



Hadronic Recoil Analysis and $B \rightarrow K^{(*)} \nu \nu$ at SuperB

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SuperB Physics workshop

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Outline

- * Theoretical and Experimental status of $B \rightarrow K^{(*)} \nu \nu$
- * **Hadronic Recoil Analysis Method** and Implementation in **Superb Fast Simulation**

- * **BaBar Full Simulation** vs **Fast Simulation** in the **BaBar** configuration

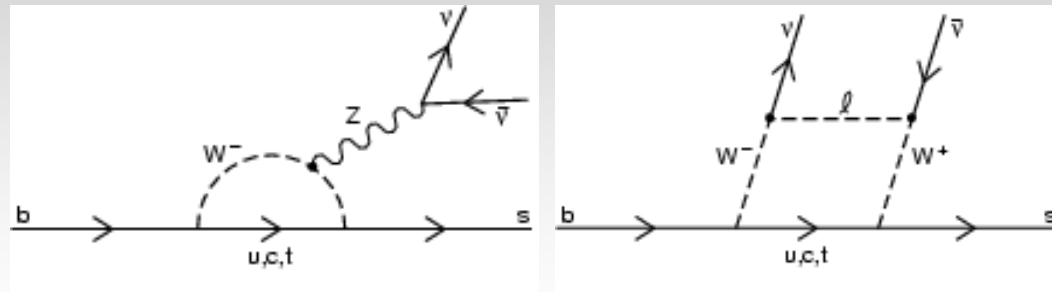
- * Comparison between **SuperB Detector geometry # 1 (DG_1)** and **SuperB Detector geometry # 4 (DG_4)**
 - Breco side
 - $B \rightarrow K^{(*)} \nu \nu$ signal side analysis

- * **SuperB** expected sensitivity on $B \rightarrow K^{(*)} \nu \nu$ branching fractions



Theoretical status

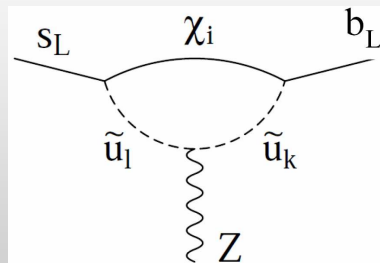
Standard Model diagrams



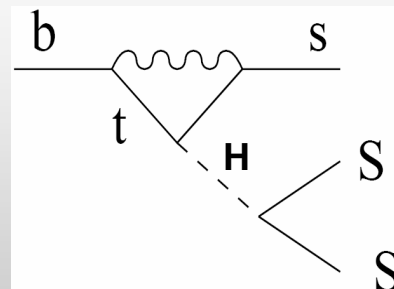
$BR_{SM}(B \rightarrow K^* \nu \bar{\nu}) = (6.8^{+1.0}_{-1.1}) \times 10^{-6}$ G.Altmannshofer et al.,
 $BR_{SM}(B \rightarrow K \nu \bar{\nu}) = (4.5 \pm 0.7) \times 10^{-6}$ TUM-HEP-709-09

* **New physics effects: some examples**

Non Standard
Z - couplings



New sources
of missing energy



Buchalla et al. hep-ph/0006136;
 Bird et al. hep-ph/0401195;
 Aliev et al. arXiv:0705.4542;
 Neubert at LLWI '09;
 Kim et al. arXiv:0904.0318;

* BR enhanced up to a **factor 50** with respect to the SM expectations



Experimental Status

* Belle experiment (Had Recoil, 535 million BB pairs)¹:

$$\mathcal{B}(B^\pm \rightarrow K^\pm \nu \bar{\nu}) < 1.4 \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K_S^0 \nu \bar{\nu}) < 1.6 \times 10^{-4}$$

$$\mathcal{B}(B^\pm \rightarrow K^{*\pm} \nu \bar{\nu}) < 1.4 \times 10^{-4}$$

$$\mathcal{B}(B^0 \rightarrow K^0 \nu \bar{\nu}) < 3.4 \times 10^{-4}$$

All the measurements
are still **consistent with**
the **SM** expectation
($O(10^{-6})$)

* BaBar (Had Recoil, 351 million BB pairs)²:

$$\mathcal{B}(B^\pm \rightarrow K^\pm \nu \bar{\nu}) < 4.2 \times 10^{-5}$$

* BaBar (Had+SL Recoil 454 million BB pairs)³:

$$\mathcal{B}(B^\pm \rightarrow K^{*\pm} \nu \bar{\nu}) < 8 \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu}) < 12 \times 10^{-5}$$

$$\mathcal{B}(B \rightarrow K^* \nu \bar{\nu}) < 8 \times 10^{-5}$$

¹ K. F. Chen et al. [BELLE Collaboration], Phys. Rev. Lett. 99, 221802 (2007).

² H. Kim on behalf of the BaBar collaboration, arXiv:hep-ex/08052365 (2008).

³ B. Aubert et al. [BaBar collaboration], Phys.Rev.D78:072007,2008

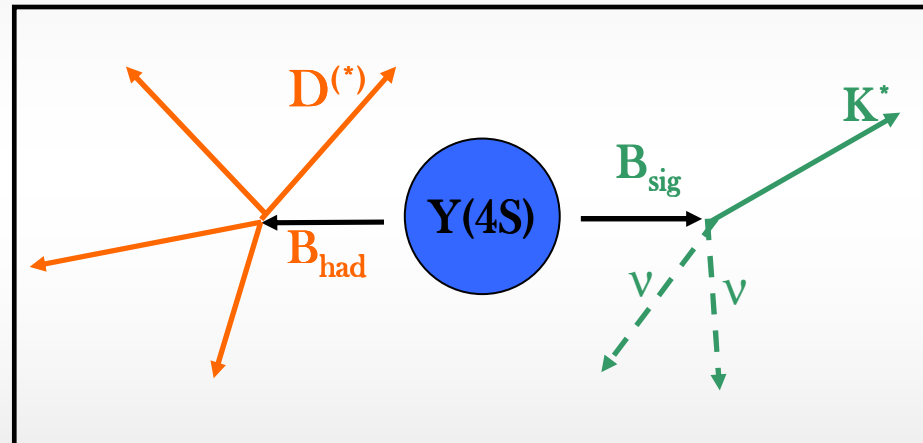


Hadronic Recoil Analysis: method

$$e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}$$

1. B_{had} reconstruction: Full reconstruction of one B meson in hadronic (or semileptonic) decays

2. B_{sig} reconstruction: look for the signal B signature, i.e. a K^* not accompanied by additional (charged or neutral) particles + missing energy



RECOIL TECHNIQUE @ b-FACTORIES

→ search for rare decay with MISSING ENERGY

(NOT FEASIBLE @ HADRONIC MACHINE)

→ two examples of SuperB benchmark channels: $B \rightarrow \tau\nu$, $B \rightarrow K^{(*)}\nu\nu$



Hadronic Breco reconstruction philosophy

* Aim: collect as many as possible fully reconstructed **B** mesons in order to study the property of the recoil

* SemiExclusive reconstruction: search for $B \rightarrow D^{(*)}X$, with $X = n\pi \ mK \ pK_s \ q\pi^0$ and $n+m+r+q < 6$, without making requirements on intermediate resonances

* Reoconstruction steps:
 - reconstruct $D \rightarrow$ hadrons

$D^{*+} \rightarrow D^0\pi^+$	$D^0 \rightarrow K^-\pi^+$	$D^+ \rightarrow K^-\pi^+\pi^-$
$D^{*0} \rightarrow D^0\pi^0$	$D^0 \rightarrow K^-\pi^+\pi^0(\gamma\gamma)$	$D^+ \rightarrow K^-\pi^+\pi^-\pi^0$
$D^{*0} \rightarrow D^0\gamma$	$D^0 \rightarrow K^-\pi^+\pi^+\pi^-$	$D^+ \rightarrow K_S^0\pi^+$
	$D^0 \rightarrow K_S^0\pi^+\pi^-$	$D^+ \rightarrow K_S^0\pi^+\pi^-\pi^+$
		$D^+ \rightarrow K_S^0\pi^+\pi^0$

- use **D** as a seed and add **X** to have a system compatible with the **B** hypotesys

* Signal box defined by using:

$$m_{ES} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

$$\Delta E = E_B^* - E_{beam}^*$$

* Sample of 1100 **B** decay modes, ordered by purity.

* In events with multiple candidates, the best one is selected according to the smallest ΔE



Hadronic Recoil Analysis in FastSim



use BaBar code, adapted to FastSim framework

* Breco side: limit the number of reconstructed modes channels according to their purity

- Breco mode classification:
 - neat : purity > 80% , $\epsilon_{\text{neat}} \approx O(10^{-4})$
 - clean : 50% < purity < 80% , $\epsilon_{\text{clean}} \approx O(10^{-3}-10^{-2})$
 - dirty : 8% < purity < 50% , $\epsilon_{\text{dirty}} \approx O(10^{-2})$
- in some BaBar analysis (i.e. $B \rightarrow \tau \nu$) only the cleanest Breco modes are used; same will be probably done with the high SuperB statistics

→ reconstruct only neat+clean modes

* Bsig side:

- $K^+ \nu \nu$
- $K_s (\pi^+ \pi^-) \nu \nu$
- $K^{*+} (K_s \pi^+, K^+ \pi^0) \nu \nu$
- $K^{*0} (K^+ \pi^-) \nu \nu$
- $\tau^+ \nu$, with $\tau^+ \rightarrow e^+ \nu \nu, \mu^+ \nu \nu, \pi^+ \nu, \rho^+ (\pi^+ \pi^0) \nu, a_1^+ (\rho^0 \pi^+) \nu$

discussed in
this talk



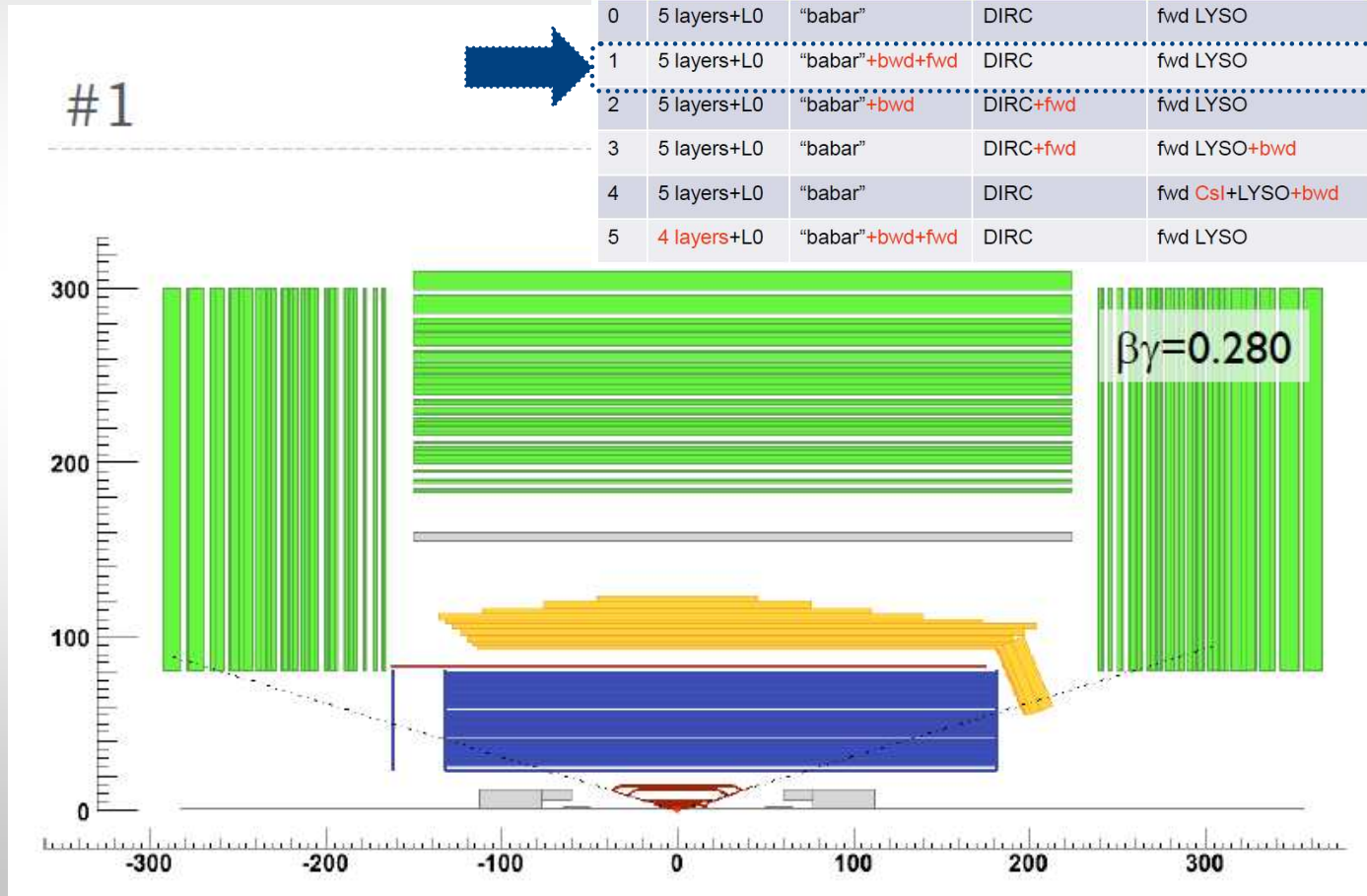
SuperB detector geometry : example I



* DetectorGeometry_1

- SVT_L0 + bwd and fwd DCH: gain in tracking and Breco reconstruction efficiencies

	SVT	DCH	PID	EMC	IFR
0	5 layers+L0	"babar"	DIRC	fwd LYSO	baseline
1	5 layers+L0	"babar"+bwd+fwd	DIRC	fwd LYSO	baseline
2	5 layers+L0	"babar"+bwd	DIRC+fwd	fwd LYSO	baseline
3	5 layers+L0	"babar"	DIRC+fwd	fwd LYSO+bwd	baseline
4	5 layers+L0	"babar"	DIRC	fwd Csl+LYSO+bwd	baseline
5	4 layers+L0	"babar"+bwd+fwd	DIRC	fwd LYSO	baseline



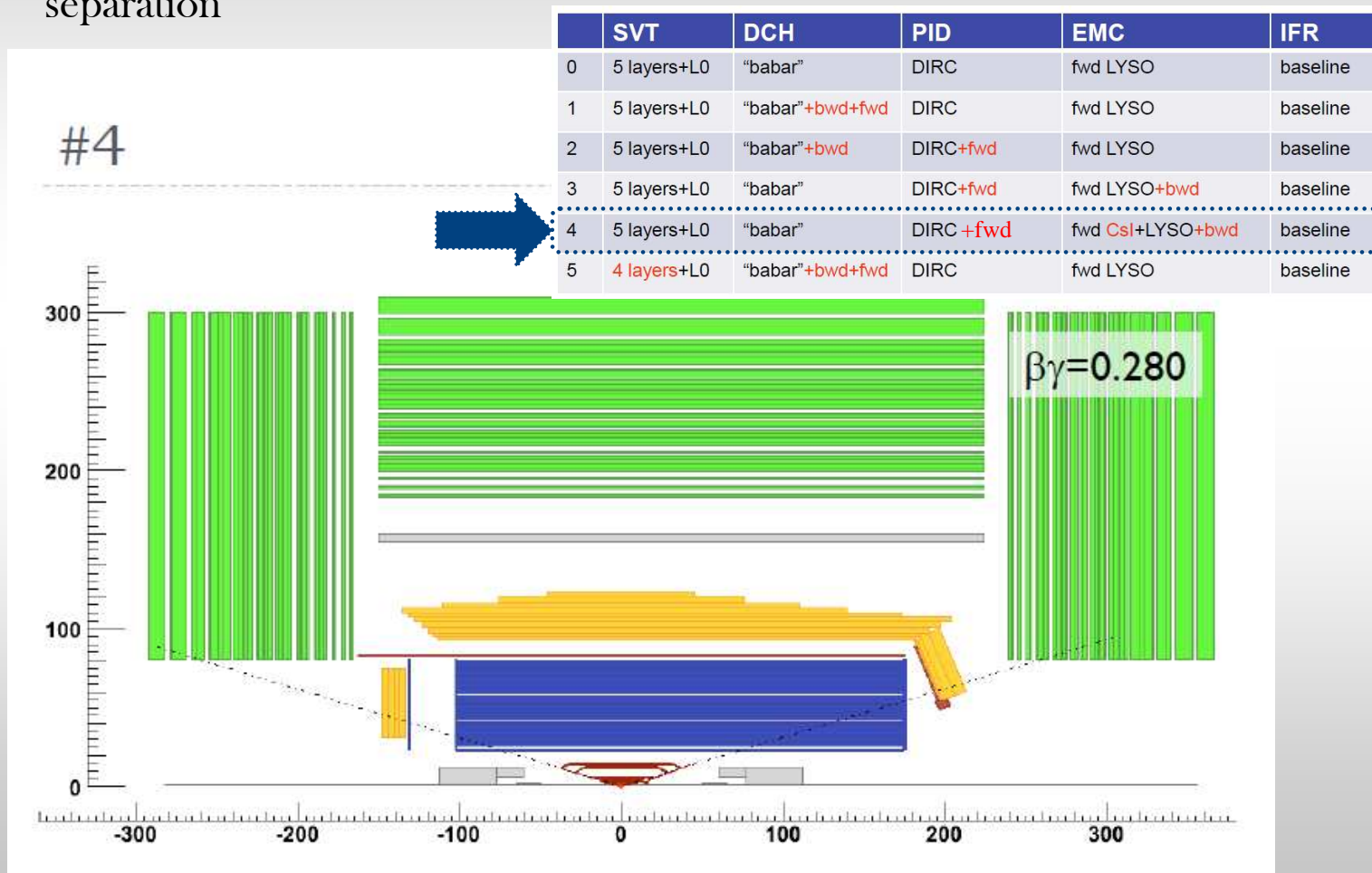


SuperB detector geometry :example II



* DetectorConfiguration_4

- SVT_L0 + fwd DIRC + bwd EMC: higher angular coverage and better $K-\pi$ separation





Data Sample for this analysis

Hadronic Breco reconstruction implemented in SuperB Fast Simulation

* Background production (run in parallel for several analysis):

- generic MC samples,
- some machine background included
- 3 detector geometry: DG_BaBar, DG_1, DG_4

* Signal MC (“private”) production:

- $B^+ \rightarrow K^+ \nu \nu, B^+ \rightarrow K^{*+} \nu \nu,$

$B^0 \rightarrow K^{*0} \nu \nu$

- 3 detector geometry
- 10^6 generated events for each sample, for each DG

Detector Geometry	Generator	N requested	Analysis	Requestor	Status	N produced
DG_1	BOB0bar_generic	50x10 ⁶	All	Dave	Complete	53.1 x10 ⁶
DG_1	B+B_generic	50x10 ⁶	All	Dave	Complete	49.4x10 ⁶
DG_1	ccbar	50x10 ⁶	DstD0ToKspipi, HadRecoil	Rolf, Elisa	Complete	49.9x10 ⁶
DG_1	uds	100x10 ⁶	HadRecoil	Elisa	Complete	49.9x10 ⁶
DG_1	B+B_tau_DX	1x10 ⁶	BtoTauNu	Chih-hsiang	Complete	1x10 ⁶
DG_4	BOB0bar_generic	50x10 ⁶	All	Dave	Complete	48.3x10 ⁶
DG_4	B+B_generic	50x10 ⁶	All	Dave	Complete	48.7x10 ⁶
DG_4	ccbar	50x10 ⁶	HadRecoil	Elisa	Complete	49.8x10 ⁶
DG_4	uds	100x10 ⁶	HadRecoil	Elisa	Complete	49.3x10 ⁶
DG_4	B+B_tau_DX	1x10 ⁶	BtoTauNu	Chih-hsiang	Complete	1x10 ⁶
DG_BaBar	BOB0bar_generic	50x10 ⁶	HadRecoil	Elisa	Complete	50x10 ⁶
DG_BaBar	B+B_generic	50x10 ⁶	HadRecoil	Elisa	Complete	50x10 ⁶
DG_BaBar	ccbar	50x10 ⁶	DstD0ToKspipi, HadRecoil	Rolf, Elisa	Complete	50x10 ⁶
DG_BaBar	B+B_tau_DX	1x10 ⁶	BtoTauNu	Chih-hsiang	Complete	1x10 ⁶



BaBaf Full Simulation
VS
SuperB Fast Simulation



Samples used

SuperB FastSim:

- B+B-, B0B0bar, ccbar MC samples (see slide 10)
- BaBar beams and detector geometry

* BaBar FullSim, Run3:

- B+B- : 49766000 gen. events
- B0B0bar : 50556000 gen. events
- ccbar : 83974000 gen. events

* Differences in reconstructed Breco modes

- BaBar FullSim: additive modes wrt FastSim, i.e. $B \rightarrow J/\psi X$, new **D** modes as seeds \rightarrow cut on **B** and **D** mode to reject most of them
- BaBar FullSim: neat+clean+dirty sample \rightarrow cut on purity

* Selection applied:

- at least one reconstructed Breco; if #Breco > 1, best candidate $\leftrightarrow |\Delta E| \min$
- $-0.09 < \Delta E < 0.05 \text{ GeV}$
- $5.270 < m_{ES} < 5.288 \text{ GeV}/c^2$



Hadronic Recoil Analysis: FastSim vs FullSim (I)

charged Breco	B0B0bar		BpBm		ccbar	
	FullSim	FastSim	FullSim	FastSim	FullSim	FastSim
≥ 1 Breco	0.0037	0.0054	0.0100	0.0115	0.0088	0.0079
deltaE cut	0.0028	0.0043	0.0081	0.0093	0.0063	0.0057
mES cut	0.0004	0.0007	0.0034	0.0032	0.0008	0.0007
$\epsilon_{\text{Fast}}/\epsilon_{\text{Full}}$	1.66		0.95		0.94	

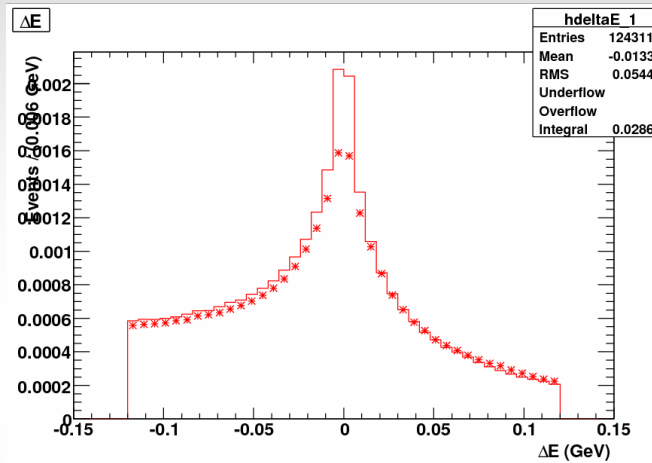
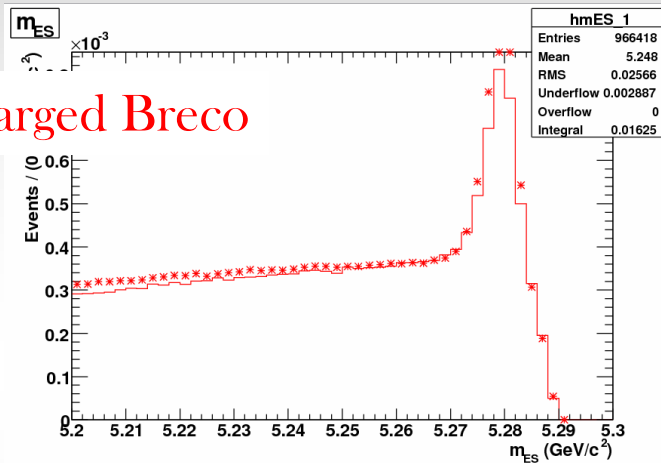
neutral Breco	B0B0bar		BpBm		ccbar	
	FullSim	FastSim	FullSim	FastSim	FullSim	FastSim
≥ 1 Breco	0.0083	0.0133	0.0031	0.0057	0.0038	0.0054
deltaE cut	0.0070	0.0116	0.0025	0.0048	0.0029	0.0043
mES cut	0.0020	0.0028	0.0003	0.0006	0.0003	0.0005
$\epsilon_{\text{Fast}}/\epsilon_{\text{Full}}$	1.40		1.92		1.57	



Hadronic Recoil Analysis: FastSim vs FullSim (II)

* m_{ES} and ΔE before the selection

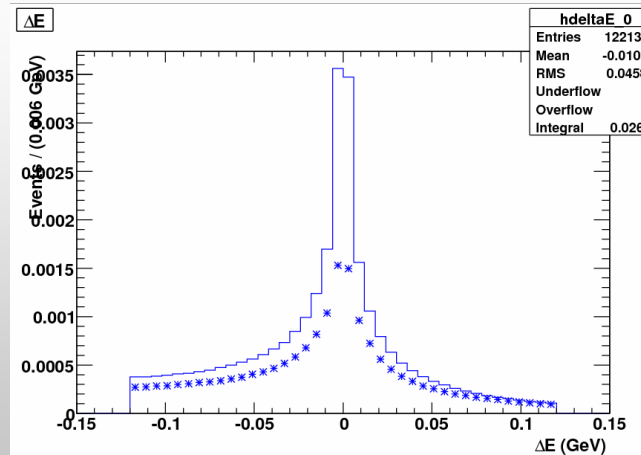
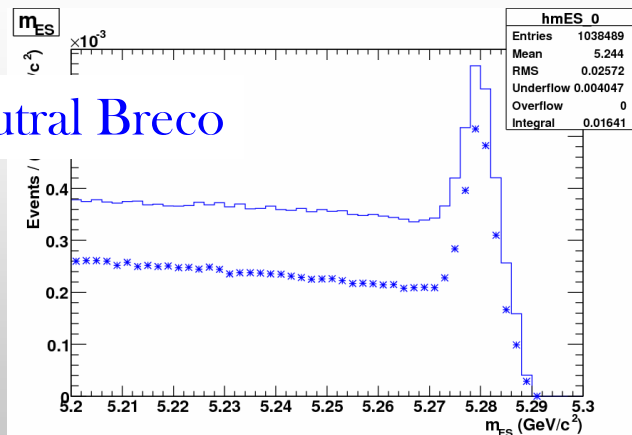
charged Breco



* BaBar FullSim
— FastSim DG_BaBar

◆ ccbar + B0B0 + B+B-

neutral Breco



◆ ccbar + B+B- + B0B0



SuperB Fast Simulation: DG_1 and DG_4



Hadronic Recoil Analysis: SuperB configs(I)

* Efficiency table for charged reconstructed Breco

charged Breco	B0B0bar		<u>BpBm</u>		ccbar		uds	
	DG_1	DG_4	DG_1	DG_4	DG_1	DG_4	DG_1	DG_4
≥ 1 Breco	0.0084	0.0089	0.0165	0.0174	0.0113	0.0120	0.0055	0.0058
deltaE cut	0.0067	0.0072	0.0135	0.0143	0.0081	0.0087	0.0038	0.0040
mES cut	0.0010	0.0011	0.0042	0.0043	0.0011	0.0012	0.0006	0.0006
$(\epsilon_{DG4} - \epsilon_{DG1})$ / ϵ_{DG1}	+5.92		<u>+3.70%</u>		+5.61%		+3.03%	



Hadronic Recoil Analysis: SuperB configs(II)

* Efficiency table for neutral reconstructed Breco

neutral Breco	<u>B0B0bar</u>		BpBm		ccbar		uds	
	DG_1	DG_4	DG_1	DG_4	DG_1	DG_4	DG_1	DG_4
≥ 1 Breco	0.0198	0.0202	0.0090	0.0092	0.0084	0.0086	0.0015	0.0015
deltaE cut	0.0174	0.0178	0.0077	0.0079	0.0068	0.0071	0.0011	0.0011
mES cut	0.0039	0.0039	0.0009	0.0009	0.0007	0.0007	0.0001	0.0001
$(\epsilon_{DG4} - \epsilon_{DG1}) / \epsilon_{DG1}$	<u>+1.76%</u>		+1.45%		+2.16%		+2.79%	

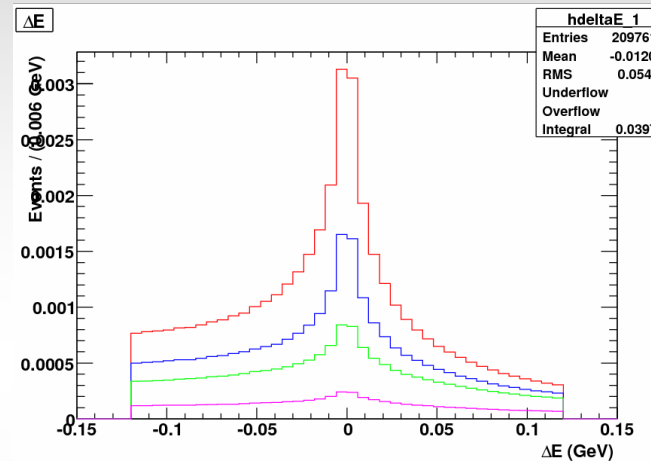
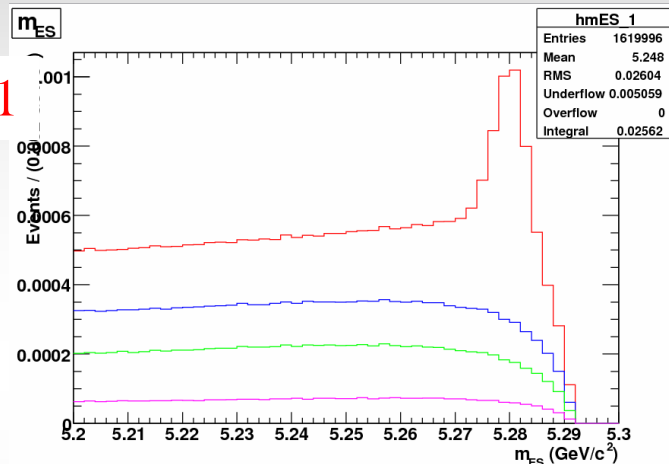


Hadronic Recoil Analysis: SuperB configs(III)



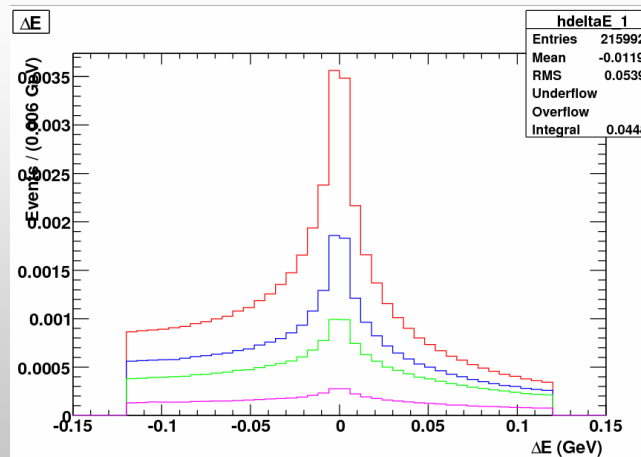
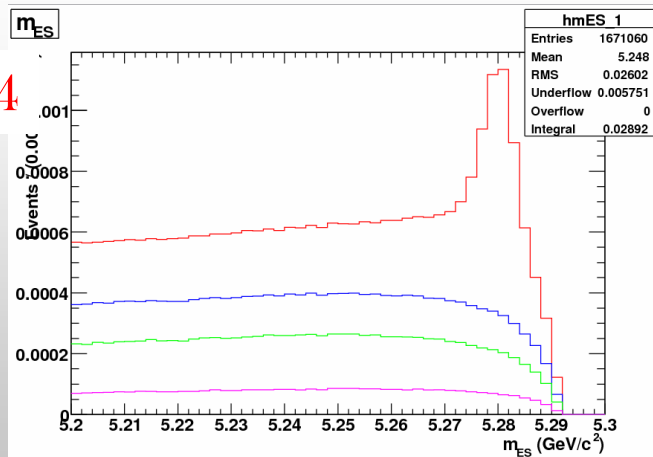
* charged Breco, ΔE before selection, and m_{ES} after ΔE selection

DG_1



— uds
 — uds + ccbar
 — uds + ccbar + B0B0
 — uds + ccbar + B0B0 + B+B-

DG_4



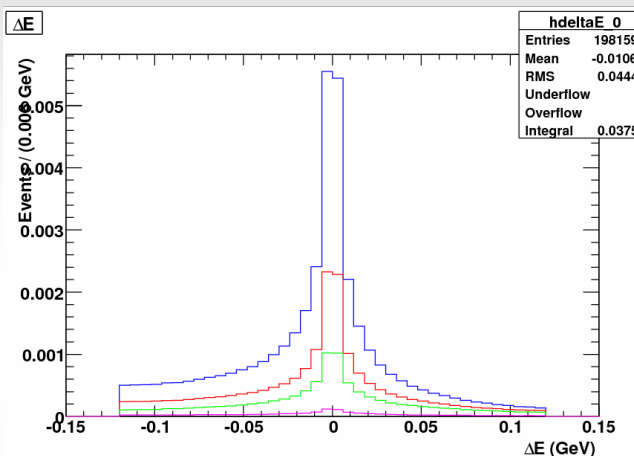
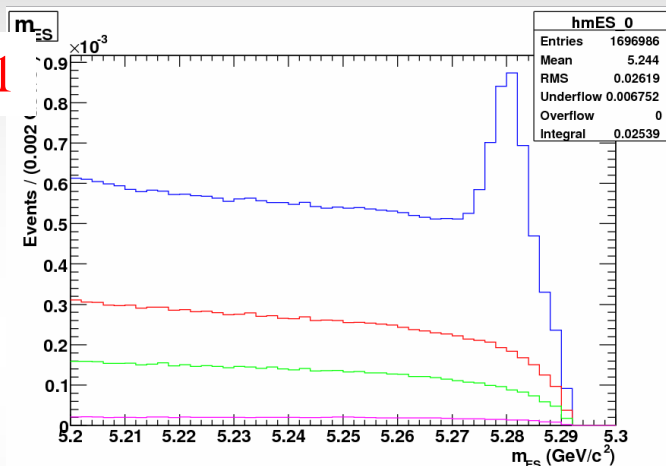
— uds
 — uds + ccbar
 — uds + ccbar + B+B-
 — uds + ccbar + B+B- + B0B0



Hadronic Recoil Analysis: SuperB configs(IV)

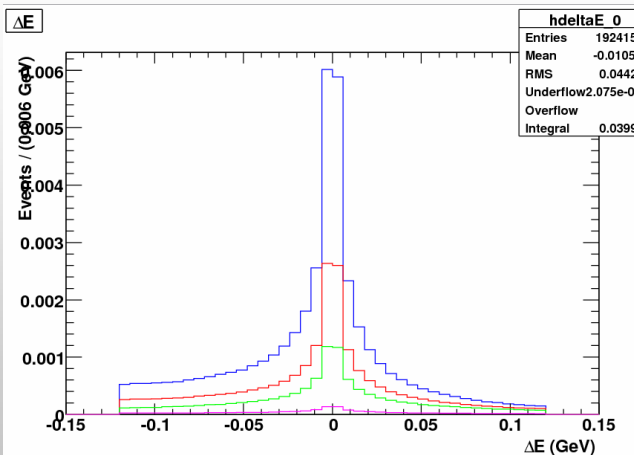
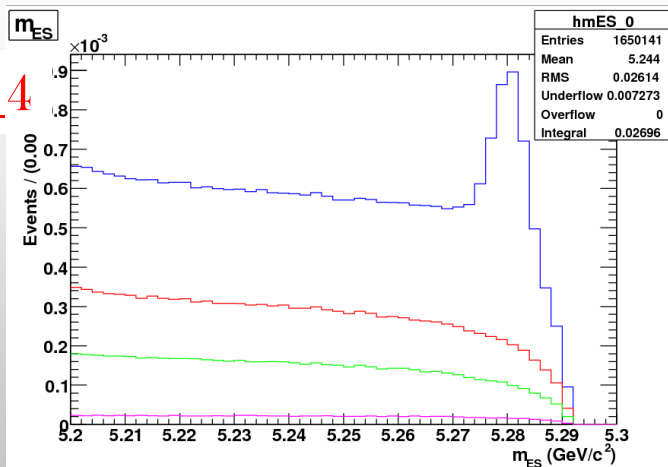
neutral Breco, ΔE before selection, and m_{ES} after ΔE selection

DG_1



- uds
- uds + ccbar
- uds + ccbar + B0B0
- uds + ccbar + B0B0 + B+B-

DG_4



- uds
- uds + ccbar
- uds + ccbar + B+B-
- uds + ccbar + B+B- + B0B0



Signal Side Analysis



B → K_{sv}: efficiency studies

BaBar cut and count analysis

- Selection:

$$Q_{\text{tag}} = \pm 1$$

$$5.270 < m_{\text{ES}} < 5.288 \text{ GeV}/c^2$$

$$|\cos\theta_{\text{Breco,Thrust}}| < 0.85$$

K candidate from Bsig

$$|\cos\theta_{\text{trk}}^*| < 0.85$$

$$N_{\text{extraTrk}} < 3$$

$$E_{\text{extra}} < 0.4 \text{ GeV}$$

$$N_{\pi^0} = 0$$

$$p_{\text{K}}^{\text{B}} > 1.1 \text{ GeV}/c$$

$$-0.85 < \cos\theta_{\text{pmiss}} < 0.9$$

$$\epsilon_{\text{TOT}} = 7.2 \times 10^{-4}$$

(no systematics or corrections included)

- reconstructed Breco modes = neat + clean + dirty

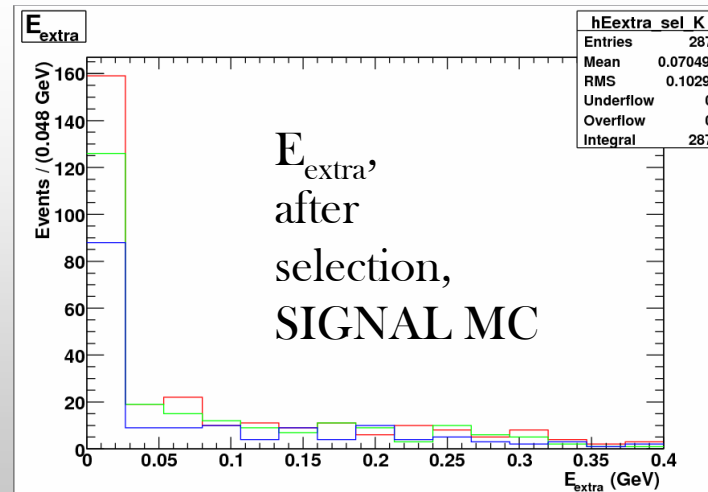
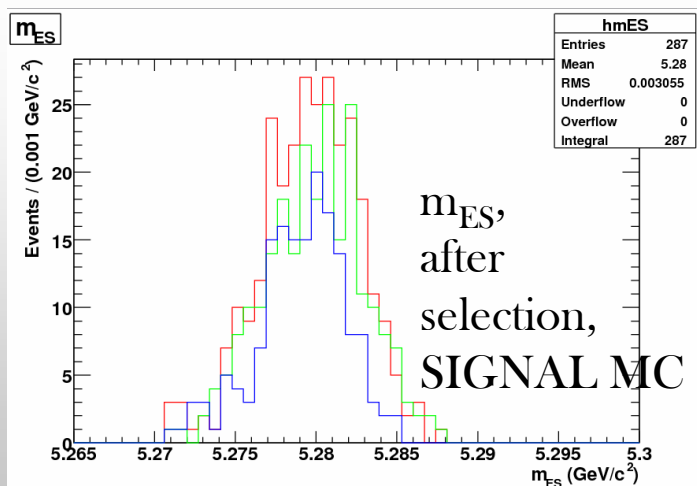
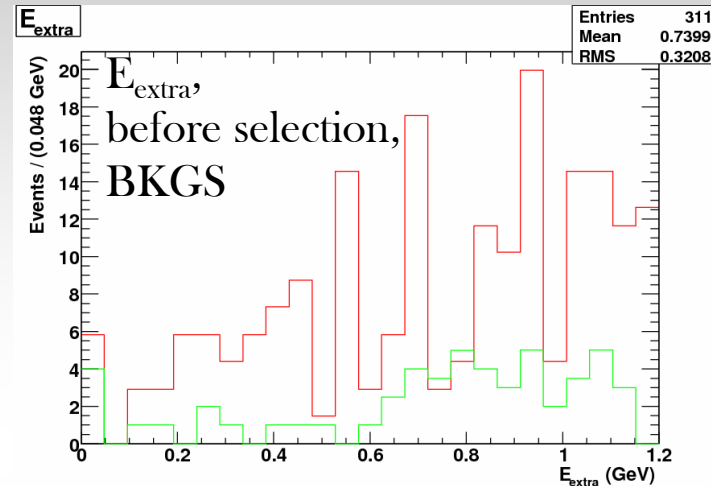
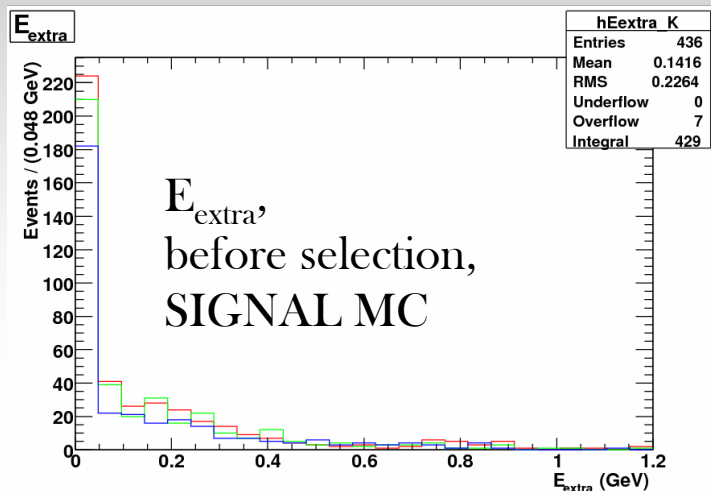
* SuperB: applying BaBar cuts **BUT** $N_{\text{extraTrk}} = 0$

	DG_BaBar	DG_1	DG_4
$\epsilon_{\text{tot, K}}$	$(1.63 \pm 0.13) \times 10^{-4}$	$(2.36 \pm 0.15) \times 10^{-4}$	$(2.87 \pm 0.17) \times 10^{-4}$
ϵ gain wrt DG_BaBar		+44.8%	+76.1%



B → Kνν: some distributions

- DG_BaBar
- DG_1
- DG_4





B → K* νν: efficiency studies (I)

BaBar cut and count analysis

- Selection:

$B_{sig} - B_{reco}$ charge correlation
 $5.270 < m_{ES} < 5.288 \text{ GeV}/c^2$
 $-0.09 < \Delta E < 0.05 \text{ GeV}$
 $|\cos\theta_{Breco, Thrust}| < 0.85$

channel	selection criteria
$K^{*\pm} \rightarrow K^{\pm} \pi^0$	$0.03 < R_2 < 0.70$ $0.004 < \cos\theta_{thrust}^* < 0.84$ $0.84 < m_{K^*} < 0.95 \text{ GeV}/c^2$ $-0.78 < \cos\theta_{miss}^* < 0.93$
$K^{*\pm} \rightarrow K_s^0 (\pi^+ \pi^-) \pi^{\pm}$	$0.0 < R_2 < 0.49$ $0.0 < \cos\theta_{thrust}^* < 0.85$ $0.86 < m_{K^*} < 0.95 \text{ GeV}/c^2$ $0.49 < m_{K_s^0} < 0.50 \text{ GeV}/c^2$ $-0.82 < \cos\theta_{miss}^* < 0.82$
$K^{*0} \rightarrow K^- \pi^+$	$0.06 < R_2 < 0.53$ $0.002 < \cos\theta_{thrust}^* < 0.85$ $0.85 < m_{K^*} < 0.97 \text{ GeV}/c^2$ $-0.86 < \cos\theta_{miss}^* < 0.90$

$E_{miss}^* + c p_{miss}^* > 4.5 \text{ GeV}$
 $E_{extra} < 0.3 \text{ GeV}$

- reconstructed Breco

modes = neat + clean + dirty

$\epsilon_{TOT} (B^+ \rightarrow K^{*+} (K^+ \pi^0) \nu \nu) = 1.01 \times 10^{-4}$
 $\epsilon_{TOT} (B^+ \rightarrow K^{*+} (K_S \pi^+) \nu \nu) = 0.74 \times 10^{-4}$
 $\epsilon_{TOT} (B^0 \rightarrow K^{*0} (K^+ \pi^-) \nu \nu) = 1.74 \times 10^{-4}$
 (no systematics or corrections included)



B → K* νν: efficiency studies (I)

SuperB: applying BaBar cuts BUT R_2 , m_{K_S} (not filled correctly at rootuple level)

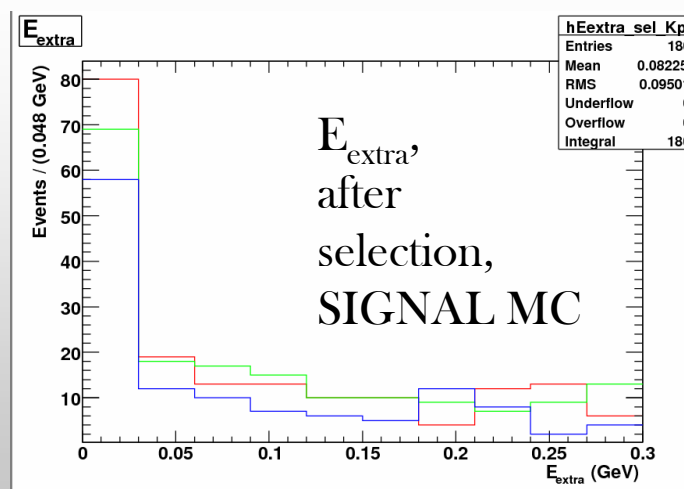
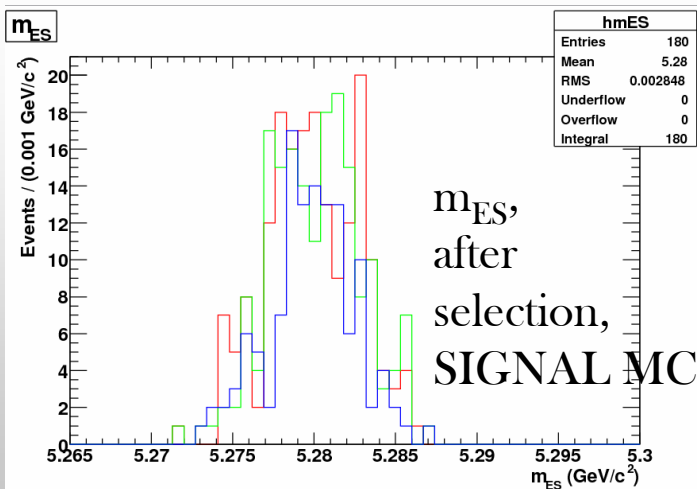
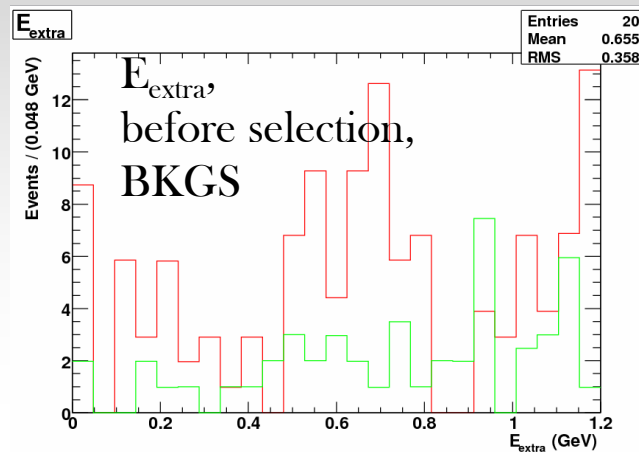
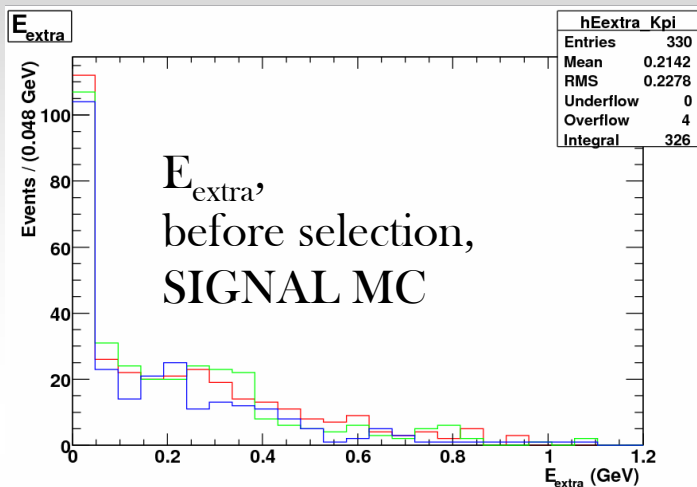
	DG_BaBar	DG_1	DG_4
$\epsilon_{\text{tot}, K^*0(K+\pi^-)}$	$(0.82 \pm 0.09) \times 10^{-4}$	$(1.18 \pm 0.10) \times 10^{-4}$	$(1.20 \pm 0.11) \times 10^{-4}$
ϵ gain wrt DG_BaBar		+42.7%	+45.2%
$\epsilon_{\text{tot}, K^{*+}(K+\pi^0)}$	$(0.40 \pm 0.06) \times 10^{-4}$	$(0.46 \pm 0.07) \times 10^{-4}$	$(0.50 \pm 0.07) \times 10^{-4}$
ϵ gain wrt DG_BaBar		+15.0%	+25.0%
$\epsilon_{\text{tot}, K^{*+}(K_S\pi^+)}$	$(0.43 \pm 0.07) \times 10^{-4}$	$(0.55 \pm 0.07) \times 10^{-4}$	$(0.64 \pm 0.08) \times 10^{-4}$
ϵ gain wrt DG_BaBar		+27.9%	+48.8%



$B \rightarrow K^* \nu \bar{\nu}$: some distributions (I)

— DG_BaBar
— DG_1
— DG_4

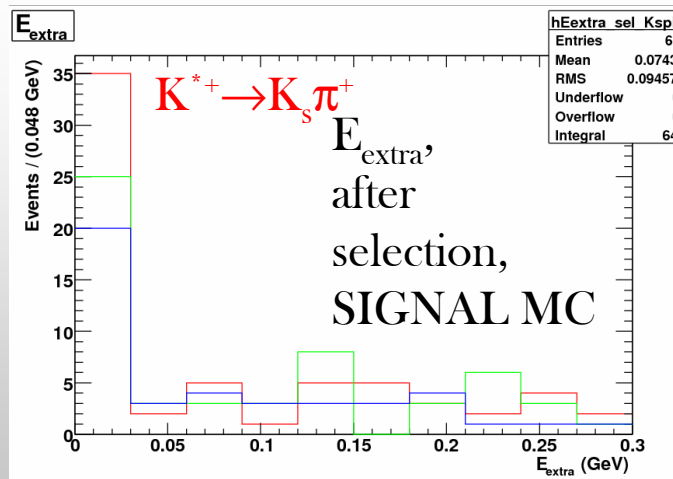
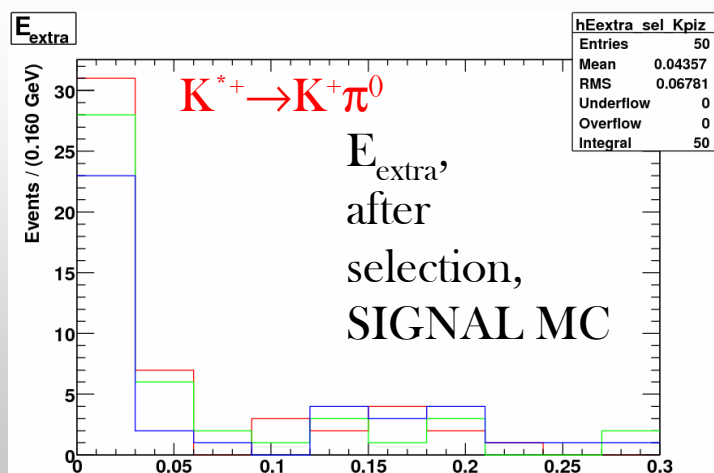
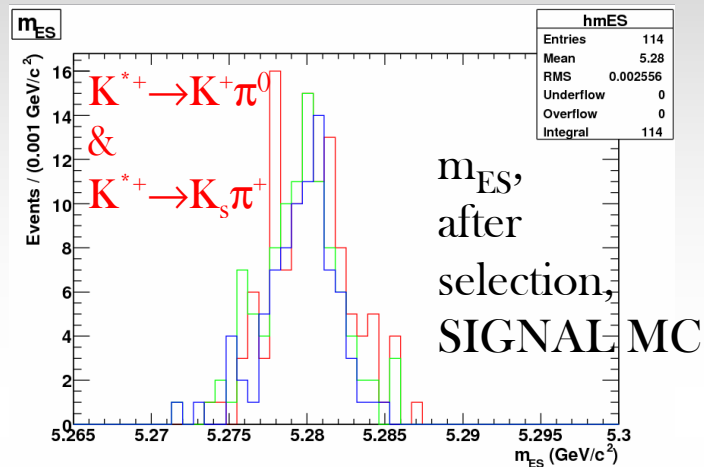
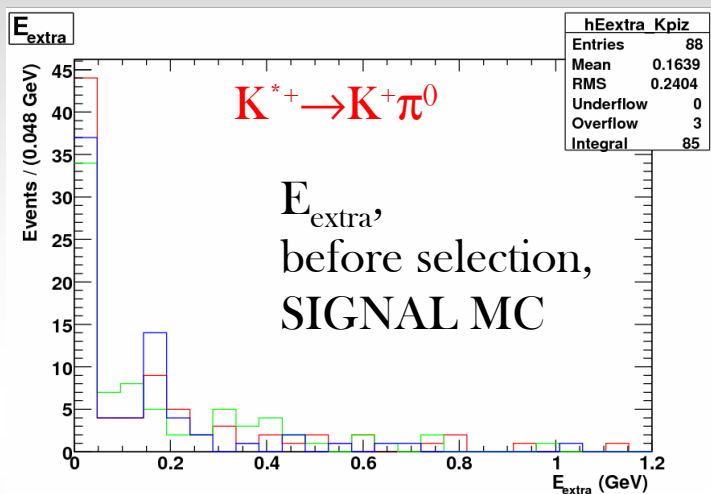
$$K^{*0} \rightarrow K^+ \pi^-$$





B → K* νν: some distributions (I)

— DG_BaBar
 — DG_1
 — DG_4





SuperB expected sensitivity



Method and uncertainties treatment

K*_{nunu}:

- FastSim : cut and count analysis (optimization done in BaBar)
 - BaBar published result: results extracted by fitting Neural Network output
- not straightforward to extrapolate BaBar results in SuperB scenario

* Knunu: applied same cut and count analysis as done in BaBar

* Compare:

- BaBar results, scaling with lumi
- SuperB DG_1 configuration
- SuperB DG_4 configuration

* start from BaBar efficiencies & Backgrounds, BaBar analysis technique

* estimate a **background reduction** of 10%, use the **efficiency gain** evaluated by comparing DG_BaBar and DG_1/DG_4

* **Systematic uncertainties**

BaBar: systematics largely dominated by MC statistics; Syst. error expected to go down with:
 $1/\sqrt{\text{MC stat}} \sim 1/\sqrt{\text{Luminosity}}$

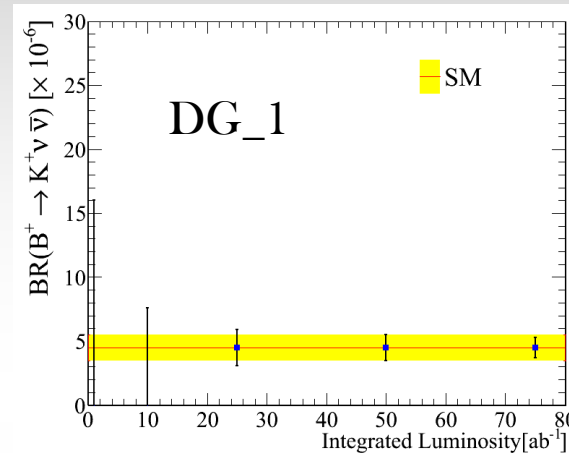
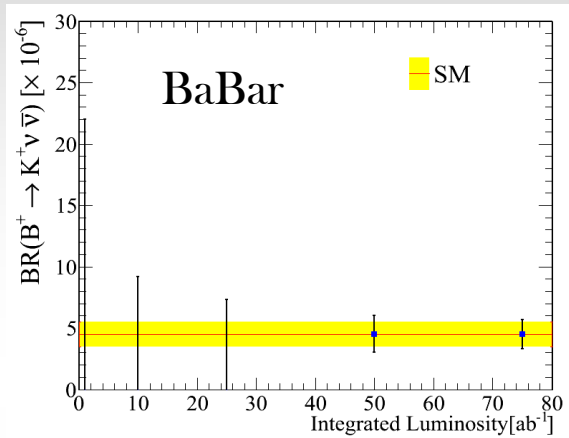
SuperB: assume a syst. error equal to the stat. error;

BR(B→Kvv) Expected sensitivity



BR as a function of luminosity

Preliminary



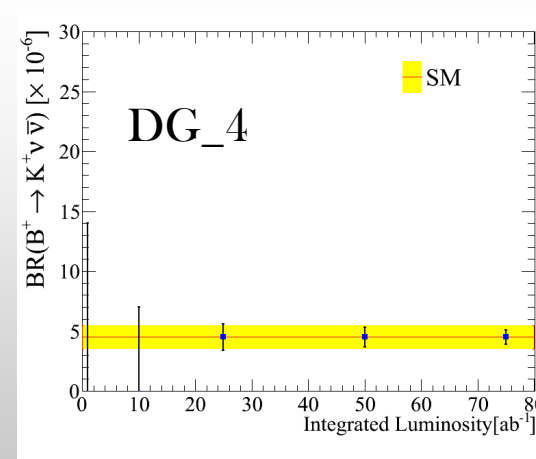
* statistics needed for signal evidence @ 3σ significance (just few scanned points)

BaBar config → 50 ab⁻¹

DG_1 → 25 ab⁻¹

DG_4 → 25 ab⁻¹ (smaller error wrt DG_1)

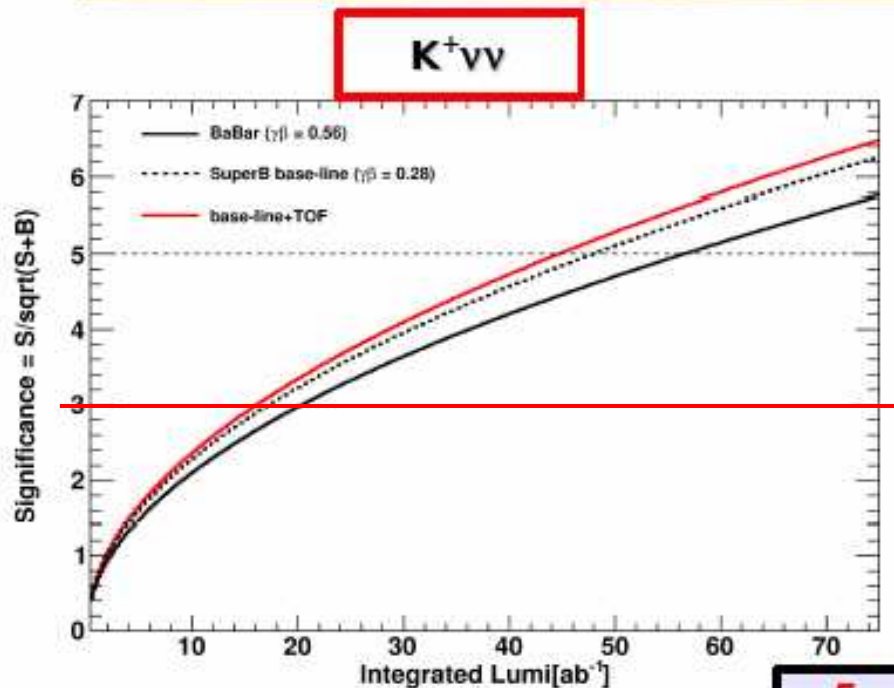
* better can be done by improving the analysis and combining with SL recoil





BR(B→Kνν) SL recoil, expected sensitivity

B⁺→K⁺νν (SL): Extrapolation



- 5σ significance (stat-only):**
- BaBar: ~55ab⁻¹
 - SuperB-base line: ~48ab⁻¹
 - +TOF: ~44ab⁻¹

Alejandro Perez,

Frascati SuperB Workshop Dec. 2nd 2009



Conclusions

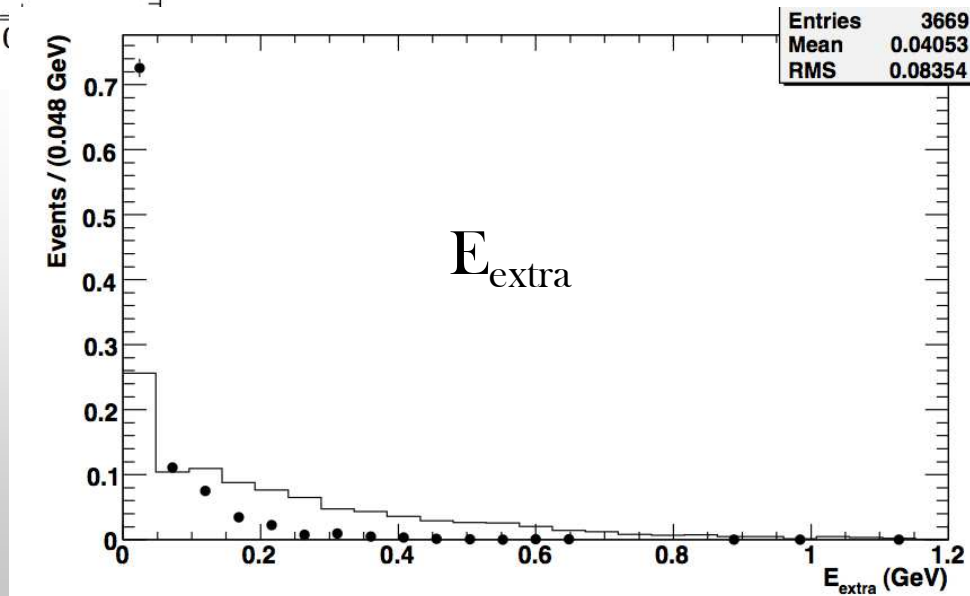
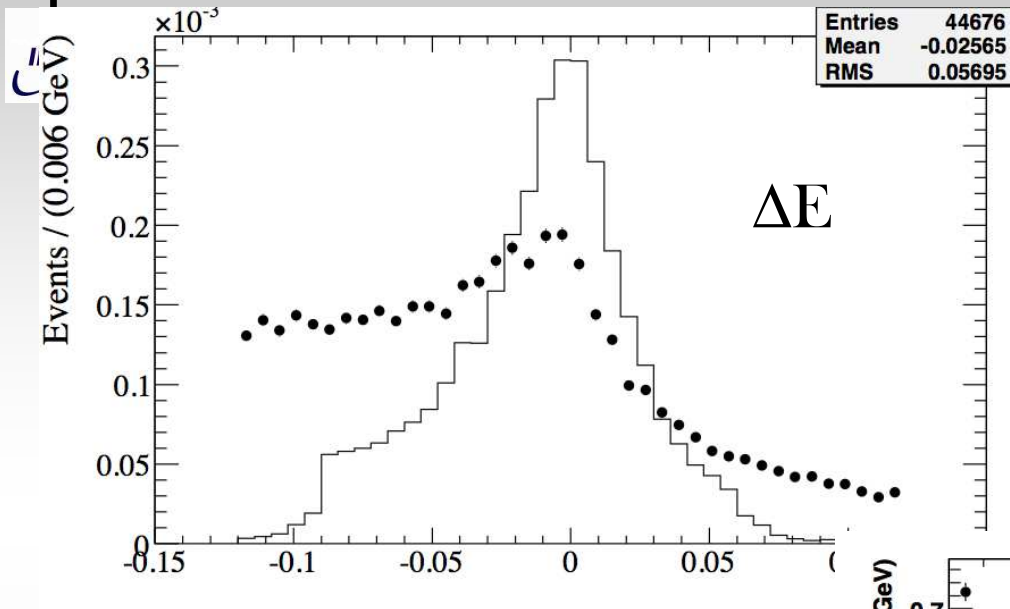
- * Hadronic Breco reconstruction provide high statistic and clean samples
→ searches of B_{sig} channels with invisible particles feasible in the recoil
- * $B \rightarrow K^{(*)} \nu \nu$: one of the SuperB benchmark channels
- * Hadronic Recoil Analysis Method and Superb Fast Simulation
- * Generic background and signal MC samples production performed
- * comparison with BaBar FullSim:
 - quite good agreement for charged Breco, still some work to do for the neutral
- * test SuperB detector geometry configuration
 - DG_4 gives higher statistics wrt DG_1, but also higher background contamination
 - DG_4 selection variables may be more discriminant → more statistics needed
- * SuperB expected sensitivity on $B \rightarrow K^{(*)} \nu \nu$ branching fractions
 - extrapolation for $K^{*} \nu \nu$ not straightforward
 - evidence for $B \rightarrow K \nu \nu$ signal @ $25 ab^{-1}$ (assuming SM BR, HAD cut and count analysis only)



Back-up slides



FastSim V.0.0.3 vs BaBar FullSim





Bkg efficiency, before signal side selection

Knunu

- BRR) bz = $5e-07$ bp : $5.44e-06$ cc : $5.8e-07$
- DG1) bz = $3.59848e-07$ (-28%) bp = $4.87854e-06$ (-10%) cc = $8.4e-07$ (+45%)
- DG4) bz = $3.52697e-07$ (-29%) bp = $5.23614e-06$ (-4%) cc = $7.83133e-07$ (+35%)

* Kstar0nunu

- BRR) bz = $1.88e-06$ bp : $3.5e-06$ cc : $3e-07$
- DG1) bz = $1.36364e-06$ (-27%) bp = $1.78138e-06$ (-49%) cc = $4.4e-07$ (+47%)
- DG4) bz = $1.53527e-06$ (-19%) bp = $2.25873e-06$ (-35%) cc = $4.21687e-07$ (+40%)

* Kstarpnunu

- Kspi

- BRR) bz = $9.4e-07$ bp : $6.6e-06$ cc : $8e-07$
 DG1) bz = $1.00379e-06$ (+7%) bp = $6.33603e-06$ (-4%) cc = $9.4e-07$ (+17%)
 DG4) bz = $1.20332e-06$ (+28%) bp = $6.55031e-06$ (-1%) cc = $1.1245e-06$ (+40%)

- Kpiz

- BRR) bz = $9.4e-07$ bp : $6.6e-06$ cc : $8e-07$
 DG1) bz = $1.13636e-07$ (-88%) bp = $9.7166e-07$ (-85%) cc = $2.4e-07$ (-70%)
 DG4) bz = $1.24481e-07$ (-87%) bp = $1.00616e-06$ (-84%) cc = $3.21285e-07$ (-60%)