

MCSTHAR++: statistical hadronization in HERWIG

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In collaboration with

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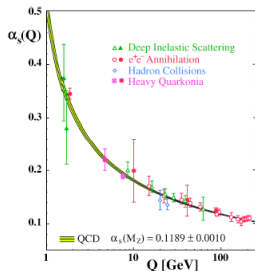
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Hadronization and QCD coupling constant

Why do we need a hadronization model?



- The behaviour of the QCD coupling constant is such that at $E \approx 1 \text{ GeV}$ perturbative calculations are not possible anymore
- A **phenomenological model** is needed to describe the **hadronization** process

S. Bethke, Prog. Part. Nucl. Phys. **58** (2007) 351

Main hadronization models

- Cluster model: **Herwig** G. Corcella et al., JHEP 0101 (2001) 010
- String model: **Pythia** T. Sjöstrand et al., JHEP 05 (2006) 026
- Modified cluster model: **Sherpa** J.C. Winter et al., Eur. Phys. J. C35 (2004) 381
- Statistical model: not yet available in any MC event generator

The statistical hadronization model

Basic ideas

- In a high-energy collision there is the production of pre-hadronic extended object called **clusters** or **fireballs**
- Each of them has well defined physical quantities

$$P, Q, S, B, C, \dots$$

is **colour neutral** and hadronizes according to a **pure statistical law**

Microcanonical description

Every **localized** multi-hadronic state within the cluster compatible with the conservation laws is equally likely

Probability to observe the final state $|f\rangle$

$$p_f \propto \langle f | P_i P_V P_i | f \rangle \quad P_i = P_P P_{Q,S,B} \quad P_V = \sum_{h_V} | h_V \rangle \langle h_V |$$

Model features and free parameters

Main features

- **Bose-Einstein** and **Fermi-Dirac** correlations
- **Interactions** among the hadrons

Free parameters of the model

- 1 γ_s Strangeness suppression parameter
- 2 ρ Energy density of the clusters

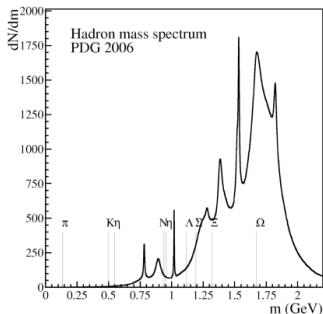
Pythia: 15 parameters

Herwig: 7 parameters

Sherpa: 15 parameters

References:

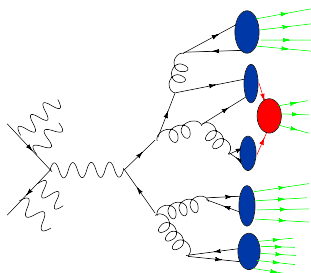
- R. Hagedorn, Nuovo Cim. Suppl. **3** (1965) 147
- F. Becattini, Z. Phys. C **69** (1996) 485
- F. Becattini, U. W. Heinz, Z. Phys. C **76** (1997) 269.
- J. Bernstein, R. Dashen, S. Ma, Phys. Rev. **187** (1969) 1



MCSTHAR++

Monte Carlo Statistical Hadron Reaction

- MCSTHAR++ implements the **statistical model** in the **microcanonical formulation**
- It is a C++ code performing the hadronization step taking as **input** the **clusters of Herwig** and giving in **output** the **primary hadrons**

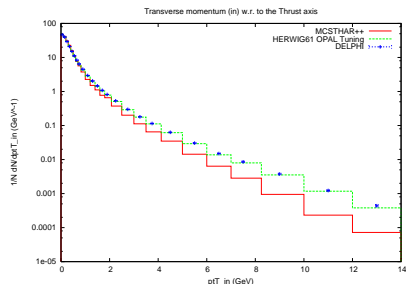
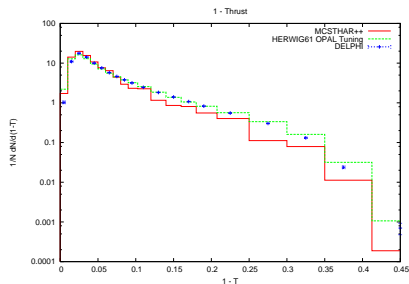


- Herwig's showers and hard scattering
- Herwig's clustering
- MCSTHAR++'s reclustering
- MCSTHAR++'s hadronization

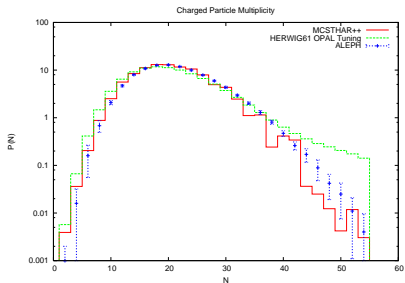
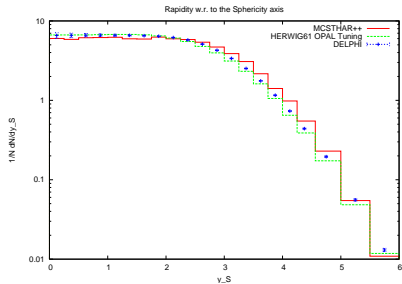
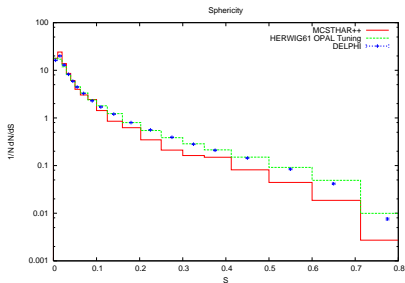
- The final decay of the unstable hadrons is performed by Herwig itself

Preliminary results @LEP (I)

- The following results are obtained with **no tuning at all of Herwig's parameters** and with a "standard" choice of MCSTHAR++'s parameter:
 - $\gamma_S = 0.65$
 - $\rho = 0.35 \text{ GeV}/fm^3$
- Comparison among **HERWIG6.510 + MCSTHAR++**, **HERWIG6.100 (OPAL tuning)** and **LEP data**



Preliminary results @LEP (II)



	MCSTHAR++	Data
All	20.93 ± 0.70	20.76 ± 0.16
γ	22.51 ± 0.68	20.97 ± 1.17
π^{+-}	18.56 ± 0.65	17.03 ± 0.16
π^0	10.71 ± 0.33	9.76 ± 0.26
ρ^{+-}	2.32 ± 0.11	2.40 ± 0.49
ρ^0	1.39 ± 0.06	1.24 ± 0.10
p	0.21 ± 0.03	1.046 ± 0.026
n	0.22 ± 0.04	0.991 ± 0.054

Conclusions

- 1 Phenomenological models are needed to describe the hadronization process
- 2 Different models are implemented in the available MC event generators
- 3 It is worth to have an independent model available for the hadronization:
 - MC generators are tuned on data at energy lower than the one of LHC (LEP and Tevatron)
 - The availability of independent models gives reliability to the theoretical predictions and their uncertainties
- 4 The statistical hadronization models have some interesting properties:
 - Small number of parameters
 - "Advanced" features: quantum statistics and interactions
- 5 The tuning of **MCSTHAR++** with **HERWIG** and **Herwig++** on LEP data is now a work in progress

Thank You!

The X(3872) example (I)

- Hadronization models are needed to study some exclusive quantity
- The X(3872) has an enigmatic nature: is it a **diquark-antidiquark** or a **$D^0\bar{D}^{0*}$ molecular** state (or something else...)?
- Assuming the molecular hypothesis, we try to **simulate prompt X(3872) production at CDF** and **compare the upper theoretical to the lower experimental bound**
- Using CDF data (CDF Coll. PRL **98** 132002 (2007)) we have

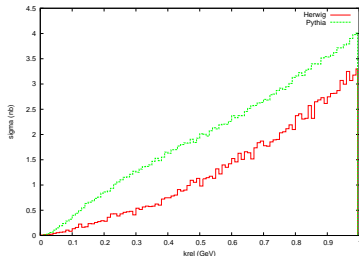
Lower experimental bound

$$\begin{aligned}\sigma(p\bar{p} \rightarrow X(3872) + \text{All})_{\text{prompt}}^{\text{min}} &> \sigma(p\bar{p} \rightarrow X + \text{All}) \times \mathcal{B}(X \rightarrow J/\psi\pi^+\pi^-) \\ &= 3.1 \pm 0.7 \text{ nb}\end{aligned}$$

$$\text{for } p_{\perp}(X) > 5 \text{ GeV}, |y(X)| < 0.6$$

The $X(3872)$ example (II)

- We integrate the $D^0 D_{\bar{0}}^*$ **relative momentum** distribution using Herwig and Pythia in the region $k_{rel} \leq 35$ MeV
- We get a **theoretical upper limit** of 0.071 nb and 0.11 nb respectively, **too low by more than one order of magnitude!**



- This tells us that the $D^0 D_{\bar{0}}^*$ molecular hypothesis is not so good...
C.B., B. Grinstein, F. Piccinini,
A.D. Polosa, C. Sabelli
Phys.Rev.Lett.103

- ...but also that it is useful to use **different hadronization schemes** for the simulations, to have an **estimate of the uncertainty introduced by the hadronization model**

X production experimental limit

- CDF measured (CDF Coll. PRL **98** 132002 (2007)) the fraction of prompt $X(3872) \rightarrow J/\psi\pi^+\pi^-$: $83.9 \pm 5.2\%$
- Using the well measured $\mathcal{B}(\psi(2S) \rightarrow \mu^+\mu^-)$

$$\frac{\sigma(p\bar{p} \rightarrow X(3872) + \text{All})_{\text{prompt}} \times \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-)}{\sigma(p\bar{p} \rightarrow \psi(2S) + \text{All})} = 4.7 \pm 0.8\%$$

Lower experimental bound

$$\begin{aligned} \sigma(p\bar{p} \rightarrow X(3872) + \text{All})_{\text{prompt}}^{\text{min}} &> \sigma(p\bar{p} \rightarrow X + \text{All}) \times \mathcal{B}(X \rightarrow J/\psi\pi^+\pi^-) \\ &= 3.1 \pm 0.7 \text{ nb} \end{aligned}$$

for $p_{\perp}(X) > 5 \text{ GeV}$, $|y(X)| < 0.6$

X production theoretical limit

- Hypothesis: $X(3872)$ is a bound state of two D mesons

E.S. Swanson, E. Braaten et al.

$$\begin{aligned}\sigma(p\bar{p} \rightarrow X(3872)) &\sim \left| \int d^3\mathbf{k} \langle X | D\bar{D}^*(\mathbf{k}) \rangle \langle D\bar{D}^*(\mathbf{k}) | p\bar{p} \rangle \right|^2 \\ &\simeq \left| \int_{\mathcal{R}} d^3\mathbf{k} \langle X | D\bar{D}^*(\mathbf{k}) \rangle \langle D\bar{D}^*(\mathbf{k}) | p\bar{p} \rangle \right|^2 \\ &\leq \int_{\mathcal{R}} d^3\mathbf{k} |\psi(\mathbf{k})|^2 \int_{\mathcal{R}} d^3\mathbf{k} |\langle D\bar{D}^*(\mathbf{k}) | p\bar{p} \rangle|^2 \\ &\leq \int_{\mathcal{R}} d^3\mathbf{k} |\langle D\bar{D}^*(\mathbf{k}) | p\bar{p} \rangle|^2 \sim \sigma(p\bar{p} \rightarrow X(3872))_{\text{prompt}}^{\text{max}}\end{aligned}$$

- \mathbf{k} is the rest-frame relative 3-momentum between the D and D^*
- $|\langle D\bar{D}^*(\mathbf{k}) | p\bar{p} \rangle|^2$ can be computed with MC simulations
- \mathcal{R} has to be given with a reasonable conservative Ansatz for the bound state wave function (we use a simple gaussian form)

Strong coupling constant

- In 1-loop approximation the QCD coupling constant is given by

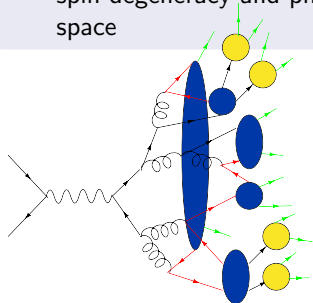
$$\alpha_s(Q^2) = \frac{\alpha_s(\mu^2)}{1 + \alpha_s(\mu^2) \beta_0 \ln \frac{Q^2}{\mu^2}}$$

- Where $\beta_0 = \frac{33 - 2N_f}{12\pi}$

Standard hadronization models (I)

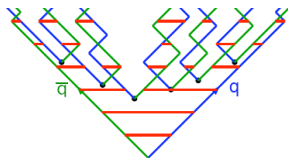
Cluster model

- Implemented in *Herwig*
- Final state quarks and antiquarks are coupled to build colorless "clusters"
- The clusters decay (mostly) into two hadrons according to spin degeneracy and phase space



String model

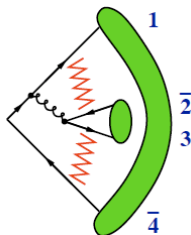
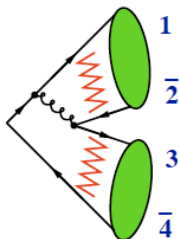
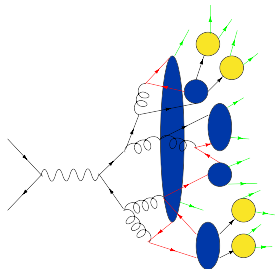
- Implemented in *Pythia*
- A color string is supposed to connect final state quarks, antiquarks and gluons (linear potential)
- Hadrons come from $q\bar{q}$ produced from the vacuum via string fragmentation



Standard hadronization models (II)

Modified cluster hadronization model

- Implemented in [Sherpa](#)
- Similar to the "standard" cluster model of Herwig, with some important extensions:
- **Soft color-reconnection** effect via the inclusion of **non-planar** diagrams, with relative suppression $\propto \frac{1}{N_C^2}$
- The **spin information of the diquarks** is accounted throughout the model
- The number of basic cluster species is enlarged (**four-quark** cluster)



The microcanonical hypothesis

Microcanonical description

Every **localized** multi-hadronic state within the cluster compatible with the conservation laws is equally likely

Probability to observe the final state $|f\rangle$

$$p_f \propto \langle f | P_i P_V P_i | f \rangle \quad P_i = P_P P_{Q,S,B} \quad P_V = \sum_{h_V} |h_V\rangle \langle h_V|$$

Main features

- **Bose-Einstein** and **Fermi-Dirac** correlations $\iff |h_V\rangle, |f\rangle$
- **Interactions** among the hadrons $\iff p'_f \propto \int \prod dm BW(m) p_f$

References:

- R. Hagedorn, Nuovo Cim. Suppl. **3** (1965) 147
- F. Becattini, Z. Phys. C **69** (1996) 485
- F. Becattini, U. W. Heinz, Z. Phys. C **76** (1997) 269.
- J. Bernstein, R. Dashen, S. Ma, Phys. Rev. **187** (1969) 1

$$C(Q) = \frac{\frac{dN(\pi^+\pi^+ + \pi^-\pi^-)}{dQ}}{\frac{dN(\pi^+\pi^-)}{dQ}}$$
$$C'(Q) = \frac{C(Q)}{C(Q)_{NoBEC}}$$

Strangeness suppression and free parameters

- To reproduce the observed **multiplicities of strange particles** a phenomenological parameter γ_s is included in the partition function

Strange particles suppression

$$\langle f | P_i P_V P_i | f \rangle \Rightarrow \gamma_s^{N_s} \langle f | P_i P_V P_i | f \rangle$$

Free parameters of the model

- 1 γ_s Strangeness suppression parameter
- 2 ρ Energy density of the clusters

PYTHIA

About **15** parameters to fit the multiplicities of **25** light quark hadrons @ LEP

HERWIG

About **7** parameters related to the tune of particle multiplicities

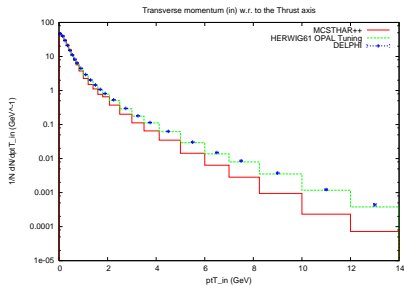
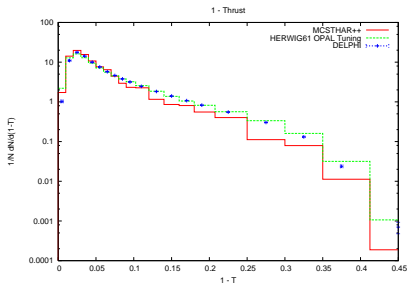
Free parameters and generator tuning

- The statistical model needs only 2 (+1) parameters: γ_s and ρ (and the cluster low mass cut M_{cut})...
- ...but there is a strong interplay with some of Herwig's free parameters, since MCSTHAR++ uses its clusters:
 - quark masses
 - gluon mass
 - quark and gluon virtuality cut
 - Λ_{QCD}
- All these parameters are involved into the QCD shower: they determinate the clusters mass, flavour composition and phase space distribution

For a fine tuning of the generator is necessary to understand the interplay between the two sets of parameters and make a global minimization

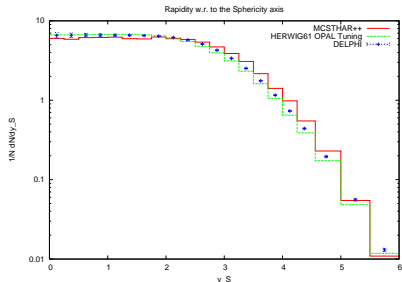
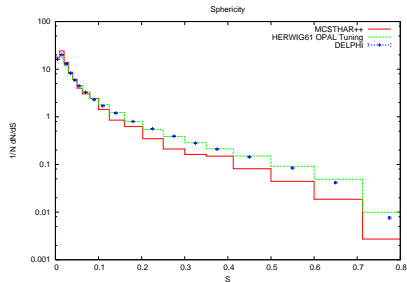
Distributions@LEP: Thrust related observables

- Comparison among **HERWIG6.510 + MCSTHAR++**, **HERWIG6.100** and **LEP data**



- $$T = \max_{\vec{n}} \frac{\sum_{j=1}^{N_P} |\vec{p}_j \cdot \vec{n}|}{\sum_{j=1}^{N_P} |\vec{p}_j|}$$

Distributions@LEP: Sphericity related observables

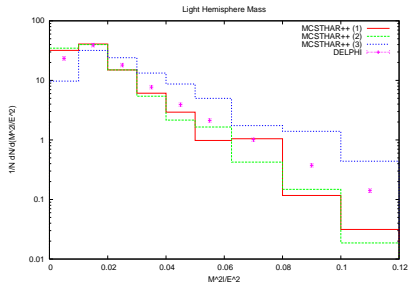
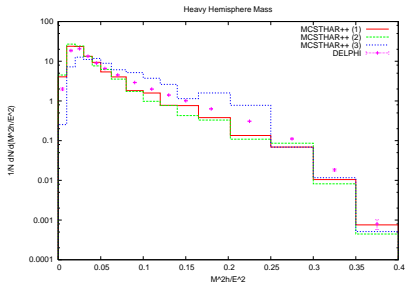


$$\bullet M^{\alpha\beta} = \sum_{j=1}^{N_P} p_j^\alpha p_j^\beta \quad \lambda_1 \geq \lambda_2 \geq \lambda_3 \quad \lambda_1 + \lambda_2 + \lambda_3 = 1$$

$$\bullet S = \frac{3}{2}(\lambda_2 + \lambda_3)$$

$$\bullet y_S = \frac{1}{2} \cdot \log \frac{E + p_S}{E - p_S}$$

Distributions@LEP: free parameters dependence



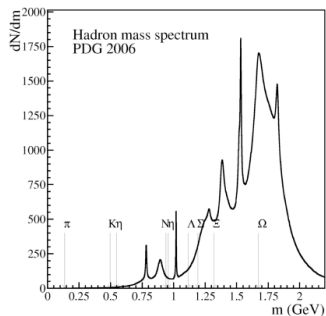
Parameter sets:

- ① $\gamma_s = 0.65$ $\rho = 0.35 \text{ GeV}/fm^3$
- ② $\gamma_s = 0.5$ $\rho = 0.2 \text{ GeV}/fm^3$
- ③ $\gamma_s = 1.0$ $\rho = 0.5 \text{ GeV}/fm^3$

- $\frac{M_h^2}{E^2} = \frac{1}{E^2} \max \left(\left(\sum_{\vec{p}_j \cdot \vec{n}_T > 0} p_j \right)^2, \left(\sum_{\vec{p}_j \cdot \vec{n}_T < 0} p_j \right)^2 \right)$

Hadron mass spectrum and Hagedorn model

- In the **Statistical Bootstrap Model** the clusters are real resonances
- They decay into hadrons in function of the available phase space
- The **mass spectrum** of these objects (clusters/resonances) can be obtained using a **bootstrap equation**



$$\frac{dN}{dm} \propto m^a \exp\left(\frac{m}{T}\right) \quad T \approx 160 \text{ MeV}$$