

Study of fundamental symmetries in the few-nucleon systems

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“Perspectives and Challenges in Nuclear Structure after 70 Years of
Shell Model”



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S. Angelo d'Ischia, Ischia, Italy



Outline

- 1 Search for the X17 boson
- 2 Theoretical study of $A = 4$ reactions
- 3 The ${}^3\text{H}(p, e^+ e^-){}^4\text{He}$ and ${}^3\text{He}(n, e^+ e^-){}^4\text{He}$ processes
- 4 Incorporating the X17
- 5 Conclusions

The X17 boson “anomaly”

The ATOMKI experiments

- [Krasznahorkay *et al.*, PRL **116**, 042501 (2016)]: “Observation of Anomalous Internal Pair Creation in ^8Be : A Possible Indication of a Light, Neutral Boson”
- [Krasznahorkay *et al.*, arXiv:1910.10459 (23 October 2019)]: “New evidence supporting the existence of the hypothetic X17 particle”
- [Krasznahorkay *et al.*, PRC **104**, 044003 (2021)]: “A new anomaly observed in ^4He supports the existence of the hypothetical X17 particle”

Reaction	m_X [MeV]	Δm_X (stat) [MeV]	Δm_X (syst) [MeV]	τ [sec]	Evidence
$^7\text{Li}(p, e^+e^-)^8\text{Be}$	16.70	0.35	0.50	10^{-14}	$> 5\sigma$
$^3\text{H}(p, e^+e^-)^4\text{He}$ (2019)	16.84	0.16	0.20		$> 7.2\sigma$
$^3\text{H}(p, e^+e^-)^4\text{He}$ (2021)	16.94	0.12	0.21		$> 8.9\sigma$

Measurements of the e^+e^- angular correlation in the internal pair conversion (IPC) nuclear transition

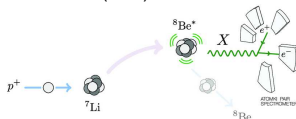


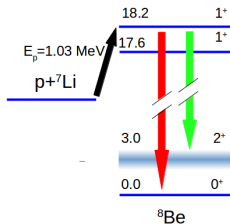
image from [Feng *et al.*, 2016]

Previous “anomalies” found in IPC

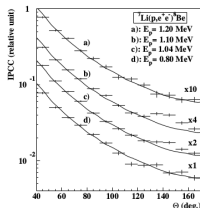
- [de Boer *et al.*, Phys. Lett. **B388**, 235 (1996); J. Phys. G **27** L29 (2001)]: IKF Frankfurt: 9 MeV Boson?
- [Vitéz *et al.*, Acta Physica Polonica B **39**, 483 (2008)]
- [de Boer & Fields, Int. J. mod. Phys. E **20**, 1787 (2011)]

The ^8Be experiment

[Krasznahorka *et al.*, PRL **116**, 042501 (2016)]



Angular distribution of the e^-e^+ pair



- [Tanedo, www.particlebites.com/?p=3970 (Aug. 25, 2016)] “The Delirium over Beryllium”
- [Zhang & Miller, 2017] “Can nuclear physics explain the anomaly observed in the internal pair production in the Beryllium-8 nucleus?”
- Last minute news!!! New paper by the ATOMKI coll. [arXiv:2205.07744](https://arxiv.org/abs/2205.07744)

Process: $^7\text{Li} + p \rightarrow (^8\text{Be})^*$

- Radiative capture: $(^8\text{Be})^* \rightarrow ^8\text{Be} + \gamma$
- IPC (standard): $(^8\text{Be})^* \rightarrow ^8\text{Be} + \gamma^* \rightarrow ^8\text{Be} + e^+e^-$
- IPC (exotic): $(^8\text{Be})^* \rightarrow ^8\text{Be} + X \rightarrow ^8\text{Be} + e^+e^-$
- Background: real γ converting to e^+e^- from interaction with the apparatus = external pair conversion (EPC)

The ^4He experiment (2019)

- [Krasznahorkay *et al.*, arXiv:1910.10459v1], [Firak *et al.*, EPJ Web Conf. **232**, 04005 (2020)]
- [Frankenthal, <https://www.particlebites.com/?p=6696> (Jan. 4, 2020)] “The Delirium over Helium” for an update of the precedent *particlebites.com* report
- cerncourier.com/a/rekindled-atomki-anomaly-merits-closer-scrutiny/
- Reaction $^3\text{H}(p, e^- e^+) ^4\text{He}$, proton beam of 0.90 MeV

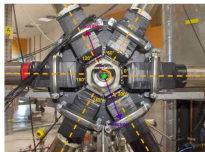
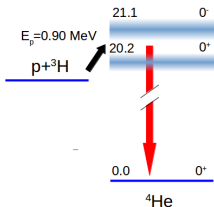
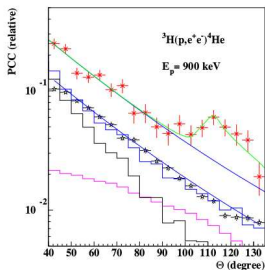


Figure 3. The Atomki nuclear spectrometer. This is an upgraded detector



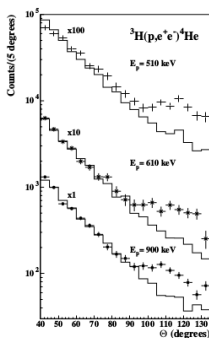
Angular distribution of the $e^- e^+$ pair
(IPC+EPC)



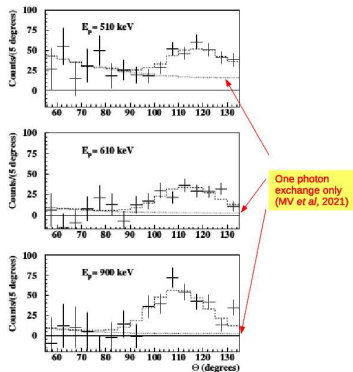
The ^4He experiment (2021)

- [Krasznahorkay *et al.*, PRC **104**, 044003 (2021)]
- Reaction $^3\text{H}(p, e^- e^+)^4\text{He}$, now 3 energies of the proton beam: 0.51, 0.61, and 0.90 MeV

Measured angular distribution of the $e^- e^+$ pairs



GEANT analysis: Subtraction of the background of pairs created EPC processes



These announcements triggered new expt. activities

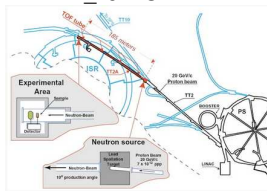
Courtesy by C. Gustavino (INFN-Rome)

Experiment	
LHCb	Charm meson decay $D^*(2007)^0 \rightarrow D^0 A' A' \rightarrow e^+ e^-$
Mu3e	Muon decay channel $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu (A' \rightarrow e^+ e^-)$
VEPP-3	$e^+ e^- \rightarrow A' \gamma$
KLOE-2	$e^+ e^- \rightarrow \gamma (X \rightarrow e^+ e^-)$
MESA	e- beam on gaseous target, to produce A'
Darklight	e- scattering of H gas target, to produce A'
HPS	e- beam on W to study $A' \rightarrow e^+ e^-$ and $A' \rightarrow \mu^+ \mu^-$
PADME	e+ beam on diamond target $e^+ e^- \rightarrow X \gamma$
NA64	$eZ \rightarrow eZ + X17$
NSL	${}^8\text{Be} (A' \rightarrow e^+ e^-)$
${}^8\text{BeP}$	${}^8\text{Be} (A' \rightarrow e^+ e^-)$
New JEDI	${}^8\text{Be}/{}^7\text{He}/d\dots (A' \rightarrow e^+ e^-)$
Montréal	${}^8\text{Be} (A' \rightarrow e^+ e^-)$
NSCL	${}^8\text{Be} (A' \rightarrow e^+ e^-)$
IUAP CTU	${}^8\text{Be}$ and ${}^4\text{He} (A' \rightarrow e^+ e^-)$
n_TOF	${}^4\text{He}$ and ${}^8\text{Be} (A' \rightarrow e^+ e^-)$ (proton and neutron beams)
MEG2	${}^8\text{Be}$
NUCLEX	${}^8\text{Be}$

In particular in Italy . . .

- PSI: ${}^7\text{Li}(p, e^+ e^-){}^8\text{Be}$ MEGII (data taking underway)
- n_ToF at CERN: ${}^3\text{He}(n, e^+ e^-){}^4\text{He}$ (planned in 2023)
- LNL: ${}^7\text{Li}(p, e^+ e^-){}^8\text{Be}$ NUCLEX (planned in 2023)
- in investigation: ${}^2\text{H}(n, e^+ e^-){}^3\text{H}$ (n_ToF) and ${}^2\text{H}(p, e^+ e^-){}^3\text{He}$ (LNGS)

n_ToF CERN



and theoretical speculations...

- [Feng *et al.*, 2016] “Protophobic Fifth Force Interpretation of the Observed Anomaly in ^8Be Nuclear Transitions”
- [Kozaczuk, Morrissey, & Stroberg, 2016] “Light axial vector bosons, nuclear transitions, and the ^8Be anomaly”
- [Delle Rose, Khalil, & Moretti, 2019] “New Physics Suggested by Atomki Anomaly”
- [Feng, Tait, & Verhaaren, 2020] “Dynamical Evidence For a Fifth Force Explanation of the ATOMKI Nuclear Anomalies”
- [Fayet, 2020] “The U boson, interpolating between a generalized dark photon or dark Z , an axial boson and an axionlike particle”
- [Alves, 2020] “Signals of the QCD axion with mass of $17 \text{ MeV}/c^2$: Nuclear transitions and light meson decays”
- “Shedding light on X17”, workshop held at Centro Fermi, Rome, Sep 6–8, 2021
- [Wong, 2022] “QED Meson Description of the X17 and Other Anomalous Particles”

Most of the speculations based on “resonance saturation”

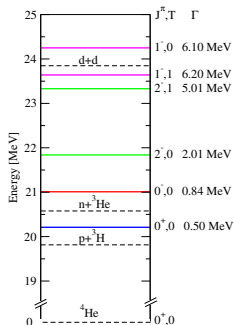
Assumed mechanism $p + ^3\text{H} \rightarrow (^4\text{He})^* \rightarrow ^4\text{He} + X$,
followed by the decay $X \rightarrow e^+ e^-$

Present calculation

Motivation of this work:

- solve accurately the $A = 4$ nuclear dynamics
- include the contribution of all relevant waves
- treat the X17 interaction within the χ PT framework

0^+ and 0^- resonances: very sensitive to the nuclear interaction



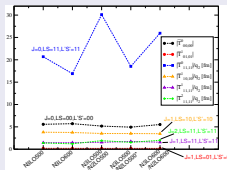
[Tilley, Weller, & Hale, 1992]

For the 0^+ resonance:

[Bacca *et al.*, 2015], [Kegel *et al.*, 2022]

For the 0^- resonance:

- $\vec{n} + ^3\text{He} \rightarrow p + ^3\text{H}$ "n3he" experiment at ORNL at $E_n = 4.6$ meV
- $A_Y = (-41 \pm 5.6 \text{ stat} \pm 0.6 \text{ sys}) \cdot 10^{-8}$



X17 interaction with electrons

- $\Gamma = 1, \gamma^5, \gamma^\mu, \gamma^\mu \gamma^5, \dots$
- $e =$ electric charge ($e > 0$)
- $X(x)$ X17 field

$$\mathcal{L} = e\epsilon_e \bar{e}(x)\Gamma e(x)X(x) + e\epsilon_u \bar{u}(x)\Gamma u(x)X(x) + \dots$$

X17 decay

- $X \rightarrow e^- e^+, \nu \bar{\nu}, \dots$
- Decay channel in $e^- e^+$ dominant [Feng *et al.*, 2016–2020]
- $\Gamma_X \approx \epsilon_e^2 \alpha M_X$
- The X17 must decay in the apparatus
 $\rightarrow |\epsilon_e| > 10^{-5}$
- Beam dump experiments:
 - SLAC E141 $|\epsilon_e| > 2 \cdot 10^{-4}$
[Alexander *et al.*, 2017]
 - NA64 $|\epsilon_e| > 6.8 \cdot 10^{-4}$ [Banerjee *et al.*, 2020]
- Direct search in $e^- e^+$ experiments:
KLOE2 $|\epsilon_e| < 2 \cdot 10^{-3}$ [Feng *et al.*; 2016]

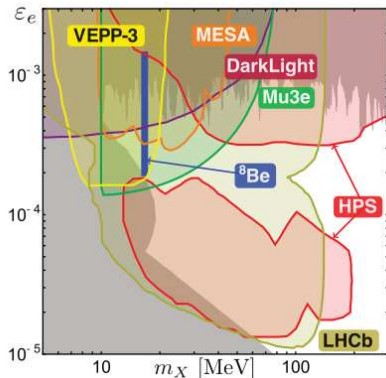


image from [Feng *et al.*, 2016]

Proposed models

“Protophobic” vector boson

[Feng *et al.*, 2016–2020]

Fifth force

Quantum numbers $J^\pi = 1^-$

NA48 limit for $\pi^0 \rightarrow \gamma X$

[Batley *et al.*, 2015]

A way out: the particle X does not couple with protons

$$|2\varepsilon_U + \varepsilon_D| < 8 \cdot 10^{-4}$$



Relation with $a_e = (g-2)_e/2$

- New estimate of α [Morel *et al.*, 2020]
- $\rightarrow \delta a_e = (4.8 \pm 3.0) \times 10^{-13} (+1.6\sigma)$
- Contribution of a vector boson X17: $\delta a_e > 0$
- Consistent with the ^8Be anomaly!

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“Piophobic” axion [Alves,

2020]

Quantum number $J^\pi = 0^-$

QCD axion with mass ~ 17 MeV generally excluded

[Alves & Weiner, 2017]

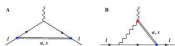
A way out: no mixing with π^0

$$\mathcal{L} = \theta_{a-\pi} X(x) \pi^0(x),$$

$$|\theta_{a-\pi}| < 10^{-4}$$

Relation with $a_e = (g-2)_e/2$

- Contribution of a pseudoscalar X17: $\delta a_e < 0$
- However, including $\mathcal{L} \sim \tilde{g} X(x) F_{\mu\nu} \tilde{F}^{\mu\nu}$, more diagrams can be considered [Barr & Zee, 1990]

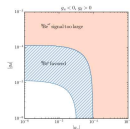


Fundamental symmetries in few-nucleon syst.

Light axial vector [Kozaczuk, Morrissey, & Stroberg, 2016]

Quantum number $J^\pi = 1^+$

In this case the NA48 limit does not apply



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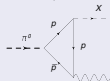
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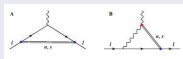
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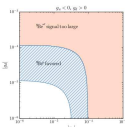


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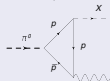
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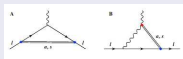
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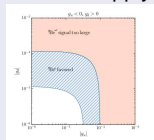


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Theoretical study of $A = 4$ reactions

Numerical techniques for $A = 4$ for scattering

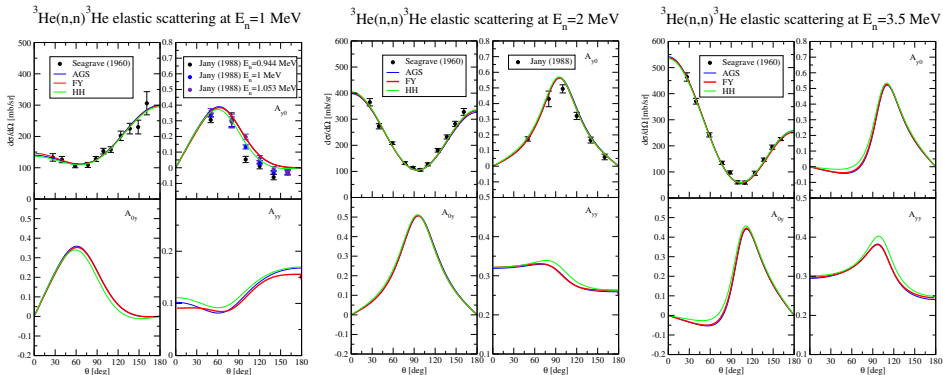
- Faddeev-Yakubovsky methods [Lazauskas & Carbonell, 2004], [Deltuva & Fonseca, 2007]
- Expansion on a basis: NCSM [Quaglioni, Navratil & Roth, 2010], Gaussians [Aoyama *et al.*, 2011], R-matrix [Descouvemont & Baye], HH [Kievsky, Marcucci, MV, *et al.*, 2008], ...

Modern nuclear interactions

- Based on χ EFT & χ -perturbation theory [Weinberg, 1966], [Callan *et al.*, 1969], [Gasser & Leutwyler, 1984]
- Expansion parameter Q/Λ_χ , $Q \sim m_\pi$, $\Lambda_\chi \approx 1$ GeV [Weinberg, 1990-1992], [Ordoñez, Ray, & Van Kolck, 1996], [Epelbaum, Hammer, & Meissner, 2009] for a review
- NN interaction:
 - Lowest order (LO) $(Q/\Lambda_\chi)^0$: one-pion-exchange potential + contact interactions
 - next-to-leading (NLO): 1 loop+dimensional regularization, etc
 - The various contributions can be visualized through TOPT diagrams
 - Cutoff $\Lambda = 400 - 600$ MeV for the non-perturbative regularization: the results should not depend on it
- 3N interaction: developed at N4LO, but for the moment practical calculations are possible only at N2LO

Benchmark test of 4N scattering calculations

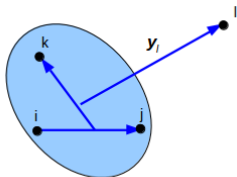
N3LO500 potential – ${}^3\text{He}(n, n){}^3\text{He}$ elastic scattering



AGS= Deltuva & Fonseca – FY= Lazauskas & Carbonell – HH= present work

Calculation of transition amplitudes

We need 1) initial/final wave functions 2) transition operators (currents & charges)



Initial/final wave functions

Ψ_4 : ${}^4\text{He}$ bound state wave function $J^\pi = 0^+$
 Ψ_{1+3} : scattering wave function – decomposed in components of definite LSJ

$$\Psi_{1+3} = \sum_{LMSS_zJJ_z} \left(\frac{1}{2} m_3 \frac{1}{2} m_1 |SS_z\rangle (LMSS_z|JJ_z) 4\pi i^L Y_{LM}^*(\hat{p}) e^{i\sigma L} \Psi_{1+3}^{LSJ} \right)$$

\mathbf{p} relative momentum

EM charge & currents transition operators

EM current from χ EFT

[Park *et al*, 1993], [Kolling *et al*, 2009], [Pastore *et al*, 2009]
Including the Δ d.o.f. [Schiavilla *et al.*, 2018]

A= Diagrams in standard χ EFT

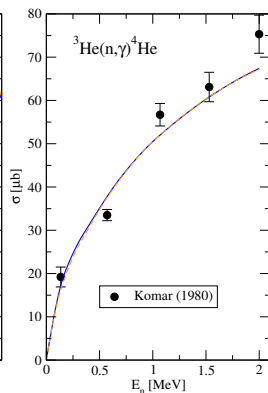
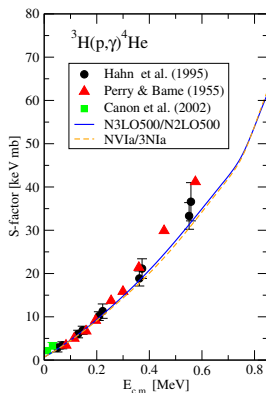
B= Diagrams with the inclusion of the Δ d.o.f. up to N2LO

	charge	A	current	charge	B	current
LO						
NLO						
N2LO						
N3LO						
N4LO						

${}^3\text{H}(p, \gamma){}^4\text{He}$ and ${}^3\text{He}(n, \gamma){}^4\text{He}$ EM captures

Interest

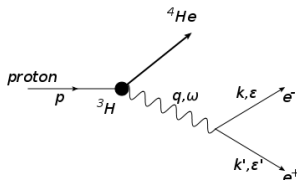
- BBN, production of ${}^4\text{He}$
- Dominated by the E_1 transition $1^- \rightarrow 0^+$
- No sensitivity to interactions/MEC
- Real γ 's conversion in $e^- e^+$ from interaction with the apparatus
- \rightarrow external pair conversion (EPC)



The ${}^3\text{H}(p, e^+ e^-){}^4\text{He}$ and ${}^3\text{He}(n, e^+ e^-){}^4\text{He}$ processes

“Standard” EM process

$$\frac{d^6\sigma}{d\epsilon d\hat{k} d\epsilon' d\hat{k}'} = \frac{\alpha^2}{8\pi^3} \frac{kk'}{Q^4 v} \delta\left(E_0 - \epsilon - \epsilon' - \frac{(\mathbf{p} - \mathbf{q})^2}{2M_4}\right) \times \sum_i v_i R_i(q, \omega)$$



$$E_0 = E_p + B_4 - B_3 \approx 20 \text{ MeV}, \quad \mathbf{q} = \mathbf{k} + \mathbf{k}', \quad \omega = \epsilon + \epsilon', \quad Q^2 = \omega^2 - q^2 > 0 \text{ “time-like”}$$

$$\cos\theta_{ee} = \hat{\mathbf{k}} \cdot \hat{\mathbf{k}'}, \quad i = L, T, TT, TT', LT, LT'$$

$$v_L = \frac{Q^4}{q^4} (\epsilon\epsilon' + \mathbf{k} \cdot \mathbf{k}' - m_e^2) \quad R_L(q, \omega) = \sum_{m_1, m_3} |\langle \Psi_4 | \rho(\mathbf{q})^\dagger | \Psi_{m_1, m_3}^{(p,t)} \rangle|^2 \sim \sum_{LSJ} |C_J^{LSJ}|^2$$

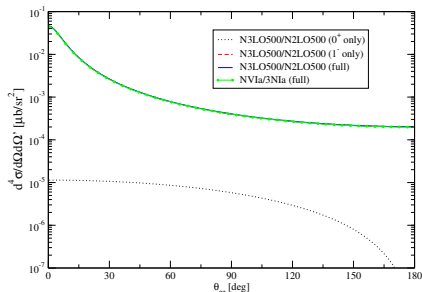
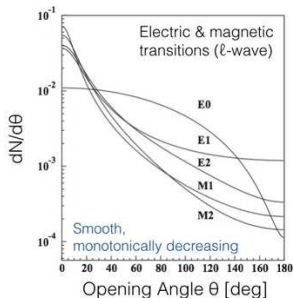
After integrating the δ over ϵ' and numerically over ϵ ($p_r = \epsilon'(k' - p \cos\theta' + k \cos\theta_{ee})/k'$)

$$\frac{d^4\sigma}{d\hat{k} d\hat{k}'} = \frac{\alpha^2}{8\pi^3} \int_{m_e}^{\epsilon_{\max}} d\epsilon \left[\frac{kk'}{Q^4 v} \frac{1}{1 + p_r/M_4} \sum_i v_i R_i \right]_{\epsilon' \approx E_0 - \epsilon}$$

${}^3\text{H}(p, e^+e^-){}^4\text{He}$ cross section in the one-photon-exchange approximation

Calculation using
N3LO500/N2LO500 + χ EFT current by
[Pastore *et al.*, 2009]
NV1a/3Na* + χ EFT current by [Schiavilla *et al.*,
2018]

Multipole angular distribution as reported in
[Tanedo,
www.particlebites.com/?p=3970]



Due to the simple q dependence of the matrix elements, it is not possible to explain any large angle “bump”

Incorporating the X17

Scales ...

- $E \sim 1$ TeV BSM mechanism (axion, SSM, ...)
- $E \sim 1$ GeV: interaction with SM particles
- $E \sim 100$ MeV: interaction with hadrons (N , π , ...)
- $E \sim 1$ MeV: nuclear physics experiments

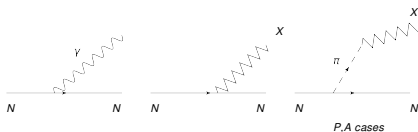
EFT approach

- 1 Start with a generic interaction Lagrangian with electrons, u and d quarks, ...
- 2 Generate the interaction at hadronic level using χ EFT
- 3 Accurately compute the matrix elements of the generated operators

Analysis similar to what done for DM interaction with nuclei

[Menéndez *et al.*, 2011–2012], [Hoferichter *et al.*, 2015–2019], [Bishara *et al.*, 2016], [Körber *et al.*, 2017], [Nogga *et al.*, 2017], [Andreoli *et al.*, 2019], [Hu *et al.*, 2021], ...

For X17: LO (+ some subleading terms) analysis [MV *et al.*, PRC **105**, 014001 (2022)]



LO (+ some subleading terms) analysis: S case

[MV *et al.*, PRC **105**, 014001 (2022)]

Scalar case at 1 GeV scale

$$\mathcal{L}_{q,X}^S(x) = \sum_{f=u,d} e \frac{\varepsilon_f m_f}{\Lambda} \bar{f}(x) f(x) X(x),$$

At hadronic level

$$\mathcal{L}_X^S(x) = e \bar{N}(x) [\eta_0^S + \eta_Z^S \tau_3] N(x) X(x)$$

$$\eta_0^S = -\frac{4 c_1 m_\pi^2}{\Lambda_S} \varepsilon_0$$

$$\eta_Z^S = -\frac{2 c_5 m_\pi^2}{\Lambda_S} \varepsilon_Z$$

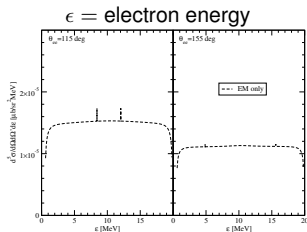
$$\varepsilon_0 = \frac{\Lambda_S}{\Lambda} \frac{m_u \varepsilon_u + m_d \varepsilon_d}{2 m_q}$$

$$\varepsilon_Z = \frac{\Lambda_S}{\Lambda} \frac{m_u \varepsilon_u - m_d \varepsilon_d}{2 m_q}$$

- Λ high energy scale (≈ 246 GeV)
- $\Lambda_S = 1$ GeV introduced for convenience
- Extended to treat also pseudoscalar (P), vector (V), and axial (X) bosons

X17-induced cross section

$$\frac{d^5\sigma}{d\epsilon d\hat{k} d\hat{k}'} = \sigma_{EM}(\epsilon) + \epsilon_e \left[\frac{R_X(\epsilon)}{D_X} + \text{c.c.} \right] + \epsilon_e^2 \frac{R_{XX}(\epsilon)}{|D_X|^2} = \sigma_{EM}(\epsilon) + \frac{\epsilon_e [R_X(\epsilon) D_X^* + \text{c.c.}] + \epsilon_e^2 R_{XX}(\epsilon)}{|D_X|^2}$$



$$\frac{1}{|D_X|^2} \rightarrow \frac{\pi}{|\alpha_i|} \frac{1}{\Gamma_X M_X} \delta(\epsilon - \epsilon_i) .$$

$$\frac{d^4\sigma}{d\hat{k} d\hat{k}'} = \left[\int_{m_e}^{E_{max}} \sigma_{EM}(\epsilon) \right] + \sum_i \left[2\epsilon_e \Im(R_X(\epsilon_i)) \frac{\pi}{|\alpha_i|} + \epsilon_e^2 R_{XX}(\epsilon) \frac{\pi}{|\alpha_i| M_X \Gamma_X} \right]$$

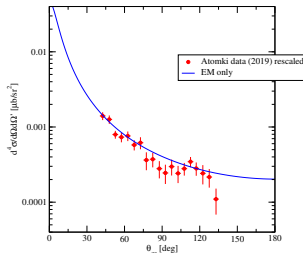
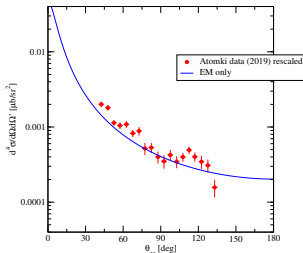
No sensitivity to ϵ_e and the interference term!!!

- Propagator of a massive particle $1/D_X = 1/(Q^2 - M_X^2)$, where $Q^2 = (k + k')^2$
- $M_X \rightarrow M_X - i\frac{\Gamma_X}{2}$
- Γ_X from the process $X \rightarrow e^+ e^-$
 - $\Gamma_X = \epsilon_e^2 \alpha M_X \sim 1 \text{ eV}$
- Condition $Q^2 - M_X^2 = 0$ verified for $\epsilon = \epsilon_i, i = 1, 2$
- For $\epsilon \approx \epsilon_i, Q^2 - M_X^2 = \alpha_i(\epsilon - \epsilon_i)$

Fit of the 2019 data

- In the perpendicular plane, the X17 signal appears for $\theta_{ee} > 110^\circ$
- only a counting rate is furnished – no information on the flux/target/efficiencies
- Procedure:
 - rescale the ATOMKI rate by a factor so to reproduce the cross section for $\theta_{ee} < 110^\circ$
 - For these angles the cross section is EM only - no unknown parameter
 - Fix $M_X, \varepsilon_u, \varepsilon_d$ to reproduce the “bump”

Problem!



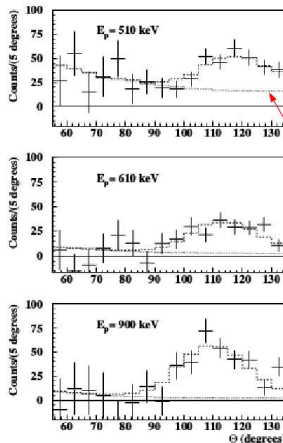
Here there is also the problem of the EPC pairs!

Fit of the 2021 data

- 2021 data: the background has been somehow subtracted
- but the procedure it is still difficult to be applied
- Furthermore: finite angular/energy resolution of the target, geometry of the detector, efficiencies, etc.

For the moment

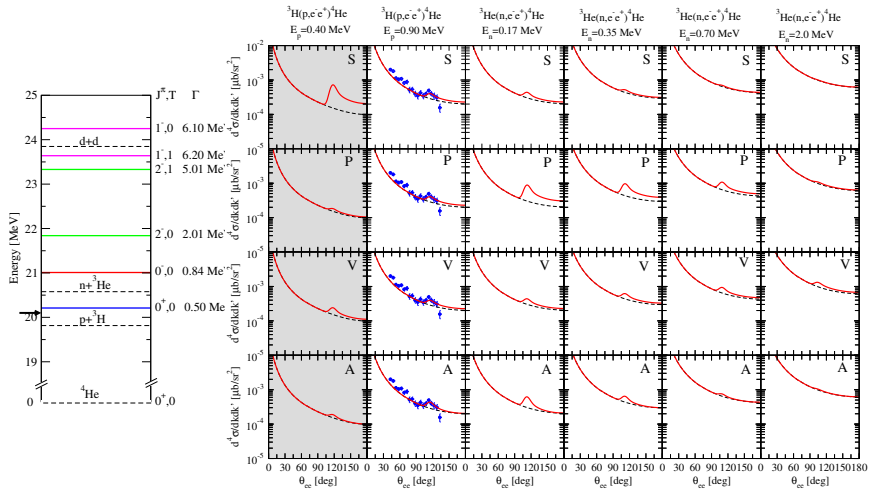
- let us study the dependence of the cross section on
 - beam energy
 - the e^+e^- emission angles
- see if it is possible to extract information on the hypothetical X17



One photon exchange only (MV et al, 2021)

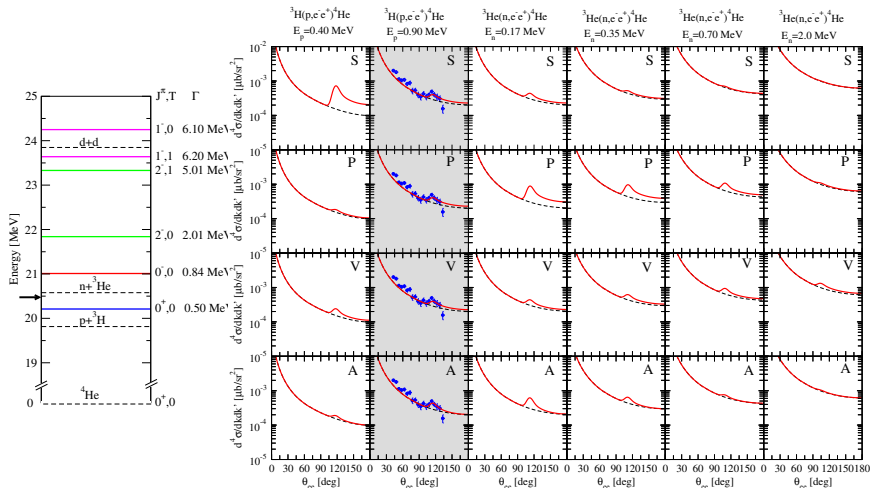
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



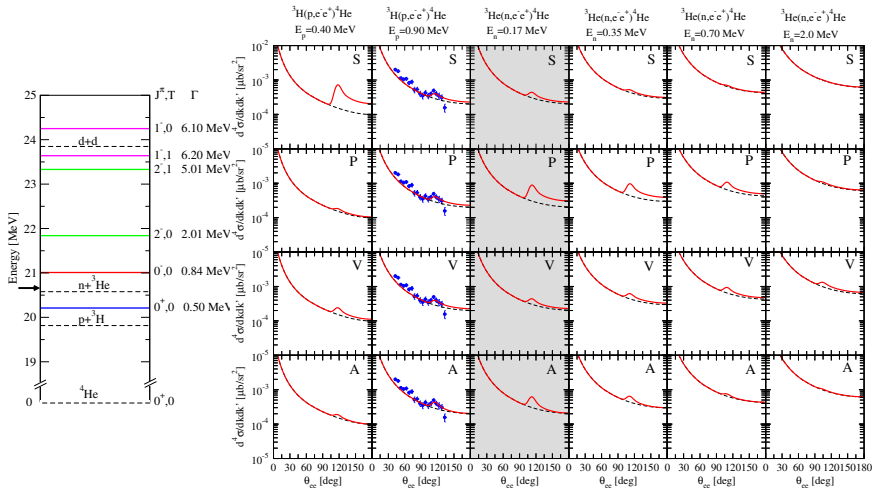
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



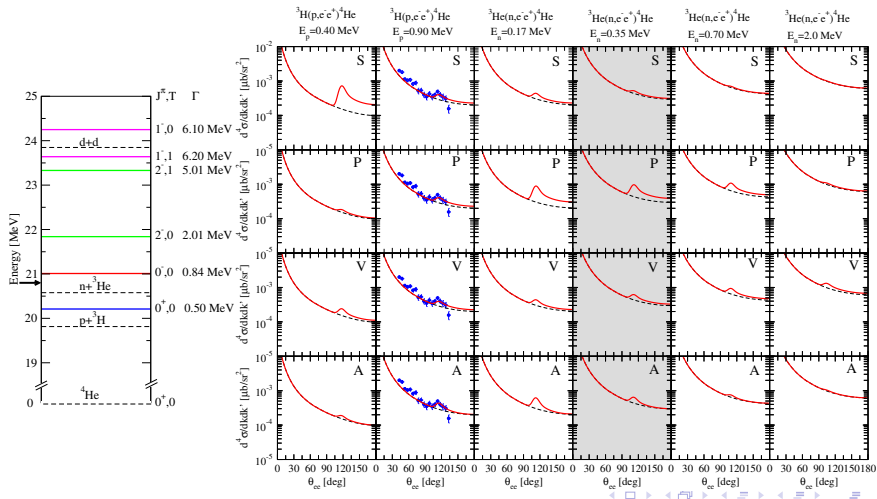
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



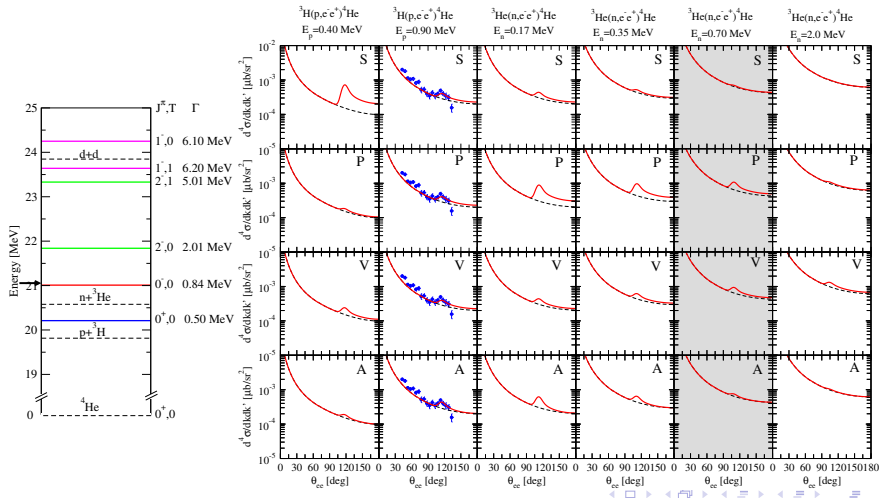
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



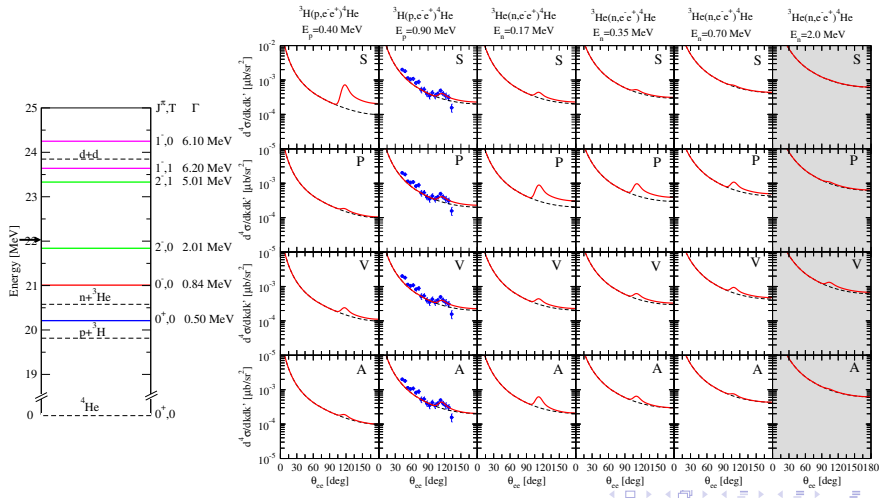
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



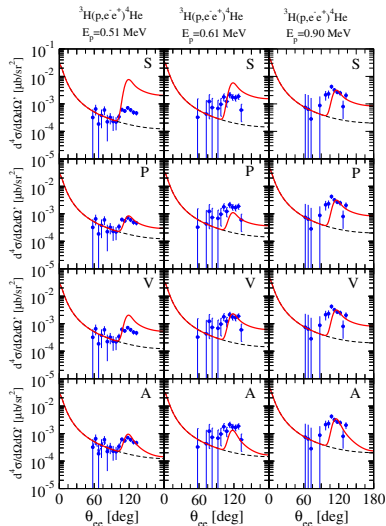
Comparison with the 2019 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



Comparison with the 2021 ATOMKI data

pair emission in the perpendicular plane – peak fitted at 0.90 MeV



Extracted coupling constants

S,P cases

$$\varepsilon_{0,z} = \frac{\Lambda_S}{\Lambda} \frac{m_u \varepsilon_u \pm m_d \varepsilon_d}{2m_q}$$

V,A cases

$$\varepsilon_{0,z} = \frac{\varepsilon_u \pm \varepsilon_d}{2}$$

Protophobic case

$$[2\varepsilon_u + \varepsilon_d = 0 \Rightarrow 3\varepsilon_0 + \varepsilon_z = 0]$$

Case	N3LO500/N2LO500		NV1a/3NIa	
	ε_0	ε_z	ε_0	ε_z
S	0.86×10^0	0	0.75×10^0	0
P	0	5.06×10^0	0	4.82×10^0
P	2.55×10^1	0	2.72×10^1	0
V	2.56×10^{-3}	$-3\varepsilon_0$	2.66×10^{-3}	$-3\varepsilon_0$
A	2.58×10^{-3}	0	2.89×10^{-3}	0

First rough estimates – very uncertain due to the aforementioned difficulties

Vector case

- $|\varepsilon_{u,d}| \sim 10^{-3}$ **Feng et al., 2016-2020]**
- Consistent!

Pseudoscalar case

- $|\varepsilon_{u,d}| \sim 1$ **Alves, 2020], Delle Rose et al., 2019]**
- too small!

Axial case

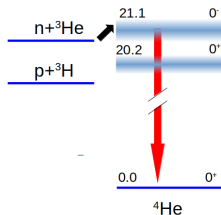
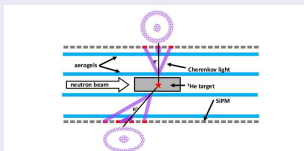
- $|\varepsilon_{u,d}| \sim 10^{-4}$ **[Kozaczuk, Morrissey, & Stroberg, 2016]**
- too small!

^4He experiment at CERN

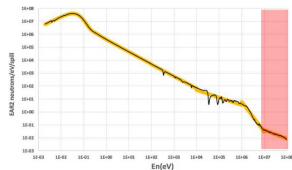
$^3\text{He}(n, e^+ e^-)^4\text{He}$ using the neutron beam of the n_ToF experiment

[MV *et al.*, PRC **105**, 014001 (2022)]

- neutron energy tagged by means of the time-of-flight
- background:
 - $^3\text{He}(n, n)^3\text{He}$
 - $^3\text{He}(n, p)^3\text{H}$: the most dangerous problem $\sigma_{(n,p)} \gg \sigma_{\text{IPC}}$
 - $^3\text{He}(n, \gamma)^4\text{He}$ followed by EPC
- Energy of the leptons is of several MeV:
 $\beta \sim 1$
- Energy of the protons \sim a few MeV:
 $\beta \ll 1$
- Cherenkov [C. Gustavino *et al.*, 2021]



Neutron energies



Conclusions and perspectives

Analysis of the ^4He ATOMKI “anomaly”

- Accurate description of the nuclear dynamics using state-of-the-art techniques
- Test with $p + ^3\text{H}$ and $n + ^3\text{He}$ EM captures data: OK!
- Contribution of the 1^- wave very significant at all energies
- Inclusion of the possible emission of an X17, vs. the beam energy and the emission angles

Perspectives

- New ^8Be experiment underway at PSI
 - Analysis of the $^7\text{Li}(p, e^+ e^-)^8\text{Be}$ process using GFMC calculation of ^8Be ground/excited states
- Collaboration with the n_ToF group
 - analysis of the $^3\text{He}(n, e^- e^+)^4\text{He}$ process
 - technical design in progress & GEANT analysis currently in progress
- $^2\text{H}(n, e^+ e^-)^3\text{H}$ and $^2\text{H}(p, e^+ e^-)^3\text{He}$ reactions to test the protophobic hypothesis
- Study of possible “standard” explanation
 - Two-photon exchange contribution [Aleksejevs *et al.*, 2021] for ^4He & ^8Be
- If the anomaly is confirmed, full χEFT treatment of the X17-nucleon interaction
- Analysis of CP-violating X17 interactions and relation to EDM's

Theoretical group

- A. Kievsky, & L.E. Marcucci - *INFN-Pisa & UniPI, Pisa*
- L. Girlanda *UniSalento & INFN-Lecce, Lecce*
- E. Filandri *UniTN, Trento*
- R. Schiavilla *ODU, Norfolk, and Jefferson Lab., Newport News*
- G. King & S. Pastore *WU, St. Louis*
- G. Salmè *INFN-RM1, Rome*

n_ToF Working group

- ❖ G. Gervino (UNITO)
 - ❖ P. Mastinu (INFN LNL)
 - ❖ C. Gustavino (INFN ROMA)
 - ❖ A. Mengoni (ENEA)
 - ❖ C. Massimi (UNIBOLOGNA)
 - ❖ N. Colonna (INFN BARI)
 - ❖ S. Fiore (ENEA ROMA)
 - ❖ A. Mazzone (CNR BARI)
 - ❖ M.C. Petrone (IFIN-HH BUCHAREST)
 - ❖ L. E. Marcucci (UNIPISA)
 - ❖ M. Viviani (INFN PISA)
 - ❖ A. Kievsky (INFN PISA)
 - ❖ L. Girlanda (UNISALENTO)
 - ❖ E. Cisbani (ISS)
 - ❖ F. Renga (INFN ROMA)
- Diagram illustrating the structure of the n_ToF Working group:
- The top 8 members (G. Gervino to M.C. Petrone) are grouped under the label **n_ToF**.
 - The next 4 members (L. E. Marcucci to L. Girlanda) are grouped under the label **Theoretical group**.
 - The bottom 2 members (E. Cisbani and F. Renga) are grouped under the label **Detector R&D**.

Working group (in evolution)

Thank you for your attention!

BACKUP SLIDES

Violation of the time-reversal symmetry

Interest: Matter-antimatter asymmetry [Sakharov, 1967] \rightarrow CP violation

At a high energy scale

- In the Standard Model (SM)
 - phase in the CKM matrix (too small)
 - possible phase in the neutrino mixing matrix (?)
 - θ -term: From $d_n < 2.9 \cdot 10^{-13} e \text{ fm}$ [Baker *et al.*, 2006] $\rightarrow |\theta| < 10^{-10}$
Strong CP problem

- Beyond Standard Model (BSM)
dimension 6 possible terms
 - Weinberg three-gluon operator
 - quark EDM term
 - quark chromo-EDM term
 - four-quark operators

- See [De Vries *et al.*, FIP 8, 218 (2020)]
for a review

At the nuclear energy scale

- Nucleons and pions d.o.f.
 - TV nucleon-pions vertices $g_{0\div 2}$
 - Three-pion vertex Δ
 - Nucleon EDMs d_p, d_n
 - Nucleon-nucleon contact terms
 $C_{1\div 5}$
- it is possible (but difficult) to relate these LEC's with those appearing in SM and BSM
- Many parameters \Rightarrow many measurements are needed!

Electric dipole moments (EDMs)

For an “elementary” particle $\mathbf{d} \propto \mathbf{J}$



If P and T are conserved $\Rightarrow \langle \vec{d}_n \rangle = 0$

- Existing measurements:
 - Electron $|d_e| < 10^{-15} e \text{ fm}$ [ACME, 2014]
 - Neutron $|d_n| < 2.9 \cdot 10^{-13} e \text{ fm}$ [Baker *et al.*, 2006]
 - Heavy nuclei ^{199}Hg , pear-shaped nuclei
- EDMS predicted by the CKM phase are 5-6 orders of magnitude smaller
- New observables
 - EDMs of charge particles (p , d , ^3H , ^3He) up to $\sim 10^{-16} e \text{ fm}$ in dedicated storage-rings [Y. K. Semertzidis, 2011]
 - $\vec{n}\vec{A}$ scattering \Rightarrow amplified by nuclear resonances [Gudkov, 1992]

EDMs of light nuclei

Solution of $H\Psi = E\Psi$ including components of both parities and then computing

$$\langle \Psi | \sum_{i=1}^A e_i r_i | \Psi \rangle$$

$$d^A = d_p a_p + d_n a_n + g_0 a_0 + g_1 a_1 + g_2 a_2 + C_1 A_1 + C_2 A_2 + C_3 A_3 + C_4 A_4 + C_5 A_5 + \Delta a_\Delta$$

Deuteron

a_p	0.939
a_n	0.939
a_1 [fm]	0.200
A_3 [fm]	0.013
A_4 [fm]	-0.013
a_Δ [fm]	-0.304

${}^3\text{H}$ and ${}^3\text{He}$

	${}^3\text{H}$	${}^3\text{He}$
a_n	-0.033	0.908
a_p	0.909	-0.033
a_0 [fm]	-0.053	0.054
a_1 [fm]	0.158	0.158
a_2 [fm]	-0.119	0.119
A_1 [fm]	0.006	-0.006
A_2 [fm]	-0.010	0.010
A_3 [fm]	-0.008	-0.008
A_4 [fm]	0.013	0.013
A_5 [fm]	-0.022	0.022
a_Δ [fm]	-0.343	-0.339

Relating X17, EDM's, $(g - 2)_l, \dots$

Browsing [ArXiv:hep-ph](https://arxiv.org/abs/hep-ph), one can find several “interesting” models
Consider, for example, [\[Marciano *et al.*, 2016\]](#), [\[Cornella *et al.*, 2019\]](#), [\[Di Luzio *et al.*, 2021\]](#)
including CP violating terms in the X17 Lagrangian

$$\mathcal{L} = \sum_{i=e,\mu,u,d,\dots} \left[g_{ii} \bar{\psi}_i (1 - \gamma^5) \psi_i + h.c. \right] X + \frac{1}{4} g X F^{\mu\nu} F_{\mu\nu} + \frac{1}{4} \tilde{g} X F^{\mu\nu} \tilde{F}_{\mu\nu}$$

Contributions to

- Atomki experiments
- $(g - 2)_e$ and $(g - 2)_\mu$
- EDM's of e, μ , neutron, nuclei



“In summary, a CPV ALP can be related to many fundamental open questions in particle physics”
[\[Di Luzio *et al.*, 2021\]](#)