



New β_s measurement at CDF



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❖ Introduction

- Context
- SM description

❖ The measurement

- Fit strategy
- Signals
- Flavor tagging

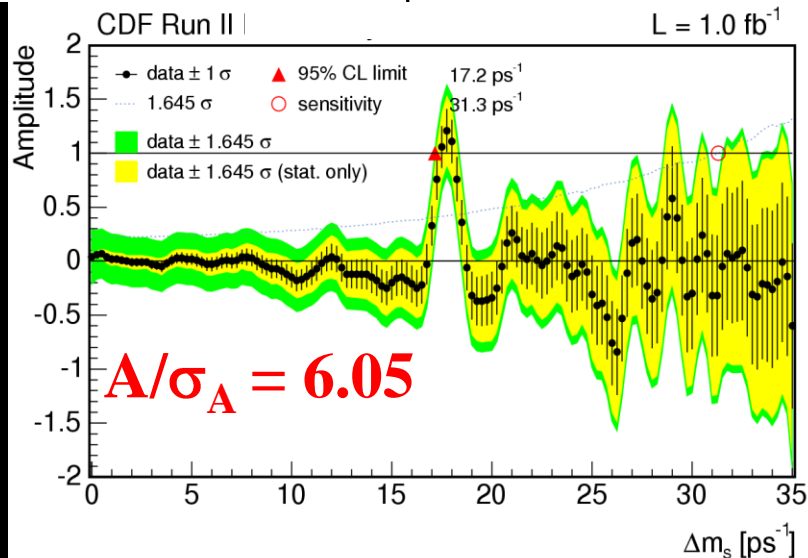
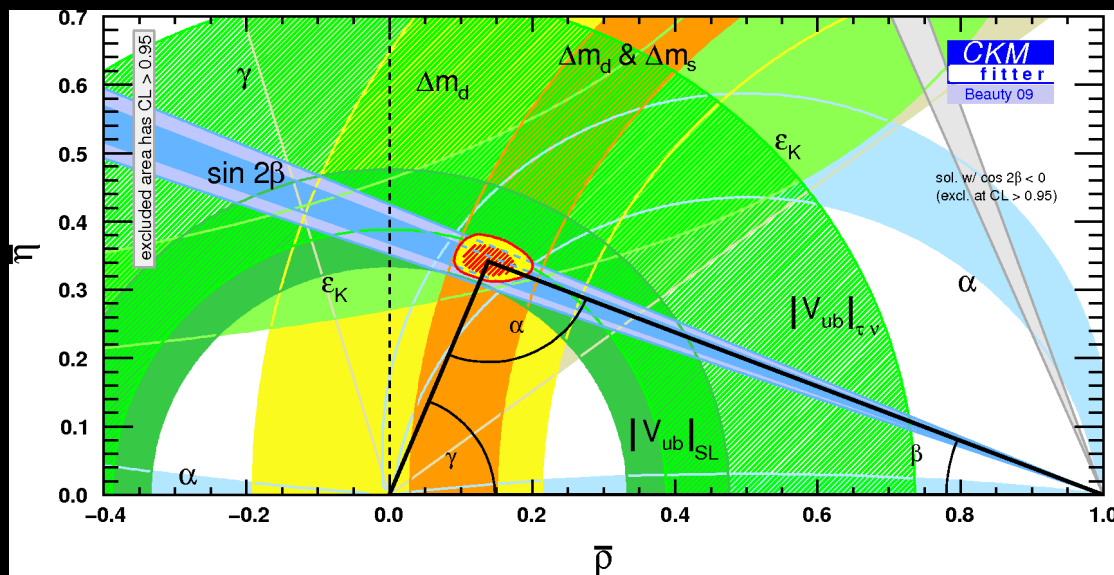
❖ Results

❖ Great SM success in B_d/B_u sector

- Thanks B-factories!
- ...but no evidence for new physics there

❖ B_s sector can still provide surprises

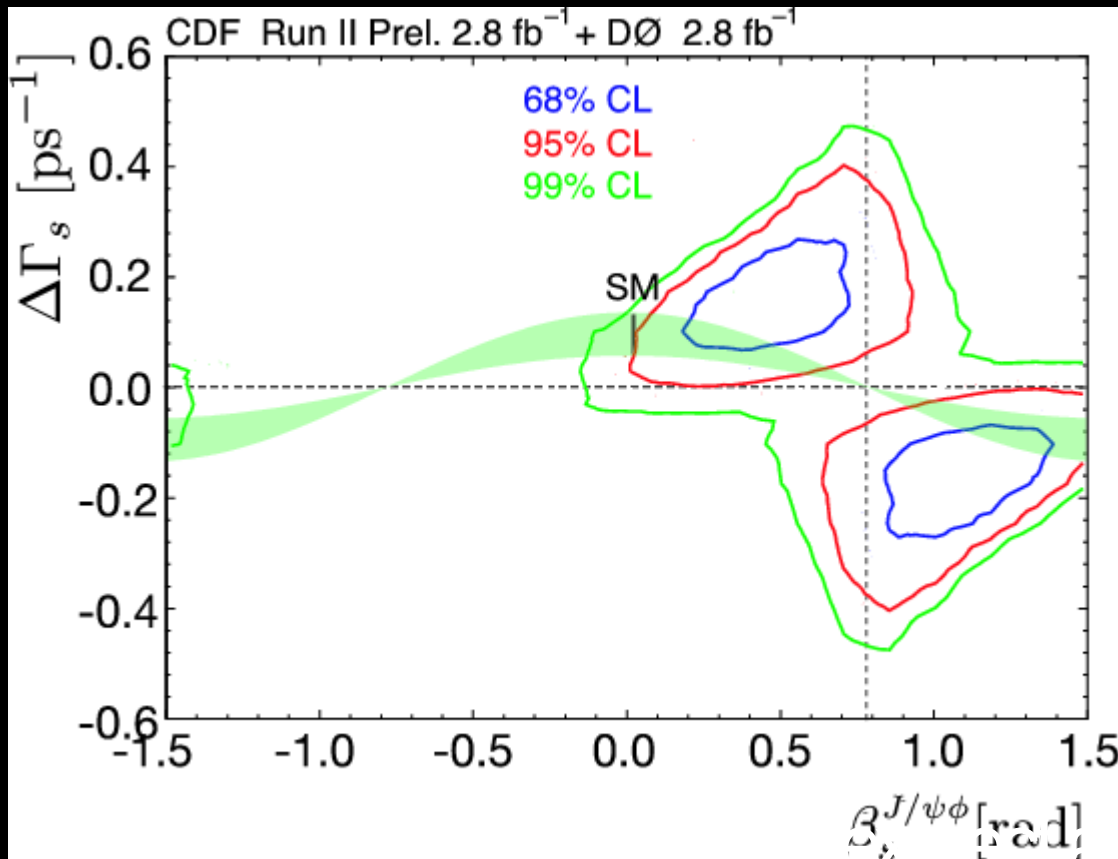
- Natural physics for Tevatron experiments
- In 2006 Δm_s measurement from B_s mixing
 - Right on the SM expectations!
- Next step is measurement of CP violating phases eg. β_s
 - ...some excitement there so far





Status July 2009

❖ Previous CDF+DØ combined results intriguing



2. Deviation from SM expectations



Related measurements

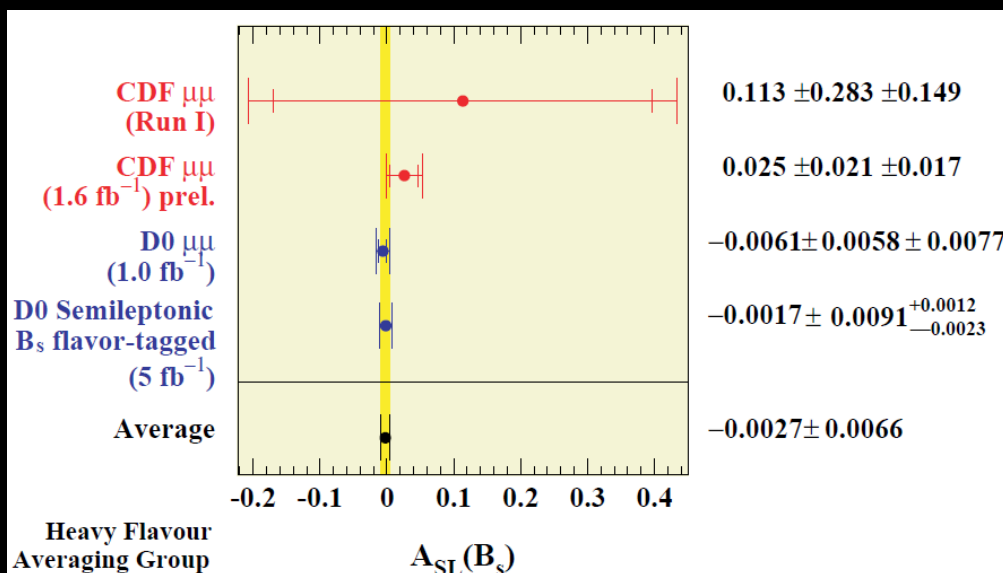


$$a_{sl} = \frac{N_{B\bar{B}}^i - N_{\bar{B}B}}{N_{B\bar{B}} + N_{\bar{B}B}}$$

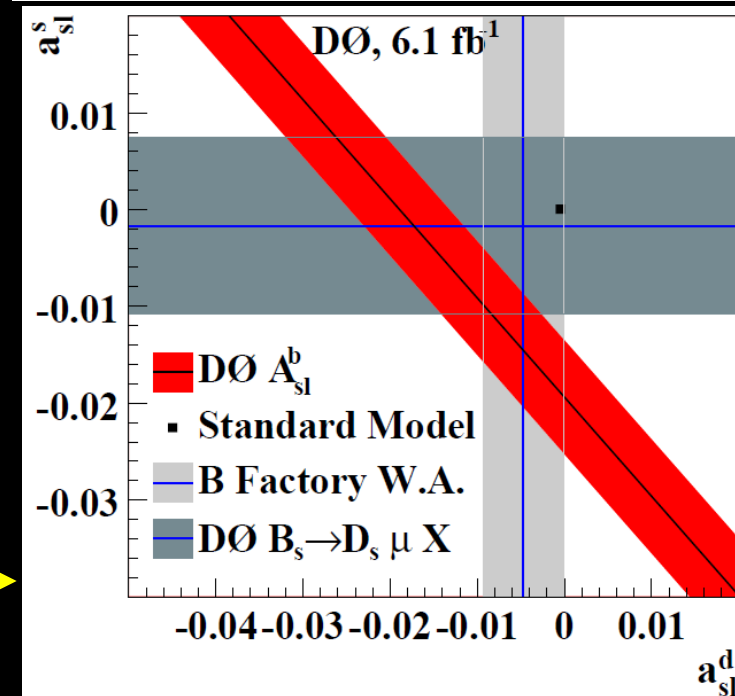
❖ Semileptonic asymmetry

- Related to $\Delta\Gamma$, Δm and β_s
- SM expectation $\sim 10^{-5}$

❖ Old results from CDF and D0:



$$a_{sl}^s = -0.0146 \pm 0.0075$$



❖ Intriguing new D0 result





β_s in SM



❖ β_s is the phase of $-V_{ts}$

- $\neq 0$ in $O(\lambda^4)$ CKM expansion

$$\text{➤ } V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} - \frac{\lambda^4}{8} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda - A^2\lambda^5(\rho + i\eta - \frac{1}{2}) & 1 - \frac{\lambda^2}{2} - (\frac{1}{8} + \frac{A}{2})\lambda^4 & A\lambda^2 \\ A\lambda^3[1 - (\rho + i\eta)(1 - \frac{\lambda^2}{2})] & \text{\textcircled{-}A\lambda^2 - A\lambda^4(\rho + i\eta - \frac{1}{2})} & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix} + \mathcal{O}(\lambda^6)$$

- Quite well constrained assuming SM and very small

CKM fitter. Sept. 2009

$$\beta_s^{SM} = \arg[-V_{ts} \text{\textcircled{V}_{tb}^*} / (V_{cs} V_{cb}^*)] = \mathbf{0.01812 \pm 0.0008}$$

All real

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Basic Theory



❖ 2 state effective theory:

- Describes mixing and CP violation
- M, Γ hermitian
 - CPT invariance: $M_{11} = M_{22}, \Gamma_{11} = \Gamma_{22}$
- After diagonalization:
 - Eigenvalues:

$$i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left(M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

$$M = \begin{pmatrix} m & m_{12} \\ m_{12}^* & m \end{pmatrix}$$

$$\Gamma = \begin{pmatrix} \gamma & \gamma_{12} \\ \gamma_{12}^* & \gamma \end{pmatrix}$$

$$\lambda_{\pm} = (m \pm \Delta m) - \frac{i}{2}(\gamma \pm \Delta \gamma)$$

$$= m - \frac{i}{2}\gamma \pm \sqrt{(m_{12} - \frac{i}{2}\gamma_{12})(m_{12}^* - \frac{i}{2}\gamma_{12}^*)}$$

- Eigenstates:

$$|B_s^H\rangle = p|B_s^0\rangle - q|\bar{B}_s^0\rangle \quad |B_s^L\rangle = p|B_s^0\rangle + q|\bar{B}_s^0\rangle$$

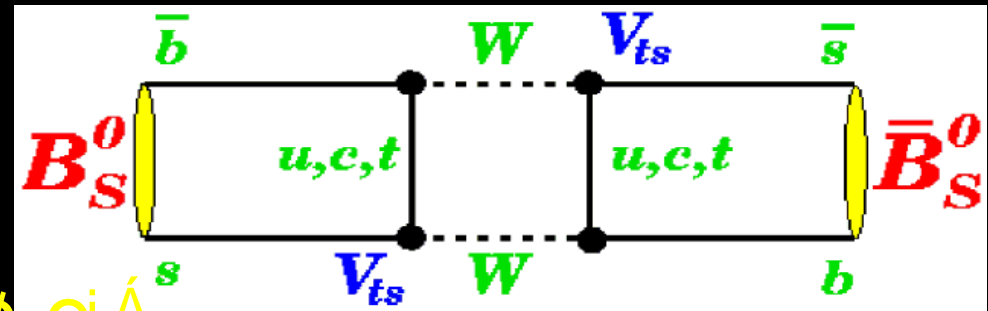
$$q = \sqrt{\frac{1}{2} \frac{m_{12} - \frac{i}{2}\gamma_{12}}{m_{12}^* - \frac{i}{2}\gamma_{12}^*}}$$



Origin of off-diagonal terms

❖ m_{12} from box diagram

- Top quark dominant
- $M_{12} \propto V_{ts}^2 \propto e^{-2i\beta_s}$



❖ New physics possible in loops!

$$M_{12} = M_{12}^{SM} \phi e^{i\Delta_{NP}}$$

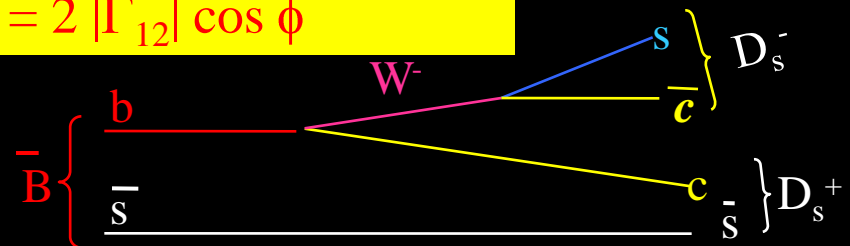
❖ Γ_{12} from common final states

- For B_s dominated by $D_s^+ D_s^-$
 - $\Delta\Gamma/\Gamma \sim 0.10$
 - Γ_{12} mostly real: $\phi_s \sim -2\beta_s$
- Tree level dominated
 - Hard to see new physics here

$$\Gamma_{12} = \sum_f \langle B|f\rangle \rho_f \langle f|\bar{B}\rangle$$

$$\Delta\Gamma = 2\text{Re}\{\Gamma_{12}/m_{12}\} |m_{12}|$$

$$= 2|\Gamma_{12}| \cos\phi$$





Measured quantities

❖ **Mixing frequency (theory limited):**

➤ $\Delta M = 2 |M_{12}|$

❖ **Width difference (statistics limited):**

➤ $\Delta \Gamma = 2 |\Gamma_{12}| \cos \phi$

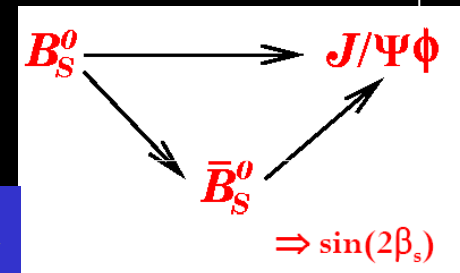
❖ **Semileptonic asymmetry (stat.+syst. limited)**

➤ $A_{SL} = \frac{\text{Im}(M_{12})}{\text{Re}(M_{12})} \sin \phi = \frac{\text{Im}(M_{12})}{\text{Re}(M_{12})} \tan \phi$

❖ **$B_s - \bar{B}_s$ interference in decay to common final state such as $J/\psi \phi$ (statistics limited)**

➤ $-\text{Im}(p/q) \sim \sin(2\beta_s) \sim -\sin \phi$

This measurement





Analysis strategy

Simplified time evolution ($\Delta\Gamma=0$) and $f = \text{CP-eigenstate}$

$$\langle f | jB(t) \rangle = e^{-i\text{Im}t} e^{i\text{Re}t} e^{i\phi} \cos(\phi - \text{Im}t) + i \frac{A_f^{\text{CP-odd}}}{A_f^{\text{CP-even}}} \sin(\phi - \text{Im}t)$$

$$\langle f | j\bar{B}(t) \rangle = e^{-i\text{Im}t} e^{i\text{Re}t} e^{-i\phi} \cos(\phi - \text{Im}t) + i \frac{A_f^{\text{CP-even}}}{A_f^{\text{CP-odd}}} \sin(\phi - \text{Im}t)$$

❖ Study time evolution of $B_s \rightarrow J/\psi\phi$ decay

- No SM weak phases in A_f ! $A_f = 1$
 - Sign depends on CP of final state
- ... but $J/\psi\phi$ is vector-vector \rightarrow mixture of CP-even and CP-odd
 - Need to perform full angular analysis to separate the components
 - $L=0$ and $L=2$ are CP-even, $L=1$ is CP-odd
 - prefer to use “transversity basis”: $A_0, A_{//}$: CP-even, A_{\perp} : CP-odd
 - Phys. Lett. B 369, 144 (1996), 184 - hep-ph/9511363
 - Need to introduce more hadronic decay amplitudes and their phases:
 - $A_0, A_{//}, A_{\perp}$ ($|A_0|^2 + |A_{//}|^2 + |A_{\perp}|^2 = 1$), $\delta_{//}, \delta_{\perp}$ (phases relative to A_0)



Full Bs decay rate formula



$$\frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} \propto |A_0|^2 \mathcal{T}_+ f_1(\vec{\rho}) + |A_{\parallel}|^2 \mathcal{T}_+ f_2(\vec{\rho})$$

$$+ |A_{\perp}|^2 \mathcal{T}_- f_3(\vec{\rho}) + |A_{\parallel}| |A_{\perp}| \mathcal{U}_+ f_4(\vec{\rho})$$

$$+ |A_0| |A_{\parallel}| \cos(\delta_{\parallel}) \mathcal{T}_+ f_5(\vec{\rho})$$

$$+ |A_0| |A_{\perp}| \mathcal{V}_+ f_6(\vec{\rho}),$$

time dependence terms

angular dependence terms

terms with β_s dependence

$$\mathcal{T}_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2)$$

$$\mp \eta \sin(2\beta_s) \sin(\Delta m_s t)],$$

terms with Δm_s dependence present if initial state of B meson (B vs anti-B) is determined (flavor tagged)

$$\mathcal{U}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)]$$

$$\mathcal{V}_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2)].$$

$$\delta_{\parallel} \equiv \text{Arg}(A_{\parallel}(0)A_0^*(0))$$

$$\delta_{\perp} \equiv \text{Arg}(A_{\perp}(0)A_0^*(0))$$

- Identification of **B** flavor at production (flavor tagging) \rightarrow better sensitivity to β_s

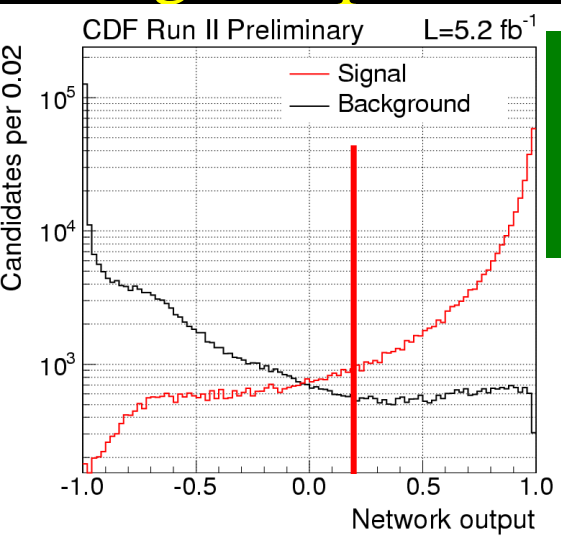


Improvements over past

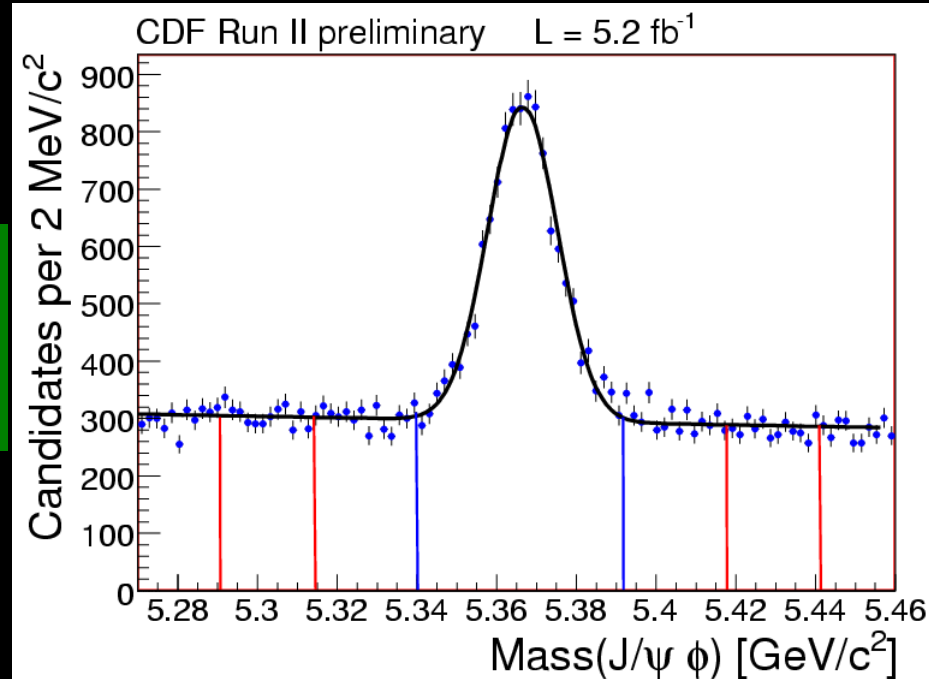


❖ Luminosity: $2.9 \rightarrow 5.2 \text{ fb}^{-1}$

❖ Signal optimization with NN



Optimized for
best β_s
resolution



➤ $\sim 6500 \text{ Bs} \rightarrow \text{J}/\psi\phi$, $S/N \sim 1$

❖ Improved flavor tagging completely recalibrated (see later)

❖ Inclusion of f_0 scalar component ($\text{Bs} \rightarrow \text{J}/\psi f_0$) (see later)

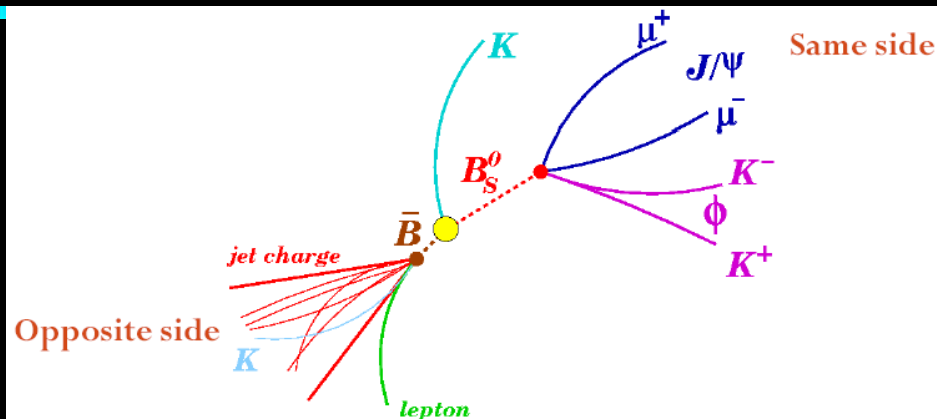


Flavor tagging



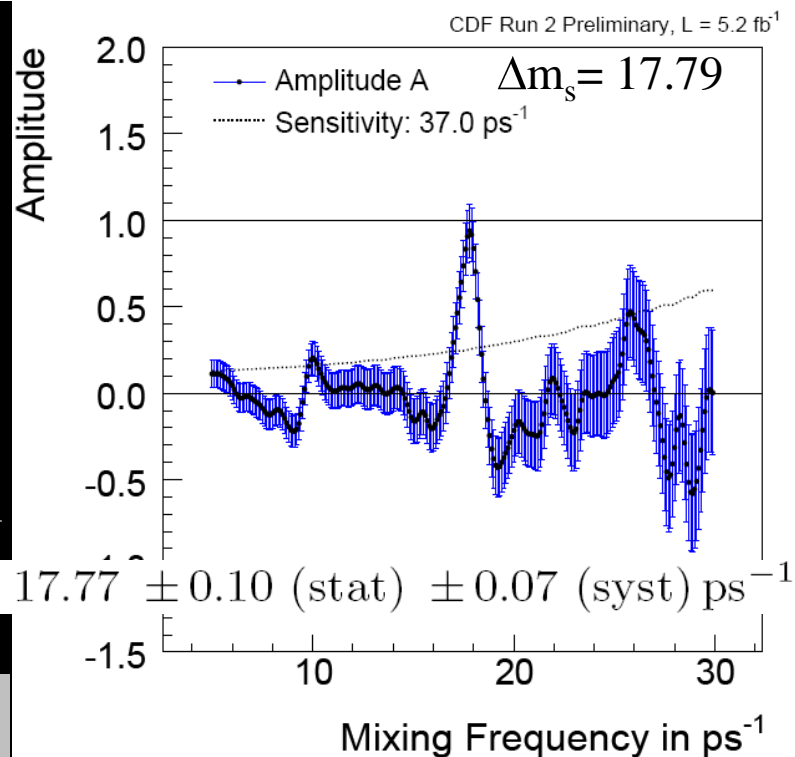
❖ Opposite side (OST)

- Jet / lepton charge
- Combined with NN
- Calibrate with 52,000 $J/\psi K^+$
- $\epsilon = 94.2 \pm 0.4\%$, $D = 11.5 \pm 0.2\%$
- $\epsilon D^2 = 1.2\%$



❖ Same side Kaon (SSKT)

- Sign of soft kaon near B_s
- Dilution from simulation
- Calibrate with $\sim 13,000 B_s \rightarrow D_s(3)\pi$
- From mixing amplitude scan
- $\epsilon D^2 = 3.2 \pm 1.4\%$



Old CDF result



Results: B_s lifetime & $\Delta\Gamma$



❖ Point measurement assuming SM

- Set $\beta_s = 0$
- Most precise measurement of B_s lifetime and $\Delta\Gamma$

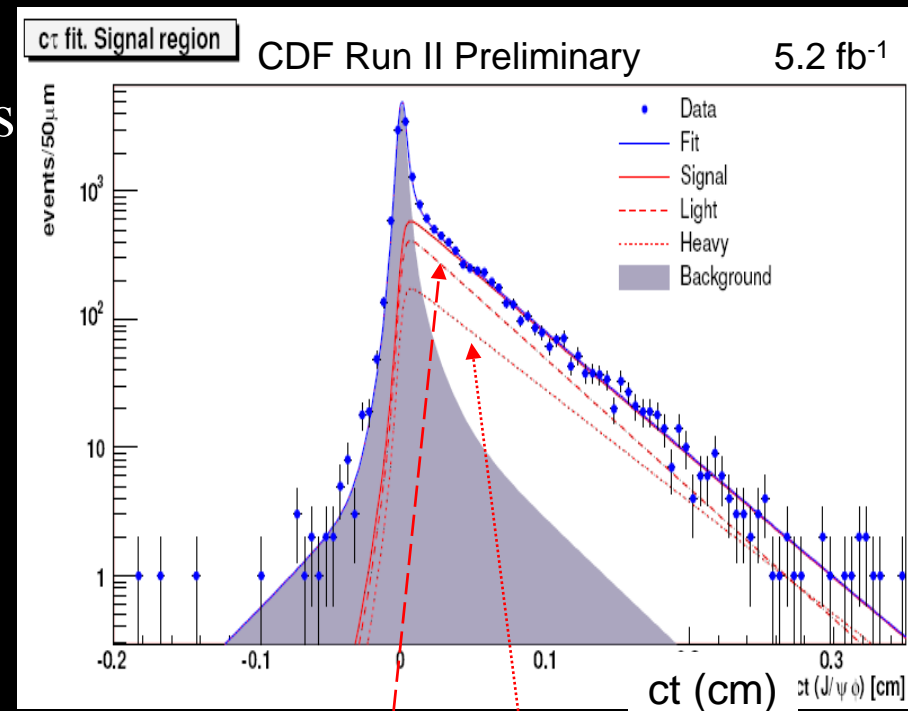
$$\tau_s = 1.53 \pm 0.025 \text{ (stat.)} \pm 0.012 \text{ (syst.) ps}$$

$$\Delta\Gamma = 0.075 \pm 0.035 \text{ (stat.)} \pm 0.01 \text{ (syst.) ps}^{-1}$$

PDG 2009 averages:

$$\tau_s = 1.472^{+0.024}_{-0.026} \text{ ps}$$

$$\Delta\Gamma_s = 0.062^{+0.034}_{-0.037} \text{ ps}^{-1}$$



CP -even (B_s^{light}) and CP -odd (B_s^{heavy}) components have different lifetimes
 $\rightarrow \Delta\Gamma \neq 0$



Results: polarization amplitudes



❖ $\beta_s = 0$ fit

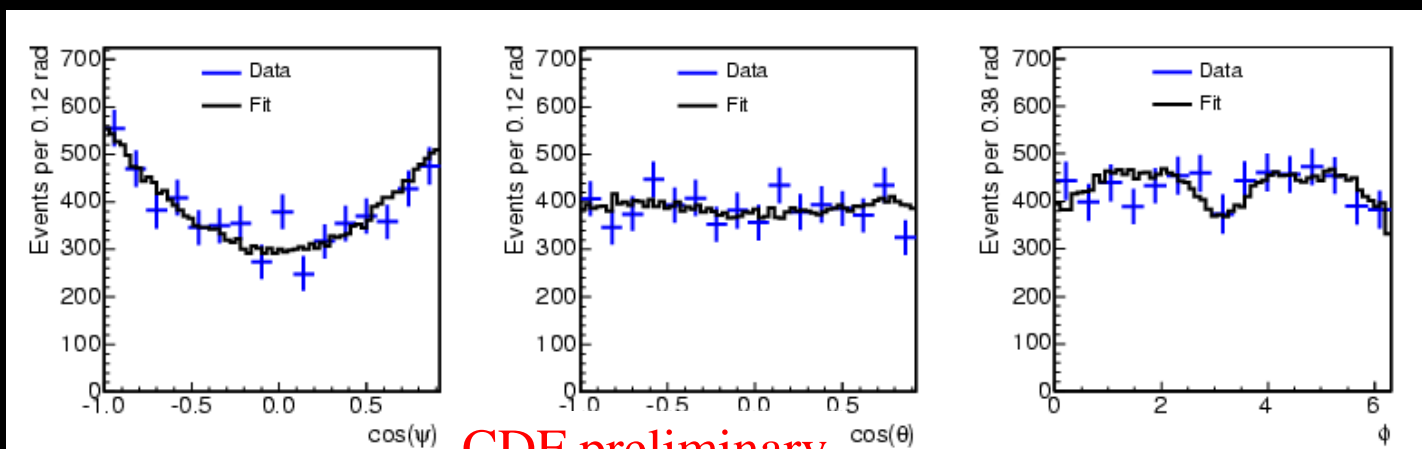
➤ Most precise measurement

$$|A_{\parallel}(0)|^2 = 0.231 \pm 0.014 \text{ (stat)} \pm 0.015 \text{ (syst.)}$$

$$|A_0(0)|^2 = 0.524 \pm 0.013 \text{ (stat)} \pm 0.015 \text{ (syst.)}$$

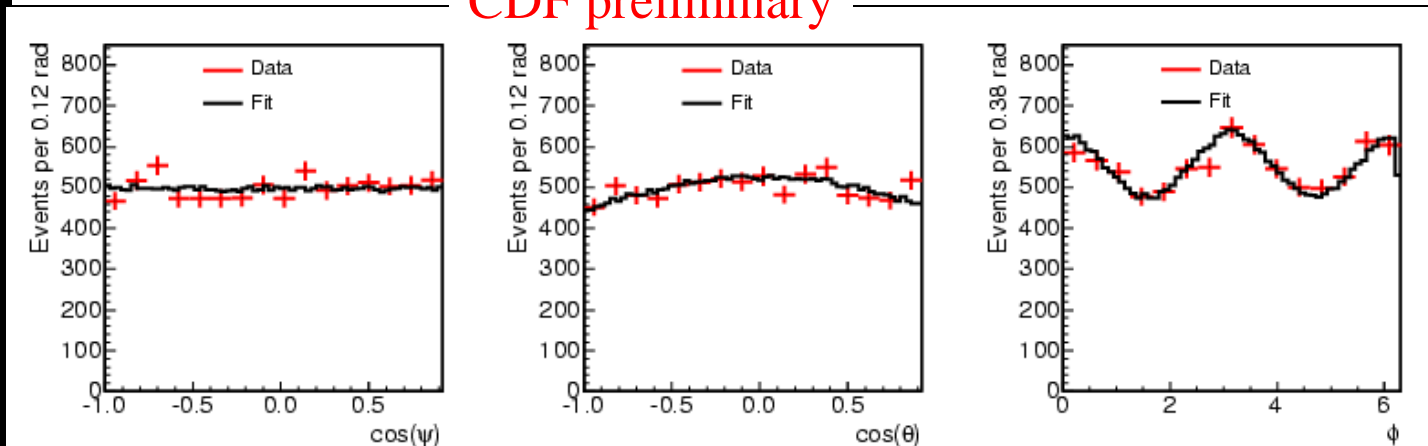
$$\phi_{\perp} = 2.95 \pm 0.64 \text{ (stat)} \pm 0.07 \text{ (syst.)}$$

Signal fit
projection



CDF preliminary

Background fit
projection





CP Violation Phase β_s with 5.2 fb^{-1} at CDF



❖ Full fit results

➤ Low statistics & dilutions

- Some parameters very non-Gaussian, including β_s

➤ Contours corrected for

- Non-gaussian effects
- Systematics

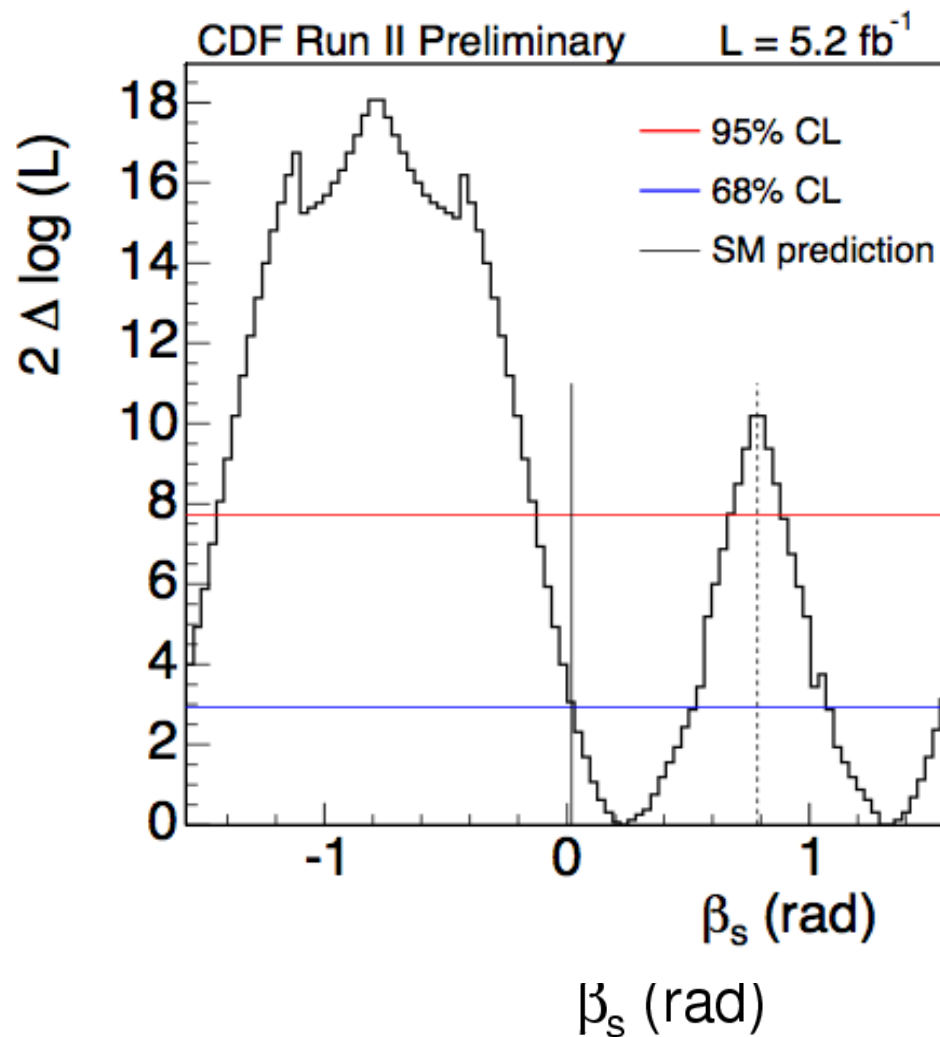
➤ Note fit symmetry

$$2\beta_s \rightarrow \pi - 2\beta_s \quad \Delta\Gamma \rightarrow -\Delta\Gamma$$

$$\delta_{\parallel} \rightarrow 2\pi - \delta_{\parallel}; \quad \delta_{\perp} \rightarrow \pi - \delta_{\perp}$$

❖ β_s projection

- $[0.02, 0.52] \cup [1.08, 1.55]$ at 68% C.L.





Effect of s-wave resonance



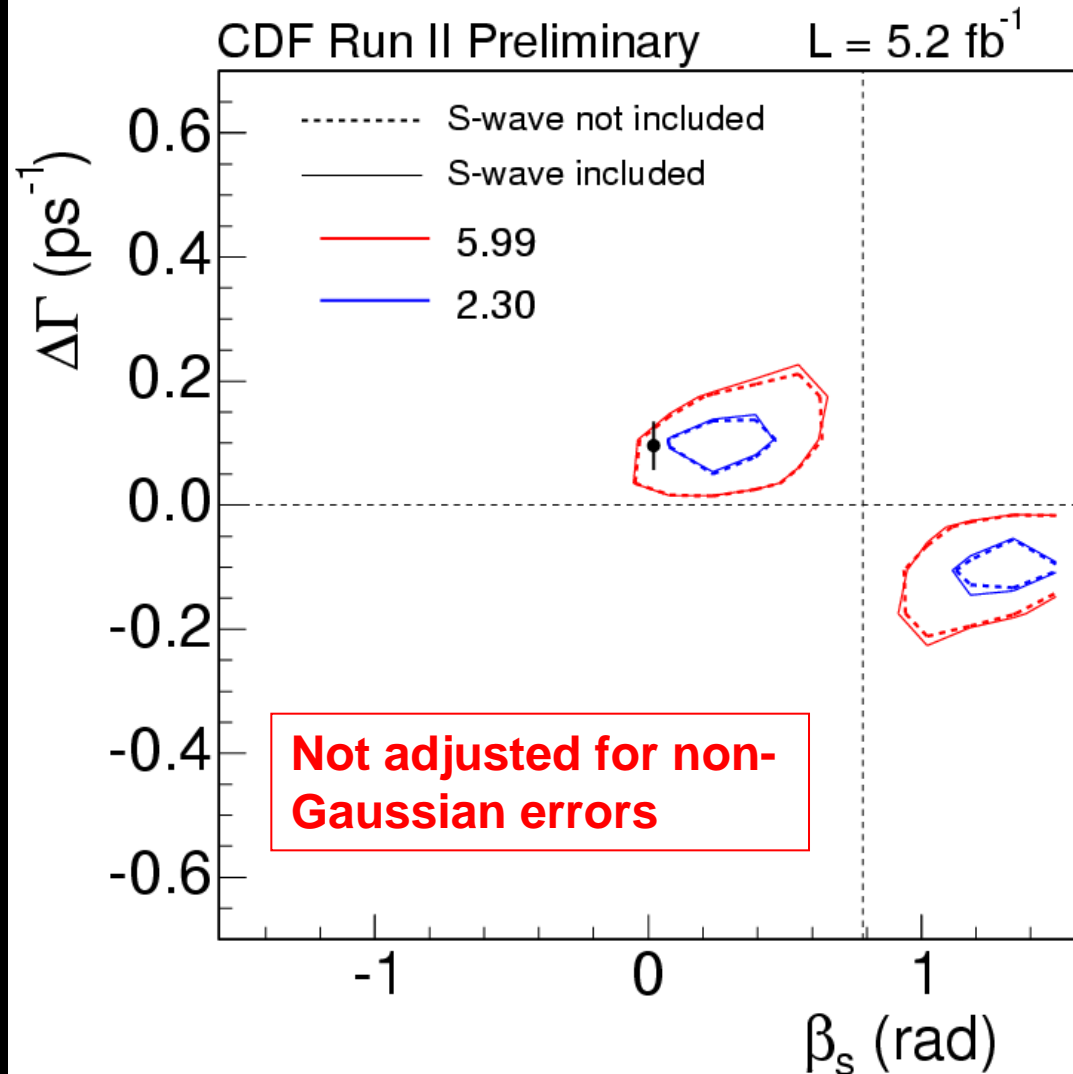
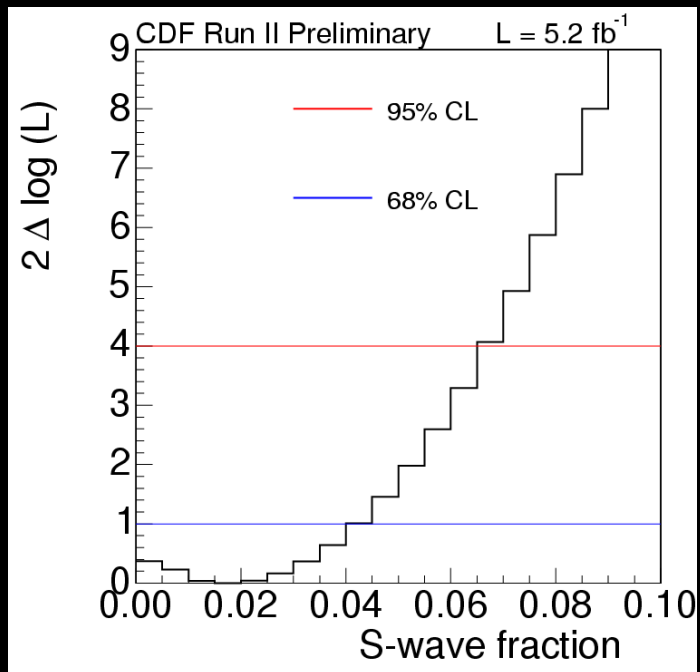
(Suggested in arXiv:0908.3627v1 [hep-ph] 25 Aug 2009)

❖ Effect of $B_s \rightarrow J/\psi f_0$

➤ Fit prefers $\sim 2\%$

■ Consistent with $m(KK)$ fit

■ $< 6.7\%$ @ 95% CL





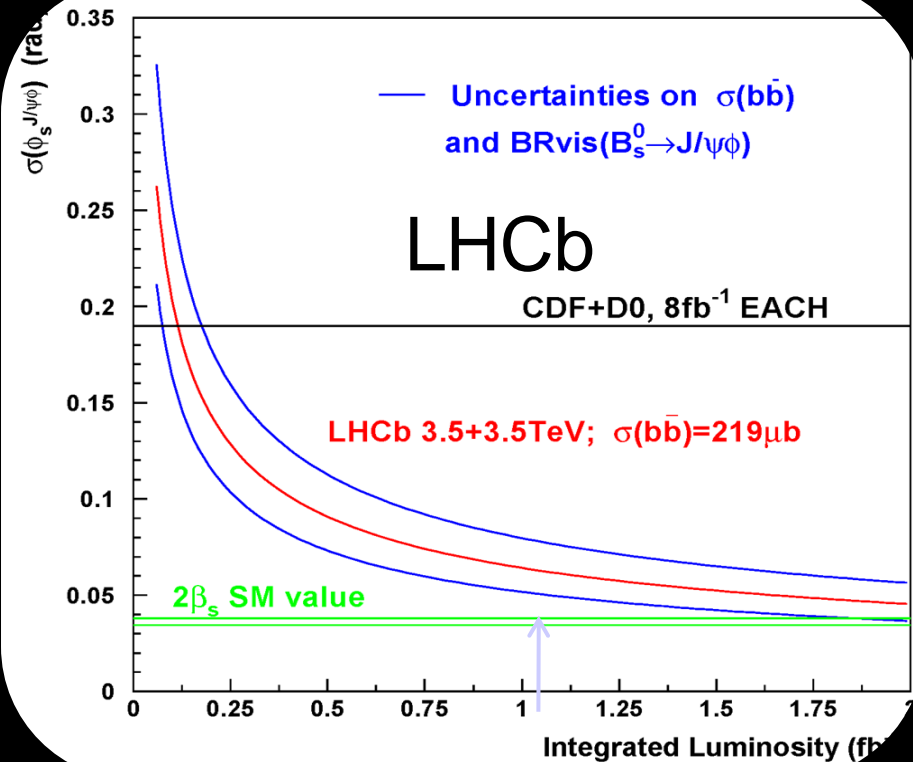
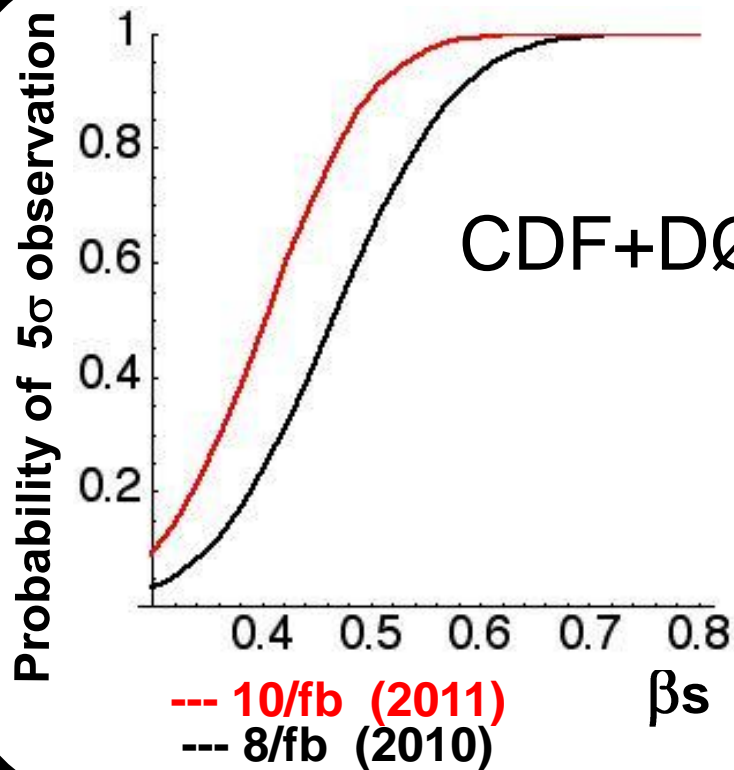
Conclusions & prospects



- ❖ Best measurement of B_s lifetime, $\Delta\Gamma$ and polarization amplitudes
- ❖ Tighter constraints on β_s
 - Improved agreement with SM ($\sim 1\sigma$)
- ❖ Future improvements
 - Statistics doubled (10 fb^{-1}) by end of 2011 Tevatron run
 - More data $\sim 25\text{-}30\%$ from track based triggers
 - Additional decay modes:
 - $\psi(2S)\phi$
 - $J/\psi f_0, f_0 \rightarrow \pi\pi$ (CP-eigenstate)



Getting hot



Tevatron 2011: discover or exclude NP in wide range of phases.

LHCb competitive (if everything turns out as expected)



Backup slides



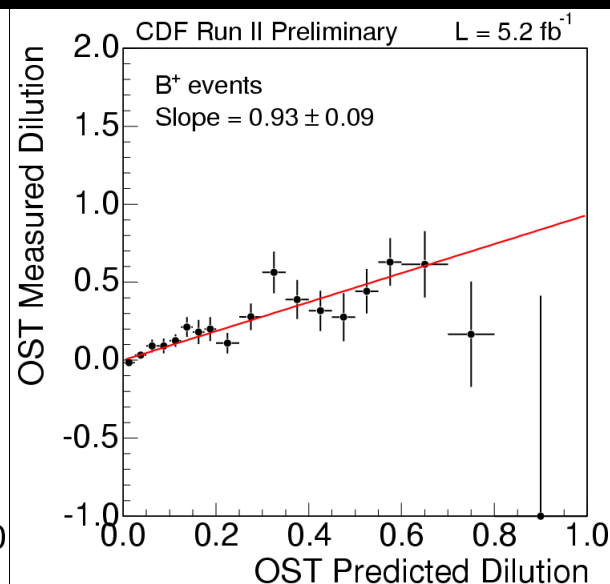
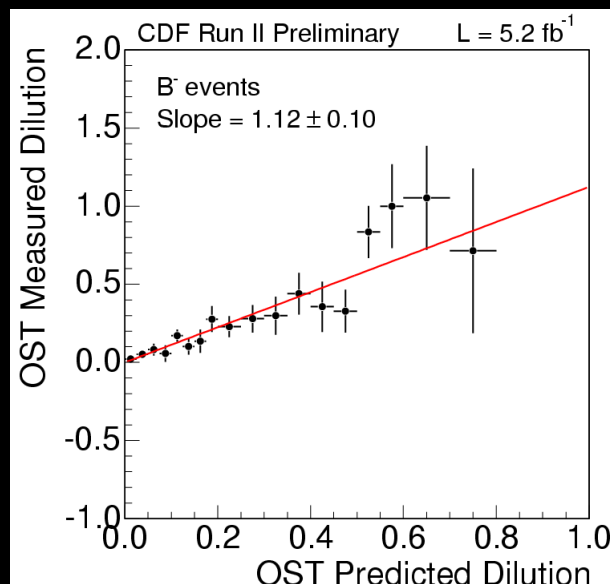
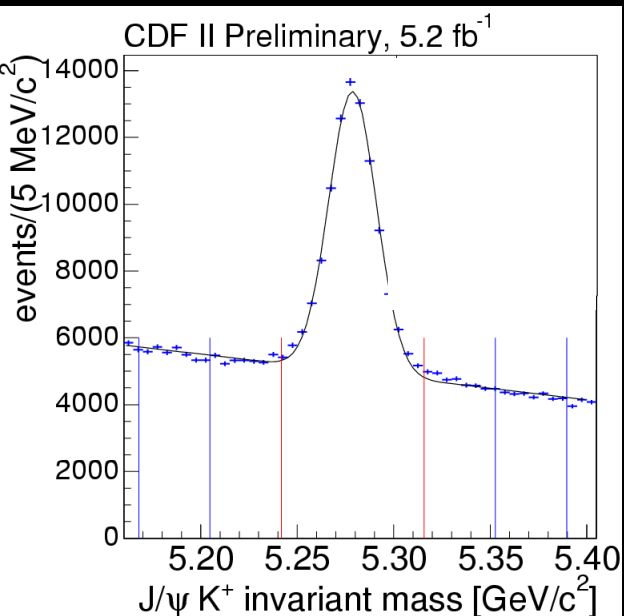
Backup slides



Opposite Side Tagging Calibration and Performance



- OST combines in a NN opposite side lepton and jet charge information
- Initially calibrated using a sample of inclusive semileptonic B decays
 - predicts tagging probability on event-by-event basis
- Re-calibrated using $\approx 52,000 B^{+/-} \rightarrow J/\Psi K^{+/-}$ decays



-OST efficiency = $94.2 \pm 0.4\%$, OST dilution = $11.5 \pm 0.2\%$

- Total tagging power = 1.2%



Same Side Tagging Calibration



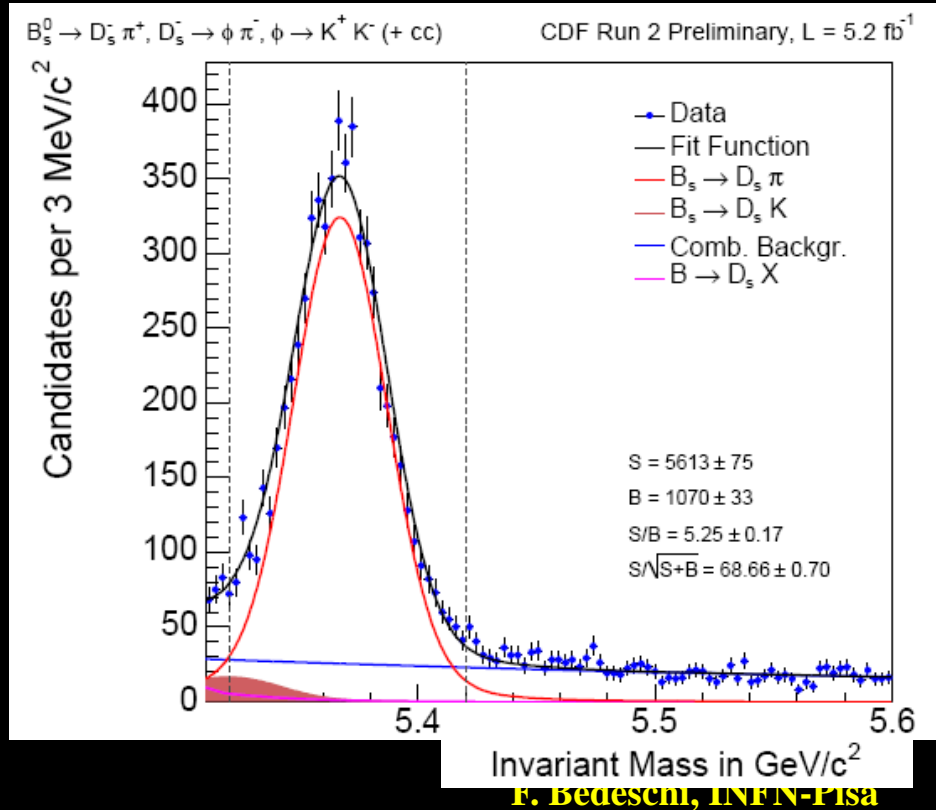
- Event-by-event predicted dilution based on simulation
- Calibrated with 5.2 fb^{-1} of data
- Simultaneously measuring the B_s mixing frequency Δm_s and the dilution scale factor A

$$P_{Sig}(ct|\sigma_{ct}, \xi = \xi_D \cdot \xi_P, D) = \frac{1}{N} \cdot \left[\frac{1}{\tau} e^{-\tilde{t}/\tau} \cdot (1 + \xi AD \cdot \cos(\Delta m_s \tilde{t})) \right] \otimes \mathcal{G}(c\tilde{t}|\sigma_{ct}) \cdot \epsilon(ct|\sigma_{ct})$$

- D – event by event predicted dilution
- ξ – tagging decision = +1, -1, 0 for B_s , B_s and un-tagged events

- Fully reconstructed B_s decays selected by displaced track trigger

Decay Channel	S
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow \phi \pi^-$	5613 ± 75
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow K^* K^-$	2761 ± 53
$B_s^0 \rightarrow D_s^- \pi^+, D_s^- \rightarrow (3\pi)^-$	2652 ± 52
$B_s^0 \rightarrow D_s^- (3\pi)^+, D_s^- \rightarrow \phi \pi^-$	1852 ± 43
Sum	12877 ± 113



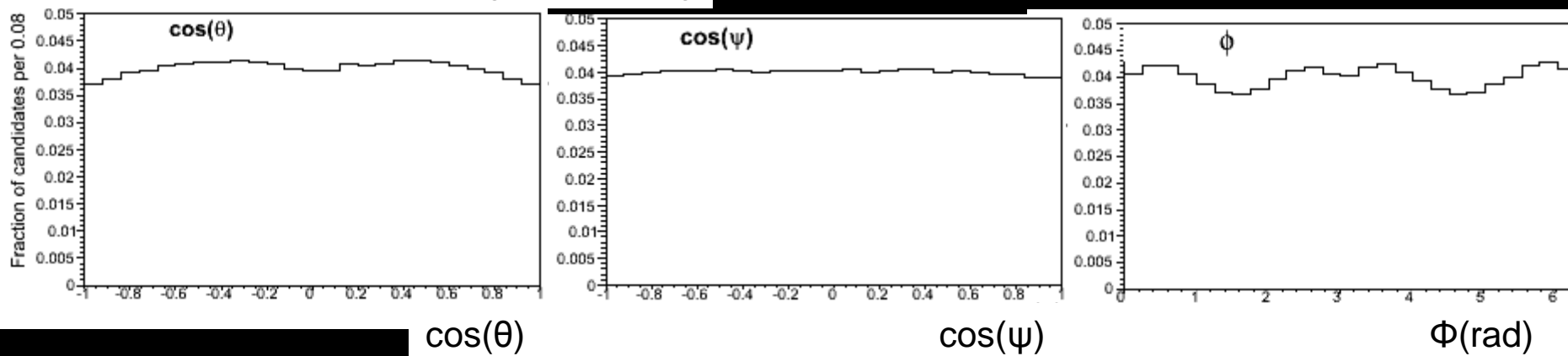


Detector Angular Efficiency



- *CP even* and *CP odd* final states have different angular distributions
 → use angles $r = (\theta, \phi, \psi)$ to statistically separate *CP even* and *CP odd* components
- Detector acceptance distorts the angular distributions
 → determine 3D angular efficiency function from simulation and account for this effect in the fit

CDF Simulation of Detector Angular Sculpting





S-Wave



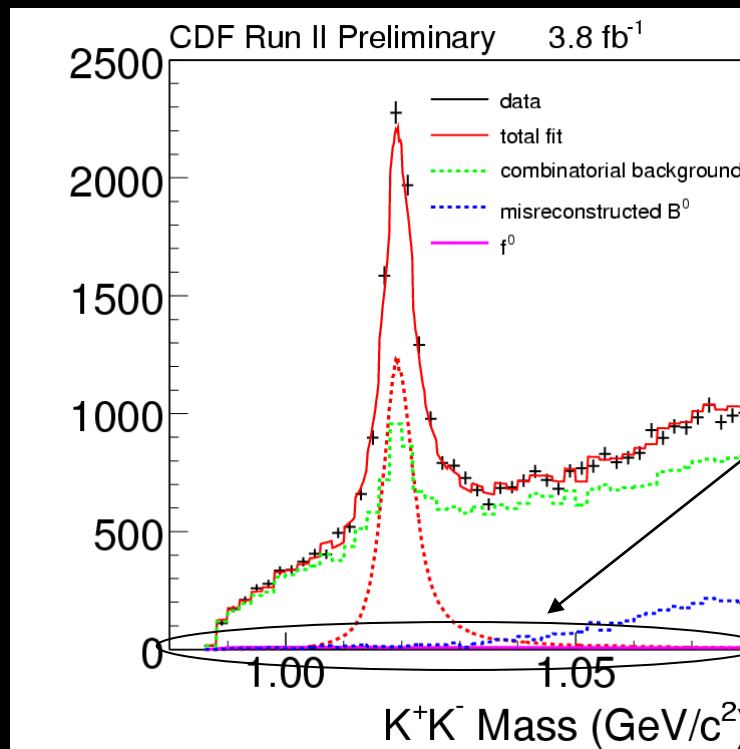
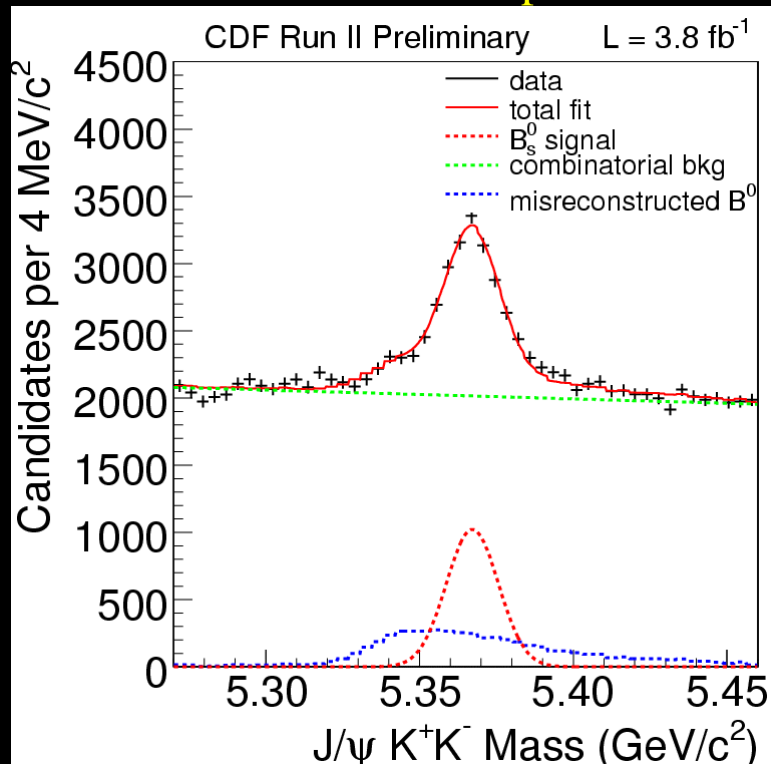
- As noted in arxiv:0812.2832v3, the final state in $B_s \rightarrow J/\Psi KK$ decays can be in an s-wave state with a $\sim 6\%$ contribution in a ± 10 MeV window around the Φ peak
- Systematic effects from neglecting such contribution were first investigated by Clarke *et al* in arxiv:0908.3627v1 where it is shown that:
 - 10% un-accounted s-wave contamination in the Φ region leads to
 - 10% bias in the measured $2b_s$, towards the SM prediction
 - 15% increase in statistical errors
- S-wave contribution can be either non-resonant or from the $f^0(980)$ resonance
- To account for potential s-wave contribution, enhance the likelihood function to account for the s-wave amplitude A_S and interference between s-wave and p-wave
- Time dependence of the s-wave amplitude A_S is *CP-odd*, same as A_{\perp}
- Mass and phase of s-wave component are assumed flat (good approximation in a narrow ± 10 MeV around the Φ mass)



S-Wave Cross Check Using KK Mass Spectrum



- Cross check the result from angular fit by fitting the KK invariant mass spectrum
- From a fit to the B_s mass distribution with wide KK mass range selection (0.980, 1.080 GeV), determine contributions of combinatorial background, mis-reconstructed B^0 , and B_s events
- Good fit of the KK mass spectrum with 2% f^0 contributions



Barely visible
S-wave
component



Non-Gaussian Regime

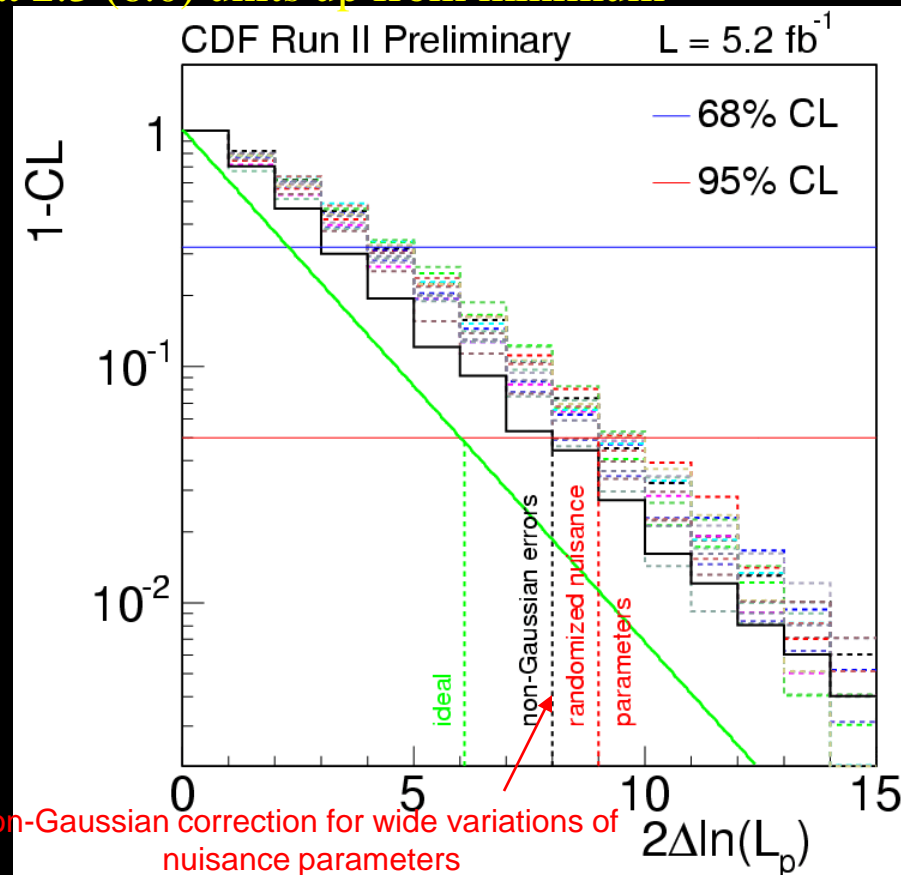
- Pseudo-experiments show that we are still not in perfect Gaussian regime
→ *quote confidence regions instead of point estimates*
- In ideal case (high statistics, Gaussian likelihood), to get the 2D 68% (95%) C.L. regions, take a slice through profiled likelihood at 2.3 (6.0) units up from minimum

- In this analysis integrated likelihood ratio distribution (black histogram) deviates from the ideal χ^2 distribution (green continuous curve)

- Using pseudo-experiments establish a “map” between Confidence Level and $2\Delta\ln(L)$

- All nuisance parameters are randomly varied within $\pm 5\sigma$ from their best fit values and maps of CL vs $2\Delta\ln(L)$ re-derived

- To establish final confidence regions use most conservative case





Systematic Uncertainties



Systematic	$\Delta\Gamma$	$c\tau_s$	$ A_{\parallel}(0) ^2$	$ A_0(0) ^2$	ϕ_{\perp}
Signal efficiency:					
Parameterisation	0.0024	0.96	0.0076	0.008	0.016
MC reweighting	0.0008	0.94	0.0129	0.0129	0.022
Signal mass model	0.0013	0.26	0.0009	0.0011	0.009
Background mass model	0.0009	1.4	0.0004	0.0005	0.004
Resolution model	0.0004	0.69	0.0002	0.0003	0.022
Background lifetime model	0.0036	2.0	0.0007	0.0011	0.058
Background angular distribution:					
Parameterisation	0.0002	0.02	0.0001	0.0001	0.001
$\sigma(c\tau)$ correlation	0.0002	0.14	0.0007	0.0007	0.006
Non-factorisation	0.0001	0.06	0.0004	0.0004	0.003
$B^0 \rightarrow J\psi K^*$ crossfeed	0.0014	0.24	0.0007	0.0010	0.006
SVX alignment	0.0006	2.0	0.0001	0.0002	0.002
Mass error	0.0001	0.58	0.0004	0.0004	0.002
$c\tau$ error	0.0012	0.17	0.0005	0.0007	0.013
Pull bias	0.0028		0.0013	0.0021	
Totals	0.01	3.6	0.015	0.015	0.07