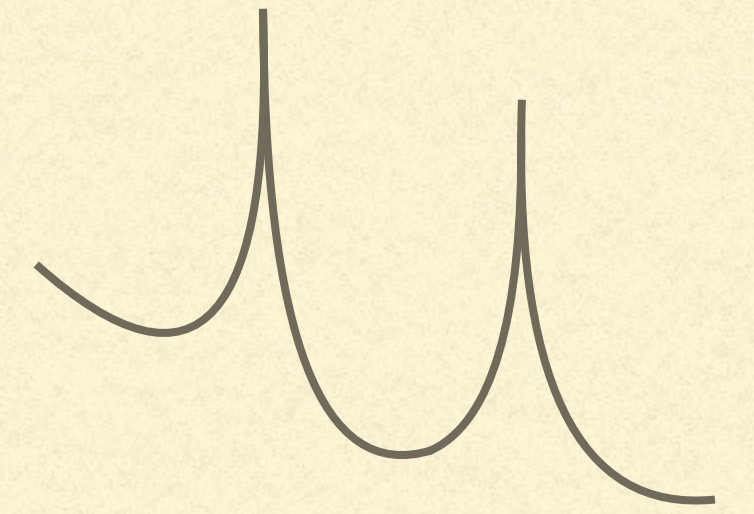
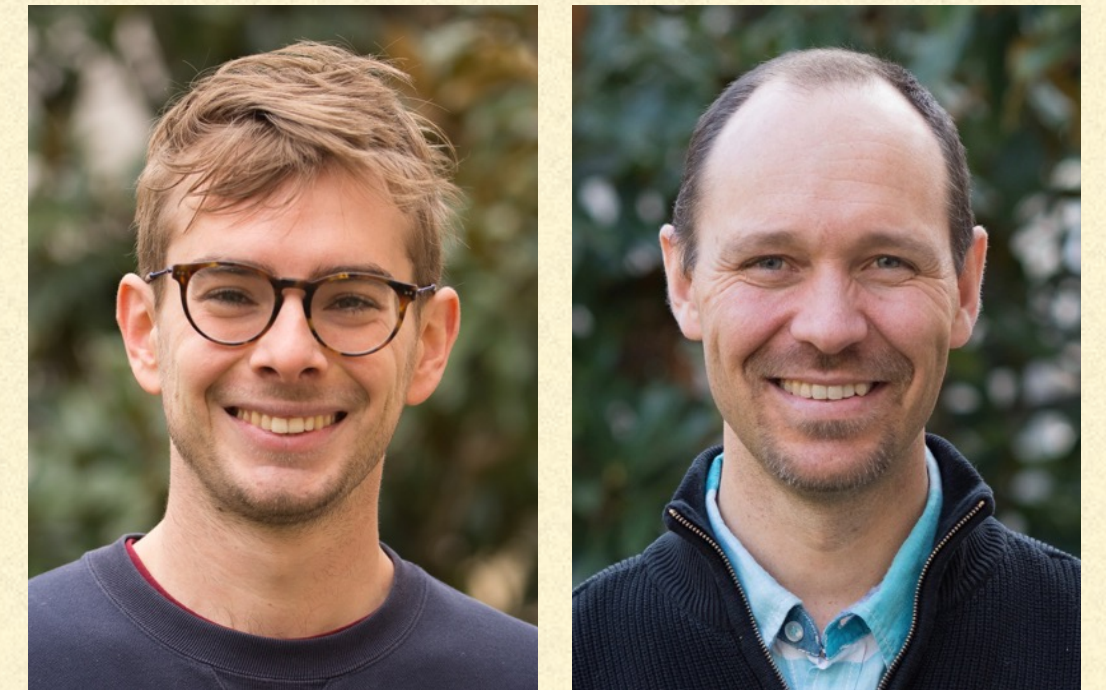


Fluctuations in a NESS: is there a universal behavior ?

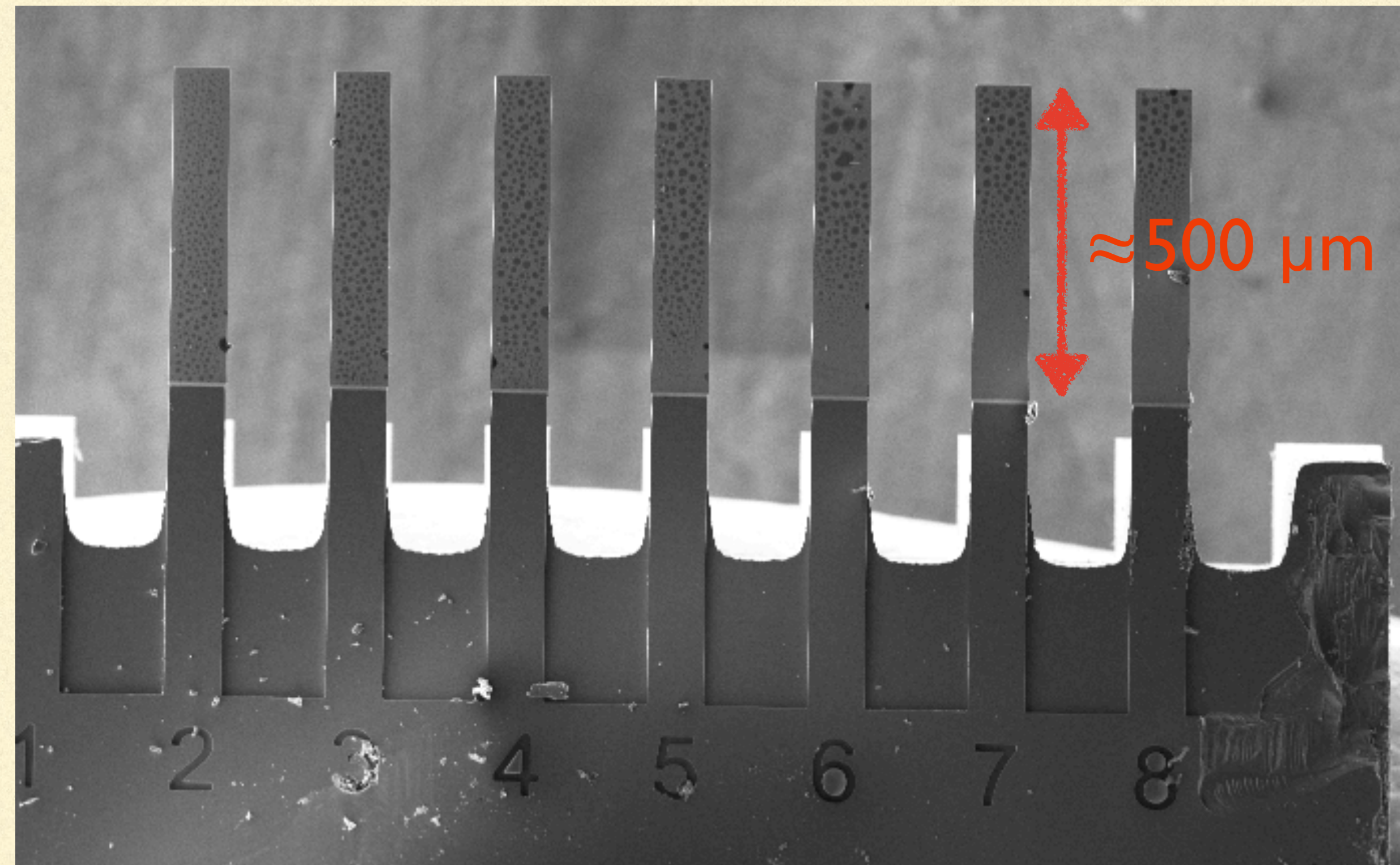
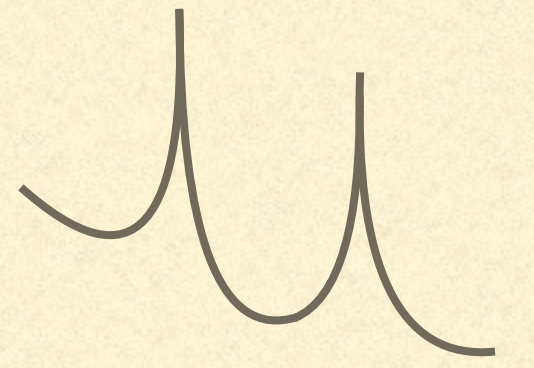


A. Fontana, L. Bellon

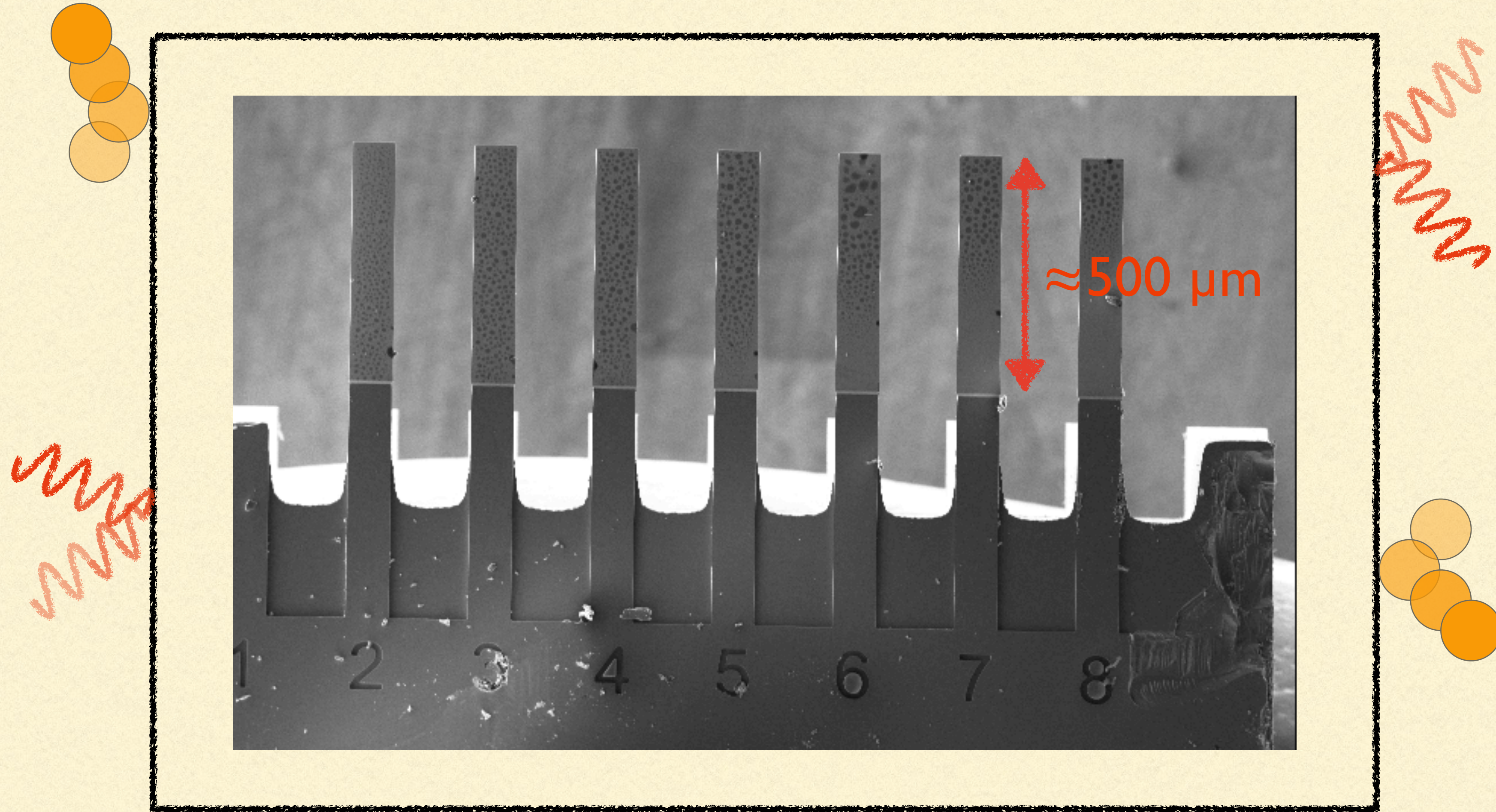
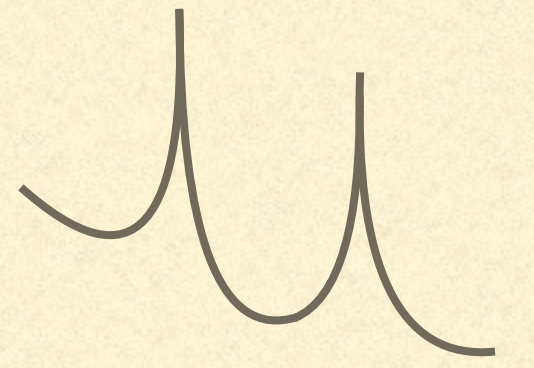
Univ Lyon, ENS de Lyon, Univ Claude Bernard, CNRS, Laboratoire de Physique



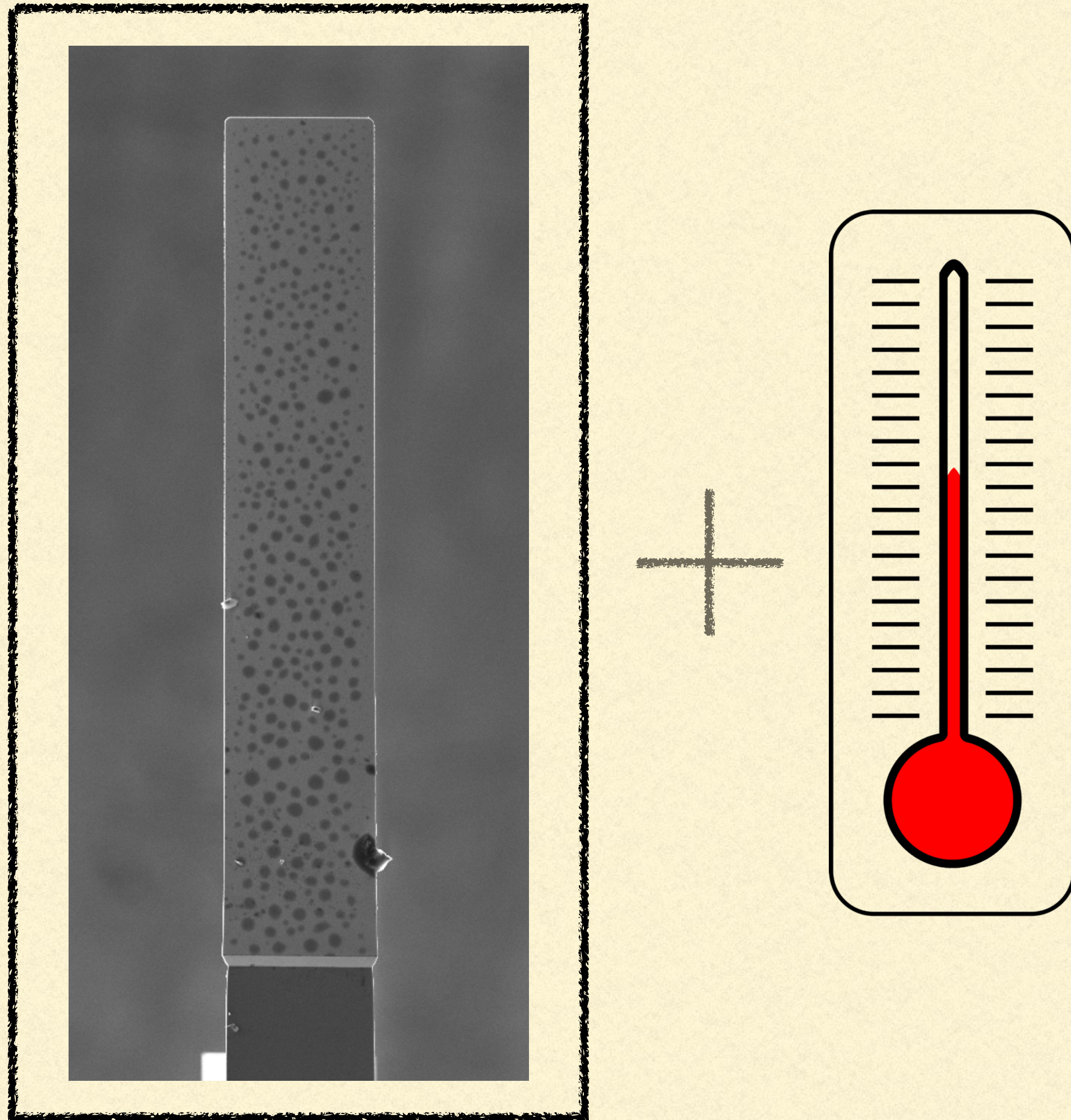
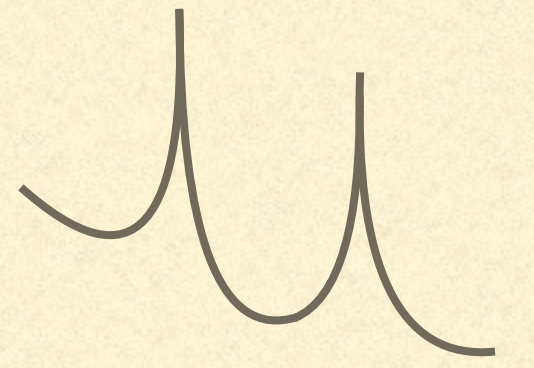
Silicon μ -cantilevers



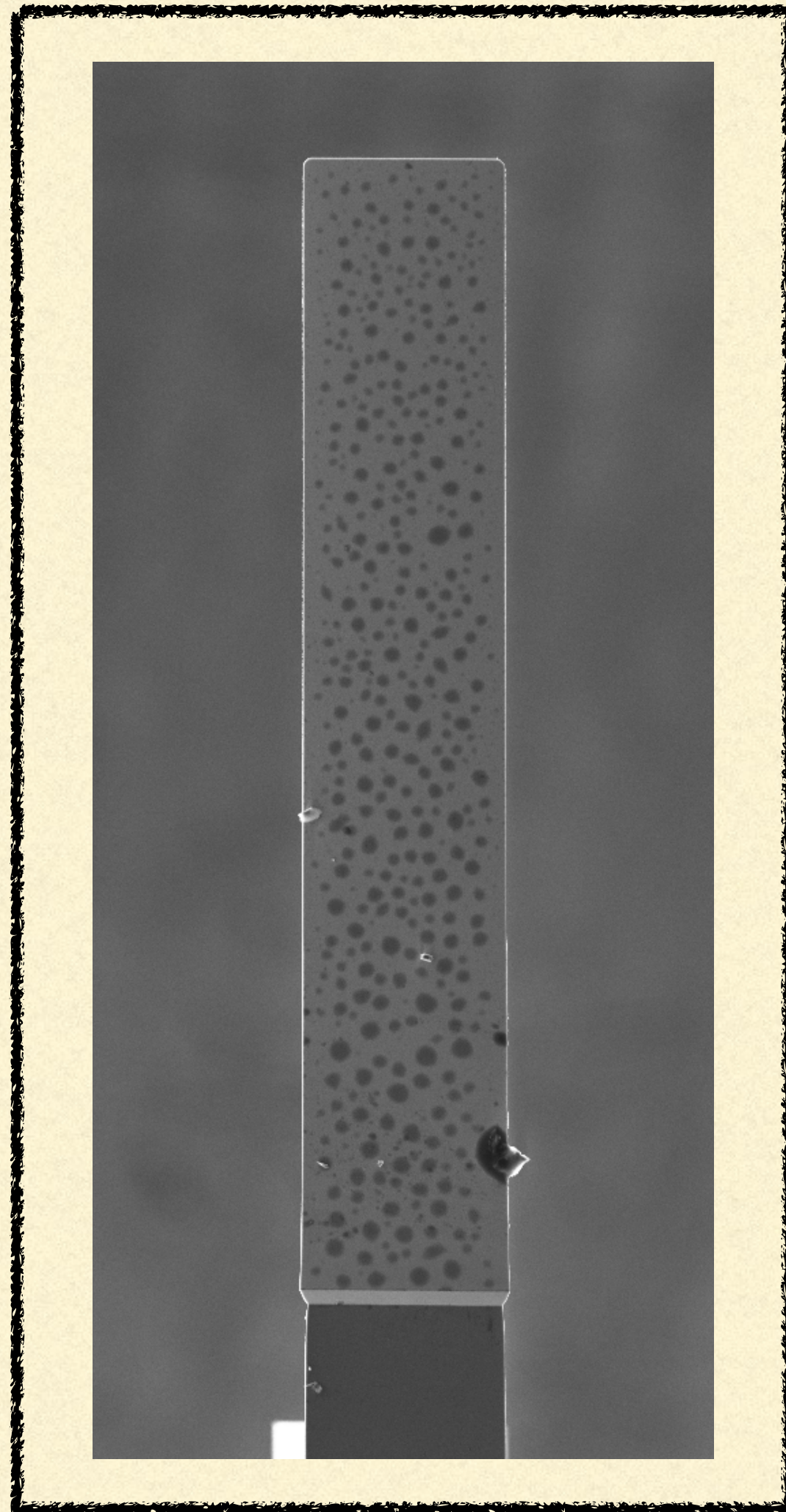
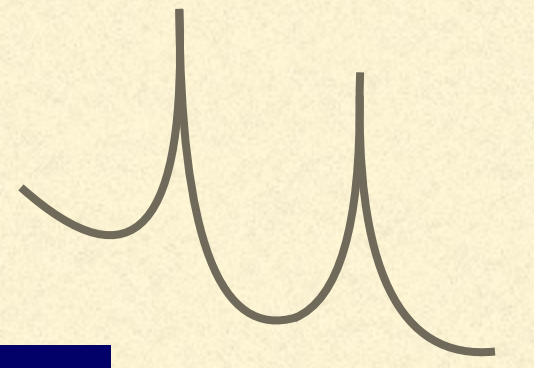
Thermal fluctuations



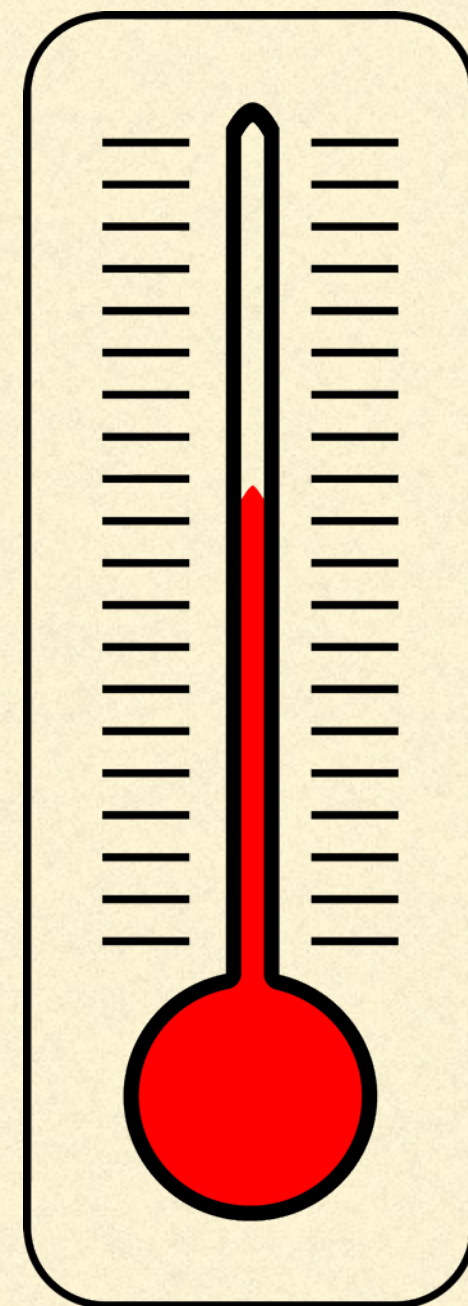
Thermal fluctuations



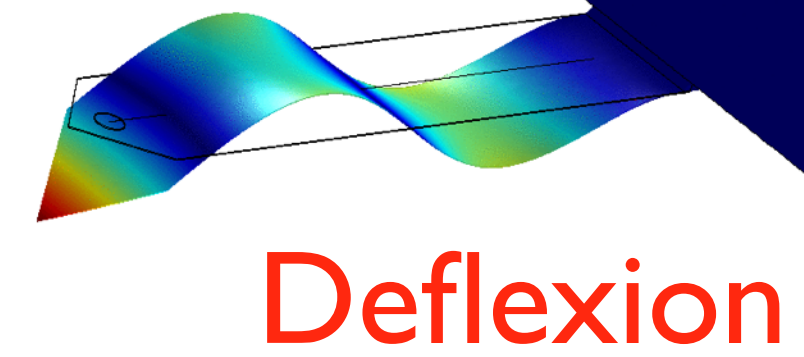
Thermal fluctuations



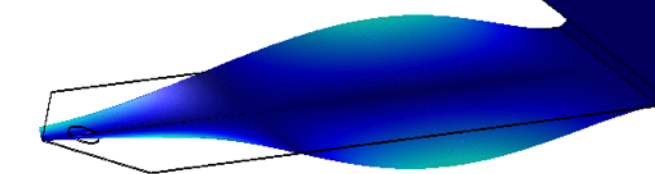
+



=

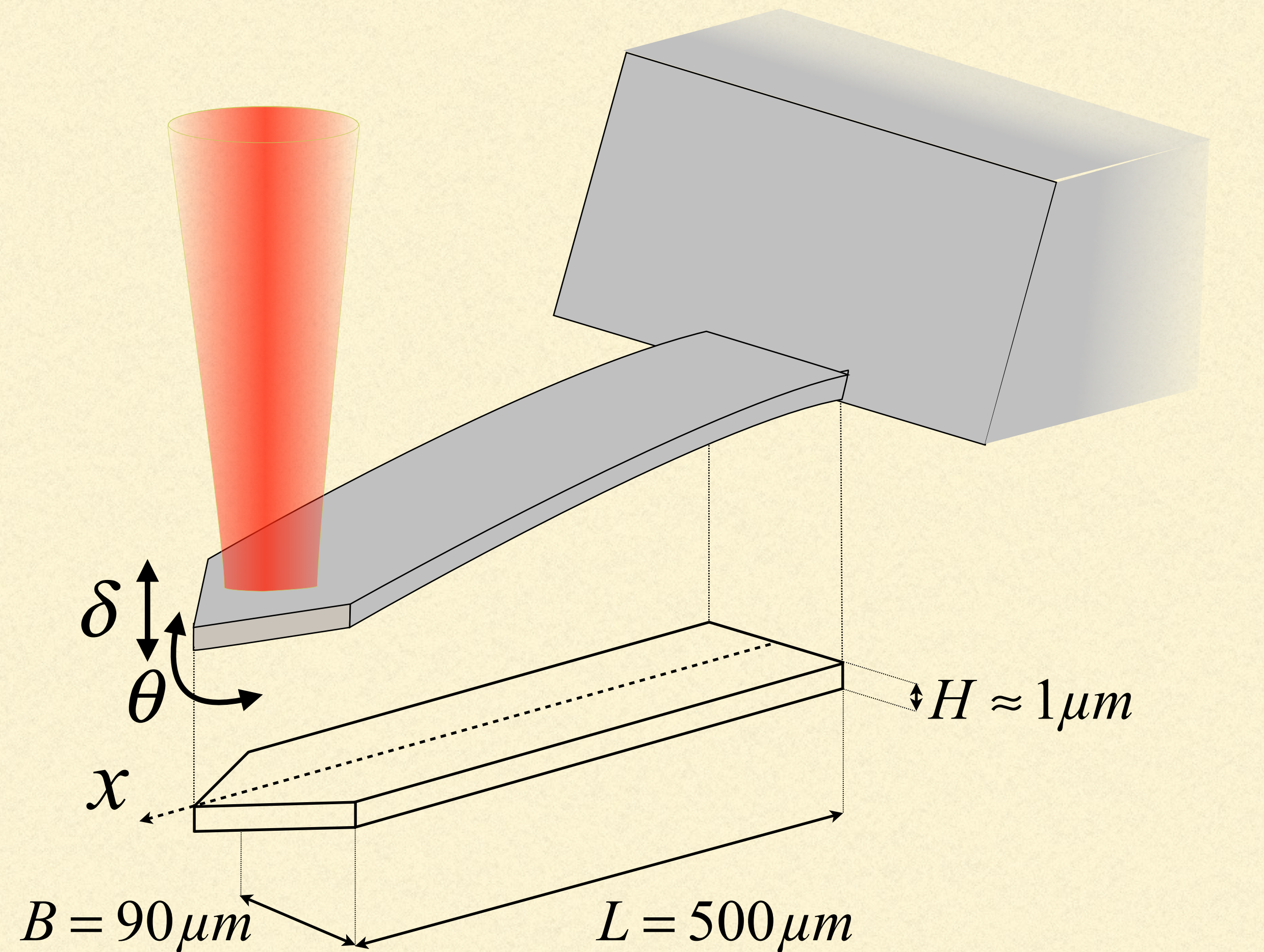
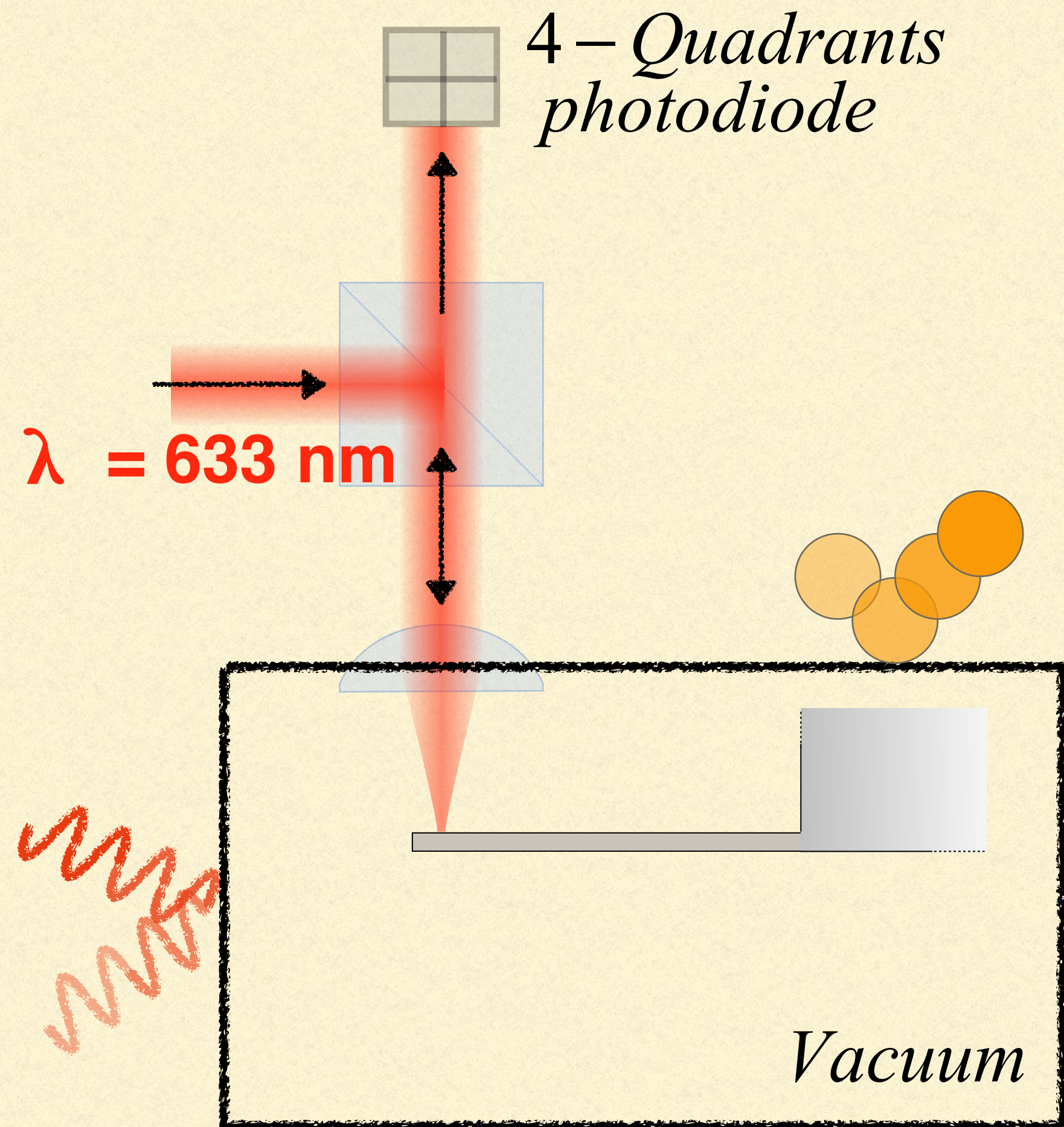


Deflexion

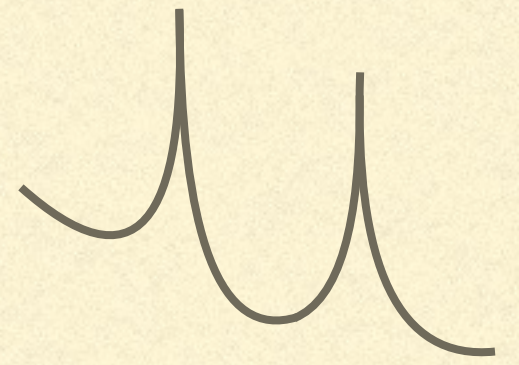


Torsion

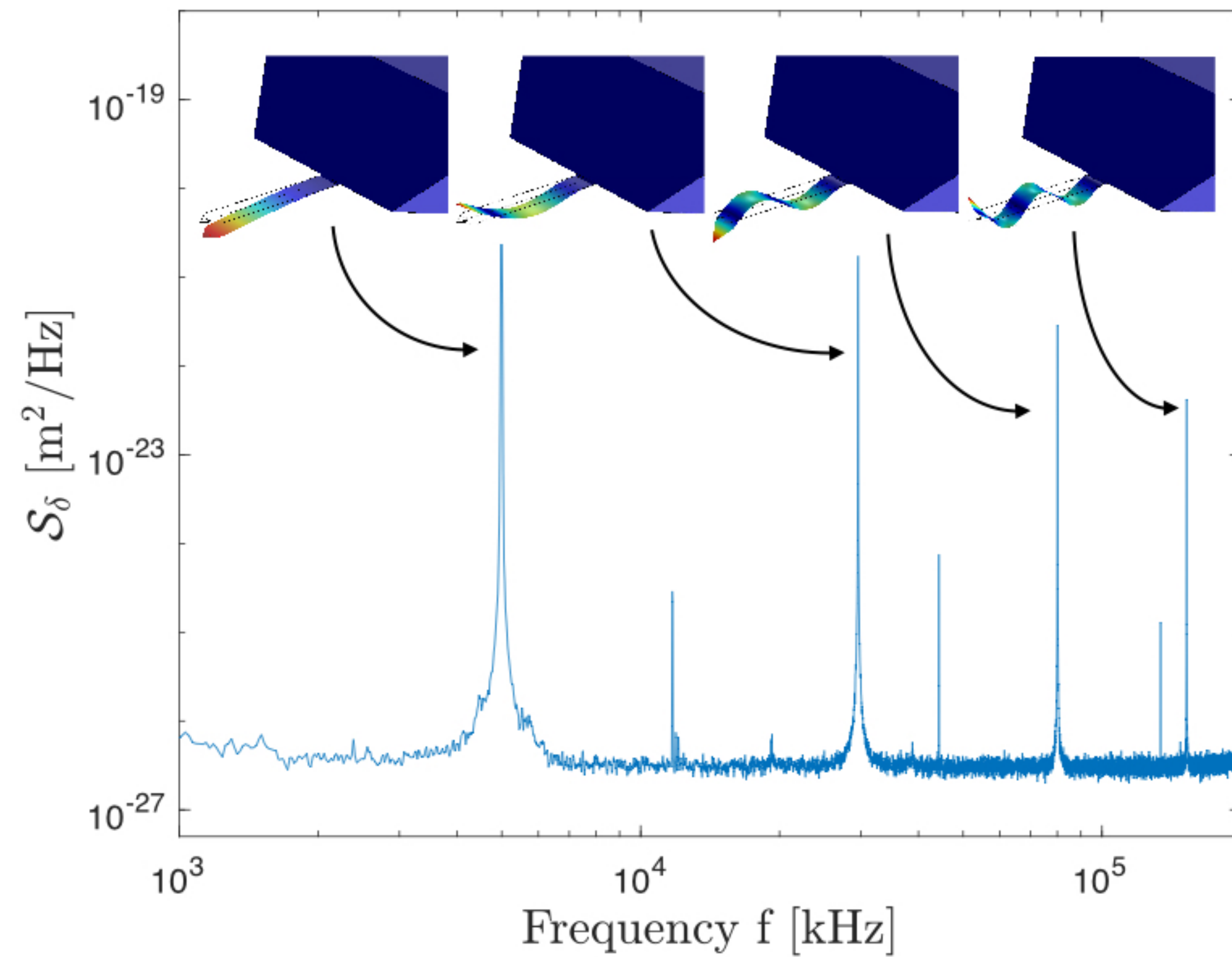
Our experiment



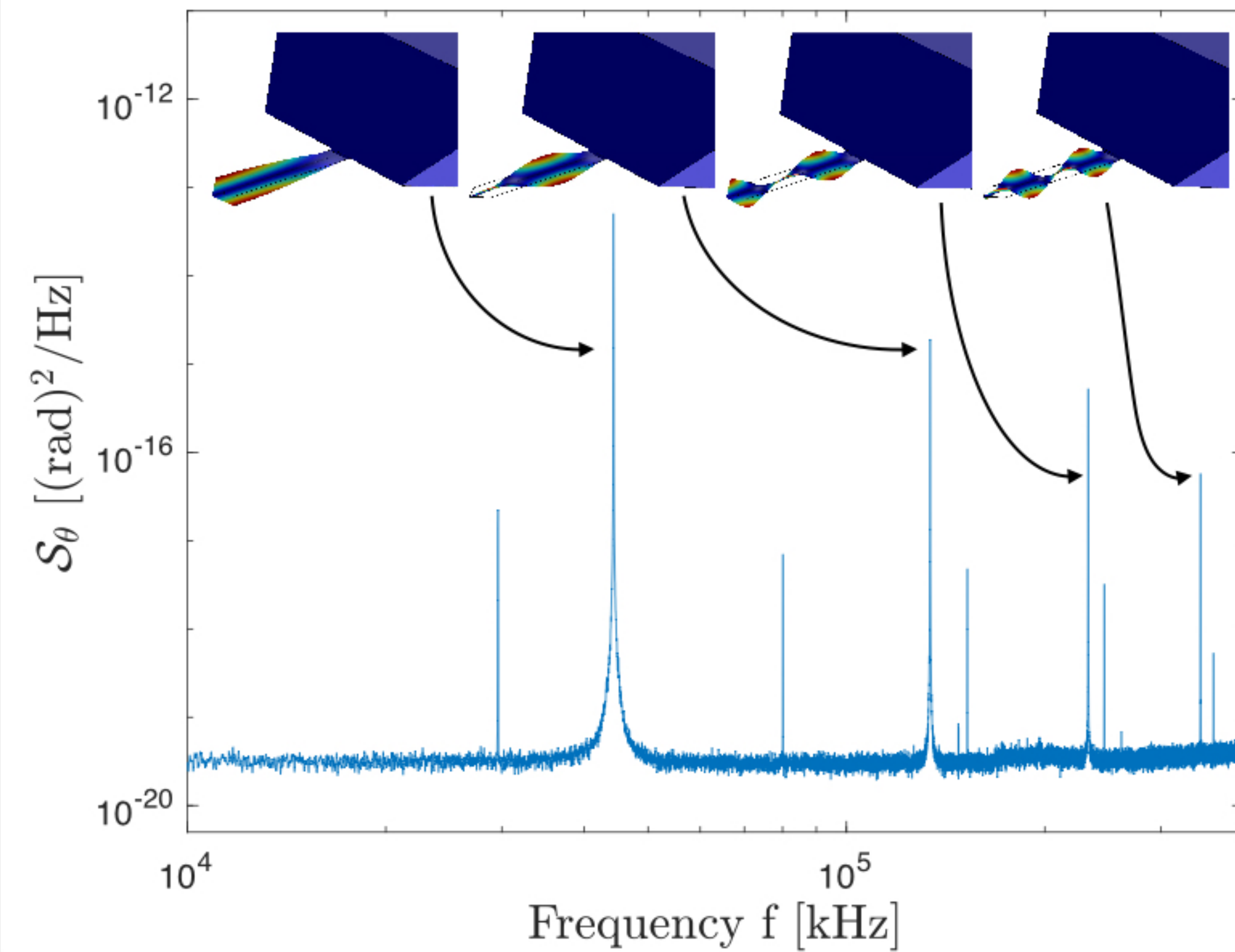
Spectra



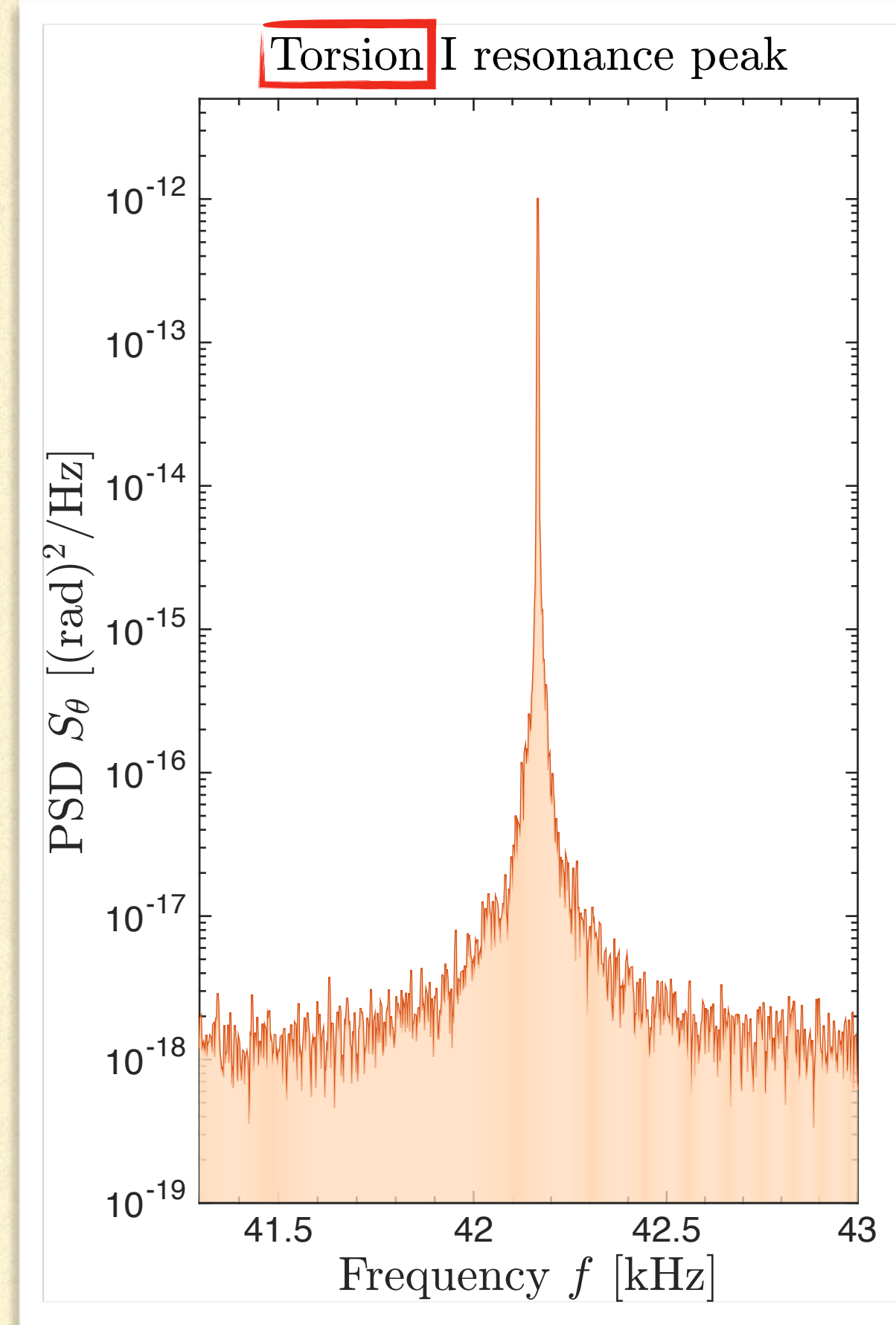
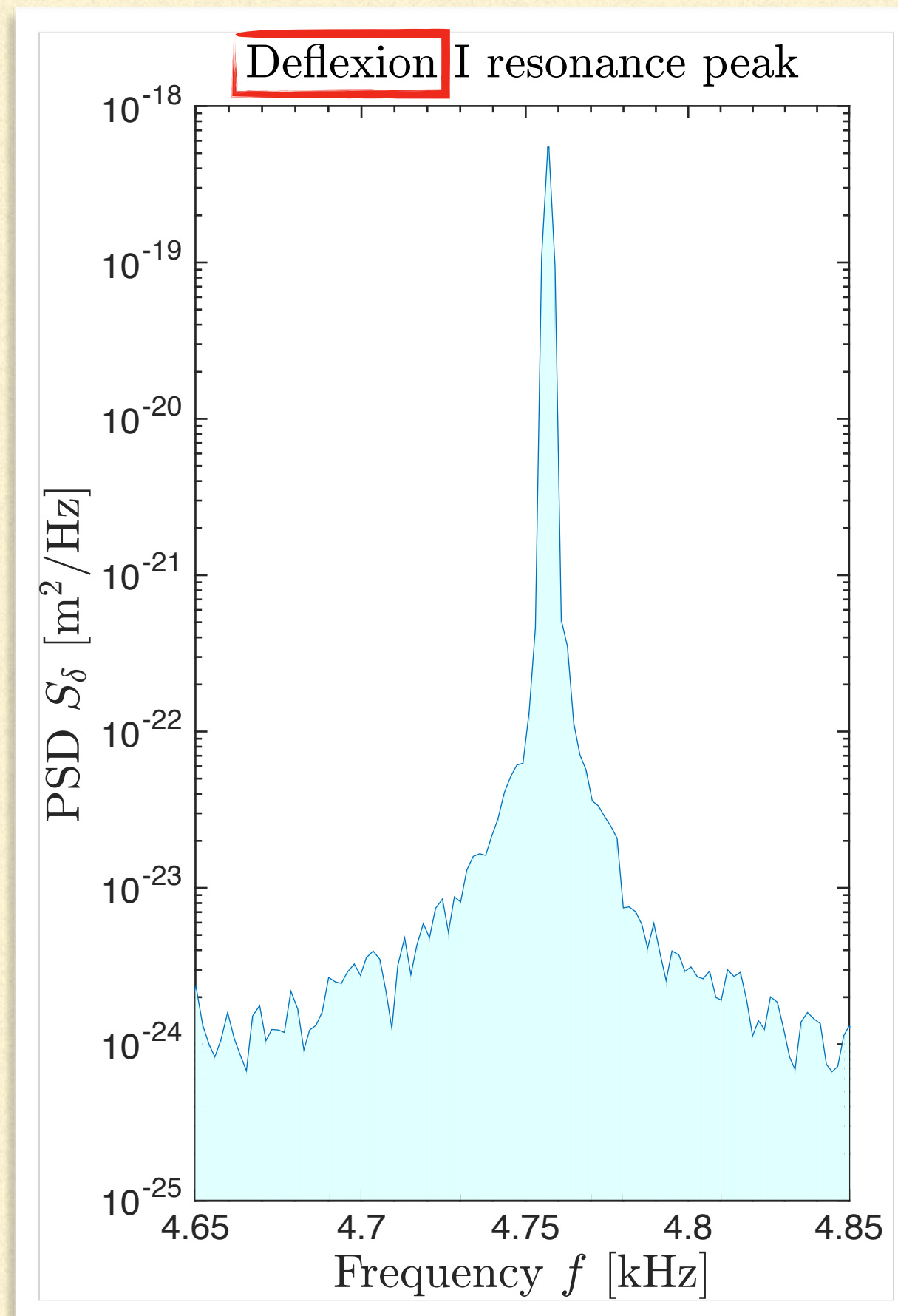
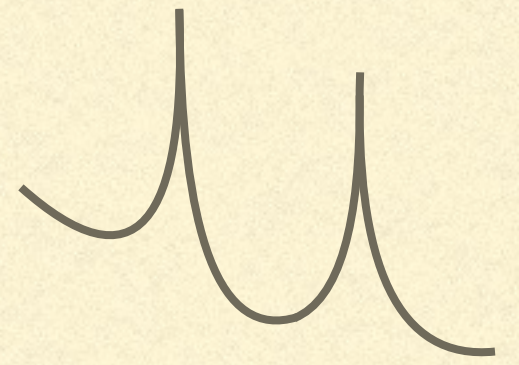
Deflexion



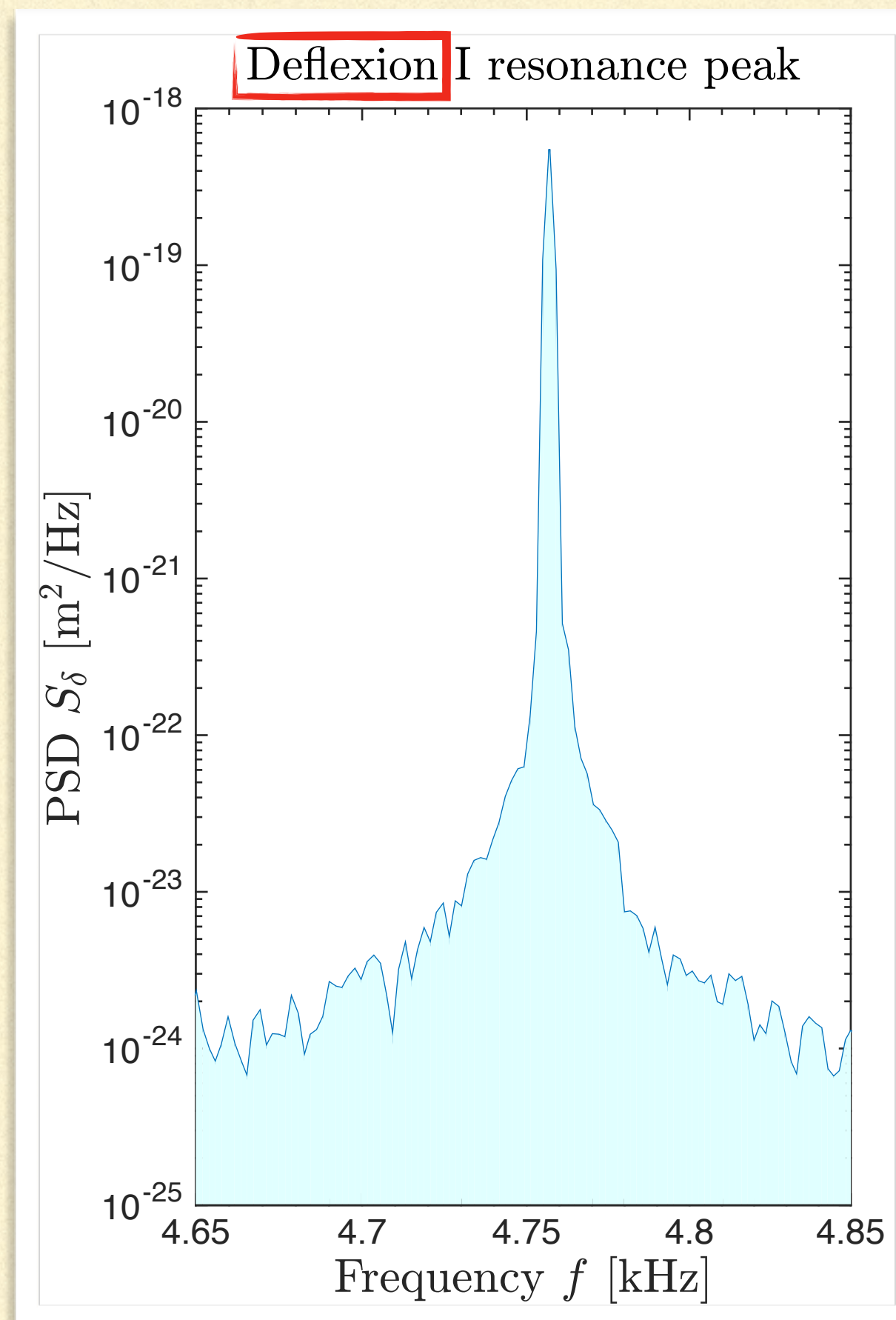
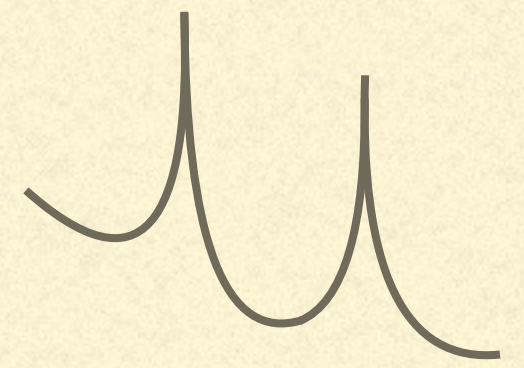
Torsion



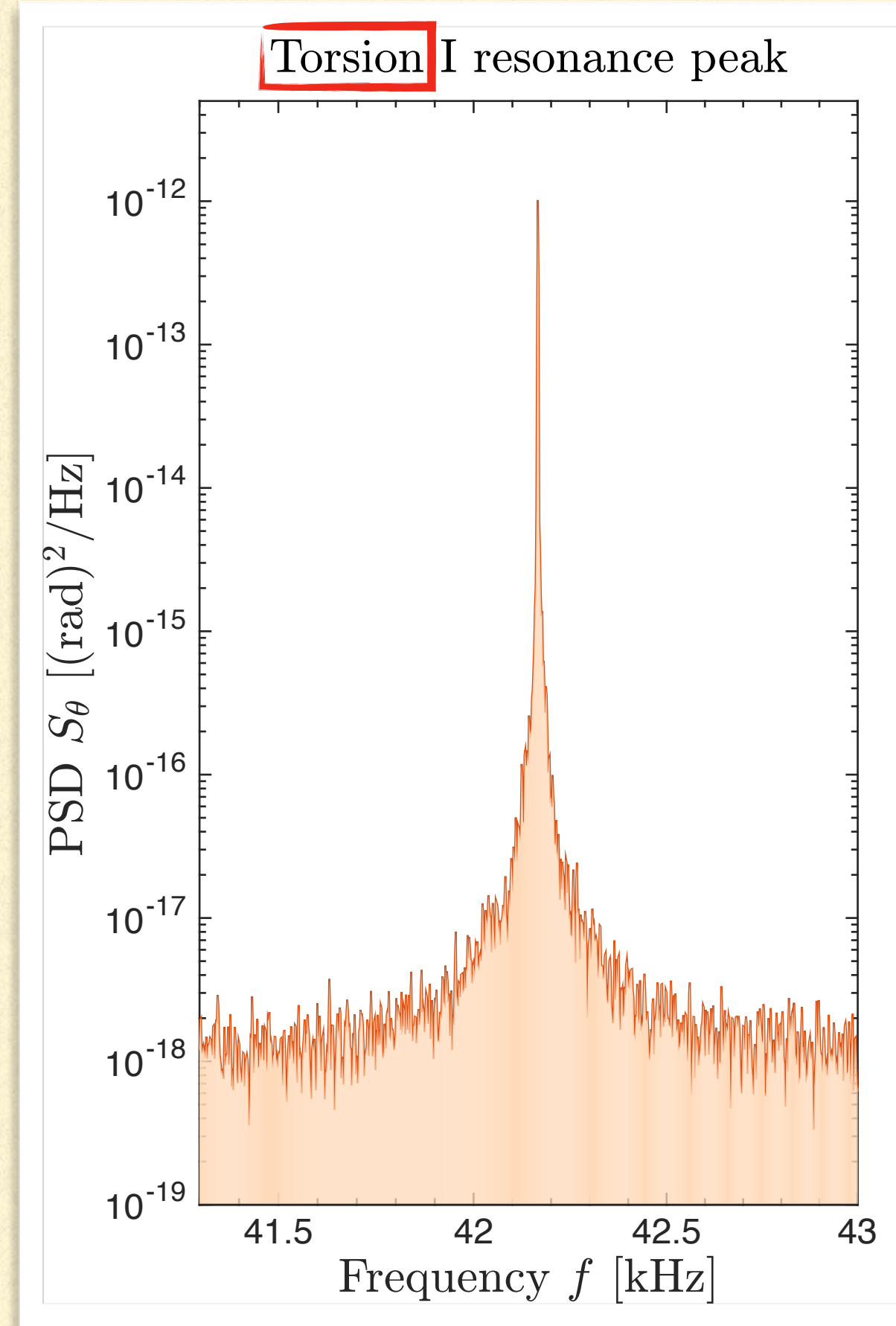
Resonance peaks



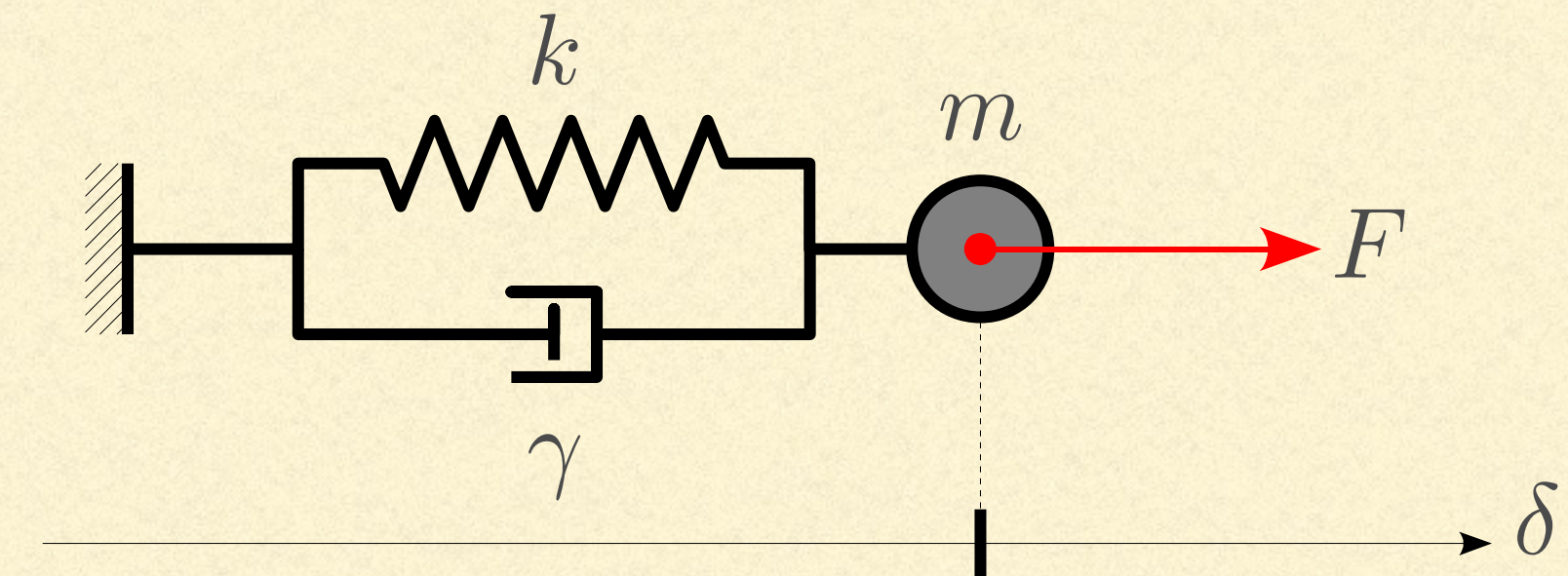
Equipartition principle



$$\langle \delta^2 \rangle = \int_{f \pm \Delta f} df \cdot S_\delta(f)$$



$$\langle \theta^2 \rangle = \int_{f \pm \Delta f} df \cdot S_\theta(f)$$

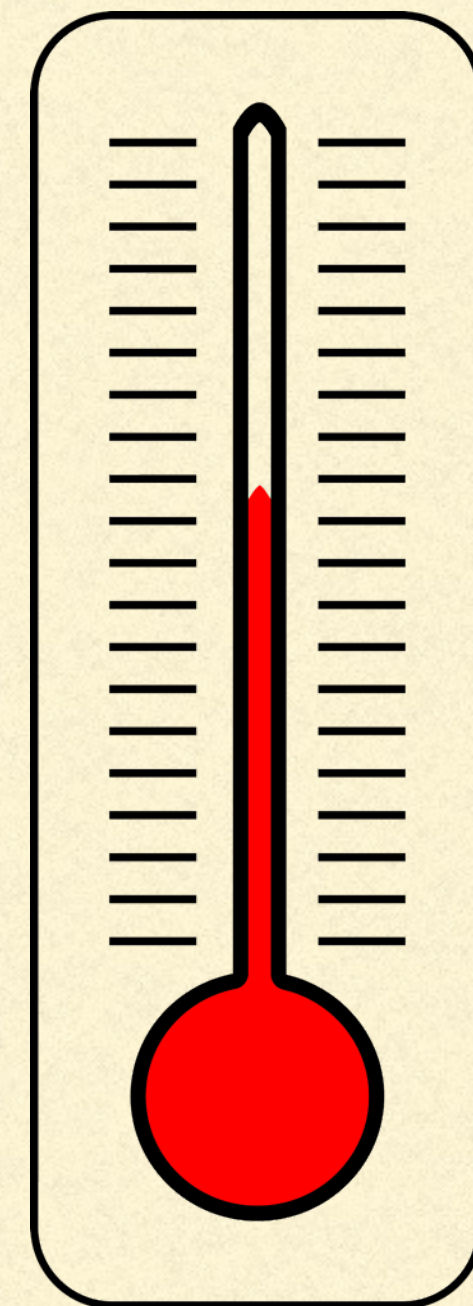
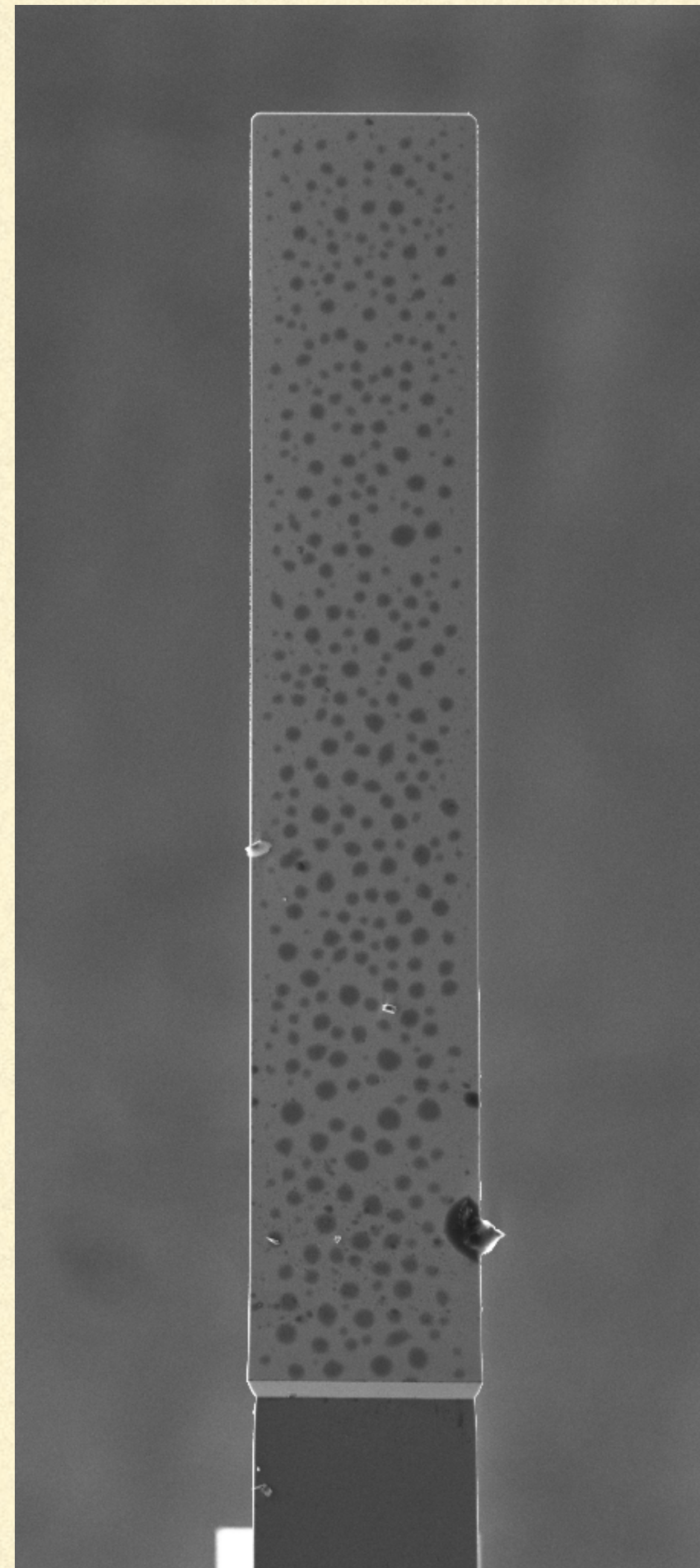
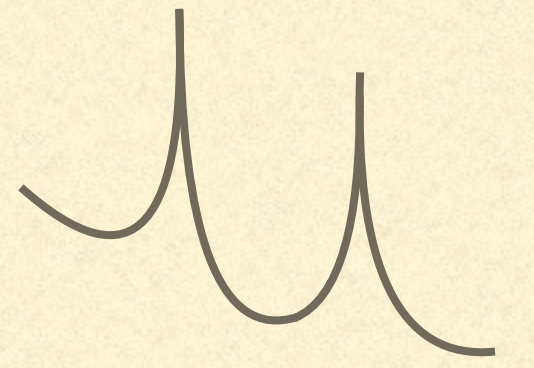


Equipartition Principle

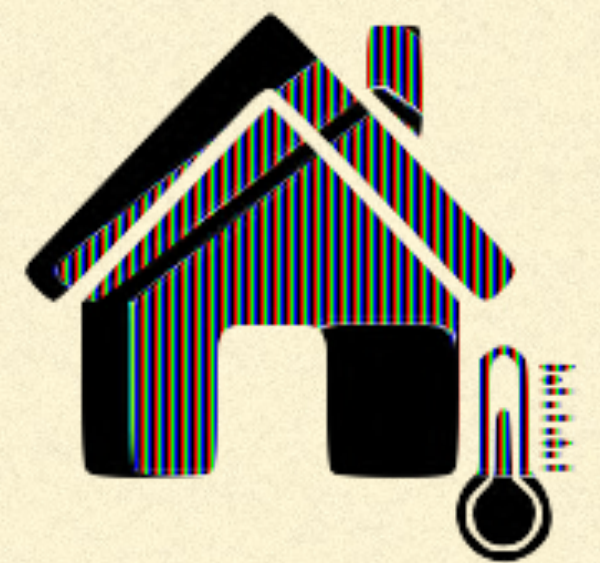
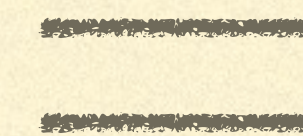
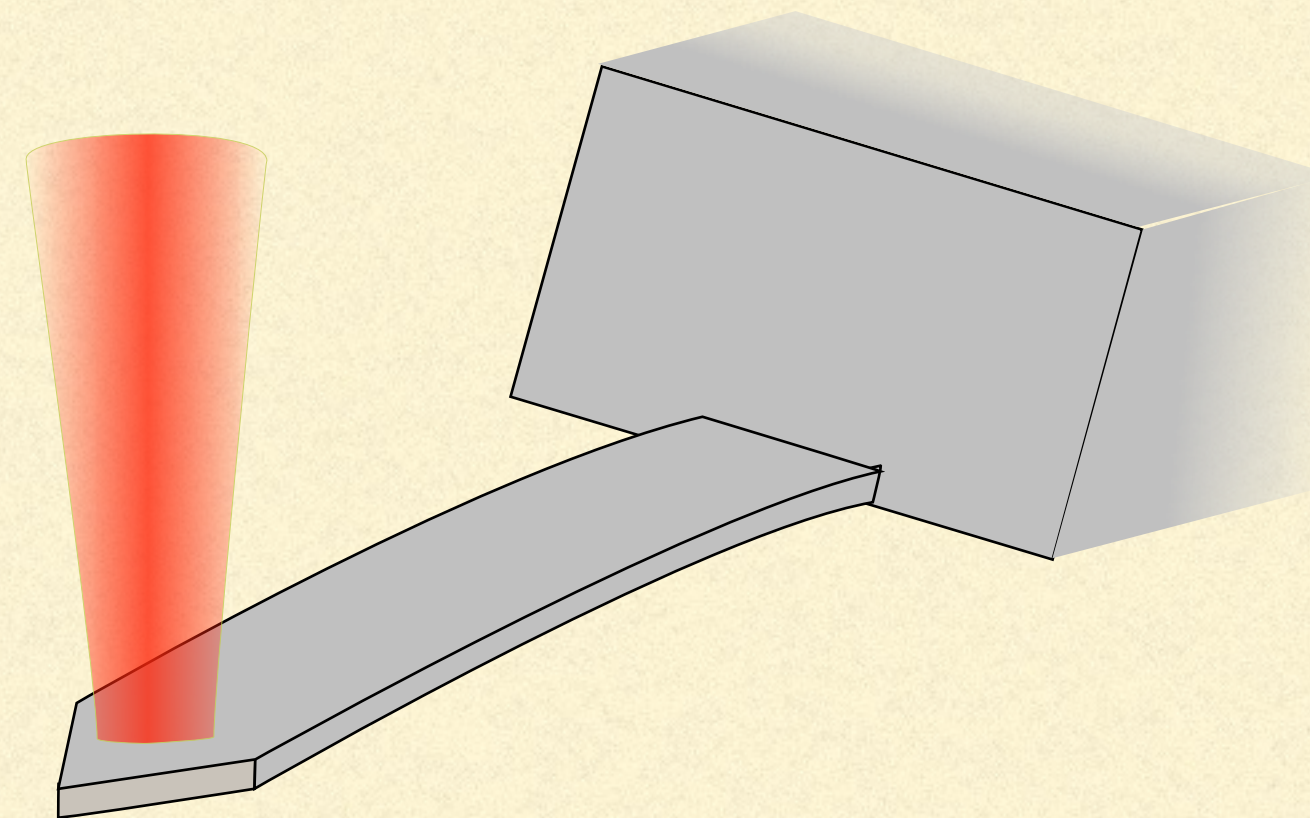
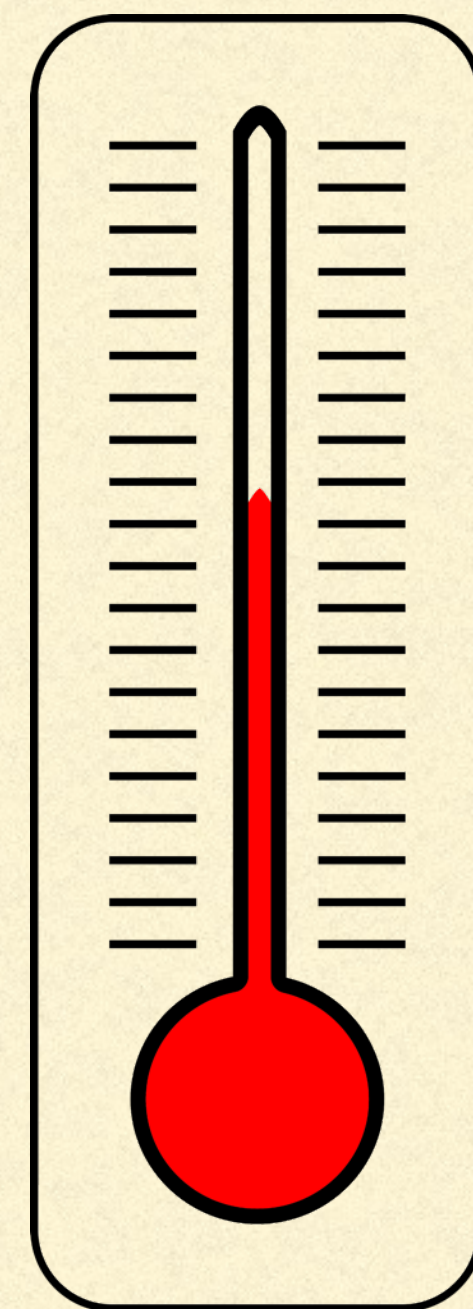
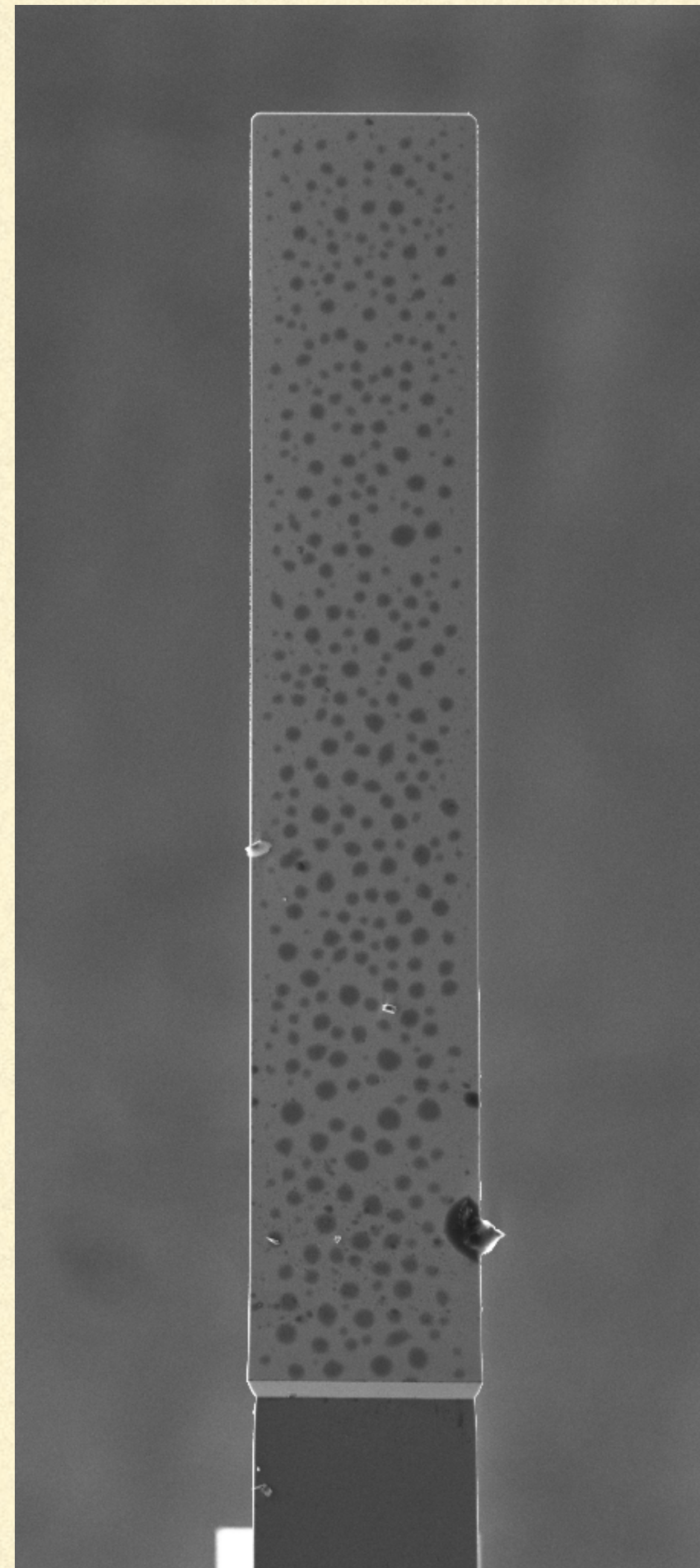
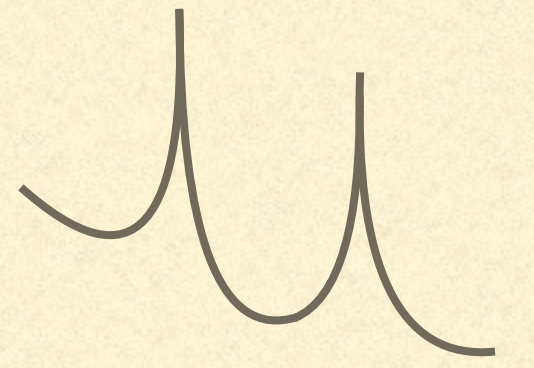
$$\frac{1}{2} k^{defl} \langle \delta^2 \rangle = \frac{1}{2} k_B T$$

$$\frac{1}{2} k^{tors} \langle \theta^2 \rangle = \frac{1}{2} k_B T$$

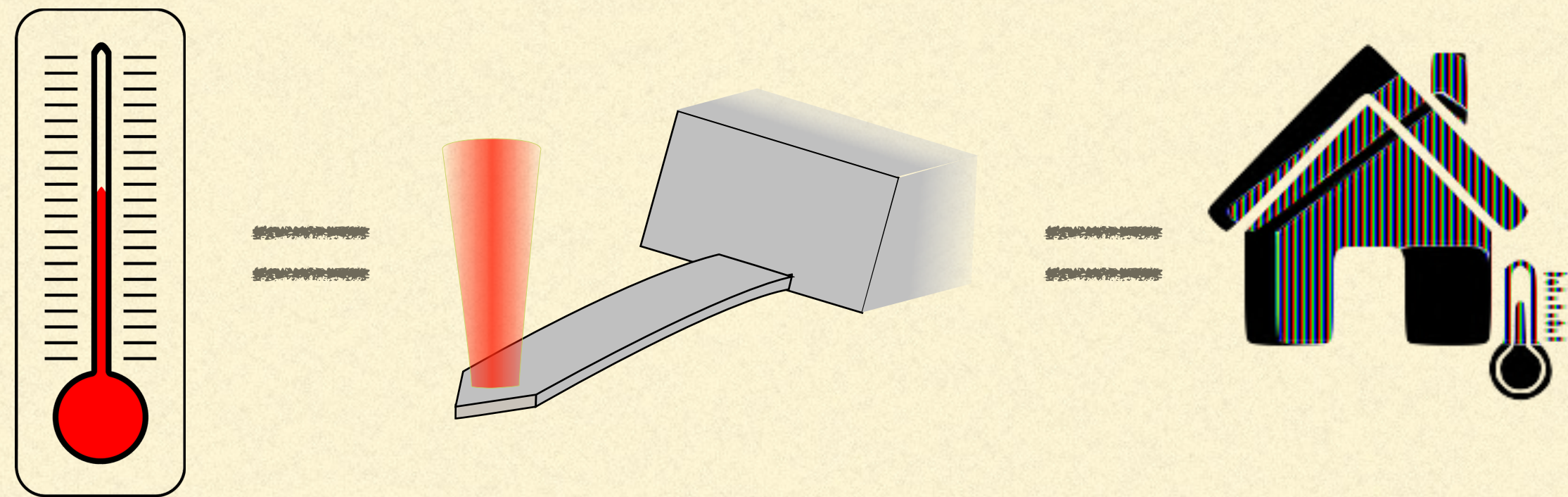
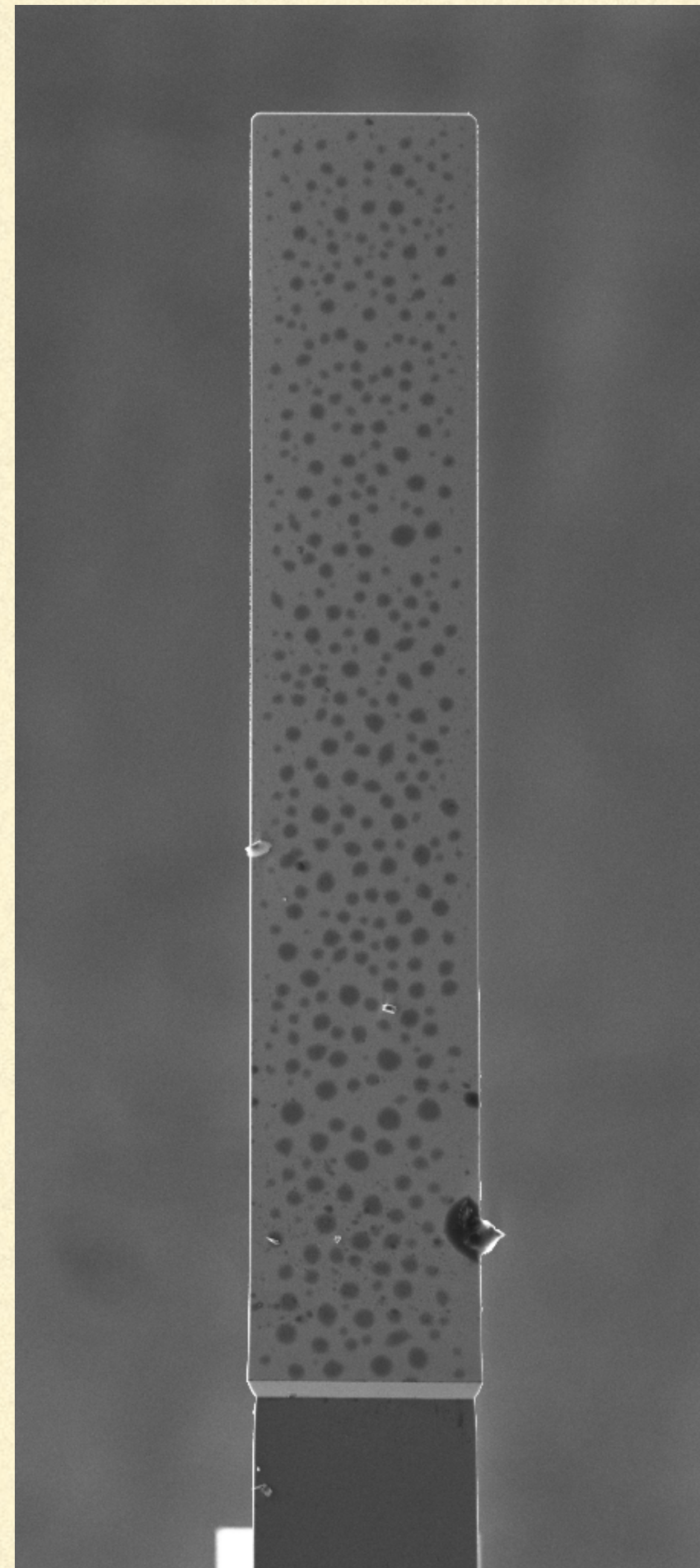
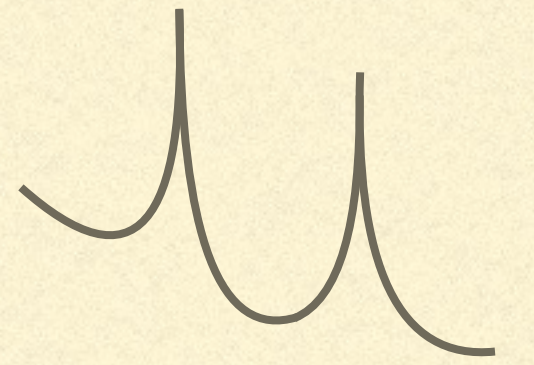
Equilibrium



Equilibrium

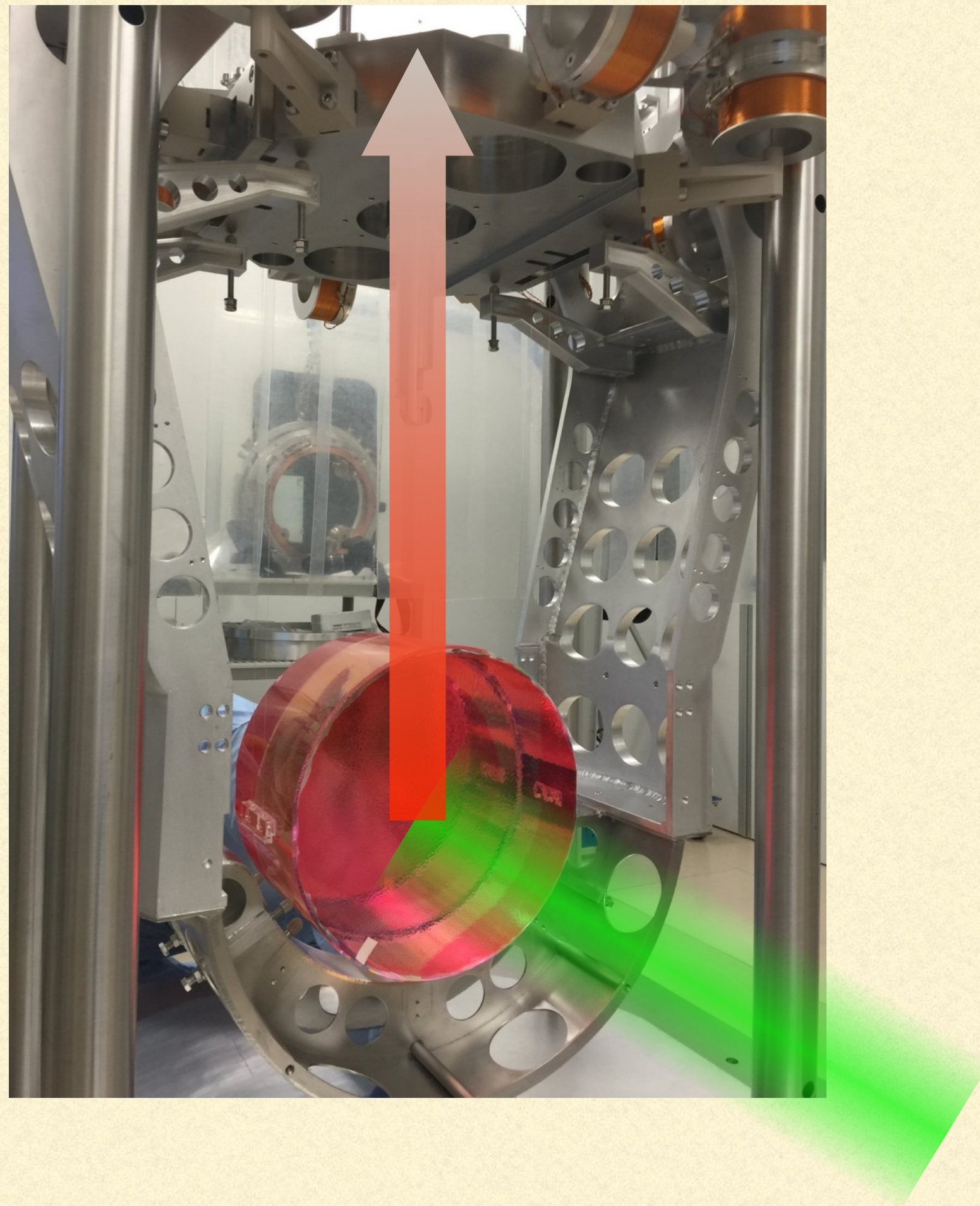
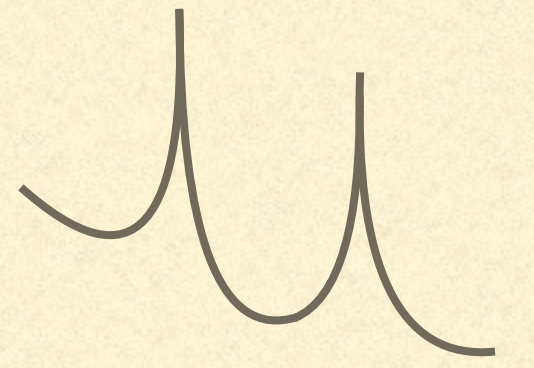


Equilibrium

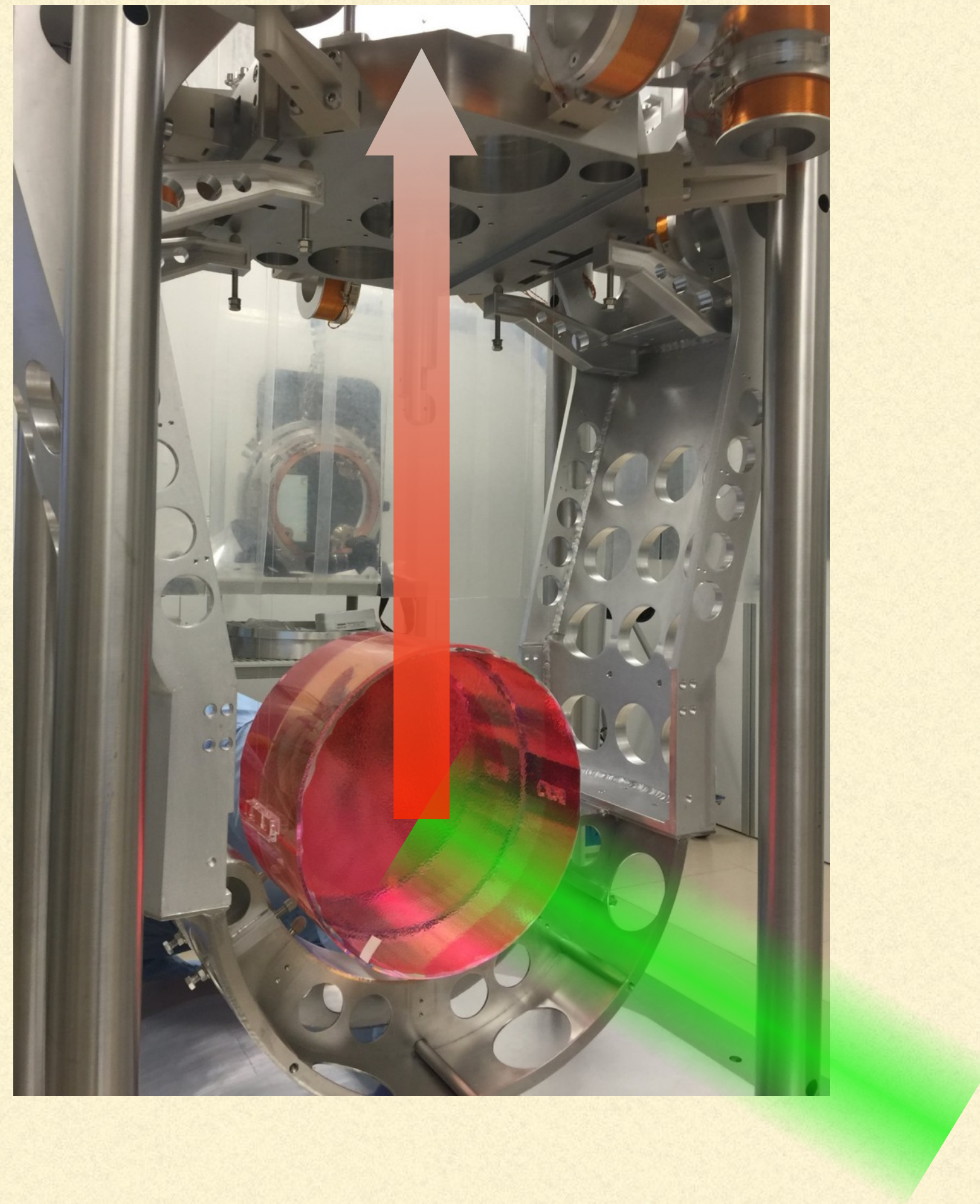
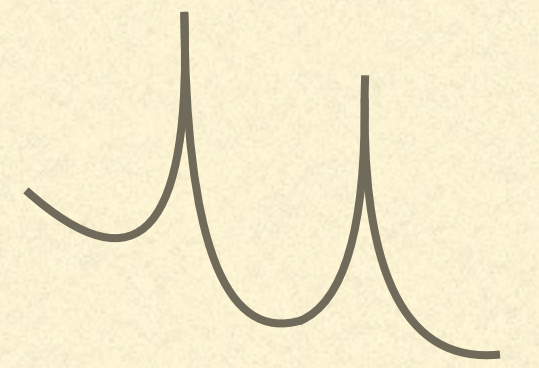


$$T = \frac{k^{defl} \langle \delta^2 \rangle}{k_B} \approx 300 K$$

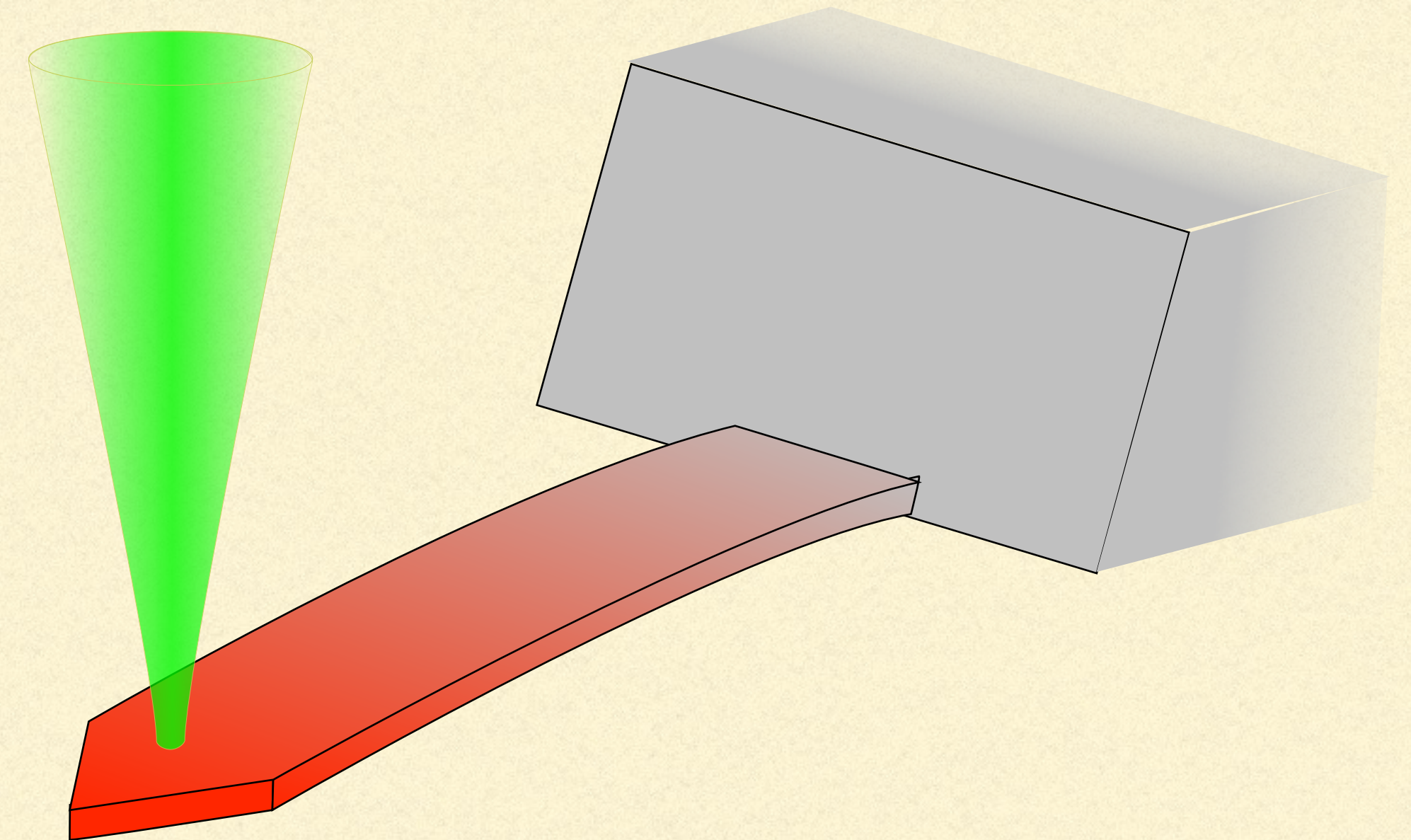
Out of equilibrium?



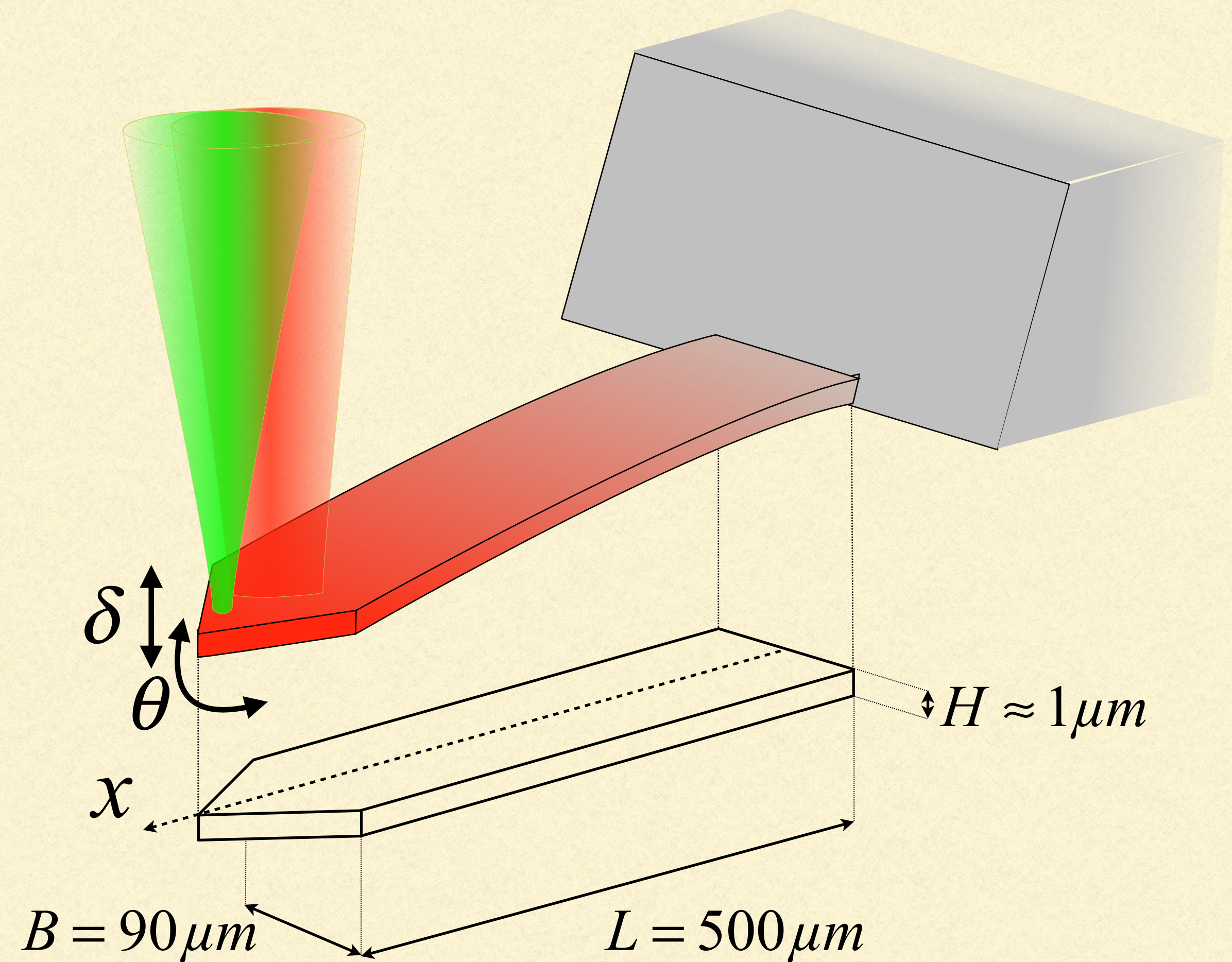
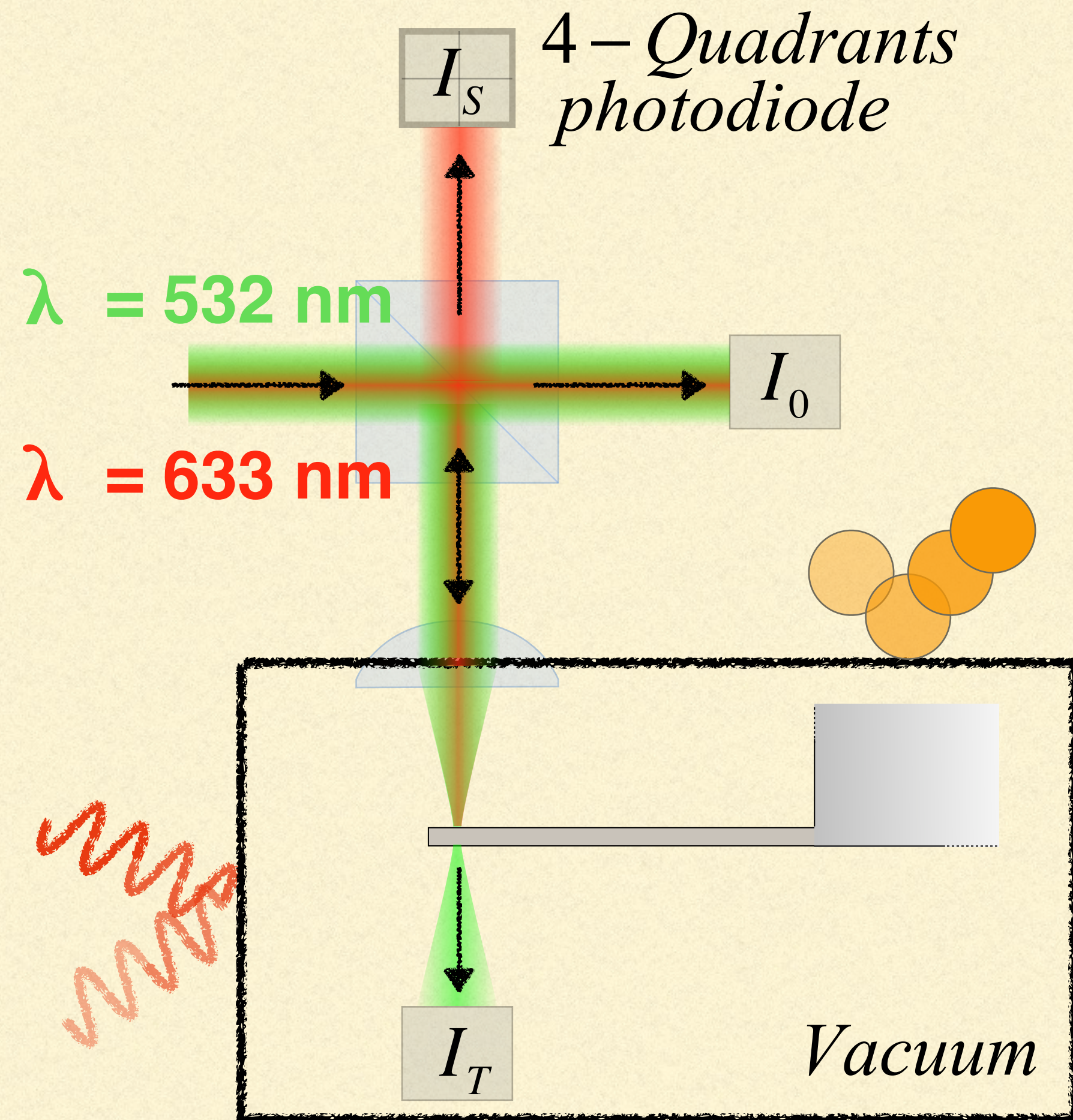
Out of equilibrium Lyon



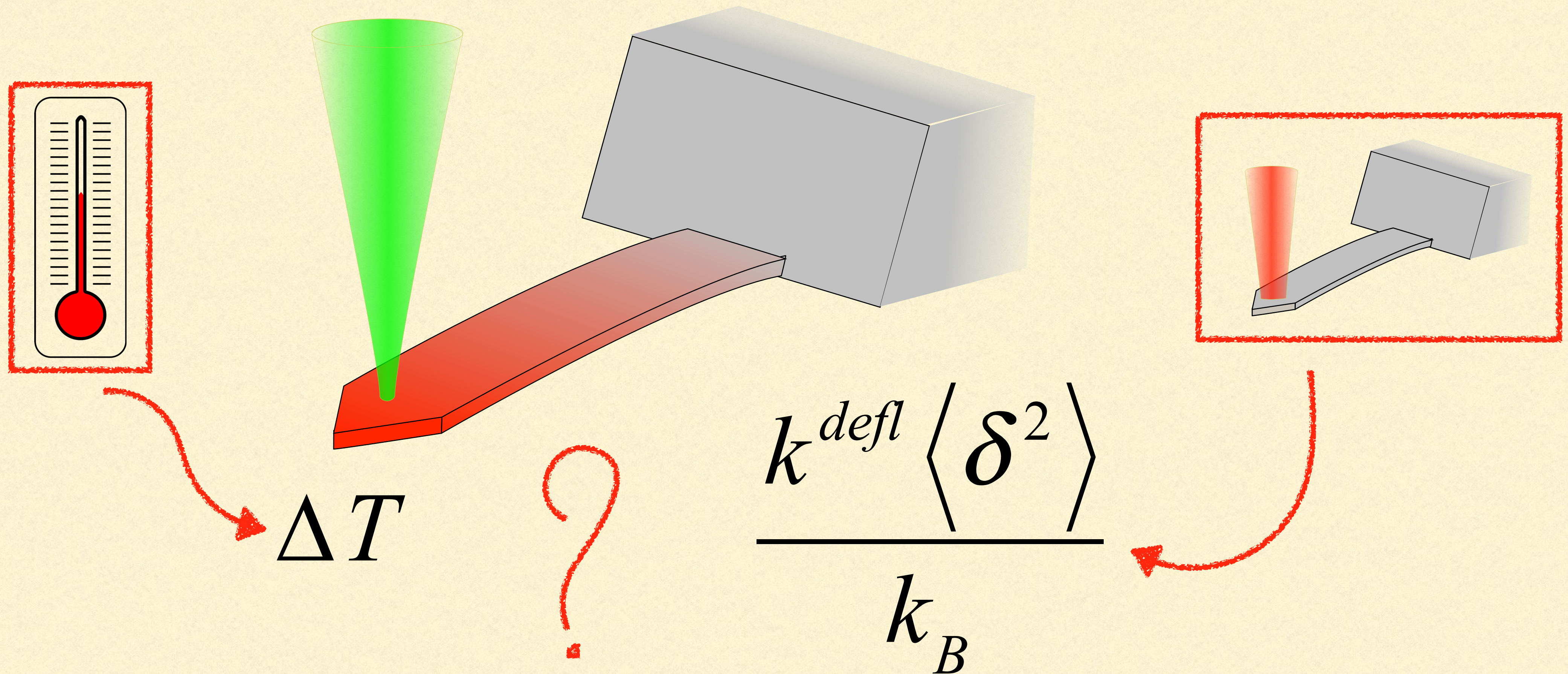
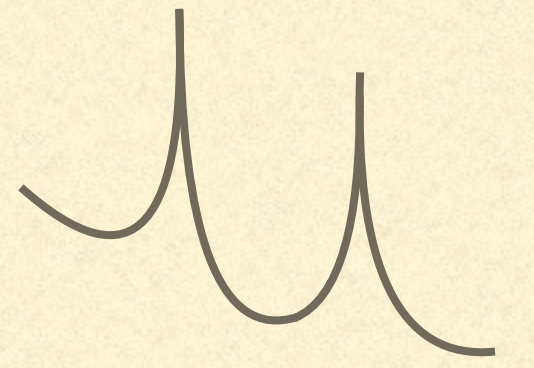
TEST BENCH



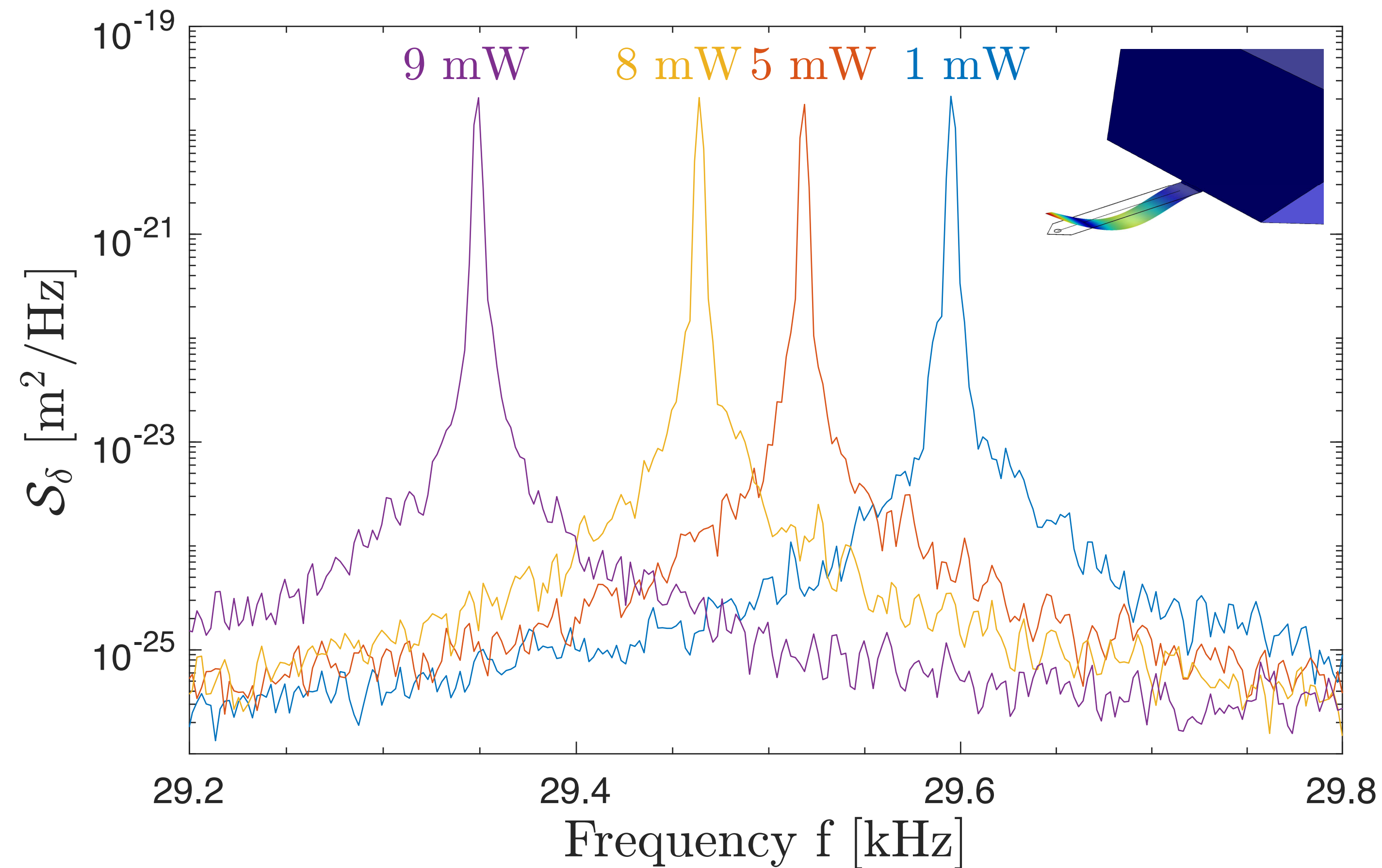
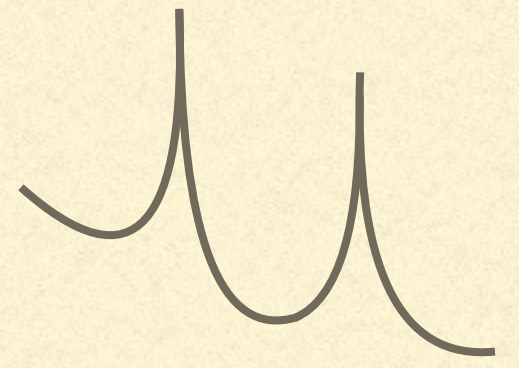
Our experiment



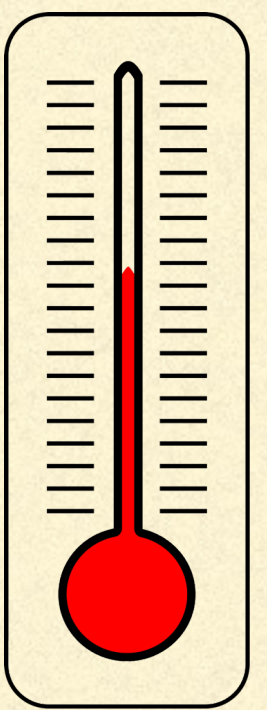
Two ingredients



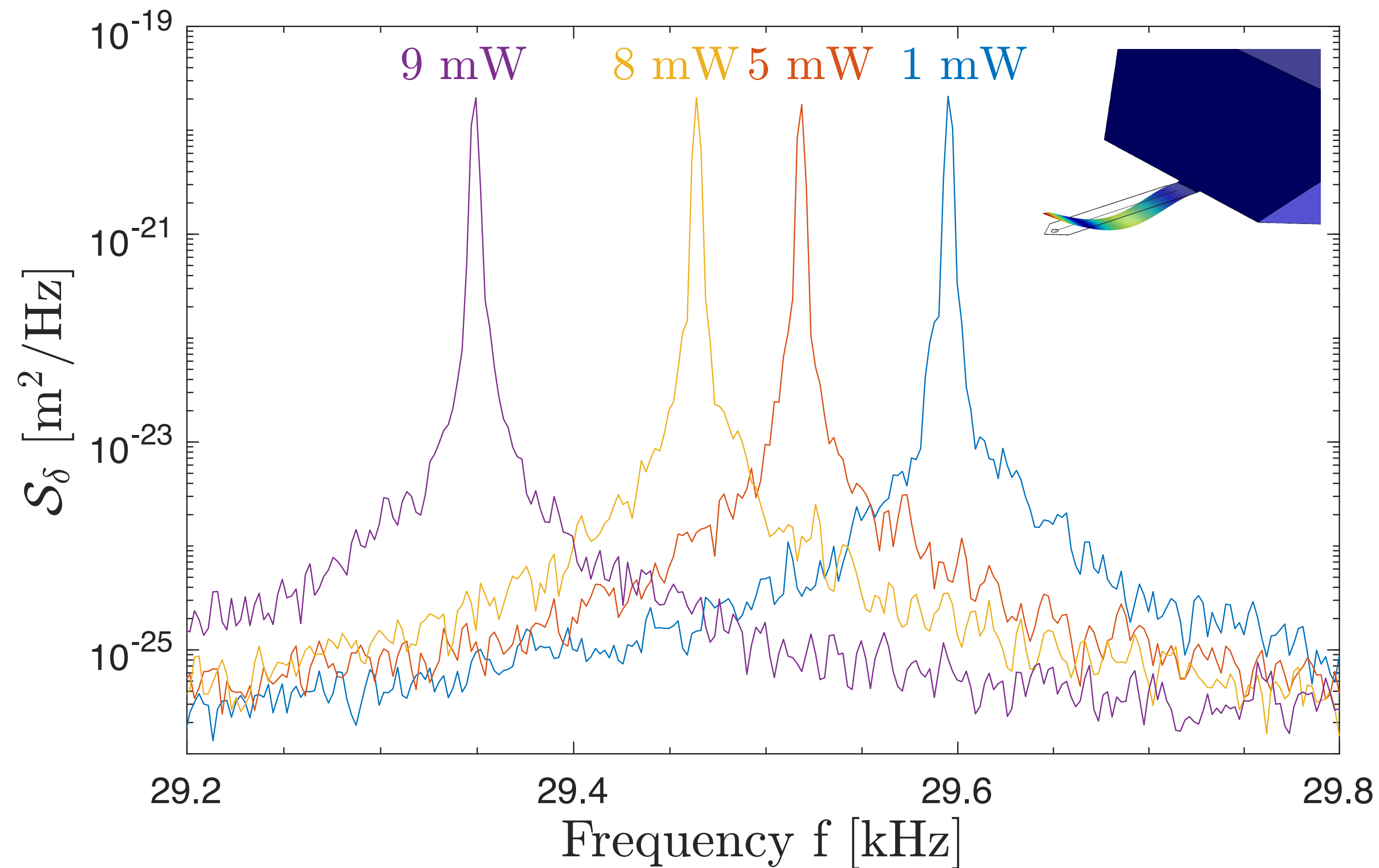
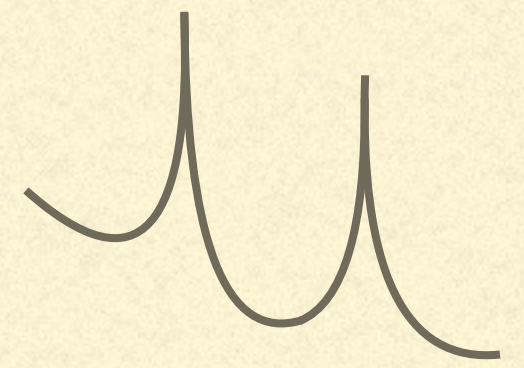
Temperature measurement



$$\omega_0 = \sqrt{\frac{k}{m}} \quad \& \quad k \propto T$$



Temperature measurement

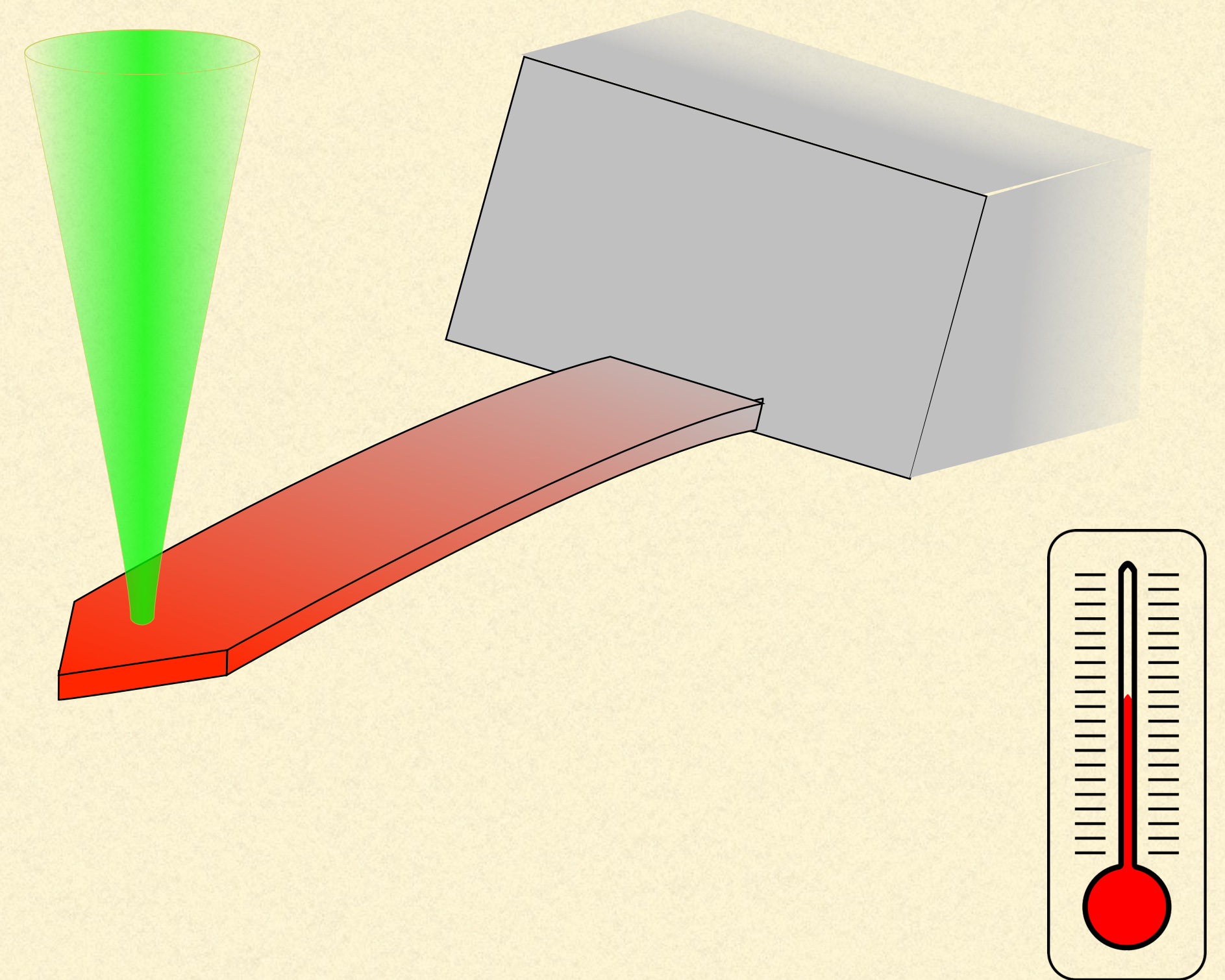
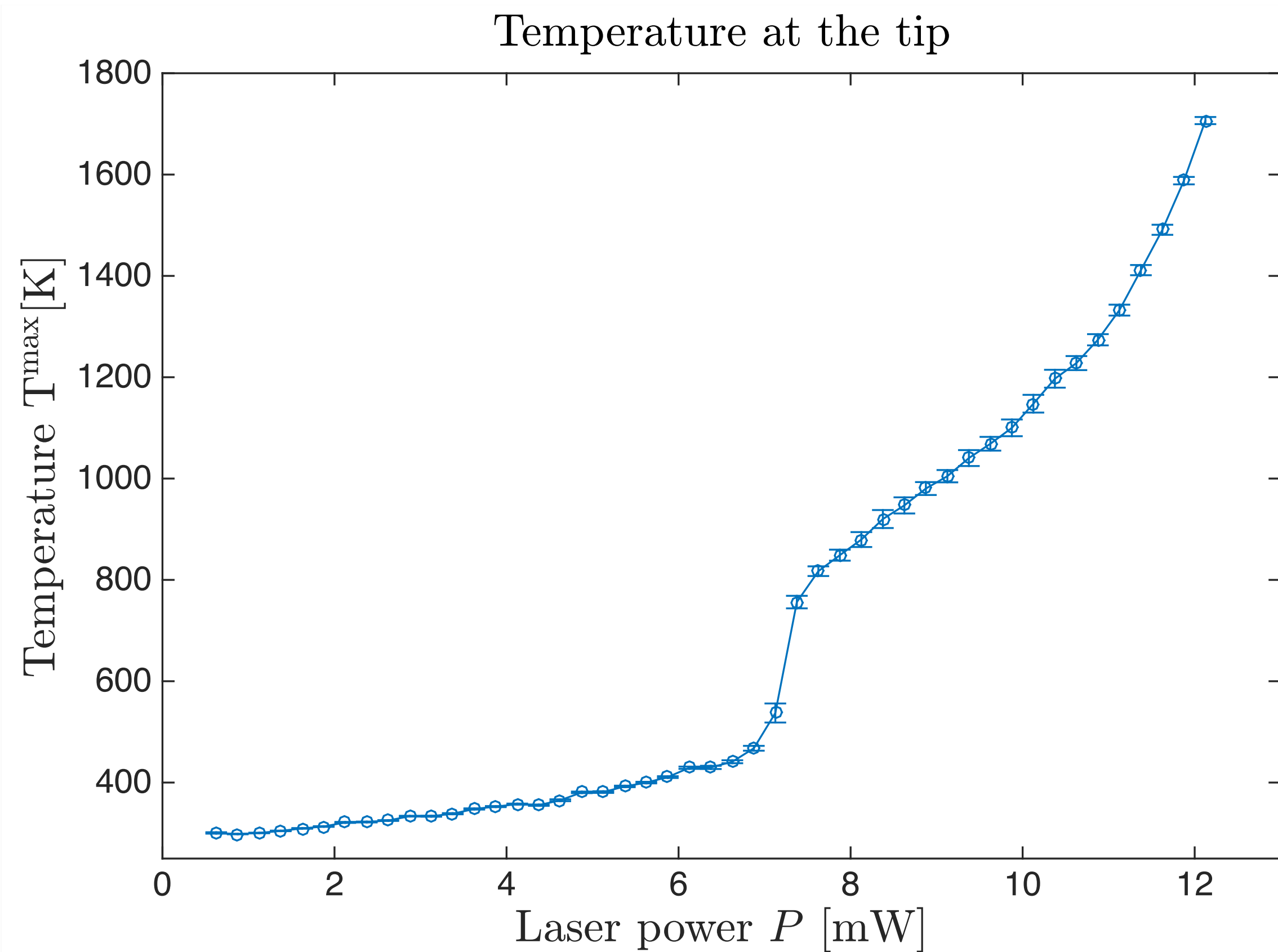
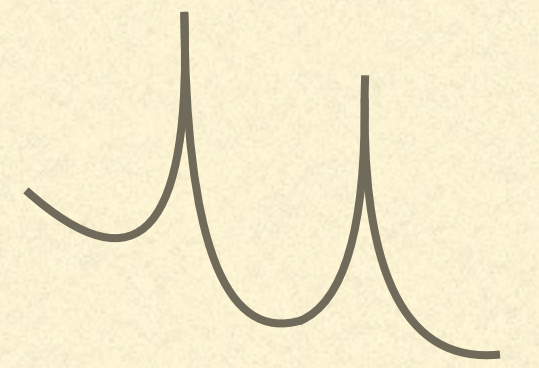


$$\omega_0 = \sqrt{\frac{k}{m}} \quad \& \quad k \propto T$$

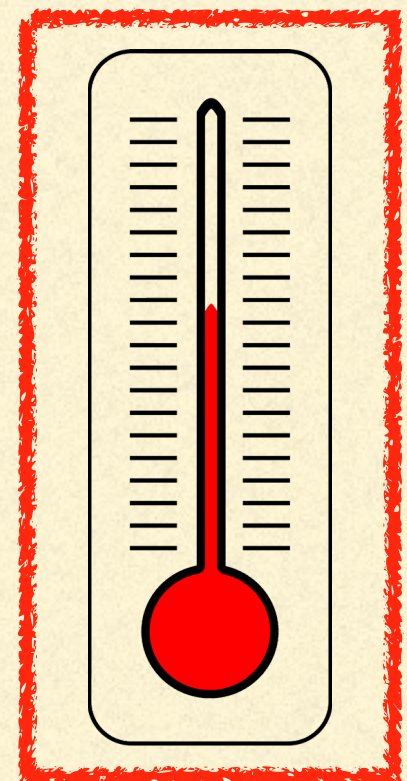
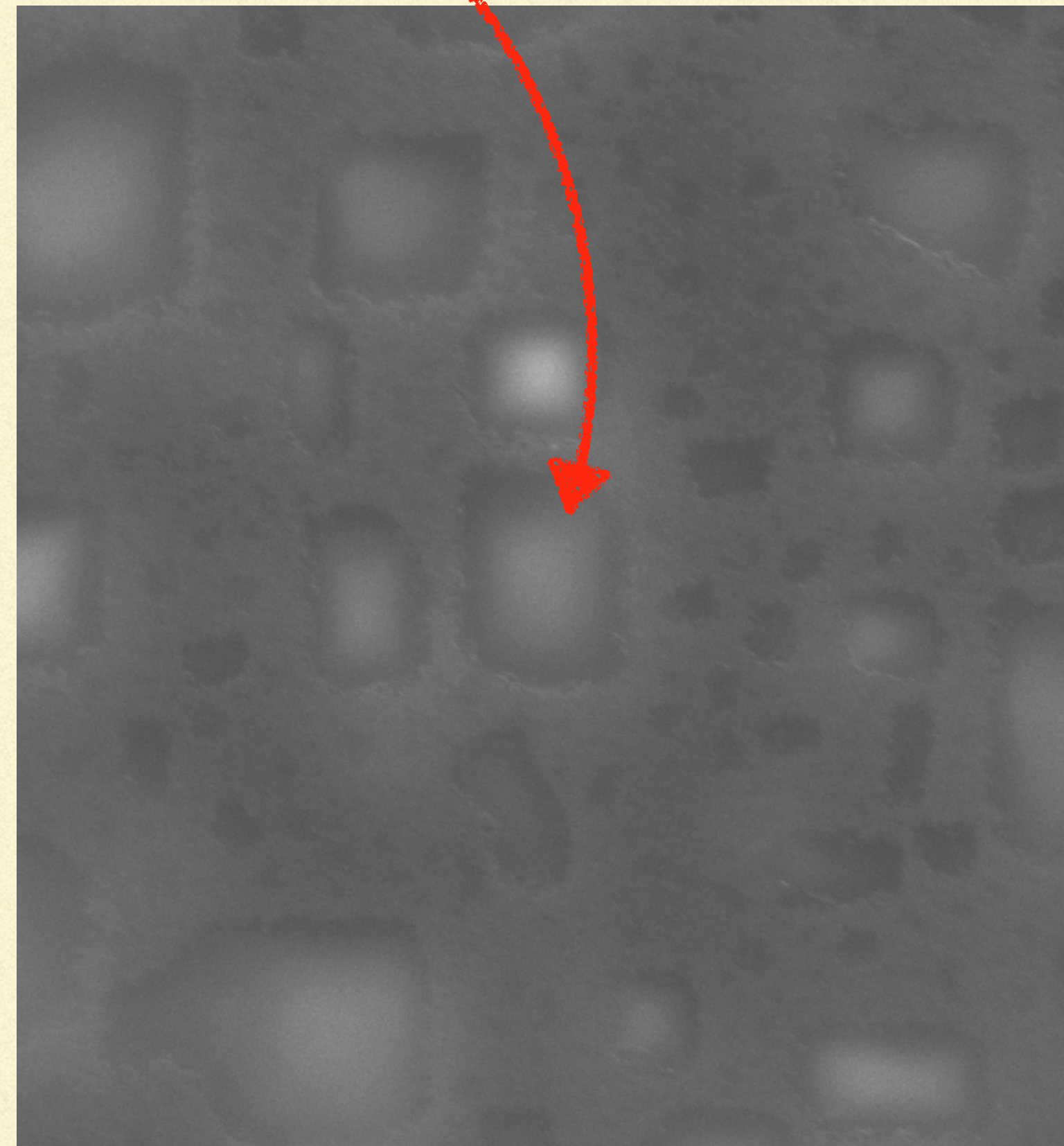
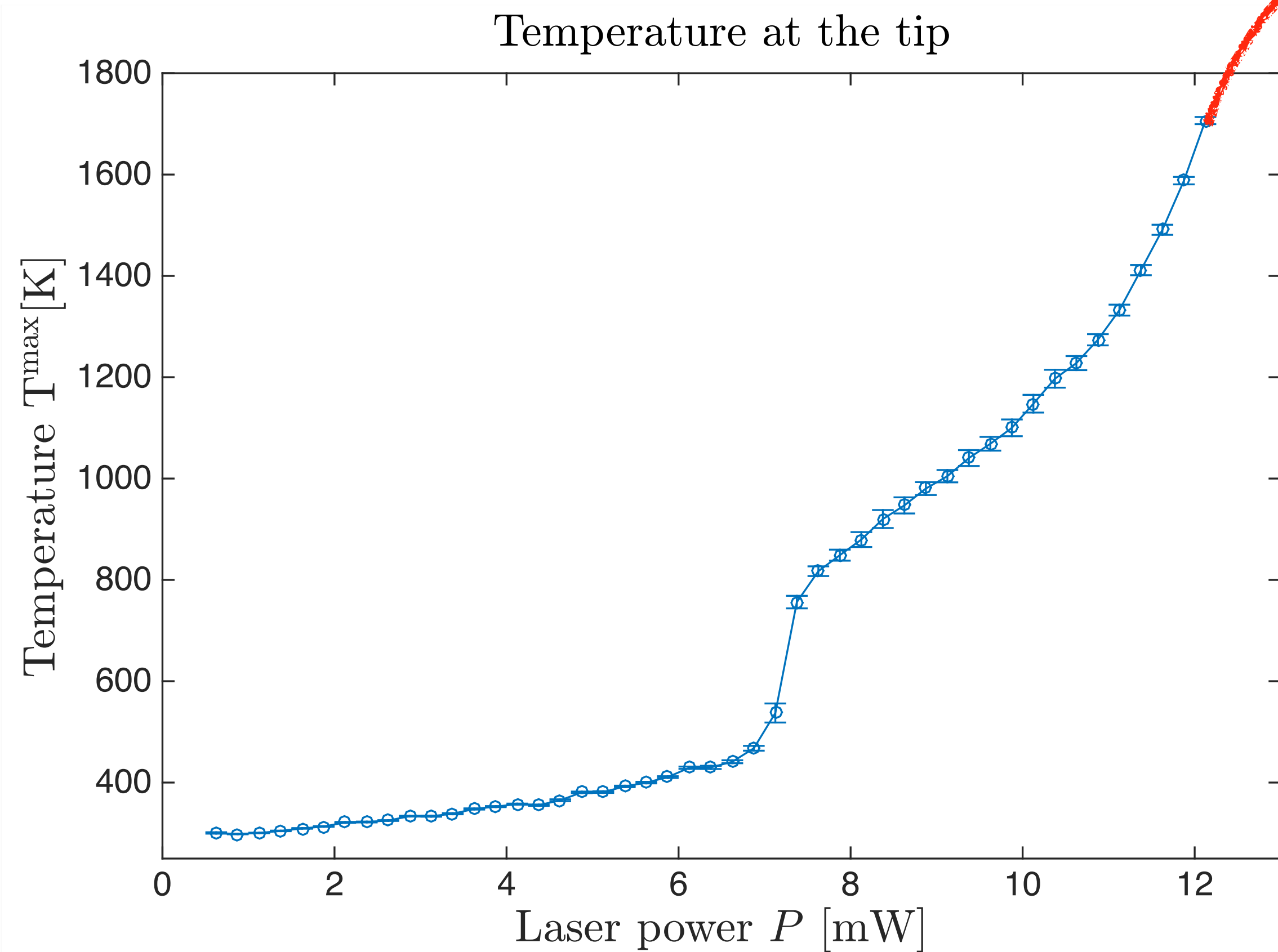
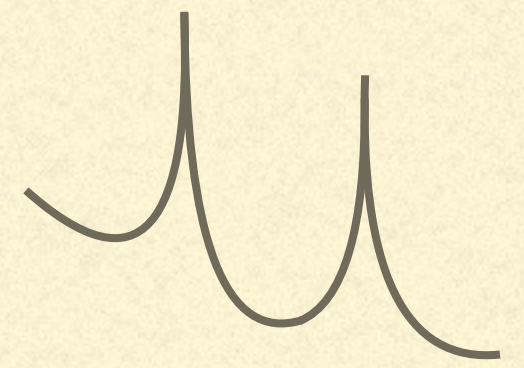
$$\frac{\Delta\omega_n}{\omega_0} \propto \Delta T_n$$

$$\Delta T_n \left(\frac{\Delta\omega_n}{\omega_0} \right)$$

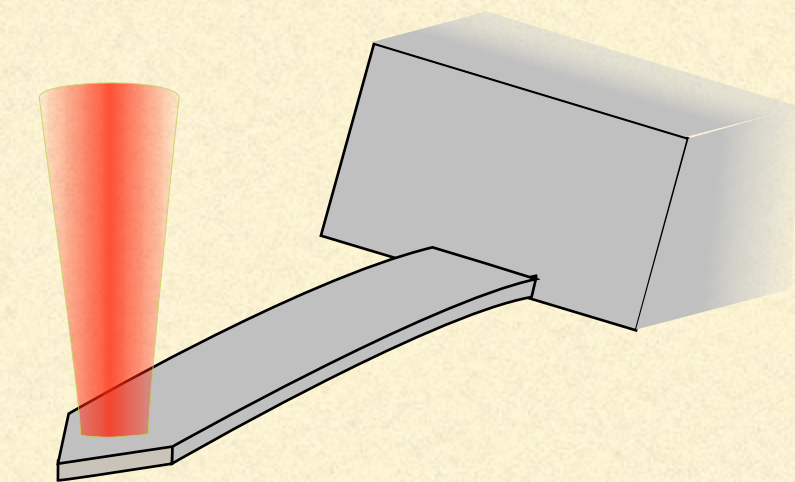
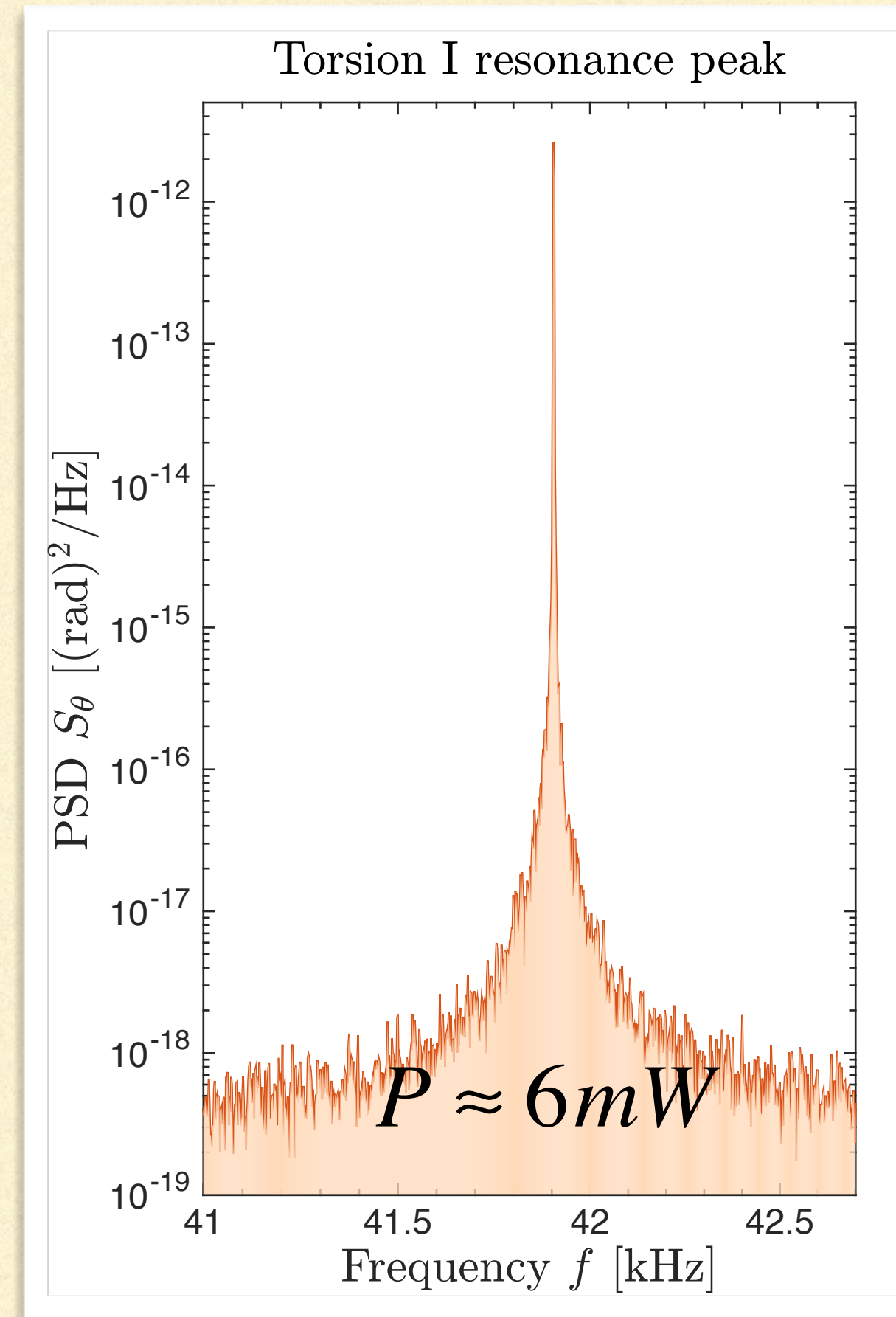
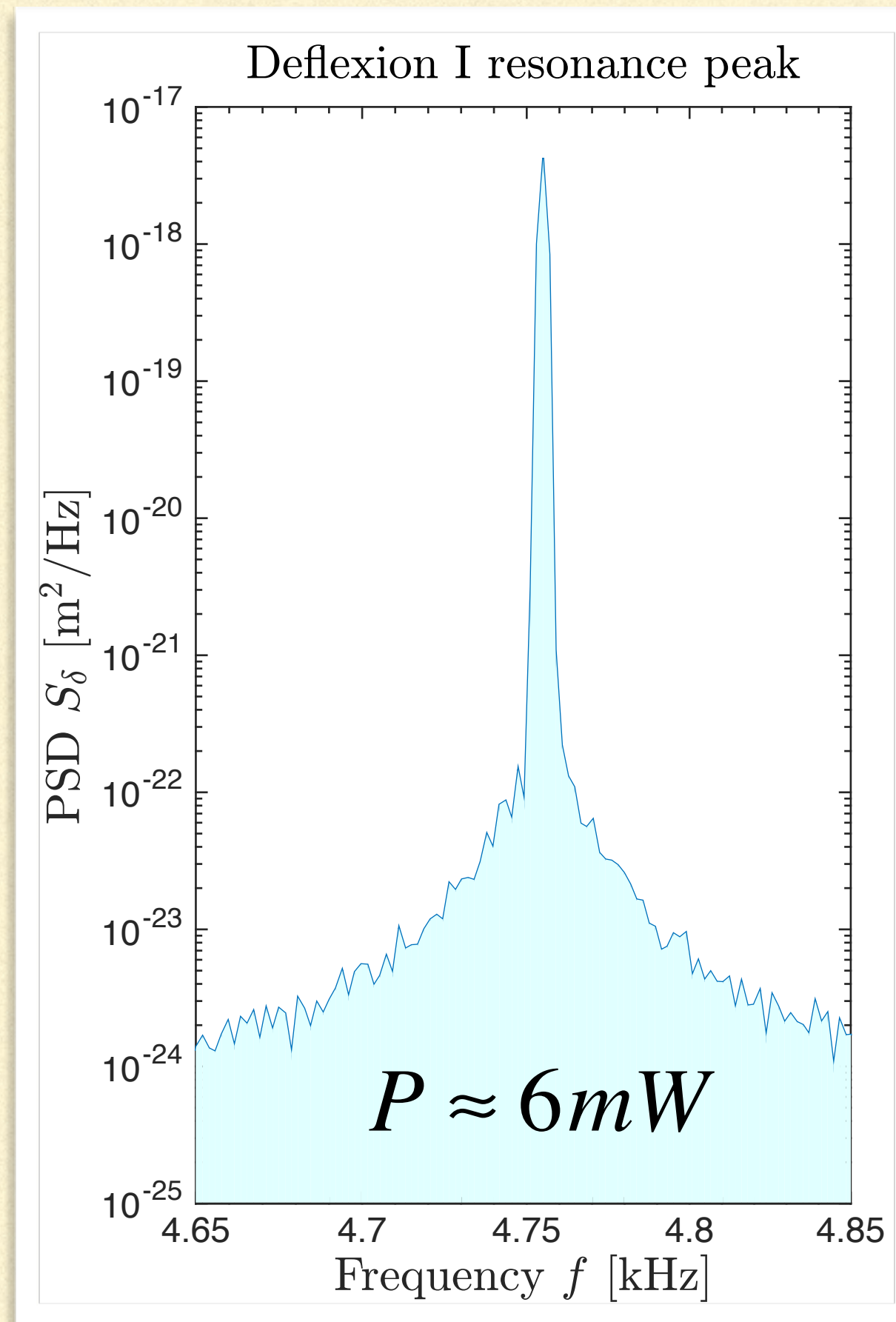
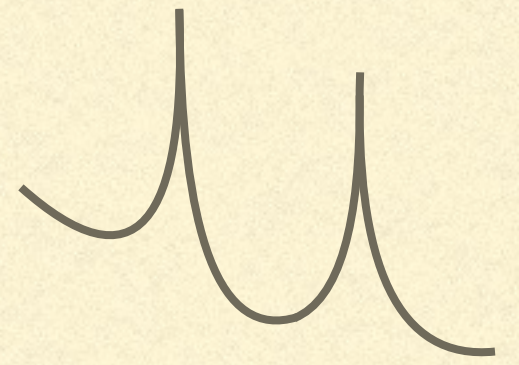
Results: $T^{\max}$



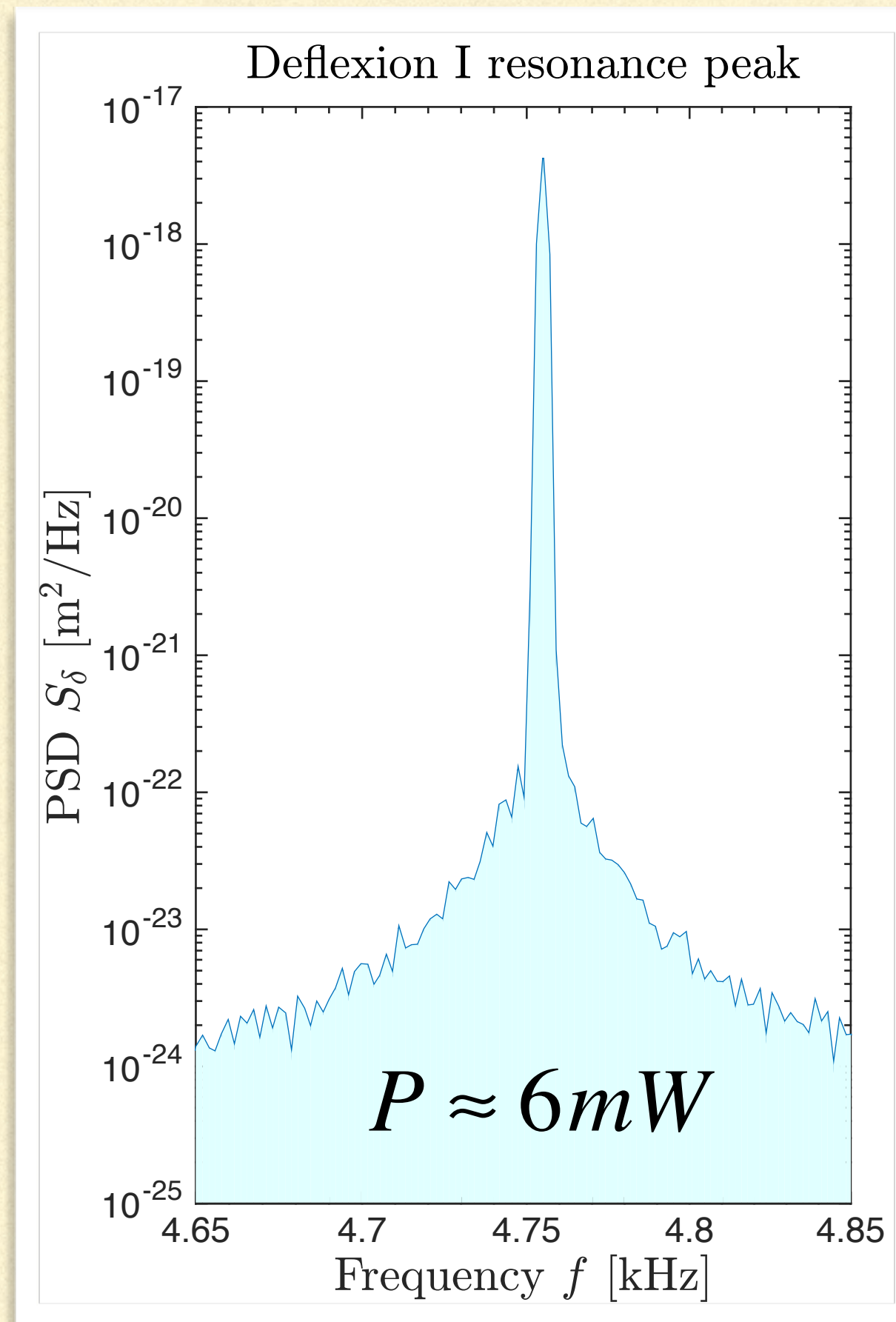
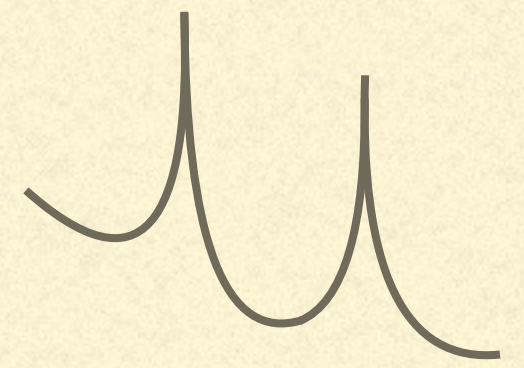
Results: fusion



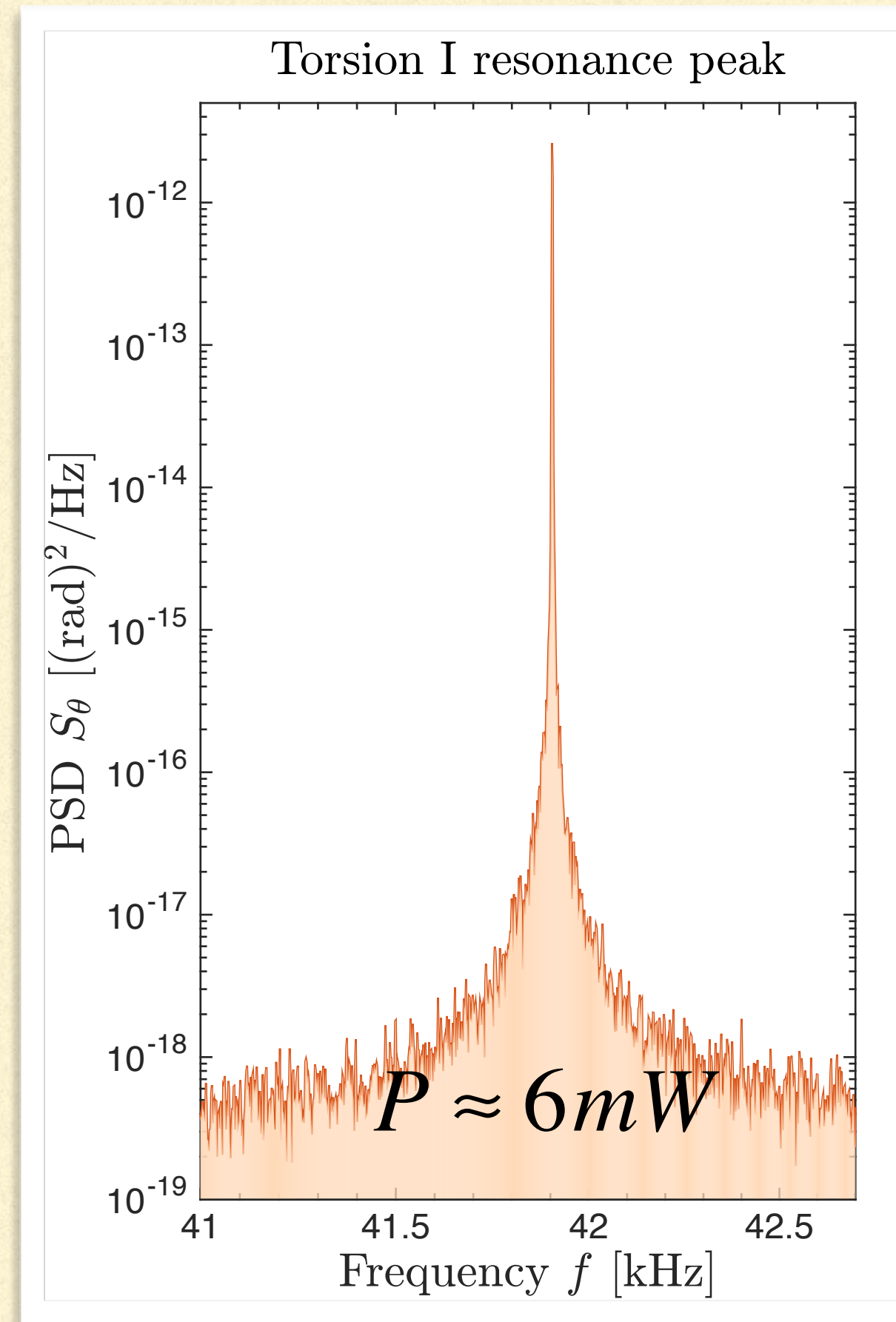
Fluctuation temperature



Fluctuation temperature: T^{eff}



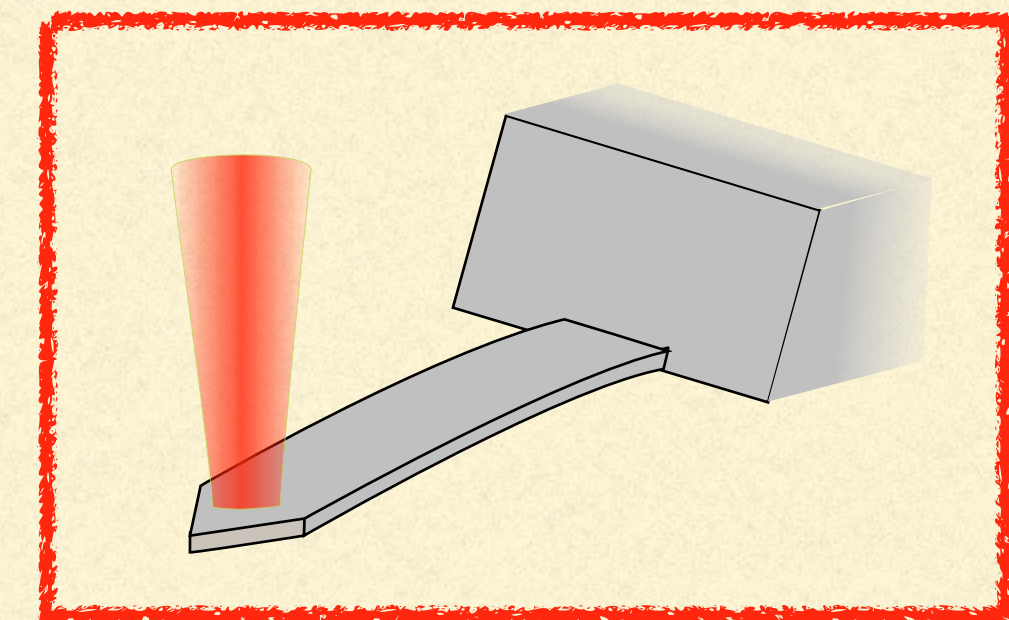
$$\langle \delta_n^2 \rangle = \int_{f_n \pm \Delta f} df \cdot S_\delta(f)$$



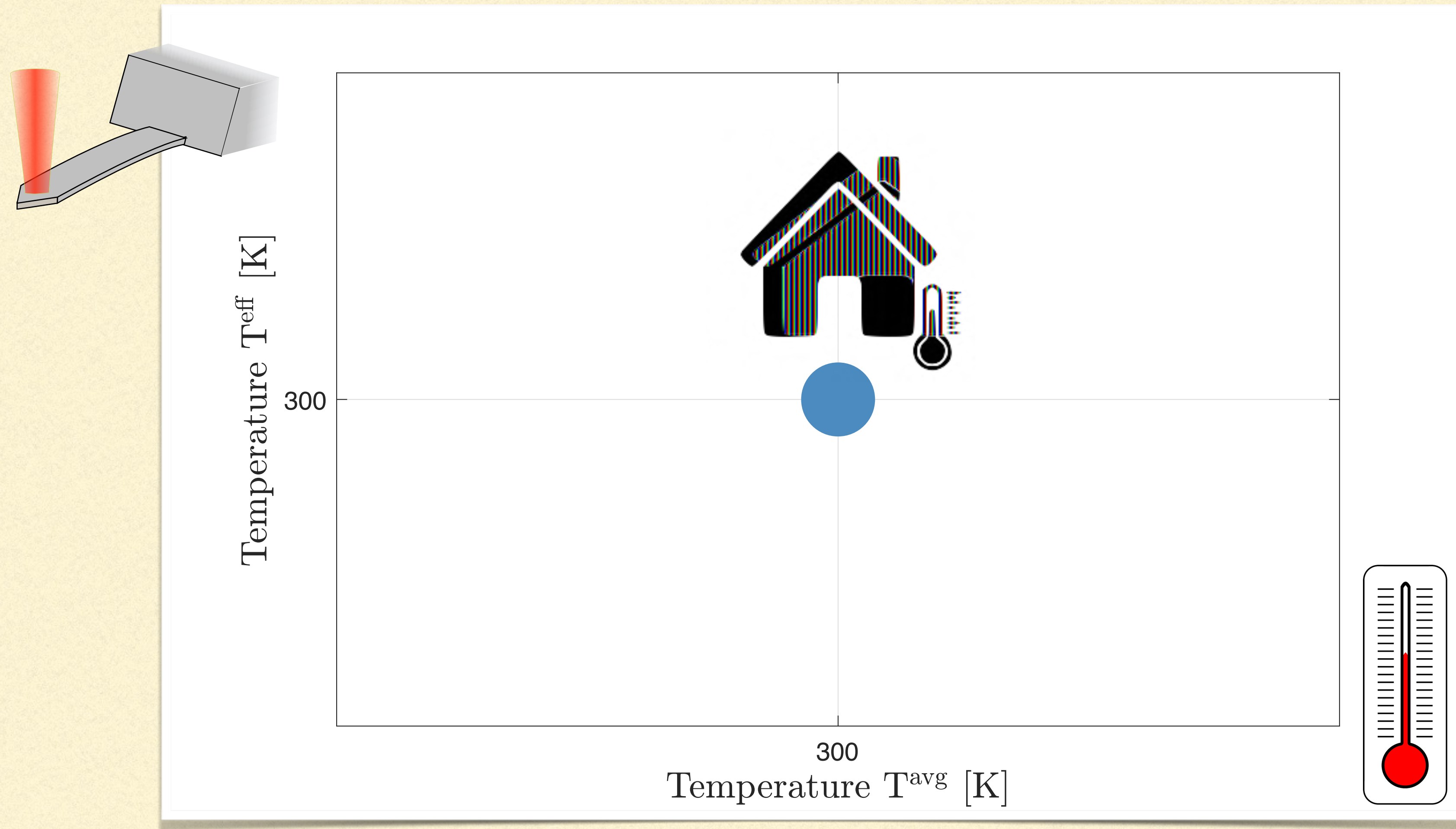
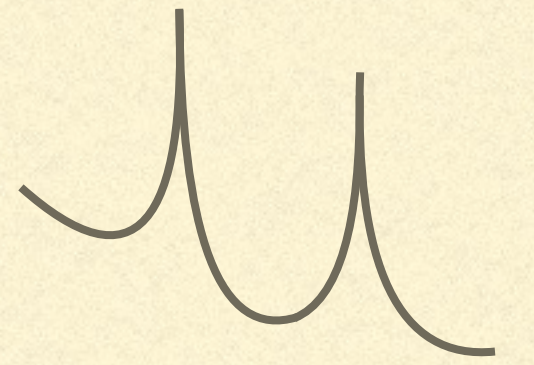
$$\langle \theta_n^2 \rangle = \int_{f_n \pm \Delta f} df \cdot S_\theta(f)$$

$$T_n^{\text{eff}} = \frac{k_n^{\text{defl}} \langle \delta_n^2 \rangle}{k_B}$$

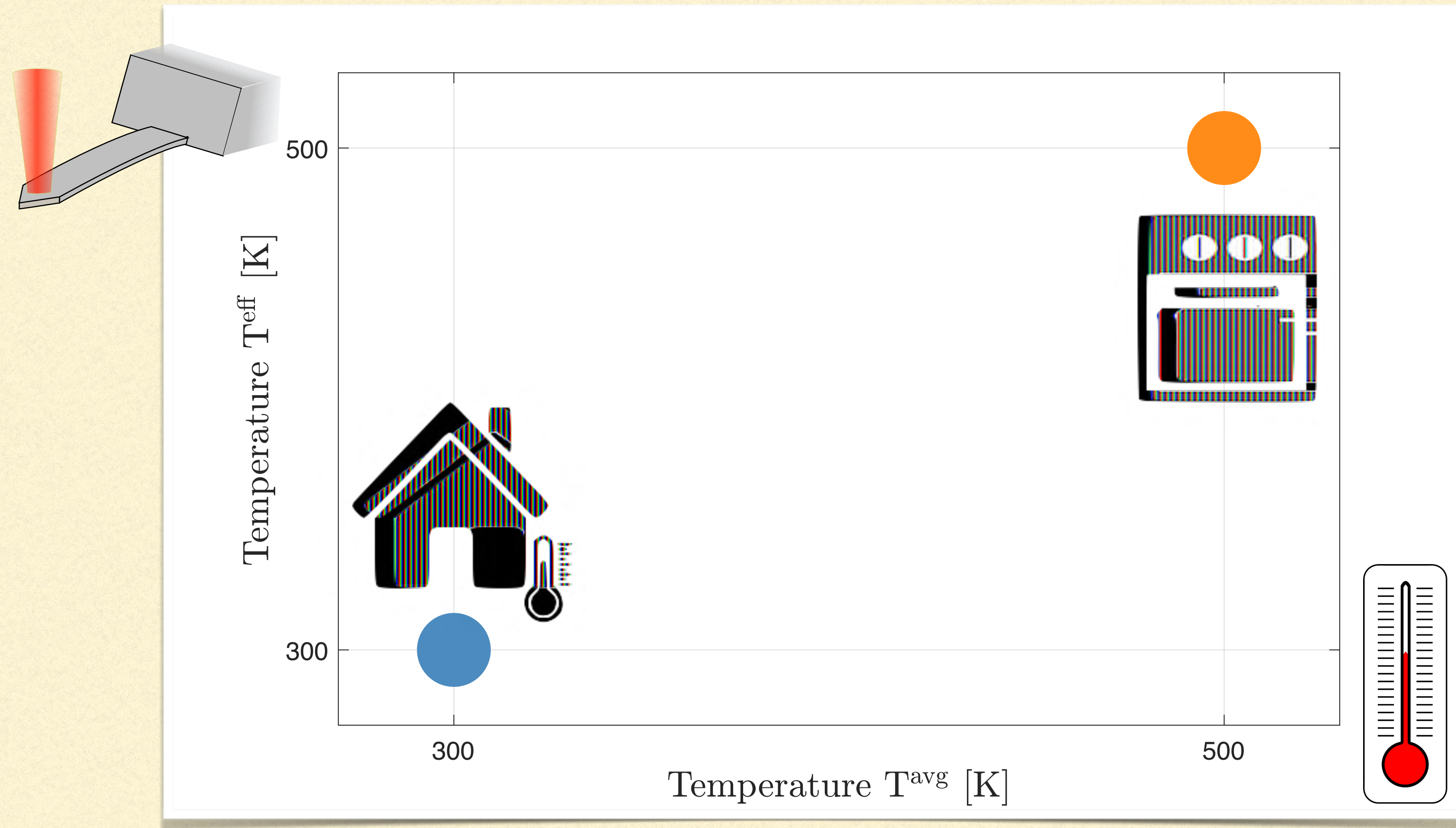
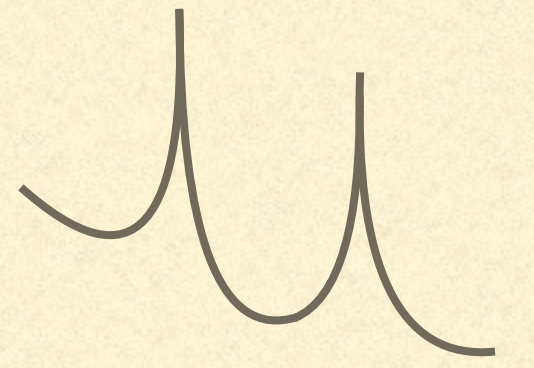
$$T_n^{\text{eff}} = \frac{k_n^{\text{tors}} \langle \theta_n^2 \rangle}{k_B}$$



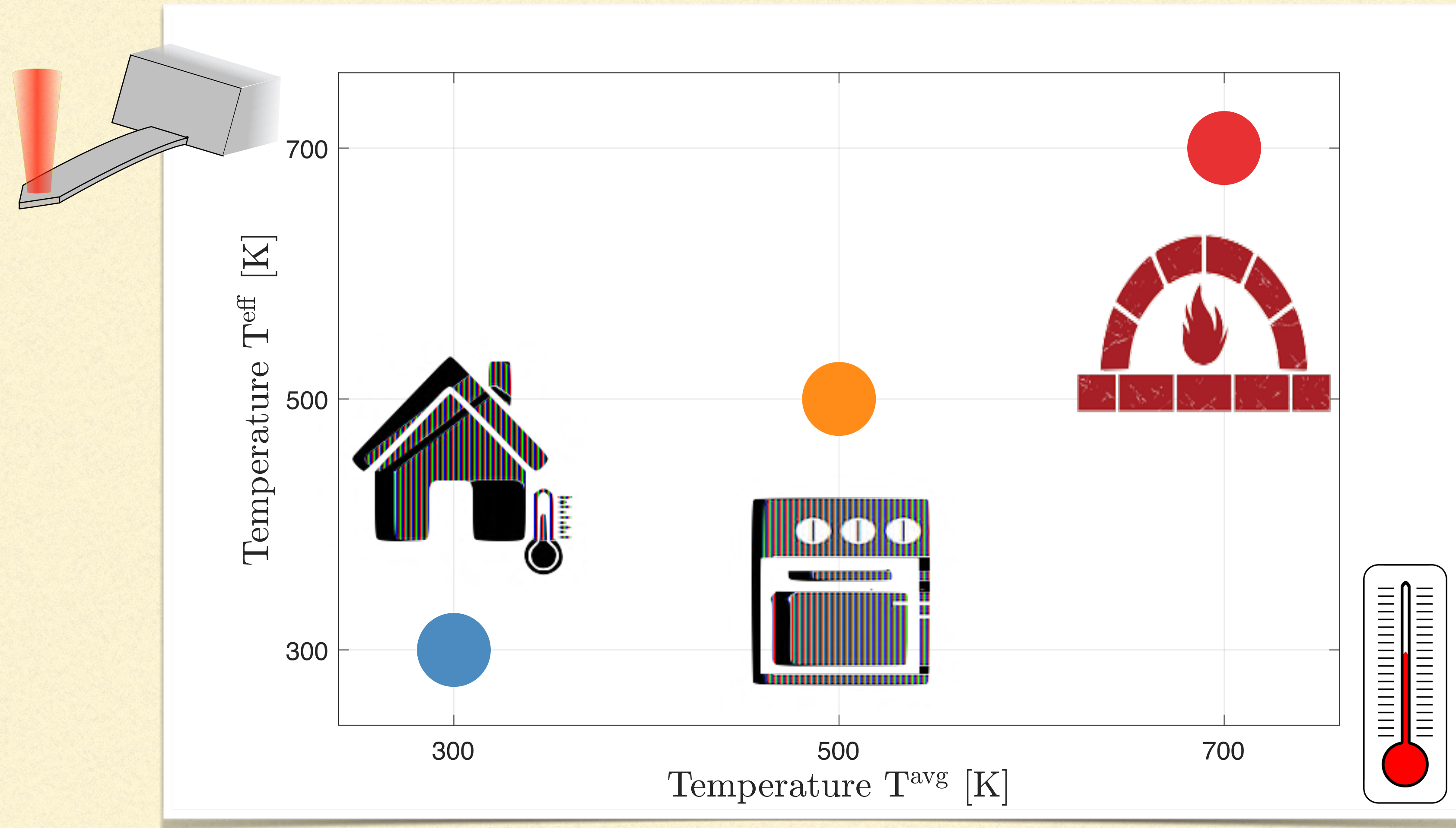
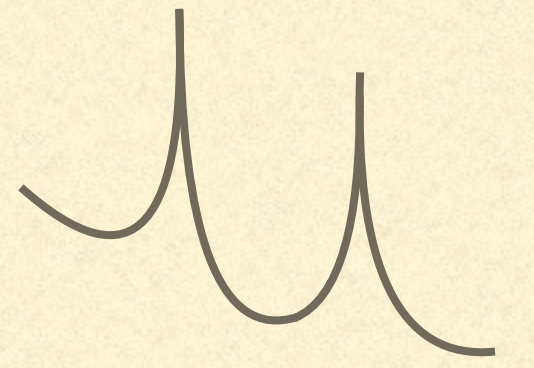
Digression to equilibrium



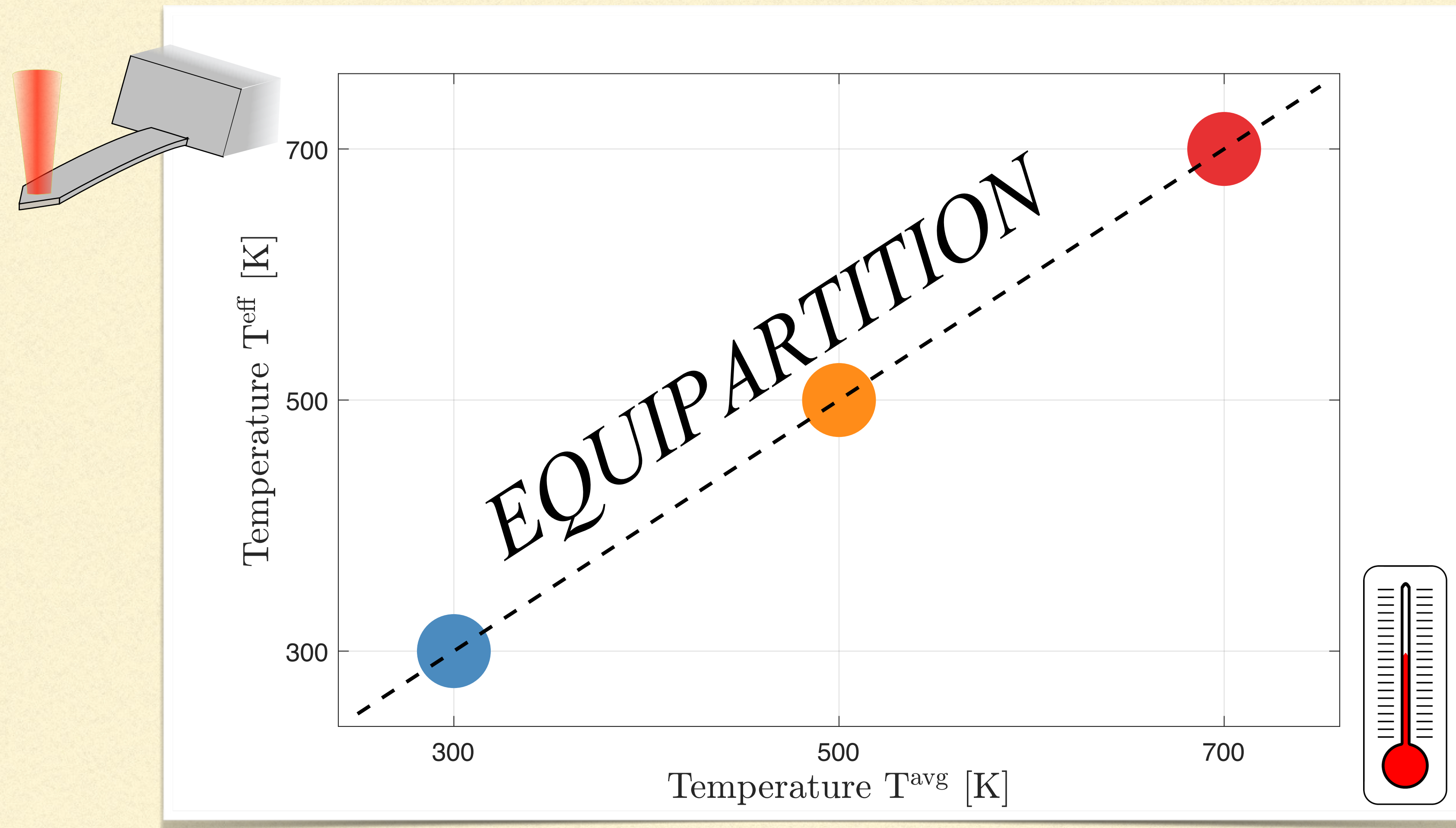
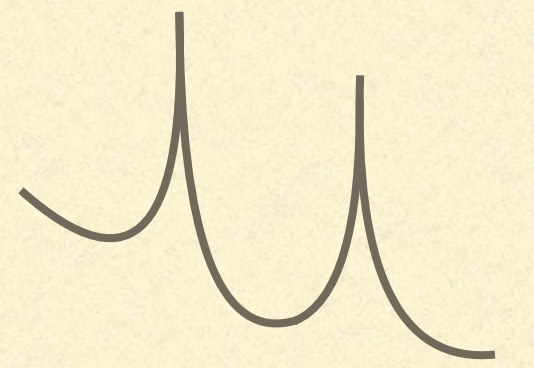
Digression to equilibrium



Digression to equilibrium

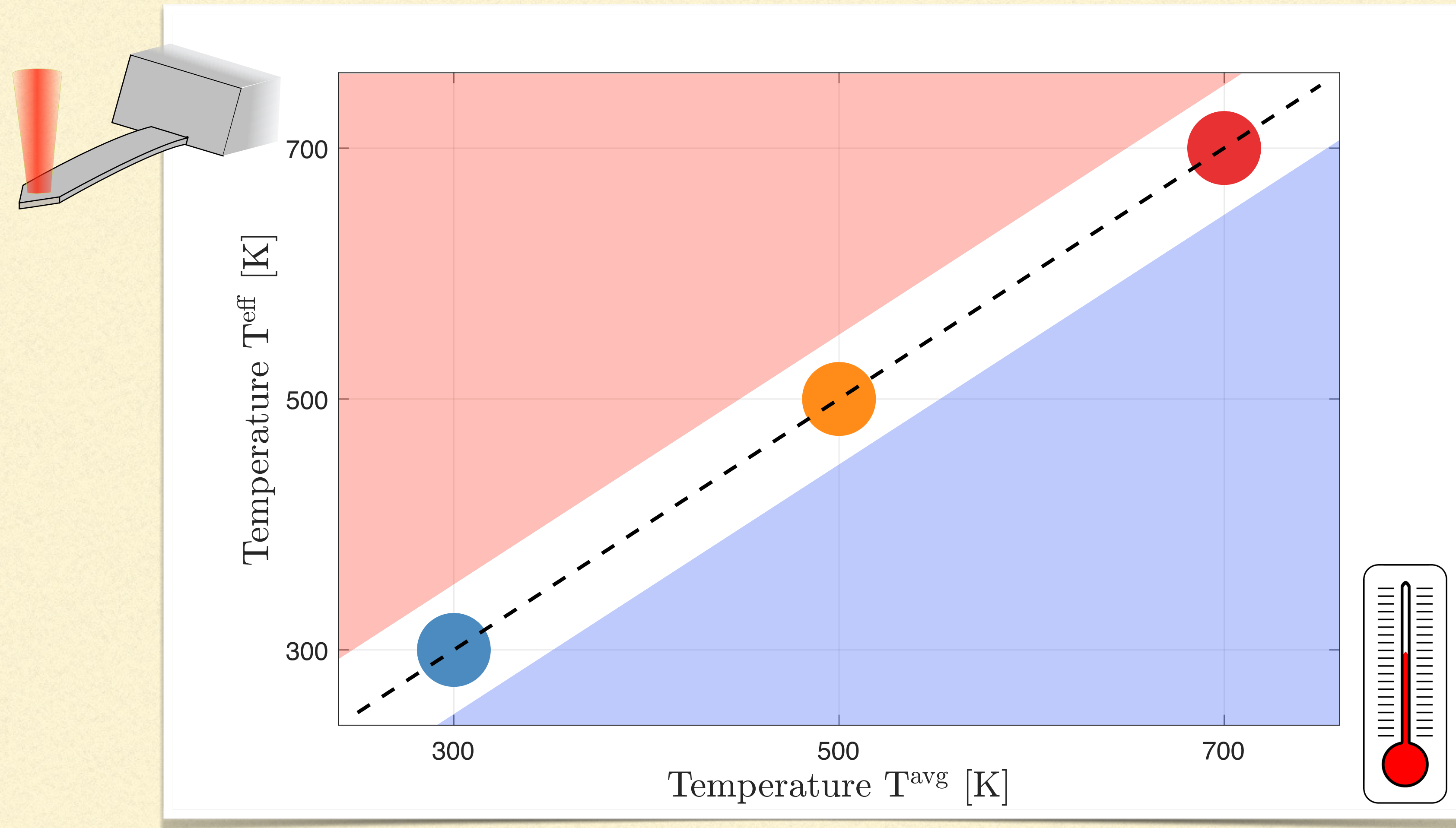
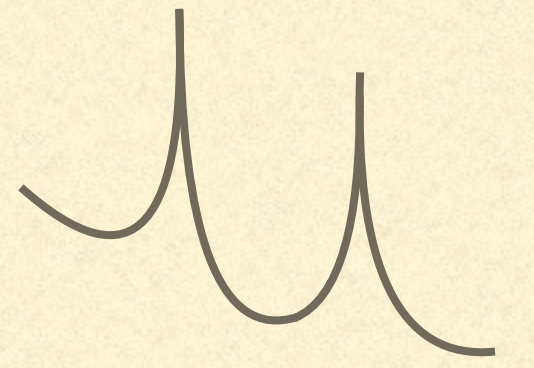


Digression to equilibrium



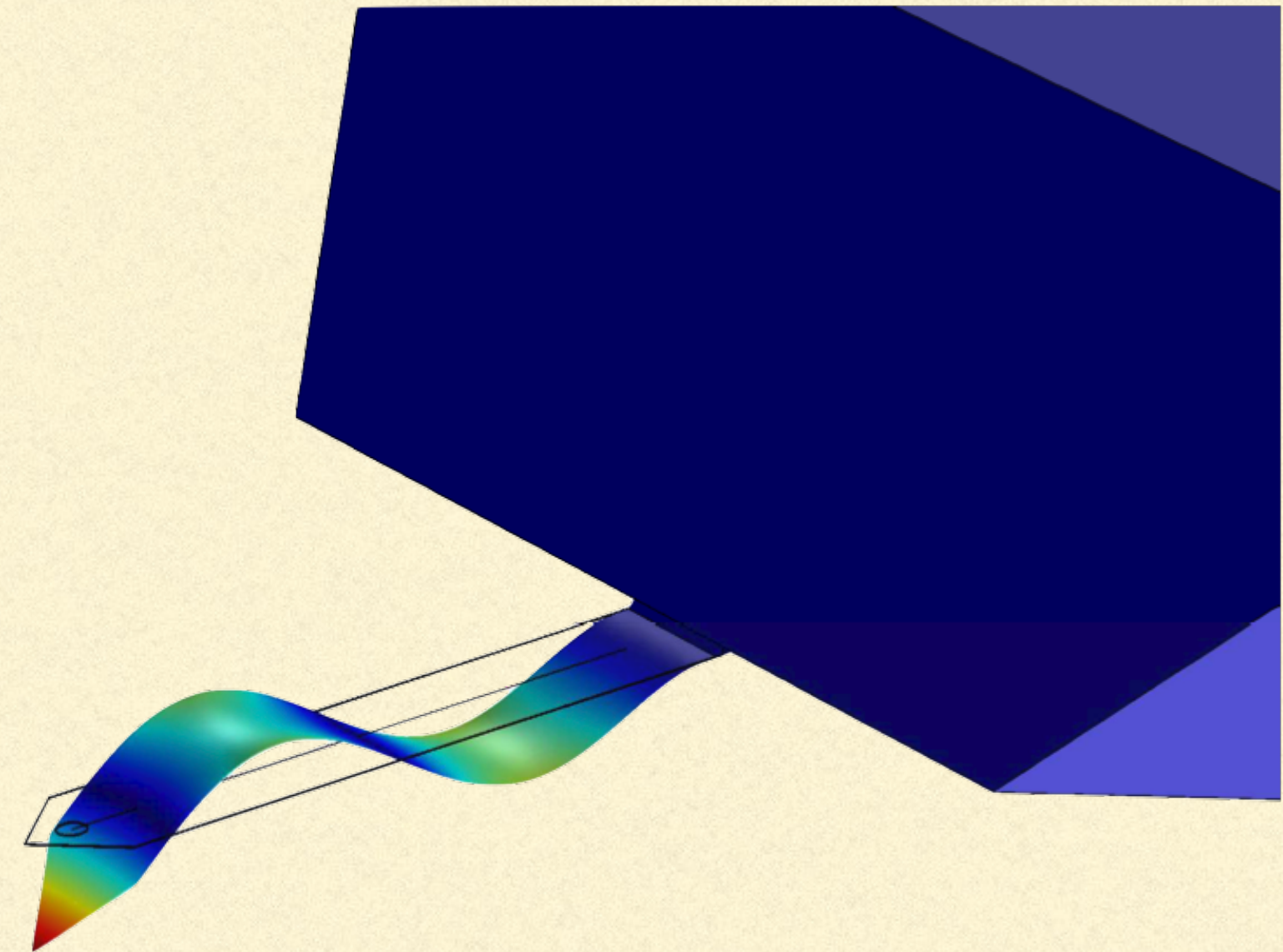
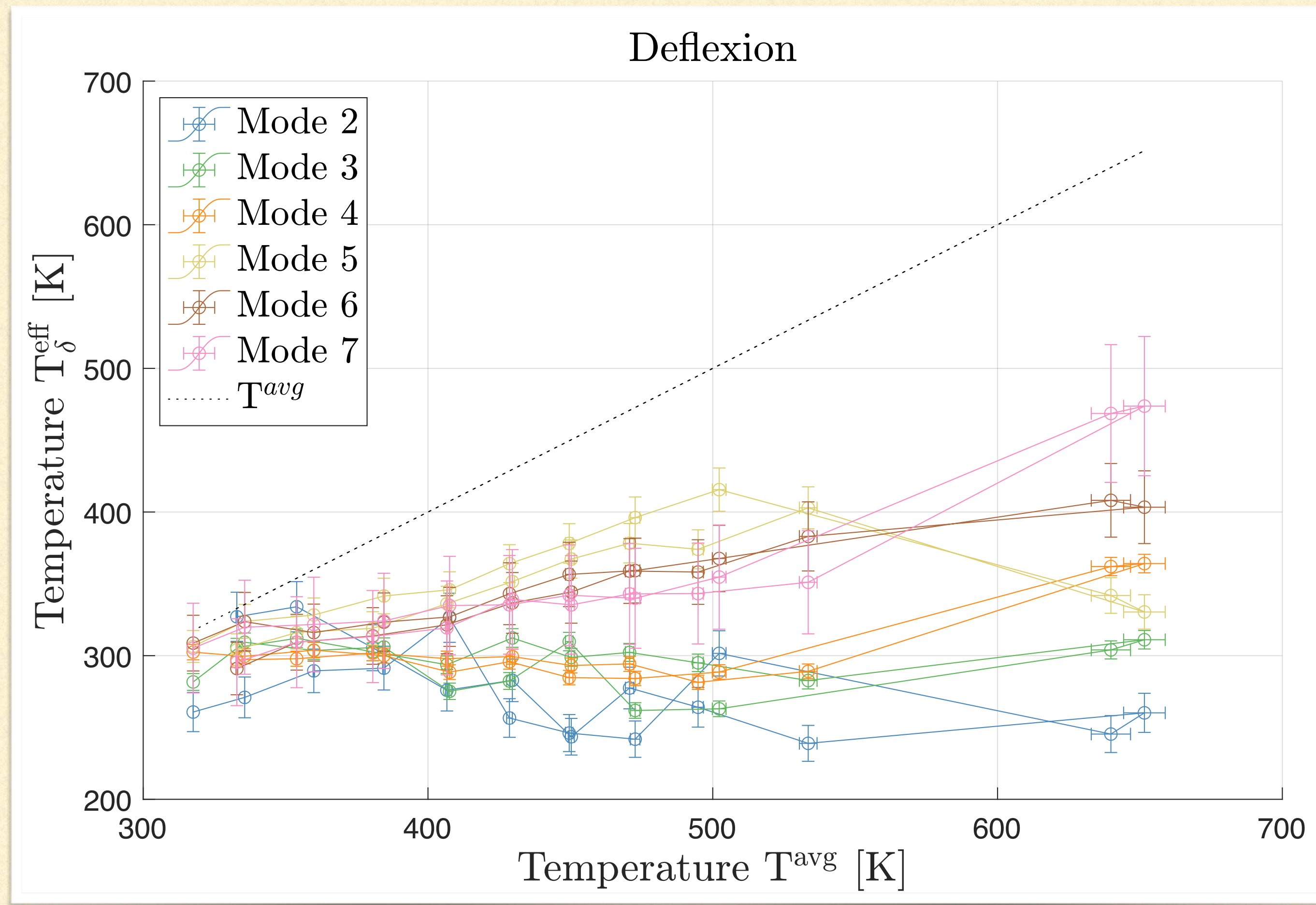
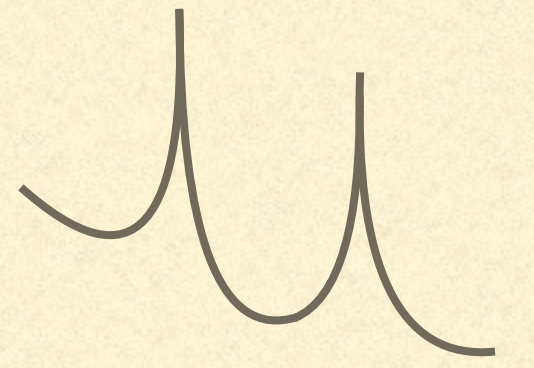
EQ

Digression to equilibrium

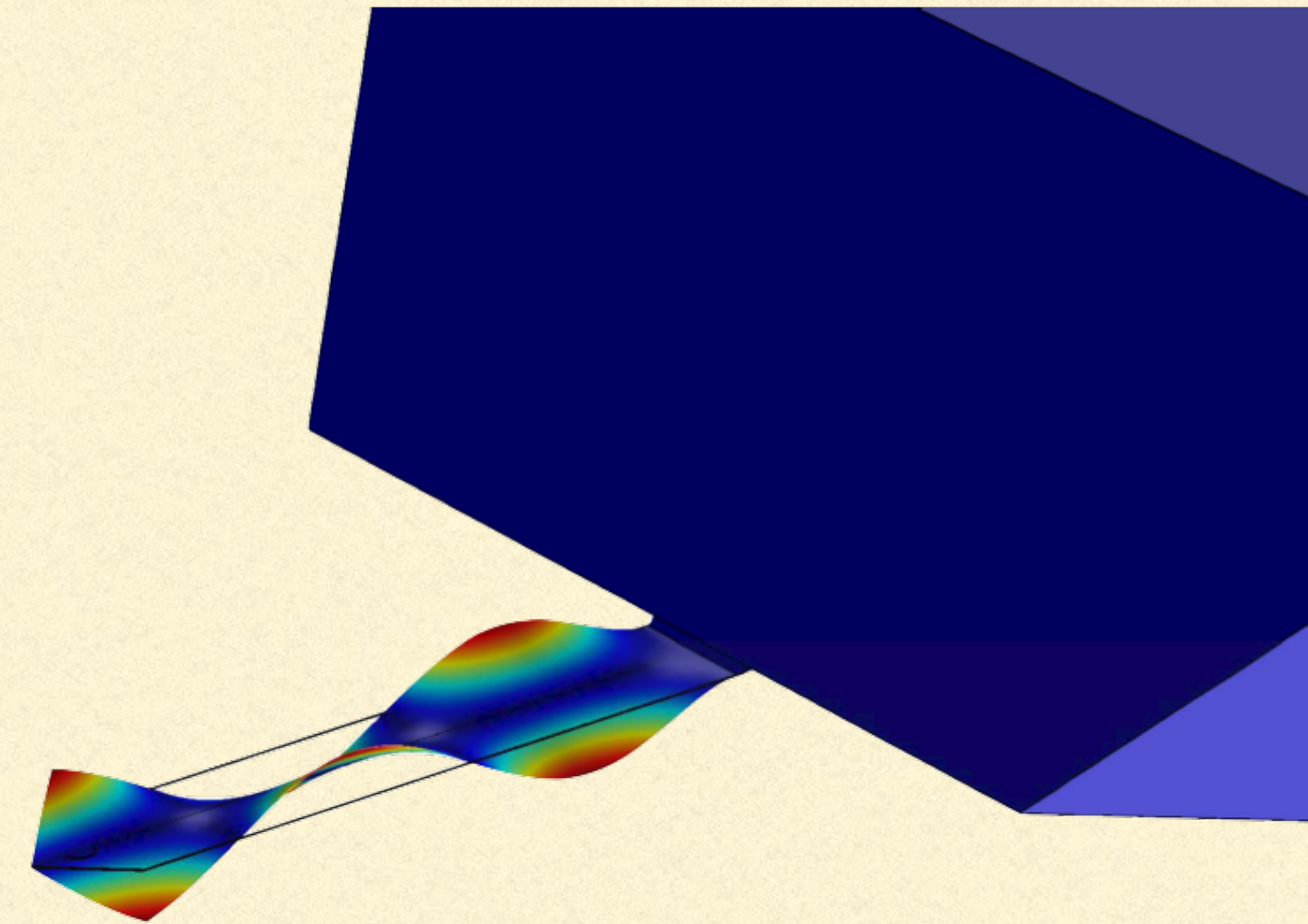
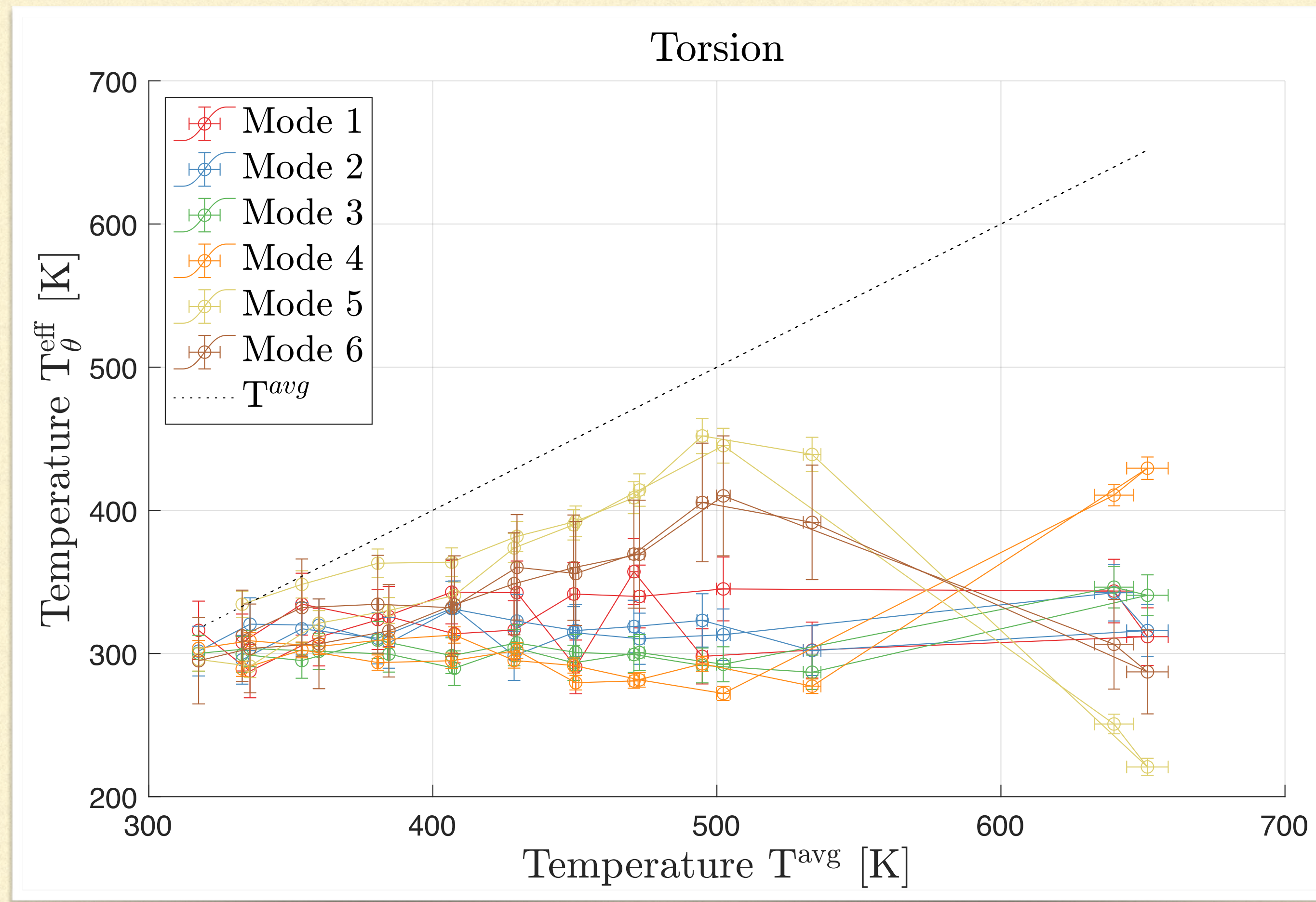
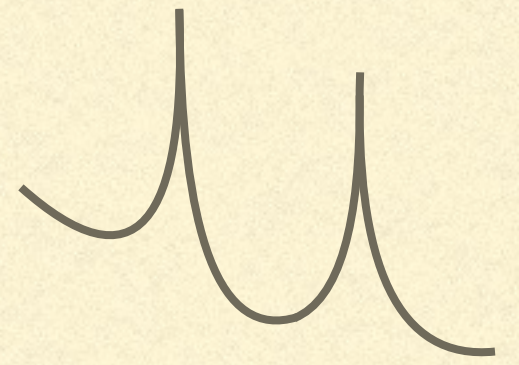


NESS?

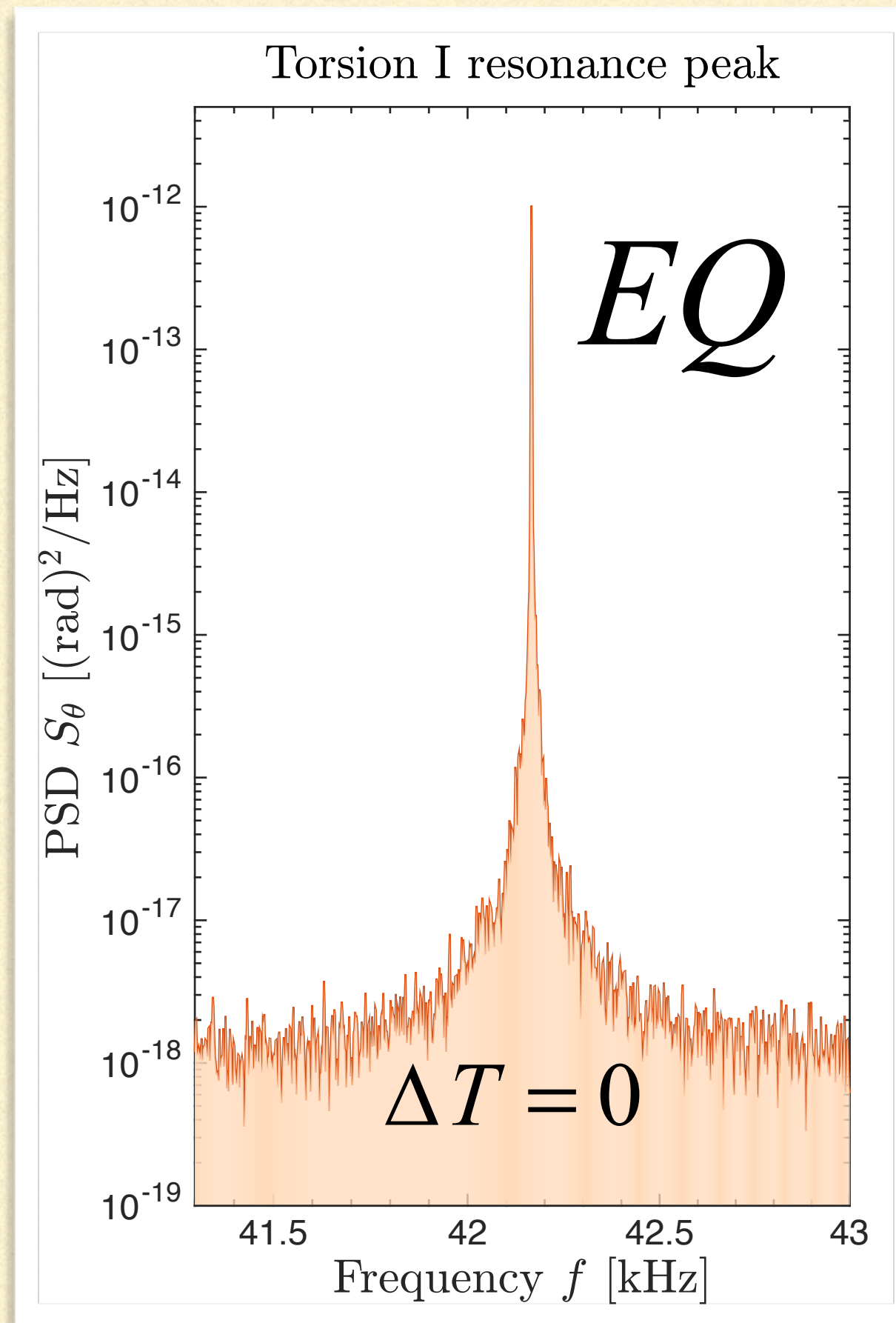
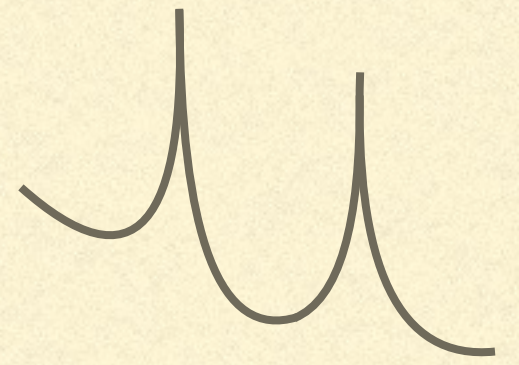
Measurements



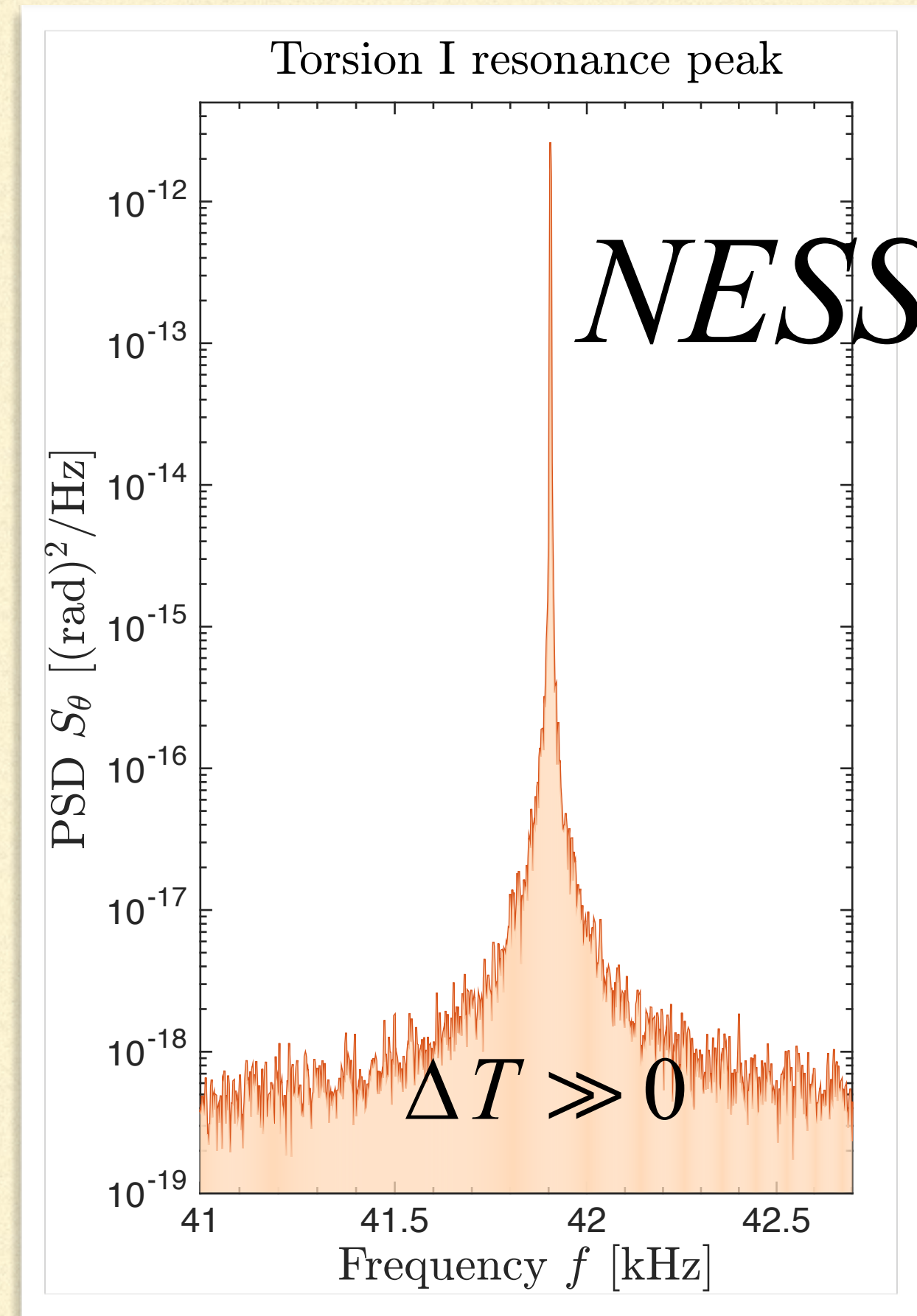
Measurements



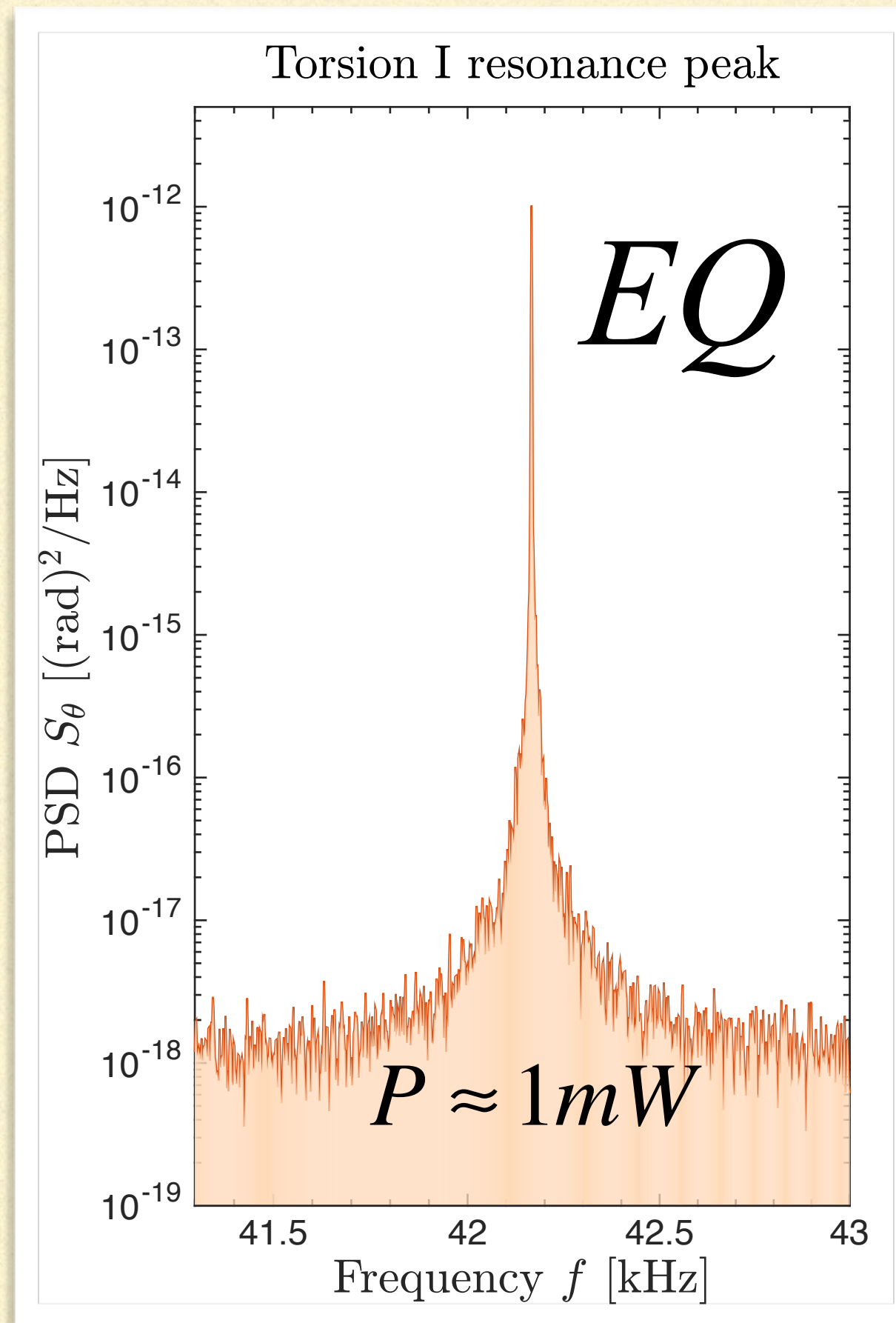
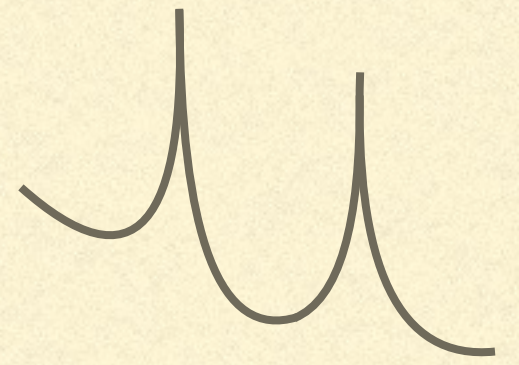
Effective temperature: ?



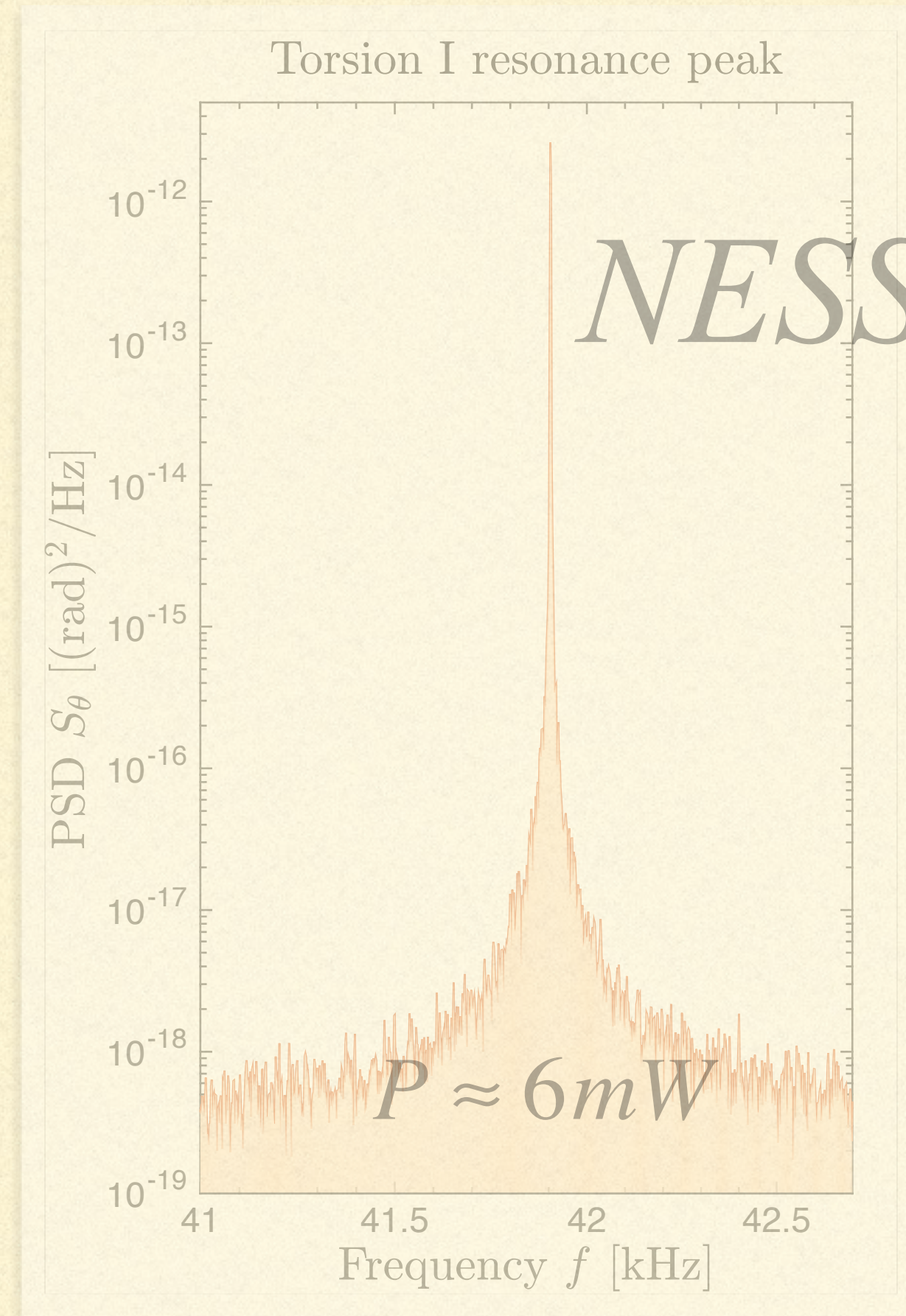
$\approx$



Effective temperature: FDT



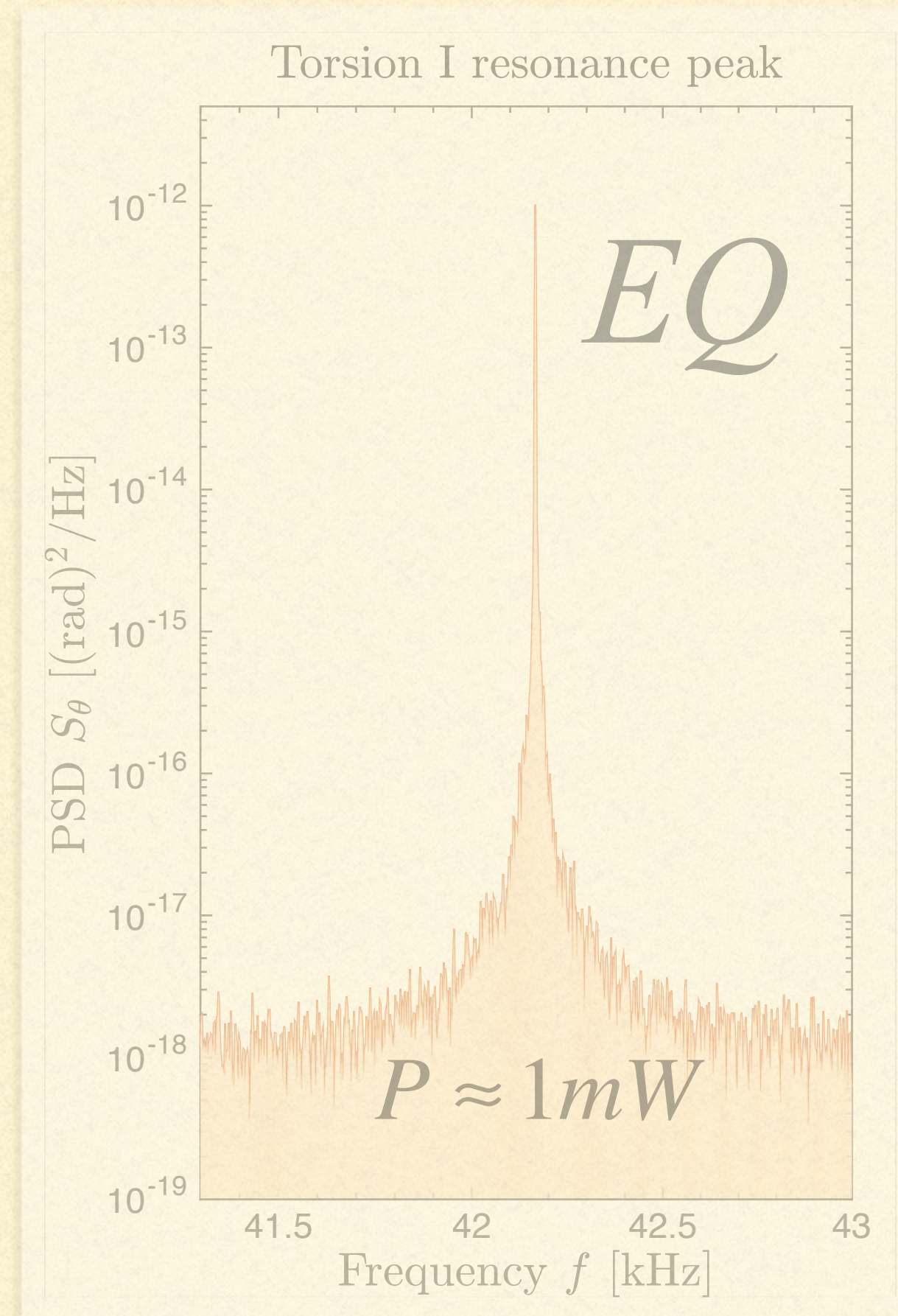
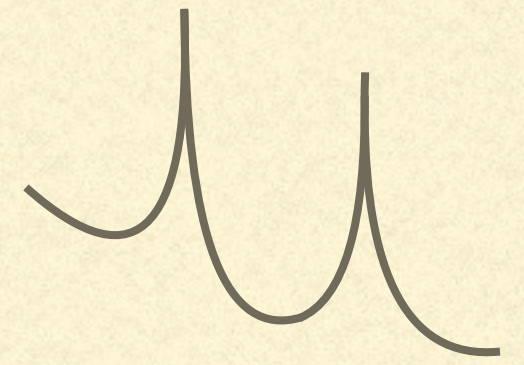
$\approx$



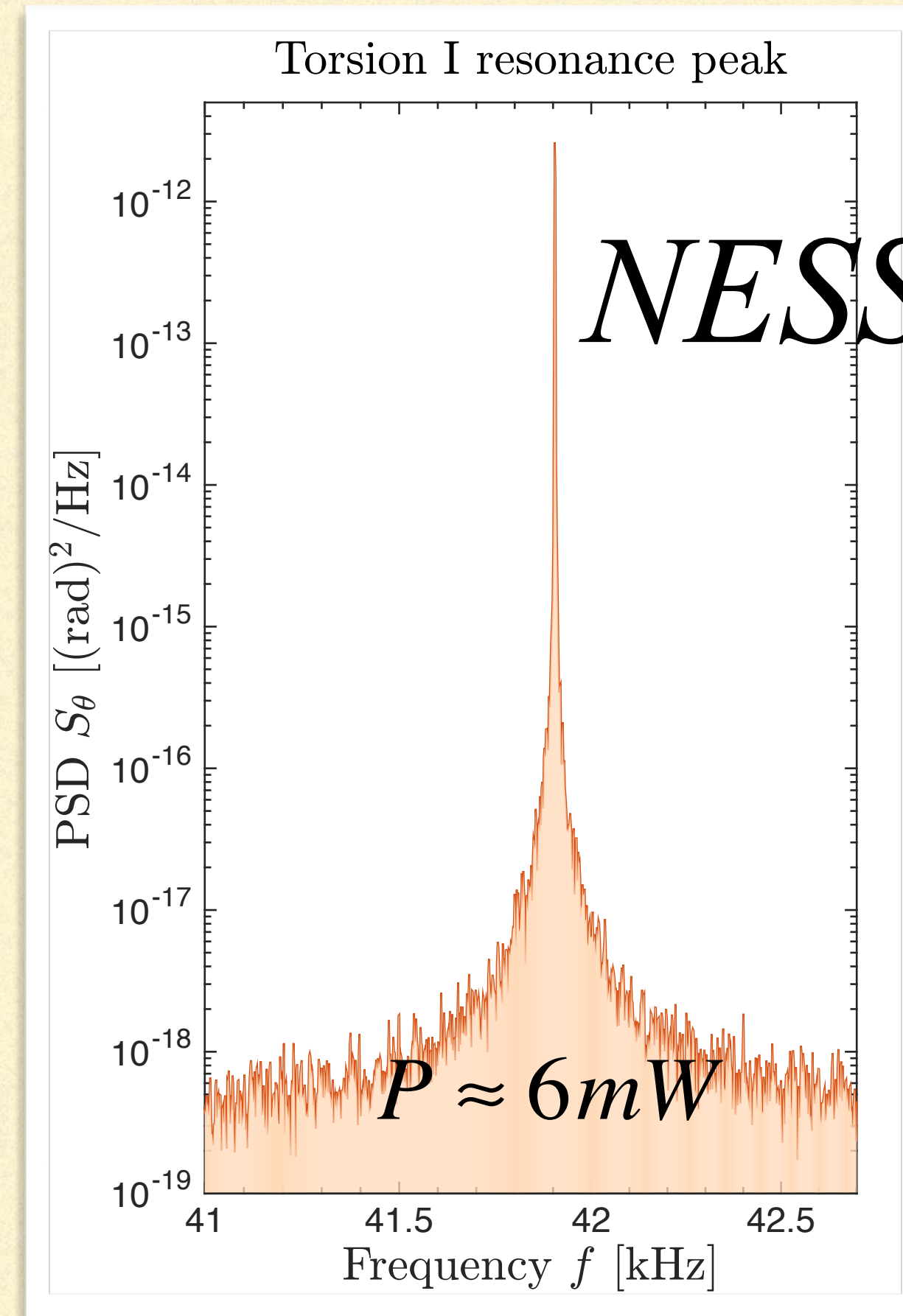
EQ

$$PSD = \frac{8k_B T}{(2\pi f)^2} \int dx \frac{E^{diss}(x)}{F^2}$$

Effective temperature: NESS FDT



$\approx$

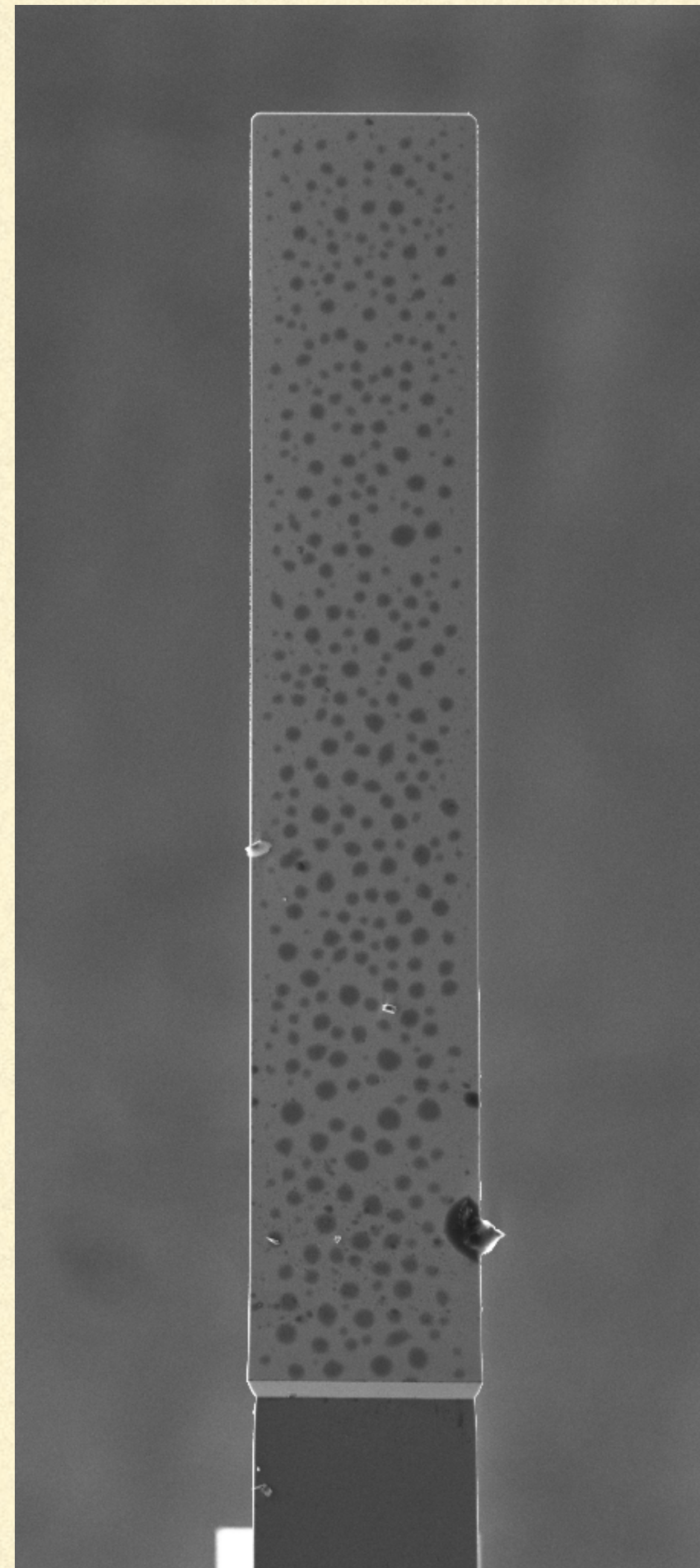
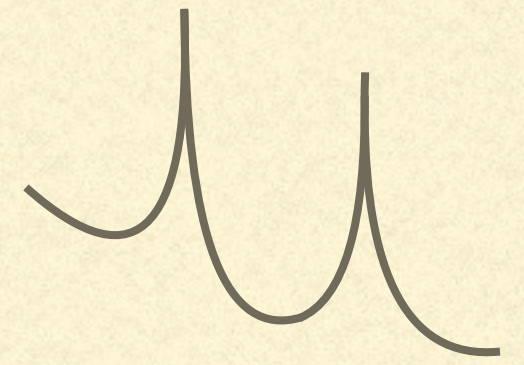


NESS

$$PSD^{(1)} = \frac{8k_B}{(2\pi f)^2} \int dx \frac{T(x) E^{diss}(x)}{F^2}$$

(1) K. Komori, et al. Physical Review
D **97**, 102001 (2018) .

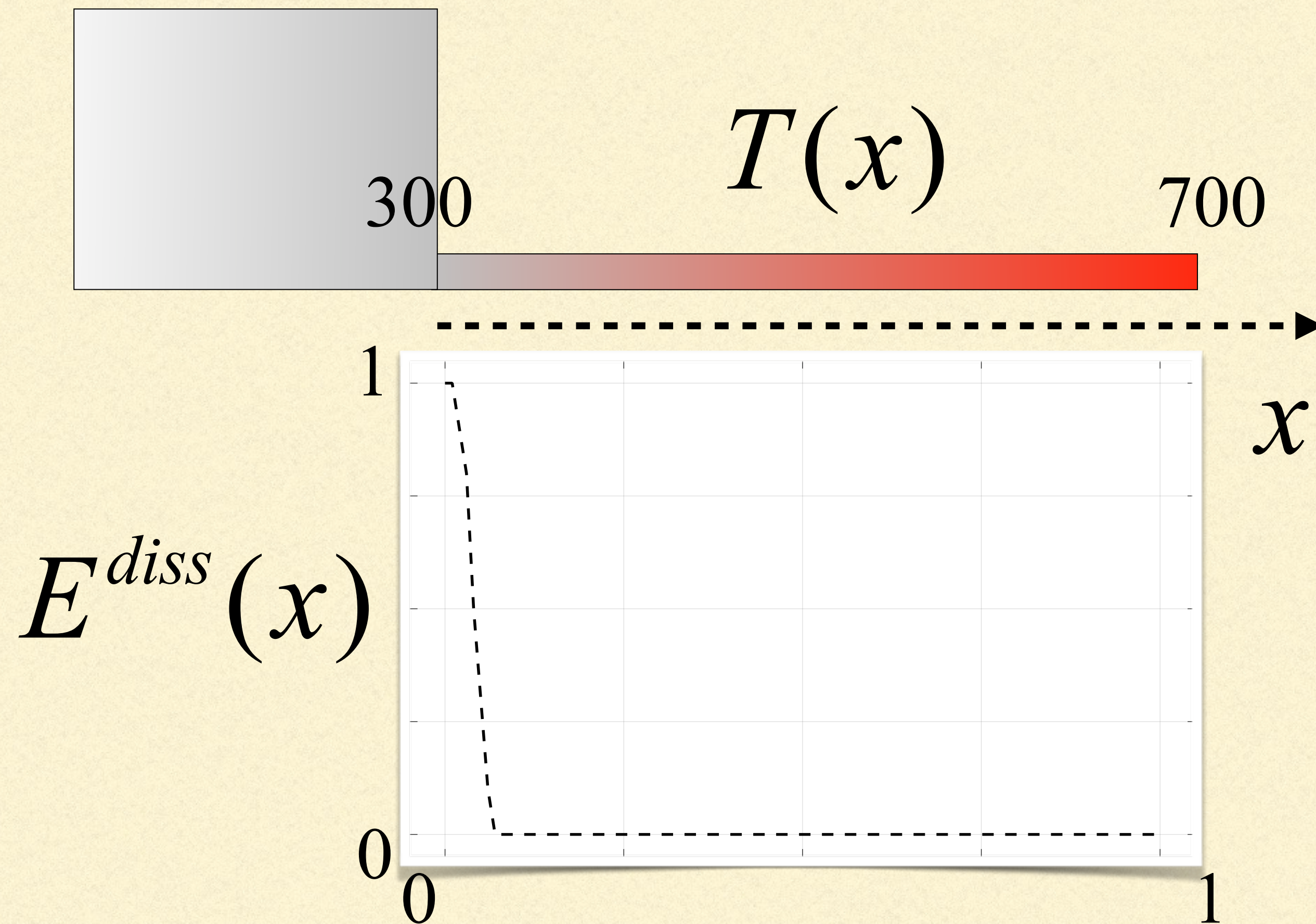
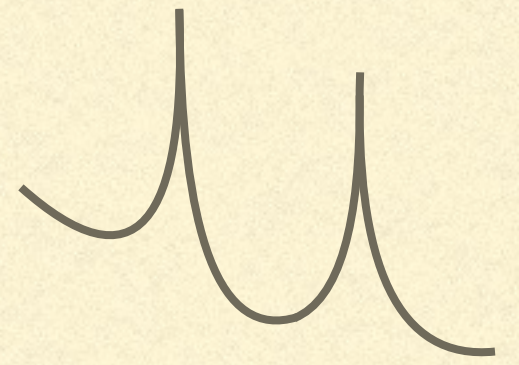
Effective temperature: E^{diss}



$$T_n^{\text{eff}} = \int dx \cdot T(x) E_n^{\text{diss}}(x)^{(2)}$$

(2) M. Geitner, et al. Physical Review
E **95**, 032138 (2017)

Effective temperature: E^{diss}

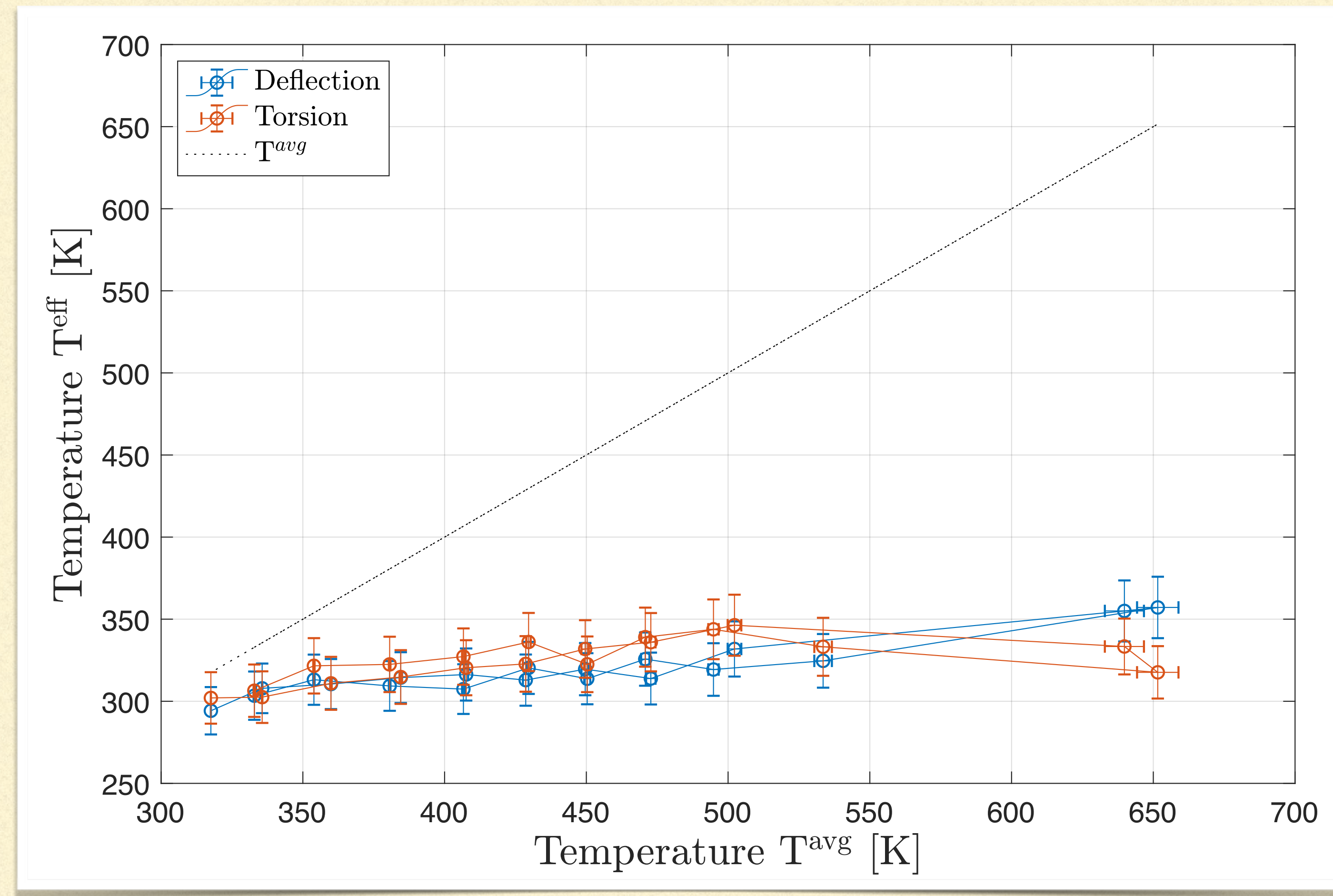
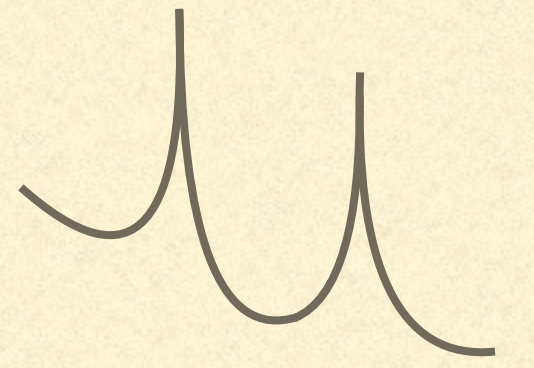


$$T_n^{\text{eff}} = \int dx \cdot T(x) E_n^{\text{diss}}(x) \quad (2)$$

$$E_n^{\text{diss}}(x) \approx \text{Dirac}(0)$$

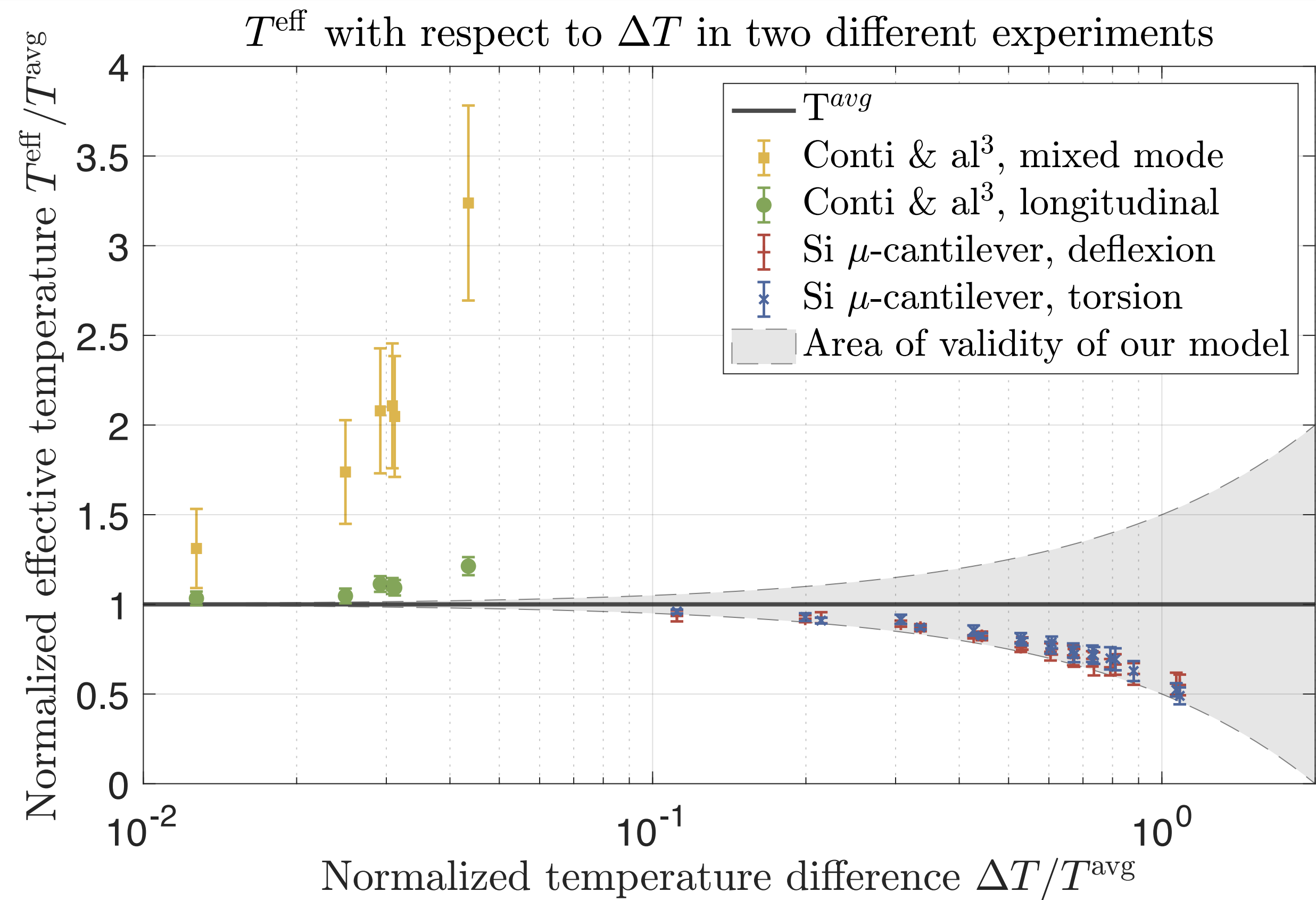
(2) M. Geitner, et al. Physical Review
E **95**, 032138 (2017)

Effective temperature: answer

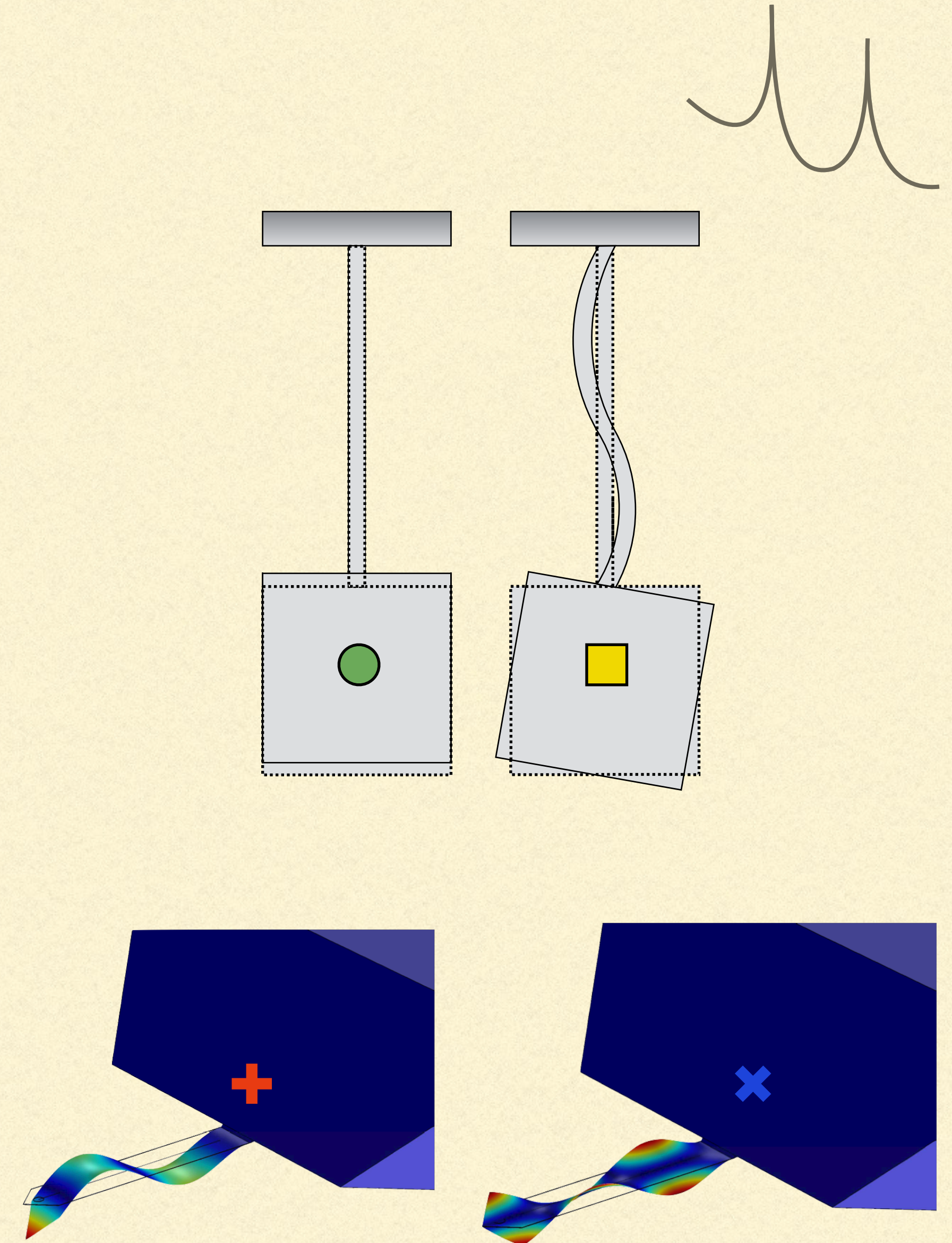


$$T_n^{eff} \approx T^{amb}$$

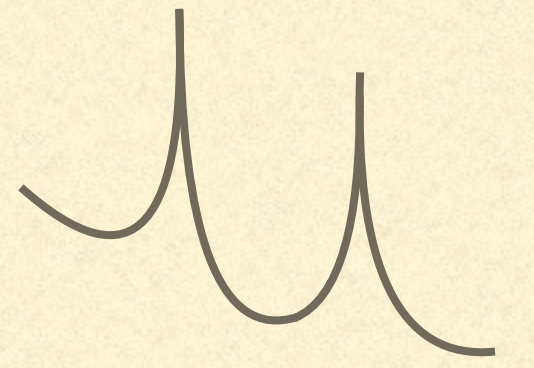
Comparison with Conti & al.⁽³⁾



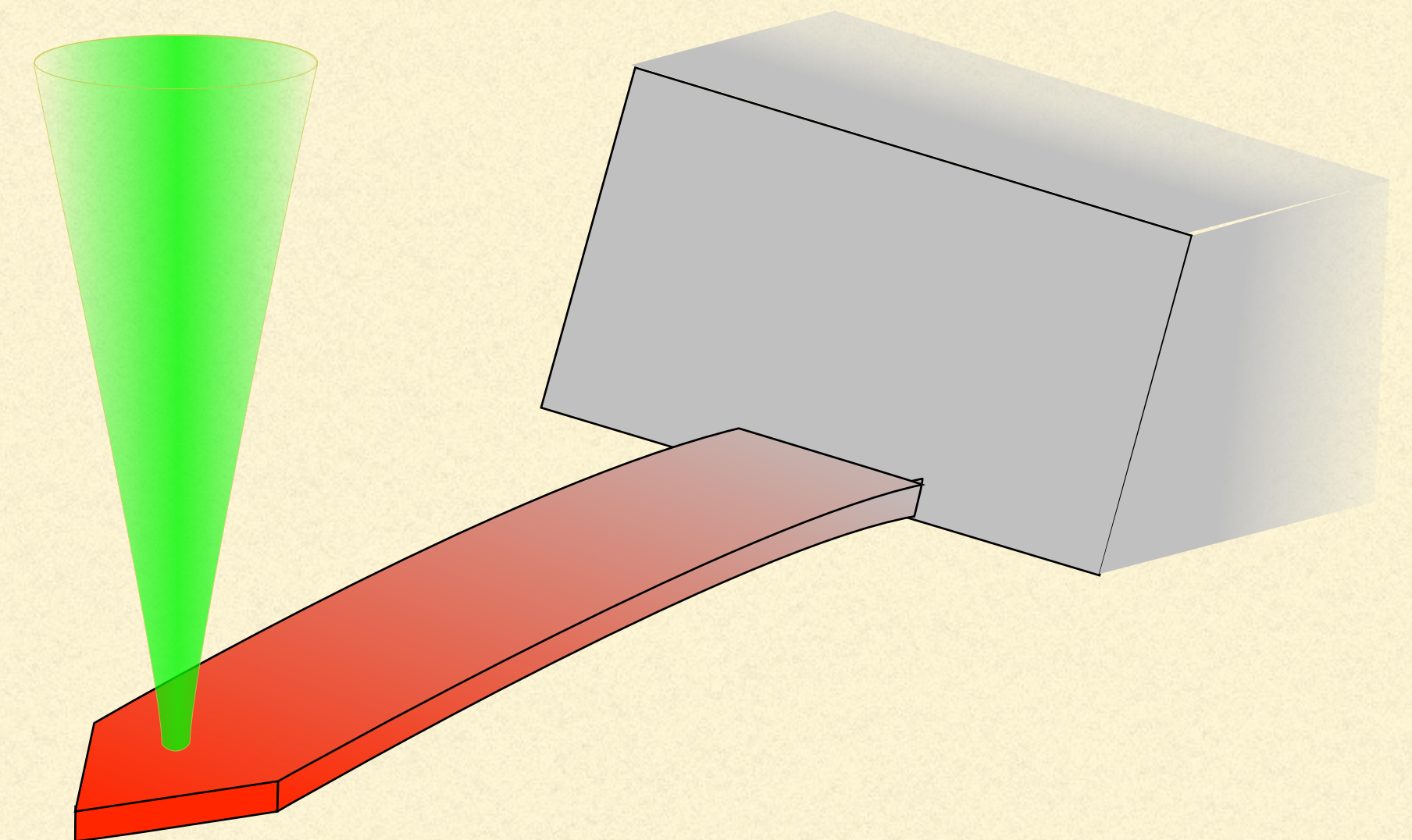
(3) L. Conti et al., J. Stat. Mech. , **P12003** (2013).

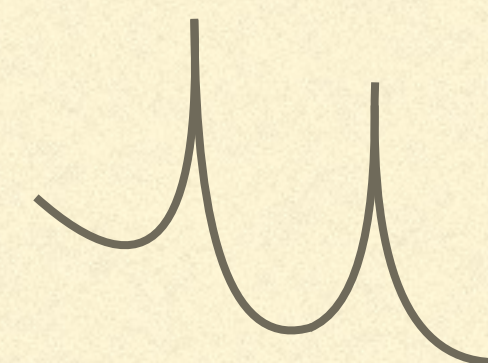


Conclusions



- We create a NESS
- We can observe a *lack* of fluctuations
- In Padua they measure an excess
- We have a large phenomenology to explore!





Thank you for your attention !