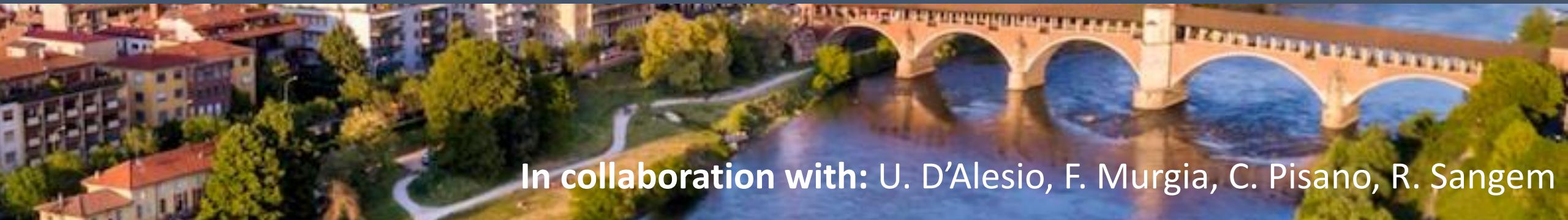


# Transversity 2022

Pavia, 23-27 May 2022

## Polarization phenomenology for quarkonium production in SIDIS



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Speaker: Luca Maxia

Università di Cagliari - INFN CA

Transversity 2022

Date: 26/05/2022



# OUTLINE

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## HERA recap

Section B

## Polarization parameter predictions for EIC ( $\lambda$ and $\nu$ )

Section C

## Rotational invariant predictions for EIC

Section D

## TMD preliminary results for EIC

Section E

# QUARKONIUM PUZZLE

Quarkonium formation is described via different **models**  
different ways to evaluate *short-* and *long-* distance scales

CSM

$$\sigma(\mathcal{Q}) = \hat{\sigma}(Q\bar{Q})|R(0)|^2$$

R. Baier & R. Rückl (1983)  
E.L. Berger & D.L. Jones (1981)

CEM

$$\sigma(\mathcal{Q}) = P_{\mathcal{Q}} \int_{2m_Q}^{M_T} \frac{d\hat{\sigma}(m_{Q\bar{Q}})}{dm_{Q\bar{Q}}} dm_{Q\bar{Q}}$$

H. Fritzsch (1977)  
F. Halzen (1977)

NRQCD

G.T. Bodwin, E. Braaten, G.P. Lepage (1997)  
P. Cho & K. Leibovich (1996)

$$\sigma(\mathcal{Q}) = \sum_n \hat{\sigma}(Q\bar{Q}[n]) \langle \mathcal{O}[n] \rangle$$

FF

G. C. Nayak, J. W. Qiu, G. Sterman (2005)  
Z. B. Kang, J. W. Qiu, G. Sterman (2014)

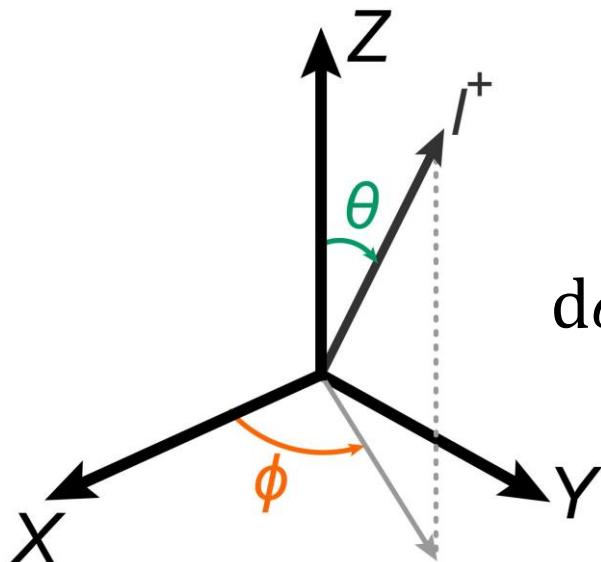
$$\begin{aligned} \sigma_{\mathcal{Q}}(p_T \gg m_{\mathcal{Q}}) = & d\hat{\sigma}_i(p_T/z) \otimes D_{i \rightarrow \mathcal{Q}}(z, m_{\mathcal{Q}}) \\ & + d\sigma_{Q\bar{Q}[c]}(P_{Q\bar{Q}[c]} = p_T/z) \otimes D_{Q\bar{Q}[c] \rightarrow \mathcal{Q}}(z, m_{\mathcal{Q}}) \end{aligned}$$

# ANGULAR STRUCTURE OF THE CROSS SECTION

J/ $\psi$  polarization is accessed by the angular distribution of its decay products

$$J/\psi \rightarrow l^+ l^-$$

Faccioli, Lourenço, Seixas, Wöhri, EPJC 69 (2010)



SIDIS cross section is parameterized as

with  $\Omega(\theta, \phi)$  solid angle of  $l^+$

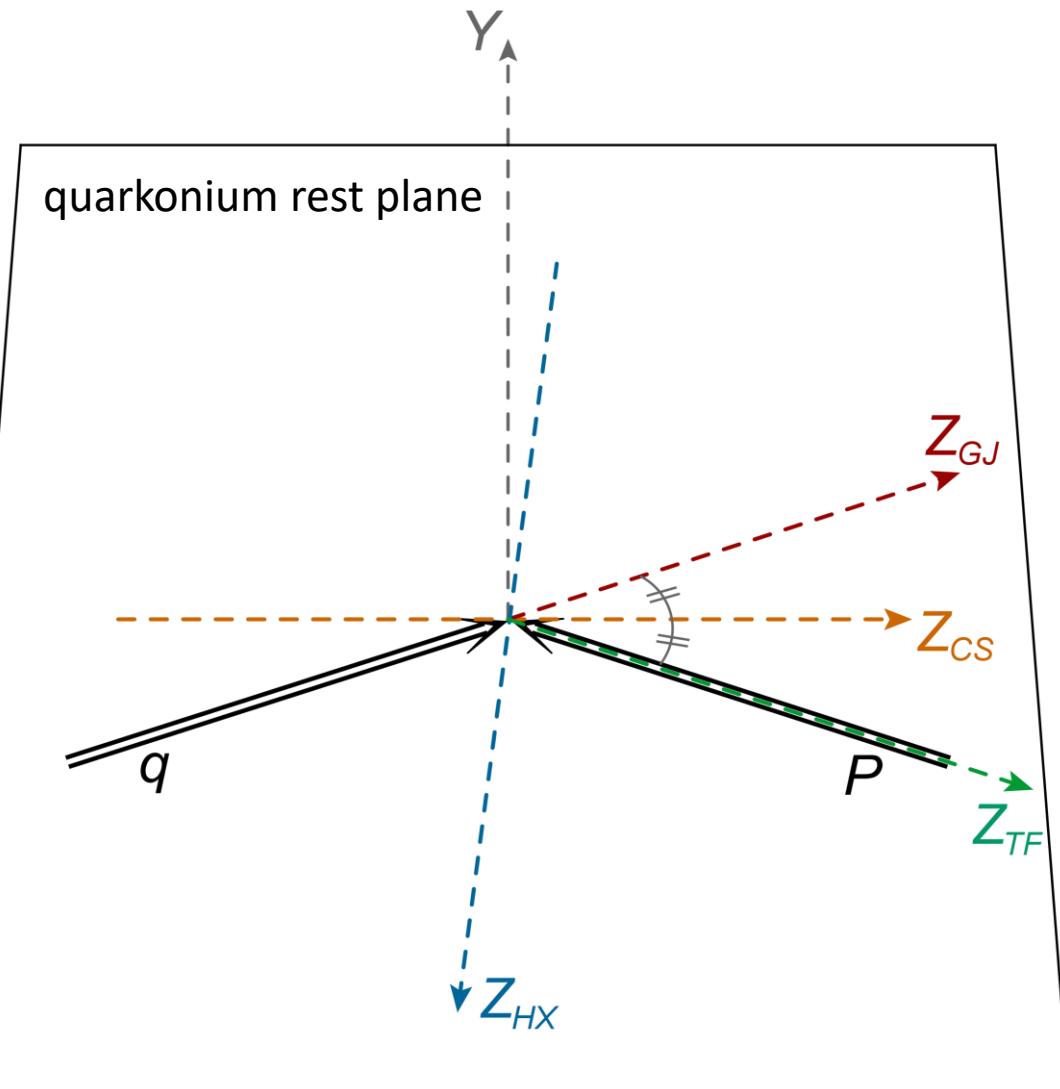
$$d\sigma \propto 1 + \lambda_\theta \cos^2 \theta + \mu_{\theta\phi} \sin 2\theta \cos \phi + \nu_{\theta\phi} \sin^2 \theta \cos 2\phi$$

Angular parameters are defined through ratio of polarized cross sections

This parameterization mimics the DY parameterization

Boer & Vogelsang, PRD 74 (2006)

# SPIN-QUANTIZATION FRAME



J/ψ polarization is studied in the  
*quarkonium rest frame*

$$\gamma^*(q) + p(P) \rightarrow J/\psi(P_\psi) + X$$

Different choices for the reference frame

**GJ**      *Gottfried-Jackson frame*

**CS**      *Collins-Soper frame*

**HX**      *Helicity frame*

**TF**      *Target frame*

Frames are related by a rotation around  $Y$ -axis

# COLLINEAR PHENOMENOLOGY

Typical experimental parameterization is usually adopted for  $d\sigma \equiv \frac{d\sigma}{dx_B dy dz d^4 P_\psi d\Omega}$

$$d\sigma \propto 1 + \lambda_\theta \cos^2 \theta + \mu_{\theta\phi} \sin 2\theta \cos \phi + \frac{\nu_{\theta\phi}}{2} \sin^2 \theta \cos 2\phi$$

$$\lambda_\theta = \frac{\mathcal{W}_T - \mathcal{W}_L}{\mathcal{W}_T + \mathcal{W}_L}$$

$$\mu_{\theta\phi} = \frac{\mathcal{W}_\Delta}{\mathcal{W}_T + \mathcal{W}_L}$$

$$\nu_{\theta\phi} = \frac{2\mathcal{W}_{\Delta\Delta}}{\mathcal{W}_T + \mathcal{W}_L}$$

Next: predictions in CSM and NRQCD  
different LDME choices

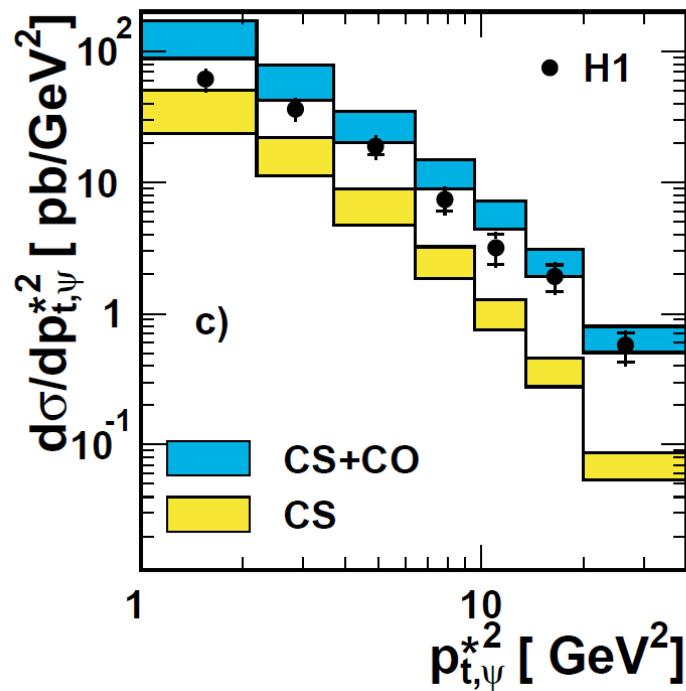
- |      |   |  |
|------|---|--|
| C12  | Chao, Ma, Shao, Wang, Zhang, PRL 108 (2012) | → includes polarization data               |
| G13  | Gong, Wan, Wang, Zhang, PRL 110 (2013)      | → tested on polarization data              |
| BK11 | Butenschoen & Kniehl, PRD 84 (2011)         | → includes low- $P_T$ photoproduction data |

# HERA UNPOLARIZED DATA

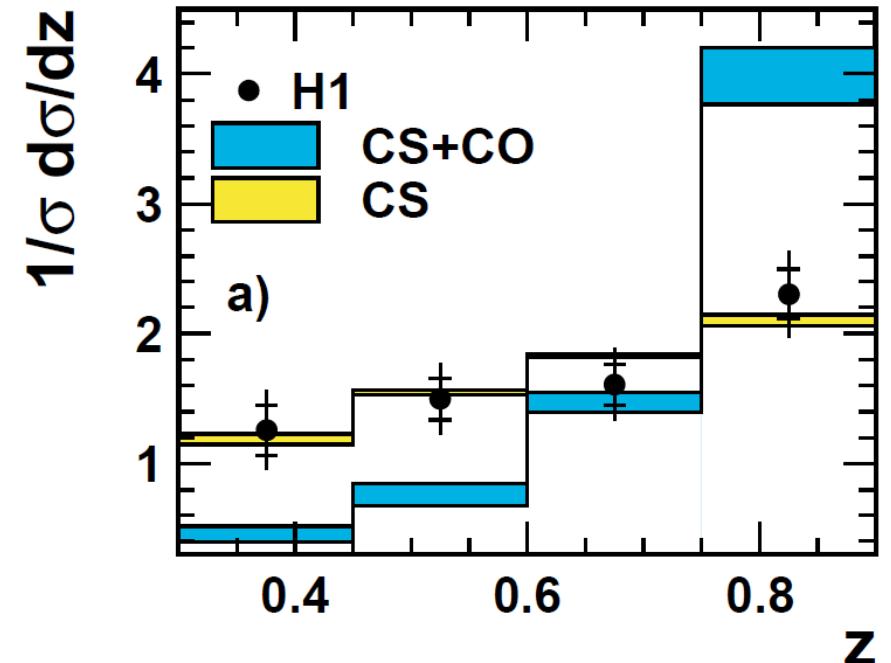
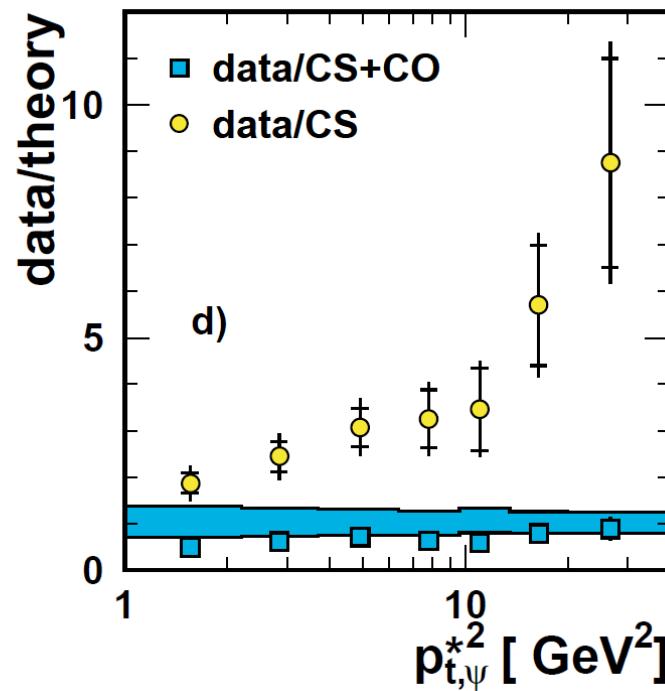
Adloff et al. (H1 Collaboration), EPJ C 25 (2002)

Kniehl & Zwirner, NPB 621 (2002)

Data from HERA collaboration



Theoretical predictions obtained by Kniehl-Zwirner



$P_T$  data show a general better agreement with NRQCD predictions

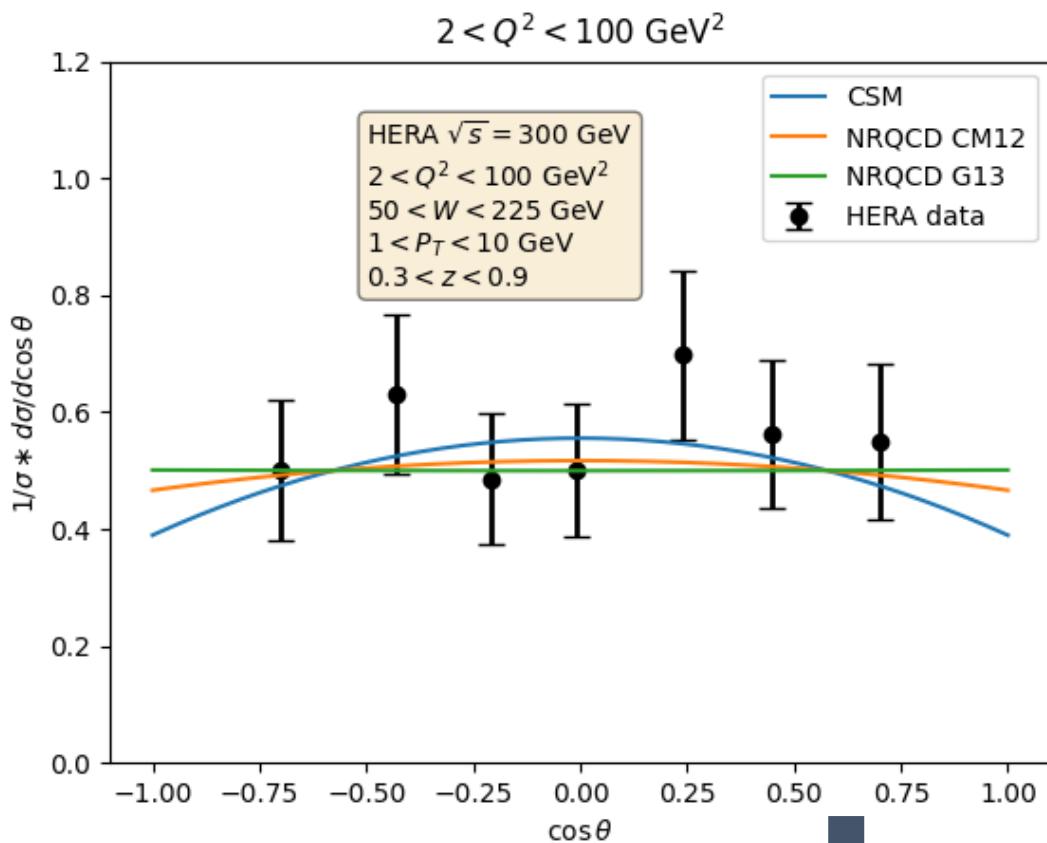
$z$  (multiplicity) data show a general better agreement with CSM predictions

# HERA POLARIZED DATA

Adloff et al. (H1 Collaboration), EPJ C 25 (2002)

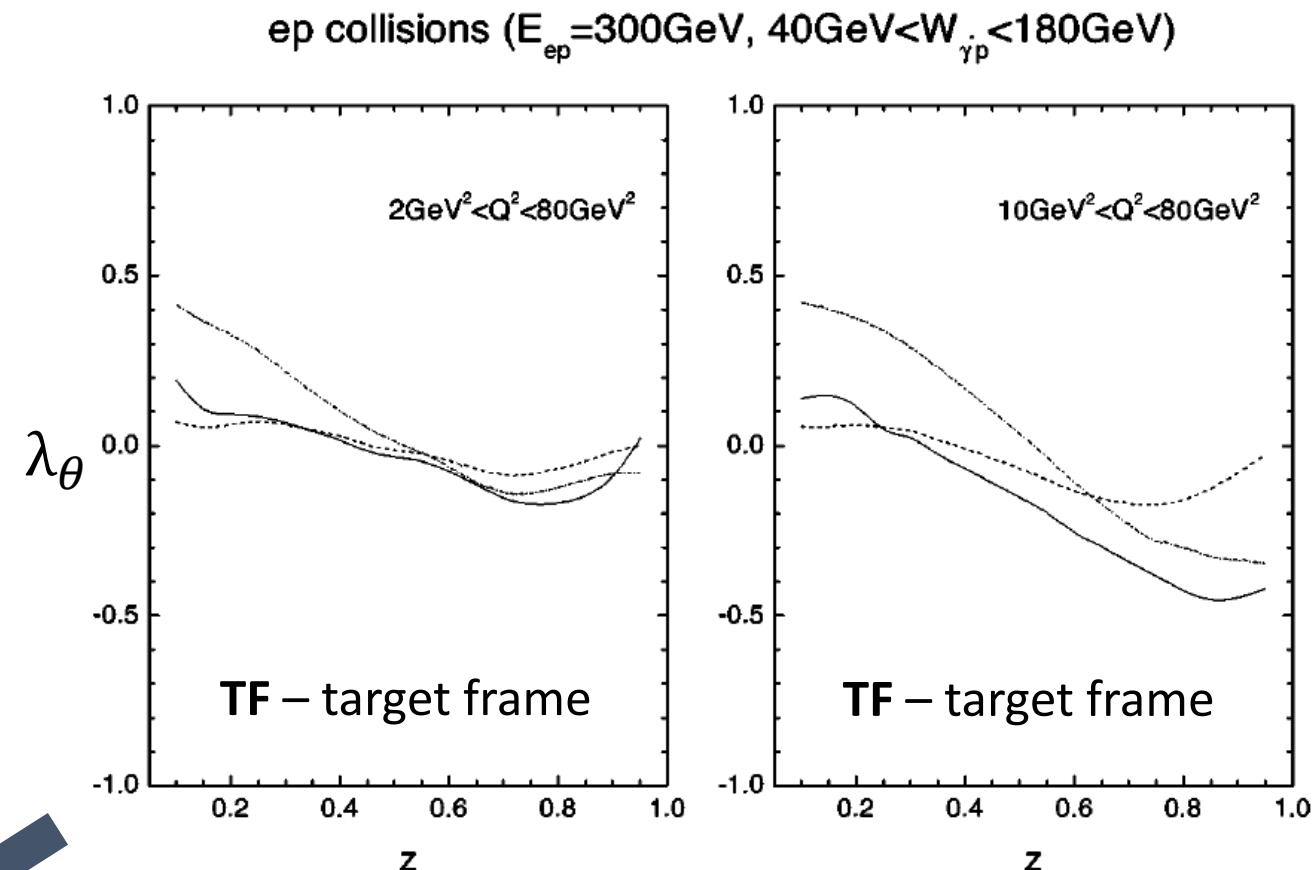
Yuan & Chao, PRD 63 (2001)

Data from HERA collaboration



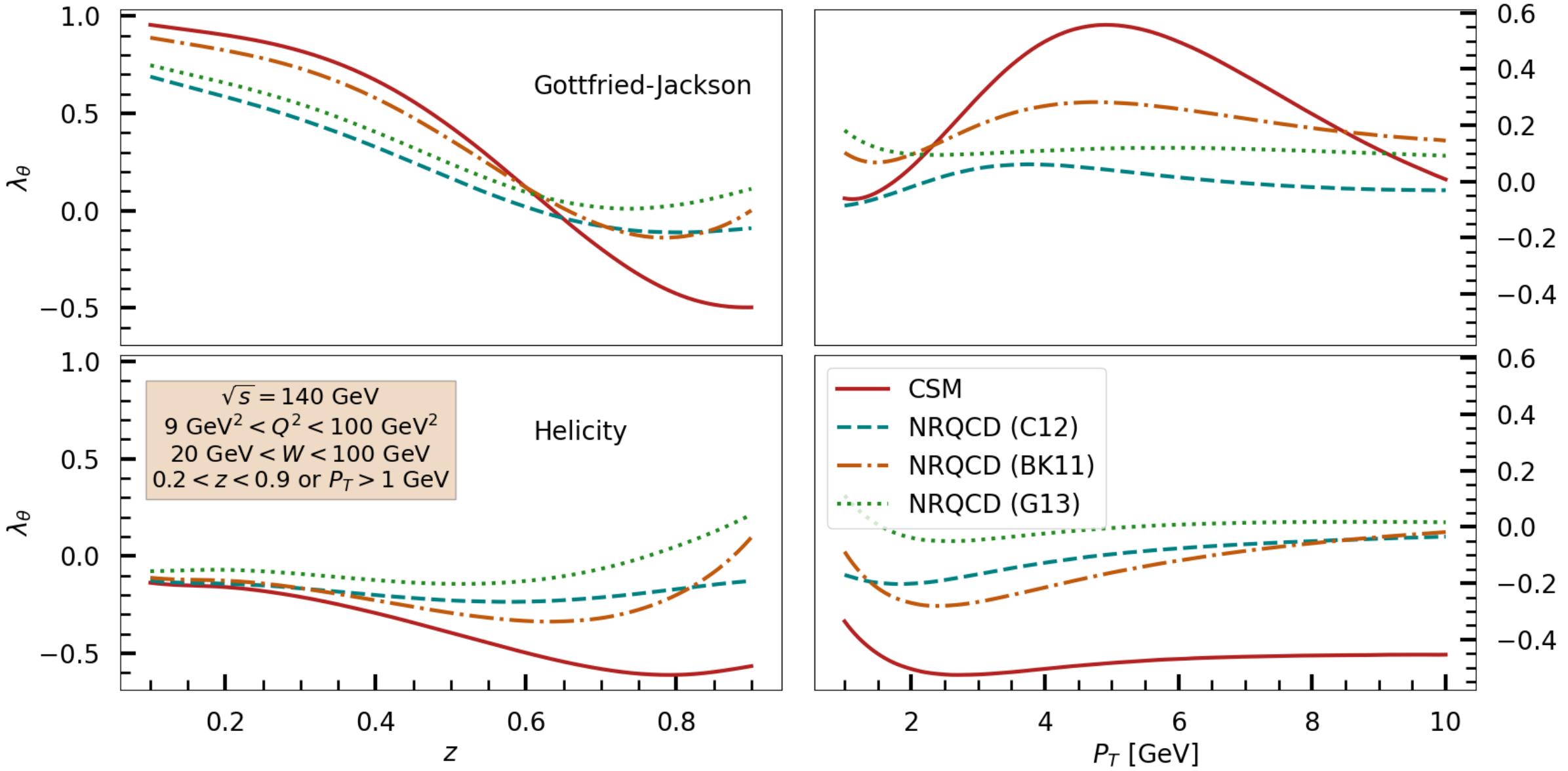
Hard to extract information

From Yuan-Chao paper

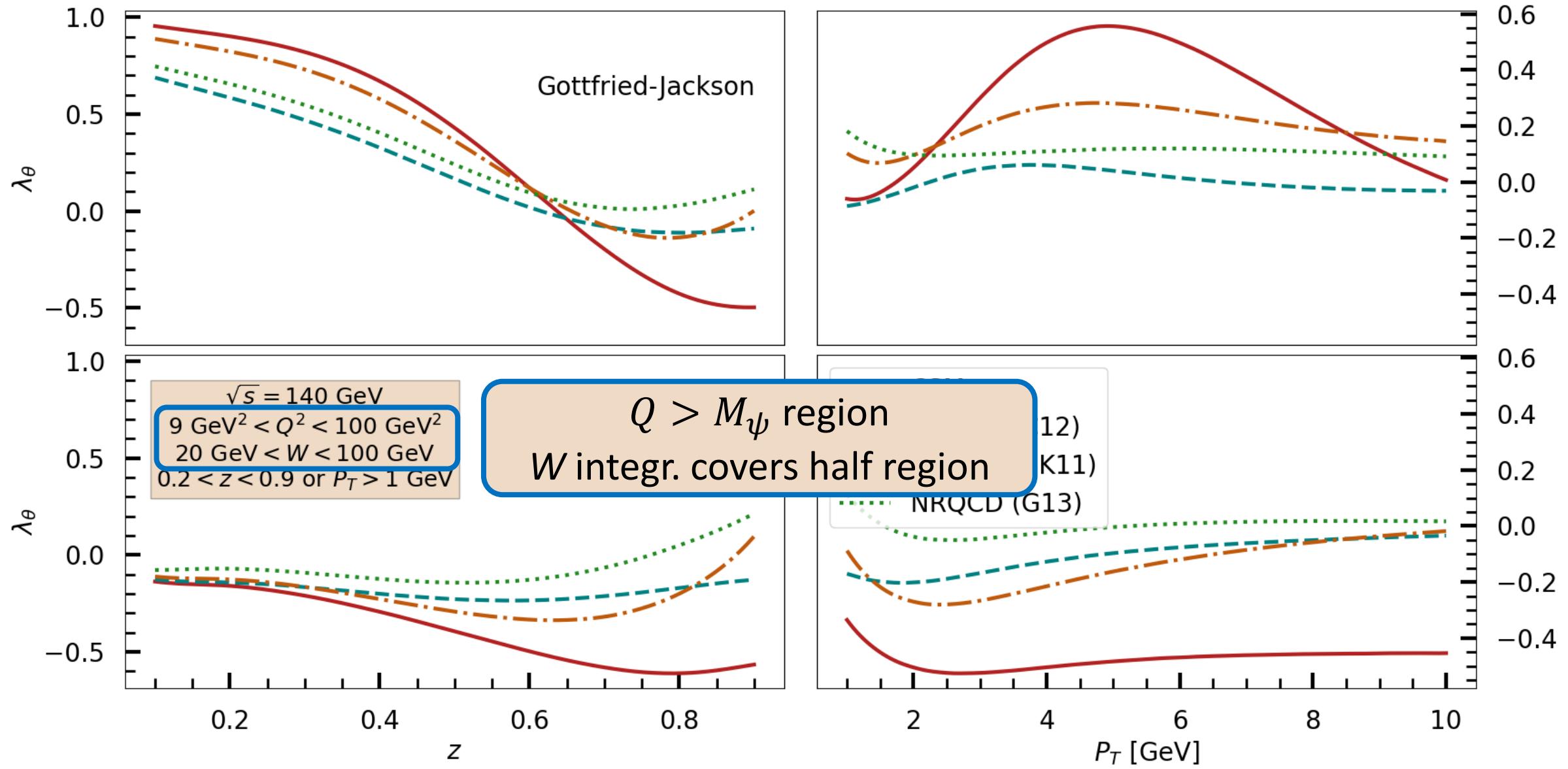


includes resolved photon contribution

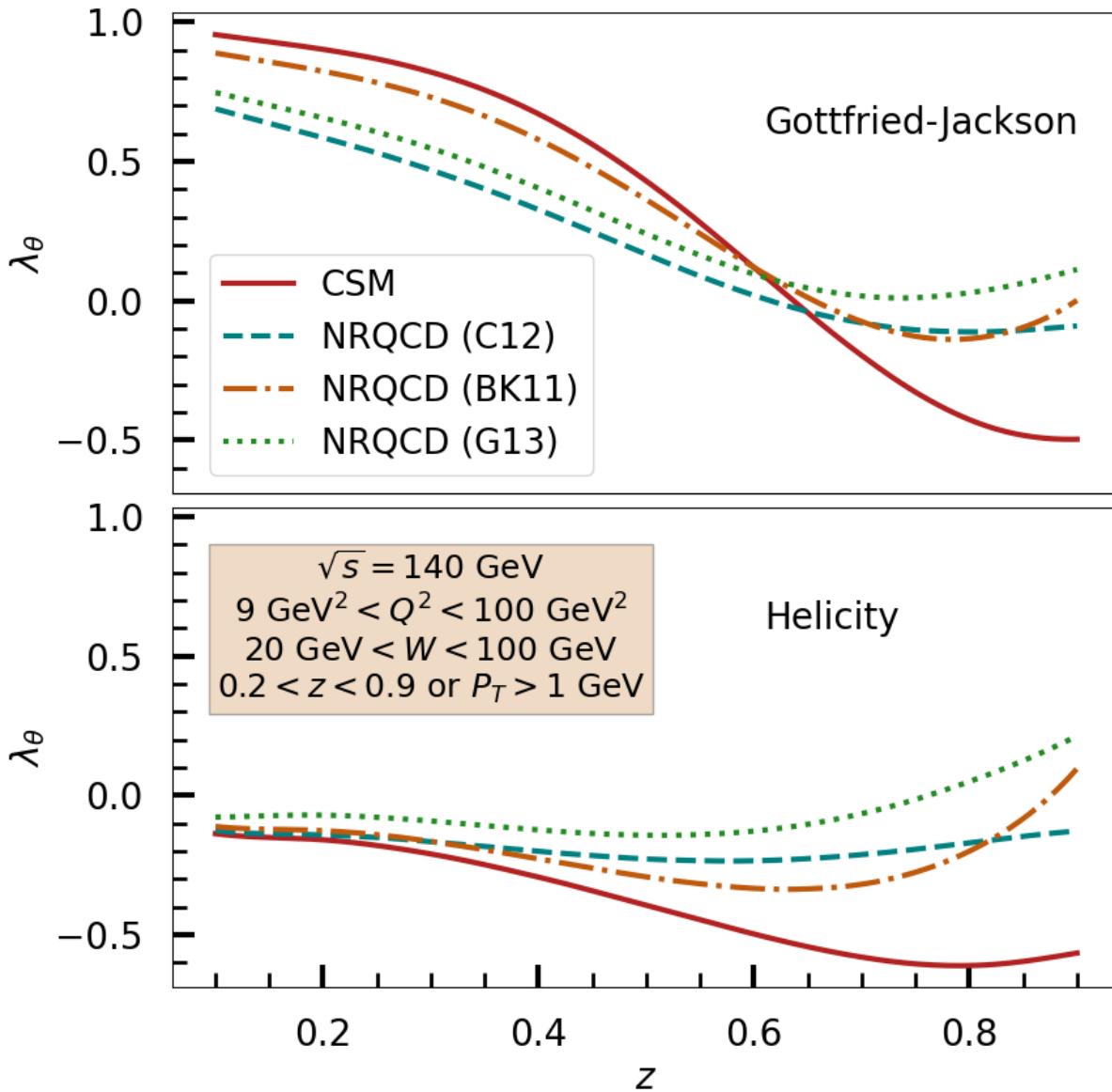
# Polarization at EIC ( $\lambda$ @140GeV)



# Polarization at EIC ( $\lambda$ @140GeV)



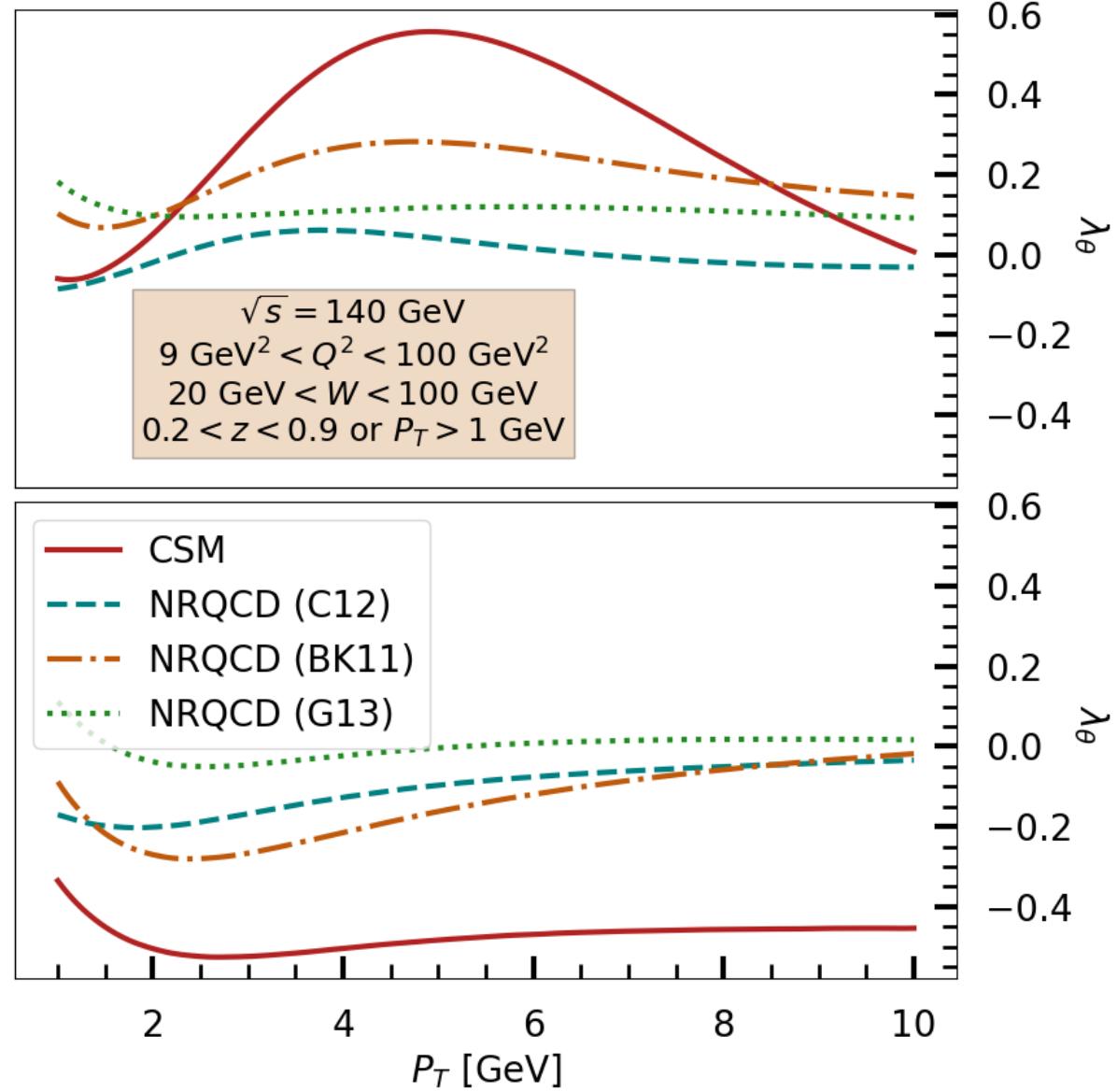
# Polarization at EIC ( $\lambda$ @140GeV)



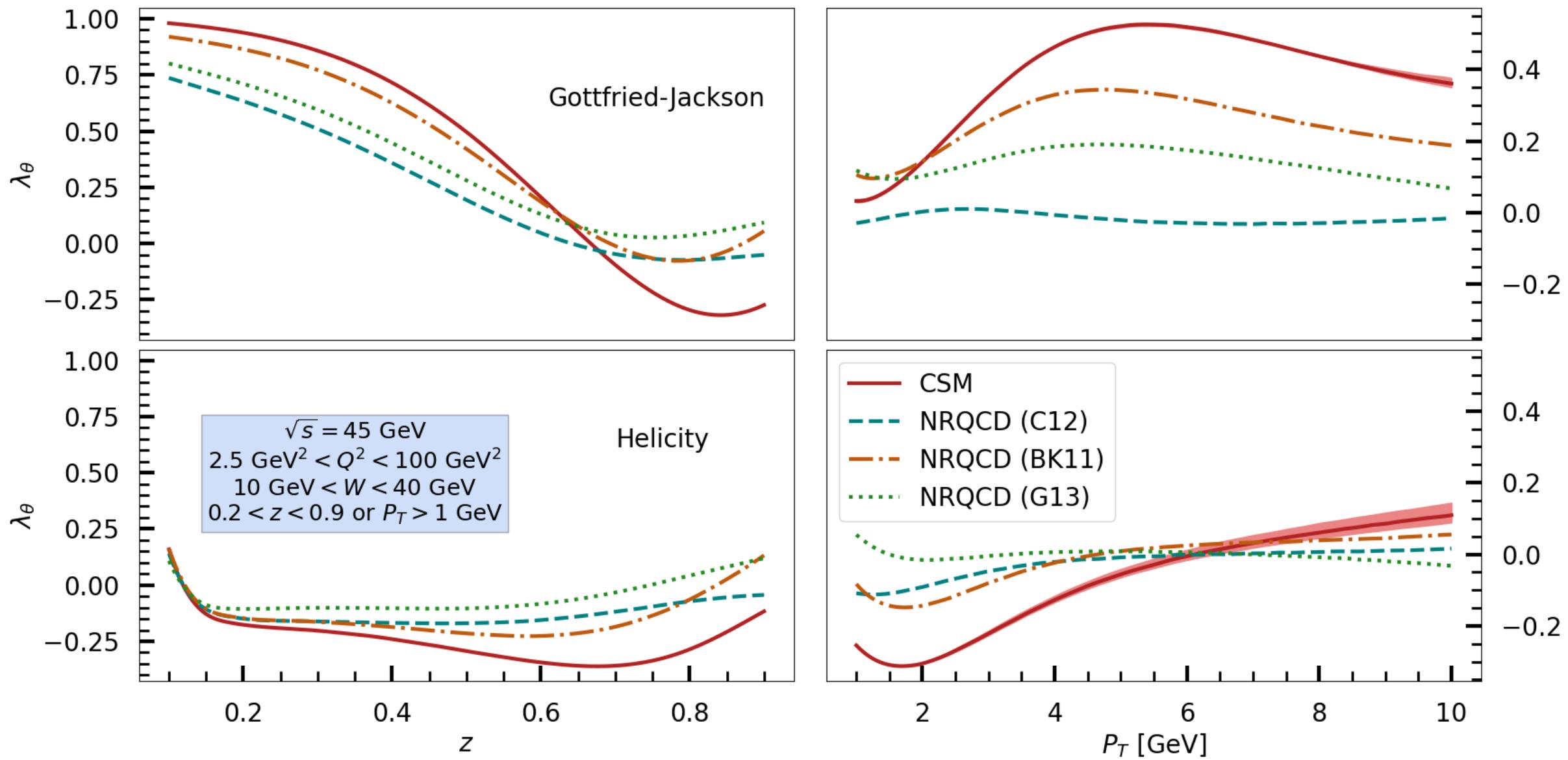
- Unpolarized cross section has a flat behaviour
- Relatively high values
- Not much difference between models and sets
- High- $z$  behaviour interest

# Polarization at EIC ( $\lambda@140\text{GeV}$ )

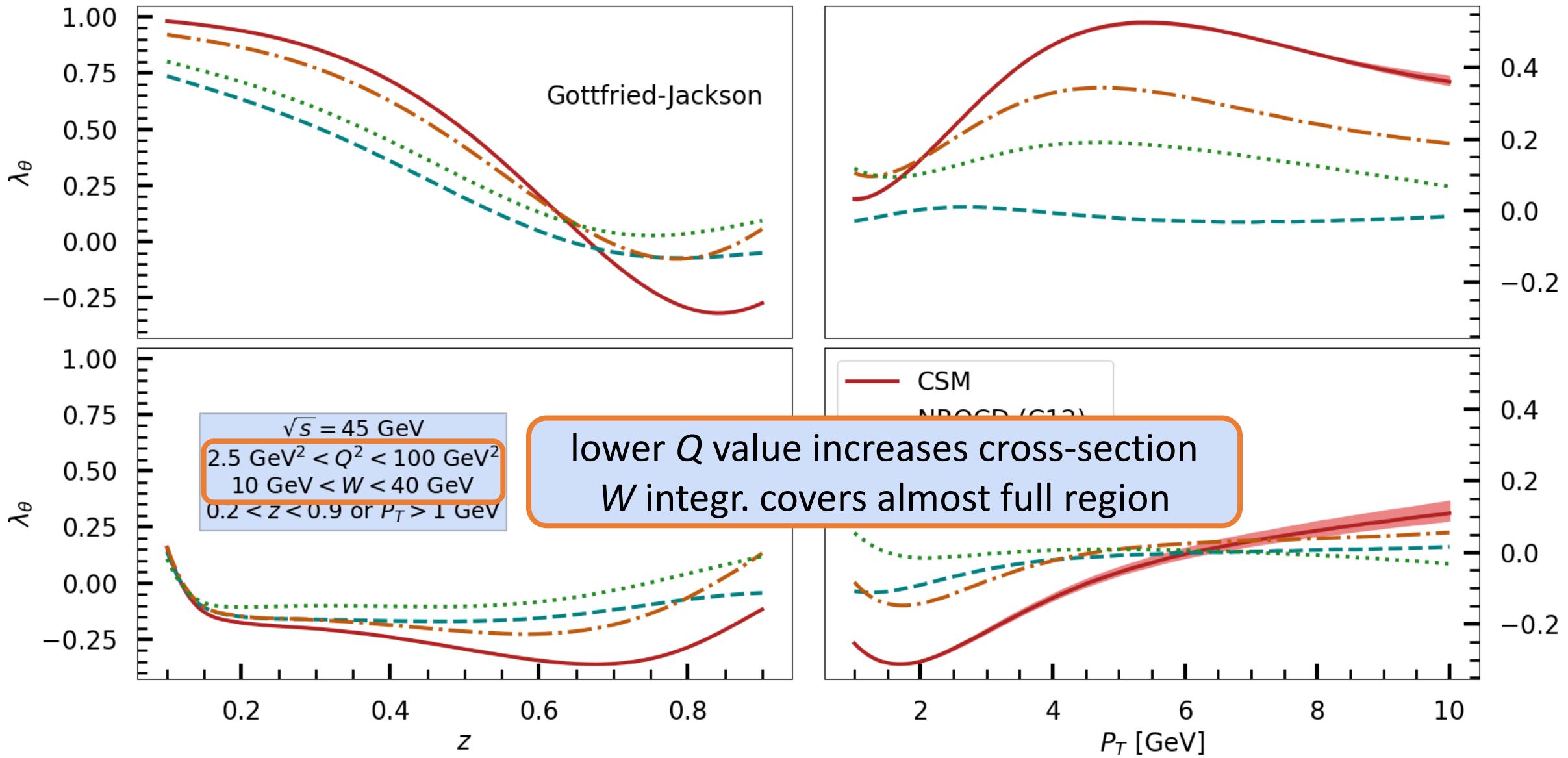
- Unpolarized cross section decreases with  $P_T$
- Different behaviour between NRQCD and CSM predictions



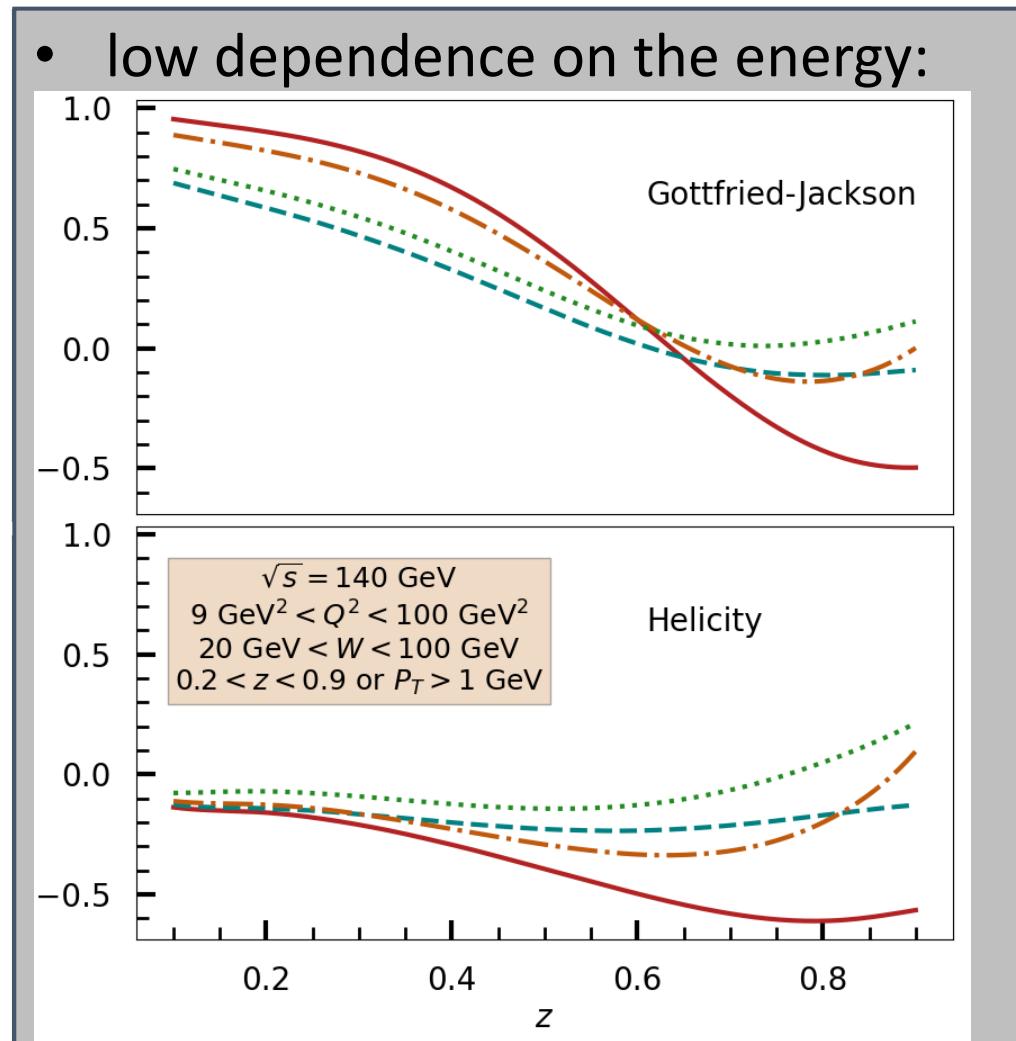
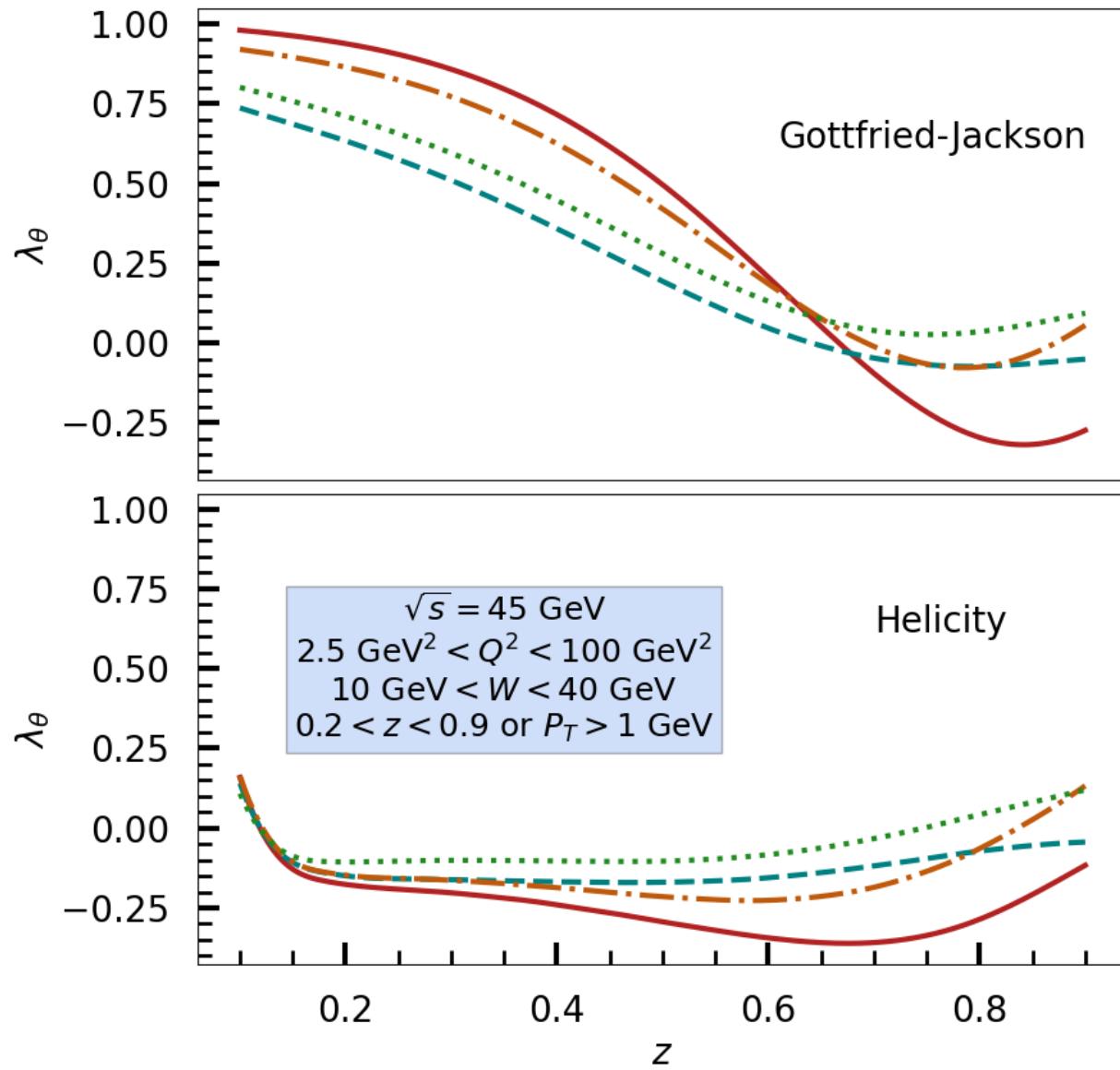
# Polarization at EIC ( $\lambda$ @45GeV)



# Polarization at EIC ( $\lambda$ @45GeV)

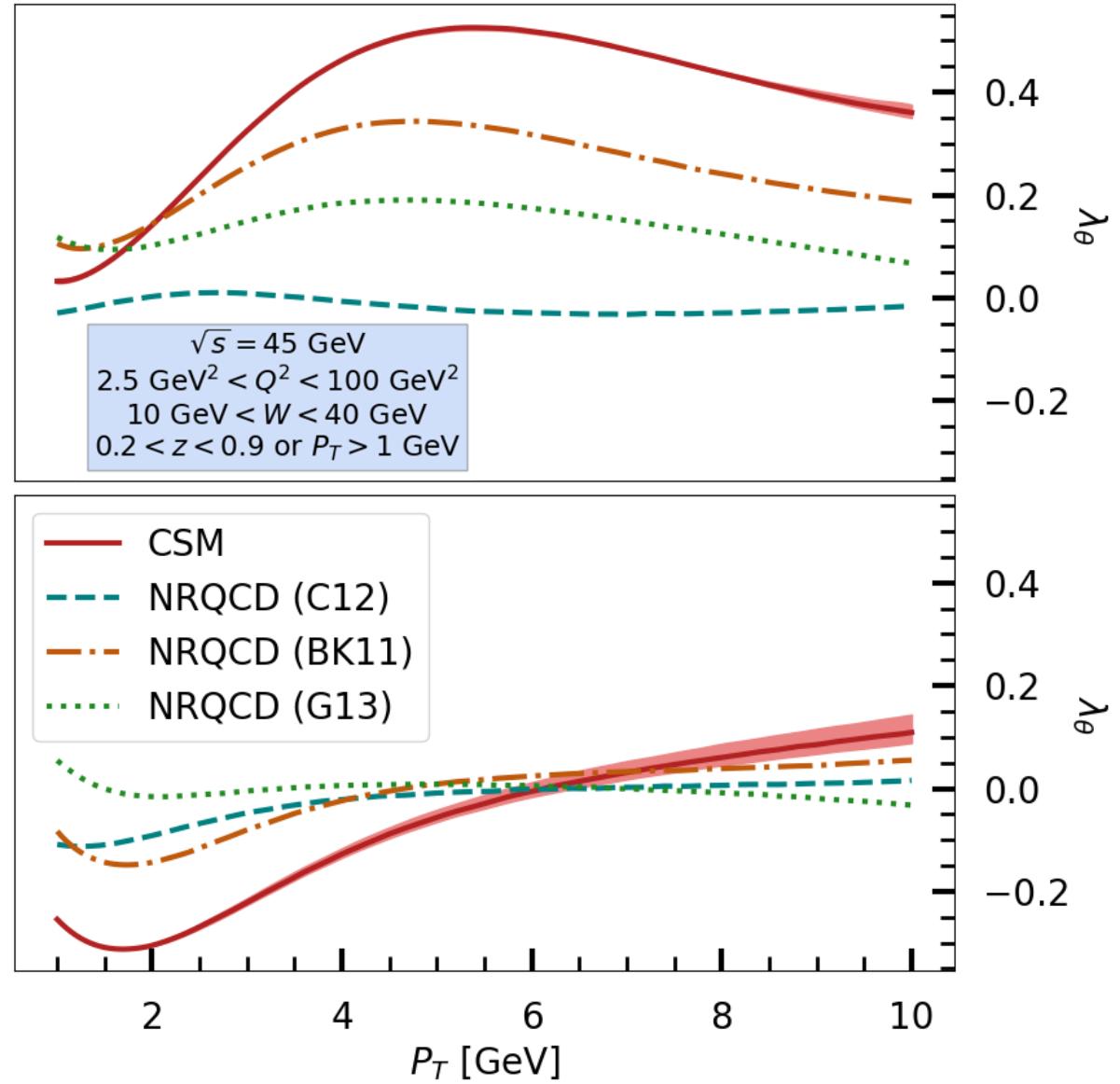
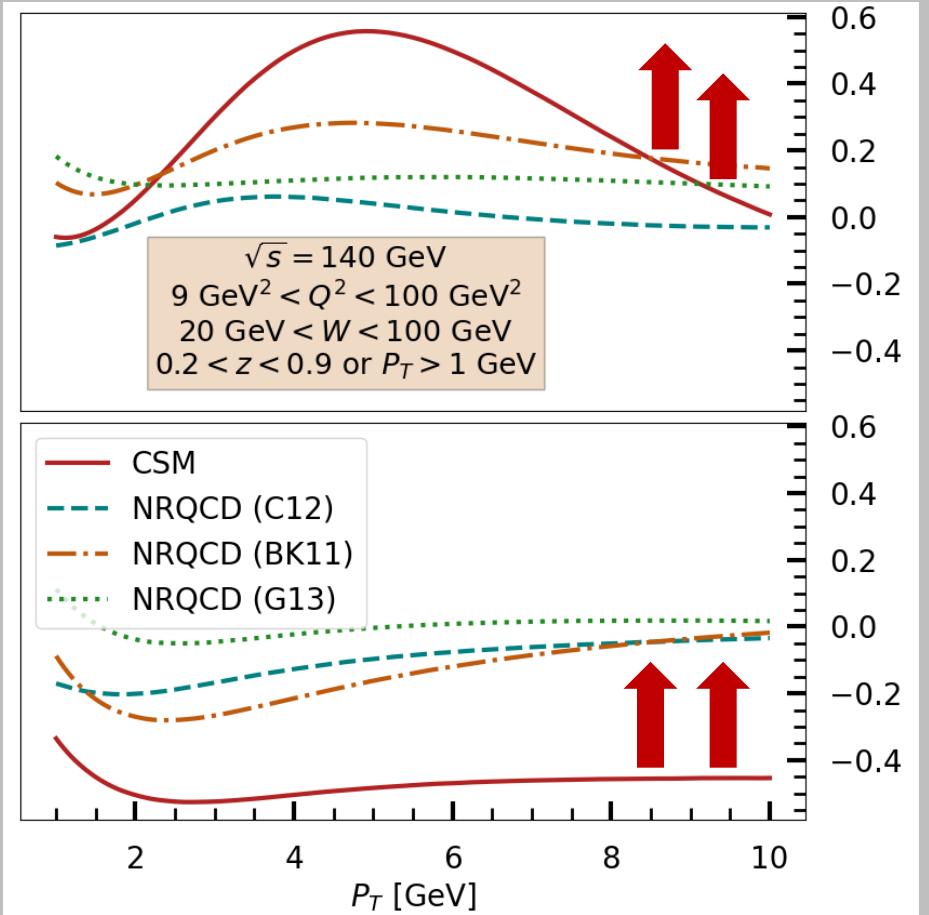


# Polarization at EIC ( $\lambda$ @45GeV)

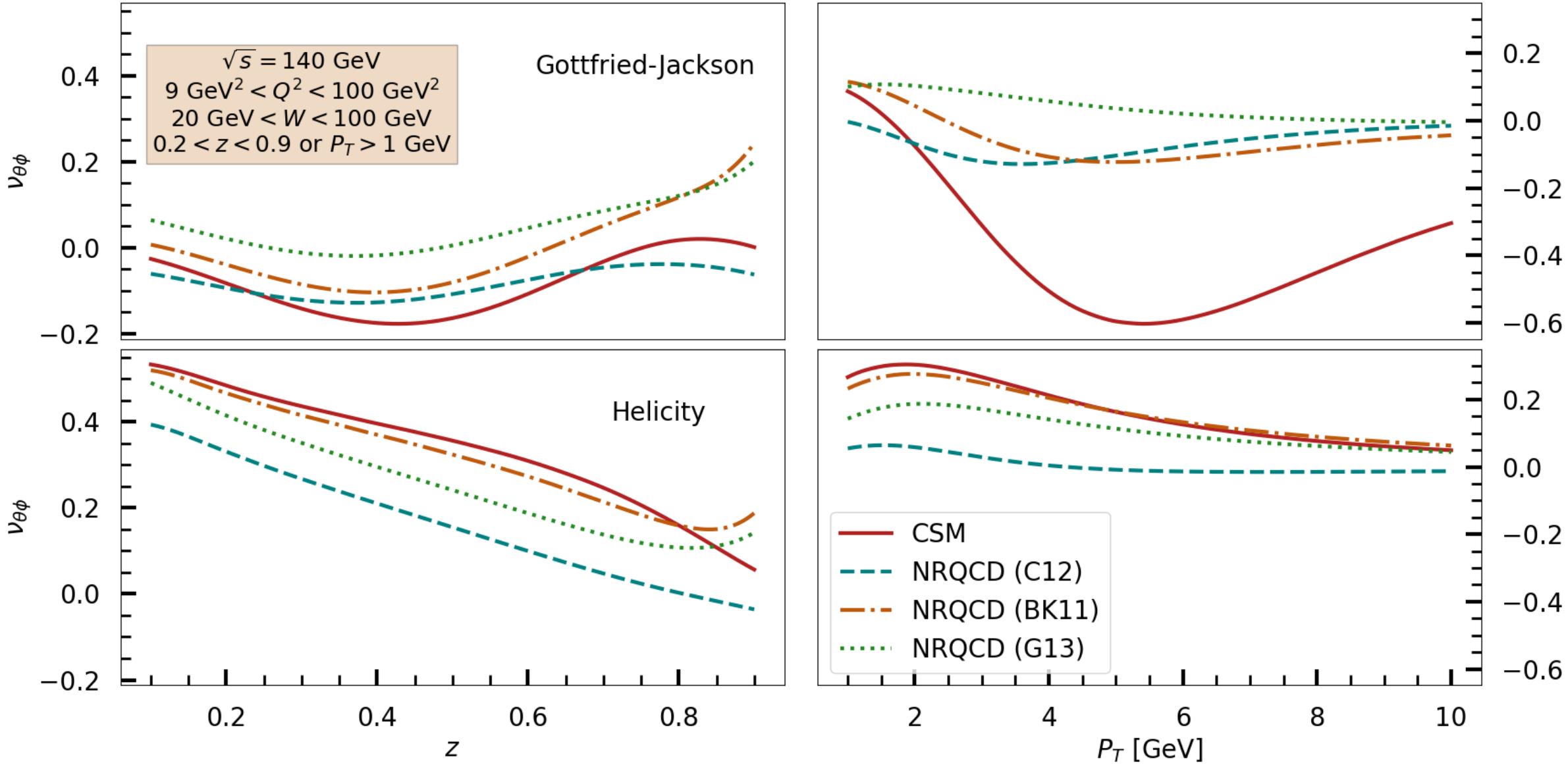


# Polarization at EIC ( $\lambda@45\text{GeV}$ )

- visible dependence on the energy:



# Polarization at EIC ( $\nu$ @140GeV)



# EIC ROTATIONAL INVARIANTS

Rotation around  $Y$ -axis from frame  $A$  to  $B$  mixes up the **angular parameters**

Like in Drell-Yan case, a rotational invariant approach can be a powerfull tool

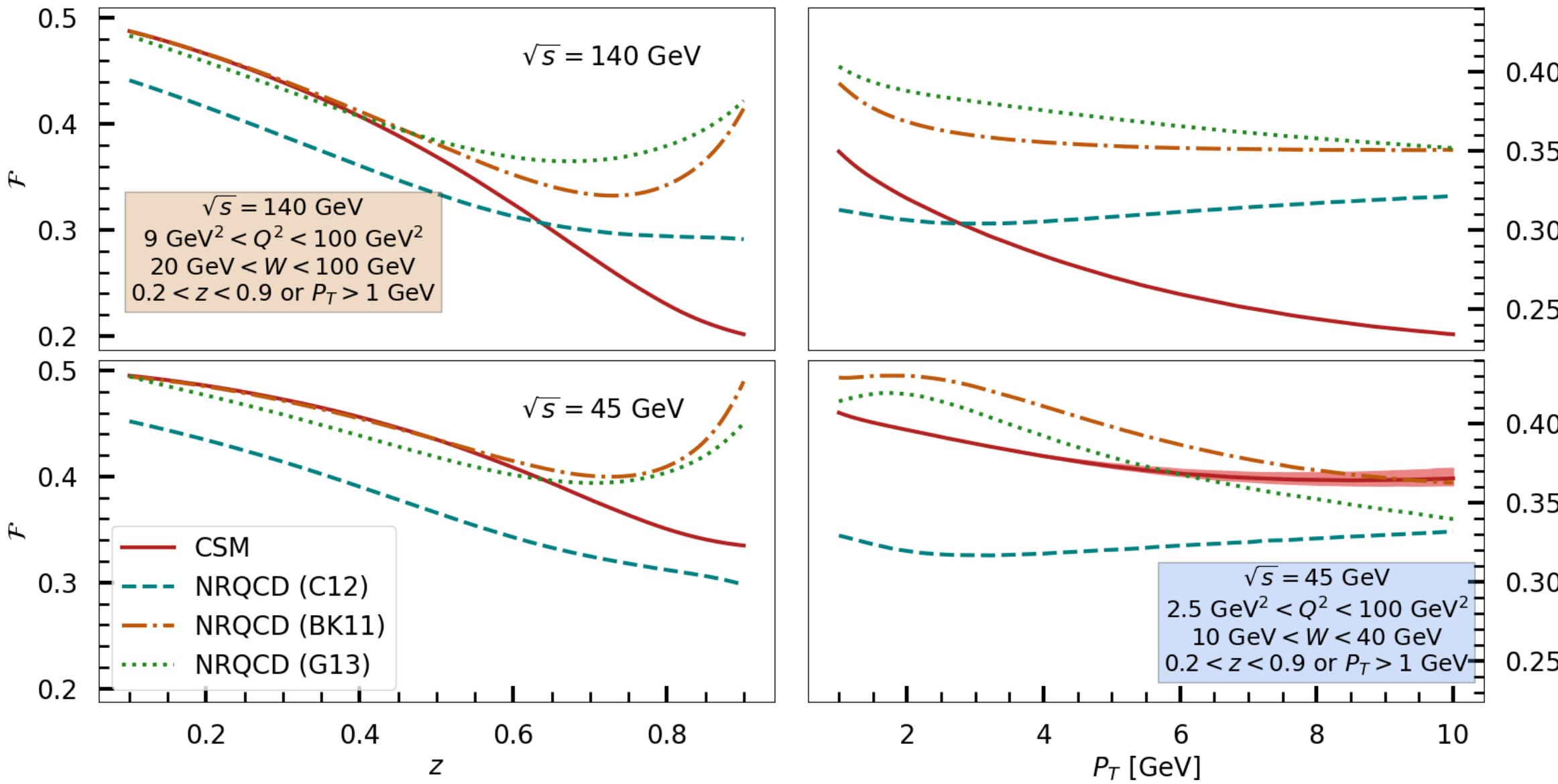
From  $\lambda_\theta$  and  $\nu_{\theta\phi}$  a family of invariant quantities can be identified, like

$$\mathcal{F} = \frac{1 + \lambda_\theta + \nu_{\theta\phi}}{3 + \lambda_\theta} \xrightarrow{\text{if Lam-Tung relation holds}} \mathcal{F} = \frac{1}{2}$$

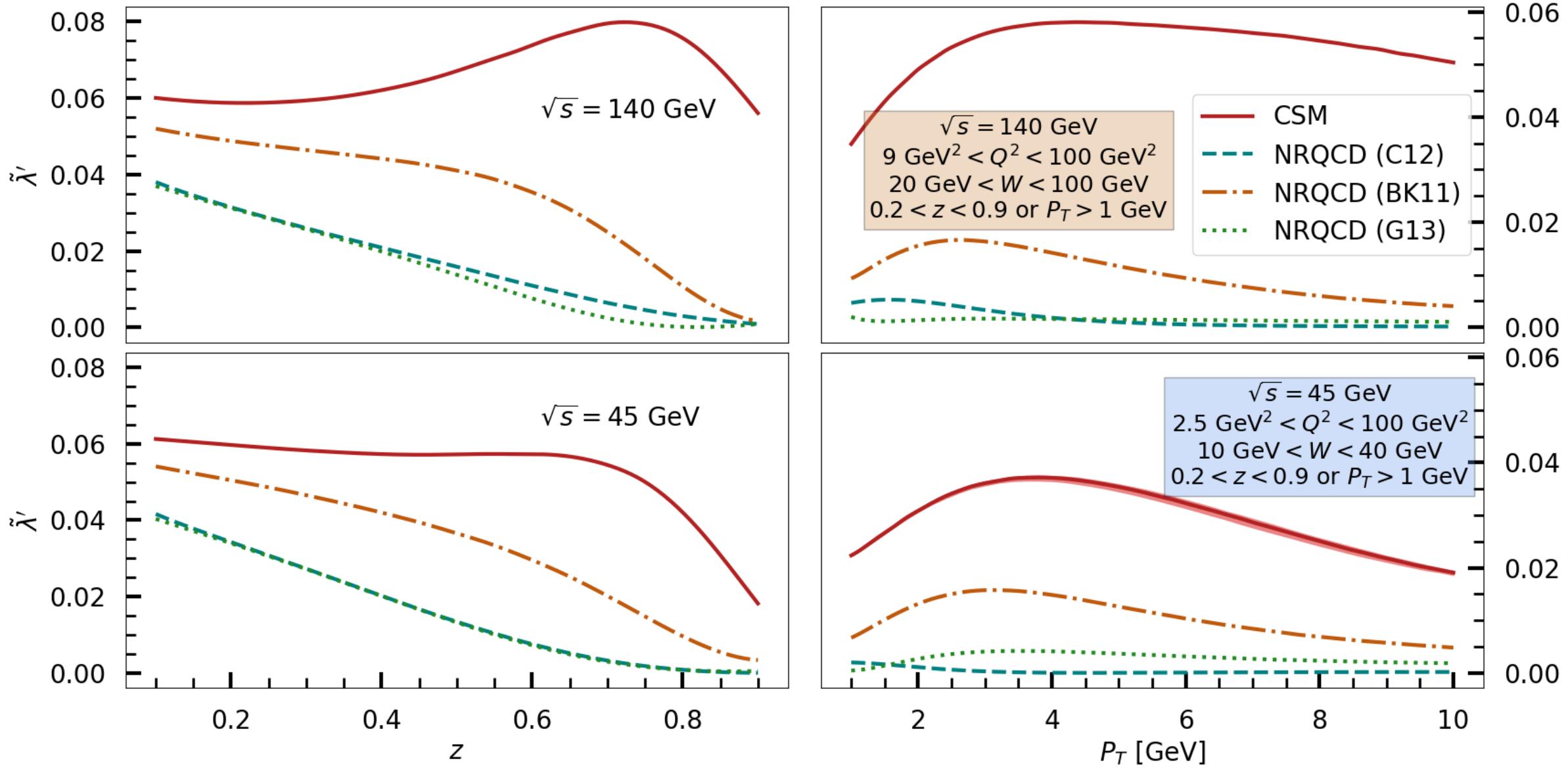
All parameters  $\lambda_\theta, \nu_{\theta\phi}, \mu_{\theta\phi}$  can identify another rotational invariant

$$\tilde{\lambda}' = \frac{(\lambda_\theta - \nu_{\theta\phi}/2)^2 + 4\mu_{\theta\phi}^2}{(3 + \lambda_\theta)^2}$$

# EIC INVARIANTS PLOT (1)



# EIC INVARIANTS PLOT (2)



# TMD INTEREST

- Access to TMD shape function

Echevarria, JHEP 10 (2019)

Fleming, Makris, Mehen, JHEP 04 (2020)

- Access to TMD  $h_1^{\perp g}$  linearly polarized gluon distribution

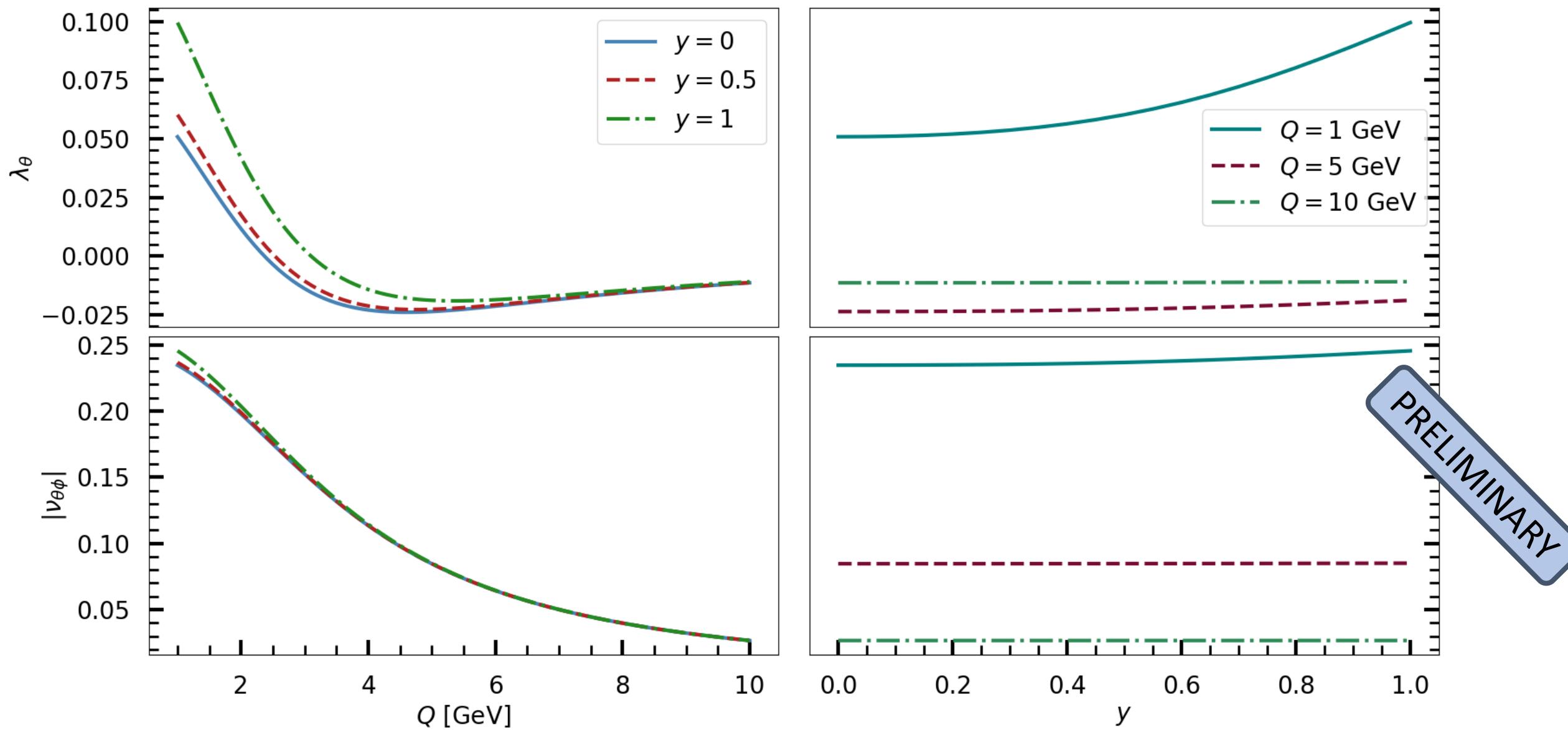
$$\text{positivity bound } \frac{p_T^2}{2m_p^2} |h_1^{\perp g}| \leq f_1^g$$

$$\mathcal{W}_T \propto \frac{1 + (1 - y)^2}{M_\psi(M_\psi^2 + Q^2)} \left[ \frac{1}{3} \mathcal{C}(f_1^g \Delta[^1S_0]) + \frac{4}{M_\psi^2} \frac{3M_\psi^4 + Q^4}{(M_\psi^2 + Q^2)^2} \mathcal{C}(f_1^g \Delta[^3P_0]) \right]$$

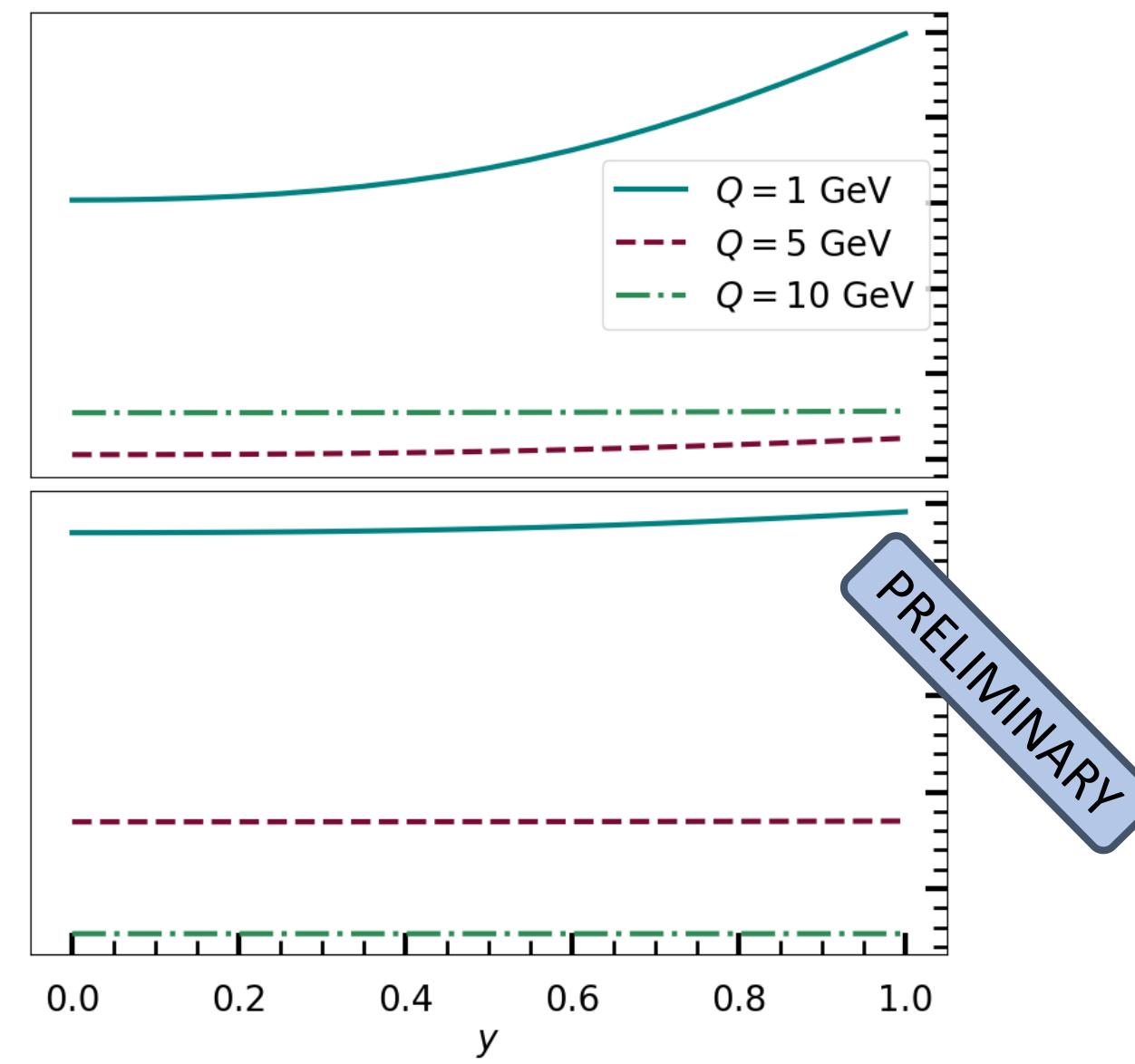
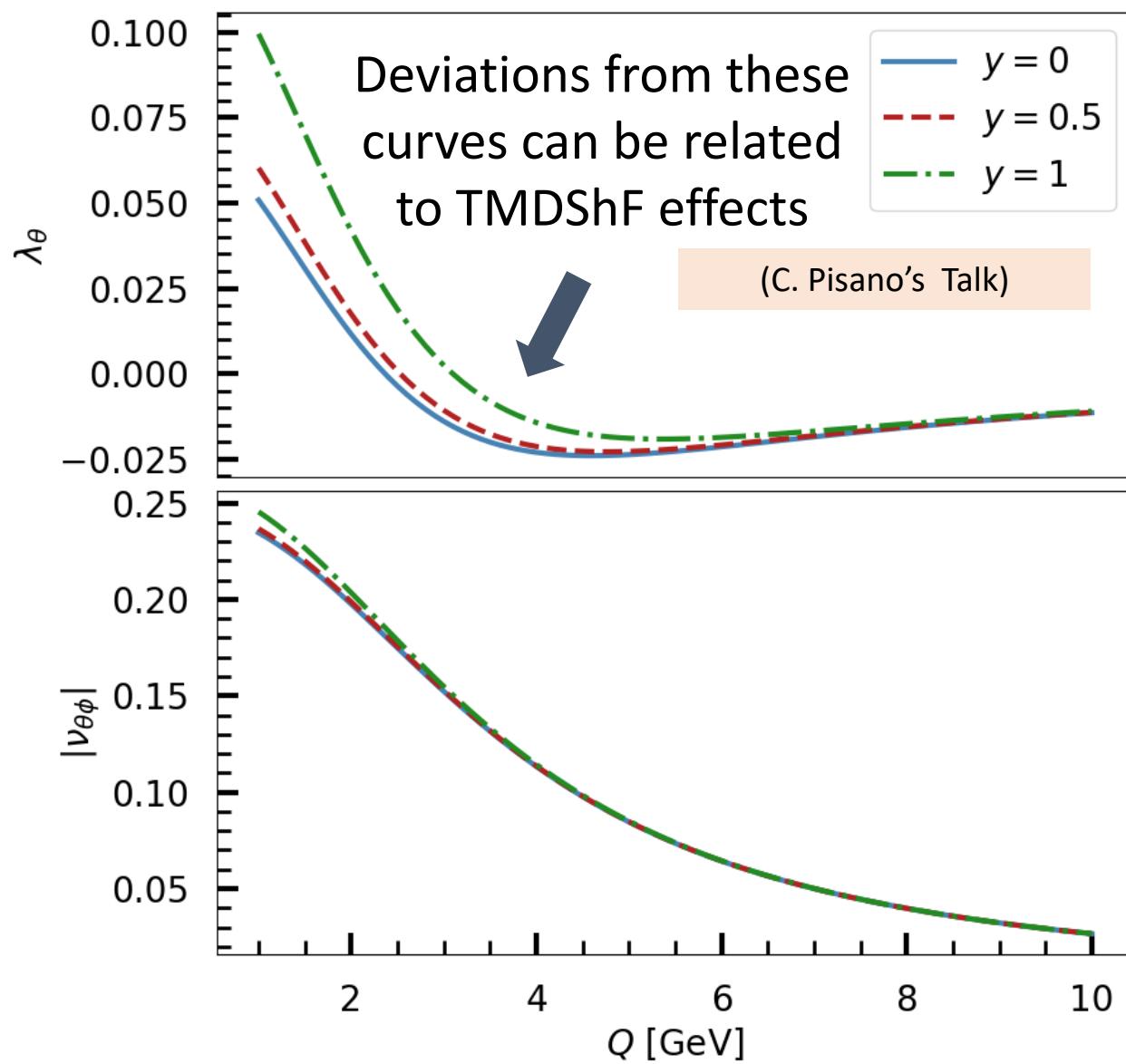
$$\mathcal{W}_L \propto \frac{1 + (1 - y)^2}{M_\psi(M_\psi^2 + Q^2)} \left[ \frac{1}{3} \mathcal{C}(f_1^g \Delta[^1S_0]) + \frac{4}{M_\psi^2} \mathcal{C}(f_1^g \Delta[^3P_0]) \right] + \frac{64Q^2(1 - y)}{M_\psi(M_\psi^2 + Q^2)^3} \mathcal{C}(f_1^g \Delta[^3P_0])$$

$$\mathcal{W}_{\Delta\Delta} \propto -8 \frac{1 + (1 - y)^2}{M_\psi(M_\psi^2 + Q^2)^2} \mathcal{C}\left(w h_1^{\perp g} \Delta[^3P_0]\right)$$

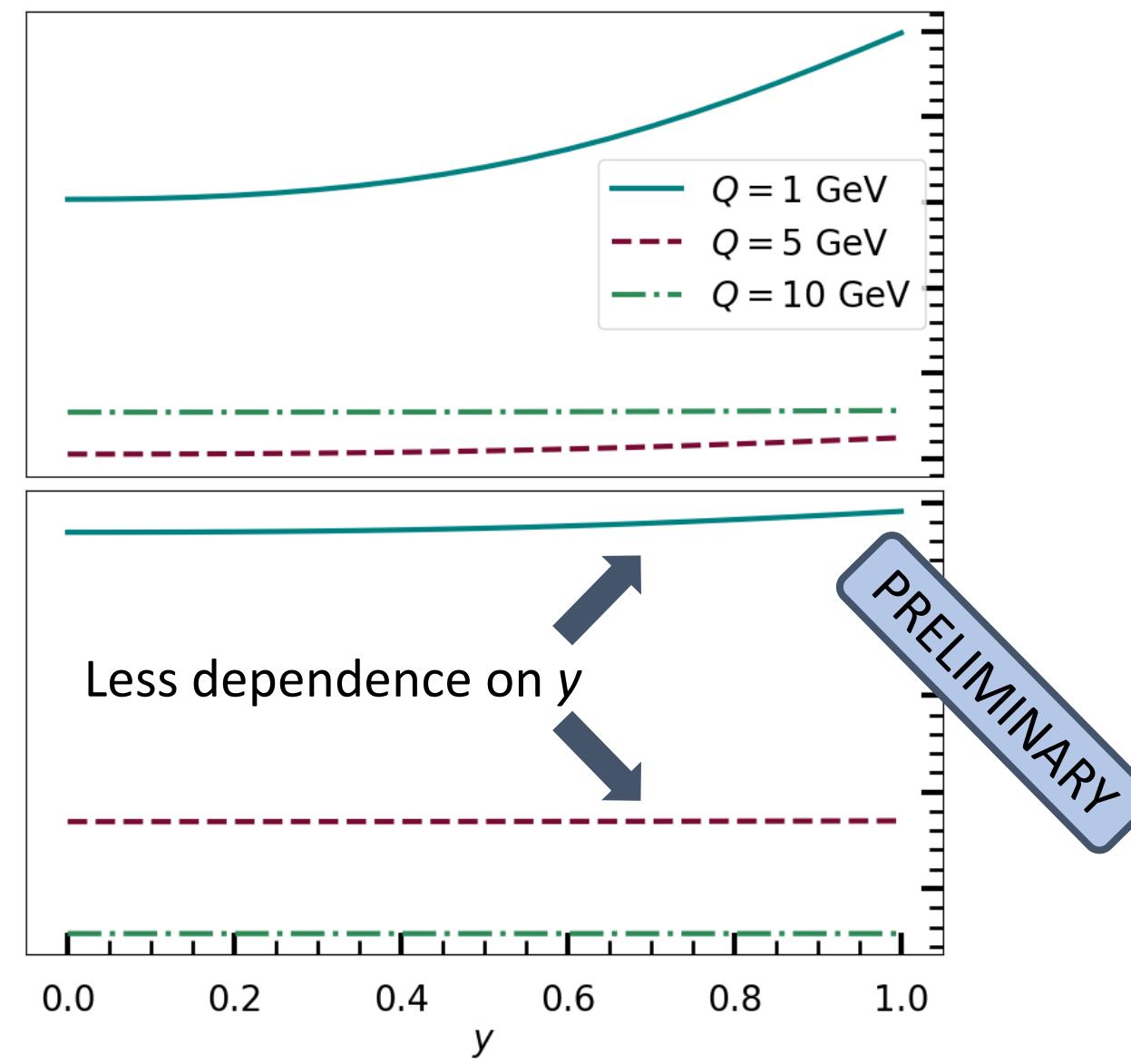
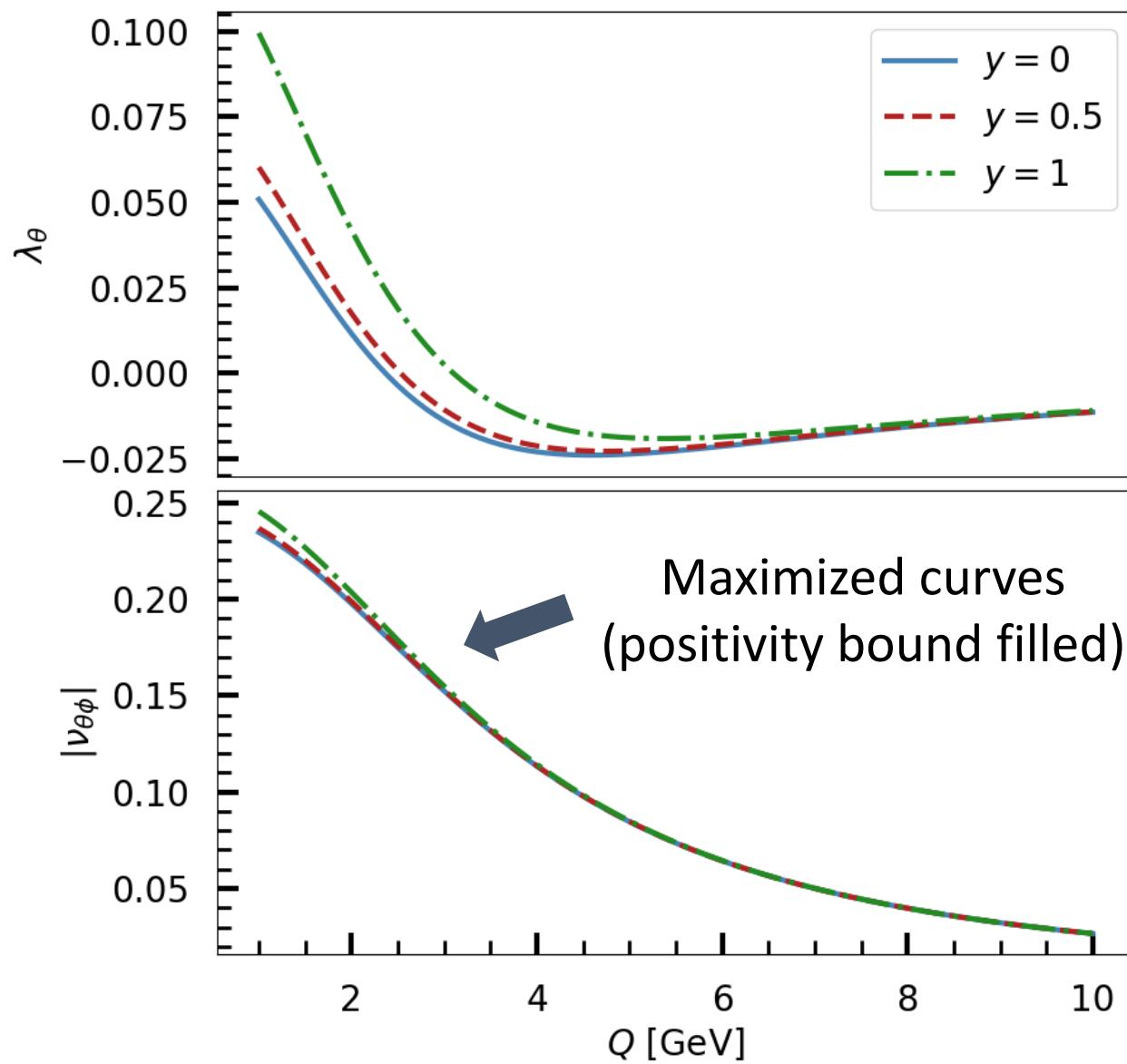
# TMD PRELIMINARY PREDICTIONS



# TMD PRELIMINARY PREDICTIONS



# TMD PRELIMINARY PREDICTIONS



# CONCLUSIONS

Importance of polarization  $J/\psi$  state analysis

Importance of full polarization measurements to achieve a complete picture

EIC luminosity could be useful in a  $P_T$  analysis

Studying the polarization behaviour at different energy/Q-binning

Rotational invariant quantities have a non-trivial behaviour

Polarization data in the TMD region can disclose the role of TMDShF

# Thanks for the attention