

# GPGPU in Theoretical Physics

F. Di Renzo  
University of Parma and I.N.F.N.

Napoli, Jan 25<sup>th</sup> 2010

Not really a review. Keep in mind instead that  
*we like novels more than dictionaries*



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)



Computer Physics Communications 177 (2007) 631–639

Computer Physics  
Communications

[www.elsevier.com/locate/cpc](http://www.elsevier.com/locate/cpc)

## Lattice QCD as a video game

Győző I. Egri<sup>a</sup>, Zoltán Fodor<sup>a,b,c,\*</sup>, Christian Hoelbling<sup>b</sup>, Sándor D. Katz<sup>a,b</sup>, Dániel Nógrádi<sup>b</sup>,  
Kálmán K. Szabó<sup>b</sup>

<sup>a</sup> *Institute for Theoretical Physics, Eötvös University, Budapest, Hungary*

<sup>b</sup> *Department of Physics, University of Wuppertal, Germany*

<sup>c</sup> *Department of Physics, University of California, San Diego, USA*

Received 2 February 2007; received in revised form 29 May 2007; accepted 7 June 2007

Available online 15 June 2007

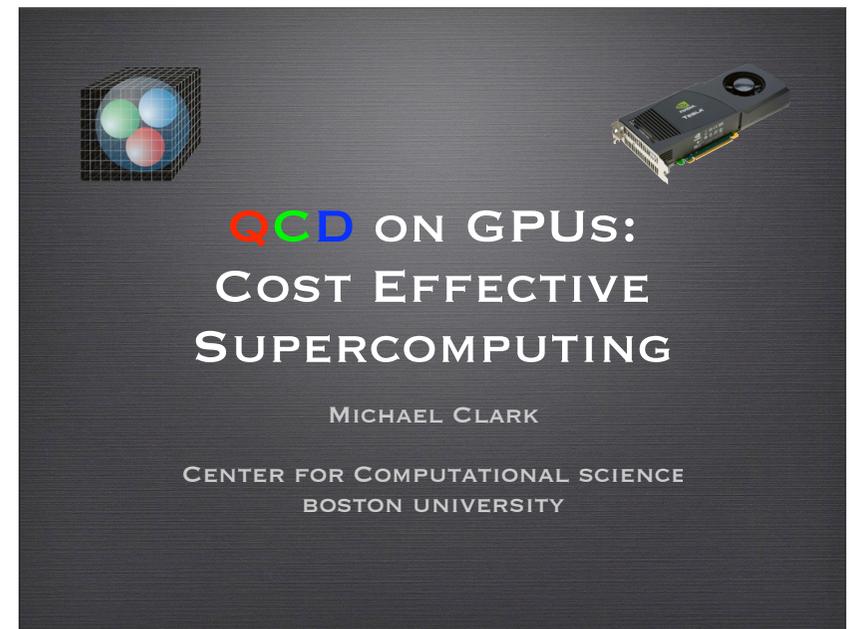
One of the pioneering papers

### Abstract

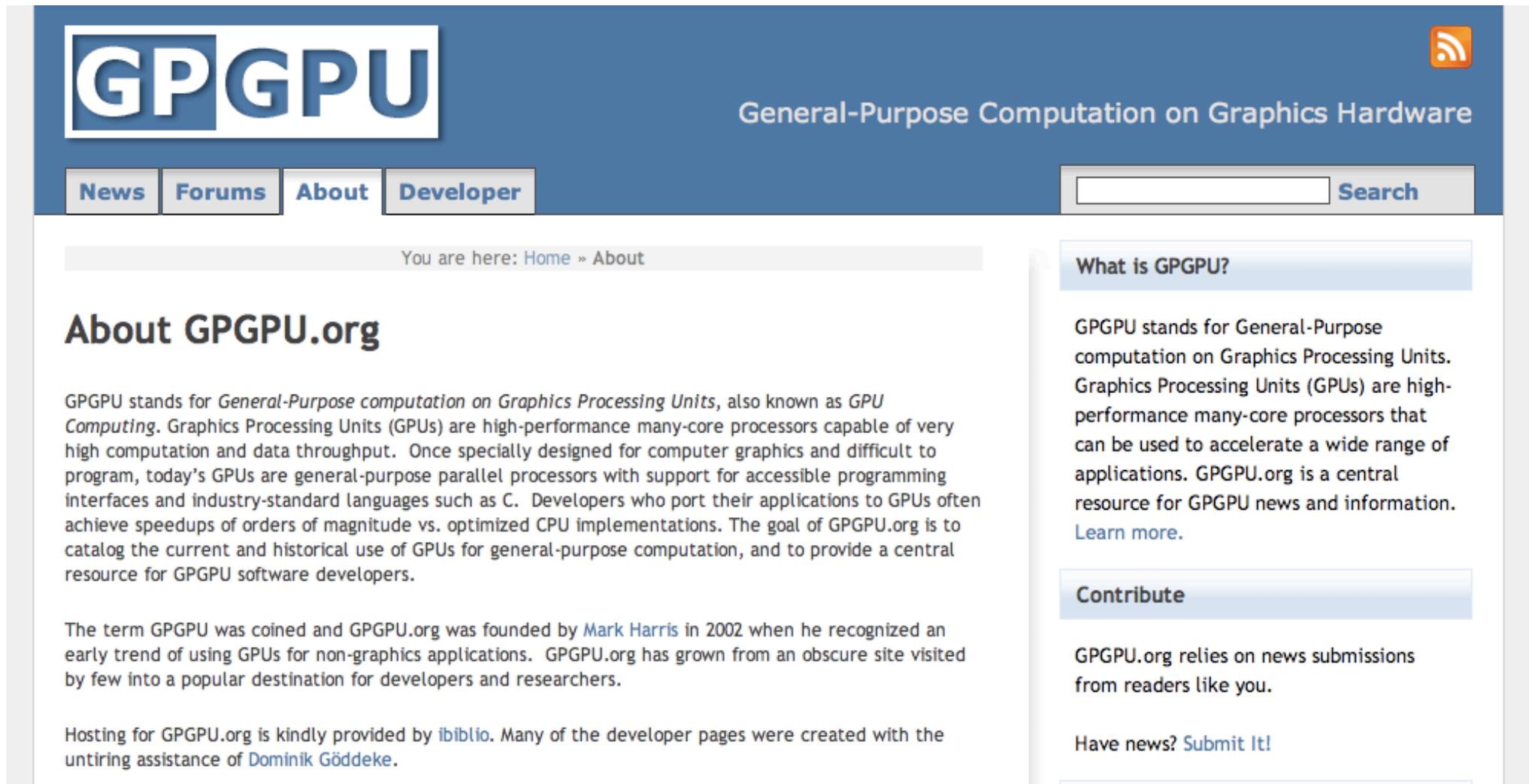
The speed, bandwidth and cost characteristics of today's PC graphics cards make them an attractive target as general purpose computational platforms. High performance can be achieved also for lattice simulations but the actual implementation can be cumbersome. This paper outlines the architecture and programming model of modern graphics cards for the lattice practitioner with the goal of exploiting these chips for Monte Carlo simulations. Sample code is also given.

© 2007 Elsevier B.V. All rights reserved.

A review talk at the 2009 Lattice Conference



Nowadays proof of existence (according to my friend Lele Tripiccione):  
is there a web page? <http://gpgpu.org>



The image shows a screenshot of the GPGPU.org website. The header features the GPGPU logo on the left and the text "General-Purpose Computation on Graphics Hardware" on the right. Below the logo are navigation tabs for "News", "Forums", "About", and "Developer". A search bar is located on the right side of the header. The main content area has a breadcrumb trail "You are here: Home » About" and a large heading "About GPGPU.org". The text explains that GPGPU stands for General-Purpose computation on Graphics Processing Units, also known as GPU Computing. It describes GPUs as high-performance many-core processors and mentions that GPGPU.org is a central resource for GPGPU news and information. A sidebar on the right contains sections titled "What is GPGPU?" and "Contribute", both providing additional information and links.

**GP GPU**

General-Purpose Computation on Graphics Hardware

News Forums About Developer

Search

You are here: Home » About

## About GPGPU.org

GPGPU stands for *General-Purpose computation on Graphics Processing Units*, also known as *GPU Computing*. Graphics Processing Units (GPUs) are high-performance many-core processors capable of very high computation and data throughput. Once specially designed for computer graphics and difficult to program, today's GPUs are general-purpose parallel processors with support for accessible programming interfaces and industry-standard languages such as C. Developers who port their applications to GPUs often achieve speedups of orders of magnitude vs. optimized CPU implementations. The goal of GPGPU.org is to catalog the current and historical use of GPUs for general-purpose computation, and to provide a central resource for GPGPU software developers.

The term GPGPU was coined and GPGPU.org was founded by [Mark Harris](#) in 2002 when he recognized an early trend of using GPUs for non-graphics applications. GPGPU.org has grown from an obscure site visited by few into a popular destination for developers and researchers.

Hosting for GPGPU.org is kindly provided by [ibiblio](#). Many of the developer pages were created with the untiring assistance of [Dominik Göddeke](#).

### What is GPGPU?

GPGPU stands for General-Purpose computation on Graphics Processing Units. Graphics Processing Units (GPUs) are high-performance many-core processors that can be used to accelerate a wide range of applications. GPGPU.org is a central resource for GPGPU news and information. [Learn more.](#)

### Contribute

GPGPU.org relies on news submissions from readers like you.

Have news? [Submit It!](#)

We can try to look for Science, Physics, Theoretical Physics ...



General-Purpose Computation on Graphics Hardware



[News](#)

[Forums](#)

[About](#)

[Developer](#)

[Search](#)

## GPU Simulations of Gravitational Many-body Problem and GPU Octrees

January 20th, 2010

This undergraduate thesis and poster by Kajuki Fujiwara and Naohito Nakasato from the University of Aizu approach a common problem in astrophysics: the many-body problem, with both brute-force and hierarchical data structures for solving it on ATI GPUs. Abstracts:

### [Fast Simulations of Gravitational Many-body Problem on RV770 GPU](#)

*Kazuki Fujiwara, Naohito Nakasato (University of Aizu)*

Abstract:

The gravitational many-body problem is a problem concerning the movement of bodies, which are interacting through gravity. However, solving the gravitational many-body problem with a CPU takes a lot of time due to  $O(N^2)$  computational complexity. In this paper, we show how to speed-up the gravitational many-body problem by using GPU. After extensive optimizations, the peak performance obtained so far is about 1 Tflops.

### [Oct-tree Method on GPU](#)

*N.Nakasato*

Abstract:

The kd-tree is a fundamental tool in computer science. Among others, an application of the kd-tree search (oct-tree method) to fast evaluation of particle interactions and neighbor search is highly important since computational complexity of these problems are reduced from  $O(N^2)$  with a brute force method to  $O(N \log N)$  with the tree method where  $N$  is a number of particles. In this paper, we present a parallel implementation of the tree method running on a graphic processor unit (GPU). We successfully run a simulation of structure formation in the universe very efficiently. On our system, which costs roughly \$900, the run with  $N \sim 2.87 \times 10^6$  particles took 5.79 hours and executed  $1.2 \times 10^{13}$  force evaluations in total. We obtained the sustained computing speed of 21.8 Gflops and the cost per Gflops of 41.6/Gflops that is two and half times better than the previous record in 2006.

Posted in [Research](#) | Tags: [Astrophysics](#), [Data Structures](#), [Papers](#), [Posters](#) | [Write a comment](#)

### What is GPGPU?

GPGPU stands for General-Purpose computation on Graphics Processing Units. Graphics Processing Units (GPUs) are high-performance many-core processors that can be used to accelerate a wide range of applications. GPGPU.org is a central resource for GPGPU news and information. [Learn more.](#)

### Contribute

GPGPU.org relies on news submissions from readers like you.

Have news? [Submit It!](#)

### Subscribe

[Entries RSS](#)

[Comments RSS](#)

[follow me](#) [Twitter feed](#)

### Categories

[Business \(51\)](#)

[Developer Resources \(170\)](#)

[Events \(98\)](#)

[Press \(39\)](#)

Again on [gpgpu.org](http://gpgpu.org), let's have a look at programming environments

## GPGPU Programming

The GPGPU programming landscape has rapidly evolved over the past several years, so that now there are several approaches to programming GPUs. Recently, convergence towards standardization has begun. Readers are recommended to browse the available material to make their own decisions on which approach to use.

### NVIDIA CUDA, AMD Stream and OpenCL

GPU Computing really took off when CUDA and Stream arrived in late 2006. These are programming interfaces and languages, designed by the GPU vendors in close proximity with the hardware, that constitute a tremendous step towards a usable, suitable, scalable and manageable future-proof programming model. [Learn more about AMD Stream](#). [Learn more about NVIDIA CUDA](#).

The Open Compute Language (OpenCL) is designed to provide a unified API for heterogeneous computing on several kinds of parallel devices, including GPUs, multicore CPUs and the Cell Broadband Engine. [Learn more about OpenCL](#).

### Sh and Brook for GPUs

High-level languages and programming environments for GPUs, in particular *BrookGPU* from Stanford University and *Sh* from the University of Waterloo were precursors to today's solutions like CUDA and OpenCL. *Sh* has been commercialized by its developers into *RapidMind* and *BrookGPU* has served as the basis for AMD's *Stream*. [Learn more about BrookGPU and Sh](#).

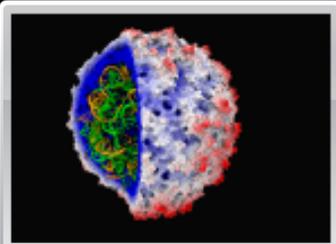
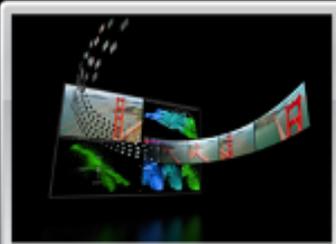
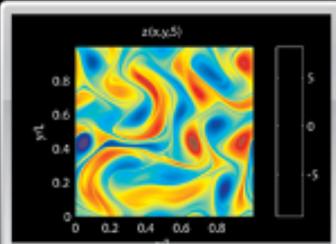
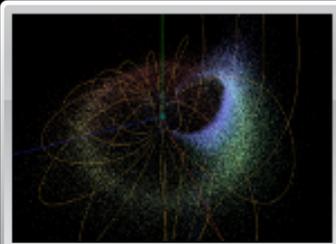
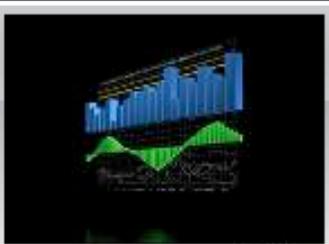
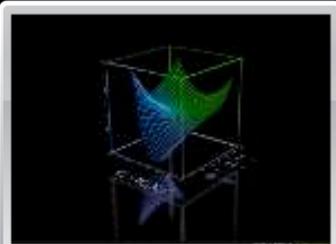
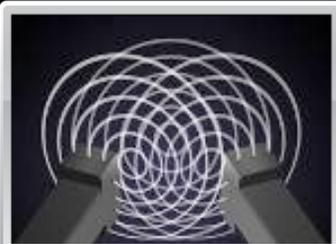
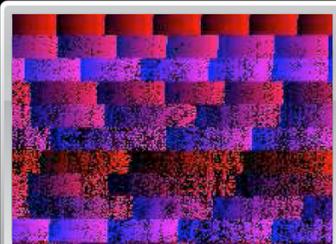
### Legacy GPGPU: Graphics APIs

In the early days, GPGPU programming was a bit hacky. Algorithms had to be cast in terms of graphics APIs such as OpenGL and Direct3D; the underlying hardware was not fully exposed or documented; and the programming was sometimes unproductive. Despite all this, a lot of ground-breaking research has been accomplished that helped pave the way to what GPU computing is now. Despite their legacy status, these older tutorials and sample applications still have some value. [Learn more about legacy GPGPU](#).

#### GPGPU Tutorials

[Supercomputing 2009 CUDA Tutorial](#)  
[PPAM 2009 GPU and OpenCL Tutorial](#)  
[ISC 2009 CUDA Tutorial](#)  
[ASPLOS 2008 CUDA Tutorial](#)  
[SUPERCOMPUTING 2008 Tutorial](#)  
[SUPERCOMPUTING 2007 Tutorial](#)  
[SIGGRAPH 2007 GPGPU Course](#)  
[SUPERCOMPUTING 2006 Tutorial](#)  
[IEEE Visualization 2005 Tutorial](#)  
[SIGGRAPH 2005 GPGPU Course](#)  
[IEEE Visualization 2004 Tutorial](#)  
[SIGGRAPH 2004 GPGPU Course](#)

Move to NVIDIA web pages: examples of CUDA applications

 <p>146X</p>	 <p>36X</p>	 <p>19X</p>	 <p>17X</p>	 <p>100X</p>
<p>Interactive visualization of volumetric white matter connectivity</p>	<p>Ionic placement for molecular dynamics simulation on GPU</p>	<p>Transcoding HD video stream to H.264</p>	<p>Fluid mechanics in Matlab using .mex file CUDA function</p>	<p>Astrophysics N-body simulation</p>
 <p>149X</p>	 <p>47X</p>	 <p>20X</p>	 <p>24X</p>	 <p>30X</p>
<p>Financial simulation of LIBOR model with swaptions</p>	<p>GLAME@lab: an M-script API for GPU linear algebra</p>	<p>Ultrasound medical imaging for cancer diagnostics</p>	<p>Highly optimized object oriented molecular dynamics</p>	<p>Cmatch exact string matching to find similar proteins and gene sequences</p>

As I told you, the style is not really that of a review  
I will basically concentrate on one type of applications (lattice),  
but I will try to make quite general comments

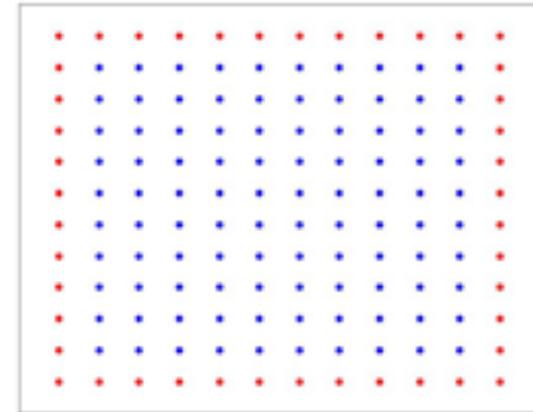
- It's a SIMD business!
- An example from Statistical Mechanics: Hybrid Monte Carlo for a spin model (keeping an eye on Lattice Gauge Theories)
- It's a SIMD business, but one does not deal in general with embarrassing parallelism (synchronizing is an issue)
- New GPGPU programming environments vs legacy GPGPU
- What can we learn from Lattice QCD?
- A single mention of a completely non-lattice application
- Conclusions

## We said it's a SIMD business

- Single Instruction Multiple Data: problems with a huge number of degrees of freedom, each roughly undergoing the same “dynamics”.
- A rough (and personally biased) distinction: lattice vs non-lattice applications (canonical example of the latter type: Molecular Dynamics).
- SIMD/MIMD classification emphasises the two main characters on the stage: FLOPS and BYTES. There are in general a given Flops/Bandwith ratio and a desired one!
- Who is the director in your program? Notice that these devices do not run an OS, so in general programming paradigm is that of number-crunching accelerators.
- As a byproduct there are in general 2 bandwidths to take into account (inside the device and CPU-GPU).

And here we go with the example: 2d XY spin model

$$H = -J \sum_{ij} \vec{s}_i \cdot \vec{s}_j = -J \sum_{ij} \cos(\theta_i - \theta_j).$$



## Il modello XY come un video gioco

Candidato Giovanni Conti

Relatore Dott. Francesco Di Renzo  
Università di Parma  
<https://www.fis.unipr.it>

28 Febbraio 2008



## It's a basic prototype of a LATTICE problem

Typical problem: compute by Monte Carlo

$$\frac{1}{N} \sum_{i=1}^{N \rightarrow \infty} O(X_i) \rightarrow \langle O \rangle_B$$

A good proptotype computation: **Hybrid Monte Carlo**. Configurations are generated via a fictitious hamiltonian system

$$\mathcal{H} = \sum_i \frac{\pi_i^2}{2} + S(\theta_i)$$

Fictitious momenta are gaussian

$$P(\pi) = \mathcal{N}_0 e^{-\frac{1}{2} \sum \pi_i^2}.$$

$$S(\theta_i) = \beta H(\theta_i),$$

$$H = -J \sum_{ij} \vec{s}_i \cdot \vec{s}_j = -J \sum_{ij} \cos(\theta_i - \theta_j).$$

Given the spin (angles) configuration, one extracts momenta and then obtains a new (extended) configuration  $\{\theta'_i, \pi'_i\}$

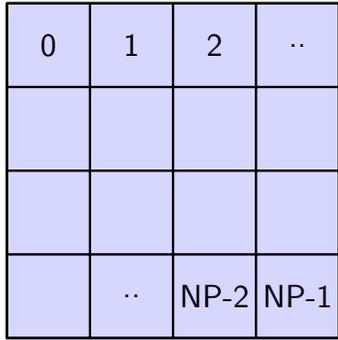
via a Hamiltonian flux

$$\dot{\theta}_i = \frac{\partial \mathcal{H}[\theta, \pi]}{\partial \pi_i}, \quad \dot{\pi}_i = -\frac{\partial \mathcal{H}[\theta, \pi]}{\partial \theta_i}.$$

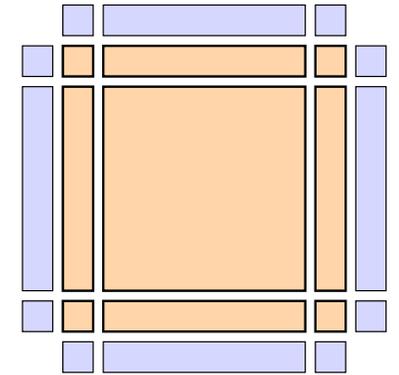
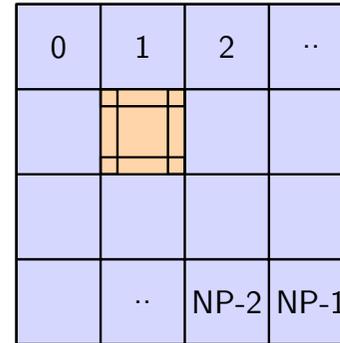
New (angles) configuration will be eventually accepted/rejected.

The equations for angles are **LOCAL**, those for angles are **NOT LOCAL**!

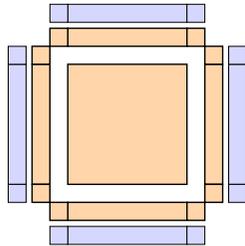
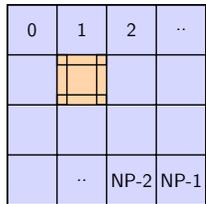
# So, how do we SIMD-solve a prototype LATTICE problem?



First step: a collection of sublattices

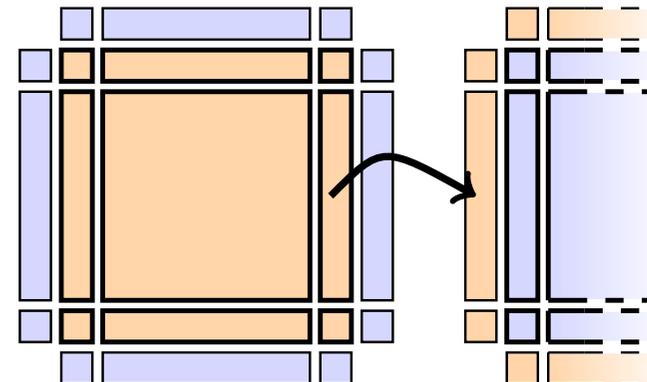


But there is a **nn interaction! Borders**



By the way: usually one wants to optimize memory

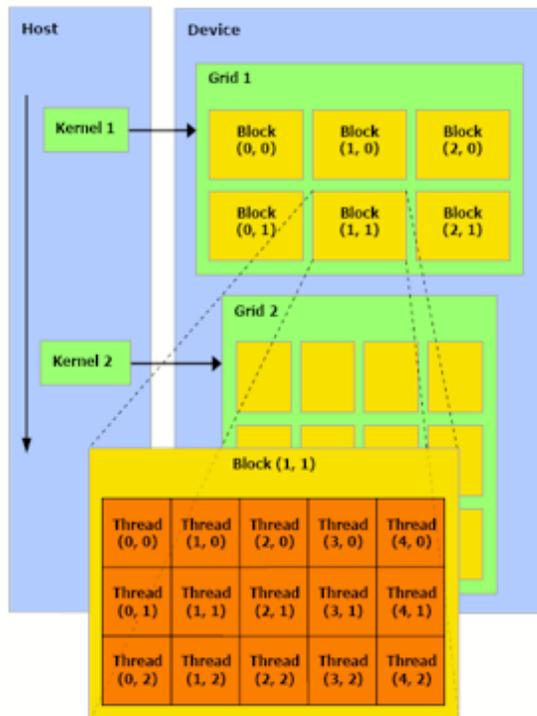
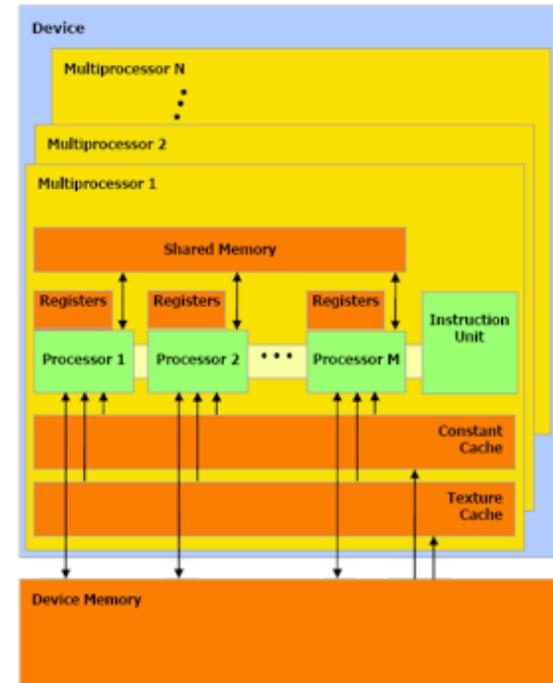
**Borders exchange** is a **synchronization** issue!  
Typically, one wants to **hide latencies with computations**.



# The typical CUDA solution (I)

The CUDA environment by nVIDIA is a quite natural exploitation of the typical GPU architecture

Notice the **memory** hierarchy! Shared memory enables nn communications and synchronization ...



CUDA basics: **grid of blocks** and **blocks of threads**

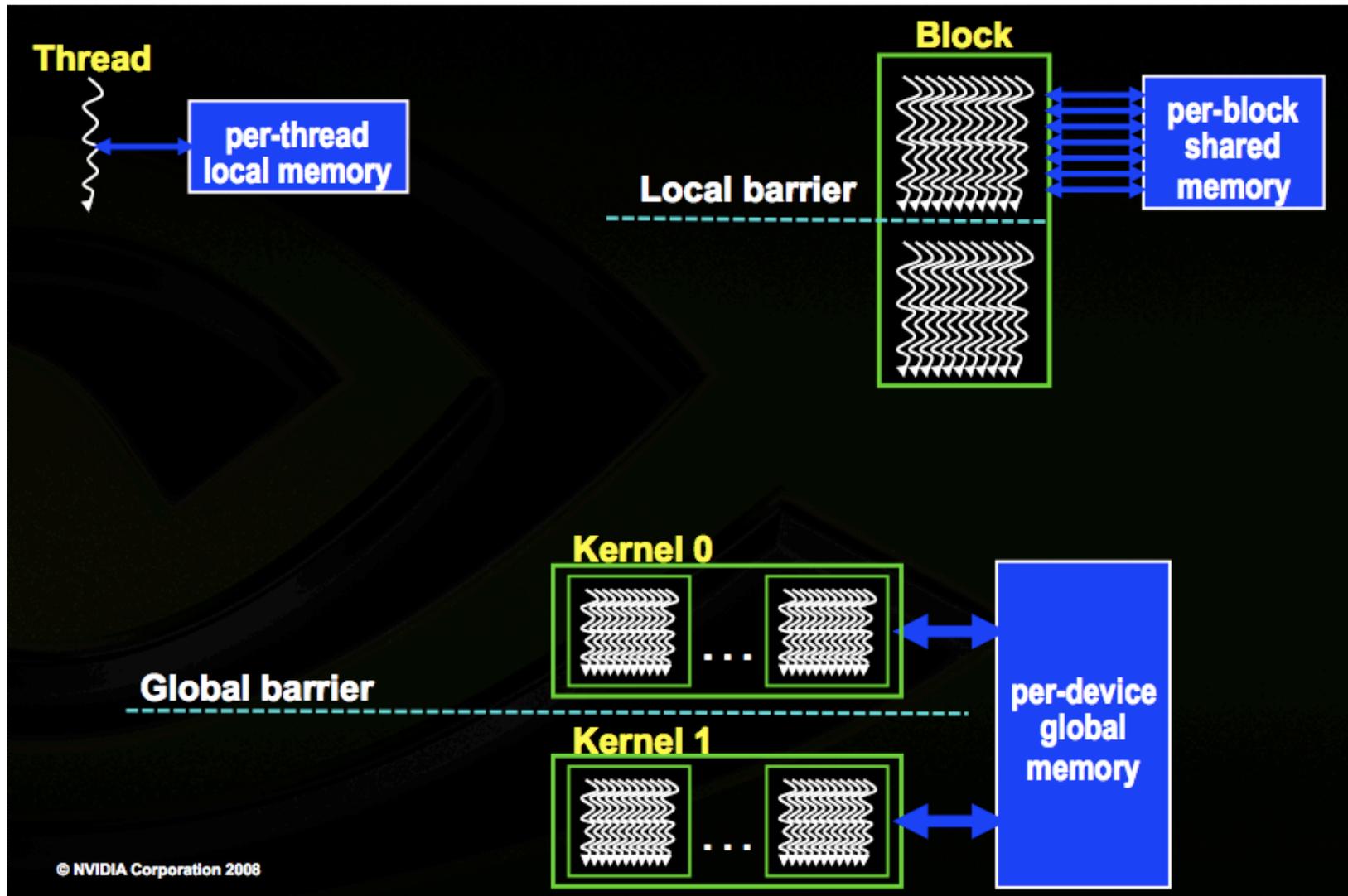
Assign **spins** to threads and **sublattices** to blocks

Since a **block** is assigned to a given **multiprocessor** one is done with **local data sharing** and **synchronization**

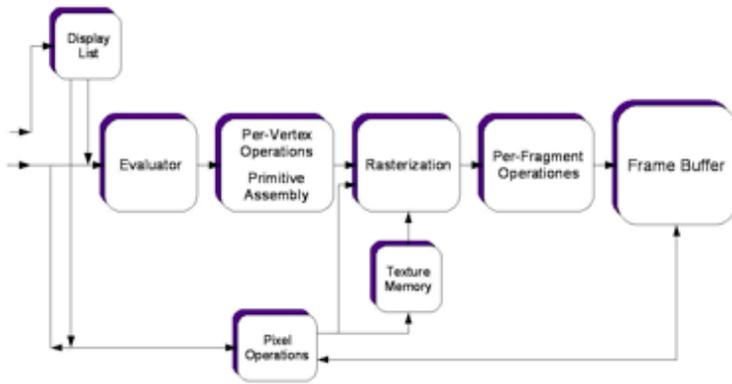
Resources are finite and blocks are sliced into **warps**

## The typical CUDA solution (II)

In general for any given (not only lattice!) problem, we can better understand the issue of data-sharing and synchronization by inspecting nVIDIA picture for that (we can now think for example of a MD problem)

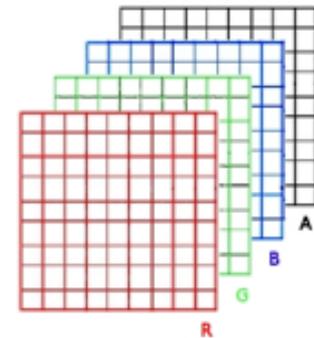


## Legacy GPGPU: talk to GPU as if you were drawing



In the end, why are GPU efficient? Because computer graphic needs a lot of work! Efficiency is nowadays obtained by a **HW graphic pipeline**.

There is a lot of work involved in getting from a 3d image to a 2d bitmap. Roughly speaking, in the end one needs a bunch of bits on a display and that's why basic datatype are **textures** (4 components for colors)



In the **OpenGL** environment one can make use of the **GLSL shading language**

a) a kernel is “enabled” to enter the graphic pipeline

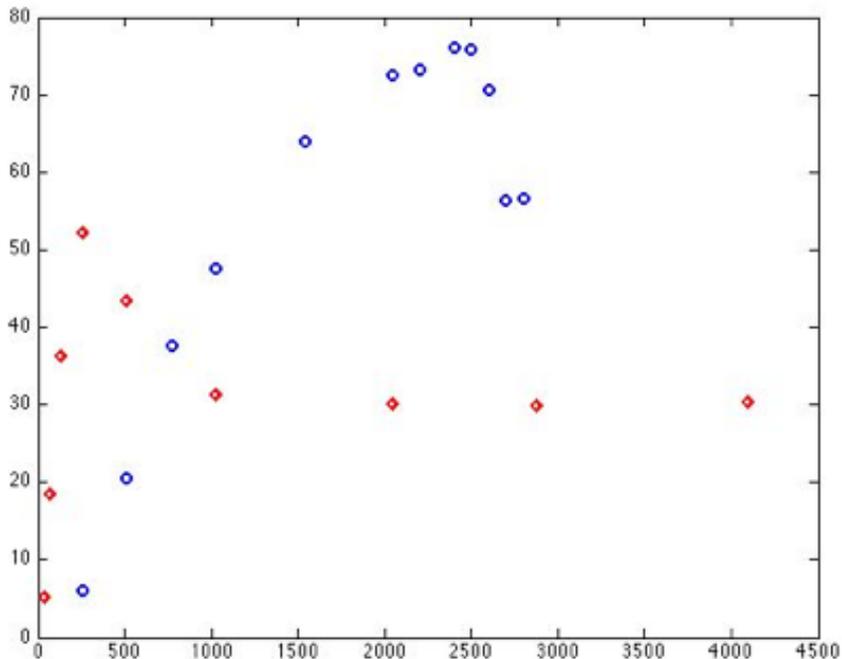
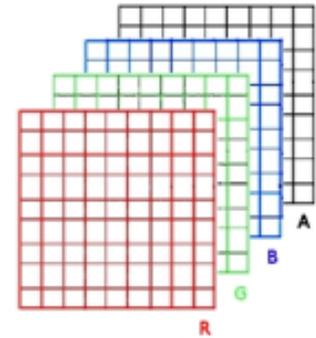
b) input means **binding textures to texture units**, output means **binding target texture to a FBO**

c) one pipeline stage is input for the following: **RW restrictions! PING PONG**

# Theoretical Physics in OpenGL...

Texels can be your spins and **texels** make a texture like **spins** make a lattice.

An **RGBA** texture accomodate 4 **replicas** of a lattice and **nn** (which are 4 in 2d) can be mapped to a texture as well.



Efficiency is not at all bad!

**x-axis** is **lattice size**, **y-axis** is **gain** with respect to a given serial code.

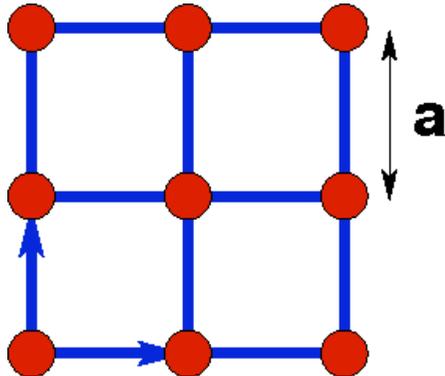
Blue point are **OpenGL** simulations

Red point **CUDA** simulations

## What do we learn in general from QCD? (I)

The spin example was made of not so many degrees of freedom... A typical problem in LQCD is the application of the **Wilson-Dirac operator**

$$\psi'_{\alpha i}(x) = \sum_{\mu=1}^4 \left\{ U_{\mu}^{ij}(x) (1 + \gamma_{\mu}^{\alpha\beta}) \psi_{\beta j}(x + \hat{\mu}) + U_{\mu}^{\dagger ij}(x - \hat{\mu}) (1 - \gamma_{\mu}^{\alpha\beta}) \psi_{\beta j}(x - \hat{\mu}) \right\}$$



- $U_{\mu}^{ij}(x)$  3x3 complex matrices, residing on **links**
- $\gamma_{\mu}^{\alpha\beta}$  4x4 complex matrices, sparse (4 complex)
- $\psi_{\alpha i}(x)$  4x3 complex (spin-color), residing on **sites**

All together, **1320 FP** on (9x12+8x9 complex) **360 FP words per site.**

## What do we learn in general from QCD? (II)

LQCD is a good place to point out a couple of strategies often useful in our problems

- We have to rely on a **HUGE Flops/Bandwidth ratio**, so a typical trick is to get slimmer data trading data for computations

12 number parameterization (Egri *et al*)

$$\begin{pmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{pmatrix} \longrightarrow \begin{pmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{pmatrix} \quad \mathbf{c} = (\mathbf{a} \times \mathbf{b})^*$$

Bytes 1440 --> 1152

Flops += 384

- SP/DP ... **precision** is an issue! GPU slow down quite a lot

**MULTIPRECISION** schemes ...

# a short Summary

- Only prototypes computations presented, to set up a picture ...
- ... so first of all we add: not only lattice and non-lattice; also completely different problems (**Feynman graphs!**)
- Mainly very efficient **number-crunching accelerators**
- Notice that we did not refer to scaling to “many-GPU”
- World is not finished with **CUDA** (AMD **Stream**; **OpenCL**; **Larrabee** is coming!). But also **OpenGL** is probably not dead...