

# Chiral and Deconfinement Transitions in SC-LQCD

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Villasimius Sardinia Italy

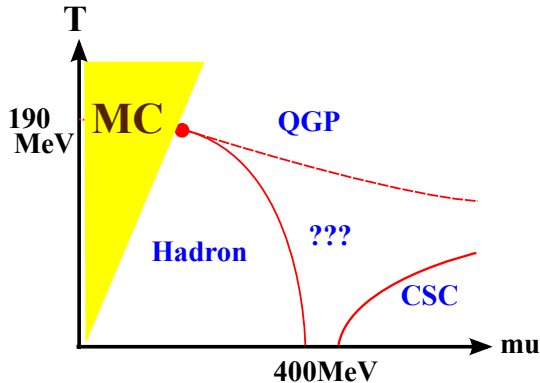
## References

- K.Miura, T.Z.Nakano, A.Ohnishi, N.Kawamoto, Phys.Rev.D**80**,('09).
- K.Miura, T.Z Nakano, A.Ohnishi, Prog.Theor.Phys.122,('09).
- T.Z.Nakano, K.Miura, A.Ohnishi, Prog.Theor.Phys.123 (2010), 825

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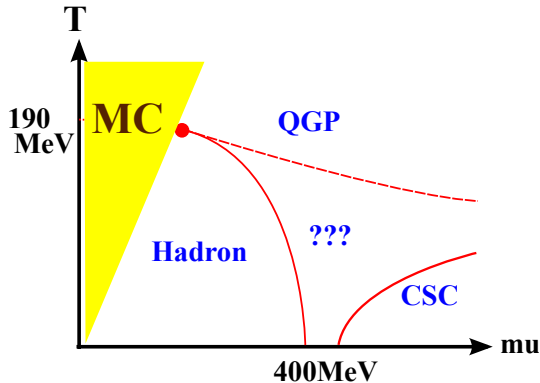
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# QCD Phase Diagram



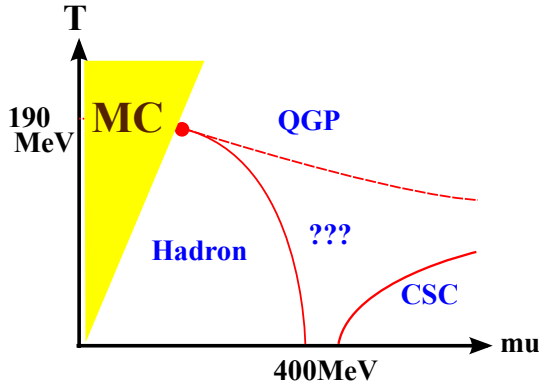
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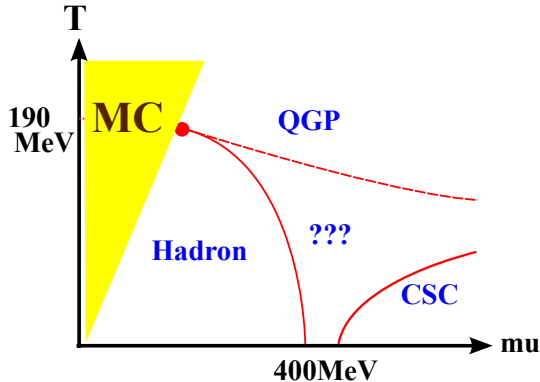
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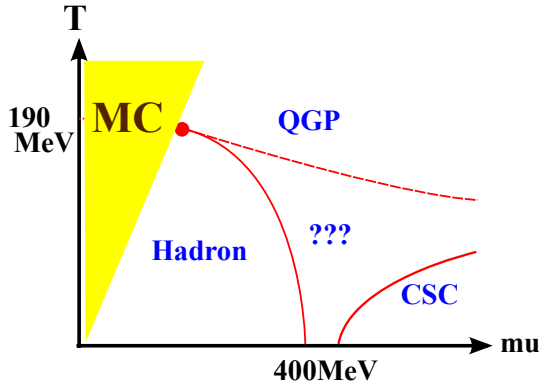
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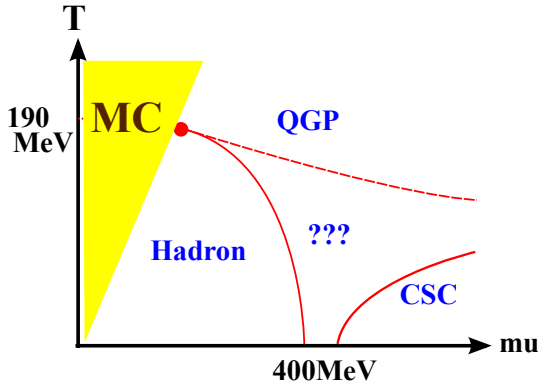
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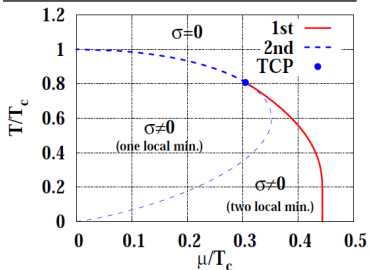
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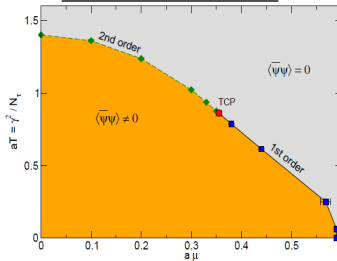
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## Phase Diagram at Strong Coupling Limit

Kawamoto-Miura-Ohnishi-Ohnuma ('07)



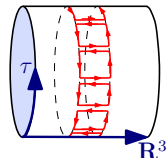
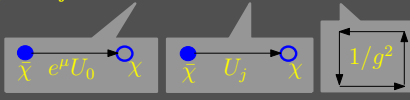
Forcrand Fromm (2009)



c.f. A. Ohnishi, Friday 18.

# Outline of Analyses ( $\beta = 6/g^2$ )

$$Z_{\text{LQCD}} = \int_{\chi, \bar{\chi}, U_0, U_j} \exp[-\mathbf{S}_F^{(\tau)} - \mathbf{S}_F^{(s)} - \mathbf{S}_G]$$



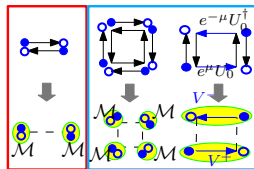
$\int \mathcal{D}U_j$  with  $1/g^2$  expansion

$1/d$  expansion Leading

Mean Field Approx.

$$\sigma \sim \langle \mathcal{M} \rangle \quad \rho_q \sim \langle V_+ + V_- \rangle$$

$\int \mathcal{D}[\chi, \bar{\chi}, U_0]$



$$\exp[-\mathcal{F}_{\text{eff}}(\mathbf{T}, \mu, \sigma, \rho_q, \mathbf{l}_p, \beta)]$$

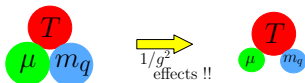
minimum search

Phase diagram





# Thermal Excitations



$$Z \sim \prod \left[ (1 + e^{-(\epsilon - \mu)/T}) (1 + e^{-(\epsilon + \mu)/T}) \right], \quad (\text{Free})$$

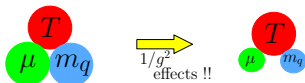
$$\rightarrow \prod \det_c \left[ (1 + L_p e^{-(E_q(\sigma) - \mu)/T}) (1 + L_p^\dagger e^{-(E_q(\sigma) + \mu)/T}) \right],$$

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$$\rightarrow \prod \det_c \left[ (1 + L_p e^{-(\tilde{E}_q(\sigma) - \tilde{\mu}(\omega_\tau))/T}) (1 + L_p^\dagger e^{-(\tilde{E}_q(\sigma) + \tilde{\mu}(\omega_\tau))/T}) \right], \quad (\text{PNLO}).$$

$$\tilde{\mu}(\beta, \omega_\tau) \simeq \mu - \beta \omega_\tau / 18, \quad \omega_\tau = -\frac{\partial F_{\text{eff}}}{\partial \mu} \equiv \rho_q. \quad (1)$$

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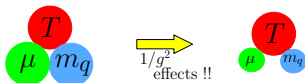
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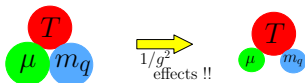
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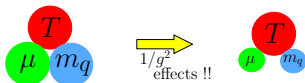
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- **Fermion:** One Species of Unrooted Staggered Fermions.
- **Chiral Symmetry:**  $U_\chi(1)$  Symmetry breaking and restorations without anomaly.
- **Approximations:**
  - ① NLO  $\mathcal{O}(1/g^2)$  in Strong coupling expansion,
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  - ③ Leading order of  $1/d$  expansion (c.f. A.Ohnishi Friday 18),
  - ④ Mean field approximation.
- **Scale:**  $a^{-1} \sim 500(\text{MeV})$  at  $\beta = 6.0$ , Kluberg-Stern et al. ('83)

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Simplest Laboratory to See Interplays among **Chiral** and **Deconfinement** Transitions with **Dynamical Density**!!

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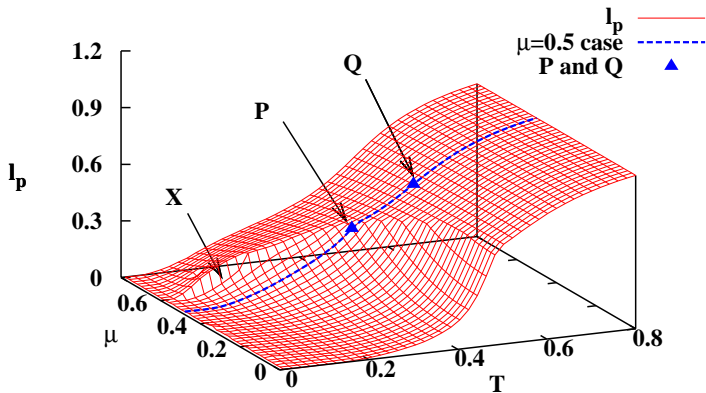
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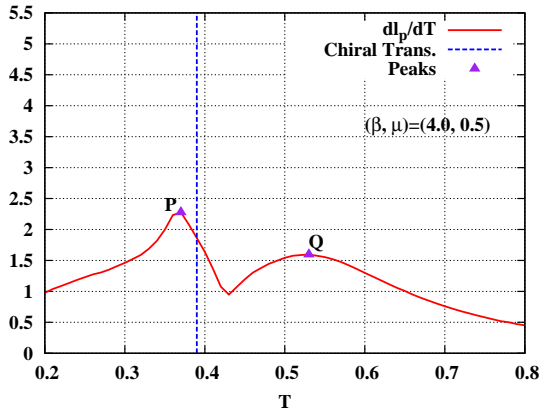
# Polyakov Loop (PNLO, $(\beta, m_0) = (4.0, 0.0)$ )

Miura, Nakano and Ohnishi, Preliminary!



# Deconfinement Cross-over ( $\beta, m_0$ ) = (4.0, 0.0)

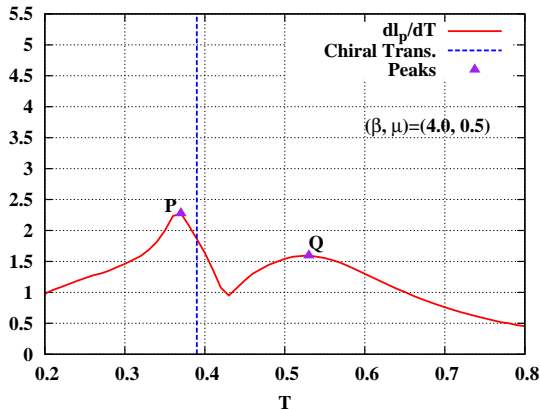
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P: Chiral Induced Deconfinement , Q: ?????

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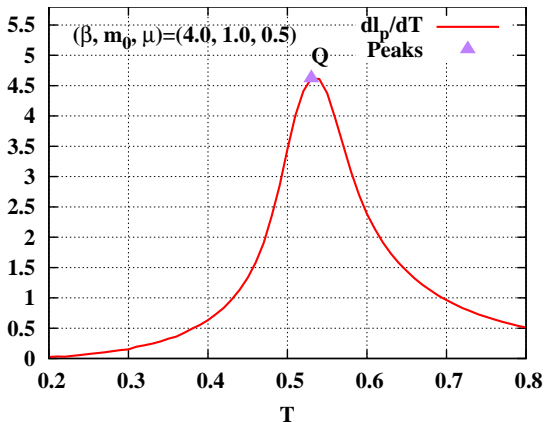
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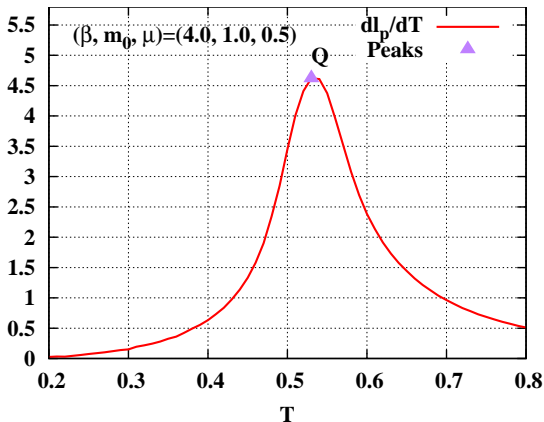
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Q:  $Z_3$  Induced Deconfinement

# Deconfinement Cross-over ( $\beta, m_0$ ) = (4.0, 1.0)

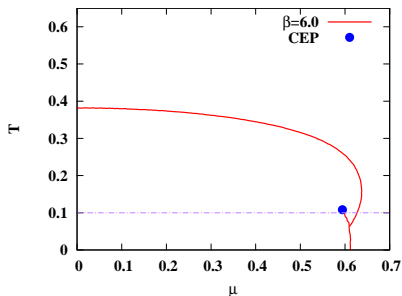
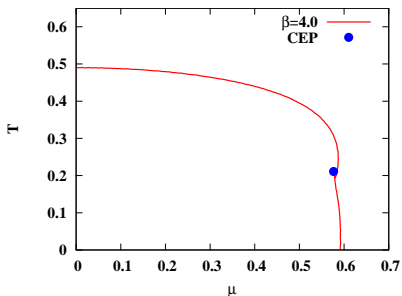
Miura, Nakano and Ohnishi, Preliminary!



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# Phase Diagram PNLO

Miura, Nakano and Ohnishi, Preliminary!

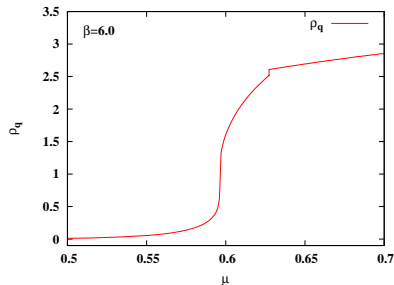
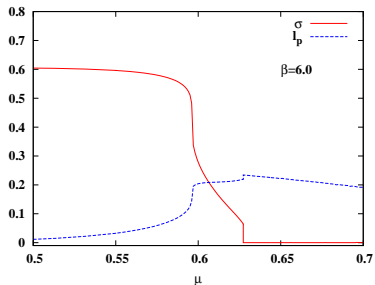


Left:  $\beta = 4.0$  in the chiral limit ,  
 Right:  $\beta = 6.0$  in the chiral limit



# PCR Matter with Polyakov Loop Effects (PNLO, $(\beta, m_0) = (6.0, 0.0)$ )

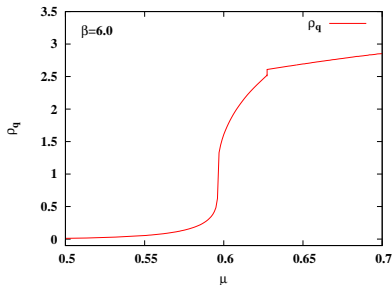
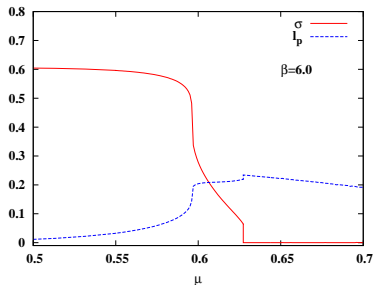
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$\tilde{\mu} \sim \tilde{E}_q$ , Partial Chiral Restored Matter,  
 (c.f. NLO Miura, Nakano, Ohnishi, Kawamoto ('09)),  
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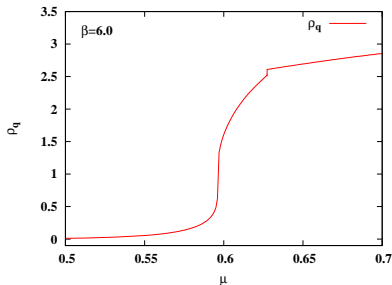
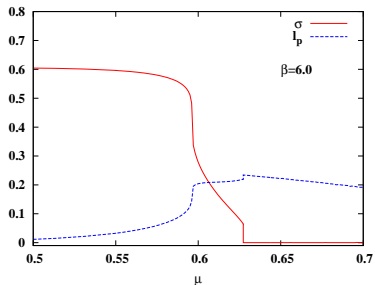
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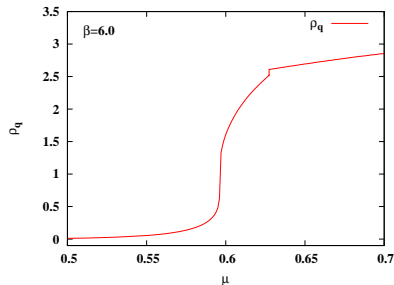
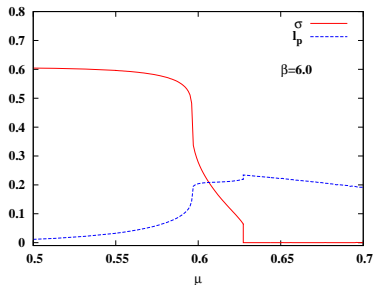
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## Summary

### Results

- We have investigated interplays between the **chiral** and **deconfinement** transitions with **dynamical quark density** effects based on the PNLO of SC-LQCD.
- We have found two sequential deconfinement cross-overs, **Chiral induced** and  **$Z_{N_c}$  induced** deconfinements.
- In the same way to NLO investigation, the **PCR matter** satisfying the balance Eq.  $\tilde{\mu} \sim \tilde{E}_q$  appears in PNLO case, and the  $I_p$  is finite in PCR, i.e. **Quark and Diquark excitation** exists (c.f. Quarkyonic).

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## Further Developments

### Toward Collaboration to LQCD-MC

- Imaginary chemical potential with Polyakov loop effects.
- Suggestion of analytic form of fitting functions in the extrapolations from  $\mu_I$  region to  $\mu$  region:  $\rho_q(\mu_I) \rightarrow \rho_q(\mu)$ ,  $(I_p(\mu_I), \bar{I}_p(\mu_I)) \rightarrow (I_p(\mu), \bar{I}_p(\mu))$ , ...
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### EXTENSIVE INVESTIGATIONS !!

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Mr. T-Z. Nakano, Next Talk!
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