

Advanced FLUKA Course



<u>1. Built-in sources</u>

- Beam definition
- Extended sources
- Colliding beams
- Synchrotron radiation (SPECSOUR)

2. User-defined sources

- User routine SOURCE
- Useful auxiliary routines
- Sampling techniques
- Two-step methods

Built-in sources

Beam de	finitio	n - 1					
Input card: BE,	۹M						
defines several beam characteristics: type of particle, energy, divergence, profile							
<u>Example</u>							
*+1+.	2+	.3+	4+	+	6+	+7+	
BEAM	3.5 -0.0824	23	-1./	0.0	0.0	U. UPROTON	

- 3.5 GeV/c [WHAT (1)] proton beam [SDUM] with weight 1 [WHAT (6)]
- Gaussian momentum distribution: 0.082425 GeV/c FWHM [WHAT (2)]
- Gaussian angular distribution: 1.7 mrad FWHM [WHAT (3)]
- no beam width along x (point-like source) [WHAT (4)]
- no beam width along y (point-like source) [WHAT (5)]

Beam definition - 2

Input card: **BEAMPOS**

If **SDUM** = blank:

defines the coordinates of the centre of the beam spot and the beam direction

<u>Example</u>

*+1	.+2	⊦ <mark>.3</mark>	.+4	+5+	6	+ 7 + .	•
BEAMPOS	0.0	0.0	-0.1	0.0	0.0	0.0	

- x-coordinate: 0.0 [WHAT(1)]
- · y-coordinate: 0.0 [WHAT(2)]
- · z-coordinate: -0.1 cm [WHAT (3)]
- · direction cosine with respect to the x-axis: 0.0 [WHAT(4)]
- · direction cosine with respect to the y-axis: 0.0 [WHAT (5)]
- WHAT (6) is not used !
- \rightarrow beam points in the positive z-direction starting at (0.,0.,-0.1)

Beam definition - 3

Input card: **BEAMAXES**

defines the beam reference frame which all parameters defined with BEAM and BEAMPOS refer to (angular divergence, transverse profile, polarization, extended sources)

Example

*+1+.	2+.	<mark>3</mark> +.	4 +	5. <mark>+.</mark> 6+7+.
BEAMAXES	1.0	0.0	0.0	0.0 0.7071068 0.7071068

- cosine of angle between x-axis of beam and x-axis of geometry frame [WHAT (1)]
 cosine of angle between x-axis of beam and y-axis of geometry frame [WHAT (2)]
 cosine of angle between x-axis of beam and z-axis of geometry frame [WHAT (3)]
 (1.,0,0) → x-axes of beam and geometry frames are parallel
- cosine of angle between z-axis of beam and x-axis of geometry frame [WHAT (4)]
- cosine of angle between z-axis of beam and y-axis of geometry frame [WHAT (5)]
- \cdot cosine of angle between z-axis of beam and z-axis of geometry frame [WHAT (6)]
 - (0.,0.7071068,0.7071068) \rightarrow z-axis of beam frame is at 45deg to both y- and z-axes of geometry frame

Extended sources - Spherical shell source

Input card: **BEAMPOS**

If SDUM = SPHE-VOL:

defines a spatially extended source in a spherical shell



Example

*+1	.+2	+3	. + 4	+5	+6	.+7+
BEAMPOS	0.0	0.0	0.0	0.0	0.0	0.0
BEAMPOS	0.0	1.0	0.0	0.0	0.0	0.0SPHE-VOI

- radius (in cm) of the inner sphere shell: 0.0 cm [WHAT (1)]
- radius (in cm) of the outer sphere shell: 1.0 cm [WHAT (2)]
- WHAT (3) WHAT (6) are not used !

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards.

Extended sources - Cylindrical shell source

Input card: **BEAMPOS**

If SDUM = CYLI-VOL:

defines a spatially extended source in a cylindrical shell with the height parallel to the z-axis of the beam frame



<u>Example</u>						
*+1	+ 2	+ <mark>3.</mark>	+	+5	+6	.+7+
BEAMPOS	0.0	0.0	0.0	0.0	0.0	0.0
BEAMPOS	0.0	1.0	0.0	1.0	0.0	0.0CYLI-VOL

- radius (in cm) of the inner cylinder defining the shell: 0.0 cm [WHAT(1)]
- radius (in cm) of the outer cylinder defining the shell: 1.0 cm [WHAT (2)]
- \cdot height (in cm) of the inner cylinder defining the shell: 0.0 cm [WHAT (3)]
- height (in cm) of the outer cylinder defining the shell: 1.0 cm [WHAT (4)]
- WHAT (5) WHAT (6) are not used !

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards.

Extended sources - Cartesian shell source

Input card: **BEAMPOS**

If SDUM = CART-VOL:

defines a spatially extended source in a Cartesian shell with the sides parallel to the beam frame axes



<u>Example</u>						
*+1.	+2	+3.	+4+	+5. <mark>.</mark> .	+6	.+7+
BEAMPOS	0.0	0.0	0.0	0.0	0.0	0.0
BEAMPOS	0.0	1.0	0.0	1.0	0.0	1.0CART-VOL

- length (in cm) of the x-side of the inner parallelepiped defining the shell: 0.0 cm [WHAT(1)]
- · length (in cm) of the x-side of the outer parallelepiped defining the shell: 1.0 cm [WHAT (2)]
- length (in cm) of the y-side of the inner parallelepiped defining the shell: 0.0 cm [WHAT (3)]
- · length (in cm) of the y-side of the outer parallelepiped defining the shell: 1.0 cm [WHAT (4)]
- · length (in cm) of the z-side of the inner parallelepiped defining the shell: 0.0 cm [WHAT (5)]
- · length (in cm) of the z-side of the outer parallelepiped defining the shell: 1.0 cm [WHAT (6)]

The shell is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction or angular distribution are those defined by BEAM, BEAMAXES and another BEAMPOS cards. 9

Extended sources - Spherical surface source

Input card: **BEAMPOS**

If SDUM = FLOOD:

defines a source distribution on a spherical surface

<u>Example</u>

*+1	+2	+3.	. + 4	+5	. <mark>+ .</mark> 6	.+7+
BEAMPOS	0.0	0.0	0.0	0.0	0.0	0.0
BEAMPOS	1.0	0.0	0.0	0.0	0.0	0.0FLOOD

- radius (in cm) of the sphere: 1.0 cm [WHAT (1)]
- WHAT (2) WHAT (6) are not used !

The surface is centred at the (x,y,z) point defined by another BEAMPOS card with **SDUM** = blank (or = **NEGATIVE**). The particle direction is sampled according to a diffusive distribution so as to generate a uniform fluence equal to $1/(\pi R^2)$ inside the sphere (in absence of materials)

Extended sources - Example

Radioactive source of ${}^{60}Co$ (two main γ -emissions: 1332.5 keV and 1173.2 keV) cylindrical shape, 2cm diameter, 2mm height along z, centre of cylinder base at origin

*+1	+2	+3	.+4	.+5	+6	.+7+
BEAM	0.0					ISOTOPE
HI-PROPE	27.0	60.0				
BEAMPOS	0.0	0.0	0.1	0.0	0.0	0.0
BEAMPOS	0.0	1.0	0.0	0.2	0.0	0.0CYLI-VOL
or						
*+1	+2	+3	.+4	.+5	+6	.+7+
BEAM 1	252.8E-6		10000.			PHOTON
BEAMPOS	0.0	0.0	0.1	0.0	0.0	0.0
BEAMPOS	0.0	1.0	0.0	0.2	0.0	0.0CYLI-VOL

 If height along x (instead of z) add

 *...+...1...+...2...+...3...+...4...+...5...+...6...+...7...+...

 BEAMAXES
 0.0
 0.0
 -1.0
 1.0
 0.0
 0.0

Speci	al sou	irces	- hadr	on-nu	Icleus	s collision
Input card	SPECS	OUR		bec	am 1	beam 2
<u>Example:</u> LHC 7 TeV/c, full cr	ossing angle	: of 285 μrac	l in yz-plane			285 μrad
Momentum (1) If SDUM = PE	vectors o	f colliding	beams: <u>thr</u>	<u>ree possi</u>	<u>bilities</u>	, , , , , , , , , , , , , , , , , , ,
SPECSOUR	0.	0.9975	6999.9999	0.0	0.997	5-6999.9999PPSOURCE
 ×, y, z-composition ×, y, z-composition 	onents of la onents of la	o momentum o momentum	for beam 1 par for beam 2 par	ticle [WH ticle [WH	AT (1-3)] HAT (4-6)]	
2) If SDUM = C SPECSOUR	ROSSASY: 7000.	142.5E-6	90.0	7000.	142.5E-	6 0.0CROSSASY
 lab momentu polar angle (azimuth angl lab momentu polar angle (m for beam rad) betwee e (deg!) def m for beam rad) betwee	1 particle n beam 1 par ining crossin 2 particle n beam 2 par	ticle momentur g plane ticle momentu	n and posit	ive z-direc [.] tive z-direc	[WHAT(1)] tion [WHAT(2)] [WHAT(3)] [WHAT(4)] ction [WHAT(5)]12

3) If sdum = cros *+1+. SPECSOUR 7	SSYM: 2 7000.	+3 142.5E-6	.+ 4 90.0	.+5	.+6	.+7+
*+1+. SPECSOUR 7	/000.	+3 142.5E-6	.+ 4 90.0	.+5	.+6	.+7+
SPECSOUR 7	7000.	142.5E-6	90.0			
				0.0	0.0	0.0CROSSSYM
 half crossing ang azimuth angle (de WHAT (4) - WHAT (le (rad) eg!) defir (6) are	ning crossing p not used !	[WHAT lane [WHAT	(2)] (3)]	rd).	
Interaction po		containg be		nuarion cu	ru).	
SPECSOUR 7	000.	142.5E-6	90.0	0.0	0.0	0.0CROSSSYN

- sigma_x in cm for Gaussian sampling around XBEAM: 12 um [WHAT (7)]
- sigma_y in cm for Gaussian sampling around YBEAM: 12 um
- sigma_z in cm for Gaussian sampling around ZBEAM: 5 cm
 - (XBEAM, YBEAM, ZBEAM) defined with BEAMPOS card

[WHAT(8)]

[WHAT(9)]

sampling limit, in sigma, applying along x, y, and z
 < 0 no limit

[WHAT(10)]

Special sources - hadron-nucleus collision

BEAM	3000.0					HEAVYION
HI-PROPE	82.0	208.0				
SPECSOUR	574000.	142.5E-6	90.0	0.0	0.0	0.0CROSSSYM
SPECSOUR	12.E-4	12.E-4	5.0			208.0&
SPECSOUR	82.					&
• ID of beam • mass numbe • charge of b	1 particle (de er of beam 2 j beam 2 particl	efault: the or particle (det e	ne of BEAM) fault: protor	[WHAT) [WHAT [WHAT	(11)] (12)] (13)]	
SPECSOUR	7000.0	0.000335	180.0	0.0	0.0	0.0CROSSSYM
SPECSOUR	0.0	0.0	5.34	0.0		0.0&
SPECSOUR	1.0	1.057E-5	1.057E-5	1.057E-5	1.057E-5	0.0&&

- sigma_th_C (rad) for the Gaussian sampling of the beam 1 particle angle [what(14)] wrt the ideal momentum in the Crossing plane
- sigma_th_O (rad) for the Gaussian sampling of the beam 1 particle angle [WHAT (15)] wrt the ideal momentum in the Orthogonal plane
- \cdot the same as wHAT (14) for beam 2 particle
- \cdot the same as wHAT (15) for beam 2 particle

Special sources - hadron-nucleus collision Three interaction types are available: \cdot i0 + i1 * 10 + i2 * 100 [WHAT (18)] iO = flag for **nuclear nonelastic** interactions elastic interactions i1 = flag for **nuclear** i2 = flag for electromagnetic dissociation (EMD) interactions default: nuclear nonelastic + EMD if selected with the PHYSICS (SDUM = EM-DISSO) card For collisions in the DPMJET energy range, don't forget (to link it as well as to

input) the following card

*+1	+2+.	3+	4 +	5+	.6+7+
PHYSICS	8000.0				LIMITS

WHAT (1) [GeV/c] must be larger than the maximum nucleon centre-of-mass momentum

Special sources - Synchrotron radiation

- Sophisticated low energy photon transport including polarization effects for Compton, photoelectric and coherent scattering, and full account for bound electron effects: already available in FLUKA since several years
- > FLUKA can model the emission of Synchrotron Radiation:
 - by any charged particle, with arbitrary orientation vs magnetic field and traversing up to 2 circular arcs or helical paths,
 - accounting for the emitted photon polarization, as a function of the emitted photon energy, and
 - sampling SR photon energy and SR photon angle

The emitting charged particle is NOT transported:

SR photons are sampled directly.

Readily usable for bending magnets and wigglers (two steps so far).



Special sources - synchrotron radiation



• $\Delta E= 8.5 \text{ GeV/turn}$ (dE/ds=1.375 keV/cm in the dipoles)

 P = 8.5 x I[mA] MW = 8.5 x <u>10mA</u> = 85 MW in the whole accelerator (dP/ds= 1.375 x I[mA] W/cm in the dipoles)

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Special sources - synchrotron radiation

FREE SPECSOUR , ELECTRON, 175.0, 979948.86, 0.0000001, 0.0, -1.0, SYNC-RAD SPECSOUR , 1050.0, -0.59467382951, 0., 1134.9997568, -.10714843289E-02, 0.0, & FIXED

particle emitting the radiation

 emitting particle momentum [GeV/c if >0] or kinetic energy [GeV if <0]
 curvature radius [cm if >0] or magnetic field [T if <0]
 photon spectrum lower limit [GeV]
 x/y-components of the magnetic field versor
 WHAT (1)]

The z-component sign is positive for SYNC-RAD and negative for SYNC-RDN

length [cm] of the emission arc [WHAT(7)]
 coordinates (x/y/z [cm]) of the starting point of a possible second arc of same length [WHAT(8/9/10)]
 x/y-components of the emitting particle direction versor at the beginning of the second arc [WHAT(11/12)]

The starting point of the first arc as well the initial direction of the emitting particle are defined in the BEAMPOS card 19

Synchrotron radiation: 2-arc example

Synchrotron radiation photon fluence



A comment about the units

All simulation results for the synchrotron radiation SPECSOUR are quoted **per simulated synchrotron radiation photon**.

From the output file (previous ex.):

<<< Synchrotron radiation source n.</pre> 1 >>> Emitting particle: ELECTRON P: 3.00000 GeV/c Initial position : 0.0000000 0.50000000 -1400.0000cm Initial direction: 0.0000000 0.10000000 0.99498744 Magnetic field: 0.0000000 2.0000000 0.0000000 т Nominal curvature radius: 500.34614 CM Nominal arc: 150.00000 cm Arc angle: 0.29979246 rad Actual curvature radius: 500.34014 Actual arc: 150.00000 cm 5870.85237 3.00000 GeV/c and gamma: Transverse n T: Critical energy: 0.0000119705 GeV Photon emission threshold 1.0000000E-07 GeV Photons >1 eV/nominal unit length: cm^-1 0.11693748

Photons/unit length 1 eV - thres.: 2.30704527E-02 cm^-1 Photons/unit length above thres.: 9.30610323E-02 cm^-1

Total energy/nominal unit length: 4.55537630E-07 GeV/cm Energy/unit length below thresh.: 7.54228751E-10 GeV/cm Energy/unit length above thresh.: 4.54783401E-07 GeV cm in this specific case we have to scale results by 150*.093061 to obtain results **per primary emitting particle**

BEAM Visualization



- Create a USRBIN covering the beam position (preferentially Cartesian X-Y-Z) with BEAMPART as scoring particle
- Set all materials to VACUUM (to speed up calculation)
- Make one run of 1 cycle
- Visualize the results:
 - in flair as USRBIN plot
 - in the geometry editor as a custom USRBIN layer (don't forget to set properly the colorband)

With USERDUMP

• Add a **USERDUMP** card selecting ONLY Source particles

- Make one run of 1 cycle
- Create a USERDUMP plot in flair: Select the "Source" tab
 - You have the ability to make
 - ID histogram plots of any of the source quantities
 - 2D scattered plots for any of the source quantities with even the possibility to overlay on a geometry image

User-defined sources

• Allows the definition of primary particle properties (in space, energy, time, direction, or mixture of particles) which cannot be described with built-in sources

• Activated with input card SOURCE. The parameter list of that card (two continuation cards possible!) allows the user to pass on up to 18 numerical values WHASOU (1-18) and one 8-character string SDUSOU via COMMON /SOURCM/

• At each call, one (or more) particle(s) must be loaded onto COMMON /FLKSTK/ (particle bank) before returning control. The relevant variable values can be read from a file, generated by some sampling algorithm, or just assigned.

• Argument list: if NOMORE=1 (output variable) the run will be terminated after exhausting the primary particles loaded onto the stack in the present call. The history number limit set with card START will be overridden.

```
LOGICAL LFIRST
*
      SAVE LFIRST
      DATA LFIRST / .TRUE. /
      NOMORE = 0
      First call initializations:
*
      IF ( LFIRST ) THEN
      *** The following 3 cards are mandatory ***
*
         LFIRST = .FALSE.
         TKESUM = ZERZER
         LUSSRC = .TRUE.
      *** User initialization ***
*
           Any first-time initialization can be inserted here, for example
                  - setting up parameters passed on via SOURCE card
                  - reading spectra from data files
      END IF
```

NPFLKA = NPFLKA + 1* Wt is the weight of the particle WTFLK (NPFLKA) = ONEONE WEIPRI = WEIPRI + WTFLK (NPFLKA) * Particle type (1=proton....). Ijbeam is the type set by the BEAM * card (Radioactive) isotope: IF (IJBEAM .EQ. -2 .AND. LRDBEA) THEN IARES = IPROA IZRES = IPROZ IISRES = IPROM CALL STISBM (IARES, IZRES, IISRES) IJHION = IPROZ * 1000 + IPROA IJHION = IJHION * 100 + KXHEAV IONID = IJHION CALL DCDION (IONID) CALL SETION (IONID) | Heavy ion: ELSE IF (IJBEAM .EQ. -2) THEN IJHION = IPROZ * 1000 + IPROA IJHION = IJHION * 100 + KXHEAV IONID = IJHION CALL DCDION (IONID) CALL SETION (IONID) ILOFLK (NPFLKA) = IJHION * | Flag this is prompt radiation LRADDC (NPFLKA) = .FALSE. | Group number for "low" energy neutrons, set to 0 anyway IGROUP (NPFLKA) = 0_____ Normal hadron: ELSE IONID = IJBEAM ILOFLK (NPFLKA) = IJBEAM * | Flag this is prompt radiation LRADDC (NPFLKA) = .FALSE. * | Group number for "low" energy neutrons, set to 0 anyway IGROUP (NPFLKA) = 0END IF _____

increase pointer in FLKSTK

weight of particle

(if varying -> biased source) total weight of primaries (don't change)

Definition of particle type

- The template sets the type of particle equal to the one defined by the BEAM card (and HI-PROPE, if used).

- Whichever valid particle type can be set inside the source (may be varying event by event)



```
* User dependent flag:
LOUSE (NPFLKA) = 0
...
* User dependent spare variables:
DO 100 ISPR = 1, MKBMX1
SPAREK (ISPR,NPFLKA) = ZERZER
100 CONTINUE
* User dependent spare flags:
DO 200 ISPR = 1, MKBMX2
ISPARK (ISPR,NPFLKA) = 0
200 CONTINUE
```

Variables that allow to store additional information in COMMON /FLKSTK/,

such as information on ancestors of a certain particle

Auxiliary routines - Random numbers

$\dots = FLRNDM (XDUMMY)$

returns a 64-bit random number [0-1)

NOTE: Fundamental for SOURCE! No other external random generators must be used, otherwise the history reproducibility will be lost.

CALL FLNRRN (RGAUSS)

returns a normally distributed random number RGAUSS

CALL FLNRR2 (RGAUS1, RGAUS2)

returns an uncorrelated pair of normally distributed random numbers RGAUS1 and RGAUS2

CALL SFECFE (SINT, COST) returns SINT and COST, sine and cosine of a random azimuthal angle SINT**2 + COST**2 = 1.D+00

CALL RACO (TXX, TYY, TZZ) returns a random 3D direction (TXX, TYY, TZZ) TXX**2 + TYY**2 + TZZ**2 = 1.D+00

Auxiliary routines - Name <-> number conv.

```
Conversion of region name to number
```

```
CALL GEON2R ( REGNAM, NREG, IERR )

Input variable:

REGNAM = region name (CHARACTER*8)

Output variables:

NREG = region number
```

IERR = error code (0 on success, 1 on failure)

Conversion of region number to name

```
CALL GEOR2N ( NREG, REGNAM, IERR )
```

Input variable:

NREG = region number

Output variables:

REGNAM = region name (CHARACTER*8)

IERR = error code (0 on success, 1 on failure)

Auxiliary routines - Others

CALL OAUXFI ('file', LUN, 'CHOPT', IERR)

to open an auxiliary file (to read data or parameters) looking automatically for the file in some default locations (temporary directory, working directory)

CALL FLABRT ('routine name', 'message')

this allows to force a FLUKA abort on user request: it might be useful to perform a debugging (using gdb for instance)

CALL SFLOOD (XXX, YYY, ZZZ, UXXX, VYYY, WZZZ)

returns a random position XXX, YYY, ZZZ on the surface of a sphere of radius 1 and centre 0 (multiply XXX, YYY, ZZZ by the actual radius and add the centre coordinates) and a random direction UXXX, VYYY, WZZZ (cosines) so as to generate a uniform fluence inside the sphere, equal to $1/(\pi R^2)$, being R the actual sphere radius.

Sampling from a distribution - Discrete

1) From the cumulative distribution

- Suppose to have a discrete random variable x, that can assume values x₁, x₂, ..., x_n, ... with probability p₁, p₂, ..., p_n, ...
- Assume $\sum_{i} p_{i} = 1$, or normalize it
- Divide the interval [0,1) in n subintervals, with limits

 $y_0 = 0, y_1 = p_1, y_2 = p_1 + p_2, \dots$

• Generate a uniform pseudo-random number ξ

 $\mathbf{y}_{i-1} \leq \boldsymbol{\xi} \boldsymbol{\cdot} \mathbf{y}_i$

• Find the *ith* y-interval such that

• Select $X = x_i$ as the sampled value

Since ξ is uniformly random:

 $P(x_i) = P(y_{i-1} \le \xi < y_i) = y_i - y_{i-1} = p_i$



Sampling from a distribution - Discrete

2) By adjusting weights

- Suppose to have a fluence energy spectrum Φ given in N discrete energy bins between E_0 and $E_N : \Phi_1, ..., \Phi_N$
- Generate a uniform pseudo-random number ξ
- Find the *ith* energy bin such that

 $E_{i-1} \leq \xi (E_N - E_0) < E_i$

- Generate another uniform pseudo-random number $\xi \in [0,1)$ and sample an energy uniformly within the *i*th energy bin
- assign a weight Φ_i to that primary particle

Note: This method is often used for spectra steeply decreasing with energy (e.g., $\Phi \sim 1/E$), where the result depends significantly on the particle cascades initiated by high energy primaries, as it ensures faster convergence to the true value.

Example Sampling from a histogram - 1

```
PARAMETER (NMAX=1000)
                                             Logical unit from input file
     DIMENSION ERG (NMAX), CUM (NMAX)
                                             as WHAT(1) of the SOURCE card.
     CHARACTER*250 LINE
     SAVE N, ERG, CUM
                                             Use OPEN card to open the file
        ( LFIRST ) THEN
                                             which contains pairs Energy-Value.
      IF
                                             First value is supposed to be 0 in
          LUNRD = NINT(WHASOU(1))
          N = 0
                                             order to set the lower energy limit.
          SUM
                = ZERZER
          EPREV = ZERZER
10
          CONTINUE
            READ (LUNRD, '(A)', ERR=9999, END=20) LINE
            READ (LINE, *, ERR=10) E, H
            N = N + 1
            IF (N .GT. NMAX)
                 CALL FLABRT ('SOURCE', 'Please increase NMAX')
    &
            IF (N .EQ. 1 .AND. ABS(H).GT.AZRZRZ)
                 CALL FLABRT (
                      'SOURCE', 'ZERO was expected as first value')
*** Create cumulative sum of dE*V
            SUM = SUM + H*(E-EPREV)
            EPREV = E
            ERG(N) = E
            CUM(N) = SUM
        GO TO 10
20
        CONTINUE
        CLOSE (LUNRD)
     END IF
9999 CALL FLABRT ('SOURCE', 'Error reading source file')
```

Example: hsource.f

Example Sampling from a histogram - 2

```
* From this point .....
*** Select a random energy interval
    C = CUM(N) * FLRNDM(C)
*** Find interval (CUM(1)=0)
    DO I=2,N
    IF (CUM(I) .GT. C) THEN
*** Found interval I, select a random energy inside
    E = ERG(I-1) + (ERG(I)-ERG(I-1))*FLRNDM(C)
    GO TO 90
    END IF
    END DO
```

1) By integration

 Integrate the distribution function *f(x)*, analytically or numerically, and normalize to 1 to obtain the normalized cumulative distribution

$$F(x) = \frac{\int_{x_{\min}}^{x} f(t)dt}{\int_{x_{\min}}^{x_{\max}} f(t)dt}$$

- Generate a uniform pseudo-random number $\xi \in [0,1)$
- Get the desired result by finding the inverse value $x = F^{-1}(\xi)$, analytically or most often numerically, i.e. by interpolation (table look-up)

Since ξ is uniformly random:

$$P(a < x < b) = P(F(a) \le \xi < F(b)) = F(b) - F(a) = \int_{a}^{b} f(x) dx$$

<u>Example</u>



Repeat N times

2) By rejection

- Let be f'(x), a normalized distribution function, which cannot be sampled by integration and inversion
- Let be g'(x), a normalized distribution function, which can be sampled, and such that $Cg'(x) \ge f'(x)$, $\forall x \in [x_{\min}, x_{\max}]$
- Sample X from g'(x), and generate a uniform pseudo-random number $\xi \in [0, 1)$
- Accept X if $\xi < f'(X)/Cg'(X)$, if not repeat the previous step The overall efficiency (accepted/sampled) is given by:

$$R = \int \frac{f'(x)}{Cg'(x)} g'(x) dx = \frac{1}{C}$$

and the probability that X is accepted is unbiased:

$$P(X)dX = \frac{1}{R}g'(X)dX \times \frac{f'(X)}{Cg'(X)} = f'(X)dX$$

<u>Example</u>

- Let be $f'(x) = (1+3x^2)/4$, $x \in [-1,1]$,
- Take g'(x)=1/2, C=2
- Generate two uniform pseudo-random numbers ξ₁, ξ₂ ∈ [0,1)
- Accept $X=2\xi_1-1$ if $\xi_2 < (1+3X^2)/4$, if not

repeat



3) By adjusting weights

- Suppose to have a fluence energy spectrum $\Phi(E)$ given in between E_0 and E_1
- Generate a uniform pseudo-random number $\xi \in [0,1)$ and calculate the sampled energy $E = E_0 + \xi (E_1 E_0)$
- Assign a weight $\Phi(E)$ to that primary particle

Two-step methods

Goal: predict radiation fields and observables in remote locations in a huge geometry



direct calculation in one step

can be highly inefficient due to the small affected phase-space

Ex.2: MYRRHA ADS

Two-step methods

Solution: split simulation into two steps.

Two different approaches are possible:

- (1) Calculation of radiation fields in a suitable location: for each particle type, calculate fluence distributions, double-differential in energy and angle
 - (2) Sample from the calculated distributions in a user-defined source, and score the interested quantities at the location of interest
- Obs: it must be clear that in this way the correlations within one full event are lost. All quantities are calculated as average quantities
 - pay attention to calculate the radiation fields in step (1) covering all the phase space relevant for step (2)
- (1) Dumping particles at the location of interest: write all information on particles entering it (type,energy, position, direction) into an external file
 - (2) Read the information from the external with a user-defined source

First approach: an example

In this example, a source term built calculating the neutrons backward emitted at the location (A) was important to calculate the average neutron and photon fluence on detectors very far from the neutron production point

