## Simulations with dynamical HISQ quarks

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## Background: $a_{\text {tad }}^{2}$ (asqtad) lattices

- Started in 1999
- $2+1$ dynamical flavors
- Lattice artifacts much smaller than naive staggered
- Lattice spacings $0.18,0.15,0.12,0.09,0.06$ and 0.045 fm
- Light quark masses $0.1 m_{s}$ to $m_{s}$ (and one at $0.05 m_{s}$ )
- Spatial sizes $2.5-5.8 \mathrm{fm}$
- Controlled continuum and chiral extrapolations
- Around 25,000 equilibrated lattices generated
- All these lattices are publicly available (NERSC,ILDG,informal)


## Next generation: "HISQ lattices"

HISQ action developed by UKQCD/HPQCD
Actually, this generation is better in several ways:

- Two-level fermion link smearing (HISQ). Taste violations about one-third of $a_{\text {tad }}^{2}$, generic lattice artifacts about one-half.
- Inclusion of dynamical charm. Mass dependent Naik term (HISQ) makes this accurate up to $a m_{c} \approx 1$.
- Larger spatial sizes, about $20 \%$ larger than similar $a_{\text {tad }}^{2}$ ensembles
- Quark loop effects in gauge action coefficients (not available when $a_{t a d}^{2}$ started)
- Better tuning of quark masses (within $\approx 2 \%$, c.f. as bad as $20 \%$ for $a_{t a d}^{2}$ )


## Physics motivation

What will, or could be, done with these lattices?

- Static quark potential (tuning)
- Local hadron spectrum (tuning)
- $f_{\pi}, f_{K}, f_{D}, f_{D_{s}}$.
- $f_{B}, f_{B_{s}}$ with Fermilab/NRQCD/HISQ $b$
- Charmonium spectroscopy
- Heavy-light semileptonic form factors
- $B_{K}$
- Strange and light quark condensates, (dark matter)
- Nucleon structure and interactions


## HISQ lattice generation

General outline of the program:

- Runs at $m_{l}=0.2 m_{s}, 0.1 m_{s}$ and $\approx 0.04 m_{s}$
- Lattice spacings: (0.045), 0.06, 0.09, 0.12, 0.15, (0.18, 0.20) fm
- Spatial volumes $<\approx 5.6 \mathrm{fm}$
- Size of ensembles $\approx 1000$ lattices
- "mass independent" - lines of constant $10 / g^{2}$ and $u_{0}$
- Determine lattice spacing from $r_{1}$ and/or $f_{s s}$
- Tune $m_{s}$ from $2 M_{K}^{2}-M_{\pi}^{2}$
- Tune $m_{c}$ from $\frac{3}{4} M_{\Psi}+\frac{1}{4} M_{\eta_{c}}$.


## Completed:

- Test scaling at fixed quark mass
- Series of ensembles with $m_{l}=0.2 m_{s}$
- Lattice spacings $0.15,0.12$ and 0.09 fm
- Extend tests of scaling (lattice artifacts) to dynamical HISQ and things other than taste violation.
- arXiv:1004.0342, and next three slides


## HISQ, June 2010

| $\beta$ | $a m_{l}$ | $a m_{s}$ | $a m_{C}$ | size | $u_{0}$ | $N_{\text {lats }}$ | s | len. | $\epsilon$ | acc. | $r_{1} / a$ | a (fm) | $m_{\pi} L$ | $\pi$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.80 | 0.013 | 0.065 | 0.838 | $16^{3} \times 48$ | 0.85535 | 1021 | 5 | 1.0 | 0.033 | 0.73 | 2.041(10) | $0.1527\left({ }_{-17}^{+10}\right)$ | 3.78 | 306 |
| 5.80 | 0.0064 | 0.064 | 0.828 | $24^{3} \times 48$ | 0.85535 | 1000 | 5 | 1.0 | 0.020 | 0.73 | 2.062(5) | $0.1512\left({ }_{-16}^{+7}\right)$ | 3.99 | 217 |
| 6.00 | 0.0102 | 0.0509 | 0.635 | $24^{3} \times 64$ | 0.86372 | 1040 | 5 | 1.0 | 0.036 | 0.66 | 2.574(5) | $0.1211\binom{+6}{-12}$ | 4.54 | 309 |
| 6.00 | 0.00507 | 0.0507 | 0.628 | $32^{3} \times 64$ | 0.86372 | 920 | 5 | 1.0 | 0.025 | 0.64 | 2.618(17) | $0.1190\left(\begin{array}{l}+9\end{array}\right)$ | 4.29 | 221 |
| 6.30 | 0.0074 | 0.037 | 0.440 | $32^{3} \times 96$ | 0.874164 | 878 | 6 | 1.5 | 0.031 | 0.68 | 3.520(7) | $0.0886\binom{+4}{-9}$ | 4.50 | 314 |
| 6.30 | 0.00363 | 0.0363 | 0.430 | $48^{3} \times 96$ | 0.874164 | 217 | 6 | 1.5 | 0.0197 | 0.66 | 3.552(15) | $0.0878\left({ }_{-10}\right)$ | 4.71 | 221 |
| 6.30 | 0.0012 | 0.0363 | 0.432 | $64^{3} \times 96$ | 0.874164 | 151 | 6 | 1.5 | 0.0123 | 0.64 | 3.594(12) | $0.0867\binom{+5}{-9}$ | 3.66 | 130 |
| 6.72 | 0.0048 | 0.024 | 0.286 | $48^{3} \times 144$ | 0.885773 | 206 | 6 | 2.0 | 0.0217 | 0.61 | 5.312(16) | $0.0587\binom{+3}{-6}$ | 4.51 | 315 |
| 6.72 | 0.0024 | 0.024 | 0.286 | $64^{3} \times 144$ | 0.885773 | 75 | 6 | 2.0 | 0.0143 | 0.67 | 5.410(15) | $0.0576\binom{+6}{-6}$ | 4.25 | 227 |

Parameters of the HISQ runs. $N_{\text {lats }}$ is the number of equilibrated lattices. "s" is the separation of the lattices in
simulation time, "len" is the length of a trajectory in simulation time, " $\epsilon$ " is the molecular dynamics step size, and
"acc." is the fraction of trajectories accepted. Our definition of the step size is such that there is one evaluation of the fermion force per step, so a complete cycle of the Omelyan integration algorithm includes two fermion action steps and six gauge action steps. The physical lattice spacing given in this table uses the determination of $r 1=0.3117(6)\binom{+12}{-31}$ fm made using $f_{\pi}$ to set the scale on the Asqtad ensembles.

## HISQ program, summary

$-1000$
$\begin{array}{llll}0.04 \mathrm{~m}_{\mathrm{s}} & \text { QpQQ } & \\ \end{array}$
$-1000$


- $0=$ done
- Goal:

Complete all these,
$\approx 1000$
lattices

## Taste symmetry

- arXiv:1004.0342
- At $m_{l}=0.2 m_{s}$
- Done earlier by UKQCD/HPQCD on quenched and asqtad sea
- Works as expected with dynamical HISQ


## Taste symmetry, expected

where we will be in three years
Pion spectrum at $a \approx 0.06$ and $0.045 \mathrm{fm}(\mathrm{MeV})$
Splittings scaled from 0.09 fm masses
Tastes good: $\log \left(m_{\pi}^{2}+a^{2} \Delta^{2}\right) \approx \log \left(m_{\pi}^{2}\right)+a^{2} \Delta^{2} / m_{\pi}^{2}$

|  | 0.06 fm | 0.06 fm | 0.045 fm |
| :---: | :---: | :---: | :---: |
| taste | $m_{s} / 10$ | $m_{s} / 27$ | $m_{s} / 27$ |
| $\pi_{5}$ | 220 | 135 | 135 |
| $\pi_{05}, \pi_{i 5}$ | 225 | 143 | 139 |
| $\pi_{i j}, \pi_{i 0}$ | 231 | 152 | 144 |
| $\pi_{i}, \pi_{0}$ | 236 | 159 | 147 |
| $\pi_{s}$ | 239 | 164 | 149 |

The $m_{s} / 10$ run is in progress, the $m_{s} / 27$ runs are for later years.

## Topology

- arXiv:1003.5695, 1004.0342

- Really does improve the gauge configurations!!
- (Other tests involve valence quarks)


## Masses



- Improvement in masses and decay constants
- But much of this depends on choice of length scale


## Charmonium dispersion relation

- $m_{l}=0.2 m_{s}$

- "Speed of light" for $\eta_{c}$
- $\vec{p}^{2}=\left(\frac{2 \pi}{L}\right)^{2} \vec{n}^{2}$
- Similar to UKQCD/HPQCD on $a_{\text {tad }}^{2}$ sea
- This is with dynamical HISQ


## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$

- charm-light $f_{P S}$
- $m_{l}=0.2 m_{s}$
- Eventually, find $f_{D}, f_{D_{s}}$ and $f_{D_{s}} / f_{D}$


## Scale setting: conventional, $r_{1}$

- Use $r_{1}=\operatorname{root}\left(r^{2} F(r)=1\right)$ to set scale
- Not a physical quantity, but a convenient interpolating quantity
- Declare that $r_{1}$ is independent of lattice spacing and sea quark masses
- Find value for $r_{1}$ by matching some physical quantity in continuum and chiral limit.
- From $f_{\pi}, r_{1}=0.311 \mathrm{fm}$.


## Scale setting: alternative, $f_{\eta_{s}}$

- HPQCD: arXiv:0910.1229
- Use $f_{s s}=f_{P S}$ at $m_{v a l}=\operatorname{root}\left(\frac{M_{P S}\left(m_{v a l}\right)}{f_{P S}\left(m_{v a l}\right)}=0.2647\right)$
- Not a physical quantity, but a convenient interpolating quantity
- Declare that $f_{s s}$ is independent of lattice spacing and sea quark masses
- Find value for $f_{s s}$ by matching some physical quantity in continuum and chiral limit.
- From $f_{\pi}, f_{s s}=$ ???
- Working estimate from $\chi$ PT: $f_{s s}=181.5 \mathrm{MeV}$.


## Scale setting: alternative, $f_{\eta_{s}}$

- Actually, can use any reference mass
- We are experimenting with $m_{\text {valence }}=0.4 m_{s}$
- Tradeoff: heavy enough to get small statistical error
- Tradeoff: light enough for reliable $\chi P T$


## Scale setting from $f_{s s}$

- GOOD: Can get very high accuracy
- GOOD: Better understood systematic errors than $r_{1}$ (fit ranges, etc.)
- GOOD: For decay constant projects, produces a self contained project
- BAD: Takes longer than static potential (unless you were going to do $f_{P S}$ anyway)
- BAD: Depends on fermion formulation: Asqtad and HISQ valence quarks give different lattice spacings for same ensemble.


## Finding the lattice spacing

| Action | $10 / g^{2}$ | $a m_{I}$ | $a m_{s}$ | $a m_{c}$ | $a\left(r_{1}\right)$ | $a\left(f_{s s, \text { asq }}\right)$ | $a\left(f_{s S, \text { HISQ }}\right)$ |
| :--- | :--- | :--- | :--- | :---: | :--- | :---: | :---: |
| asqtad | 6.76 | 0.01 | 0.05 | - | $0.1178(2)$ | $0.1373(2)$ | $0.1264(11)$ |
| asqtad | 7.09 | 0.0062 | 0.031 | - | $0.0845(1)$ | $0.0905(3)$ | $0.0878(7)$ |
| asqtad | 7.46 | 0.0036 | 0.018 | - | $0.0588(2)$ | $0.0607(1)$ | $0.0601(5)$ |
| asqtad | 7.81 | 0.0028 | 0.014 | - | $0.0436(2)$ | $0.0444(1)$ | $0.0443(4)$ |
| HISQ | 5.80 | 0.013 | 0.065 | 0.838 | $0.1527(7)$ | na | $0.1558(3)$ |
| HISQ | 6.00 | 0.0102 | 0.0509 | 0.635 | $0.1211(2)$ | na | $0.1244(2)$ |
| HISQ | 6.30 | 0.0074 | 0.037 | 0.440 | $0.0884(2)$ | na | $0.0900(1)$ |

Lattice spacing in fermi from $r_{1}=0.3117 \mathrm{fm}$ (us),
$f_{s S}$ with Asqtad sea (us),
$f_{s s}$ with HISQ sea (from HPQCD for Asqtad sea ensembles).
Errors on $a\left(r_{1}\right)$ are statistical only - they do not include the errors in $r_{1}=0.3108(15)\left({ }_{-79}^{+26}\right) \mathrm{fm}$.
Errors on HISQ/Asqtad $a(H I S Q)$ are from HPQCD.
Errors on HISQ/HISQ a(HISQ) are statistical, no autocorrelations.
Errors on Asq/Asq a(Asq) are statistical, no autocorrelations.
$Z \approx 1.4$

## Finding the lattice spacing

- fractional differences in a determinations

- All agree as $a \rightarrow 0$


## Summary

- The HISQ action reduces lattice artifacts relative to the Asqtad action
- Cost for lattice generation is around twice as large (depending on quark mass)
- Four ensembles completed, five more in production
- Main motivation is high precision QCD
- We expect the lattices will be useful for a wide range of QCD studies


## Extra Slides

## Is $r_{1}=0.3117 \mathrm{fm}$ ?

- We have four dynamical quark flavors
- $\frac{1}{m_{c} r_{1}} \approx 0.65$, so charm quark might matter.
- At $m_{l} \approx 0.2 m_{s}$ four flavor HISQ $r_{0} / r_{1}$ is about 0.01 larger that three flavor Asqtad
- Can't tell if this is from different $n_{f}$ or different action. (Asqtad $r_{0} / r_{1}$ increases as a decreases).
- Eventually, matching $f_{\pi}$ or $b \bar{b}$ spectrum will sort this out.


## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$

- First approximation - just plug into current analysis with smaller taste violation parameters.
- What issues arise in extending analysis up to charm quark mass?
- Need to include adjustments for mistuned quark masses, as always.


## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$

$$
\begin{aligned}
& -M_{P S}^{2} /\left(m_{A}+m_{B}\right) \\
& -m_{l}=0.2 m_{s}
\end{aligned}
$$



## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$



## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$

- charm-light $f_{P S}$
- $m_{l}=0.2 m_{s}$
- Find $f_{D_{s}} / f_{D}$ ?


## $m_{\text {pseudo }}$ and $f_{\text {pseudo }}$

- charm-light $f_{P S}$
- $a=0.09 \mathrm{fm}$

- Find $f_{D_{s}} / f_{D}$ ?


## Scale setting from $f_{s s}$

| Ensemble | $a\left(r_{1}\right)$ | $a($ Asq) | a(HISQ) |
| :---: | :---: | :---: | :---: |
| b6572m0097m04845 | 0.1453(9) | 0.1771(?)(linear) | 0.1583(13) |
| b6586m0194m04845 | 0.1473(8) | 0.1769(?)(linear) | $0.1595(14)$ |
| b676m005m050 | 0.1175 (2) | 0.1360 (?)(linear) | 0.1247 (10) |
| b676m010m050 | 0.1178 (2) | 0.1397 (2?)(linear) | 0.1264 (11) |
| b679m020m050 | 0.1175(2) | 0.1368(?)(linear) | 0.1263 (11) |
| b709m0062m031 | 0.0845(1) | 0.09080(27)(linear) | 0.0878(7) |
| b709m0062m031 | 0.0845(1) | $0.08732(21)(q u a d)$ | $0.0878(7)$ |
| b711m0124m031 | 0.0842(2) | 0.09146 (28)(linear) | 0.0884(7) |
| b746m0036m018 | 0.0588(2) | $0.06057(11)$ (linear) | 0.0601(5) |
| b746m0036m018 | 0.0588(2) | $0.06074(13)(q u a d)$ | 0.0601(5) |
| b781m0028m014 | 0.0436(2) | 0.04455(08)(linear) | $0.0443(4)$ |
| b781m0028m014 | 0.0436(2) | $0.04444(09)(q u a d)$ | 0.0443(4) |
| b580m013m065m838 | 0.1524(3) | na | 0.15444(22 |
| b580m013m065m838 | 0.1524(3) | na | 0.15581(31 |
| b600m0102m0509m635 | 0.1208(2) | na | 0.12358(12 |
| b600m0102m0509m635 | 0.1208(2) | na | 0.12434(16 |

## Scaling




## Scaling




## Time distribution

How much time is used in generating/measuring?

- It depends (on masses, precision, algorithm, ...
- Focus on the largest current lattice: $a=0.06 \mathrm{fm}$, $m_{l}=m_{s} / 10$
Timings for the $64^{3} \times 144$ mass $0.0024 / 0.024 / 0.286$ run. Lattices are saved every six time units (three trajectories)
operation generate(RHMC) generate(RHMD)(est) static potential point spectrum ( $8 \times 3$ sources) pseudoscalars ( $4 \times 6$ sources)

30K 15K

The pseudoscalar measurement is expensive because it includes valence quarks down to $m_{s} / 20$. Largest uncertainties are in generation, since step size still being adjusted and RHMD trials underway.

## Scaling




- As we know, HISQ scales better than Asqtad.
- HOWEVER, maybe $r_{1}$ is not an optimal quantity for setting the scale, we need fair comparison.


## Charmonium spectroscopy



## Charmonium spectroscopy

- Need 2 S and higher source
- Need nonrelativistic P-wave source
- What physics are we trying to address?

