# Particle acceleration at astrophysical sources



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Multimessanger data analysis in the era of CTA — Sexten center for Astrophysics, 24-28 June 2019



- A quick outlook to Cosmic Ray spectrum
- The SNR paradigm
- Diffusive shock acceleration
- Particle escape from sources
- PWN: Relativistic Shocks & Magnetic Reconnection



G. Morlino — Sexten, June 28<sup>th</sup>, 2019



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# Origin of Galactic CRs



Zwicky & Baade were the first to postulate that SNR could be plausible sources of CRs (1934). But they concluded it was impossible because thought CR were extragalactic.

Vitali Lazarevich Ginzburg made the argument for SNRs as sources of galactic CR in the 60's in a more quantitative form.



$$W_{CR} \sim U_{CR} Vol_{CR} / \tau_{res} \approx 10^{40} erg/s \implies \frac{W_{CR}}{W_{SN}} \approx 0.03 \div 0.3$$
$$W_{SN} \sim R_{SN} E_{SN} \approx 3.10^{41} erg/s \implies \frac{W_{CR}}{W_{SN}} \approx 0.03 \div 0.3$$

In principle ~10% of the SN kinetic energy is enough to explain the CR energy density

What kind of mechanism can transfer energy to non-thermal particle in a power law spectrum?

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### Where does acceleration occur?

#### Diffusive Shock Acceleration (proposed in the '70s)



Repeated multiple scatterings produce small energy gain at each shock crossing Why particles diffuse?

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# Particle motion in presence of magnetic perturbations

#### **Equation of motion**

 $\frac{d \boldsymbol{p}}{dt} = q \frac{\boldsymbol{v}}{c} (\boldsymbol{B}_0 + \delta \boldsymbol{B});$  $\boldsymbol{p}_z = mc \, \boldsymbol{\gamma} \boldsymbol{\mu}; \quad \boldsymbol{\mu} = \cos(\theta)$ 



$$mc\gamma \frac{d\mu}{dt} = q(1-\mu^2)^{1/2} [\cos(\Omega t)\delta B_y - \sin(\Omega t)\delta B_x]$$

Average value of the variance over a time  $\Delta t$ :

$$\left\langle \Delta \mu^{2} \right\rangle = \frac{q^{2}(1-\mu^{2})}{(mc\gamma)^{2}} B_{k}^{2} \int dt \int dt \, \cos\left[\left(\Omega - kv\mu\right)t + \phi\right] \cos\left[\left(\Omega - kv\mu\right)t' + \phi\right];$$

$$\left\langle \frac{\Delta \mu^{2}}{\Delta t} \right\rangle_{\phi} = \frac{q^{2}(1-\mu^{2})\pi B_{k}^{2}}{(mc\gamma)^{2}} \, \frac{1}{v\mu} \delta\left(k - \frac{\Omega}{v\mu}\right) \quad \longleftarrow \text{ Resonant condition}$$

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IN A GENERAL CASE ONE DOES NOT HAVE A SINGLE WAVE BUT RATHER A POWER SPECTRUM:

 $P(k) = \delta B_k^2 / 8 \pi$ 

**THEREFORE INTEGRATING OVER ALL OF THEM:** 

$$D_{\mu\mu} = \left\langle \frac{\Delta \mu^2}{\Delta t} \right\rangle = \frac{q^2 (1 - \mu^2) \pi}{(mc \, \gamma)^2} \frac{8 \pi}{\nu \mu} \int dk \frac{\delta B_k^2}{8 \pi} \,\delta \left( k - \frac{\Omega}{\nu \mu} \right) = \pi (1 - \mu^2) \Omega \, k_{res} \frac{P(k_{res})}{B_0^2 / 8 \pi}$$
OR IN A MORE IMMEDIATE FORMALISM:  $D_{\theta\theta} = \pi \Omega k_{res} F(k_{res})$ 
THE DEFLECTION ANGLE CHANGES BY ORDER UNITY IN A TIME:

 $\tau \approx \frac{1}{\Omega k_{res} F(k_{res})} \qquad D_{zz} = \frac{1}{3} v(v\tau) \approx \frac{v^2}{\Omega k_{res} F(k_{res})} \qquad \text{SPATIAL DIFF}$ 

**IFFUSION** 

### Particle scattering

• Each time that a resonance occurs, the particle changes pitch angle randomly by  $\Delta \theta \sim \delta B/B$ 

• The resonance occurs only for right-hand polarized waves for particles moving to the right (and vice-versa)

• The resonant conditions tell us that:

- If  $k \ll 1/r_{\rm L}$  particles surf adiabatically
- If  $k >> 1/r_{\rm L}$  particles do not feel the waves

### Where do the waves come from?

# From diffusion to energy gain

- All acceleration mechanism are electromagnetic in nature
- Magnetic field do not makes work on charged particles!
- We need electric fields.
- But in the majority of astrophysical sources conductivity ] ∞, hence <*E*> = 0
- The majority of acceleration mechanism are stochastic

$$\langle \vec{E} \rangle = 0 \quad \langle \vec{E}^2 \rangle \neq 0$$

## A quick look to 2<sup>nd</sup> order Fermi acceleration (Fermi, 1949)



**Using Lorents transforations** 

$$E' = \gamma E_i (1 - \beta \mu)$$
  

$$E_f' = E_i' = E'$$
  

$$E_f = \gamma E' (1 + \beta \mu')$$
  

$$\rightarrow E_f = \gamma^2 E_i (1 - \beta \mu) (1 + \beta \mu')$$

$$\left\langle \frac{\Delta E}{E} \right\rangle_{\mu'} = \int \frac{E_f - E_i}{E_i} d\mu' = 2 \left[ \gamma^2 (1 - \beta \mu) - 1 \right]$$

Assuming isotropy in the cloud's reference frame

$$\frac{\Delta E}{E}\Big|_{\mu'\mu} = \int_{-1}^{1} d\mu \frac{1}{2} (1-\beta\mu) 2 \Big[\gamma^{2} (1-\beta\mu) - 1\Big] \propto \beta^{2}$$

Losses and gains are both present but do not compensate exactly

#### The energy gain is too small to explain the CR spectrum

### Shocks in the Universe



### The nature of collisionless shock

A shock is a discontinuity solution of the fluid equations where a supersonic fluid becomes subsonic (i.e. the entropy increases)



1) What produces the transition?

2) Does the fluid equations describe correctly astrophysical plasmas?

### The nature of collisionless shock

#### What produce the shock transition?

 $\lambda_{mfp} \sim \frac{1}{n\sigma} = \begin{cases} \frac{1}{N_A \rho_{air} (2\pi a_0^2)} \sim 10^{-7} cm & \text{Collisions in air} \\ \frac{1}{n_{ISM} \sigma_{Coul}} > 1 pc & \text{Collisions in the ISM} \end{cases}$ 

But observationally (from Balmer emission):

$$\lambda_{sh} \ll 10^{15} cm = 3 \times 10^{-4} pc$$

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#### Length-scale for EM processes:

Electron skin depth 
$$\sigma_{pe} = \left(\frac{4\pi n_e e^2}{m_e}\right)^{1/2} = 5.3 \times 10^5 n_e^{-1/2} cm$$
  
Ion skin depth  $\sigma_{pi} = \left(\frac{4\pi n_i e^2}{m_i}\right)^{1/2} = 2.3 \times 10^7 n_i^{-1/2} cm$   
*p*'s Larmor radius  $r_L(v_{sh}) = \frac{m_p v_{sh} c}{eB} = 10^{10} \left(\frac{v_{sh}}{3000 \, km/s}\right) \left(\frac{B}{3\mu G}\right)^{-1} cm$   
Shock thickness  
between these  
two lengthscale

### Electro-magnetic instabilities in a shock

The shock transition is mediated by electromagnetic interactions. Collisions have no role  $\rightarrow$  the Mach number does not properly describe the shock properties

Alvénic Mach number is more appropriate:

$$M_{A} = \frac{v_{sh}}{v_{A}}; \quad v_{A} = \frac{B}{\sqrt{4\pi\rho}} \approx 2 B_{\mu G} \left(\frac{n}{cm^{-3}}\right)^{-1/2} km/s$$

Alfvén waves are a combination of electromagnetic-hydromagnetic waves

Analogy with waves on a string:  $v = \sqrt{T/\mu}$ ;  $T \rightarrow B^2/4\pi$ ,  $\mu \rightarrow \rho$ 

Collisionless shocks require  $M_{_{A}} > 1$ 

#### Which instability is responsible for the shock transition?

- Two stream instability
- Weibel instability
- Oblique instability
- Filamentation

The relative importance depends on the initial conditions of the plasma

\* ...

# Fermi mechanism applied to shocks: test particle approach



MICROSCOPIC APPROACH

Assuming isotropic distribution in all reference frames:

$$\left| \left( \frac{\Delta E}{E} \right) = \frac{4}{3} \frac{u_1 - u_2}{c}; \quad P_{esc} = 4 \frac{u_1}{c}; \right|$$
  
Stochastic acceleration:  
$$n(E) = \frac{dN}{dE} \propto E^{-\alpha};$$
$$\alpha = 1 - \frac{\ln P_{ret}}{\ln \Delta E/E} \approx 1 + \frac{P_{esc}}{\Delta E/E} = \frac{r+1}{r-1}$$
For strong shocks and mono-atomic gas:  
$$r = \frac{u_1}{u_2} \rightarrow 4$$
$$n(E) = E^{-2} \sim n(p) = p^{-4}$$

# Maximum energy

The maximum energy is obtained comparing the acceleration time with the age of the accelerator and the energy losses

$$t_{\rm acc} = \frac{t_{\rm cycle}}{\Delta E/E}$$

Time for one cycle upstream  $\rightarrow$  downstream  $\rightarrow$  upstream

Equating the particle injected from downstream with the particles upstream:

Energy losses are usually negligible for protons but are important for electrons

$$t_{cycle} = \tau_{diff,1} + \tau_{diff,2}$$

$$\frac{nc}{4}\Sigma\tau_{diff,1} = n\Sigma\frac{D_1}{u_1} \longrightarrow \tau_{diff,1} = \frac{4D_1}{c\,u_1} \wedge \tau_{diff,2} = \frac{4D_2}{c\,u_2}$$

$$t_{\rm acc} = \frac{t_{\rm cycle}}{\Delta E/E} = \frac{3}{u_1 - u_2} \left( \frac{D_1}{u_1} + \frac{D_2}{u_2} \right) \approx 8 \frac{D_1}{u_{\rm sh}^2}$$

# Maximum energy

Maximum energy can increase only during the ejecta dominated phase of the SNRs because  $u_{sh} \sim const$ 

$$\begin{cases} t_{ST} = R_{ST} / u_{sh} \\ \frac{1}{2} M_{ej} u_{sh}^{2} = E_{SN} \\ \frac{4\pi}{3} \rho_{ISM} R_{ST}^{3} = M_{ej} \end{cases} \qquad t_{ST} \approx 50 \left(\frac{M_{ej}}{M_{\odot}}\right)^{\frac{5}{6}} \left(\frac{E_{SN}}{10^{51} \text{erg}}\right)^{-\frac{1}{2}} \left(\frac{n_{ISM}}{\text{cm}^{-3}}\right)^{-\frac{1}{3}} \text{yr},$$

Using the diffusion coefficient from quasi-linear theory:

$$D = \frac{1}{3} \frac{r_L v}{F(k_{res})}; \quad F(k) = \frac{\delta B^2}{B_0^2}$$

$$t_{acc} = t_{ST} \implies E_{max} = 5 \times 10^{13} Z \mathscr{F}(k_{min}) \left(\frac{B_0}{\mu G}\right) \left(\frac{M_{ej}}{M_{\odot}}\right)^{-\frac{1}{6}} \left(\frac{E_{SN}}{10^{51} \text{erg}}\right)^{\frac{1}{2}} \left(\frac{n_{ISM}}{\text{cm}^{-3}}\right)^{-\frac{1}{3}} \text{eV}$$

High energies, up to PeV, can be achieved only if F(k) >> 1. This condition requires amplification of the Magnetic field

### Predictions of diffusive shock acceleration

(1) Spectrum: 
$$f_{CR}(p) \propto p^{-4} \rightarrow f_{CR}(E) \propto E^{-2}$$
  
(2) Acceleration efficiency: ~10%  
(3) Maximum energy:  $E_{max} \simeq 50 \left(\frac{\delta B}{B_0}\right) \left(\frac{B_0}{\mu G}\right) TeV$   
Strong dependence on magnetic field

High energies, up to PeV, can be achieved only if  $(\delta B/B_0)^2 >> 1$ 

This condition requires amplification of the magnetic field

### Fermi acceleration at work

#### [From Gargaté & Spitkovsky (2013)]



### PIC simulation of particle acceleration



### Particle injection and shock reformation



### Non-thermal spectrum from SNRs



# Gamma-rays from SNRs: what's wrong with DSA?



Middle-aged SNRs (~20.000 yrs) hadronic emission • steep spectra  $\sim E^{-3}$  $\blacktriangleright E_{\rm max} < 1 {
m TeV}$ Young SNRs (~2000 yr) ► Hadronic/leptonic? Hard spectra  $\blacktriangleright E_{max} \sim 10\text{-}100 \text{ TeV}$ Very young SNRs (~300 yr) ▶ hadronic • steep spectra  $\sim E^{-2.3}$ ▶  $E_{\text{max}} \sim 10\text{-}100 \text{ TeV}$ Not enough to explain the Knee at ~ PeV

### Magnetic field amplification: observations

Chandra X-ray map. Data for the green sector are from Cassam-Chenaï et al (2007)



Thin non-thermal X-ray filaments provide evidence for magnetic field amplification

[Hwang el al(2002); Bamba et al (2005)]

\_212



#### X-ray thickness = Synchrotron losslength

$$\begin{cases} D = r_L c/3 \propto E B^{-1} \\ \tau_{syn} = \frac{3 m_e c^2}{4 \sigma_T c \gamma \beta^2 U_B} \propto E B^{-2} \end{cases}$$

$$\Delta \simeq \sqrt{D \tau_{syn}} \propto B^{-3/2}$$

$$B \sim 200-300 \ \mu G >> B$$

ISM

### Where is the magnetic field amplified?

**DOWNSTREAM:** MHD instabilities (shear-like)

**UPSTREAM:** only through instabilities driven by CRs (Streaming, Bell)

BUT we need amplification upstream of the shock to reach high energies

Low magnetic field upstream produces a more extended emission NOT OBSERVED!



# Magnetic field amplification: Theory

How is the magnetic field amplified?

#### **Resonant Straming instability**

[e.g. Skilling (1975), Bell & Lucek (2001), Amato & Blasi (2006), Blasi (2014)] Particles amplify Alfvèn waves with wave-number  $k=1/r_{I}(p)$  Fast growth rate but

$$\left(\frac{\delta B}{B_0}\right)^2 \simeq 1$$

$$E_{max} \approx 100 \, TeV$$

A factor 10 below the knee

# Magnetic field amplification: Theory

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# Magnetic field amplification: Theory

How is the magnetic field amplified?



### The non-linear fashion of DSA

Magnetic turbulence produce diffusion of particles → isotropization

Particles amplify the magnetic turbulence Shock transfers momentum to particles through waves locked to the plasma

### Particle escape from SNRs

If particles are not released all at the same time, in general:

Spectrum injected into the Galaxy  $f_{esc}(p) \neq f_{SNR}(p)$ 

Spectrum inside SNRs

### Particle escape from SNRs

If particles are not released all at the same time, in general:

Assume that at time t only particles at maximum momentum  $p_{max}(t)$  can escape

$$4\pi f_{esc}(p) c p p^{2} dp = \left[\xi_{esc}(t)\right] \frac{1}{2} \rho V_{sh}^{3} 4\pi R_{sh}^{2} dt$$
  
Released energy Converted Incoming  
fraction Energy flux

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### Pulsar Wind Nebulae



### The Crab nebula (where we have learnt most of what we know)



Source of B field and particles: NS suggested before pulsar discovery (Pacini '67) Primary emission mechanism: synchrotron radiation by relativistic particles in a intense (>few × 100 B<sub>ISM</sub>) ordered (high degree of polarization, in radio, optical and even γ-rays, Dean et al. 08) magnetic field



### **THE BASIC PICTURE**



### **THE TERMINATION SHOCK**

THE RADIUS OF THE TERMINATION SHOCK CAN BE DERIVED FROM THE PRESSURE BALANCE BETWEEN THE RELATIVISTIC WIND AND THE NON-RELATIVISTIC NEBULA:  $R_{TS} R_N (V_N / C)^{1/2} 10^9 \cdot 10^{10} R_{LC}$  (REES & GUNN 74) - HERE WE ASSUMED THAT THE MAGNETIC PRESSURE IS NEGLIGIBLE, NOT TRUE IN GENERAL – In the Crab  $R_{TS} \sim 0.1$  pc

Composition: mainly pairs maybe a fraction of ions Geometry: perpendicular where magnetized even if field not perfectly toroidal Magnetization:  $\sigma = B^2/4\pi n\Gamma mc^2 \rightarrow \sigma \sim V_N/c \ll 1$ , a paradox



### A MORE REALISTIC STRUCTURE OF THE TERMINATION SHOCK



#### The termination shock is not spherical



### ACCELERATION AT THE TERMINATION SHOCK

# Is the termination shock able to accelerate particles?

• Cold high relativistic wind:  $\gamma > 10^5$   $\rightarrow$  particles are catched by the shock as  $\mu < 1/\gamma$ 



### ACCELERATION AT THE TERMINATION SHOCK

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- Cold high relativistic wind:  $\gamma > 10^5$   $\rightarrow$  particles are catched by the shock as  $\mu < 1/\gamma$
- High magnetization:

$$\sigma_1 = \frac{B_1^2}{4\pi \gamma_1 n_1 m_e c^2} > 1$$

### ACCELERATION AT THE TERMINATION SHOCK

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- High magnetization:

$$\sigma_1 = \frac{B_1^2}{4\pi \gamma_1 n_1 m_e c^2} > 1$$

• Perpendicular shock configuration (Parker's spiral configuration)

Fermi-shock acceleration seems not suitable





It is difficult for particles to diffuse upstream

### **STRIPED WINDS + TERMINATION SHOCK**

#### From Sironi & Spitkovsky (2012)



 $\frac{\langle B_y \rangle}{B_0} = \frac{\alpha}{2 - |\alpha|} \rightarrow -1 < \alpha < 1$ 

MHD shock drives the reconnection of magnetic field

### **MAGNETIC RECONNECTION IN ONE SLIDE**



Magnetic field lines compressed at the shock can reconnect

Magnetic islands is where particles' energization occurs





### **Particle spectrum from MF reconnection**

- Slope of accelerated particles depends on magnetization  $\sigma$
- For  $\sigma \in [;:-;::] \rightarrow f(E) = E^{-s}$  with  $s \in [1-2]$





### **SPECTRUM OF CRAB**



### Conclusions

#### Supernava Remnants

- Diffusive shock acceleration is the main way to produce non-thermal particles
- DSA makes important prediction
  - Power law spectra indipendent on the diffusion properties
  - Maximum energy that can reach ~ 1 PeV ] requires MFA
  - Strong evidence for magnetic field amplification induced by CRs
    - Gamma-ray emission more complex than expected (environmental effects?)
    - Lack of PeVatrons (very young SNR or other class of sources needed?)

#### **Pulsar Wind Nebulae**

- Shock acceleration is unlike to be efficient in relativistic shocks
- Magnetic reconnection can be the main acceleration mechanism at least for low energy particles (<~ TeV)</li>

### Thanks!