

# A Toy Monte Carlo to estimate the Radiative Muon Capture background for $\mu^-e^+$ conversion

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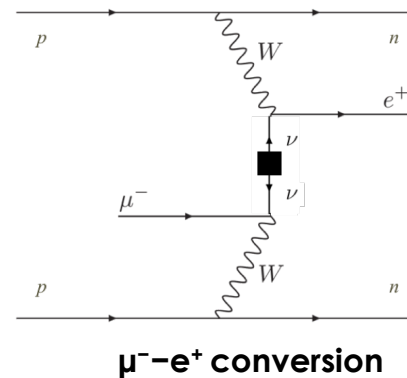
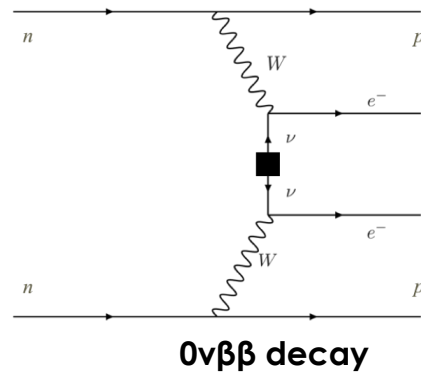


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# Lepton Number Violation

- As well as for CLFV, an observation of LNV will represent a clear sign of New Physics
- Processes with the change of Lepton Number by 2 ( $\Delta L = 2$ ) have been mostly explored through the  $0\nu\beta\beta$  decay, which correspond to an investigation on the  $ee$  sector.

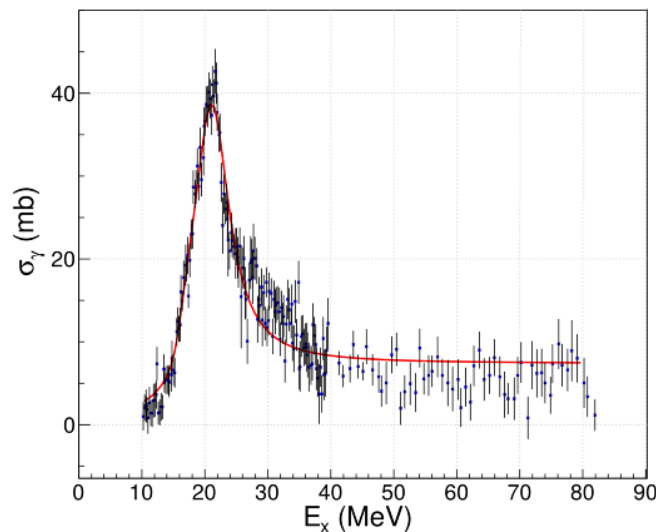


- Even if the sensitivity of  $0\nu\beta\beta$  to LNV is prominent with respect to the one of muon conversion, flavour effect can strongly reduce the rate of  $0\nu\beta\beta$  ( diagonal sector) favouring processes occurring in off-diagonal sector, like the  $\mu^- - e^+$  conversion.

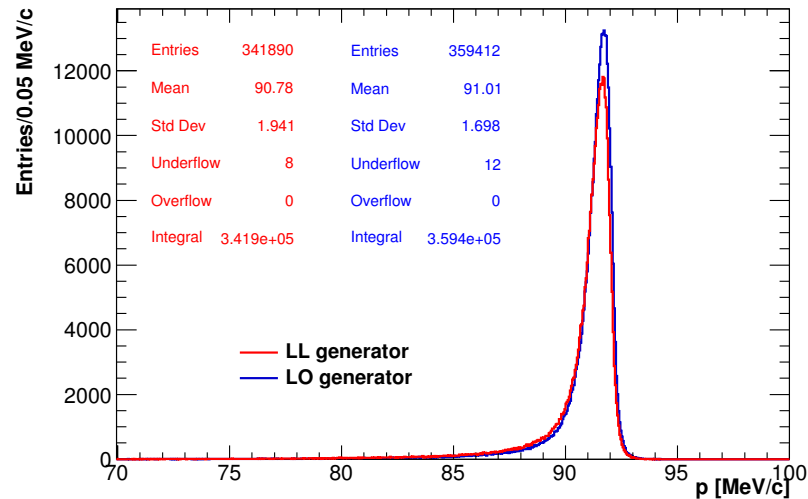
# $\mu^- - e^+$ conversion

- Mu2e will search for the  $\mu^- + {}^{27}\text{Al} \rightarrow e^+ + {}^{27}\text{Na}$
- Conversion can undergo through:
  - Giant Dipole Resonance: modelled with a Breit-Wigner distribution with 21.1 MeV mean and a width of 6.7 MeV  $\rightarrow E_{e^+} = 83.9$  MeV. Strongly suffer from RMC background
  - Ground State Transition:  **$E_{e^+} = 92.32$  MeV**

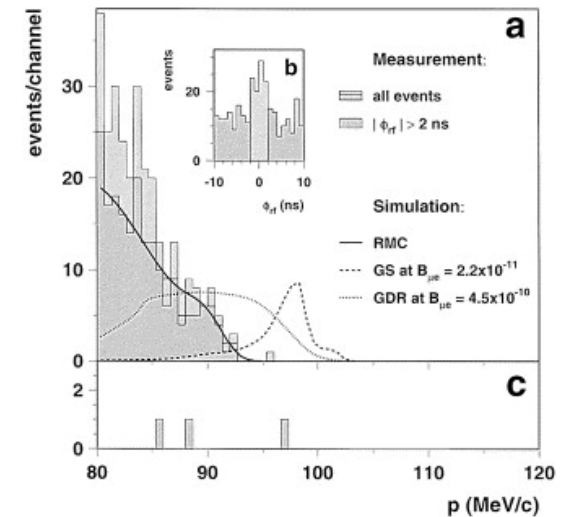
Giant Dipole Resonance



Ground State



Sindrum-II results



In the following we consider only the ground state transition. We will look for signal requiring 1  $e^+$  track only satisfying a set of Quality Track to reduce the high tails.

$$B_{\mu^- e^+}^{GS} < 1.7 \cdot 10^{-12} \quad (90\% \text{ CL})$$

$$B_{\mu^- e^+}^{GDR} < 3.6 \cdot 10^{-11} \quad (90\% \text{ CL})$$

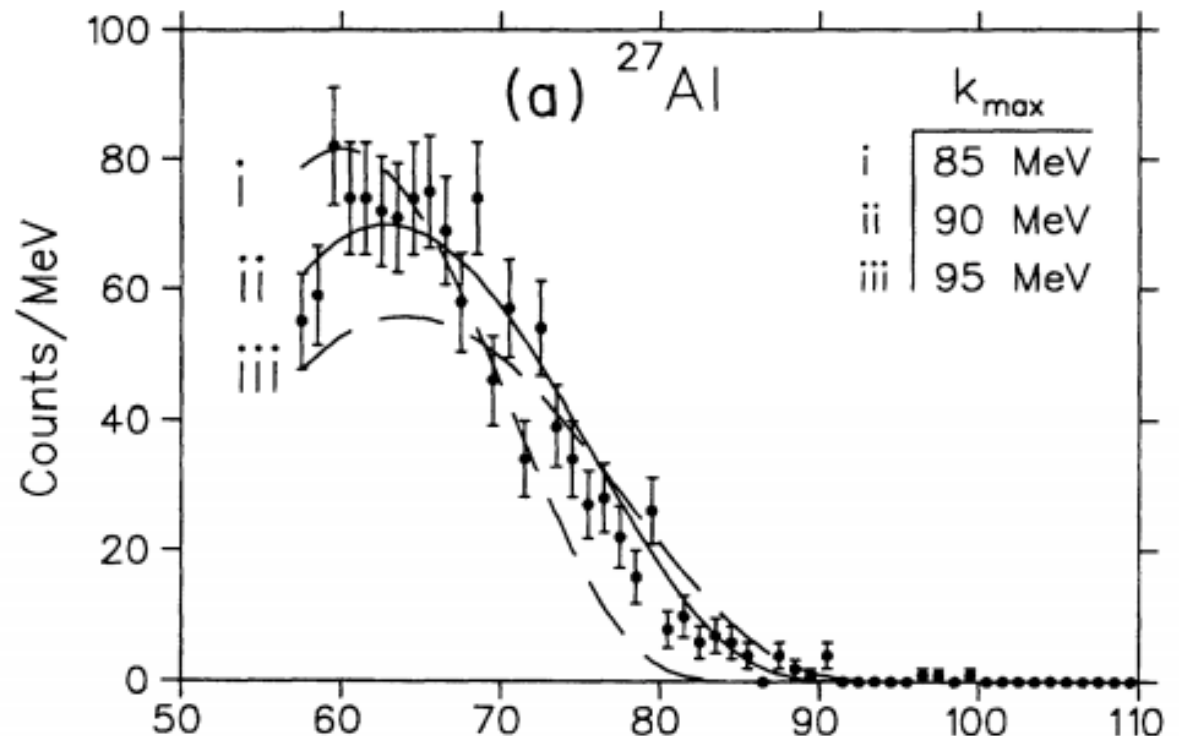
J. Kaulard et al., *Improved limit on the branching ratio of  $\mu^- \rightarrow e^+$  conversion on titanium*. Phys. Lett. B 422, 334 (1998).

# Background

- Prominent background:
  - **Radiative Muon Capture:** detailed description in this presentation
  - **Cosmic Rays :** they should be smaller than 0.4 events as in the case of CE since the  $e^+, e^-$  observed in CR generated sample is similar. A large production of CR is under way.
  - **Antiprotons:** when not decaying in the TS they can interact in ST and produce delayed secondaries.
  - **Radiative Pion Capture:** Pions that survive to arrive at the aluminum stopping target during the delayed live gate can potentially give rise to a large background from the  $\pi^- + \text{Al} \rightarrow \gamma(*) + \text{X}$  process. Only the one produced late could represent a real background

# Radiative Muon Capture

- From previous considerations, we expect that the prominent background for the  $\mu^- - e^+$  search will be positron produced in the  $\mu^- + {}^{27}\text{Al} \rightarrow \gamma + \nu_\mu + {}^{27}\text{Mg}$
- The photon in the final state can convert internally or externally, potentially yielding a positron with an energy consistent with that of a conversion positron.
- Last reported measures from TRIUMF experiment on Al stated an endpoint of the  $E_\gamma$  distribution at  $k_{\text{max}} \sim 90 \text{ MeV}$  depending on the years of the publication



# TOY MC: Procedure

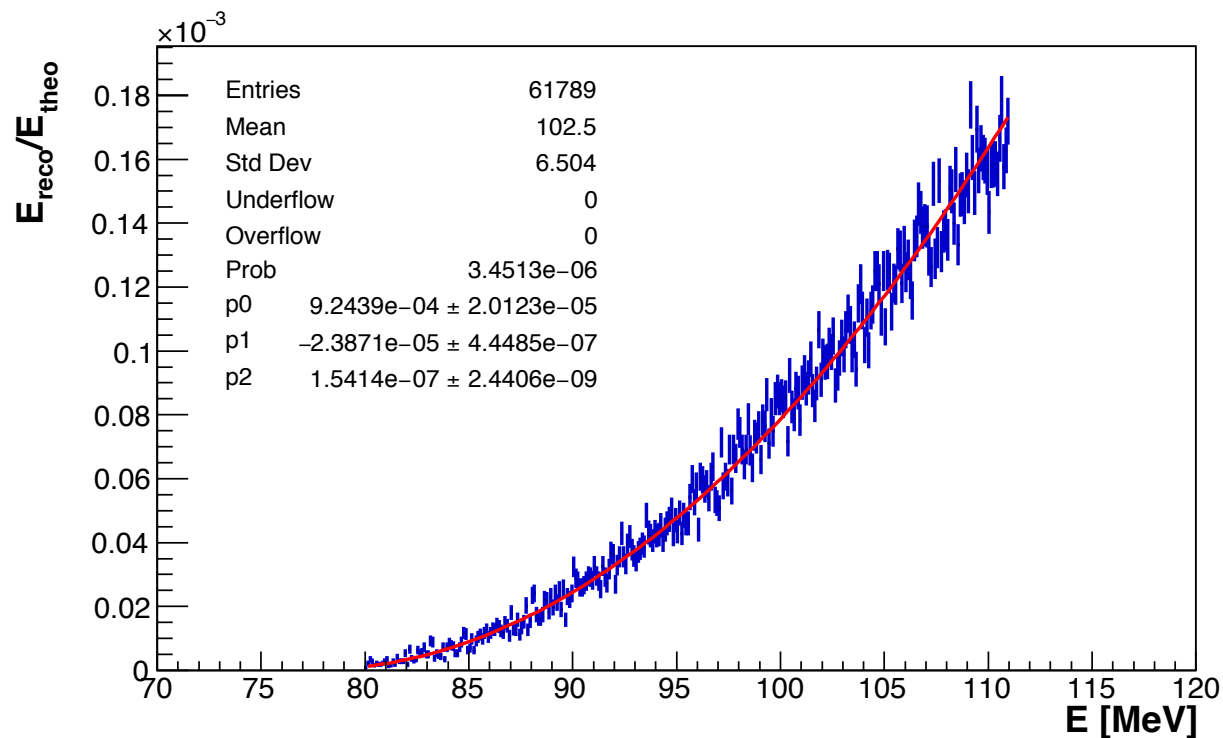
- Since the production of photons with the right RMC spectrum and the tracker acceptance are small numbers, a full simulation of this background will take months. We therefore evaluated the number of background expected at the end of the analysis cut with a Toy MC based on:
  - A fast parametrisation of the tracker acceptance as a function of  $E_\gamma$
  - An application of the RMC spectrum
  - an  $e^+$  momentum extraction from a 2D plot between  $P_{e^+}$  -  $E_\gamma$
  - a convolution with two different curve of momentum resolution

In the following 3 different  $k_{\max}$  will be investigated.  
 $k_{\max} = 90.1$  MeV,  $91.6$  MeV ( $\sigma = 0.5$  MeV),  $91.9$  MeV ( $\sigma = 1.8$  MeV)  
These value have been selected following the results of the TRIUMF experiment and Mu2e collaboration calculation supposing a  $\sigma = 0.5$  MeV on  $k_{\max}$

# Obtaining the Fitting function

- Even if the photons are generated flat from 80-111 MeV.
- For each photon in the flat gamma spectrum, we saved only the events that have particles detected in the tracker. Knowing the total number of generated photon and the reconstructed one, the tracker acceptance can

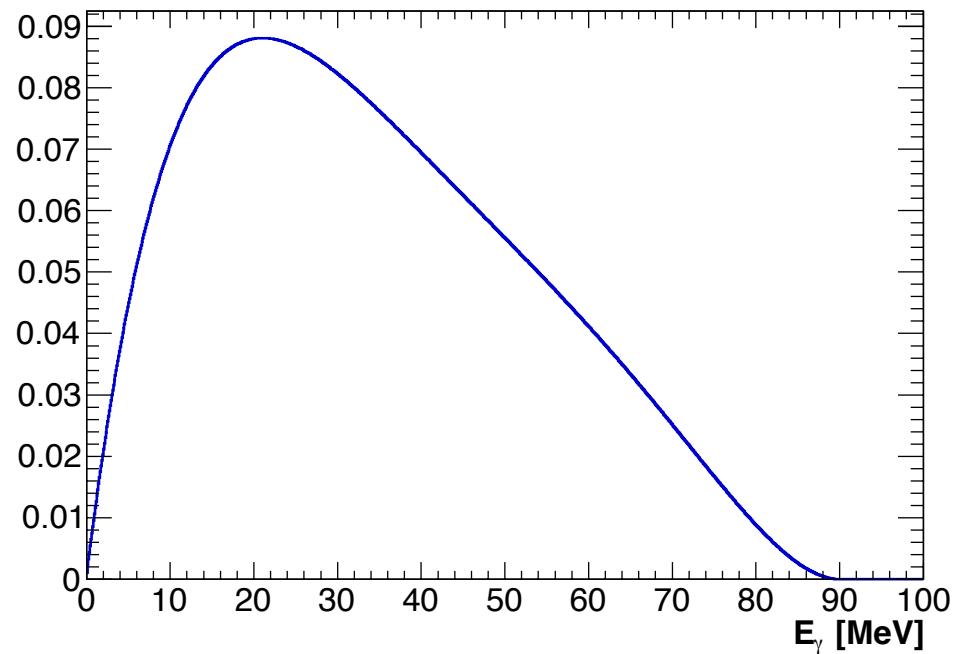
be evaluated in each bin as:  $\alpha_i = \frac{E_i^{reco}}{E_i^{theo}}$



# Consider only RMC

- The RMC can be modelled using the Closure approximation:

$$\frac{d\Lambda_\gamma(E_\gamma)}{dE_\gamma} = N (1 - 2x + 2x^2) x(1 - x)^2 \quad x = \frac{E_\gamma}{k_{max}}$$

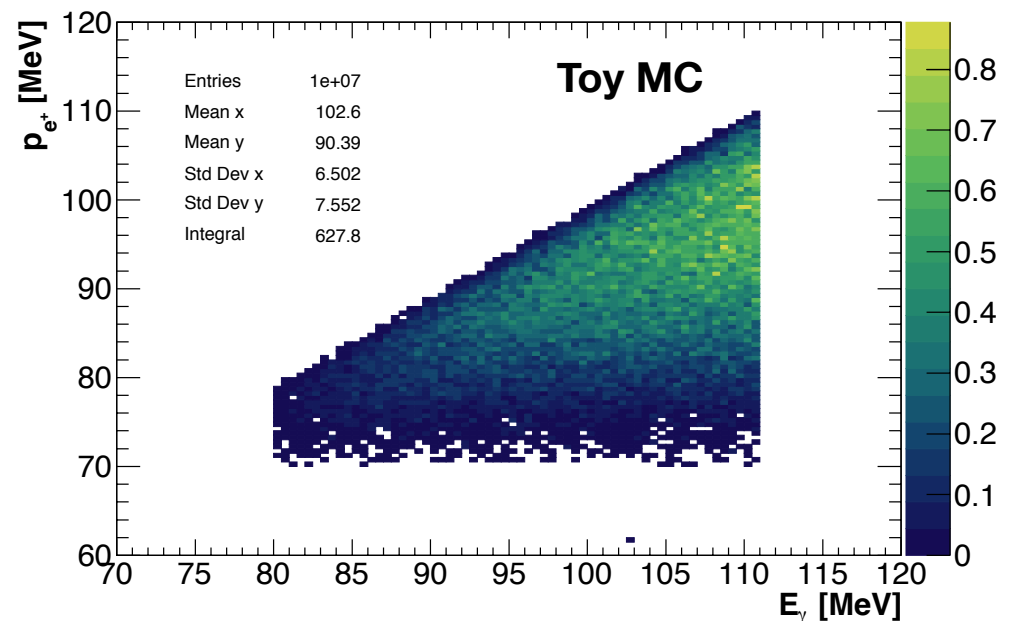
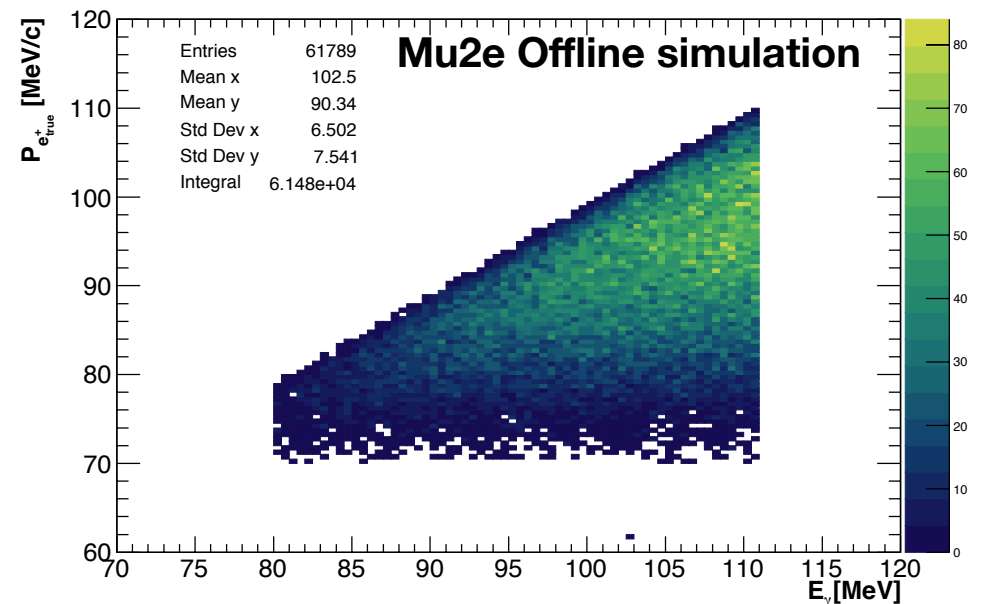


- Each Toy MC photon energy is weighted following the Closure Approximation to account only for the RMC process



# Obtaining the fitting function

- From the Official Simulation the 2D histogram  $p_{\text{true}}$  vs  $E_\gamma$  is divided in 0.1 MeV slices and the projection on the  $p_{\text{true}}$  axis is saved.
- Extract from a flat distribution and apply the acceptance correction and then extract from the relative  $p_{\text{true}}$  slice a momentum
- Good agreement shown:
  - Offline:  $9.8 \times 10^8$  events simulated correspond to  $6.148 \times 10^4$  reconstructed events  $\rightarrow$  627.34 expected reconstructed events considering  $10^7$  events
  - MC toy: 627.8 event produced



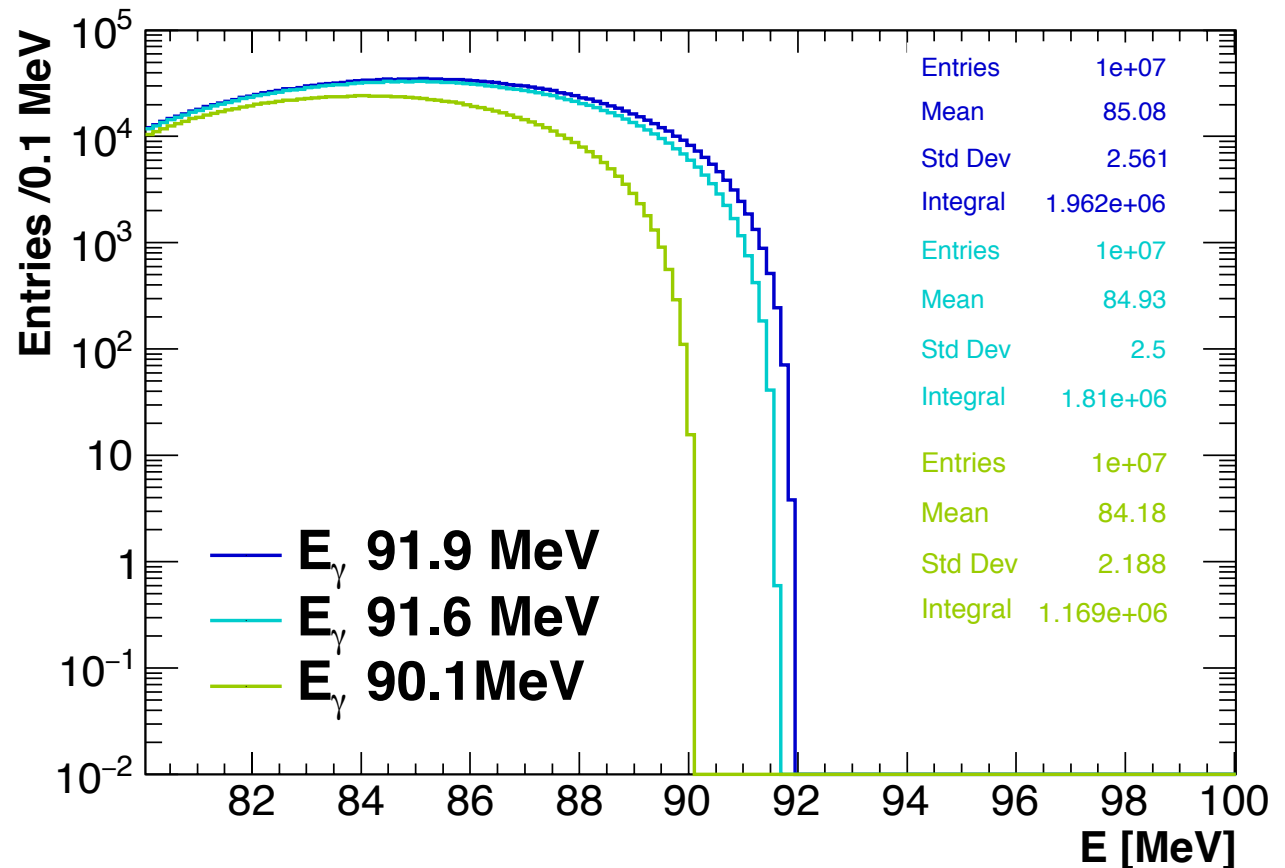
# $E_\gamma$ distribution

- It is necessary to scale to entire Mu2e Life time using :

$$SF = N_{pot} \times \mathcal{P}_{stop} \times P_{\mu capt} \times \mathcal{P}_{clos} \times \frac{\mathcal{R}(E > 80)}{\mathcal{R}(E > 57)} \quad \frac{\mathcal{R}(E > 80)}{\mathcal{R}(E > 57)} = \frac{\int_{E>80} (1 - 2x + 2x^2)x(1 - x)^2 dx}{\int_{E>57} (1 - 2x + 2x^2)x(1 - x)^2 dx}$$

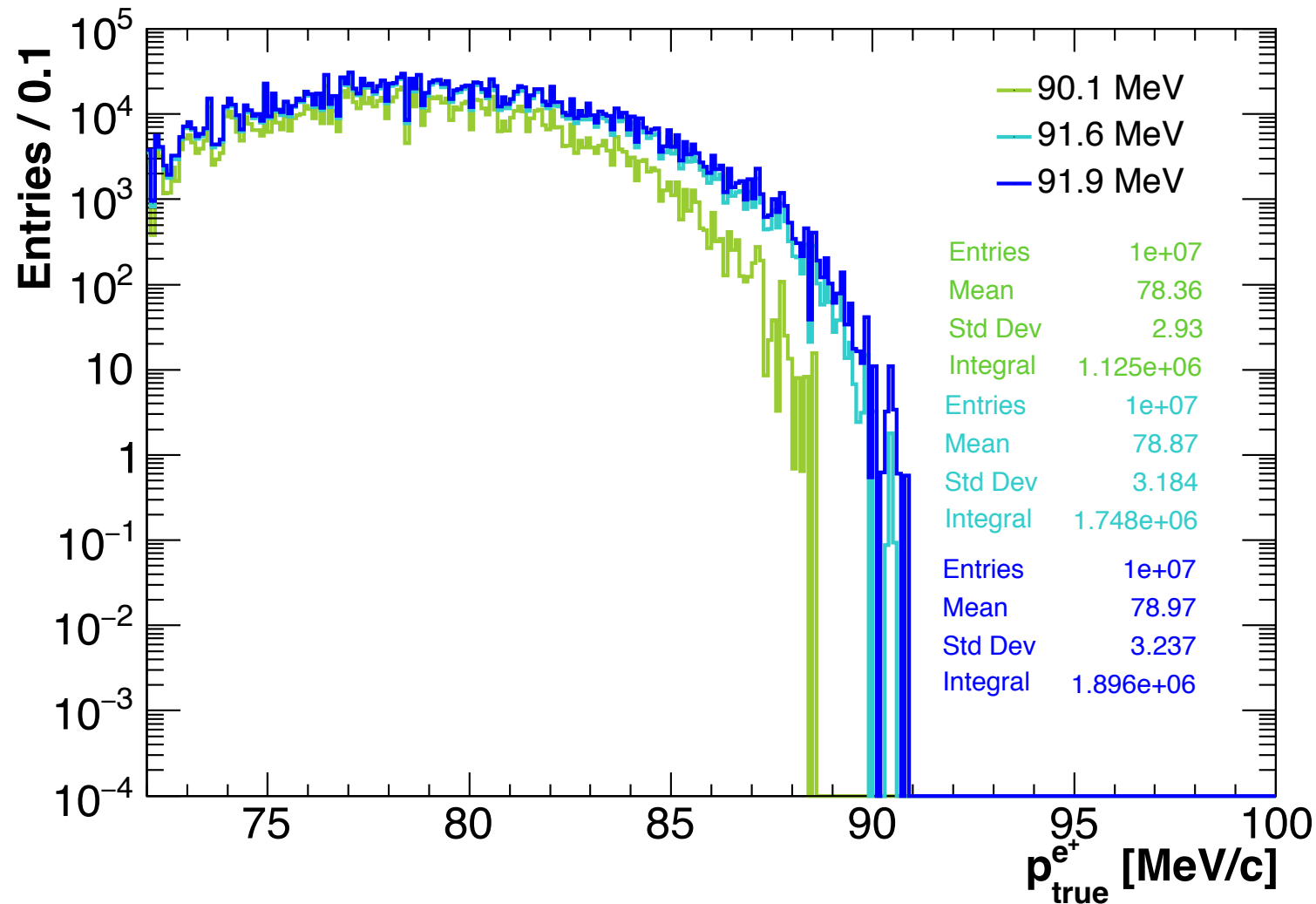
$N_{POT} = 3.6 \times 10^{20}$   
 $P_{stop} = 0.015$   
 $P_{\mu capt} = 0.61$   
 $P_{clos} = 1.43 \times 10^{-5}$

- As a control we produce the  $E_\gamma$  spectrum scaled for acceptance in the tracker and RMC weights



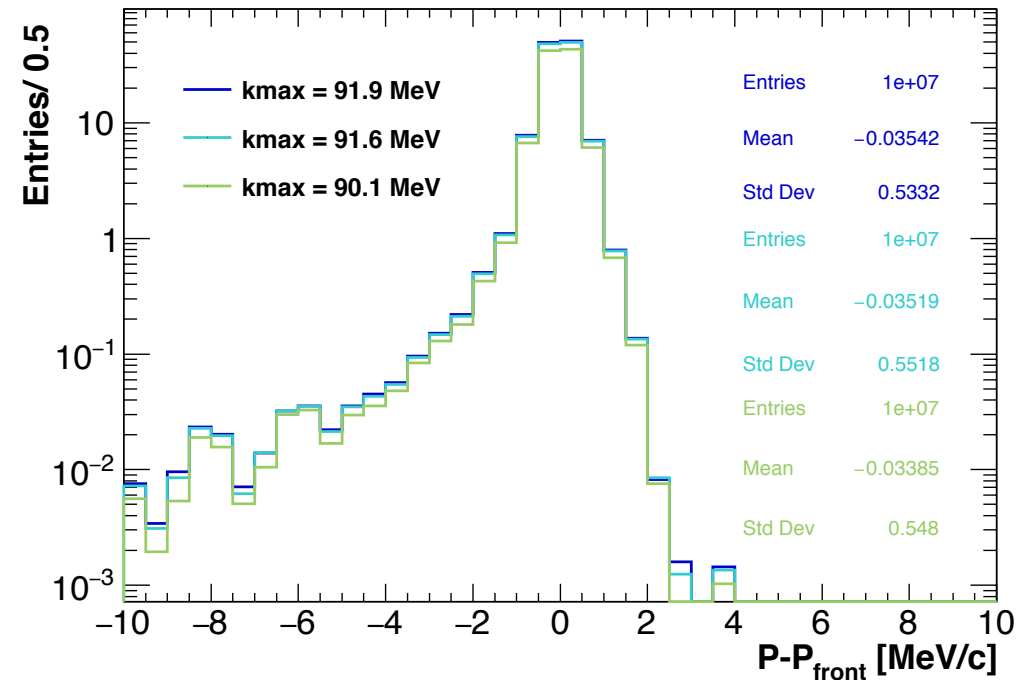
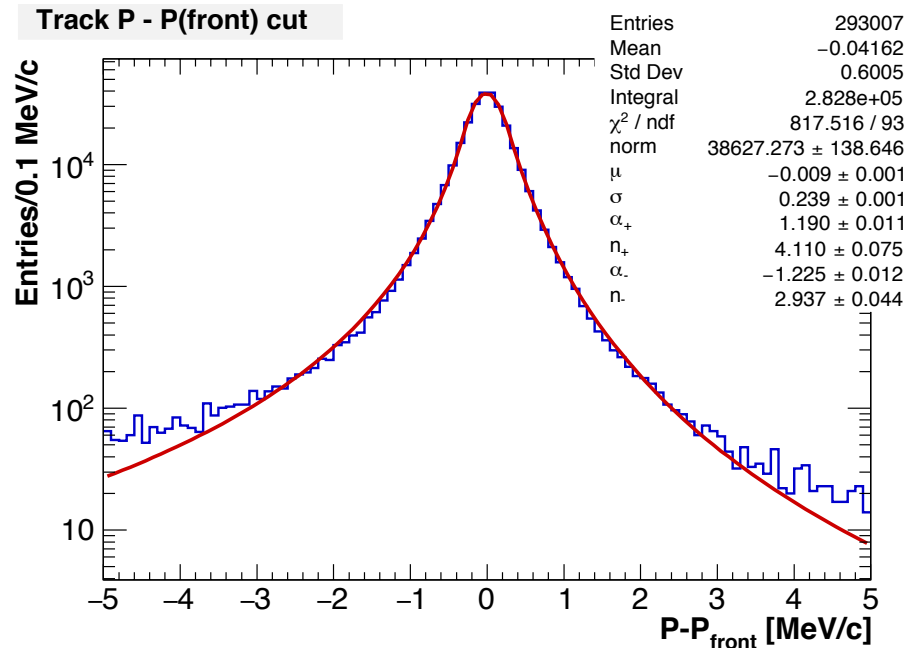
# $e^+$ momentum extraction

- The positron momentum is directly extracted from the 2D plot be per each photon energy already scaled

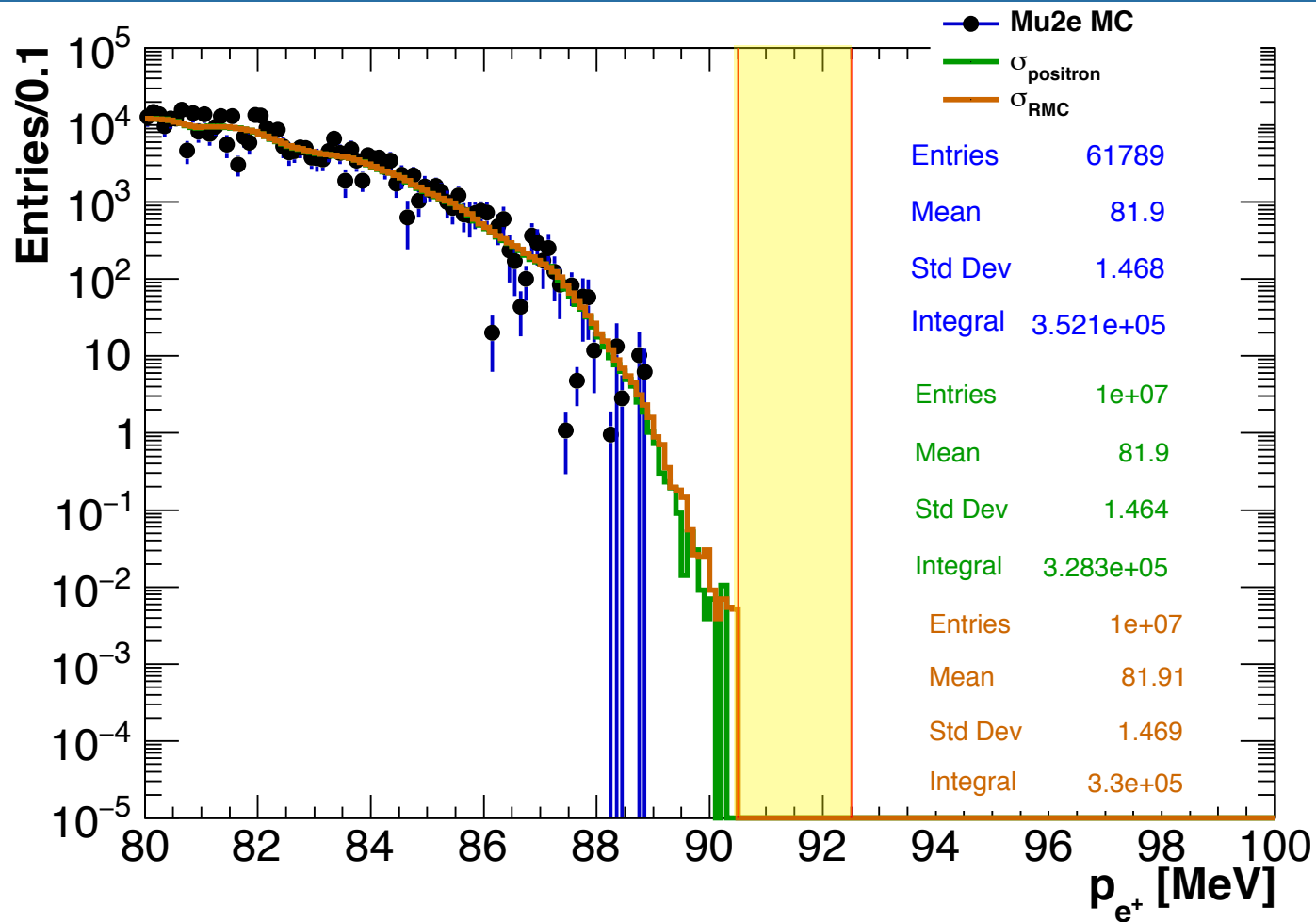


# Add the resolution effect

- Add the tracking resolution effect following two different strategies:
  - extract the resolution from the Conversion positron dataset
  - extract the resolution from the RMC dataset

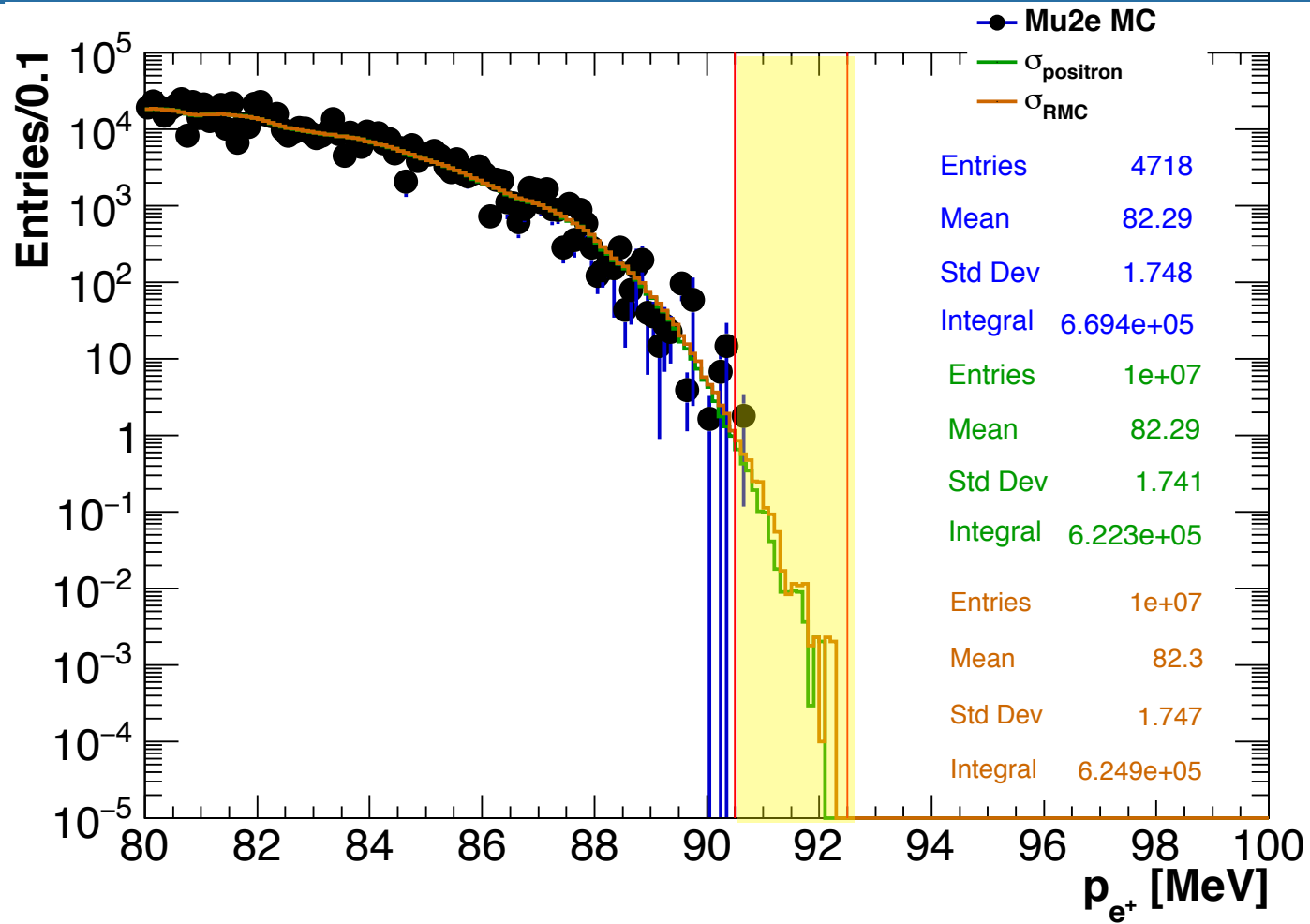


# Momentum distribution ( $k_{\text{max}} = 90.1 \text{ MeV}$ )



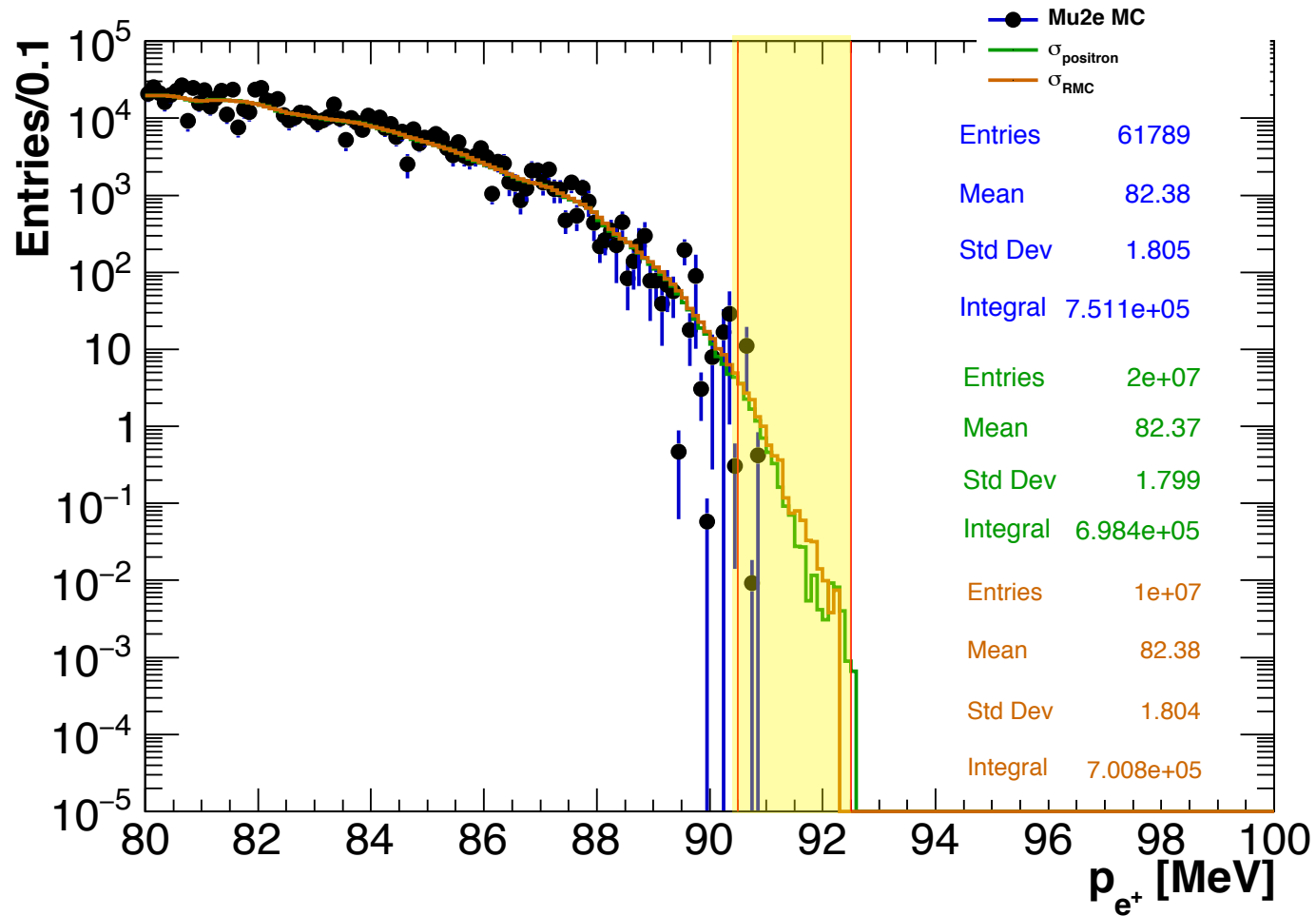
Simulation type	Integral(72,kmax)	Integral (80,88)	Integral
Mu2e MC	$1.281 \times 10^6$	$3.521 \times 10^5$	0
Toy (Cephus reso)	$1.124 \times 10^6$	$3.281 \times 10^5$	0
Toy (RMC reso)	$1.125 \times 10^6$	$3.299 \times 10^5$	0

# Momentum distribution ( $k_{\max} = 91.6 \text{ MeV}$ )



Simulation type	Integral(72,kmax)	Integral (80,88)	Integral
Mu2e MC	$1.963 \times 10^6$	$6.677 \times 10^5$	$1.801 \pm 1.27$
Toy (Cephus reso)	$1.747 \times 10^6$	$6.203 \times 10^5$	1.926
Toy (RMC reso)	$1.747 \times 10^6$	$6.227 \times 10^5$	2.728

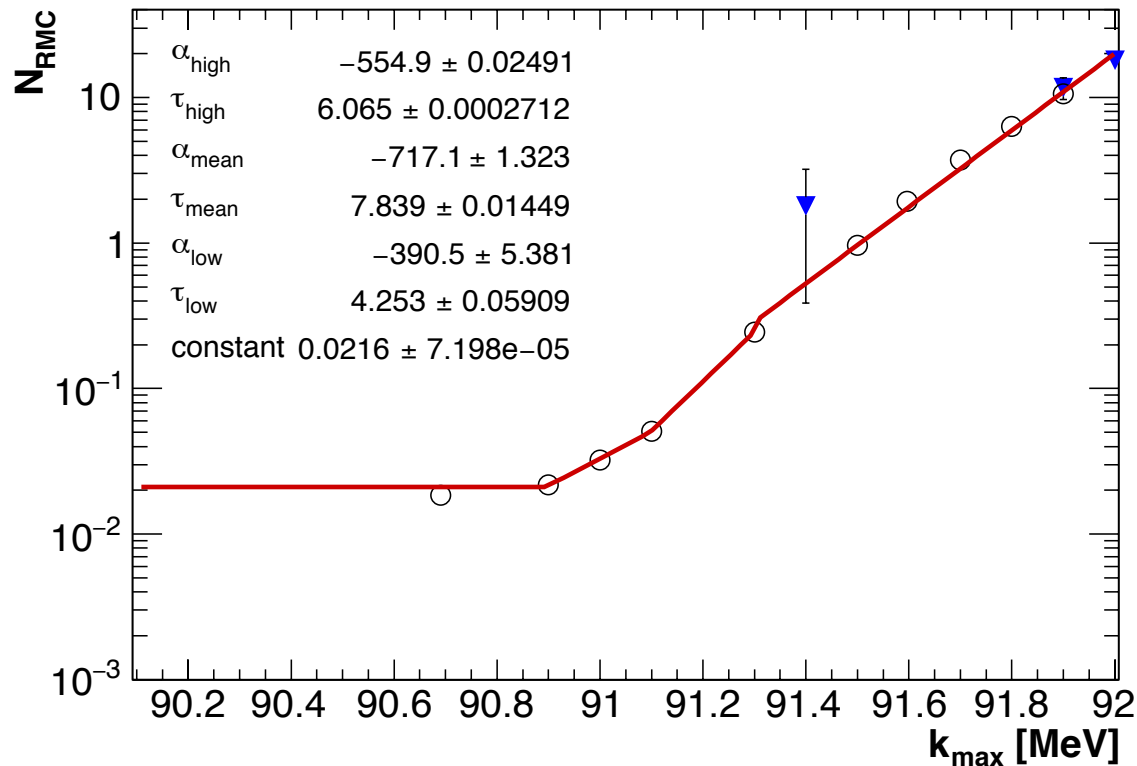
# Momentum distribution ( $k_{\max} = 91.9 \text{ MeV}$ )



Simulation type	Integral(72,kmax)	Integral (80,88)	Integral
Mu2e MC	$2.123 \times 10^6$	$7.481 \times 10^5$	$11.66 \pm 5.83$
Toy (Cephus reso)	$1.895 \times 10^6$	$6.951 \times 10^5$	10.568
Toy (RMC reso)	$1.894 \times 10^6$	$6.973 \times 10^5$	12.608

# Towards the upper limits...

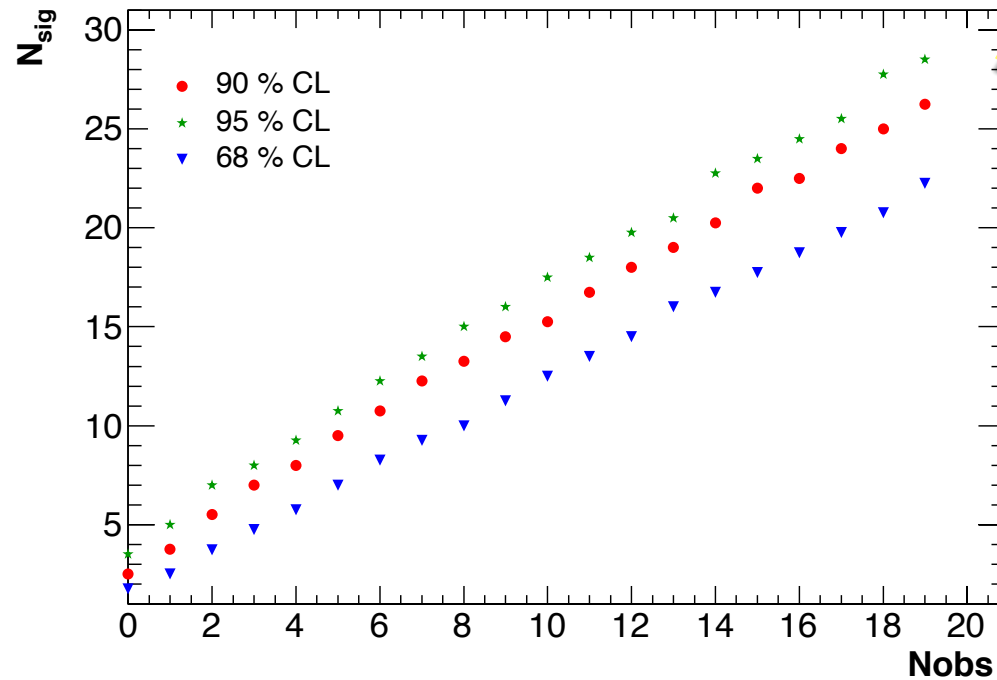
- Varying the  $k_{\max}$  of the RMC spectrum in a 2 MeV range correspond to a variation of  $\sim 10$  backgrounds events



- Uniformly extract the background from the function fitting the data
- Uniformly extract the signal between 0-40



# Upper limit



Results obtained  
using  
the CLs technique

- The sensitivity can be obtained assuming ( $N_{e^+} = 8.26 \times 10^{15}$ )
  - $N_{\text{POT}} = 3.6 \times 10^{20}$ ;
  - Acceptance loss 10%
  - Reconstruction reduction 17%

- $$\mathcal{R}_{\mu e^+} = \frac{N_{sig}}{N_{e^+} \cdot \mathcal{A} \cdot \epsilon}$$

- If No event will be observed:  $\mathcal{R}_{\mu e^+} \leq 3 \times 10^{-16}$  @ 90% CL

# Conclusion

- First attempt to evaluate the Mu2e sensitivity to the  $\mu^- \rightarrow e^+$  conversion almost completed
- $\mathcal{R}_{\mu e^+} \leq 3 \times 10^{-16}$  @ 90% CL obtained
- Repeat the sensitivity evaluation changing the background modelling ( gaussian around 90.1 MeV with  $\sigma=0.5$  MeV and  $\sigma=1.8$  MeV)