



Nucleon structure and the Generalized Parton Distributions

Adam HOBART on behalf of the CLAS collaboration

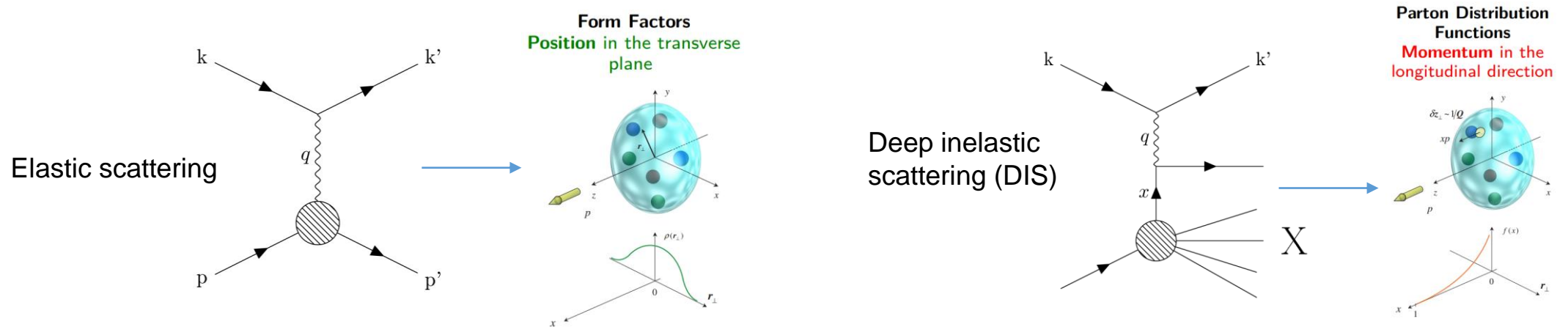
Transversity 2022, 23 – 27 May





What are GPDs?

- QCD at low energies: non perturbative regime
 - Need **structure functions** to describe nucleon structure



Uni-dimensional information on nucleon structure



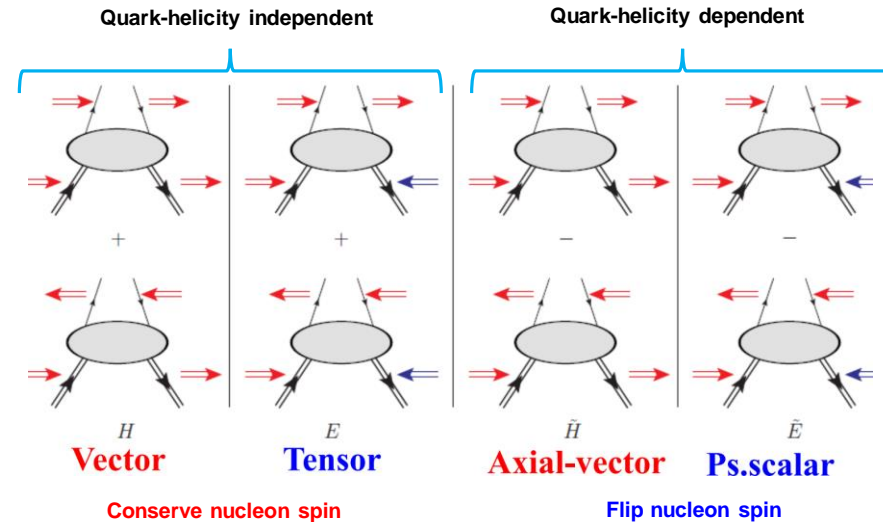
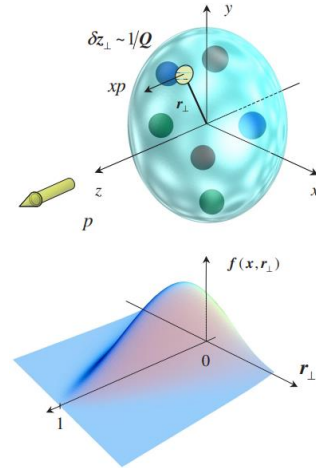
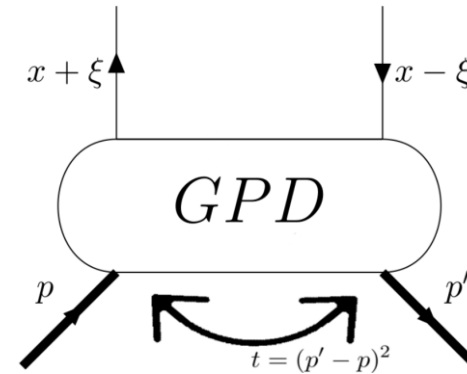
What are GPDs?

- QCD at low energies: non perturbative regime
 - Need **structure functions** to describe nucleon structure

GPDs

Correlation of transverse position and longitudinal momentum of partons in the nucleon & the spin structure

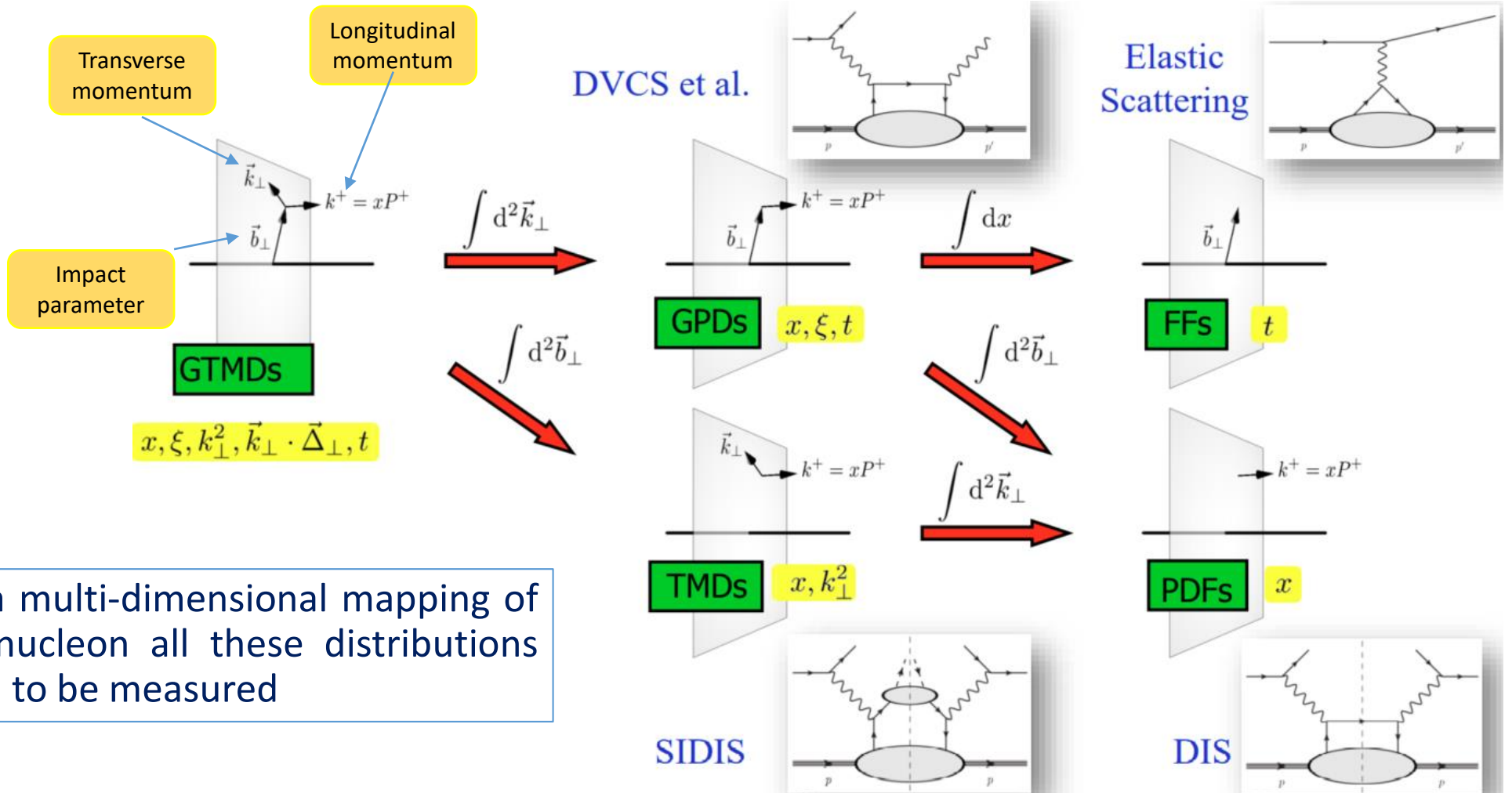
- GPDs can be accessed through **exclusive leptonproduction reactions**
- At leading order QCD, chiral-even (quark helicity is conserved), quark sector: **4 GPDs** for each quark flavor H, \tilde{H}, E and \tilde{E}
- GPDs depend on x, ξ and $t = (p' - p)^2$



Belitsky, Radyushkin, Physics Reports, 2005



Multi-dimensional mapping of nucleon structure



For a multi-dimensional mapping of the nucleon all these distributions need to be measured



Why are GPDs important?

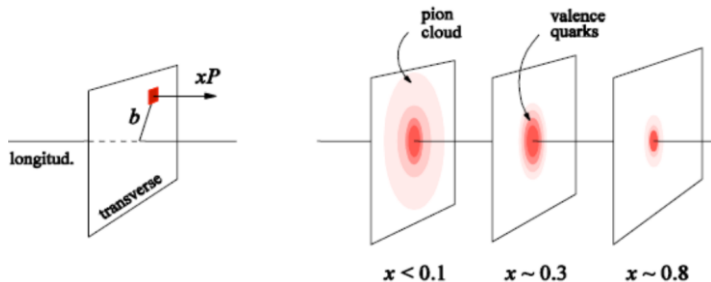
- GPDs: Fourier transforms of non-local, non-diagonal QCD operators

Nucleon tomography

M. Burkardt, PRD 62, 71503 (2000)

$$q(x, b_{\perp}) = \int_0^{\infty} \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{i\Delta_{\perp} b_{\perp}} H(x, 0, -\Delta_{\perp}^2)$$

$$\Delta q(x, b_{\perp}) = \int_0^{\infty} \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{i\Delta_{\perp} b_{\perp}} \tilde{H}(x, 0, -\Delta_{\perp}^2)$$



Quark angular momentum

X. Ji, Phy.Rev.Lett.78,610(1997)

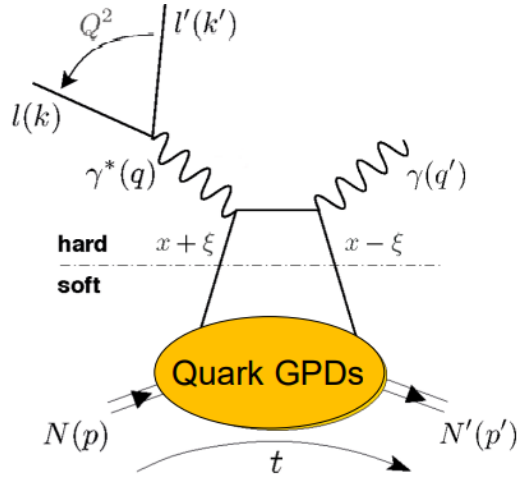
$$\frac{1}{2} \int_{-1}^1 x dx (H(x, \xi, t=0) + E(x, \xi, t=0)) = J = \frac{1}{2} \Delta\Sigma + \Delta L$$

$$\text{Nucleon spin: } \frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta L + \Delta G$$

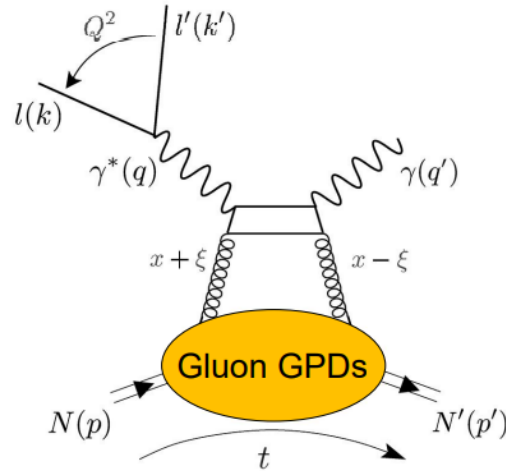
- The intrinsic spin of the quarks can not explain the origin of the spin of the nucleon (**nucleon Spin Crisis**)
- Intrinsic spin of the gluons??
- GPDs: quantify the contribution of orbital angular momentum of quarks to the nucleon spin



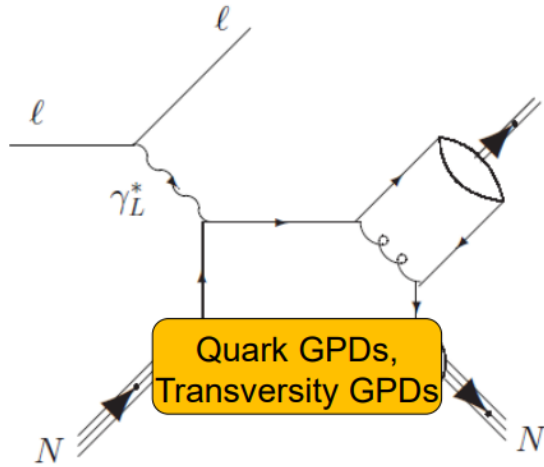
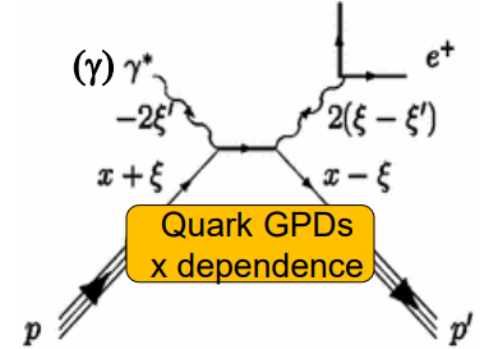
Exclusive reactions giving access to GPDs



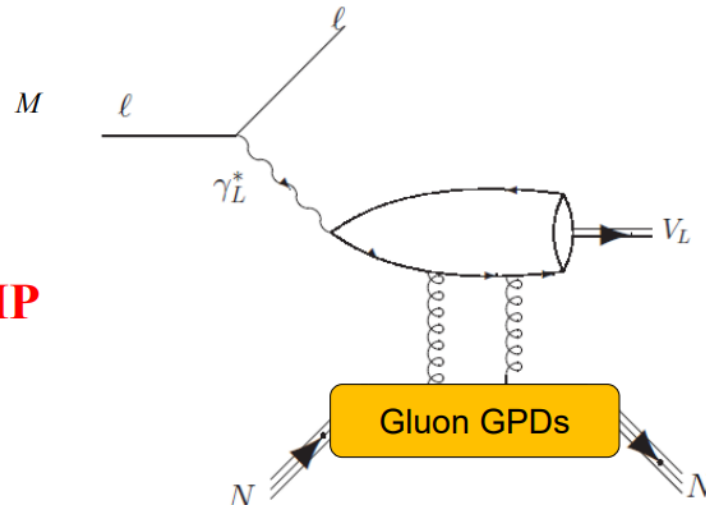
DVCS



(TCS), DDVCS



DVMP



$$Q^2 = -(k-k')^2$$

$$x_B = Q^2/2Mv \quad v = E_e - E_{e'}$$

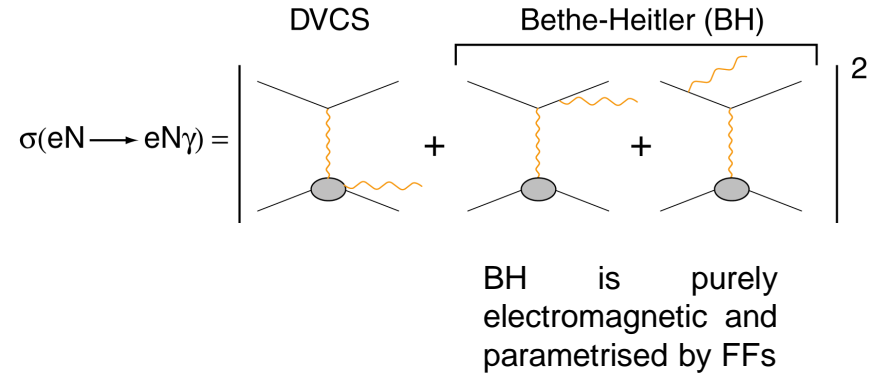
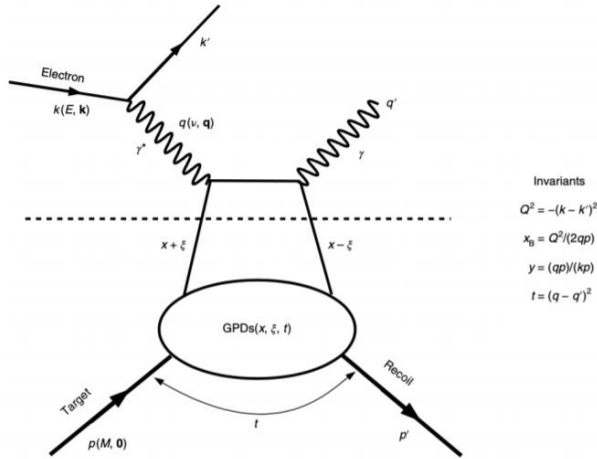
$$x+\xi, x-\xi \text{ long. mom. fract.}$$

$$t = \Delta^2 = (p-p')^2$$

$$\xi \cong x_B/(2-x_B)$$



Deeply Virtual Compton Scattering of leptons off nucleons



- DVCS allows access to 4 complex GPDs-related quantities: Compton Form Factors (ξ, t) (CFFs)

$$\mathcal{H} = \sum_q e_q^2 \left\{ i \pi [H^q(\xi, \xi, t) - H^q(-\xi, \xi, t)] + \mathcal{P} \int_{-1}^1 dx H^q(x, \xi, t) \left[\frac{1}{\xi-x} - \frac{1}{\xi+x} \right] \right\}$$

- x can not be accessed experimentally by DVCS: Models needed to map the x dependence



- Experimentally measured observables:
 - Contribution from both the **DVCS and BH amplitudes**
 - In order to be sensitive to the **DVCS-BH interference part (linear in CFFs)** we should have:
 - Beam polarized and/or target polarized
 - Each measured asymmetry gives access to **combinations of CFFs**
 - The **separation of CFFs** requires the measurement of several observables
 - Depending on the target (**proton or neutron**): different **sensitivity to the CFFs** (GPDs)
 - The **flavor separation of GPDs** requires measurements on both nucleons

$$(H, E)_u(\xi, \xi, t) = \frac{9}{15} \left[4(H, E)_p(\xi, \xi, t) - (H, E)_n(\xi, \xi, t) \right]$$

$$(H, E)_d(\xi, \xi, t) = \frac{9}{15} \left[4(H, E)_n(\xi, \xi, t) - (H, E)_p(\xi, \xi, t) \right]$$



Polarized beam, unpolarized target

$$\Delta\sigma_{LU} \sim \sin(\phi) \Im\{F_1 \mathbf{H} + \xi(F_1 + F_2) \tilde{\mathbf{H}} - k F_2 \mathbf{E} + \dots\}$$

Unpolarized beam, polarized target

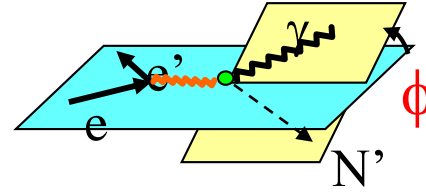
$$\Delta\sigma_{UL} \sim \sin(\phi) \Im\left\{F_1 \tilde{\mathbf{H}} + \xi(F_1 + F_2) \left(\mathbf{H} + \frac{x_b}{2} \mathbf{E}\right) - \xi k F_2 \tilde{\mathbf{E}}\right\}$$

polarized beam, longitudinal polarized target

$$\Delta\sigma_{LL} \sim (A + B \cos(\phi)) \Re\{F_1 \tilde{\mathbf{H}} + \xi(F_1 + F_2) \left(\mathbf{H} + \frac{x_b}{2} \mathbf{E}\right) + \dots\}$$

unpolarized beam, transverse polarized target

$$\Delta\sigma_{UT} \sim \cos(\phi) \sin(\phi_s - \phi) \Im\{k(F_2 \mathbf{H} - F_1 \mathbf{E}) + \dots\}$$



Observable	Proton	Neutron
$\Delta\sigma_{LU}$	$\Im\{\mathbf{H}_p, \tilde{\mathbf{H}}_p, E_p\}$	$\Im\{H_n, \tilde{H}_n, \mathbf{E}_n\}$
$\Delta\sigma_{UL}$	$\Im\{\mathbf{H}_p, \tilde{\mathbf{H}}_p\}$	$\Im\{\mathbf{H}_n, E_n\}$
$\Delta\sigma_{LL}$	$\Re\{\mathbf{H}_p, \tilde{\mathbf{H}}_p\}$	$\Re\{\mathbf{H}_n, E_n\}$
$\Delta\sigma_{UT}$	$\Im\{\mathbf{H}_p, E_p\}$	$\Im\{\mathbf{H}_n\}$



GPD-aimed experiments worldwide

• JLAB

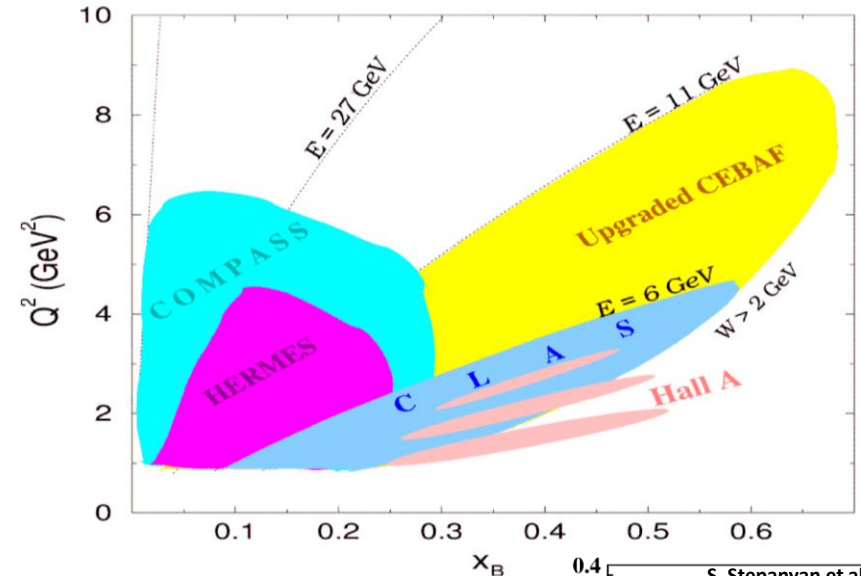
- Hall A: cross sections and beam-polarised cross section differences measurements
- Hall B (CLAS/CLAS12): beam and target spin asymmetries + cross section measurements over large phase-space acceptance

• DESY

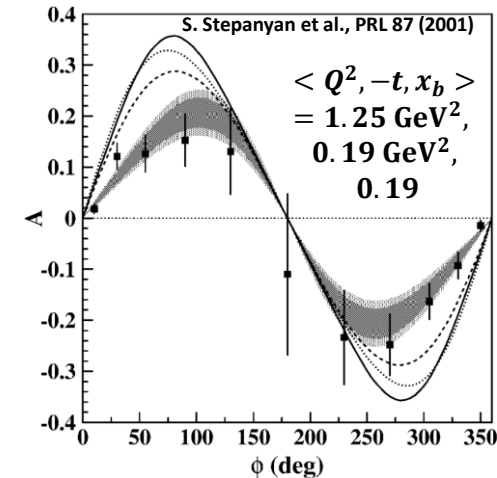
- HERMES: low- x_b low- Q^2 moments of spin asymmetries measurements
- ZEUS: cross section measurements

• CERN

- COMPASS: low- x_b high- Q^2 cross section measurements



$ep \rightarrow epX$, from CLAS data:
First observation of DVCS-BH interference

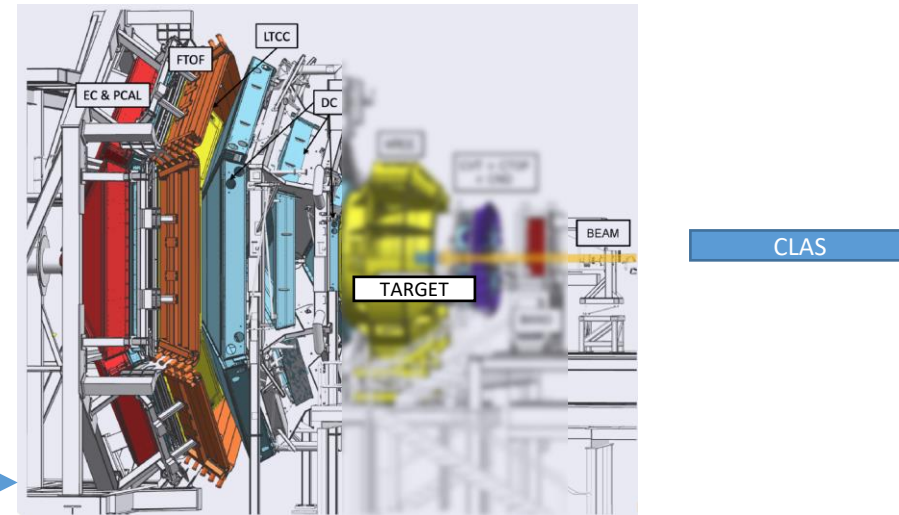
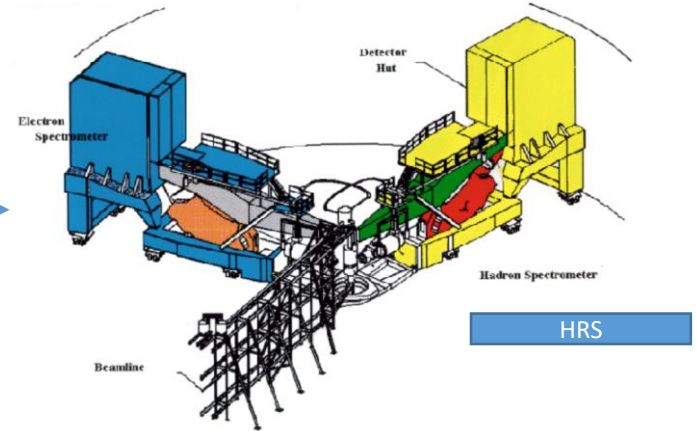
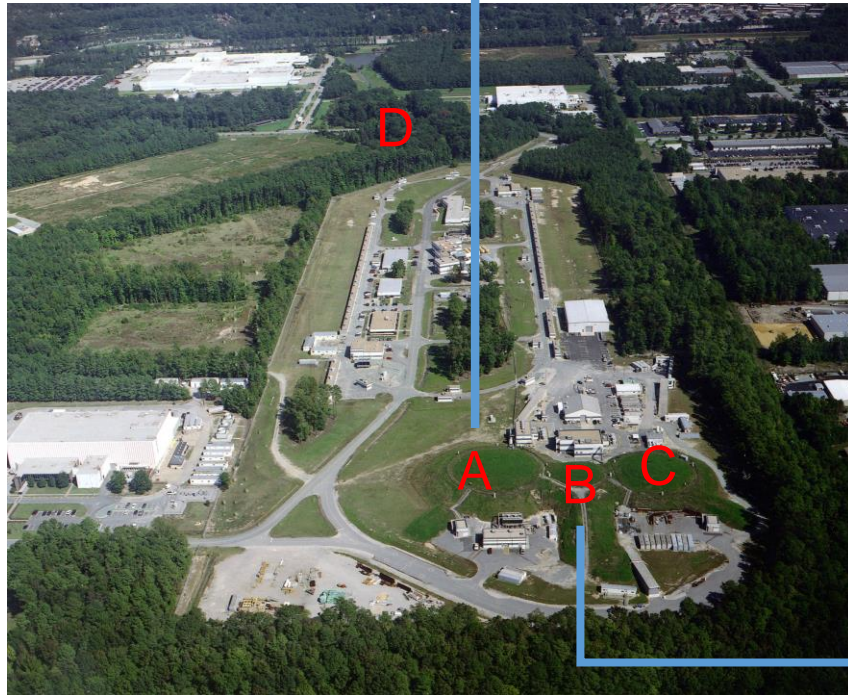




The CEBAF at Jefferson Laboratory

Continuous Electron Beam Accelerator Facility

- Up to 12 GeV electrons
- Two anti-parallel linacs, with recirculating arcs on both ends
- 4 experimental halls

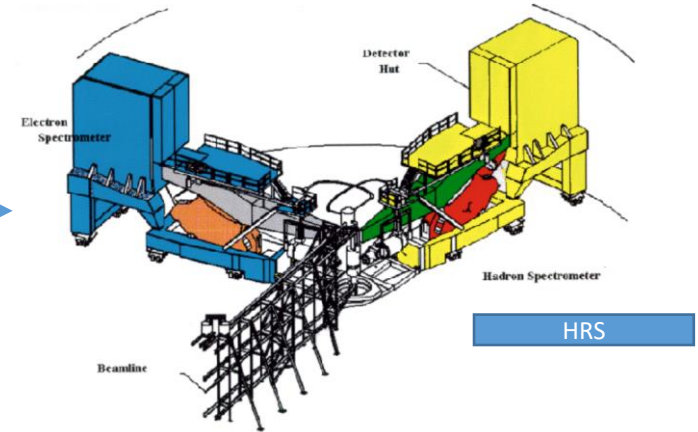




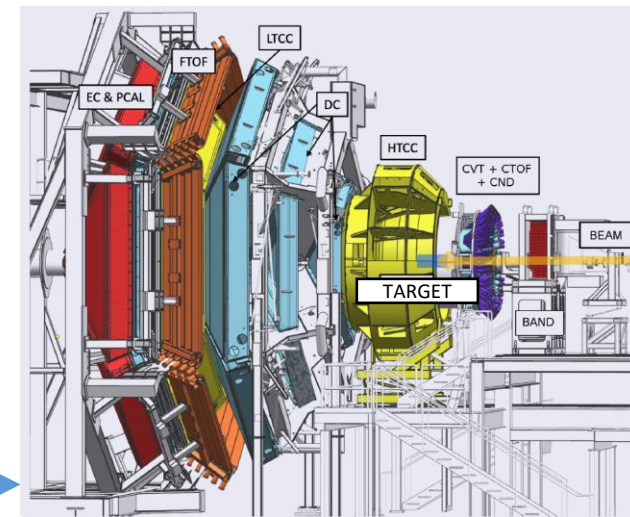
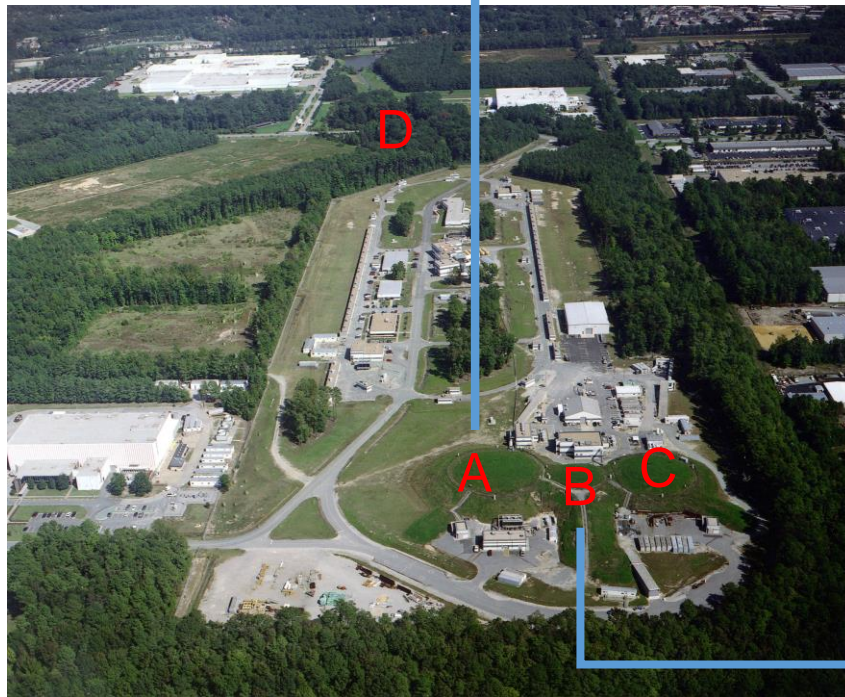
The CEBAF at Jefferson Laboratory

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HRS

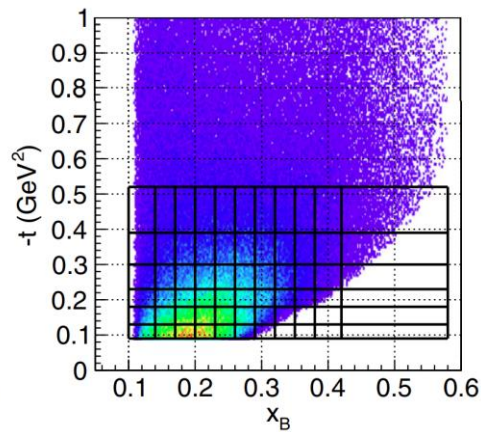
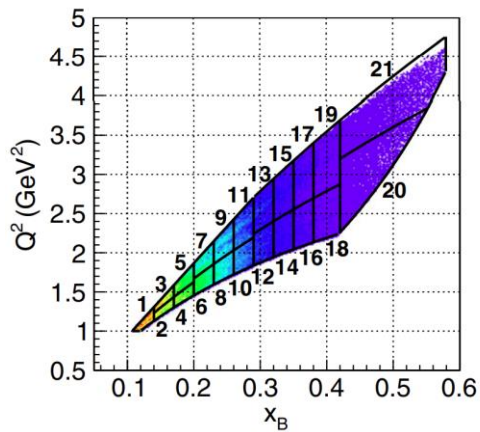


CLAS12

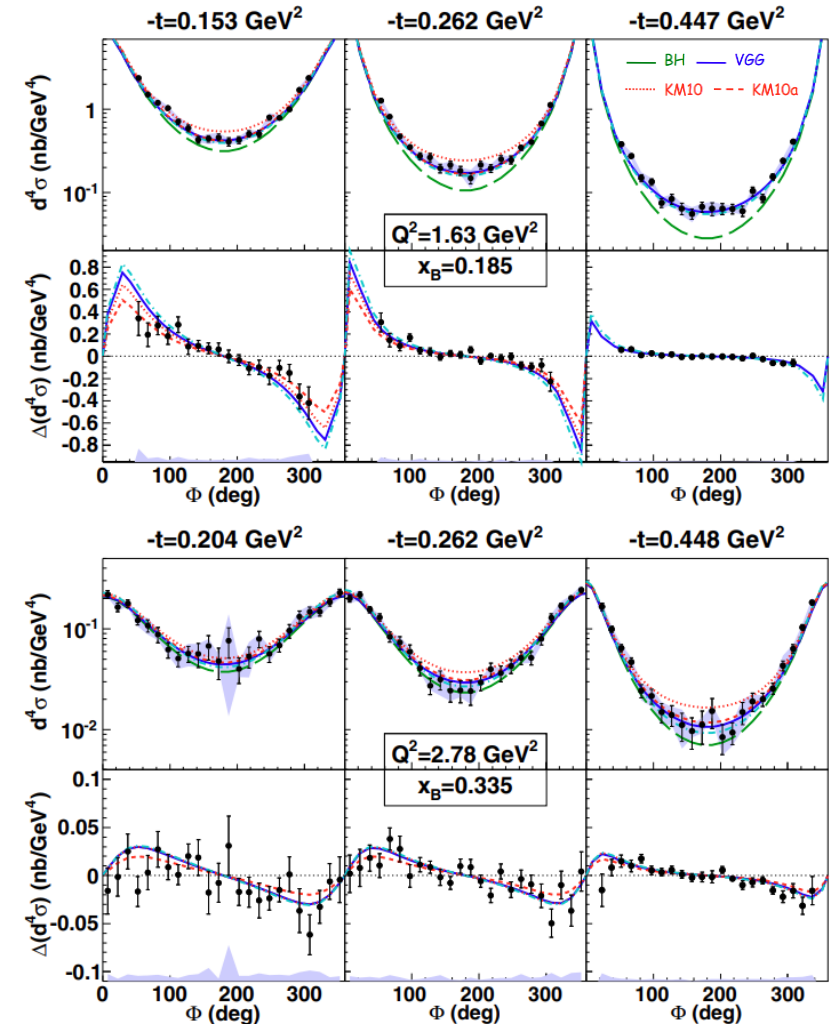


CLAS: unpolarized and beam-polarized cross sections at ~ 6 GeV

- Beam energy ~ 5.75 GeV
- Beam polarization $\sim 80\%$
- Target LH2
- 110 (Q^2, x_b, t) kinematical bins in total

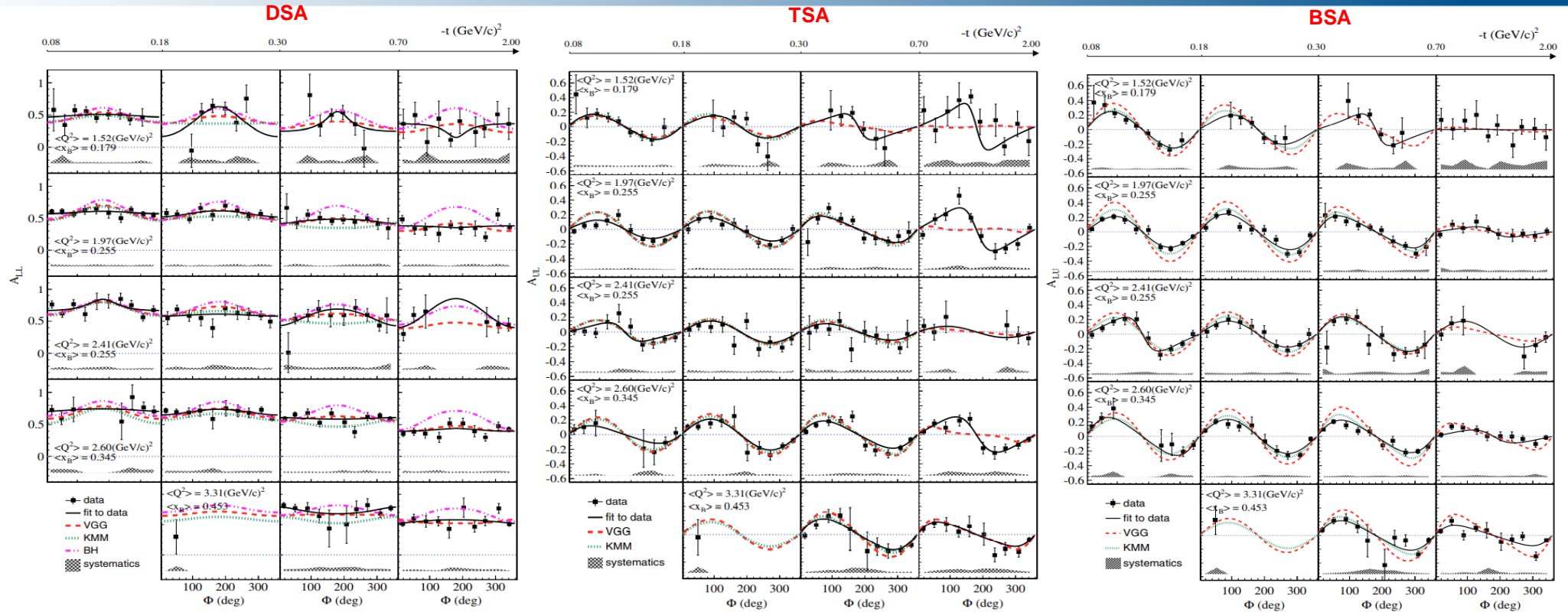


H.S. Jo et al., PRL 115, 212003 (2015)





CLAS: DVCS on longitudinally polarized target at ~ 6 GeV



- Beam energy ~ 5.9 GeV and longitudinally polarized NH₃ ($P \sim 80\%$)
- Observables: Beam, Target and double Spin Asymmetries
- Bins: 5 $Q^2 - x_b$ bins, 4 t bins and 10 Φ bins

w.r.t previous pioneering CLAS6 data
Improved statistics x10 at low $-t$
Extended kinematic coverage

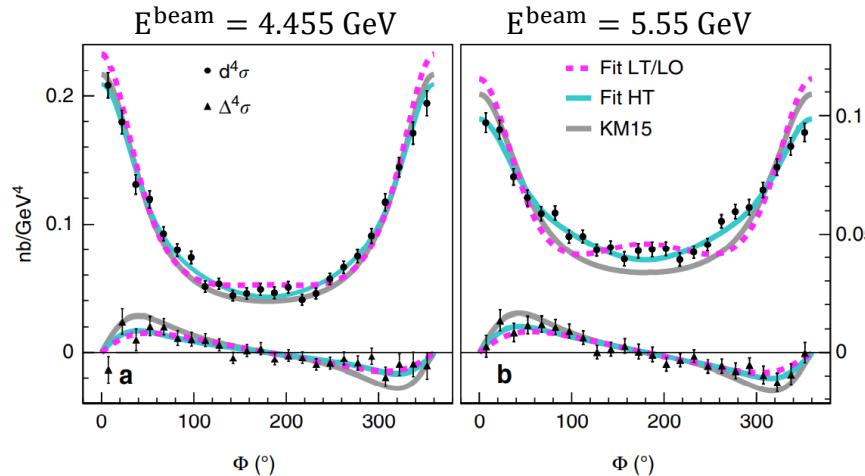
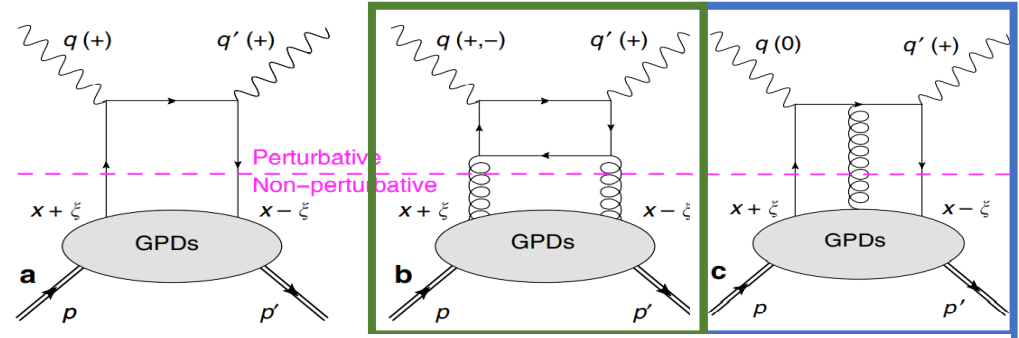
E. Seder et al., PRL 114 (2015) 032001
S. Pisano et al., PRD 91, 052014 (2015)



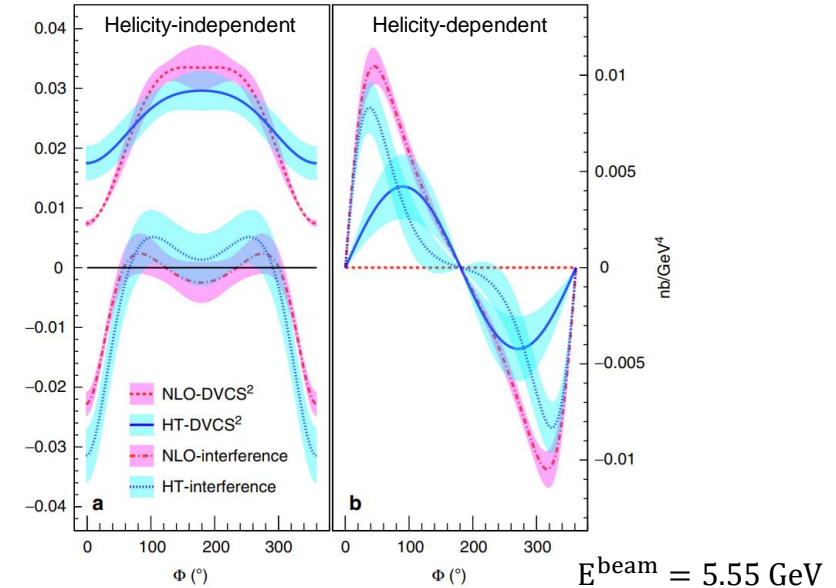
Hall A: High-precision DVCS at 6 GeV

M. Defurne et al., Nature Communications 8, 1408 (2017)

- Quantify the sensitivity to LT-NLO contributions or higher twist (HT) (gluon exchange)
- Different beam energies used to separate BH-DVCS interference and DVCS² contributions



$Q^2 = 1.75 \text{ GeV}^2$, $x_B = 0.36$, and $t = -0.30 \text{ GeV}^2$





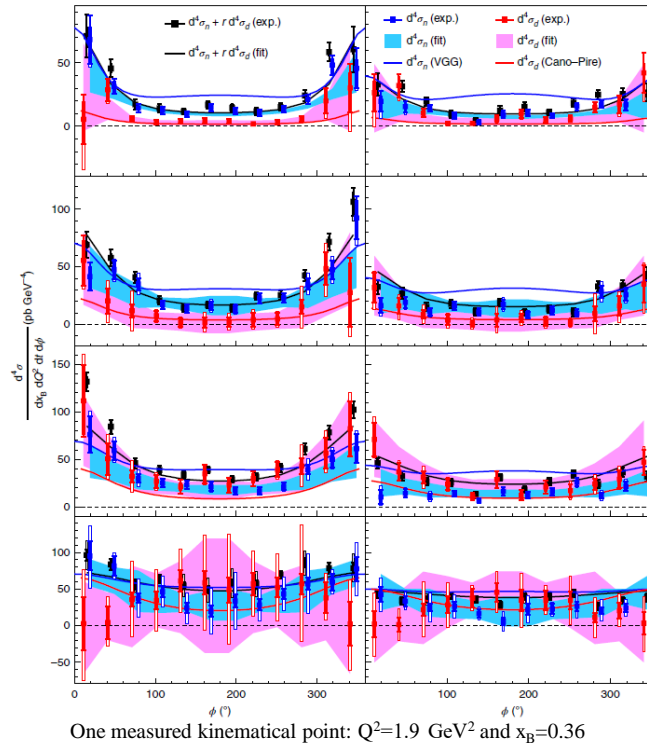
Hall A: nDVCS with an unpolarized deuterium target at ~6 GeV

- nDVCS
 - Beam-energy « Rosenbluth » separation of nDVCS CS using an LD2 target and two different beam energies
 - First observation of non-zero nDVCS CS

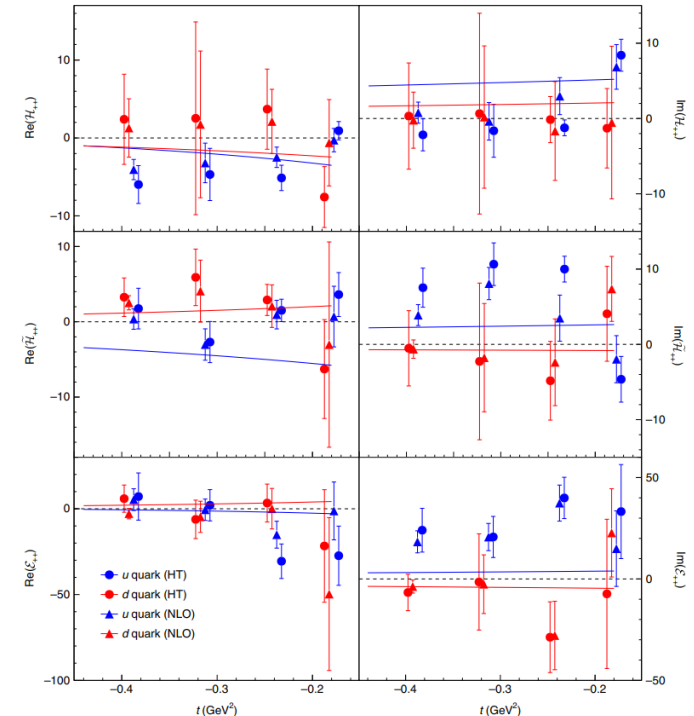
• No neutron detection $D(e, e'\gamma)X - H(e, e'\gamma)X = n(e, e'\gamma)n + d(e, e'\gamma)d + \dots$

- Scattering off neutron (nDVCS): GPD E
 - Determination of the **Ji sum rule**: Contribution of the orbital angular momentum of quarks to the nucleon spin

$$\frac{1}{2} \int_{-1}^1 x dx (H(x, \xi, t=0) + E(x, \xi, t=0)) = J$$



+data from: Mazouz, M. et al. Phys. Rev. Lett. 99, 242501 (2007).



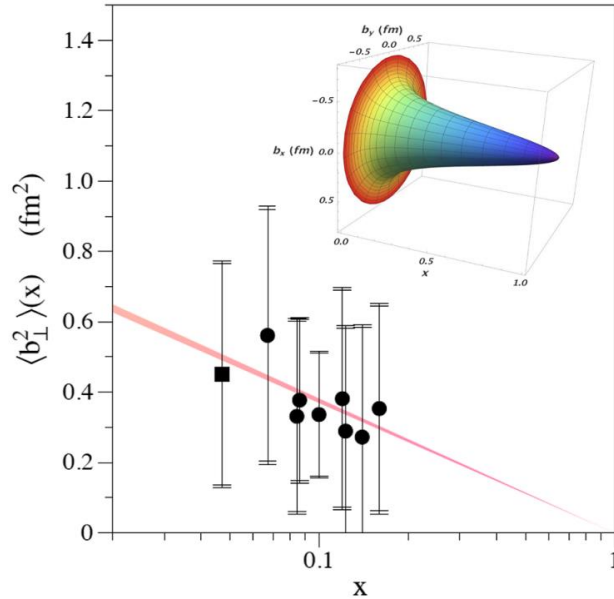
Benali, M., Desnaut, C., Mazouz, M. et al. Nat. Phys. 16, 191–198 (2020)



What did we learn from JLAB data at ~6 GeV?

• Tomography of the proton

- Obtained from local fits to HERMES, CLAS, and Hall-A data ($\mathcal{S}H$ + model dependent assumptions for x dependence)

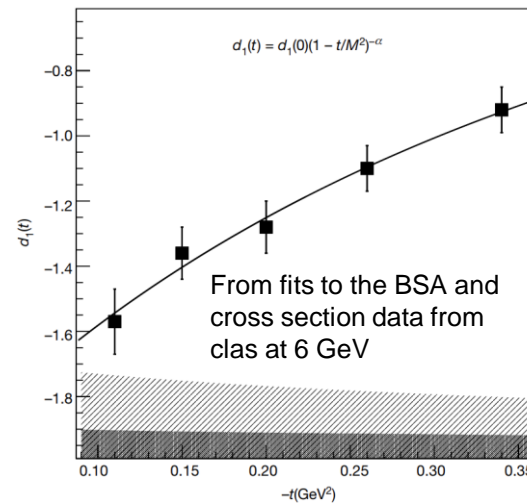


R. Dupré, M. Guidal, M.Vanderhaeghen, PRD95, 011501 (2017)

• The pressure distribution inside the proton

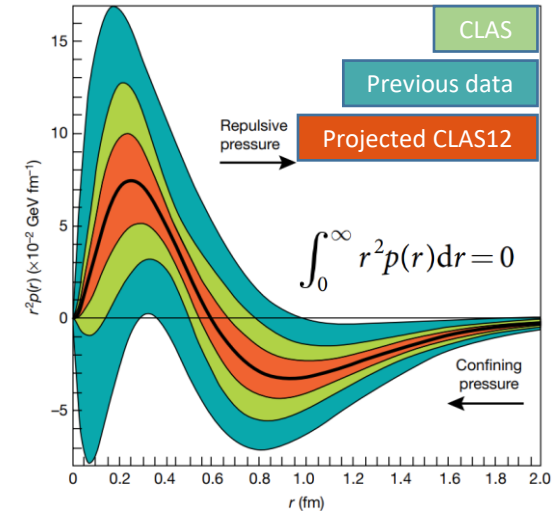
• Gravitational form factor

- $\int xH(x, \xi, t)dx = M_2(t) + \frac{4}{5}\xi^2 d_1(t)$
- $d_1(t) \propto \int \frac{j_0(r\sqrt{-t})}{2t} \rho(r)d^3r$



From fits to the BSA and cross section data from clas at 6 GeV

V. Burkert, L. Elouadrhiri, F.X. Girod, Nature 557, 396-399 (2018)





CLAS12: First observation of Timelike Compton Scattering

P. Chatagnon et al. (CLAS), Phys. Rev. Lett. 127, 262501 (2021)

- Test of universality of GPDs: direct comparison between DVCS and TCS results
- Real part of CFFs and D-term: TCS unpolarized cross section is sensitive to $\Re\{H\}$
- D-term can be related to the mechanical properties of the nucleon.

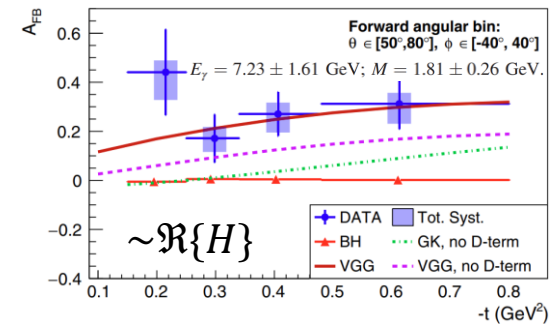
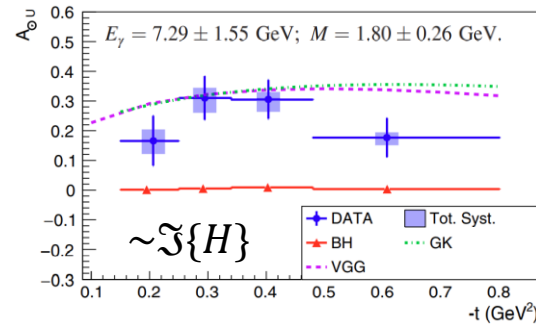
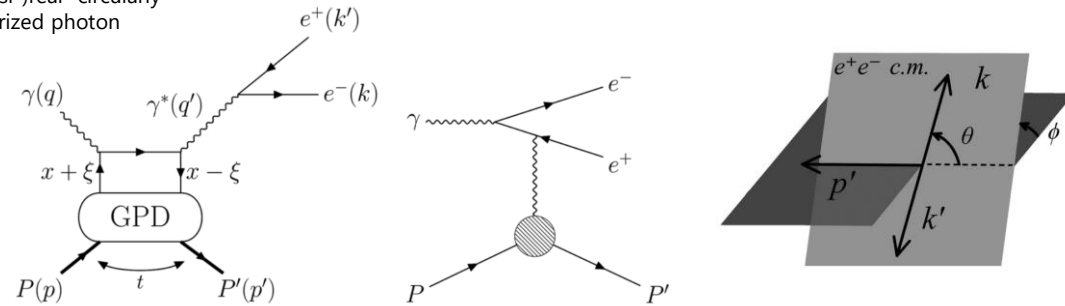
$$\text{Re}\mathcal{H}(\xi, t) \stackrel{\text{lo}}{=} D(t) + \mathcal{P} \int_{-1}^1 dx \left(\frac{1}{\xi-x} - \frac{1}{\xi+x} \right) \text{Im}\mathcal{H}(x, t)$$

$$D(t) = \frac{1}{2} \int_{-1}^1 \frac{D(z, t)}{1-z} dz \quad D(z, t) = (1-z^2) [d_1(t) C_1^{3/2}(z) + \dots]$$

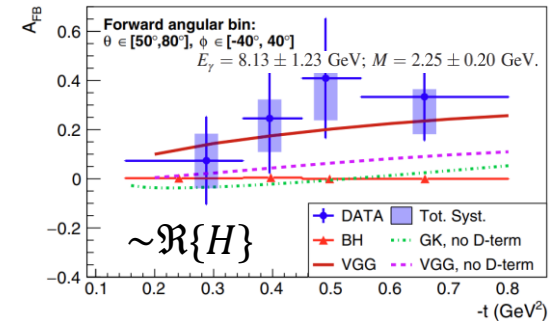
Measured observables:

- Beam helicity asymmetry: $\Im\{H\}$
- Forward-backward asymmetry: $\Re\{H\}$

(quasi-)real circularly-polarized photon



- GPDs are universal functions
- Data compatible with model including D-term: understand the internal pressure of proton





CLAS12: DVCS off proton

G. Christiaens, M. Defurne, D. Sokhan to be published soon

- Polarised beam (86%) with energy 10.6 GeV
- Unpolarised LH2 target
- 64 (Q^2, x_b, t) kinematical bins

Comparisons with KM15 and VGG/GK models

Kumericki, Kresimir and Muller, Dieter, EPJ Web of Conferences 112, 01012 (2016).

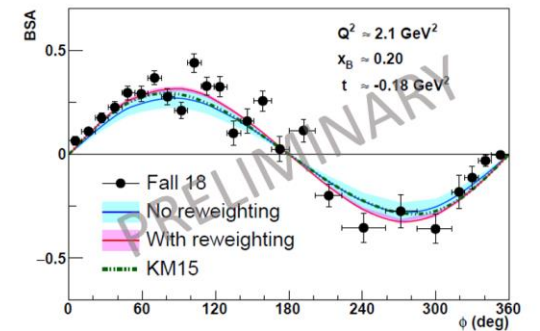
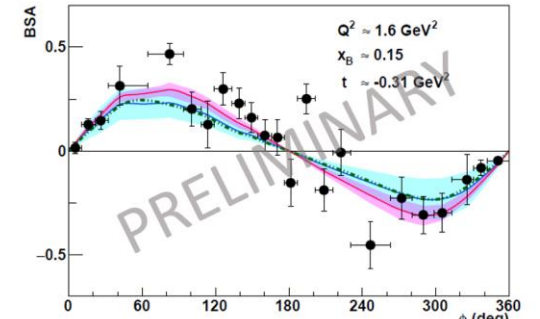
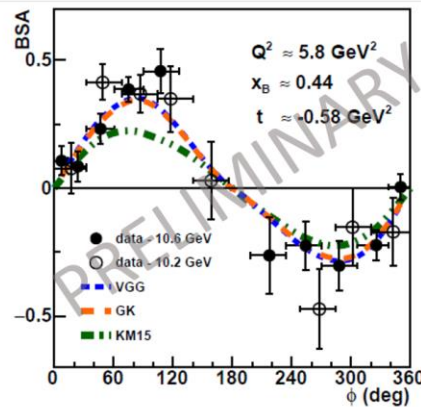
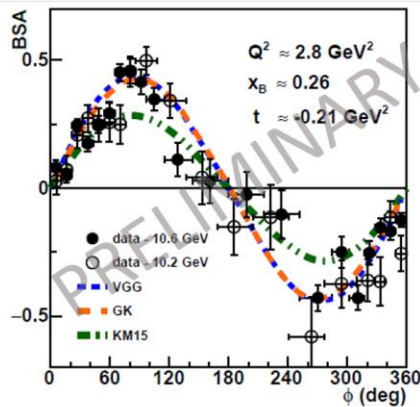
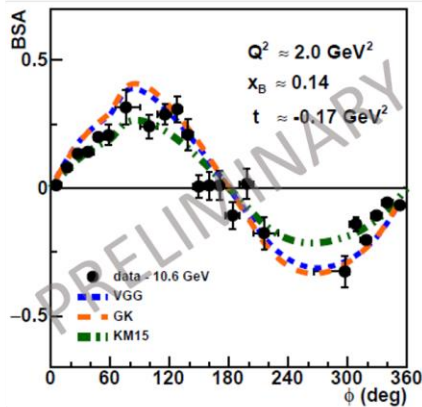
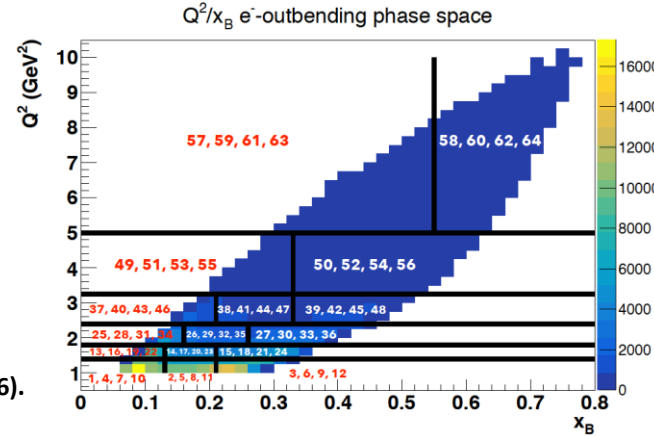
S. V. Goloskokov and P. Kroll, EPJC 65, 10.1140 (2009)

M. Vanderhaeghen, P. A. Guichon, and M. Guidal, Phys.Rev. D60, 094017 (1999)

H. Moutarde, P. Sznajder, and J. Wagner, EPJC 79, 614 (2019)

- Deriving the mean and standard deviation of a 100 ANN-predictions produced by a global fit (PARTONS)
- The new data are shown to be in good agreement

Extended kinematical coverage

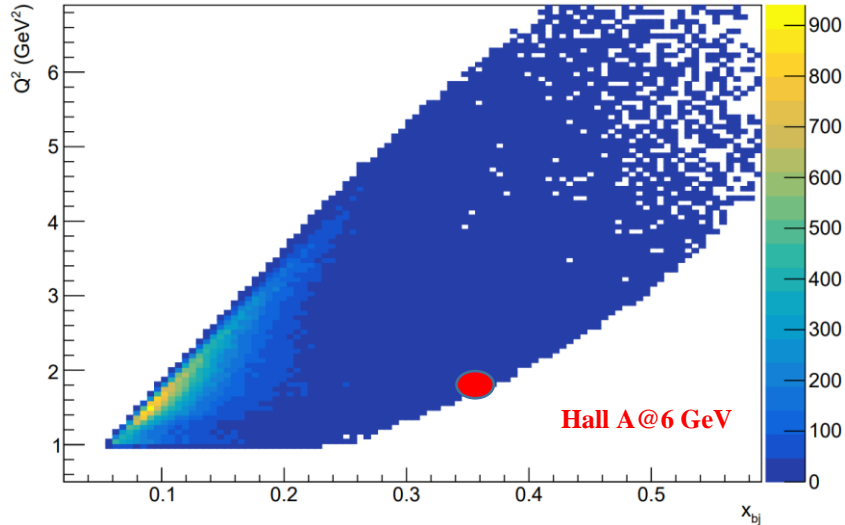




CLAS12: nDVCS with an unpolarized deuterium target

First-time measurement of nDVCS with detection of the active neutron

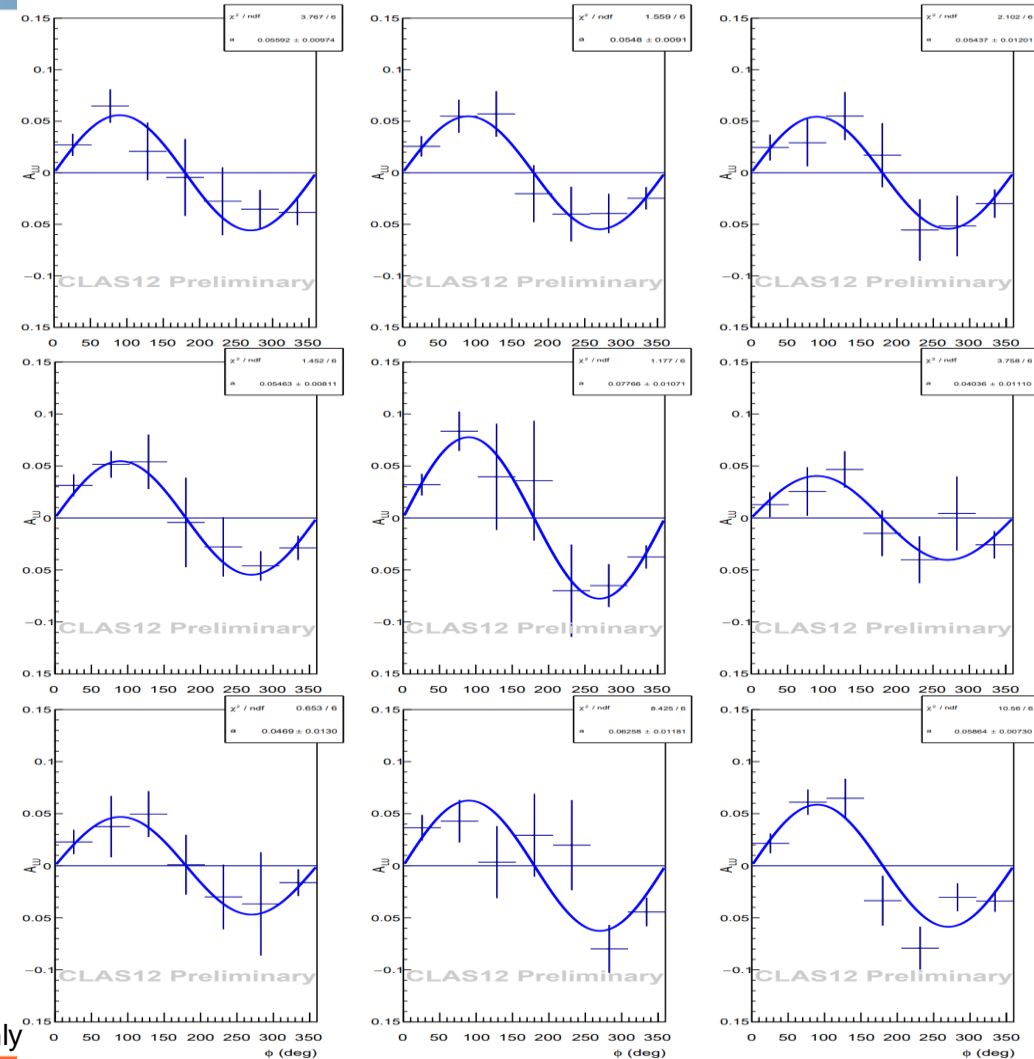
Q^2 vs x_b



Q^2 bins

x_b bins

t bins



Errors are statistical only

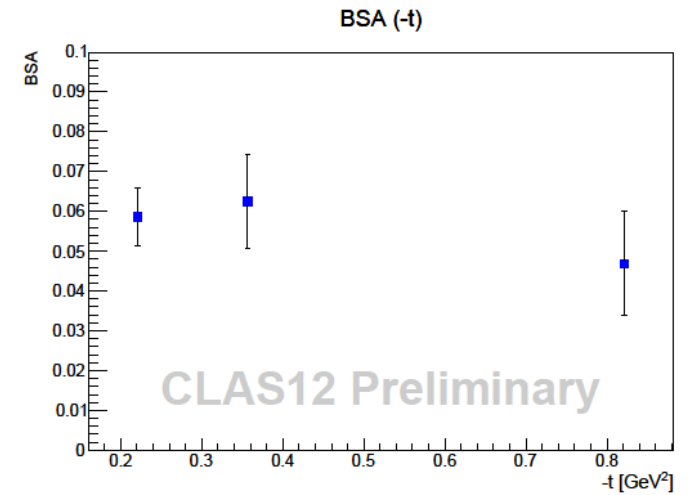
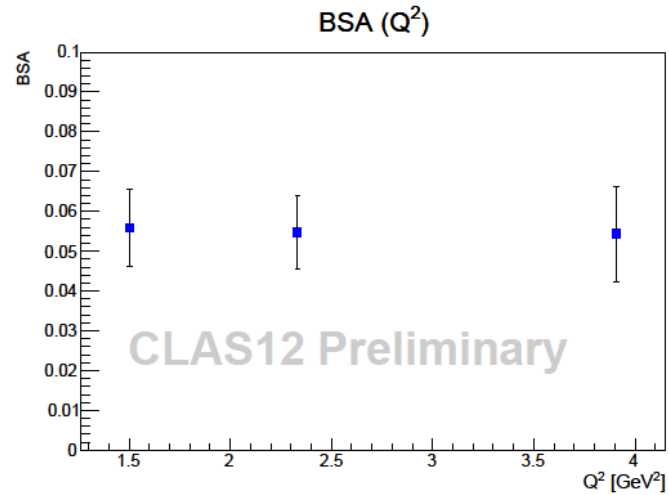
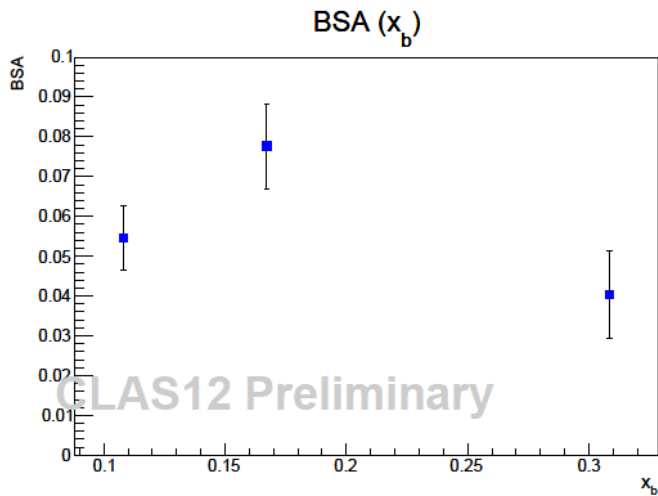
• Compared to the previous experiment, CLAS12 provides :

- The possibility to scan the BSA of nDVCS on a wide phase space
- The possibility to reach the high Q^2 high x_b region of the phase space
- Exclusive measurement with the detection of the active neutron



CLAS12: nDVCS with an unpolarized deuterium target

$$\Delta\sigma_{LU} \sim \sin(\phi) \Im\{F_1 \mathbf{H} + \xi(F_1 + F_2) \tilde{\mathbf{H}} - k F_2 \mathbf{E} + \dots\}$$

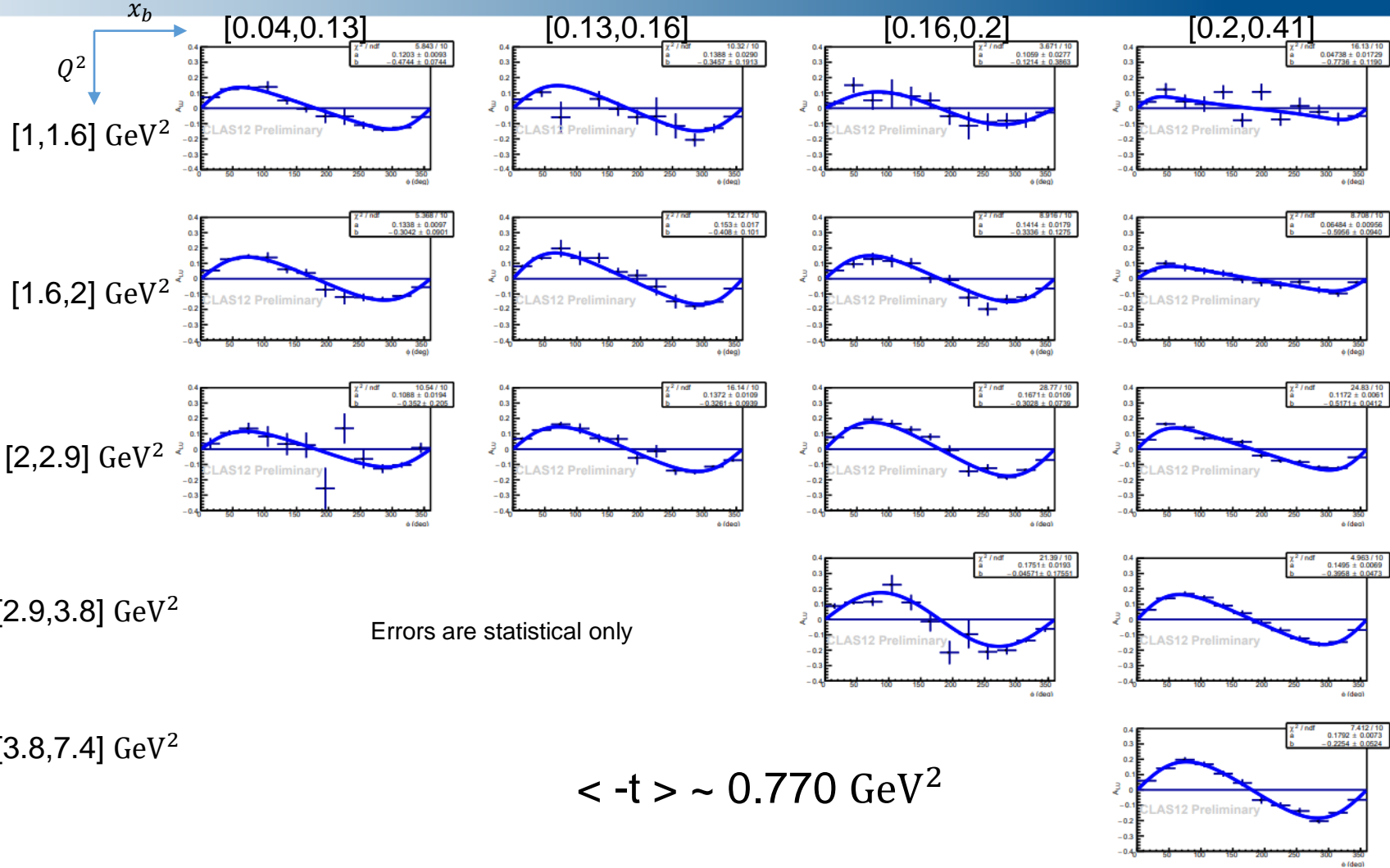


Errors are statistical only



CLAS12: pDVCS with an unpolarized deuterium target

First-time measurement of incoherent pDVCS on deuteron



Scattering off proton (pDVCS): GPD H

Quantify medium effects: Essential for the extraction of BSA of a "free" neutron (deconvoluting medium effect via comparison with DVCS on hydrogen target)

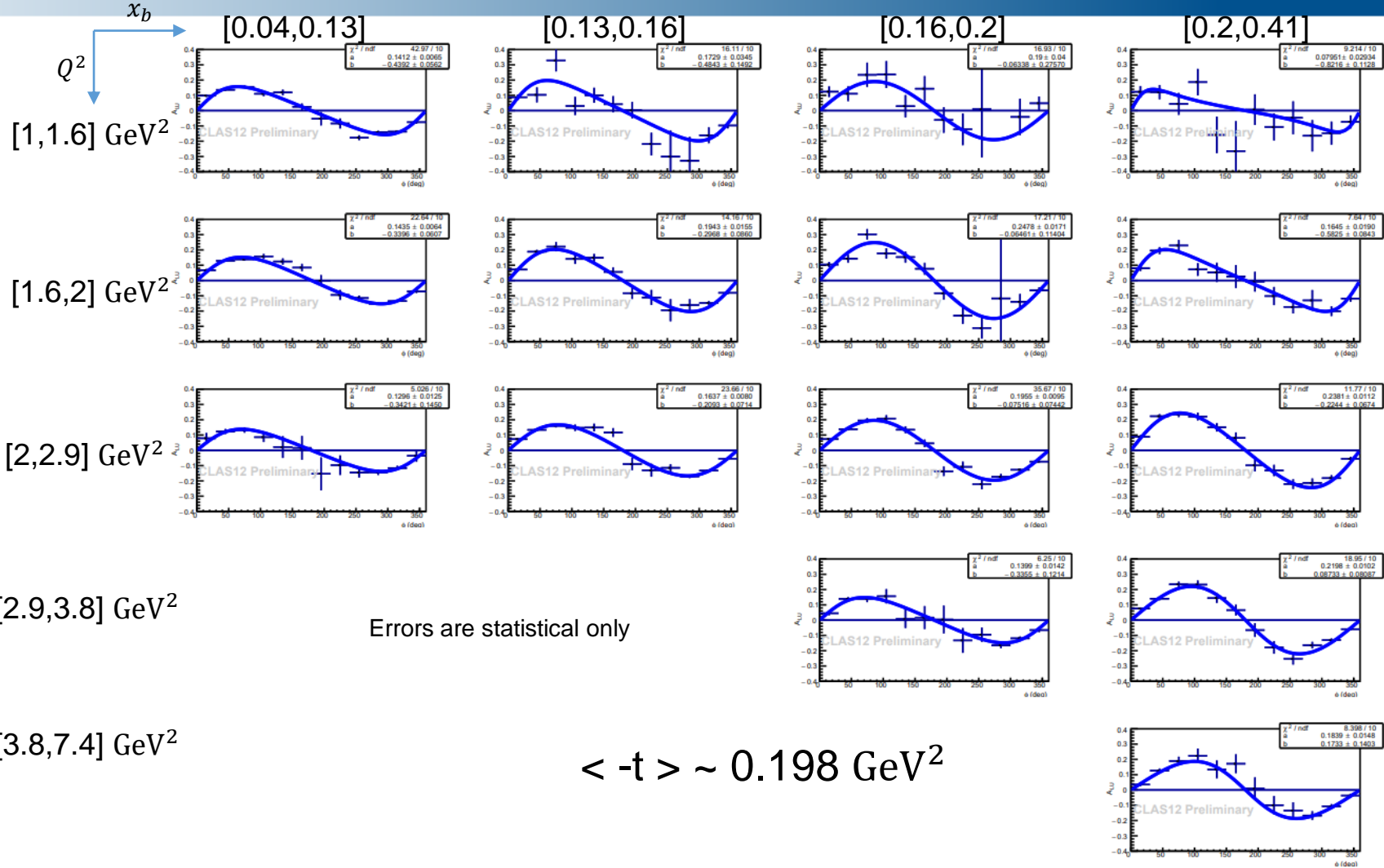


CLAS12: pDVCS with an unpolarized deuterium target

First-time measurement of incoherent pDVCS on deuteron

Scattering off proton (pDVCS): GPD H

Quantify medium effects: Essential for the extraction of BSA of a "free" neutron (deconvoluting medium effect via comparison with DVCS on hydrogen target)





- Deuteron DVCS: Physics observable to extract is Beam Spin Asymmetry (BSA)

$$\Delta\sigma_{LU} \sim \sin(\phi) \Im \left\{ \frac{2G_1 \mathbf{H}_1 + (G_1 - \tau G_3)(\mathbf{H}_1 - 2\tau \mathbf{H}_3) + \frac{2}{3} \tau G_3 \mathbf{H}_5}{2G_1^2 + (G_1 - 2\tau G_3)^2} \right\}$$

- Spin 1: 9 GPDs for each quark flavor
 - BSA of DVCS off deuterium is sensitive to 3 of them
- + DV π^0 P of deuterium (BSA- soon)
- + longitudinally polarized target (ITSA(p), IDSA(p) – data to be collected starting this summer)
- + transversally polarized target (tTSA, complementary to nDVCS-data for the GPD E extraction; expected data taking in ~2025)
- +



Conclusions

- GPDs are powerful tool to explore the structure of the nucleons and nuclei
 - Nucleon tomography, quark angular momentum, distribution of forces in the nucleon
- Exclusive reactions can provide important information on nucleon structure via the extraction of GPDs
- GPDs require complex extraction from data
- JLAB (Hall A/CLAS) data: rich information about the nucleon structure
 - First tomographic image of the proton
 - Quarks shear forces and pressure distribution inside the proton
- CLAS12 offers a wide kinematical reach over which the GPDs dependence on different kinematical variables can be scanned
 - New data to add constraints on GPDs in unexplored regions of the phase space
 - Possibilities to measure new observables using different experimental configurations
 - Flavor separation of GPDs