

# Flavor Structures of SUSY models

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SuperB Physics Workshop, Frascati, 03 December 2009

- Introduction
- Example of “scatter plot” study
- Comments on “benchmarks”

## Introduction

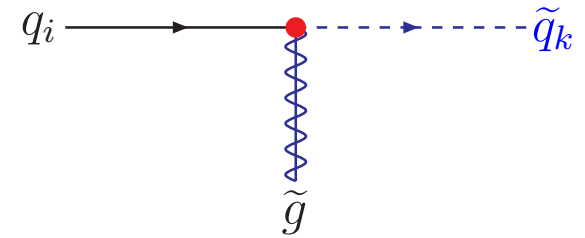
Minimal Supersymmetric Standard Model: a promising candidate for the physics beyond the SM.

MSSM = SM (gauge, Higgs, quarks/leptons, Yukawa)  
+ extra Higgs doublet (type-II at tree level)  
+ Supersymmetry (superpartners, interactions)  
+ soft SUSY breaking ( $> 100$  parameters).

Sources of flavor mixing:

- Yukawa couplings  $\rightarrow$  CKM (as in the SM).
- Soft SUSY breaking terms:
  - ▷ Squark/slepton mass matrices,
  - ▷ Trilinear scalar couplings (“A”-terms).

Mismatch between quark and squark mass bases  
 $\Rightarrow$  flavor mixing in quark–squark–“inos” couplings.



Mass matrices of down-type quarks and squarks:

$$\mathcal{M}_d = Y_D v_1,$$

$$\mathcal{M}_{\tilde{d}}^2 = \begin{pmatrix} m_Q^2 + Y_D^\dagger Y_D v_1^2 + D_{d_L} & A_D^\dagger v_1 - \mu Y_D^\dagger v_2 \\ A_D v_1 - \mu^* Y_D v_2 & m_D^2 + Y_D Y_D^\dagger v_1^2 + D_{d_R} \end{pmatrix}, \quad \begin{array}{l} \leftarrow \tilde{d}_L \\ \leftarrow \tilde{d}_R \end{array}$$

not simultaneously diagonalized *due to the soft SUSY breaking terms*  $m_Q^2$ ,  $m_D^2$  and  $A_D$ .

Studying flavor mixing in the MSSM



Studying structure of soft SUSY breaking terms.

## Model dependent approach

Assume a SUSY model (scenario), where flavor structures are introduced at energy scales higher than the EW scale.

- flavor-blind SUSY breaking (mSUGRA, ...).
- extra Yukawa couplings (GUT,  $\nu_R$ , ...).
- flavor symmetry (controls Yukawa and SUSY breaking), ...



Calculate the MSSM parameters at the EW scale.

- Flavor structures at high energy scales are encoded through RG running.



Evaluate low energy flavor observables and compare with experimental results to obtain constraints/allowed regions in the model parameter space.

## Model independent approach

Parametrize general MSSM at the EW scale.

- Define model independent parameters that characterize flavor mixing of SUSY breaking sector.

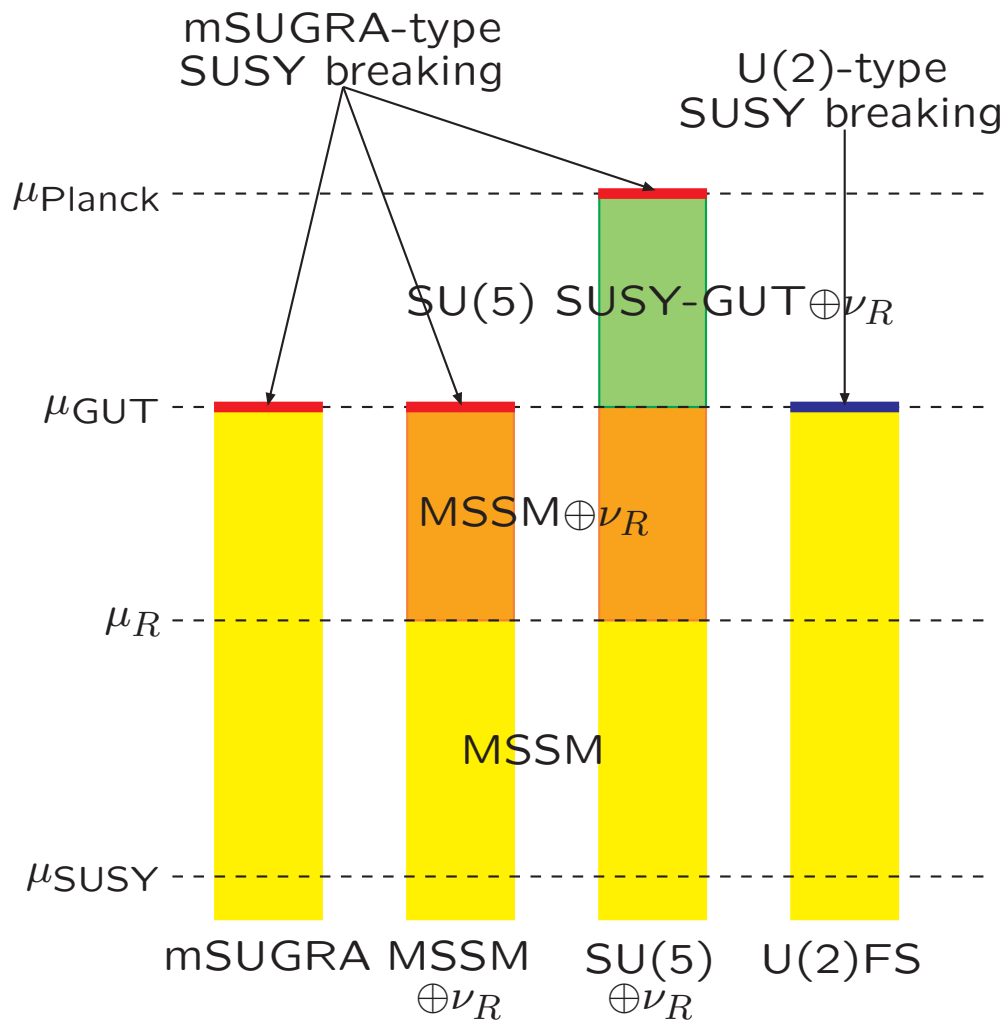


Evaluate low energy flavor observables and compare with experimental results to obtain constraints/allowed regions in the model-independent parameters.

- Computations in “” are the same for both approaches.

# Examples of “model dependent” approach

T. G., Y. Okada, T. Shindou and M. Tanaka, PRD77(2008)095010 [arXiv:0711.2935]



- mSUGRA
  - ▷ Flavor-blind SUSY breaking  $m_0, m_{1/2}, A_0$ .
  - ▷ Source of flavor mixing:  $Y_{U,D}$  ( $V_{\text{CKM}}$ ) only.
- MSSM  $\oplus \nu_R$ 
  - ▷  $\nu_R$  introduced for neutrino masses (seesaw).
  - ▷  $Y_\nu$  affects running  $> \mu_R$ .
  - ▷ GUT: quark  $\Leftrightarrow$  lepton  $> \mu_G$ .
- U(2) flavor symmetry
  - ▷ FS controls Yukawas and SUSY breaking.

## Flavor mixing/CPV source

- $V_{CKM}$  (all cases)  $\Rightarrow \tilde{q}_L$  mixing (running).
  - ▷ Significant in  $B(b \rightarrow s \gamma)$ ,  $\tan \beta$  enhanced corrections.
  - ▷ GUT  $\Rightarrow \tilde{\ell}_R$  mixing (Barbieri-Hall).  $\mathbf{10} = \{q_L, (u_R)^c, (e_R)^c\}$ .
- $Y_\nu$  (cases with  $\nu_R$ 's)  $\Rightarrow \tilde{\ell}_L$  mixing (running above  $\mu_R$ ).
  - ▷ GUT  $\Rightarrow \tilde{d}_R$  mixing (Moroi)  $\bar{\mathbf{5}} = \{(d_R)^c, \ell_L\}$ .
- $m_{Q,U,D}^2(\mu_{GUT})$  (U(2)FS).
  - ▷ U(2) structure neglected in (s)lepton sector.
- SUSY CPV phases ( $\phi_A, \phi_\mu, \dots$ ).
  - ▷ Affect CP asymmetries in  $b$  decays, EDMs ( $e, n, \text{Hg}$ ).

## U(2) flavor symmetry model

[Barbieri, Hall and Romanino, PLB401(1997)47]

Motivation: to explain

- hierarchical structure of quark masses and CKM matrix,
- degeneracy of 1st and 2nd generation squarks (in order to suppress SUSY contributions to  $K - \bar{K}$  mixing).

Assumptions:

- Transformation properties under FS:
  - ▷ 1st and 2nd generations  $\Rightarrow$  doublets of U(2).
  - ▷ 3rd generation and Higgs  $\Rightarrow$  singlet of U(2).
- Two-stage flavor symmetry breaking:
  - ▷ U(2)  $\xrightarrow{\epsilon}$  U(1)  $\xrightarrow{\epsilon'}$  no symmetry.

$$Y_q \approx y_q \begin{pmatrix} 0 & a_q \epsilon' & 0 \\ -a_q \epsilon' & d_q \epsilon & b_q \epsilon \\ 0 & c_q \epsilon & 1 \end{pmatrix}, \quad m_{\tilde{q}}^2 \approx m_{\tilde{q}}^2 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 + r_{22}^{\tilde{q}} \epsilon^2 & r_{23}^{\tilde{q}} \epsilon \\ 0 & r_{23}^{\tilde{q}*} \epsilon & r_{33}^{\tilde{q}} \end{pmatrix}.$$

$$V_{cb} = O(\epsilon), \quad V_{us} = O(\epsilon'/\epsilon).$$



Three flavon fields are introduced:

$$\Phi^i, \quad S^{ij} = S^{ji}, \quad A^{ij} = -A^{ji}, \quad i, j = 1, 2.$$

U(2) symmetric superpotential for Yukawas:

$$\begin{aligned} W_{U(2)} = & y_U \left( U_3^c Q_3 H_2 + \frac{b_U}{M_F} \Phi^i U_i^c Q_3 H_2 + \frac{c_U}{M_F} U_3^c \Phi^i Q_i H_2 \right. \\ & \left. + \frac{d_U}{M_F} S^{ij} U_i^c Q_j H_2 + \frac{a_U}{M_F} A^{ij} U_i^c Q_j H_2 \right) \\ & + y_D \left( D_3^c Q_3 H_1 + \frac{b_D}{M_F} \Phi^i D_i^c Q_3 H_1 + \frac{c_D}{M_F} D_3^c \Phi^i Q_i H_1 \right. \\ & \left. + \frac{d_D}{M_F} S^{ij} D_i^c Q_j H_1 + \frac{a_D}{M_F} A^{ij} D_i^c Q_j H_1 \right). \end{aligned}$$

$$\frac{\langle \Phi^i \rangle}{M_F} = \delta^{i2} \epsilon, \quad \frac{\langle S^{ij} \rangle}{M_F} = \delta^{i2} \delta^{j2} \epsilon, \quad \frac{\langle A^{ij} \rangle}{M_F} = \epsilon^{ij} \epsilon'.$$

## U(2)FS: more on Yukawa matrices

The Yukawa matrices of the U(2) structure

$$Y_q = f_q \begin{pmatrix} 0 & a_q \lambda^3 & 0 \\ -a_q \lambda^3 & d_q \lambda^2 & b_q \lambda^2 \\ 0 & c_q \lambda^2 & 1 \end{pmatrix}, \quad (\lambda \sim 0.2),$$

lead to relations among eigenvalues (quark masses) and CKM matrix elements:

$$\left| \frac{y_u}{y_c} \right| = \left| \frac{V_{ub}}{V_{cb}} \right|^2 (1 + O(\lambda^2)), \quad \left| \frac{y_d}{y_s} \right| = \left| \frac{V_{td}}{V_{ts}} \right|^2 (1 + O(\lambda^2)),$$

that fail numerically.

## U(2)FS: more on Yukawa matrices

In our calculations, we cheat:

- Diagonalize Yukawa matrices at the GUT scale (identified as FSB scale) to obtain eigenvalues  $y_{u,d,s,c,b,t}$  and  $V_{CKM}$ .
- Write Yukawa matrices  $Y_{U,D}^{U(2)}$  of the U(2) form in terms of  $y_{s,c,b,t}$ ,  $V_{CKM}$  and input parameters  $b_U$ ,  $c_U$ ,  $b_D$  and  $\lambda$  (with expansion formulae in powers of  $\lambda$ ).
- Find unitary matrices that diagonalize  $Y_{U,D}^{U(2)}$ .
  - ▷ Eigenvalues  $y_{u,d}$  are different from original ones.
- Rotate original (diagonalized) Yukawa matrices with the unitary matrices obtained above.

## U(2)FS: more on Yukawa matrices

Example of “pseudo-U(2)” Yukawa matrices

(with  $\lambda = 0.2$  and randomly chosen  $b_U, c_U, b_D$ ):

$$|Y_U| = \begin{pmatrix} 3.5 \times 10^{-6} & 7.5 \times 10^{-5} & 1.9 \times 10^{-8} \\ 7.5 \times 10^{-5} & 3.6 \times 10^{-3} & 4.2 \times 10^{-2} \\ 2.5 \times 10^{-8} & 3.1 \times 10^{-2} & 4.8 \times 10^{-1} \end{pmatrix},$$

$$|Y_D| = \begin{pmatrix} 5.2 \times 10^{-5} & 4.8 \times 10^{-4} & 2.9 \times 10^{-7} \\ 4.8 \times 10^{-4} & 2.5 \times 10^{-3} & 5.8 \times 10^{-3} \\ 4.6 \times 10^{-7} & 4.9 \times 10^{-3} & 1.6 \times 10^{-1} \end{pmatrix}.$$

In this basis, we take

$$m_\Phi^2 = m_0^2 r_0^\Phi \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 + r_{22}^\Phi \lambda^4 & r_{23}^\Phi \lambda^2 \\ 0 & r_{23}^{\Phi*} \lambda^2 & r_{33}^\Phi \end{pmatrix}, \quad \Phi = Q, U, D.$$

## Structure of the neutrino mass matrices ( $\text{MSSM} \oplus \nu_R$ , $\text{SU}(5) \oplus \nu_R$ )

**Light:**  $|\Delta m_{32}^2|(\text{atm}) \gg \Delta m_{21}^2(\text{sol})$

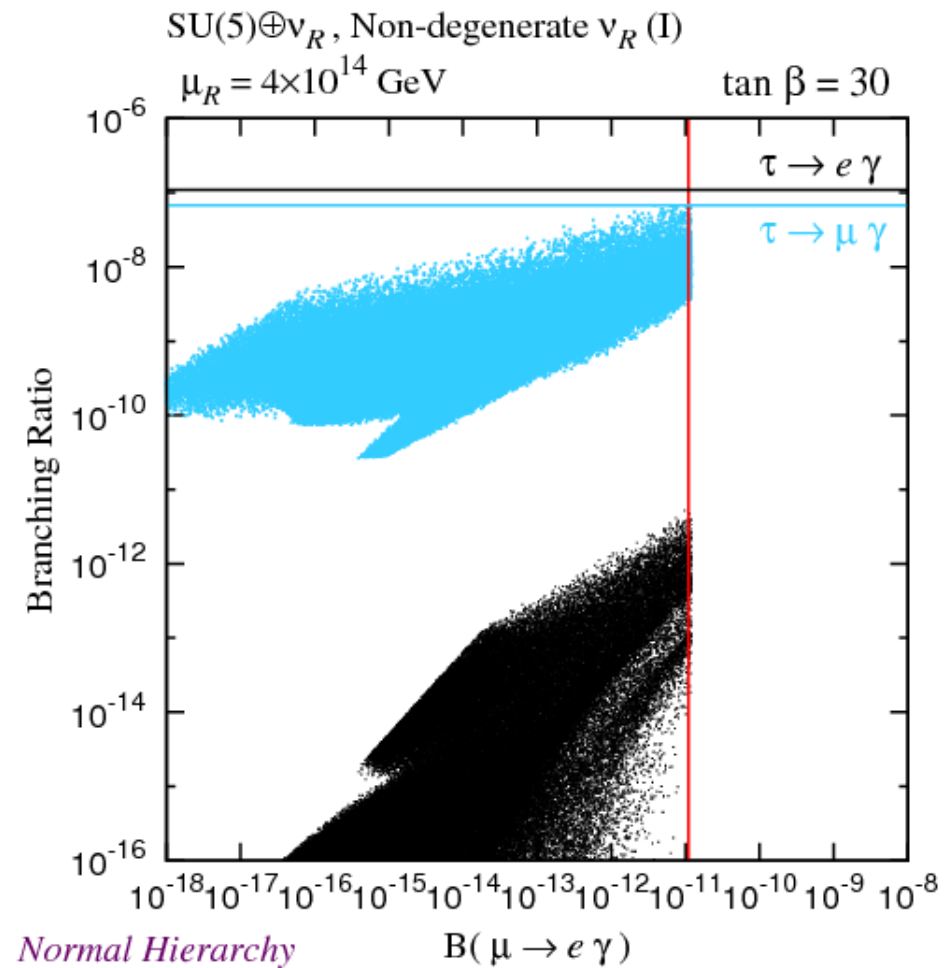
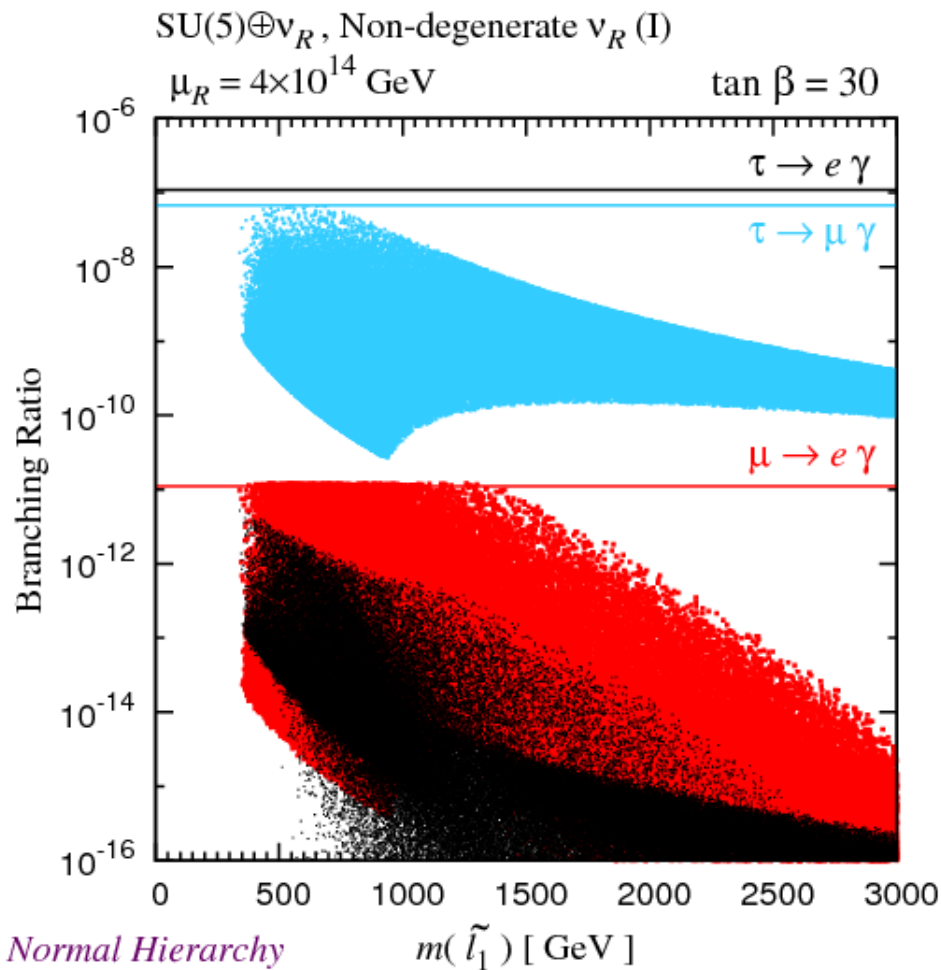
- Normal Hierarchy
  - ▷  $m_3 \gg m_2 \gg m_1 = 0.003\text{eV}$ .  
( $\Delta m_{21}^2 \gg m_1^2$ )
- Inverted Hierarchy
  - ▷  $m_2 > m_1 \gg m_3$ .
- Degenerate
  - ▷  $m_3 > m_2 > m_1$ ,  
 $m_1^2 = (0.1\text{eV})^2 \gg |\Delta m_{32}^2|$ .

**Heavy ( $\nu_R$ ):**

- Degenerate  $\nu_R$ :  $M_{\nu_R} \propto \mathbf{1}$ .
    - ▷  $\mu \rightarrow e \gamma$  enhanced.
  - Non-Degenerate  $\nu_R$ :  $M_{\nu_R} \not\propto \mathbf{1}$ .
    - ▷ More free parameters in  $Y_\nu$ .
    - ▷  $\mu \rightarrow e \gamma$  suppression possible.
- (I)  $(Y_\nu)_{12} = (Y_\nu)_{21} = 0$ ,  
 $(Y_\nu)_{13} = (Y_\nu)_{31} = 0$ .
- (II)  $(Y_\nu)_{12} = (Y_\nu)_{21} = 0$ ,  
 $(Y_\nu)_{23} = (Y_\nu)_{32} = 0$ .

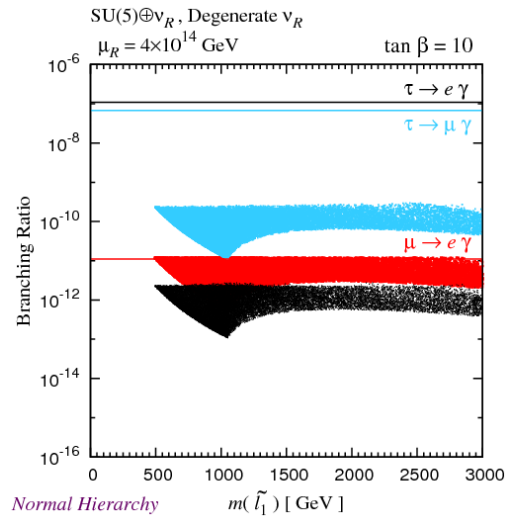
**LFV:**  $\mu \rightarrow e \gamma$ ,  $\tau \rightarrow \mu \gamma$ ,  $\tau \rightarrow e \gamma$

$SU(5) \oplus \nu_R$ , Non-degenerate  $\nu_R$  (I), Normal Hierarchy

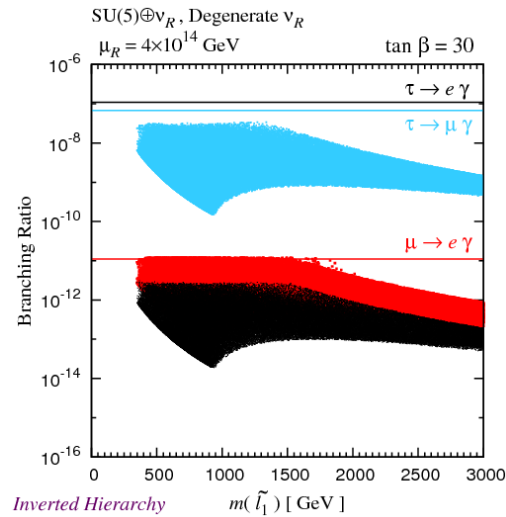


$m_{1/2}(\mu_G) \leq 1.5 \text{ TeV}$ ,  $m_0(\mu_P) \leq 4 \text{ TeV}$  scanned.

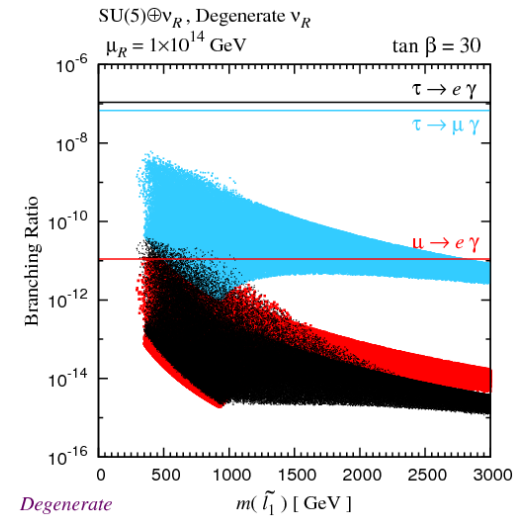
$\mu \rightarrow e \gamma, \tau \rightarrow \mu \gamma, \tau \rightarrow e \gamma$ :  $SU(5) \oplus \nu_R$  ( $Y_\nu$  &  $\mu_P \leftrightarrow \mu_G$  running)



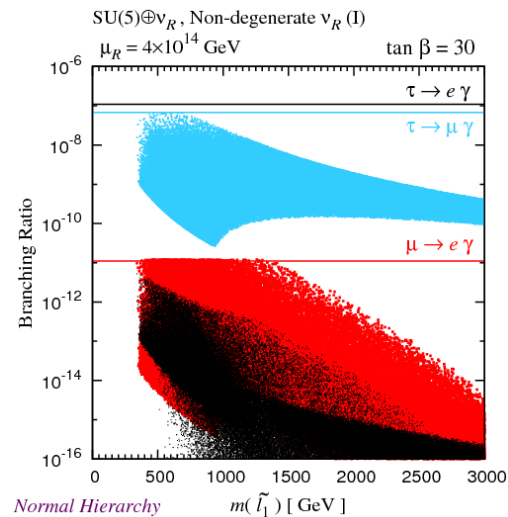
$D\nu_R$ -NH



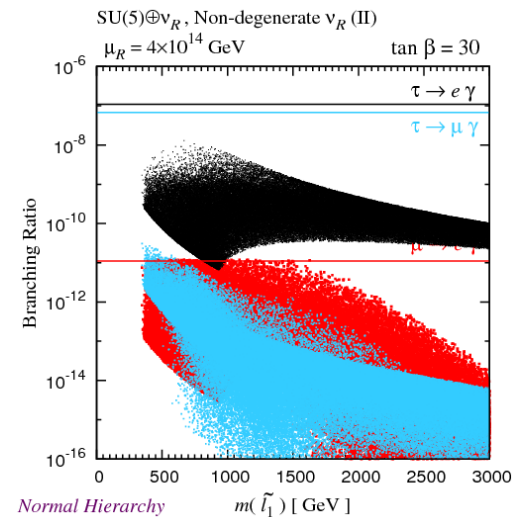
$D\nu_R$ -IH



$D\nu_R$ -D

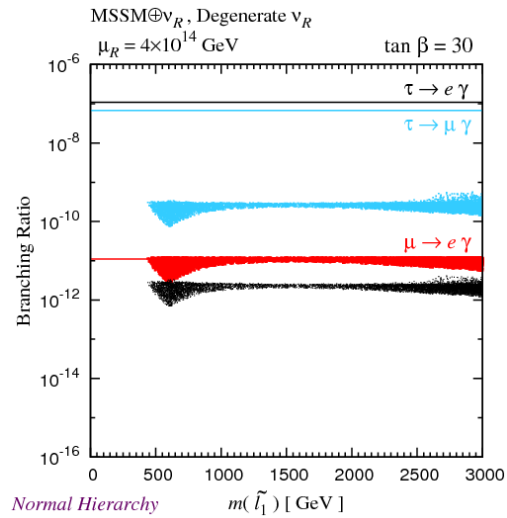


$ND\nu_R$ (I)-NH

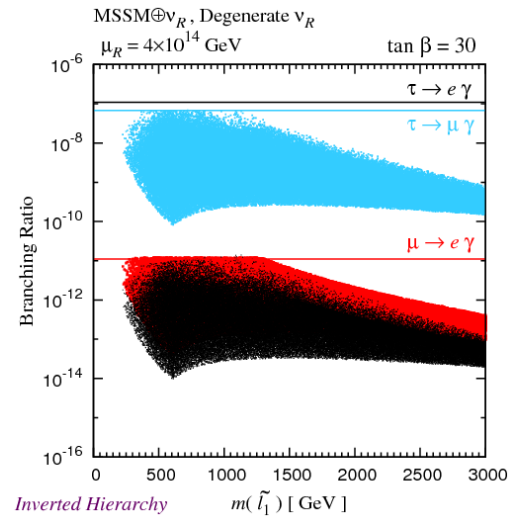


$ND\nu_R$ (II)-NH

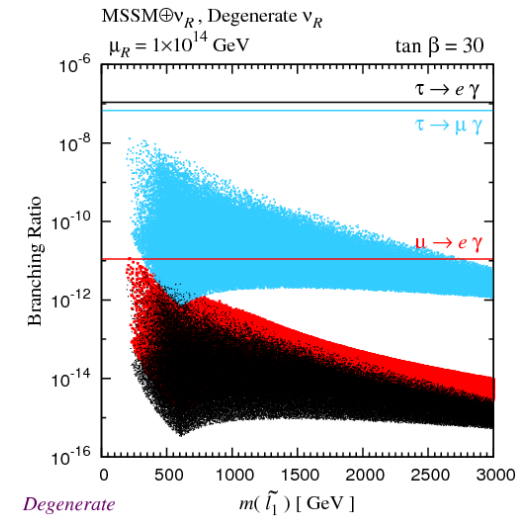
# $\mu \rightarrow e \gamma, \tau \rightarrow \mu \gamma, \tau \rightarrow e \gamma$ : $\text{MSSM} \oplus \nu_R$ ( $Y_\nu$ only)



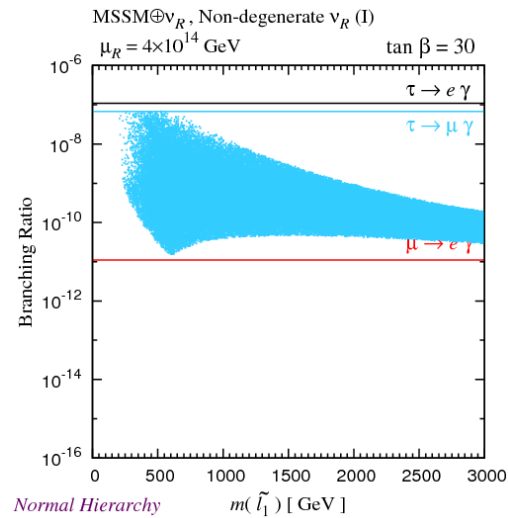
$D\nu_R$ -NH



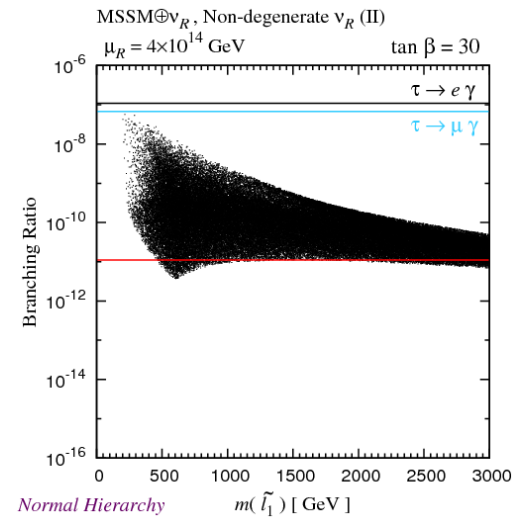
$D\nu_R$ -IH



$D\nu_R$ -D



$ND\nu_R$ (I)-NH



$ND\nu_R$ (II)-NH



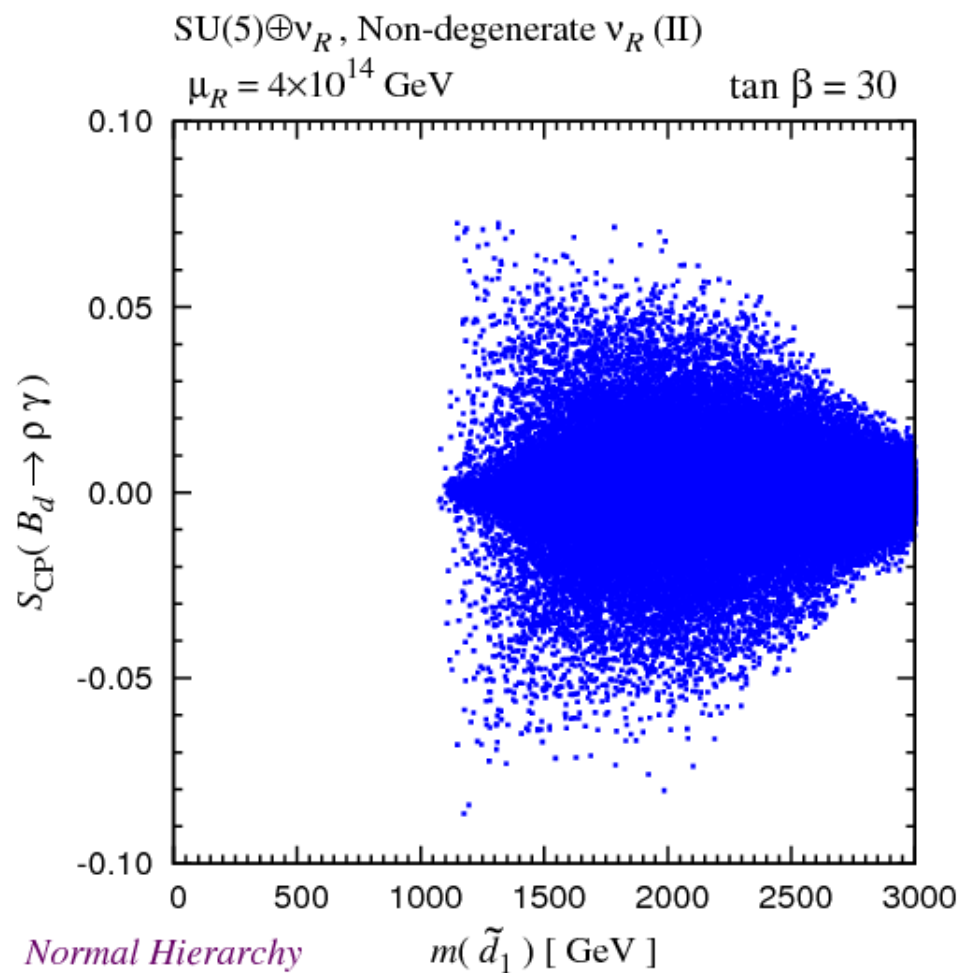
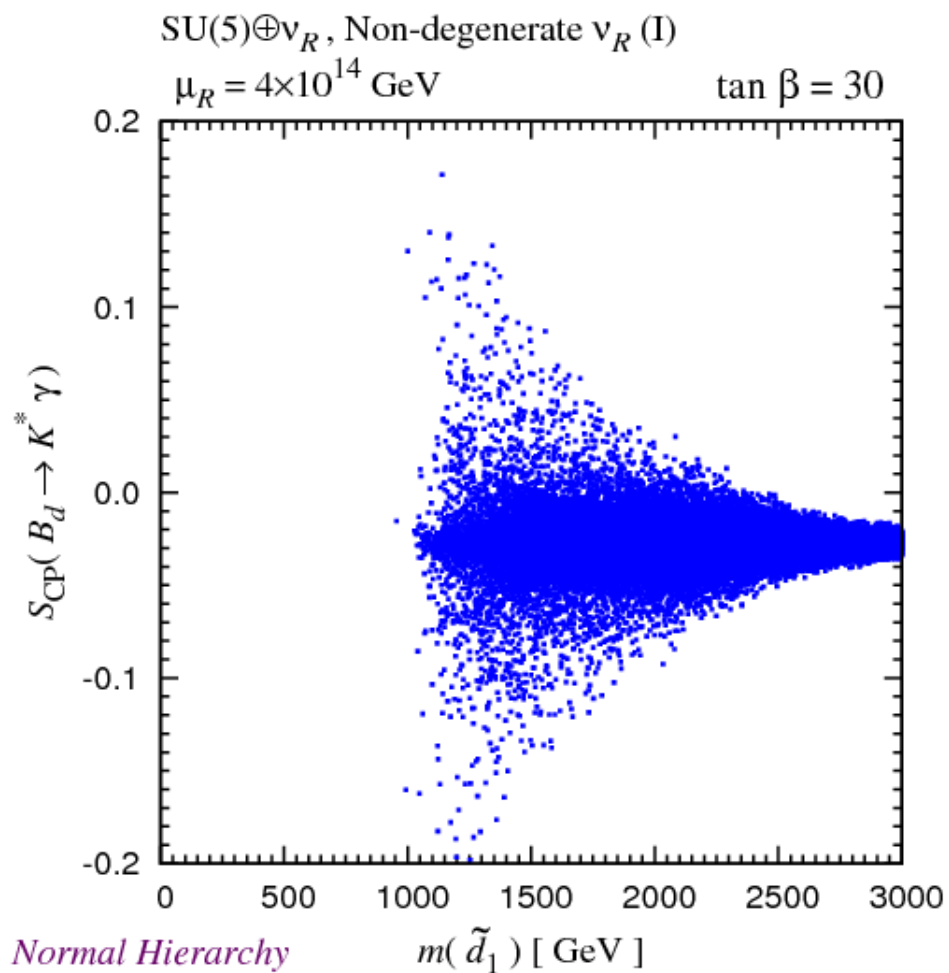
## Time-dependent CP asymmetries in $b \rightarrow s/b \rightarrow d$ decays

- $S_{\text{CP}}(B_d \rightarrow K^* \gamma), S_{\text{CP}}(B_d \rightarrow \rho \gamma)$ 
  - ▷  $B_d - \bar{B}_d$  mixing  $\otimes$   $b \rightarrow s(d) \gamma$  decay.
  - ▷ Interference between  $b_R \rightarrow s(d)_L \gamma_L$  and  $(\bar{b}_L) \rightarrow (\overline{s(d)_R}) \gamma_L$ ; suppressed by  $m_{s,d}/m_b$  in SM (Atwood-Gronau-Soni).
- $S_{\text{CP}}(B_d \rightarrow \phi K_S)$ 
  - ▷  $B_d - \bar{B}_d$  mixing  $\otimes$   $b \rightarrow s s \bar{s}$  decay.
  - ▷ Differs from  $S_{\text{CP}}(B_d \rightarrow J/\psi K_S)$  if new phase exists in  $b \rightarrow s$  penguin amplitude.
- $S_{\text{CP}}(B_s \rightarrow J/\psi \phi)$ 
  - ▷  $B_s - \bar{B}_s$  mixing  $\otimes$   $b \rightarrow s c \bar{c}$  decay.
  - ▷ Small in SM; enhanced if new phase exists in  $B_s - \bar{B}_s$  mixing.

$\Rightarrow$   $\tilde{d}_R$  mixing can contribute to all.

- Significant in  $\text{SU}(5) \text{ SUSY-GUT} \oplus \nu_R$  and  $\text{U}(2)\text{FS}$ .

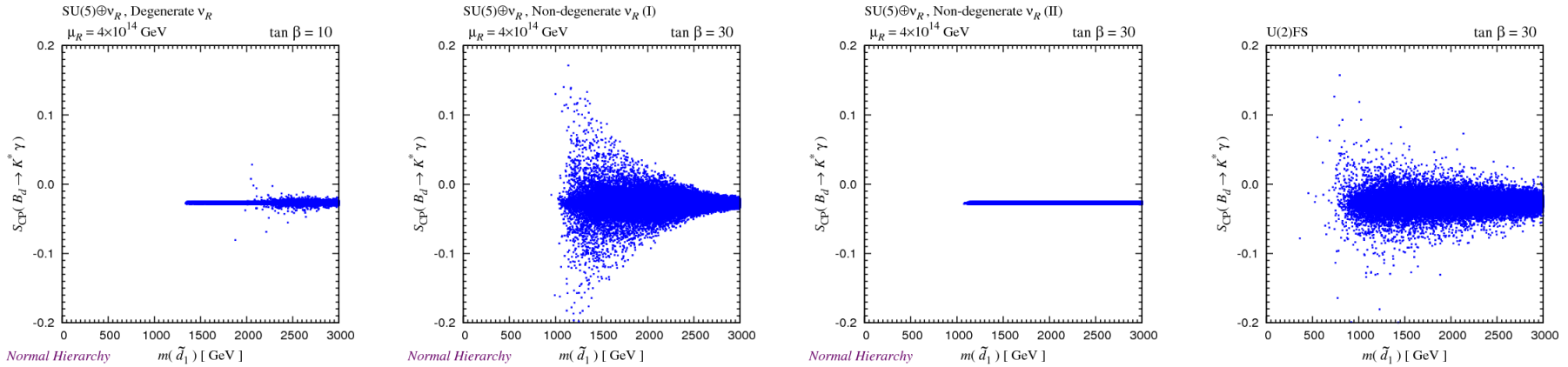
$S_{\text{CP}}(B_d \rightarrow K^* \gamma) [b \rightarrow s], S_{\text{CP}}(B_d \rightarrow \rho \gamma) [b \rightarrow d]$



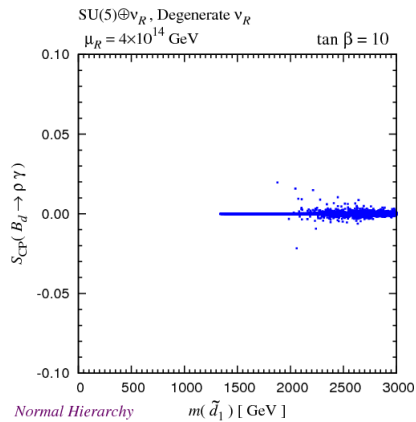
# $S_{CP}(B_d \rightarrow K^* \gamma)$ [ $b \rightarrow s$ ], $S_{CP}(B_d \rightarrow \rho \gamma)$ [ $b \rightarrow d$ ]

Significant in  $SU(5) \oplus \nu_R$ ,  $U(2)FS$ ; small in mSUGRA,  $MSSM \oplus \nu_R$ .

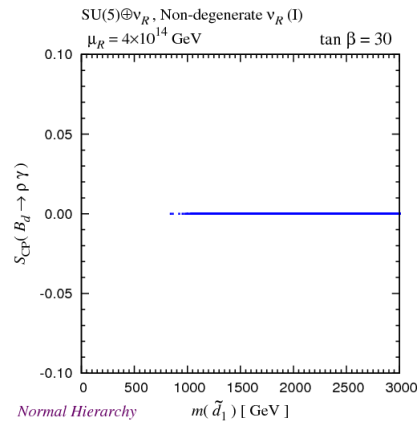
## $S_{CP}(B_d \rightarrow K^* \gamma)$ vs. $m(\tilde{d}_1)$



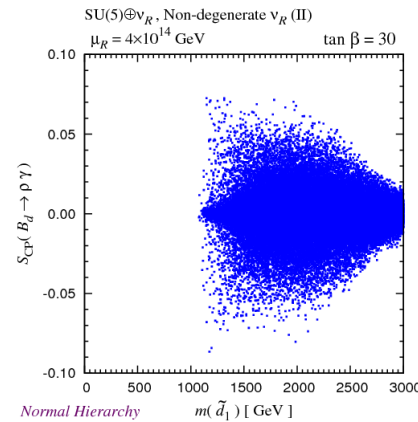
## $D\nu_R$ -NH



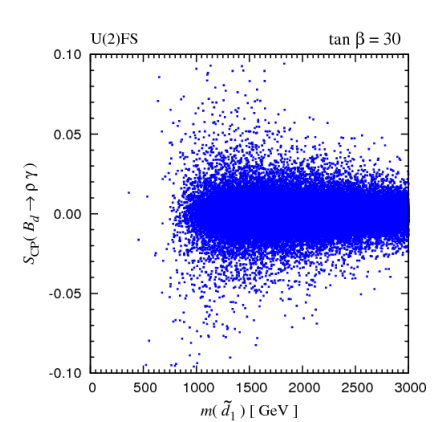
## $ND\nu_R$ (I)-NH



## $ND\nu_R$ (II)-NH



## $U(2)FS$

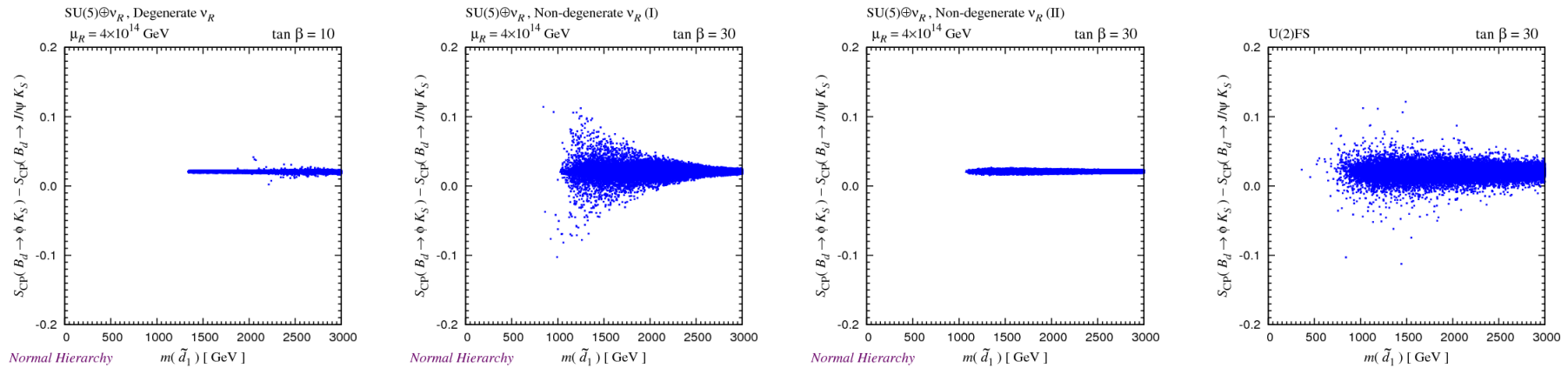


## $S_{CP}(B_d \rightarrow \rho \gamma)$ vs. $m(\tilde{d}_1)$

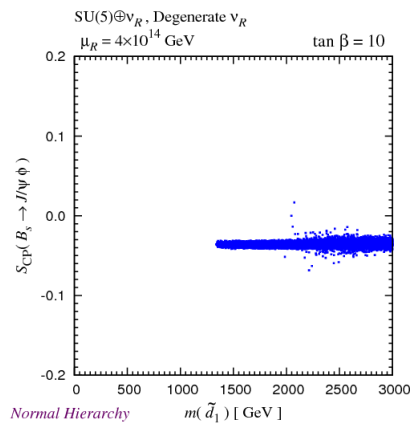
# $S_{CP}(B_d \rightarrow \phi K_S), S_{CP}(B_s \rightarrow J/\psi\phi)$ [ $b \rightarrow s$ ]

Significant in  $SU(5) \oplus \nu_R$ ,  $U(2)FS$ ; small in mSUGRA,  $MSSM \oplus \nu_R$ .

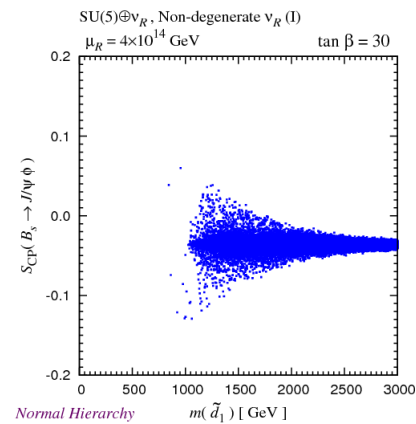
## $S_{CP}(B_d \rightarrow \phi K_S) - S_{CP}(B_d \rightarrow J/\psi K_S)$ vs. $m(\tilde{d}_1)$



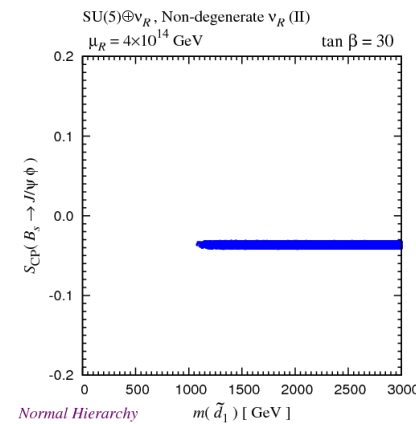
## $D\nu_R$ -NH



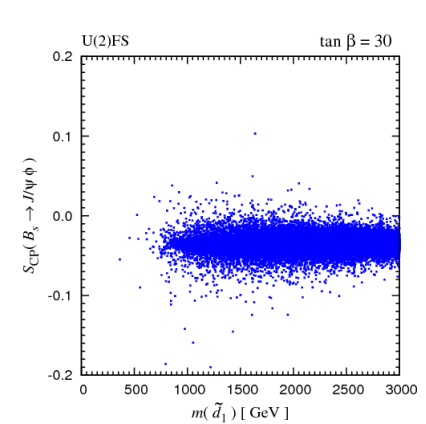
## $ND\nu_R$ (I)-NH



## $ND\nu_R$ (II)-NH



## $U(2)FS$



## $S_{CP}(B_s \rightarrow J/\psi\phi)$ vs. $m(\tilde{d}_1)$

## Summary: LFV

Model	$\mu \rightarrow e\gamma$	$\tau \rightarrow \mu\gamma$	$\tau \rightarrow e\gamma$
<b>MSSM <math>\oplus \nu_R</math></b>			
Degenerate $\nu_R$ , NH	✓		
Degenerate $\nu_R$ , IH	✓	✓	
Degenerate $\nu_R$ , D	✓	✓	
Non-degen. $\nu_R$ (I), NH		✓	
Non-degen. $\nu_R$ (II), NH			✓
<b>SU(5) <math>\oplus \nu_R</math></b>			
Degenerate $\nu_R$ , NH	✓		
Degenerate $\nu_R$ , IH	✓	✓	
Degenerate $\nu_R$ , D	✓	✓	
Non-degen. $\nu_R$ (I), NH	✓	✓	
Non-degen. $\nu_R$ (II), NH	✓		✓
Exp. sensitivity	$10^{-13}$	$2 - 8 \times 10^{-9}$	
	MEG	SuperB@50 – 75ab <sup>-1</sup>	

✓:  $B(\mu \rightarrow e\gamma) \sim 10^{-11}$ ,  $B(\tau \rightarrow \mu(e)\gamma) \sim 10^{-8}$  possible.

## Summary: Time-dependent CPV in $b \rightarrow s(d)$

	$S_{\text{CP}}(K^*\gamma)$	$S_{\text{CP}}(\rho\gamma)$	$\Delta S_{\text{CP}}(\phi K_S)$	$S_{\text{CP}}(B_s \rightarrow J/\psi\phi)$
SU(5) $\oplus\nu_R$				
D $\nu_R$ , NH	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$
D $\nu_R$ , IH	$\sim 0.2$	$\sim 0.02$	$\sim 0.2$	$\sim 0.1$
D $\nu_R$ , D	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$
ND $\nu_R$ (I), NH	$\sim 0.2$		$\sim 0.1$	$\sim 0.1$
ND $\nu_R$ (II), NH		$\sim 0.1$		
U(2)FS	$\sim 0.2$	$\sim 0.1$	$\sim 0.1$	$\sim 0.1$
Exp. precision	0.02 – 0.03	0.08 – 0.12	0.02 – 0.03	$\sim 0.01$
		SuperB@50 – 75ab $^{-1}$		LHCb@10fb $^{-1}$

- Small in mSUGRA, MSSM $\oplus\nu_R$ .

## Benchmark points

In many studies, parameter scans are carried out in the free parameter space of the model.

Parameter scan (scatter plots) tells us:

- Pattern of signals (deviations from SM predictions).
- A region in the space of observables where the model cannot reach.

...but picking up representative points from a bunch of scatter plots is not easy.

A list of *numbers* is requested for simulation study

⇒ “benchmark points” .

## Benchmark points

Definition of a “point” ?

- A set of MSSM parameters (one point in  $>100$  dimensional parameter space).
  - ▷ Parametrization (mass insertion, SLHA2, ...)?
  - ▷ Basis (super-CKM), renormalization scheme ( $\overline{DR}$ , on-shell, ...)  
and scale?
- A list of (flavor) observables.
  - ▷ Flavor observables.
  - ▷ SUSY particle spectrum and couplings (for “interplay” or comparison with “SPS” s).
- Other “intermediate” variables (Wilson coefficients, ...)?

How to choose a “good” point?

- Theoretically well-motivated.
- Rich experimental signals.
  - ▷ Different patterns.



## Super-CKM basis

A supersymmetric (but  $SU(2)$  breaking) basis for quarks/squarks, where:

- quark mass (Yukawa) matrices are diagonal;
  - ▷ in what renormalization scheme?
- same basis applied for squarks  $\Rightarrow$  supersymmetric parts of squark mass matrices are diagonal; SUSY breaking parts are not.

$$\begin{pmatrix} V_{CKM}^\dagger & u_L \\ & d_L \end{pmatrix} \begin{pmatrix} u_R \\ d_R \end{pmatrix} \Leftarrow \text{SUSY} \Rightarrow \begin{pmatrix} V_{CKM}^\dagger & \tilde{u}_L \\ & \tilde{d}_L \end{pmatrix} \begin{pmatrix} \tilde{u}_R \\ \tilde{d}_R \end{pmatrix}$$

## Mass insertion parametrization

$$\mathcal{M}_{\tilde{q}}^2 = m_{\tilde{q}}^2 \left[ \mathbf{1} + \begin{pmatrix} \delta_{LL}^q & \delta_{LR}^q \\ \delta_{RL}^q & \delta_{RR}^q \end{pmatrix} \right], \quad q = u, d.$$

Parametrization of a squark mass matrix with:

- An “average” squark mass  $m_{\tilde{q}}$ :  $m_{\tilde{q}}^2 = \text{tr } \mathcal{M}_{\tilde{q}}^2 / 6$ .
- “Mass insertion parameters”  $\delta$ 's
  - ▷ Two  $3 \times 3$  hermitian matrices  $\delta_{LL}^q$  and  $\delta_{RR}^q$ ;
  - ▷ A  $3 \times 3$  complex matrix  $\delta_{LR}^q = \delta_{RL}^{q\dagger}$ .
- In super-CKM basis, defined by tree-level “running” parameters in  $\overline{\text{DR}}$  scheme, evaluated at  $m_Z(?)$ .
- Both supersymmetric and SUSY breaking parts included.
- Several different definitions are used in literature.

## Example?

Squark/slepton mass matrices in mass insertion parametrization looks like...

$$m_{\tilde{d}}/\text{GeV} = 6.06228921\text{e}+02 \quad m_{\tilde{u}}/\text{GeV} = 5.87494919\text{e}+02$$

$$m_{\tilde{e}}/\text{GeV} = 3.78445819\text{e}+02 \quad m_{\tilde{\nu}}/\text{GeV} = 3.74915197\text{e}+02$$

$$\begin{aligned} \text{Re}(\delta_{LL}^d)_{11} &= 1.96204471\text{e}-01 & \text{Re}(\delta_{LL}^d)_{22} &= 1.95401509\text{e}-01 & \text{Re}(\delta_{LL}^d)_{33} &= -4.09617128\text{e}-01 \\ \text{Re}(\delta_{LL}^d)_{12} &= 1.55159093\text{e}-04 & \text{Re}(\delta_{LL}^d)_{13} &= -3.74657889\text{e}-03 & \text{Re}(\delta_{LL}^d)_{23} &= 1.89581433\text{e}-02 \\ \text{Im}(\delta_{LL}^d)_{12} &= 7.33798173\text{e}-05 & \text{Im}(\delta_{LL}^d)_{13} &= -1.69467815\text{e}-03 & \text{Im}(\delta_{LL}^d)_{23} &= -3.66826205\text{e}-04 \end{aligned}$$

$$\begin{aligned} \text{Re}(\delta_{RR}^d)_{11} &= 1.21046867\text{e}-01 & \text{Re}(\delta_{RR}^d)_{22} &= 7.44399324\text{e}-02 & \text{Re}(\delta_{RR}^d)_{33} &= -1.77475651\text{e}-01 \\ \text{Re}(\delta_{RR}^d)_{12} &= 1.16908068\text{e}-07 & \text{Re}(\delta_{RR}^d)_{13} &= 2.66037561\text{e}-07 & \text{Re}(\delta_{RR}^d)_{23} &= -1.28909769\text{e}-05 \\ \text{Im}(\delta_{RR}^d)_{12} &= 9.44683072\text{e}-08 & \text{Im}(\delta_{RR}^d)_{13} &= 1.89860024\text{e}-07 & \text{Im}(\delta_{RR}^d)_{23} &= -2.29376316\text{e}-02 \end{aligned}$$

$$\begin{aligned} \text{Re}(\delta_{LR}^d)_{11} &= 1.09503668\text{e}-04 & \text{Re}(\delta_{LR}^d)_{12} &= 6.64443466\text{e}-10 & \text{Re}(\delta_{LR}^d)_{13} &= -1.06114203\text{e}-08 \\ \text{Re}(\delta_{LR}^d)_{21} &= 6.81504386\text{e}-09 & \text{Re}(\delta_{LR}^d)_{22} &= 1.99112393\text{e}-03 & \text{Re}(\delta_{LR}^d)_{23} &= 2.92716354\text{e}-07 \\ \text{Re}(\delta_{LR}^d)_{31} &= -9.13006336\text{e}-06 & \text{Re}(\delta_{LR}^d)_{32} &= 4.61891379\text{e}-05 & \text{Re}(\delta_{LR}^d)_{33} &= 1.09682506\text{e}-01 \\ \text{Im}(\delta_{LR}^d)_{11} &= -1.30278509\text{e}-15 & \text{Im}(\delta_{LR}^d)_{12} &= 3.16262352\text{e}-10 & \text{Im}(\delta_{LR}^d)_{13} &= -4.63202875\text{e}-09 \\ \text{Im}(\delta_{LR}^d)_{21} &= -3.22944052\text{e}-09 & \text{Im}(\delta_{LR}^d)_{22} &= -6.90796809\text{e}-13 & \text{Im}(\delta_{LR}^d)_{23} &= -4.41018263\text{e}-05 \\ \text{Im}(\delta_{LR}^d)_{31} &= 4.11561337\text{e}-06 & \text{Im}(\delta_{LR}^d)_{32} &= 1.76138113\text{e}-06 & \text{Im}(\delta_{LR}^d)_{33} &= 3.27148344\text{e}-11 \end{aligned}$$

$+\delta_{LL,RR,LR}^u + \delta_{LL,RR,LR}^e + \delta_{LL}^\nu + \text{other MSSM parameters.}$

## Conclusion

- Flavor physics provides us with information about (flavor) structure of SUSY breaking sector.
- So far, there are a lot of “parameter scan” or “scatter plot” studies, that show interesting patterns of signals.  
⇒ We may be able to pick up several points as “benchmarks” for SuperB simulation study.
- We agreed with basic parts of the “benchmark”:
  - ▷ Definitions of parameters (as “common language”).
  - ▷ (List of observables).
- Searches/updates required to find out favorable point(s).
  - ▷ Computational tools (public or private) sufficiently prepared?
    - \* Almighty code may not exist, then....?