



# Status of the SPARC



## Working Point

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SPARC Review Committee

23 September 2003

# Outline

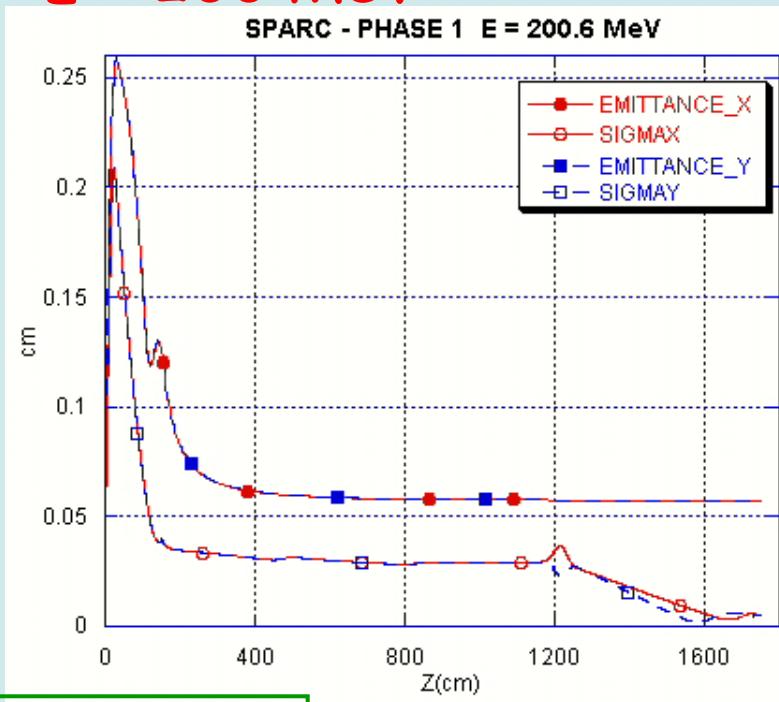
- \* Previous Working point
- \* Strategy for the parameters optimization studies
- \* Optimized working point
- \* Implications of this variation
- \* High bunch current with velocity bunching
- \* Conclusions

# PARMELA Start-to-End Simulation

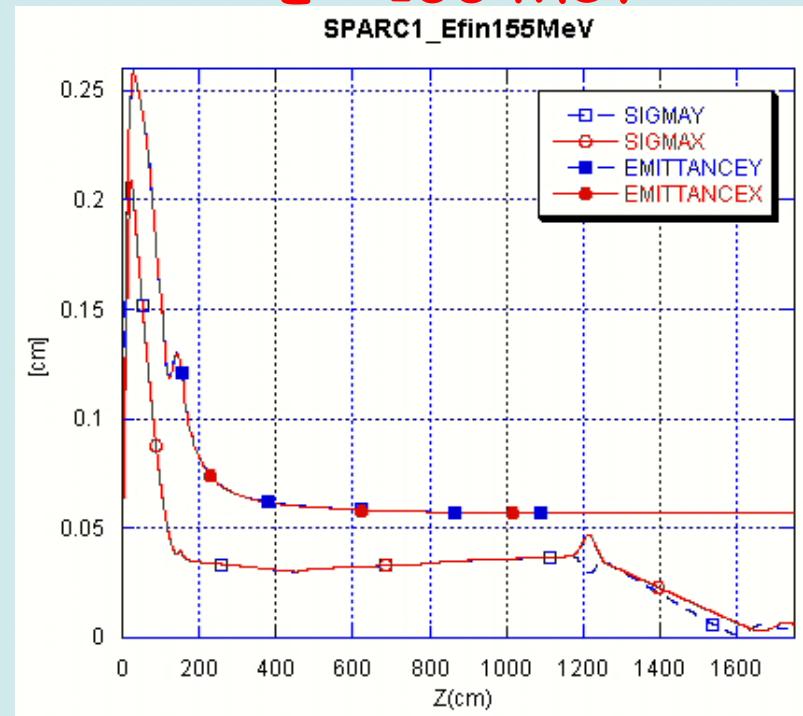
(Previous working point: Q=1nC; L=11.7ps; R=1mm)

3 RF str.: 25+12.5+12.5 MV/m  
B(solenoid) = 750G

E = 200 MeV



E = 155 MeV



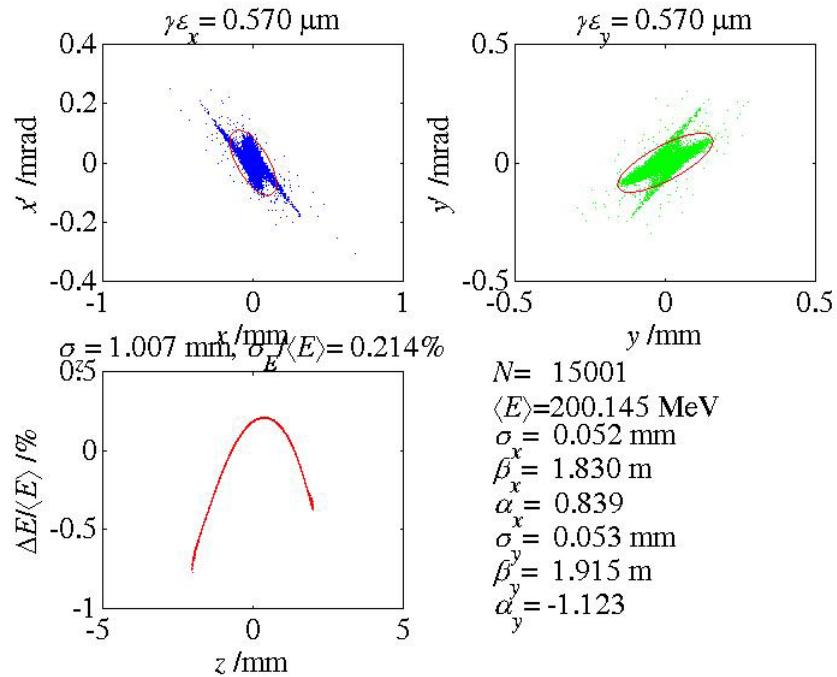
PARMELA simulations  
rms values:  
@undulator entrance :

$$\langle \varepsilon_x \rangle = 0.57 \text{ mm mrad}$$

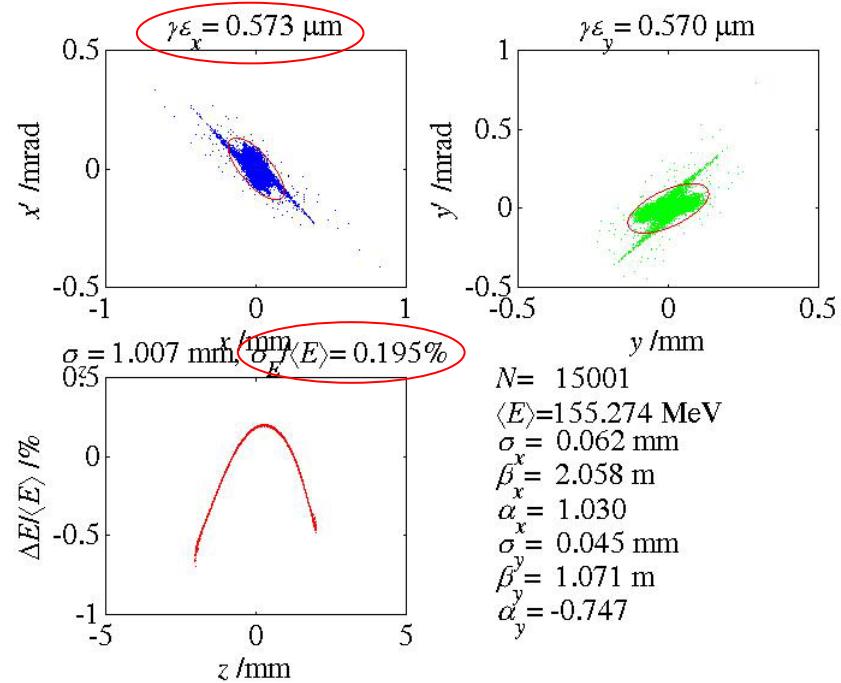
$$\langle \sigma_E/E \rangle = 2 \cdot 10^{-3}$$

# Beam characterization @undulator entrance:

$E = 200 \text{ MeV}$



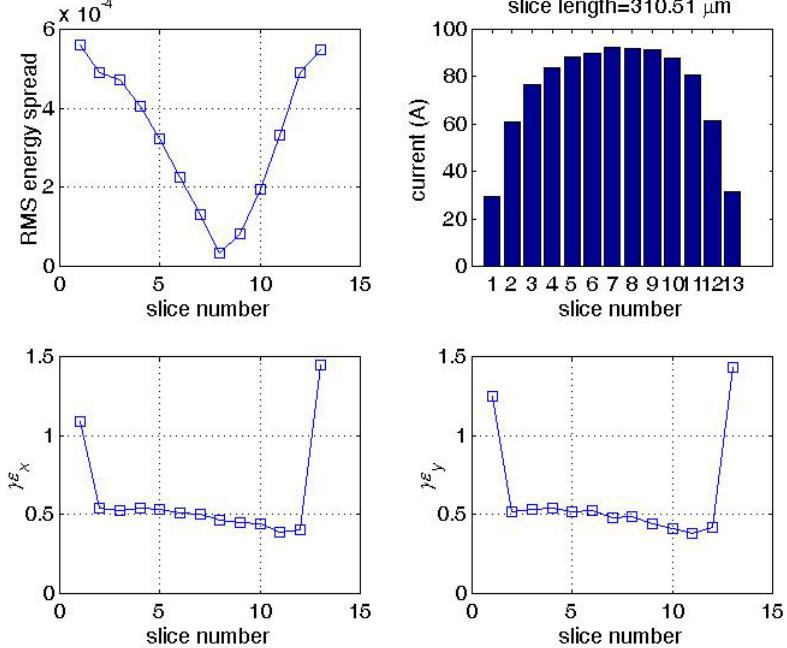
$E = 155 \text{ MeV}$



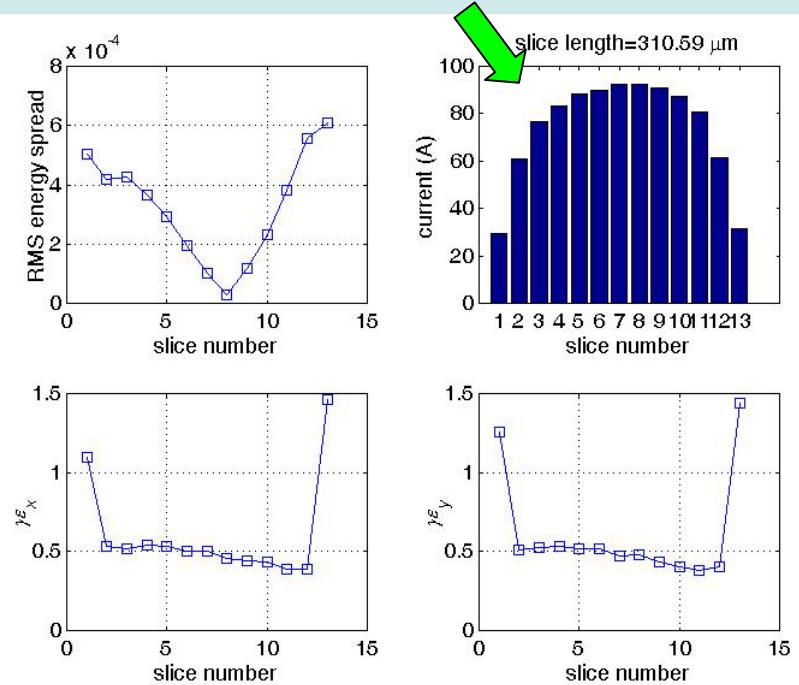
# Slice analysis @undulator entrance (PARMELA output)

previous  
working point:  
 $Q=1\text{nC}$ ;  $L=11.7\text{ps}$ ;  $R=1\text{mm}$

$E = 200 \text{ MeV}$



$E = 155 \text{ MeV}$



# Slice analysis @undulator entrance (PARMELA output)

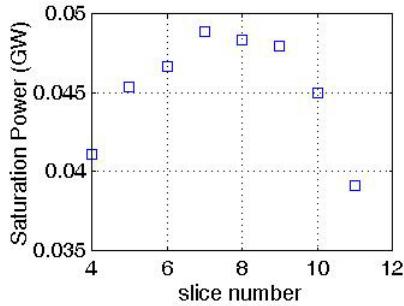
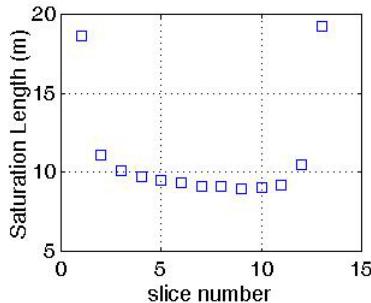
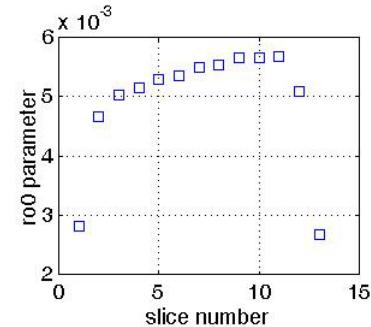
13 slices

$\lambda_u = 3 \text{ cm}$

$\langle\beta\rangle_{\text{und}} = 1.6 \text{ m}$

$E = 200 \text{ MeV}$

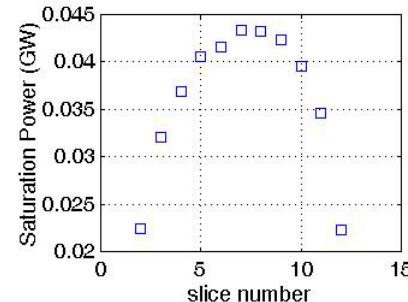
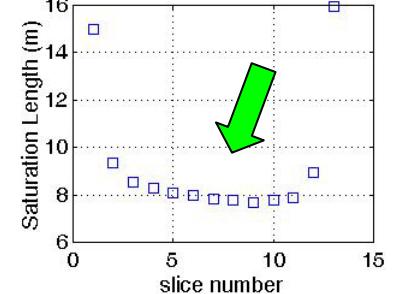
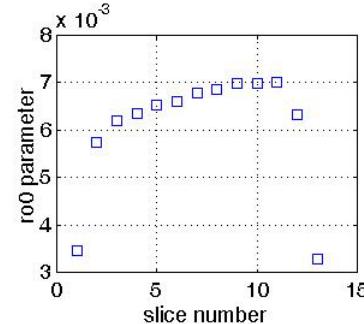
$\lambda_r = 290 \text{ nm}$



$\langle P_{\text{sat}} \rangle = 0.045 \text{ GW}$   
 rms pulse length = 702.490 um  
 pulse length = 8285.900 fsec  
 saturation length = 10.000 m  
 e-beam efficiency = 73.108%  
 e-beam peak current = 0.088 kA

$E = 155 \text{ MeV}$

$\lambda_r = 530 \text{ nm}$

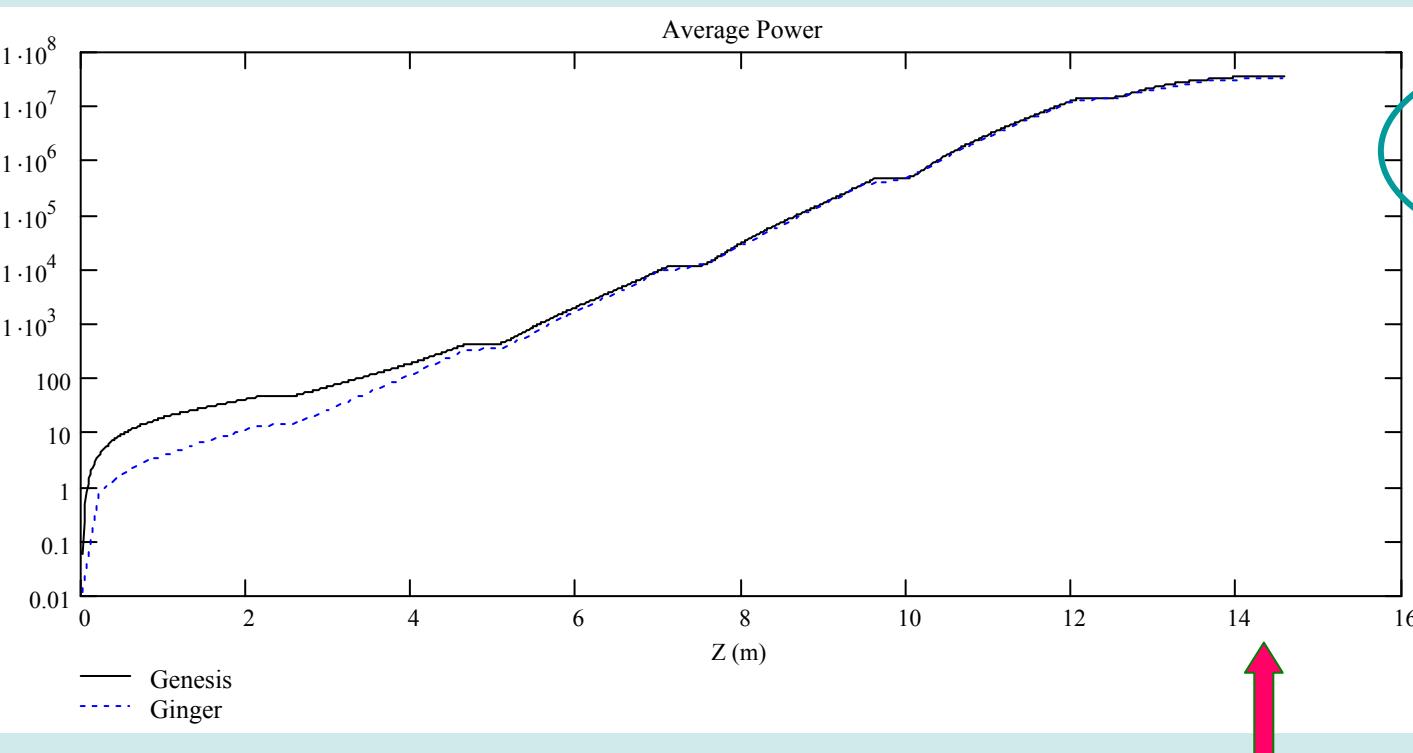


$\langle P_{\text{sat}} \rangle = 0.036 \text{ GW}$   
 rms pulse length = 924.947 um  
 pulse length = 11396.327 fsec  
 saturation length = 10.000 m  
 e-beam efficiency = 93.687%  
 e-beam peak current = 0.082 kA

We slightly moved some parameters to further optimize this WP

# Saturation in the last undulator section

Result obtained using both  
Ginger and Genesis



$$\lambda_u = 3\text{cm}$$

$$K=2$$

$$L_u = 14.5\text{ m}$$

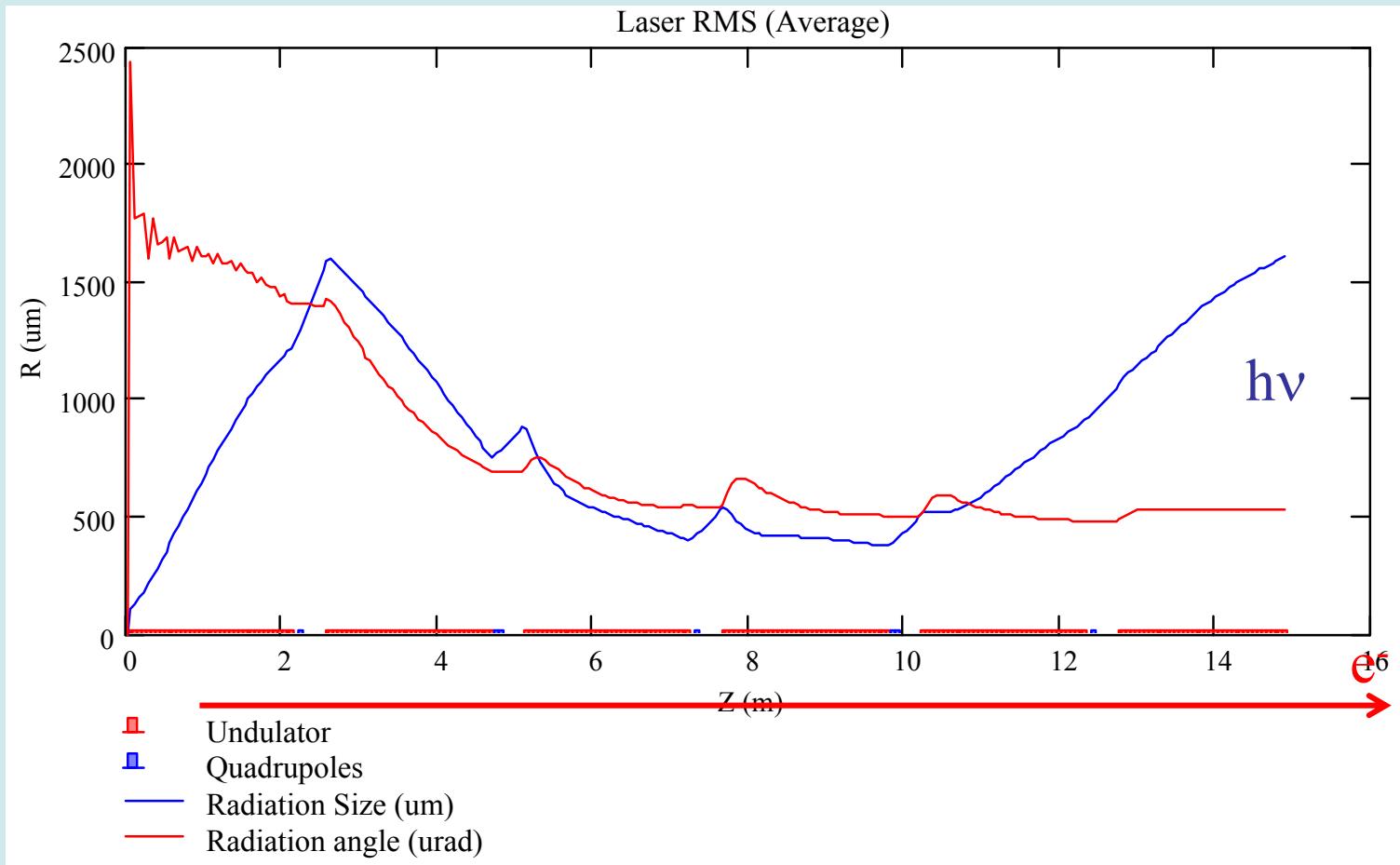
$$I=85\text{A}$$

$$\varepsilon_{\text{slice}} = 1 \text{ mm-mrad}$$
$$(\sigma_E/E)_{\text{slice}} = 6 \cdot 10^{-4}$$

Taking into account  
tolerances,  
misalignments,  
errors,...

$$L_{\text{sat}} \sim 14.2 \text{ m}$$

# SPARC-FEL is dominated by Diffraction



the photon beam is not overlapped to the electron beam  
through all the undulator

the photon beam is not focussed as the electron beam

# Motivations and Strategies

(JBR et al. SPARC-BD-03-004)

$$L_g \approx L_{1D} \left( 1 + 0.45 \left( \frac{L_{1D}}{Z_R} \right)^{0.57} + \dots \right)$$

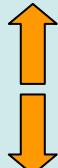
Xie scaling accounts for diffraction effects  
+ .....

$$L_{1D} \propto \frac{\lambda_u}{\rho} \propto \left( \frac{\lambda_u \epsilon_n}{I} \right)^{1/3}$$



$$\frac{L_{1D}}{Z_R} \propto \frac{\lambda_u^{4/3}}{I^{1/3} \epsilon_n^{2/3}}$$

$$Z_R \propto \frac{\epsilon_n}{\lambda_u}$$



$$\lambda_r = \frac{\lambda_u}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$

$$K \approx \lambda_u \exp \left[ -5.08 \frac{g/\lambda_u}{\lambda_u} - 1.54 \left( \frac{g/\lambda_u}{\lambda_u} \right)^2 \right]$$

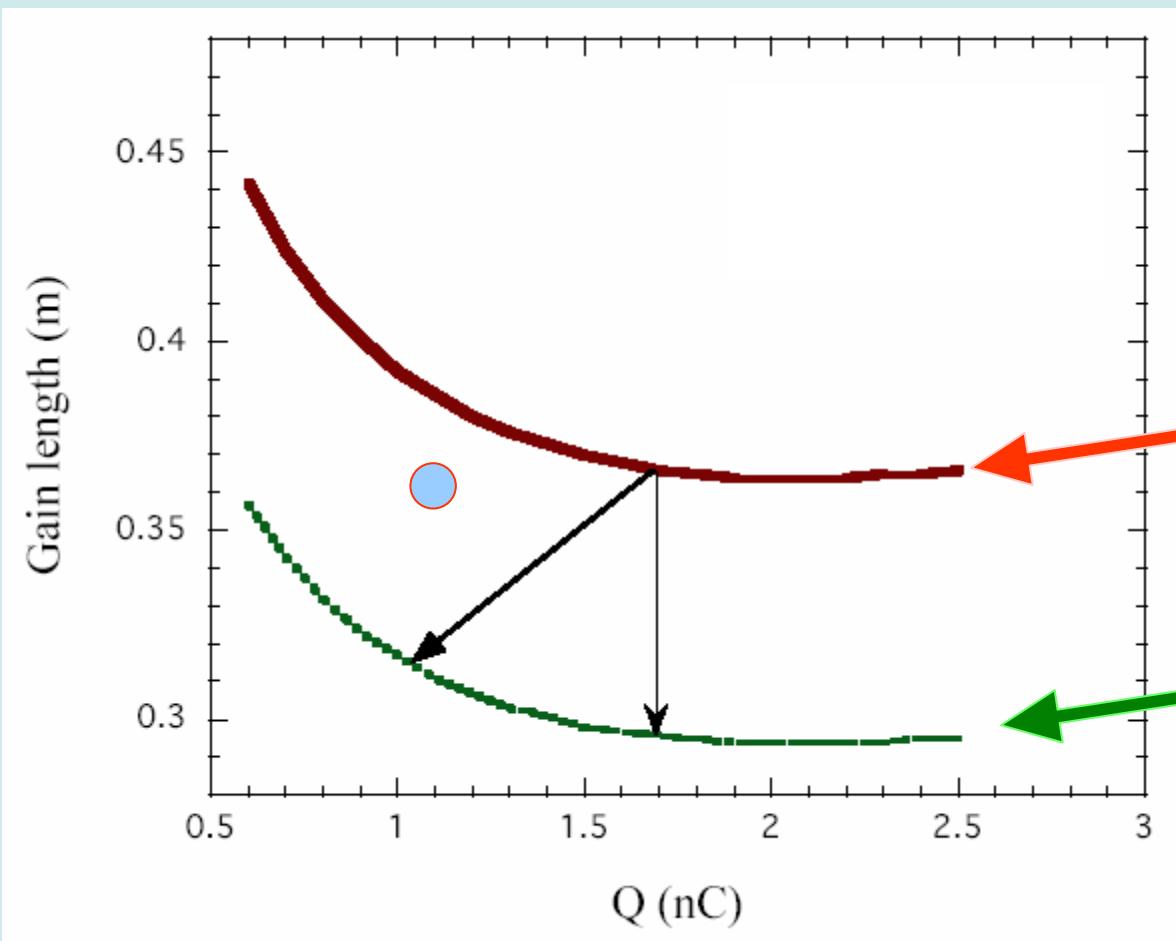


What about the undulator gap?

# Gain length vs bunch charge for the SPARC FEL

previous WP:  
 $gap=9\text{mm}$   
 $\lambda_u=3\text{cm}$

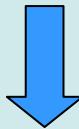
NEW WP:  
 $gap=9\text{mm}$   
 $\lambda_u=2.8\text{cm}$



$gap=10\text{mm}$   
 $\lambda_u=3\text{cm}$

$gap=6.6\text{mm}$   
 $\lambda_u=2.5\text{cm}$

Adopted strategy  
to decrease the saturation length:



- \* Increase the slice current up to 100A  
for at least 50% of the bunch
- \* Reduce the undulator period  $\lambda_u$

There are different possibilities  
to increase the bunch current while  
keeping the bunch density constant

1. Keep constant the longitudinal length  $\Rightarrow$  Increase transverse area

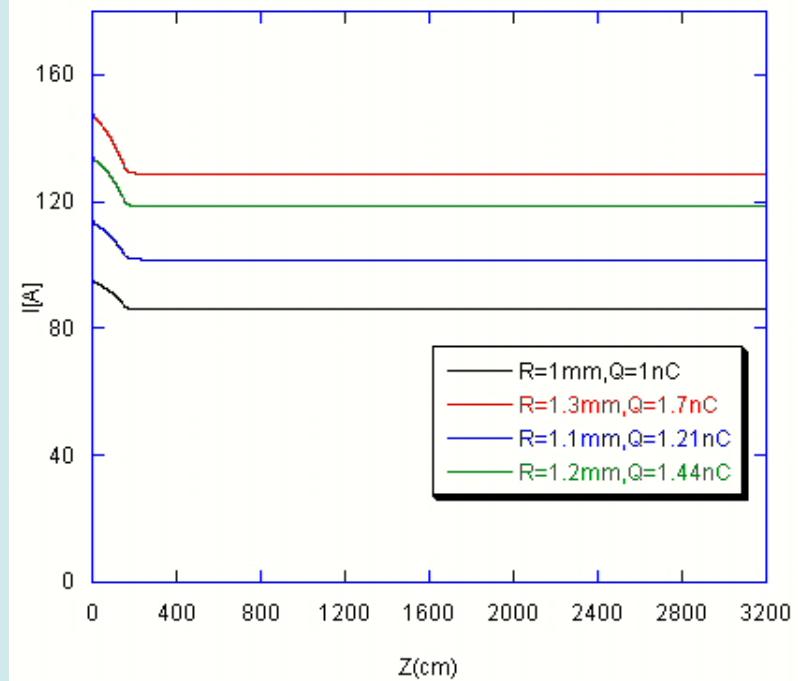
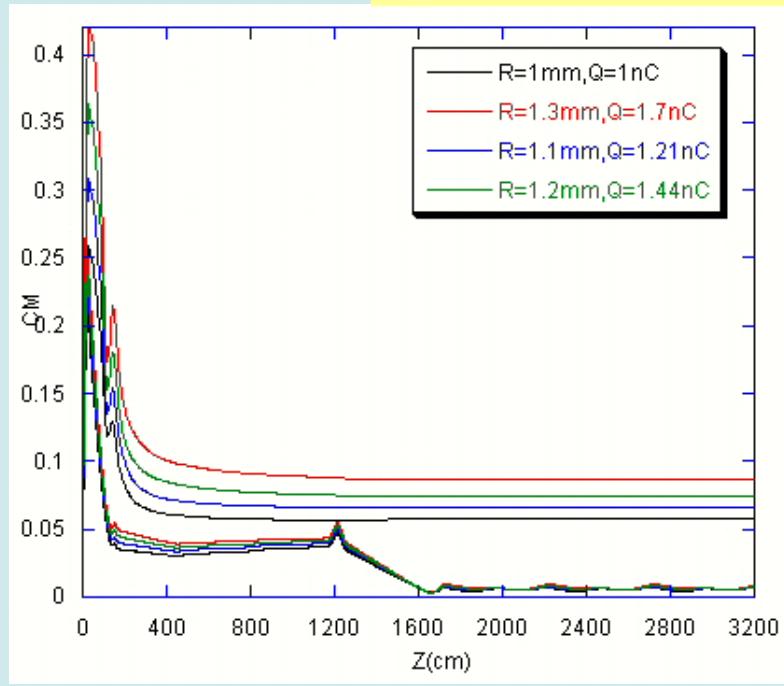
$$\sigma_z = \text{const.} \Rightarrow \sigma_x \propto \sqrt{Q} \Rightarrow I \propto Q$$

2. Keep constant the linear charge density  $\Rightarrow$  (and transverse size slightly increased)  
Bunch length is shortened

$$\frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$

# PARMELA Start-to-End Simulation

$$\sigma_z = \text{const.} \Rightarrow \sigma_x \propto \sqrt{Q} \Rightarrow I \propto Q$$



@ undulator  
entrance:  
( $z=18\text{m}$ )

$Q=1\text{nC}; R=1\text{mm}$

$\varepsilon_x=0.570\mu\text{m}$

$\langle I \rangle = 82\text{A}$

$Q=1.21\text{nC}; R=1.1\text{mm}$

$\varepsilon_x=0.665\mu\text{m}$

$\langle I \rangle \sim 102\text{A}$

$Q=1.44\text{nC}; R=1.2\text{mm}$

$\varepsilon_x=0.746\mu\text{m}$

$\langle I \rangle \sim 118.5\text{A}$

$Q=1.7\text{ nC}; R=1.3\text{mm}$

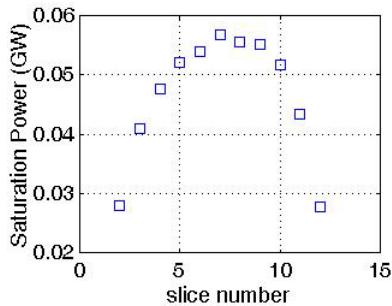
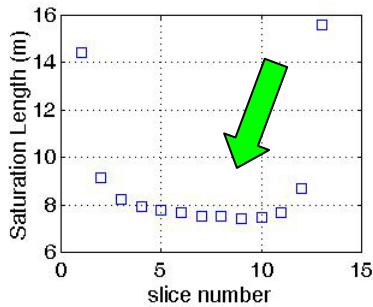
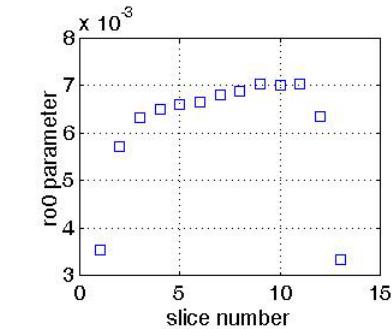
$\varepsilon_x=0.869\mu\text{m}$

$\langle I \rangle \sim 128\text{A}$

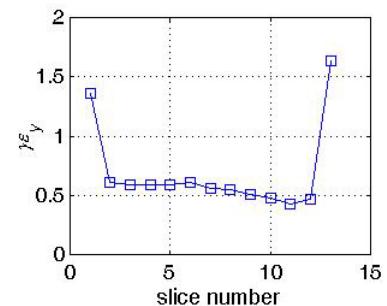
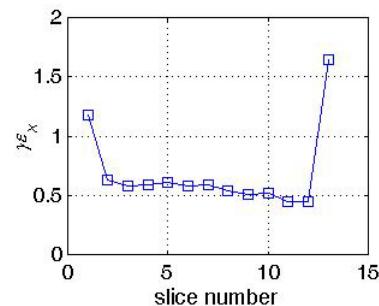
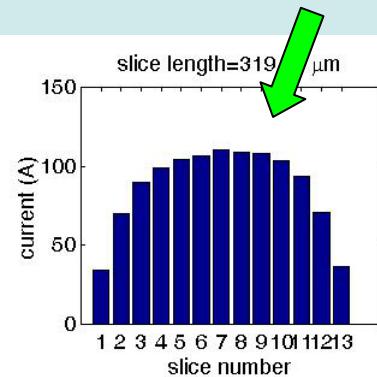
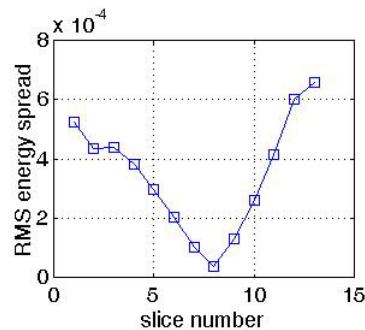
# Slice Analysis at the undulator entrance

$Q=1.2\text{nC}$ ;  $R=1.1\text{mm}$ ;  
pulse length=11.7ps

13 slices  
 $\lambda=0.03\text{ cm}$   
 $\langle\beta\rangle_{\text{und}}=1.6\text{m}$   
 $\lambda_{\text{rad}}=530\text{ nm}$



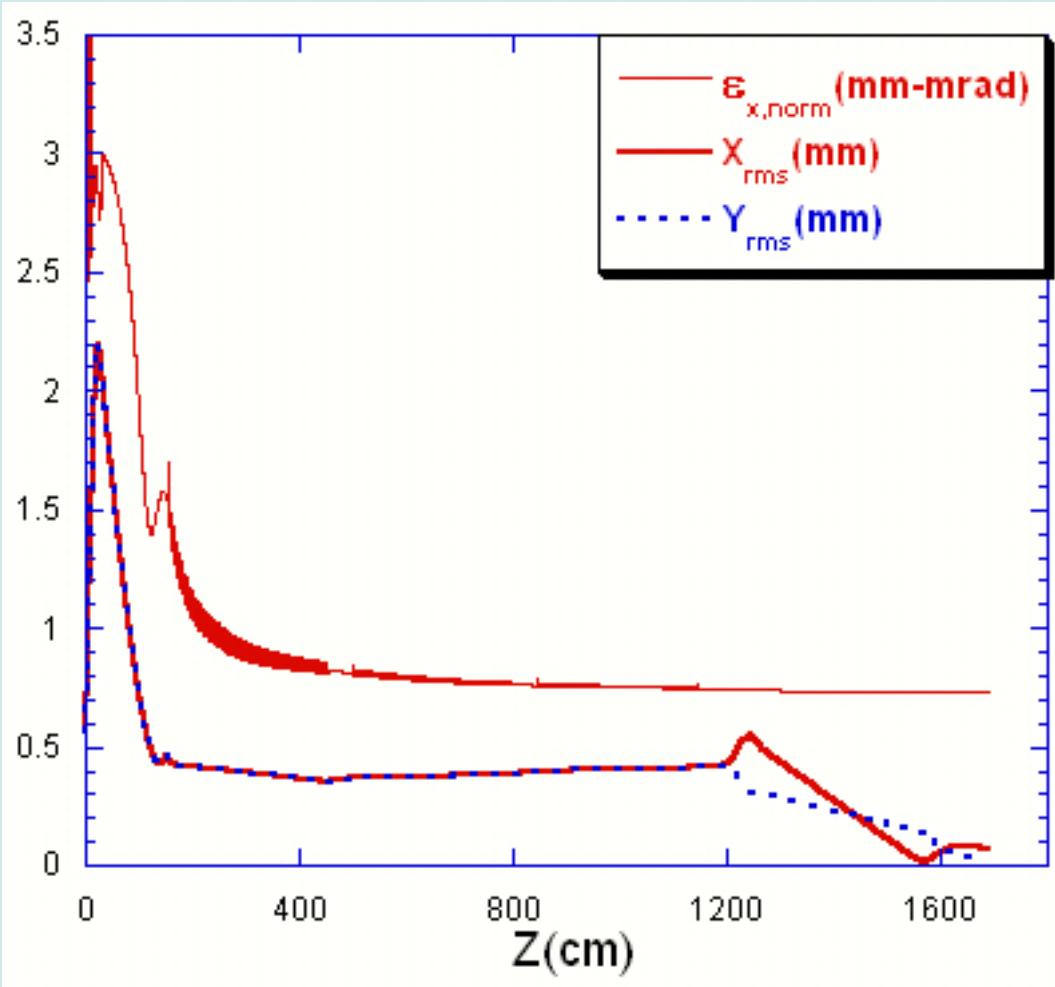
$\langle P_{\text{sat}} \rangle = 0.047\text{ GW}$   
rms pulse length=946.063 um  
pulse length=11714.588 fsec  
saturation length= 10.000 m  
e-beam efficiency= 93.760%  
e-beam peak current= 0.097kA



$I_{\text{slice}} > 110\text{A}$  in >60% beam  
 $L_{\text{SAT}} \sim 7\text{m}$

$$\frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$

## PARMELA simulation up to the entrance of the undulator



$$\epsilon_{\text{th}} = 0.34 \text{ mm mrad}$$

$$Q = 1.1 \text{nC} ; R = 1.13 \text{mm}$$

$$\text{Pulse length(FWHM)} = 10 \text{ps}$$

$$\text{Rise time} = 1 \text{ps}$$

$$\text{Gun peak field} = 120 \text{MV/m}$$

$$\text{Injection phase} = 33^\circ$$

$$B_{\text{sol}}(\text{gun}) = 2.73 \text{KGauss}$$

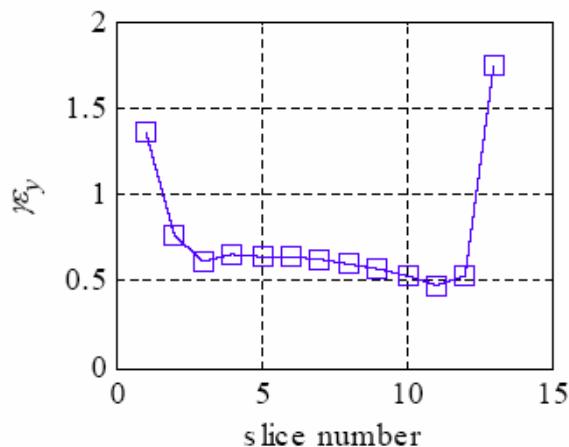
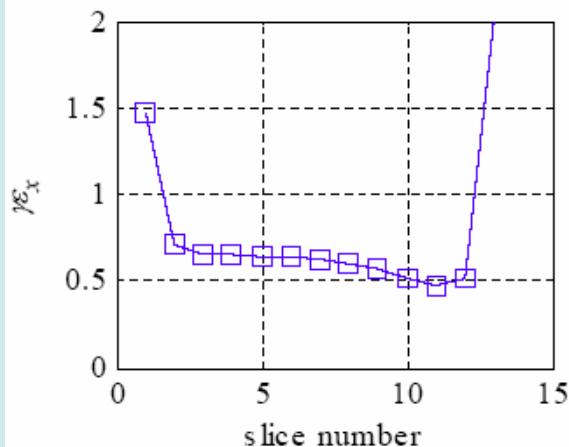
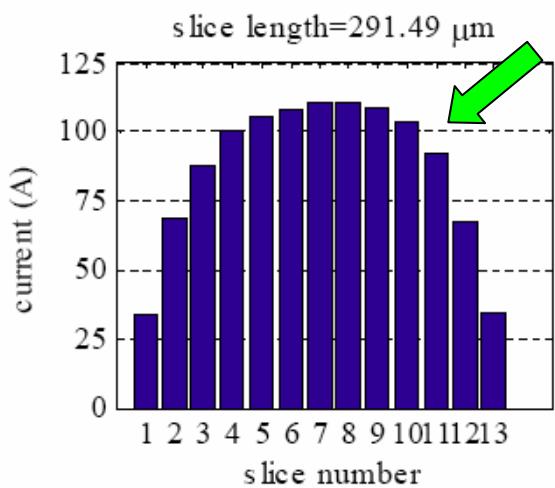
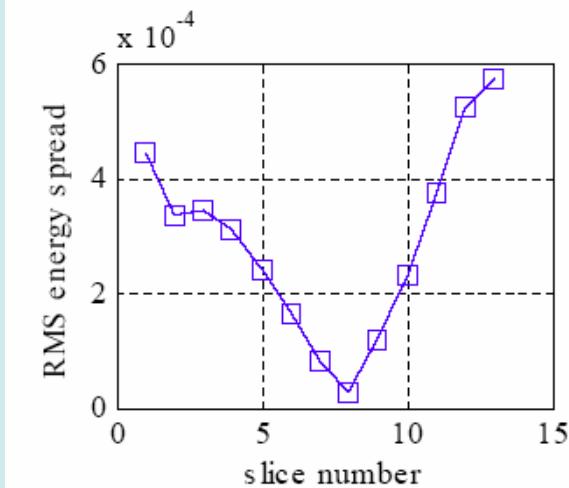
$$B_{\text{sol}}(1\text{TW}) = 750 \text{ Gauss}$$

$$\epsilon_{x,\text{rms}} = 0.74 \text{ mm mrad}$$



$$\frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$

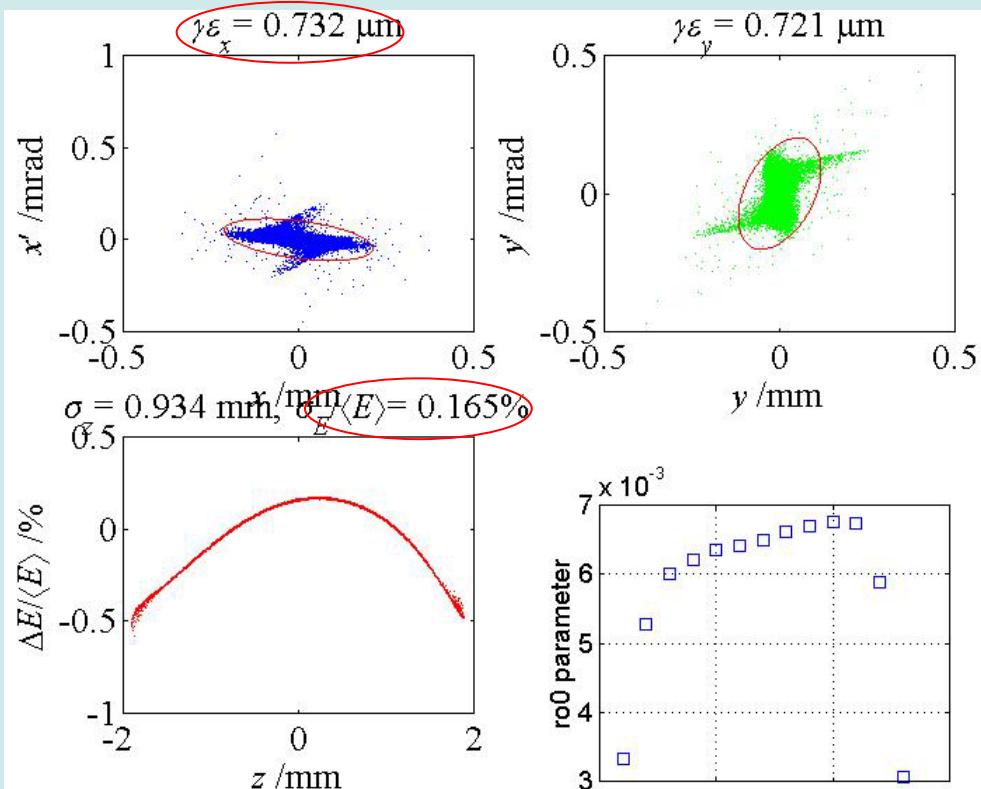
**Q=1.1 nC, pulse length (FWHM) = 10 psec, rise time=1 psec**



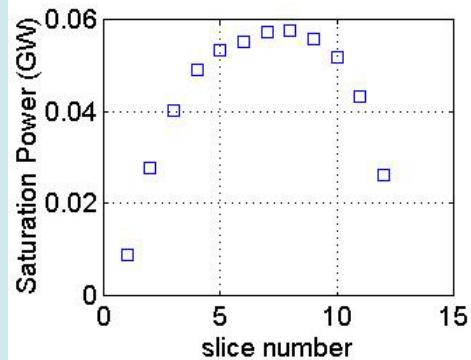
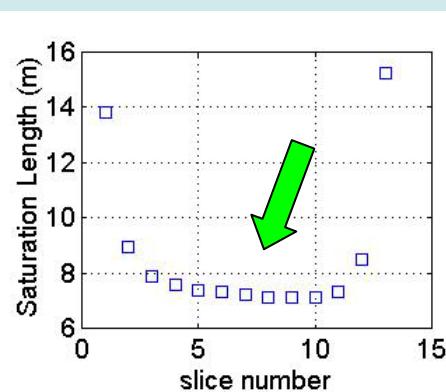
**Max. slice  
current=110 A**

**Current  $\geq 100$  A  
in 54% beam**

**Projected  
emittance= 0.75  
mm mrad**



$$\frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$



$\langle P_{\text{sat}} \rangle = 0.044 \text{ GW}$   
rms pulse length=895.979 um  
pulse length=11667.829 fsec  
saturation length= 14.000 m  
e-beam efficiency= 96.921%  
e-beam peak current= 0.091kA

$L_{\text{SAT}} < 8 \text{ m}$   
in >60% beam

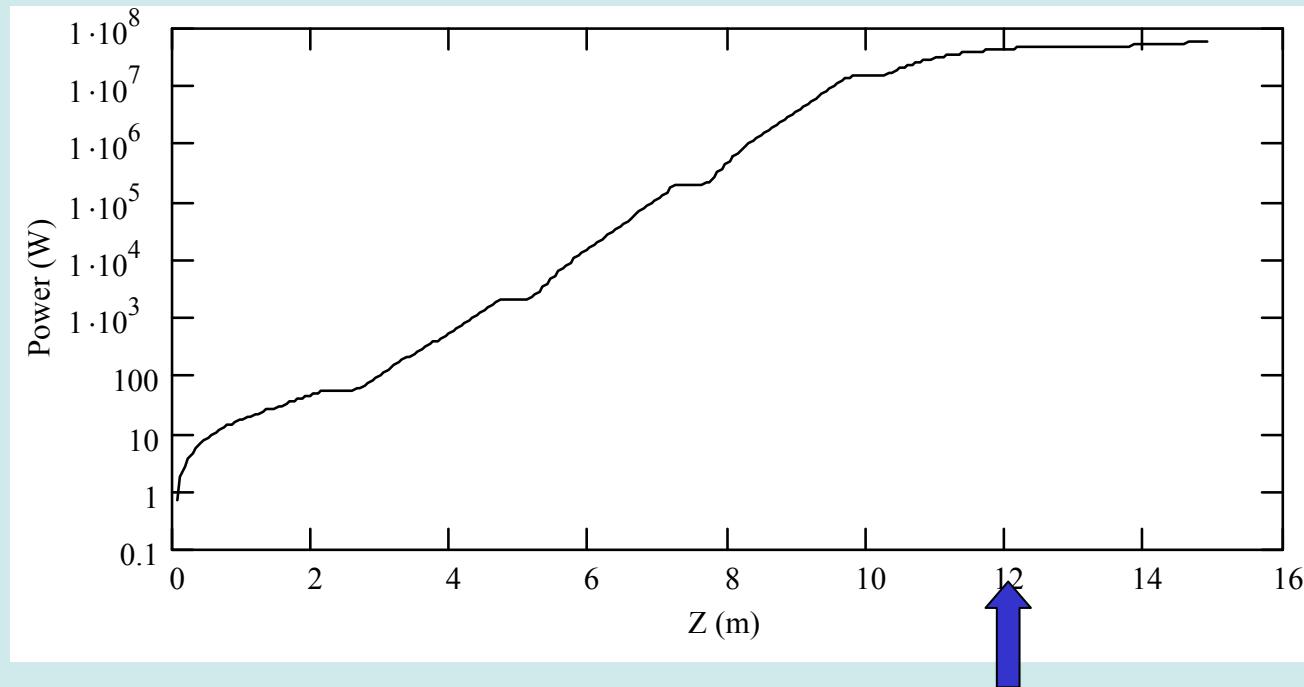
We gained ~15%  
in the saturation  
length

$$\lambda_u = 2.8\text{cm}; \text{gap} = 9\text{mm}$$

$$I_{\text{peak}} = 110A / 100A \text{ (50\% bunch)}$$

$$\varepsilon_{\text{slice}} = 1 \text{ mm-mrad}$$

$$(\sigma_E/E)_{\text{slice}} = 6 \cdot 10^{-4}$$



$$L_{\text{sat}} \sim 12 \text{ m}$$

(it was 14.2m)

# to summarize: last Parameter List

**Red:** modified parameters

**Blue:** confirmed old relevant parameters

Black: no change

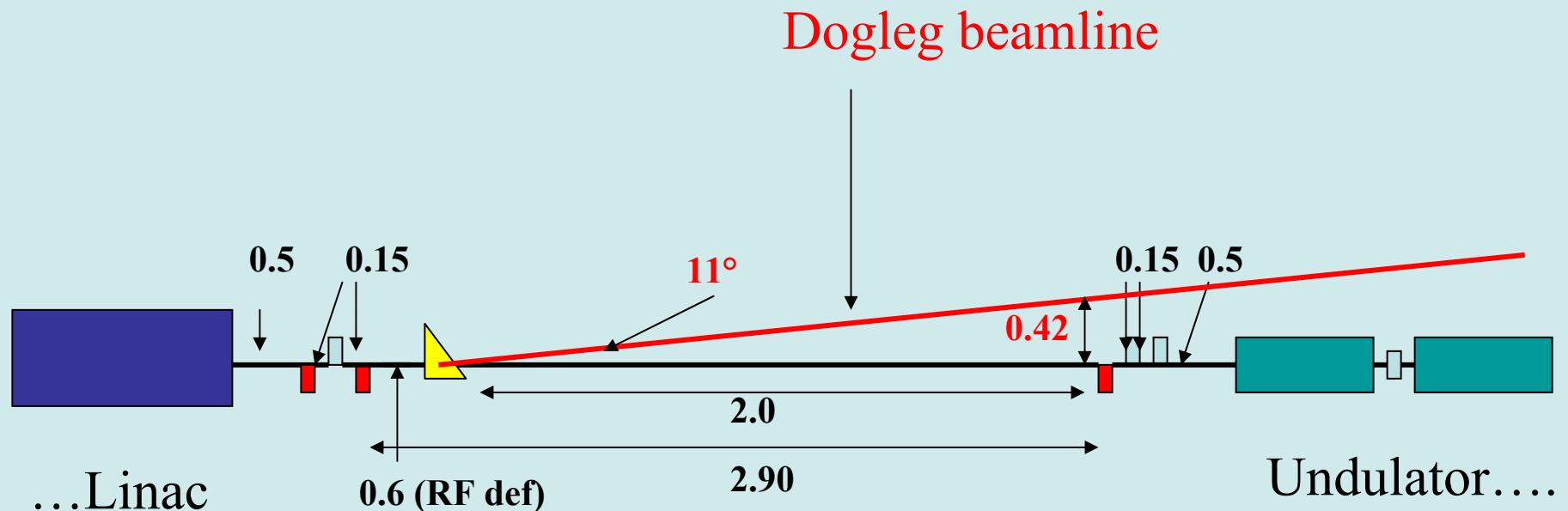
	Electron Beam Energy (MeV)	155	
	<b>Bunch charge (nC)</b>	<b>1.1</b>	(1)
	Repetition rate (Hz)	1-10	
	Cathode peak field (MV/m)	120	
	Peak solenoid field @ 0.19 m (T)	0.273	
	<b>Photocathode spot size (mm, hard edge radius)</b>	<b>1.13</b>	(1)
	<b>Central RF launch phase (RF deg)</b>	<b>33</b>	
	<b>Laser pulse duration, flat top (ps)</b>	<b>10</b>	(12)
	Laser pulse rise time (ps) 10%→90%	1	
	Bunch energy @ gun exit (MeV)	5.6	
	<b>Bunch peak current @ linac exit (A)</b>	<b>100</b>	(85)
	<b>Rms normalized transverse emittance @ lin ac exit (mm-mrad); includes thermal comp. (0.3)</b>	<b>&lt; 2</b>	
	<b>Rms slice norm. emittance (300 μm slice)</b>	<b>&lt; 1</b>	
	Rms longitudinal emittance (deg.keV)	1000	
	<b>Rms total correlated energy spread (%)</b>	<b>0.2</b>	
	<b>Rms incorrelated energy spread (%)</b>	<b>0.06</b>	(0.05)
	Rms beam spot size @ linac exit (mm)	0.4	
	Rms bunch length @ linac exit (mm)	1	

## last FEL Parameter List

Undulator period [cm]	2.8
Undulator parameter K	2.143
Undulator gap [mm]	9.25
# Undulator sections	6
# Undulator periods per section	78
Drift length between undulator sections [cm]	36.5
Additional quadrupole gradient [T/m]	5.438
Additional quadrupole length [cm]	8.4
FEL radiation wavelength (fundamental) [nm]	499.6
Average beta function [m]	1.516
Expected saturation length [m]	< 12

# Transfer Line sketch

- Total TL length = 5.4 m (it was 6 m)  $\rightarrow$  Some space is gained
- RF deflector included



# Transfer Line for SPARC @150 MeV with 3 SLAC sections

- Total TL length = 5.4 m, 6 quadrupoles (2 triplets)
- Beam characteristics at end of Linac (HOMDYN):
  - $z = 11.58 \text{ m}$
  - $\beta_x = 68.761 \text{ m}, \beta_y = 69.799 \text{ m}$
  - $\alpha_x = -3.547, \alpha_y = -3.602$
  - $E = 155.32 \text{ MeV}$
  - $\varepsilon_x = \varepsilon_y = 0.7 \mu\text{m}$  (normalized, slice)
- Opt. Functions at the undulator entrance:
  - $\beta_x = 1.999 \text{ m}, \beta_y = 0.677 \text{ m}, \alpha_x = 0.878, \alpha_y = -0.787$

# SPARC RF compressor studies:

parameters for  $E \sim 155\text{MeV}$  and  
3 TRW structures

...BUT WITH  
velocity bunching



$E(\text{gun}) = 120 \text{ MV/m}$

$Q = 1 \text{ nC}$

$R = 1 \text{ mm}$

$\Delta t = 11.65 \text{ ps}$

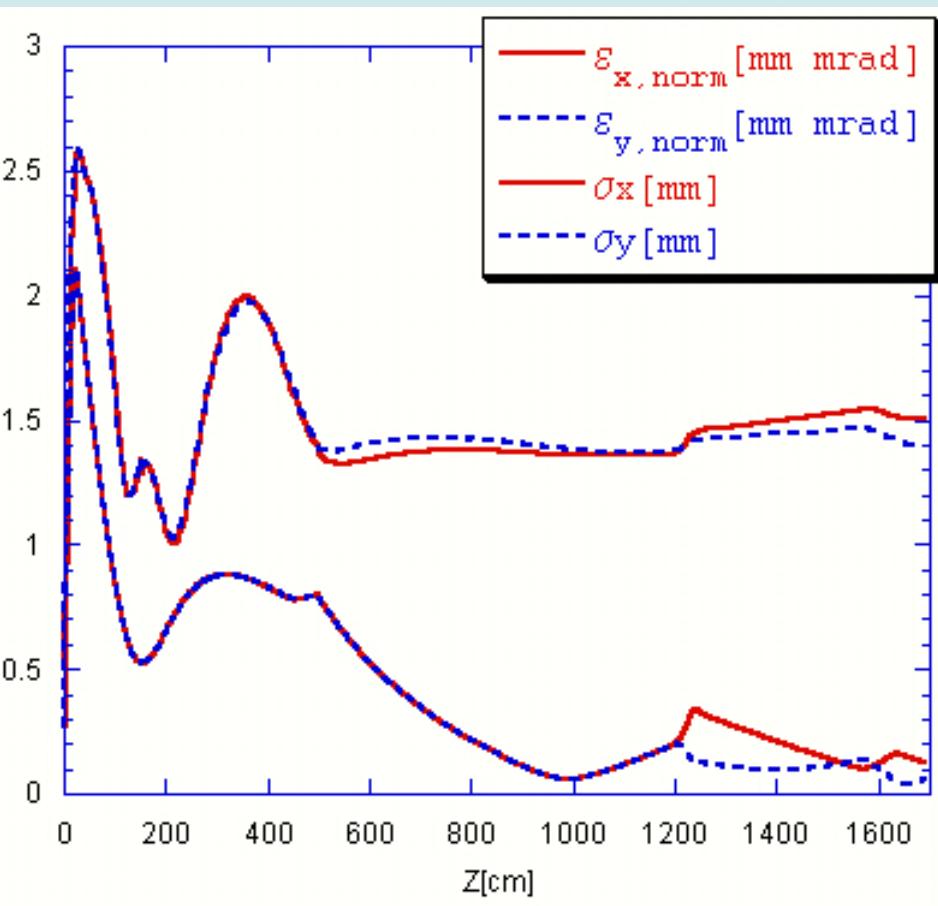
$\phi_{\text{inj}} = 33\text{deg}$

$B(\text{gun}) = 2730 \text{ G}$

$B(\text{I TRW}) = 650 \text{ G}$        $\phi = -83 \text{ deg}$

$B(\text{II TRW}) = 950 \text{ G}$       *on crest*

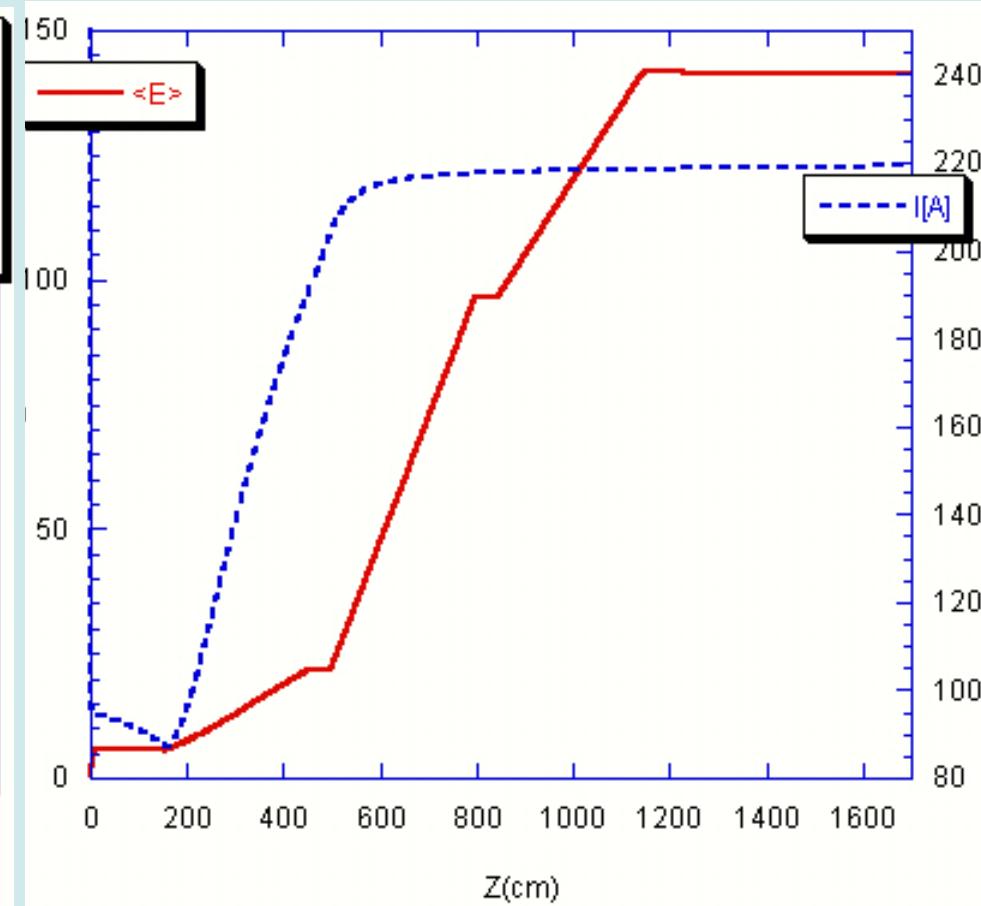
$B(\text{III TRW}) = 1000 \text{ G}$       *on crest*



$$\langle \varepsilon_x \rangle = 1.506 \mu\text{m}$$

$$\langle \varepsilon_y \rangle = 1.391 \mu\text{m}$$

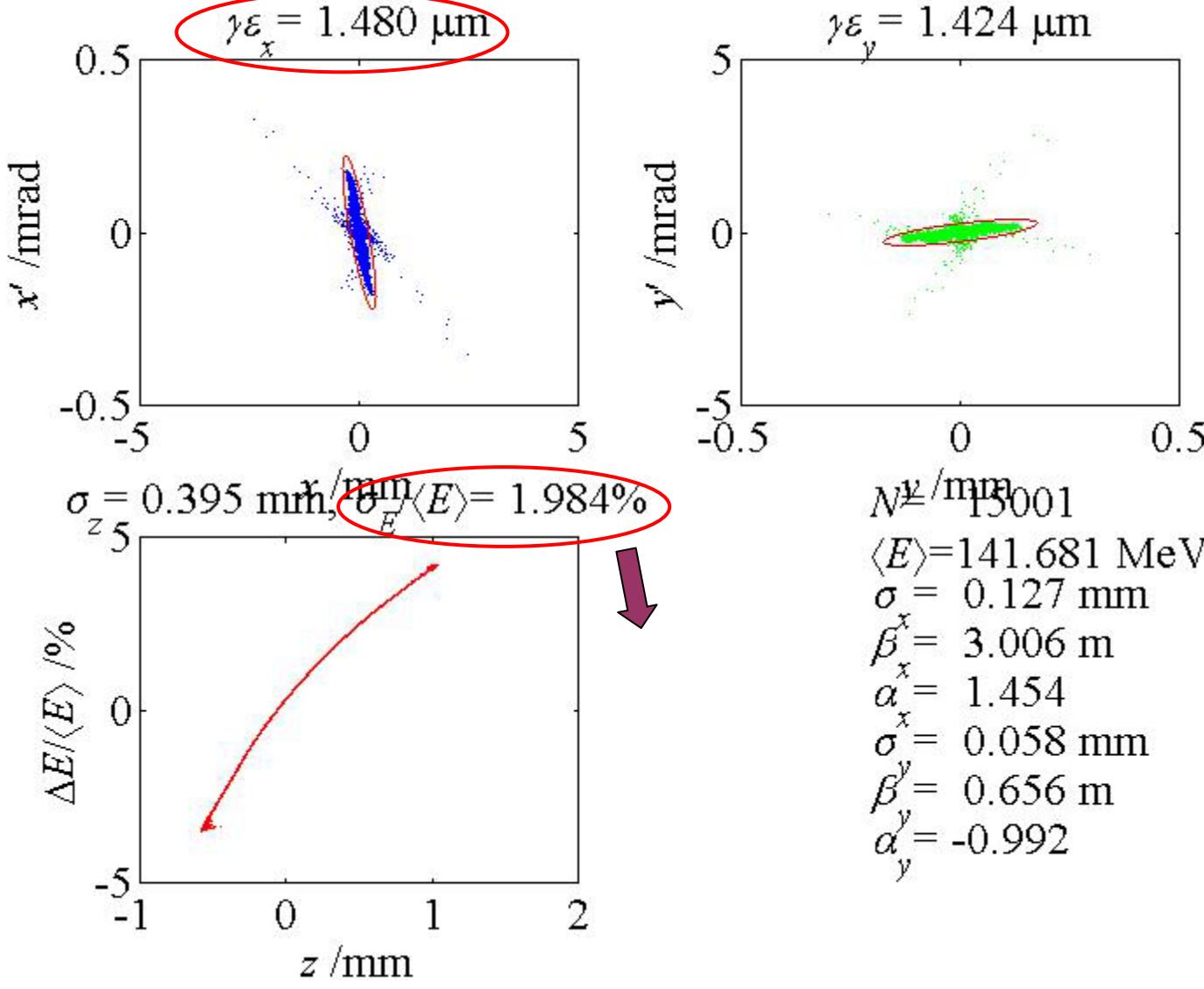
AT UNDULATOR ENTRANCE



$$I = 219 \text{ A}$$

$$\langle E \rangle = 141.6 \text{ MeV}$$

## Electron beam at undulator entrance

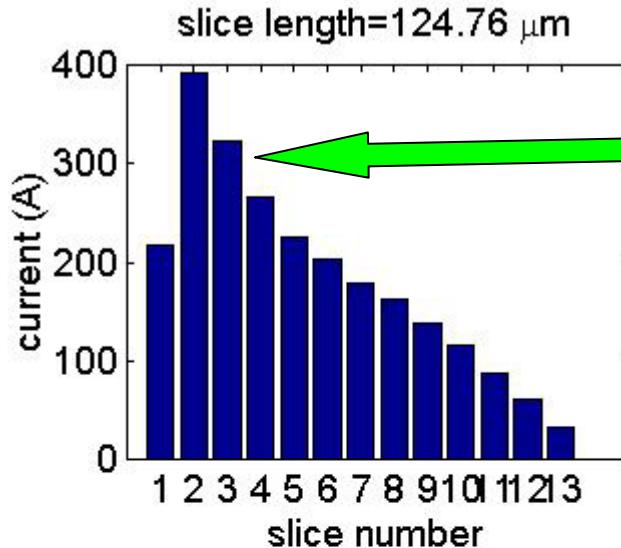
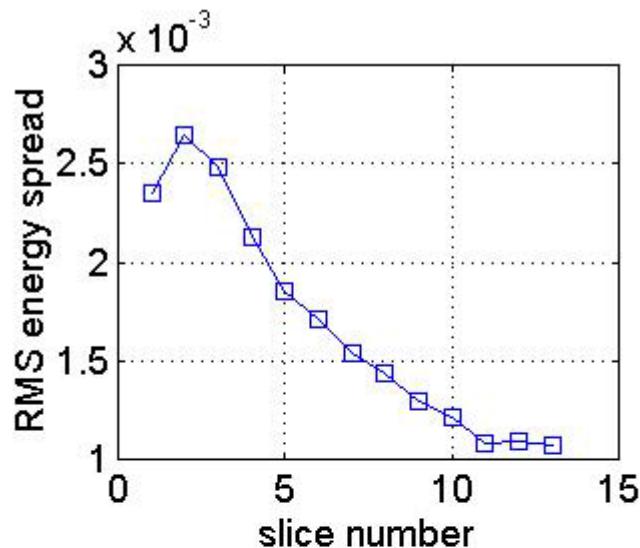


No attempt to minimize the energy spread  
(II and III TRW phase on crest)

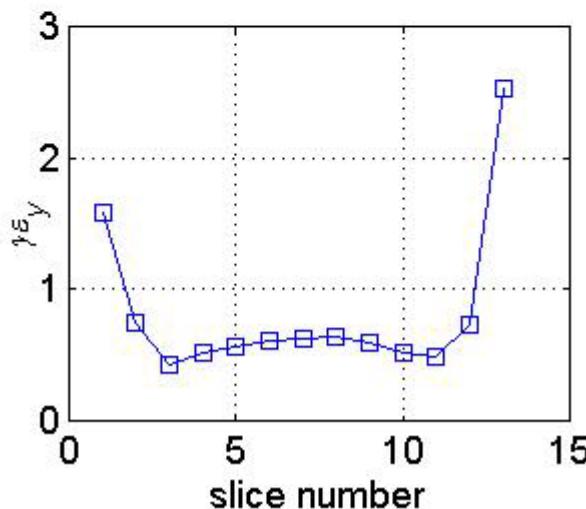
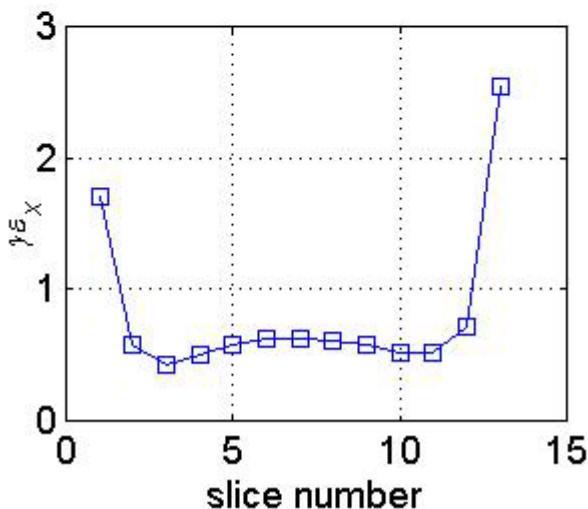
# Slice Analysis at undulator entrance

Very large slice current

$I_{slice} > 200A$   
~50% of beam



3<sup>rd</sup> slice:  
 $\varepsilon_n = 0.43 \mu m$   
 $I = 323 A$   
 $L_{sat} = 6.5 m$



Small  
slice emittance

## Conclusions for the RF compressor studies

- Parameters have been optimized for RF compression at ~155MeV and 3 TRW to have  $I \sim 200A$  @undulator entrance.
- The beam energy spread is ~2%, BUT the slice energy spread is small  
(in the range between  $1 \cdot 10^{-3}$  and  $3 \cdot 10^{-3}$ )
- Each slice has a LARGE current  
(~50% of the beam has  $I_{slice} > 200A$ !)



Every slice will saturate

it is also possible to select one particular slice

# Conclusions

- \* Optimized the working point :it is very close to previous one  
BUT now:  $\langle I_{slice} \rangle \sim 100A$  (instead of  $\sim 85A$ )
- \* The strategy has been to increase a bit the bunch charge while shortening the bunch length
- \* The gain is essentially in the calculated saturation length: it is reduced by  $\sim 15\%$ .

**Best experimental results at high charge:  
 $\varepsilon_n \approx 1.2$  mm mrad at  $Q=1$  nC, pulse length=9 psec FWHM,  
 $\varepsilon_n \approx 1.5$  mm mrad at  $Q=1.2$  nC**

## EXPERIMENTAL STUDIES OF PHOTOCATHODE RF GUN WITH LASER PULSE SHAPING

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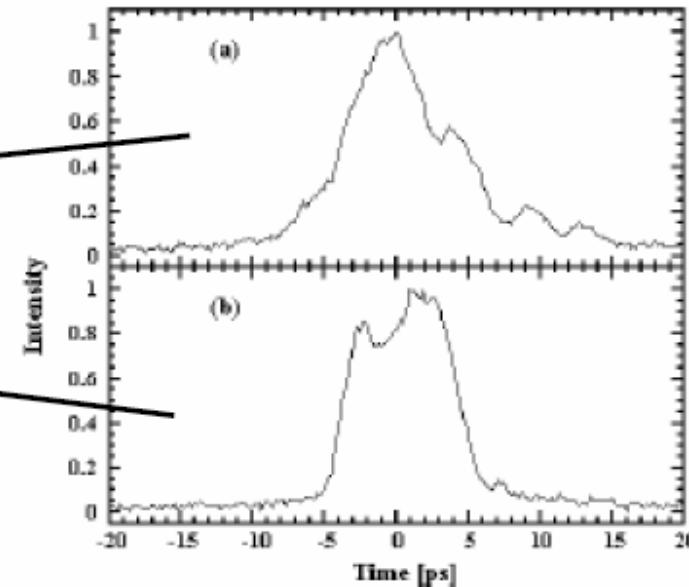
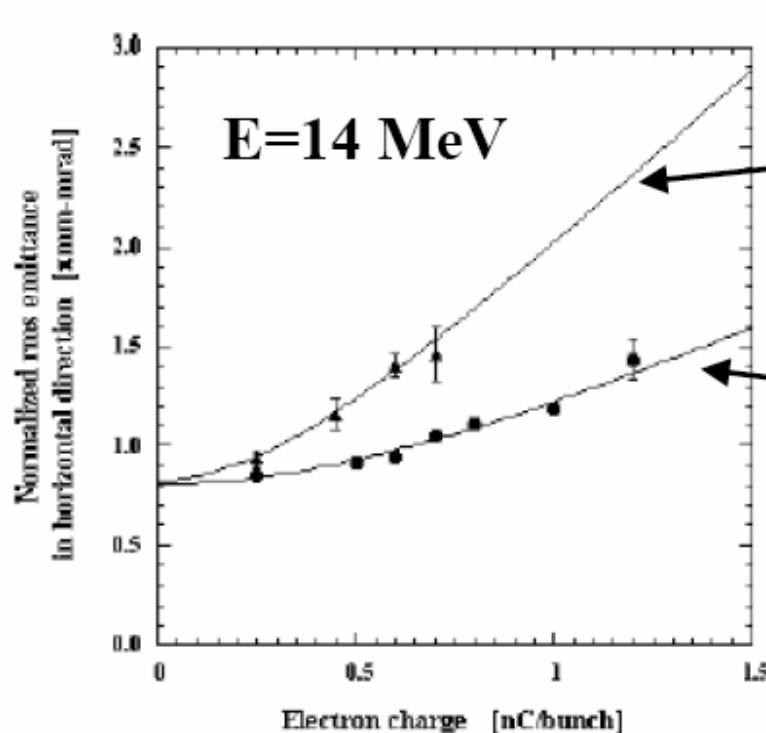


Figure 2: Temporal distributions of the Gaussian (a) and square (b) laser pulse shapes with a pulse length  $\approx 9$  ps FWHM.

## current vs beam density: scaling laws (JBR et al.)

$$\sigma_x'' + \frac{(\beta\gamma)'}{\beta\gamma} \sigma_x' + k_{sol}\sigma_x -$$

$$\frac{2I_{slice}(\sigma_x / \sigma_z)}{I_0(\beta\gamma)^3 \sigma_x} = 0$$

$$= k_{sc} \cdot \sigma_x$$

beamline  
unchanged  
if  $k_{sc}$  constant

$$k_{sc} \propto \frac{Q}{V} \propto \frac{Q}{\sigma_z} \cdot \frac{1}{\sigma_x^2} \cdot g\left(\frac{\sigma_x}{\sigma_z}\right) \equiv \text{const.}$$

Constant aspect ratio

$$1. \quad \sigma_z = \text{const.} \Rightarrow \sigma_x \propto \sqrt{Q} \Rightarrow I \propto Q$$

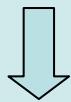
$$2. \quad \frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$

$$3. \quad Q = \text{const.} \Rightarrow \sigma_x \propto \frac{1}{\sqrt{\sigma_z}} \Rightarrow I \propto \frac{1}{\sigma_z}$$

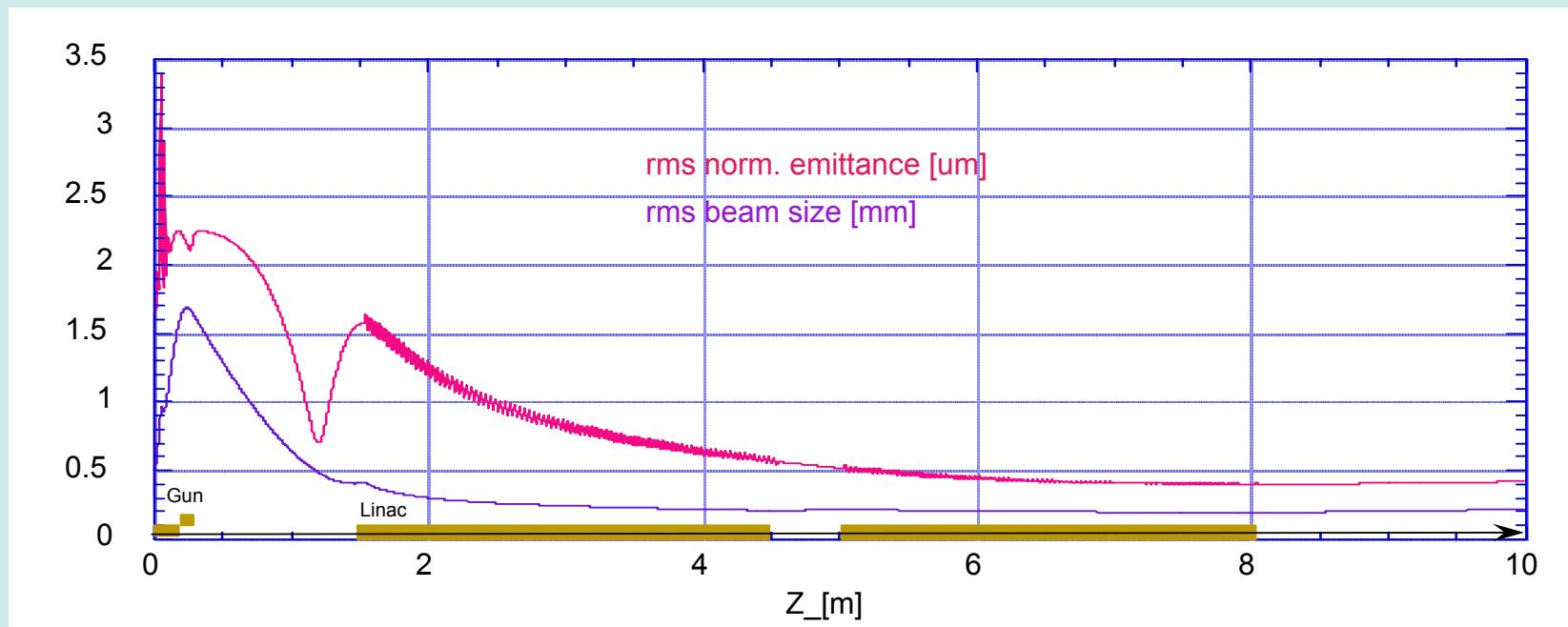
$$\sigma_x \propto \sigma_z \Rightarrow$$

$$Q \propto \sigma_z^3 \Rightarrow I \propto \sigma_z^2$$

Maintenance of emittance compensation requires  
keeping the beam plasma frequency constant



Beam density constant



$$\frac{Q}{\sigma_z} = \text{const.} \Rightarrow \sigma_x \propto \sqrt{\frac{Q}{\sigma_z}}$$

## SUMMARY OF RESULTS

Q (nC)	$\tau$ = FWHM pulse duration (psec)*	Beam fraction with $\geq 100$ A	Projected rms norm. Emittance (mm- mrad)	Max. Slice rms norm. emittance (mm- mrad)**	Total RMS energy spread	Max. Slice RMS energy spread**
1	11.7	0 % (max. curr. Slice ~92 A) (average bunch current ~86A)	0.6	0.5	2e-3	5e-4
1	10	23% (max. curr. Slice ~102 A) (average bunch current ~94A)	0.67	0.6	1.62e-3	5e-4
1.1	10	54 % (max. curr. Slice~110 A) (average bunch current ~102A)	0.75	0.71	1.65e-3	5.2 e-4
1.2	10	60 % (max. curr. Slice ~120 A) (average bunch current ~110A)	0.81	0.79	1.66e-3	5.4e-4
1	9	50% (max. curr. Slice ~110 A) (average bunch current ~101A)	0.8	0.73	1.67e-3	4.2e-4
1.1	9	58 % (max.curr Slice~120 A) (average bunch current ~110A)	0.86	0.82	1.67e-3	4.3e-4

\* Rise time=1 psec, \*\* 85% beam

Slice length  $\cong 300$   $\mu$ m

**1.1 nC, 10 psec meet the requirement on current  
with the minimum emittance**