

# Testing SUSY Flavour Models at Super*B*

based on arXiv:0909.1333 [hep-ph]

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in collaboration with  
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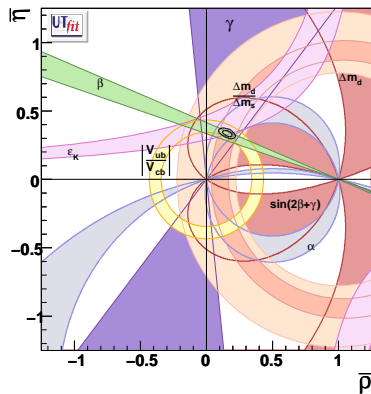
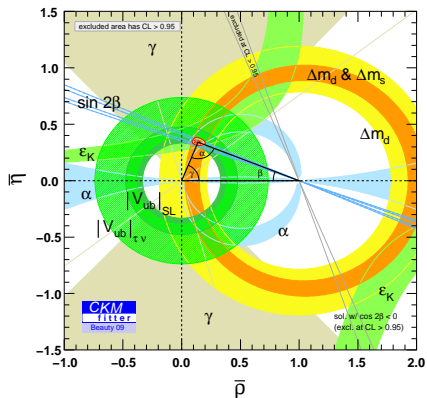


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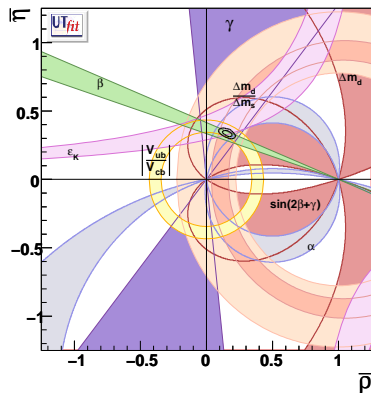
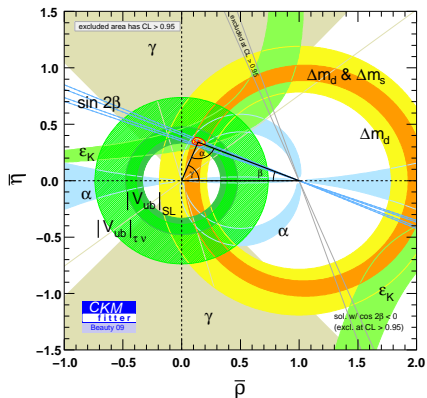


- 1 Hints for New Physics?
- 2 The SUSY flavour problem & flavour models
- 3 Flavour models &  $B$  decays: numerical results
- 4 Summary

# Status of CKM fits



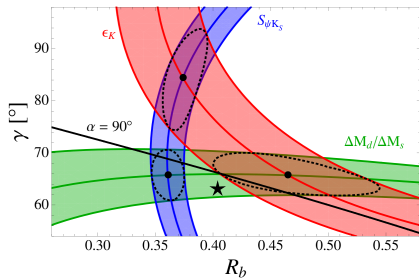
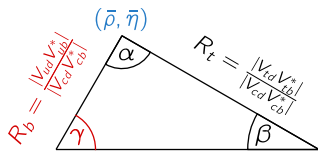
Impressive confirmation of the CKM mechanism of CP violation!



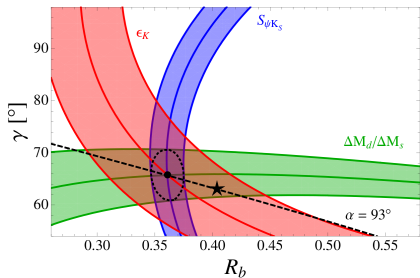
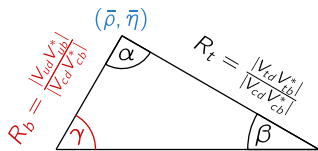
Impressive confirmation of the CKM mechanism of CP violation!

With some small tensions ...

- Recent theoretical improvements in  $\epsilon_K$  expose some tensions in the UT analysis [Lunghi & Soni, Buras & Guadagnoli]
- Look at  $\epsilon_K$ ,  $S_{\psi K_S}$  ( $\sin 2\beta$ ),  $\Delta M_d/\Delta M_s$  in the  $R_b$ - $\gamma$  plane
- $R_b$ ,  $\gamma$  can be obtained from tree-level processes



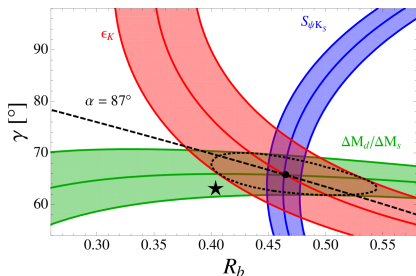
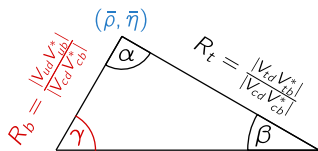
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Possible solutions:

- +24% NP effect in  $\epsilon_K$

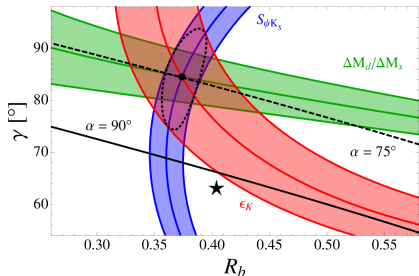
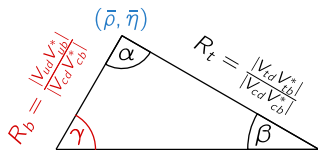
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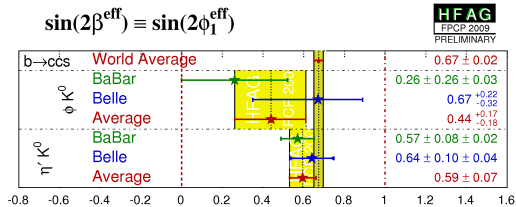
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- $-6.5^\circ$  NP phase in  $B_d$  mixing
- $-22\%$  NP effect in  $\Delta M_d / \Delta M_s$  (requiring  $\alpha \sim 74^\circ$ )

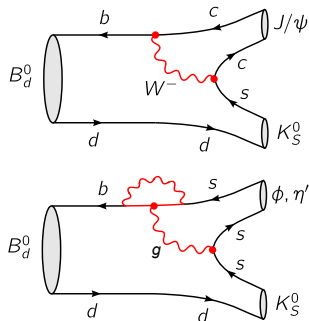


- In the SM, mixing-induced CP asymmetries in  $B_d \rightarrow \psi K_S, \phi K_S, \eta' K_S$  all  $\approx \sin 2\beta$
- $B_d \rightarrow \psi K_S$  dominated by tree level,  $\phi K_S$  and  $\eta' K_S$  are loop-induced

Data indicate  $S_{\phi K_S} < S_{\eta' K_S} < S_{\psi K_S}$



[adapted from HFAG]

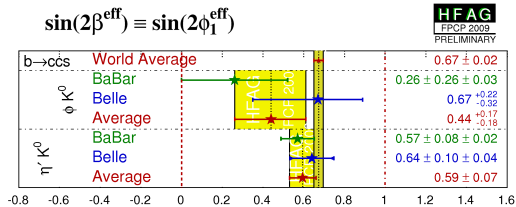


New physics in the decay amplitudes?

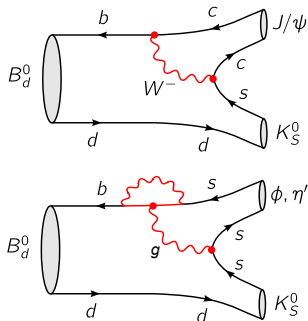
# $\sin 2\beta_{\text{eff}}$ tensions

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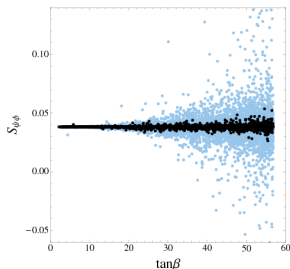
New physics in the decay amplitudes?

Can only be resolved at SuperB

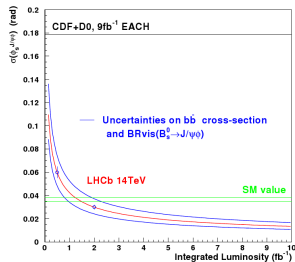
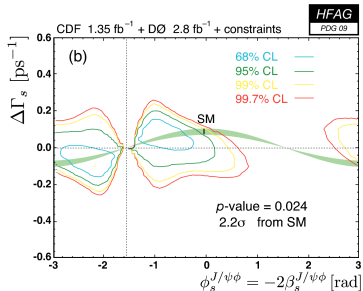
- $S_{\psi\phi}$ : mixing-induced CP asymmetry in  $B_s \rightarrow J/\psi\phi$
- $S_{\psi\phi} = \sin 2(\beta_s + \phi_{B_s}^{\text{NP}})$
- $S_{\psi\phi}^{\text{SM}} \approx 0.035$

Recent Tevatron data favour  
 $0.20 \leq S_{\psi\phi} \leq 0.98$

New physics in the  $B_s$  mixing phase?



- Sizable  $S_{\psi\phi}$  impossible in MFV MSSM
- Will be measured at LHCb



## Main goals of our analysis:

- 1 Find well-motivated SUSY models which can generate large effects in  $S_{\psi\phi}$
- 2 Check whether  $S_{\phi K_S}$  anomaly and UT tensions can be solved as well

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- 3 How can Super*B* help distinguish between these models?

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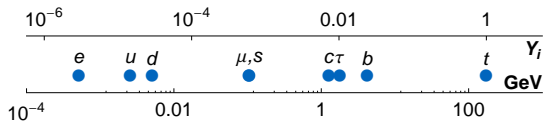
## The SUSY flavour problem

- Most of the 105 additional parameters in the MSSM violate flavour
- $O(1)$  values are strongly disfavoured by the excellent agreement of the SM with the flavour data

## Possible solutions

- 1 Decoupling
  - ▶ Sfermion mass scale very high
  - ▶ Clashes with the gauge hierarchy problem
- 2 Degeneracy
  - ▶ Sfermion masses nearly degenerate
  - ▶ Arises in models with low-scale SUSY breaking
  - ▶ Partly spoiled by RG evolution
- 3 Alignment
  - ▶ Quark and squark mass matrices aligned

Flavour violation is highly non-generic already in the SM!

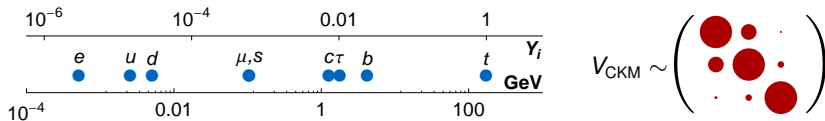


$$V_{\text{CKM}} \sim \begin{pmatrix} \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet \end{pmatrix}$$

The two problems should be related!



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## Minimal Flavour Violation (MFV)

- Yukawa couplings are the only sources of flavour violation
- Effective theory
- Pragmatic approach
- Pessimistic phenomenology

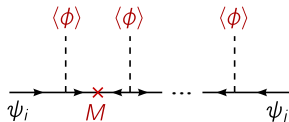
## Flavour Models

- Flavour structure of Yukawa couplings and soft terms generated by spontaneous breaking of a flavour symmetry
- Ambitious approach
- Diverse phenomenology

Main idea: hierarchies in Yukawa couplings generated by spontaneous breakdown of flavour symmetry (horizontal symmetry, family symmetry)

- Generalization of the Froggatt-Nielsen mechanism
- Yukawa hierarchies explained by different powers of small  $\epsilon$ :

$$\Rightarrow Y_{ij} \propto \left( \frac{\langle \phi \rangle}{M} \right)^{(a_i+b_j)} = \epsilon^{(a_i+b_j)}$$



- Possible to **relate Yukawa** matrices and **sfermion** mass matrices/trilinear couplings

SUSY flavour models can explain the origin of the hierarchies in the Yukawa couplings *and* solve the SUSY flavour problem

- Many different viable models exist, with abelian or non-abelian flavour symmetries

## The SUSY CP problem

$O(1)$  values for many of the  $O(50)$  phases in the MSSM are strongly disfavoured by experimental bounds, in particular EDMs

### Common solution in Flavour Models:

- CP is conserved in the “underlying” theory
- CP broken spontaneously by flavon VEVs
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### Applying the same approach to MFV: [Paradisi & DS, 0906.4551]

- The MFV principle does not forbid new phases beyond the CKM
- Assume CP conservation in the limit of flavour blindness
- CP violated by MFV-compatible terms breaking the flavour blindness
- **Viable but interesting** CP-phenomenology

## Abelian vs. Non-abelian

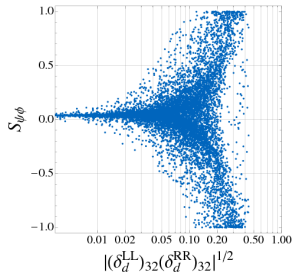
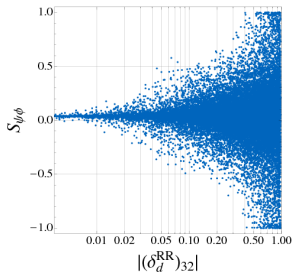
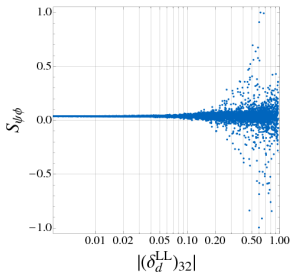
- In most non-abelian models, 1st & 2nd generatio sfermions are **approximately degenerate**
  - ▶ Suppressed contributions to  $1 \leftrightarrow 2$  transitions, in particular  $D^0-\bar{D}^0$  mixing
- In abelian models, sfermions of different generations need **not be degenerate**
  - ▶  $O(1)$  1-2 mass splitting leads to  $O(\lambda) (\delta_{\bar{u}}^{LL})_{12}$  in the SCKM basis
  - ▶ Large effects in  $D^0-\bar{D}^0$  mixing

## Chirality structure of flavour violating terms

- Different flavour symmetries lead to different patterns of flavour violation
- Mass insertions:  $M_d^2 = \text{diag}(\tilde{m}^2) + \tilde{m}^2 \begin{pmatrix} \delta_d^{LL} & \delta_d^{LR} \\ \delta_d^{RL} & \delta_d^{RR} \end{pmatrix}$
- $\delta^{LL}$ ,  $\delta^{RR}$ ,  $\delta^{LR}$  fixed by the flavour symmetry (up to  $O(1)$  factors)

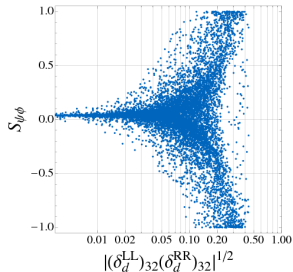
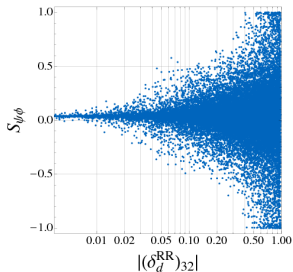
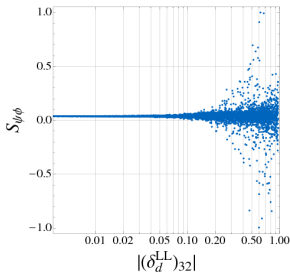
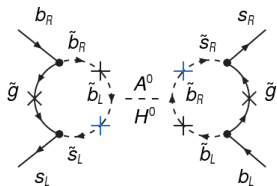
How to generate large NP effects in  $S_{\psi\phi}$ ?

- LR MIs strongly constrained by  $b \rightarrow s\gamma$
- Sizable effects in  $S_{\psi\phi}$  possible in particular with simultaneous LL and RR MIs
- LL MIs are always generated by RG effects even if vanishing at the GUT scale



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4 representative flavour models with different chirality structures in the  $\tilde{d}$  sector:

AC model

[Agashe, Carone]

$U(1)$

Large,  $O(1)$  RR  
mass insertions

AKM model

[Antusch, King, Malinsky]

$SU(3)$

Only CKM-like RR  
mass insertions

RVV model [Ross,

Velasco-Sevilla, Vives]

$SU(3)$

CKM-like LL & RR  
mass insertions

$\delta$ LL model

[e.g. Hall, Murayama]

$(S_3)^3$

Only CKM-like LL  
mass insertions

$$\delta_d^{LL} \sim \begin{pmatrix} \cdot & 0 & 0 \\ 0 & \cdot & \lambda^2 \\ 0 & \lambda^2 & \cdot \end{pmatrix}$$

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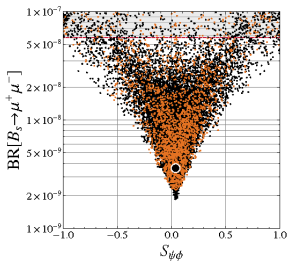
[cf. also Calibbi et al.  
(2009)]



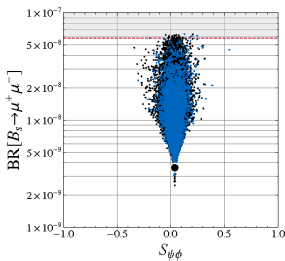
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- Both observables can deviate significantly from the SM in all 3 models
- large  $S_{\psi\phi} \Rightarrow$  large  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$  in the AC and AKM models
- Correlation arises from dominance of Higgs penguin contributions

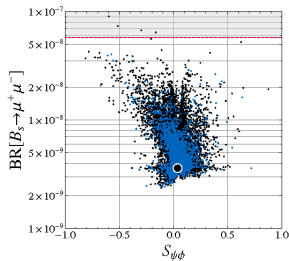
AC



AKM



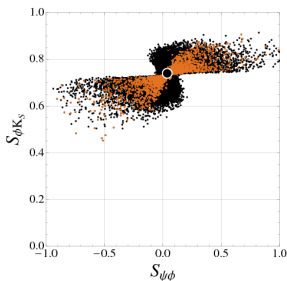
RVV



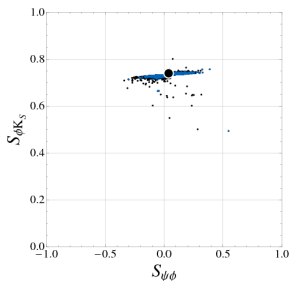
- **Orange points:** UT tension solved through contribution to  $\Delta M_d / \Delta M_s$
- **Blue points:** UT tension solved through contribution to  $\epsilon_K$
- Scan ranges:  $m_0 < 2 \text{ TeV}$ ,  $M_{1/2} < 1 \text{ TeV}$ ,  $|A_0| < 3m_0$ ,  $5 < \tan \beta < 55$ ,  $O(1)$  parameters varied within  $[\frac{1}{2}, 2]$

- In the AC model, both  $S_{\phi K_S}$  and  $S_{\psi\phi}$  can have large effects, but a simultaneous *enhancement* of  $S_{\psi\phi}$  and *suppression* of  $S_{\phi K_S}$  (as indicated by the data) is impossible
- $S_{\phi K_S}$  nearly SM-like in AKM and RVV models

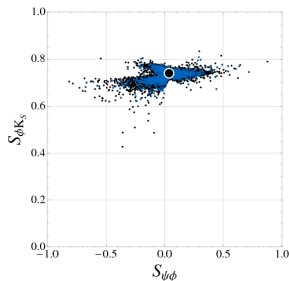
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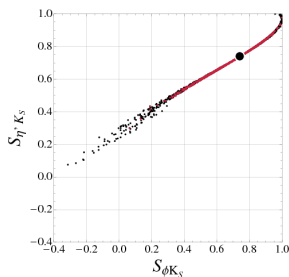
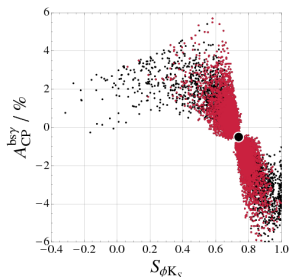
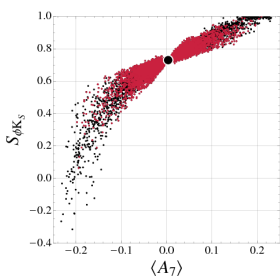
RVV



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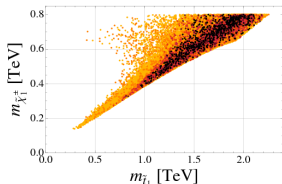
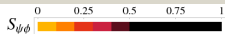
Pattern of NP effects in the  $\delta LL$  model:

- No large effects in  $S_{\psi\phi}$
- Large, correlated effects in  $S_{\phi K_S}$ ,  $S_{\eta' K_S}$ ,  $A_{CP}(b \rightarrow s\gamma)$ ,  $\langle A_{7,8} \rangle$
- $\langle A_{7,8} \rangle$ : T-odd CP asymmetries in  $B \rightarrow K^* \ell^+ \ell^-$

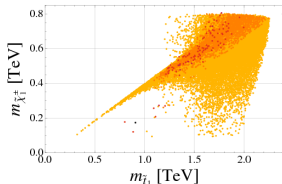
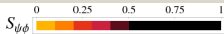


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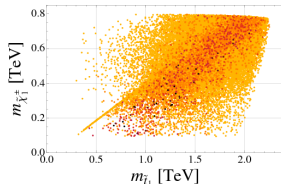
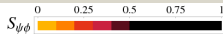
## AC



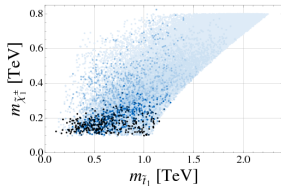
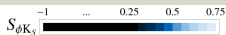
## AKM



## RVV







## $\delta LL$



- Large effects in  $S_{\psi\phi}$  even possible for spectra beyond the LHC reach in the models with RH currents
- Large effects in  $S_{\phi K_S}$  not possible for spectra beyond the LHC reach in the  $\delta LL$  model

# “DNA-Flavour Test” at SuperB

	GMSSM	AC	RVV2	AKM	$\delta$ LL	FBMSSM		
$S_{\phi K_S}$ $A_{CP}(B \rightarrow X_S \gamma)$ $B \rightarrow K^{(*)} \nu \bar{\nu}$ $\tau \rightarrow \mu \gamma$	★★★★	★★★★	●●	■	★★★★	★★★★		
$D^0 - \bar{D}^0$ $A_{7,8}(B \rightarrow K^* \mu^+ \mu^-)$ $A_9(B \rightarrow K^* \mu^+ \mu^-)$	★★★★	★★★★	■	■	■	■		 vs. 
$S_{\psi \phi}$ $B_s \rightarrow \mu^+ \mu^-$	★★★★	★★★★	★★★★	★★★★	■	■		
$\epsilon_K$ $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ $K_L \rightarrow \pi^0 \nu \bar{\nu}$	★★★★	■	★★★★	★★★★	■	■		
$\mu \rightarrow e \gamma$ $\mu + N \rightarrow e + N$ $d_n$ $d_e$ $(g-2)_\mu$	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★		
	★★★★	★★★★	★★★★	★★★★	★★★★	★★★★		
	★★★★	★★★★	★★★★	★★★★	●●	★★★★		
	★★★★	★★★★	★★★★	●●	■	★★★★		
	★★★★	★★★★	★★★★	●●	★★★★	★★★★		