} \xrightarrow{m \rightarrow 0} 0?$$

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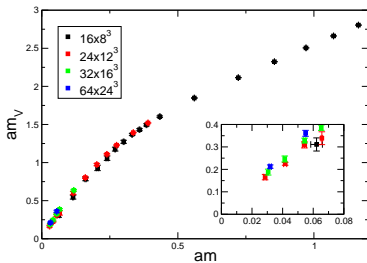
$$\frac{m_{PS}^2}{m} \xrightarrow{m \rightarrow 0} 0?$$



$$0 < \gamma < 1?$$

# Vector Meson

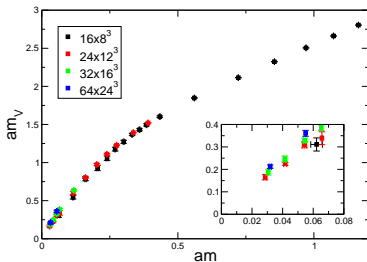
$$\text{QCD: } \frac{m_V}{m_{PS}} \xrightarrow{m \rightarrow 0} \infty$$



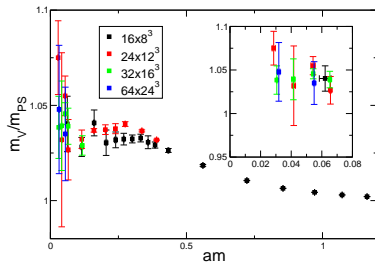
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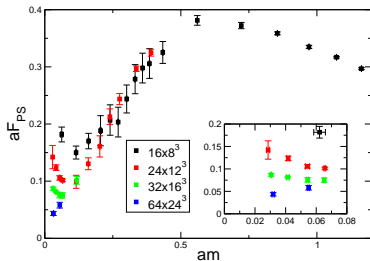
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# Pseudoscalar Decay Constant

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- Leads to large fluctuations at large times, on small volumes

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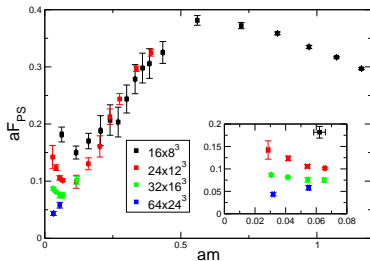


$V$  effects large

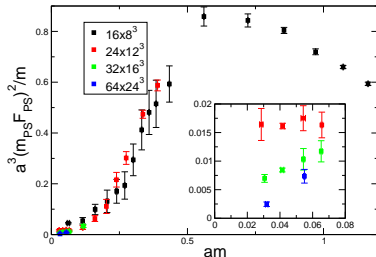


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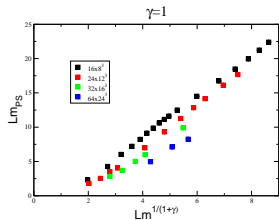
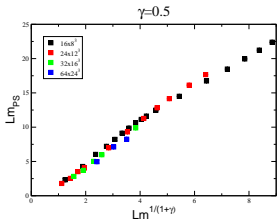
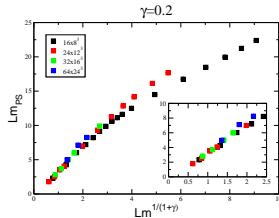
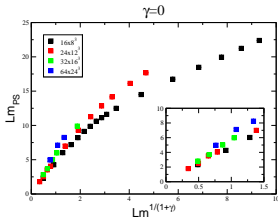
$V$  effects large



$$\frac{(m_{PS} F_{PS})^2}{m} \xrightarrow{m \rightarrow 0} 0?$$

# Finite Volume Scaling

$$LM = f(x) \quad x = (Lm)^\rho$$



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# Summary

- Supported the results in [DDL<sup>+</sup>10a, DDL<sup>+</sup>10b]
- Clarified reliability of fits
- Accounted for systematics where present
- Further indications of near-conformal dynamics

# Plateaux

- Define effective observable  $M(t) \xrightarrow[t \rightarrow \frac{T}{2}]{} M$
- Examine behaviour at large times
- Fit over range of  $t$  over which  $M(t)$  roughly constant

## Effective Observables

$$M = \lim_{t \rightarrow \frac{L_t}{2}} M(t)$$

- We use *Prony* method [FCLP09] (1 mass) to compute effective masses
- Fits using 2 masses disfavoured because of inflated uncertainties on ground state mass

$$a^2 |G_{\text{PS}}|(t) = \sqrt{V_s \frac{2am_{\text{PS}}(t)C_{\gamma_5}(t)}{h_+(m_{\text{PS}}(t), \bar{T}, t)}}$$

- Also trialled different effective observable definitions.
  - Impact limited
  - Where possible, chosen definition giving best fit

## Combining Data Sets

$$M_1 \pm \sigma_1$$

$$M_2 \pm \sigma_2$$

$$\begin{aligned} M' &= \frac{\frac{M_1}{\sigma_1^2} + \frac{M_2}{\sigma_2^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_2^2}} \\ &= \frac{\sigma_2^2 M_1 + \sigma_1^2 M_2}{\sigma_1^2 + \sigma_2^2} \end{aligned}$$

$$\begin{aligned} \sigma' &= \frac{1}{\sqrt{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_2^2}}} \times \left( 1 + \frac{(M_1 - M_2)^2}{\sigma_1^2 + \sigma_2^2} \right) \\ &= \frac{\sigma_1 \sigma_2}{\sqrt{\sigma_1^2 + \sigma_2^2}} \times \left( 1 + \frac{(M_1 - M_2)^2}{\sigma_1^2 + \sigma_2^2} \right) \end{aligned}$$



Francis Bursa, Luigi Del Debbio, Liam Keegan, Claudio Pica, and Thomas Pickup.

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Eoin Kerrane

Introduction

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**Addenda**