

Flavour Physics Effects of a 4th Generation



Stefan Recksiegel

TUM

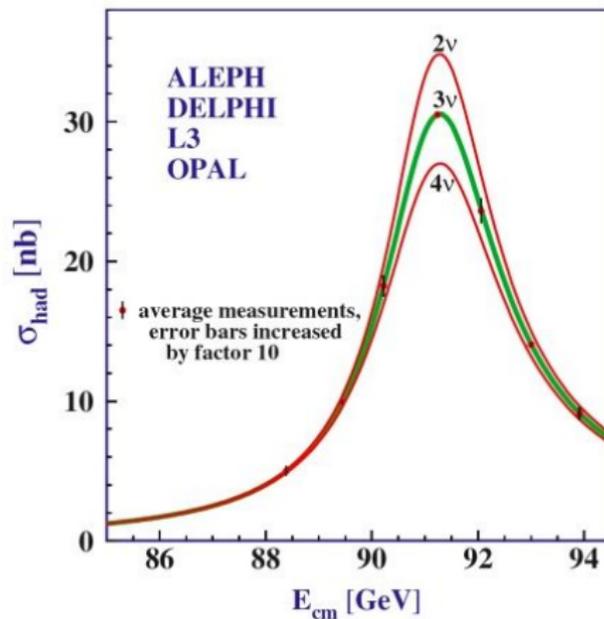
Capri, 7th July 2010

- 1 Introduction
 - Why (not) four generations ?
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 - The effective dimension of the parameter space of SM4
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Why (not) four generations ?

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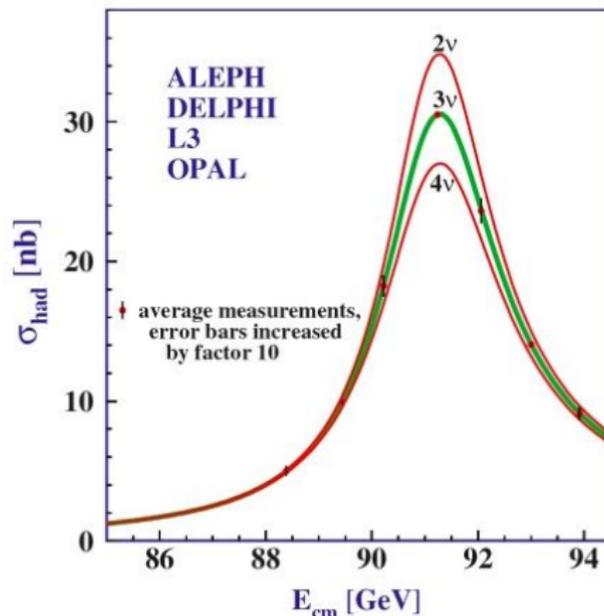
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See-Saw (or whatever) different for 4G, Dirac mass ? Not a problem.

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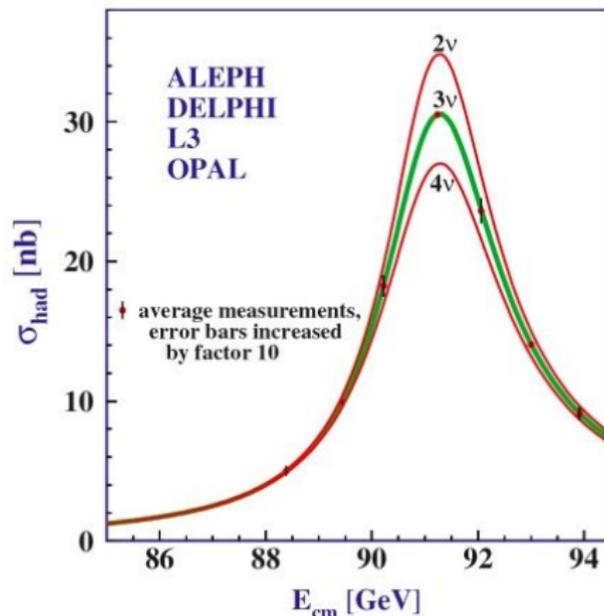
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Non-decoupling radiative corrections to

Electroweak Precision Observables (EWPO)

T parameter and $Zb\bar{b}$ vertex corrections are modified.

Upper bound on s_{34} as a function of $m_{t'}$:

$$|\sin \theta_{34}| \leq \frac{M_W}{m_{t'}}$$

(Chanowitz '09)

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- The most **obvious extension** to the SM
- Avoid necessity for **light Higgs**
See above: Modification of EWPO, “blue band plot” changes
- **SU(5) gauge coupling unification** possible without SUSY
- **Electroweak baryogenesis** might be viable
- Relieve tension in **SM3 fits**
- ...
- **Interesting phenomenology**

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(A. Lenz: “*The most boring extension to the SM*”)
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SM4: The SM with a 4th Generation

The SM with a 4th Generation

The **4th Generation** has been **well studied**, e.g. “find ti fourth”:

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1) Simultaneous Extraction of the Fermi constant and PMNS matrix elements in the presence of a fourth generation.

Heiko Lacker, Andreas Menzel, . HU-EP-10-10, Mar 2010. 16pp. [Temporary entry](#)
 e-Print: [arXiv:1003.4532](#) [hep-ph]

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2) Dynamical symmetry breaking with a fourth generation.

D. Delepine, M. Napsuciale, C.A. Vaquera-Araujo, . Mar 2010. 14pp. [Temporary entry](#)
 e-Print: [arXiv:1003.3267](#) [hep-ph]

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3) Dynamical Electroweak Symmetry Breaking and Fourth Family.

Michio Hashimoto, . KEK-TH-1354, Mar 2010. 8pp. [Temporary entry](#)
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4) Patterns of Flavour Violation in the Presence of a Fourth Generation of Quarks and Leptons.

Andrzej J. Buras, Bjorn Duling, Thorsten Feldmann, Tillmann Heidsieck, Christoph Promberger, Stefan Recksiegel, . TUM-HEP-750-10, Feb 2010. 79pp. [Temporary entry](#)
 e-Print: [arXiv:1002.2126](#) [hep-ph]

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1) **Simultaneous Extraction of the Fermi constant and PMNS matrix elements in the presence of a fourth generation.**
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[Abstract and Comments](#) and [CIT](#) from arXiv.org preprint. [arXiv:1003.0432v1 \[hep-ph\]](#) | [arXiv:1003.0432v2 \[hep-ph\]](#)
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2) **Dynamic symmetry breaking with a fourth generation.**
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Burdman, Chanowitz, Frampton, Holdom, Hou, Hung, King, Soni, ...

A lot more citations (and plots) in

Buras/Duling/Feldmann/Heidsiek/Promberger/SR, arXiv:1002.2126

The CKM Matrix for 4 generations

Five additional parameters: θ_{14} , θ_{24} , θ_{34} , δ_{14} and δ_{24} . (+masses, +leptons)

V_{CKM4} can be written as the product of a **new matrix** and V_{CKM3} :

($c_{14} = \cos \theta_{14}$, ...)

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New mixing, new phases

⇒

SM4 goes **beyond MFV** !

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(Buras et al. 01, D'Ambrosio et al. 02)

Models are **MFV** if there are **no new sources** of Flavour Violation (i.e. only SM-Yukawa).

Examples of **MFV**:

- **Universal extra dimensions** (UED) (Appelquist, Cheng, Dobrescu)
- **SUSY** with universal soft-scalar masses and trilinear soft terms proportional to Yukawa couplings (squark, quark masses aligned)
- **Little Higgs** without T-parity (no *mirror quarks*)

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The theoretical framework

SM4 goes **beyond MFV**, but **operator structure** of the SM3 effective Hamiltonian **remains intact** (c.f. LHT, but unlike SUSY).

⇒ Introduce generalised complex **master functions**

$$S_i, X_i, Y_i, Z_i, D'_i, E'_i, E_i \quad (i = K, d, s)$$

Observables can be written in terms of these functions, e.g. **$B\bar{B}$ mixing**:

$$M_{12}^q = \frac{G_F^2}{12\pi^2} F_{B_q}^2 \hat{B}_{B_q} m_{B_q} M_W^2 \lambda_t^{(q)*2} \eta_B S_q^*$$

Just like **SM3**, but $S_0 \rightarrow S_q$.

Master Functions

The new **master functions** are composed of the old functions, e.g.

$$S_q = S_0(x_t) + \left(\frac{\lambda_{t'}^{(q)}}{\lambda_t^{(q)}} \right)^2 S_0(x_{t'}) + 2 \frac{\lambda_{t'}^{(q)}}{\lambda_t^{(q)}} S_0(x_t, x_{t'}),$$

and **CKM(4)** factors,

$$\lambda_i^{(K)} = V_{is}^* V_{id}, \quad \lambda_i^{(d)} = V_{ib}^* V_{id}, \quad \lambda_i^{(s)} = V_{ib}^* V_{is}.$$

Similar to the SM(3) case, **unitarity**, e.g.:

$$\lambda_u^{(K)} + \lambda_c^{(K)} + \lambda_t^{(K)} + \lambda_{t'}^{(K)} = 0.$$

Flavour Physics Constraints

Flavour Physics Observables

We require the **observables**

$$\varepsilon_K, \quad \Delta M_K, \quad \Delta M_q, \quad \Delta M_d/\Delta M_s, \quad S_{\psi K_S}$$

to lie inside their **experimental 1σ ranges**.

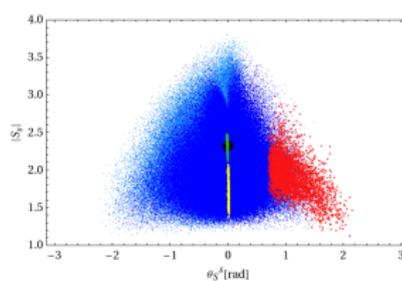
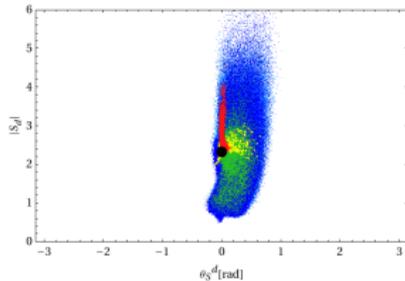
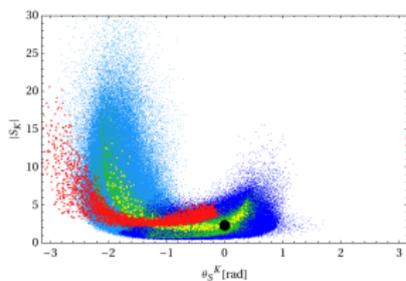
For ΔM_K we employ a larger range due to the large **hadronic uncertainty**, the SM3 **short distance contribution** is only 70% of the measured value.

Also, we impose (looser) **constraints** on $\text{Br}(B \rightarrow X_s \ell^+ \ell^-)$, $\text{Br}(B \rightarrow X_s \gamma)$, $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ and $B_{s,d} \rightarrow \mu^+ \mu^-$.

We generate a **large number of random points** in parameter space and keep only those that satisfy all **tree level CKM constraints** and those listed above.

Numerical results

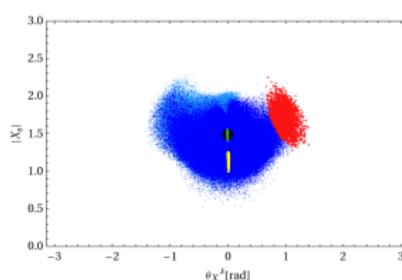
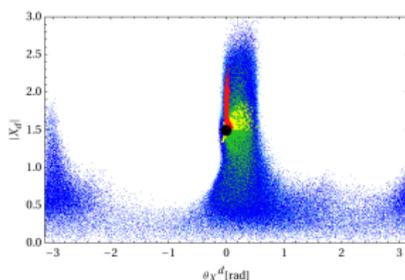
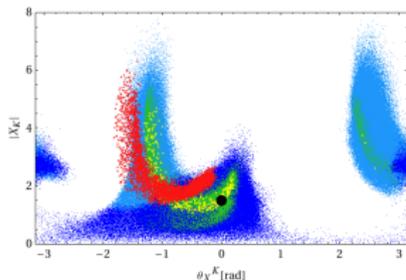
Violation of Universality



$\uparrow \text{Arg} S_i$ against $|S_i|$ \uparrow

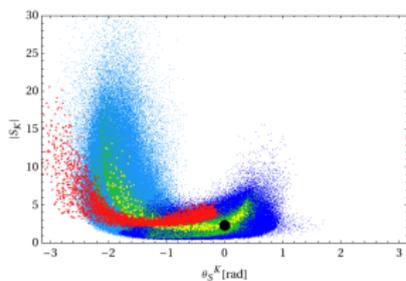
$i = K, d, s$

$\downarrow \text{Arg} X_i$ against $|X_i|$ \downarrow

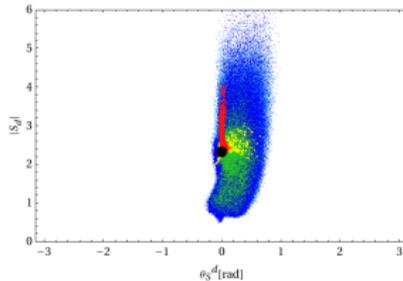


In **SM3** (●), the functions are **real** and **independent** of the meson system !

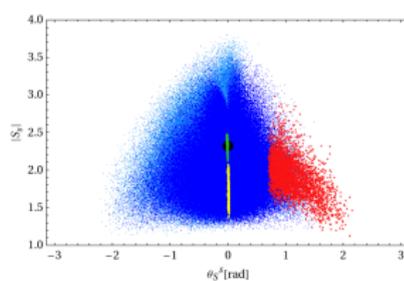
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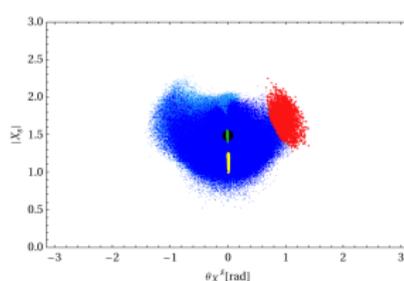
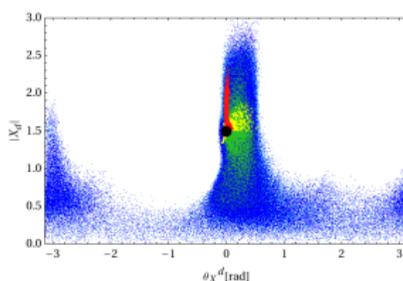
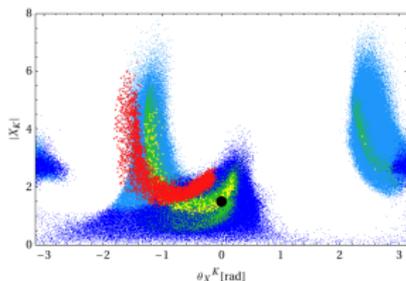
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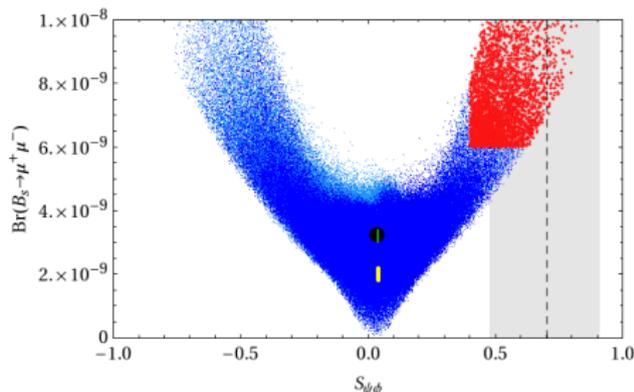
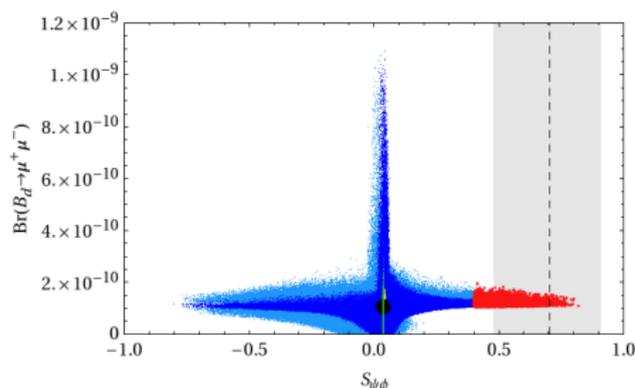
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Effects **largest in K system** because $\lambda_{t'}^{(q)} / \lambda_t^{(q)}$ and $\lambda_t^{(K)} \ll \lambda_t^{(d)} < \lambda_t^{(s)}$

Colour coding

	Scenario1	Scenario2	Scenario3
$S_{\psi\phi}$	0.04 ± 0.01	0.04 ± 0.01	≥ 0.4
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$	$(2 \pm 0.2) \cdot 10^{-9}$	$(3.2 \pm 0.2) \cdot 10^{-9}$	$\geq 6 \cdot 10^{-9}$



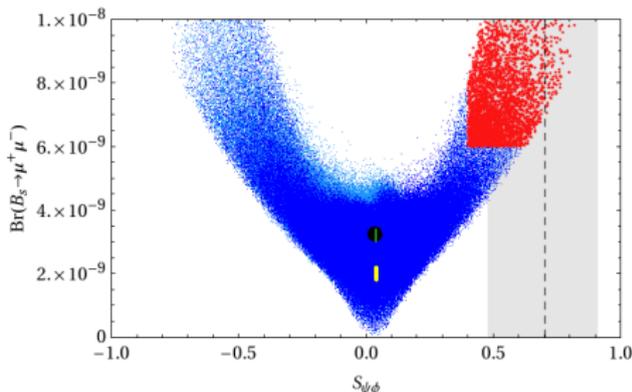
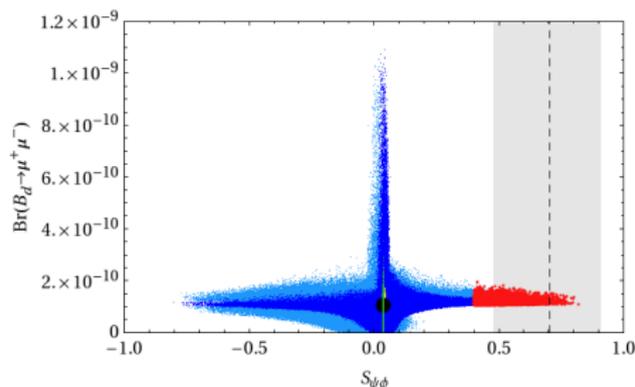
$\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ and $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ as a function of $S_{\psi\phi}$

Exp. bounds: $\text{Br}(B_s \rightarrow \mu^+ \mu^-) \leq 3.3$ (5.3) $\cdot 10^{-8}$, $\text{Br}(B_d \rightarrow \mu^+ \mu^-) \leq 1 \cdot 10^{-8}$.

$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ is **correlated with $S_{\psi\phi}$** , $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ is not !

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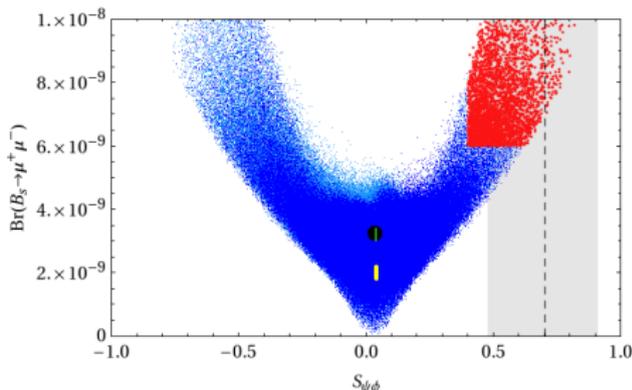
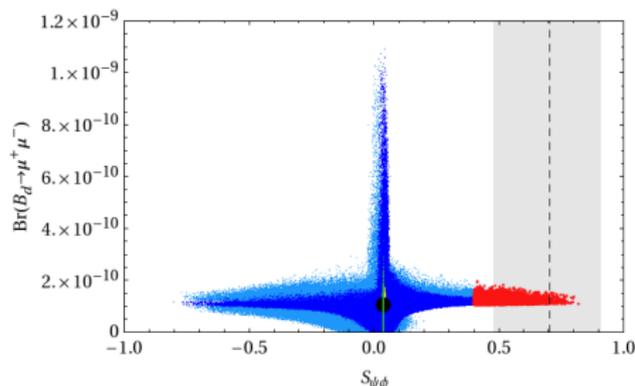
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$S_{\psi\phi}$ can go up to the **current measured value!**

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$S_{\psi\phi}$	0.04 ± 0.01	0.04 ± 0.01	≥ 0.4
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$	$(2 \pm 0.2) \cdot 10^{-9}$	$(3.2 \pm 0.2) \cdot 10^{-9}$	$\geq 6 \cdot 10^{-9}$



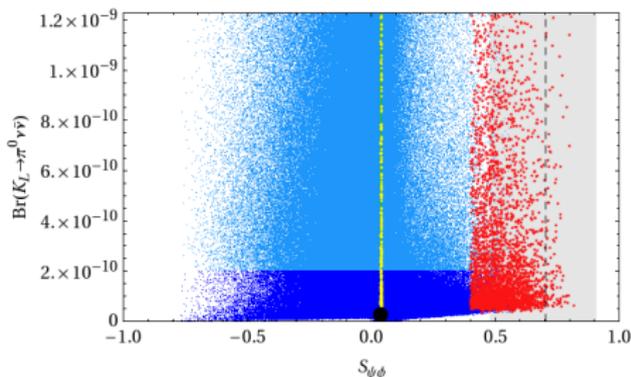
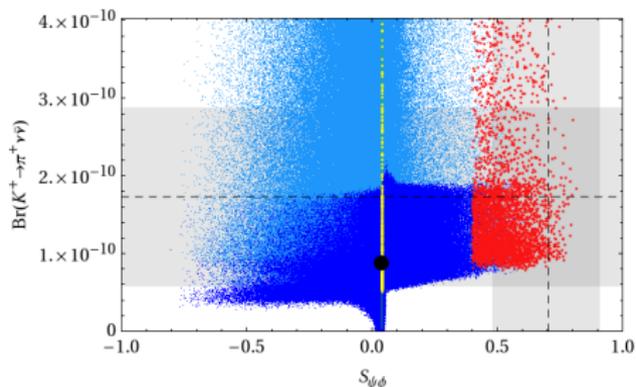
$\text{Br}(B_d \rightarrow \mu^+ \mu^-)$ and $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ as a function of $S_{\psi\phi}$

Exp. bounds: $\text{Br}(B_s \rightarrow \mu^+ \mu^-) \leq 3.3$ (5.3) $\cdot 10^{-8}$, $\text{Br}(B_d \rightarrow \mu^+ \mu^-) \leq 1 \cdot 10^{-8}$.

$\text{Br}(B_{s/d} \rightarrow \mu^+ \mu^-)$ can be **significantly enhanced!** (\rightarrow LHCb)

Colour coding II

Dark blue/light blue indicates size of $\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$.



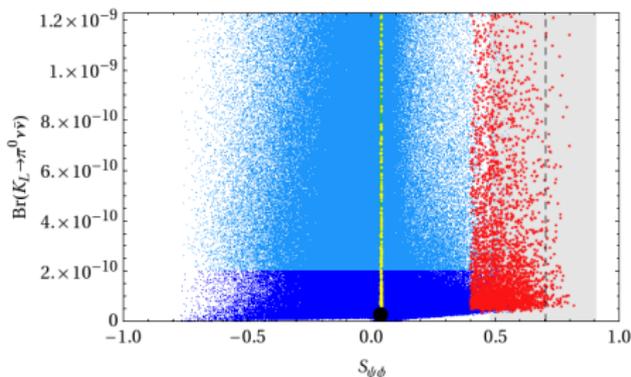
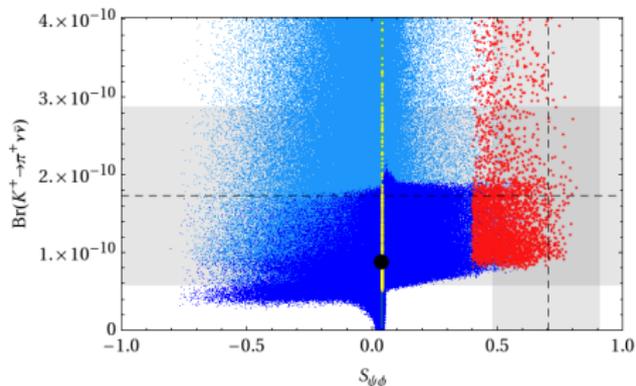
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$ and $\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ as functions of $S_{\psi\phi}$

$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ can be significantly enhanced !

Interesting decay channel because theoretically very clean measure of \mathcal{CP} .

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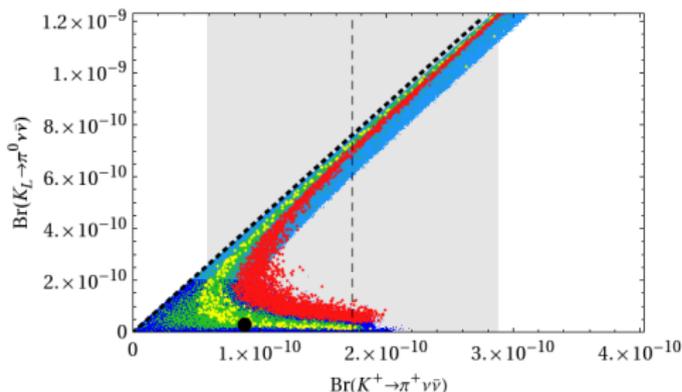
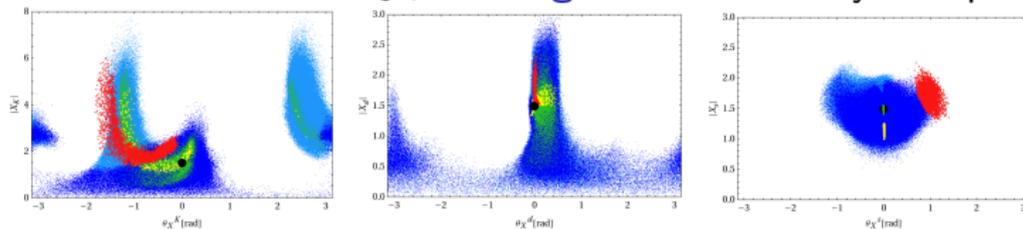
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Interesting decay channel because **theoretically very clean** measure of \mathcal{CP} .

$$K^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ and } K_L \rightarrow \pi^0 \nu \bar{\nu}$$

Reminder: Scenarios restrict B_s , but large effects in K system possible !



$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ against $\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$

$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$ can be **large**, close to the Grossman-Nir-bound !

Interesting: Large $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ only for large $K_L \rightarrow \pi^0 \nu \bar{\nu}$.

\Rightarrow Structure of BRs, **correlation** with $K_L \rightarrow \mu^+ \mu^-$

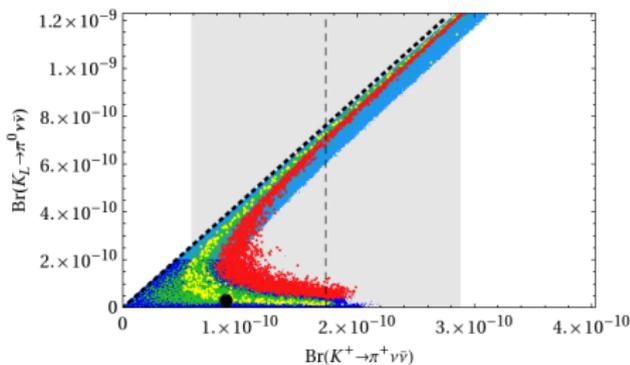
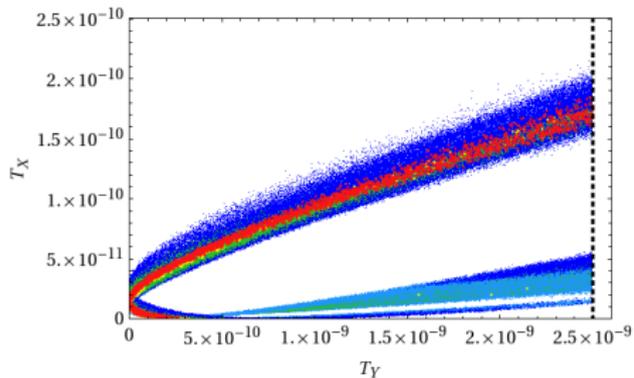
$$K_L \rightarrow \mu^+ \mu^-$$

Limit $\text{Br}(K_L \rightarrow \mu^+ \mu^-)_{\text{SD}} \leq 2.5 \cdot 10^{-9}$ is **saturated** in SM4. (SM3: ~ 0.8)

Define $T_Y \equiv \text{Br}(K_L \rightarrow \mu^+ \mu^-)_{\text{SD}}$, $T_X \equiv \kappa_+ \left(\frac{\text{Re} \lambda_c^{(K)}}{V_{us}} P_c^I(X) + \frac{\text{Re}(\lambda_t^{(K)} X_K^I)}{V_{us}^5} \right)^2$, then

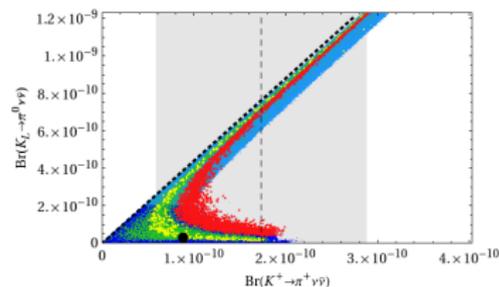
$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \frac{\kappa_+}{\kappa_L} \text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) + T_X$$

Correlation between T_X and $T_Y \Rightarrow$ Observed behaviour for K_L, K^+

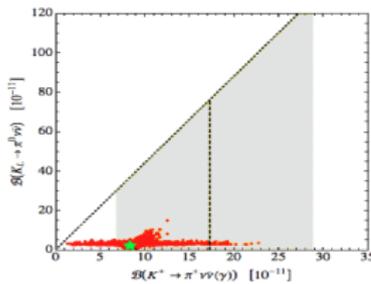


Comparison with other NP models

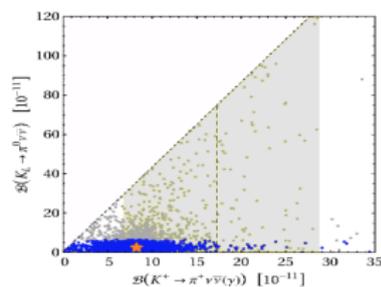
How can we distinguish between **different models of New Physics** ?



4G



LHT



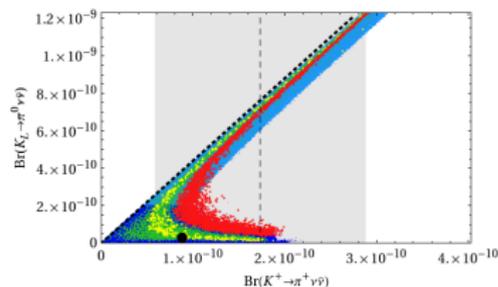
RS

Littlest Higgs with T parity and Randall-Sundrum produce similar signatures for $K_L/K^+ \rightarrow \pi \nu \bar{\nu}$, 4G is different !

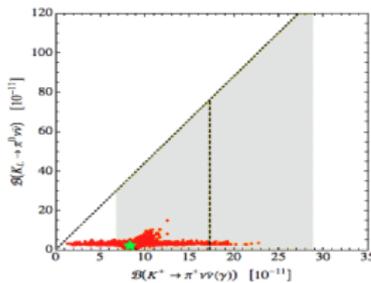
(Thanks to U. Haisch for RS plot)

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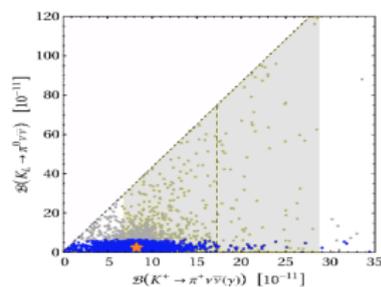
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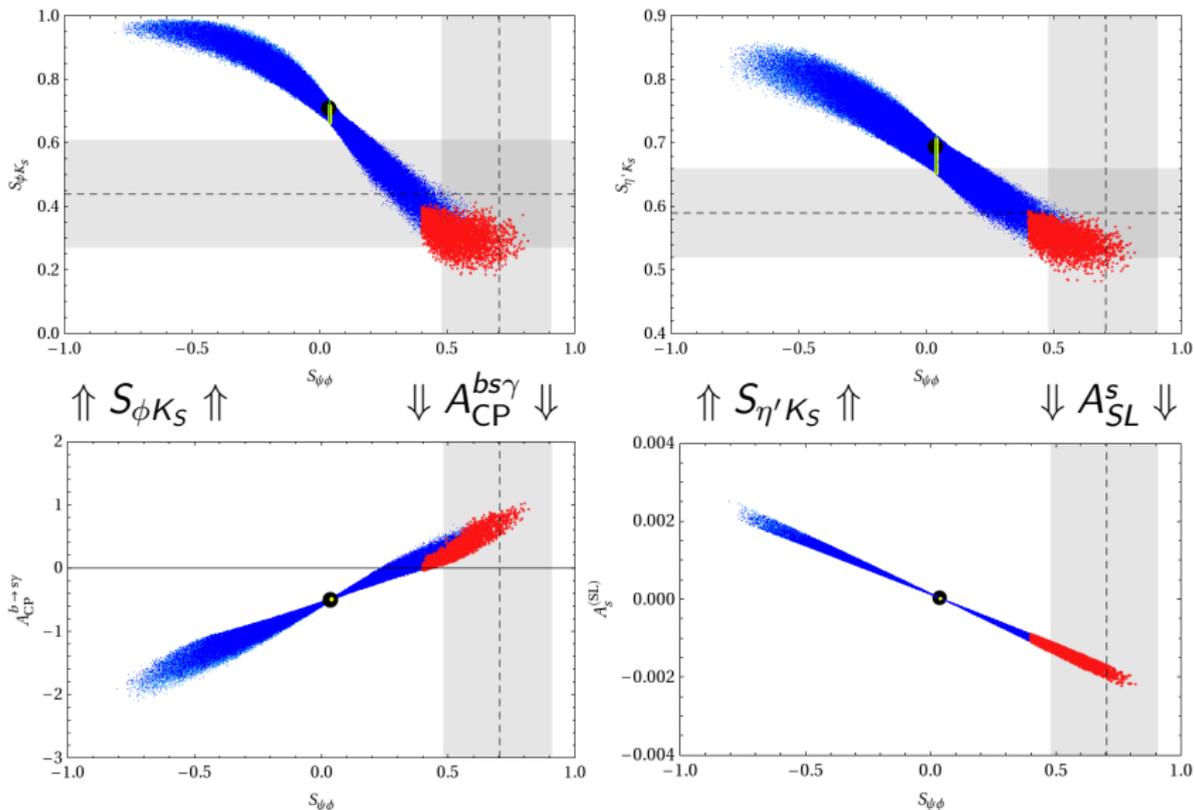


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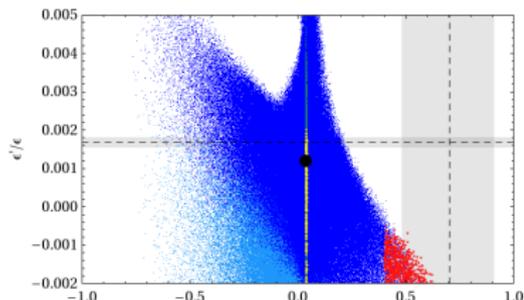
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CP asymmetries as a function of $S_{\psi\phi}$

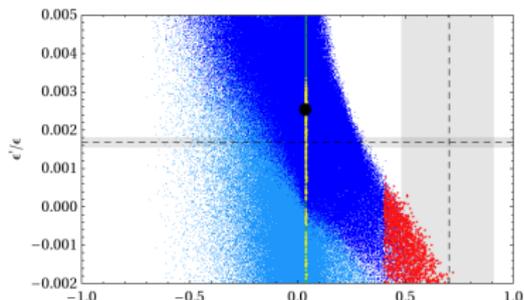


Direct \mathcal{CP} in the Kaon system: ε'/ε

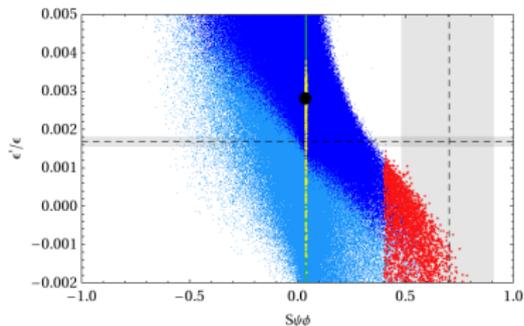
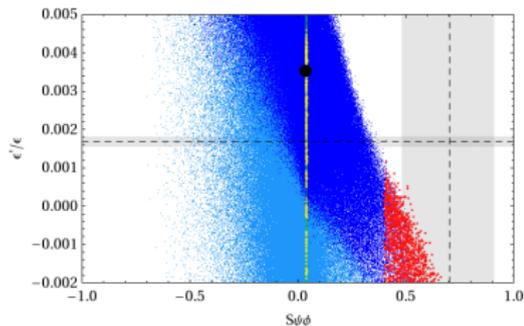
ε'/ε depends strong on two **hadronic parameters**: R_6 and R_8



$\uparrow (1.0, 1.0) \uparrow S_{\phi\phi} \downarrow (2.0, 1.0) \downarrow$



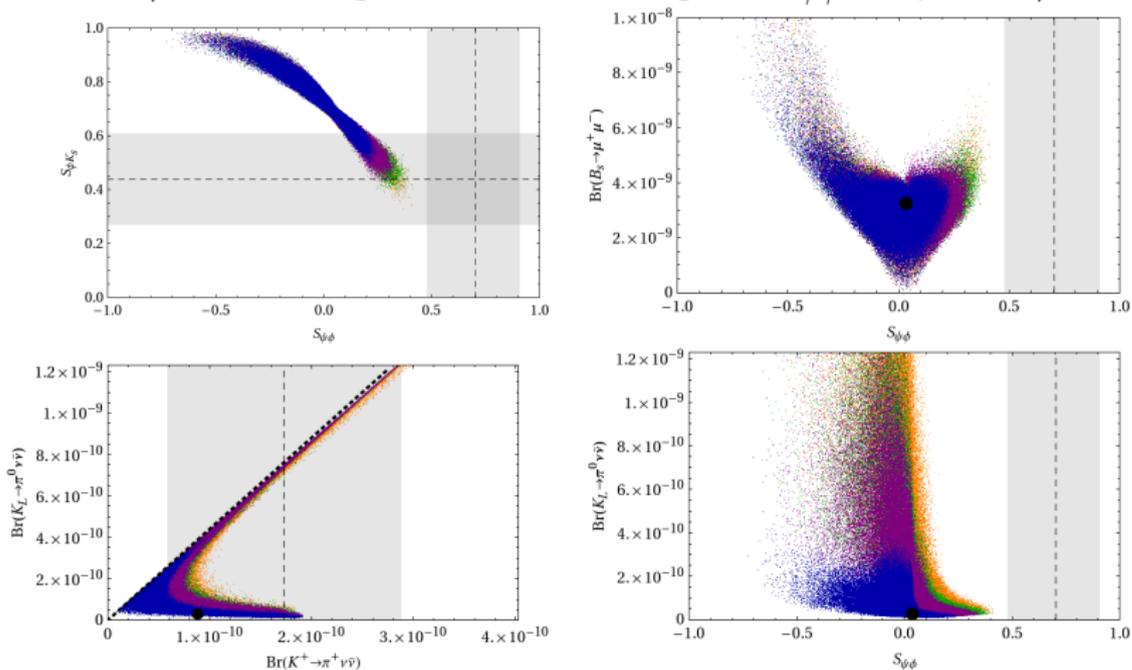
$\uparrow (1.5, 0.8) \uparrow S_{\phi\phi} \downarrow (1.5, 0.5) \downarrow$



All values of the hadr. param. are **consistent** with experiment in SM4...

Direct \mathcal{CP} in the Kaon system: ε'/ε

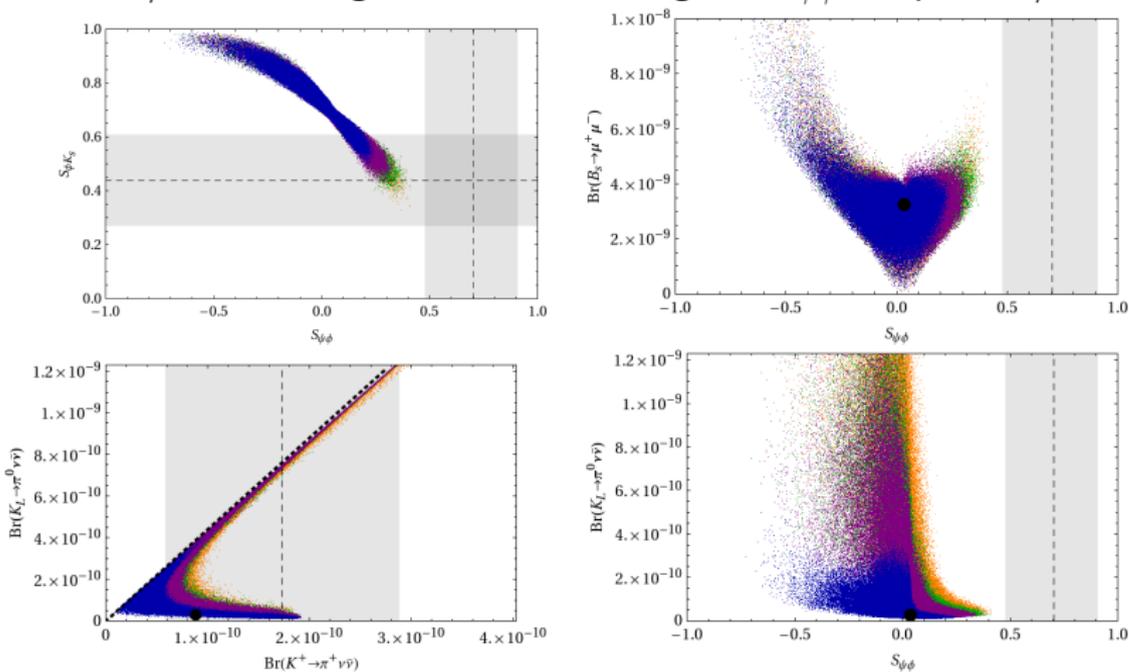
... but ε'/ε can still give constraints, e.g. on $S_{\psi\phi}$: Impose ε'/ε bound!



(The colours correspond to different values for R_6 and R_8 on prev. slide)

Direct \mathcal{CP} in the Kaon system: ε'/ε

... but ε'/ε can still give constraints, e.g. on $S_{\psi\phi}$: Impose ε'/ε bound!



If we take ε'/ε seriously, very large values for $S_{\psi\phi}$ are excluded !

Scaling Scenarios

Scaling Scenarios

The **Wolfenstein expansion**

$$\lambda \equiv s_{12}, \quad s_{23} \equiv A\lambda^2, \quad s_{13}e^{i\delta_{13}} \equiv A\lambda^3(\rho + i\eta) \equiv A\lambda^3 z_\rho$$

can be **generalised to 4G**:

$$s_{14}e^{i\delta_{14}} = \lambda^{n_1} z_\tau, \quad s_{24}e^{i\delta_{24}} = \lambda^{n_2} z_\sigma, \quad s_{34} = \lambda^{n_3} B$$

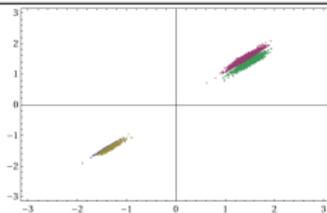
$$A, B, z_i \sim \mathcal{O}(1)$$

Scaling scenarios are defined by (n_1, n_2, n_3) .

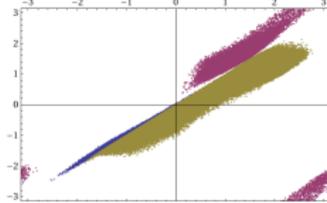
We can **classify the valid parameter points** according to these scenarios.

(n_1, n_2, n_3) Correlation δ_{24} vs. δ_{14}

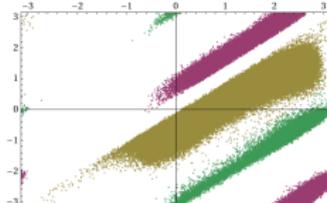
Assignment

 $(2, 1, 1)$
 $(2, 2, 1)$ 

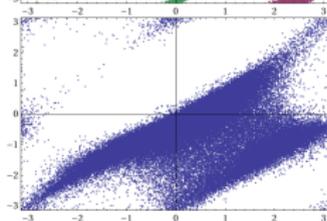
$$\rightarrow \left\{ \begin{array}{l} \text{class 1a: } \delta_{14} < \delta_{24} < \delta_{14} + \frac{\pi}{8}, \quad \delta_{24} < 0. \\ \text{class 1b: } \delta_{14} - \frac{\pi}{8} < \delta_{24} < \delta_{14}, \quad \delta_{24} < 0. \\ \text{class 2a: } \delta_{14} < \delta_{24} < \delta_{14} + \frac{\pi}{8}, \quad \delta_{24} > 0. \\ \text{class 2b: } \delta_{14} - \frac{\pi}{8} < \delta_{24} < \delta_{14}, \quad \delta_{24} > 0. \end{array} \right.$$

 $(3, 2, 1)$ 

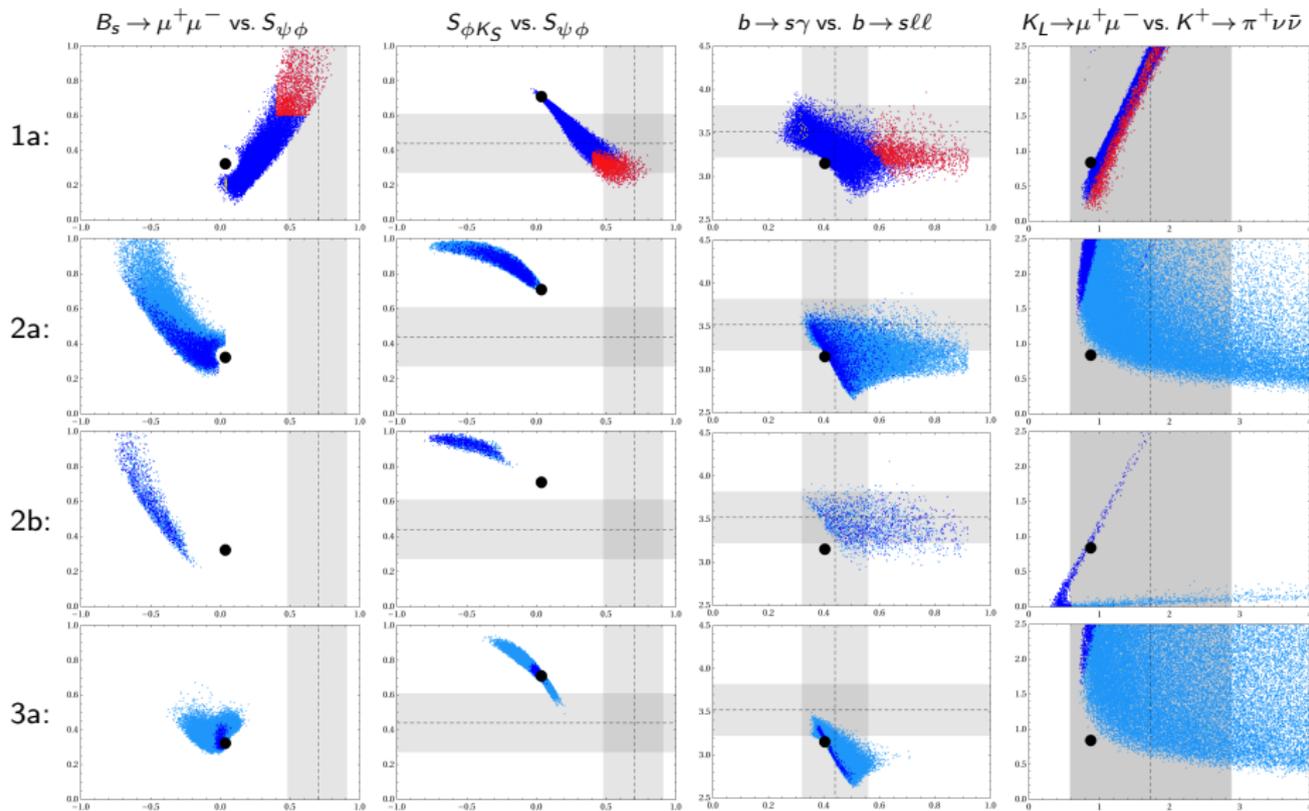
$$\rightarrow \left\{ \begin{array}{l} \text{class 1a: } \delta_{14} < \delta_{24} < \delta_{14} + \frac{\pi}{8}, \quad \delta_{24} < 0. \\ \text{class 2a/3a: } \delta_{14} < \delta_{24} < \delta_{14} + \frac{3\pi}{8}, \quad \delta_{24} > 0. \\ \text{class 3b: } \delta_{14} - \frac{3\pi}{8} < \delta_{24} < \delta_{14}. \end{array} \right.$$

 $(3, 3, 1)$
 $(3, 3, 2)$ 

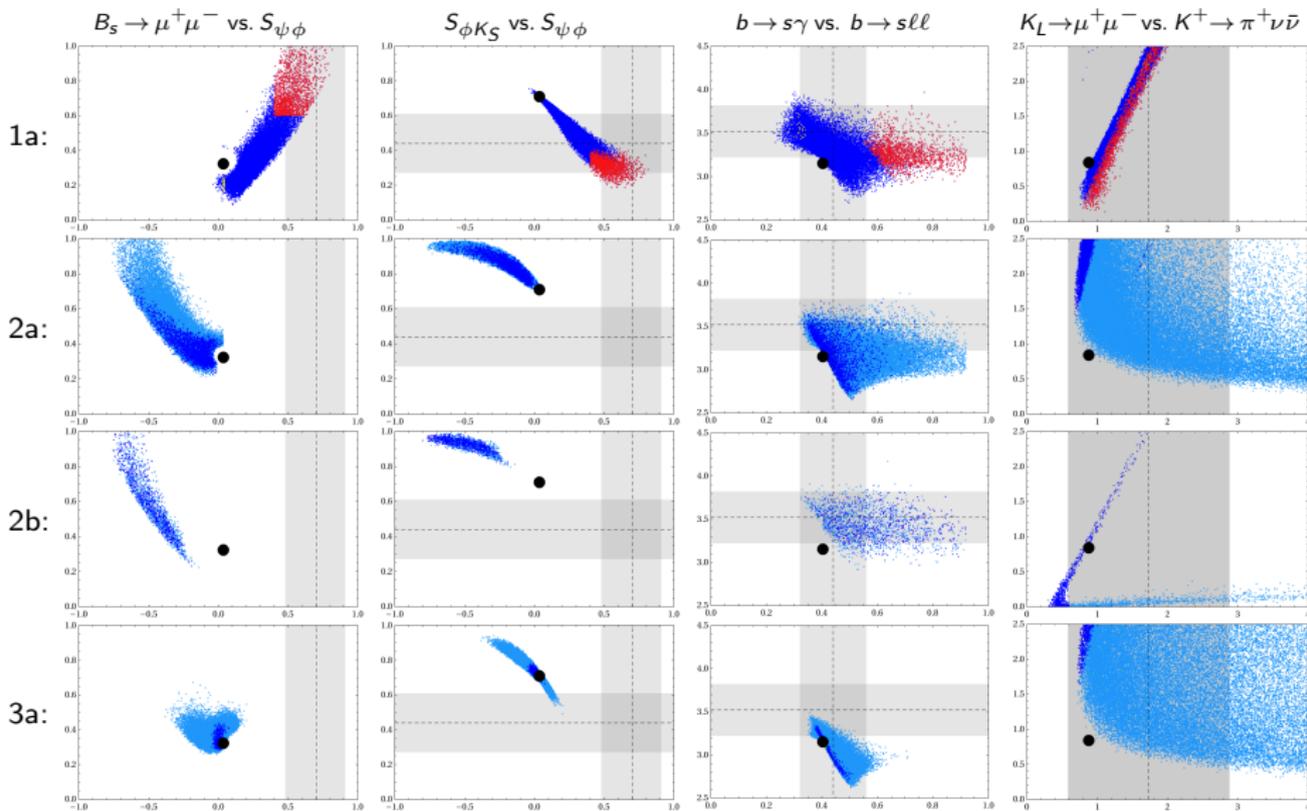
$$\rightarrow \left\{ \begin{array}{l} \text{class 3a: } \delta_{14} + \frac{\pi}{8} < \delta_{24} < \delta_{14} + \frac{\pi}{2}. \\ \text{class 3b: } \delta_{14} - \frac{3\pi}{4} < \delta_{24} < \delta_{14}. \\ \text{class 4: } \delta_{14} - \frac{9\pi}{8} < \delta_{24} < \delta_{14} - \frac{3\pi}{4}. \end{array} \right.$$

 $(4, 3, 1)$
 $(4, 3, 2)$ 

$$\rightarrow \left\{ \begin{array}{l} \text{class 5: } \delta_{14} - \frac{3\pi}{2} < \delta_{24} < \delta_{14} + \frac{\pi}{4} \end{array} \right.$$



→ We can determine the scaling scenario (and thereby the 4G parameters) from correlations.



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Dimensional Analysis

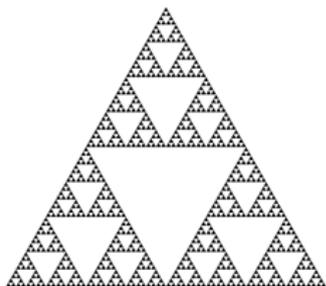
Fractal Dimensions

Hausdorff dimension

A geometric shape has *Hausdorff dimension* d if the relationship between its mass m and length L is

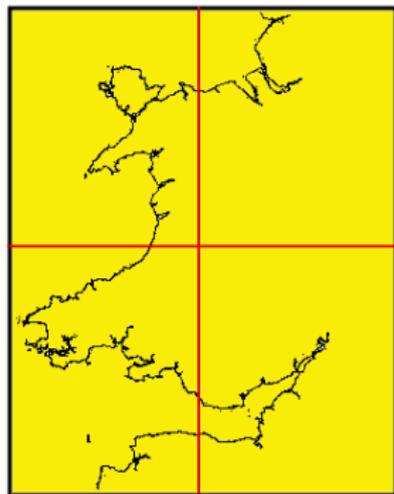
$$m \propto L^d$$

This coincides with the “normal life” understanding of dimensionality for integer d . For Fractals, d is not an integer.



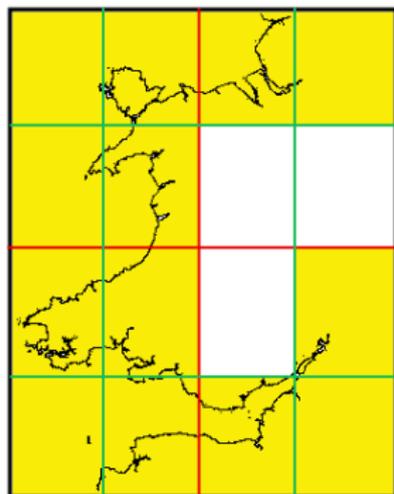
E.g. *Sierpinski triangle*: mass triples when size doubles
 $\rightarrow d = \log(3)/\log(2) \approx 1.585$

The Box Counting algorithm

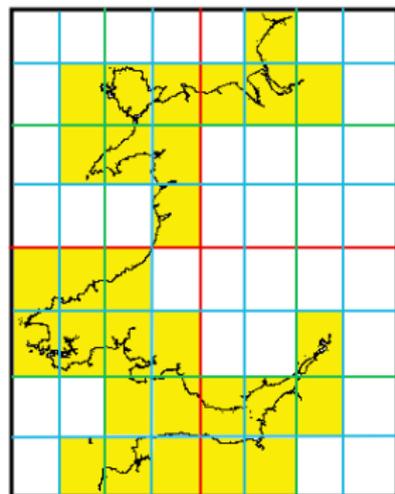


1/1

4/4



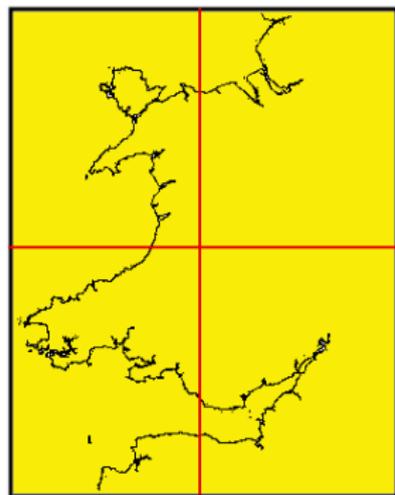
13/16



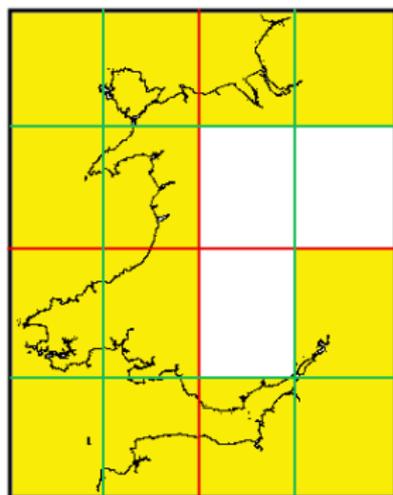
28/64

For **solid** objects, the fill ratio will approach a **constant**,
 for a **line**, it will approach $1/n$ ($n \times n$ boxes). For a fractal, ...

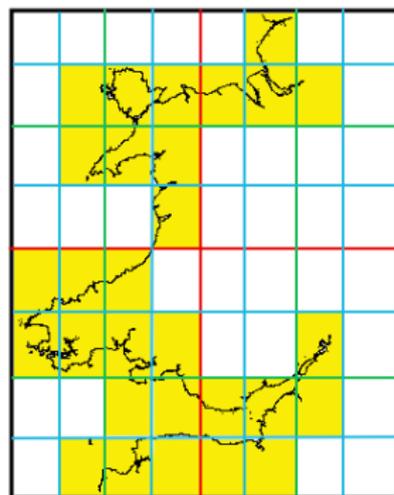
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1/1 4/4



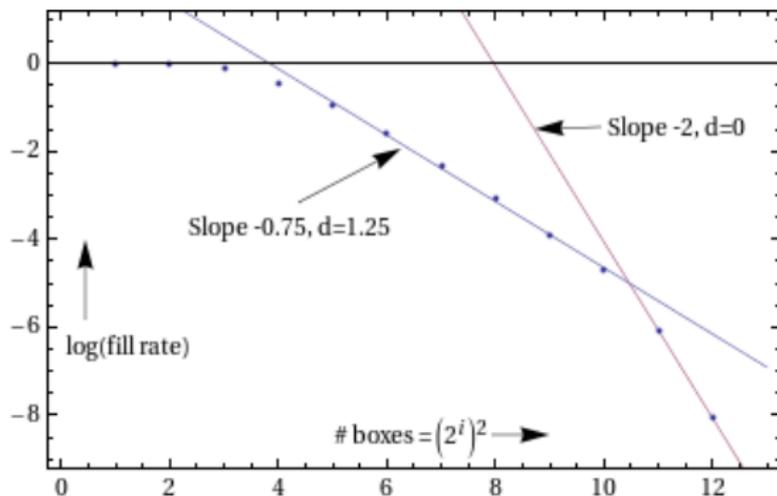
13/16



28/64

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We can make a logarithmic plot of the fill ratio:

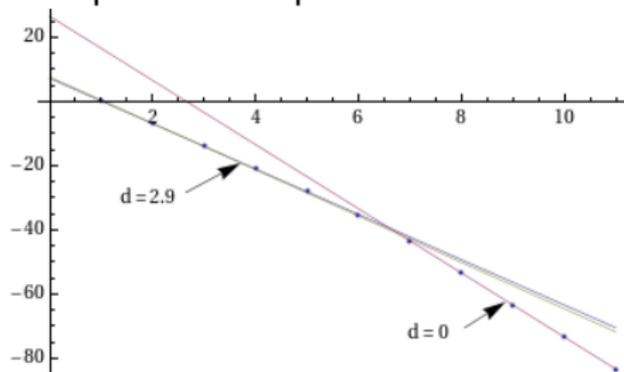


The dimension of the **British coastline** is **1.25**

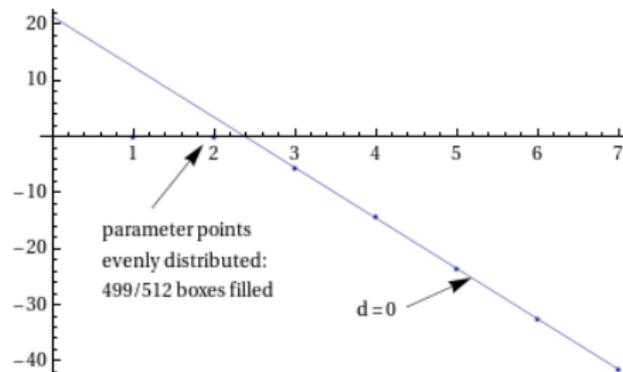
(Benoît Mandelbrot, 1967)

The effective dimension of the parameter space of SM4

The parameter space in **SM4** ...



... and in **LHT**

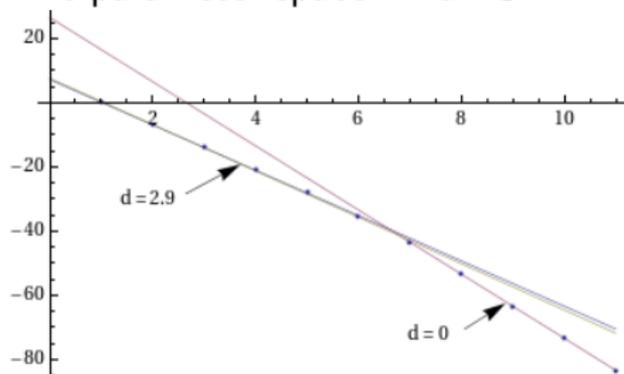


In **SM4**, the valid points in parameter space lie on a complicated structure in 10-dim. space with an **effective dimension** of ~ 3 .

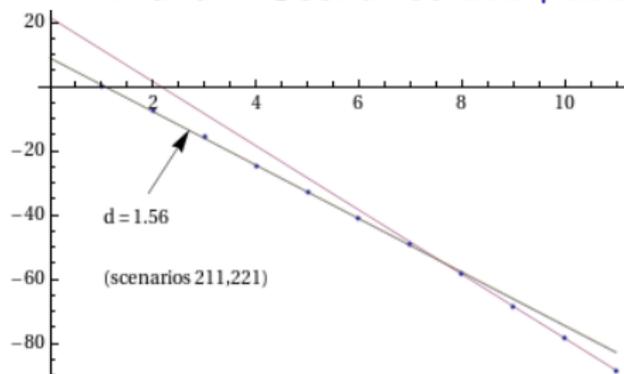
In **LHT**, the valid points are **distributed evenly** over the parameter space, the exp. constraints are fulfilled by **tuning** the mixing parameters and the mirror fermion masses.

Dimension of parameter space of sub-Scenarios

The parameter space in **full SM4** ...



... and in **Scenarios 211+221**

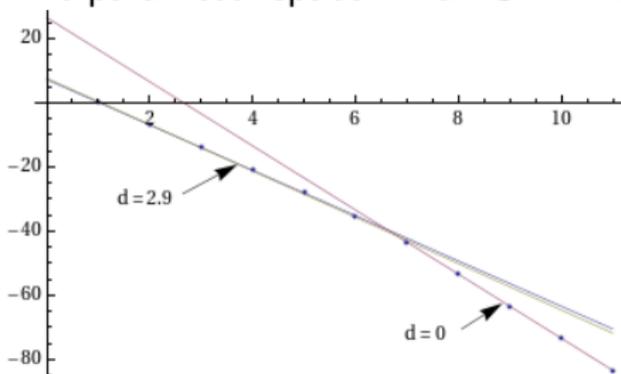


If we restrict ourselves to certain **Scenarios** (i.e. scaling of the mixing parameters), the **effective dimension** of the parameters space **decreases**.

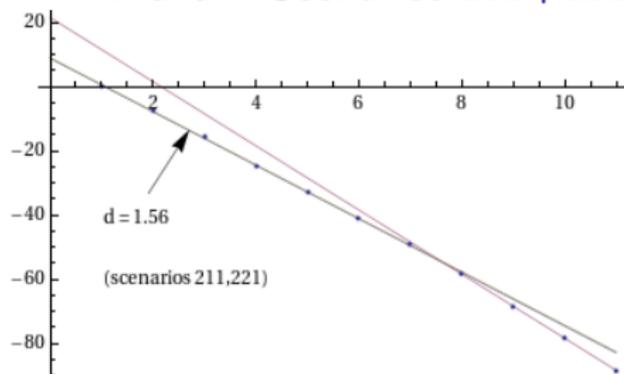
Effective **measure of distribution** of data points, correlations, tuning.

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 Contrary to popular belief, not excluded by LEP, EWPO, ...
- Spectacular effects in **Flavour Physics** observables are possible
LHC(b): $S_{\psi\phi}, B_s \rightarrow \mu^+\mu^-$ (physics started Mar30th)
- Tension between **experimental results** and SM3 can be relieved
 (Explanation of the $S_{\psi\phi}$ **anomaly** involves a significant **enhancement** of $\text{Br}(B_s \rightarrow \mu^+\mu^-)$!)
- ϵ'/ϵ seems to exclude very large values for $S_{\psi\phi}$
- The **signature** of SM4 is different from **other NP models**
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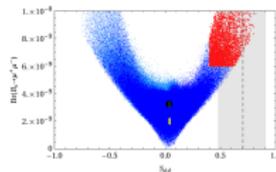
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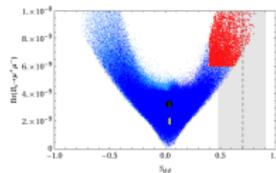


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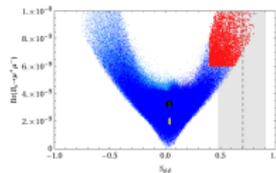


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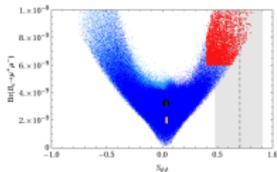


- ϵ'/ϵ seems to exclude very large values for $S_{\psi\phi}$
- The **signature** of SM4 is different from **other NP models**
- Once 4G has been found, study parameters from **correlations** of observables.

Conclusions and Outlook

- The **SM4** is a **viable** and **interesting** extension of the **SM(3)**
Contrary to popular belief, not excluded by LEP, EWPO, ...
- Spectacular effects in **Flavour Physics** observables are possible
LHC(b): $S_{\psi\phi}, B_s \rightarrow \mu^+\mu^-$ (physics started Mar30th)
- Tension between **experimental results** and SM3 can be relieved

(Explanation of the $S_{\psi\phi}$ **anomaly** involves a significant **enhancement** of $\text{Br}(B_s \rightarrow \mu^+\mu^-)$!)



- ϵ'/ϵ seems to exclude very large values for $S_{\psi\phi}$
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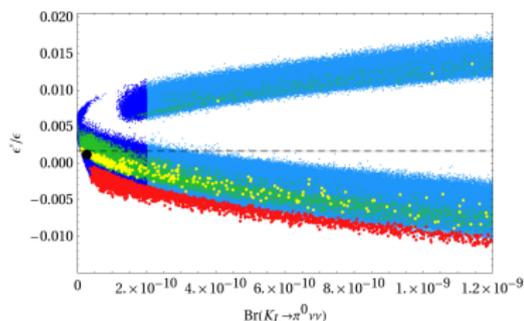


Thank you!

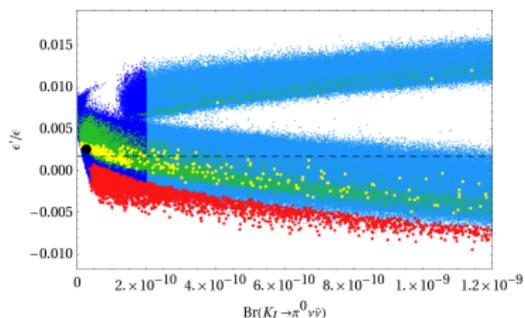
Backup Slides

Correlation between ε'/ε and $K_L \rightarrow \pi^0 \nu \bar{\nu}$

ε'/ε does **not** really restrict $K_L \rightarrow \pi^0 \nu \bar{\nu}$:



↑ (1.0, 1.0) ↑ ↓ (2.0, 1.0) ↓



↑ (1.5, 0.8) ↑ ↓ (1.5, 0.5) ↓

