



EFT approach in Dark Matter searches

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Based on 1307.2253, 1402.1275 and 1405.3101

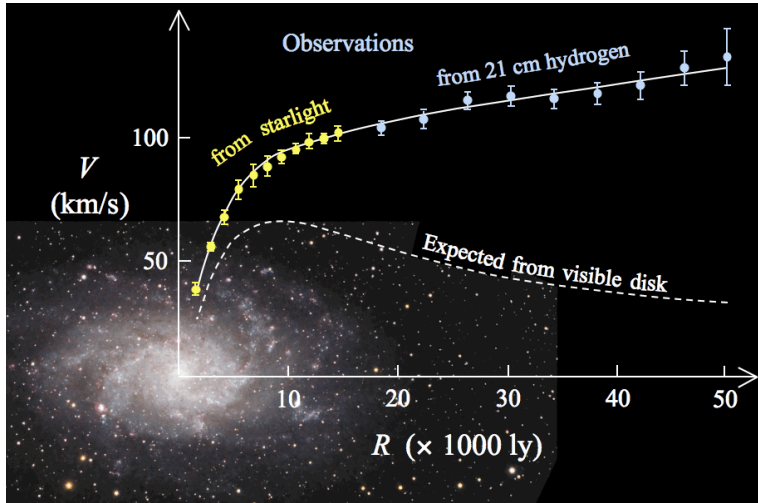
EM with G. Busoni, A. De Simone, J. Gramling, T. Jacques, T. Riotto

Outline

- Introduction: evidences, candidates, WIMPs
- DM searches at the LHC
- LHC: what models should we use?
 - Effective theories and validity concerns
 - Simplified models
- Conclusion

Evidences

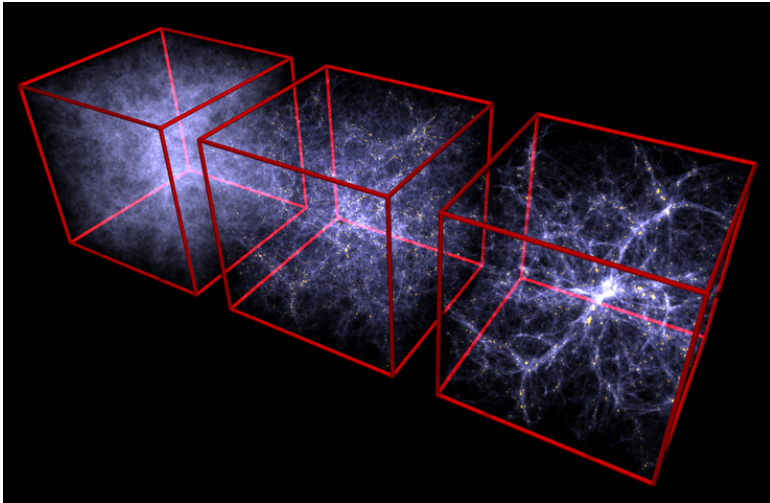
Galaxies



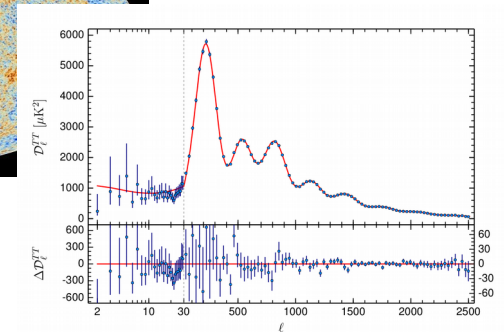
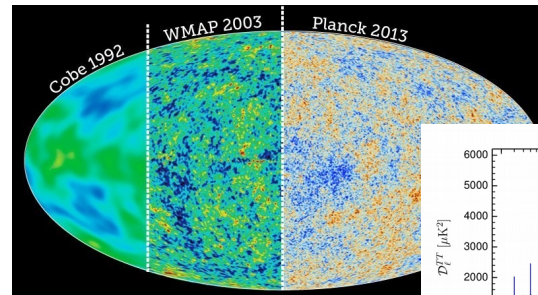
Galaxy clusters



Structure formation



Cosmic Microwave Background



The “WIMP miracle”

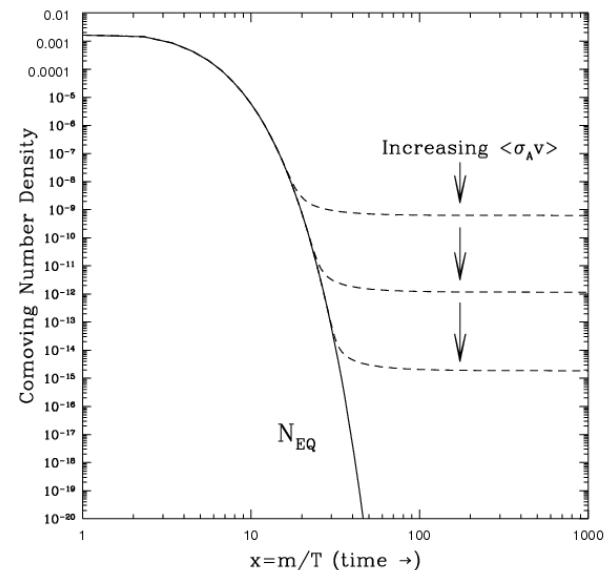
New BSM particles are needed. How are they produced?

Thermal freeze-out mechanism

DM initially in thermal equilibrium in the expanding universe

$$\dot{n} + 3Hn = -\langle\sigma v\rangle (n^2 - n_{\text{eq}}^2)$$

When $\Gamma \sim H$ the DM decouples and its comoving number density remains fixed



The WIMP miracle:

A particle with mass around the weak scale interacting with weak force (as the ones we expect from solutions to the naturalness problem) has automatically the correct relic abundance

DM – SM interaction

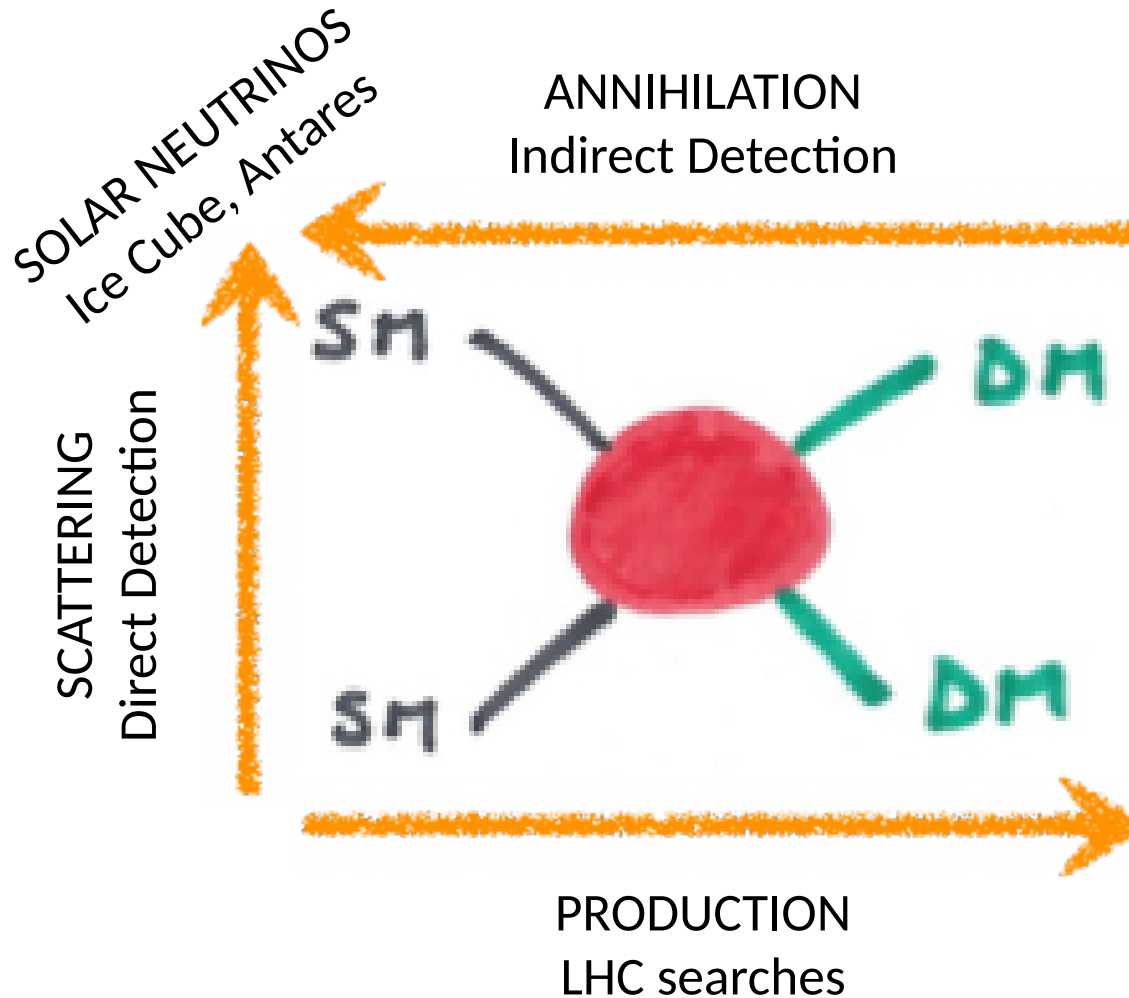
How does DM interact with the SM?

1) **Gravitationally:** DM gravitates, and leaves its imprint on LSS dynamics, formation, CMB...

2) **Non gravitationally:** we don't know, but

- It's our only hope!
- Plenty of BSM models predict DM candidates (SUSY & other naturalness related constructions, axions, ...)
- DM production mechanism
- How can we probe this interaction?

How can we test DM interactions with the Standard Model?



DM at the LHC

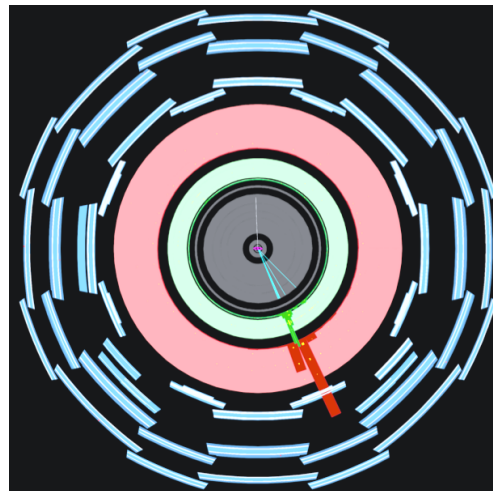
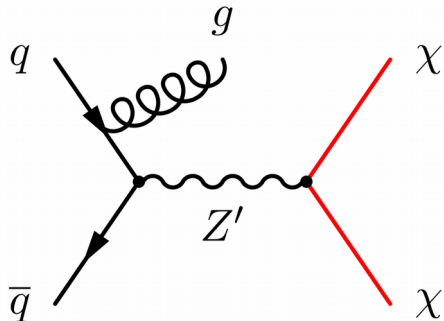
Trivial observation: WIMP particles do not interact with the detectors



**Tag DM events with
some recoiling SM particle**

e.g. “mono-X + MET” searches

a single SM object recoiling against some
unpaired momentum in the transverse plane

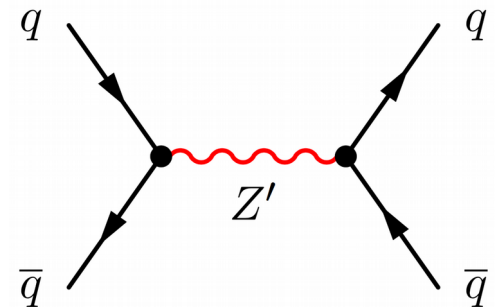


ATLAS mono-jet event, CERN courier

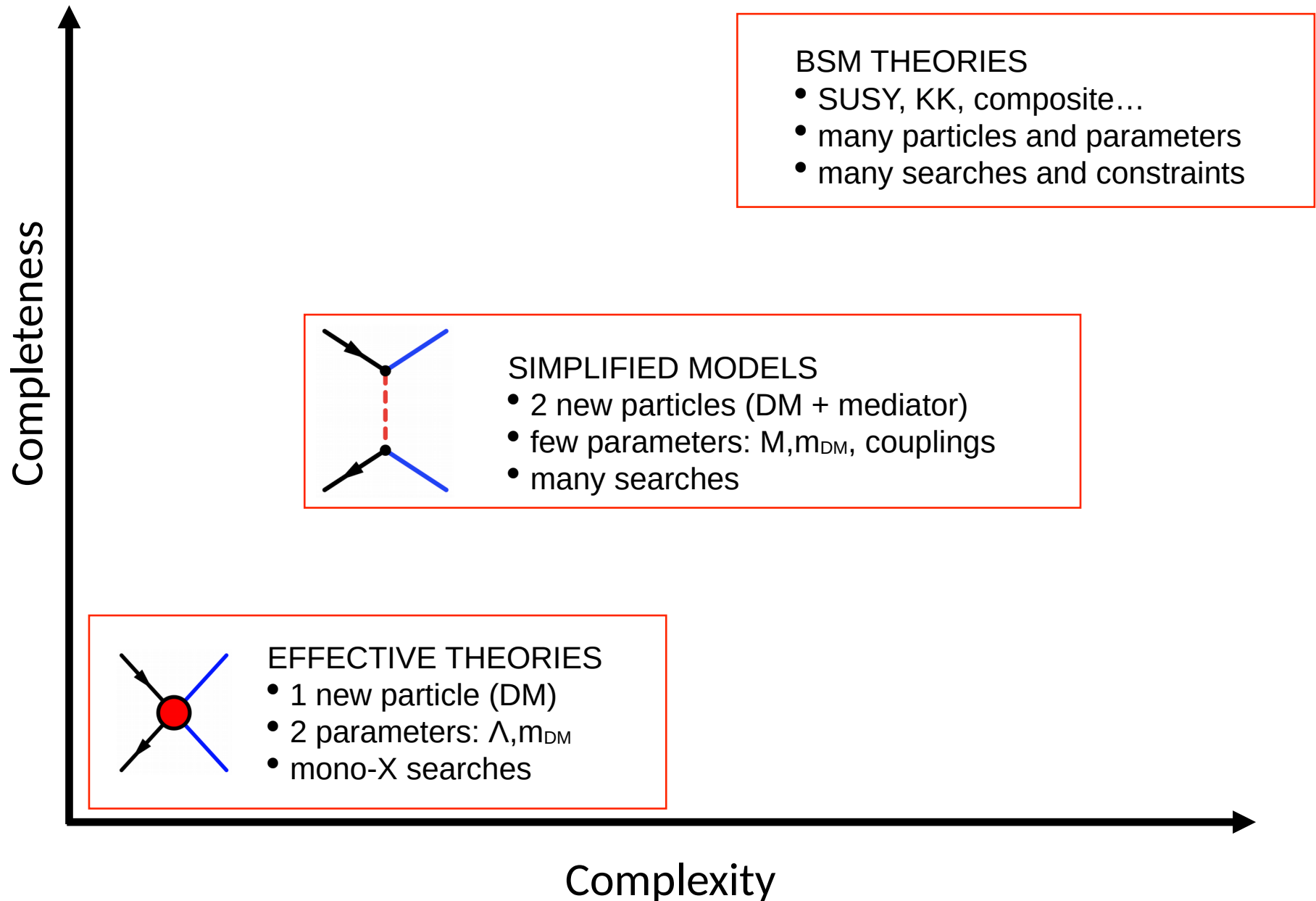
**Study the “dark sector”
independently of DM**

e.g. “di-jet” searches

the mediator is produced and decays back into a
quark - antiquark pair



DM “models”



Why EFT

Effective operators have a number of advantages as a tool for DM searches:

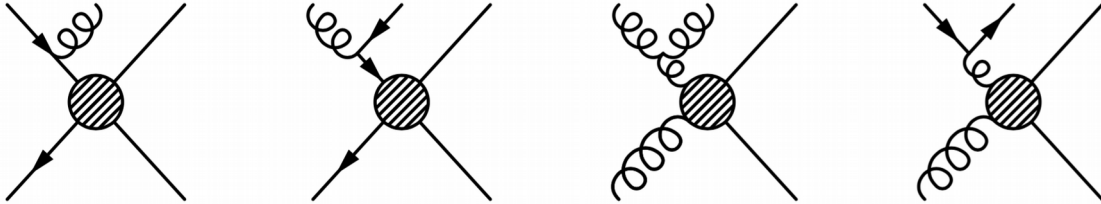
- Simple, minimal number of parameters
- “Universal”: whatever BSM theory lead to the same set of effective operators
- Suitable for strongly interacting dark sectors
- ~~Exploit complementarity: LHC can probe the same effective operator as Direct/Indirect searches~~

EFT description

Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu, 1008.1783, PRD

The simplest description is EFT
(with initial state radiation)

$$\mathcal{L} = \bar{\psi} (i\partial \cdot \gamma - m) \psi + \frac{\mathcal{O}_6}{\Lambda^2} + \frac{\mathcal{O}_8}{\Lambda^4} \dots$$

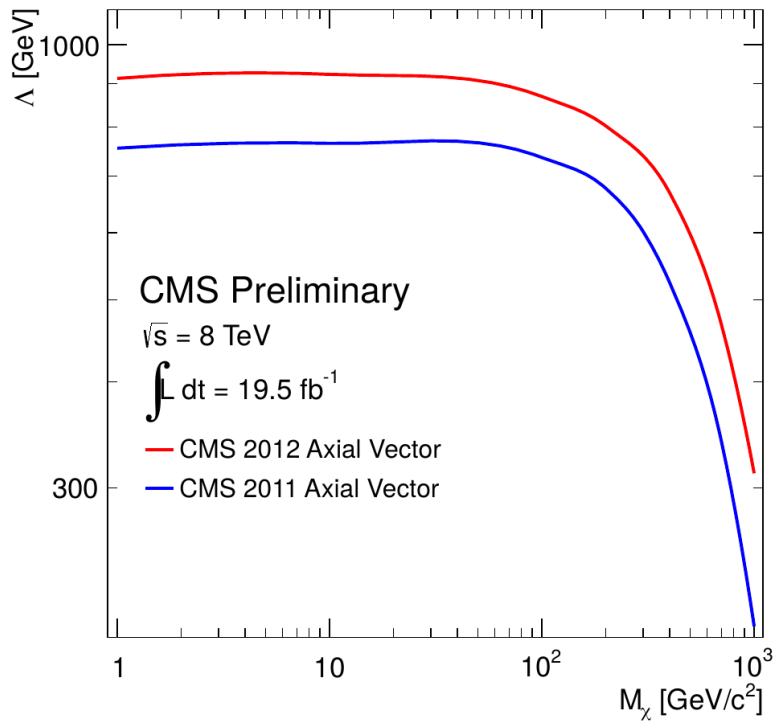


- Write a complete set of dim-6 operators (e.g. in the s-channel)
- Assume DM production happens only through one of these
- Derive bounds on the plane ($m_{\text{DM}}-\Lambda$) for that operator

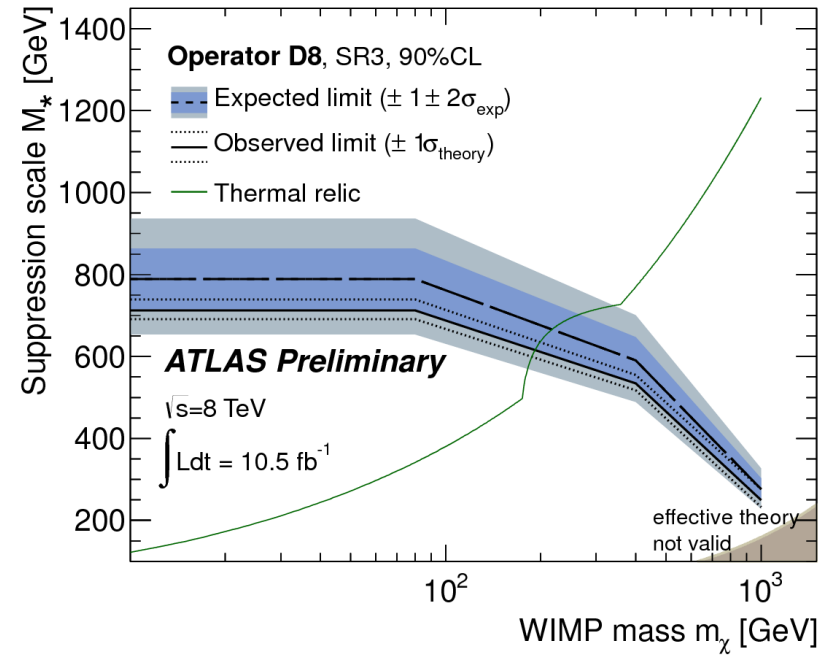
Name	Operator	Coefficient
D1	$\bar{\chi}\chi \bar{q}q$	m_q/Λ^3
D1'	$\bar{\chi}\chi \bar{q}q$	$1/\Lambda^2$
D2	$\bar{\chi}\gamma^5\chi \bar{q}q$	im_q/Λ^3
D2'	$\bar{\chi}\gamma^5\chi \bar{q}q$	i/Λ^2
D3	$\bar{\chi}\chi \bar{q}\gamma^5q$	im_q/Λ^3
D3'	$\bar{\chi}\chi \bar{q}\gamma^5q$	i/Λ^2
D4	$\bar{\chi}\gamma^5\chi \bar{q}\gamma^5q$	m_q/Λ^3
D4'	$\bar{\chi}\gamma^5\chi \bar{q}\gamma^5q$	$1/\Lambda^2$
D5	$\bar{\chi}\gamma_\mu\chi \bar{q}\gamma^\mu q$	$1/\Lambda^2$
D6	$\bar{\chi}\gamma_\mu\gamma^5\chi \bar{q}\gamma^\mu q$	$1/\Lambda^2$
D7	$\bar{\chi}\gamma_\mu\chi \bar{q}\gamma^\mu\gamma^5q$	$1/\Lambda^2$
D8	$\bar{\chi}\gamma_\mu\gamma^5\chi \bar{q}\gamma^\mu\gamma^5q$	$1/\Lambda^2$
D9	$\bar{\chi}\sigma_{\mu\nu}\chi \bar{q}\sigma^{\mu\nu}q$	$1/\Lambda^2$
D10	$\bar{\chi}\sigma_{\mu\nu}\gamma^5\chi \bar{q}\sigma^{\mu\nu}q$	i/Λ^2
D11	$\bar{\chi}\chi G^{\mu\nu}G_{\mu\nu}$	$\alpha_s/4\Lambda^3$
D12	$\bar{\chi}\gamma^5\chi G^{\mu\nu}G_{\mu\nu}$	$i\alpha_s/4\Lambda^3$
D13	$\bar{\chi}\chi G^{\mu\nu}\tilde{G}_{\mu\nu}$	$i\alpha_s/4\Lambda^3$
D14	$\bar{\chi}\gamma^5\chi G^{\mu\nu}\tilde{G}_{\mu\nu}$	$\alpha_s/4\Lambda^3$

EFT description

Effective operators have been used extensively by ATLAS / CMS



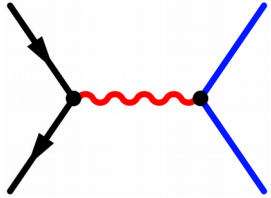
CMS-PAS-EXO-12-048



ATLAS-CONF-2012-147

Validity of the EFT

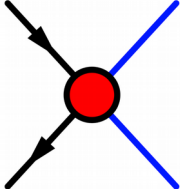
The validity of effective theories is limited in energy by their cut-off scale



A Feynman diagram showing a t-channel exchange between two fermion pairs. Two black lines with arrows (representing fermions) enter from the left, and two blue lines (representing fermions) exit to the right. They are connected by a red wavy line (representing a scalar or vector mediator).

$$\sim \frac{g_\chi g_q}{Q_{\text{tr}}^2 - M^2} = -\frac{g_\chi g_q}{M^2} \left(1 + \cancel{\frac{Q_{\text{tr}}^2}{\Lambda^2}} + \cancel{\frac{Q_{\text{tr}}^4}{\Lambda^4}} + \dots \right)$$

A curved arrow points from the wavy line in the first diagram to a red circle in the second diagram.



A Feynman diagram showing a contact interaction. Two black lines with arrows enter from the left, and two blue lines exit to the right, all meeting at a central red circle.

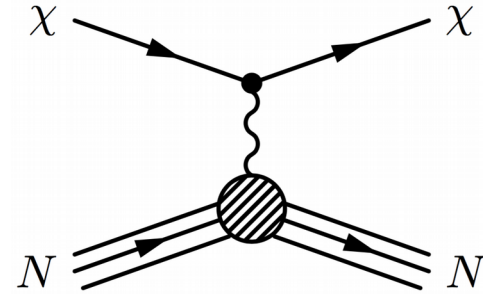
$$= \frac{1}{\Lambda^2} (\bar{\chi} \Gamma_a \chi) (\bar{q} \Gamma_b q)$$

One should check that the energy scale of the process under study is smaller than Λ

Validity of the EFT

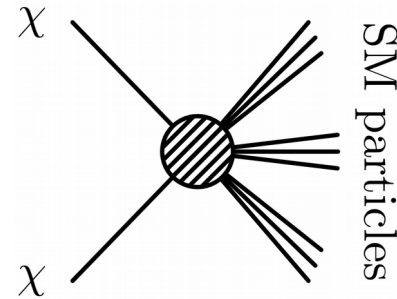
Direct detection

$$\langle Q_{\text{tr}}^2 \rangle \approx \mathcal{O}(100 \text{ MeV})^2 \ll \Lambda^2$$



Indirect detection

$$v \sim 10^{-3}, m_\chi < M_{\text{med}}$$

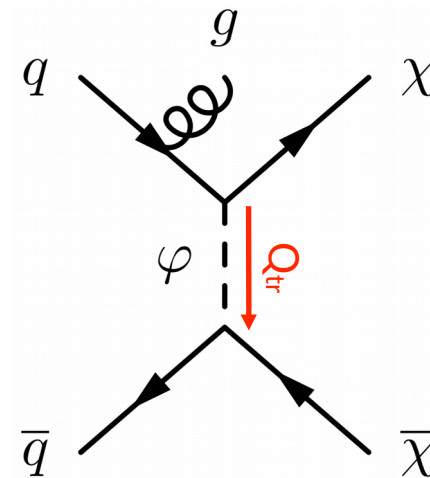
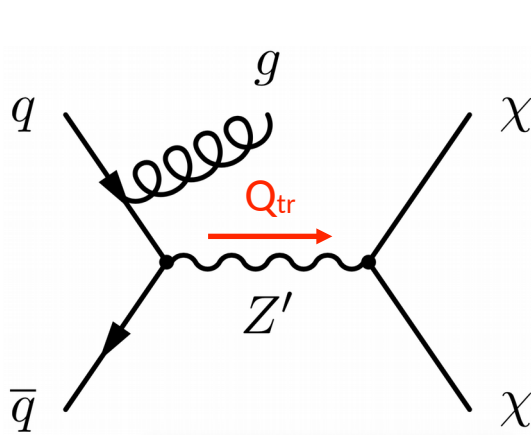


In both cases, the EFT is typically safe

Validity of the EFT

At the LHC, the typical momentum exchanged is very large

$$\langle Q_{\text{tr}}^2 \rangle \sim \mathcal{O}(1 \text{ TeV})^2 \sim \Lambda^2$$



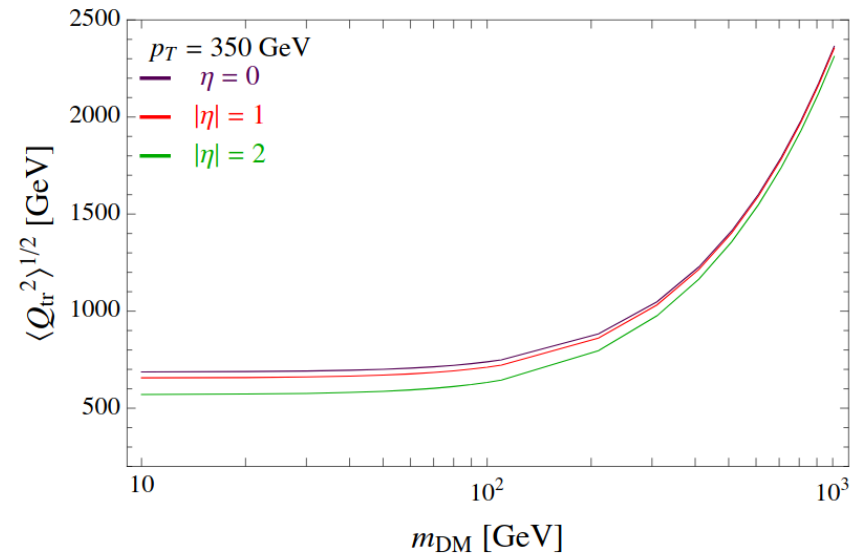
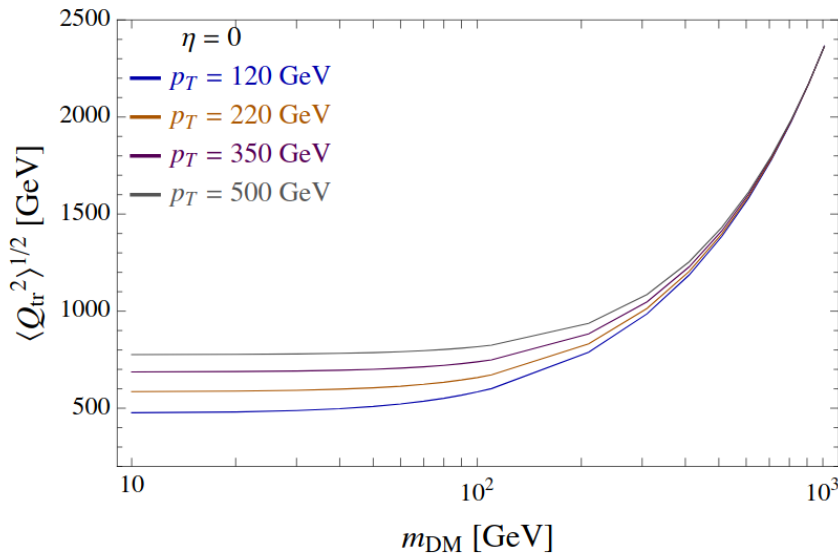
The effective description is expected to fail

Validity of the EFT

Momentum exchanged in a $qq \rightarrow XXg$ process

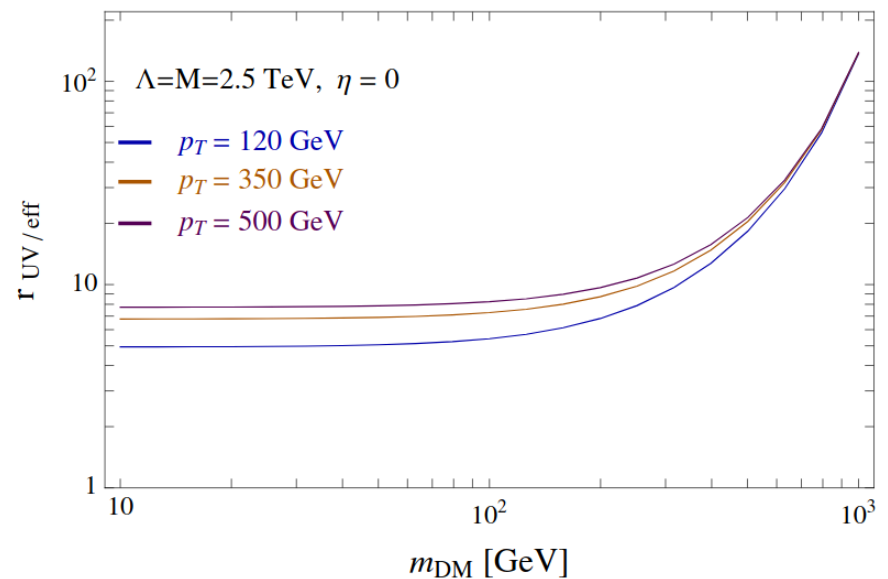
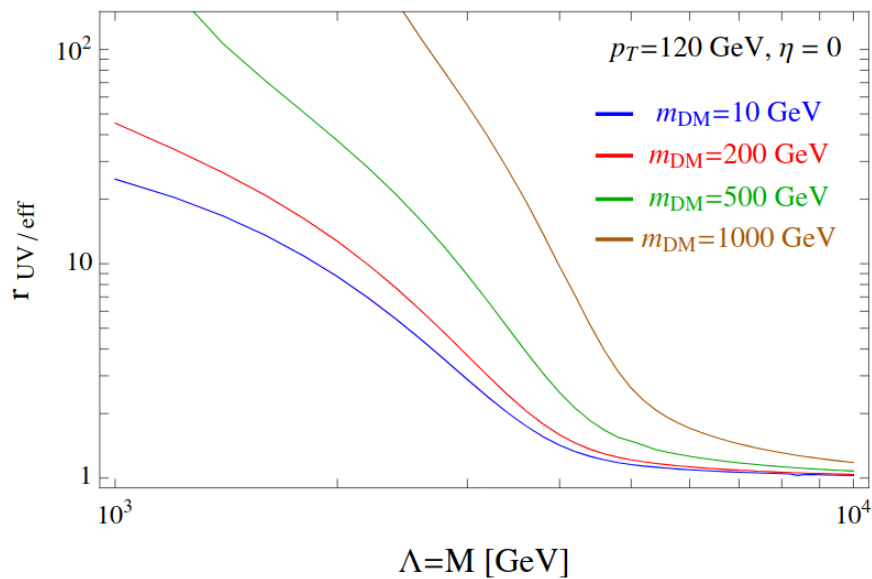
$$Q_{\text{tr}}^2 = (p_q + p_{\bar{q}} - p_g)^2 = x_1 x_2 s - \sqrt{s} p_T (x_1 e^{-\eta} x_2 e^{\eta})$$

Average over pdfs



Compare with a simple UV completion

$$\mathcal{L}_{\text{UV}} \supset \frac{1}{2} M_{\text{med}}^2 S^2 - g_q \bar{q} q S - g_\chi \bar{\chi} \chi S \quad \text{vs.} \quad \mathcal{L}_{\text{EFT}} \supset \frac{1}{\Lambda^2} \bar{q} q \bar{\chi} \chi$$



EFT works better for heavy mediator, light DM, low p_T

Measure the EFT validity

Experiments used to impose loose conditions on the EFT validity

- EFT is reliable if

$$\Lambda = \frac{M_{\text{med}}}{\sqrt{g_\chi g_q}} > \frac{Q_{\text{tr}}}{\sqrt{g_\chi g_q}}$$

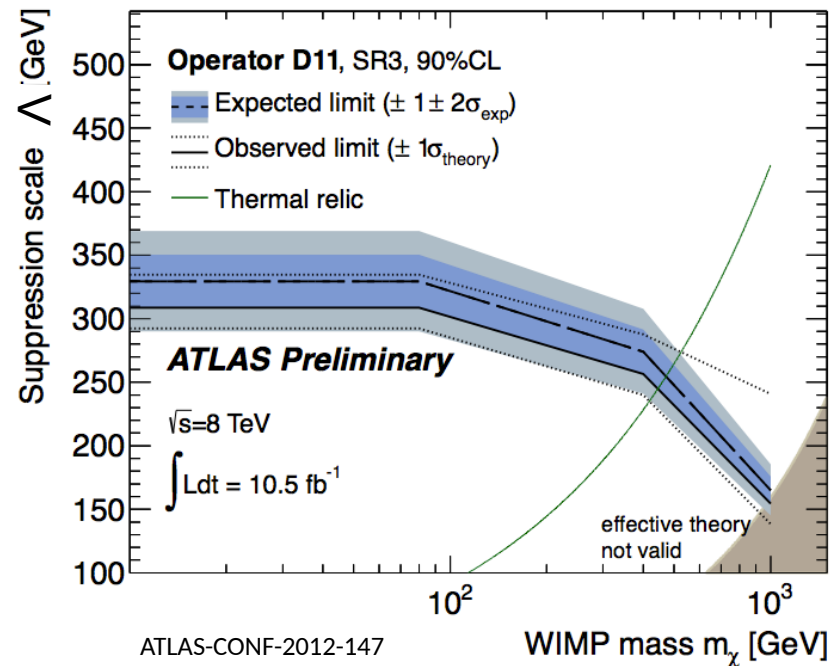
- To produce DM on shell (in the s-channel)

$$Q_{\text{tr}} > 2m_\chi$$

- Perturbativity: $g \lesssim 4\pi$

- The validity condition is then

$$\Lambda > \frac{m_\chi}{2\pi}$$



Cross section imposing $Q_{\text{tr}} < \Lambda$

To quantify the goodness/badness of EFT we can compute the cross section with or without imposing the condition on Q_{tr}

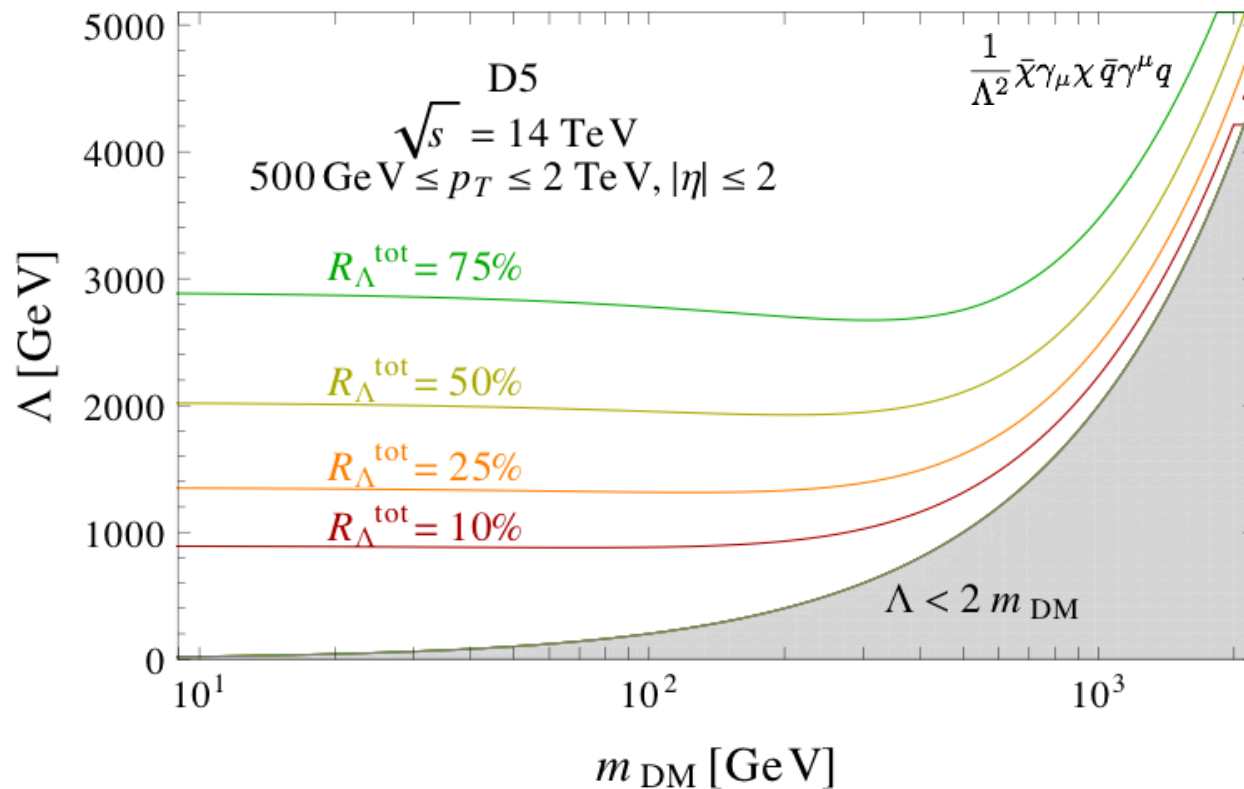
$$R_{\Lambda}^{\text{tot}}(m_{\text{DM}}, \Lambda) \equiv \frac{\sigma_{\text{eff}}|_{Q_{\text{tr}} < \Lambda}}{\sigma_{\text{eff}}} = \frac{\int_{p_{\text{T}}^{\text{min}}}^{p_{\text{T}}^{\text{max}}} dp_{\text{T}} \int_{-2}^2 d\eta \left. \frac{d^2 \sigma_{\text{eff}}}{dp_{\text{T}} d\eta} \right|_{Q_{\text{tr}} < \Lambda}}{\int_{p_{\text{T}}^{\text{min}}}^{p_{\text{T}}^{\text{max}}} dp_{\text{T}} \int_{-2}^2 d\eta \frac{d^2 \sigma_{\text{eff}}}{dp_{\text{T}} d\eta}}$$

$R_{\Lambda} \approx$ fraction of events in the EFT validity region (for $g=1$)

- $R_{\Lambda} \approx 1 \Rightarrow$ EFT valid
- $R_{\Lambda} \lesssim 1 \Rightarrow$ EFT not valid

Implications for LHC searches

Results for D5 at 14 TeV:



The non-validity region of EFT is much larger than the one naively excluded

Rescale existing EFT bounds

Neglecting all uncertainties, the bounds have a simple scaling with Λ :

$$N_{\text{signal}} \sim \frac{1}{\Lambda^4} \tilde{N}_{\text{signal}} \quad (\text{for dim-6 operator})$$

Bounds are obtained imposing

$$N_{\text{signal}} < N_{\text{obs}} \Rightarrow \Lambda > \Lambda_{\text{exp}} \equiv \left(\frac{\tilde{N}_{\text{signal}}}{N_{\text{obs}}} \right)^{1/4}$$

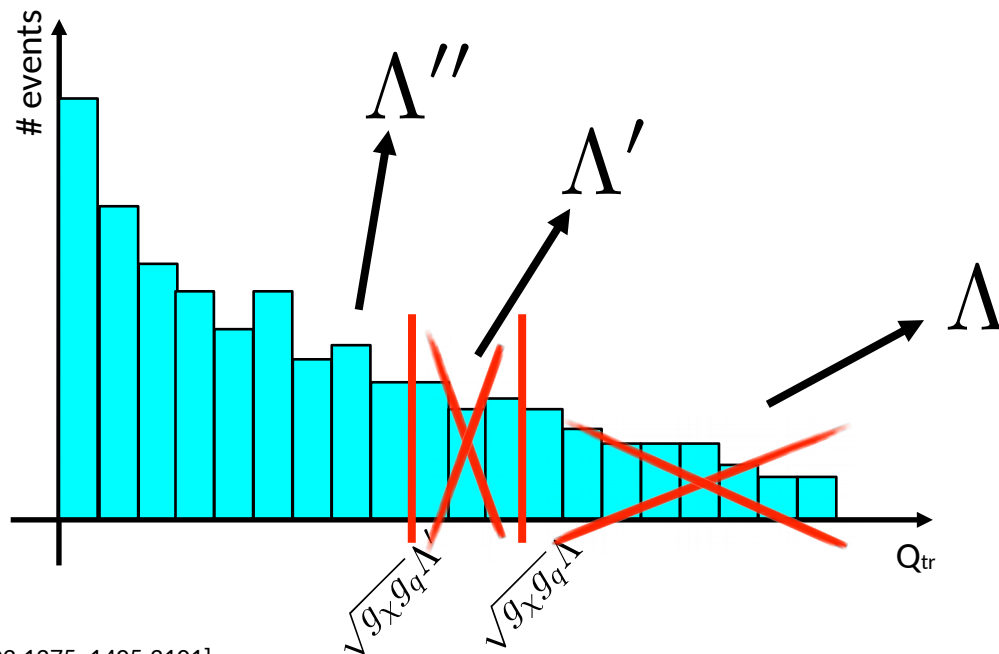
By rescaling $N_{\text{signal}} \rightarrow R_{\Lambda} N_{\text{signal}}$ the new bound is obtained by solving

$$\Lambda(m_{\chi}) > R_{\Lambda}(m_{\chi}) \Lambda_{\text{exp}}(m_{\chi})$$

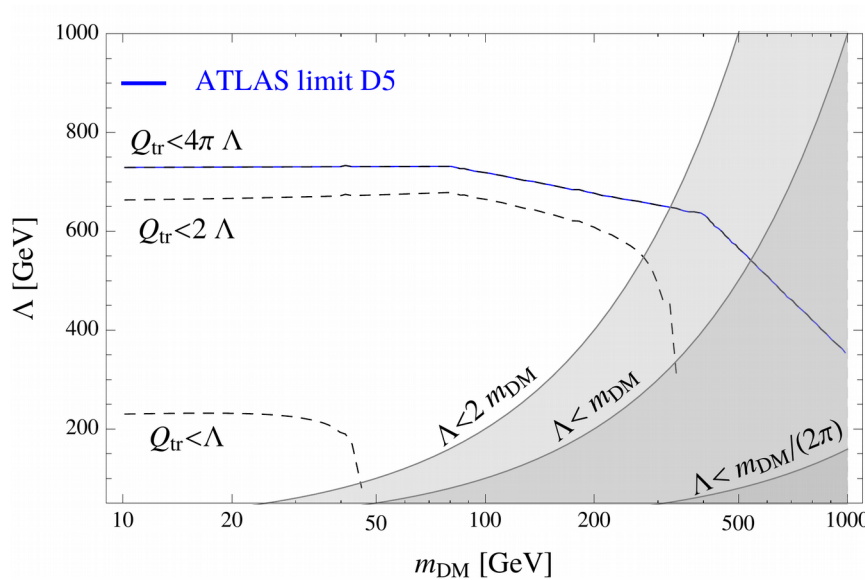
Rescale EFT bounds

Rescale the limits on Λ by considering only a fraction R_Λ of the events:

- Fix m_χ , g_q , g_χ
- Reject events with $Q_{\text{tr}} > \sqrt{g_\chi g_q} \Lambda$
- Obtain a new limit Λ' and reiterate



Implications for LHC searches



$$D5 : \quad \bar{q} \gamma_{\mu} q \bar{\chi} \gamma^{\mu} \chi$$

Atlas limits from
ATLAS-CONF-2012-147

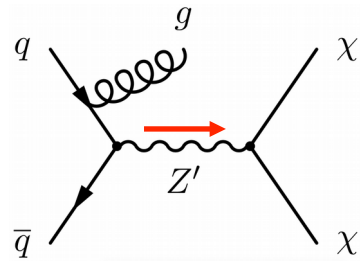
- Simple rescaling of existing limits is only suitable for simple cut-and-count analysis
- Info about the kinematic distribution can be exploited by applying the cut

$$Q_{\text{tr}}^2 < \sqrt{g_q g_{\chi}} M_{\text{med}}^2$$

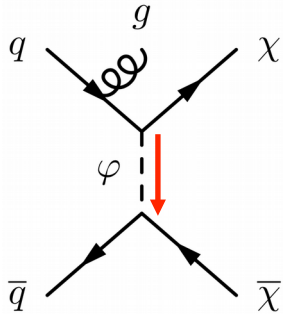
at the generator level

Limitations

- The definition of Q_{tr} depends on the UV completion



$$Q_{\text{tr}}^2|_s = (p_\chi + p_{\bar{\chi}})^2$$



$$Q_{\text{tr}}^2|_t = (p_\chi + p_{\bar{q}})^2$$

in general (e.g. composite models) it's not clear a priori what's the correct choice

- Also the choice of the UV-cutoff depends on unknown UV physics

$$Q_{\text{tr}}^2 < \sqrt{g_\chi g_q} M_{\text{med}}^2$$

More robust EFT bounds

Racco, Wulzer, Zwirner, 1502.04701, JHEP

We want to get robust EFT bounds without relying on assumption about the UV

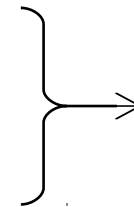
$$\mathcal{L} = \bar{\chi}(i\partial \cdot \gamma - m_\chi)\chi + \frac{1}{\Lambda^2}\mathcal{O}_6 \quad \text{(assuming only 1 dim-6 operator)}$$

Three relevant scales:

m_χ DM mass

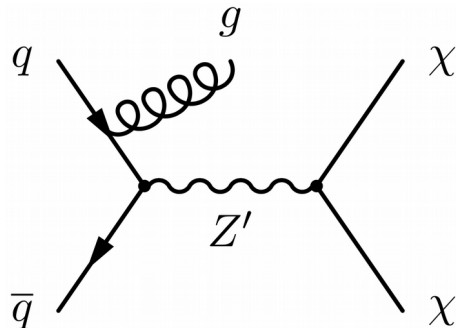
Λ EFT scale

Λ_{cut} Cut-off scale



In general define

$$\Lambda_{\text{cut}} = g_* \Lambda$$

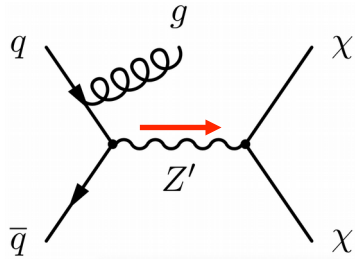


For a simple UV completion with an s-channel mediator the relation is obvious

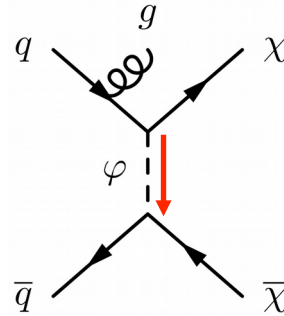
$$\Lambda = \frac{M_{\text{med}}}{\sqrt{g_\chi g_q}} \quad \Lambda_{\text{cut}} = M_{\text{med}}$$

More robust EFT bounds

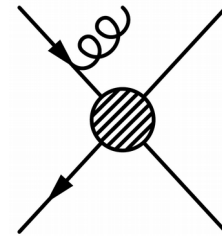
Racco, Wulzer, Zwirner, 1502.04701, JHEP



$$Q_{\text{tr}}^2|_s = (p_\chi + p_{\bar{\chi}})^2$$



$$Q_{\text{tr}}^2|_t = (p_\chi + p_{\bar{q}})^2$$



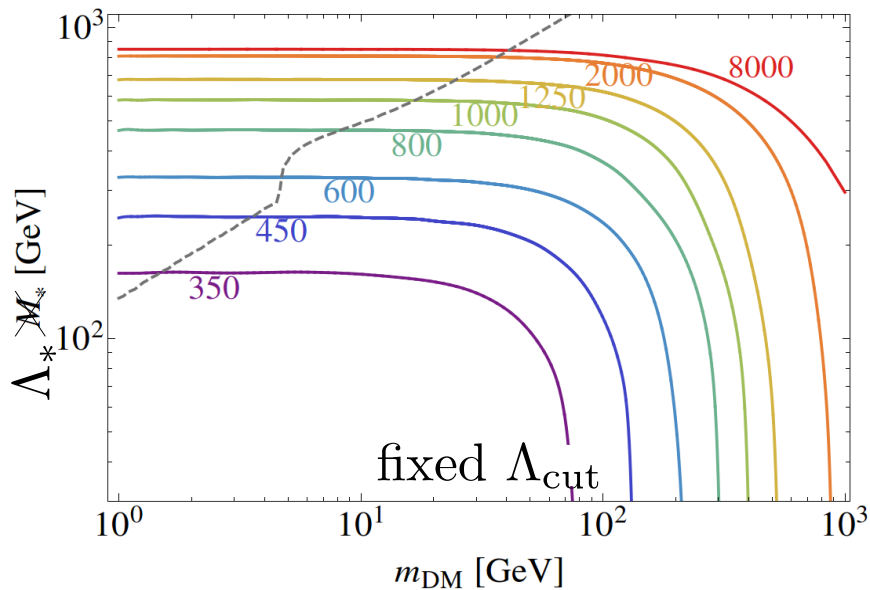
$$Q_{\text{tr}}^2 = ?$$

The definition of Q_{tr} depends on the UV completion. A *model-independent, conservative* condition uses the centre of mass energy of the hard process.

$$E_{\text{cm}}^2 \equiv (p_\chi + p_{\bar{\chi}} + p_g)^2 < \Lambda_{\text{cut}}^2$$

More robust EFT bounds

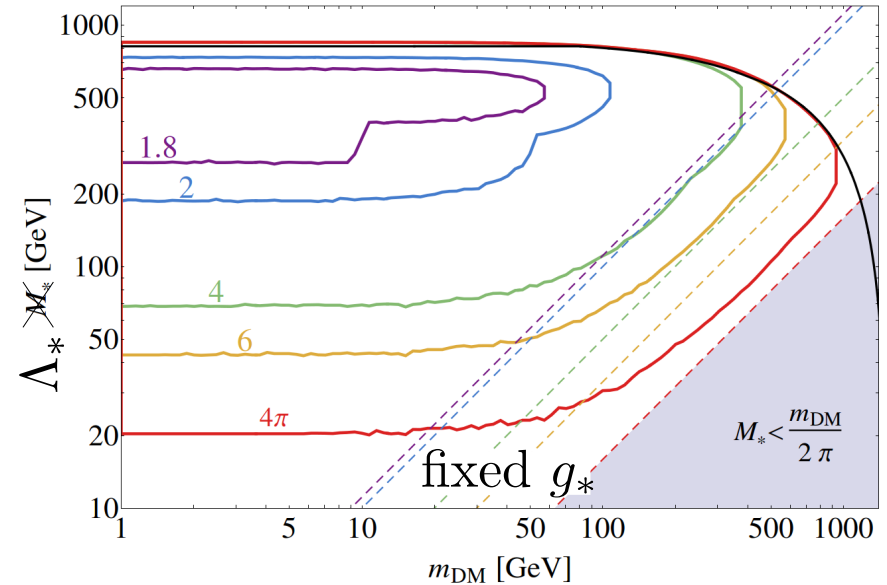
Racco, Wulzer, Zwirner, 1502.04701, JHEP



$$E_{\text{cm}}^{\text{min}} = p_T^{\text{jet}} + \sqrt{(p_T^{\text{jet}})^2 + m_\chi^2}$$

$$\Rightarrow m_\chi^{\text{max}} = \frac{\Lambda_{\text{cut}}}{2} \sqrt{1 - 2 \frac{p_T^{\text{jet}}}{\Lambda_{\text{cut}}}}$$

- Sharp cut at maximal m_χ
- Better for lower p_T signal regions (especially for low Λ_{cut})



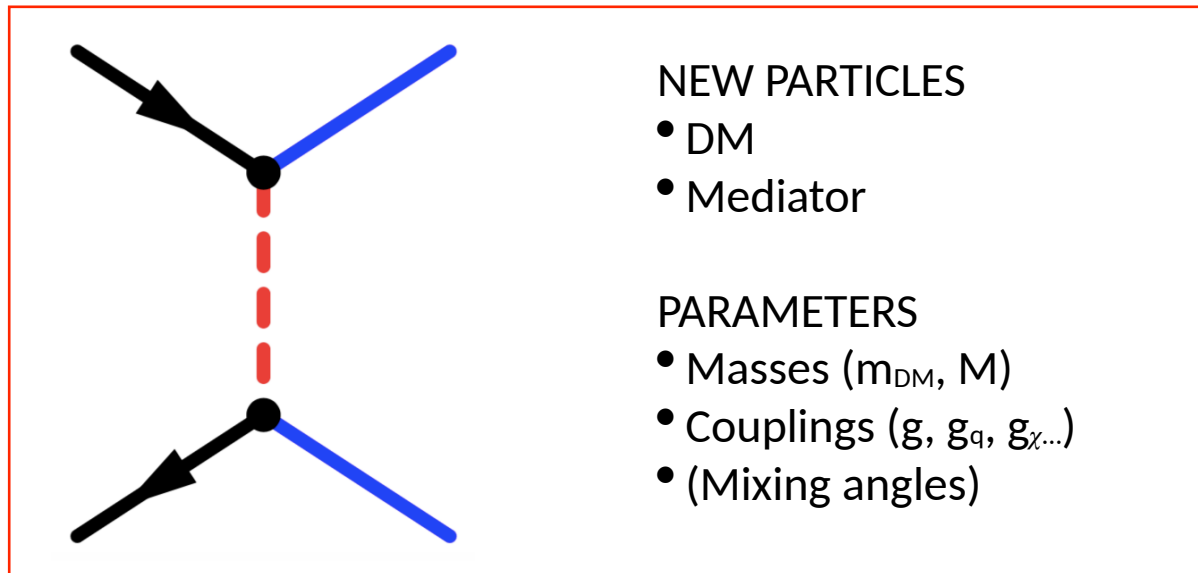
$$\Lambda_{\text{cut}} = g_* \Lambda_*$$

No sensitivity for low Λ_{cut} due to the low Λ_{cut} (for fixed g_*)

Beyond EFT: simplified models

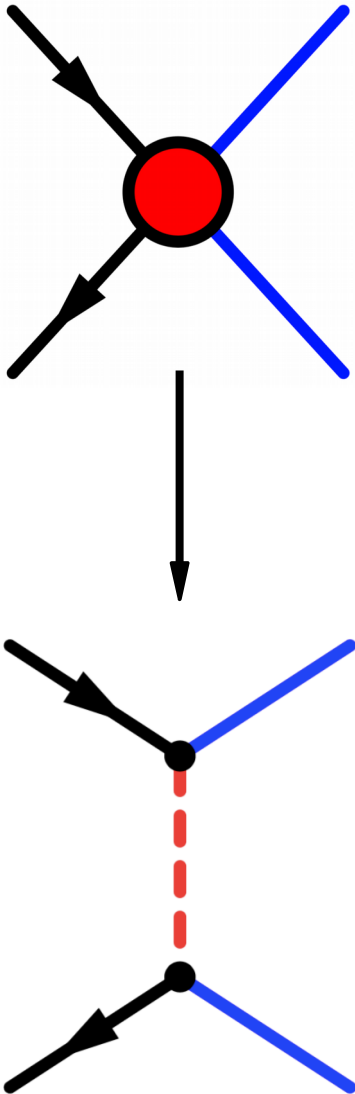
Simplified Models

Beyond EFT: consider a set of simple toy models



Implementation in LHC searches for DM still in progress (DM@LHC working group)

Simplified Models



Can grasp the most relevant physical features of a full theory including DM



Theoretically consistent



Richer phenomenology: other channels and searches complementary to mono-X



More parameters (couplings) → higher dimensional space to constrain

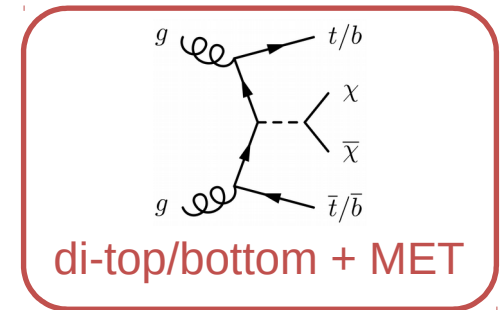
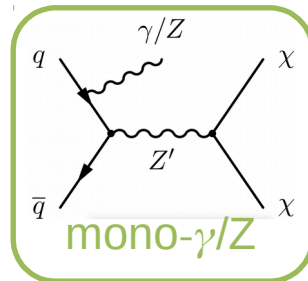
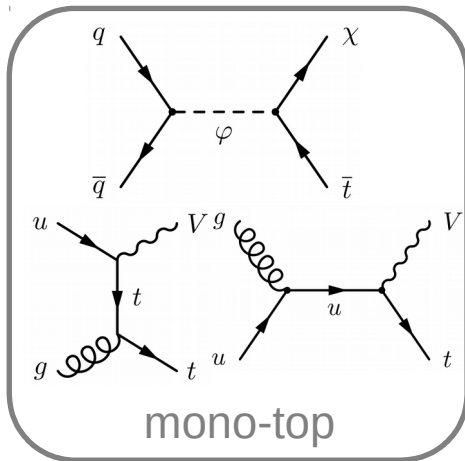
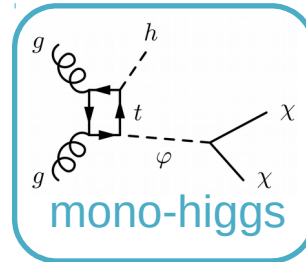
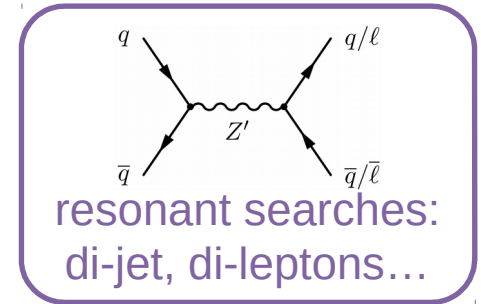
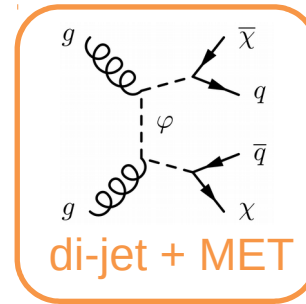
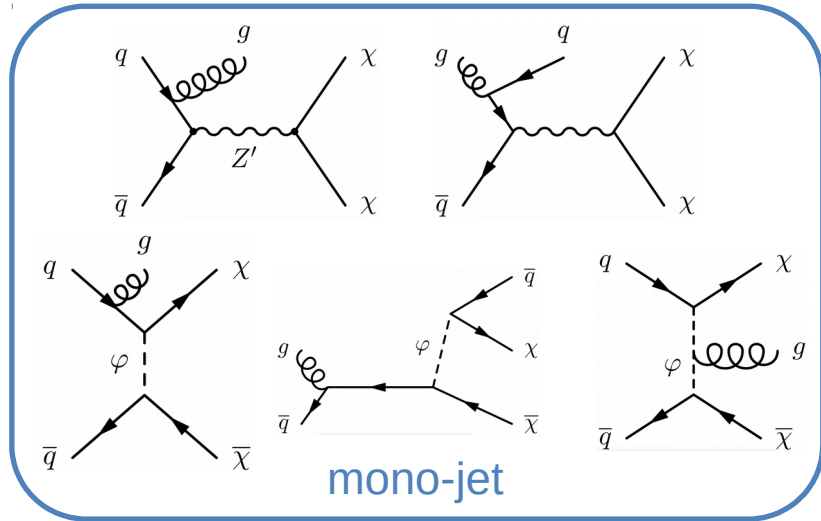


How to present constraints?



Not suitable for strongly interacting dark sectors

LHC results on simplified models



Simplified models vs. EFT

Simplified models and effective operators are complementary

1) No 1-to-1 correspondence between EFT and simp. Mods.

$$\mathcal{L}_A = \mathcal{L}_{\text{SM}} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + \frac{1}{2} m_{Z'}^2 Z'_\mu Z'^\mu + \frac{1}{2} \bar{\chi} (i \partial \cdot \gamma - m_\chi) \chi + Z'_\mu \left(g_q \sum_q \bar{q} \gamma^\mu \gamma^5 q + g_\chi \bar{\chi} \gamma^\mu \gamma^5 \chi \right)$$

$$\mathcal{L}_A^{\text{EFT}} = - \frac{g_q g_\chi}{m_{Z'}^2} \bar{\chi} \gamma_\mu \gamma^5 \chi \sum_q (\bar{q} \gamma^\mu \gamma^5 q)$$

$$\mathcal{L}_B = \mathcal{L}_{\text{SM}} + \mathcal{L}_\chi + \mathcal{L}_{\tilde{q}} + \mathcal{L}_{\text{int}}^B,$$

$$\mathcal{L}_{\tilde{q}} = \sum_{i=1}^3 \left[(\partial^\mu \tilde{u}_{iL})^\dagger (\partial_\mu \tilde{u}_{iL}) + (\partial^\mu \tilde{d}_{iL})^\dagger (\partial_\mu \tilde{d}_{iL}) + (\partial^\mu \tilde{u}_{iR})^\dagger (\partial_\mu \tilde{u}_{iR}) + (\partial^\mu \tilde{d}_{iR})^\dagger (\partial_\mu \tilde{d}_{iR}) \right. \\ \left. = - \tilde{m}^2 \left(\tilde{u}_{iL}^\dagger \tilde{u}_{iL} + \tilde{d}_{iL}^\dagger \tilde{d}_{iL} + \tilde{u}_{iR}^\dagger \tilde{u}_{iR} + \tilde{d}_{iR}^\dagger \tilde{d}_{iR} \right) \right] + \dots,$$

$$\mathcal{L}_{\text{int}}^B = - g_\chi \left[\sum_{i=1}^3 \left(\tilde{u}_{iL} \bar{u}_{iL} + \tilde{d}_{iL} \bar{d}_{iL} + \tilde{u}_{iR} \bar{u}_{iR} + \tilde{d}_{iR} \bar{d}_{iR} \right) \chi + \text{h.c.} \right]$$

$$\mathcal{L}_B^{\text{EFT}} = - \frac{g_\chi^2}{4 \tilde{m}^2} (\bar{\chi} \gamma^\mu \gamma^5 \chi) \left[\sum_{i=1}^3 (\bar{u}_i \gamma_\mu \gamma^5 u_i + \bar{d}_i \gamma_\mu \gamma^5 d_i) \right]$$

Simplified models vs. EFT

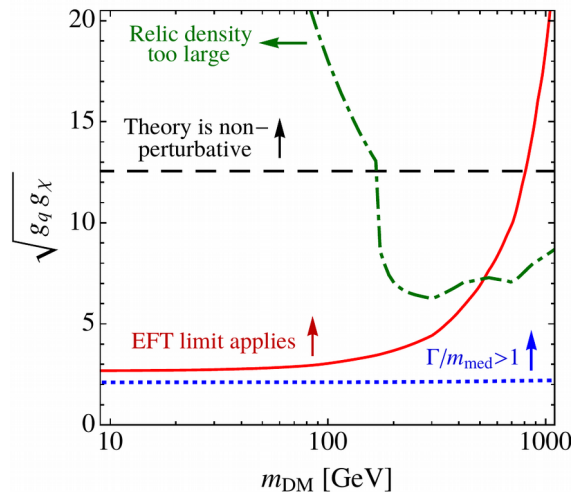
2) EFT limits on simplified models require larger couplings

$$\Lambda = M_{\text{med}} / \sqrt{g_\chi g_q}$$

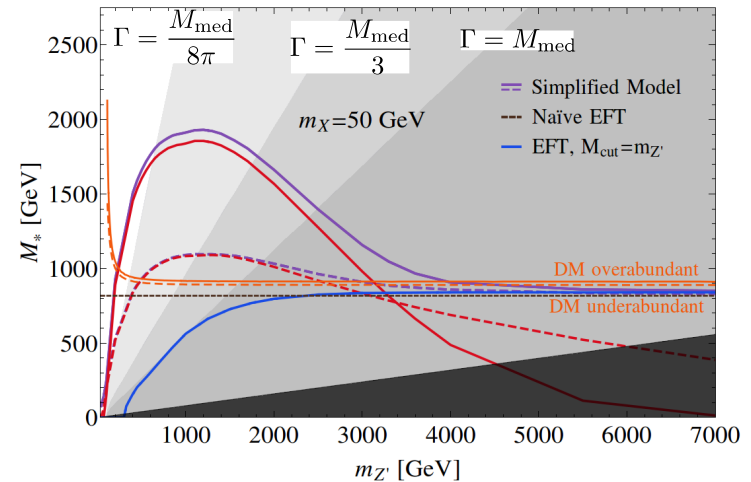
but then the (minimal) width becomes non-perturbative

$$\frac{\Gamma}{M_{\text{med}}} = \frac{1}{12\pi} \sum_f n_c^f g_f^2 \left(1 - \frac{4m_f^2}{M_{\text{med}}^2} \right)^{3/2}$$

Buchmueller, Dolan, McCabe, 1308.6799, JHEP



Racco, Wulzer, Zwirner, 1502.04701, JHEP



Fixed width and large M_{med} gives the correct EFT limit but it's unphysical from the simplified model point of view

Simplified models vs. EFT

Simplified models and effective operators are different tools.
Both are useful, both should be used.

Going from simplified models to EFTs is not as simple as sending Λ to infinity.

In turn, each EFT can have multiple UV completions in terms of simplified models

Some literature

- Busoni, De Simone, Gramling, Jacques, Morgante, Riotto: 1307.2253 (Phys. Lett. B), 1402.1275 (JCAP), 1405.3101 (JCAP)
- Berlin, Lin, Wang: 1402.7074 (JHEP)
- Racco, Wulzer, Zwirner: 1502.0471 (JHEP)
- Buchmuller, Dolan, McCabe: 1308.6799 (JHEP)
comparison of EFT vs. simp. mods.
- Shoemaker, Vecchi: 1112.5457, PRD & Endo, Yamamoto: 1403.6610 (JHEP)
perturbative unitarity constraints
- Bell, Busoni, Kobakhidze, Long, Schmidt: 1602.02722 (JHEP)
unitarization with K-matrix formalism
- Bruggisser, Riva, Urbano: 1607.02474 SciPost Phys., 1607.02475 (JHEP)
EFT for strongly interacting dark sectors
- Alanne, Goertz: 1712.07626
mixed approach EFT + mediator
- White papers: 1409.2893, 1409.4075, 1506.03116 (Phys. Dark Universe)
contain a summary of the discussion about EFTs and simp. mods.
- ATLAS/CMS DM Forum \longrightarrow DM@LHC working group: 1507.00966 (Phys. Dark Univ.)
"state-of-the-art" for EFT in LHC DM searches

Conclusions

Conclusions

- ❖ Effective operators are a simple and useful tool for DM searches.
- ❖ They are the most “universal” tool we have
- ❖ Truncations/rescaling techniques are needed to obtain reliable bounds
- ❖ Simplified models are complementary and can be constrained with a larger variety of searches, but at the price of an higher model dependence

KEEP SEARCHING!

