

What cosmology can tell us about neutrinos

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Outline

- Measuring neutrinos with cosmology:
 - Neutrino thermal history
 - Observables
 - Constraints
- Future: constraints and (perhaps) detection
- Conclusions

Timeline

Temperature	Process and Observables	ν Constraints
$T_\gamma \sim 1 \text{ MeV} (z \sim 10^8)$	ν decoupling	
$T_\gamma \sim 0.8 \text{ MeV} (z \sim 10^8)$	BBN	Flavour, Number
$T_\gamma \sim 1 \text{ eV} (z \sim 1100)$	CMB	Number, (Mass)
$T_\nu \sim m_\nu / 3 (z \sim 1890 * m_\nu / \text{eV})$	ν nr transition	
$T_\gamma \sim 0.2 \text{ meV} (z \sim 0)$	LSS	Mass, (Number)

What Cosmology cannot tell us:

- Mixing angles
- Phases
- Dirac vs Majorana
- Hierarchy ...

Neutrino decoupling

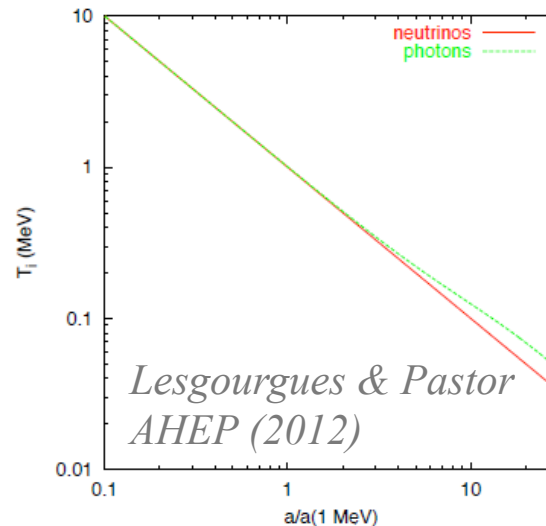
In the primordial Universe weak interactions keep neutrinos in equilibrium with the heat bath.

$$\Gamma \sim G_F^2 T^5 < H$$

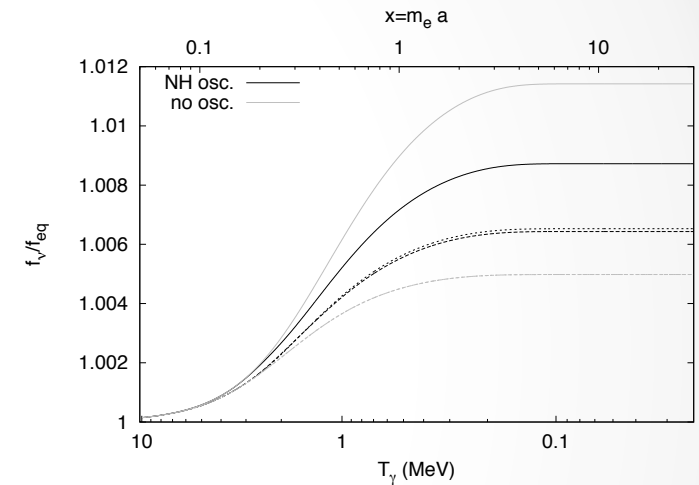
$$T_{\nu, \text{dec}} \sim 1 \text{ MeV} \rightarrow \text{HDM}$$

$$e^+e^- \rightarrow \gamma\gamma$$

$$T_\nu / T_\gamma = (4/11)^{1/3}$$



de Salas & Pastor, JCAP (2016)



$$\rho_{\text{rad}} = \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

N_{eff} Effective number of relativistic degrees of freedom

❖ Other relativistic relics can contribute to N_{eff}

❖ This equation holds after decoupling and as long as all neutrinos are relativistic

❖ $N_{\text{eff}}^{\text{SM}} = 3.045$ *de Salas & Pastor, JCAP (2016)*

Neutrino number and BBN

Shortly after neutrino decoupling the weak interactions that kept neutrons and protons in statistical equilibrium freeze out.

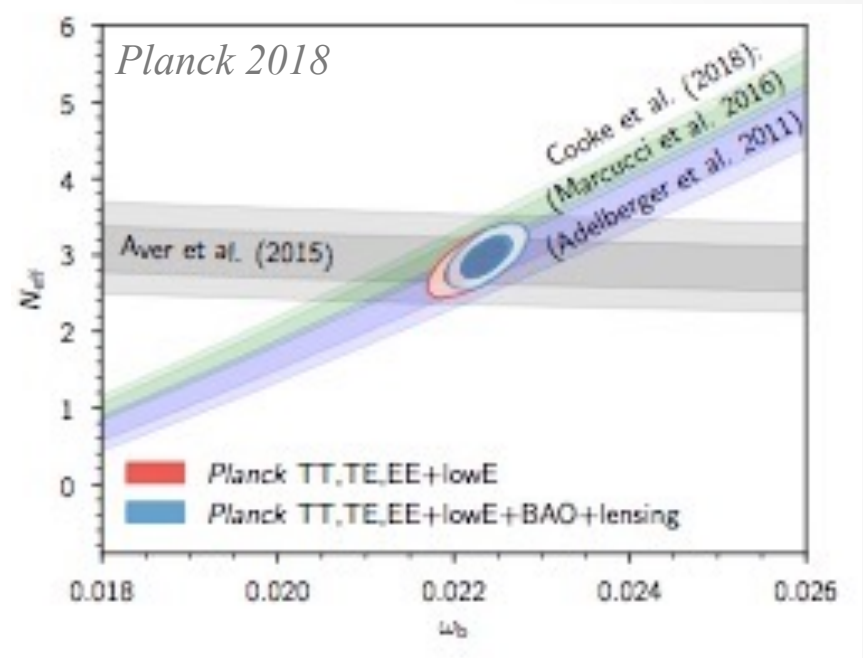
$$H = \Gamma|_{T=T_{\text{freeze}}} \quad T_{\text{freeze}} \approx 0.6 g_*^{1/6} \text{ MeV}$$

$$\left. \frac{n_n}{n_p} \right|_{T=T_{\text{freeze}}} \approx \exp\left(-\frac{(m_n - m_p)}{T_{\text{freeze}}}\right) \approx \frac{1}{6}$$

$$Y_p \approx \left. \frac{2n_n / n_p}{1 + n_n / n_p} \right|_{T \approx 0.2 \text{ MeV}} \propto f(g_*, \Omega_b h^2)$$

$$g_* \rightarrow g_* + \frac{7}{4} \Delta N_{\text{eff}}$$

$$\left| Y_p^{\text{theo}} - Y_p^{\text{obs}} \right|_{\Omega_b} \rightarrow \Delta N_{\text{eff}} \big|_{\Omega_b}$$

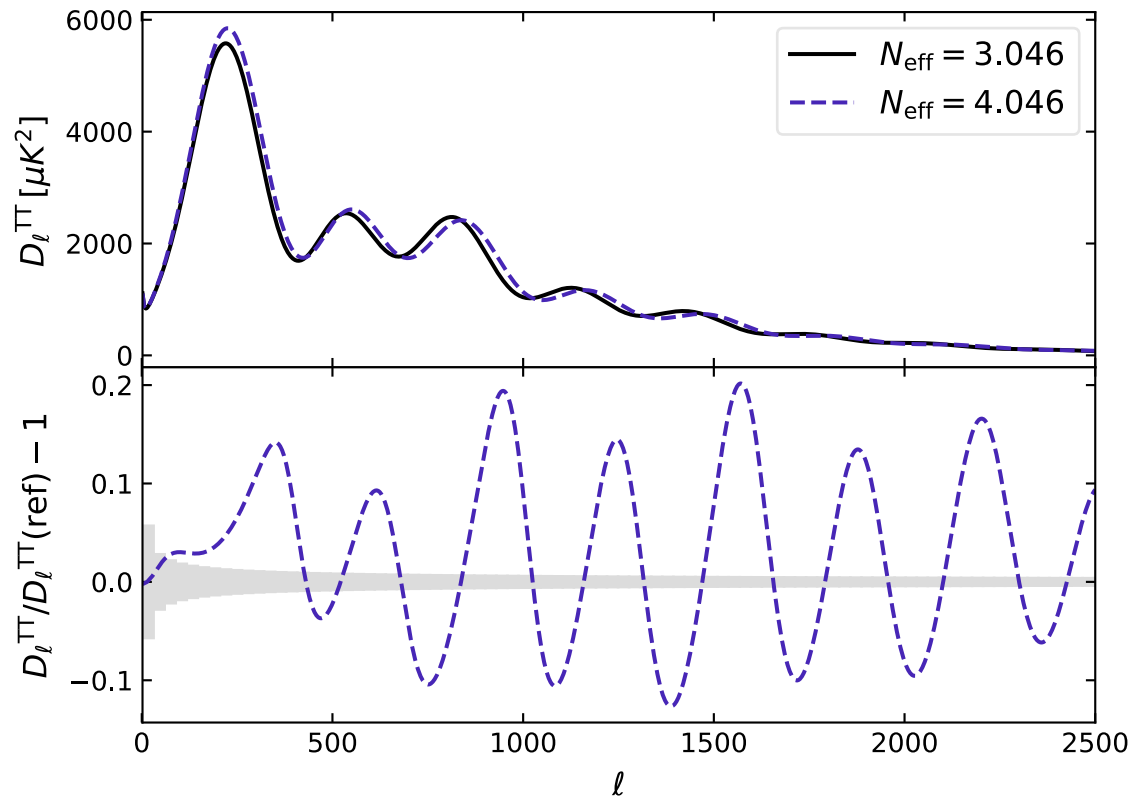


Planck TT,TE,EE + lowE + He [Aver+ JCAP (2015)] + D [Cooke+ ApJ (2018)]

$N_{\text{eff}} = 2.89 \pm 0.29$ (95% c.l.) experimental rate Adelberger+ Rev. Mod. Phys (2011)

$N_{\text{eff}} = 3.05 \pm 0.27$ (95% c.l.) theoretical rate Marcucci+ PRL (2016)

Neutrino number and CMB



- Early ISW

$$\dot{\phi} < 0$$

- Shift of the peak position

$$r_s = \int_0^{t_*} c_s dt / a = \int_0^{a_*} \frac{c_s}{a^2} \frac{da}{H} \propto \frac{1}{H}$$

- Silk damping

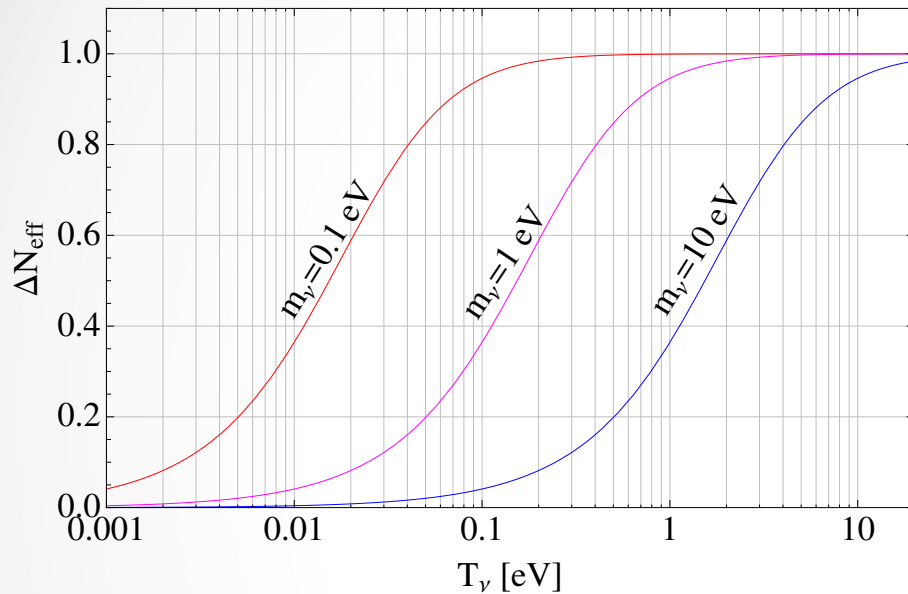
$$\exp\left[-(2r_d / \lambda_d)^2\right]$$

Planck 2018 TT + lowE: $N_{\text{eff}} = 3.00^{+0.57}_{-0.53}$ (95%cl)

Planck 2018 TTTEEE + lowE: $N_{\text{eff}} = 2.92^{+0.36}_{-0.37}$ (95%cl)

Neutrino number and CMB

Jacques+ PRD (2013)



$$\Delta N_{\text{eff}} = \frac{\rho_{\nu, \text{extra}}}{\rho_{\nu, m=0}^{\text{thermal}}} \left(\frac{P_{\nu, \text{extra}} / \rho_{\nu, \text{extra}}}{1/3} \right)$$

$$\rho = \frac{g}{2\pi^2} \int dp E p^2 f(p)$$

$$P = \frac{g}{2\pi^2} \int dp \frac{P^4}{3E} f(p)$$

$$T_{\nu} |_{\gamma, \text{dec}} = 0.7 \text{ eV}$$

$$\text{CMB: } N_{\text{eff}} = 2.92^{+0.36}_{-0.37} \text{ (95\%cl)}$$

Is a 10 eV “extra” neutrino consistent with CMB bounds? NO, it is not!

Neutrino mass and CMB

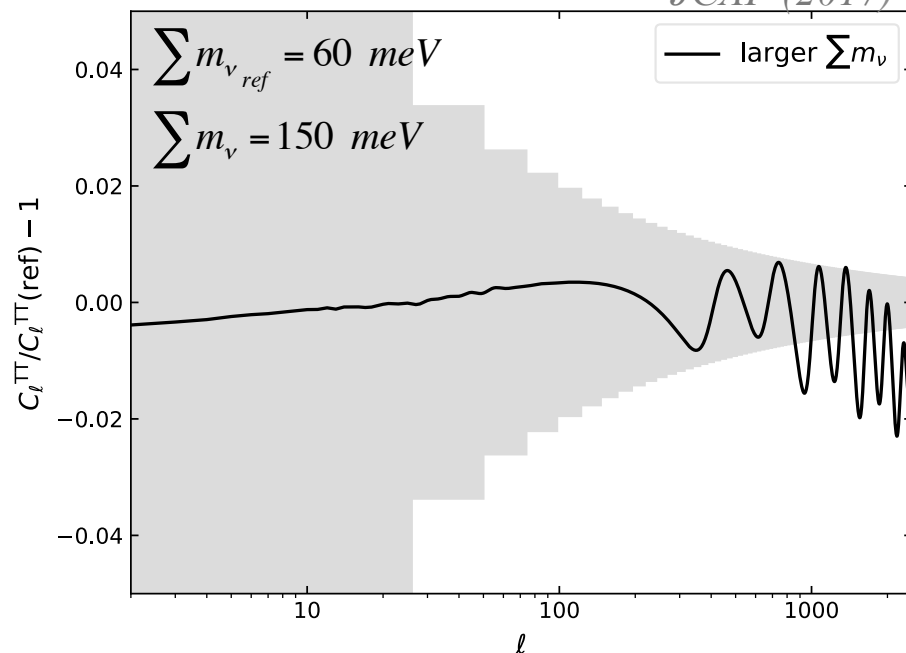
MA, Brinckmann, Lesgourgues, Poulin
JCAP (2017)

$$\Omega_\nu h^2 = \frac{\rho_\nu}{\rho_c} = \frac{\sum m_\nu}{93.14 \text{ eV}}$$

Note: $m_1 = m_2 = m_3$

$m_1, \Delta m_{\text{sun}}^2, \Delta m_{\text{atm}}^2 \rightarrow 0.1\% \Delta P(k)/P(k)$

- Background effects ($z_{\text{eq}}, d_A, z_\Lambda$)
- Perturbation effects (early ISW)



Neutrino mass and CMB

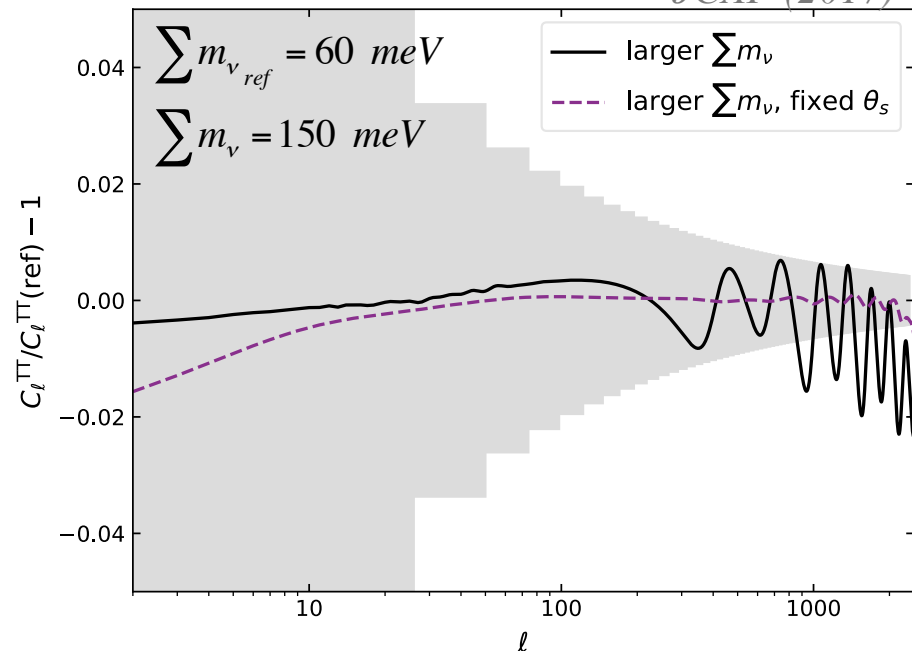
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→ Correlation between M_ν and H_0 (TTTEEE) and also ω_{cdm} (TTTEEE+lensing)

Planck 2018 TT + lowE: $\Sigma m_\nu < 0.54 \text{ eV}$ (95%cl)

Planck 2018 TTTEEE + lowE: $\Sigma m_\nu < 0.26 \text{ eV}$ (95%cl)

→ CMB data alone (even future cosmic variance limited CMB surveys) cannot measure M_ν

Neutrino non-relativistic transition

When neutrinos become non-relativistic

$$z_{\text{nr}} \approx 1890 (m_{\nu,i}/1\text{eV}),$$

they travel through the Universe with a thermal velocity

$$v_{\text{th},i} = \langle p \rangle / m_{\nu,i} \approx 3T_{\nu,i} / m_{\nu,i} \approx 150 (1+z) (1\text{eV}/m_{\nu,i}) \text{ km/s}$$

Neutrinos cannot be confined below the characteristic free-streaming scale defined by $V_{\text{th},i}$.

$$k_{\text{nr},i}(z) \equiv \frac{H(z_{\text{nr},i})}{(1+z_{\text{nr},i})} = 0.0145 \text{ Mpc}^{-1} \left(\frac{m_{\nu,i}}{1\text{eV}} \right)^{1/2} \Omega_m^{1/2} h$$

Neutrino mass and LSS

$$P(k, z) = \left\langle \left| \delta_m(k, z) \right|^2 \right\rangle$$

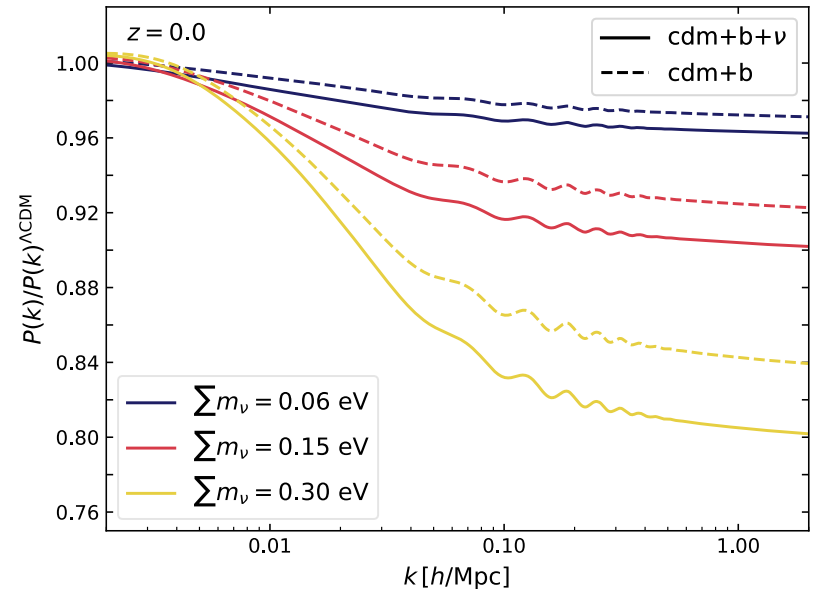
$$\delta_m = \frac{\delta \rho_m}{\bar{\rho}_m}$$

$$\frac{k^2}{a^2} \phi = -4\pi G(\delta \rho_m) \quad (\delta \rho_v \ll \delta \rho_{cdm})$$

$$H^2 = \frac{8\pi G}{3} (\rho_\gamma + \rho_b + \rho_{cdm} + \rho_v + \rho_\Lambda)$$

$$\delta_{cdm} \propto a$$

$$\delta_{cdm} \propto a^{1-3/5 f_v}$$



$$\frac{P_c(k)^v}{P_c(k)^{\Lambda CDM}} \approx 1 - 6f_v$$

$$\frac{P_m(k)^v}{P_m(k)^{\Lambda CDM}} \approx 1 - 8f_v$$

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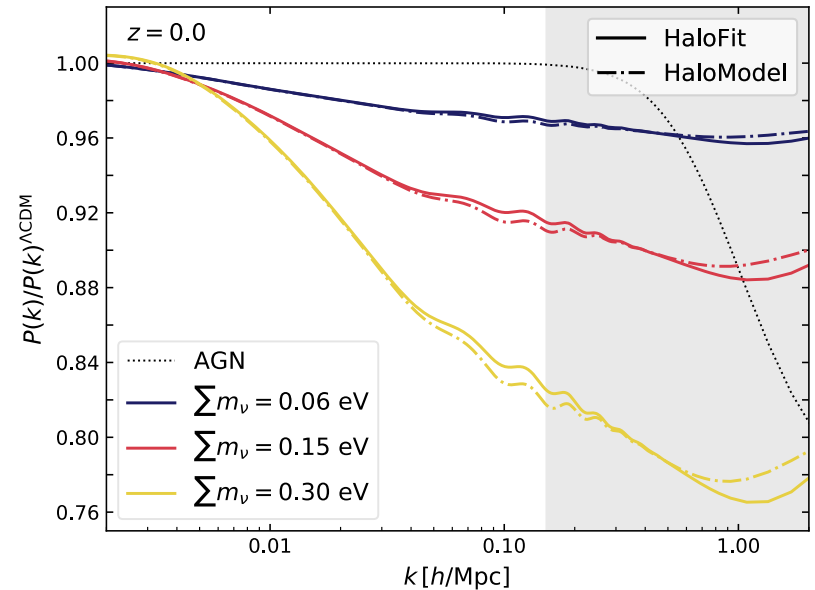
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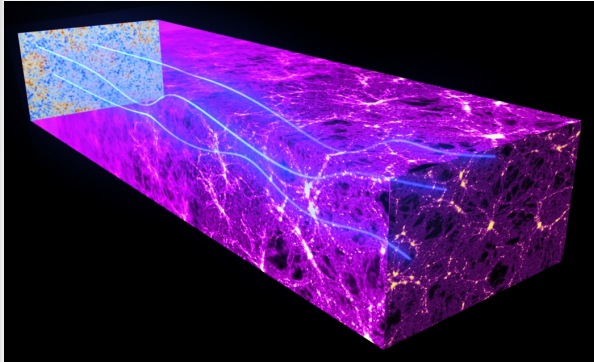


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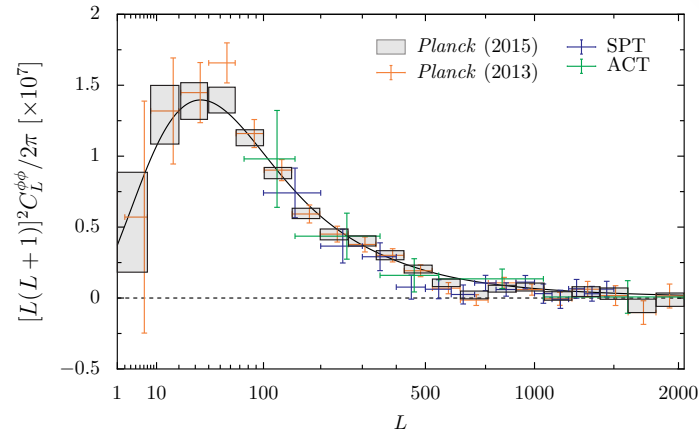
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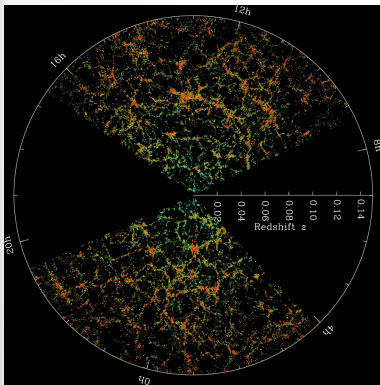
CMB



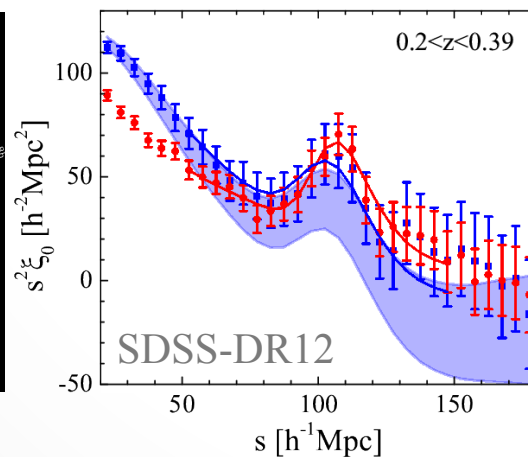
Lensing



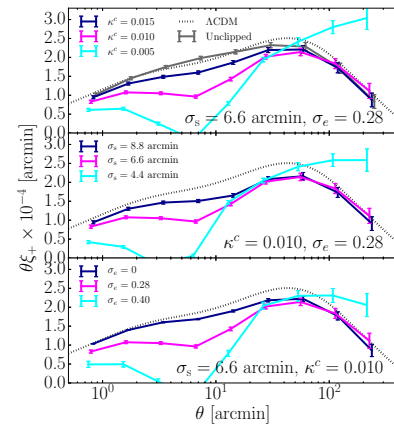
Galaxy surveys



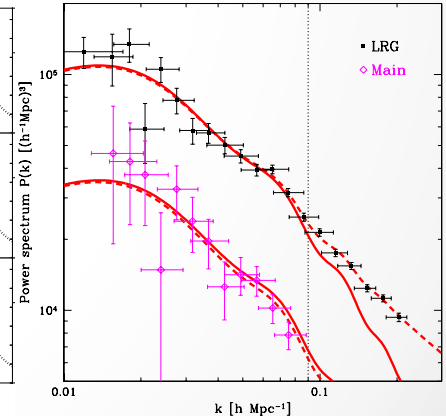
BAO



Cosmic shear



Galaxy clustering



...and more ... (e.g., RSD)

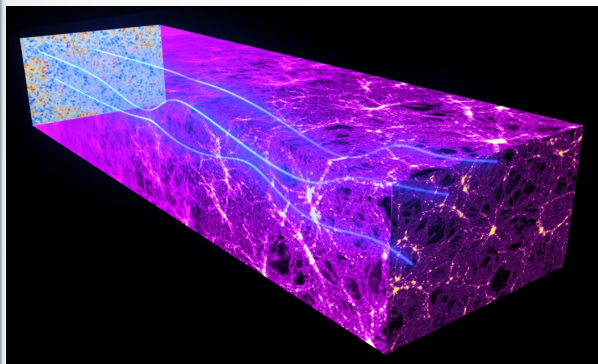
KiDS

Giblin+ MNRAS(2018)

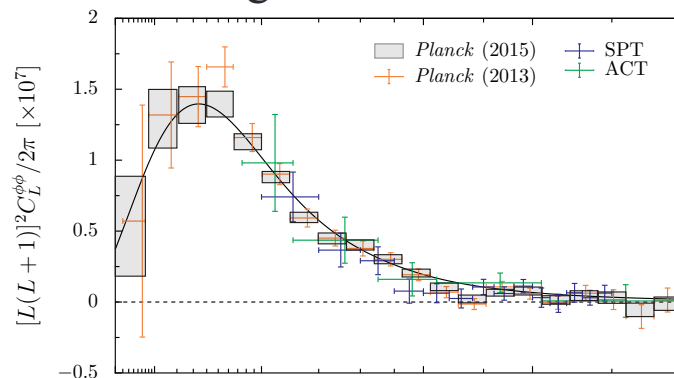
Tegmark+ PRD(2006)

Neutrino mass and LSS

CMB

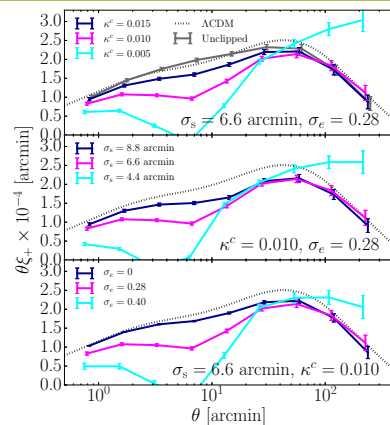
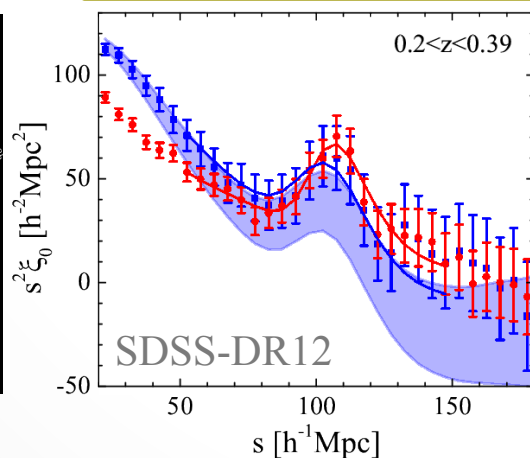
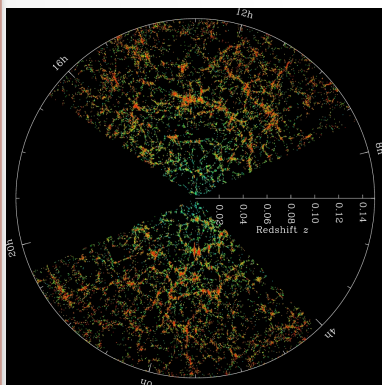


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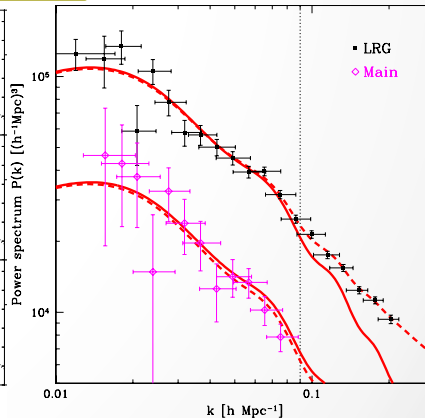


Planck 2018 TT,TE,EE+lowE+lensing+BAO:
 $\Sigma m_\nu < 0.12$ eV (95%cl)

Galaxy surveys



galaxy clustering



...and more ... (e.g., RSD)

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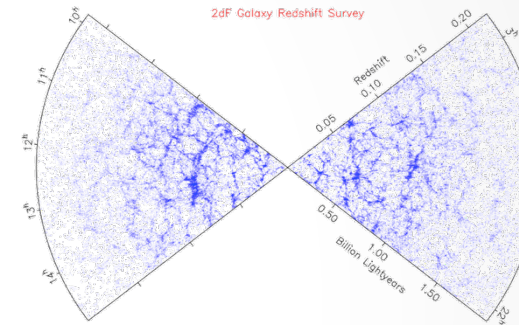
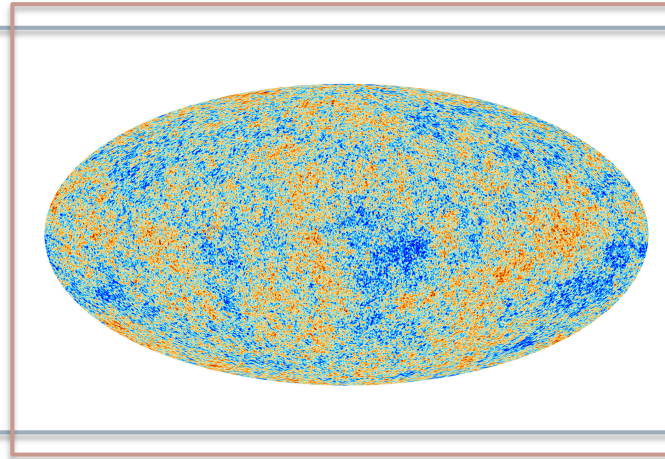
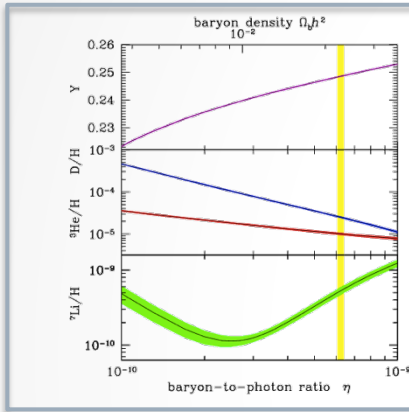
Tegmark+ PRD(2006)

Where we stand

$z \sim 10^8$ ($T \sim 1$ MeV)

$z \sim 1100$ ($T \sim 1$ eV)

$z < 3$



N_{eff} & flavour

N_{eff} & (Σm_ν)

(N_{eff}) & Σm_ν

$$N_{\text{eff}} = 2.92^{+0.36}_{-0.37} \text{ (95\%cl)}$$

TT,TE,EE + lowE

$$\Sigma m_\nu < 0.12 \text{ eV (95\%cl)}$$

... + lensing + BAO

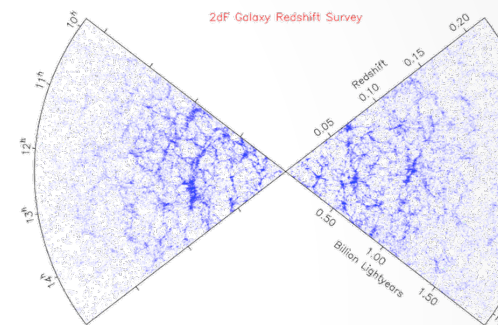
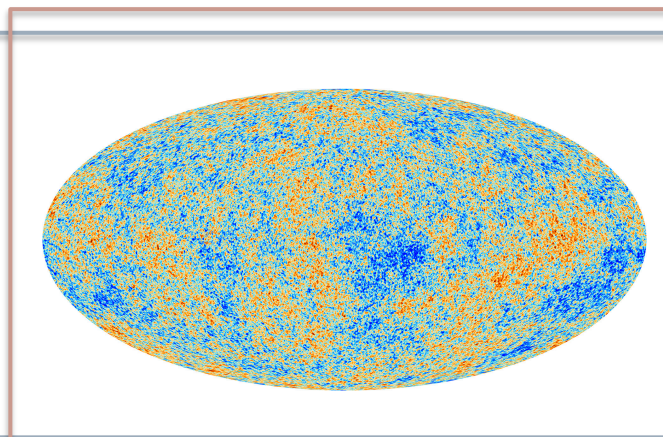
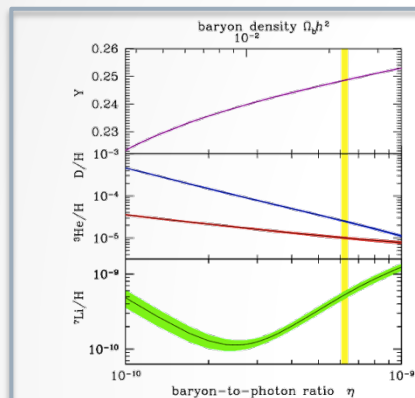
Planck 2018

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Planck 2018

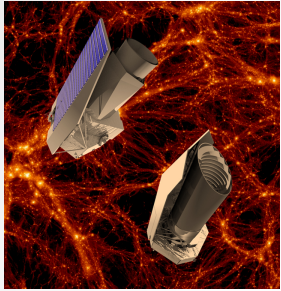
eV ν_s are:

too many

and

too heavy

Neutrino mass: future sensitivity



Euclid (2021)
1% accuracy:
galaxy clustering,
cosmic shear



SKA
21cm survey

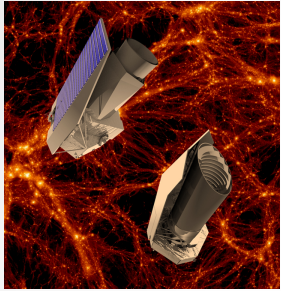
Sprengr, MA, Brinckmann, Clesse, Lesgourgues, JCAP (2019) MCMC forecast

Fiducial = 0.06 eV equally distributed among 3 neutrino species

Conservative vs. Optimistic uncertainty on small scales

	Planck+Euclid	Planck+Euclid+SKA1-IM
Conservative	24 meV	18 meV
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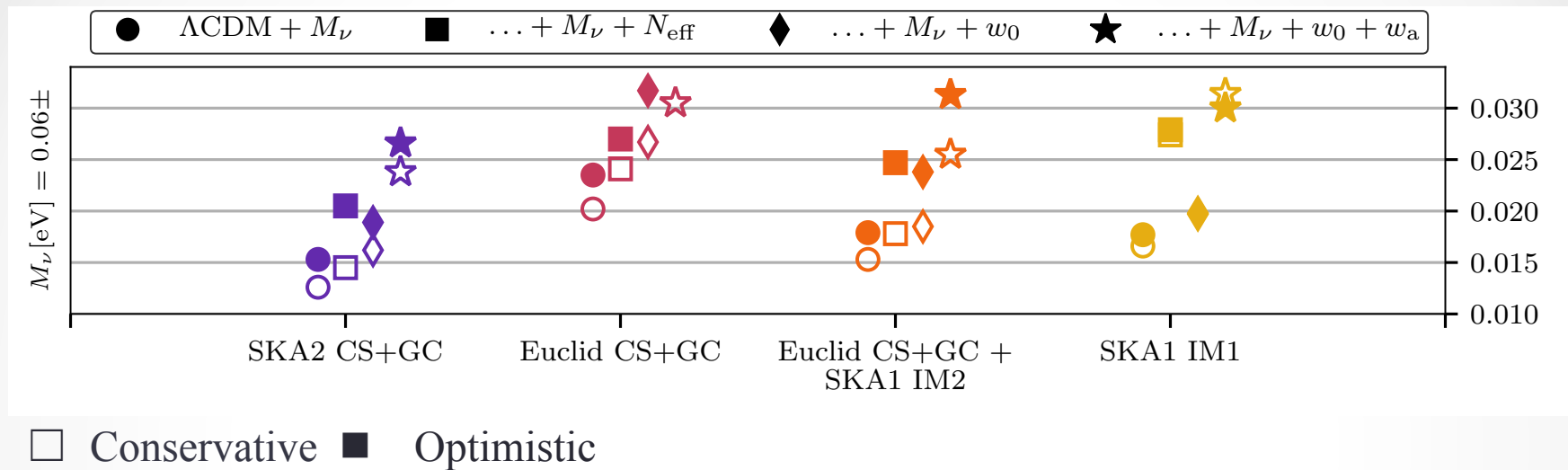
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Note: IO indirectly disfavoured

Neutrino mass: model dependence

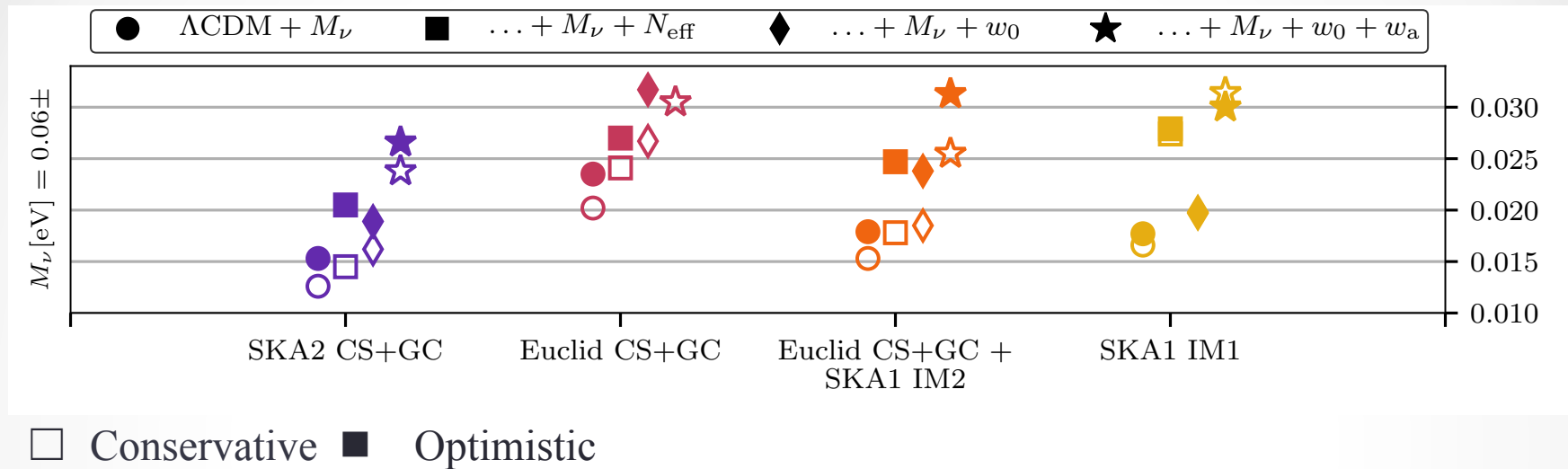


Planck+Euclid	N_{eff}	w_0 (fixed w_a)	w_0 (+ w_a)	w_a
Conservative	0.065	0.0154	0.0285	0.099
Optimistic	0.046	0.0121	0.0214	0.071

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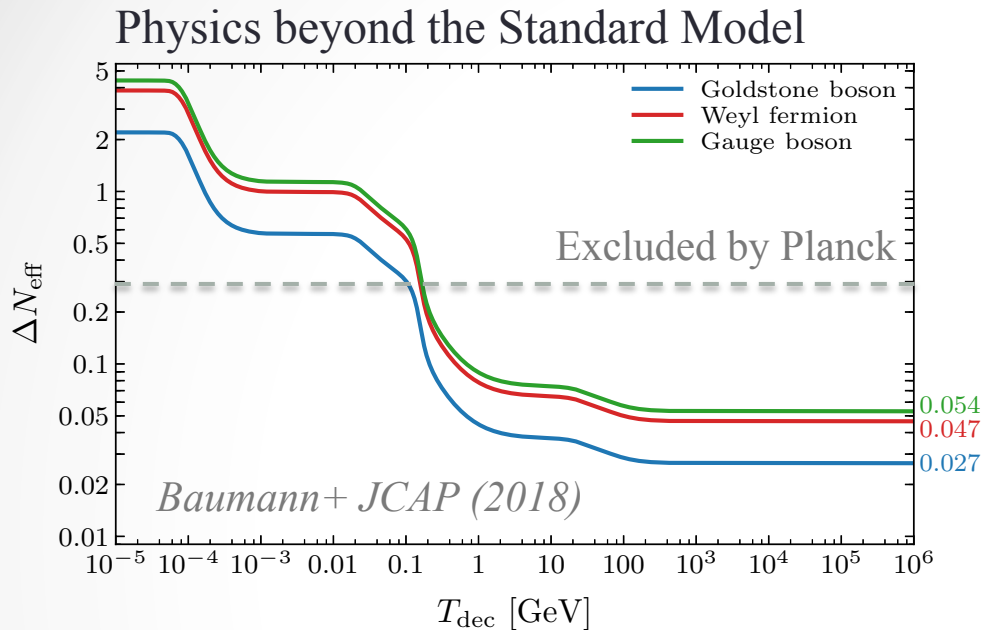


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Brinckmann, Hooper, MA, Lesgourgues, Sprenger, JCAP (2019)

N_{eff}: future sensitivity



$$\Delta N_{eff} = \frac{\rho_{v,extra}}{\rho_{v,m=0}^{thermal}} \left(\frac{P_{v,extra} / \rho_{v,extra}}{1/3} \right)$$

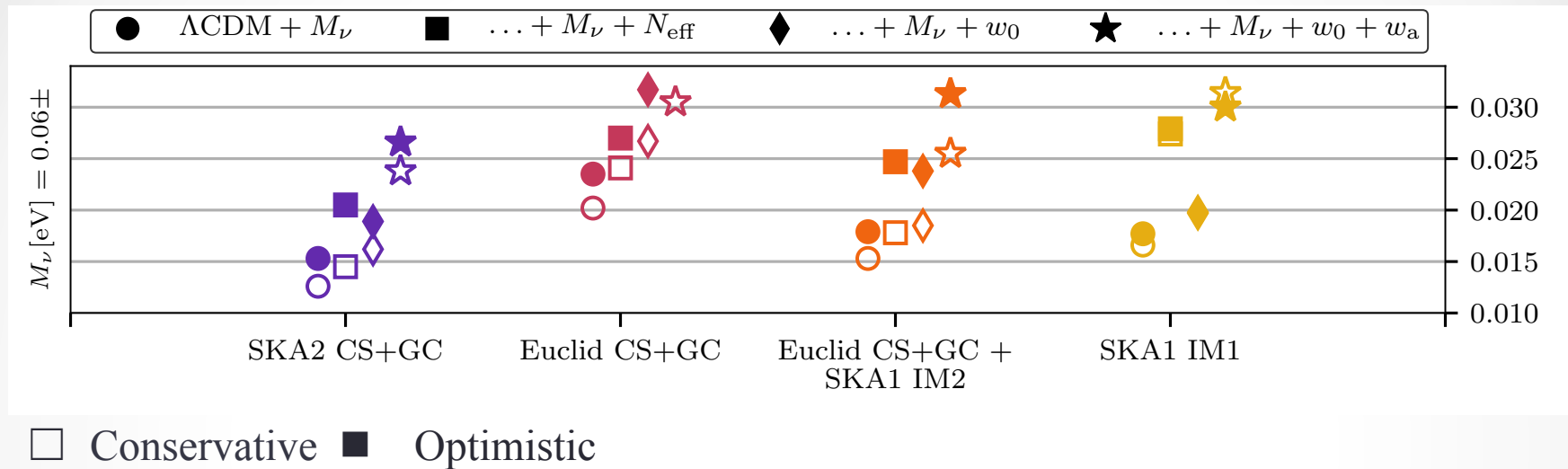
$$= \left(\frac{T_{v,extra}}{T_{v,m=0}^{thermal}} \right)^4 \left(\frac{P_{v,extra} / \rho_{v,extra}}{1/3} \right)$$

} Future CMB + Euclid + SKA

Models that can be excluded:

- Neutrino Non-Standard interactions (solution of the H_0 tension)
- Non-Abelian Dark Matter (solution of the σ_8 tension)
- Self-Interacting Dark Matter (solution of the small scale crisis)
- ...

Neutrino mass: model dependence



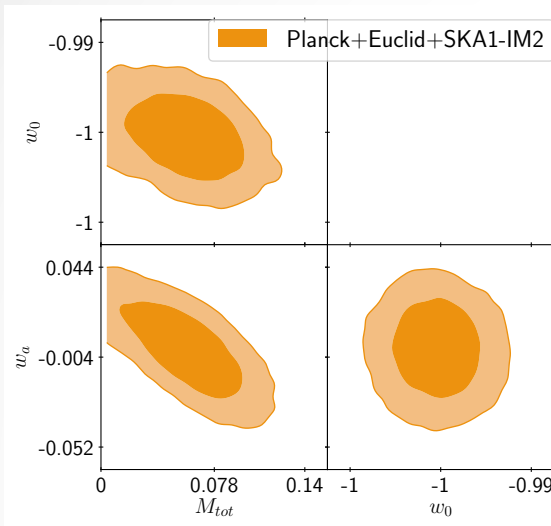
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Brinckmann, Hooper, MA, Lesgourgues, Sprenger, JCAP (2019)

CLP: $w(a) = w_0 + w_a(1-a)$

Neutrino mass and Dark Energy



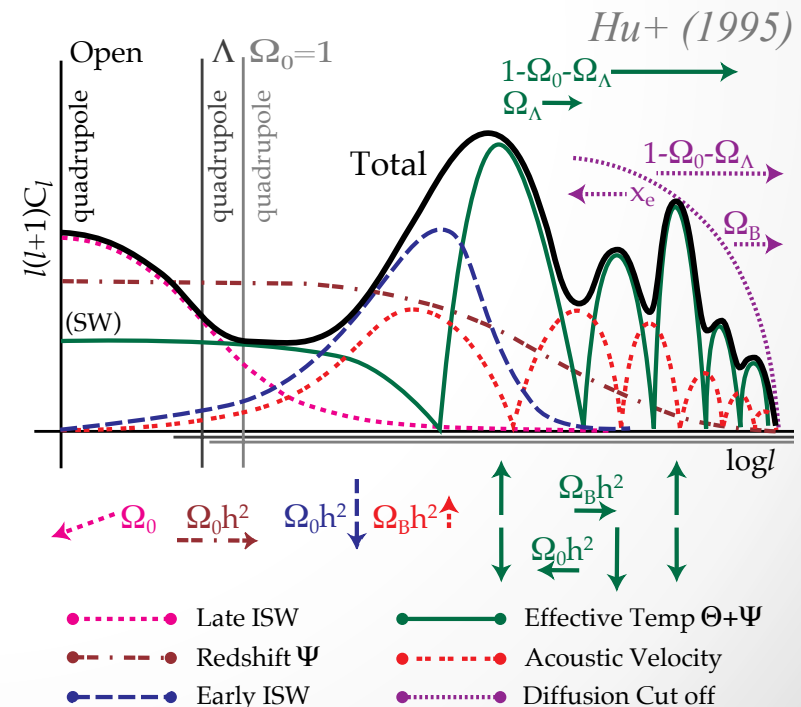
How to break the degeneracy?
ISW-galaxy clustering cross-correlation

(In alphabetical order) Maria Archidiacono, Alessandro Gruppuso, Massimiliano Lattanzi, Nicoletta Mauri, Marina Migliaccio, Diego Molinari, Paolo Natoli, Luca Pagano, Laura Patrizii, Gabriele Sirri, Matteo Tenti, Alessandro Renzi, and the Euclid CMBXC SWG

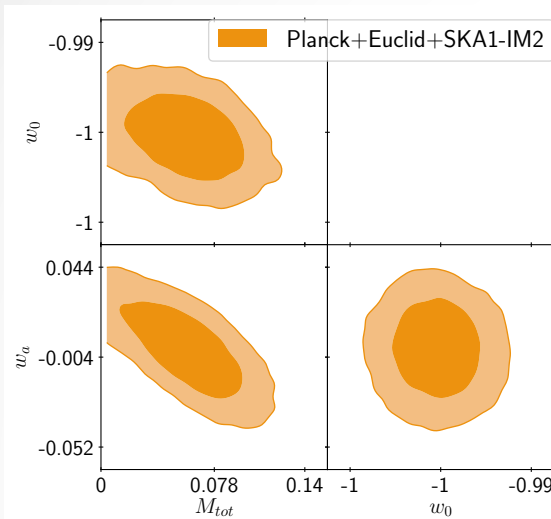
During Λ (or, more in general, DE)
the gravitational potentials ϕ decay
→ Late ISW

vs.

Growth of structure
→ Galaxy clustering



Neutrino mass and Dark Energy



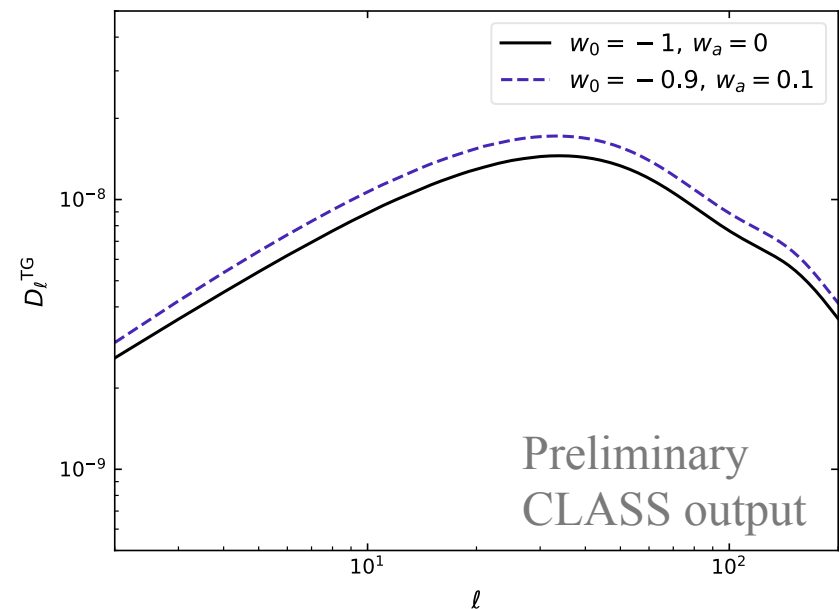
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Conclusions

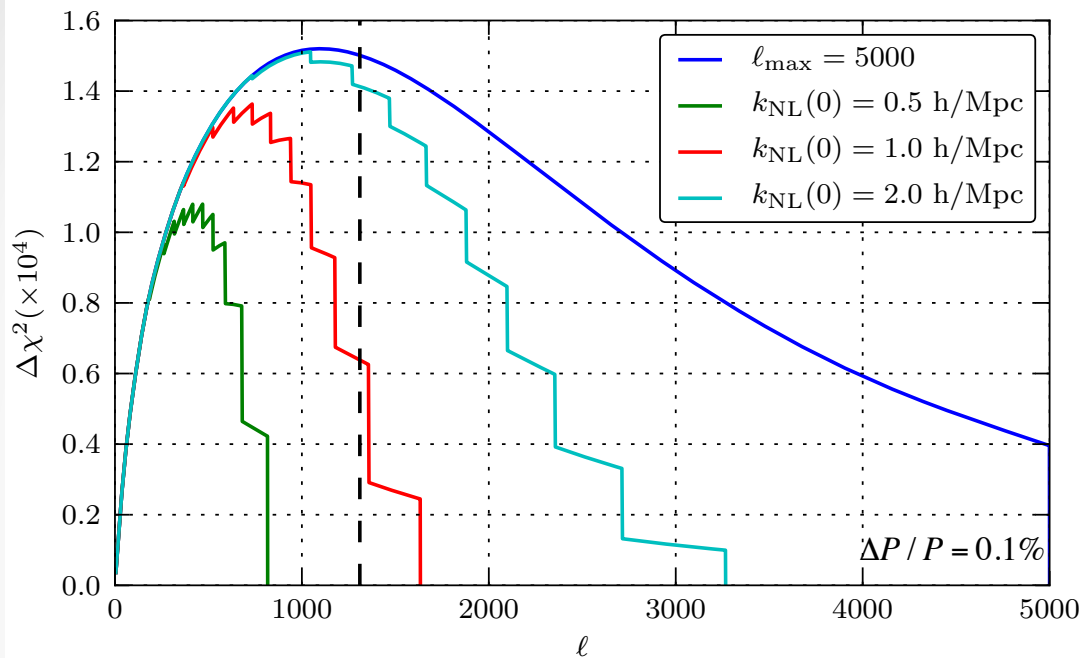
- Cosmology is a powerful tool to constrain neutrino physics, but the results have to be taken with a grain of salt because of model dependence
- Future galaxy and hydrogen surveys will be able to detect the neutrino mass sum in the minimal extension of the Λ CDM
- Ongoing work: ISW-GC Euclid CMBXC
- Complementarity with ground-based experiments (KATRIN $m_\beta < 1.1$ eV)

Conclusions

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“The most exciting phrase to hear in science, the one that heralds new discoveries, is not ‘Eureka!’ but ‘That’s funny ...’” Isaac Asimov

Theoretical uncertainties: CS



Sprenger, MA+ JCAP (2019)

$$k_{nl}(z) \propto k_{nl}(0)(1+z)^{2/(2+n_s)}$$

$$l_{\max}^{zi} = k_{nl}(z) \times \bar{r}_{peak}^{zi}$$

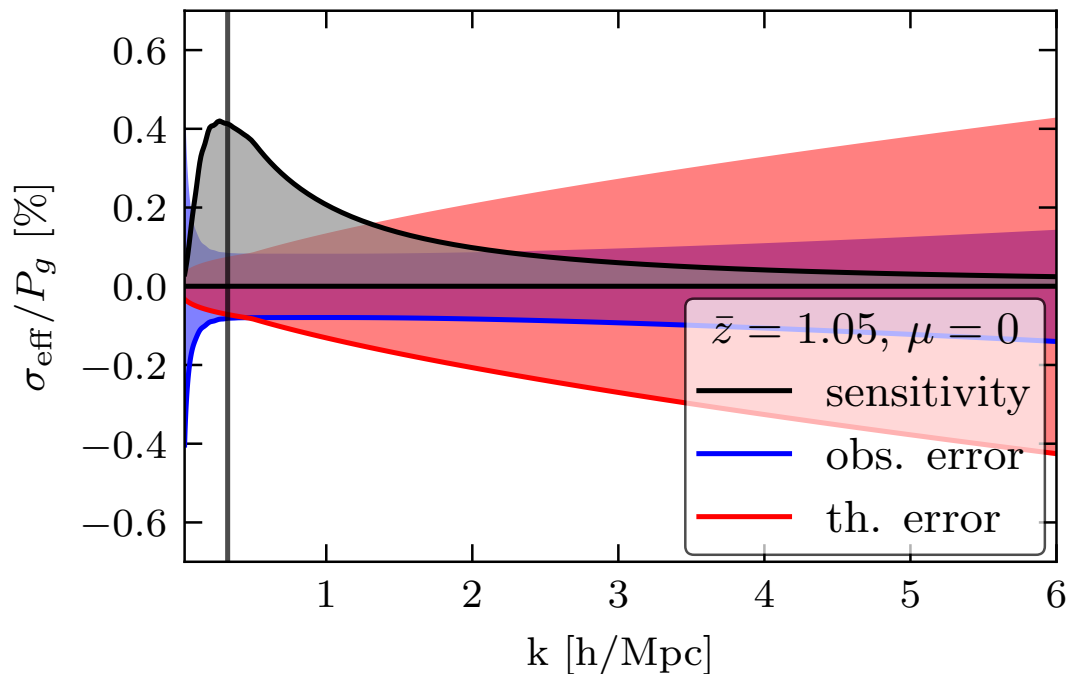
k_{\max}	$100\omega_b$	ω_{cdm}	θ_s	$\ln(10^{10}A_s)$	n_s	τ_{reio}	M_ν [eV]
0.5 h/Mpc	0.77	0.27	0.97	0.94	0.72	0.96	0.50
1.0 h/Mpc	0.76	0.27	0.94	0.95	0.70	0.98	0.41
2.0 h/Mpc	0.76	0.25	0.97	0.94	0.65	0.97	0.36
$\ell_{\max} = 5000$	0.74	0.24	0.94	0.94	0.58	0.96	0.30
Planck only	1.00	1.00	1.00	1.00	1.00	1.00	1.00

Conservative: $k_{nl}(0)=0.5$ h/Mpc

Optimistic: $k_{nl}(0)=2.0$ h/Mpc

	Planck+Euclid-CS
Conservative	43 meV
Optimistic	30 meV

Theoretical uncertainties: GC



Sprenger, MA+ JCAP (2019)

$$\frac{d\chi^2}{dkd\mu} = \left[\frac{\Delta P_g(k, \mu, \bar{z})}{\sigma_{eff}(k, \mu, \bar{z})} \right]^2$$

$$\sigma_{eff}(k, \mu, \bar{z}) = \sigma_{obs}(k, \mu, \bar{z}) \left[k^2 \frac{V_r(\bar{z})}{2(2\pi)^2} \right]^{-1/2}$$

$$\sigma_{eff}(k, \mu, \bar{z}) \propto k^{-2}$$

$$\alpha = \frac{\delta P_g}{P_g} \left\{ \begin{array}{l} 0.33\% \text{ at } k=0.01 \text{ h/Mpc} \\ 1\% \text{ at } k=0.3 \text{ h/Mpc} \\ 10\% \text{ at } k=10 \text{ h/Mpc} \end{array} \right.$$

Conservative: $k_{nl}(0)=0.2 \text{ h/Mpc}$

Optimistic: th. err. & $k_{max}(0)=10 \text{ h/Mpc}$

	Planck+Euclid-GC
Conservative	26 meV
Optimistic	20 meV

Cosmological tensions

$H_0 = (67.4 \pm 0.5) \text{ km/s/Mpc}$ (68% c.l.) (Planck TT,TE,EE+lowE, Λ CDM)

$H_0 = (74.03 \pm 1.42) \text{ km/s/Mpc}$ (68% c.l.) *Riess+ Apj (2019)*

4.4 σ tension

σ_8 tension between Planck and CFHTLenS, KiDS *Hildebrandt+ (2018)*
alleviated by DES *Abbott+ (2018)*

Two possible model extensions each one solving one tension

