

# Heavy Neutral Leptons at Colliders: LFV, LNV and Heavy Neutrino-Antineutrino Oscillations

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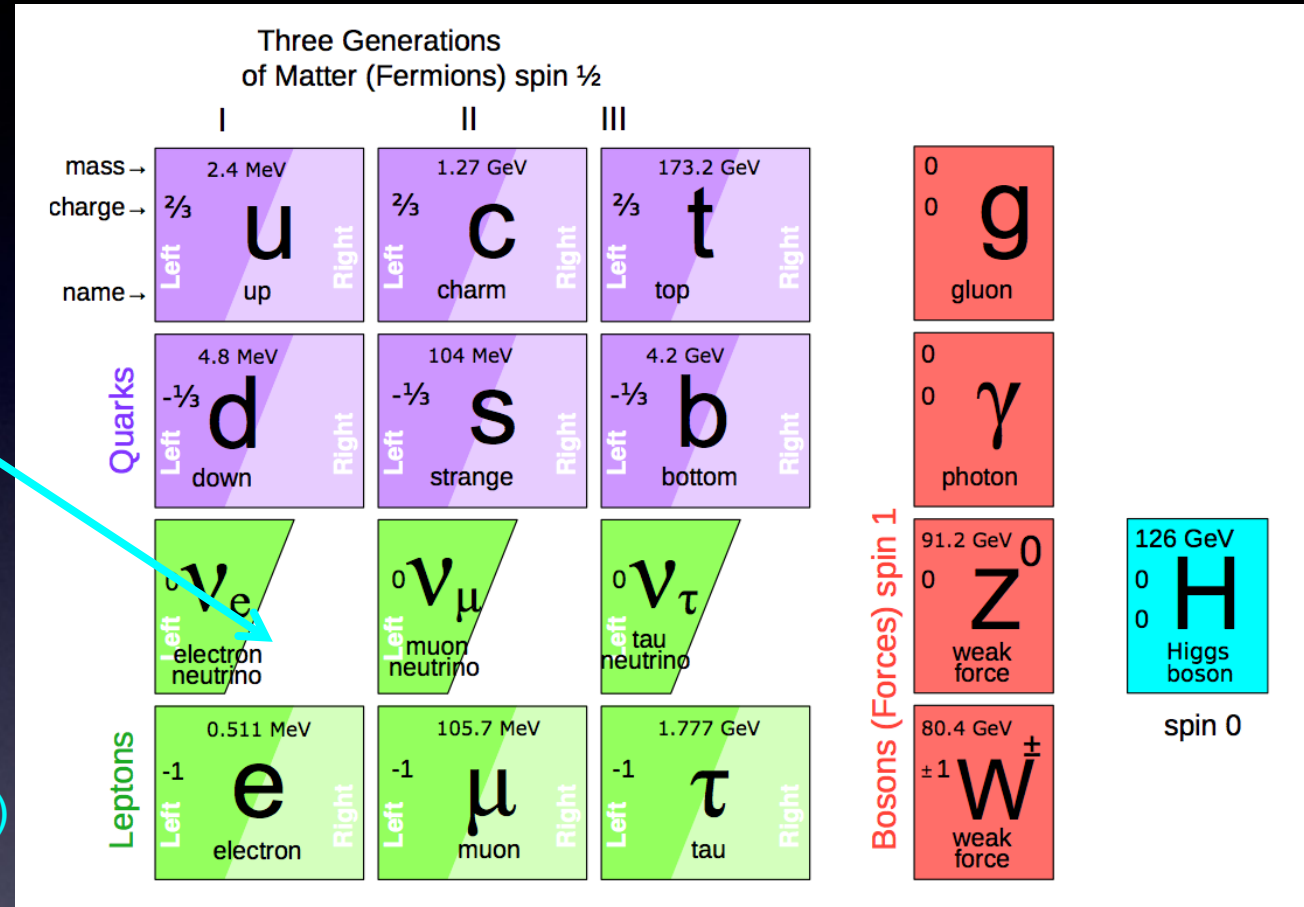
Workshop FP Capri - "Neutrinos, Flavour and Beyond",  
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# Heavy Neutral Leptons – the right SM extension to explain the light neutrino masses?

There are no right-chiral neutrino states ( $\nu_{Ri}$ ) in the Standard Model

→  $\nu_{Ri}$  would be completely neutral under all SM symmetries (HNLs  
 ↔ RH neutrinos  
 ↔ sterile neutrinos)



Adding  $\nu_{Ri}$  leads to the following extra terms in the Lagrangian density:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{2} \overline{\nu_R^I} M_{IJ}^N \nu_R^{cJ} - (Y_N)_{I\alpha} \overline{\nu_R^I} \tilde{\phi}^\dagger L^\alpha + \text{H.c.}$$

$M^N$ : sterile  $\nu$  mass matrix

$Y_N$ : neutrino Yukawa matrix  
 (→ Dirac mass terms)

# High Scale vs. Low Scale Seesaw

Smallness of light neutrino masses may be a consequence of:

→ Large RH  
neutrino masses

→ Approximate  
"Lepton-number"-  
like symmetry

"High Scale Seesaw"

"Low Scale Seesaw"

... can well operate at EW/TeV energies accessible to colliders, with potentially "unsuppressed" Yukawa couplings → testable at colliders!

# Low Scale Seesaw with "Symmetry protection"

Example for protective "lepton number"-like symmetry (case of 2HNLs):

	$L_\alpha$	$V_{R1}$	$V_{R2}$
"Lepton-#"	+1	+1	-1

→

With 2 HNLs (min # to explain  $m_\nu$ ) and exact symmetry

$$\mathcal{L}_N = - \overline{N_R}^{-1} M N_R^c - y_\alpha \overline{N_R}^{-1} \tilde{\phi}^\dagger L^\alpha + \text{H.c.}$$

→ Note: "Symmetry protection" requires pairs of sterile (right-handed) neutrinos ... which form "pseudo-Dirac pairs"!

For comparison: most general seesaw with 2 HNLs:

$$M_\nu^{\text{general}} = \begin{pmatrix} 0 & m_D & m'_D \\ (m_D)^T & M' & M \\ (m'_D)^T & M & M'' \end{pmatrix}$$

when  $\varepsilon$ -terms "get larger"

From general 2 HNL seesaw to "symmetry limit"

Approximate symmetry (with "small"  $\varepsilon$ -terms breaking it):

In the symmetry limit

with basis  $\Psi = (\nu_L, (N_R^1)^c, (N_R^2)^c)$

$$M_\nu = \begin{pmatrix} 0 & m_D & 0 \\ (m_D)^T & 0 & M \\ 0 & M & 0 \end{pmatrix}$$

from symmetry to approximate symmetry

$$M_\nu^{\text{general}} = \begin{pmatrix} 0 & m_D & \varepsilon \\ (m_D)^T & \varepsilon' & M \\ \varepsilon^T & M & \varepsilon'' \end{pmatrix}$$

# Low Scale Seesaw with "Symmetry protection"

→ Light neutrino masses induced from small breaking of the "L-like" symmetry ( $m_\nu \sim \epsilon$ )

$$\mathcal{L}_N = - \overline{N_R}^1 M N_R^c - y_\alpha \overline{N_R}^1 \tilde{\phi}^\dagger L^\alpha + \text{H.c.}$$

+ symmetry breaking terms  $\mathcal{O}(\epsilon)$

"Inverse" seesaw: \*

$$M_\nu = \begin{pmatrix} 0 & m_D & 0 \\ (m_D)^T & 0 & M \\ 0 & M & \epsilon \end{pmatrix}$$

$$\rightarrow m_\nu \sim \epsilon \frac{m_D^T m_D}{M^2}$$

Estimate for induced **HNL mass splitting  $\Delta M$**  in "inverse" seesaw:

$$\Delta M^{\text{inv}} = \frac{m_{\nu_i}}{|\theta^2|}$$

"Linear" seesaw: \*

$$M_\nu = \begin{pmatrix} 0 & m_D & \epsilon \\ (m_D)^T & 0 & M \\ \epsilon^T & M & 0 \end{pmatrix}$$

$$\rightarrow m_\nu \sim \frac{\epsilon^T m_D}{M}$$

In "minimal linear seesaw" (2 HNLs):

$$\Delta M_{\text{NH}}^{\text{lin}} = m_{\nu_3} - m_{\nu_2} \stackrel{m_{\nu_1}=0}{=} 0.042 \text{ eV}$$

$$\Delta M_{\text{IH}}^{\text{lin}} = m_{\nu_2} - m_{\nu_1} \stackrel{m_{\nu_3}=0}{=} 0.00075 \text{ eV}$$

cf. S. A., E. Cazzato, O. Fischer (arXiv:1709.03797)

also: ... no tree-level  $m_\nu$

$$M_\nu = \begin{pmatrix} 0 & m_D & 0 \\ (m_D)^T & \epsilon & M \\ 0 & M & 0 \end{pmatrix}$$

\*) Note: names "inverse" and "linear" seesaw used here to indicate the position of the  $\epsilon$ -term in  $M_\nu$

For low scale seesaw models, see e.g.: D. Wyler, L. Wolfenstein ('83), R. N. Mohapatra, J. W. F. Valle ('86), M. Shaposhnikov ('07), J. Kersten, A. Y. Smirnov ('07), M. B. Gavela, T. Hambye, D. Hernandez, P. Hernandez ('09), M. Malinsky, J. C. Romao, J. W. F. Valle ('05), S.A., Hohl, King, Susic (in SO(10) with low scale Z', arXiv:1712.05366) ...

# Benchmark scenario: The SPSS (= Symmetry Protected Seesaw Scenario)

... captures the phenomenology of a dominant "pseudo-Dirac"-like HNL pair at colliders  
 ... without the constraints of a restricted pure 2HNL model ( $\leftrightarrow$  correlations between  $y_\alpha$ )

$$Y_\nu = \begin{pmatrix} y_{\nu e} & 0 \\ y_{\nu \mu} & 0 \dots \\ y_{\nu e} & 0 \end{pmatrix}, \quad M = \begin{pmatrix} 0 & M_R & & & \\ M_R & 0 & & & \\ \dots & & \dots & & \\ & & & * & * \dots \\ 0 & & & * & * \dots \end{pmatrix}$$

+  $O(\epsilon)$   
 perturbations  
 to generate the  
 light neutrino  
 mass  
 (which we can  
 often neglect for  
 collider studies)

For details on the SPSS, see:  
 S.A., O. Fischer (arXiv:1502.05915)

Additional sterile neutrinos can exist, but assumed to  
 have no effects at colliders (which can be realised  
 easily, e.g. by giving lepton number = 0 to them).

The SPSS in the "symmetry limit"

# We consider the SPSS (Symmetry Protected Seesaw Scenario)

In the  
symmetry  
limit:

$$\mathcal{L}_N = - \overline{N_R}^1 M N_R^c - y_\alpha \overline{N_R}^1 \tilde{\phi}^\dagger L^\alpha + \text{H.c.} \\ + \dots \text{ (terms from additional sterile vs)}$$



# We consider the SPSS (Symmetry Protected Seesaw Scenario)

In the  
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$$\mathcal{L}_N = - \overline{N_R}^1 M N_R^c - y_\alpha \overline{N_R}^1 \tilde{\phi}^\dagger L^\alpha + \text{H.c.} \\ + \dots \text{ (terms from additional sterile vs)}$$

4 Parameters:  
 $M, y_\alpha, (\alpha=e,\mu,\tau)$

# We consider the SPSS (Symmetry Protected Seesaw Scenario)

In the  
symmetry  
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$$\mathcal{L}_N = - \overline{N_R}^1 M N_R^c - y_\alpha \overline{N_R}^1 \tilde{\phi}^\dagger L^\alpha + \text{H.c.} \\ + \dots \text{ (terms from additional sterile vs)}$$

After EW symmetry breaking, we diagonalize the 5x5 mass matrix:

Mass eigenstates:

$$\tilde{n}_j = (\nu_1, \nu_2, \nu_3, N_4, N_5)_j^T = U_{j\alpha}^\dagger n_\alpha$$

“light” and “heavy”  
neutrinos

with:

$$n = (\nu_{eL}, \nu_{\mu L}, \nu_{\tau L}, (N_R^1)^c, (N_R^2)^c)^T$$

“active” and “sterile”  
neutrinos

This defines the 5x5 mixing matrix U.

# We consider the SPSS: Instead of the $y_\alpha$ , we use the active sterile mixing angles $\theta_\alpha$ ( $\alpha=e,\mu,\tau$ )

In the symmetry limit:

$$\mathcal{L}_N = - \overline{N_R}^1 M N_R^c{}^2 - y_\alpha \overline{N_R}^1 \tilde{\phi}^\dagger L^\alpha + \text{H.c.} \\ + \dots \text{ (terms from additional sterile vs)}$$

- ▶ The leptonic mixing matrix to leading order in the active-sterile mixing parameters:

$$U_{5 \times 5} = \begin{pmatrix} \mathcal{N}_{1e} & \mathcal{N}_{1\mu} & \mathcal{N}_{1\tau} & -\frac{i}{\sqrt{2}}\theta_e & \frac{1}{\sqrt{2}}\theta_e \\ \mathcal{N}_{2e} & \mathcal{N}_{2\mu} & \mathcal{N}_{2\tau} & -\frac{i}{\sqrt{2}}\theta_\mu & \frac{1}{\sqrt{2}}\theta_\mu \\ \mathcal{N}_{3e} & \mathcal{N}_{3\mu} & \mathcal{N}_{3\tau} & -\frac{i}{\sqrt{2}}\theta_\tau & \frac{1}{\sqrt{2}}\theta_\tau \\ 0 & 0 & 0 & \frac{i}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\theta_e^* & -\theta_\mu^* & -\theta_\tau^* & \frac{-i}{\sqrt{2}}(1 - \frac{1}{2}\theta^2) & \frac{1}{\sqrt{2}}(1 - \frac{1}{2}\theta^2) \end{pmatrix}$$

Parameters:

$M, y_\alpha$  ( $\alpha=e,\mu,\tau$ )  
or

equivalently

$M, \theta_\alpha$  ( $\alpha=e,\mu,\tau$ )

- ▶ Active-sterile neutrino mixing parameters:

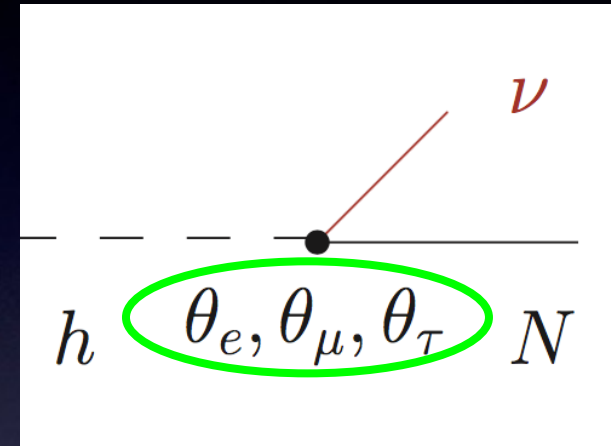
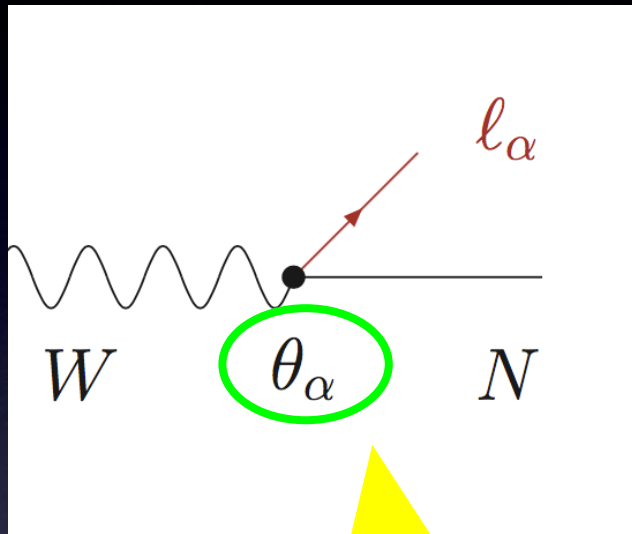
$$\theta_\alpha = \frac{y_\alpha^*}{\sqrt{2}} \frac{v_{EW}}{M}, \quad \alpha = e, \mu, \tau$$

Sterile neutrinos mix with the active ones → the heavy neutrinos (= mass eigenstates) participate in weak interactions!

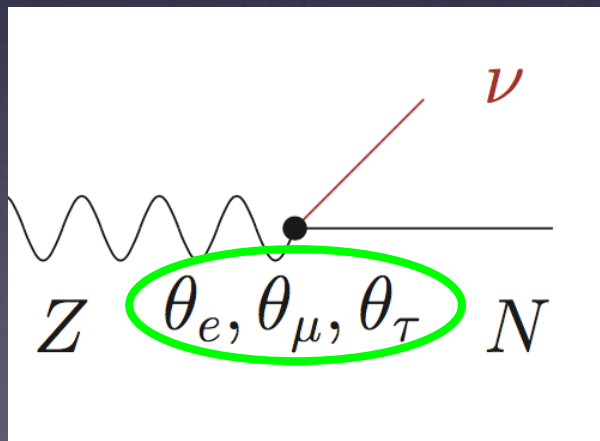
$$U = \begin{pmatrix} \mathcal{N}_{1e} & \mathcal{N}_{1\mu} & \mathcal{N}_{1\tau} & -\frac{i}{\sqrt{2}}\theta_e & \frac{1}{\sqrt{2}}\theta_e \\ \mathcal{N}_{2e} & \mathcal{N}_{2\mu} & \mathcal{N}_{2\tau} & -\frac{i}{\sqrt{2}}\theta_\mu & \frac{1}{\sqrt{2}}\theta_\mu \\ \mathcal{N}_{3e} & \mathcal{N}_{3\mu} & \mathcal{N}_{3\tau} & -\frac{i}{\sqrt{2}}\theta_\tau & \frac{1}{\sqrt{2}}\theta_\tau \\ 0 & 0 & 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\theta_e^* & -\theta_\mu^* & -\theta_\tau^* & \frac{-i}{\sqrt{2}}(1 - \frac{1}{2}\theta^2) & \frac{1}{\sqrt{2}}(1 - \frac{1}{2}\theta^2) \end{pmatrix}$$

⇒ heavy neutrinos can get produced also in weak interaction processes!

# Heavy neutrino interactions



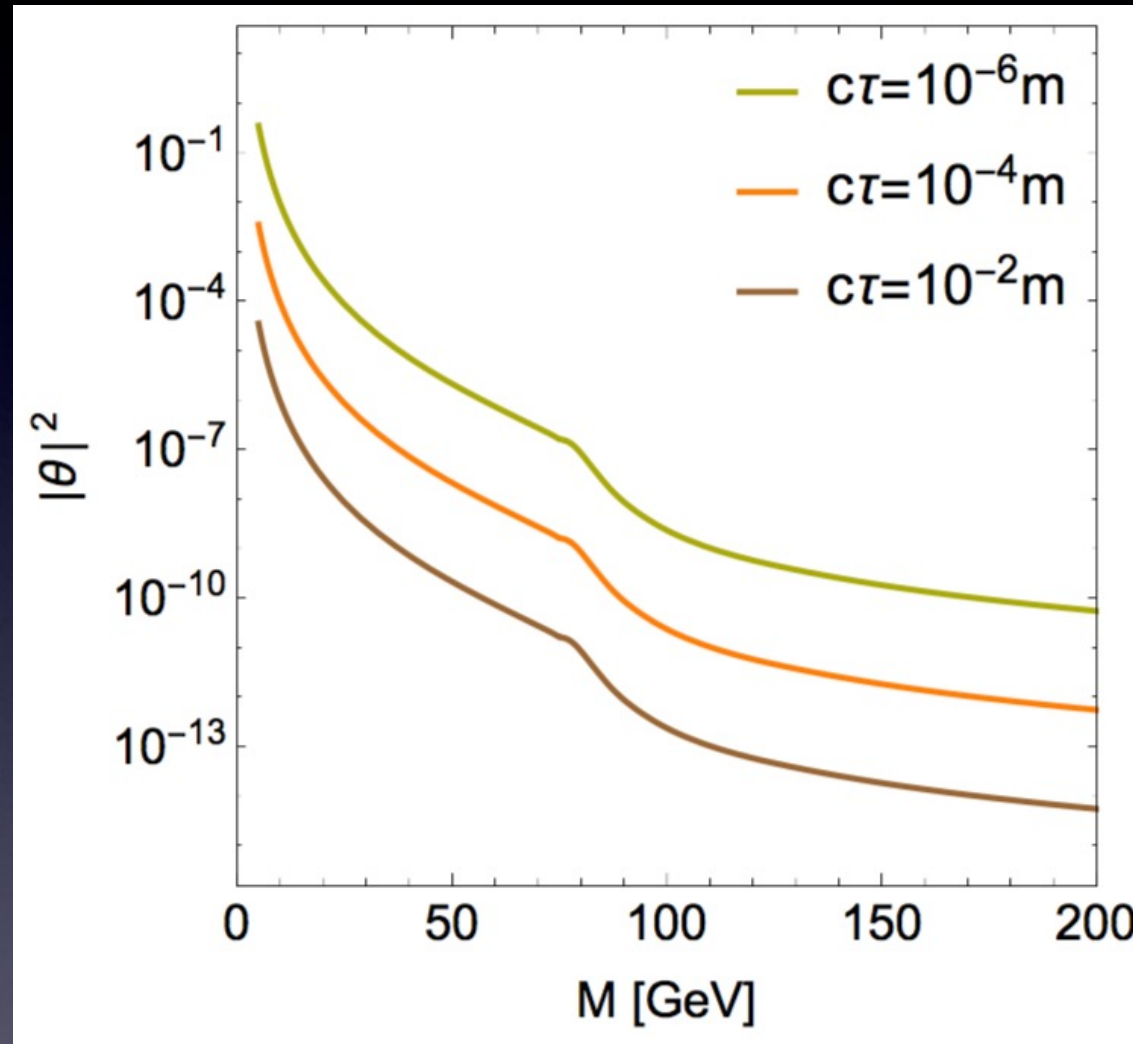
When  $W$  bosons are involved, there is a possible sensitivity to the flavour-dependent  $\theta_\alpha$



... vertices for production and for decay ...

# Lifetime and decay length of heavy neutrinos:

**For  $M < m_W$ , they can be long-lived!**



Note: Decay length in the laboratory frame is:

$$c\tau \sqrt{\gamma^2 - 1}$$

cf. S. A., E. Cazzato, O. Fischer  
(arXiv:1709.03797)

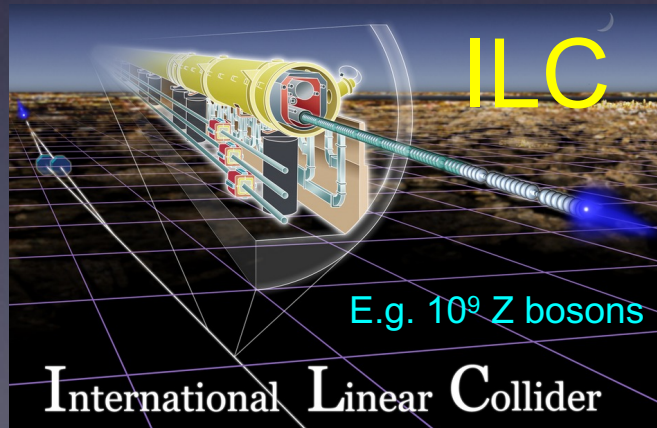
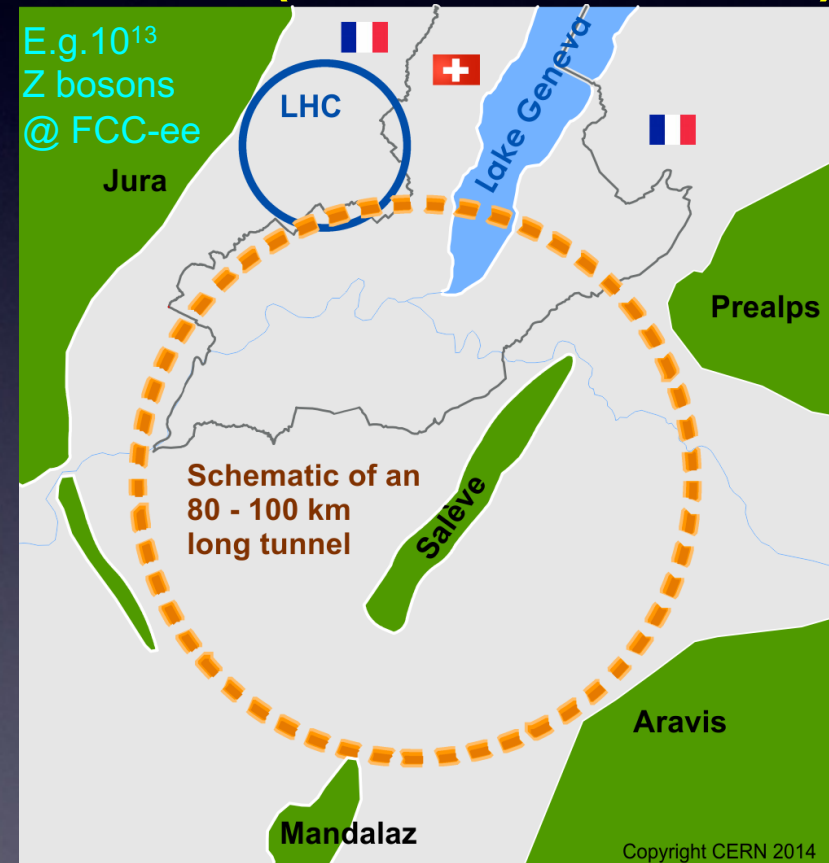
# What are the sensitivities for probing HNLs at future collider experiments?

Note: I will consider the SPSS as a benchmark scenario and restrict myself to  $M > 10$  GeV

# Ambitious plans for future colliders ... ... different collider types: $e^+e^-$ , $pp$ , $ep$



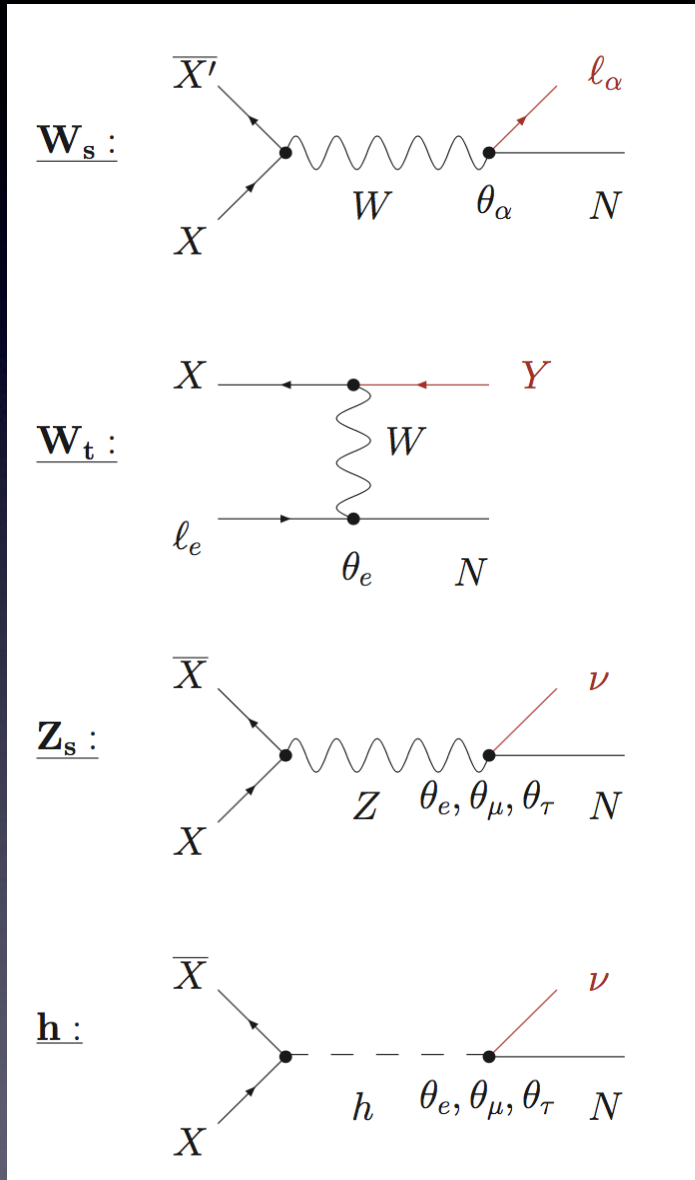
## FCC (-ee, -hh, -eh)





# Systematic assessment of signatures of sterile neutrinos at colliders

S.A., E. Cazzato, O. Fischer (arXiv:1612.02728),  
See also many other works by many authors ...



Different collider types feature different production channels ...

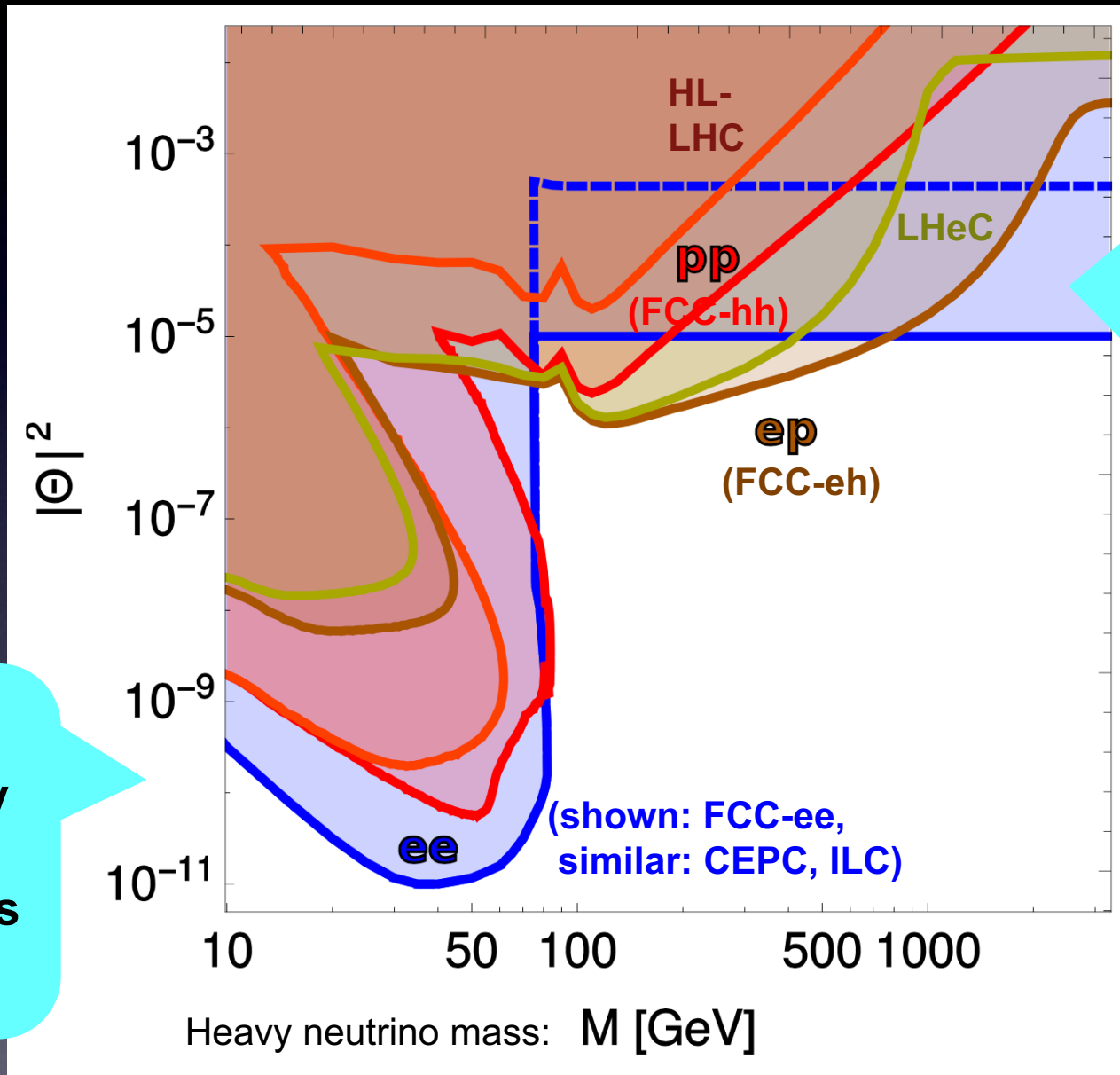
(at LO)

	$e^-e^+$	$pp$	$e^-p$
$\mathbf{W}_s$	×	✓ + LNV/LFV	×
$\mathbf{W}_t$	✓	×	✓ + LNV/LFV *
$\mathbf{Z}_s$	✓	✓	×
$\mathbf{h}$	(✓)	(✓)	(✓)

... helps a lot to suppress SM background!

\*) unambiguous (i.e. clear from final state), no SM background at parton level (but of course background with e.g. extra neutrinos)

# Summary: Estimated sensitivities at future ee, pp and ep colliders



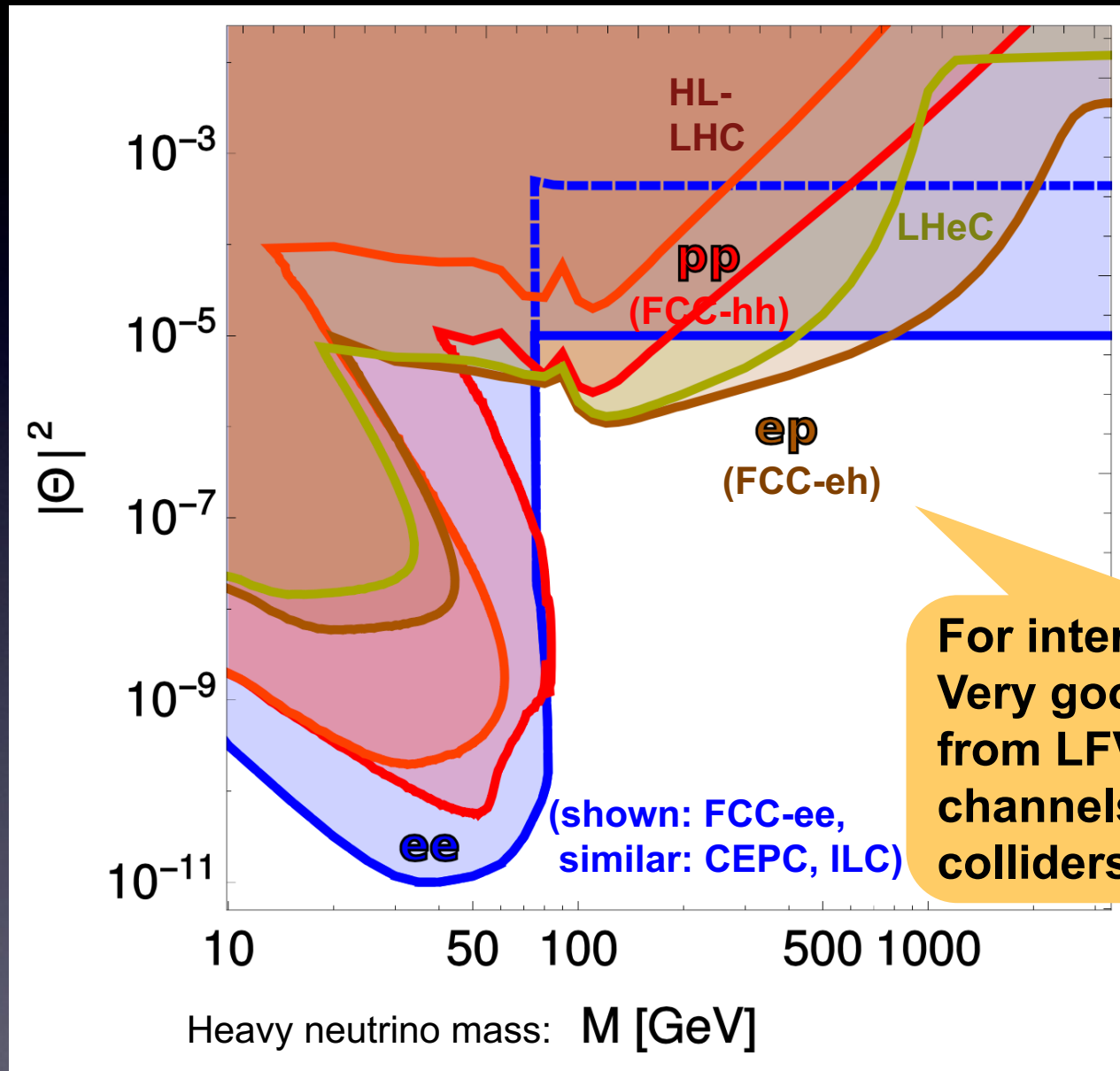
For  $M < m_W$ :  
Best sensitivity  
from displaced  
vertex searches  
at FCC-ee

For  $M \gg O(\text{TeV})$ :  
Very good  
sensitivity  
from EWPO  
measurements  
at FCC-ee

Also, future exp on:  
 $\mu \rightarrow e \gamma, \mu \rightarrow 3e,$   
 $\mu - e$  conversion in  
nuclei very sensitive!

Plot from: S.A.,  
E. Cazzato, O. Fischer  
(arXiv:1612.02728)

# Summary: Estimated sensitivities at future ee, pp and ep colliders



Note: Sensitivity to different combinations of active-sterile mixing angles!

For intermediate  $M$ :  
Very good sensitivities from LFV (but LNC) channels at pp and ep colliders (FCC-hh & -eh)

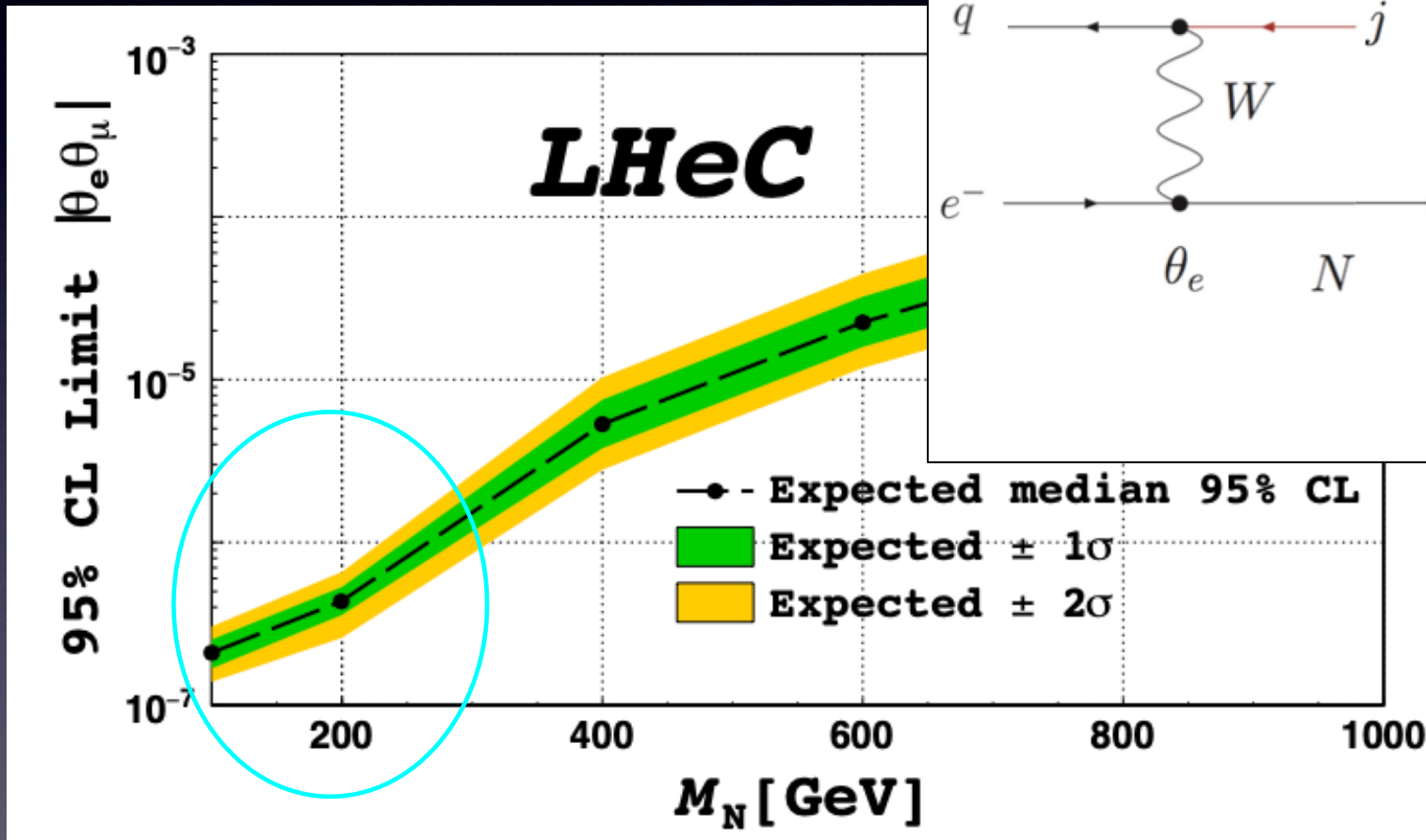
Plot from: S.A., E. Cazzato, O. Fischer (arXiv:1612.02728)

# Sensitivity of lepton-trijet searches at ep colliders

update!

LFV lepton-trijet signature at LHeC and FCC-eh:  
Sensitivity from analysis at the reconstructed level

“lepton-trijet” signature at ep colliders (LHeC, FCC-eh)  $l_\alpha^- jjj$  with e.g.  $\alpha = \tau^-$  or  $\mu^-$



Extremely sensitive!

LHeC with  $1 \text{ ab}^{-1}$

S.A., A. Hammad, O. Fischer (arXiv:1908.02852)

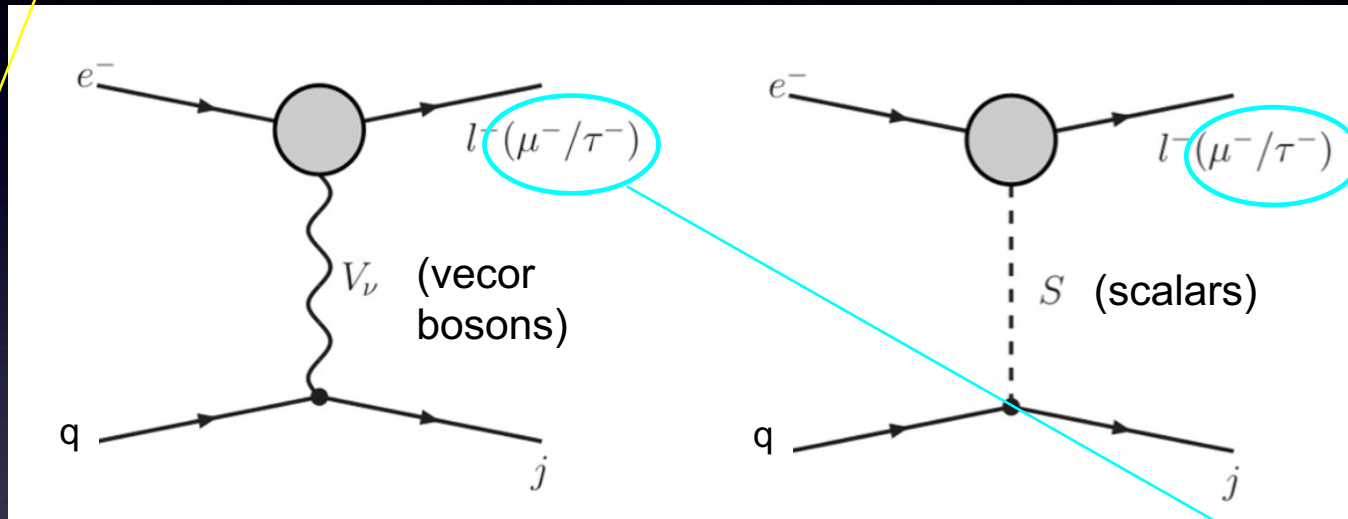
In addition, as we found out recently:  
LFV at ep colliders can also probe  
HNLs with much larger masses!

Novel signature: cLFV from effective  
 $e\text{-}\mu$  and  $e\text{-}\tau$  conversion operators  
at LHeC/FCC-eh

# cLFV searches via $e\text{-}\mu$ and $e\text{-}\tau$ conversion at ep colliders

S.A., A. Hammad, A. Rashed (arXiv:2010.08907)

Effective description:



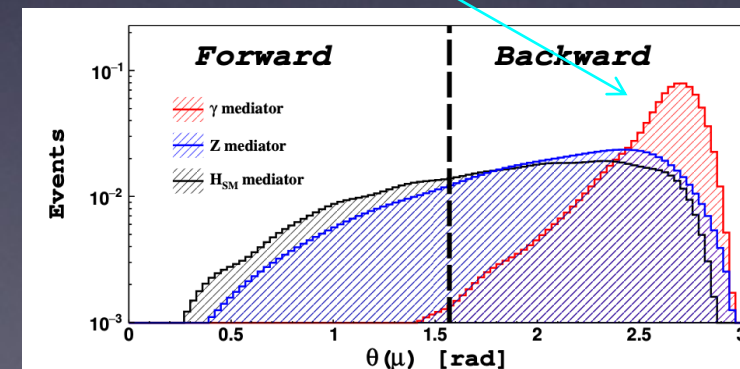
Effective operators:

$$\mathcal{L}_{\text{eff}}^{\text{scalar}} = \bar{\ell}_\alpha P_{L,R} \ell_\beta S N_{L,R}$$

$$\mathcal{L}_{\text{eff}}^{\text{monopole}} = \bar{\ell}_\alpha \gamma_\mu P_{L,R} \ell_\beta [A_{L,R} g^{\mu\nu} + B_{L,R} (g^{\mu\nu} q^2 - q^\mu q^\nu)] V_\nu$$

$$\mathcal{L}_{\text{eff}}^{\text{dipole}} = \bar{\ell}_\alpha \sigma^{\mu\nu} P_{L,R} \ell_\beta q_\mu V_\nu D_{L,R}$$

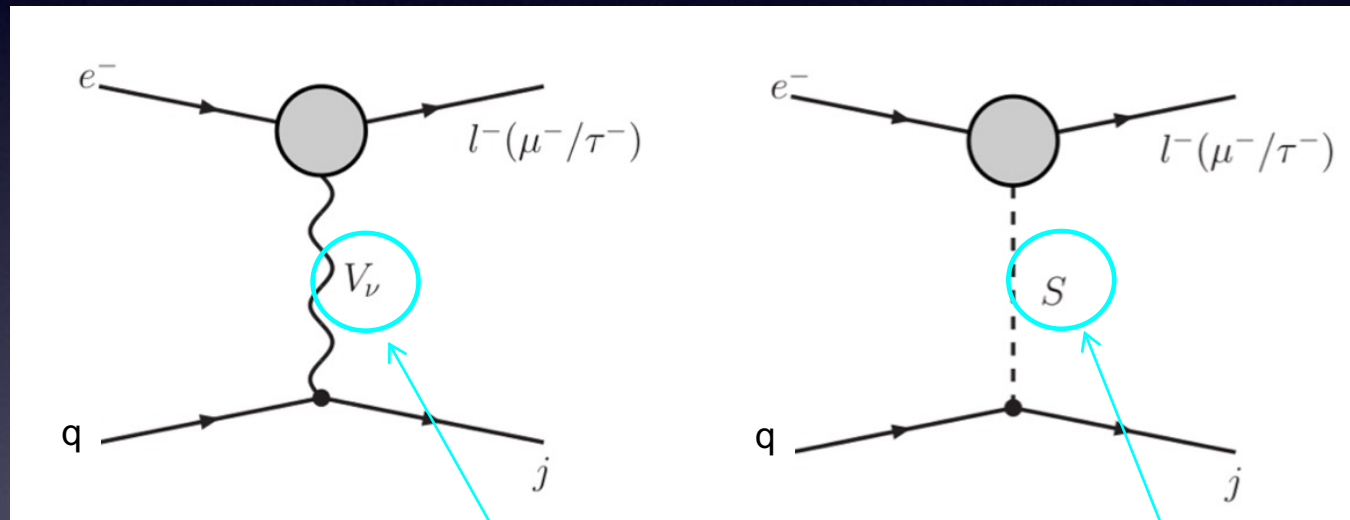
Scattered dominantly in backward direction of the detector!



# *cLFV searches via $e$ - $\mu$ and $e$ - $\tau$ conversion at $ep$ colliders*

S.A., A. Hammad, A. Rashed (arXiv:2010.08907)

Effective description:



Can probe new vector bosons (e.g. LFV via  $Z'$ ) or scalars ...

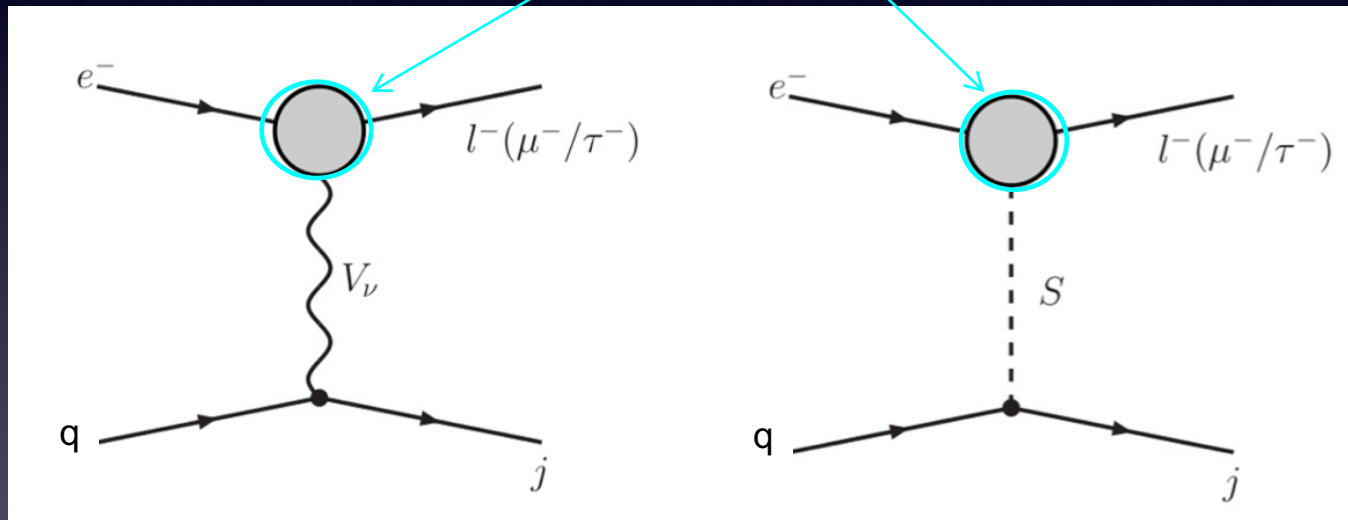
S.A., A. Hammad, A. Rashed (arXiv:2003.11091)

# *cLFV searches via e- $\mu$ and e- $\tau$ conversion at ep colliders*

S.A., A. Hammad, A. Rashed (arXiv:2010.08907)

Can probe effective FCNC vertices (here  $V = \gamma, Z, S = h$ )

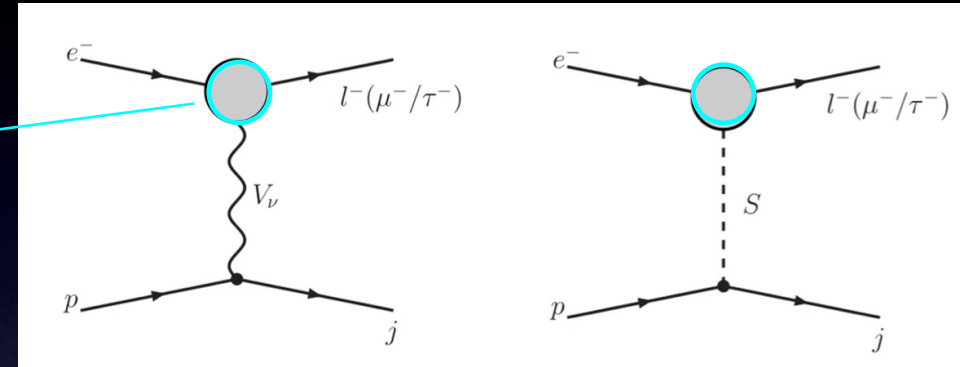
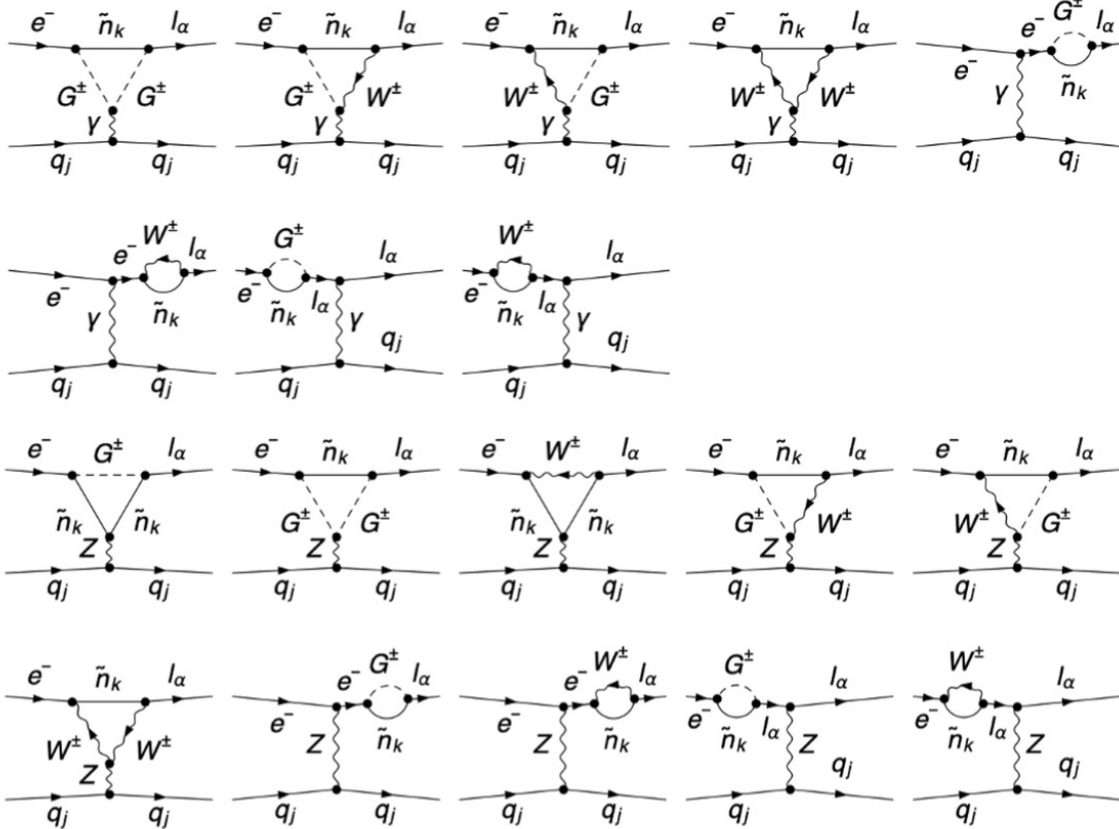
Effective description:





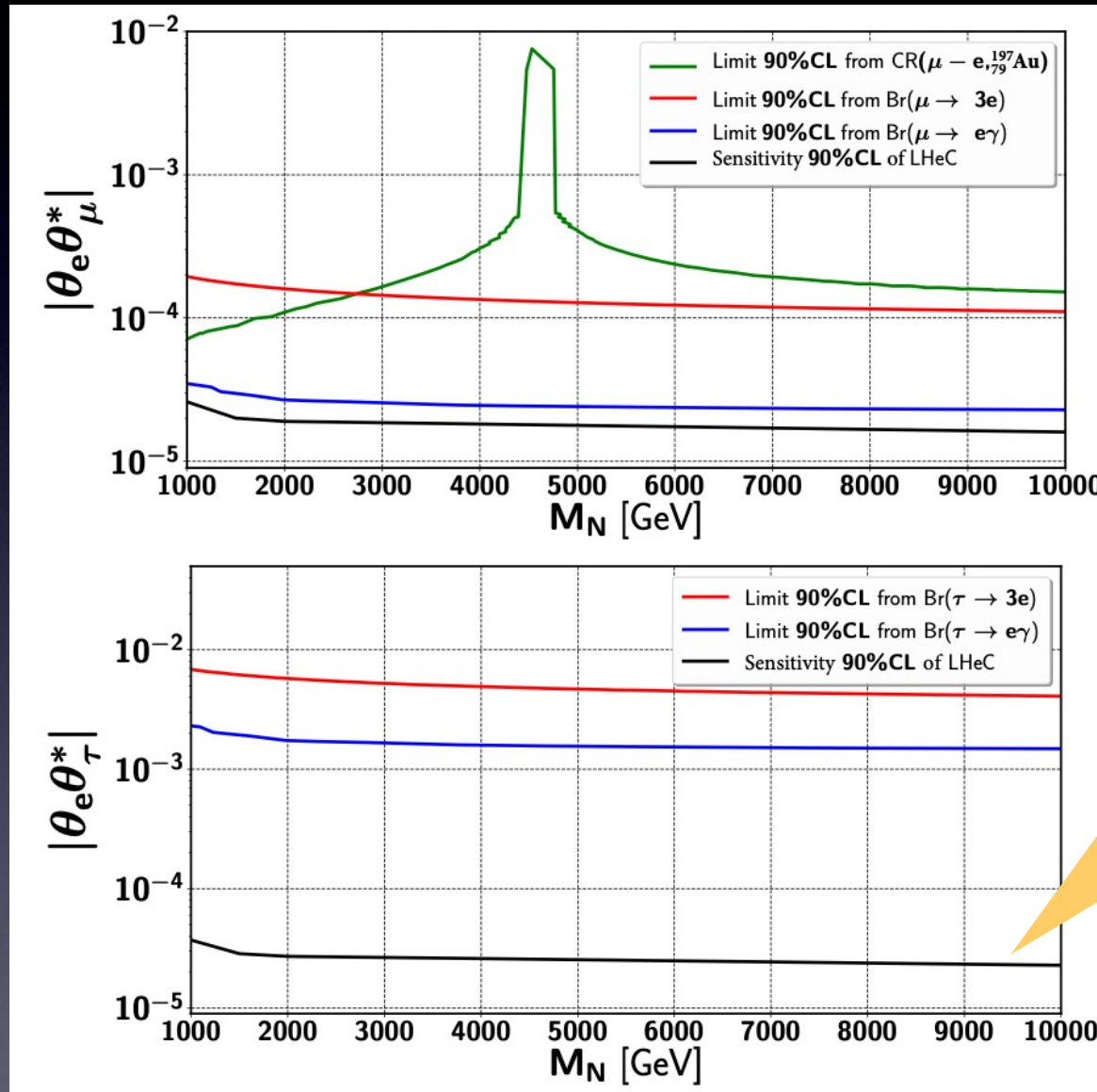
# cLFV searches via $e\text{-}\mu$ and $e\text{-}\tau$ conversion at ep colliders

In the SM extended by HNLs:



S.A., A. Hammad, A. Rashed (arXiv:2010.08907)

# Sensitivity at LHeC for HNLs with masses far above $M_W$ via $e$ - $\mu$ and $e$ - $\tau$ conversion



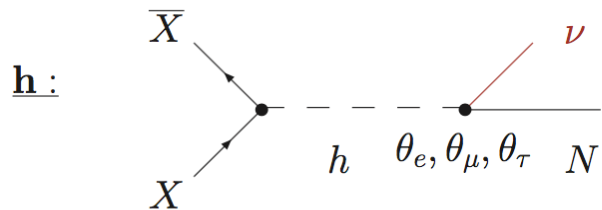
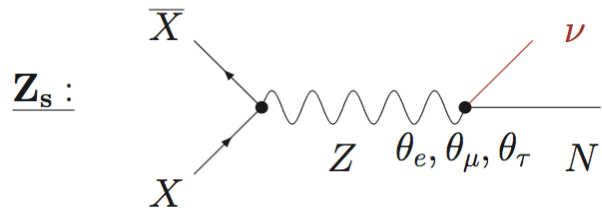
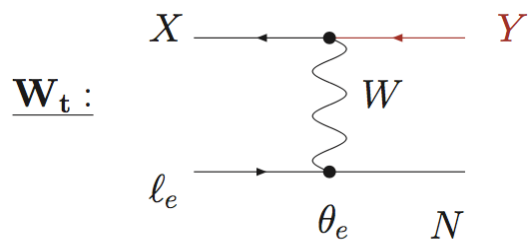
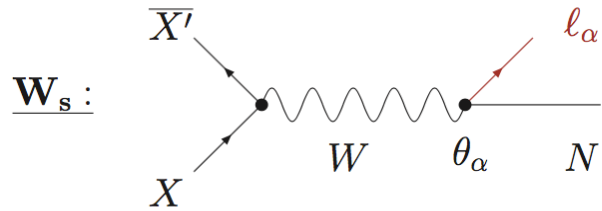
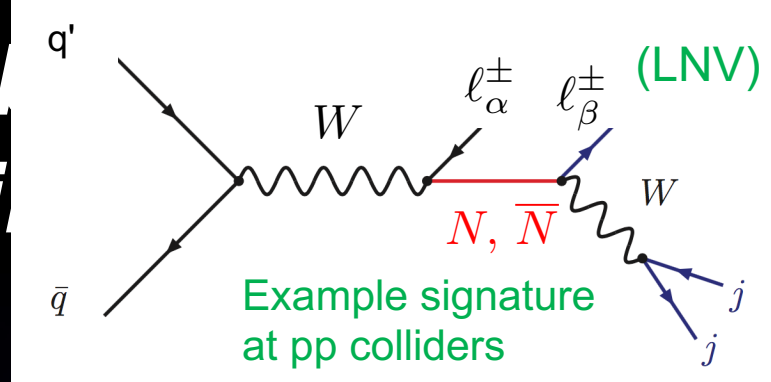
LHeC with  $3 \text{ ab}^{-1}$

To my knowledge, this search channel could yield the best sensitivity to  $e$ - $\tau$  cLFV (among the currently envisioned experiments)!

S.A., A. Hammad, A. Rashed  
(arXiv:2010.08907)

Beyond the "L-like"-symmetry limit:  
Can we observe LNV from the HNLs  
(required to generate light  $m_\nu$ )?

# Signatures for lepton number violation from sterile neutrinos

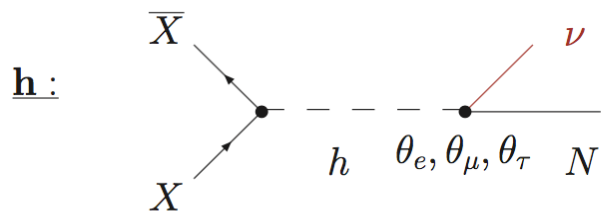
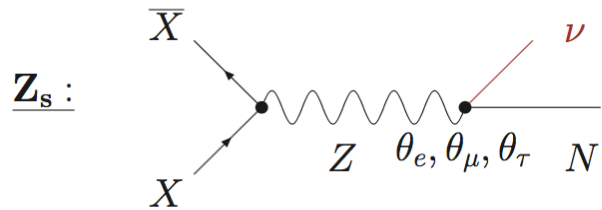
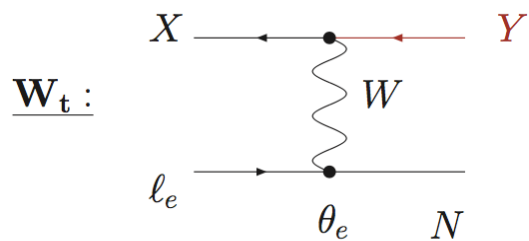
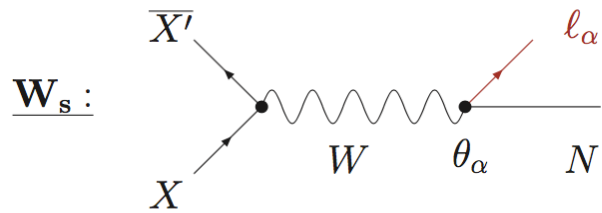
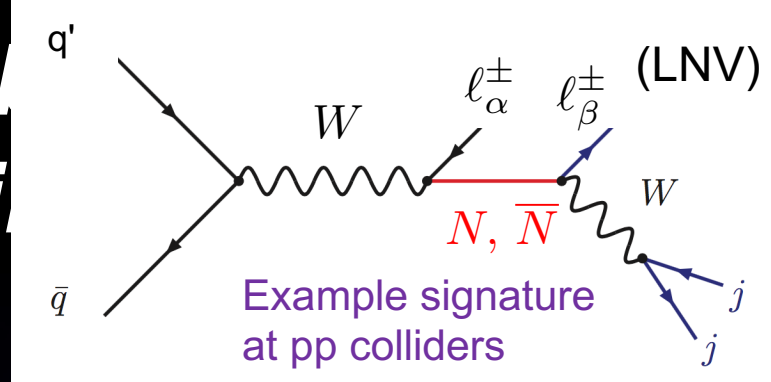


	$e^-e^+$	$pp$	$e^-p$
$\underline{W_s}$	×	✓ + LNV / LFV	×
$\underline{W_t}$	✓	×	✓ + LNV / LFV
$\underline{Z_s}$	✓	✓	×
$\underline{h}$	(✓)	(✓)	(✓)

**Lepton-number violating (LNV) signatures possible (with no SM background at parton level) but expected to be strongly suppressed by the (approximate) protective “lepton number”-like symmetry!**

See e.g. discussion in [Kersten, Smirnov \(2007\)](#)  
 → LNV from neutrino mass generation not observable at LHC

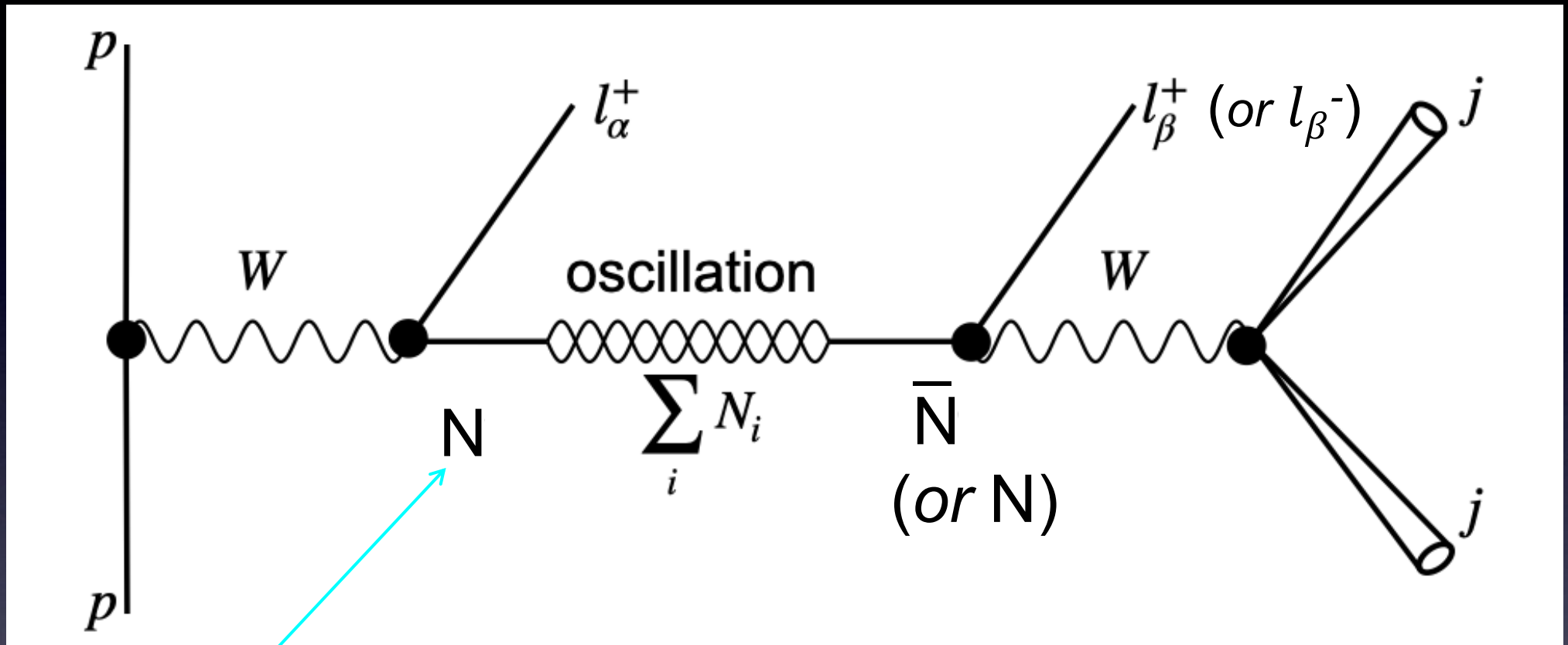
# Signatures for lepton number from sterile neutrinos



	$e^-e^+$	$pp$	$e^-p$
$\underline{W}_s$	$\times$	$\checkmark$ +LNV/LFV	$\times$
$\underline{W}_t$	$\checkmark$	$\times$	$\checkmark$ +LNV/LFV
$\underline{Z}_s$	$\checkmark$	$\checkmark$	$\times$
$\underline{h}$	( $\checkmark$ )	( $\checkmark$ )	( $\checkmark$ )

Statement not entirely valid when one takes into account the possibility of Heavy Neutrino-Antineutrino Oscillations!

# Heavy Neutrino-Antineutrino Oscillations

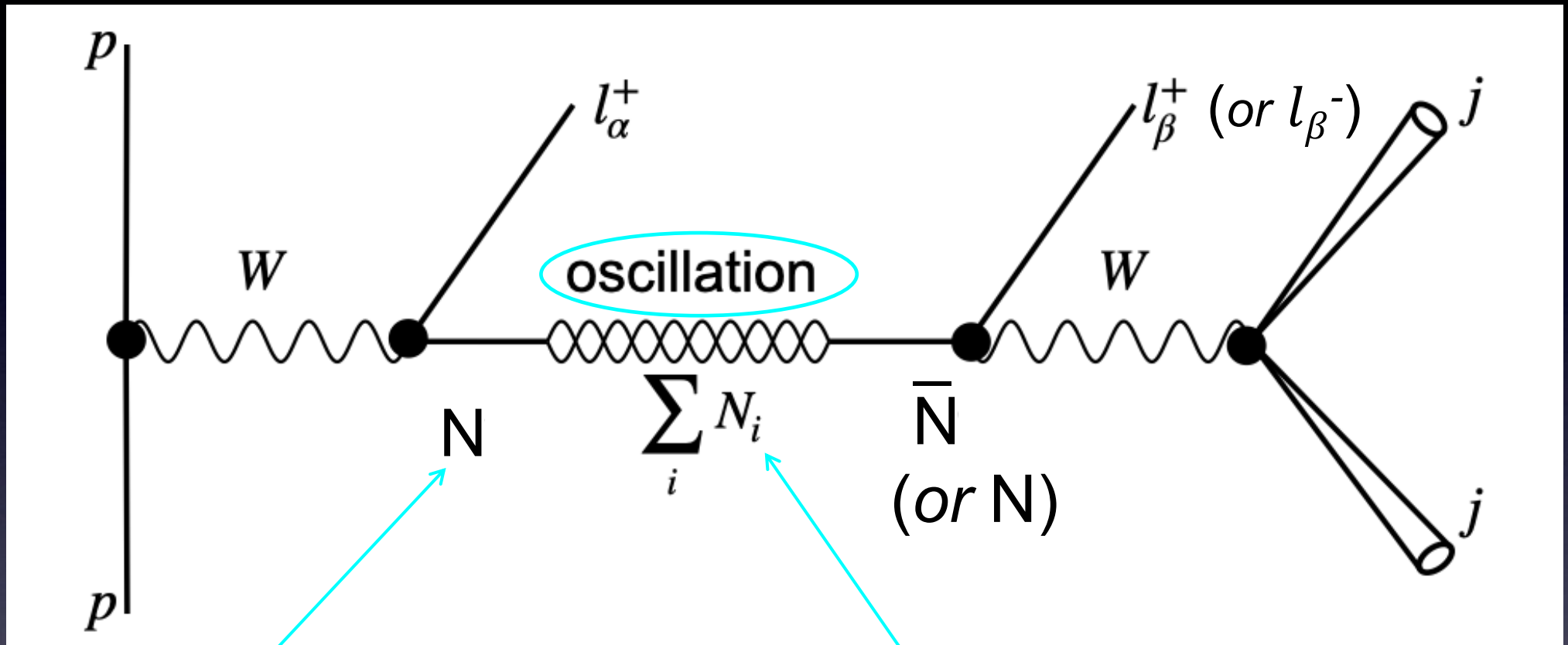


Interaction states: Produced from W decay  
 - "Heavy Neutrinos N" (together with  $l_{\alpha}^{+}$ )  
 - "Heavy Antineutrinos  $\bar{N}$ " (together with  $l_{\alpha}^{-}$ )

They are superpositions of the mass eigenstates:

$$\bar{N} = 1/\sqrt{2}(iN_4 + N_5) \quad N = 1/\sqrt{2}(-iN_4 + N_5)$$

# Heavy Neutrino-Antineutrino Oscillations



Interaction states: Produced from W decay

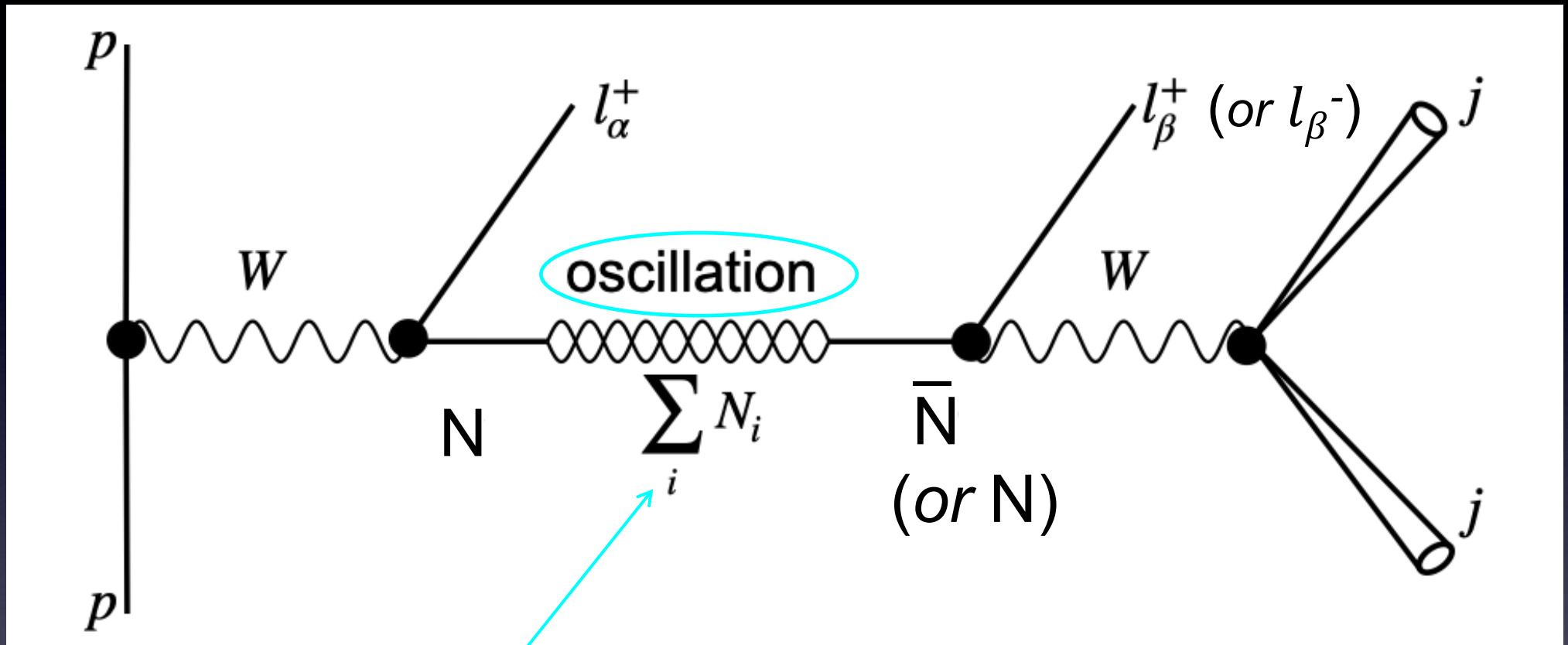
- "Heavy Neutrinos N" (together with  $l_\alpha^+$ )
- "Heavy Antineutrinos  $\bar{N}$ " (together with  $l_\alpha^-$ )

Due to the  $O(\varepsilon)$  perturbations to generate the light neutrino masses:  $\rightarrow$  **mass splitting  $\Delta M$**  between the heavy mass eigenstates  $N_4$  and  $N_5$   
 $\rightarrow$  propagation of interfering mass eigenstates induces oscillations between  $\bar{N}$  and N

They are superpositions of the mass eigenstates:

$$\bar{N} = 1/\sqrt{2}(iN_4 + N_5) \quad N = 1/\sqrt{2}(-iN_4 + N_5)$$

# Heavy Neutrino-Antineutrino Oscillations



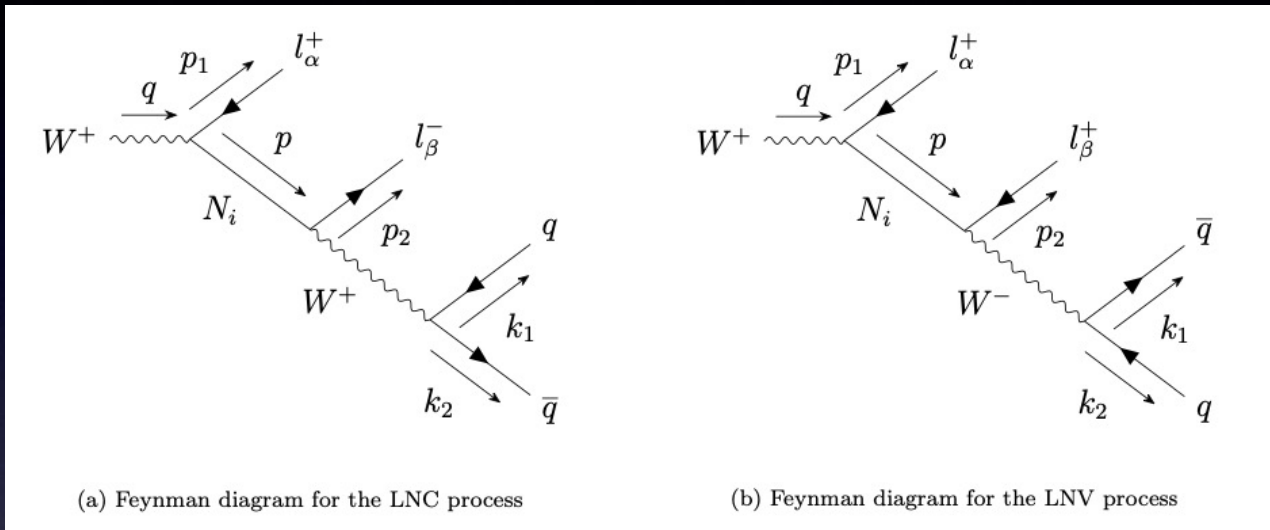
Due to the  $O(\varepsilon)$  perturbations to generate the light neutrino masses:  $\rightarrow$  **mass splitting  $\Delta M$**  between the heavy mass eigenstates  $N_4$  and  $N_5$   
 $\rightarrow$  propagating mass eigenstates induce **oscillations between  $N$  and  $\bar{N}$**

Since an  $N$  decays into a  $l_\alpha^-$  and a  $\bar{N}$  into a  $l_\alpha^+$ , the Heavy Neutrino-Antineutrino Oscillations lead to an **oscillation between LNC and LNV final states**, as a function of the oscillation time (or travelled distance)



# We recently studied the Heavy Neutrino-Antineutrino Oscillations in QFT ...

Study in QFT (using the formalism of external wave packets [cf. Beuthe 2001])



$$\mathcal{A} = \langle f | \hat{T} \left( \exp \left( -i \int d^4x \mathcal{H}_I \right) \right) - \mathbf{1} | i \rangle$$

→ Full oscillation formulae

Oscillation formulae in the SPSS (with  $\varepsilon$ -perturbations, in an expansion):

$$P_{\alpha\beta}^{LNV}(L) = \frac{1}{2 \sum_{\beta} |\theta_{\alpha}|^2 |\theta_{\beta}|^2} \left( |\theta_{\alpha}|^2 |\theta_{\beta}|^2 (1 - \cos(\phi_{45} L)) \right. \\ \left. - 2(I_{\beta} |\theta_{\alpha}|^2 + I_{\alpha} |\theta_{\beta}|^2) \sin(\phi_{45} L) \right),$$

← LO

← NLO

$$P_{\alpha\beta}^{LNC}(L) = \frac{1}{2 \sum_{\beta} |\theta_{\alpha}|^2 |\theta_{\beta}|^2} \left( |\theta_{\alpha}|^2 |\theta_{\beta}|^2 (1 + \cos(\phi_{45} L)) \right. \\ \left. - 2(I_{\beta} |\theta_{\alpha}|^2 - I_{\alpha} |\theta_{\beta}|^2) \sin(\phi_{45} L) \right).$$

← LO

← NLO

where

$$I_{\beta} := \text{Im}(\theta_{\beta}^* \theta'_{\beta} \exp(-2i\Phi)),$$

$$\phi_{ij} := -\frac{2\pi}{L_{ij}^{osc}} = -\frac{m_i^2 - m_j^2}{2|\mathbf{p}_0|},$$

$$\Phi := \frac{1}{2} \text{Arg}(\vec{\theta}' \cdot \vec{\theta}^*).$$

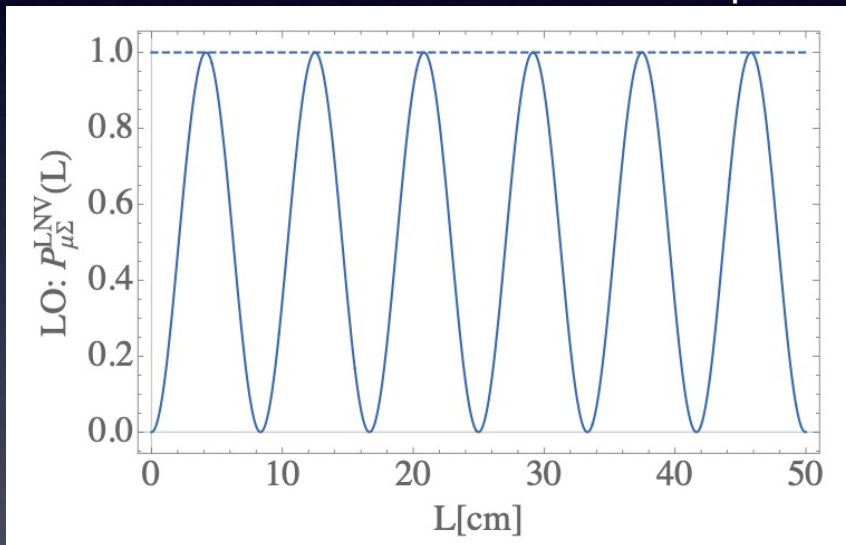
S.A., J. Roskopp (arXiv:2012.05763)

# We recently studied the Heavy Neutrino-Antineutrino Oscillations in QFT ...

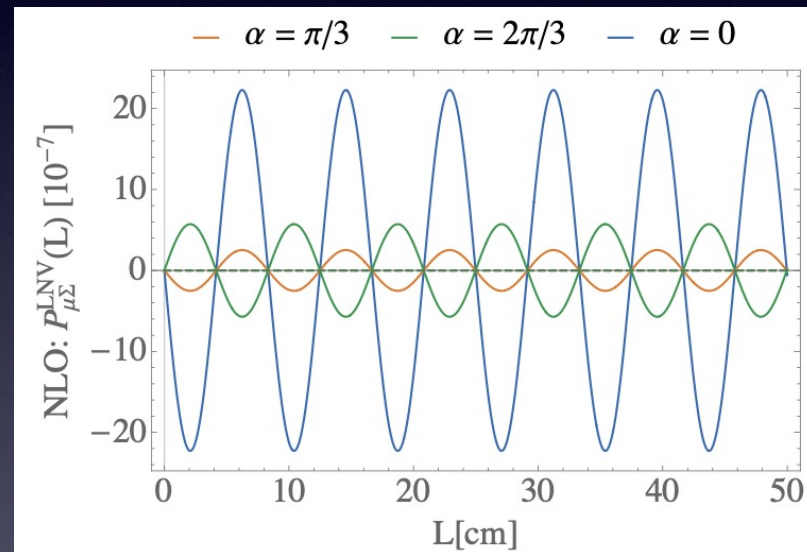
$$P_{\alpha\beta}^{LNV}(L) = \frac{1}{2 \sum_{\beta} |\theta_{\alpha}|^2 |\theta_{\beta}|^2} \left( |\theta_{\alpha}|^2 |\theta_{\beta}|^2 (1 - \cos(\phi_{45}L)) - 2(I_{\beta} |\theta_{\alpha}|^2 + I_{\alpha} |\theta_{\beta}|^2) \sin(\phi_{45}L) \right),$$

$$P_{\alpha\beta}^{LNC}(L) = \frac{1}{2 \sum_{\beta} |\theta_{\alpha}|^2 |\theta_{\beta}|^2} \left( |\theta_{\alpha}|^2 |\theta_{\beta}|^2 (1 + \cos(\phi_{45}L)) - 2(I_{\beta} |\theta_{\alpha}|^2 - I_{\alpha} |\theta_{\beta}|^2) \sin(\phi_{45}L) \right).$$

LO: ... for some chosen benchmark point



NLO:



NLO effects are "flavour oscillations" ... oscillations remain when summing LNC+LNV  
... they go to 0 when additionally summing over all outgoing flavours

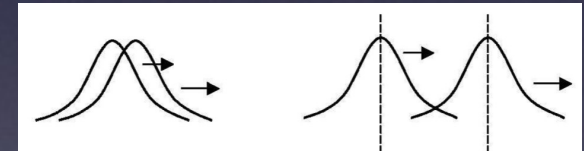
$$P_{\alpha\beta}^{LNC}(L) + P_{\alpha\beta}^{LNV}(L) = \frac{1}{\sum_{\beta} |\theta_{\alpha}|^2 |\theta_{\beta}|^2} \left( |\theta_{\alpha}|^2 |\theta_{\beta}|^2 - 2I_{\beta} |\theta_{\alpha}|^2 \sin(\phi_{45}L) \right)$$

S.A., J. Roskopp (arXiv:2012.05763)

# We recently studied the Heavy Neutrino-Antineutrino Oscillations in QFT ...

Furthermore:

- We confirmed the LO formulae used in previous works.  
See e.g.: G. Anamiati, M. Hirsch and E. Nardi (2016), G. Cvetič, C. S. Kim, R. Kogerler and J. Zamora-Saa (2015), ... (see also Refs in arXiv:2012.05763 for other works)
- We showed that in the SPSS +  $\varepsilon$ -terms: only  $\Delta M$  (as additional parameter) relevant for describing the oscillations at LO  
→ Proposal of the **SPSS $\Delta M$**  (i.e. the SPSS plus only  $\Delta M$  as additional parameter) as suitable benchmark scenario
- We carefully discussed how the "observability conditions" can be checked (such as e.g. if coherence is maintained, etc.)  
→ satisfied for the considered parameter region
- We discussed the NLO effects (i.e. the flavour oscillations) and showed that for the considered benchmark point they are tiny.

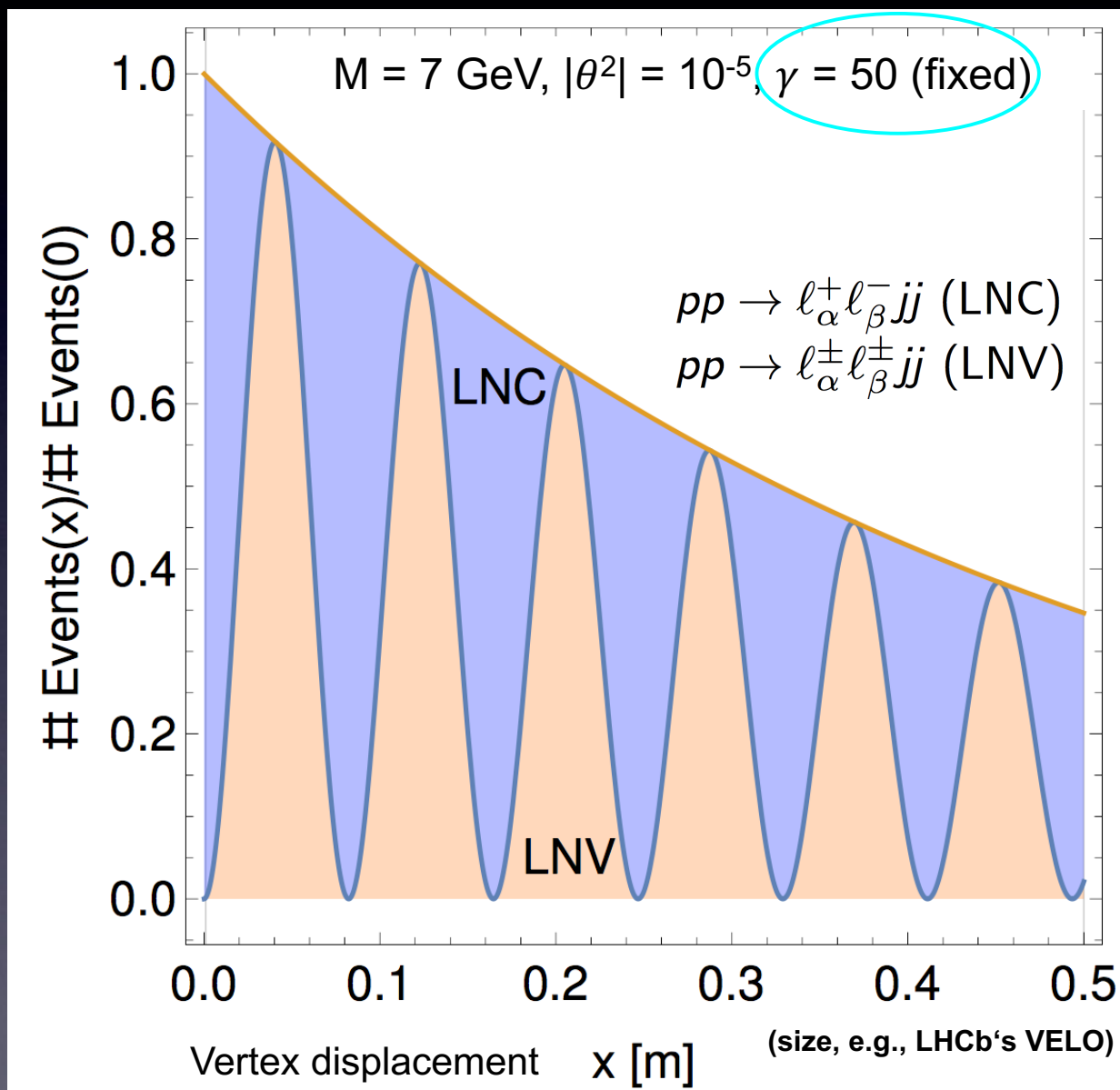


S.A., J. Roszkopp (arXiv:2012.05763)

# Signal: Oscillating fraction of LNV / LNC decays with lifetime ( $\rightarrow$ displacement)

**Example:**  
Linear seesaw  
(inverse mass  
ordering)

(using the prediction  
for  $\Delta M$  in the minimal  
linear seesaw  
model for inverse  
neutrino mass  
ordering)



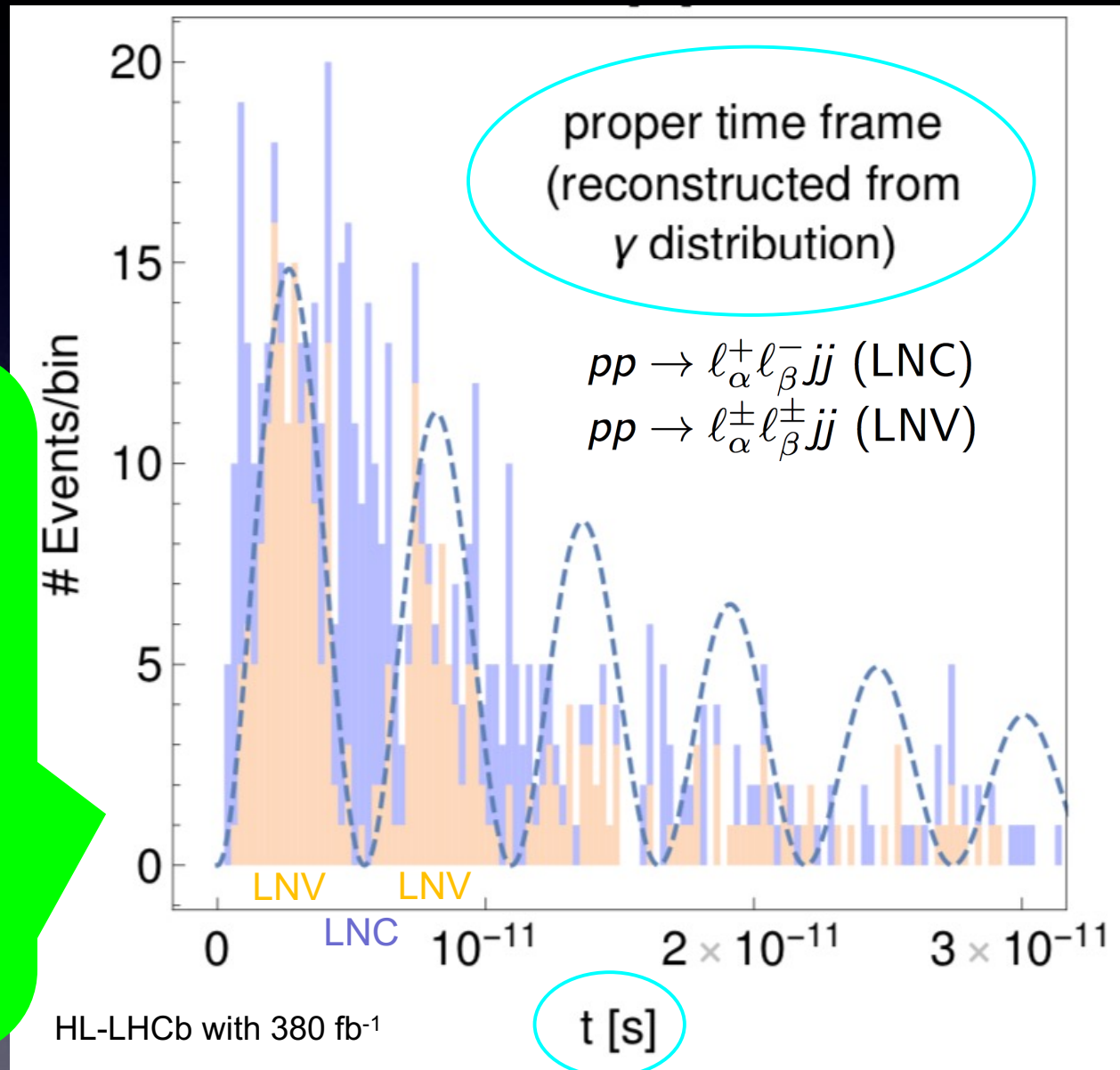
For this plot: fixed  $\gamma$   
factor (instead of  
distribution), no  
uncertainties yet.

S. A., E. Cazzato,  
O. Fischer  
(arXiv:1709.03797)

# Estimate: Simulated signal including uncertainties in proper time frame ...

Example:  
Linear seesaw  
(inverse mass ordering)

Full analysis at the reconstructed level in preparation ... plus Madgraph "patch" for simulating the oscillations, SPSS $\Delta$ M model file (with Johannes Roskopp and Jan Hajer)



Distribution of  $\gamma$  factors included  
→ one has to reconstruct signal as function of lifetime (not displacement)

S. A., E. Cazzato,  
O. Fischer  
(arXiv:1709.03797)

... a little remark on the LNV, and the recent discussion about testing "Dirac HNL" vs. "Majorana HNL"

# ***... given the various potentially observable phenomena, including LNV***

→ **SPSS $\Delta$ M** (i.e. the SPSS with  $\Delta$ M as additional free parameter) appears to be a **useful benchmark scenario (can capture all of the effects discussed in my talk 😊)\***

→ ... effects **cannot** be described by

- **1 Majorana HNL** (LNV/LNC ratio always 50%- no oscillations, for observable effects too large  $m_{\nu i}$ , need at least 2 to describe  $m_\nu$  😞)
- **1 Dirac HNL** (no LNV – no oscillations, no contribution to  $m_\nu$  😞)

***\*) or alternatively of course a full 2+n HNL model***

# Summary

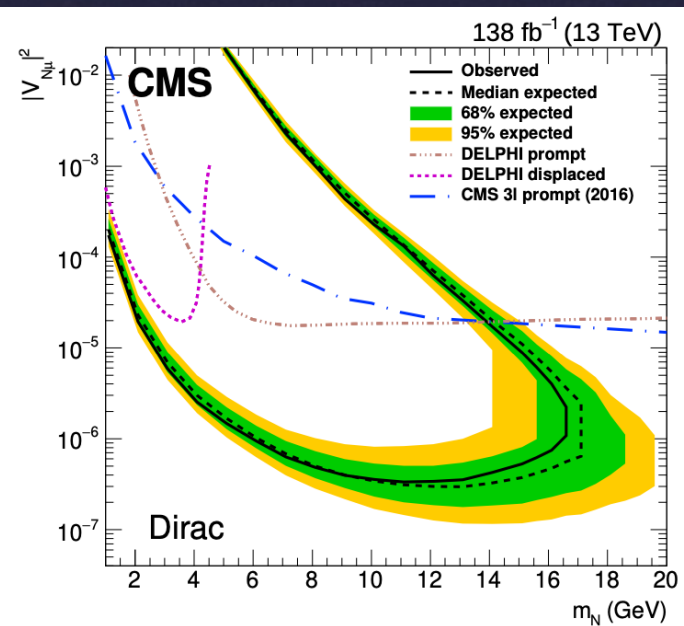
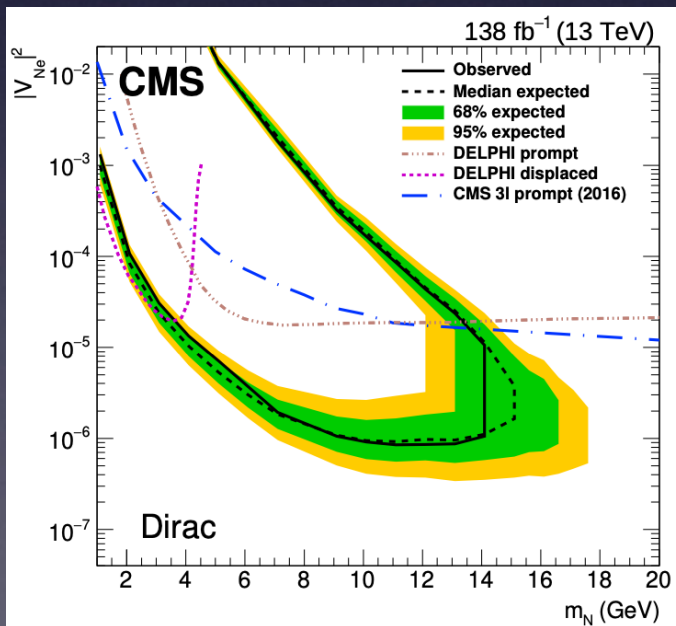
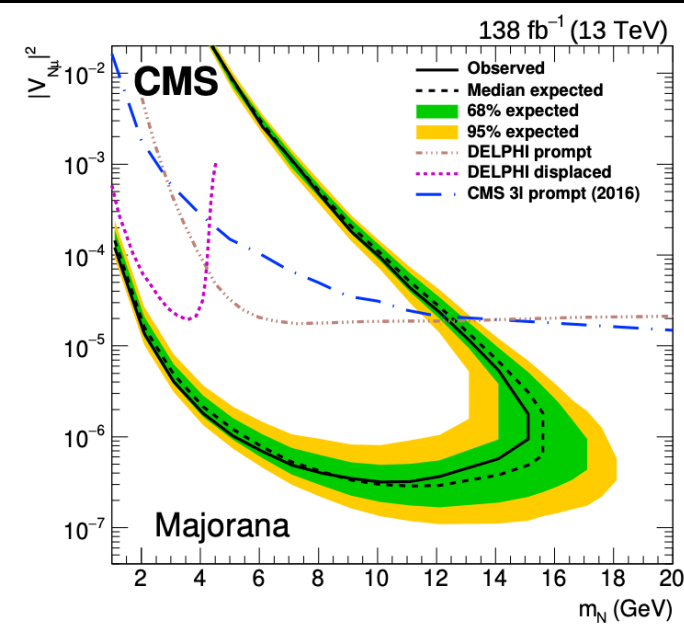
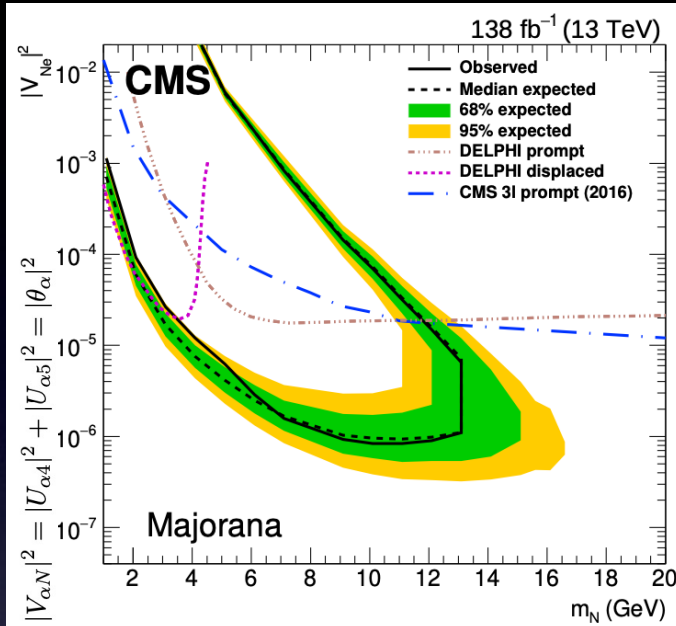
- With protective “lepton number”-like symmetry, the small observed  $m_\nu$  can be explained with “large  $y_\nu$ ” and  $\sim$  EW/TeV scale  $M_R$ . **Low scale Seesaw: HNLs testable at present and future colliders**
- → Benchmark scenario: **SPSS (or SPSS $\Delta$ M)**
- **LFV (but LNC) signatures** can be very sensitive, especially at future ep colliders.
- **LNV**, although (apparently) suppressed by the “lepton number”-like symmetry, can be observable at colliders. It can be understood as emerging from **Heavy Neutrino-Antineutrino Oscillations**
- Opens up possibilities for testing neutrino mass generation at colliders ...
- In summary: **Fascinating prospects for probing HNLs at future colliders!**



**Thanks for  
your attention!**

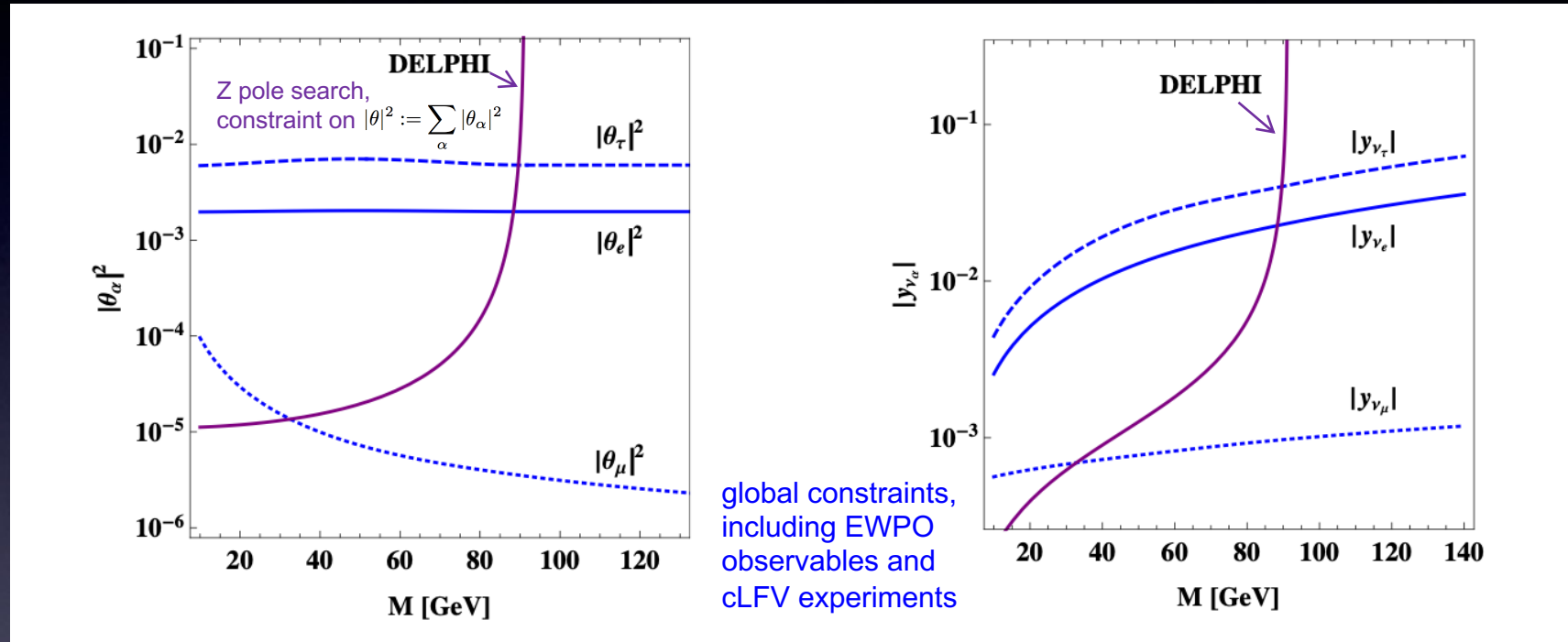
# Extra Slides 1: Present constraints

# Strongest bounds for $M < M_W$ currently by CMS



CMS Collaboration  
arXiv: 2201.05578

# In addition: Constraints from precision experiments (EWPO, cLFV, ...) – also apply to higher $M$



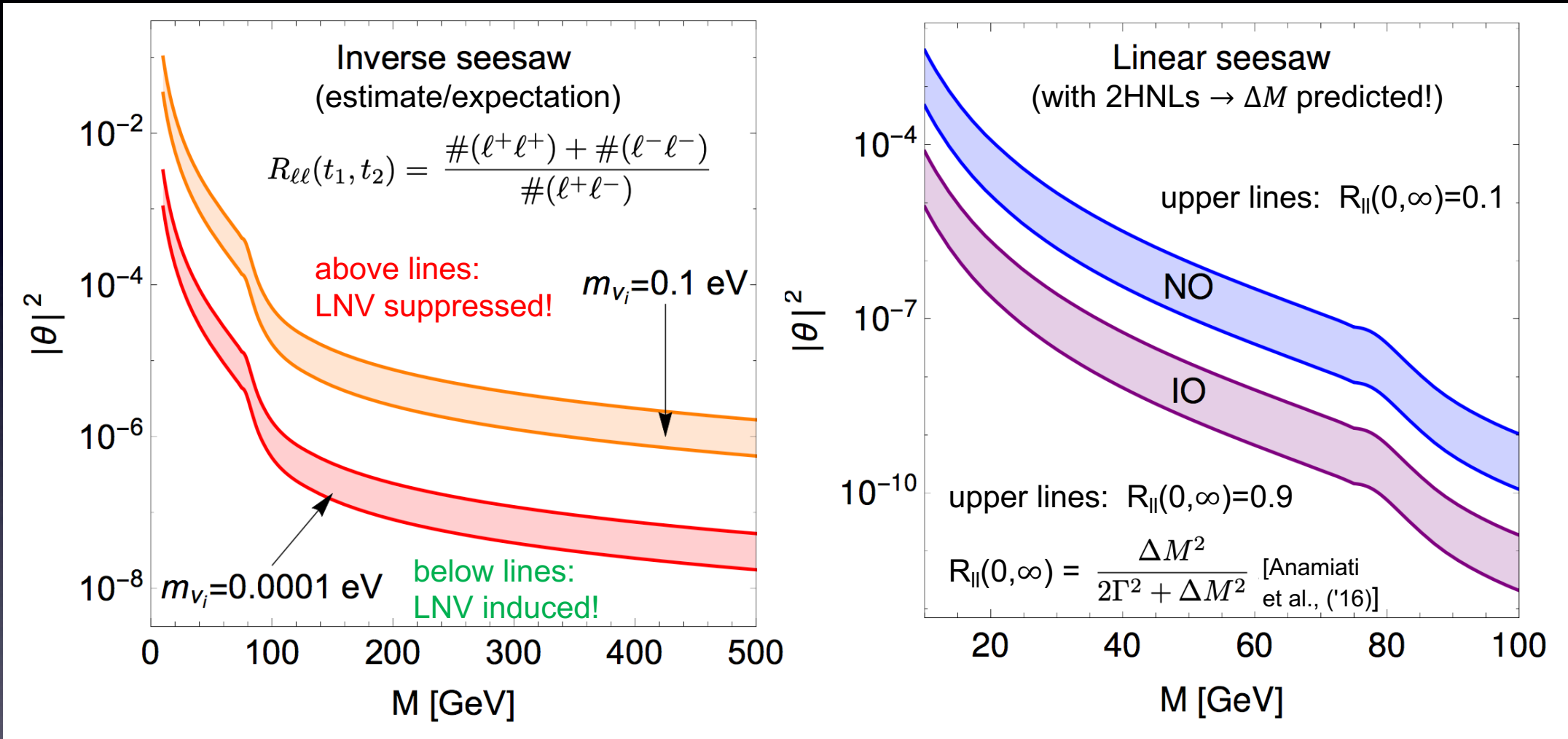
Constraints from global fit ( $M > 10$  GeV): S.A., O. Fischer (arXiv:1502.05915)

For a similar study, see also: E. Fernandez-Martinez, J. Hernandez-Garcia, J. Lopez-Pavon (arXiv:1605.08774)

Constraints for smaller  $M$ , see e.g.: M. Drewes, B. Garbrecht (arXiv:1502.00477)

# Extra Slides 2: SPSS parameters for which LNV is induced

# For which parameters is LNV induced? Even if not resolvable → "integrated effect"



Plot from S. A., E. Cazzato, O. Fischer (arXiv:1709.03797)

Integrated effect, see also: G. Anamiati, M. Hirsch and E. Nardi (hep-ph/1607.05641), M. Drewes, J. Klaric, P. Klose (hep-ph/1907.13034)