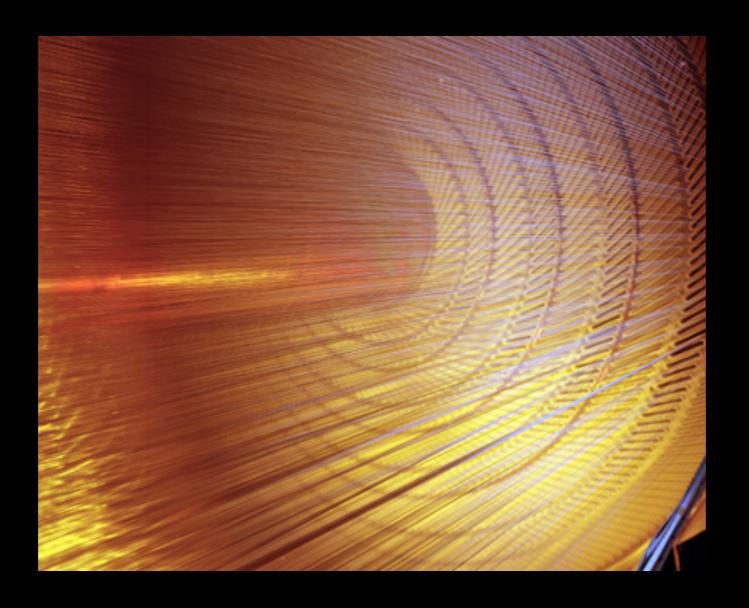
# High-precision measurement of the W boson mass with the CDF II detector





**Chris Hays, Oxford University** 

QCD@Work 29 June, 2022

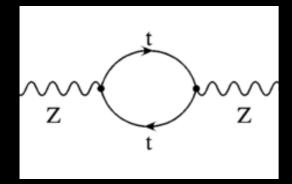


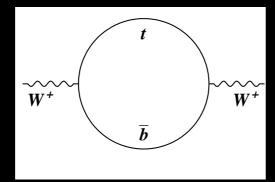
## Electroweak boson masses

#### Gauge boson masses

$$m_Z = \frac{v}{2} \sqrt{g^2 + g^2}$$

$$m_W = \frac{v}{2}g$$





$$m_W^2 = \frac{\hbar^3}{c} \frac{\pi \alpha_{EM}}{\sqrt{2}G_F(1 - m_W^2/m_Z^2)(1 - \Delta r)}$$

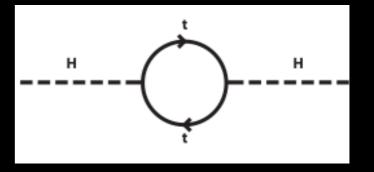
$$\Delta r_{tb} = \frac{c}{\hbar^3} \frac{-3G_F m_W^2}{8\sqrt{2}\pi^2 (m_Z^2 - m_W^2)} \times \left[ m_t^2 + m_b^2 - \frac{2m_t^2 m_b^2}{m_t^2 - m_b^2} \ln(m_t^2/m_b^2) \right]$$

SM calculation of W boson mass yields  $81358 \pm 4 \text{ MeV}$ 

Erler & Freitas PDG (2022)

Higgs boson mass

$$m_H = v\sqrt{2\lambda}$$



Naively integrating to a cutoff scale  $\Lambda$ :

$$\Delta m_H = \frac{3g^2 m_t^2}{16\pi^2 m_W^2} \Lambda^2$$

If there is no new physics up to scale  $\Lambda$  then we have 'fine-tuning' to cancel the quantum corrections

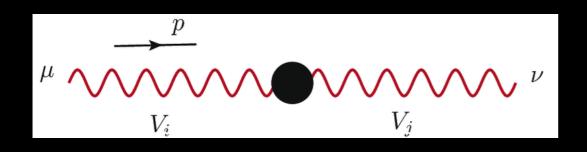
1% fine tuning:  $\Lambda = 6.6$  TeV

**Motivates TeV-scale new physics** 

#### W boson mass

More generally the SM effective field theory parameterizes high-scale effects

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}^{(5)} + \mathcal{L}^{(6)} + \mathcal{L}^{(7)} + \cdots, \qquad \mathcal{L}^{(d)} = \sum_{i=1}^{n_d} \frac{C_i^{(d)}}{\Lambda^{d-4}} Q_i^{(d)} \quad \text{for } d > 4.$$



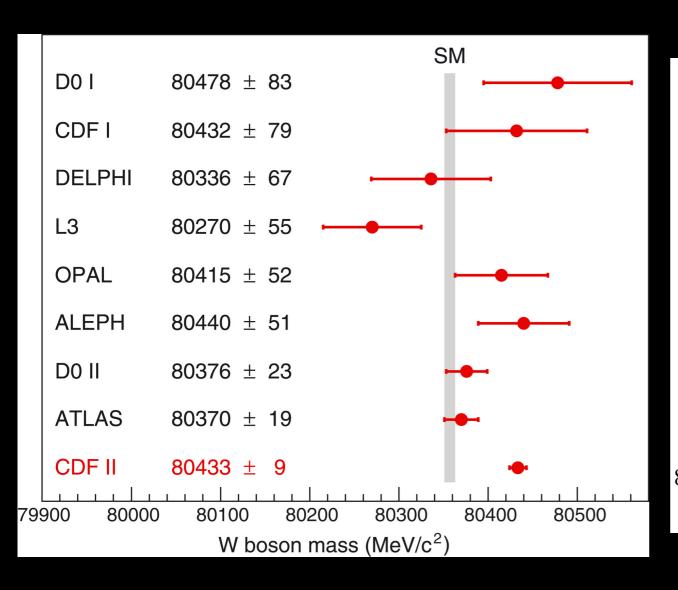
$$\frac{\delta m_W}{m_W} = \left(0.34c_{HD} + 0.72c_{HWB} + 0.37c_{Hl3} - 0.19c_{ll1}\right) \frac{v^2}{\Lambda^2}$$

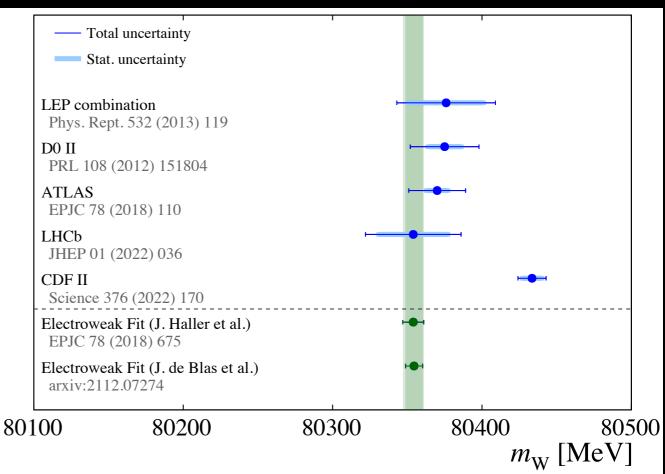
For  $\delta m_W/m_W=0.1\,\%$  and c<sub>HD</sub>=1,  $\Lambda=4.5\,{\rm TeV}$  e.g. Z' boson

For  $\delta m_W/m_W=0.1\,\%$  and c<sub>HWB</sub>=1,  $\Lambda=6.6\,\mathrm{TeV}$  e.g. compositeness

Smaller  $c_i \rightarrow smaller \Lambda$ 

#### W boson mass measurements



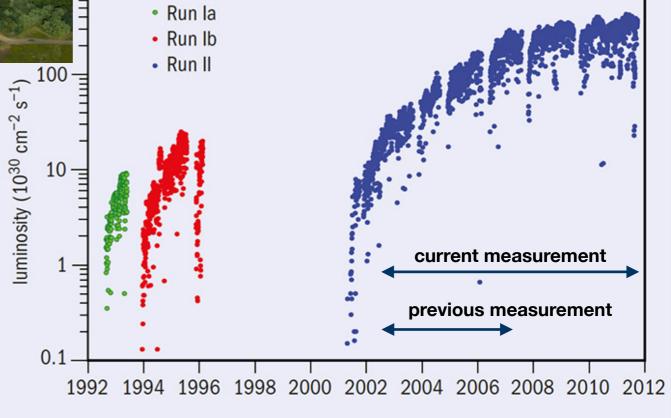


## **CDF II measurement of the W boson mass**

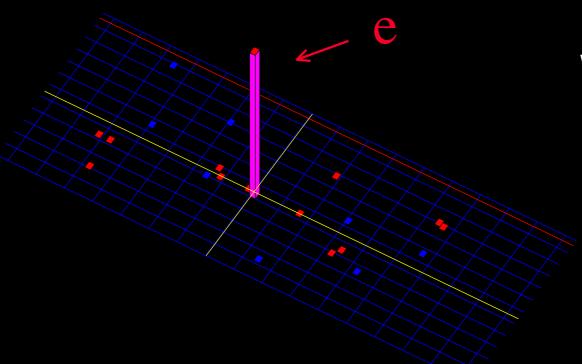


 $\sqrt{s}=1.96$  TeV proton-antiproton collisions from the Fermilab Tevatron

Measurement uses complete Tevatron Run II data set



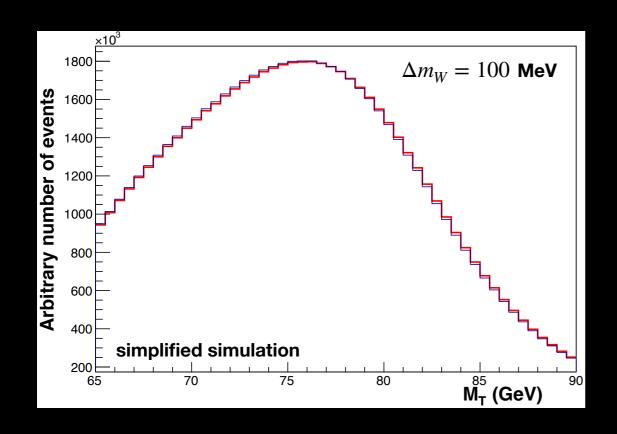
#### **CDF II measurement of the W boson mass**

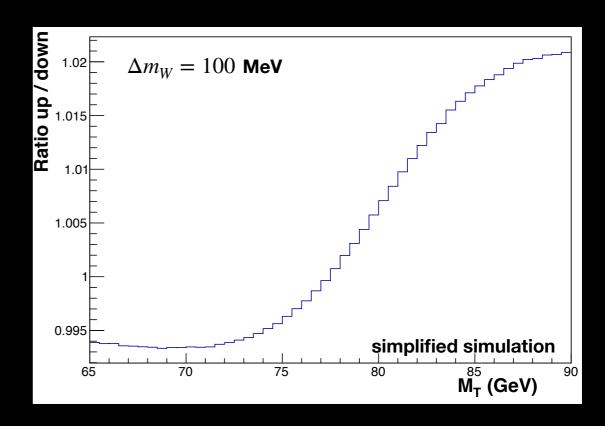


W bosons identified in their decays to  $e \nu$  and  $\mu \nu$ 

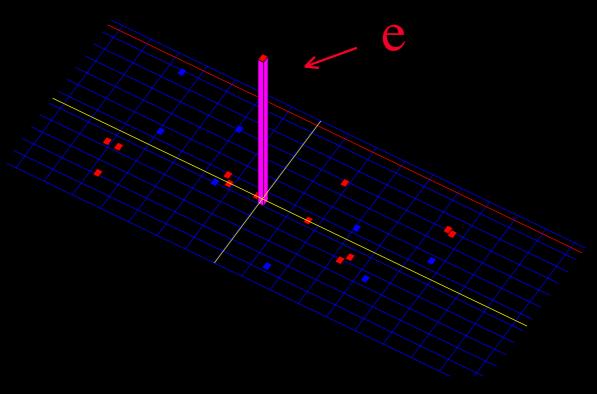
Mass measured by fitting template distributions of transverse momentum and mass

$$m_T = \sqrt{2p_T^{\ l} p_T \left(1 - \cos \Delta \phi\right)}$$

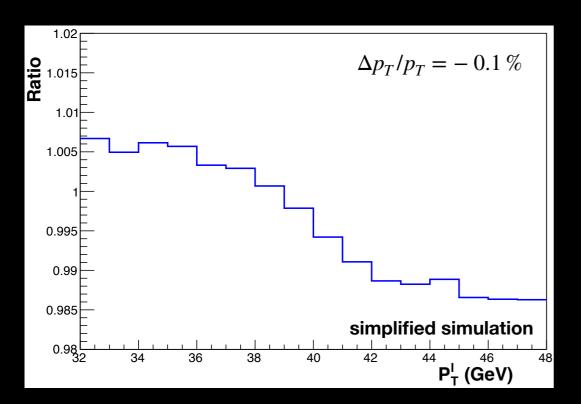




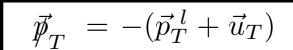
## **Calibrations**

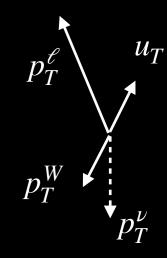


Charged lepton scale

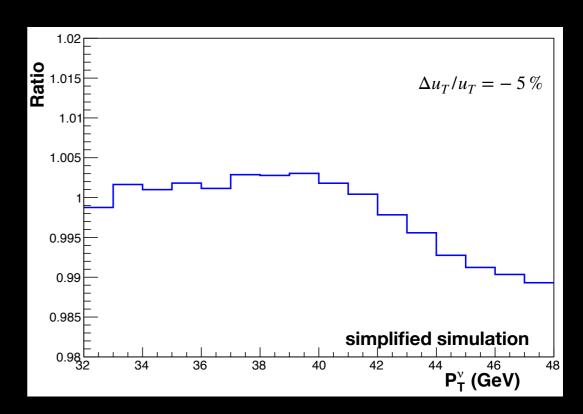


Measurement requires precise calibrations and momentum scale and resoution



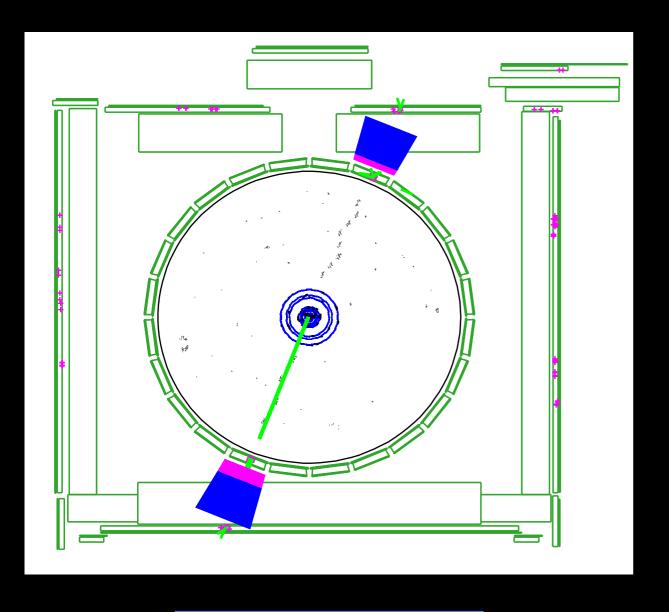


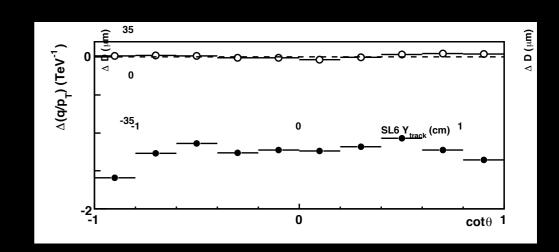
Recoil scale

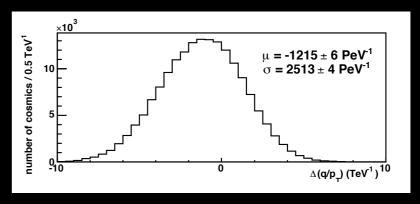


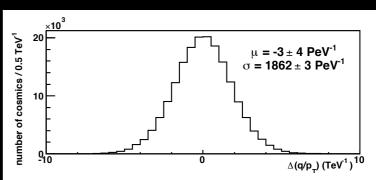
First step is to align the drift chamber (the "central outer tracker" or COT)

Two degrees of freedom (shift & rotation) for each of 2520 cells made up of twelve sense wires constrained using hit residuals from cosmic-ray tracks





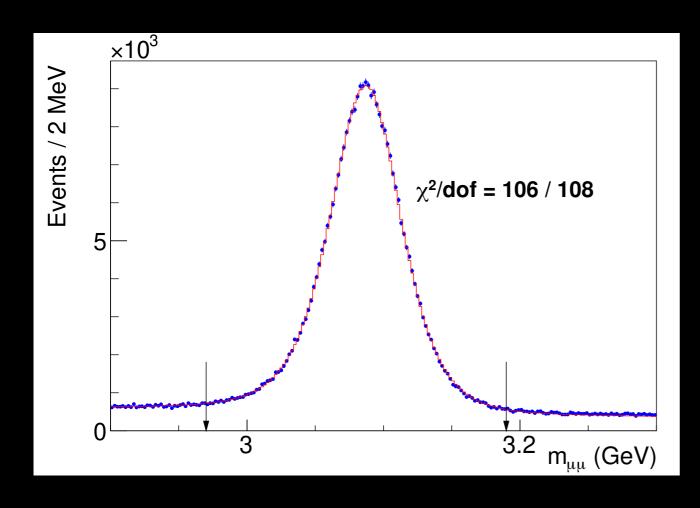


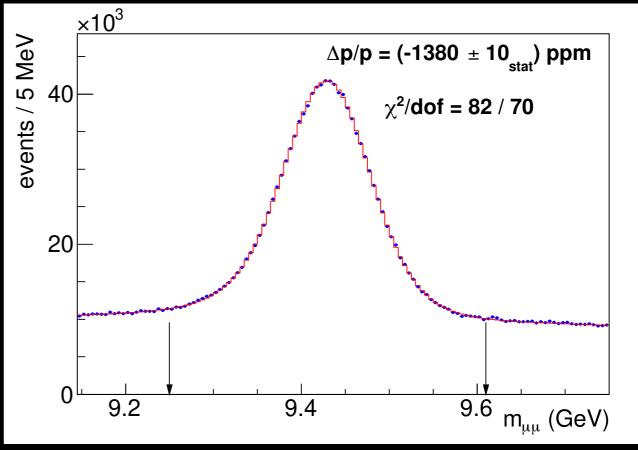


Second step is to calibrate the momentum scale using  $J/\psi$  and  $\Upsilon$  decays to muons

#### **Simulation:**

Adjust kinematics to match the data Model resonance shape using hit-level simulation and NLO form factor for QED radiation

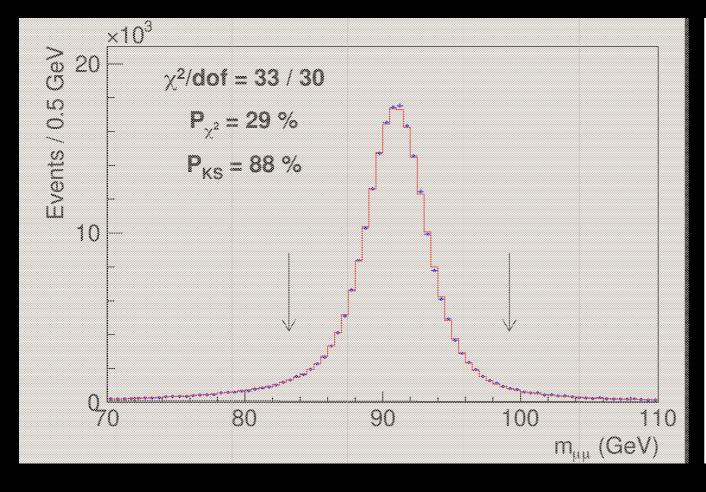


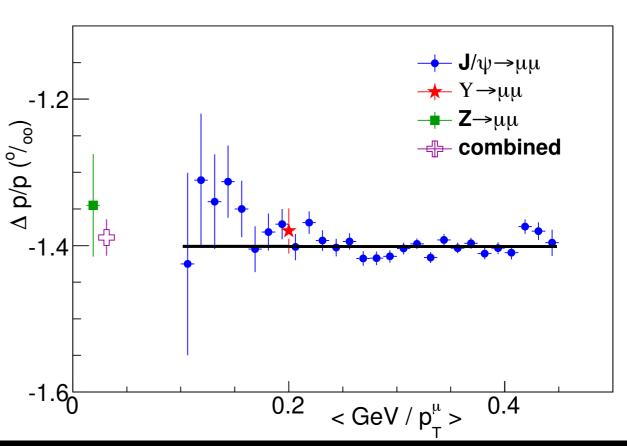


Final step is to measure the Z boson mass

$$M_Z = 91\ 192.0 \pm 6.4_{stat} \pm 4.0_{sys} \, \mathrm{MeV}$$

Result blinded with [-50,50] MeV offset until previous steps were complete Combine all measurements into a final charged-track momentum scale



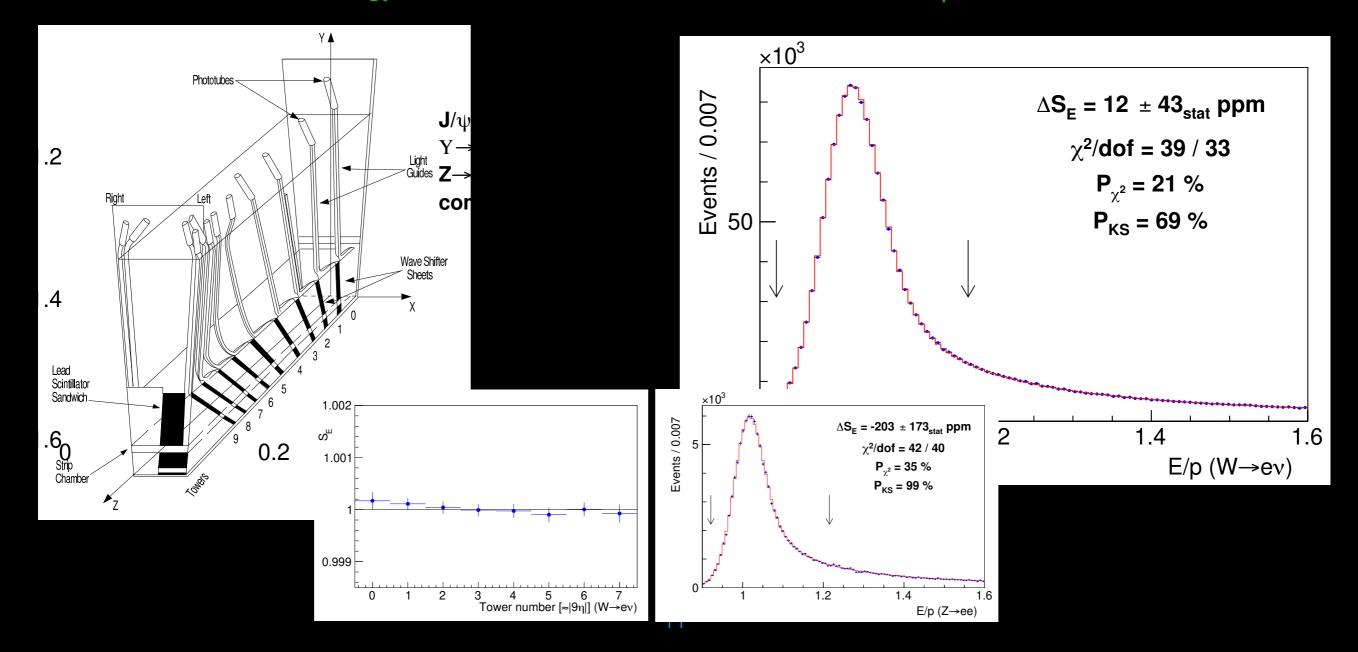


#### Electron momentum calibration

First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

#### **Data corrections:**

Use mean E/p to remove time dependence & response variations in tower Fit ratio of calorimeter energy to track momentum to correct each tower in  $\eta$ 



#### Electron momentum calibration

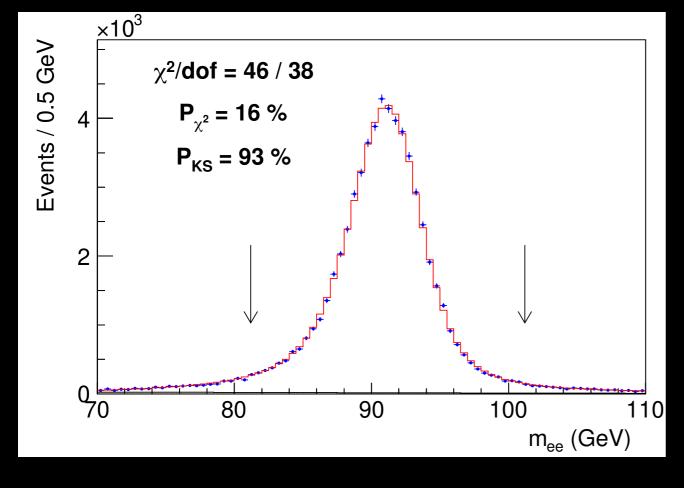
Second step is the measurement of the Z boson mass

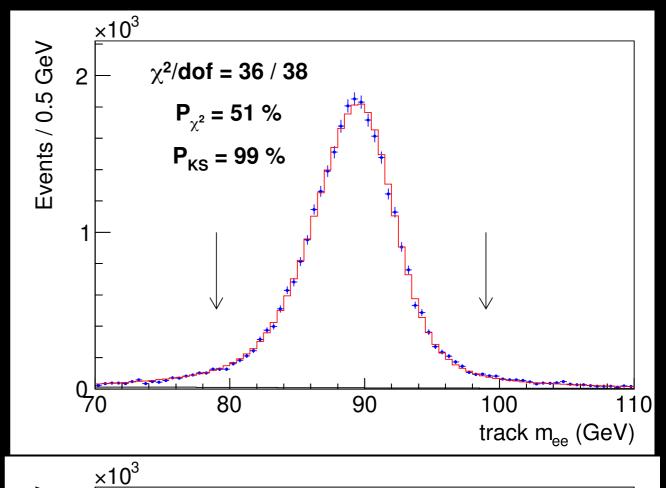
$$M_Z = 91\ 194.3 \pm 13.8_{stat} \pm 7.6_{sys} \text{ MeV}$$

As a consistency check measure mass using only track information

e.g.  $M_Z = 91\ 215.2 \pm 22.4$  MeV for non-radiative electrons (E/p<1.1)

Same blinding as for muon channel



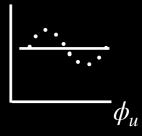


 $\chi^2/dof = 62 / 58$ 

#### Recoil momentum calibration

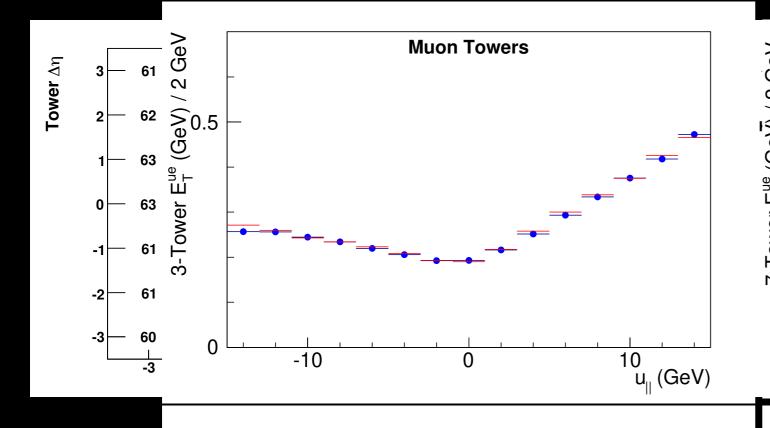
#### First step is the alignment of the calorimeters

Misalignments relative to the beam axis cause a modulation in the recoil direction Alignment performed separately for each run period using minimum-bias data



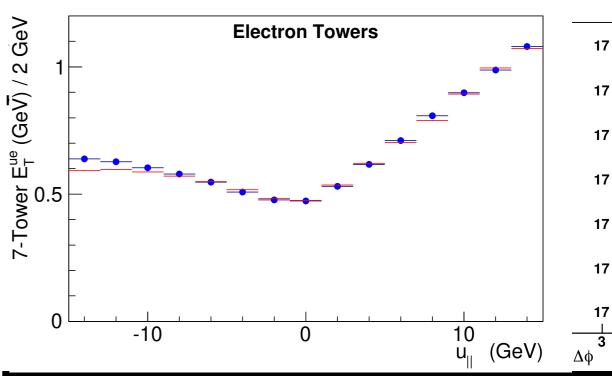
#### Second step is the reconstruction of the recoil

Remove towers traversed by identified leptons
Remove corresponding recoil energy in simulation using towers rotated by 90° validate using towers rotated by 180°



**Muon Towers** 

e<



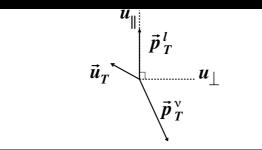
Flectron Towers

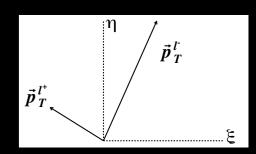
## Recoil momentum calibration

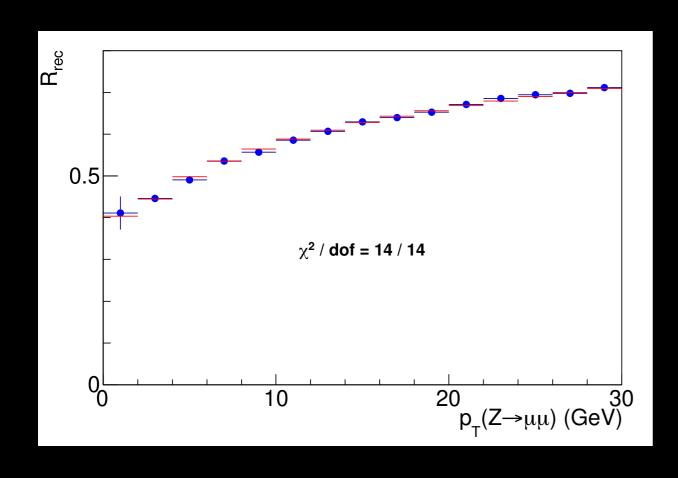
Third step is the calibration of the recoil response

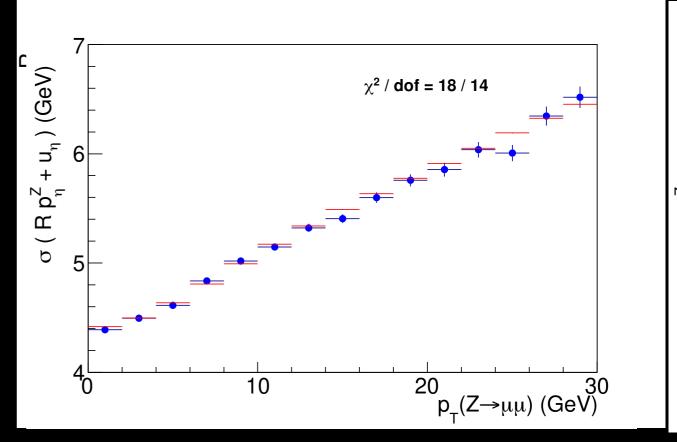
Balance recoil against direction of pTZ

Check calibration using ratio of recoil magnitude to p<sub>T</sub><sup>Z</sup> alor







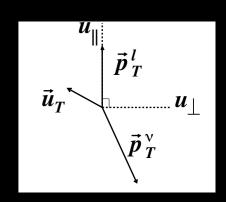


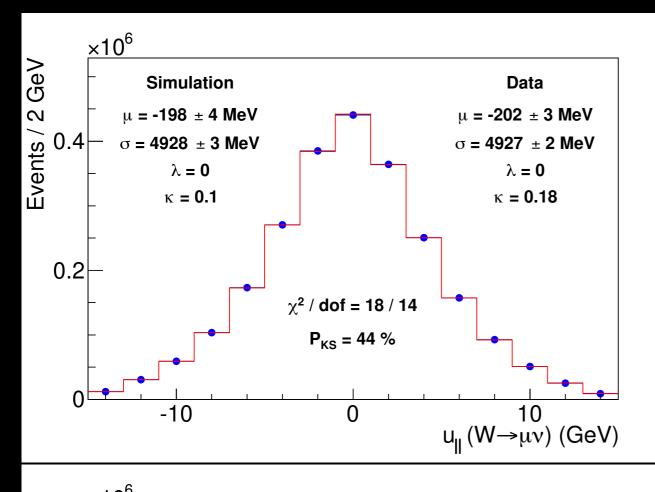
#### **Recoil momentum validation**

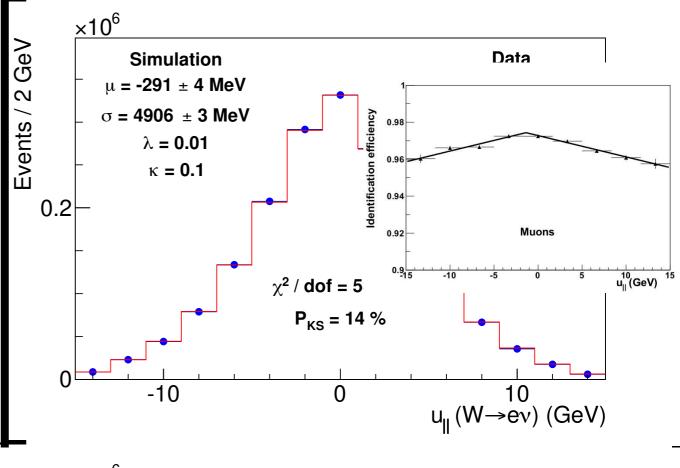
#### W boson recoil distributions validate the model

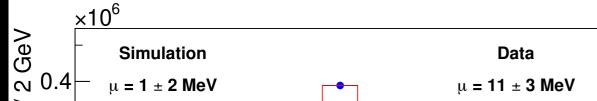
Most important is the recoil projected along the charged-lepton's momentum  $(u_{||})$ 

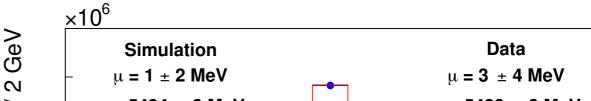
$$m_T \approx 2p_T \sqrt{1 + u_{||}/p_T} \approx 2p_T + u_{||}$$

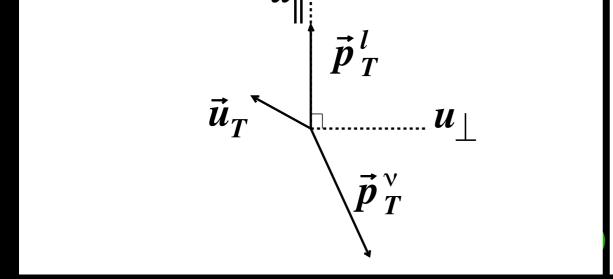


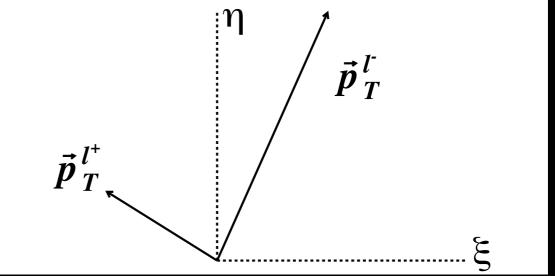






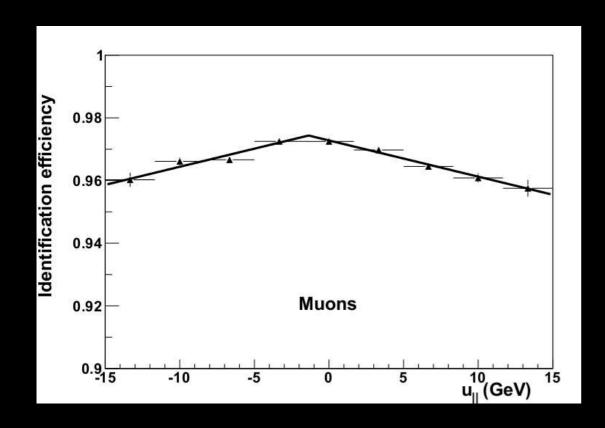




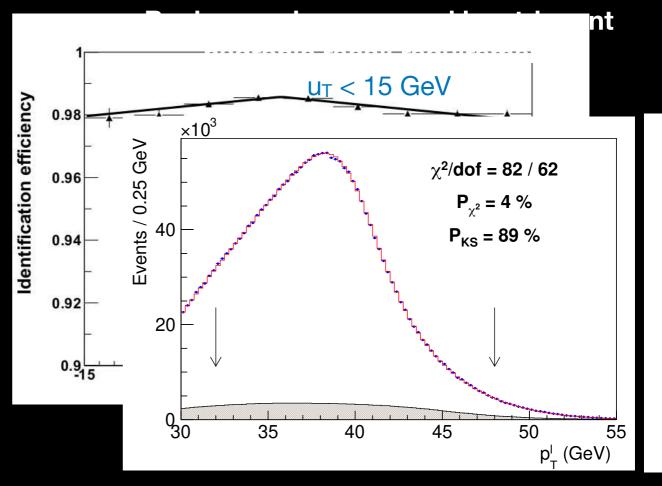


Offline id also loose, efficiencies vary by 2% as hadronic recoil direction changes

#### No lepton isolation requirement in trigger or offline selection



2.4 M  $W \to \mu \nu$  candidates 1.8 M  $W \to e \nu$  candidates



×10

Events / 0.25 GeV

Other kinematic requirements

Lepton and missing  $p_T$  in the range 30-55 GeV Transverse mass in the range 60-100 GeV

# Events / GeV

## W boson production

Transverse mass insensitive to  $p_T^{\hspace{-0.5mm}W}$  to first order

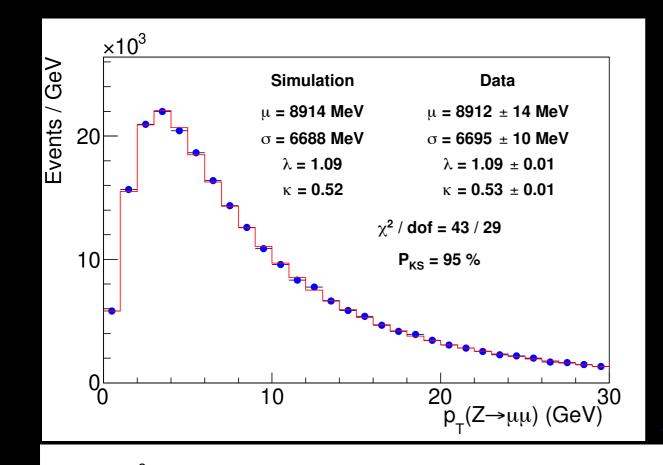
O(1 MeV) change in m<sub>W</sub> for each % change in p<sub>T</sub>W from 0-30 GeV

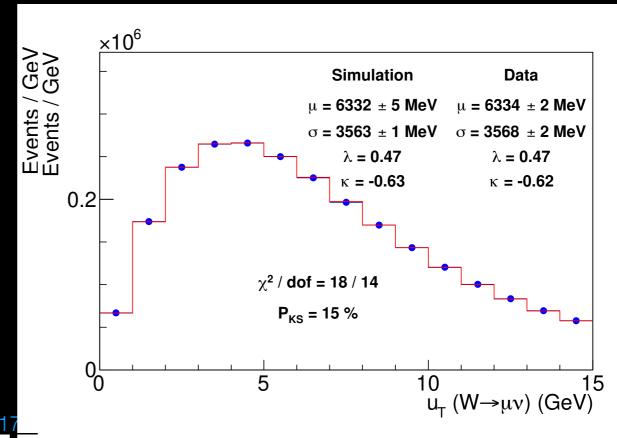
Lepton p<sub>T</sub> distributions more sensitive to p<sub>T</sub>W

Generate events with Resbos: non-perturbative parameters & NNLL resummation

Z boson p<sub>T</sub> used to constrain one non-perturbative parameter and the perturbative coupling

Parameterized Resbos model describes observed W boson recoil uncertainty estimated using DYQT and constrained with data





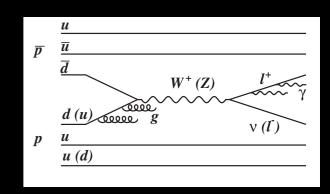
# W boson production and decay

Parton distributions impact the measurement through lepton acceptance

Restriction in  $\eta$  reduces the fraction of low-p<sub>T</sub> leptons

#### Small correction applied to update to NNPDF3.1 NNLO PDF

The set with the most W charge asymmetry measurements at the time



#### Uncertainty determined using a principal component analysis on the replica set

Measurement sensitive to ~15 eigenvectors

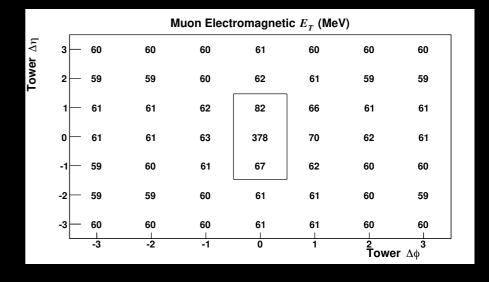
Leading 25 eigenvectors used to estimate uncertainty (3.9 MeV)

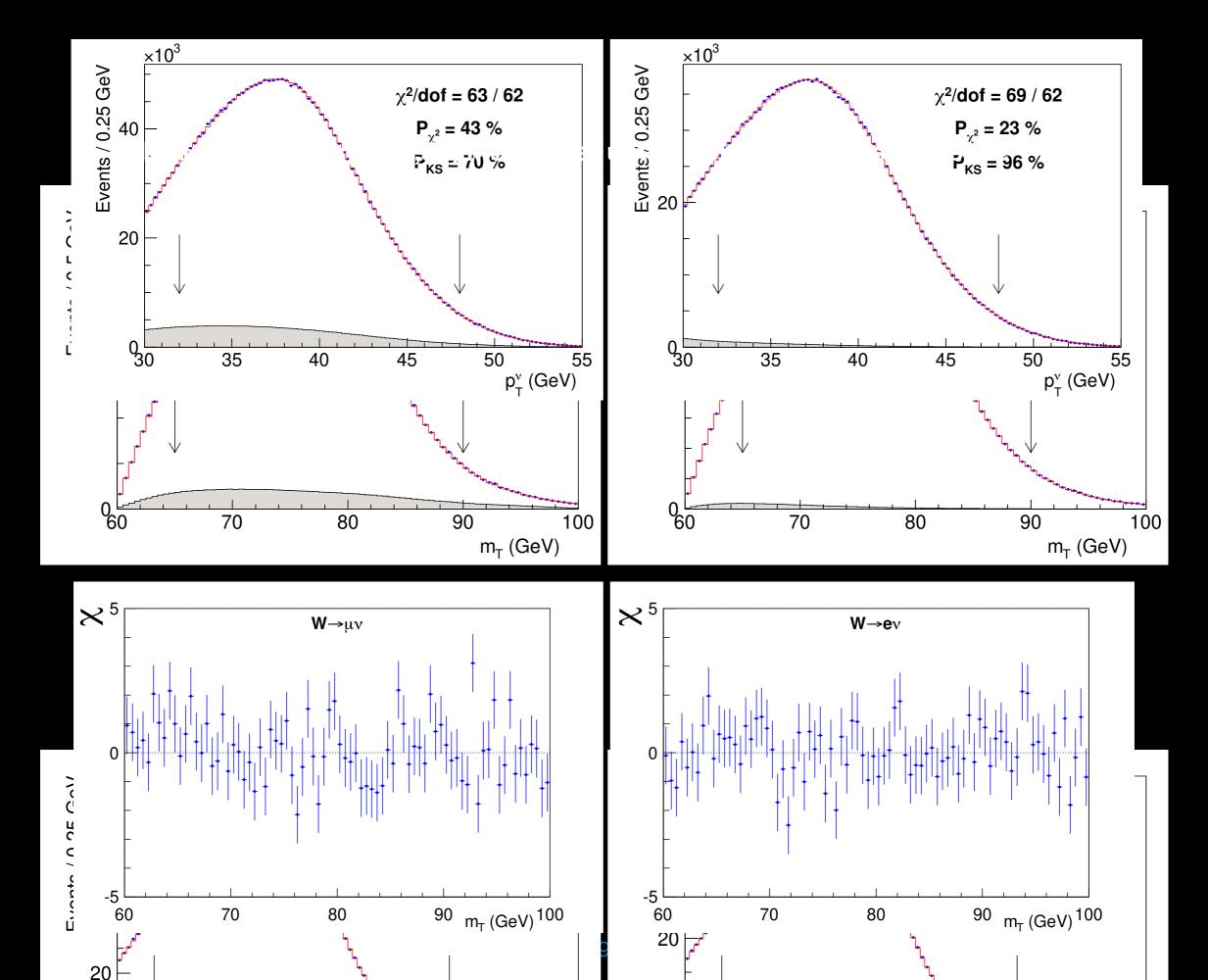
Three general NNLO PDF sets (NNPDF3.1, CT18, and MMHT14) have a range of  $\pm 2.1$  MeV from mean

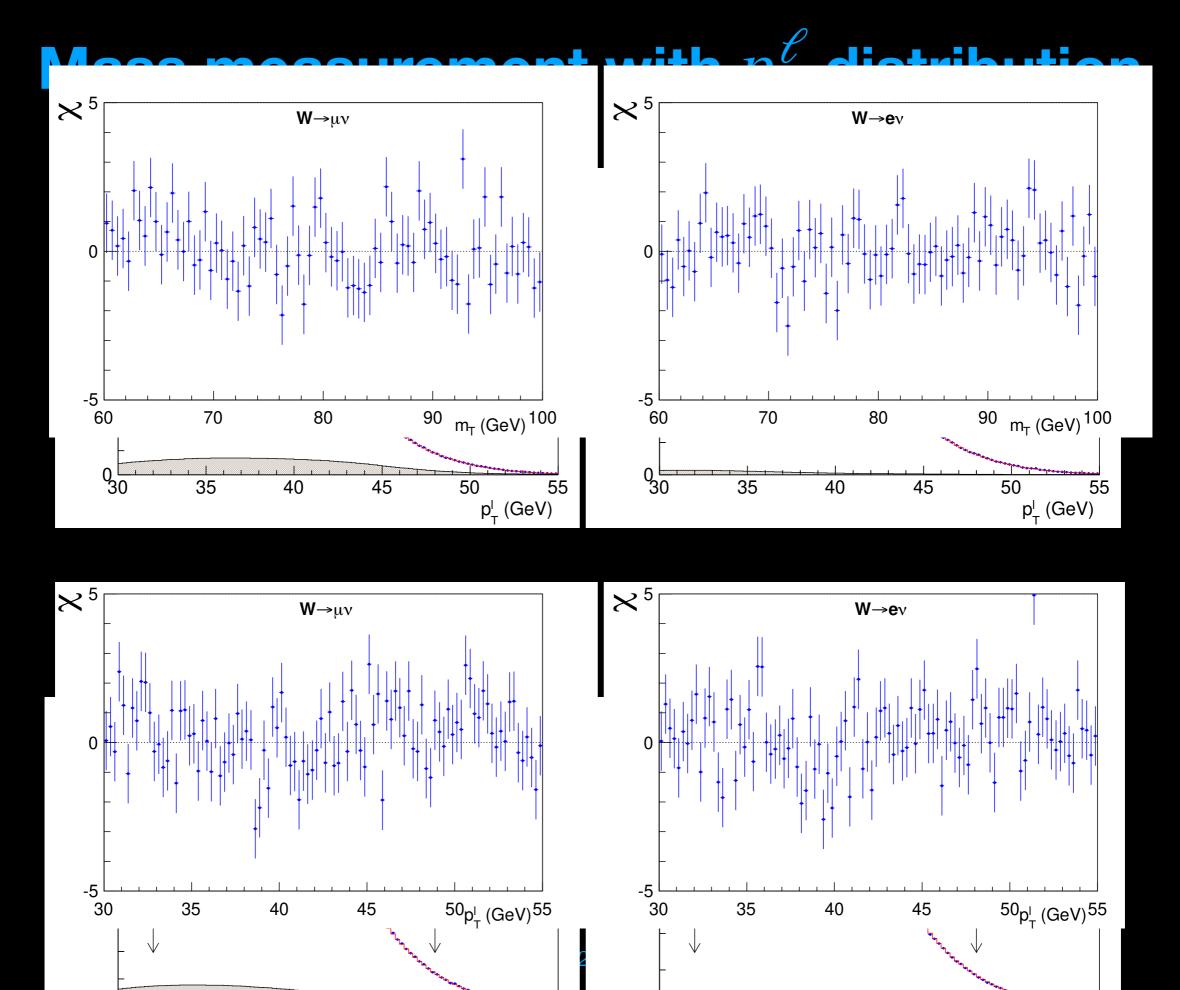
#### Photos resummation with ME corrections used to model final-state photon radiation

validated by studying the average radiation in EM towers around the charged lepton,

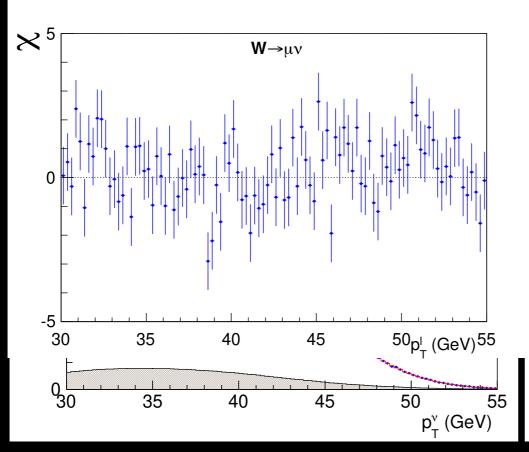
and with the Z mass measurement

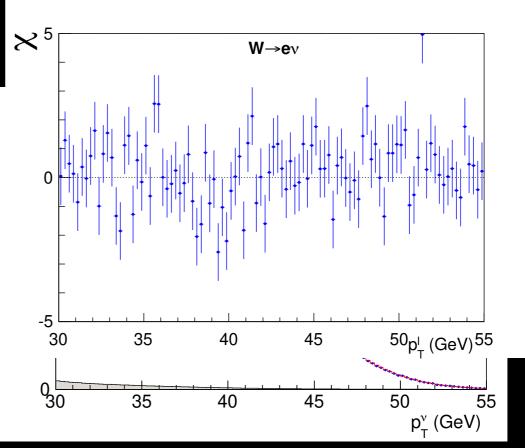


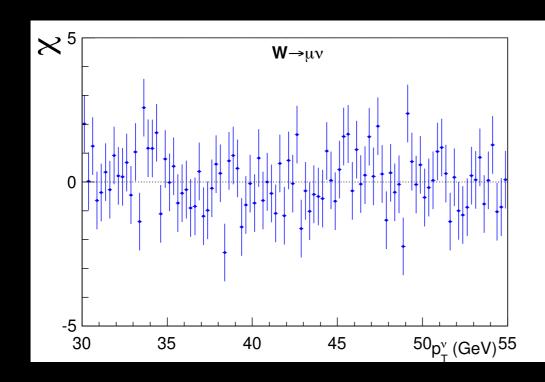


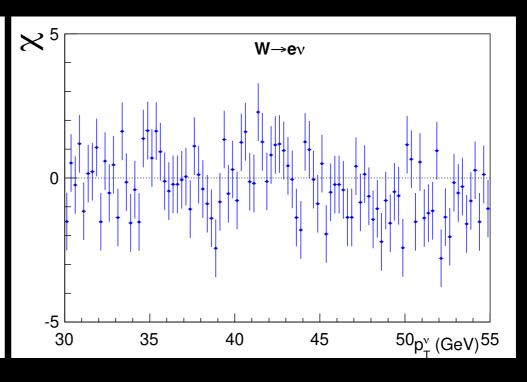


## Mass measurement with $p_{T}^{\nu}$ distribution









# W boson mass measurement

Combination	$m_T$ :	fit	$p_T^\ell$ f	it	$p_T^ u$ fi	t	Value (MeV)	$\chi^2/\mathrm{dof}$	Probability
	Electrons	Muons	Electrons	Muons	Electrons	Muons			(%)
$\overline{m_T}$	✓	<b>√</b>					$80\ 439.0 \pm 9.8$	1.2 / 1	28
$p_T^\ell$			✓	$\checkmark$			$80\ 421.2 \pm 11.9$	0.9 / 1	36
$p_T^{ u}$					✓	$\checkmark$	$80\ 427.7 \pm 13.8$	0.0 / 1	91
$m_T \ \& \ p_T^\ell$	✓	$\checkmark$	✓	$\checkmark$			$80\ 435.4 \pm 9.5$	4.8 / 3	19
$m_T~\&~p_T^{ u}$	✓	$\checkmark$			✓	$\checkmark$	$80\ 437.9 \pm 9.7$	2.2  / 3	53
$p_T^\ell \ \& \ p_T^ u$			✓	$\checkmark$	$\checkmark$	$\checkmark$	$80\ 424.1 \pm 10.1$	1.1 / 3	78
Electrons	✓		✓		$\checkmark$		$80\ 424.6 \pm 13.2$	3.3 / 2	19
Muons		$\checkmark$		$\checkmark$		$\checkmark$	$80\ 437.9 \pm 11.0$	3.6 / 2	17
All	✓	$\checkmark$	✓	$\checkmark$	<b>√</b>	$\checkmark$	$80\ 433.5 \pm 9.4$	7.4 / 5	20

Fit difference	Muon channel	Electron channel
$\overline{M_W(\ell^+)} - M_W(\ell^-)$	$-7.8\pm18.5_{\mathrm{stat}}\pm12.7_{\mathrm{COT}}$	$14.7 \pm 21.3_{\rm stat} \pm 7.7_{\rm stat}^{\rm E/p} \ (0.4 \pm 21.3_{\rm stat})$
$M_W(\phi_\ell > 0) - M_W(\phi_\ell < 0)$	$24.4 \pm 18.5_{\rm stat}$	$9.9 \pm 21.3_{\rm stat} \pm 7.5_{\rm stat}^{\rm E/p} \ (-0.8 \pm 21.3_{\rm stat})$
$M_Z(\text{run} > 271100) - M_Z(\text{run} < 271100)$	$5.2 \pm 12.2_{\rm stat}$	$63.2 \pm 29.9_{\rm stat} \pm 8.2_{\rm stat}^{\rm E/p} \ (-16.0 \pm 29.9_{\rm stat})$

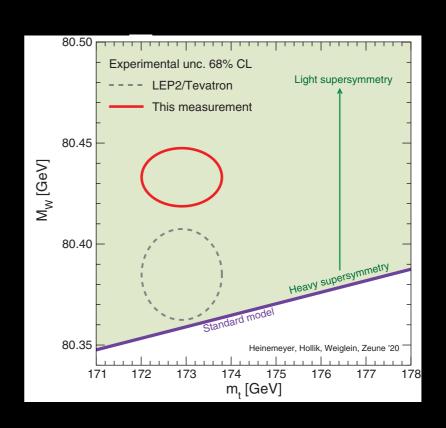
## Summary

#### The W boson mass is a sensitive quantity to high-scale physics

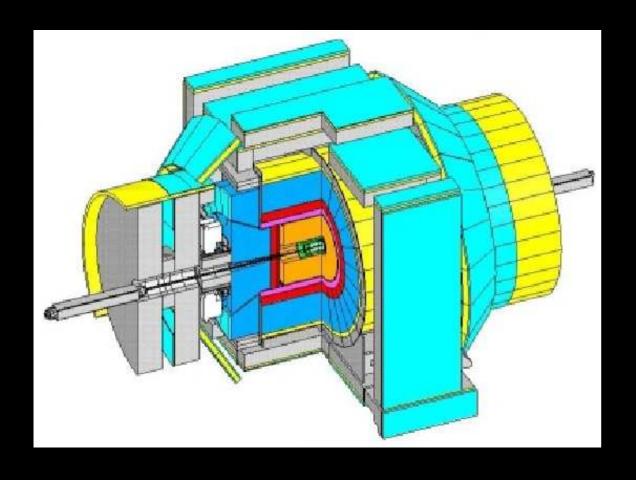
A measurement of mw with <10 MeV precision has been achieved with the complete CDF data set The result of >20 years of experience with the CDF II detector

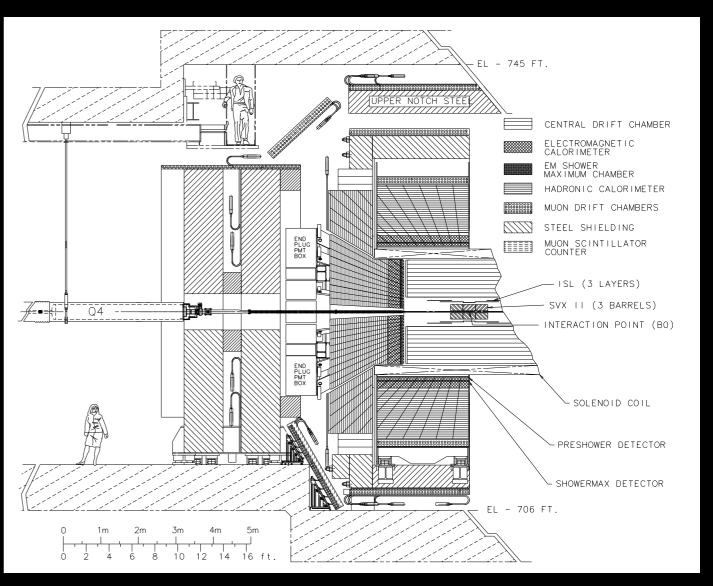
Measured mass deviates from the SM by ~0.1% with high significance

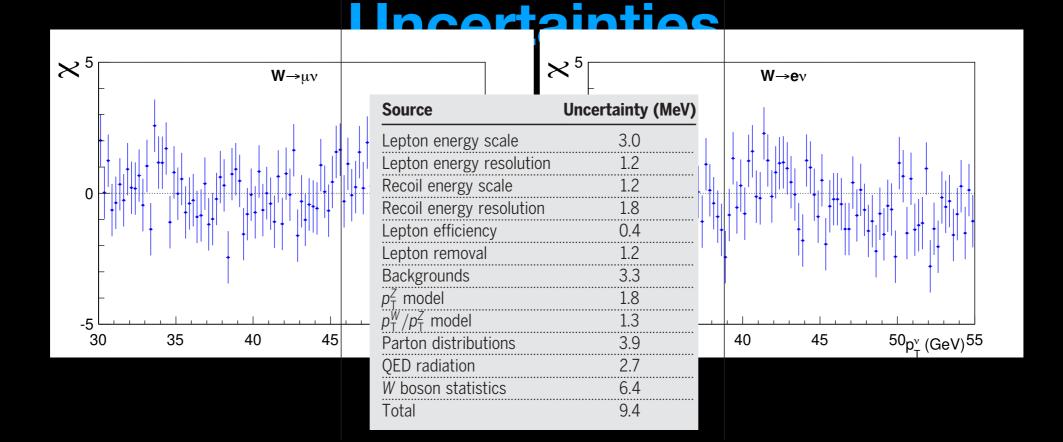
Distribution	W boson mass (MeV)	$\chi^2$ /dof
$m_{T}(e,v)$	$80,429.1 \pm 10.3_{stat} \pm 8.5_{syst}$	39/48
$p_{T}^{\ell}(e)$	80,411.4 ± 10.7 <sub>stat</sub> ± 11.8 <sub>syst</sub>	83/62
$p_{\mathrm{T}}^{\mathrm{v}}(e)$	80,426.3 ± 14.5 <sub>stat</sub> ± 11.7 <sub>syst</sub>	69/62
$m_{T}(\mu, \mathbf{v})$	80,446.1 ± 9.2 <sub>stat</sub> ± 7.3 <sub>syst</sub>	50/48
$ ho_{T}^{\ell}(\mu)$	80,428.2 ± 9.6 <sub>stat</sub> ± 10.3 <sub>syst</sub>	82/62
$p_{\mathrm{T}}^{\mathrm{v}}(\mu)$	80,428.9 ± 13.1 <sub>stat</sub> ± 10.9 <sub>syst</sub>	63/62
Combination	80,433.5 ± 6.4 <sub>stat</sub> ± 6.9 <sub>syst</sub>	7.4/5



# Backup







Source of systematic		$m_T$ fit			$p_T^\ell$ fit			$p_T^{\nu}$ fit	
uncertainty	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton energy scale	5.8	2.1	1.8	5.8	2.1	1.8	5.8	2.1	1.8
Lepton energy resolution	0.9	0.3	-0.3	0.9	0.3	-0.3	0.9	0.3	-0.3
Recoil energy scale	1.8	1.8	1.8	3.5	3.5	3.5	0.7	0.7	0.7
Recoil energy resolution	1.8	1.8	1.8	3.6	3.6	3.6	5.2	5.2	5.2
Lepton $u_{  }$ efficiency	0.5	0.5	0	1.3	1.0	0	2.6	2.1	0
Lepton removal	1.0	1.7	0	0	0	0	2.0	3.4	0
Backgrounds	2.6	3.9	0	6.6	6.4	0	6.4	6.8	0
$p_T^Z \text{ model}$	0.7	0.7	0.7	2.3	2.3	2.3	0.9	0.9	0.9
$p_T^W/p_T^Z$ model	0.8	0.8	0.8	2.3	2.3	2.3	0.9	0.9	0.9
Parton distributions	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9	3.9
QED radiation	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7	2.7
Statistical	10.3	9.2	0	10.7	9.6	0	14.5	13.1	0
Total	13.5	11.8	5.8	16.0	14.1	7.9	18.8	17.1	7.4
					<u> </u>				

# **Background fractions**

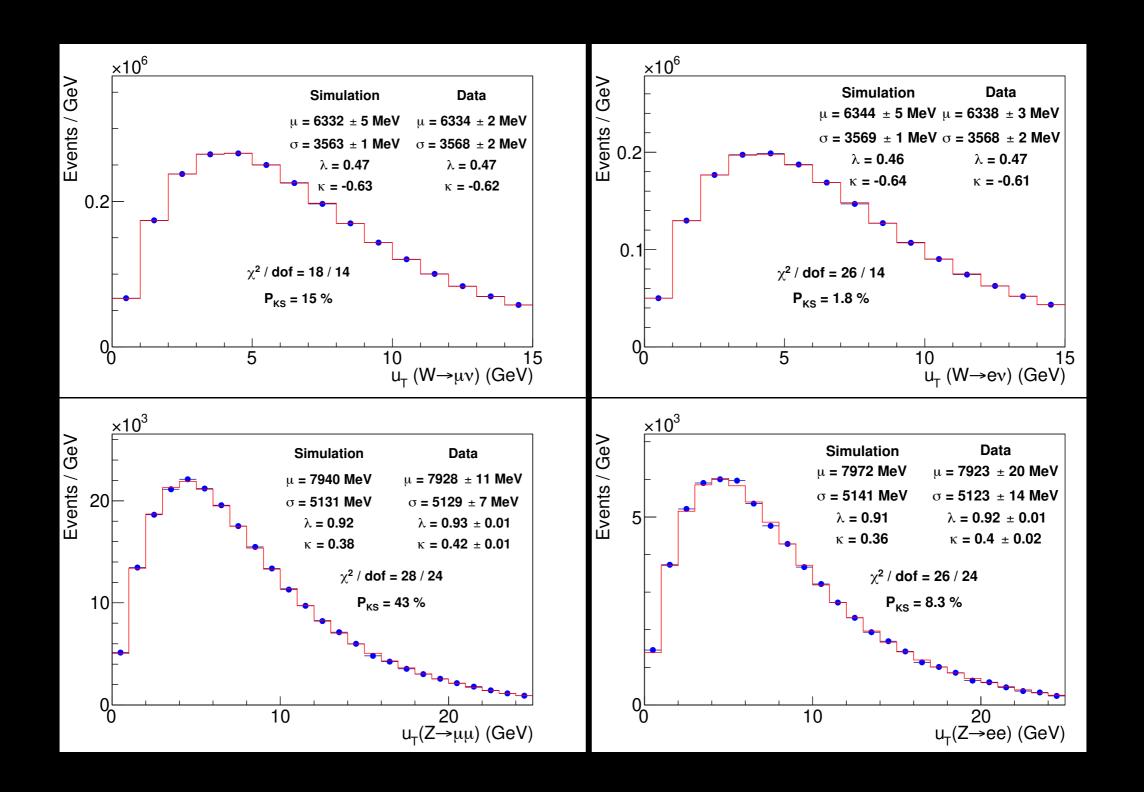
	Fraction	8	$\delta M_W \; ({ m MeV})$	7)
Source	(%)	$m_T$ fit	$p_T^\mu$ fit	$p_T^{\nu}$ fit
$Z/\gamma^* \to \mu\mu$	$7.37 \pm 0.10$	1.6(0.7)	3.6(0.3)	0.1(1.5)
$W \to  au  u$	$0.880\pm0.004$	0.1(0.0)	0.1(0.0)	0.1(0.0)
Hadronic jets	$0.01 \pm 0.04$	0.1(0.8)	-0.6 (0.8)	2.4 (0.5)
Decays in flight	$0.20 \pm 0.14$	1.3(3.1)	1.3(5.0)	-5.2 (3.2)
Cosmic rays	$0.01 \pm 0.01$	0.3(0.0)	0.5(0.0)	0.3(0.3)
Total	$8.47 \pm 0.18$	$2.\overline{1} (3.3)$	3.9 (5.1)	$5.\overline{7} (3.6)$

	Fraction	$\delta M_W \; ({ m MeV})$				
Source	(%)	$m_T$ fit	$p_T^e$ fit	$p_T^{\nu}$ fit		
$Z/\gamma^* \to ee$	$0.134 \pm 0.003$	0.2 (0.3)	0.3 (0.0)	0.0 (0.6)		
W  o  au  u	$0.94 \pm 0.01$	0.6(0.0)	0.6(0.0)	0.6(0.0)		
Hadronic jets	$0.34 \pm 0.08$	2.2(1.2)	0.9(6.5)	6.2 (-1.1)		
Total	$1.41 \pm 0.08$	2.3 (1.2)	1.1 (6.5)	6.2 (1.3)		
	<u> </u>					

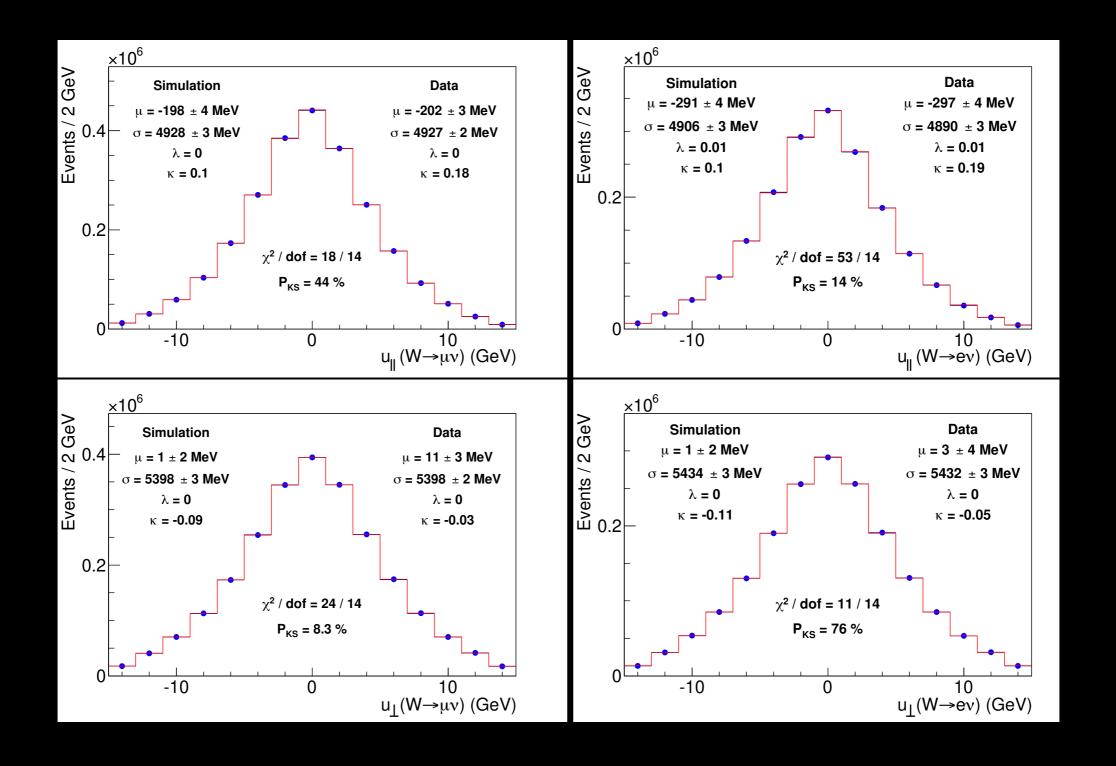
# **Initial state LO & NLO**

W+ initial	Туре	Pythia LO	Madgraph LO	Madgraph NLO
u dbar	V-V	81.7%	82.0%	82.7%
dbar u	S-S	8.9%	9.0%	8.8%
u sbar	V-S	1.6%	1.9%	1.8%
sbar u	S-S	0.3%	0.3%	0.3%
c sbar	S-S	2.9%	2.9%	-
sbar c	S-S	2.9%	2.9%	-
c dbar	S-V	0.7%	0.7%	-
dbar c	S-S	0.2%	0.2%	-
u g	v-g		-	3.7%
g dbar	g-v		-	1.8%
g u	g-s		-	0.4%
dbar g	s-g		-	0.5%
g sbar	g-s		_	0.02%
sbar g	s-g		-	0.02%

## Recoil in W & Z events



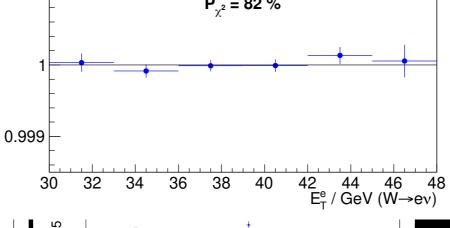
# Recoil projections in W events

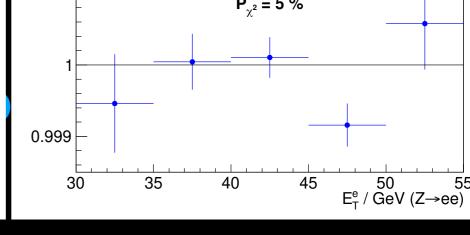


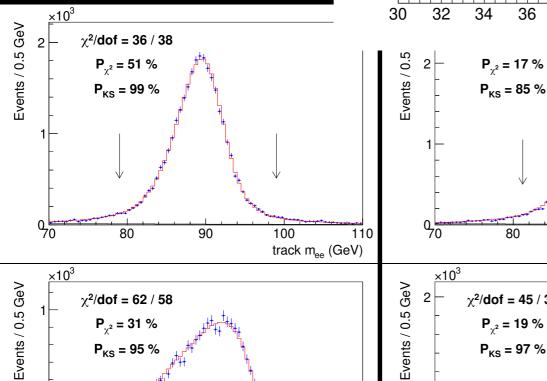
# Recoil model parameters

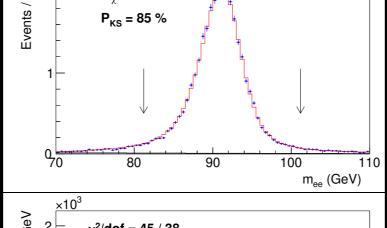
Parameter	Description	Source	$m_T$	$p_T^\ell$	$p_T^{ u}$
a	average response	Fig. S23	-1.6	-2.9	-0.2
b	response non-linearity	Fig. S23	-0.8	-2.0	0.7
Response			1.8	3.5	0.7
$N_V$	spectator interactions	Fig. S24	0.5	-3.2	3.6
$s_{ m had}$	sampling resolution	Fig. S24	0.3	0.3	0.8
$f_{\pi^0}^4$	EM fluctuations at low $u_T$	Fig. S25	-0.3	-0.2	-1.0
$f_{\pi^0}^{15}$	EM fluctuations at high $u_T$	Fig. S25	-0.3	-0.3	-0.2
$\alpha$	angular resolution at low $u_T$	Fig. S26	1.4	0.1	2.5
$\beta$	angular resolution at intermediate $u_T$	Fig. S26	0.2	0.1	0.7
$\gamma$	angular resolution at high $u_T$	Fig. S26	0.3	0.3	0.7
$f_2^a$	average dijet component	Fig. S27	0.1	-1.1	0.8
$f_2^s$	variation of dijet component with $u_T$	Fig. S27	-0.1	-0.2	-0.1
$k_{\xi}$	average dijet resolution	Fig. S28	-0.1	0.1	-0.3
$\delta_{\xi}$	fluctuations in dijet resolution	Fig. S28	-0.2	0.2	-1.1
$A_{\xi}$	higher-order term in dijet resolution	Fig. S28	0.1	-1.0	0.7
$\mu_{\xi}$		Fig. S28	-0.5	-0.4	-0.9
$\epsilon_{\xi}$		Fig. S28	0.1	-0.2	0.4
$S_{\xi}^{+}$		Fig. S28	0.5	-0.4	1.4
$S_{\xi}^{-}$		Fig. S28	-0.3	-0.2	-0.5
$q_{\xi}$		Fig. S28	-0.2	0.0	0.2
Resolution			1.8	3.6	5.2

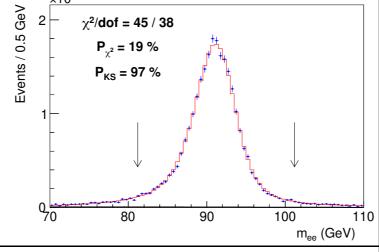
# Z mass fit

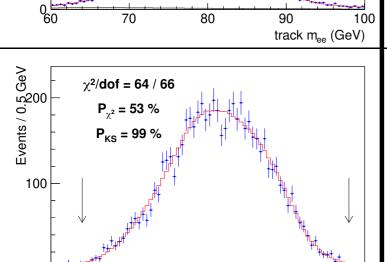












70

80

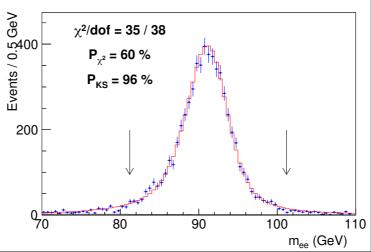
 $track \; m_{ee} \; (GeV)$ 

 $P_{\chi^2} = 31 \%$ 

P<sub>KS</sub> = 95 %

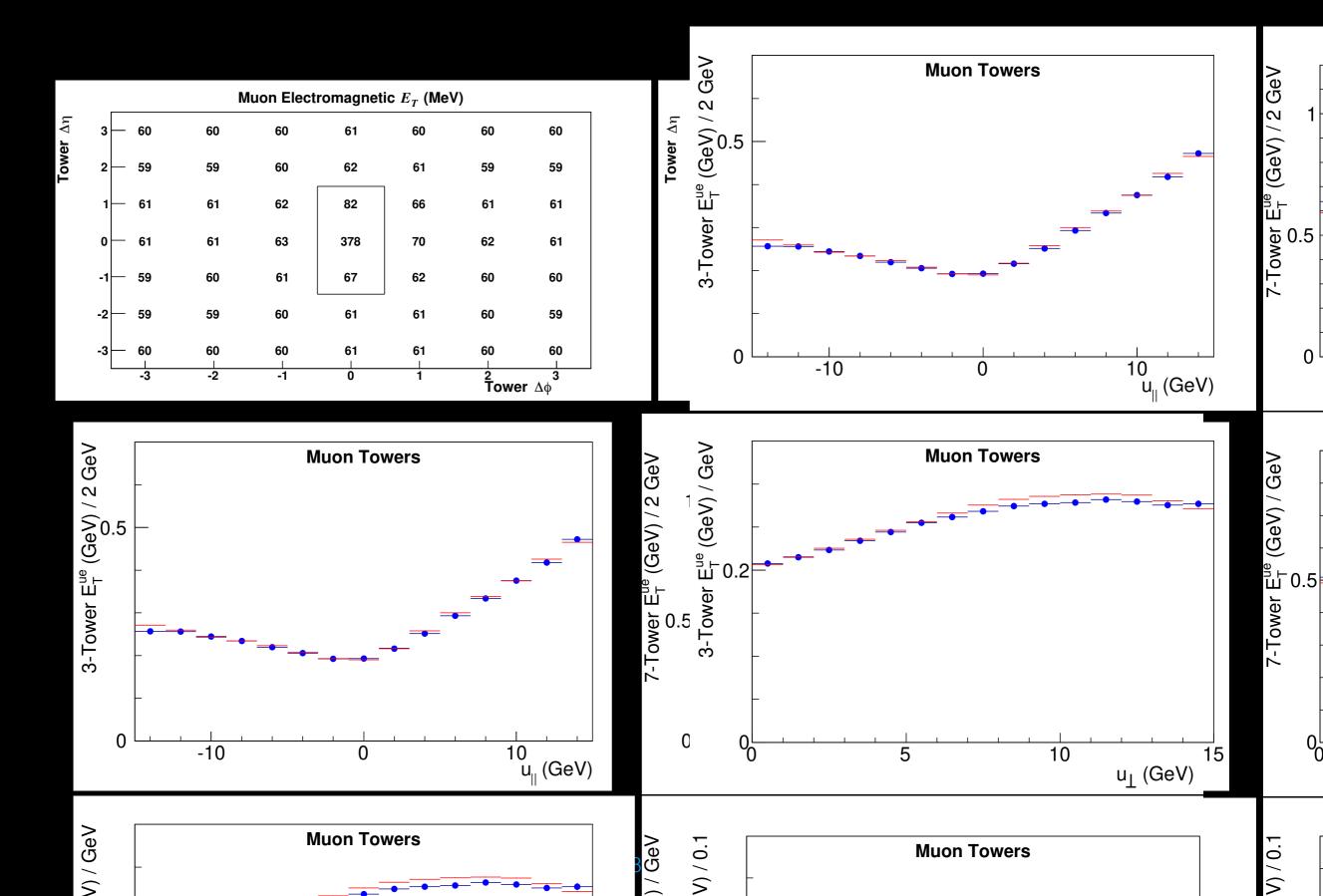
60

0.5

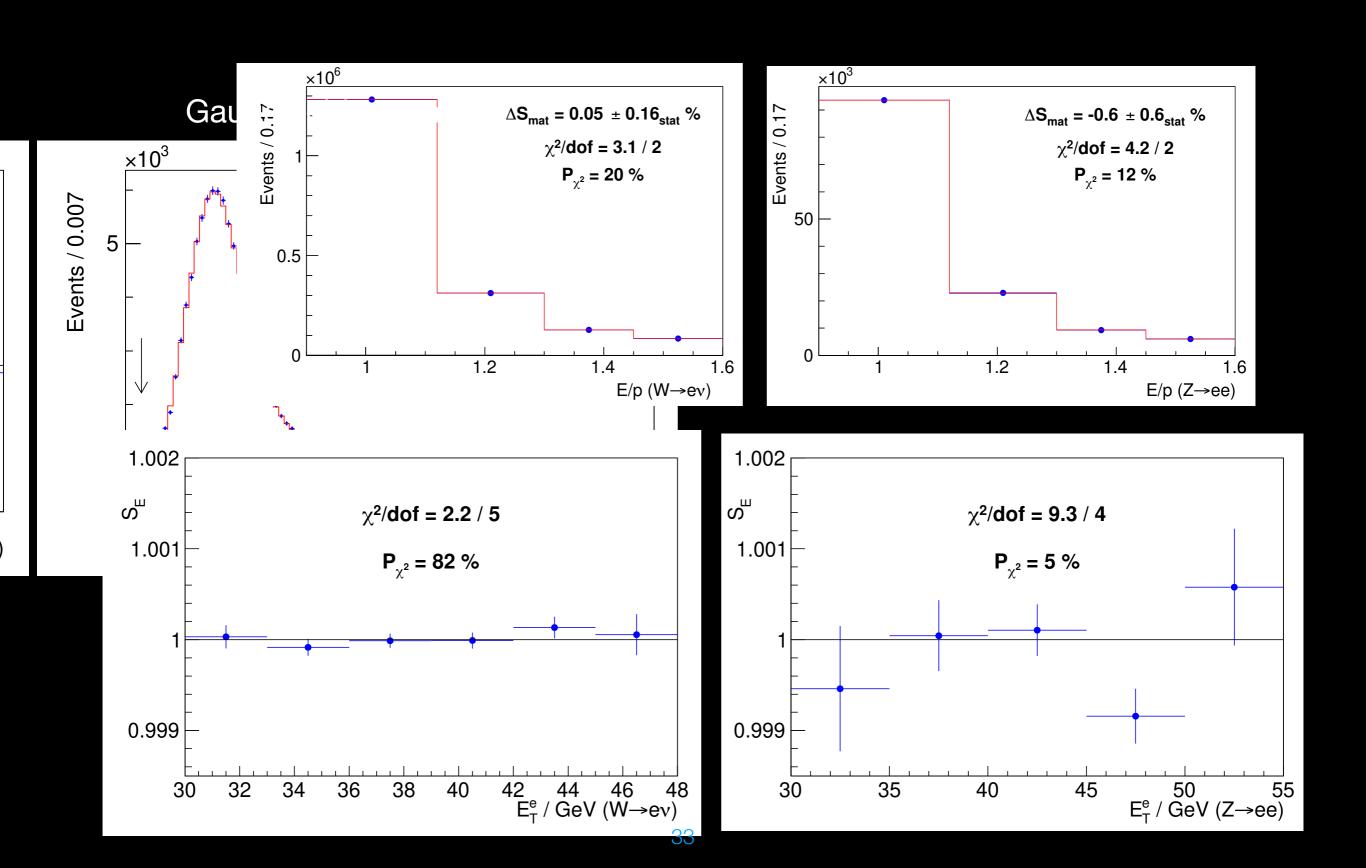


Electrons	Calorimeter	Track
E/p < 1.1 only	$91190.9\pm19.7$	$91215.2\pm22.4$
E/p > 1.1 and $E/p < 1.1$	$91201.1\pm21.5$	$91259.9 \pm 39.0$
E/p > 1.1 only	$91184.5 \pm 46.4$	$91167.7\pm109.9$

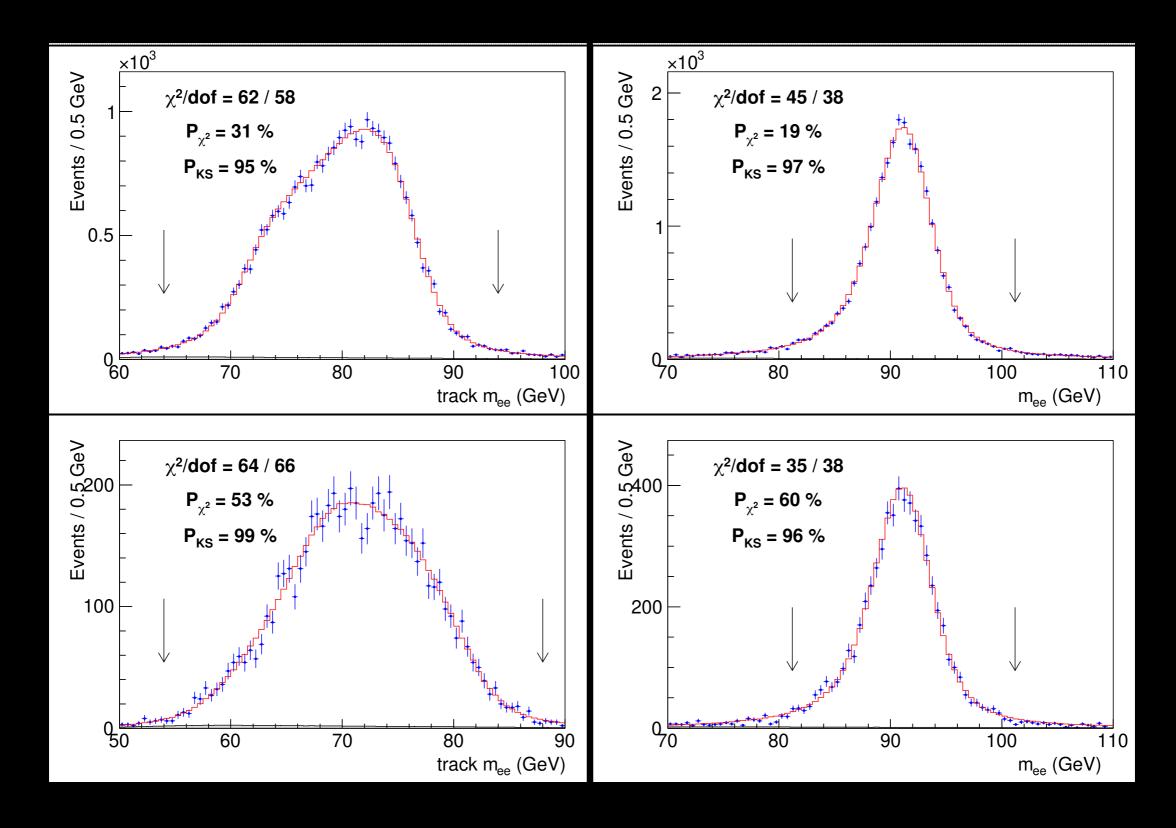
## Recoil reconstruction in muon channel



### **Electron momentum calibration**



## Electron momentum calibration



Source	$J/\psi \text{ (ppm)}$	Υ (ppm)	Correlation (%)
QED	1	1	100
Magnetic field non-uniformity	13	13	100
Ionizing material correction	11	8	100
Resolution model	10	1	100
Background model	7	6	0
COT alignment correction	4	8	0
Trigger efficiency	18	9	100
Fit range	2	1	100
$\Delta p/p$ step size	2	2	0
World-average mass value	4	27	0
Total systematic	29	34	16 ppm
Statistical NBC (BC)	2	13(10)	0
Total	29	36	16 ppm

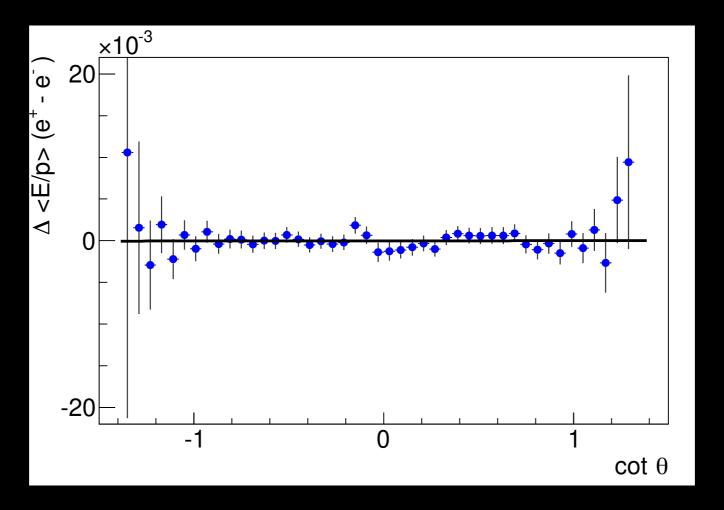
#### Track momentum calibration

Residual tracker misalignments studied using difference in E/p between electrons and positrons

Correction as a function of polar angle applied to measured tracks from W and Z decays

Linear dependence on cot theta would cause a bias in the mw mass fit

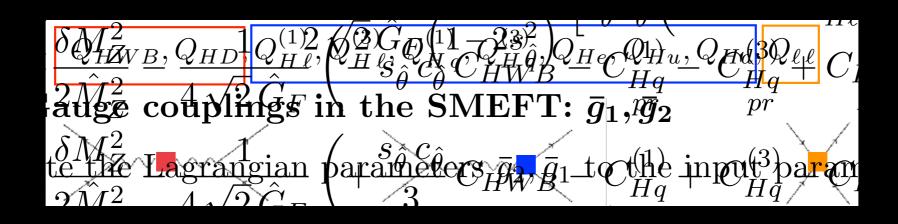
No linear correction required, statistical precision from E/p constrains the bias to <0.8 MeV



## Measurement updates

Method or technique	impact
Detailed treatment of parton distribution functions	+3.5  MeV
Resolved beam-constraining bias in CDF reconstruction	+10 MeV
Improved COT alignment and drift model [65]	uniformity
Improved modeling of calorimeter tower resolution	uniformity
Temporal uniformity calibration of CEM towers	uniformity
Lepton removal procedure corrected for luminosity	uniformity
Higher-order calculation of QED radiation in $J/\psi$ and $\Upsilon$ decays	accuracy
Modeling kurtosis of hadronic recoil energy resolution	accuracy
Improved modeling of hadronic recoil angular resolution	accuracy
Modeling dijet contribution to recoil resolution	accuracy
Explicit luminosity matching of pileup	accuracy
Modeling kurtosis of pileup resolution	accuracy
Theory model of $p_T^W/p_T^Z$ spectrum ratio	accuracy
Constraint from $p_T^W$ data spectrum	robustness
Cross-check of $p_T^Z$ tuning	robustness

### Electroweak observables at dimension 6



Parameter	Input Value
$\hat{m}_Z$	$91.1875 \pm 0.0021$
$\hat{G}_F$	$1.1663787(6) \times 10^{-5}$
$\hat{lpha}_{ew}$	1/137.035999074(94)

$$\frac{\delta m_W^2}{\hat{m}_W^2} = \hat{\Delta} \left[ 4 C_{HWB} + \frac{c_{\hat{\theta}}}{s_{\hat{\theta}}} C_{HD} + 4 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{H\ell}^{(3)} - 2 \frac{s_{\hat{\theta}}}{c_{\hat{\theta}}} C_{\ell \ell} \right]$$

Experimental Value	Ref.	SM Theoretical Value	Ref.
$91.1875 \pm 0.0021$	[19]	_	_
$80.385 \pm 0.015$	[49]	$80.365 \pm 0.004$	[50]
$2.4952 \pm 0.0023$	[19]	$2.4942 \pm 0.0005$	[48]
$20.767 \pm 0.025$	[19]	$20.751 \pm 0.005$	[48]
$0.1721 \pm 0.0030$	[19]	$0.17223 \pm 0.00005$	[48]
$0.21629 \pm 0.00066$	[19]	$0.21580 \pm 0.00015$	[48]
$41.540 \pm 0.037$	[19]	$41.488 \pm 0.006$	[48]
$0.0171 \pm 0.0010$	[19]	$0.01616 \pm 0.00008$	[32]
$0.0707 \pm 0.0035$	[19]	$0.0735 \pm 0.0002$	[32]
$0.0992 \pm 0.0016$	[19]	$0.1029 \pm 0.0003$	[32]
	$91.1875 \pm 0.0021$ $80.385 \pm 0.015$ $2.4952 \pm 0.0023$ $20.767 \pm 0.025$ $0.1721 \pm 0.0030$ $0.21629 \pm 0.00066$ $41.540 \pm 0.037$ $0.0171 \pm 0.0010$ $0.0707 \pm 0.0035$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$



## W boson mass fit results

Distribution	W-boson mass (MeV)	$\chi^2/\mathrm{dof}$
$m_T(e, u)$	$80\ 429.1 \pm 10.3_{\rm stat} \pm 8.5_{\rm syst}$	39/48
$p_T^\ell(e)$	$80\ 411.4 \pm 10.7_{\rm stat} \pm 11.8_{\rm syst}$	83/62
$p_T^{ u}(e)$	$80\ 426.3 \pm 14.5_{\rm stat} \pm 11.7_{\rm syst}$	69/62
$m_T(\mu, u)$	$80\ 446.1 \pm 9.2_{\rm stat} \pm 7.3_{\rm syst}$	50/48
$p_T^\ell(\mu)$	$80\ 428.2 \pm 9.6_{\rm stat} \pm 10.3_{\rm syst}$	82/62
$p_T^{ u}(\mu)$	$80\ 428.9 \pm 13.1_{\rm stat} \pm 10.9_{\rm syst}$	63/62
combination	$80\ 433.5 \pm 6.4_{\rm stat} \pm 6.9_{\rm syst}$	7.4/5

Distribution	$M_W$ (MeV)	$\chi^2/\text{d.o.f}$
$W \to e\nu$		
$m_T$	$80408 \pm 19$	52/48
$p_T^{ ilde{\ell}}$	$80393 \pm 21$	60/62
$p_T^{\nu}$	$80431 \pm 25$	71/62
$W \to \mu\nu$		•
$m_T$	$80379 \pm 16$	57/48
$p_T^{\hat{\ell}}$	$80348 \pm 18$	58/62
$p_T^{\nu}$	$80406 \pm 22$	82/62

## Boson masses

#### Higgs field potential

# The n $\mathbf{A}V(\phi)$ the va covari V(W)There

$$m_H = v\sqrt{2\lambda} = 125 \text{ GeV}$$
  $\lambda \approx 0.1$ 

#### Gauge field potential

$$V = -\frac{g^2 v^2}{8} [(W_{\mu}^+)^2 + (W_{\mu}^-)^2] - \frac{v^2 (g^2 + g^2)}{8} Z^{\mu} Z_{\mu}$$

$$m_W = \frac{v}{2}g$$

$$m_Z = \frac{v}{2}\sqrt{g^2 + g^2}$$

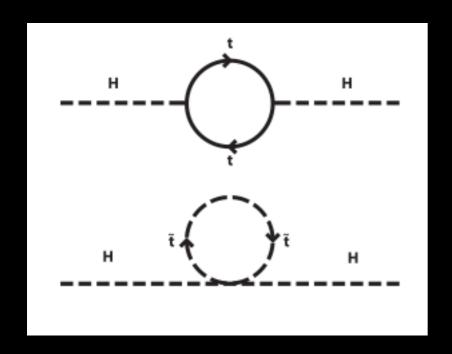
$$v = 246$$
 GeV and  $g = 0.64$ :

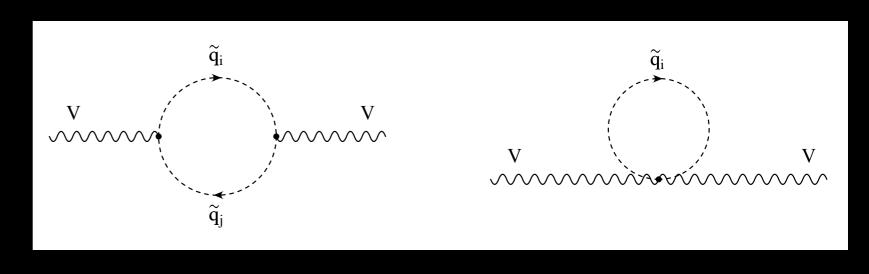
$$m_W = 78.7 \text{ GeV}$$

## W boson mass

The W boson mass is the most sensitive observable to sources of 'naturalness'

Classic example: Supersymmetry

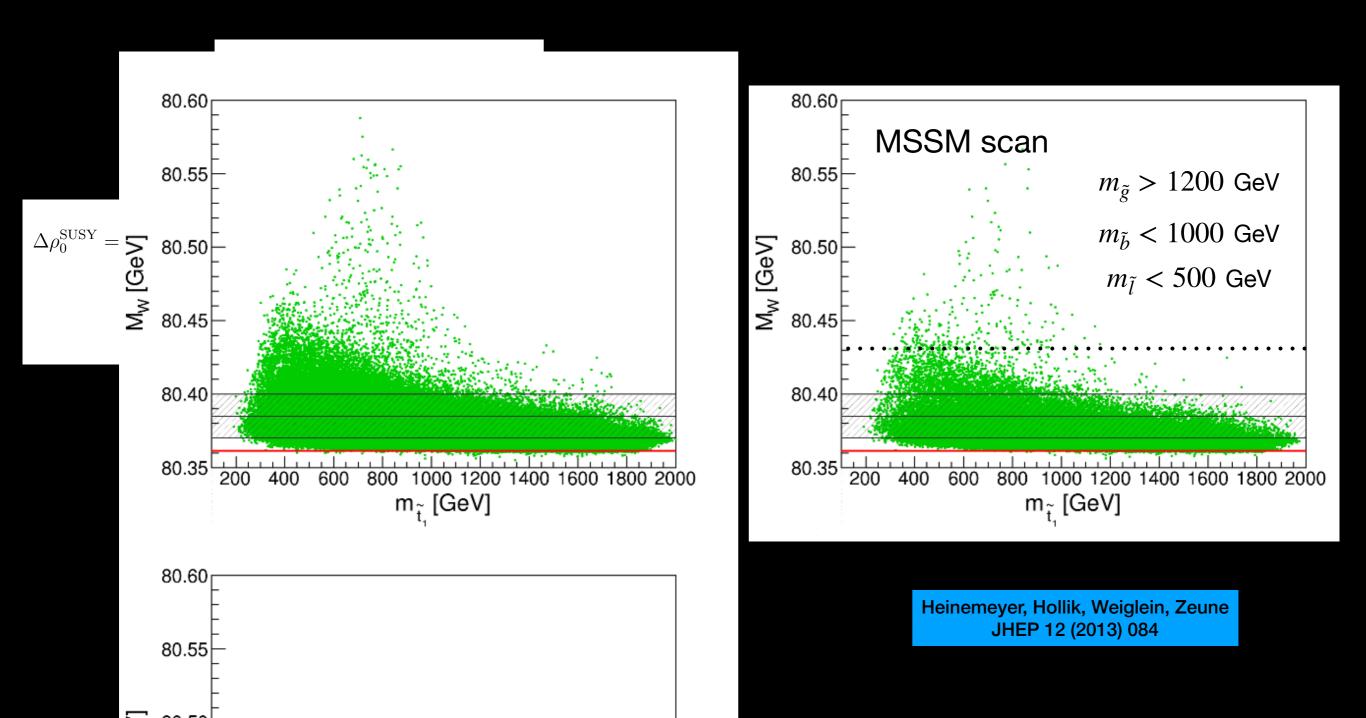




Mass splittings in supersymmetric isospin doublets: different mass shifts for W & Z bosons

## W boson mass

Difference in corrections to W and Z propagators encapsulated by  $\rho$  parameter



#### $\chi^2$ /dof = 52 / 48

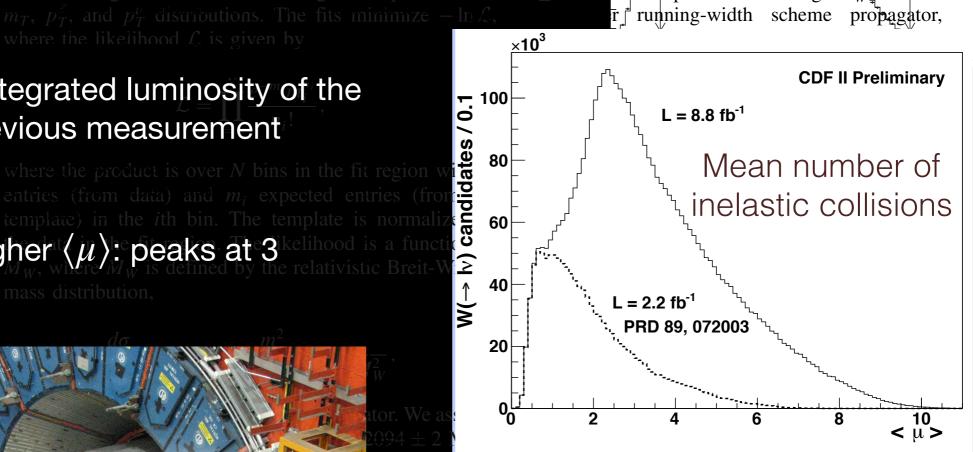
## CDF II measurement of the

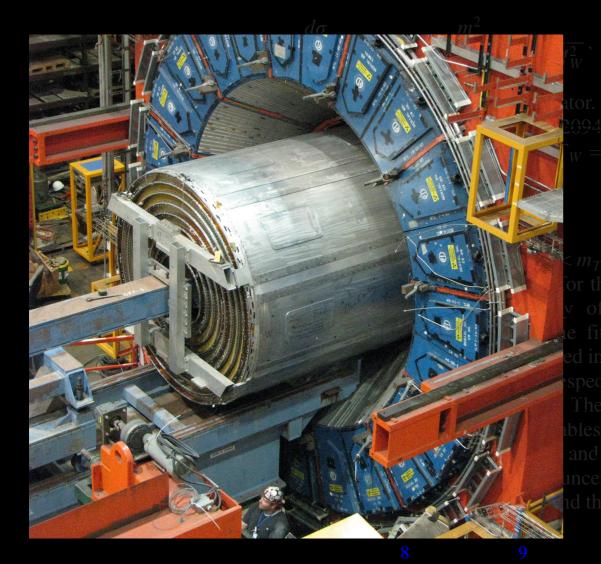
PHYSICAL REVIEW D **88,** 052018 (2013) he  $\int$  templates for fitting  $M_{W_1}$  assume

4x the integrated luminosity of the

previous measurement

Higher  $\langle \mu \rangle$ : peaks at 3





#### CDF II detector consists of

silicon vertex detector large drift chamber coarse calorimeter towers outer muon chambers

### **Detector simulation**

#### **Developed custom simulation for analysis**

Models ionization energy loss, multiple scattering, bremsstrahlung, photon conversion, Compton scattering

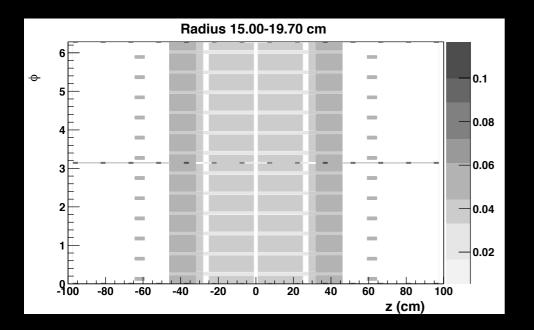
Acceptance map for muon detectors

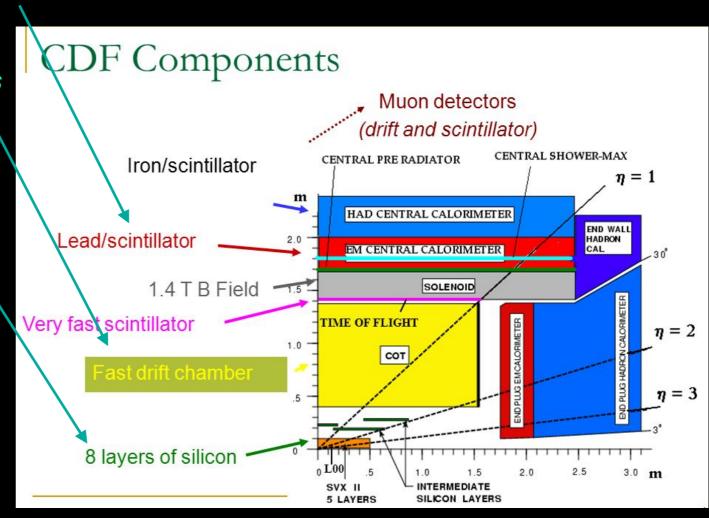
Parameterized GEANT4 model of electromagnetic calorimeter showers Includes shower losses due to finite calorimeter thickness

Kotwal & CH, NIMA 729, 25 (2013)

Hit-level model of central outer tracker Layer-by-layer resolution functions and efficiencies

Material map of inner silicon detector Includes radiation lengths and Bethe-Bloch terms

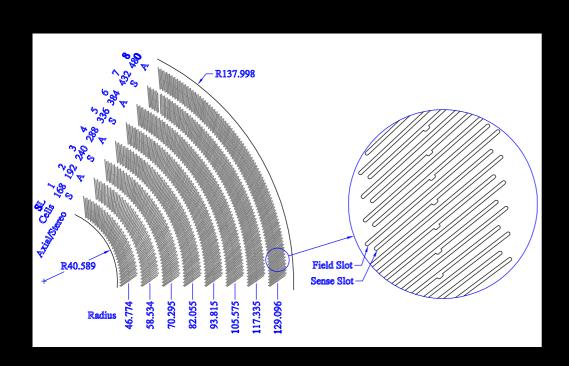


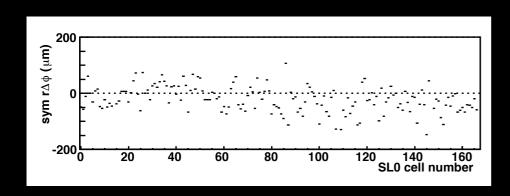


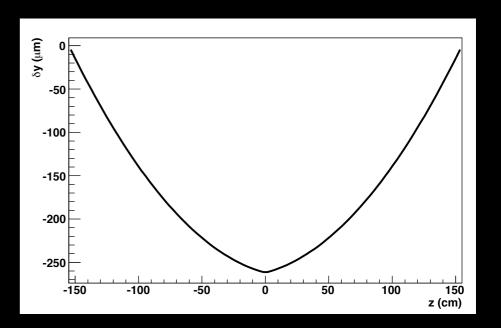
## Muon momentum calibration

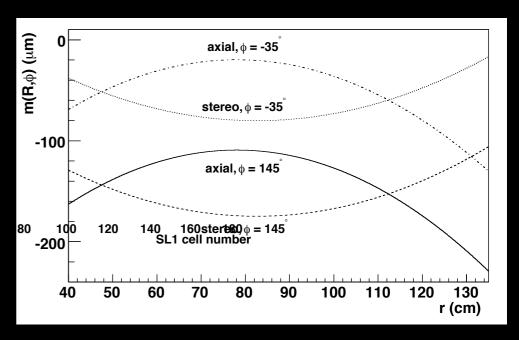
First step is to align the drift chamber (the "central outer tracker" or COT)

Two parameters for the electrostatic deflection of the wire within the chamber constrained using difference between fit parameters of incoming and outgoing cosmic-ray tracks







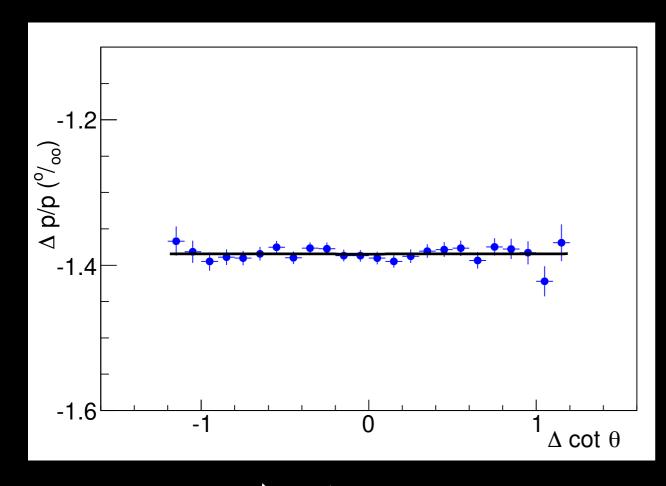


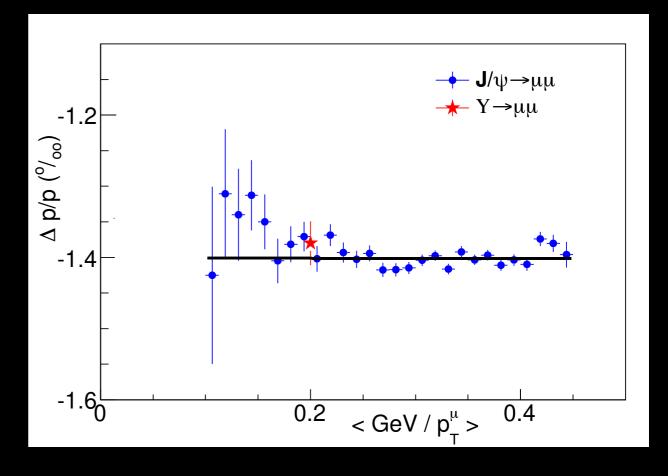
## Muon momentum calibration

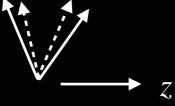
Second step is to calibrate the momentum scale using  $J/\psi$  decays to muons

#### **Simulation corrections:**

Correct the length scale of the tracker with mass measurement as a function of  $\Delta \cot \theta$  Correct the amount of upstream material with mass measurement as a function of  $p_T^{-1}$ 





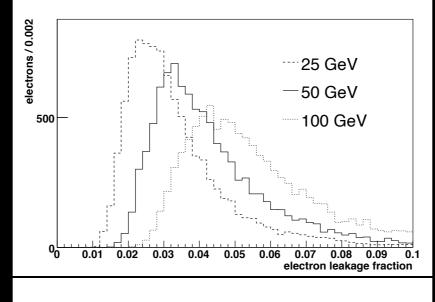


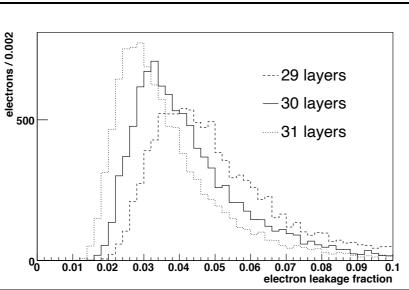
### Electron momentum calibration

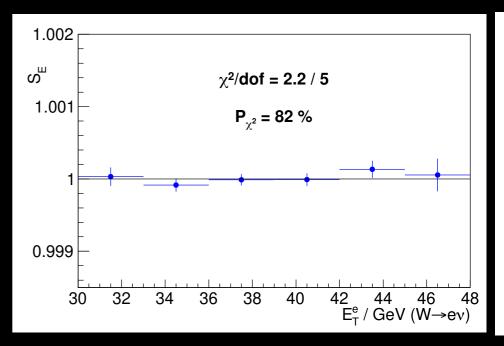
First step is to transfer the track calibration to the calorimeter (E/p) using W & Z decays

Parameterize calorimeter shower deposition and leakage based on GEANT4 Determine small calorimeter thickness corrections using region of low E/p in data Fit calorimeter scale as a function of  $E_T$  to correct for any remaining energy dependence

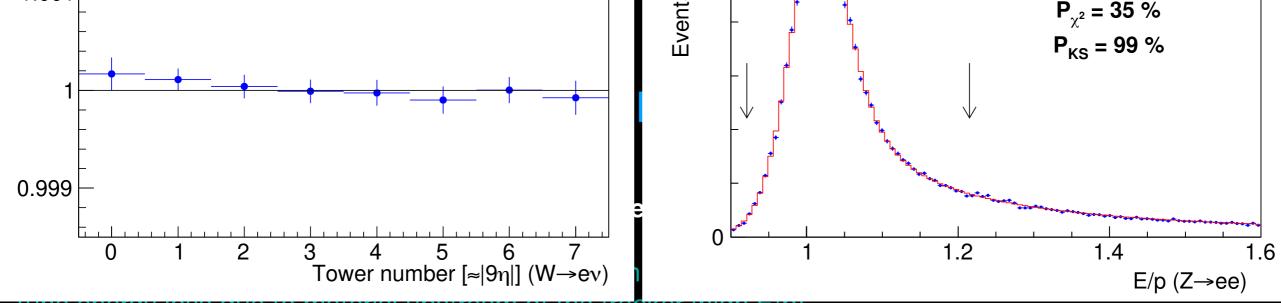
Tower	Thickness $(x_0)$	Number of lead sheets
0	17.9	30
1	18.2	30
2	18.2	29
3	17.8	27
4	18.0	26
5	17.7	24
6	18.1	23
7	17.7	21
8	18.0	20





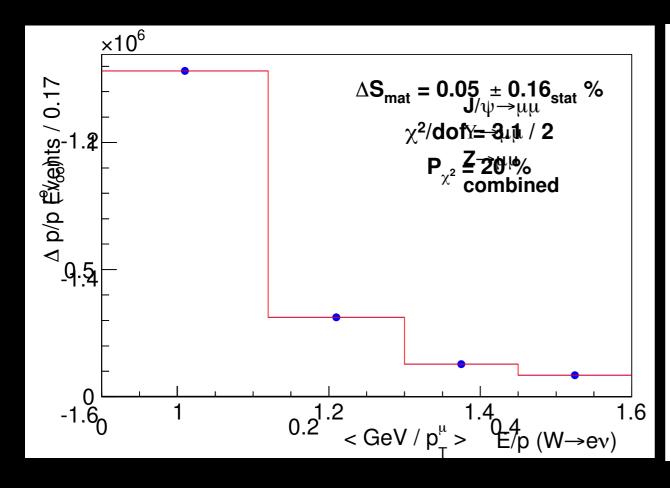


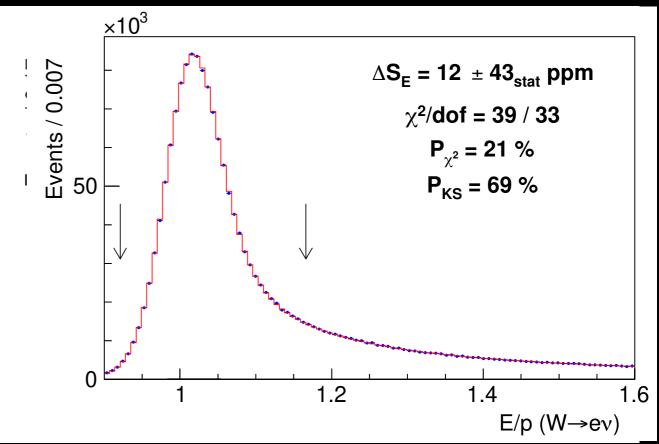
Kotwal & CH, NIMA 729, 25 (2013)

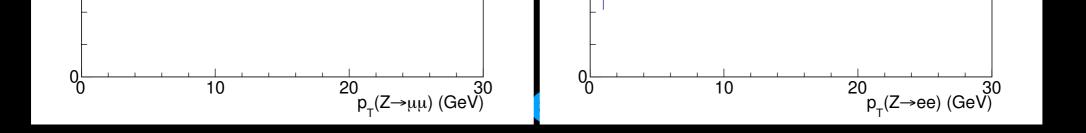


Tune energy loss due to material upstream of the tracker (nigh E/p)

Sampling resolution given by 
$$\sigma_E/E = \sqrt{\frac{12.6 \,\%}{E_T}} + \kappa^2$$
 with  $\kappa = 0.7 - 1.1 \,\%$  increasing with tower  $\eta$ 

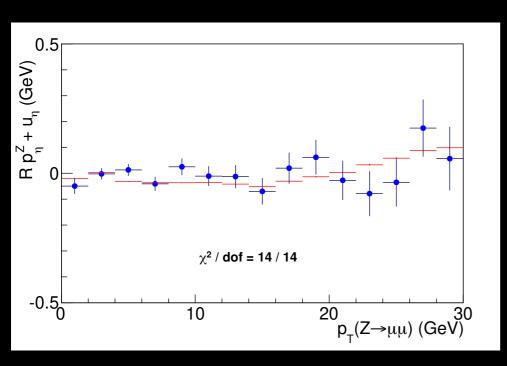


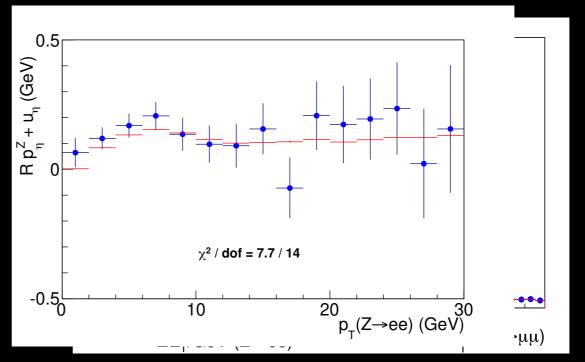


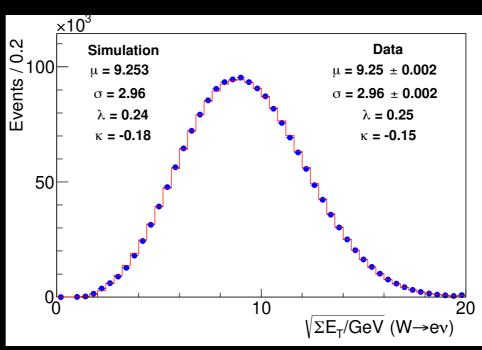


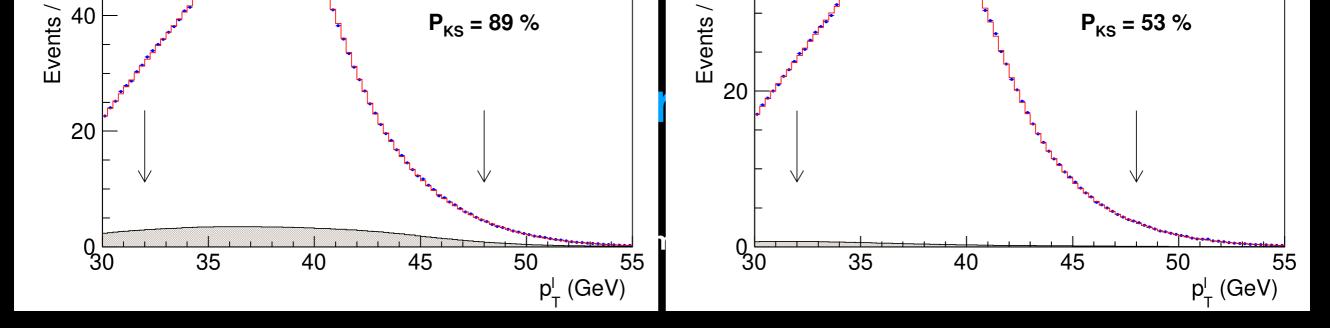
#### Fourth step is the calibration of the recoil resolution

Includes jet-like energy and angular resolution, additional dijet fraction term, and pileup



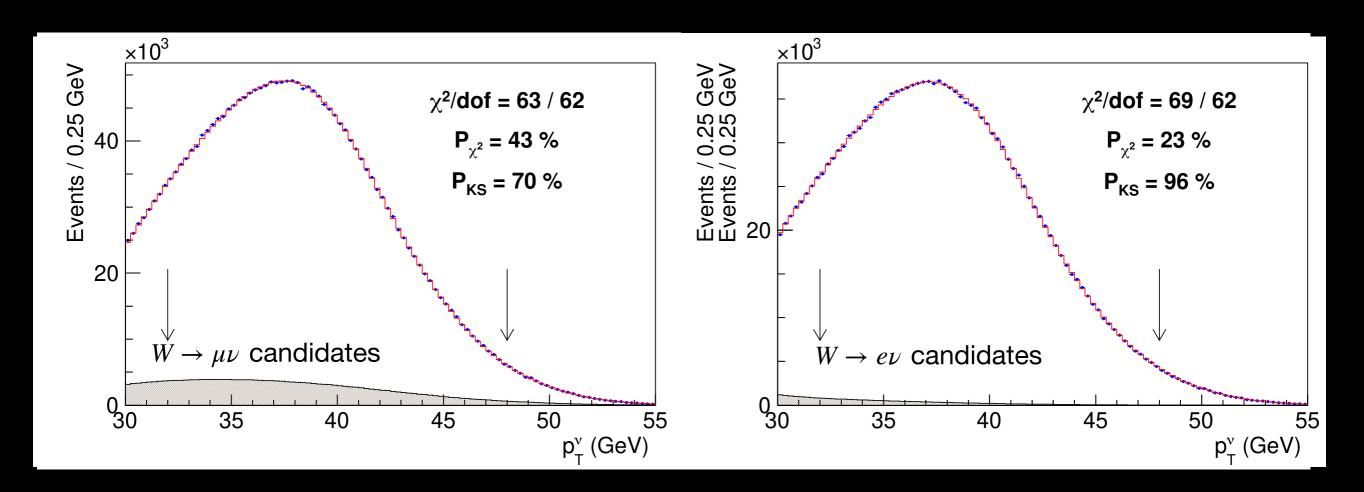




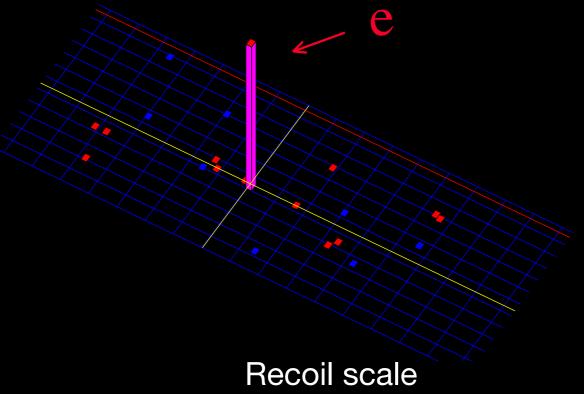


Largest background is  $Z \to \mu\mu$  with one unreconstructed muon: **7.4% of data sample**  $W \to \tau\nu$  background is ~1% in each channel: largest background in electron sample

Background from hadrons misreconstructed as leptons estimated using data: 0.2-0.3%

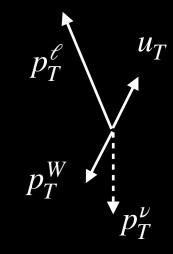


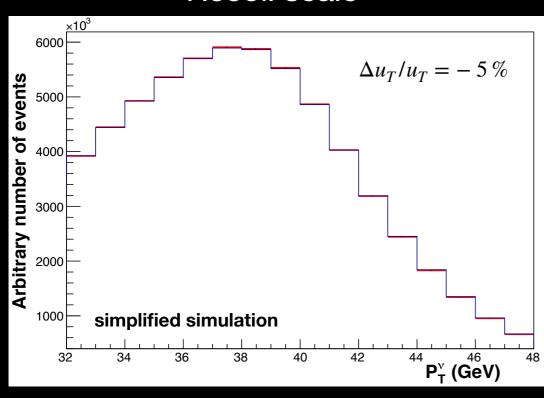
## **Calibrations**

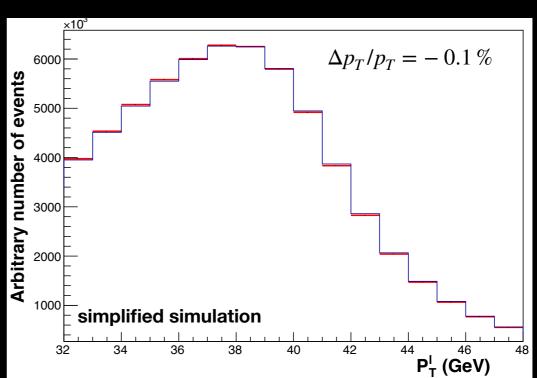


Measurement requires precise calibrations and momentum scale and resoution

$$\vec{p}_T = -(\vec{p}_T^{\ l} + \vec{u}_T)$$



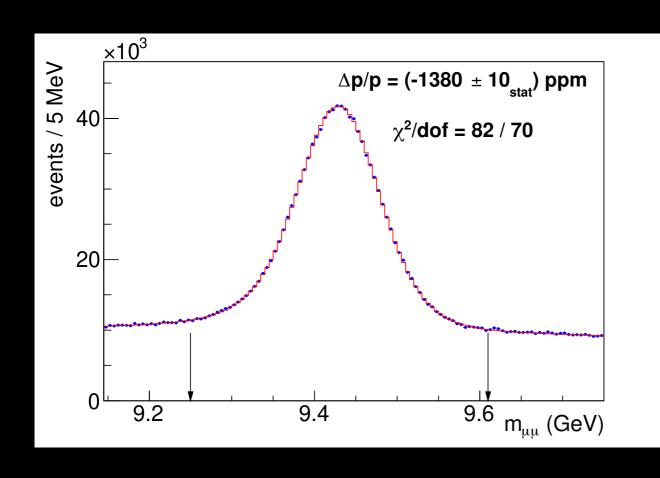


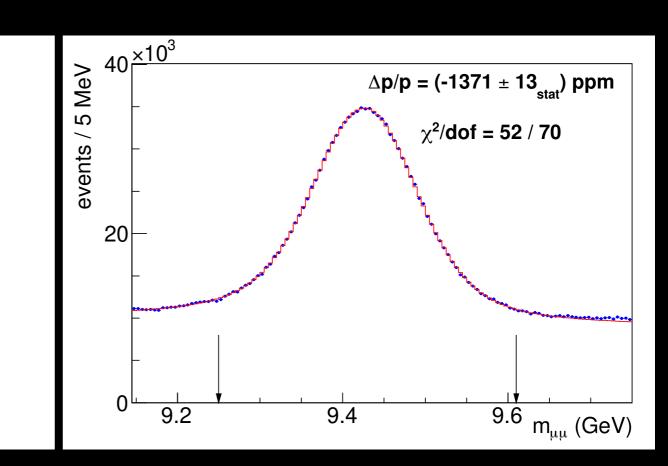


## Muon momentum calibration

Third step is to calibrate the scale using  $\Upsilon$  decays to muons

Compare fit results with and without constraining the track to the collision point





with constraint

without constraint