

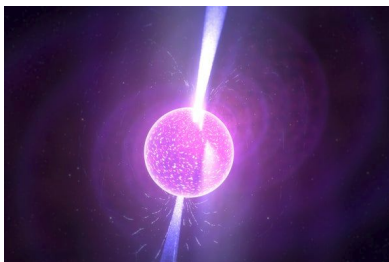
# $K^-$ multi-nucleon absorption processes and kaonic bound state search by AMADEUS

Raffaele Del Grande<sup>1,2\*</sup>

<sup>1</sup> INFN Laboratori Nazionali di Frascati, Frascati, Italy

<sup>2</sup> CENTRO FERMI - Museo Storico della Fisica e Centro Studi e Ricerche "Enrico Fermi", Roma, Italy

*On the behalf of the AMADEUS collaboration*



**Strange Matter Workshop**  
**Strangeness studies in Italy and Japan**

15-17 October 2019

Frascati, Italy

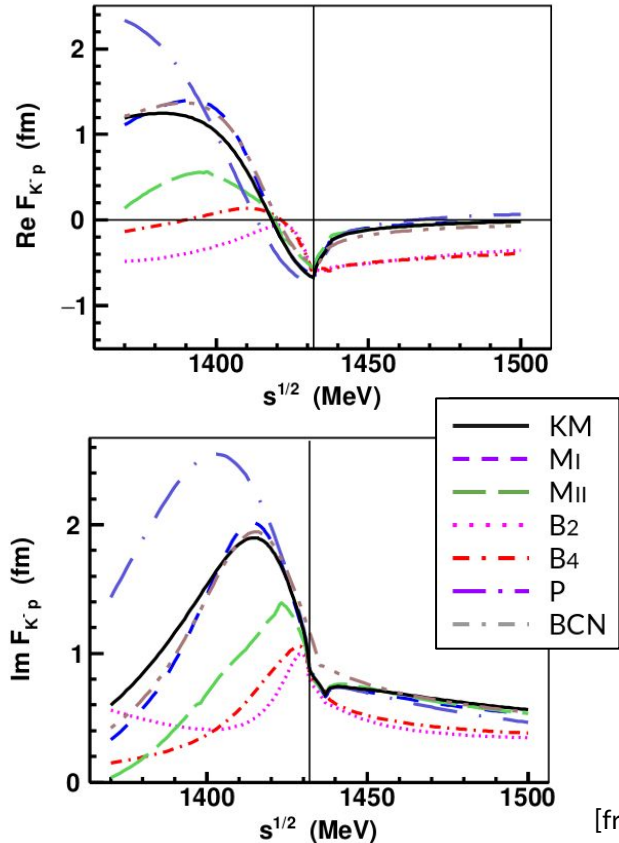
\*[raffaele.delgrande@Inf.infn.it](mailto:raffaele.delgrande@Inf.infn.it)

# Motivation

**AMADEUS** (Antikaonic Matter At DAΦNE: an Experiment with Unravelling Spectroscopy ) investigates **low-energy  $K^-$  absorption in nuclei** with the aim to extract information on:

- $K^-N$  interaction above and below threshold
  - $\Lambda(1405)$  nature
  - kaonic bound states
- $K^-NN$ ,  $K^-NNN$ ,  $K^-NNNN$  (multi-nucleon) interactions
  - essential for the determination of  $K^-$ -nuclei optical potential
- In medium modification of the  $K^-N$  interaction
  - partial restoration of chiral symmetry  $\rightarrow$  hadrons mass origin
  - Equation of State of Neutron Stars
  - modification of  $\Lambda(1405)$  and  $\Sigma(1385)$  properties in nuclear medium

# K<sup>-</sup>p scattering amplitude



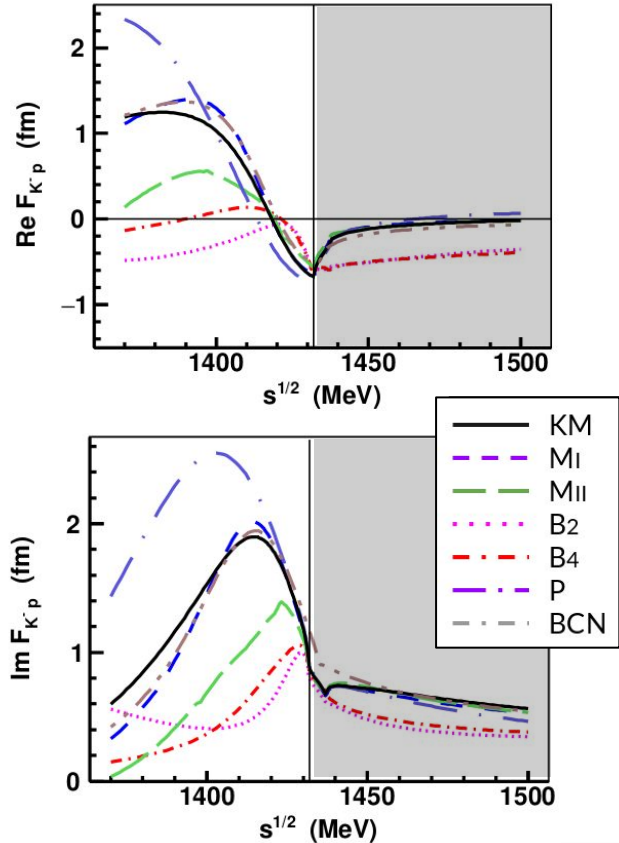
## K<sup>-</sup>p scattering amplitude with Chiral models

- Kyoto-Munich (KM)  
Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98
- Murcia (MI, MII)  
Z. H. Guo, J. A. Oller, Phys. Rev. C 87 (2013) 035202
- Bonn (B2, B4)  
M. Mai, U.-G. Meißner - Eur. Phys. J. A 51 (2015) 30
- Prague (P)  
A. C., J. Smejkal, Nucl. Phys. A 881 (2012) 115
- Barcelona (BCN)  
A. Feijoo, V. Magas, À. Ramos, Phys. Rev. C 99 (2019) 035211

**Large discrepancies in the region below threshold!**

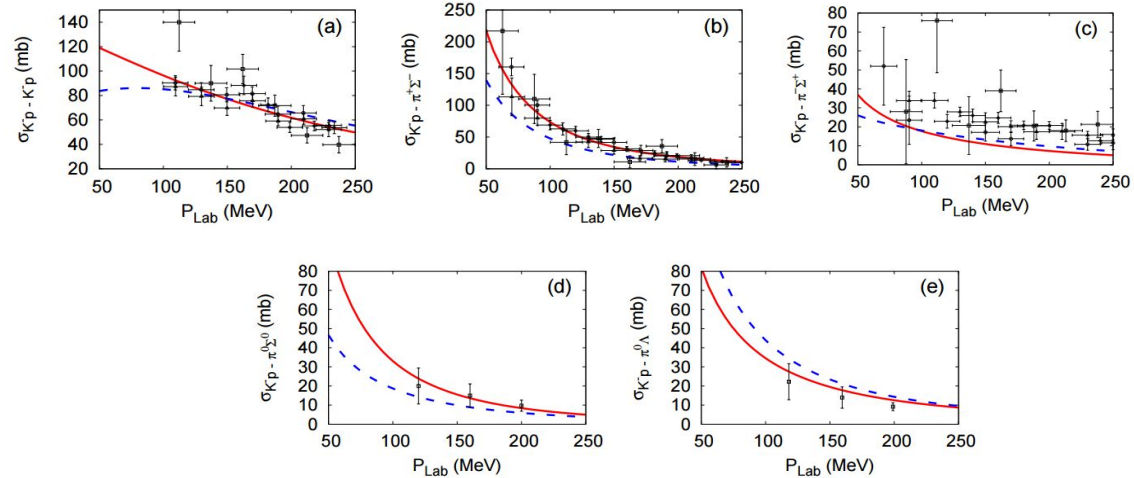
[from A. Cieply talk at MENU2019 conference]

# Experimental constraints above threshold

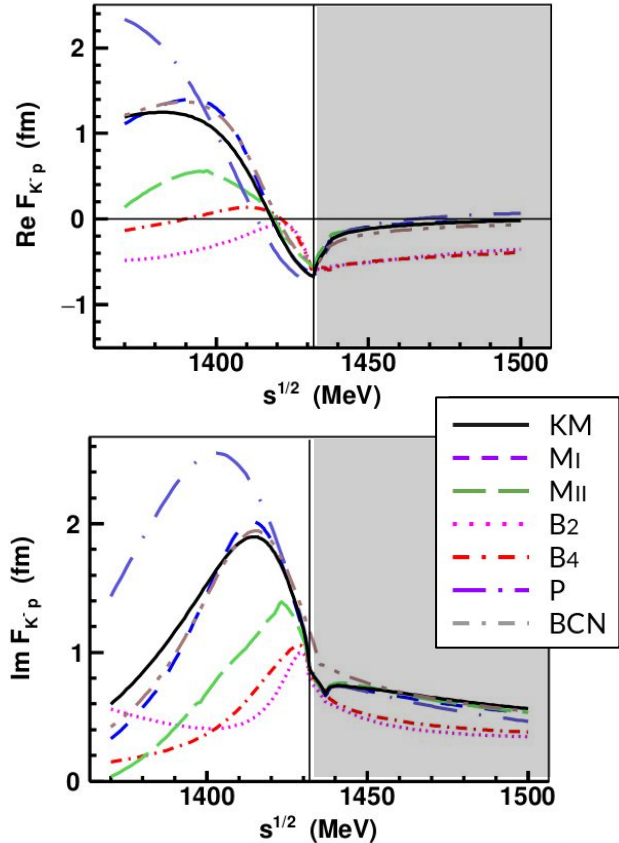


## K-p elastic and inelastic low-energy cross sections

- - - **Phen.** [Y. Ikeda and T. Sato, Phys. Rev. C76, 035203 (2007)]  
— **Chiral** [S. Ohnishi, Y. Ikeda, T. Hyodo, W. Weise, Phys.Rev. C93 (2016) no.2, 025207]

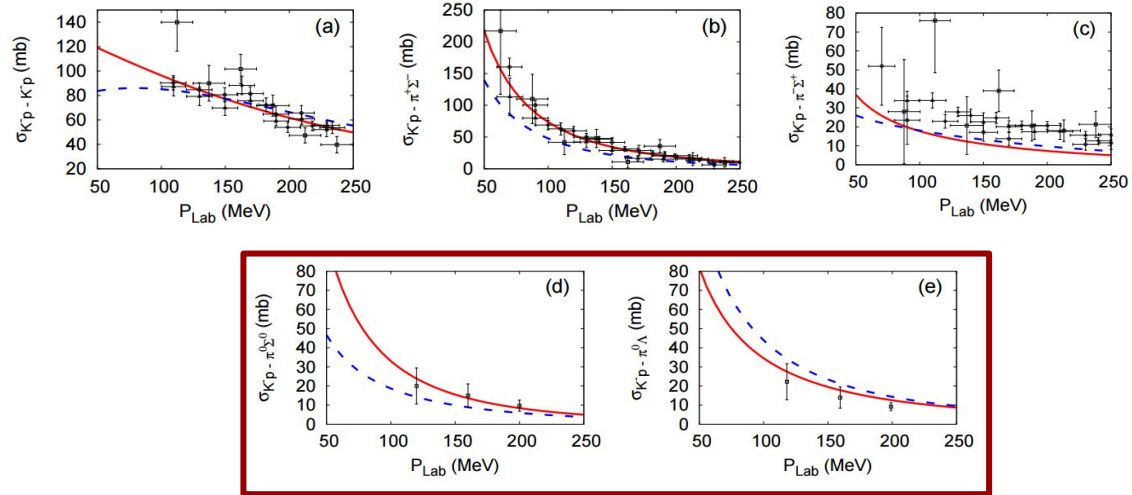


# Experimental constraints above threshold



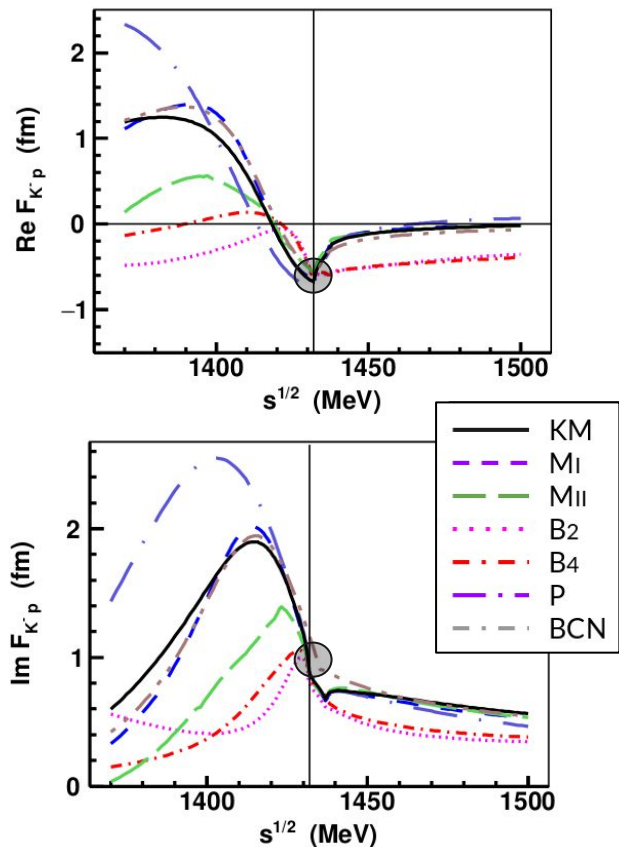
## K-p elastic and inelastic low-energy cross sections

--- Phen. [Y. Ikeda and T. Sato, Phys. Rev. C76, 035203 (2007)]  
--- Chiral [S. Ohnishi, Y. Ikeda, T. Hyodo, W. Weise, Phys.Rev. C93 (2016) no.2, 025207]

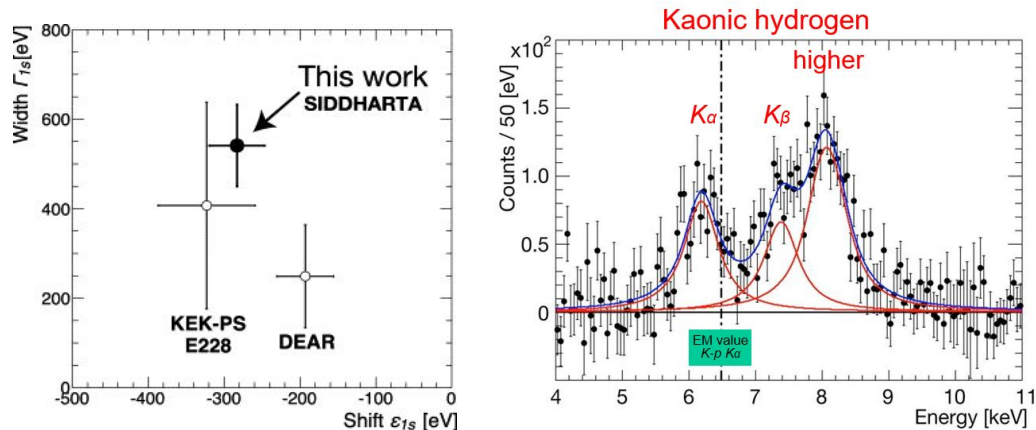


no data for  $p_K < 100$  MeV/c

# Experimental constraints at threshold



Precise SIDDHARTA measurement of kaonic hydrogen 1s level shift and width



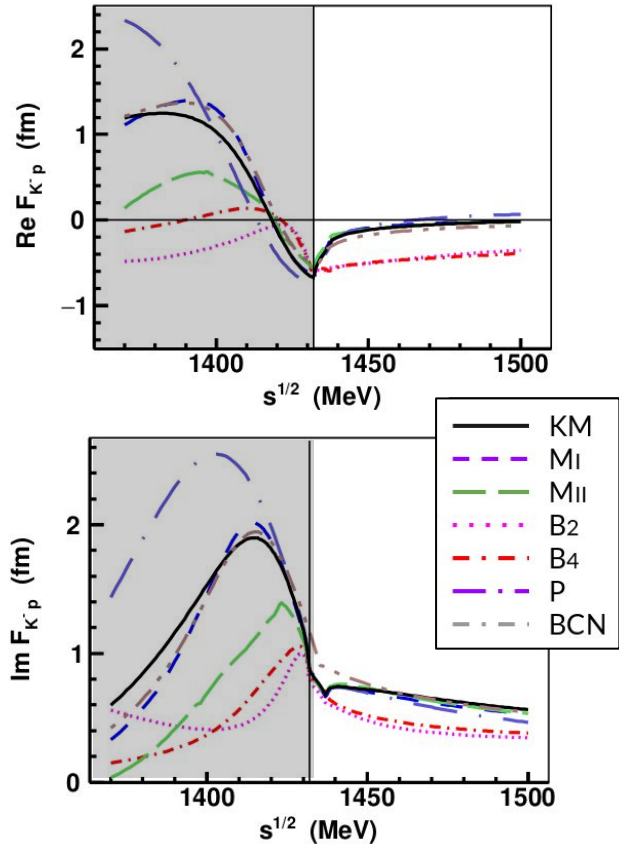
M. Bazzi et al., 2011. (SIDDHARTA Coll.), Phys. Lett. B704, 113

$$\Delta E_N(1s) = 283 \pm 36(\text{stat.}) \pm 6(\text{syst.}) \text{ eV}$$

$$\Gamma(1s) = 541 \pm 89(\text{stat.}) \pm 22(\text{syst.}) \text{ eV}$$

$$\epsilon + \frac{i\Gamma}{2} = 2\alpha^3 \mu^2 a_{K^-p} = 412 \frac{\text{eV}}{\text{fm}} a_{K^-p}$$

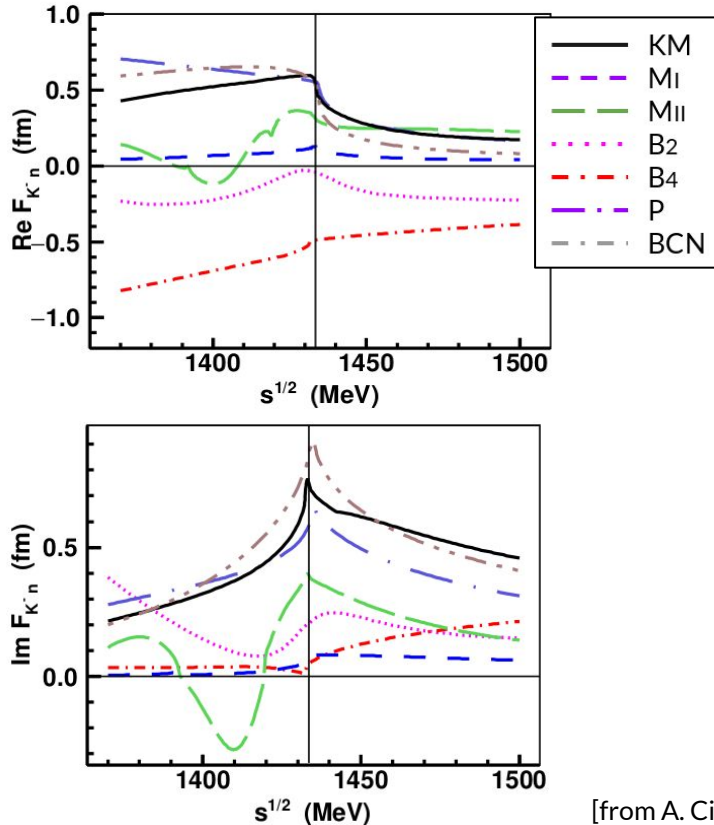
# Below threshold



No data below threshold

**NEW EXPERIMENTAL  
CONSTRAINTS ARE  
STRONGLY NEEDED!!**

# K<sup>-</sup>n scattering amplitude



## K<sup>-</sup>n scattering amplitude with Chiral models

Large spread in  $l=1$  channel

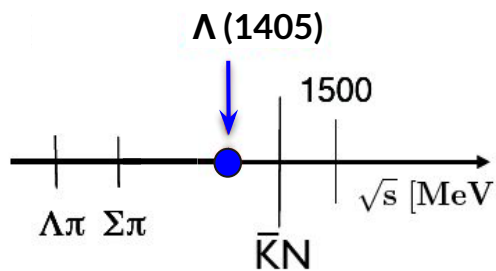
Experimental information is totally missing:

- **SIDDHARTA-2** → **first experimental constraint at threshold**
- **AMADEUS** → **first experimental constraint below threshold**

[from A. Cieply talk at MENU2019 conference]

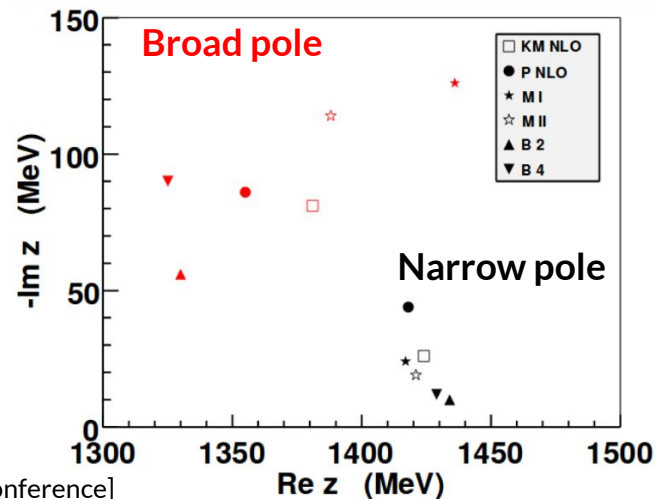
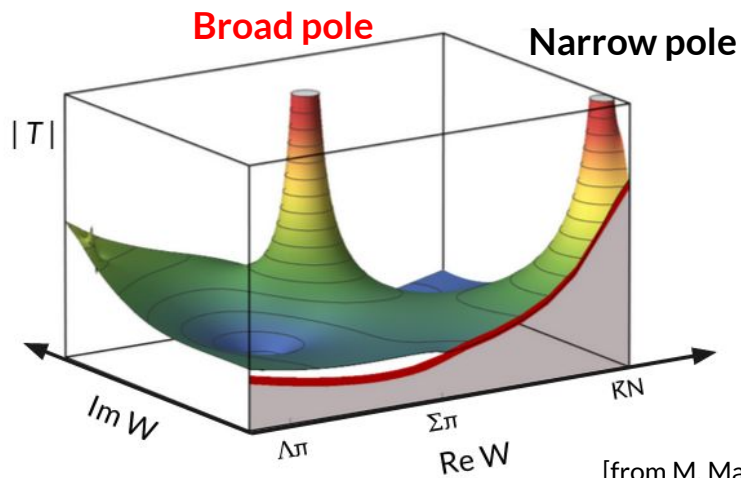


# Impact on $\Lambda(1405)$ nature



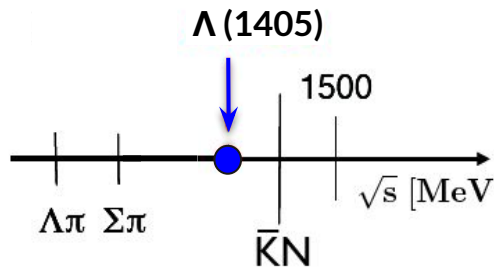
The  $\Lambda(1405)$  state does not fit with the simple three quarks model ( $uds$ ) and it is commonly accepted to be **partially, a  $\bar{K}N$  bound state**.

**Chiral models:** dynamical origin. Two poles of the scattering amplitude  $\rightarrow$  pole positions is model dependent (relative contributions not measured experimentally)



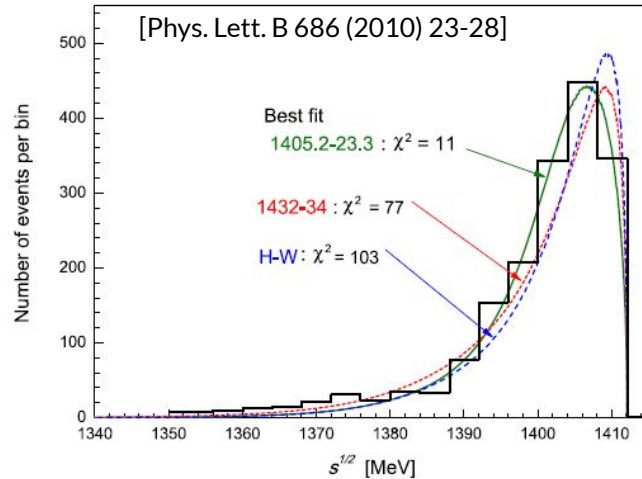
[from M. Mai talk at NSTAR19 conference]

# Impact on $\Lambda(1405)$ nature

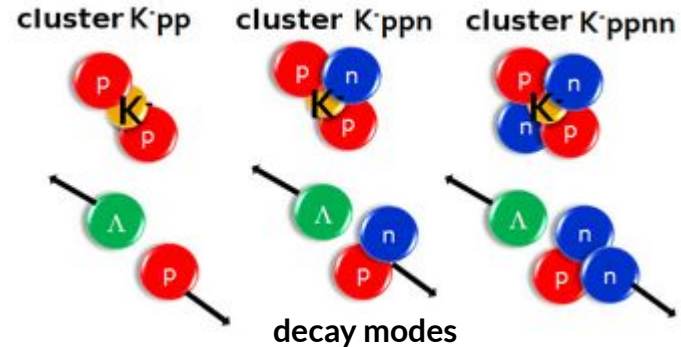


The  $\Lambda(1405)$  state does not fit with the simple three quarks model ( $uds$ ) and it is commonly accepted to be **partially, a  $\bar{K}N$  bound state**.

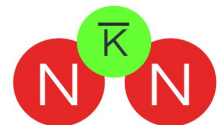
**Single pole ansatz (Esmaili-Akaishi-Yamazaki phenomenological potentials model):** Very strongly attractive  $\bar{K}N$  interaction  $\rightarrow$  existence of deeply bound kaonic bound states



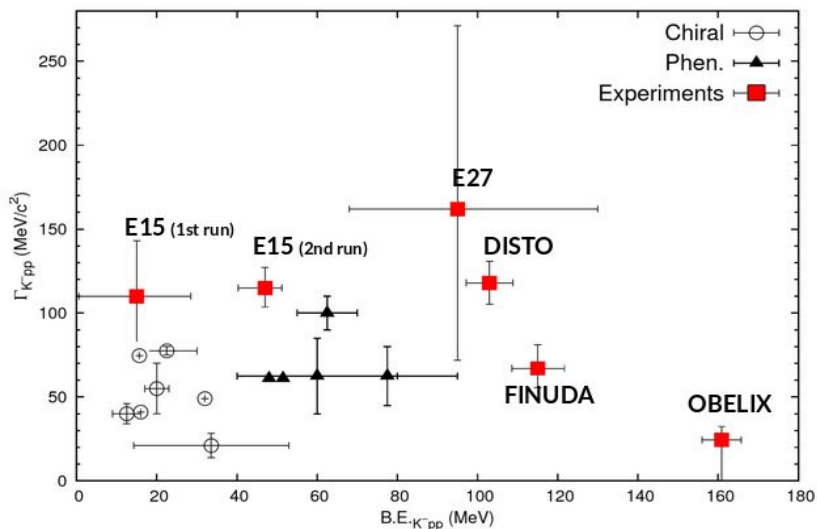
## Kaonic Bound States



# K<sup>-</sup>pp bound state



- KN input model is critical for the theoretical interpretation
- different bound state production mechanisms are experimentally investigated
- **E15** → **first clear evidence** in K<sup>-</sup> induced reactions (theoretical interpretation by Sekihara, Oset, Ramos)



Theory

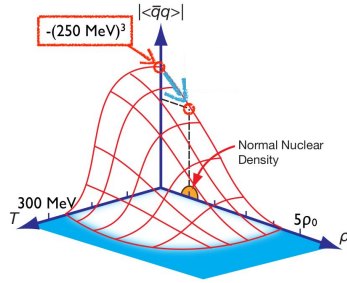
	BE (MeV)	Γ (MeV)	Reference
Dote, Hyodo, Weise	17-23	40-70	Phys.Rev.C79 (2009) 014003
Akaishi, Yamazaki	48	61	Phys.Rev.C65 (2002) 044005
Barnea, Gal, Liverts	16	41	Phys.Lett.B712 (2012) 132-137
Ikeda, Sato	60-95	45-80	Phys.Rev.C76 (2007) 035203
Ikeda, Kamano, Sato	9-16	34-46	Prog.Theor.Phys. (2010) 124(3): 533
Shevchenko, Gal, Mares	55-70	90-110	Phys.Rev.Lett.98 (2007) 082301
Revai, Shevchenko	32	49	Phys.Rev.C90 (2014) no.3, 034004
Maeda, Akaishi, Yamazaki	51.5	61	Proc.Jpn.Acad.B 89, (2013) 418
Bicudo	14.2-53	13.8-28.3	Phys.Rev.D76 (2007) 031502
Bayar, Oset	15-30	75-80	Nucl.Phys.A914 (2013) 349
Wycech, Green	40-80	40-85	Phys.Rev.C79 (2009) 014001
Sekihara, Oset, Ramos	16	72	Prog.Theor.Phys.(2016) no.12, 123D03
Sekihara, Oset, Ramos	20	80	E. Oset talk at UJ Symposium 2019

Experiments

Experiment	BE (MeV)	Γ (MeV)	Reference
FINUDA	115 <sup>+6</sup> <sub>-5</sub> (stat.) <sup>+3</sup> <sub>-4</sub> (syst.)	67 <sup>+14</sup> <sub>-11</sub> (stat.) <sup>+2</sup> <sub>-3</sub> (syst.)	PRL 94 (2005), 212303
OBELIX	160.9 ± 4.9	< 24.4 ± 8.0	NPA 789 (2007), 222
E549	-	-	MPLA 23 (2008), 2520
DISTO	103 ± 3 (stat.) ± 5 (syst.)	118 ± 8 (stat.) ± 10 (syst.)	PRL 104 (2010), 132502
LEPS/SPring-8	Upper Limit	-	PLB 728 (2014), 616
HADES	Upper Limit	-	PLB 742 (2015), 242
E27	95 <sup>+18</sup> <sub>-17</sub> (stat.) <sup>+30</sup> <sub>-21</sub> (syst.)	162 <sup>+87</sup> <sub>-45</sub> (stat.) <sup>+66</sup> <sub>-78</sub> (syst.)	PTEP (2015), 021D01
AMADEUS	Upper Limit	-	PLB 758 (2016), 134
E15	15 <sup>+6</sup> <sub>-8</sub> (stat.) ± 12 (syst.)	110 <sup>+19</sup> <sub>-17</sub> (stat.) ± 27 (syst.)	PTEP (2016), 051D01
E15 (2 <sup>nd</sup> run)	47 ± 3 (stat.) <sup>+3</sup> <sub>-5</sub> (syst.)	115 ± 7 (stat.) <sup>+10</sup> <sub>-20</sub> (syst.)	PLB 789 (2019), 620

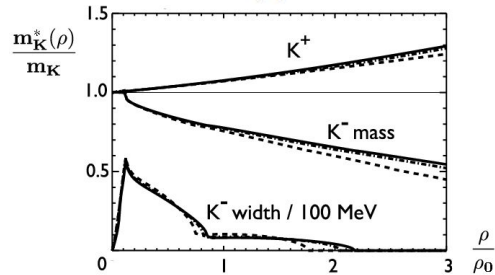
# Impact on in-medium $\bar{K}N$ interaction

- Partial restoration of chiral symmetry in medium

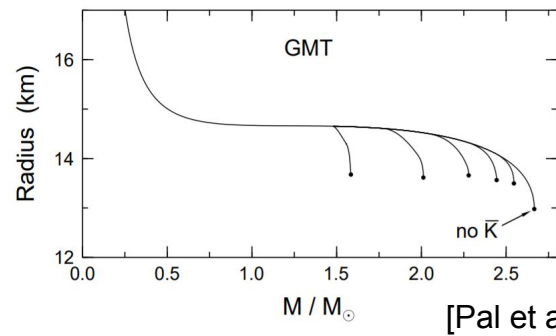
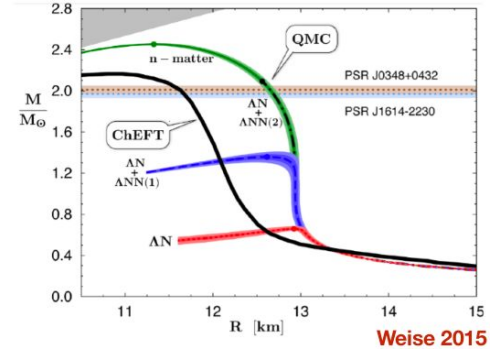
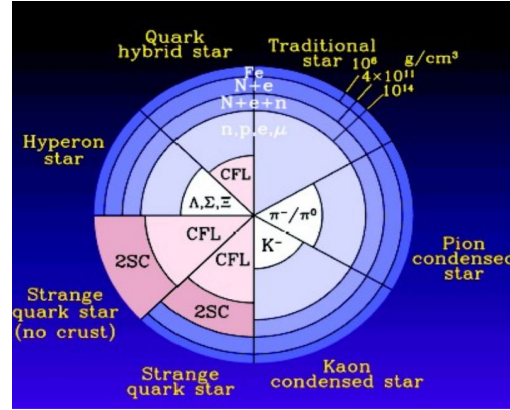


kaon mass modification:

$$m_K^{*2} = m_K^2 - \frac{\Sigma_{KN}}{f_\pi^2} \rho + \mathcal{O}(k_F^4)$$



- Impact on Equation of State (EoS) of Neutron Stars:







$K^-$  condensate can change EoS-stiffness

but: hyperons become more relevant at higher densities  
[Gal et al. (2016)]

[Pal et al. (2000)]

# Goals of AMADEUS

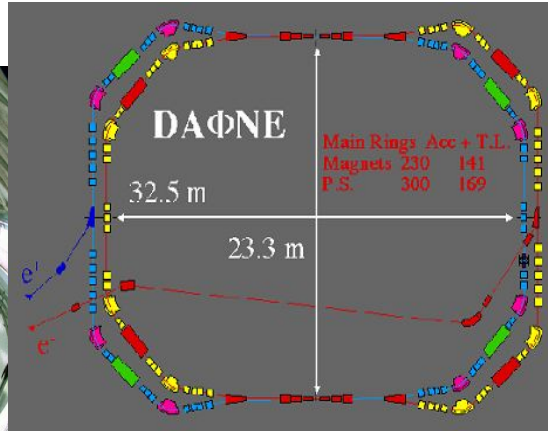
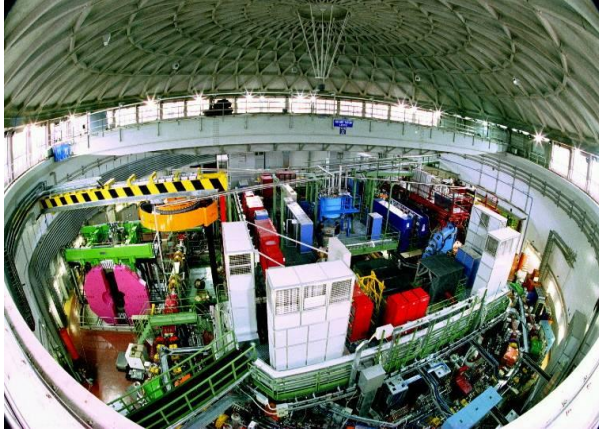
Unprecedented studies of the **low-energy charged kaons interactions in nuclear matter**: solid and gaseous targets (H,  $^4\text{He}$ ,  $^8\text{Be}$ ,  $^{12}\text{C}$  ...) in order to obtain unique quality information about:

1. Controversial nature of the  $\Lambda$  (1405) and  $\bar{K}N$  amplitude below threshold   **$Y\pi$  CORRELATION STUDIES**  
(i.e.  $\Lambda\pi$  and  $\Sigma\pi$  and final states)
2. Low-energy charged kaon cross sections for momenta of 100 MeV/c 
3. a) Interaction of  $K^-$  with one and more nucleons (single and multi-nucleon  $K^-$  absorption)   **$YN$  CORRELATION STUDIES**  
(i.e.  $\Lambda p$ ,  $\Sigma^0 p$ , and  $\Lambda t$  final states)  
b) possible existence of kaonic bound states 
4.  **$YN$  scattering**  $\rightarrow$  extremely poor experimental information from scattering data  
(helpful to understand the EoS of Neutron Stars)

# DAΦNE the $\Phi$ factory

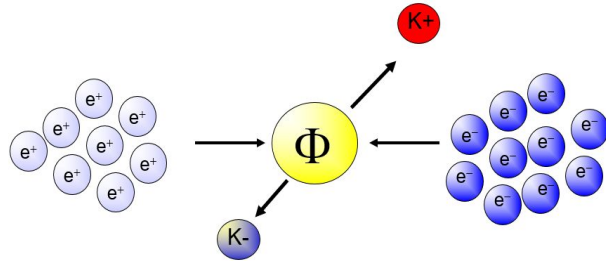


Istituto Nazionale di Fisica Nucleare  
LABORATORI NAZIONALI DI FRASCATI



- $e^+ e^-$  at 510 MeV
- $\phi$  resonance decays at 49.2 % in  $K^+ K^-$  back to back pair
- Very low momentum ( $\approx 127$  MeV)  $K^-$  beam
- Flux of produced kaons: about 1000/second

Best low momentum  $K^-$  factory in the world



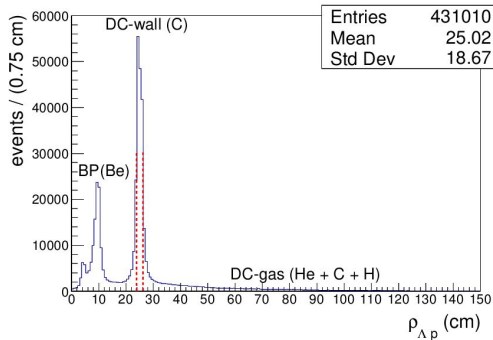
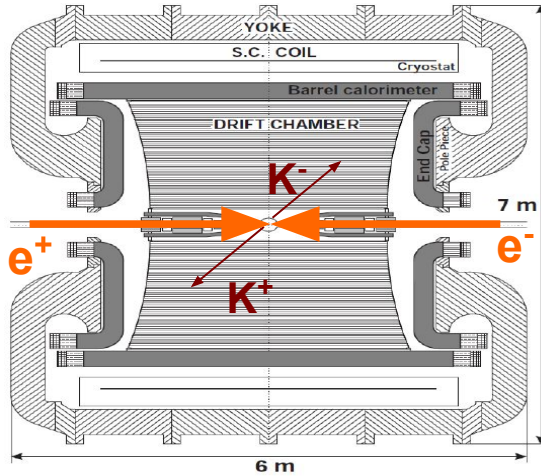
Suitable for low-energy kaon physics:

→ **Kaonic atoms** (**SIDDHARTA-2**)

→ **Kaon-nucleons/nuclei interaction** studies  
(**AMADEUS**)

# AMADEUS step 0

## The KLOE detector



- Cylindrical drift chamber with a  $4\pi$  geometry and electromagnetic calorimeter
- **96% acceptance**
- optimized in the energy range of all **charged particles** involved
- **good performance** in detecting **photons and neutrons** checked by kloNe group

[M. Anelli et al., Nucl Inst. Meth. A 581, 368 (2007)]

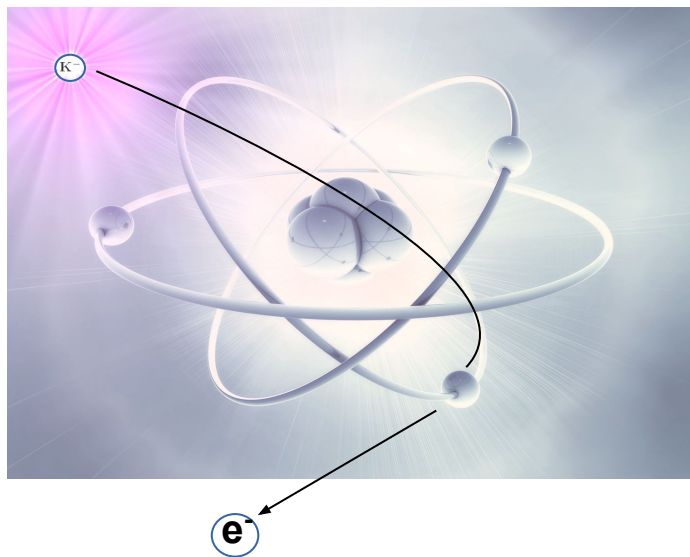
Possibility to use **KLOE materials** as an active target

- DC wall (750  $\mu\text{m}$  C foil, 150  $\mu\text{m}$  Al foil);
- DC gas (90% He, 10%  $\text{C}_4\text{H}_{10}$ ).

# K<sup>-</sup> absorptions at-rest and in-flight

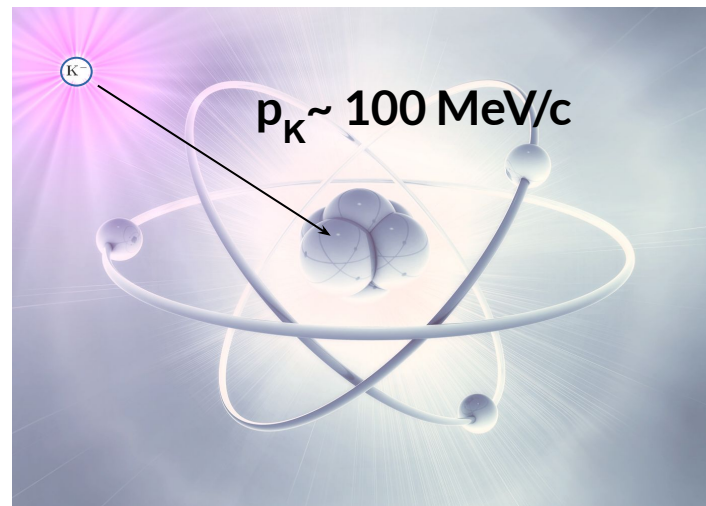
## AT-REST

K<sup>-</sup> absorbed from atomic orbitals  
( $p_K \sim 0 \text{ MeV/c}$ )



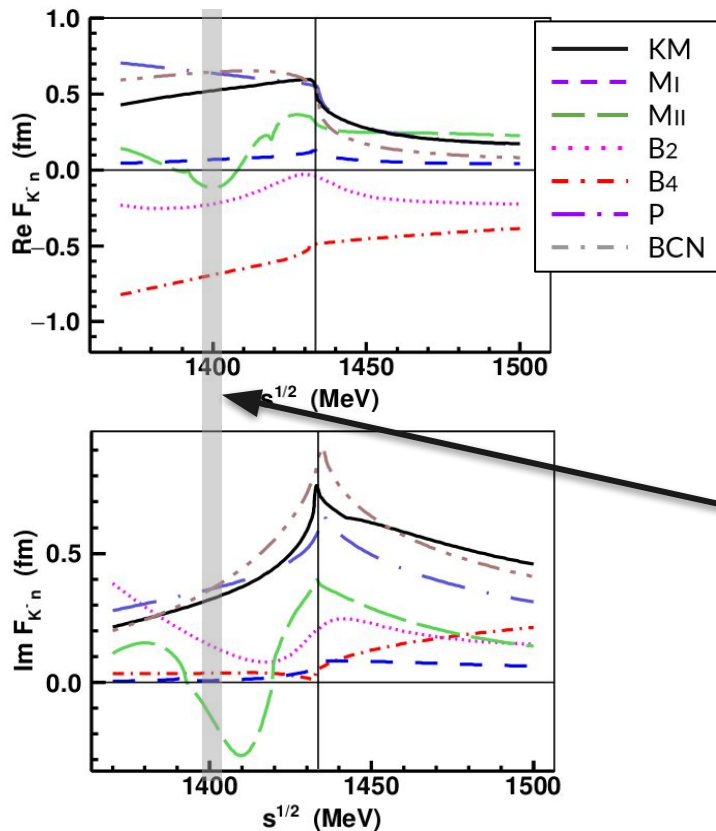
## IN-FLIGHT

( $p_K \sim 100 \text{ MeV/c}$ )





# Experimental constraints at threshold



## $K^-n$ scattering amplitude with Chiral models

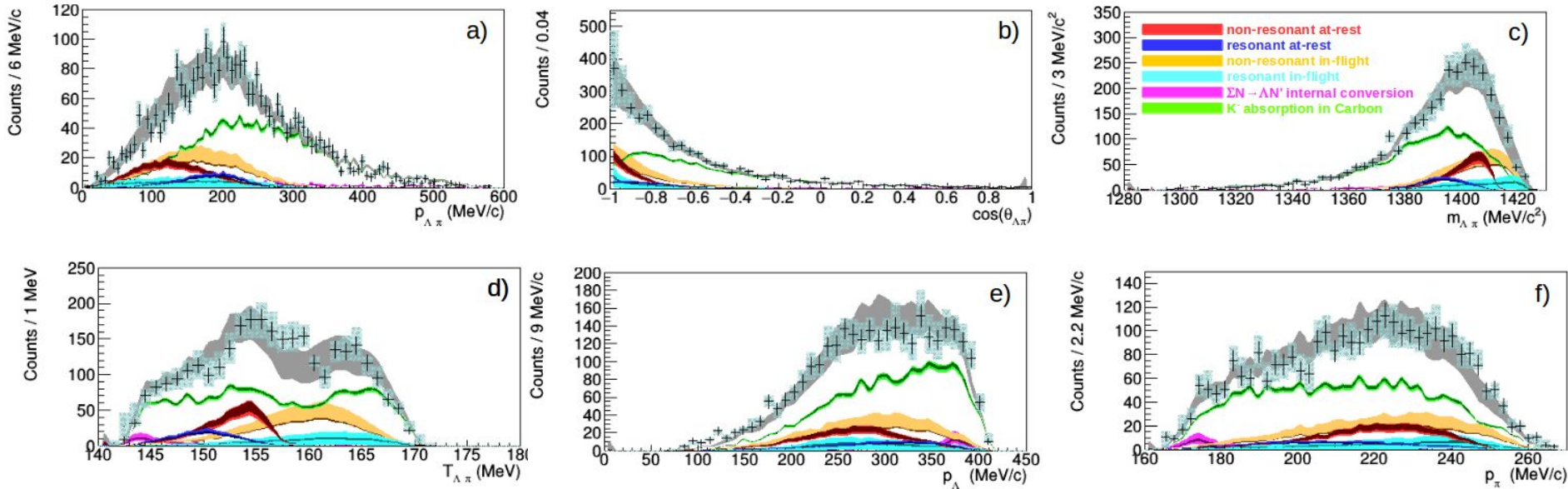
Large spread in  $l=1$  channel

Experimental information is totally missing:

- **SIDDHARTA-2** → **first experimental constraint at threshold**
- **AMADEUS** → **First determination of the non-resonant transition amplitude below threshold**  
Investigated using:  
 $K^- "n" \rightarrow \Lambda \pi^-$  to extract  $|f_{\Lambda \pi}^{N-R}(l=1)|$   
**below threshold**

# Simultaneous fit : $p_{\Lambda\pi^-} - m_{\Lambda\pi^-} - \cos\theta_{\Lambda\pi^-}$

Investigated using:  $K^- n \ ^3\text{He} \rightarrow \Lambda\pi^- \ ^3\text{He}$



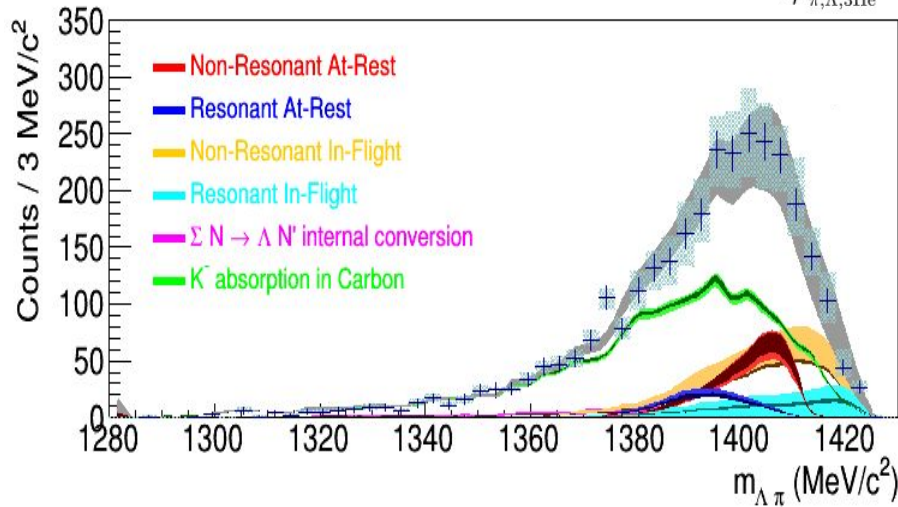
[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

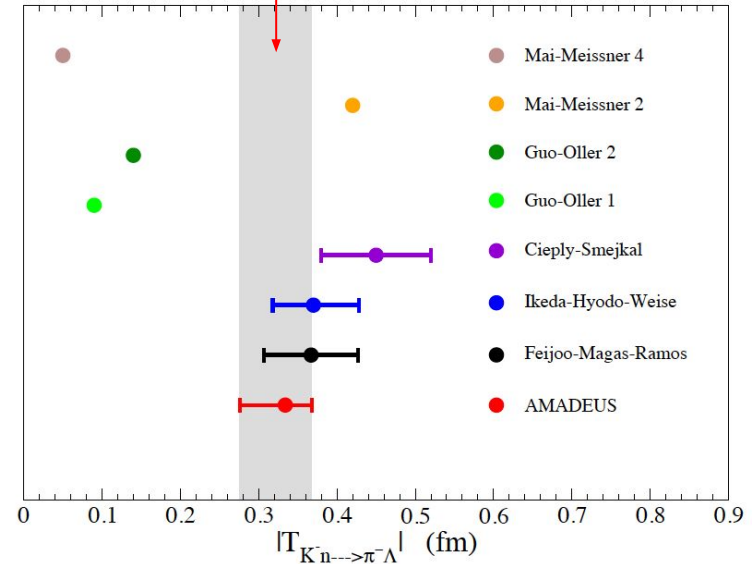
# Outcome of the measurement

Investigated using:  $K^- "n" {}^3\text{He} \rightarrow \Lambda \pi^- {}^3\text{He}$

$$E_{K\Lambda n} \sim -B_n - \left\langle \frac{p_{\Lambda\pi}^2}{2\mu_{\pi,\Lambda,3\text{He}}} \right\rangle$$



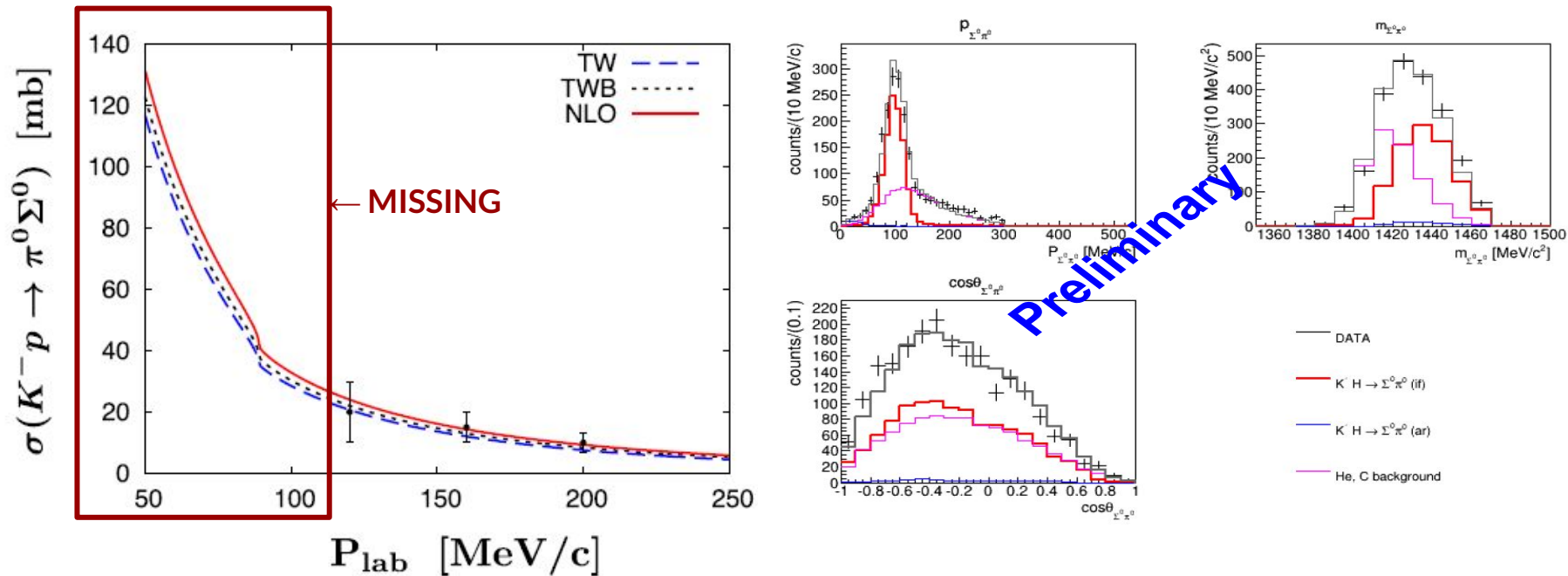
$$|f_{ar}^s| = (0.334 \pm 0.018 \text{ stat}_{-0.058}^{+0.034} \text{ syst}) \text{ fm.}$$



[K. Piscicchia, S. Wycech, L. Fabbietti et al. Phys.Lett. B782 (2018) 339-345]

[K. Piscicchia, S. Wycech, C. Curceanu, Nucl. Phys. A 954 (2016) 75-93]

# $K^-p \rightarrow \Sigma^0\pi^0$ cross section



**Figure 14.**  $K^-p \rightarrow \Sigma^0\pi^0$  cross section as function of  $K^-$  laboratory momentum. The black points represent the experimental data from [15, 16], the corresponding uncertainty on the kaon momentum is not shown in this figure. The solid red curve with the shaded uncertainty band represents the theoretical calculation in Ref. [12]. The blue point is the measurement of this work.

[15] W. E. Humphrey and R. R. Ross, Phys. Rev. 127 (1962) 1305  
 [16] J. K. Kim, Columbia University Report No. NEVIS-149 (1966)  
 [12] Y. Ikeda, T. Hyodo, W. Weise, Nucl. Phys. A 881 (2012) 98

# K<sup>-</sup> multi-nucleon absorptions

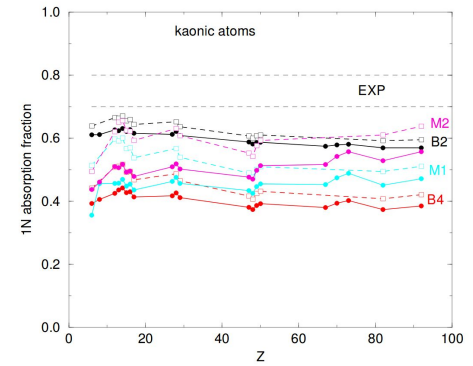
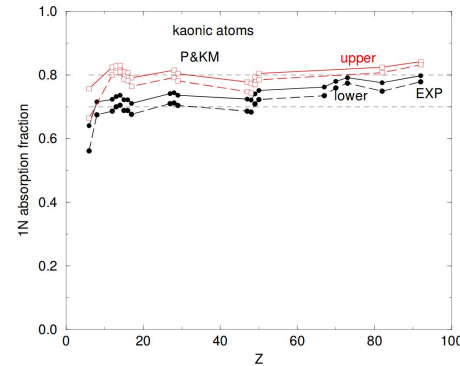
In K<sup>-</sup>-nuclei optical potential a K<sup>-</sup> multi-nucleon absorption term is necessary to fit the kaonic atoms data:

$$V_{K^-}(\rho) = V_{K^-}^{(1)}(\rho) + V_{K^-}^{(2)}(\rho) \rightarrow \text{multi-nucleon term}$$

[E. Friedman, A. Gal, Nucl. Phys. A 959, 66 (2017)]

[Hrtánková, J. & Mareš, J. Phys. Rev. C96, 015205 (2017)]

single nucleon term from chiral models



- Single nucleon absorption (1NA):

K<sup>-</sup> “N” → Y π → pionic processes

- Two nucleon absorption (2NA):

K<sup>-</sup> “NN” → Y N

- Three nucleon absorption (3NA):

K<sup>-</sup> “NNN” → Y (NN)

non-pionic processes

- Four nucleon absorption (4NA):

K<sup>-</sup> “NNNN” → Y (NNN)

bound nucleons = “N”, “NN”, “NNN”, “NNNN”

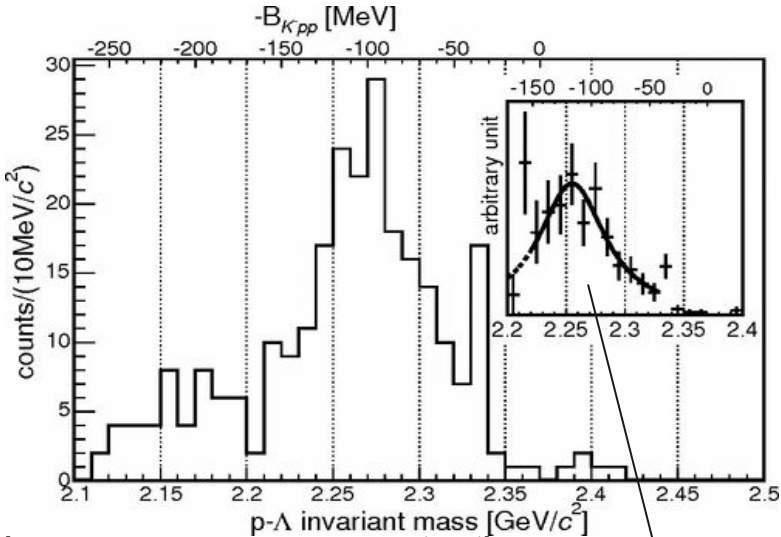
bound or unbound nucleons = (NN), (NNN)

Y = Λ, Σ

# Experimental search in $K^-$ induced reactions

FINUDA at DAΦNE:  $K^-_{\text{stop}} + X \rightarrow \Lambda + p + X'$

only back-to-back  $\Lambda p$  pairs ( $\cos\theta_{\Lambda p} < -0.8$ ) **detected particles**



[M. Agnello et al., Phys. Rev. Lett. 94, 212303 (2005)]

Interpreted as the signal of:

**extracted parameters:**

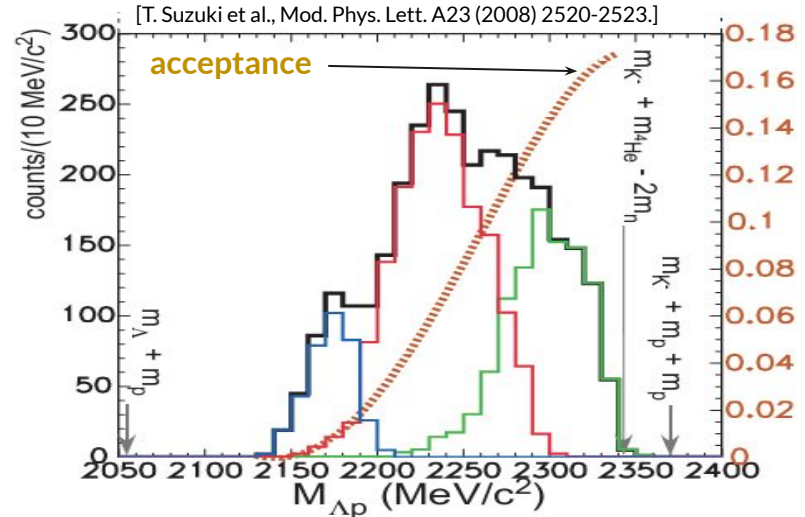
$K^- pp \rightarrow \Lambda + p$

$$BE = (115^{+6}_{-5}(\text{stat.})^{+3}_{-4}(\text{syst.})) \text{ MeV}$$

$$\Gamma = (67^{+14}_{-11}(\text{stat.})^{+2}_{-3}(\text{syst.})) \text{ MeV}/c^2$$

E549 at KEK:  $K^-_{\text{stop}} + {}^4\text{He} \rightarrow \Lambda + p + X'$

**detected particles**



[T. Suzuki et al., Mod. Phys. Lett. A23 (2008) 2520-2523.]

Using the missing mass information, three components to the invariant mass spectrum are found:

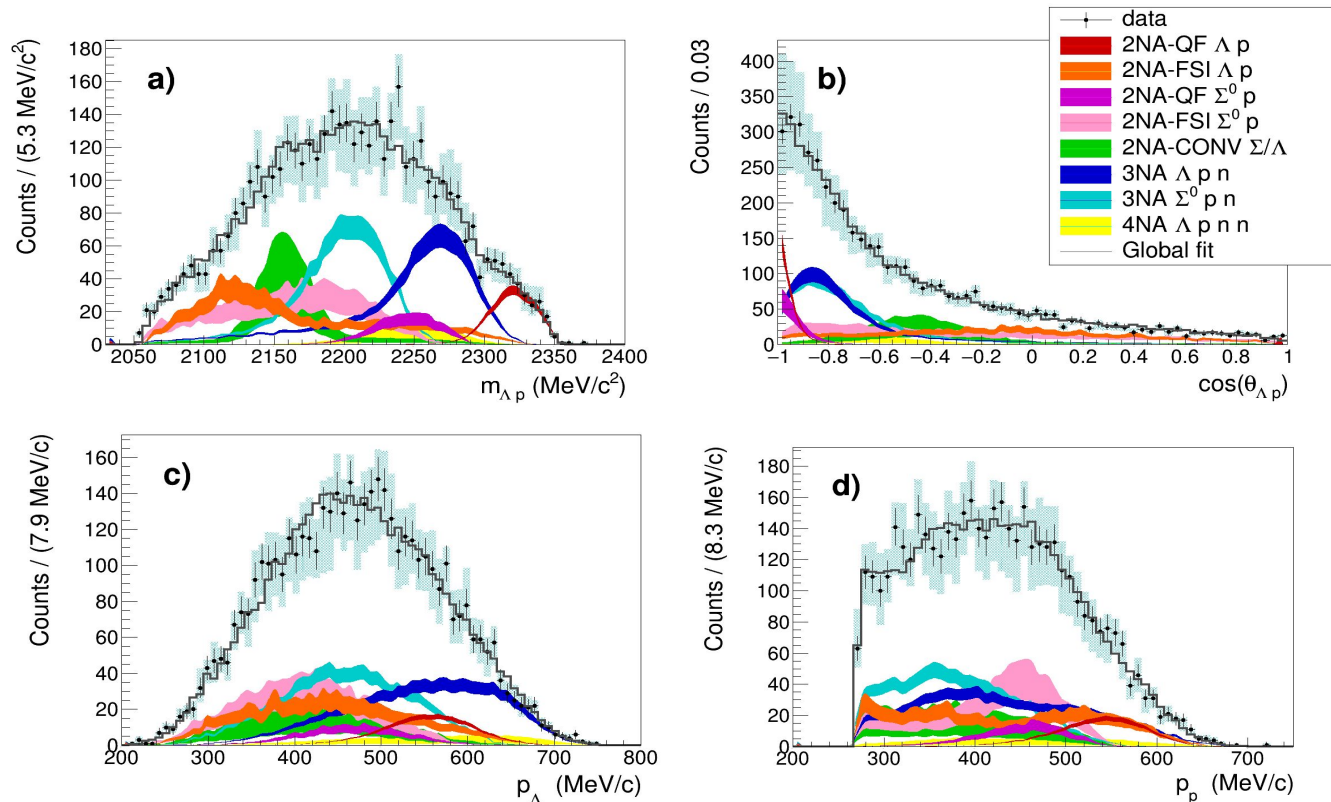
- **1NA:**  $K^-$  single nucleon absorption
- **2NA:**  $K^-$  two nucleon absorption
- **2NA + conversion, multi-nucleon, or Bound State?**

# $\Lambda$ p analysis: $K^- + {}^{12}\text{C} \rightarrow \Lambda + p + R$

Simultaneous fit of:

- $\Lambda$ p invariant mass;
- angular correlation;
- proton momentum;
- $\Lambda$  momentum.

Total reduced  $\chi^2$ :  $\chi^2/\text{dof} = 0.94$



[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]

[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

# $\Lambda p$ analysis: $K^-$ multi-nucleon absorption BRs and $\sigma$

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190 ]

Process	Branching Ratio (%)	$\sigma$ (mb)	@	$p_K$ (MeV/c)
2NA-QF $\Lambda p$	$0.25 \pm 0.02$ (stat.) $^{+0.01}_{-0.02}$ (syst.)	$2.8 \pm 0.3$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Lambda p$	$6.2 \pm 1.4$ (stat.) $^{+0.5}_{-0.6}$ (syst.)	$69 \pm 15$ (stat.) $\pm 6$ (syst.)	@	$128 \pm 29$
2NA-QF $\Sigma^0 p$	$0.35 \pm 0.09$ (stat.) $^{+0.13}_{-0.06}$ (syst.)	$3.9 \pm 1.0$ (stat.) $^{+1.4}_{-0.7}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Sigma^0 p$	$7.2 \pm 2.2$ (stat.) $^{+4.2}_{-5.4}$ (syst.)	$80 \pm 25$ (stat.) $^{+46}_{-60}$ (syst.)	@	$128 \pm 29$
2NA-CONV $\Sigma/\Lambda$	$2.1 \pm 1.2$ (stat.) $^{+0.9}_{-0.5}$ (syst.)	-		
3NA $\Lambda pn$	$1.4 \pm 0.2$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	$15 \pm 2$ (stat.) $\pm 2$ (syst.)	@	$117 \pm 23$
3NA $\Sigma^0 pn$	$3.7 \pm 0.4$ (stat.) $^{+0.2}_{-0.4}$ (syst.)	$41 \pm 4$ (stat.) $^{+2}_{-5}$ (syst.)	@	$117 \pm 23$
4NA $\Lambda pnn$	$0.13 \pm 0.09$ (stat.) $^{+0.08}_{-0.07}$ (syst.)	-		
Global $\Lambda(\Sigma^0)p$	$21 \pm 3$ (stat.) $^{+5}_{-6}$ (syst.)	-		

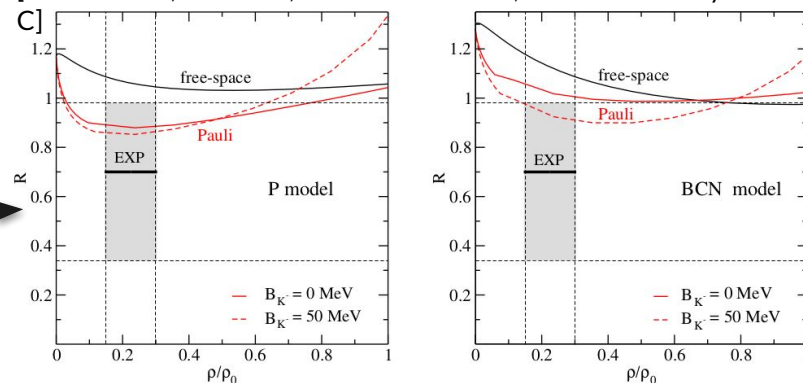
The ratio between the branching ratios of the 2NA-QF in the  $\Lambda p$  channel and in the  $\Sigma^0 p$  is measured to be:

$$\mathcal{R} = \frac{BR(K^- pp \rightarrow \Lambda p)}{BR(K^- pp \rightarrow \Sigma^0 p)} = 0.7 \pm 0.2(\text{stat.})^{+0.2}_{-0.3}(\text{syst.})$$

and the ratio between the corresponding phase spaces is  $\mathcal{R}' \simeq 1.22$ .

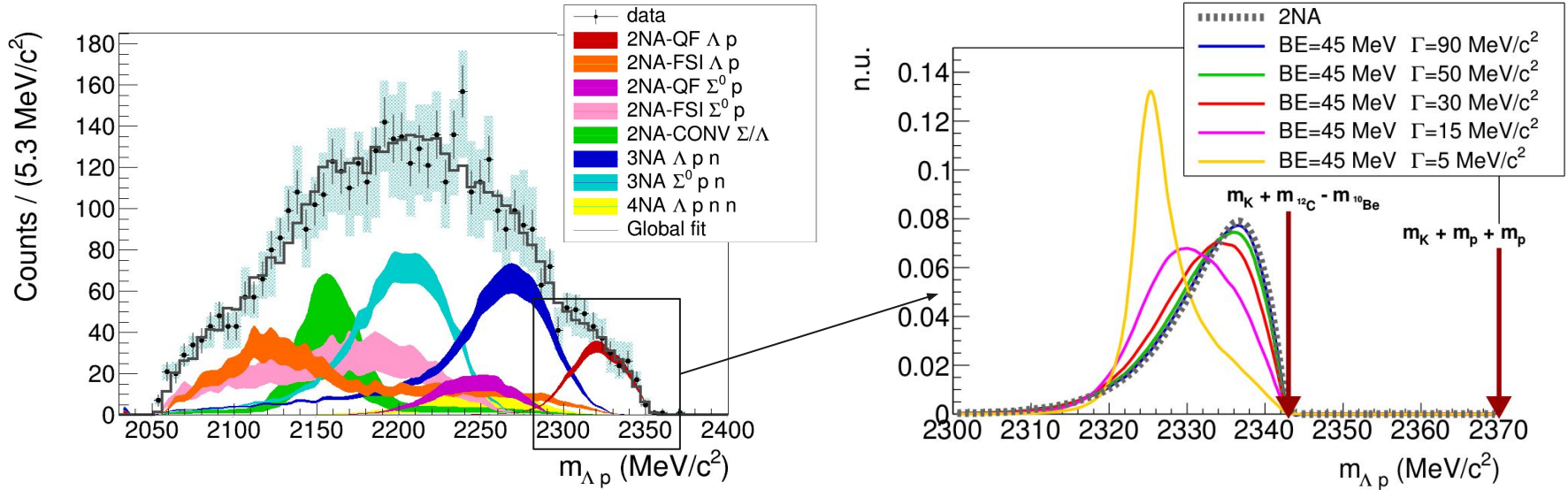
## Information on the in-medium dynamics

[J. Hrtánková, A. Ramos, arXiv:1910.01336, submitted to Phys. Rev.





# $\Lambda$ p analysis: $K^-$ pp bound state

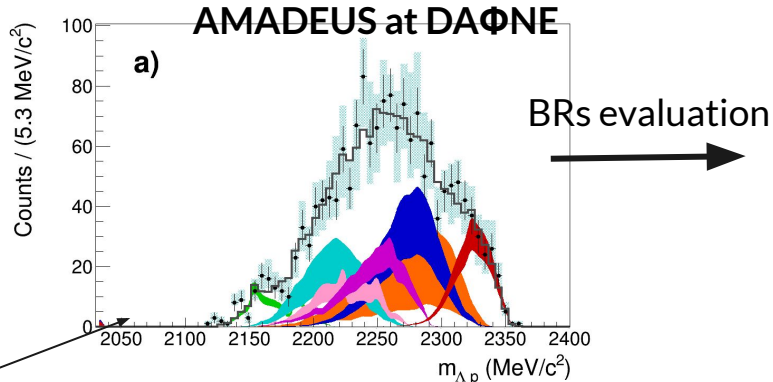


$K^-$ pp bound state contribution **completely overlaps** with the  $K^-$ 2NA

[R. Del Grande, K. Piscicchia, O. Vazquez Doce et al., Eur.Phys.J. C79 (2019) no.3, 190]

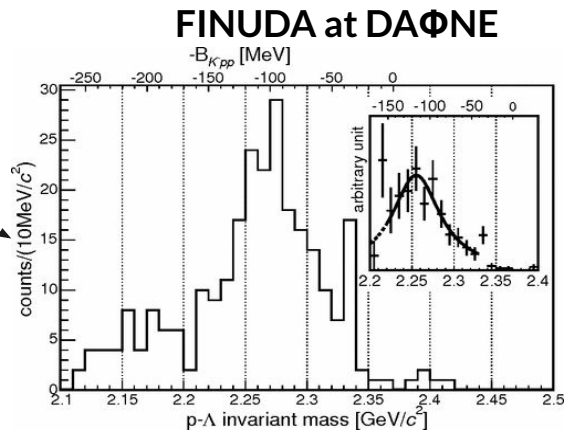
[R. Del Grande, K. Piscicchia, S. Wycech, Acta Phys. Pol. B 48 (2017) 1881]

# $\Lambda_p$ analysis: $K^-$ pp bound state search

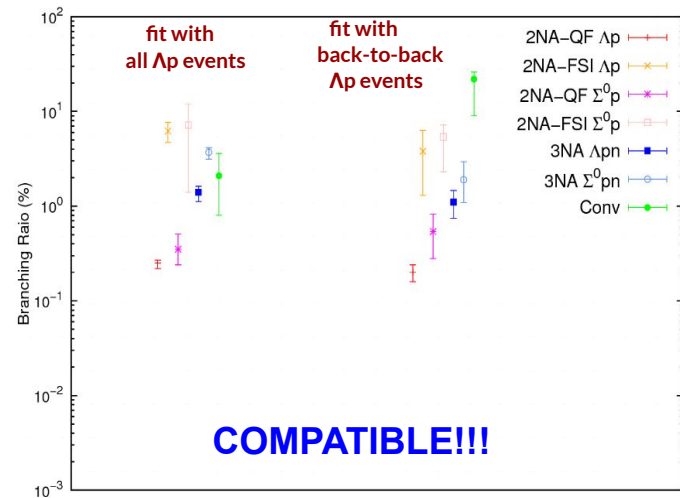


Process	Branching Ratio (%)
2NA-QF $\Lambda p$	$0.20 \pm 0.04(\text{stat.}) \pm 0.02(\text{syst.})$
2NA-FSI $\Lambda p$	$3.8 \pm 2.3(\text{stat.}) \pm 1.1(\text{syst.})$
2NA-QF $\Sigma^0 p$	$0.54 \pm 0.20(\text{stat.})^{+0.20}_{-0.16}(\text{syst.})$
2NA-FSI $\Sigma^0 p$	$5.4 \pm 1.5(\text{stat.})^{+1.0}_{-2.7}(\text{syst.})$
2NA-CONV $\Sigma/\Lambda$	$22 \pm 4(\text{stat.})^{+1}_{-12}(\text{syst.})$
3NA $\Lambda pn$	$1.1 \pm 0.3(\text{stat.}) \pm 0.2(\text{syst.})$
3NA $\Sigma^0 pn$	$1.9 \pm 0.7(\text{stat.})^{+0.8}_{-0.4}(\text{syst.})$

only **back-to-back**  $\Lambda p$  pairs ( $\cos\theta_{\Lambda p} < -0.8$ )



[M. Agnello et al., Phys. Rev. Lett. 94, 212303 (2005)]



# $\Lambda t$ analysis: Cross section and BR for 4NA

GOLDEN CHANNEL to extrapolate the  $K^-$  4NA



## Previous data:

- in  $^4\text{He}$ : bubble chamber experiment

/M. Roosen, J. H. Wickens, Il Nuovo Cimento 66, 101 (1981)/

only 3 events compatible with  $\Lambda t$  kinematics found

$$\text{BR}(K^- ^4\text{He} \rightarrow \Lambda t) = (3 \pm 2) \times 10^{-4} / K_{\text{stop}}^- \rightarrow \text{global, no 4NA}$$

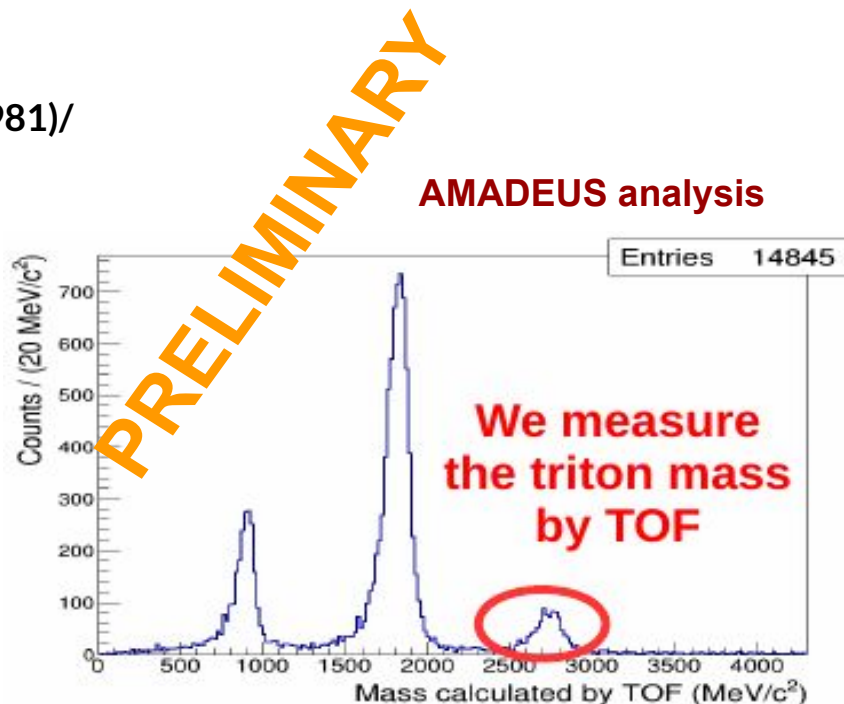
- in solid targets:  $^6,7\text{Li}$ ,  $^9\text{Be}$  (FINUDA)

/Phys. Lett. B, 229 (2008)/

40 events, only back-to-back data

$$\Lambda t \text{ emission yield} \rightarrow 10^{-3} - 10^{-4} / K_{\text{stop}}^-$$

$\rightarrow$  global, no 4NA



# At analysis: Cross section and BR for 4NA in $K^- ^4\text{He} \rightarrow \text{At}$ process

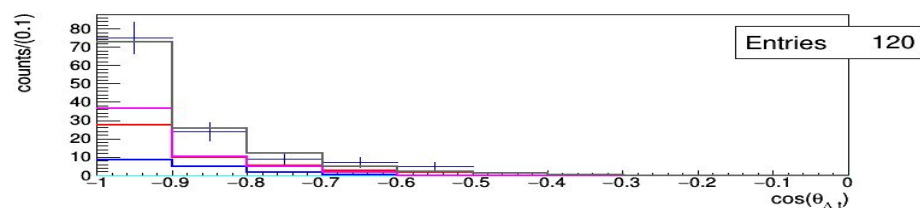
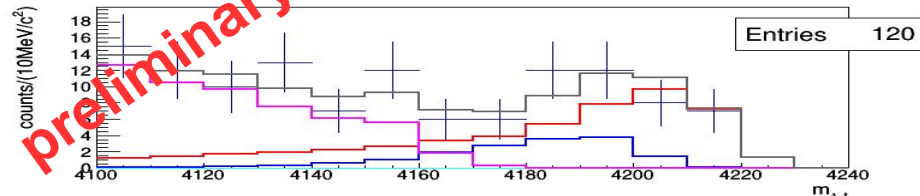
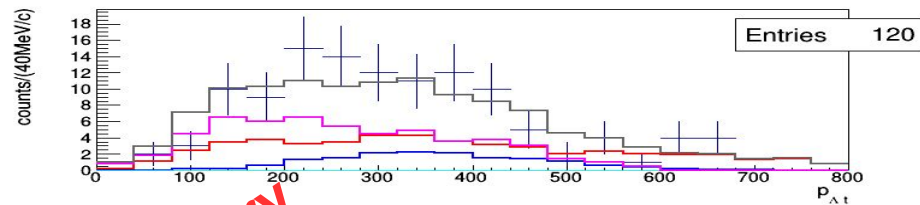
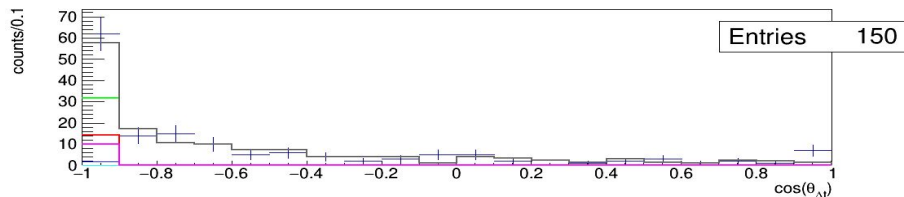
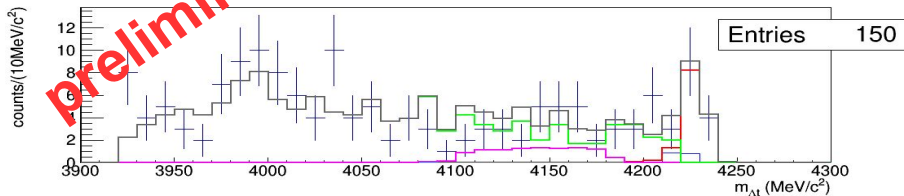
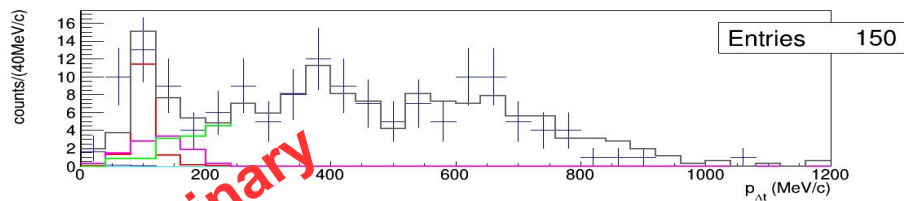
$$\text{BR}(K^- ^4\text{He}(4\text{NA}) \rightarrow \text{At}) < 2.0 \times 10^{-4} / K_{\text{stop}} \text{ (95\% c. l.)}$$

$$\begin{aligned} \sigma(100 \pm 19 \text{ MeV/c}) (K^- ^4\text{He}(4\text{NA}) \rightarrow \text{At}) &= \\ &= (0.81 \pm 0.21 \text{ (stat)}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb} \end{aligned}$$

$$\text{BR}(K^- ^{12}\text{C}(4\text{NA}) \rightarrow \text{At } ^8\text{Be}) = 1.5 \pm 0.5 \times 10^{-4} \text{ (stat)} / K_{\text{stop}}$$

$$\sigma(K^- ^{12}\text{C}(4\text{NA}) \rightarrow \text{At } ^8\text{Be}) = 0.58 \pm 0.11 \text{ (stat)} \text{ mb}$$

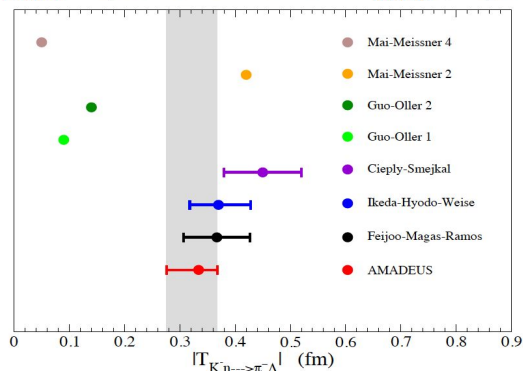
$$\sigma(K^- ^{12}\text{C}(4\text{NA}) \rightarrow \Sigma^0 t ^8\text{Be}) = 1.88 \pm 0.35 \text{ (stat)} \text{ mb}$$



# Summary

## K<sup>-</sup>n amplitude below threshold

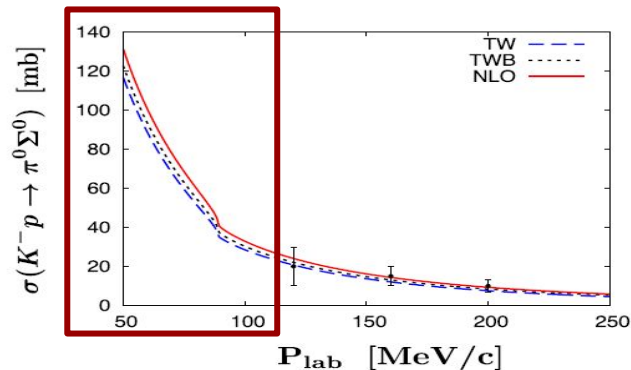
$$|f_{ar}^s| = (0.334 \pm 0.018 \text{ stat}^{+0.034}_{-0.058} \text{ syst}) \text{ fm.}$$



## $\Lambda$ p channel: 2NA, 3NA and 4NA BRs and $\sigma$

Process	Branching Ratio (%)	$\sigma$ (mb)	@	$p_K$ (MeV/c)
2NA-QF $\Lambda p$	$0.25 \pm 0.02$ (stat.) $^{+0.01}_{-0.02}$ (syst.)	$2.8 \pm 0.3$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Lambda p$	$6.2 \pm 1.4$ (stat.) $^{+0.5}_{-0.6}$ (syst.)	$69 \pm 15$ (stat.) $\pm 6$ (syst.)	@	$128 \pm 29$
2NA-QF $\Sigma^0 p$	$0.35 \pm 0.09$ (stat.) $^{+0.13}_{-0.06}$ (syst.)	$3.9 \pm 1.0$ (stat.) $^{+1.4}_{-0.7}$ (syst.)	@	$128 \pm 29$
2NA-FSI $\Sigma^0 p$	$7.2 \pm 2.2$ (stat.) $^{+4.2}_{-5.4}$ (syst.)	$80 \pm 25$ (stat.) $^{+46}_{-60}$ (syst.)	@	$128 \pm 29$
2NA-CONV $\Sigma/\Lambda$	$2.1 \pm 1.2$ (stat.) $^{+0.9}_{-0.5}$ (syst.)	-	-	-
3NA $\Lambda p n$	$1.4 \pm 0.2$ (stat.) $^{+0.1}_{-0.2}$ (syst.)	$15 \pm 2$ (stat.) $\pm 2$ (syst.)	@	$117 \pm 23$
3NA $\Sigma^0 p n$	$3.7 \pm 0.4$ (stat.) $^{+0.2}_{-0.4}$ (syst.)	$41 \pm 4$ (stat.) $^{+2}_{-5}$ (syst.)	@	$117 \pm 23$
4NA $\Lambda p n n$	$0.13 \pm 0.09$ (stat.) $^{+0.08}_{-0.07}$ (syst.)	-	-	-
Global $\Lambda(\Sigma^0)p$	$21 \pm 3$ (stat.) $^{+5}_{-6}$ (syst.)	-	-	-

## K<sup>-</sup>p $\rightarrow$ $\Sigma^0 \pi^0$ cross section



## $\Lambda$ t channel: 4NA BRs and $\sigma$

$$\text{BR}(K^-4\text{He}(4\text{NA}) \rightarrow \Lambda t) < 2.0 \times 10^{-4} / K_{\text{stop}} \text{ (95\% c.l.)}$$

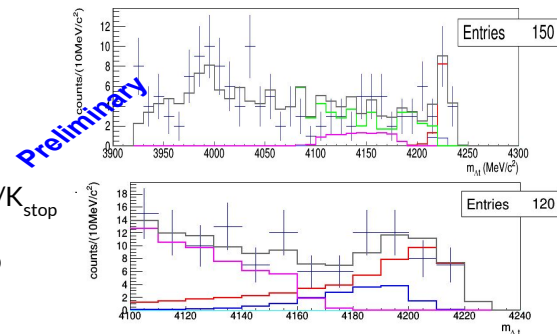
$$\sigma(100 \pm 19 \text{ MeV/c}) (K^-4\text{He}(4\text{NA}) \rightarrow \Lambda t) =$$

$$= (0.81 \pm 0.21 \text{ (stat)}^{+0.03}_{-0.04} \text{ (syst)}) \text{ mb}$$

$$\text{BR}(K^-^{12}\text{C}(4\text{NA}) \rightarrow \Lambda t \text{ } ^8\text{Be}) = 1.5 \pm 0.5 \times 10^{-4} \text{ (stat)} / K_{\text{stop}}$$

$$\sigma(K^-^{12}\text{C}(4\text{NA}) \rightarrow \Lambda t \text{ } ^8\text{Be}) = 0.58 \pm 0.11 \text{ (stat)} \text{ mb}$$

$$\sigma(K^-^{12}\text{C}(4\text{NA}) \rightarrow \Sigma^0 t \text{ } ^8\text{Be}) = 1.88 \pm 0.35 \text{ (stat)} \text{ mb}$$



**Thank You**