

# CPV tests with rare kaon decays

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On behalf of NA48 collaboration

BEACH 2010 - IX International Conference on Hyperons, Charm and Beauty Hadrons



## NA48

Main goal: Search for direct CPV:  
Measurement of  $\epsilon'/\epsilon$

Beams:  $K_L + K_S$  beam

## NA48/2

Main goal: Search for direct CPV:  
Charge asymmetry measurement

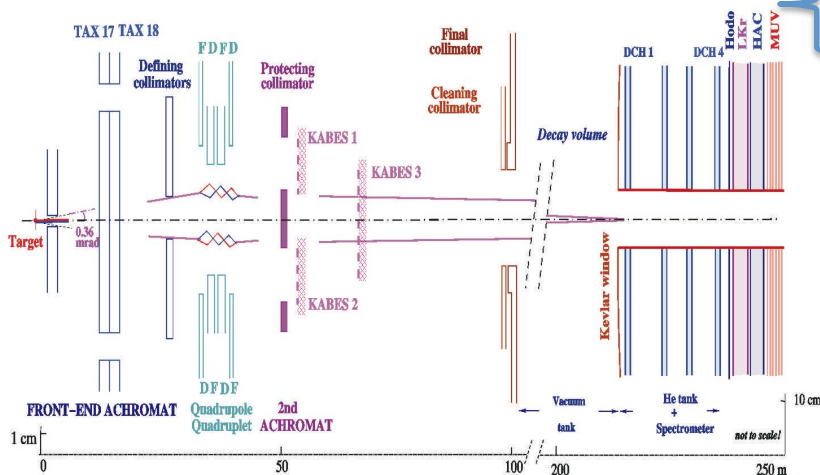
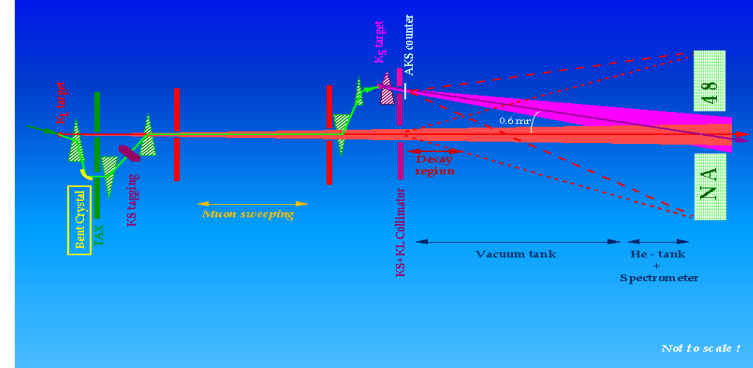
Beams:  $K^+ + K^-$  beam

## NA48/1

Main goal: Rare  $K_S$  and  
hyperon decays

Beams:  $K_S$  beam

### THE SIMULTANEOUS $K_L$ AND $K_S$ BEAMS



1997

1998

1999

2000

2001

2002

2003

2004

2005

2013



See talks by E.Goudzovskiy & G. Ruggiero

➤ **Magnetic spectrometer (4 DCHs):**

- 4 views : redundancy  $\Rightarrow$  high efficiency;
- $\Delta p/p = 1.0\% \oplus 0.044\% * p$  [GeV/c]

➤ **Hodoscope**

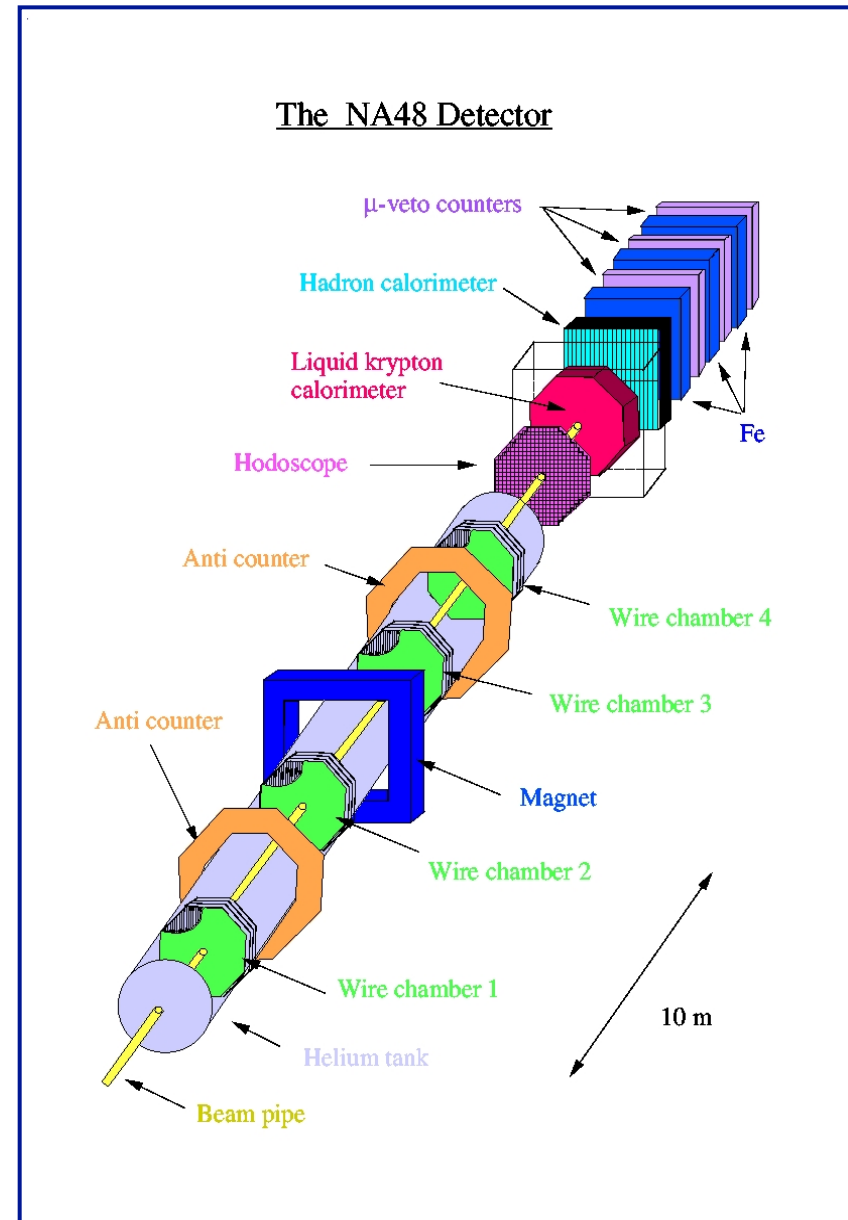
- fast trigger;
- precise time measurement ( $\sigma_t = 150$  ps) .

➤ **Liquid Krypton EM calorimeter (LKr)**

- Quasi-homogeneous ionization chamber
- 27 electromagnetic radiation lengths long active volume
- Segmented transversally 13248 cells, 2x2 cm<sup>2</sup>
- Energy resolution (E in GeV):

$$\frac{\sigma(E)}{E} = \frac{0.032}{\sqrt{E}} \oplus \frac{0.09}{E} \oplus 0.0042$$

Presented by E. Goudzovskiy, this session



# Rare decays with NA48/1

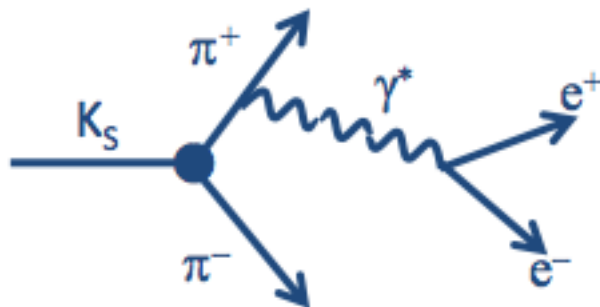
Unlike the  $K_L \rightarrow \pi^+\pi^-e^+e^-$  decay mode in which the  $CP=+1$  Inner Bremsstrahlung process competes with the  $CP=-1$  Direct Emission (M1) term, the  $K_S \rightarrow \pi^+\pi^-e^+e^-$  decay proceeds mainly via Inner Bremsstrahlung

**No sizeable interference between CP-even and CP-odd terms in KS mode**  
**CP-violating  $A_\phi$  asymmetry expected to be zero**

$$A_\phi = \frac{N_{\pi\pi e e}(\sin\phi\cos\phi > 0) - N_{\pi\pi e e}(\sin\phi\cos\phi < 0)}{N_{\pi\pi e e}(\sin\phi\cos\phi > 0) + N_{\pi\pi e e}(\sin\phi\cos\phi < 0)}$$

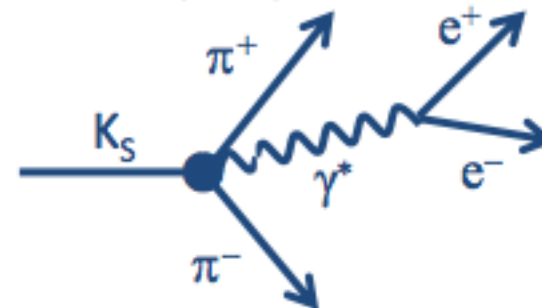
$\phi$  is the angle between  $e^+e^-$  and  $\pi^+\pi^-$  planes in the kaon rest frame

Possible contribution from Direct Emission (E1) to the decay amplitude



**Dominant Inner Bremsstrahlung**

?



**Direct Emission: E1, M1, E2, ....**

First observation by NA48 with '98 data (56 evts)

Full data set ('98+'99, HI KS):

677 candidates (mainly HI KS) ; bkg ~ 1 evt.

$BR(K_S \rightarrow \pi^+\pi^-e^+e^-) = (4.69 \pm 0.30) \cdot 10^{-5}$

$A_\phi = (-1.1 \pm 4.1) \%$



2002 NA48-1: more than 20 k  $K_S \rightarrow \pi^+\pi^-e^+e^-$  decays

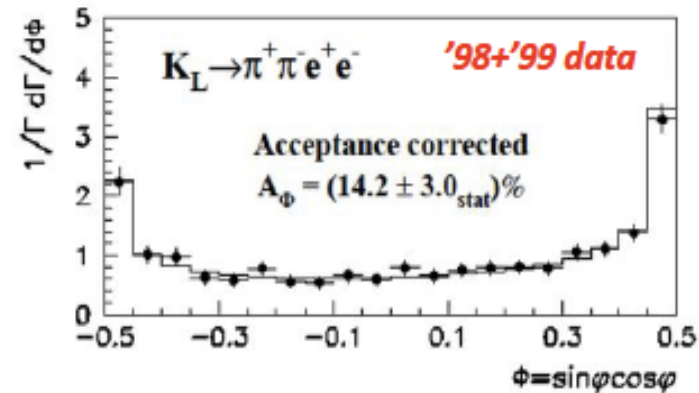
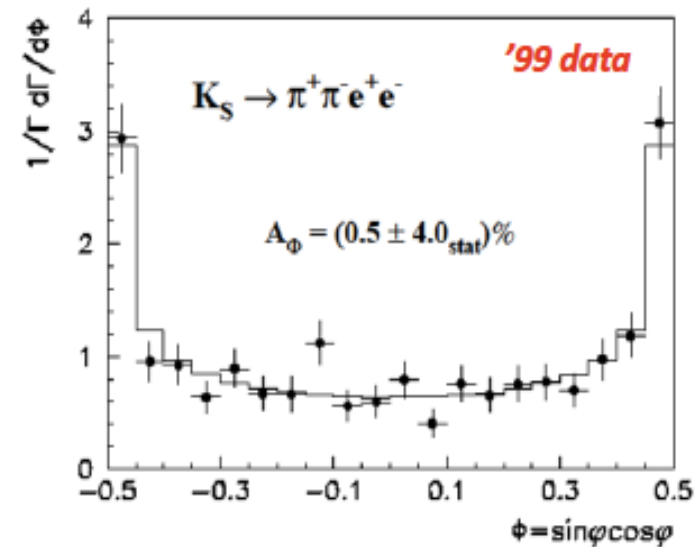
Improve significantly BR measurement

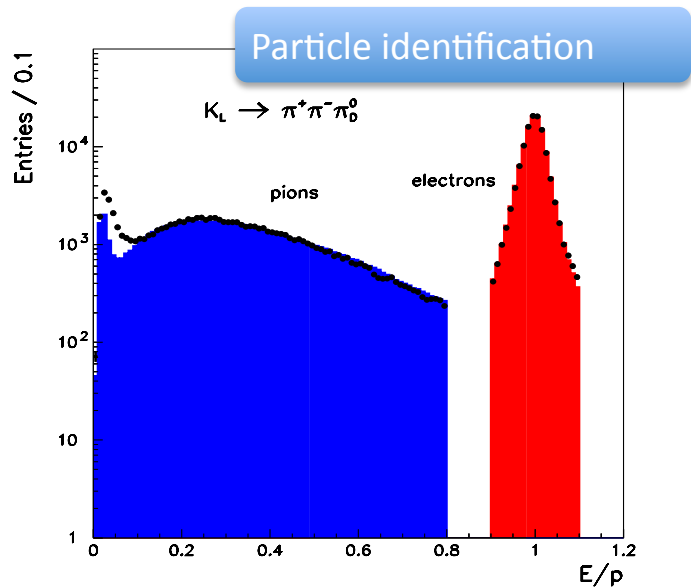
(Use  $K_L \rightarrow \pi^+\pi^-\pi^0$  decays as normalization –same selection criteria, one gamma in addition )

Accuracy on  $A_\phi$  better than 1%

Look for direct emission (E1)

*EPL C30, 33-49 (2003)*





MC simulation (bckg estimation; acc calculation)

Radiative corrections :

PHOTOS + coulomb corrections

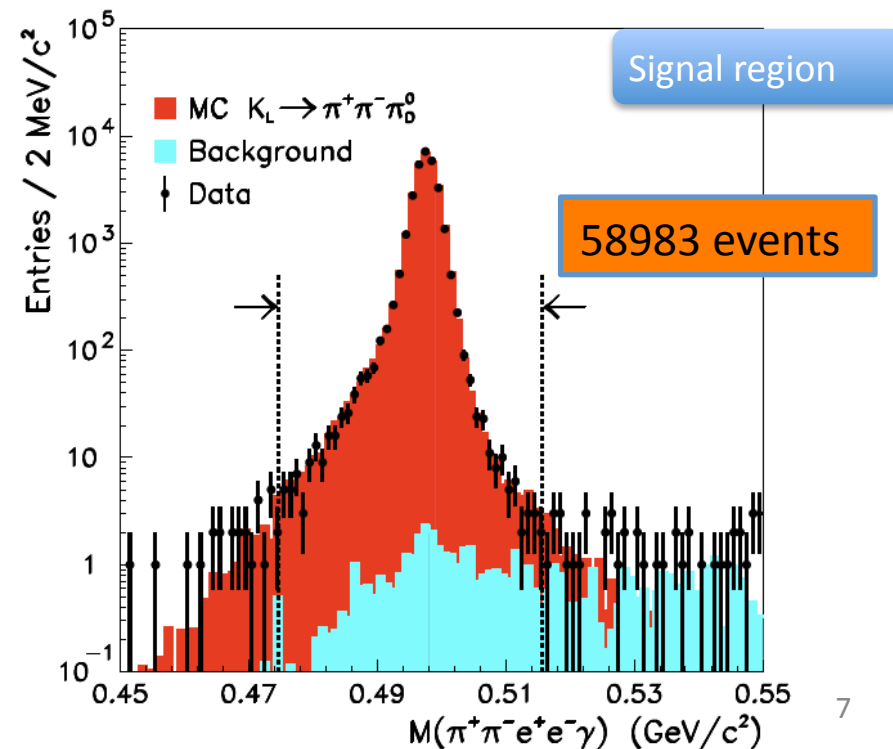
Kaon spectrum modified, beam  
shape tuned with  $K_L \rightarrow \pi^+ \pi^- \pi^0$  decays

DCH resolution functions, efficiencies included

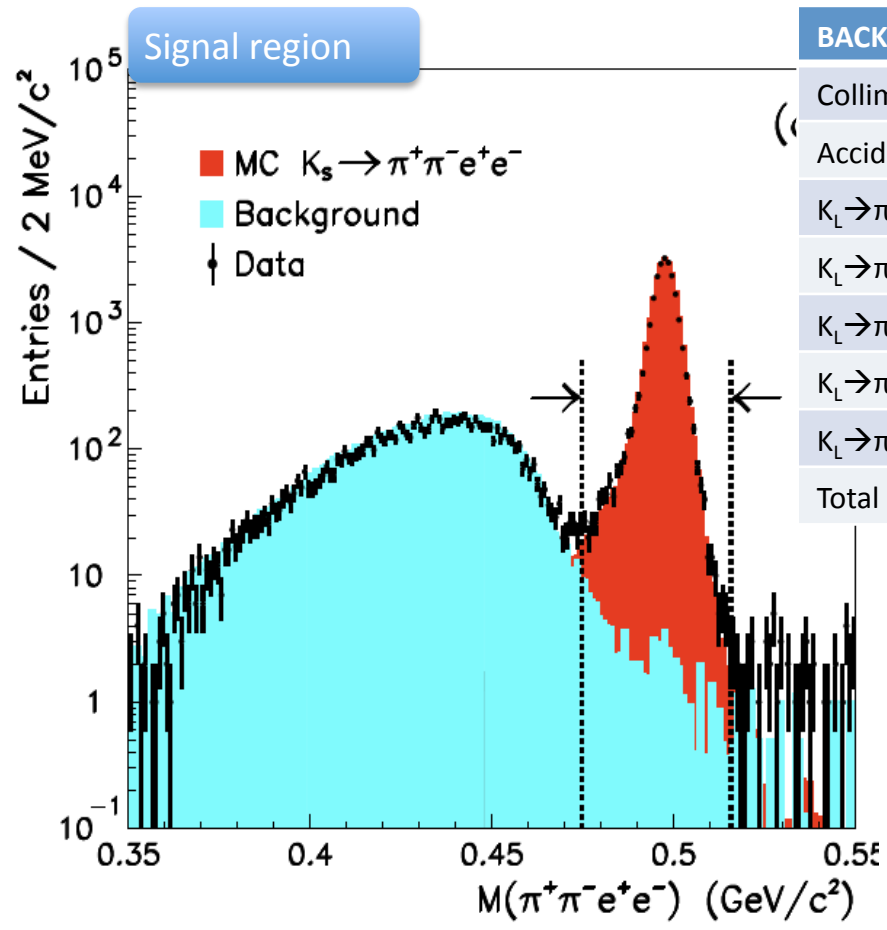
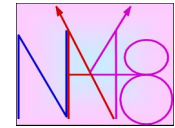
Additional resolution on  $\theta_{ee}$

GEANT3 based

BACKGROUND Source	N events
Collimator scattering	$3.7 \pm 3.7$
Accidental activity	$8.0 \pm 2.6$
$K_S \rightarrow \pi^+ \pi^- e^+ e^-$ bremsstrahlung	$11.6 \pm 1.4$
$K_S \rightarrow \pi^+ \pi^- \pi^0$	$3.7 \pm 5.8$
$K_L \rightarrow \pi^+ \pi^- \pi^0$ ; $\pi^0 \rightarrow e^+ e^- e^-$	$27.0 \pm 1.1$
$K_L \rightarrow \pi^+ \pi^- \gamma$ ; $\gamma \rightarrow e^+ e^-$	$1.1 \pm 1.1$
Total	$55.1 \pm 5.7$



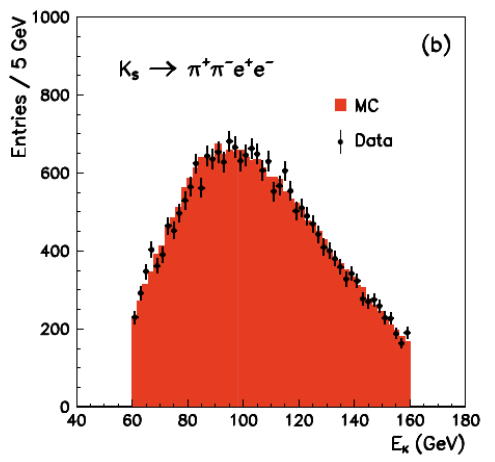
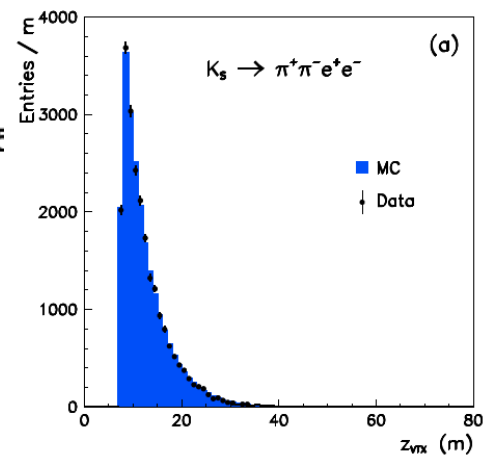
# NA48/1 $K_S \rightarrow \pi^+\pi^-e^+e^-$ decay – signal and background



BACKGROUND Source	N events
Collimator scattering	$16.2 \pm 5.7$
Accidental activity	$11.0 \pm 3.2$
$K_L \rightarrow \pi^+\pi^-e^+e^-$	$12.4 \pm 0.8$
$K_L \rightarrow \pi^+\pi^-\pi^0$	$52.0 \pm 7.7$
$K_L \rightarrow \pi^+\pi^-\pi^0; \pi^0 \rightarrow e^+e^-e^+e^-$	$10.3 \pm 1.1$
$K_L \rightarrow \pi^+\pi^-\pi^0; \pi^0 \rightarrow e^+e^-$	$0.6 \pm 0.1$
$K_L \rightarrow \pi^+\pi^-\gamma; \gamma \rightarrow e^+e^-$	$0.5 \pm 0.5$
Total	$103.0 \pm 10.2$

22966 candidate events

Good Data/MC agreement





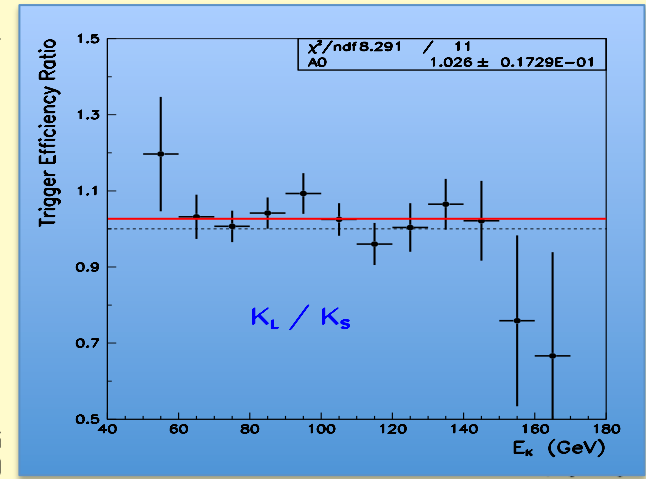
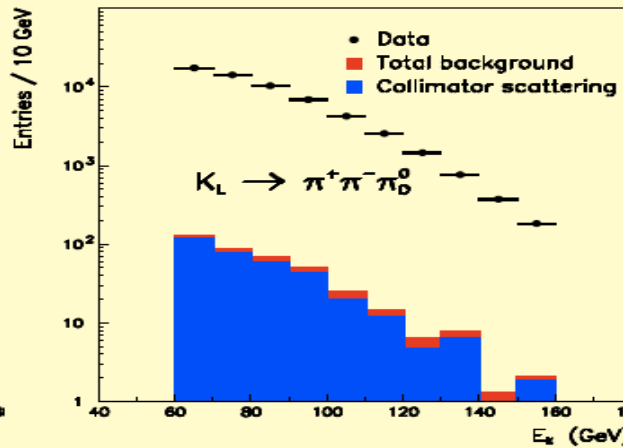
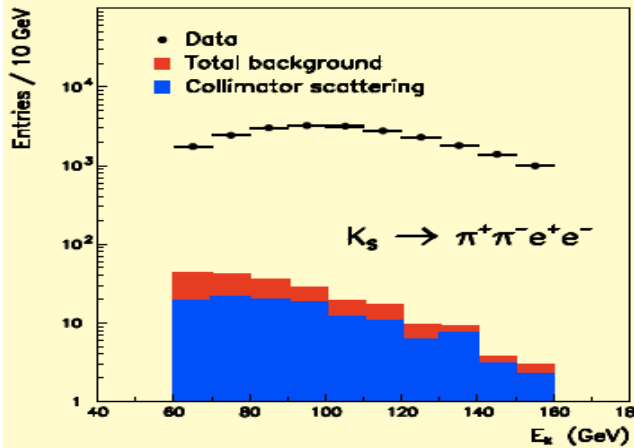
# NA48/1 $K_S \rightarrow \pi^+ \pi^- e^+ e^-$ branching ratio measurement (inputs)



$$\frac{\text{BR}(K_S \rightarrow \pi^+ \pi^- e^+ e^-)}{\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi_D^0)} = \frac{N_{\pi\pi ee}}{N_{\pi\pi\pi_D^0}} \frac{A_{\pi\pi\pi_D^0}}{A_{\pi\pi ee}} R_\varepsilon R_K$$

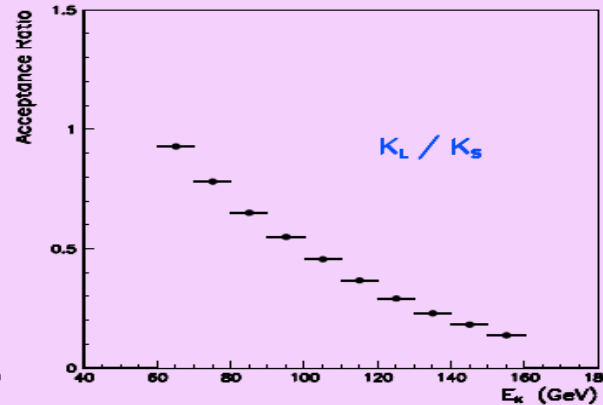
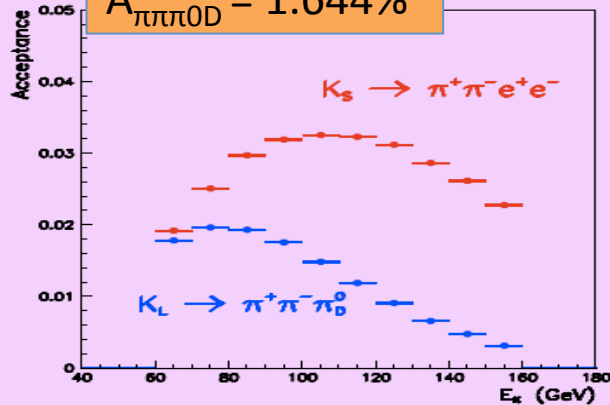
$N_{\pi\pi ee}$ ,  $N_{\pi\pi\pi_D^0}$ : # of evts after bkg. subtr.  
 $A_{\pi\pi ee}$ ,  $A_{\pi\pi\pi_D^0}$ : acceptances  
 $R_\varepsilon$ : trigger efficiency ratio  
 $R_K$ :  $K_L / K_S$  flux ratio

Analysis performed in 10 bins of  $E_K$  (60 to 160 GeV)

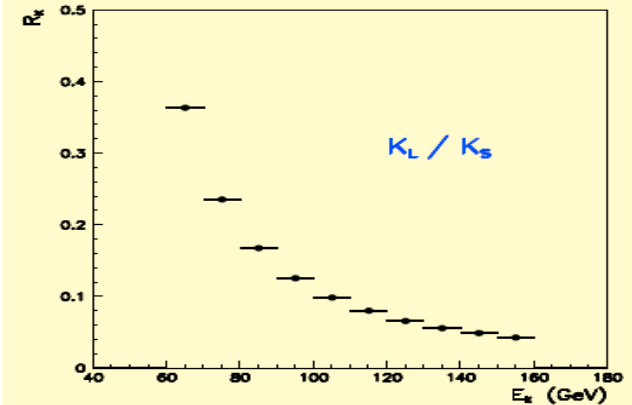


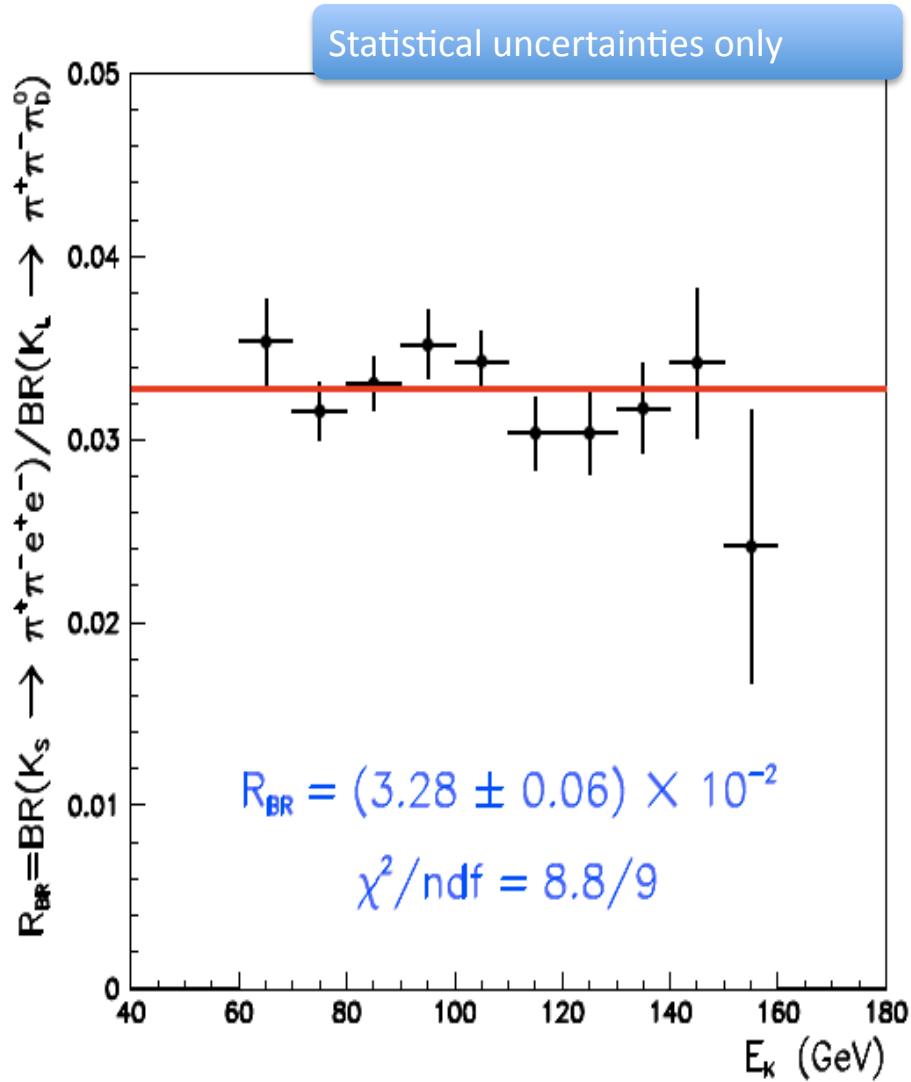
$A_{\pi\pi ee} = 2.804\%$   
 $A_{\pi\pi\pi_D^0} = 1.644\%$

Acceptance



$K_L / K_S$  flux ratio





Source	$\sigma_{syst}$ (%)
$K_L \rightarrow \pi^+ \pi^- \pi^0$ matrix element	$\pm 0.2$
Background subtraction	$\pm 0.1$
Radiative corrections	$\pm 0.4$
Trigger efficiency	$\pm 0.4$
$e - \pi$ separation	$\pm 0.2$
$\pi$ decay	$\pm 0.6$
Beam parameters	$\pm 0.1$
Geometrical cuts	$\pm 0.7$
KL,S lifetimes	$\pm 0.3$
Kinematical cuts	$\pm 0.3$
Reconstruction	$\pm 0.3$
Total	$\pm 1.2$



Assuming no contribution from E1 direct emission:

$$\begin{aligned} \text{BR}(K_S \rightarrow \pi^+\pi^-e^+e^-) / \text{BR}(K_L \rightarrow \pi^+\pi^-\pi^0_D) &= (3.28 \pm 0.06 \text{ stat} \pm 0.04 \text{ syst}) \times 10^{-2} \\ &= (3.28 \pm 0.07) \times 10^{-2} \end{aligned}$$

In agreement with '98 +'99 result

$$(3.12 \pm 0.17) \times 10^{-2}$$

$$\text{BR}(K_S \rightarrow \pi^+\pi^-e^+e^-) = (4.93 \pm 0.14) \times 10^{-5}$$

In agreement with '98 +'99 result

$$(4.69 \pm 0.30) \times 10^{-5}$$

Using

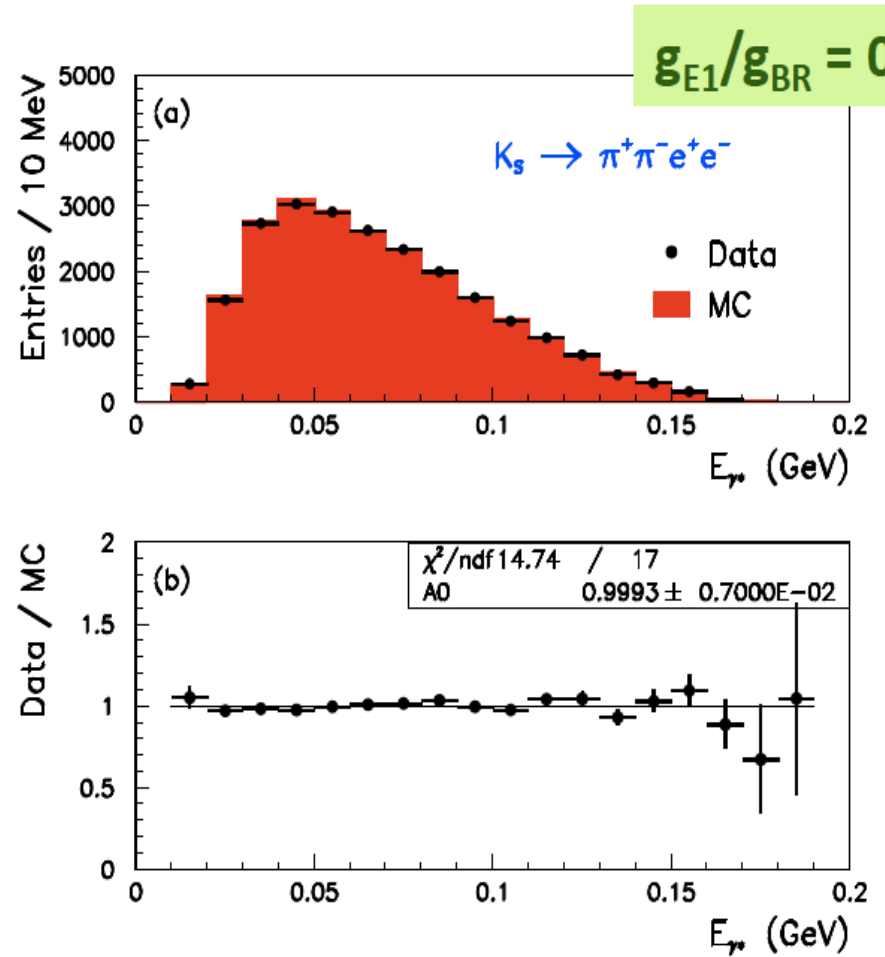
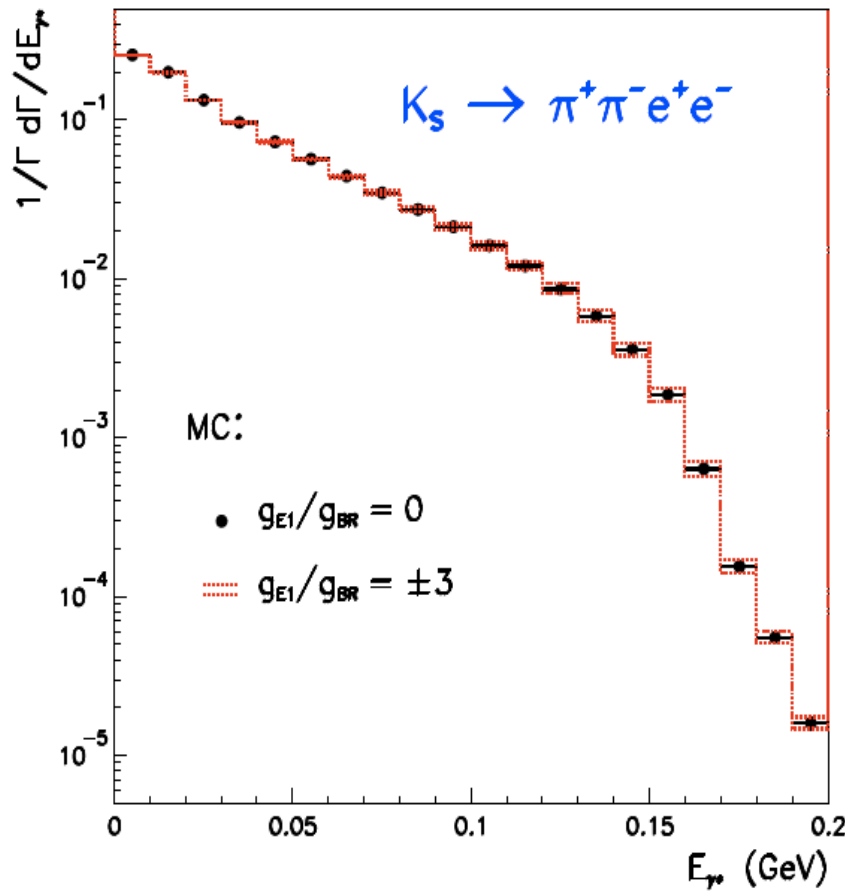
$$\text{BR}(K_L \rightarrow \pi^+\pi^-e^+e^-) / \text{BR}(K_S \rightarrow \pi^+\pi^-e^+e^-) = |\eta_{+-}|^2 (\tau_L / \tau_S):$$

$$\text{BR}(K_L \rightarrow \pi^+\pi^-e^+e^-) = (1.41 \pm 0.04) \times 10^{-7} \quad \text{CP violating part}$$

Consistent with Sehgal and Wanninger ('92)

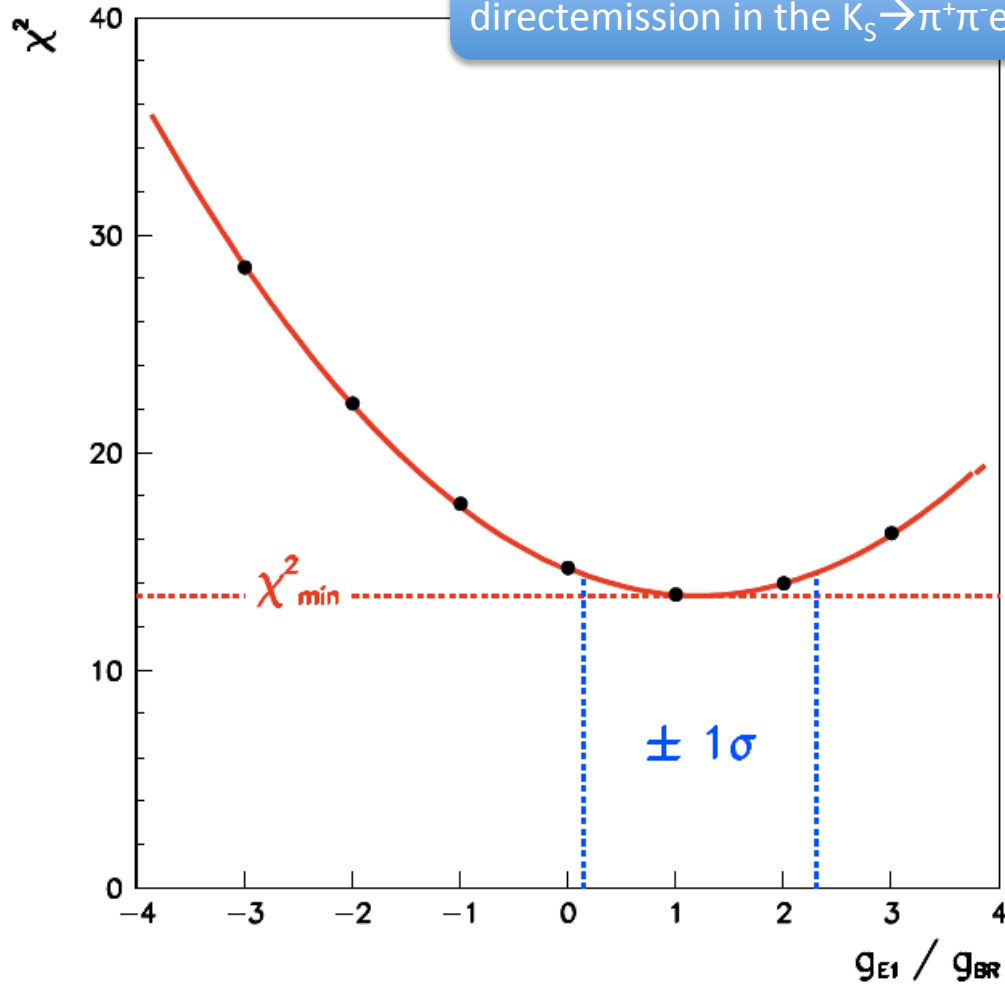
Following the formalism of Sehgal and Winningen ('92)

$$M = e |f_S| \{ g_{BR} e^{i\delta_0} [p_{+\mu}/p_+ \cdot k - p_{-\mu}/p_- \cdot k] + g_{E1} e^{i\delta_1} [(p_- \cdot k) p_{+\mu}] - (p_+ \cdot k) p_{-\mu} \} \{ u(k_-) \gamma^\mu v(k_+) / k^2 \}$$





This result is consistent with no observation of E1 directemission in the  $K_S \rightarrow \pi^+ \pi^- e^+ e^-$  decay



$$g_{E1}/g_{BR} = 1.5 \pm 1.1 \quad (\chi^2/ndf = 12.8/17)$$

$$|g_{E1}|/|g_{BR}| < 3.0 \text{ @ 90\% CL}$$

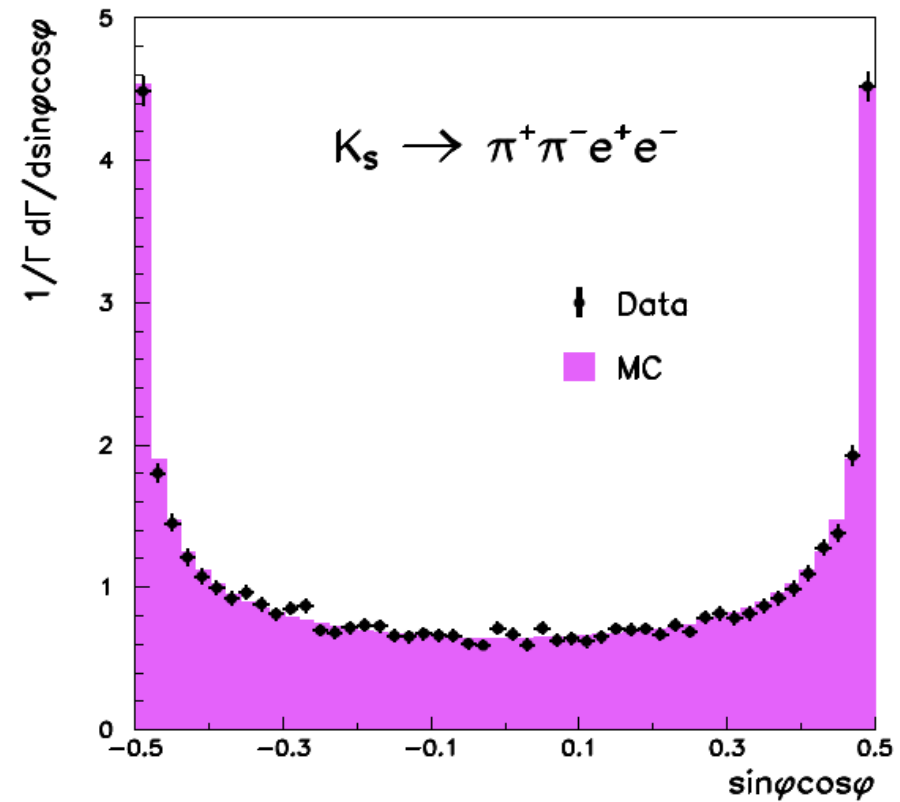
( $\pm 0.8\%$  contribution to BR)

~10 times better than analysis  
by Sehgal and Wanninger ('92)  
of the  $K_S \rightarrow \pi^+ \pi^- \gamma$  mode:  
 $Re(g_{E1}/g_{BR}) = -8 \pm 8$

## Systematical uncertainties

Source	$\sigma_{A\phi}$ (%)
Radiative corrections	$\pm 0.1$
Geometrical cuts	$\pm 0.3$
Kinematical cuts	$\pm 0.2$
$e - \pi$ separation	$\pm 0.1$
Trigger	$\pm 0.1$
$\pi$ decay	$\pm 0.1$
Total	$\pm 0.4$

Largest contributions from  $e^+e^-$  opening angle and inner radii cuts in DCHs and LKr.



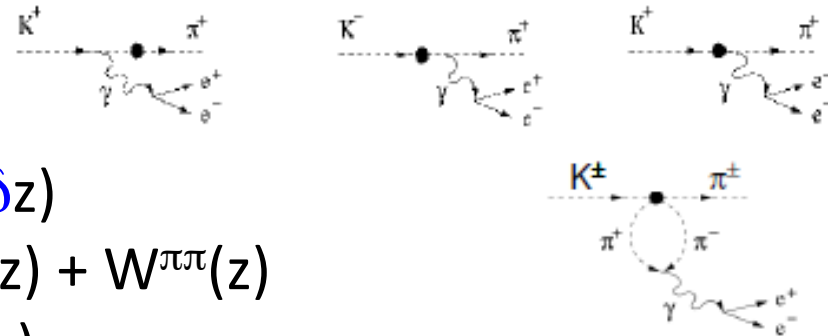
**Result:**  $A\phi = (-0.4 \pm 0.7_{\text{stat}} \pm 0.4_{\text{syst}}) \%$   
 or  $A\phi = (-0.4 \pm 0.8) \%$      $|A\phi| < 1.5 \% @ 90\% \text{ CL}$ ,  
 No evidence for a CP-violating contribution in the  $K_S \rightarrow \pi^+ \pi^- e^+ e^-$  decay amplitude was observed.

# Rare decays with NA48/2

$$d\Gamma_{\pi ee}/dz \sim \rho(z) \cdot |W(z)|^2$$

$z=(M_{ee}/M_K)^2$ ,  $\rho(z)$  phase space factor

- suppressed FCNC processes
- one-photon exchange
- useful test for ChPT



- (1) polynomial:  $W(z) = G_F M_K^2 \cdot f_0 \cdot (1 + \delta z)$
- (2) ChPT  $O(p^6)$ :  $W(z) = G_F M_K^2 \cdot (a_+, b_+, z) + W^{\pi\pi}(z)$
- (3) ChPT, large- $N_c$  QCD:  $W(z) = W(w, \beta, z)$
- (4) Mesonic ChPT:  $W(z) = W(M_a, M_\rho, z)$

- (2) D'Ambrosio et al. JHEP 8 (1998) 4  
 (3) S. Friot et al. PLB 595 (2004) 301  
 (4) Dubnickova et al. hep-ph/0611175

$(f_0, \delta)$  or  $(a_+, b_+)$  or  $(w, \beta)$  or  $(M_a, M_\rho)$  determine a model-dependent BR

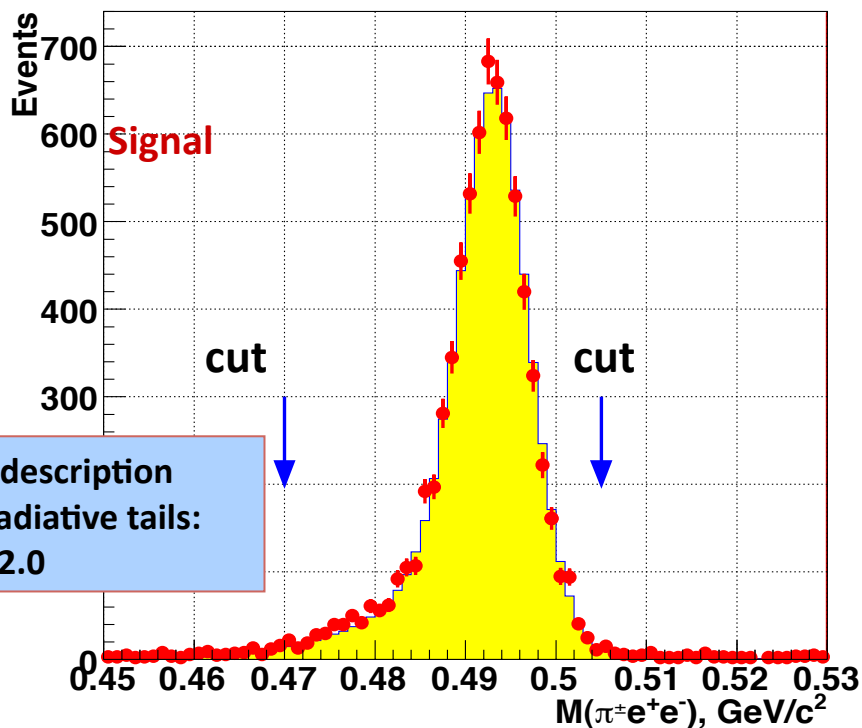
- Parameters of models and BR in full kinematical range
- Model-independent BR ( $z > 0.08$ ) in visible kinematical range
- CPV asymmetry  $\Delta = BR_{K^+} - BR_{K^-} / BR_{K^+}^{16} + BR_{K^-}$   
 (Theory:  $\sim 10^{-5}$  SM;  $\sim 10^{-3}$  SUSY)



Selections of both channels based on very similar conditions: systematics (trigger, PID) in the BR ratio cancel partially

ⓐ  $M_{ee} > 140$  MeV – cut for bg suppression

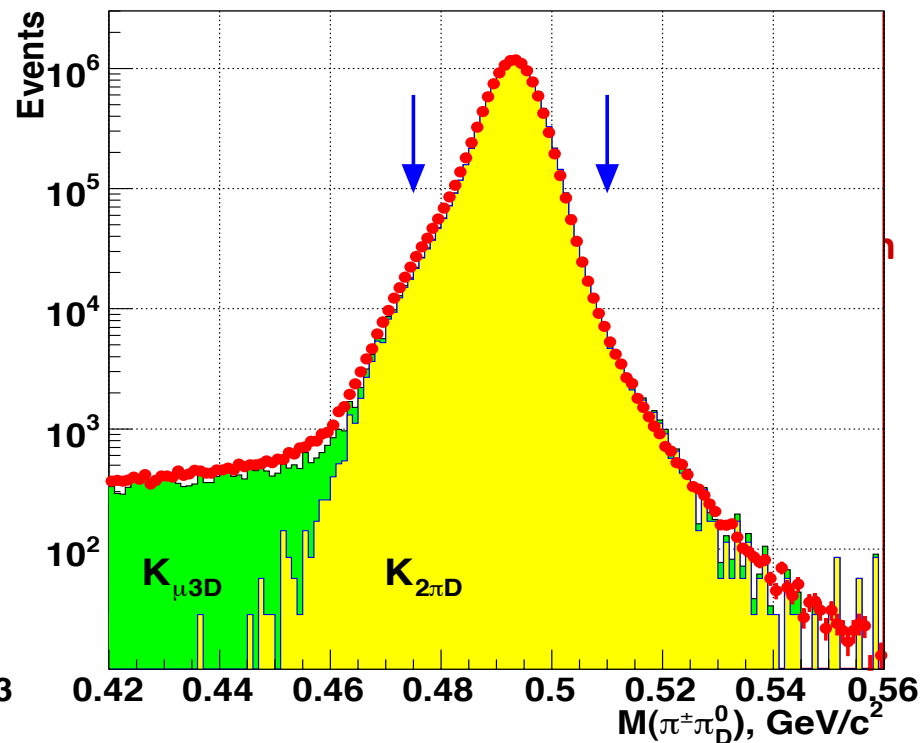
ⓑ Additional  $\gamma$  in the normalisation channel



Perfect description of the radiative tails: Photos 2.0

**7253 candidates**

BG: 71 events estimated with data  
BG/SIG.  $\sim 1.0\%$

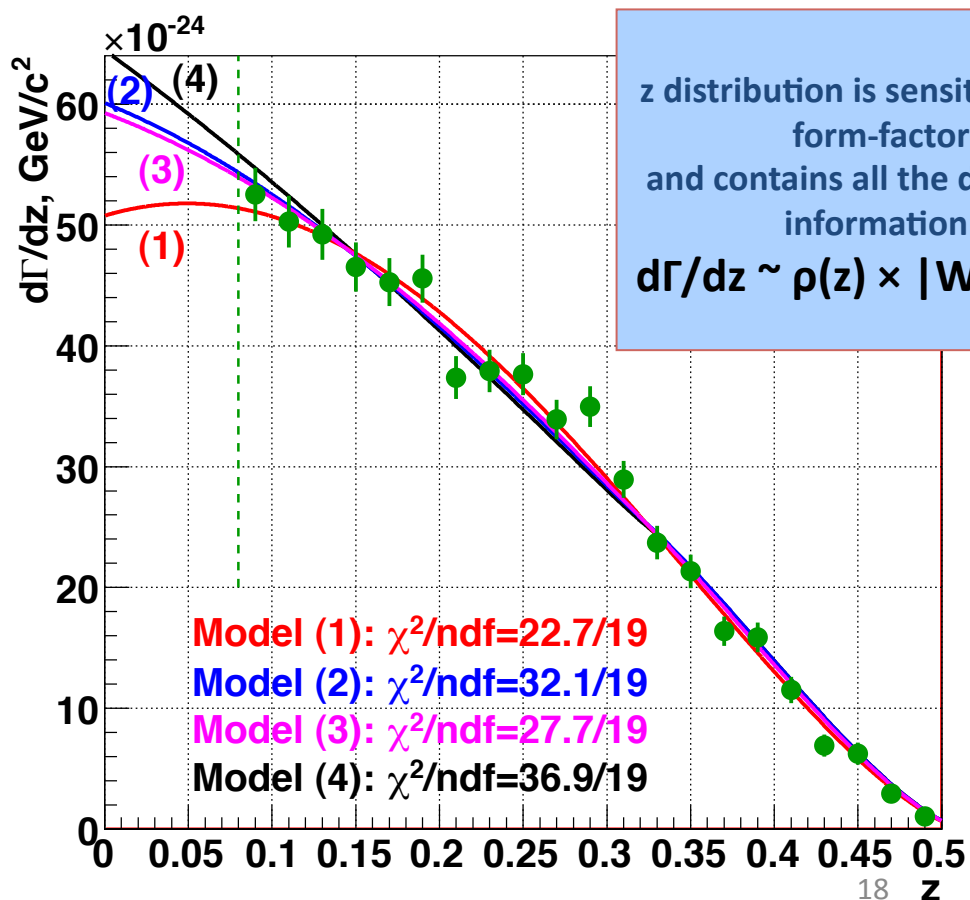


**12.12 M candidates**

BG/Signal  $\sim 0.15\%$   
BG subtracted with MC

## GOALS

- Model-independent BR integrating  $d\Gamma/dz$  in the observable  $z$  region
- Model dependent BRs using fit parameters.
- All models agree reasonably well with data



## Fit results

$$\bar{\delta} = 2.32 \pm 0.18_{\text{stat+syst}}$$

$$|f_0| = 0.531 \pm 0.016_{\text{stat+syst}}$$

$$a_+ = -0.578 \pm 0.016_{\text{stat+syst}}$$

$$b_+ = -0.779 \pm 0.066_{\text{stat+syst}}$$

$$w = 0.057 \pm 0.007_{\text{stat+syst}}$$

$$\beta = 3.45 \pm 0.30_{\text{stat+syst}}$$

$$M_a = 0.974 \pm 0.035_{\text{stat+syst}} \text{ GeV}$$

$$M_\rho = 0.716 \pm 0.014_{\text{stat+syst}} \text{ GeV}$$

## Model independent measurement

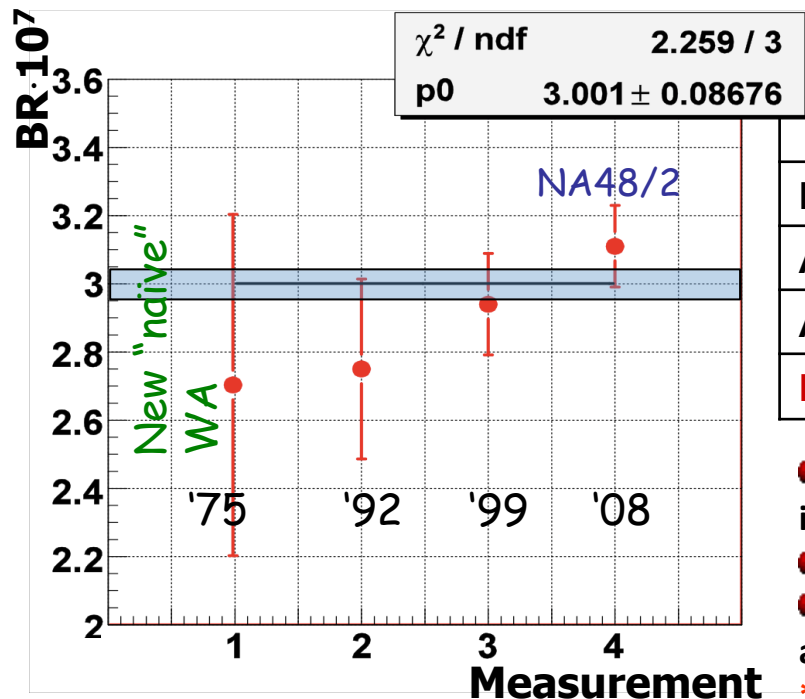
$$BR_{mi} \times 10^7 (M_{ee} > 140 \text{ MeV}/c^2) = 2.28 \pm 0.03_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.06_{\text{ext}} = 2.28 \pm 0.08$$

## Combined result of the 4 models

$$BR = (3.11 \pm 0.04_{\text{stat}} \pm 0.05_{\text{syst}} \pm 0.08_{\text{ext}} \pm 0.07_{\text{model}}) \times 10^{-7} = (3.11 \pm 0.12) \times 10^{-7}$$

## CP violating asymmetry (first measurement! correlated $K^+/K^-$ uncertainties excluded):

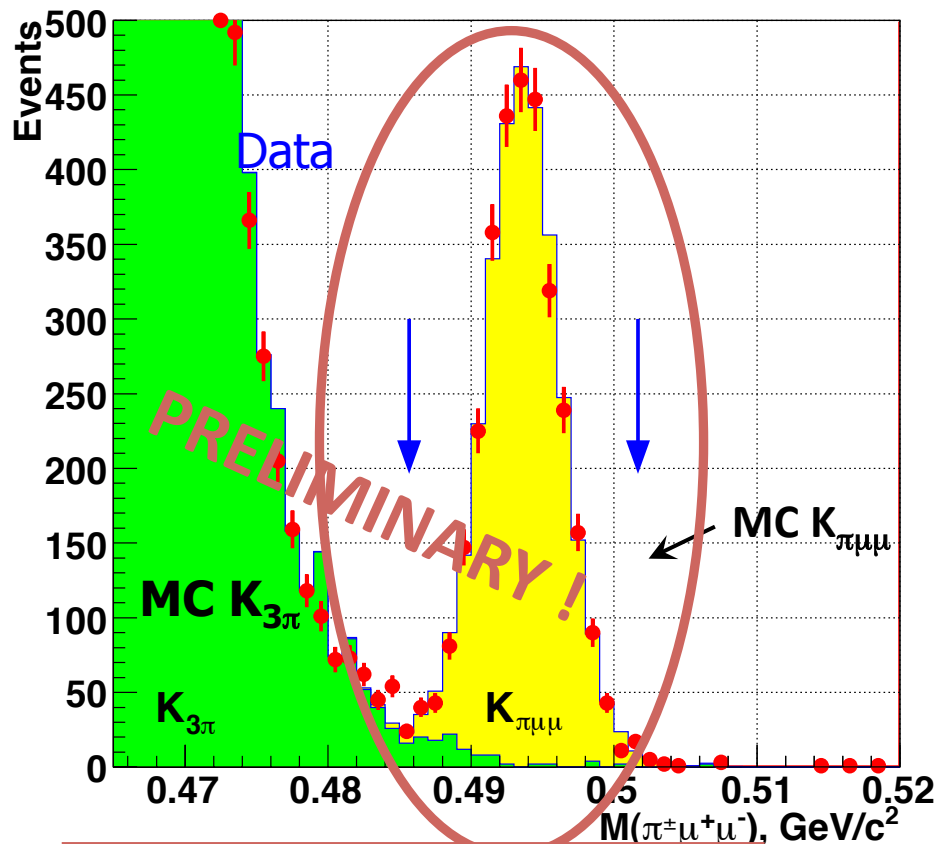
$$\Delta(K_{\pi ee}^{\pm}) = (BR^+ - BR^-) / (BR^+ + BR^-) = (-2.2 \pm 1.5_{\text{stat}} \pm 0.6_{\text{syst}})\%$$



Measurement	events	BR×10 <sup>7</sup>
Bloch et al., PL 56 (1975) B201	(41)	2.70±0.50
Alliegro et al.[E777], PRL 68 (1992) 278	(500)	2.75±0.26
Appel et al. [E865], PRL 83 (1999) 4482	(10000)	2.94±0.15
<b>NA48/2 final (2009)</b>	<b>(7253)</b>	<b>3.11±0.12</b>

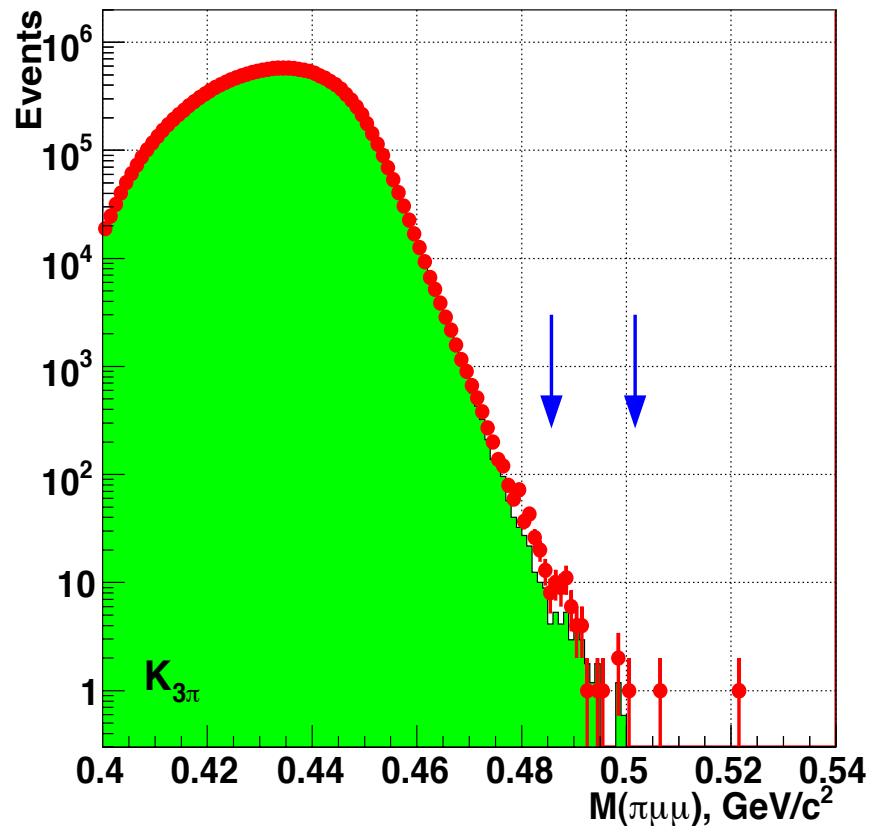
- Form factor measurements for Model 1, 2 and 3\* in agreement with previous measurements
  - Model 4 – never tested before
  - J.Prades, e-Print: arXiv:0707.1789 [hep-ph], predicts (up to its sign)  $a_+ = -(0.6^{+0.6}_{-0.23})$ , in agreement with our result<sub>19</sub>
- \*fit done by the authors of Model 3 using BNL E865 data

Data: Normal  $\mu^+ \mu^-$  candidates



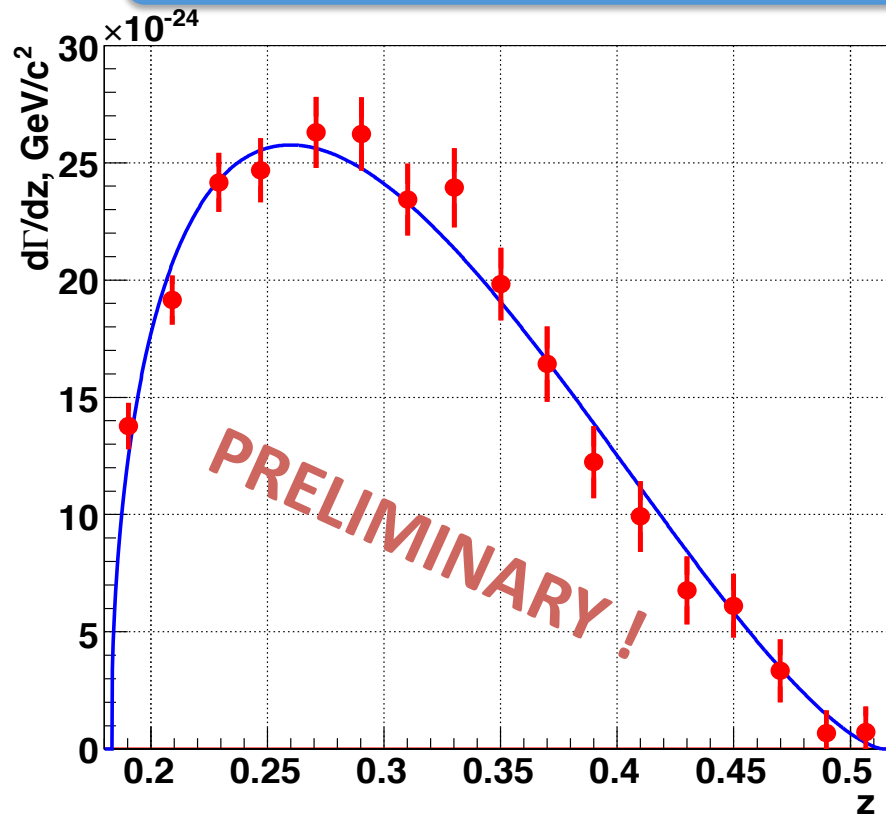
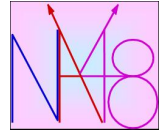
**3120 reconstructed events**  
in the signal region:  
**4 times larger sample than**  
the existing world statistics!

Same sign events



**Good background control**

$$B/(S+B) = (3.3 \pm 0.5_{\text{stat}})\%$$



CPV charge asymmetry:

$$\Delta(K^\pm \rightarrow \pi \mu \mu) = (1.1 \pm 2.3) \times 10^{-2}$$

Forward-backward  
asymmetry:

$$A_{FB} = \frac{N(\cos \theta_{K\mu} > 0) - N(\cos \theta_{K\mu} < 0)}{N(\cos \theta_{K\mu} > 0) + N(\cos \theta_{K\mu} < 0)}$$

where  $\Theta_{K\mu}$  is the angle between the kaon (or pion) and the opposite sign muon in dimuon rest frame.

$$A_{FB} = (-2.4 \pm 1.8) \times 10^{-2}$$

### Linear

$$f_0 = 0.470 \pm 0.039$$

$$\delta = 3.11 \pm 0.56$$

$$\chi^2/\text{ndf} = 12.0/15$$

### ChPT

$$a_+ = -0.575 \pm 0.038$$

$$b_+ = -0.813 \pm 0.142$$

$$\chi^2/\text{ndf} = 14.8/15$$

### ChPT + large- $N_c$ QCD

$$w = 0.064 \pm 0.014$$

$$\beta = 3.77 \pm 0.61$$

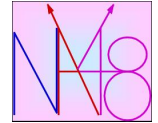
$$\chi^2/\text{ndf} = 13.7/15$$

### “Meson” ChPT

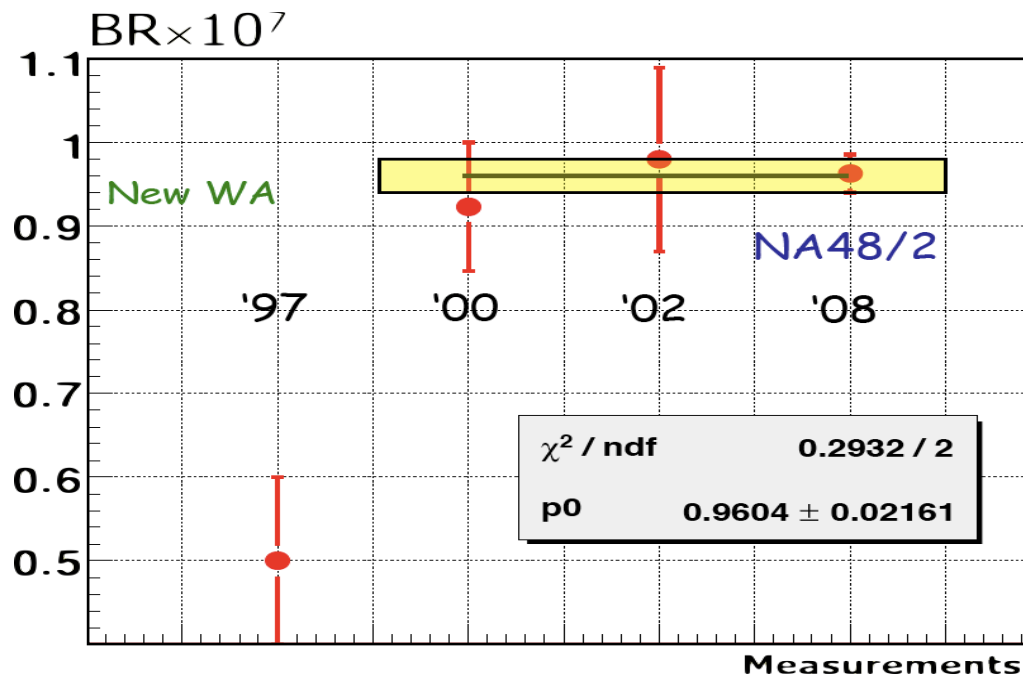
$$M_a = 1.014 \pm 0.090$$

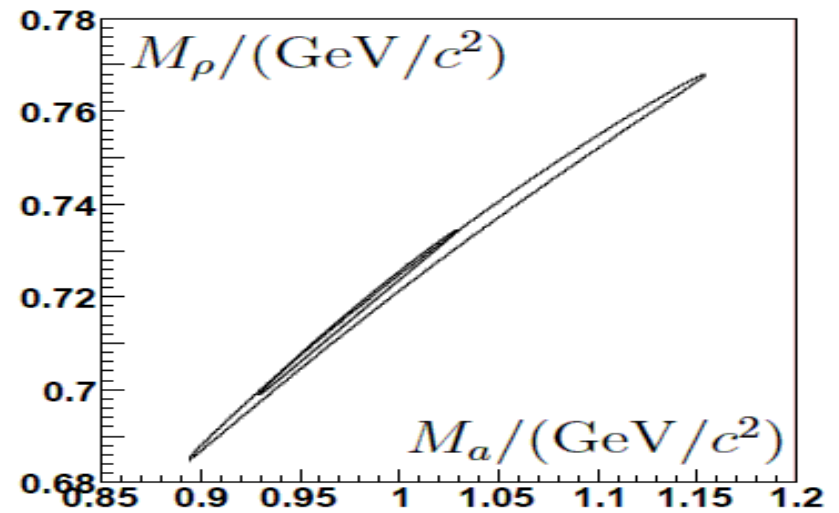
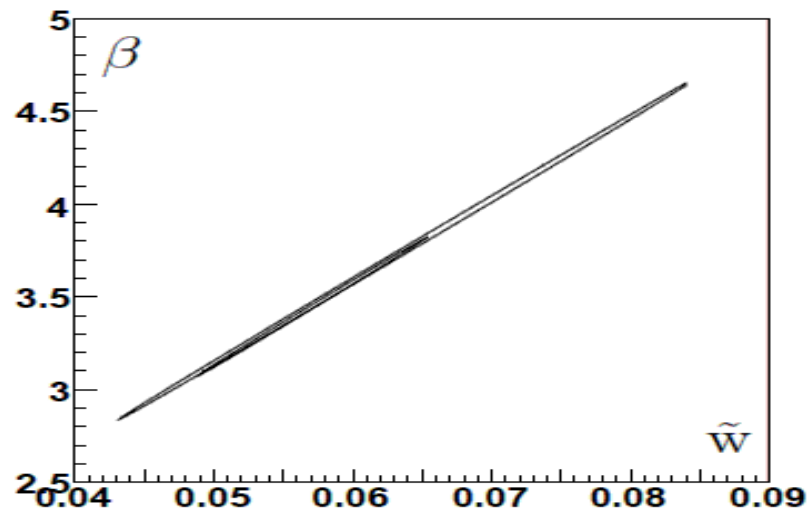
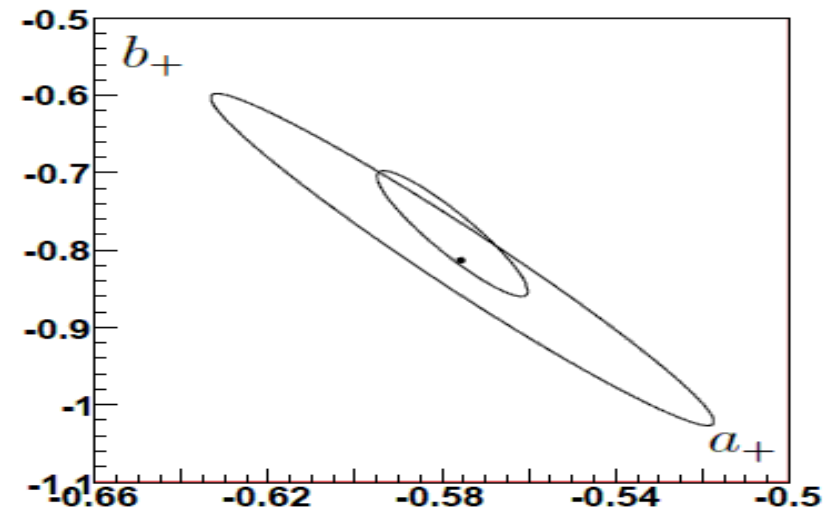
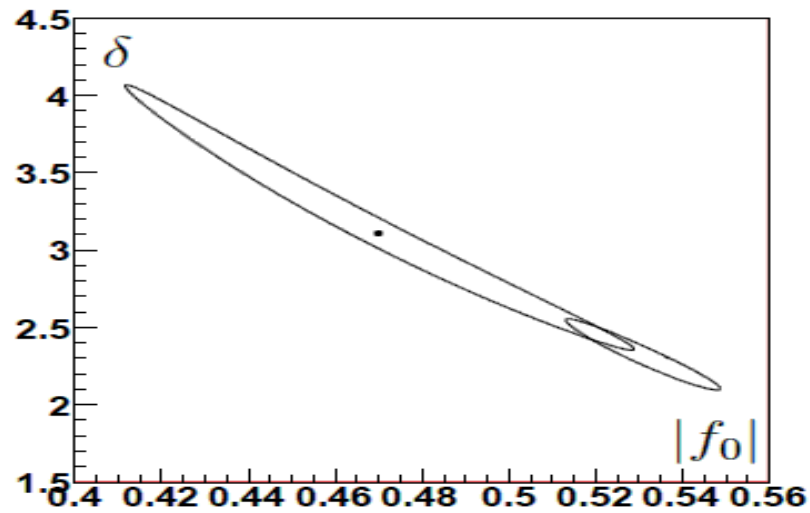
$$M_\rho = 0.725 \pm 0.028$$

$$\chi^2/\text{ndf} = 15.4/15$$



Measurement	events	background	BR $\times 10^8$
Adler et al. [E787], PRL 79 (1997) 2204	207	11%	$5.0 \pm 1.0$
Ma et al. [E865], PRL 84 (2000) 2580	430	6.5%	$9.22 \pm 0.77$
Park et al. [HyperCP], PRL 88 (2002) 111801	110	~3%	$9.8 \pm 1.1$
NA48/2 (present analysis)	3120	3.3%	$9.62 \pm 0.23$





● **Improved measurement of  $BR(K_S \rightarrow \pi^+ \pi^- e^+ e^-) / BR(K_L \rightarrow \pi^+ \pi^- \pi^0)$  and of  $BR(K_S \rightarrow \pi^+ \pi^- e^+ e^-)$  with the 2002 data**

- ⊙ Upper limit on  $g_{E1}/g_{BR}$  obtained
- ⊙  $A_\phi$  asymmetry consistent with zero.  
No CP-violating effect observed in the  $K_S \rightarrow \pi^+ \pi^- e^+ e^-$  decay
- ⊙ All measurements indicate that the  $BR(K_S \rightarrow \pi^+ \pi^- e^+ e^-)$  decay can be well described by the Inner Bremsstrahlung process.
- ⊙ Paper prepared to submit to PLB



● **Precise measurement of  $K^\pm \rightarrow \pi^\pm e^+ e^-$**

- ⊙ Precision comparable with world's best;
- ⊙ **BR** and **form factor measurements** in agreement with ChPT and other measurements;
- ⊙ First limit on **CPV asymmetry**.
- ⊙ Paper published in PLB

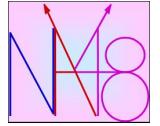
● **Precise measurement of  $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$  - preliminary results**

- ⊙ Four times larger sample than the existing world statistics has been collected
- ⊙ Unprecedented precision achieved. Results in agreement with previous measurements and with NA48/2 results.
- ⊙ Limit on **CPV asymmetry** and forward back asymmetry.
- ⊙ Paper prepared to submit to PLB





BACK UP



# BACK UP SLIDES

Model	Parameter	Statistical	Background	Muon ID	Pion ID	External
(1)	$ f_0 $	0.036	0.014	0	0	0.002
	$\delta$	0.52	0.20	0.01	0	0
(2)	$a_+$	0.034	0.017	0	0.002	0.002
	$b_+$	0.123	0.070	0.005	0.006	0.005
(3)	$\tilde{w}$	0.012	0.007	0	0.001	0
	$\beta$	0.54	0.29	0.02	0.02	0.02
(4)	$M_a/\text{GeV}$	0.070	0.044	0.002	0.001	0.001
	$M_b/\text{GeV}$	0.023	0.014	0.001	0.001	0.001
	$\text{BR} \times 10^8$	0.20	0.04	0.04	0.08	0.07