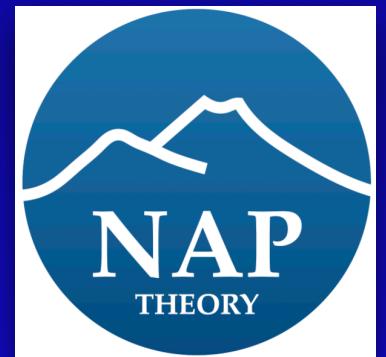


# *Dark Matter in the Milky Way*

*Fabio Iocco*

*Università Federico II, NAPOLI*



# What is the actual distribution of DM in the Milky Way?



And most notably in the proximity of the Sun?

And in the Galactic Center, too? Please bear with me until the end.

# *Dark Matter in the Milky Way*

**FROM THE SKIES TO THE UNDERGROUND,**

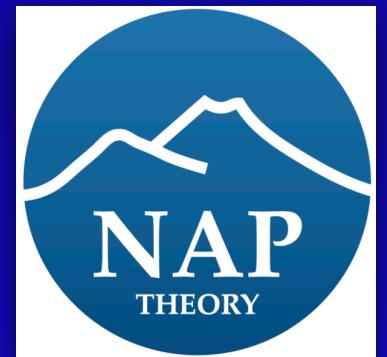
**HOW ASTROPHYSICAL UNCERTAINTIES  
AFFECT SYNERGIC SEARCHES FOR DM.**

**CHAPTER ONE: A GALAXY CLOSE, CLOSE BY**

**CHAPTER ONE: A GALAXY CLOSE, CLOSE BY**

*Fabio Iocco*

*Università Federico II, NAPOLI*



# The Milky Way: literature credits



# *The origin of the Milky Way*



[Jacopo Tintoretto, ca 1575. The National Gallery, London]

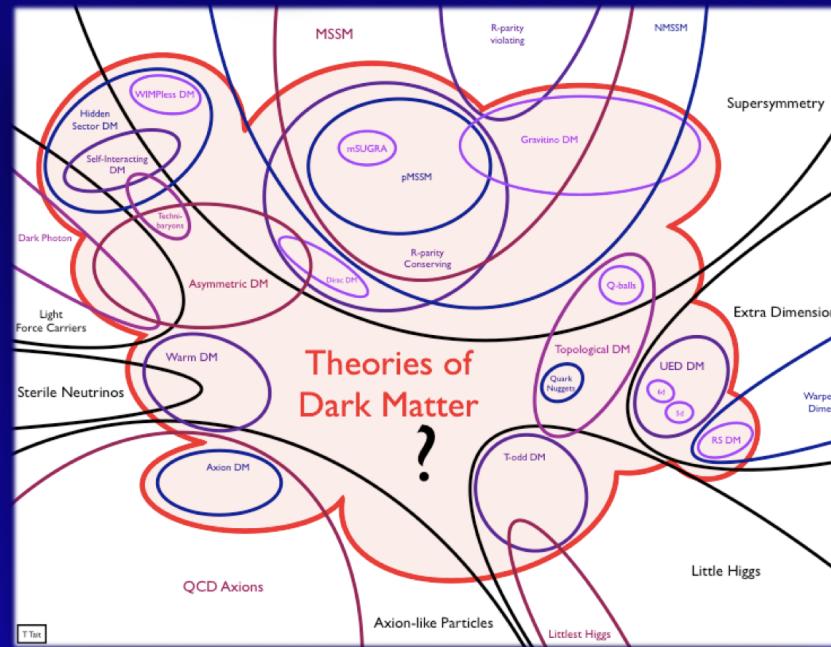
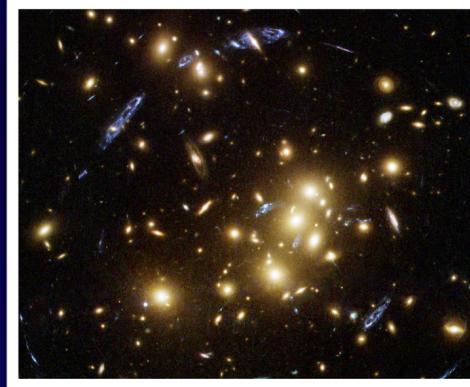
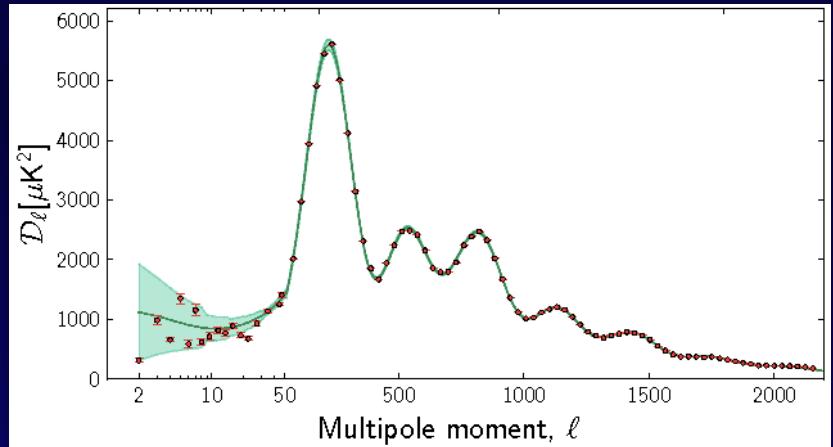
# *The origin of the Milky Way*



[Peter Paul Rubens, ca 1636. Museo del Prado, Madrid]

# Dark Matter

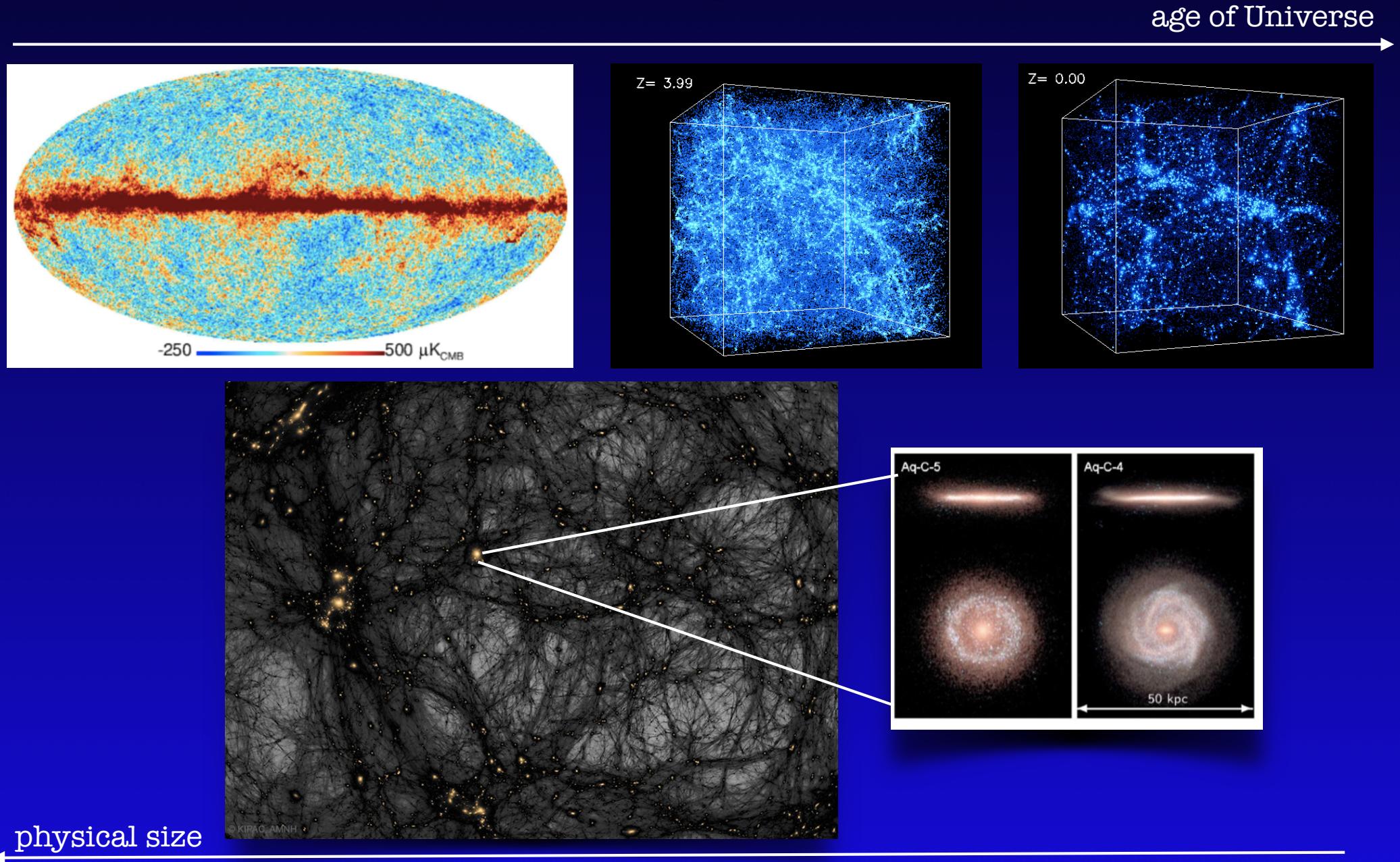
*Evidence over large range of scales*



NATURE STILL UNKNOWN

# *A story of $\Lambda$ CDM*

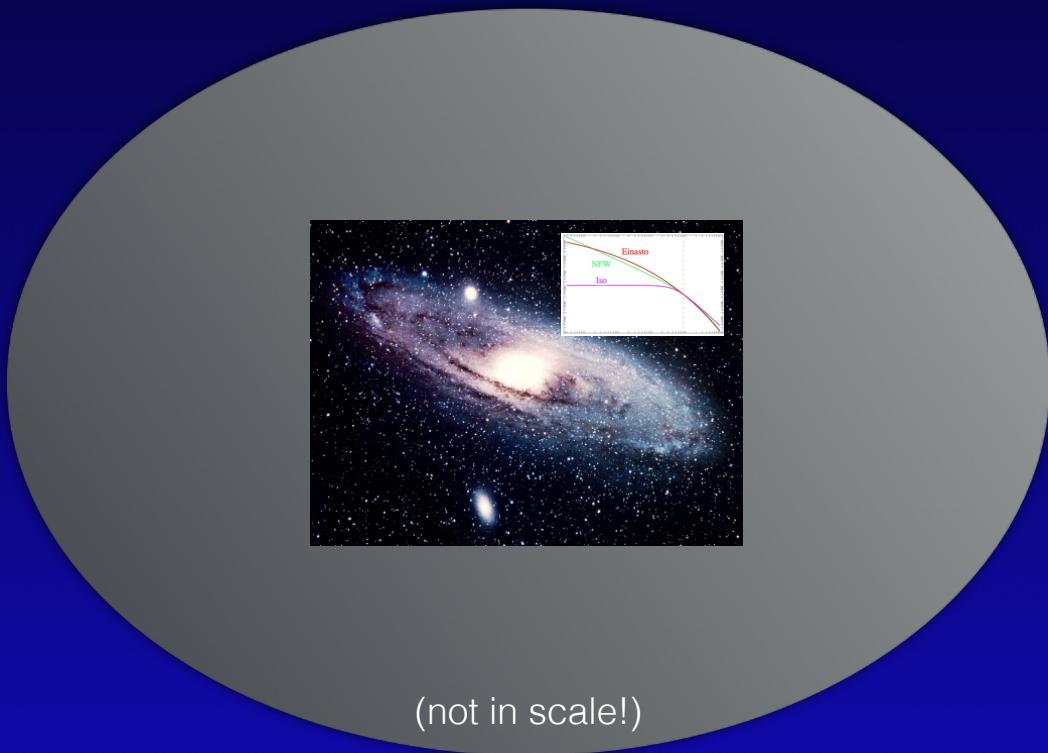
## *I: structure formation*



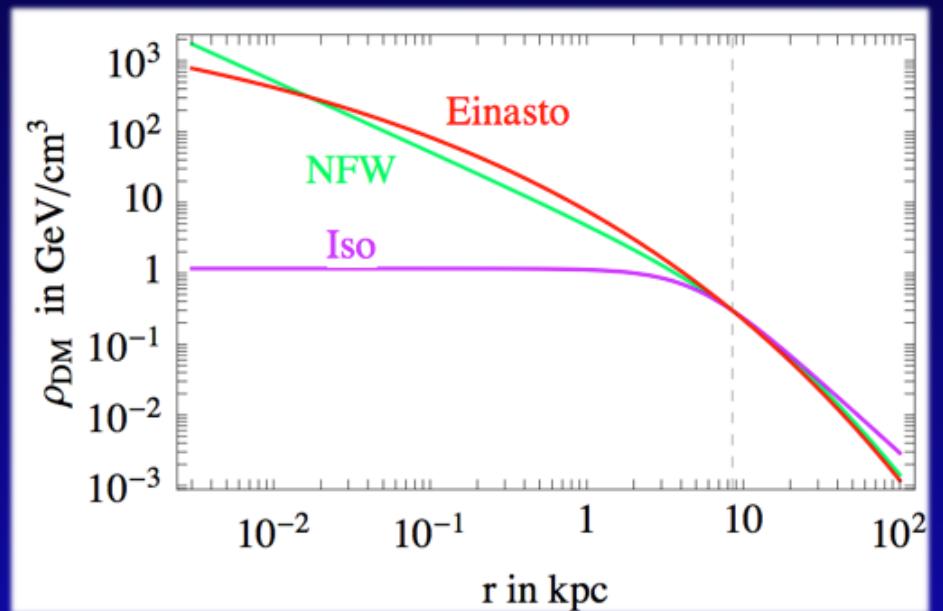
# *A story of $\Lambda$ CDM*

## *II. the single halo*

A “universal” DM profile?



(not in scale!)

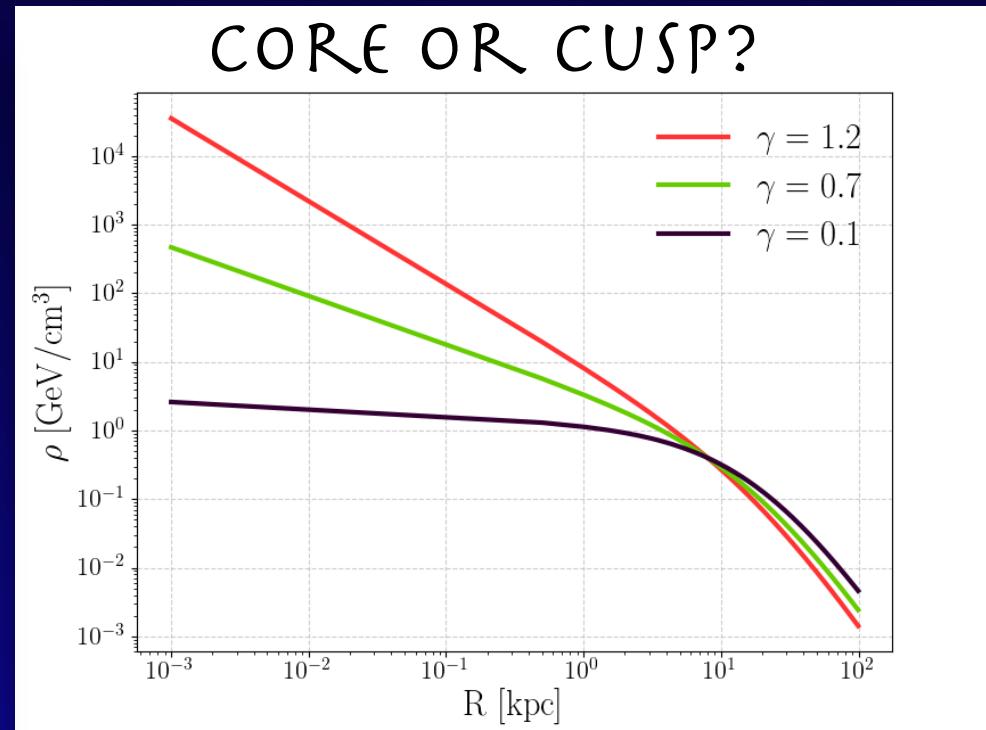
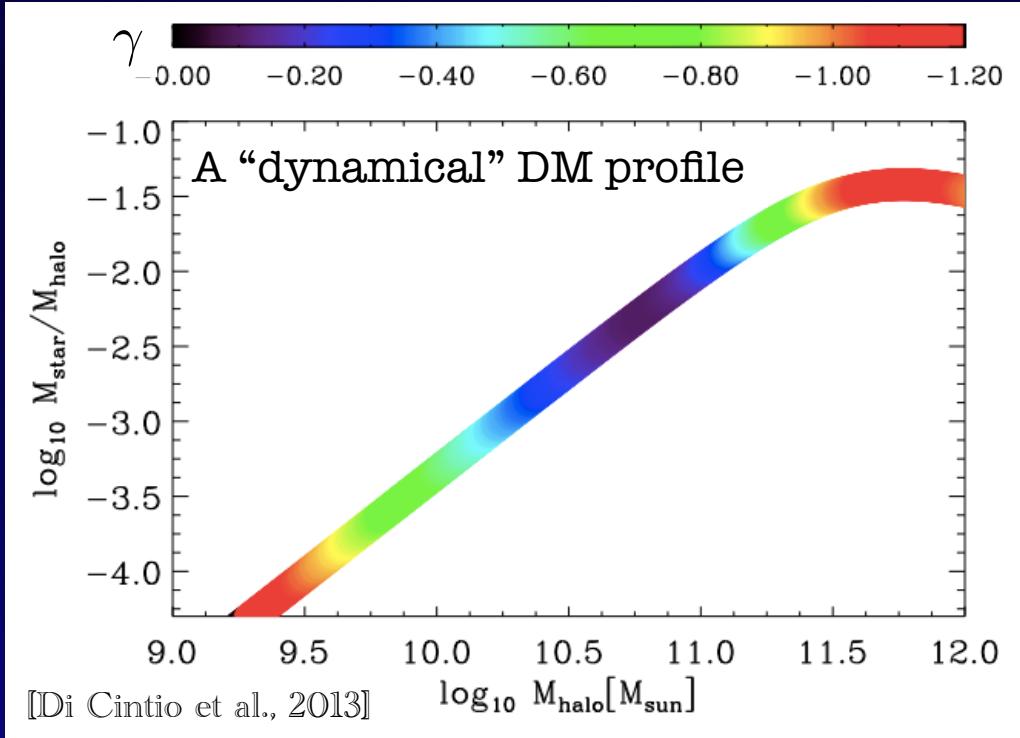


NAVARRO-FRENK-WHITE

$$\rho(R) \propto \frac{R_s}{R} \left(1 + \frac{R}{R_s}\right)^{-2}$$

# *A story of $\Lambda$ CDM*

## *III. the dark matter distribution*



generalized NFW

$$\rho_{DM}(R) \propto \rho_0 \left( \frac{R}{R_s} \right)^{-\gamma} \left( 1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

# What is the actual distribution of DM in the Milky Way?

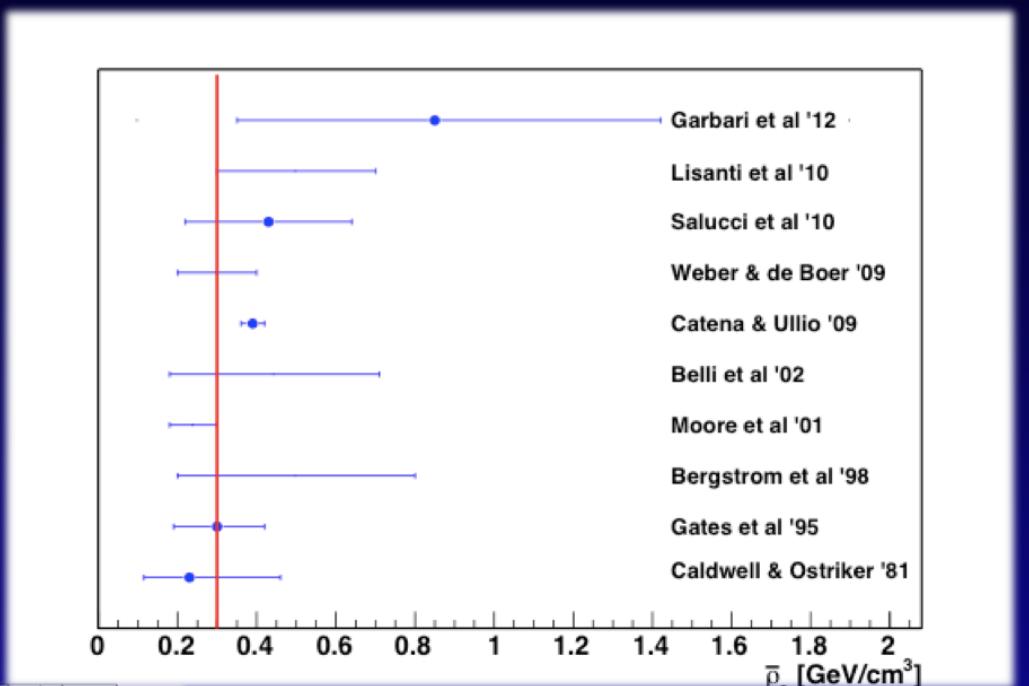
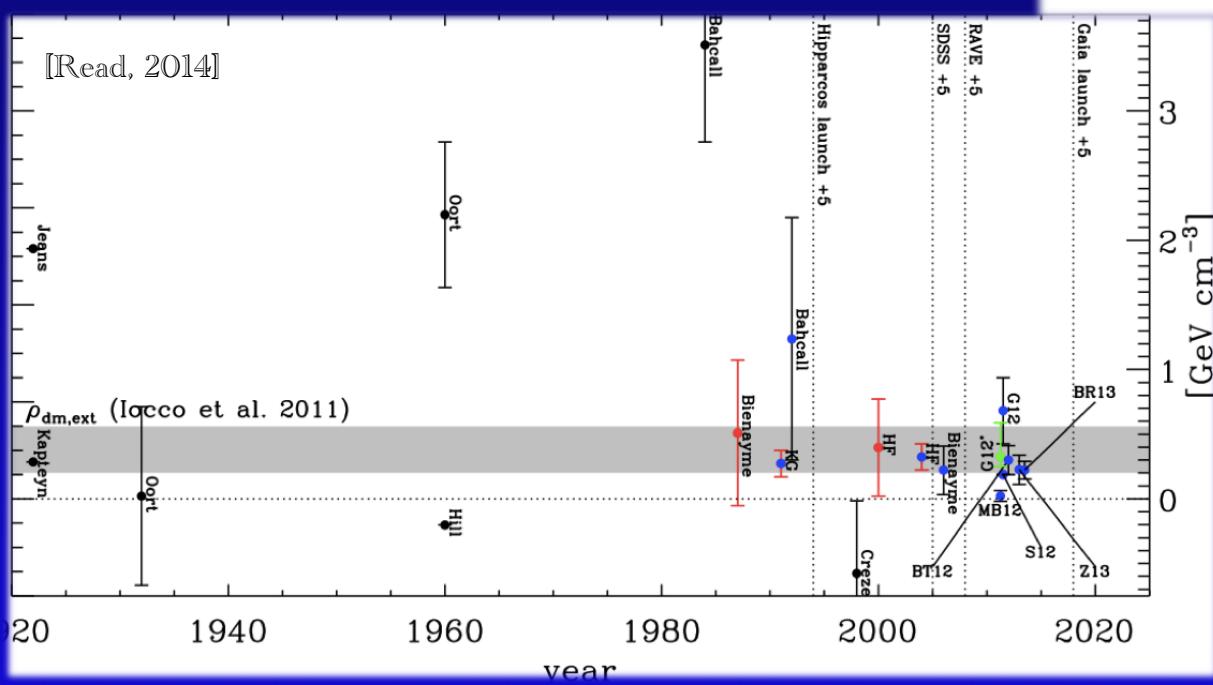


And most notably in the proximity of the Sun?

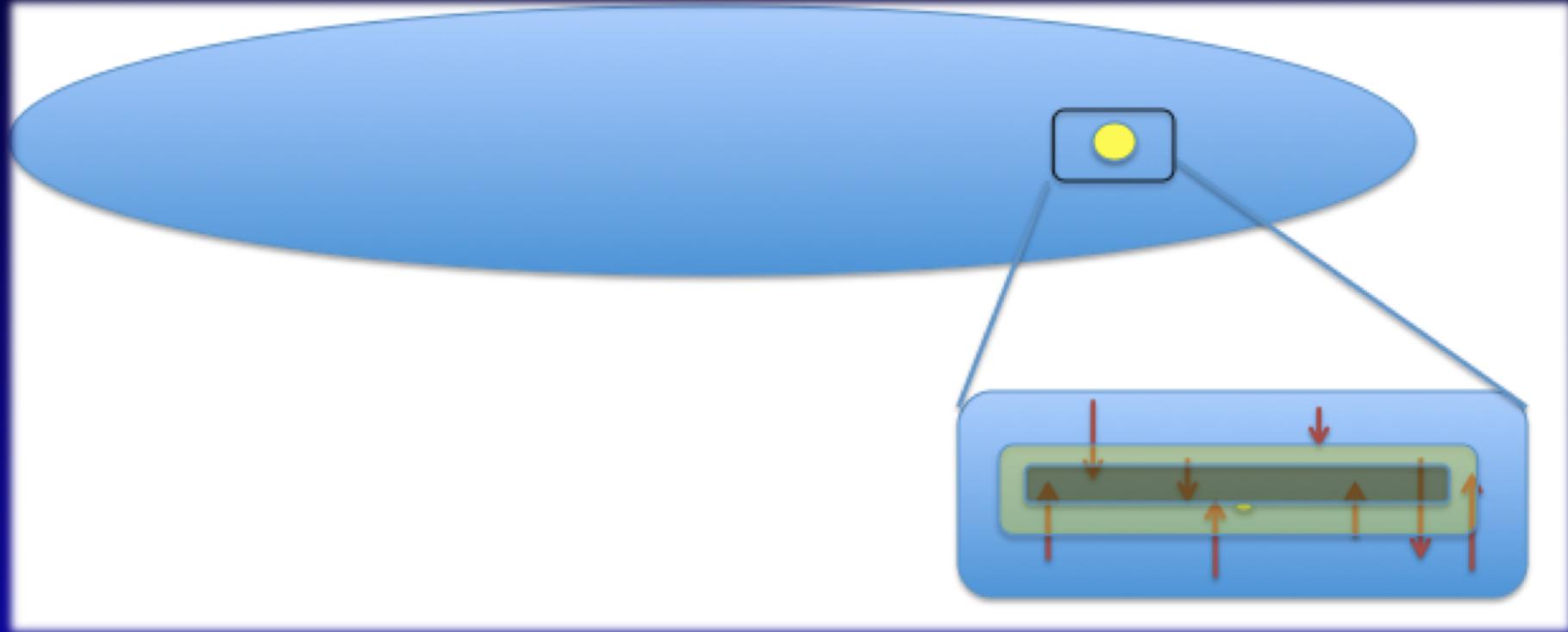
And the Galactic Center, as requested. Please bear with me until the end.

# Empirical determination of local DM density

Determinations of  
local DM density  
are consistent, but noisy



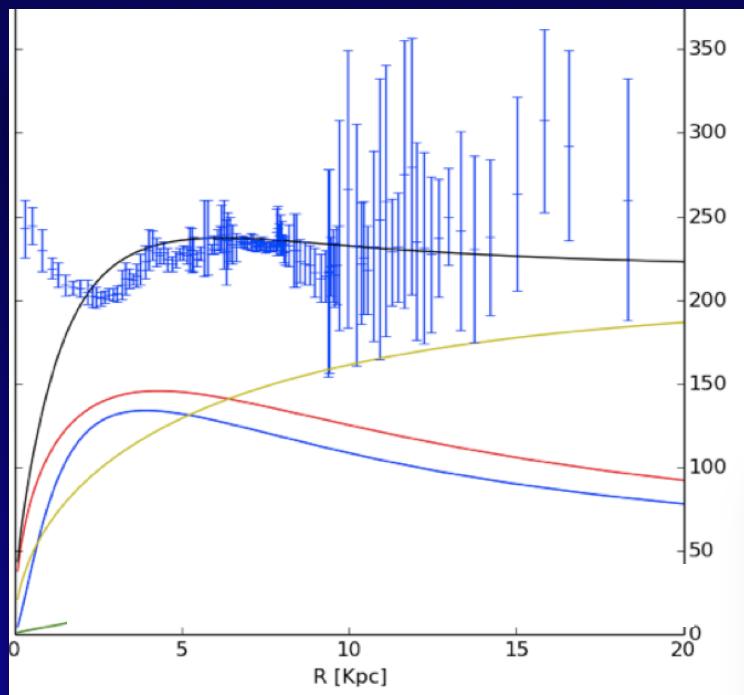
# Local determination of $\rho_0$



Vertical motion of stars in local region  $O(100\text{pc})$  provides total Grav Pot  
Subtracting visible (stellar) contribution  
Obtain (or not) DM without assuming its presence

# Inferring the whole DM distribution (MW's ‘backbone’)

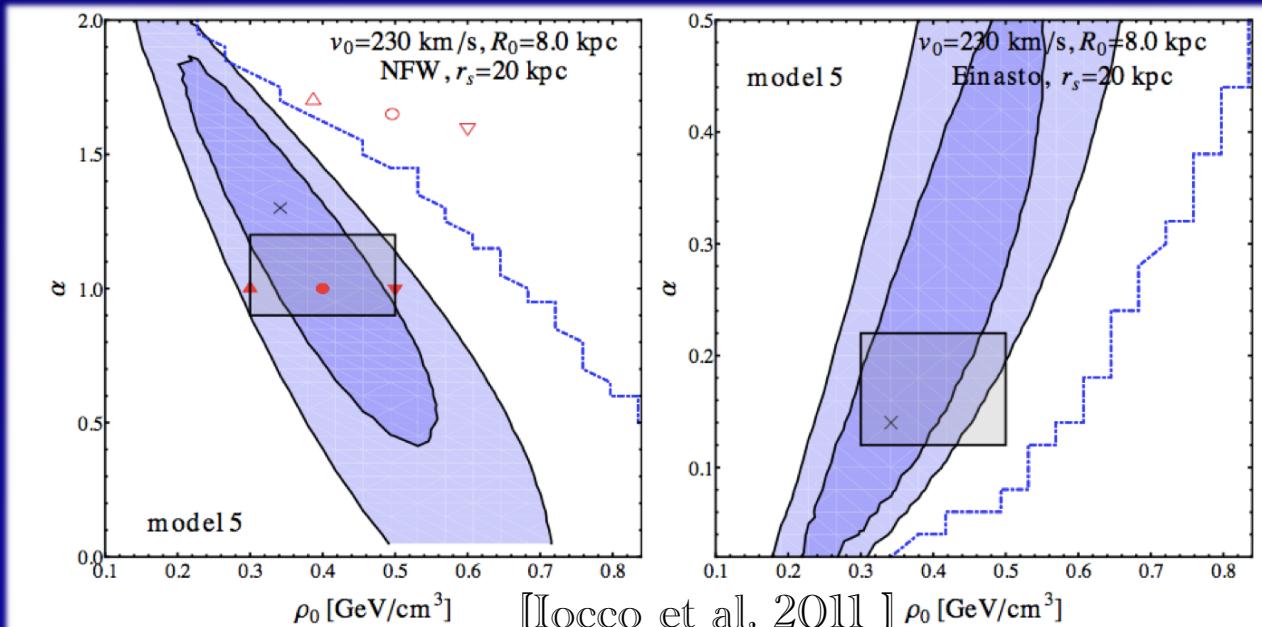
Fitting a pre-assigned shape  
on top of luminous



$$\text{gNFW} \quad \rho_{DM}(R) \propto \rho_0 \left( \frac{R}{R_s} \right)^{-\gamma} \left( 1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

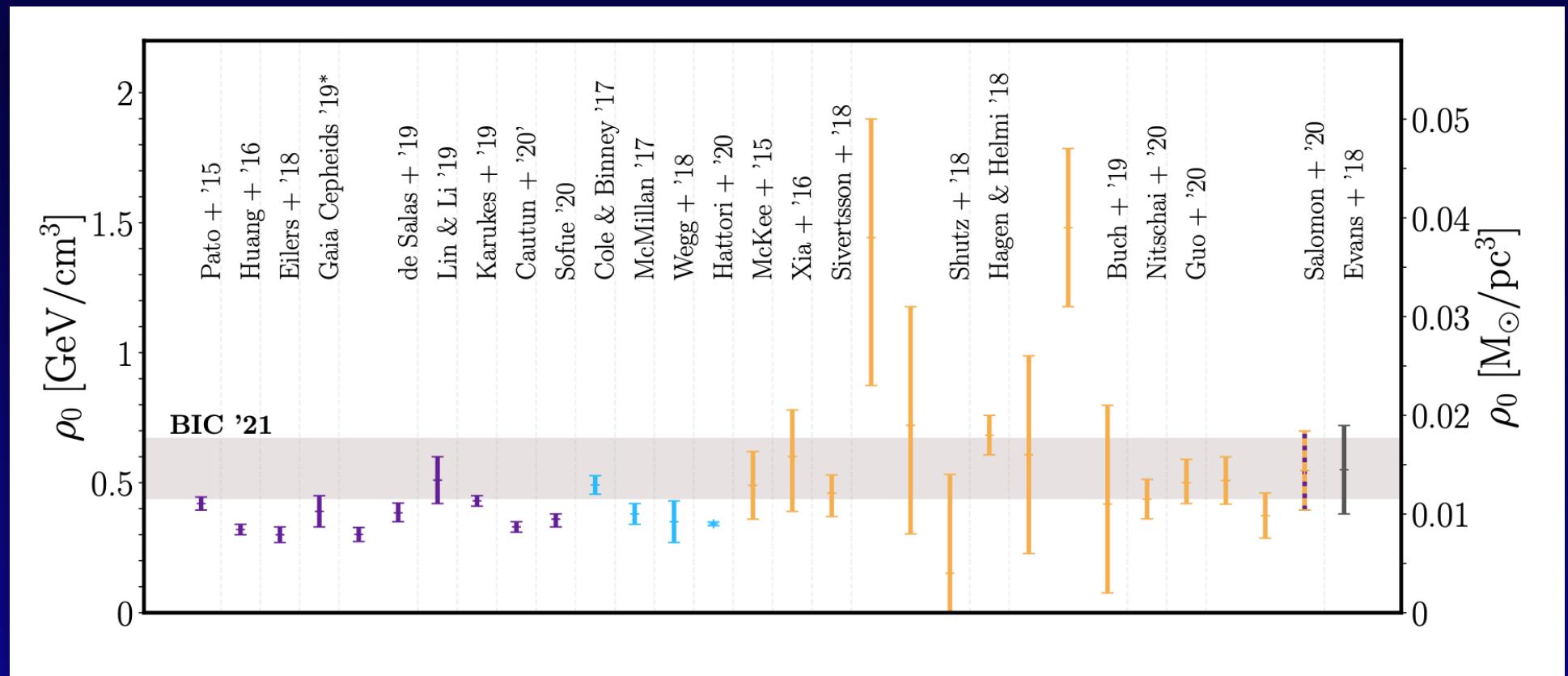
$$\rho_{DM}(R) \propto \rho_0 \exp \left[ -\frac{2}{\gamma} \left( \left( \frac{R}{R_s} \right)^\gamma - 1 \right) \right]$$

Einasto



[many authors, e.g.  
Iocco et al. 2011 ]

# Empirical determination of local DM density: recent determinations

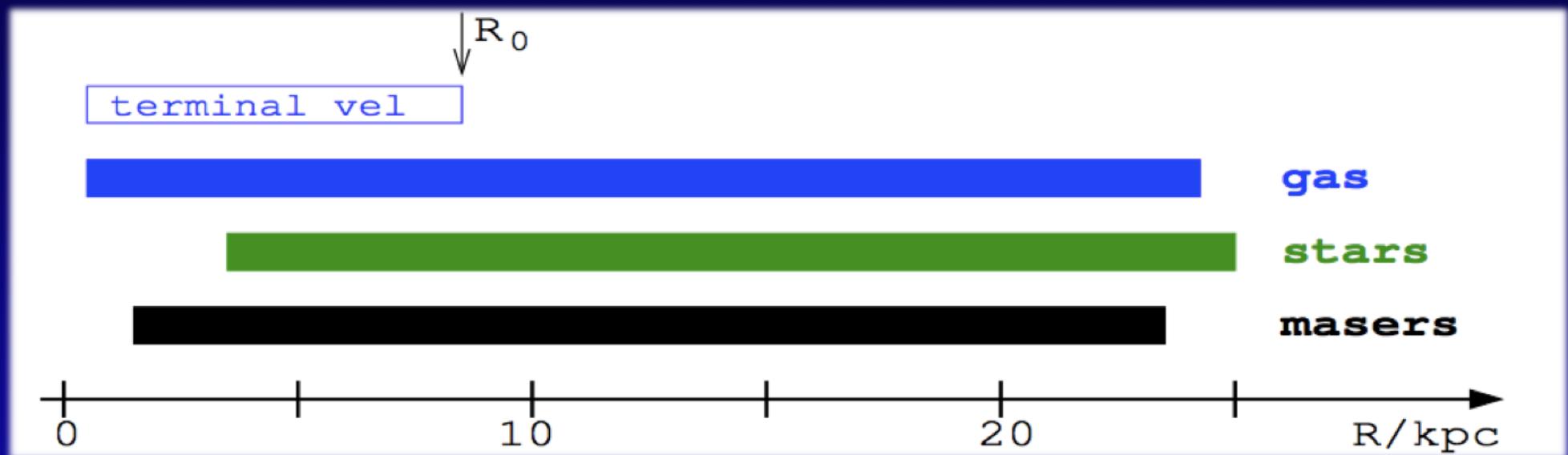


# The case of the Milky Way Recipe for unifying data & formalism.

Ingredients:

- The observed rotation curve
- The “expected” rotation curve
- Some “grano salis”
- Working hypothesis (later on)

# The Milky Way: observed rotation curve the tracers of the gravitational potential



## Doppler shift

1. gas (21cm, H $\alpha$ , CO)
2. stars (H, He, O, ...)
3. masers (H<sub>2</sub>O, CH<sub>3</sub>OH, ...)

## distance

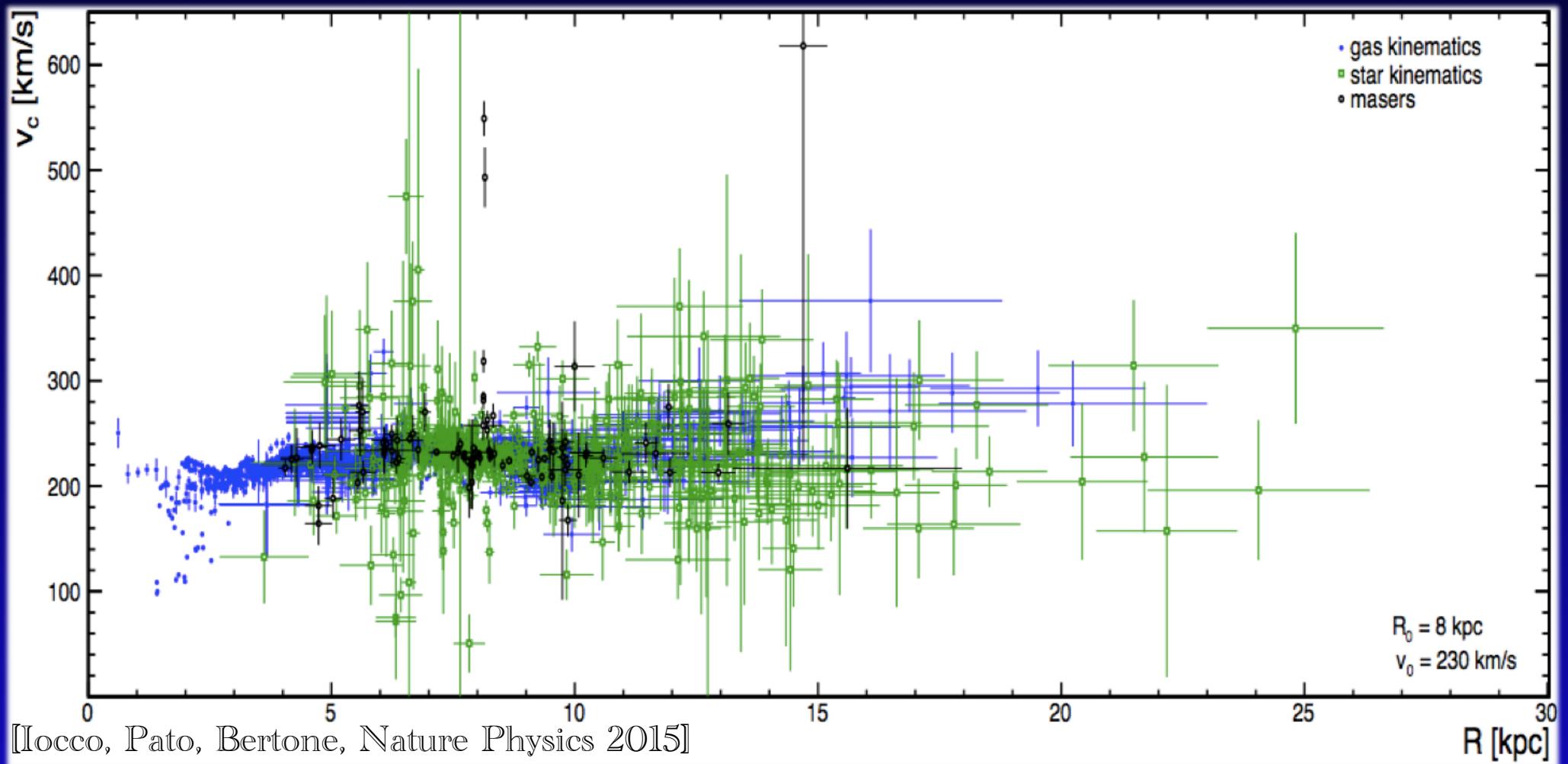
1. terminal velocities (gas)
2. photo-spectroscopy (stars)
3. parallax (masers)

# The Milky Way: observed rotation curve the data: a new compilation

	<b>Object type</b>	<b>R [kpc]</b>	<b>quadrants</b>	<b># objects</b>
<b>gas</b>	HI terminal velocities			
	Fich+ '89	2.1 – 8.0	1,4	149
	Malhotra '95	2.1 – 7.5	1,4	110
	McClure-Griffiths & Dickey '07	2.8 – 7.6	4	701
	HI thickness method			
	Honma & Sofue '97	6.8 – 20.2	–	13
	CO terminal velocities			
	Burton & Gordon '78	1.4 – 7.9	1	284
	Clemens '85	1.9 – 8.0	1	143
	Knapp+ '85	0.6 – 7.8	1	37
<b>stars</b>	Luna+ '06	2.0 – 8.0	4	272
	HII regions			
	Blitz '79	8.7 – 11.0	2,3	3
	Fich+ '89	9.4 – 12.5	3	5
	Turbide & Moffat '93	11.8 – 14.7	3	5
	Brand & Blitz '93	6.2 – 16.5	1,2,3,4	148
	Hou+ '09	3.5 – 15.5	1,2,3,4	274
	giant molecular clouds			
	Hou+ '09	6.0 – 13.7	1,2,3,4	30
	open clusters			
<b>masers</b>	Frinchaboy & Majewski '08	4.6 – 10.7	1,2,3,4	60
	planetary nebulae			
	Durand+ '98	3.6 – 12.6	1,2,3,4	79
	classical cepheids			
	Pont+ '94	5.1 – 14.4	1,2,3,4	245
	Pont+ '97	10.2 – 18.5	2,3,4	32
	carbon stars			
	Demers & Battinelli '07	9.3 – 22.2	1,2,3	55
	Battinelli+ '13	12.1 – 24.8	1,2	35
	masers			
	Reid+ '14	4.0 – 15.6	1,2,3,4	80
	Honma+ '12	7.7 – 9.9	1,2,3,4	11
	Stepanishchev & Bobylev '11	8.3	3	1
	Xu+ '13	7.9	4	1
	Bobylev & Bajkova '13	4.7 – 9.4	1,2,4	7

Conclusions don't change if using  
See Benito Iocco Cuoco 2021

# The Milky Way Rotation Curve as observed



All tracers, optimized for precision between  $R=3-20$  kpc  
For more details on data treatment (as well as inclusion of different datasets) ...

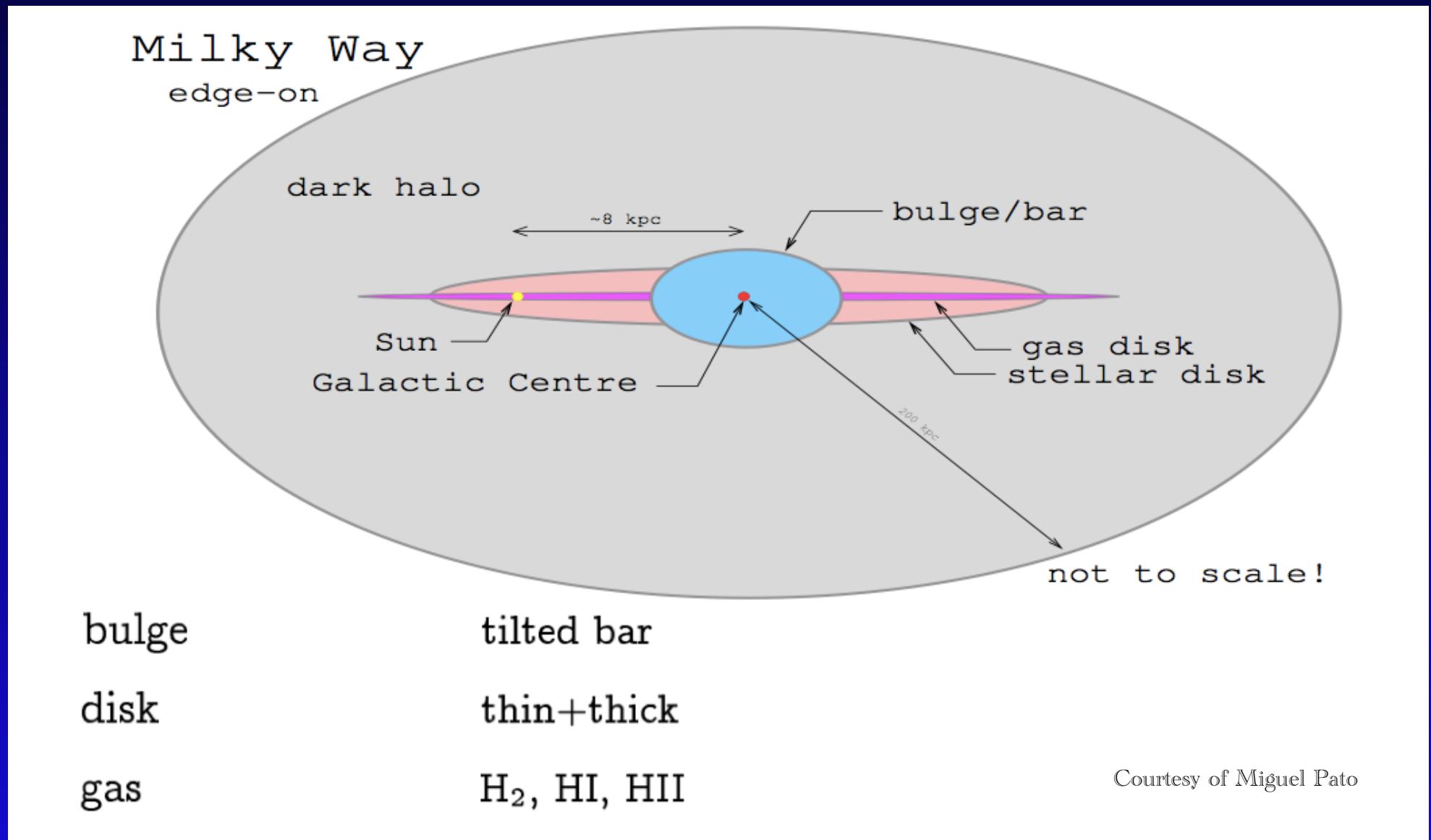
# The Milky Way: ‘expected’ rotation curve from visible (baryon) component

$$\Phi_{\text{baryon}} = \Phi_{\text{bulge}} + \Phi_{\text{disk}} + \Phi_{\text{gas}}$$

$$\rho_i(x, y, z) \rightarrow \phi_i(r, \theta, \varphi) \rightarrow v_{c,i}^2(R) = \sum_{\varphi} R \frac{d\phi_i}{dr}(R, \pi/2, \varphi)$$

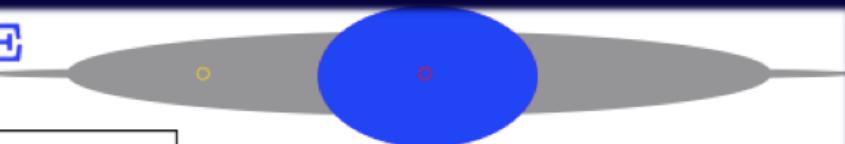
Constructing the curve expected from observed mass profiles

# The Milky Way: expected rotation curve the baryonic components



# The luminous Milky Way: observations of morphology

## 2. BARYONS: STELLAR BULGE



$$\rho_{\text{bulge}} = \rho_0 f(x, y, z)$$

morphology  $f(x, y, z)$

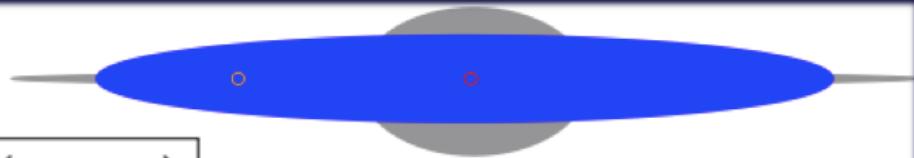
Stanek+ '97 (E2)	$e^{-r}$	0.9:0.4:0.3	24°	optical
Stanek+ '97 (G2)	$e^{-r_s^2/2}$	1.2:0.6:0.4	25°	optical
Zhao '96	$e^{-r_s^2/2} + r_a^{-1.85} e^{-r_a}$	1.5:0.6:0.4	20°	infrared
Bissantz & Gerhard '02	$e^{-r_s^2}/(1+r)^{1.8}$	2.8:0.9:1.1	20°	infrared
Lopez-Corredoira+ '07	Ferrer potential	7.8:1.2:0.2	43°	infrared/optical
Vanhollebeke+ '09	$e^{-r_s^2}/(1+r)^{1.8}$	2.6:1.8:0.8	15°	infrared/optical
Robin+ '12	$\operatorname{sech}^2(-r_s) + e^{-r_s}$	1.5:0.5:0.4	13°	infrared

normalisation  $\rho_0$  and its statistical uncertainties

microlensing optical depth:  $\langle \tau \rangle = 2.17^{+0.47}_{-0.38} \times 10^{-6}$ ,  $(\ell, b) = (1.50^\circ, -2.68^\circ)$   
(MACHO '05)

# The luminous Milky Way: observations of morphology

## 2. BARYONS: STELLAR DISK



$$\rho_{\text{disk}} = \rho_0 f(x, y, z)$$

morphology  $f(x, y, z)$

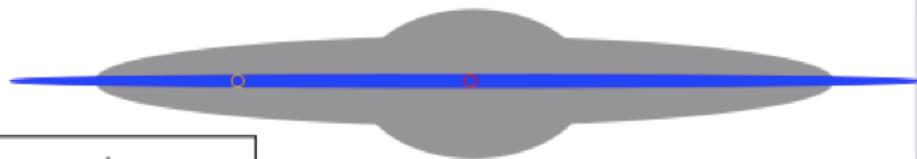
Han & Gould '03	$e^{-R} \operatorname{sech}^2(z)$ $e^{-R- z }$	2.8:0.27 2.8:0.44	thin thick	optical
Calchi-Novati & Mancini '11	$e^{-R- z }$ $e^{-R- z }$	2.8:0.25 4.1:0.75	thin thick	optical
deJong+ '10	$e^{-R- z }$ $e^{-R- z }$ $(R^2 + z^2)^{-2.75/2}$	2.8:0.25 4.1:0.75 1.0:0.88	thin thick halo	optical
Jurić+ '08	$e^{-R- z }$ $e^{-R- z }$ $(R^2 + z^2)^{-2.77/2}$	2.2:0.25 3.3:0.74 1.0:0.64	thin thick halo	optical
Bovy & Rix '13	$e^{-R- z }$	2.2:0.40	single	optical

normalization and its statistical uncertainties

local surface density:  $\Sigma_* = 38 \pm 4 \text{M}_\odot/\text{pc}^2$  [Bovy & Rix '13]

# The luminous Milky Way: observations of morphology

## 2. BARYONS: GAS



$$n_{\text{H}} = 2n_{\text{H}_2} + n_{\text{HI}} + n_{\text{HII}}$$

### morphology

Ferrière '12	$r < 0.01 \text{ kpc}$	$M_{\text{gas}} \sim 7 \times 10^5 \text{ M}_{\odot}$		CO, 21cm, H $\alpha$ , ...
Ferrière+ '07	$r = 0.01 - 2 \text{ kpc}$	CMZ, holed disk CMZ, holed disk warm, hot, very hot	H <sub>2</sub> H I H II	CO 21cm disp. meas.
Ferrière '98	$r = 3 - 20 \text{ kpc}$	molecular ring cold, warm warm, hot	H <sub>2</sub> H I H II	CO 21cm disp. meas., H $\alpha$
Moskalenko+ '02	$r = 3 - 20 \text{ kpc}$	molecular ring	H <sub>2</sub> H I H II	CO 21cm disp. meas.

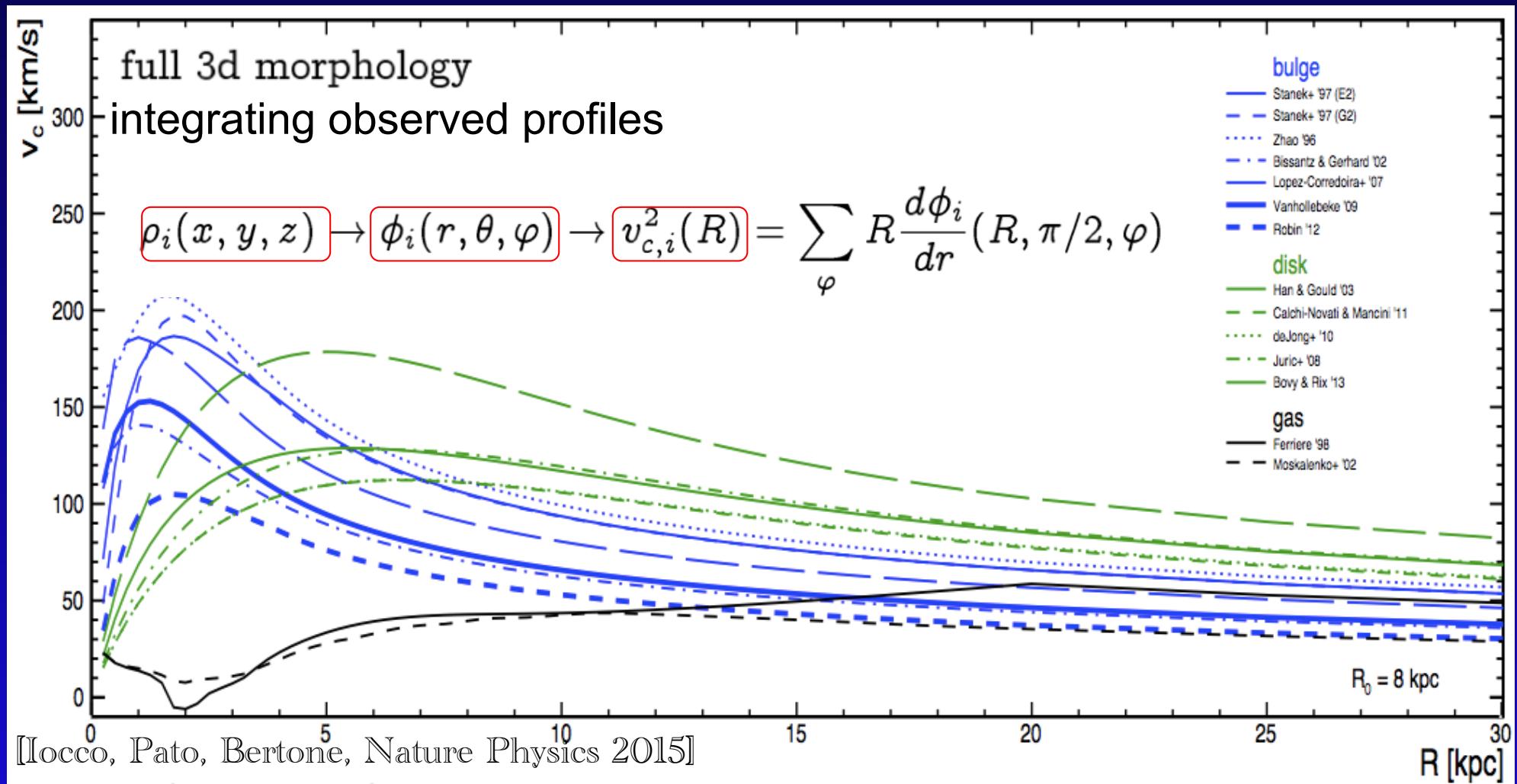
### uncertainties

CO-to-H<sub>2</sub> factor:  $X_{\text{CO}} = 0.25 - 1.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$  for  $r < 2 \text{ kpc}$   
 $X_{\text{CO}} = 0.50 - 3.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$  for  $r > 2 \text{ kpc}$

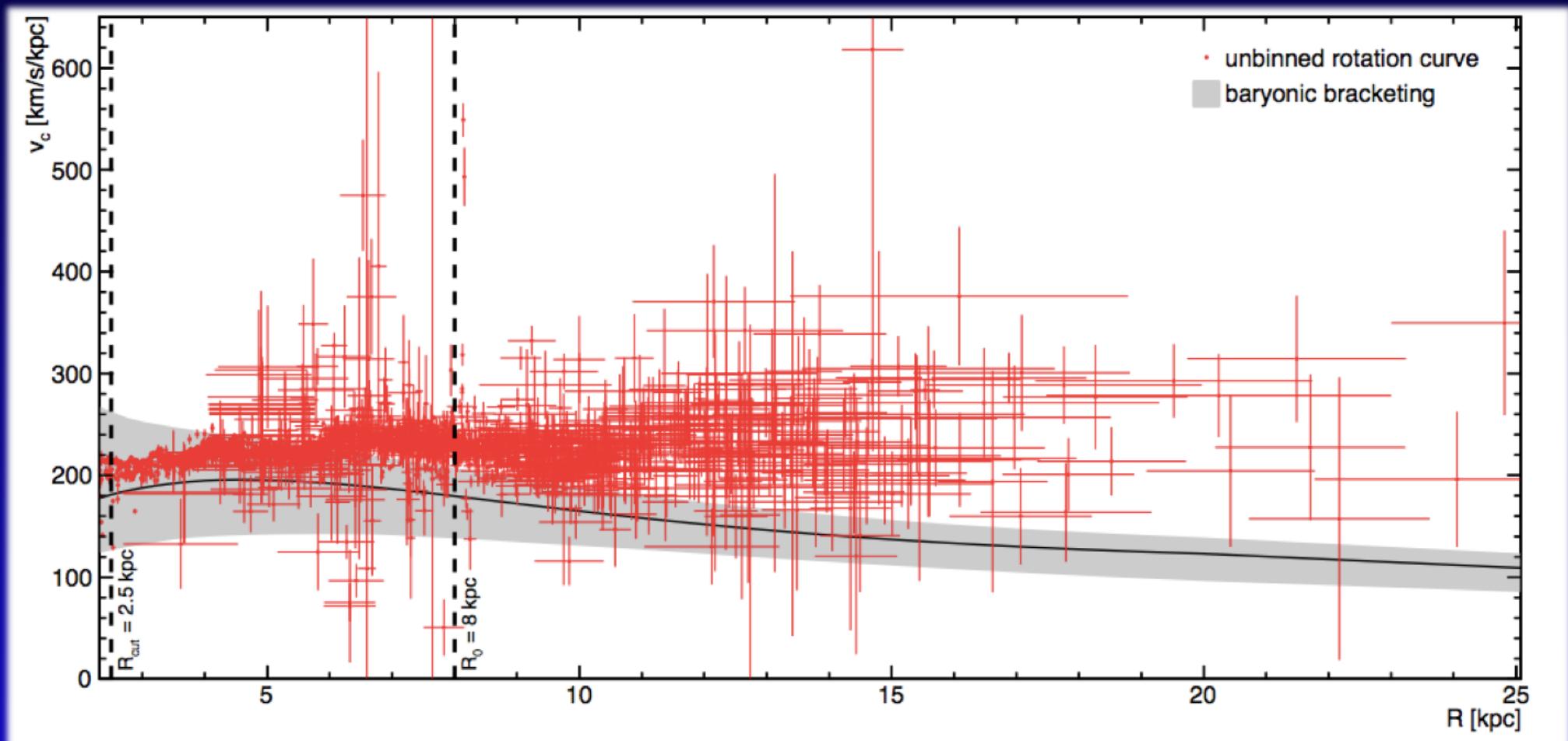
[Ferrière+ '07, Ackermann '12]

# The luminous Milky Way: expected rotation curve

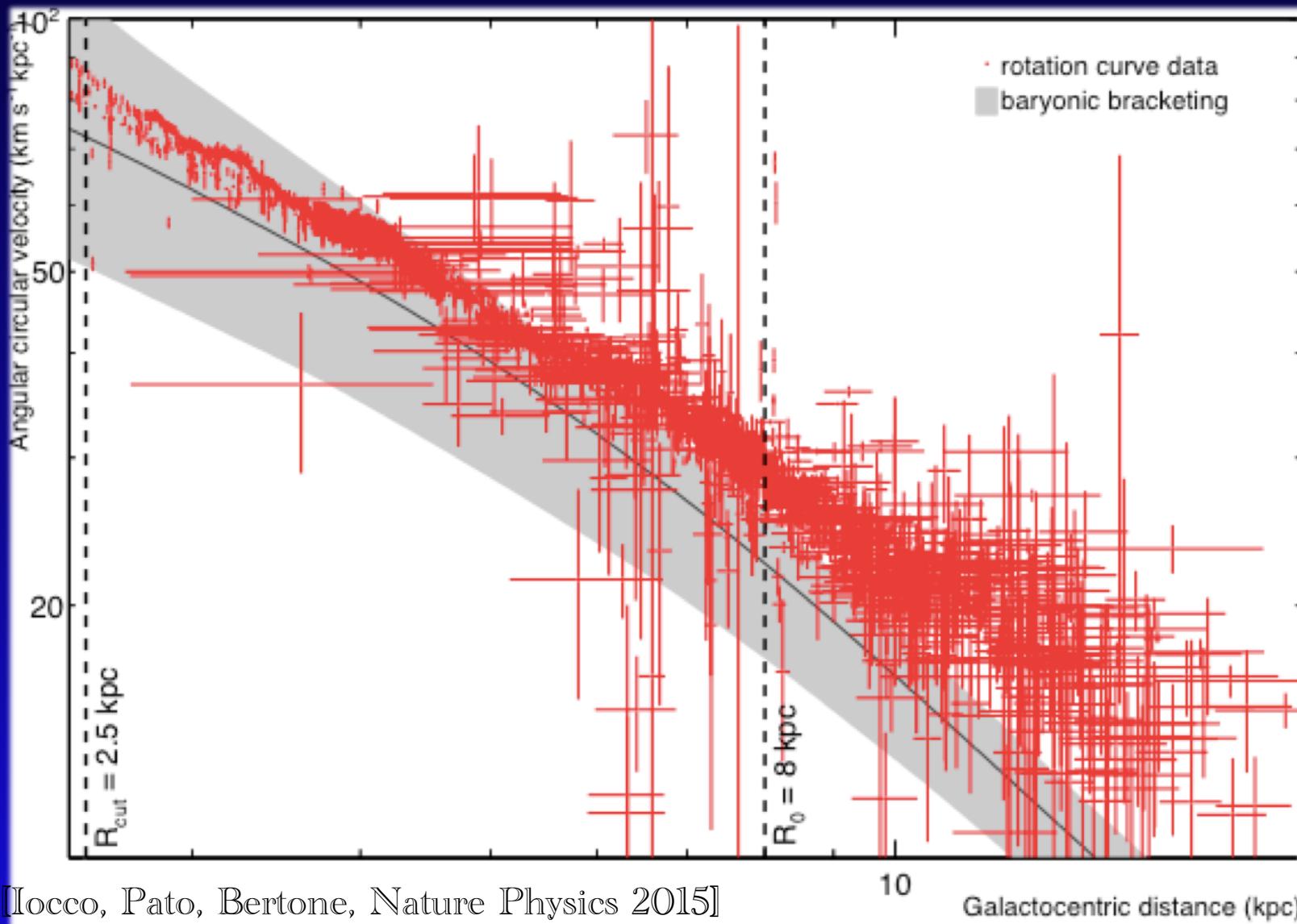
$$\phi_i(r, \theta, \varphi) = -4\pi G \sum_{l,m} \frac{Y_{lm}(\theta, \varphi)}{2l+1} \left[ \frac{1}{r^{l+1}} \int_0^r \rho_{i,lm}(a) a^{l+2} da + r^l \int_r^\infty \rho_{i,lm}(a) a^{1-l} da \right]$$



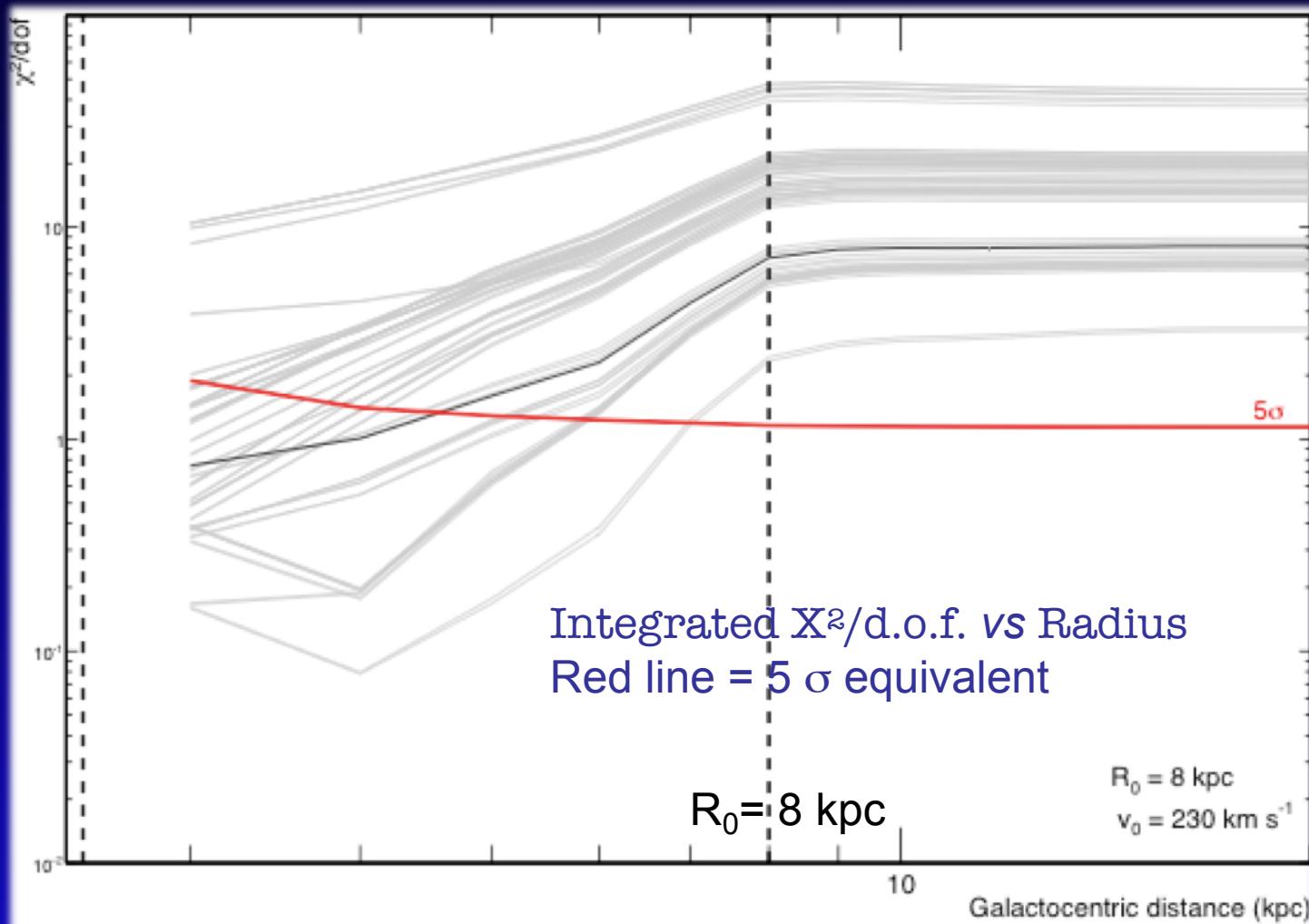
# The Milky Way: testing expectations (with no additional assumptions)



# The Milky Way: testing expectations (with no additional assumption) (and some technical detail))



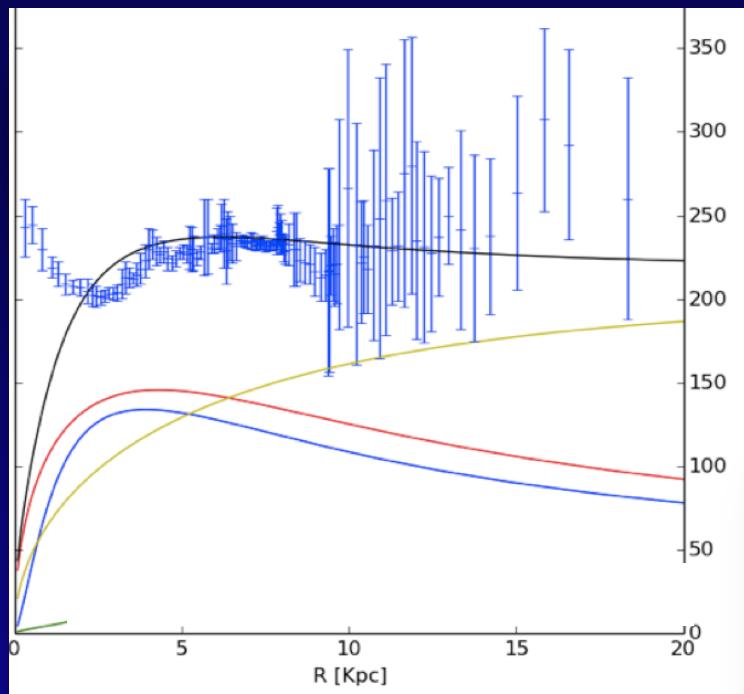
# Do the baryon-only curves fit with the observed RC?



Answer is NO:  
Every single model above  $5\sigma$ , already at  $R < R_0$ !!

# Inferring the DM density structure

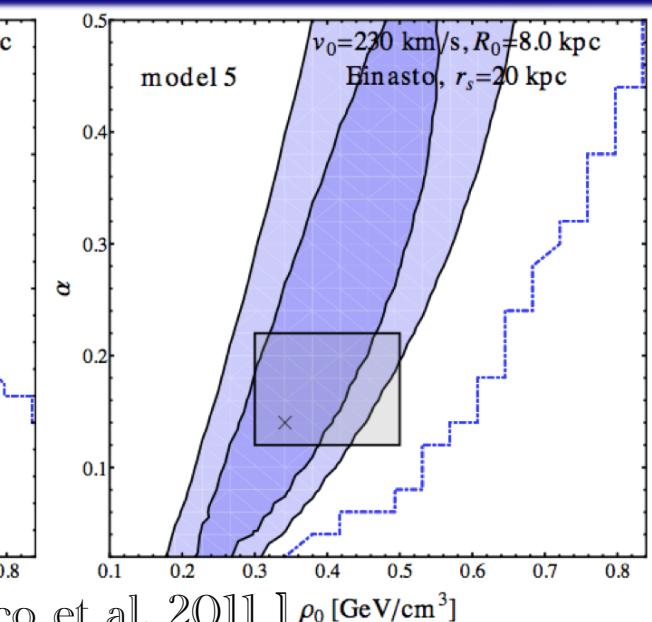
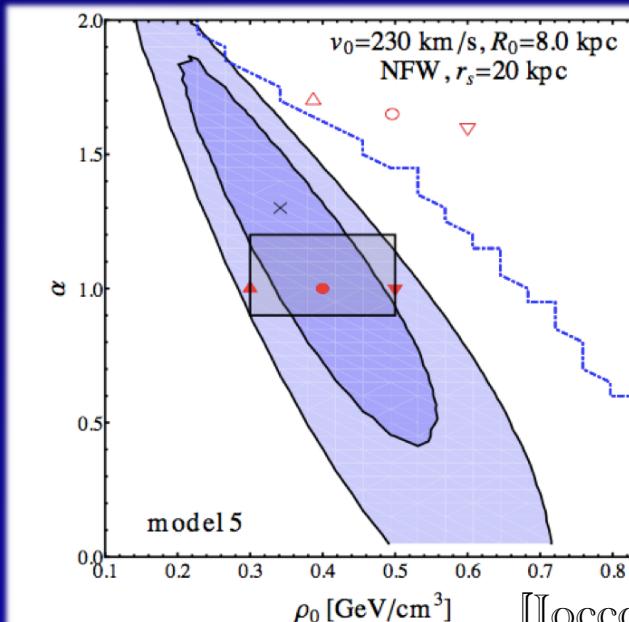
Fitting a pre-assigned shape  
on top of luminous



$$\text{gNFW} \quad \rho_{DM}(R) \propto \rho_0 \left( \frac{R}{R_s} \right)^{-\gamma} \left( 1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

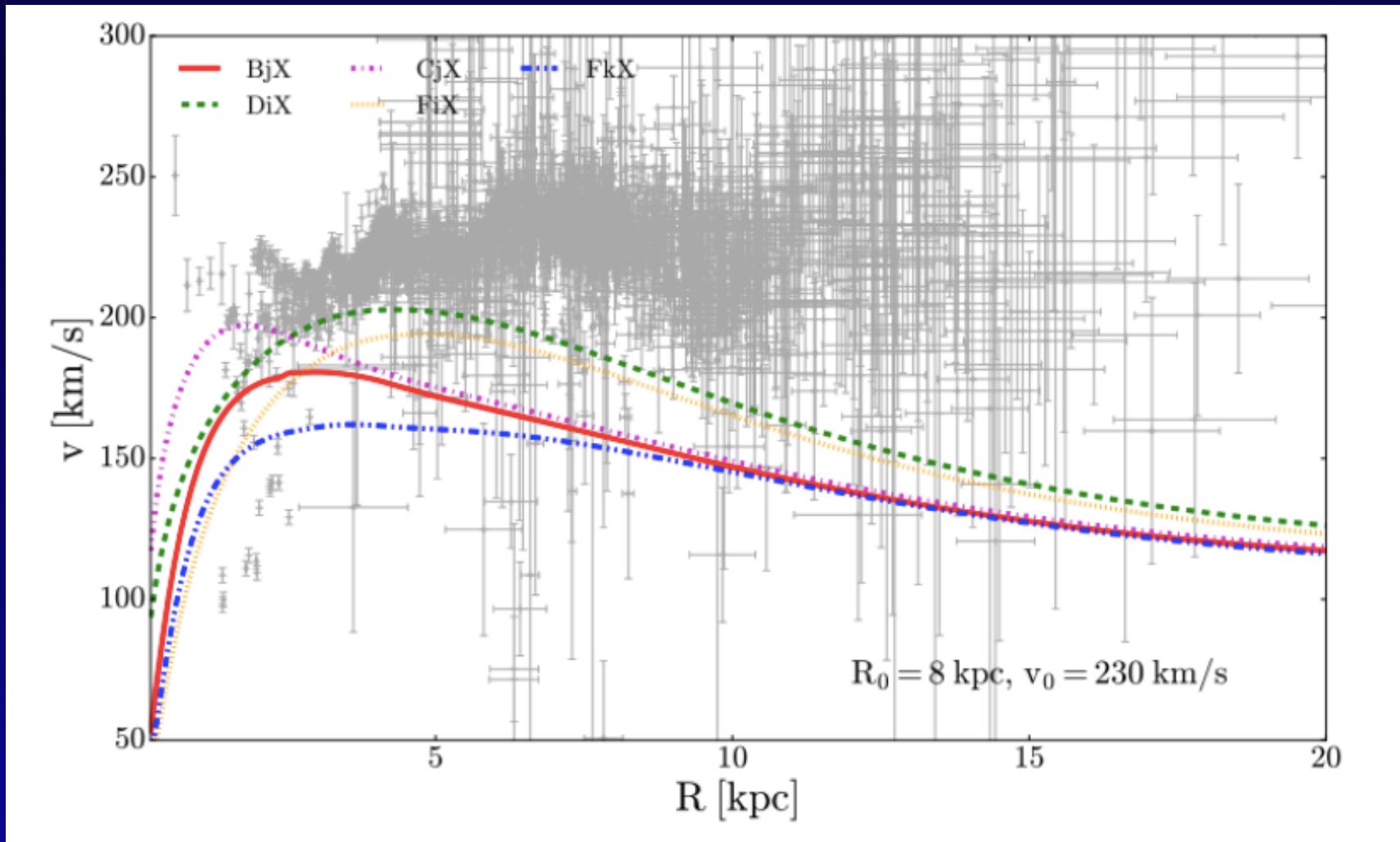
$$\rho_{DM}(R) \propto \rho_0 \exp \left[ -\frac{2}{\gamma} \left( \left( \frac{R}{R_s} \right)^\gamma - 1 \right) \right]$$

Einasto

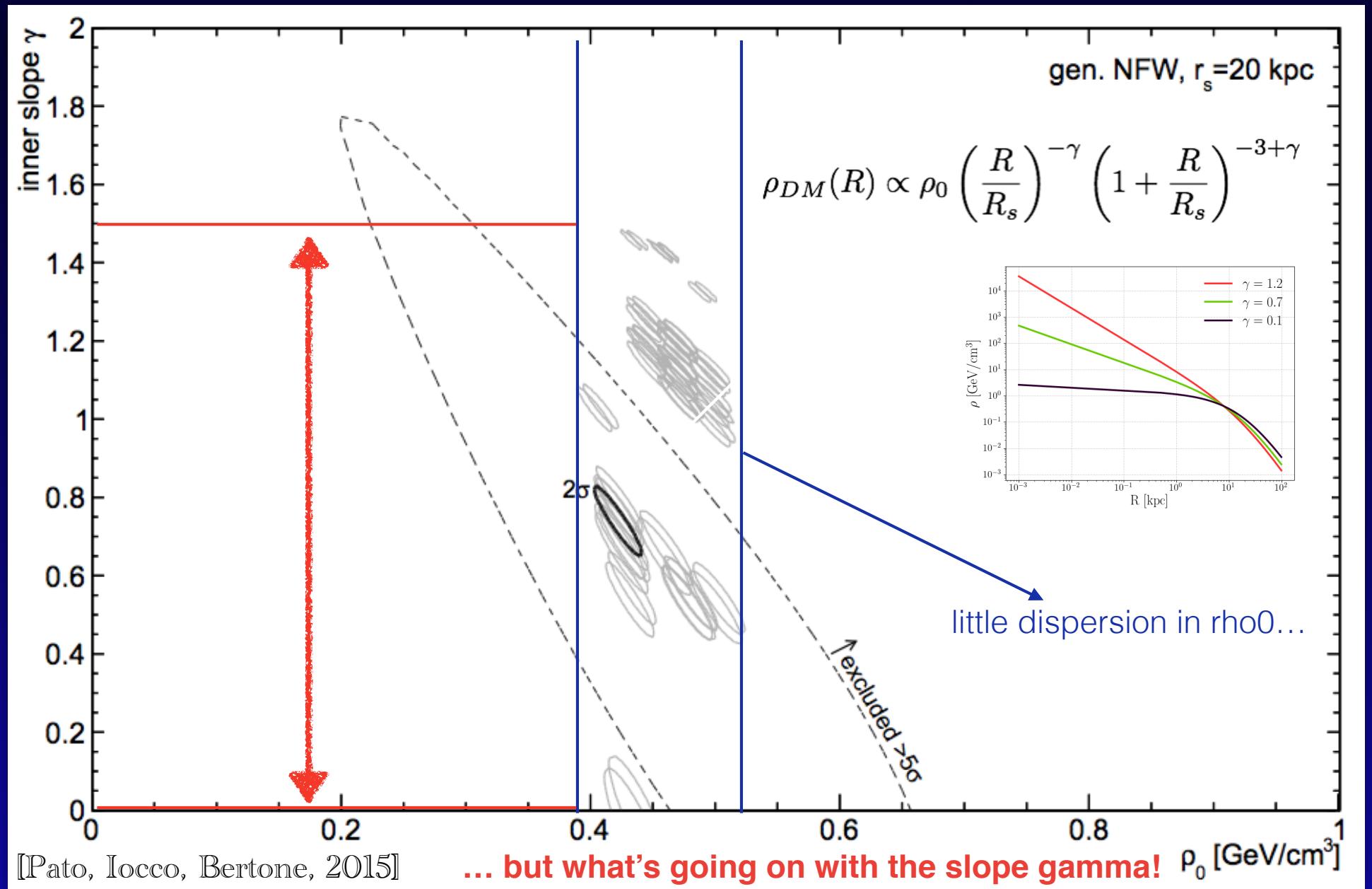


[many authors, e.g.  
Iocco et al. 2011 ]

# *Systematic uncertainties (luminous component)*

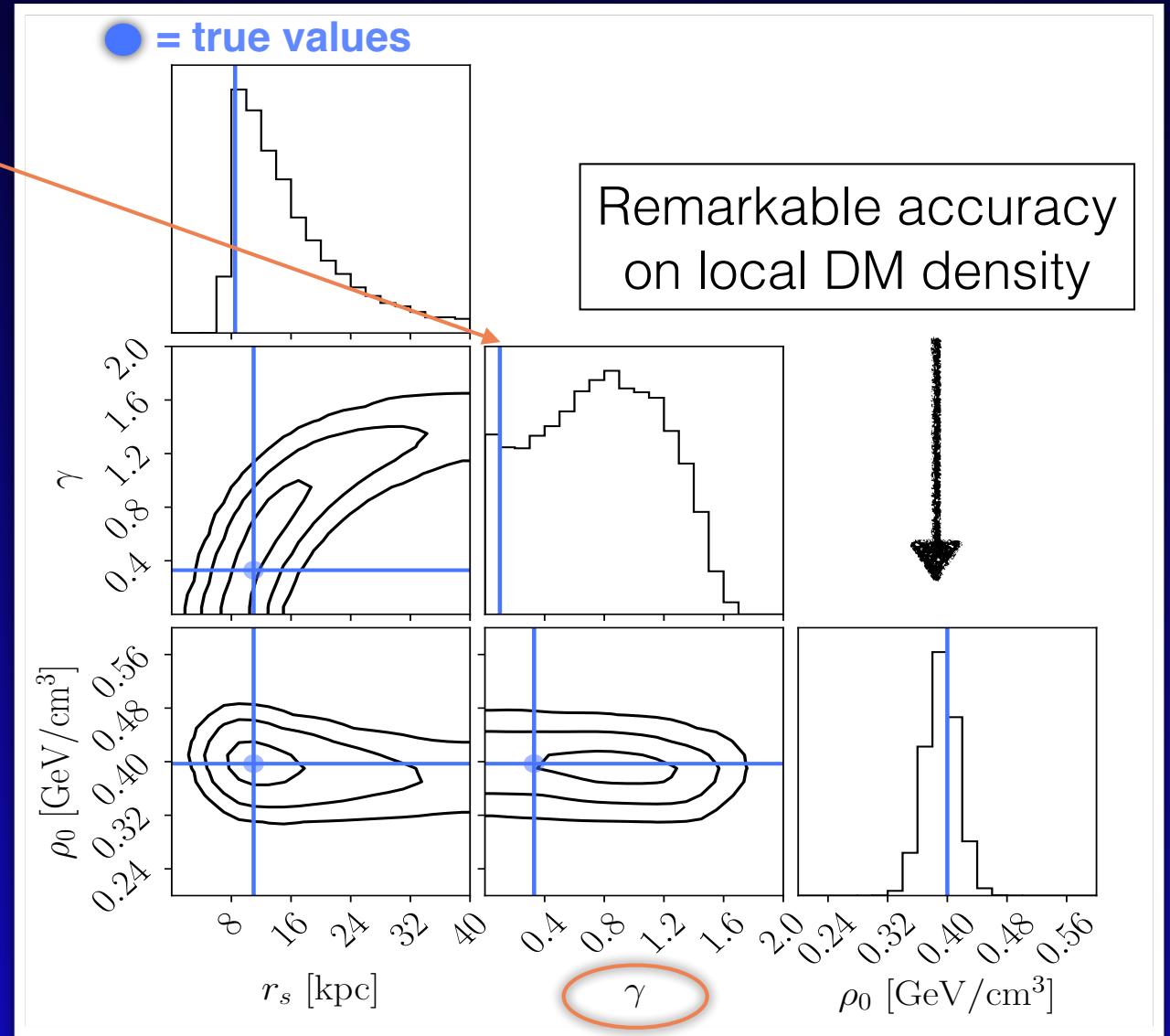
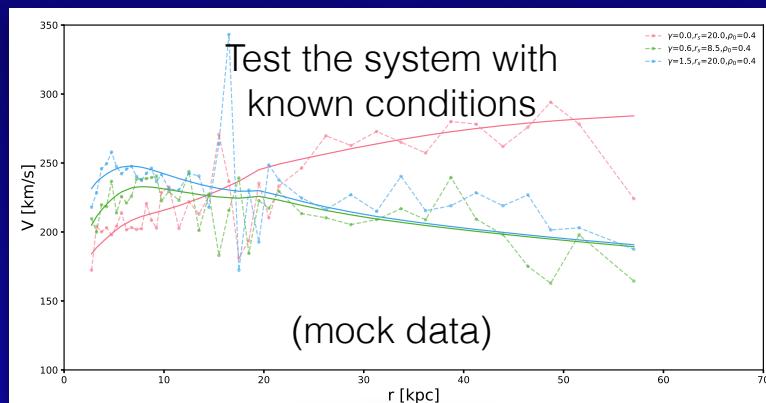


# Extracting the DM density structure



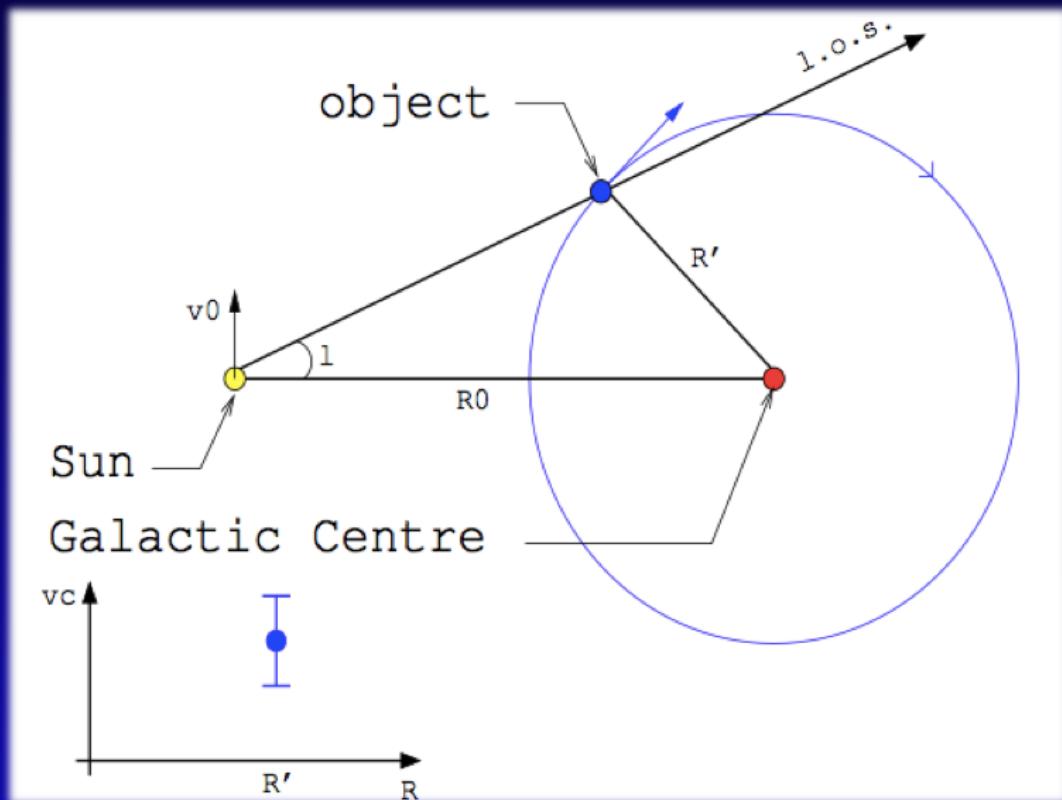
# What to do of our measurement?

(Our instrument is very precise. Is it accurate?)



# The Milky Way: observed rotation curve

Neglecting some quite remarkable uncertainties (for now)



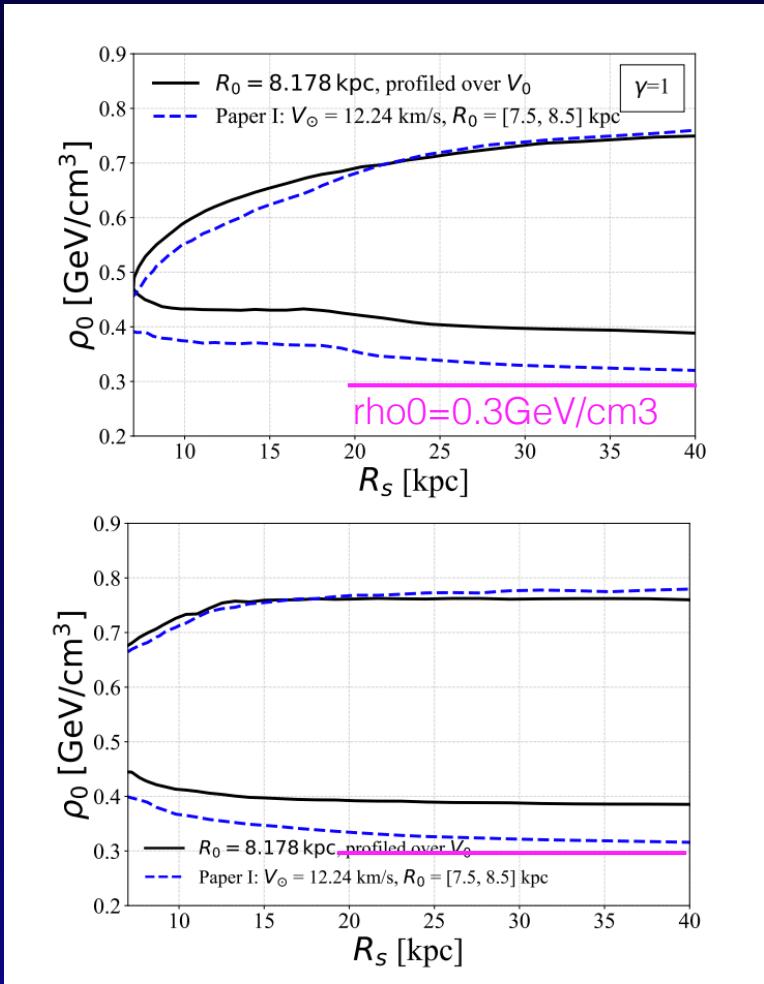
$$v_{\text{LSR}}^{\text{l.o.s.}} = \left( \frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$

observing tracers from our own position,  
transforming into GC-centric reference frame

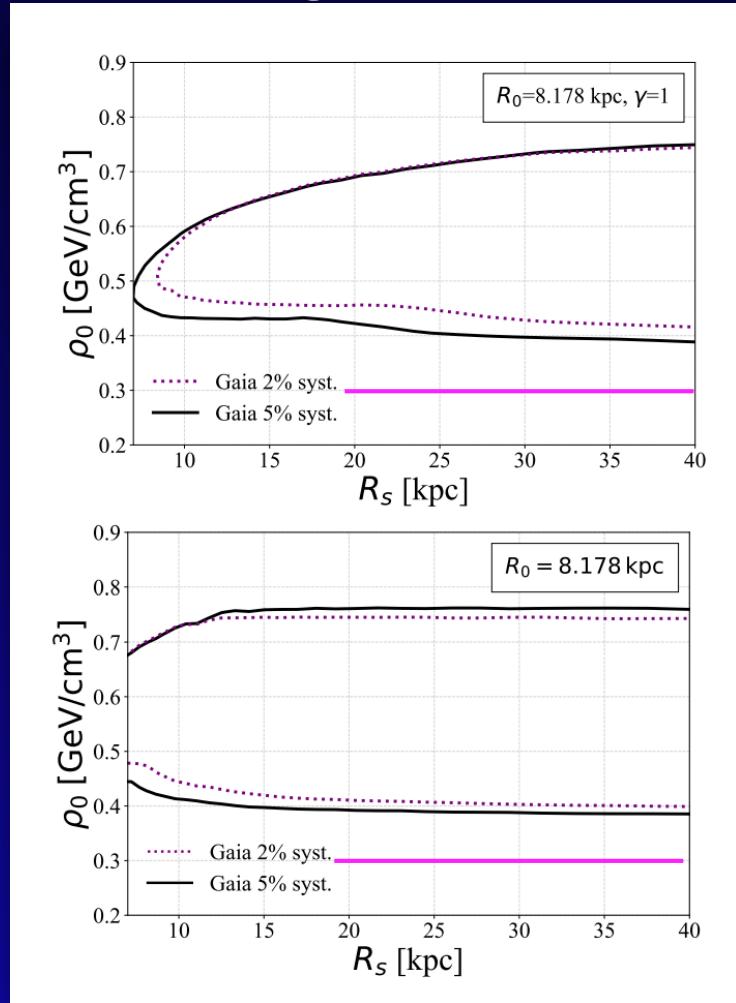
Uncertainties on  $(R_0, v_0)$   
ultimately affects our  
determination of  
( $\rho_0$ ,  $\gamma$ )

# *Profiling over Galactic uncertainties*

## Testing approaches



## Testing datasets



Please use the full likelihood:  
publicly available!!

<https://github.com/mariabenitocst/UncertaintiesDMinTheMW>  
[Benito, Iocco, Cuoco, PDU 2021, arXiv:2009.13523]

# Direct and indirect searches of WIMP DM *complementary to colliders*

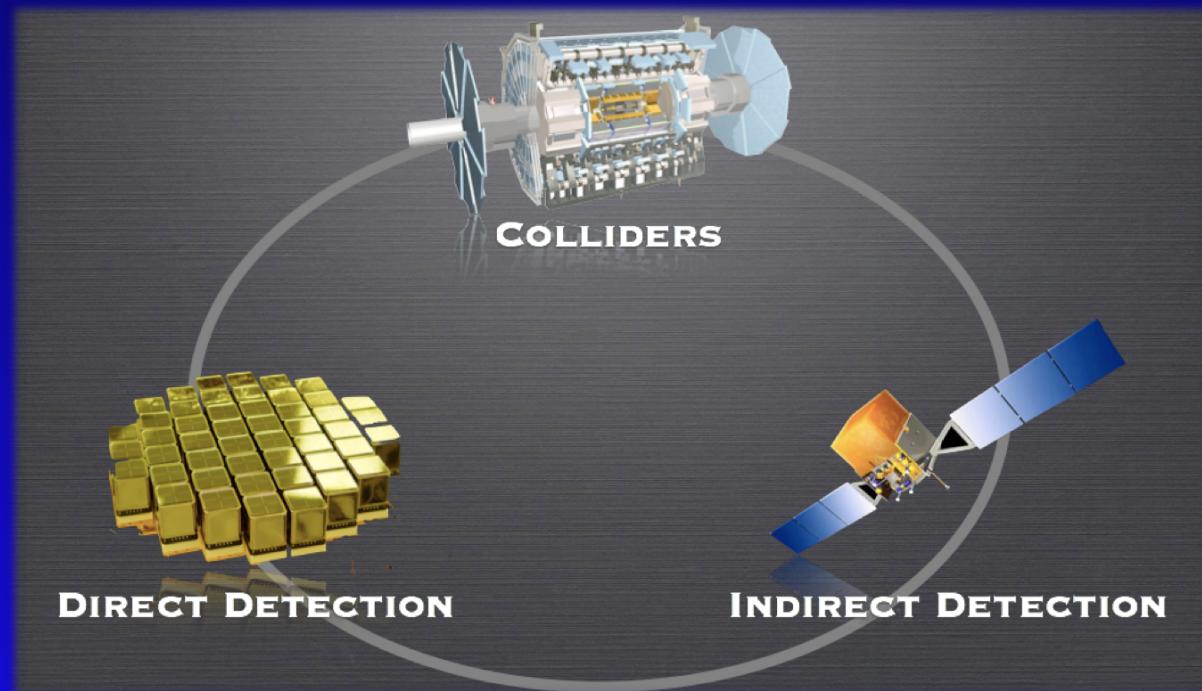
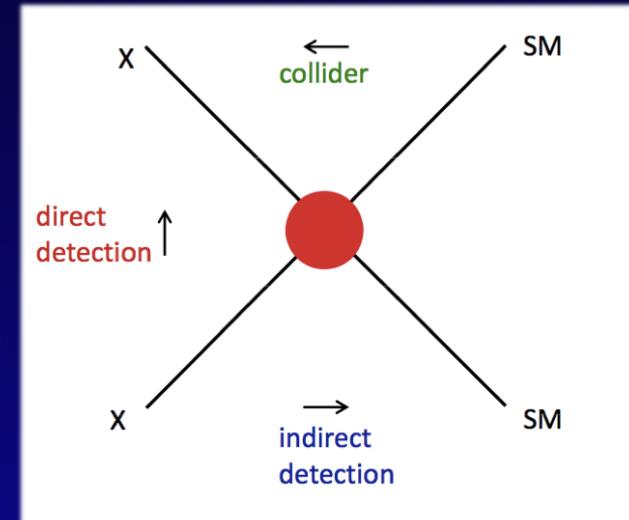
Direct detection:

DM scattering against nuclei, recoil

Indirect detection:

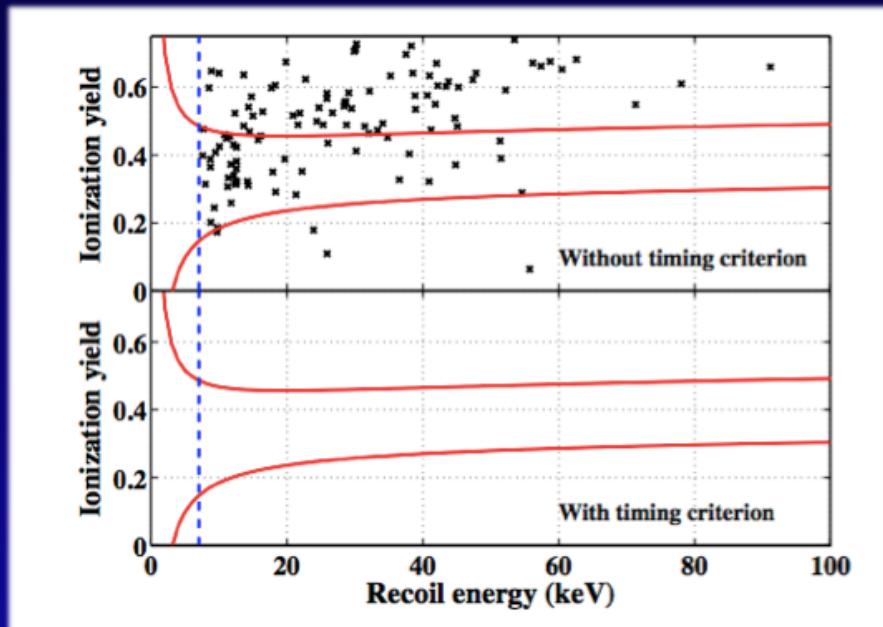
Annihilation in astrophysical envir.  
Observation of SM products of annih.

Production at LHC

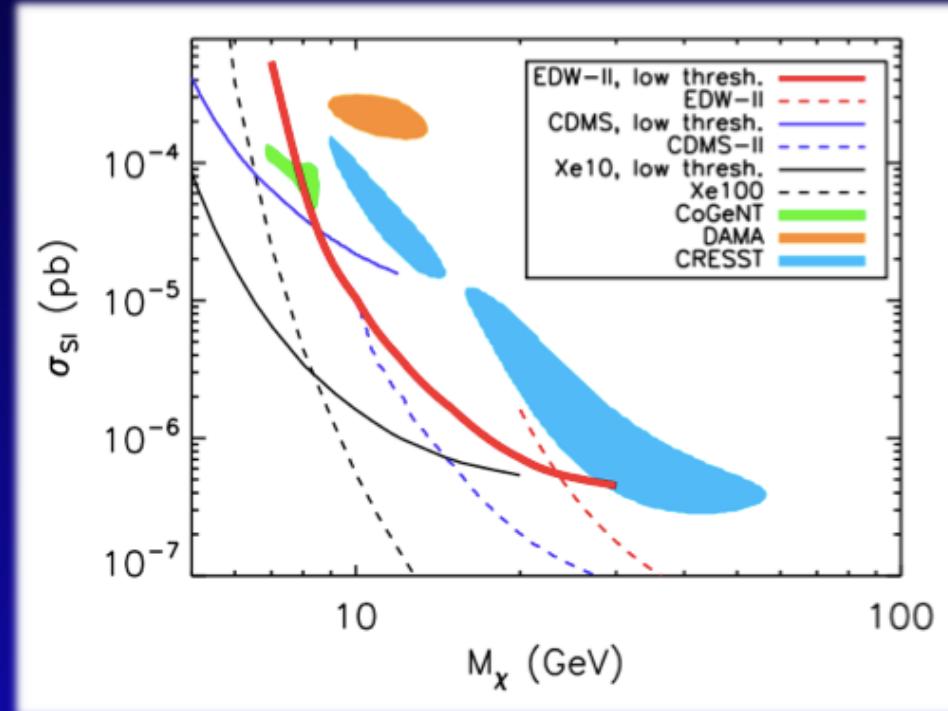


# Direct Detection: principles and dependencies (to go...)

from this



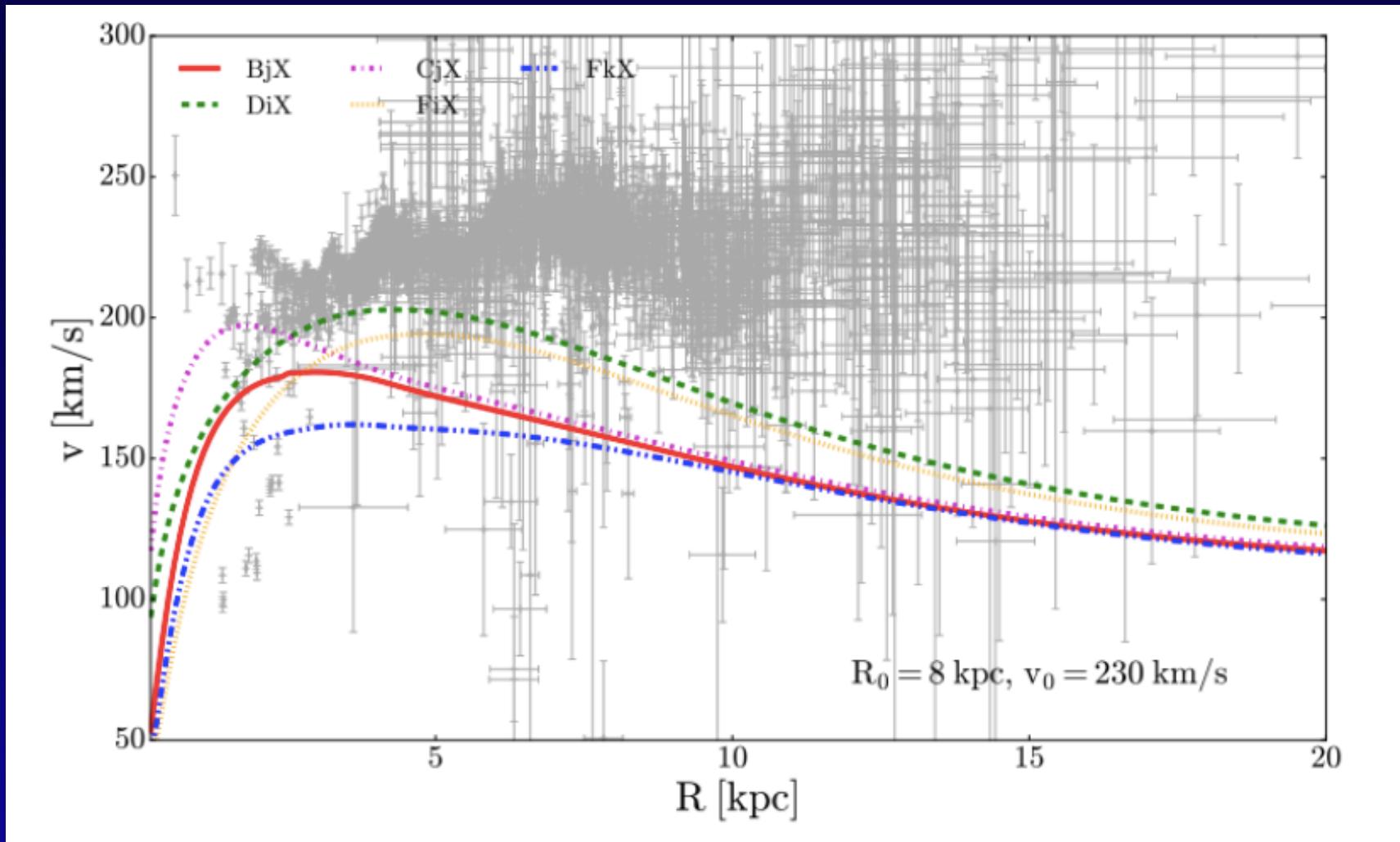
to this



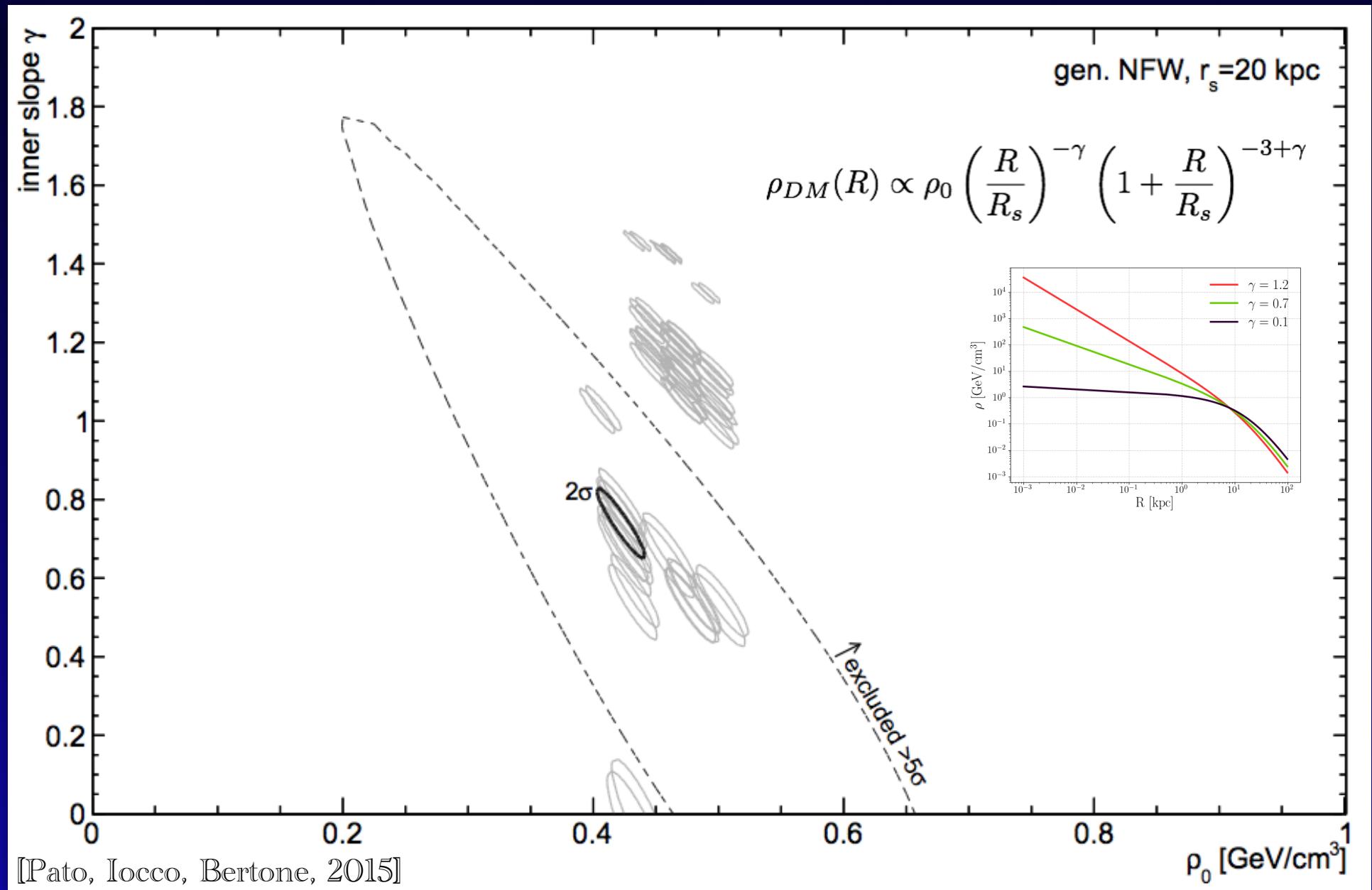
you need this

$$\frac{dR}{dE} \propto \frac{1}{\mu^2} \frac{\sigma_\chi}{m_\chi} \rho_0 \eta(v, t)$$

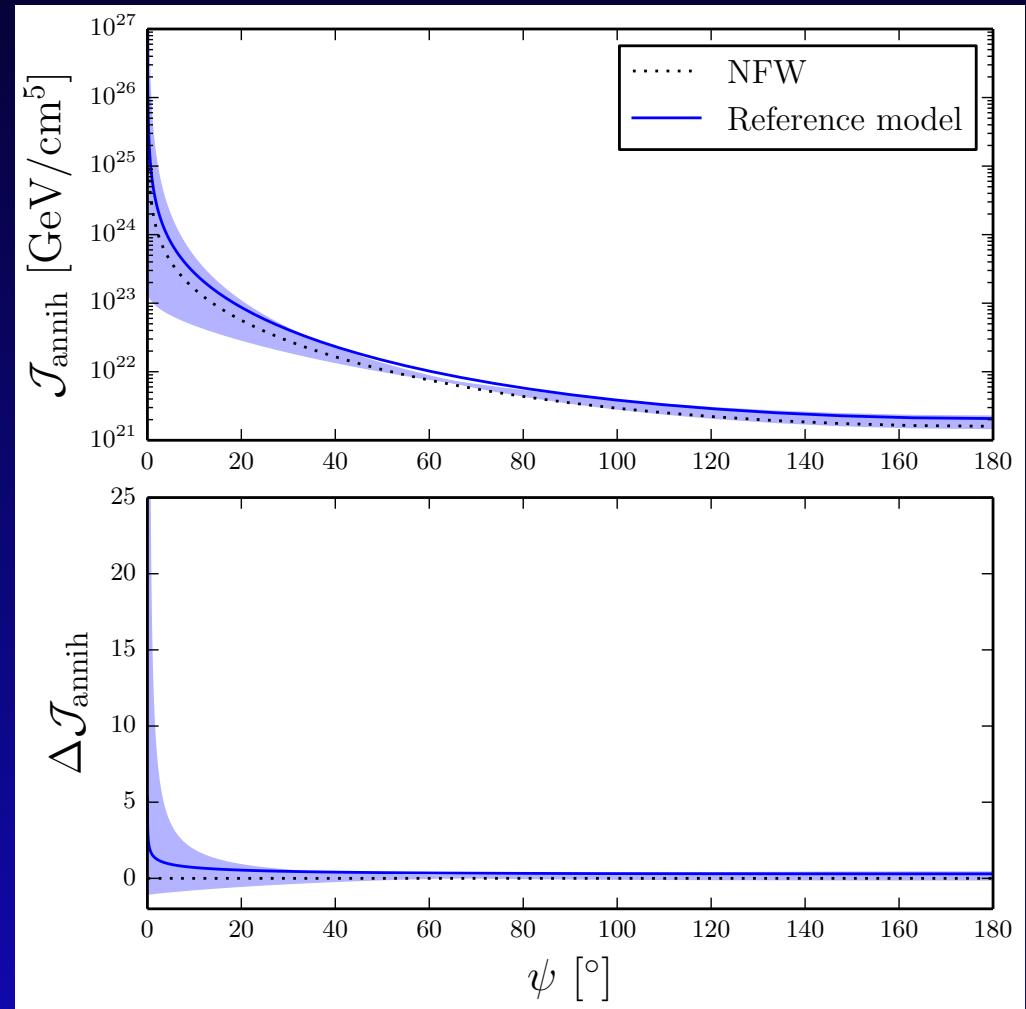
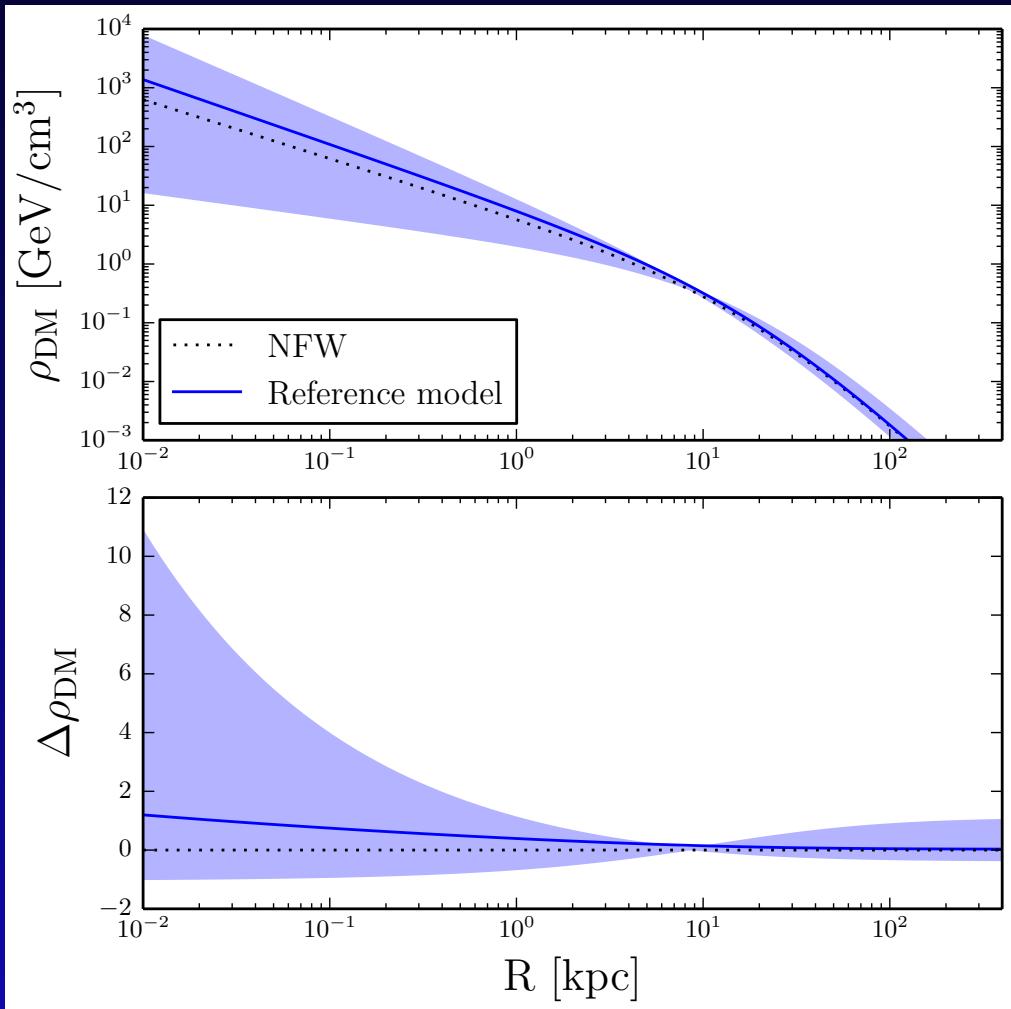
# *Systematic uncertainties (luminous component)*



# Extracting the DM density structure

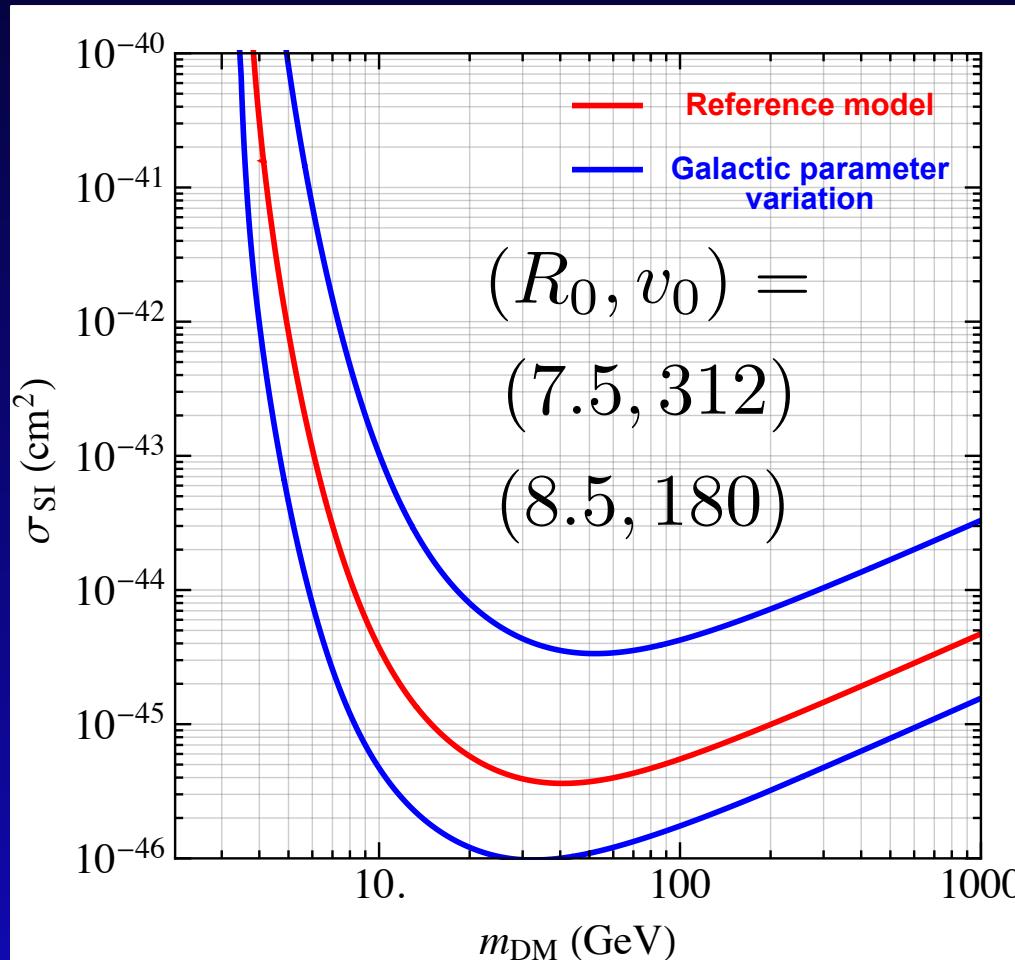


# But do Galactic uncertainties affect PP, for real?



$$J_{\text{annih}} \propto \int_{\text{los}} \rho^2(r) dV$$

It is well known that uncertainties affect Direct Detection



2015 LUX limits, varying astrophysical uncertainties

[Benito, Bernàl, Bozorgnia, Calore, Iocco, JCAP 2017, arXiv:1612.02010]

Let's quantify this effect in a specific case:  
Singlet Scalar DM

$$V = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \mu_S^2 S^2 + \lambda_S S^4 + \lambda_{HS} |H|^2 S^2$$

$$v_H = 246 \text{ GeV} \quad \langle S \rangle = 0$$

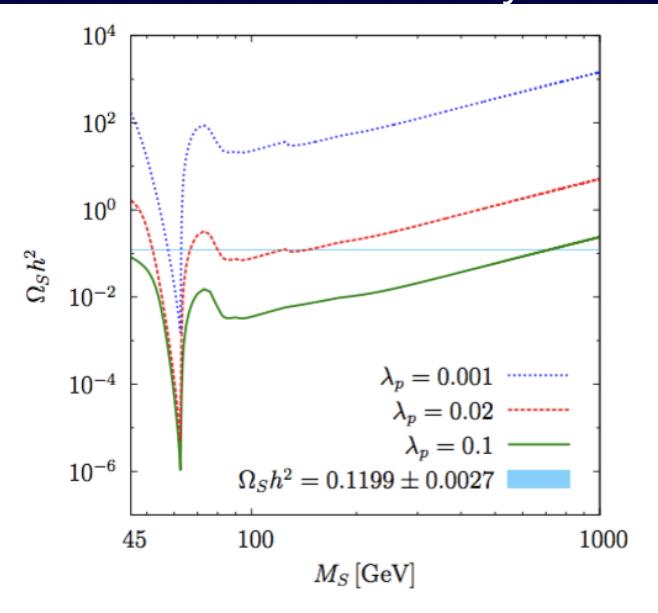
$$m_S^2 = 2 \mu_S^2 + \lambda_{HS} v_H^2$$

“WIMP phenomenology” entirely dictated by the Higgs coupling and physical DM mass.

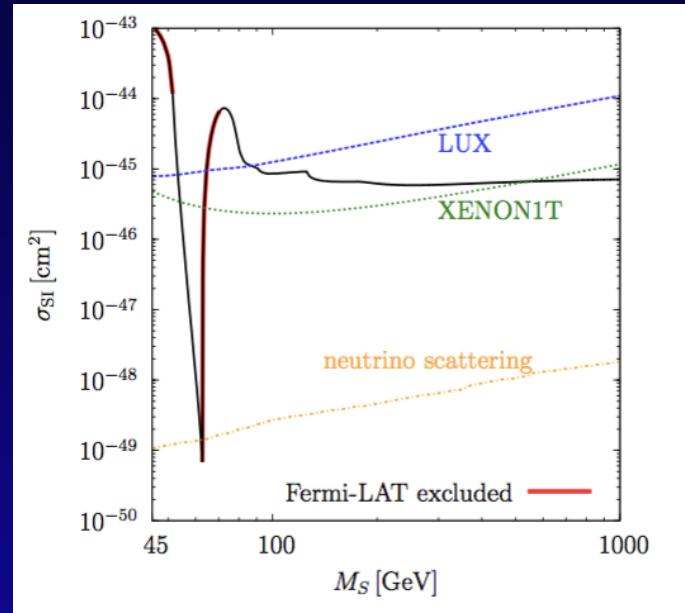
# Singlet Scalar DM

## Constraints and interplay of experiments

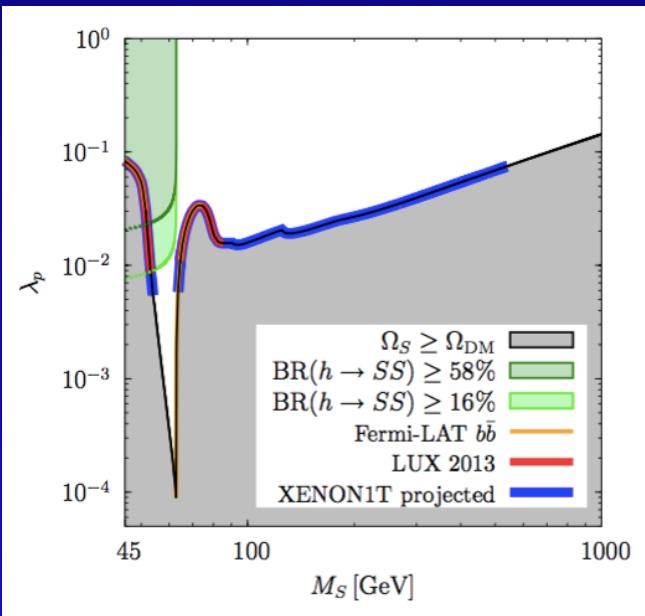
Relic density



Direct detection



Combined

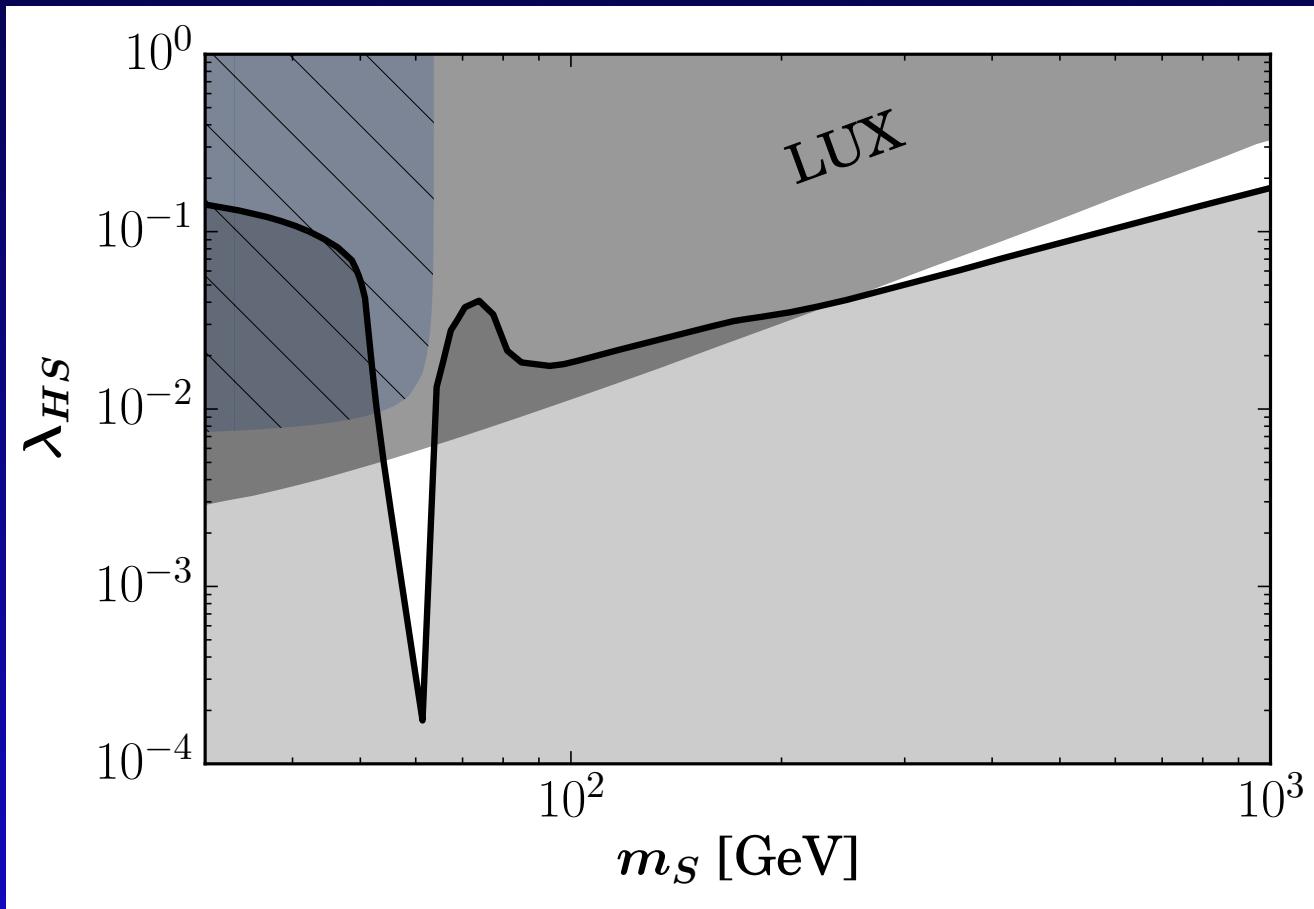


[Duerr et al, 2015]

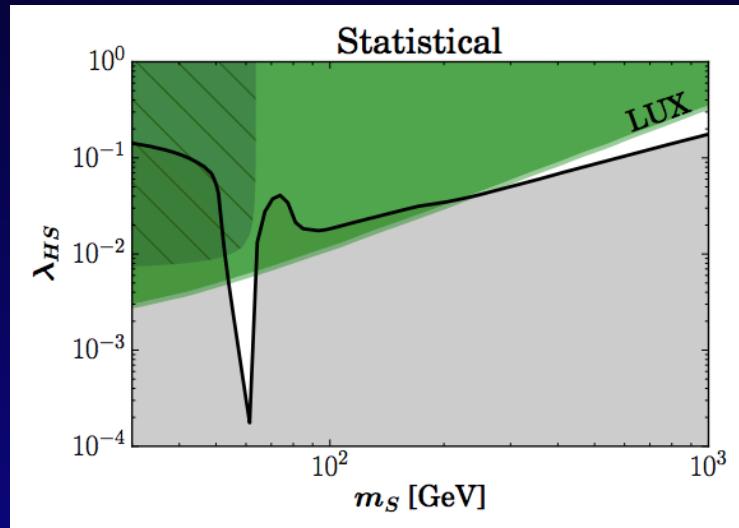
# Singlet Scalar DM

## Constraints and interplay of experiments

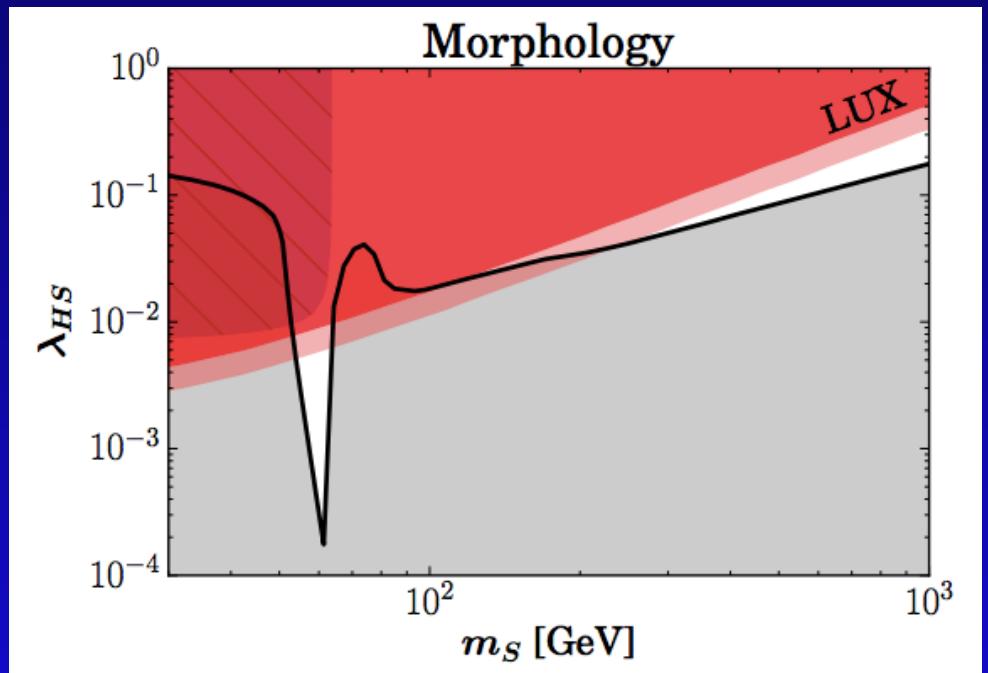
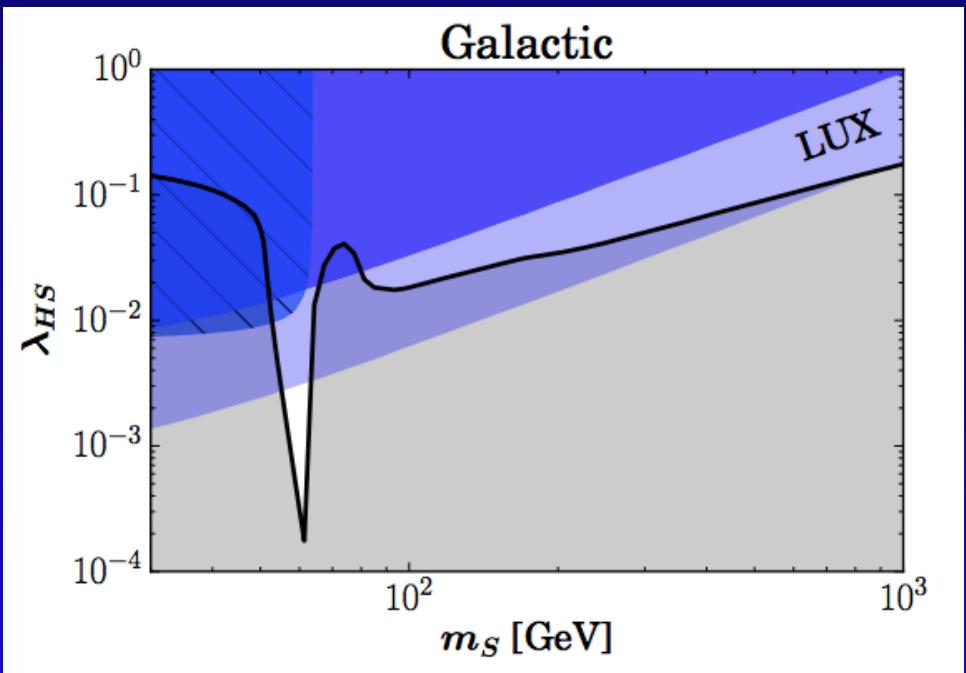
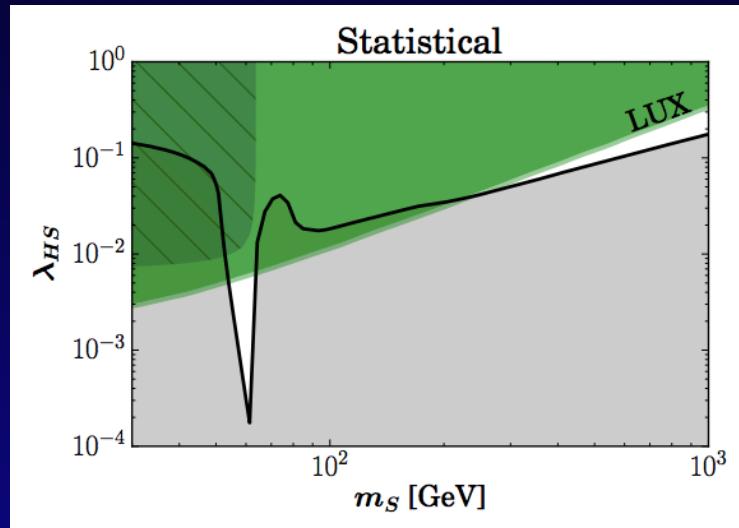
$$V = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \mu_S^2 S^2 + \lambda_S S^4 + \lambda_{HS} |H|^2 S^2$$



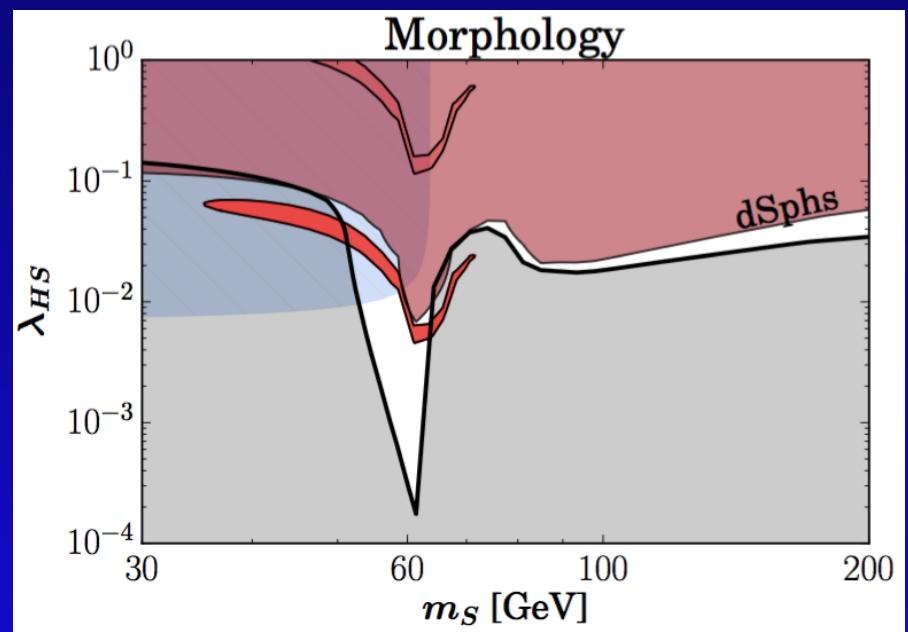
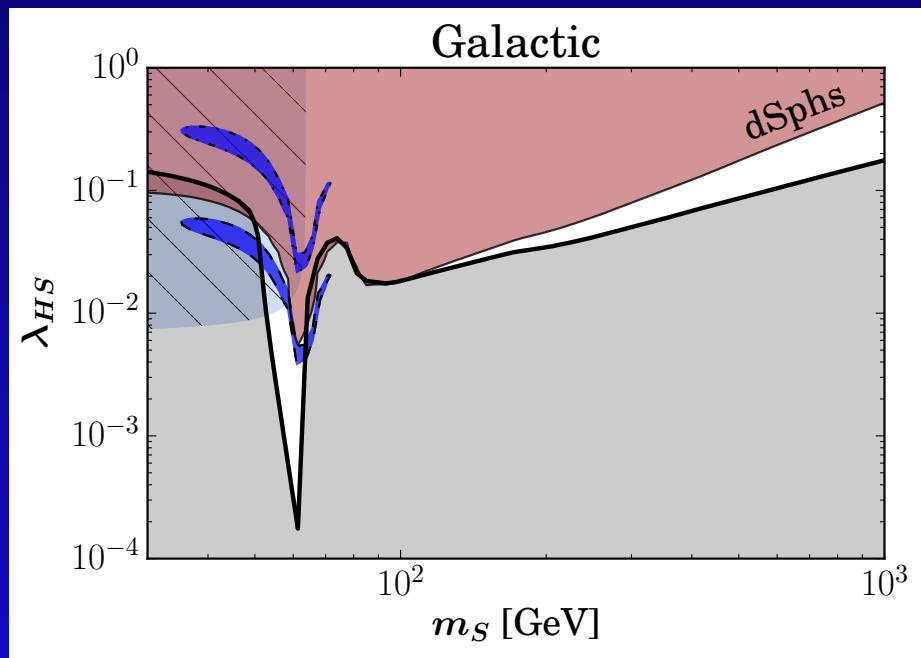
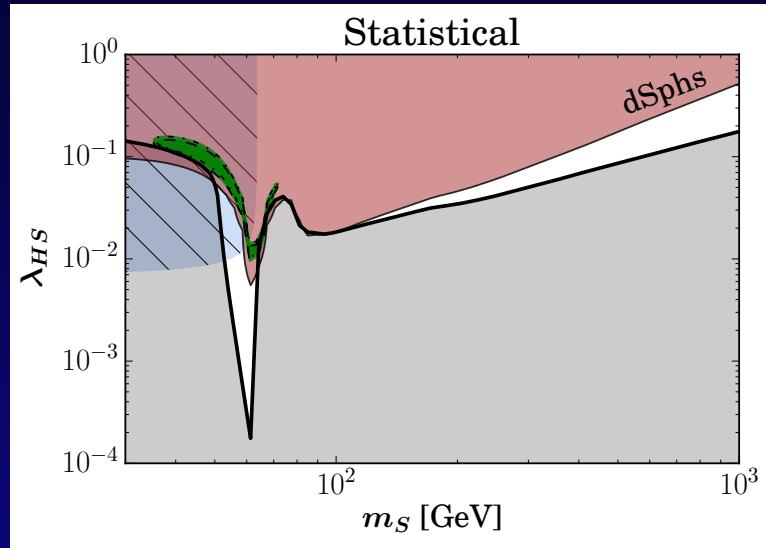
# Let's look at the effect of astrophysics uncertainties: Direct Detection



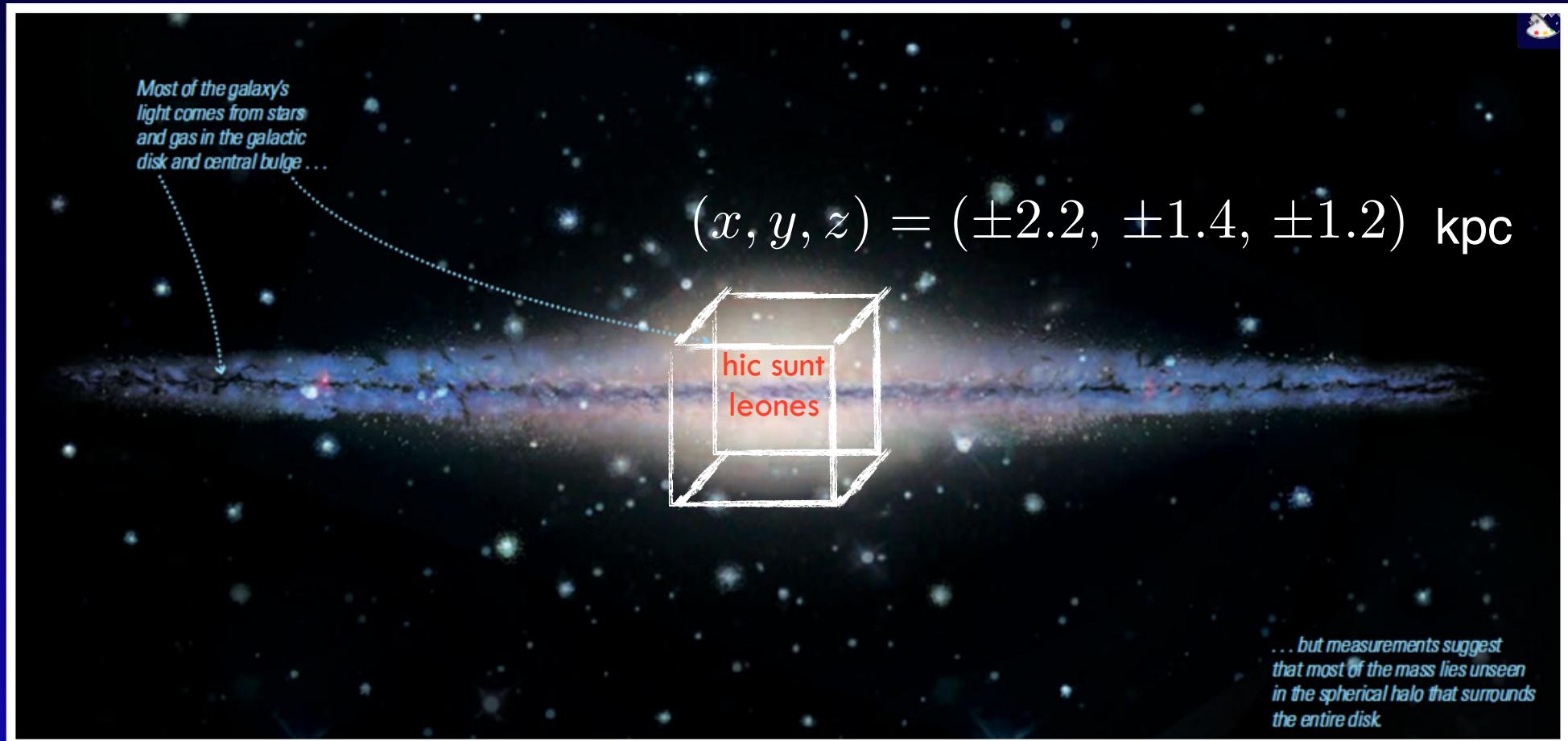
# Let's look at the effect of astrophysics uncertainties: Direct Detection



# Let's look at the effect of astrophysics uncertainties: Indirect Detection



# Galactic Center: a beast of its own



## Total mass

$$M_{total} = (1.85 \pm 0.05) \times 10^{10} M_{\odot}$$

Portail +  
MNRAS 465 (2017)

## Stellar mass

$$M_*^i = \int_{box} \rho_*^i(x, y, z) dV$$

[Iocco & Benito] PDU 15 (2017)

# Methodology: Allowed DM mass

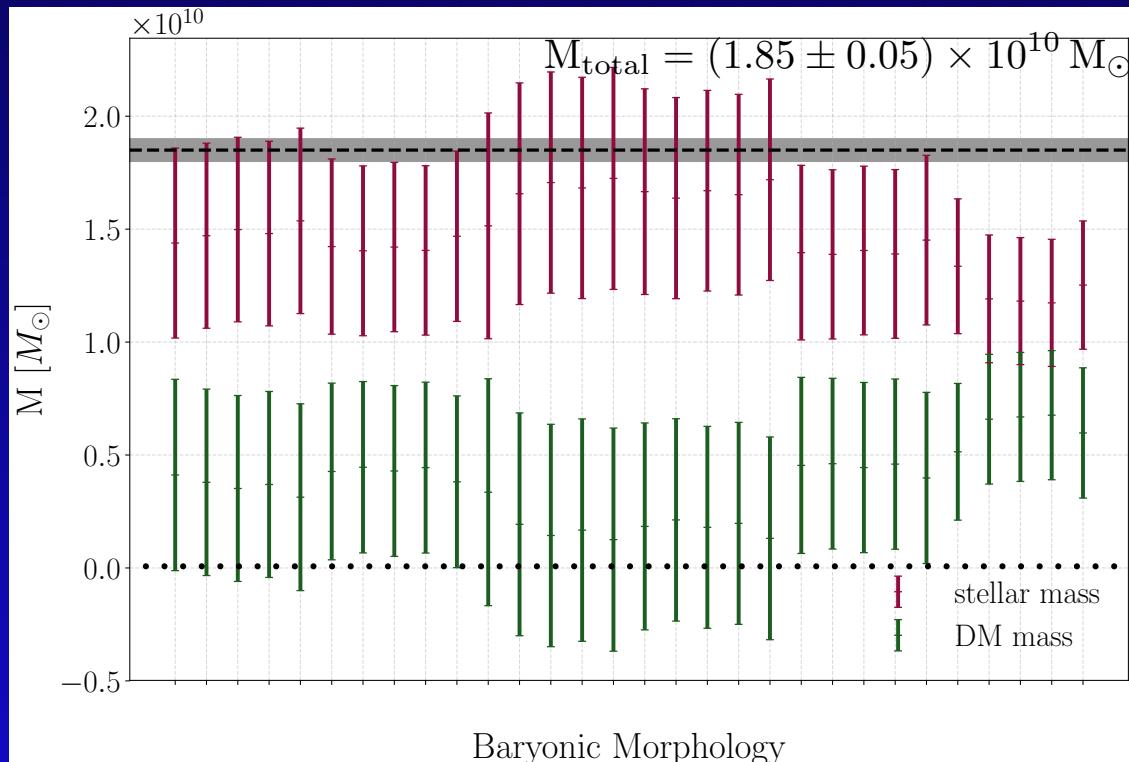
$$M_{\text{total}} - M_*^i = M_{\text{DM}}^i$$

$$\sigma_{M_{\text{DM}}} = \sqrt{\sigma_{M_{\text{total}}}^2 + \sigma_{M_*^i}^2}$$

$$M_* = (1.1 - 1.7) \times 10^{10} M_\odot$$

$$M_{\text{DM}} = (0.1 - 0.7) \times 10^{10} M_\odot$$

**DM mass corresponds to 7-37%**



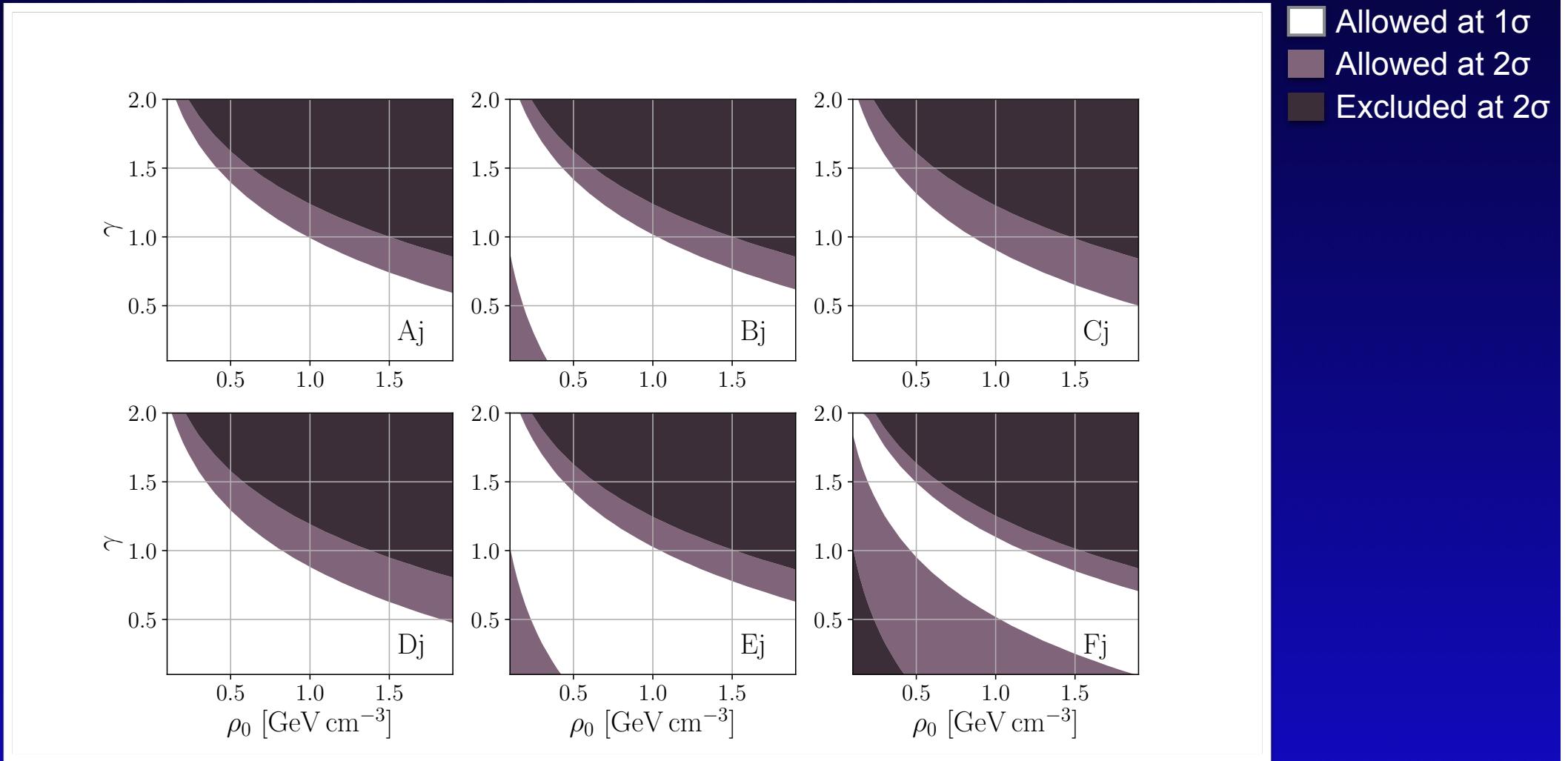
**gNFW density profile**

$$\rho_{\text{DM}}(r) = \rho_0 \left( \frac{R_0}{r} \right)^\gamma \left( \frac{R_s + R_0}{R_s + r} \right)^{3-\gamma}$$

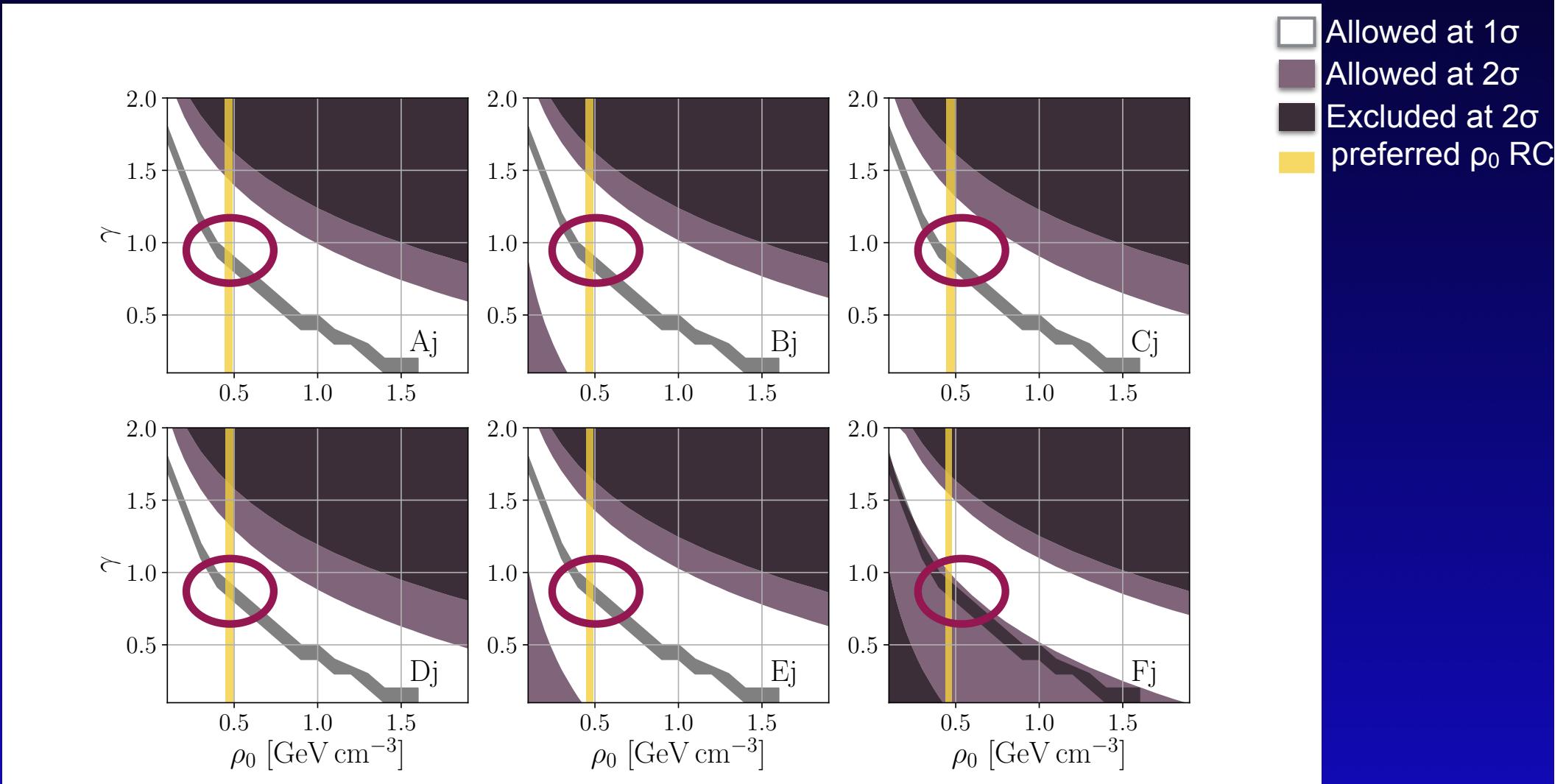
Study parameter space that gives a mass in excess or deficit with respect to the allowed DM mass

# Galactic Bulge Region

## Results: varying bulge morphology



# Galactic Bulge Region and RC curve compatibility



$$M_{\text{DM}} = (0.32 \pm 0.05) \times 10^{10} M_{\odot}$$

“the dark matter density of our model has a [...] Portail + shallow cusp or a **core in the bulge region**”

Portail +  
MNRAS 465 (2017)

[Iocco & Benito, 2017]

arXiv:1611.09861

(+ M. Benito’s thesis)

# *Cuncta stricte*

- Determining the local DM density from actual data is possible
- RC method is accurate and precise, in spite of large range of observational systematic and statistical uncertainties.
- Slope (i.e. full profile of MW) is not very accurate, and quite depending from several systematics. (Galactic Center region further complicated.)
- Astrophysical uncertainties are actually affecting determination of PP, in virtuous interplay with collider physics, direct and indirect probes.
- Providing a ready-to-use likelihood for PP use, including astrophysical uncertainties on DM distribution