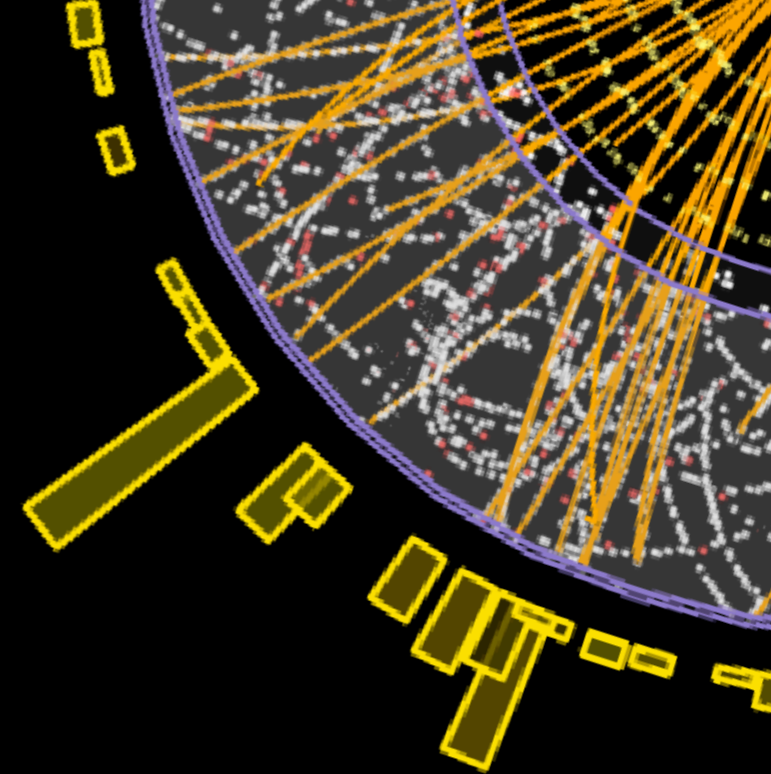


Valerio Ippolito & Livia Soffi

INFN Sezione di Roma / Sapienza Università di Roma



THE PRECISION FRONTIER AT THE LHC

status and perspective of SM precision physics



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The Big Picture

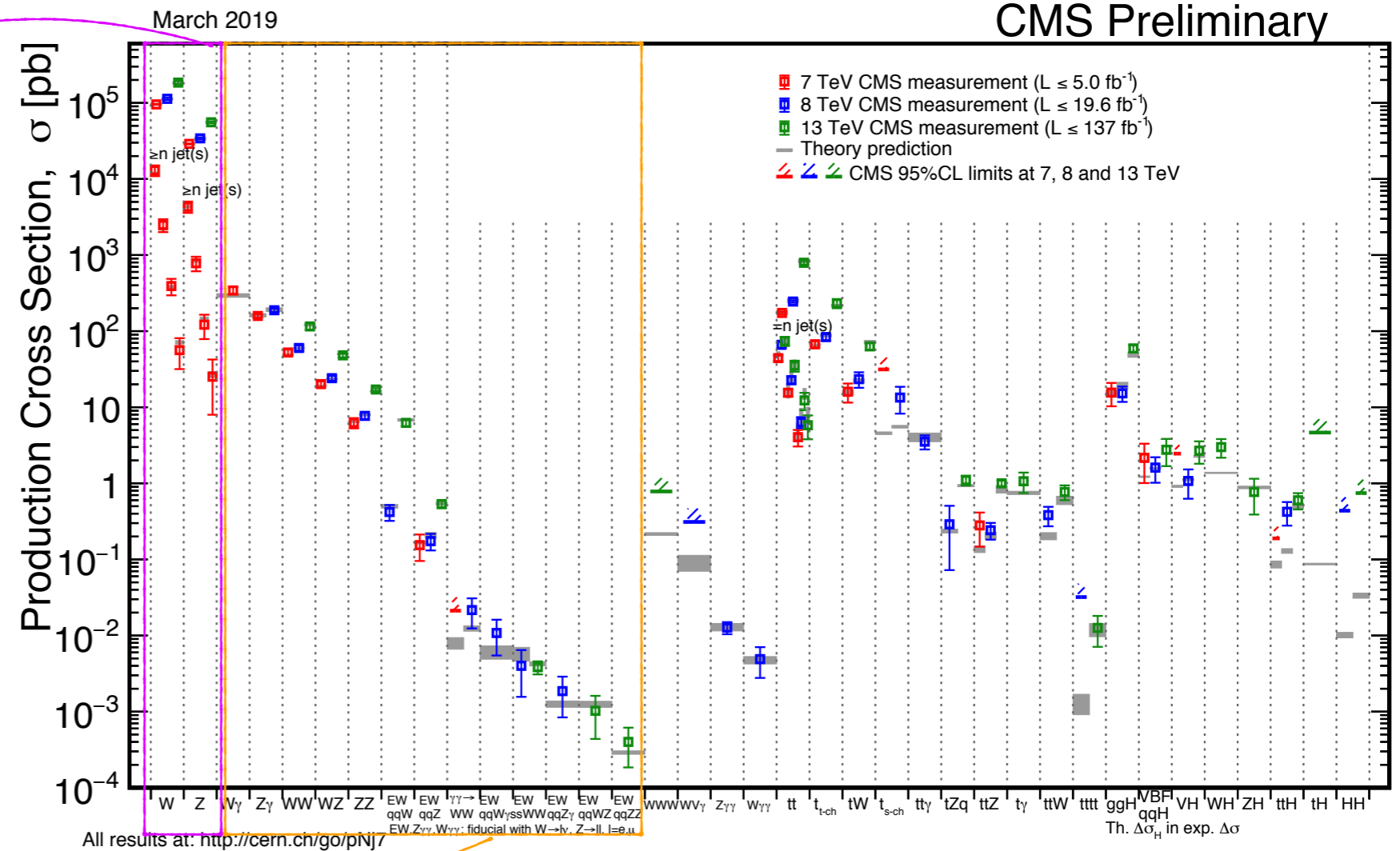
- **ATLAS and CMS** precisely measure **SM processes involving gauge bosons, top quarks and Higgs boson**

Single Boson production

- High xsecs
- Measurements of SM *EWK parameters*

DiBoson/VBS/VBF

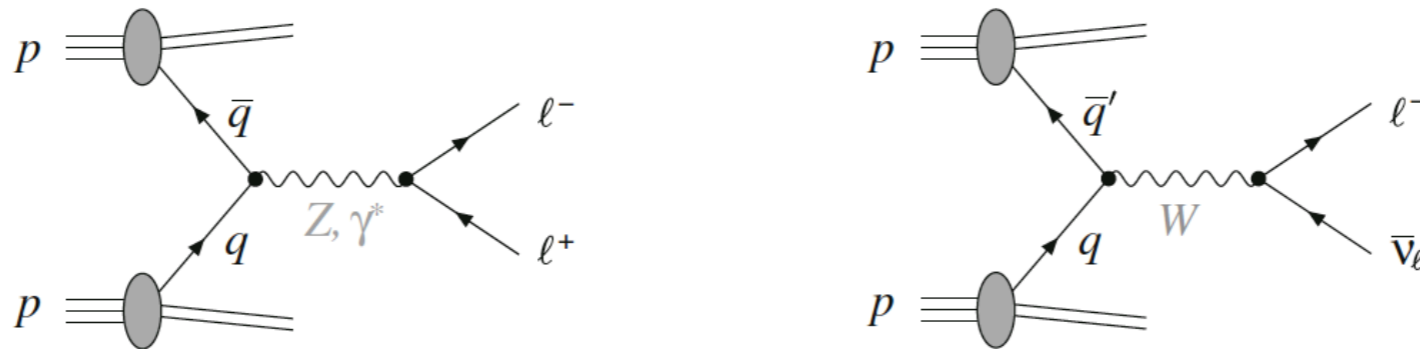
- Era of *precision measurements*
- First *Observation at 13 TeV*



- Multiple **interdependent parameters** measured separately
- Very high cross-section processes used to **calibrate our objects/MC**
- Complementarity **Beyond-the-standard-model searches:** deviations from SM
- Many opportunities at **Run3 and HL LHC**

W/Z production via / DY processes

- Observables sensitive to both **QCD and EW sectors** of the Standard Model
- Theory cross sections computed up to **NNLO in QCD and NLO in EW**
- Total and differential cross-sections sensitive to the **proton structure(PDFs)**
- Purely **leptonic decays** are a very clean experimental signature



In the SM, 3 parameters (g, g', v) defines the EW sector connected to observables:

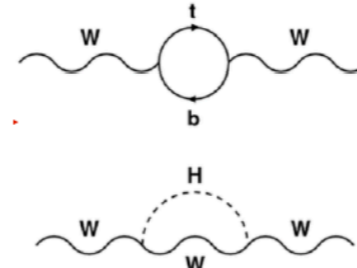
$$M_W = \frac{v|g|}{2}, \quad M_Z = \frac{v\sqrt{g^2 + g'^2}}{2}, \quad \cos\theta_W = \frac{m_W}{m_Z}$$

- **Mass of the W (Z)** measured at LHC and Tevatron (LEP) with millions of events
- Weak **mixing angle θ_W** from precision Z measurements

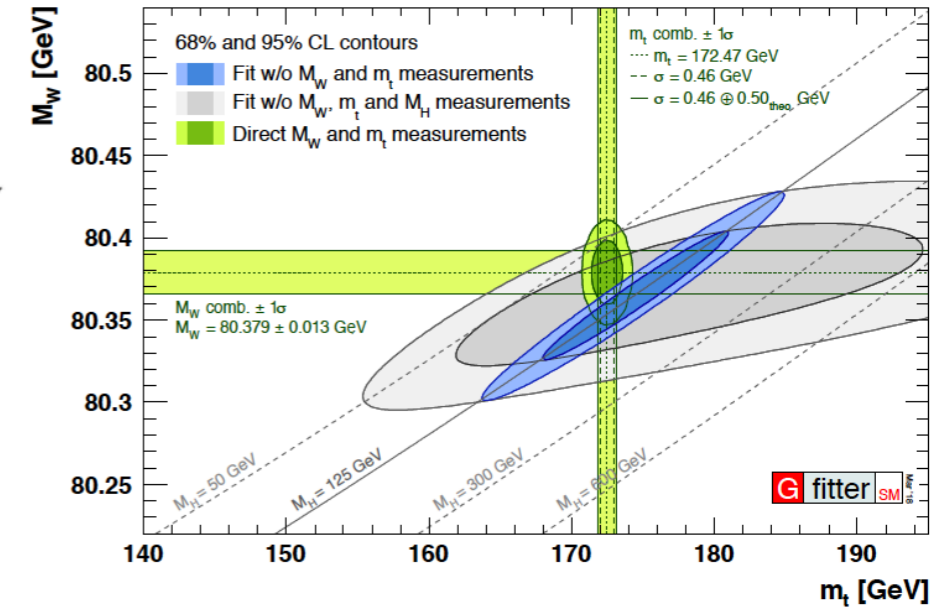
M_W measurement at LHC I

- The relation M_W , m_t , and M_H provides stringent test of the SM and is sensitive to NP

$$m_W^2 \left(1 - \frac{m_W^2}{m_Z^2} \right) = \frac{\pi\alpha}{\sqrt{2}G_\mu} (1 + \Delta r)$$



$$\Delta m_W^{theory} = 8 \text{ MeV} < \Delta m_W^{exp} = 15 \text{ MeV}$$

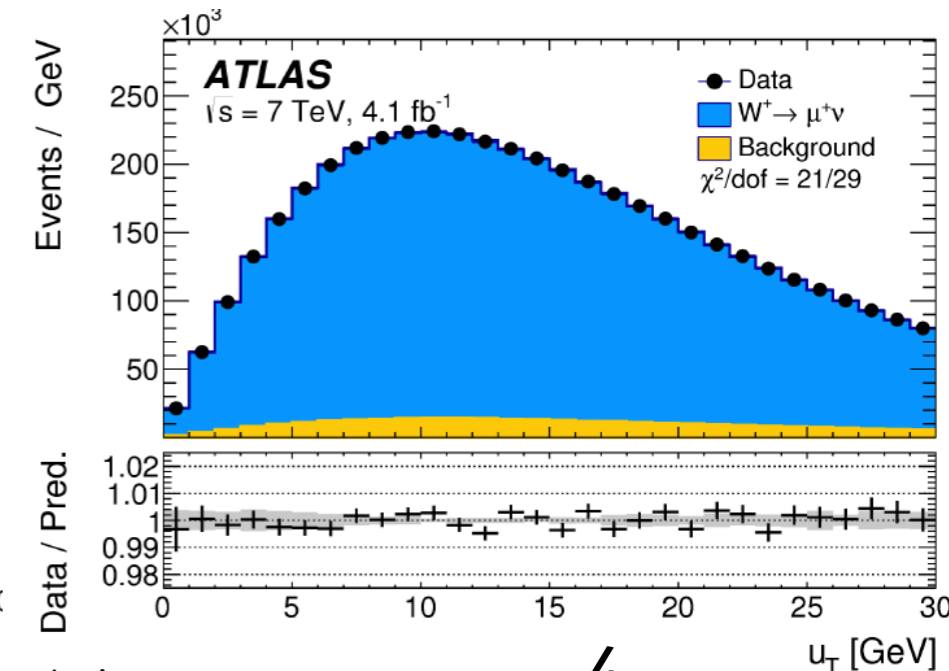
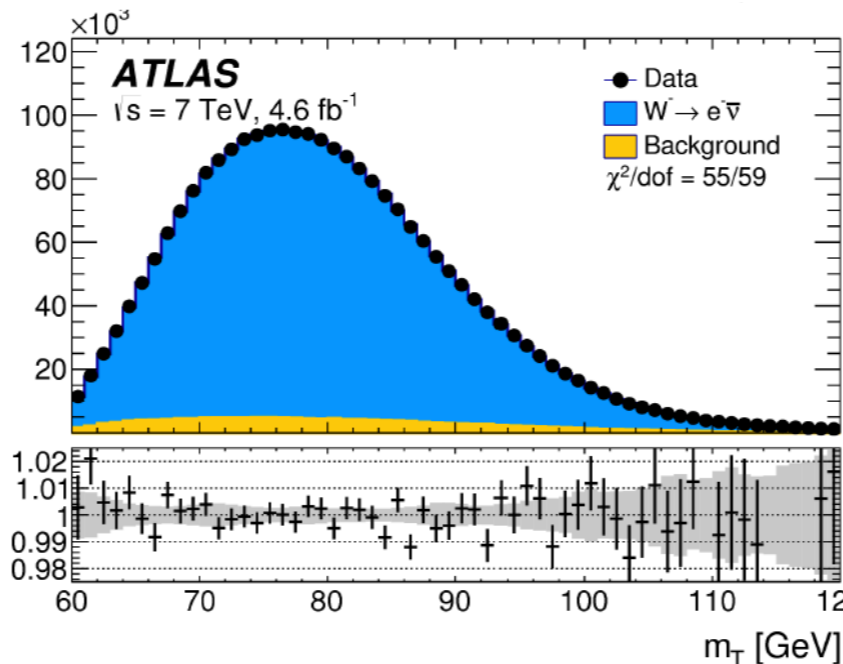
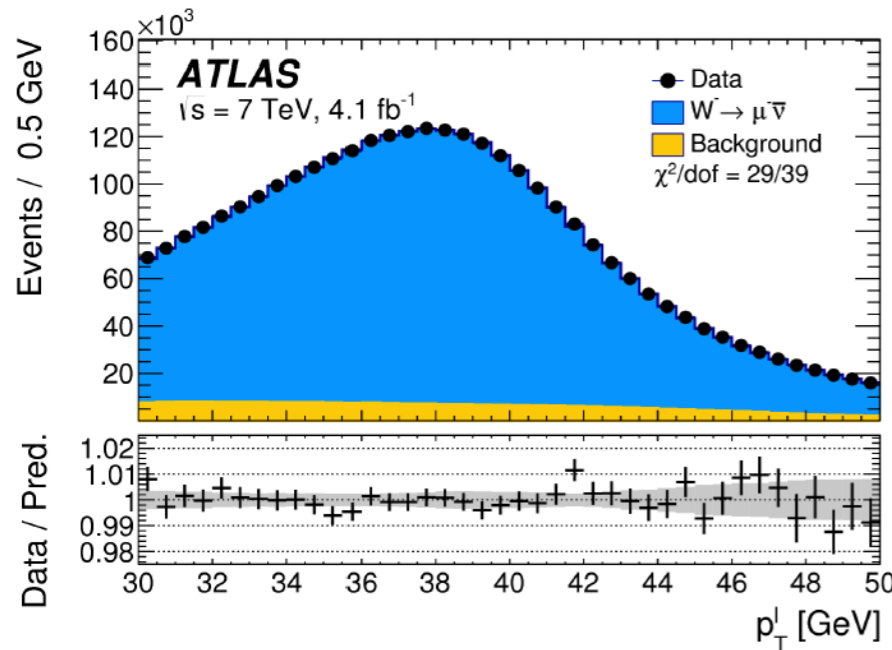


- Current **ATLAS measurement** (4.7 fb^{-1} data @ 7 TeV) of m_W performed using **1D $p_{T\ell}$, $p_{T\text{miss}}$ and m_T distributions**

$$\vec{p}_T^{\text{miss}} = -(\vec{p}_T^\ell + \vec{u}_T) \quad m_T = \sqrt{2p_T^\ell p_T^{\text{miss}} (1 - \cos \Delta\phi)}$$

- u_T being the recoil provides an estimate of the W boson p_T

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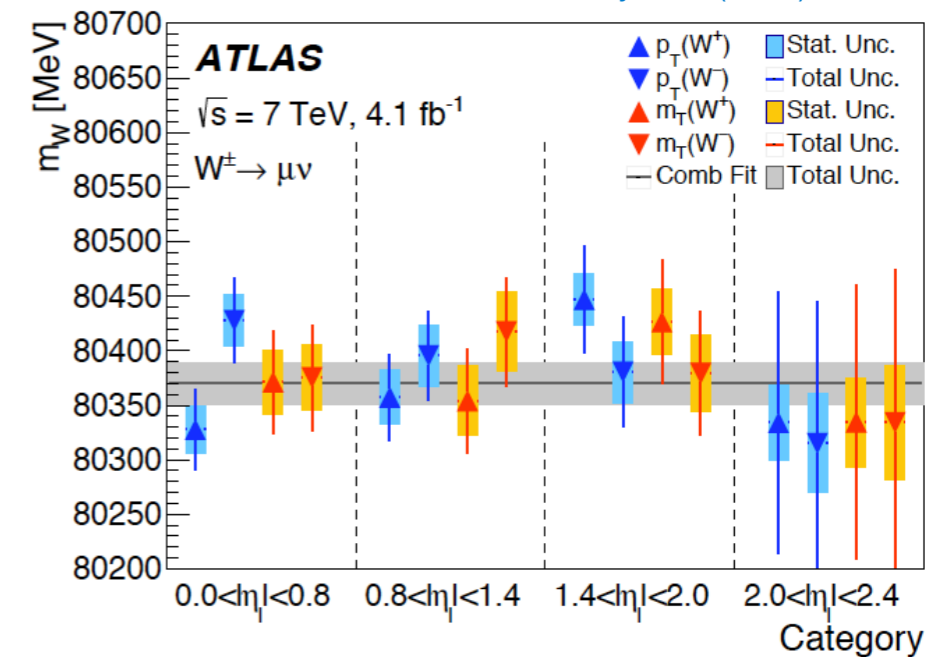
M_W measurement at LHC II

$$m_W = 80370 \pm 7(\text{stat.}) \pm 11(\text{exp.}) \pm 8.3(\text{QCD}) \pm 5.5(\text{EWK}) \pm 9.2(\text{PDF}) \text{ MeV}$$

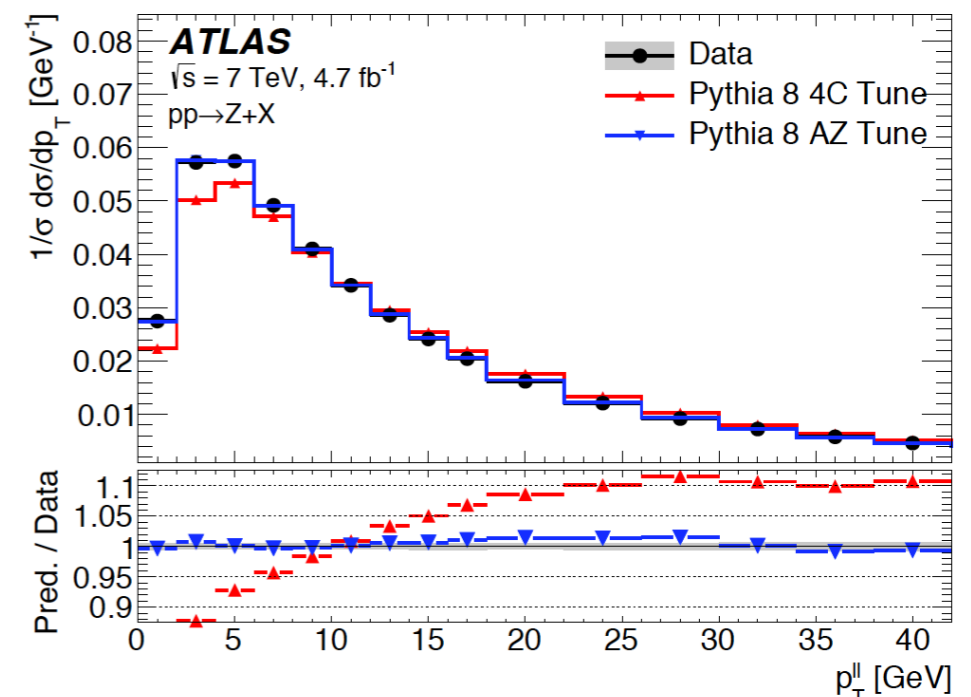
- **PDFs** determine the W rapidity spectrum and lepton decay angles through W polarization
- **PDFs** large role at the LHC w.r.t Tevatron: pp need sea quarks (25% vs 5% second generation quark)
- W p_T in relevant region driven by large logarithms in **QCD calculation**
- Current measurement **using Z p_T to constrain W,**

- Better direct measurement w/ low pileup runs
- Better understanding of heavy-favour PDFs

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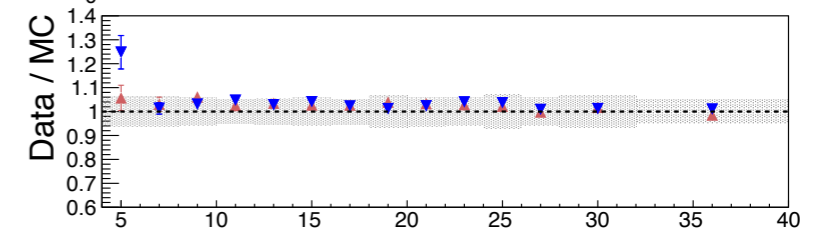
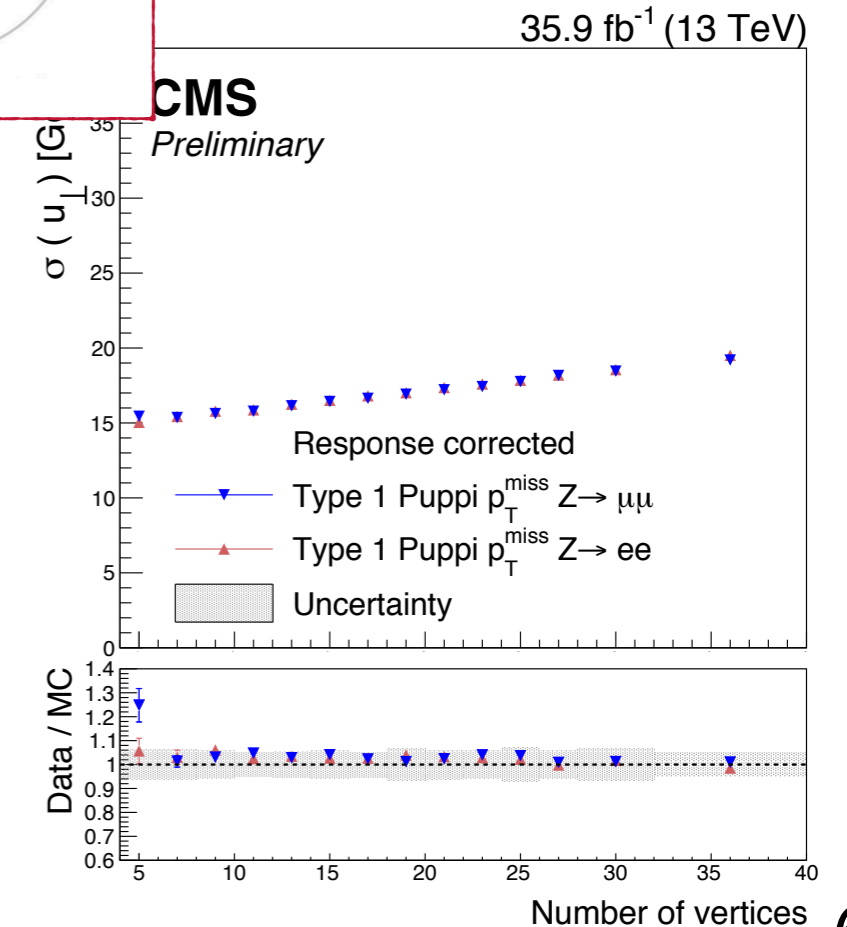
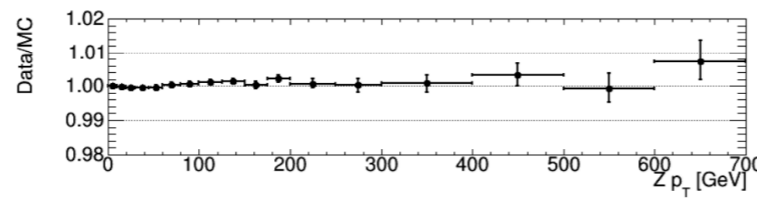
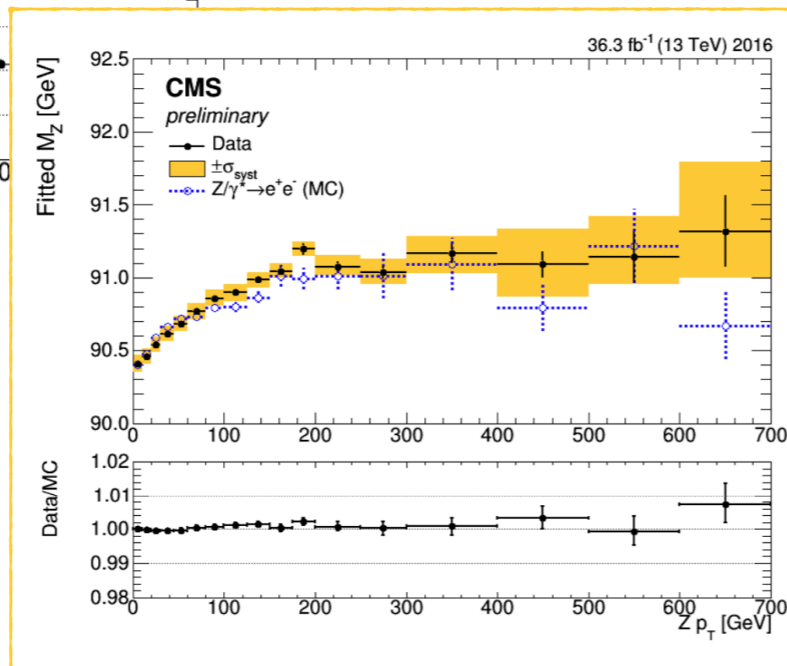
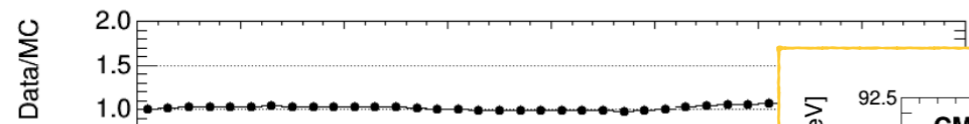
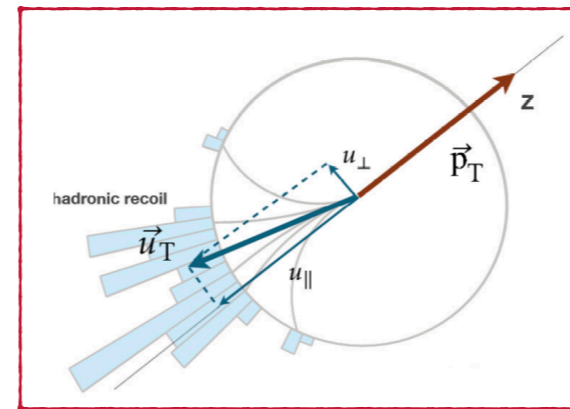
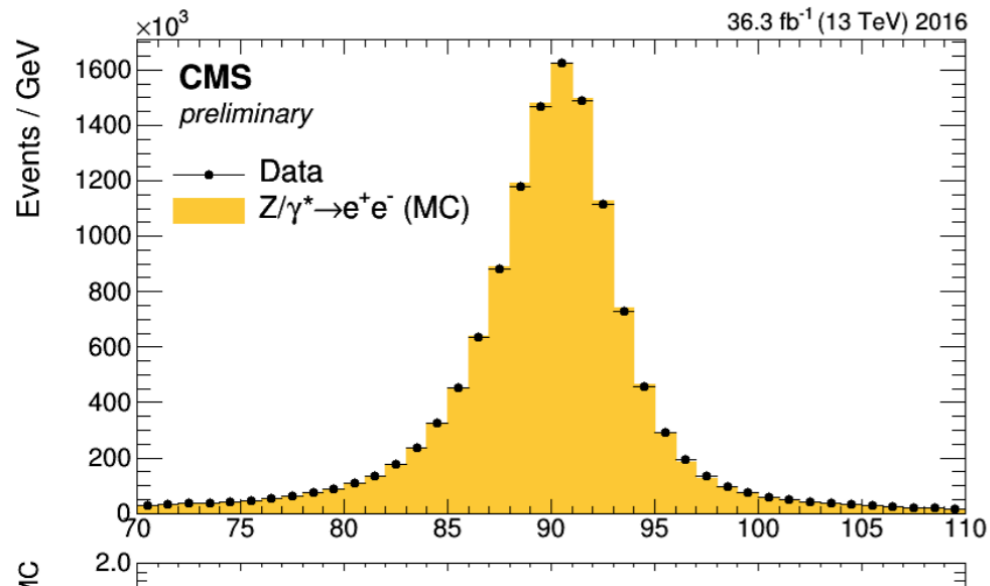


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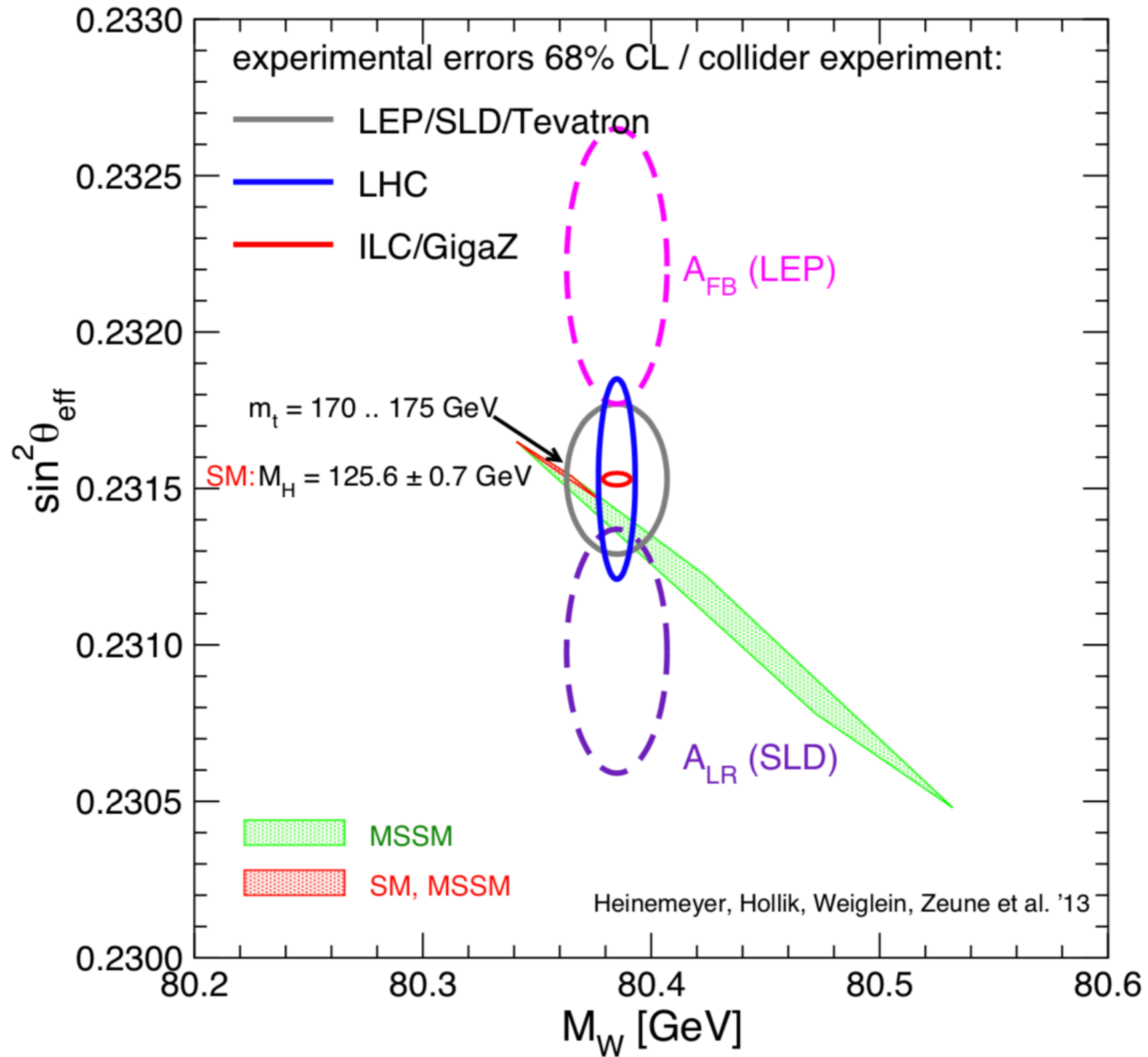


Z boson: the Standard Candle

- **Energy calibrations** , **lepton-selection** efficiencies and **missing energy calibration** of detector response impacts both precision measurement and searches
- **Z(II)+jets** event sample allows several validation and consistency tests of **detector performances**



THE CASE OF $\sin^2\theta_{\text{eff}}$

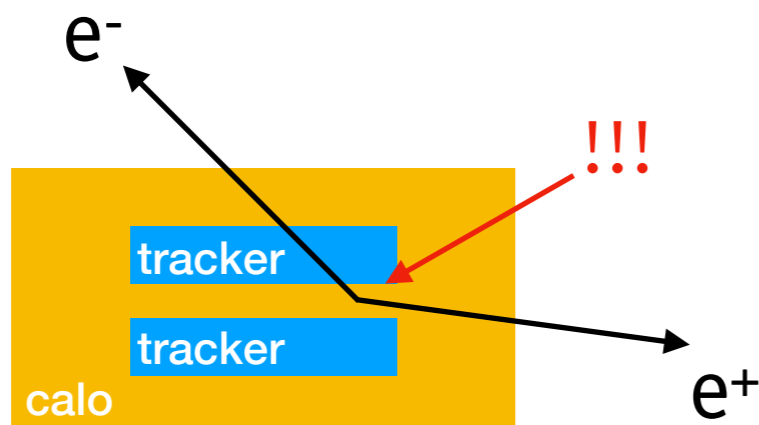


ATLAS, CMS OR LHCb?

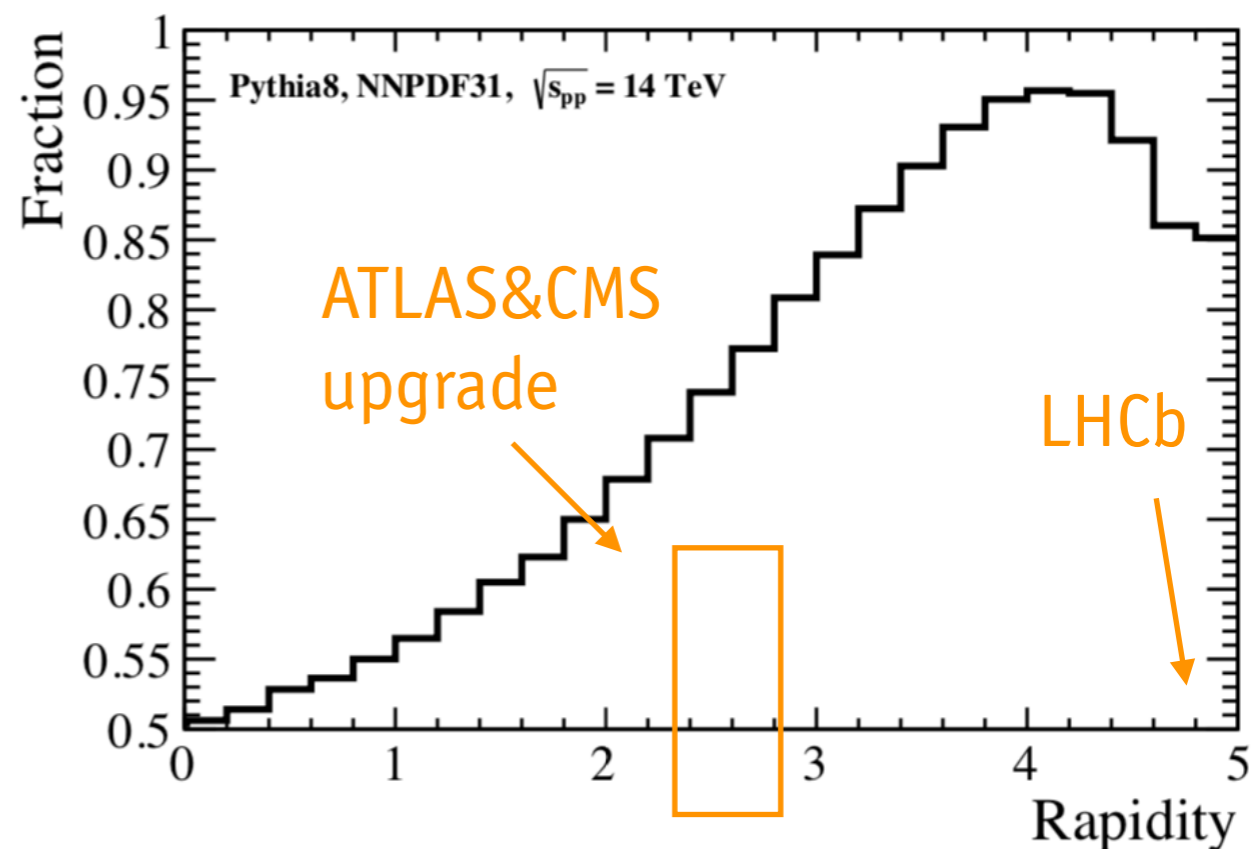
$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

what's the qbar direction?

- easy at LEP
- LHC: only if Z is boosted
 - forward region
 - challenge for lepton ID!



$$q\bar{q} \rightarrow Z/\gamma^* \rightarrow \ell^+\ell^-$$

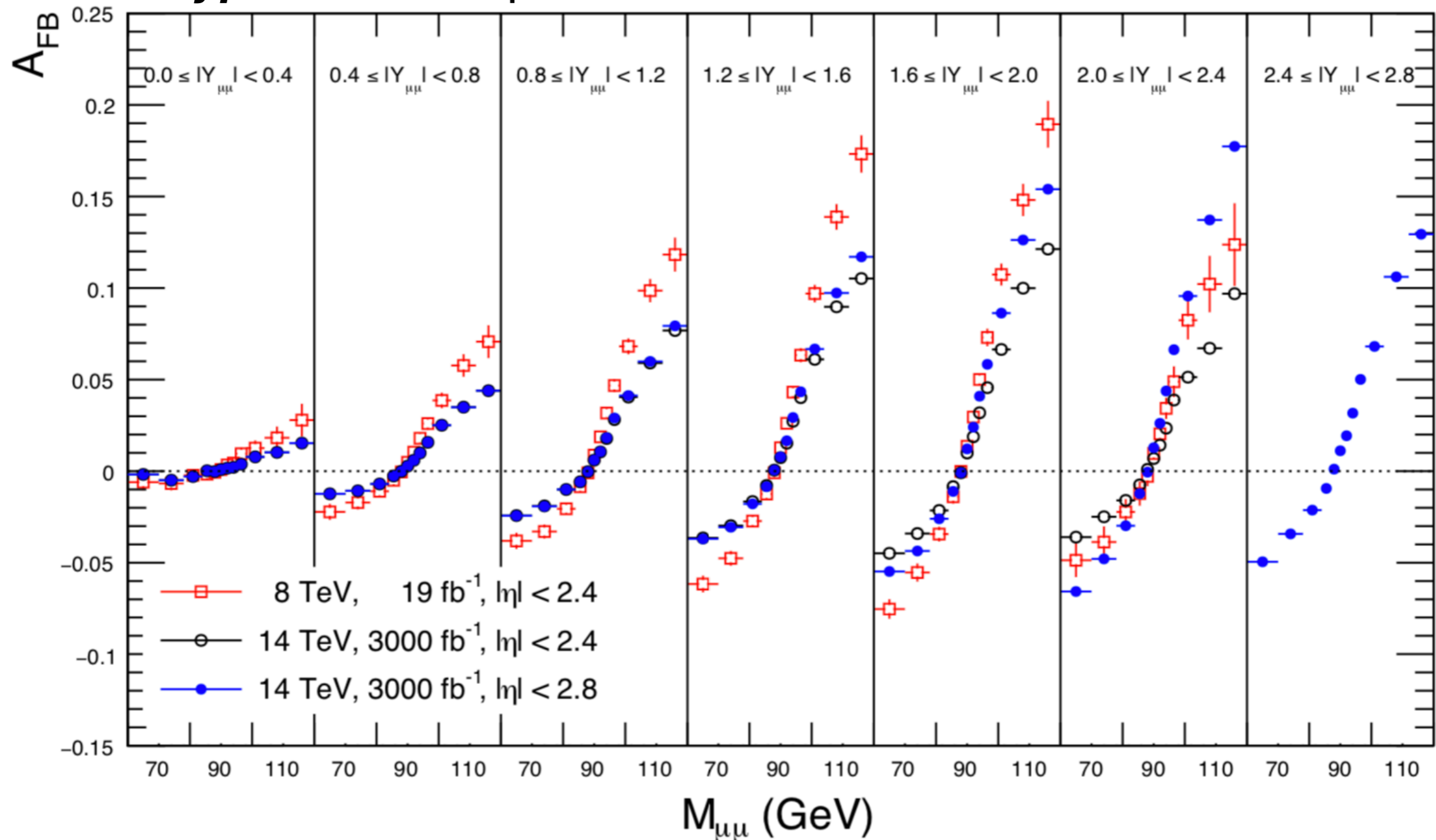


THE ASYMMETRY

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

- m_{ll} tails vs Z pole are complementary
- can simultaneously constrain PDFs and measure A_{FB}

A *typical* LHC experiment



Future Prospects in Precision Physics at HL LHC

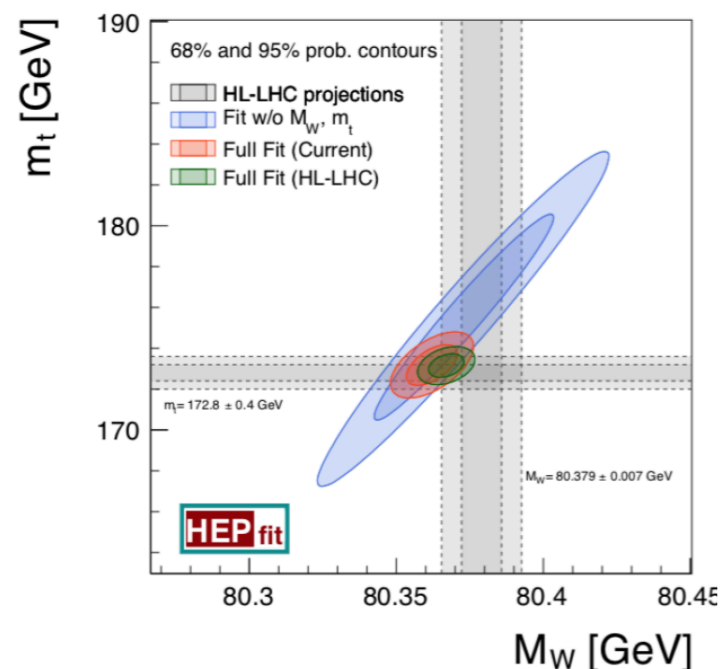
HL-LHC: @14 TeV w/ Inst. Lumi $7.2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$, $\langle \mu \rangle \sim 200$

New detectors and methods \longleftrightarrow Improved statistics and systematics

- ML techniques, New **Triggers**, **Timing Detectors**
- Extended **acceptance** and forward topologies
- Experimental unc. at the level of statistical uncertainties
- Reduced **theory and PDF** uncertainties

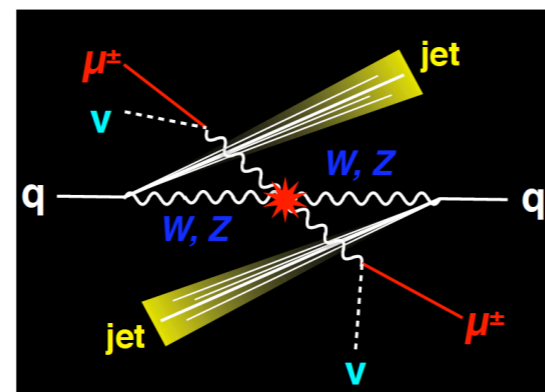
Global EW fit

- M_W , m_t , and M_H
- θ_W

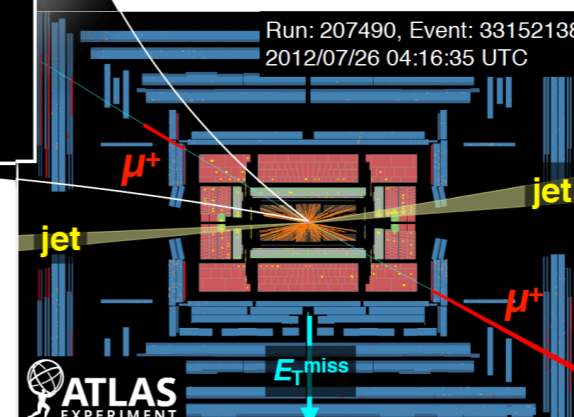


Multiboson processes

- VBF
- VBS
- Triple and quartic couplings
- Probe high dim operators and NP

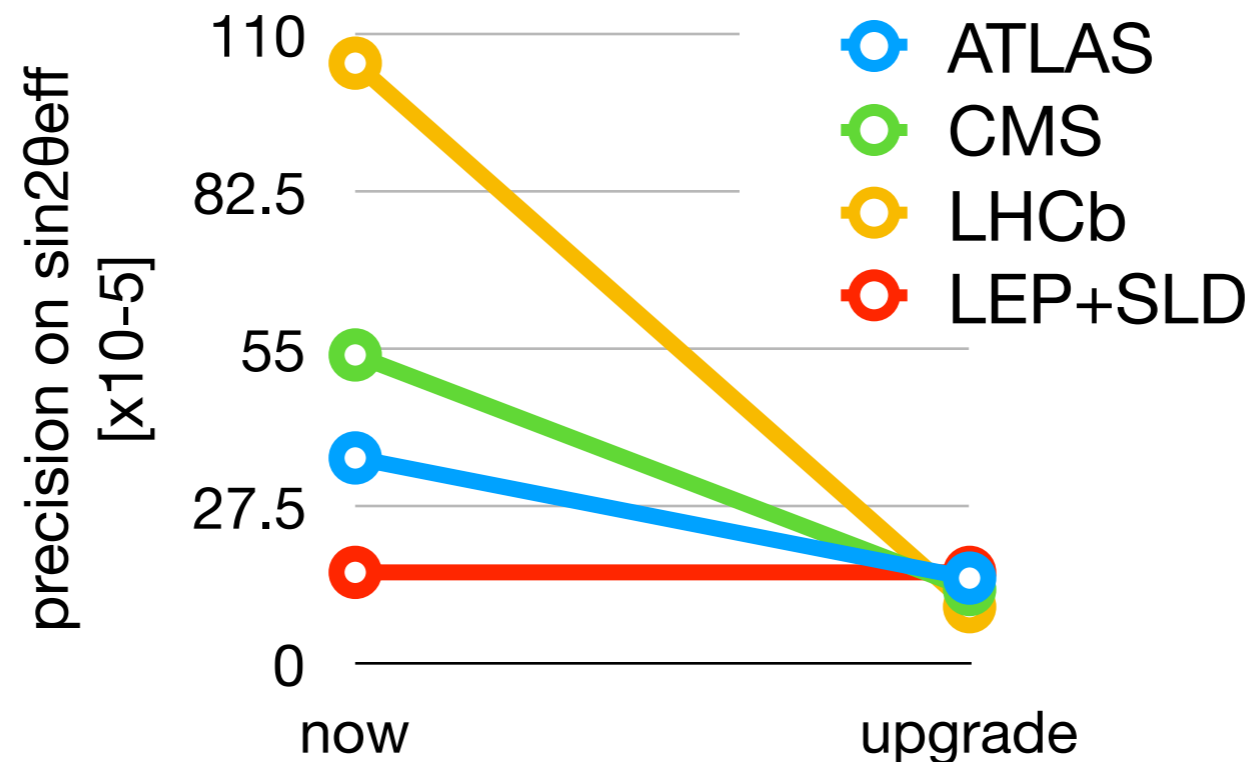


<http://indico.cern.ch/e/687651>



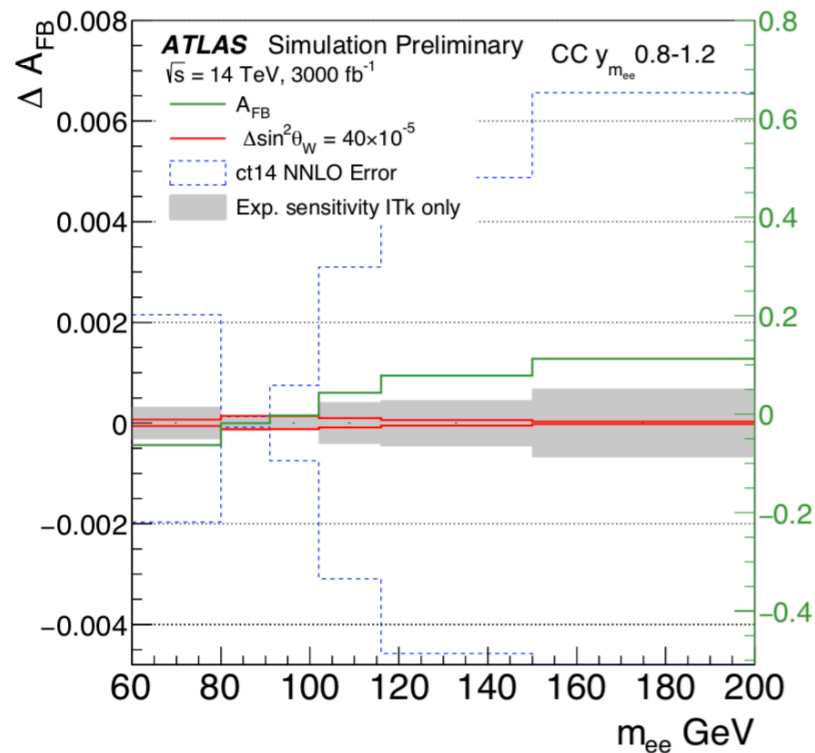
THE FUTURE OF $\sin^2\theta_{\text{eff}}$

- planned ATLAS/CMS eta extension improves**
 stats gets 30% better, PDFs 20% better
- LHCb Upgrade II can beat the LEP+SLD combo**
 300 fb⁻¹ and fully-software trigger (lepton (p_{T1}, p_{T2}) > (20, 5) GeV)
- constrain PDF uncertainties with N-differential DY?**
 $m_{ll}, p_T \dots$

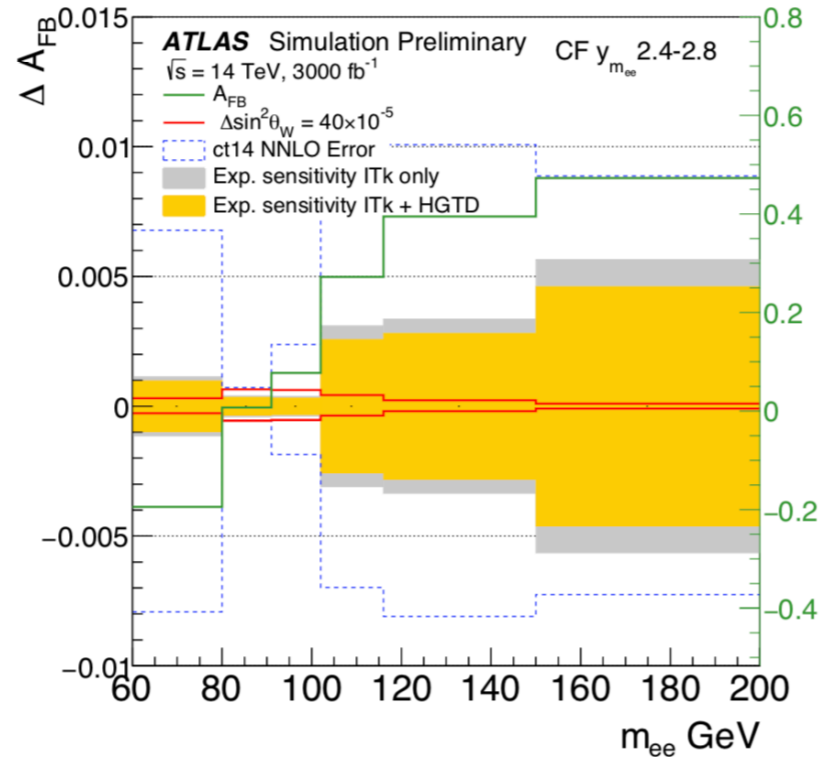


WHAT IF WE ADD A TIMING DETECTOR?

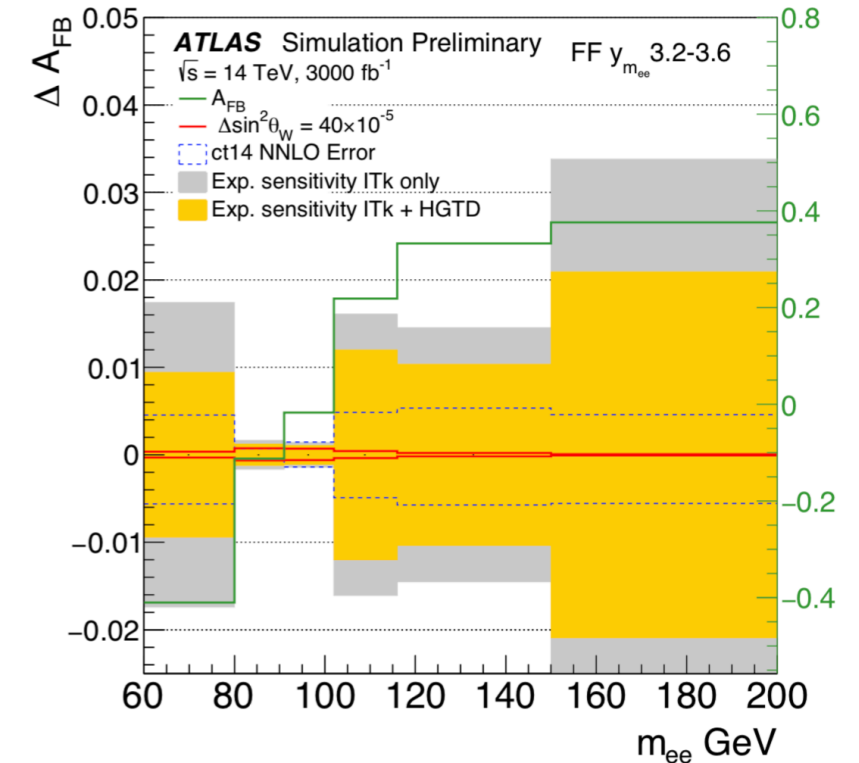
two central electrons



one central, one forward

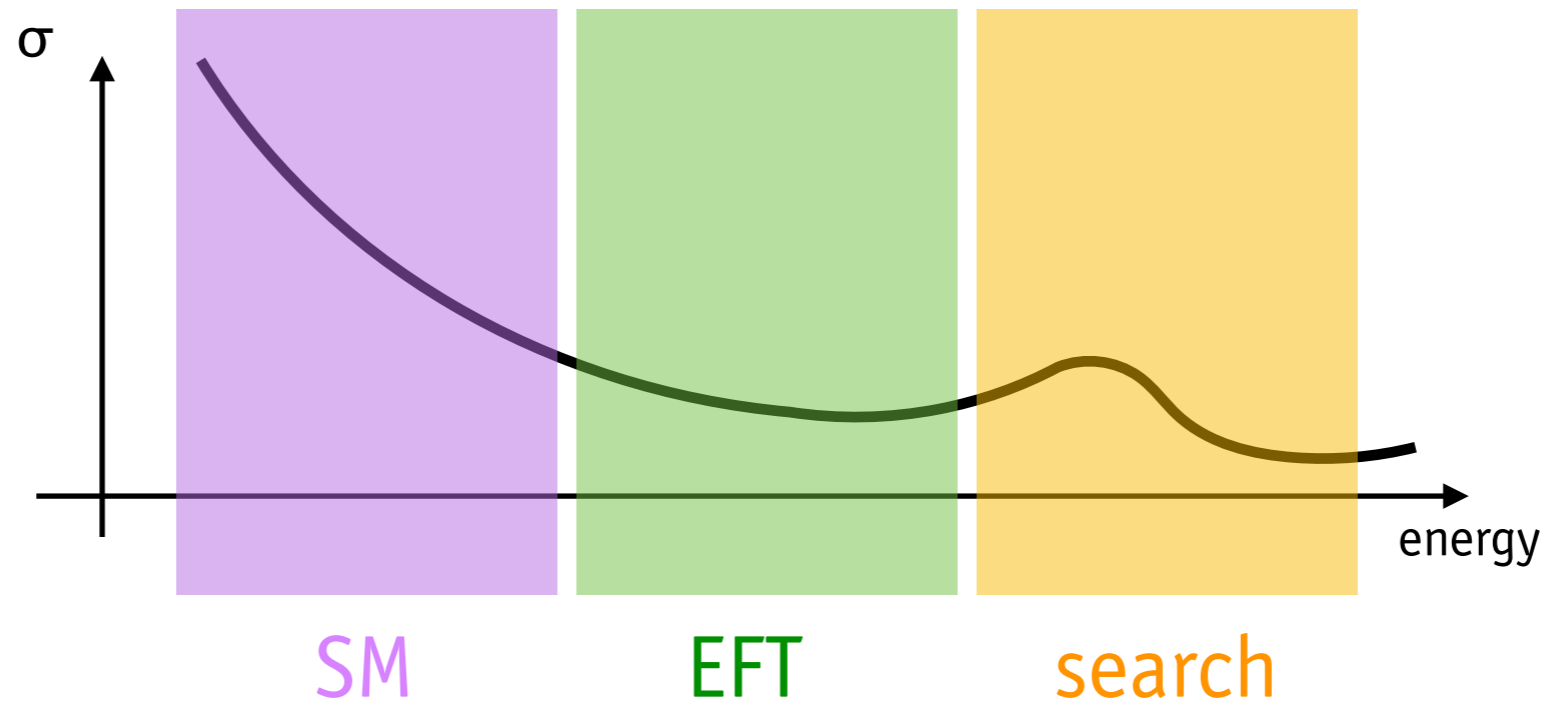


two forward electrons



- to suppress pile-up, measure when (aka where) jets are produced
 - reject forward jets which look like electrons: 20% better sensitivity
- combined precision on $\sin^2(\theta_{\text{eff}})$: $(18 \pm 16_{[\text{PDF}] \pm 9_{[\text{exp}]}}) \times 10^{-5}$
 - more precise than all single-experiment result so far

LHC VS LEP



experiment	energy	what	how precisely
LEP-I	mZ	Z properties	‰
LEP-II	from diboson threshold to 208 GeV	off-shell Z properties, trilinear gauge interactions	%
LHC	13 TeV COM	H couplings	10% ?

HOW? OBLIQUE PARAMETERS

- Z-pole observables
$$-\frac{\hat{S}}{4m_W^2} (H^\dagger \tau^a H) W_{\mu\nu}^a B^{\mu\nu}$$
 - LEP: ~ 100 GeV, %-% accuracy
 - LHC: ~ 1000 GeV, 10% accuracy
 - new physics not enhanced by energy

- off-Z-pole observable
$$-\frac{Y}{4m_W^2} \left(\partial_\rho B_{\mu\nu} \right)^2$$
 - LEP: ~ 100 GeV, %-% accuracy
 - LHC: ~ 1000 GeV, 10% accuracy
 - new physics enhanced by $(E_{\text{LHC}}/E_{\text{LEP}})^2 \sim 100$

can then re-interpret within simplified models of new physics
 → [HepData](#) / [Rivet](#) routines for differential measurements are important...

WHY DRELL-YAN?

strategy: extend the SM lagrangian with dimension-6 operators and measure Drell-Yan processes

$$-\frac{W}{4m_W^2} \left(D_\rho W_{\mu\nu}^a \right)^2$$

$$-\frac{Y}{4m_W^2} \left(\partial_\rho B_{\mu\nu} \right)^2$$

neutral and charged Drell-Yan propagators

$$t = s/c = \sin(\theta_w)/\cos(\theta_w)$$

Z boson $P_N =$

$$\frac{1}{q^2} - \frac{t^2 W + Y}{m_Z^2} \frac{t \left((Y + \hat{T}) c^2 + s^2 W - \hat{S} \right)}{(c^2 - s^2)(q^2 - m_Z^2)} + \frac{t(Y - W)}{m_Z^2} \frac{1 + T - W - t^2 Y}{q^2 - m_Z^2} - \frac{t^2 Y + W}{m_Z^2}$$

on-pole: LEP wins

off-pole: LHC can surpass LEP

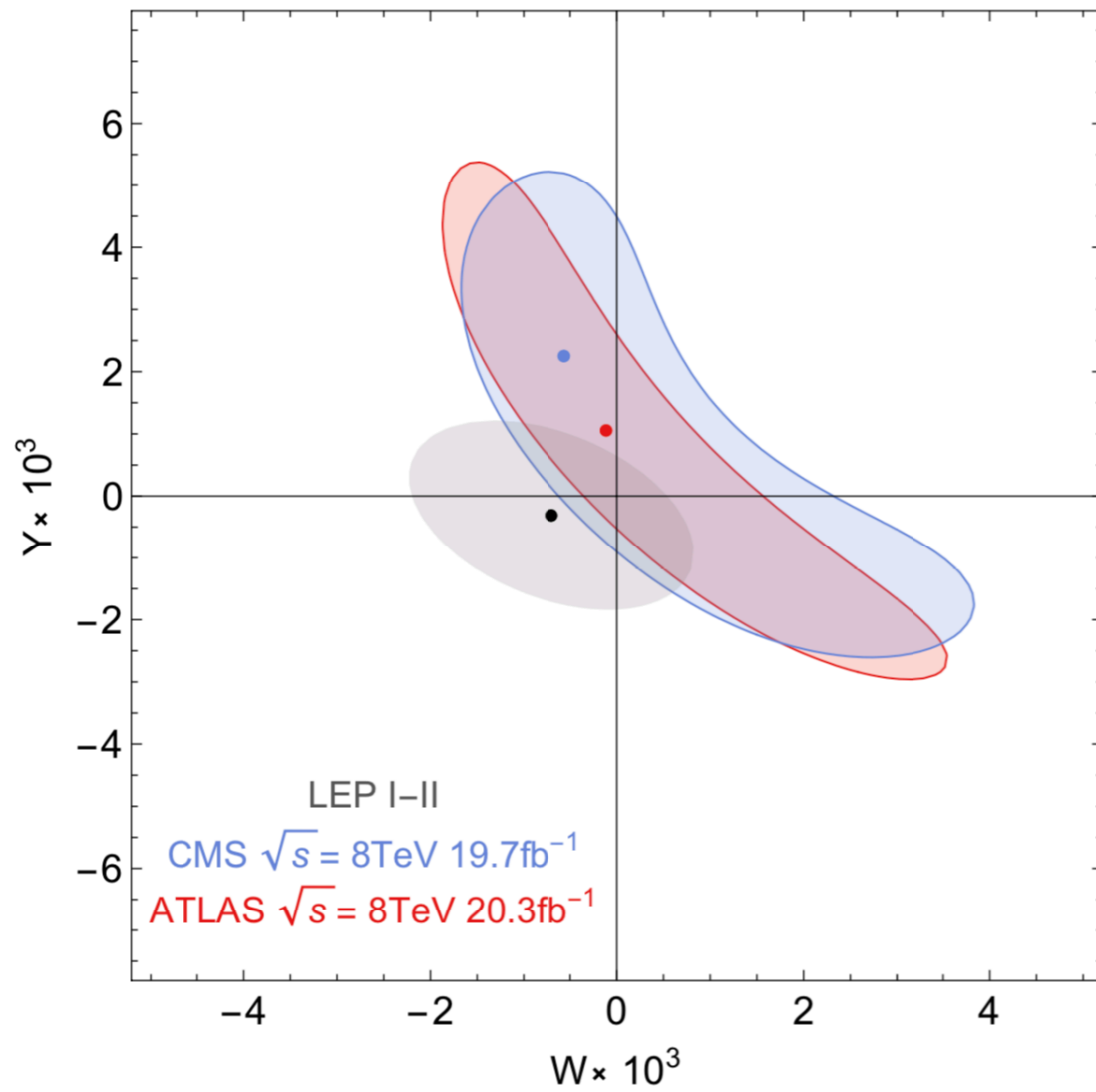
W boson $P_C =$

$$\frac{1 + \frac{\left((\hat{T} - W - t^2 Y) - 2t^2 (\hat{S} - W - Y) \right)}{1 - t^2}}{q^2 - m_W^2} - \frac{W}{m_W^2}$$

WHY DRELL-YAN?

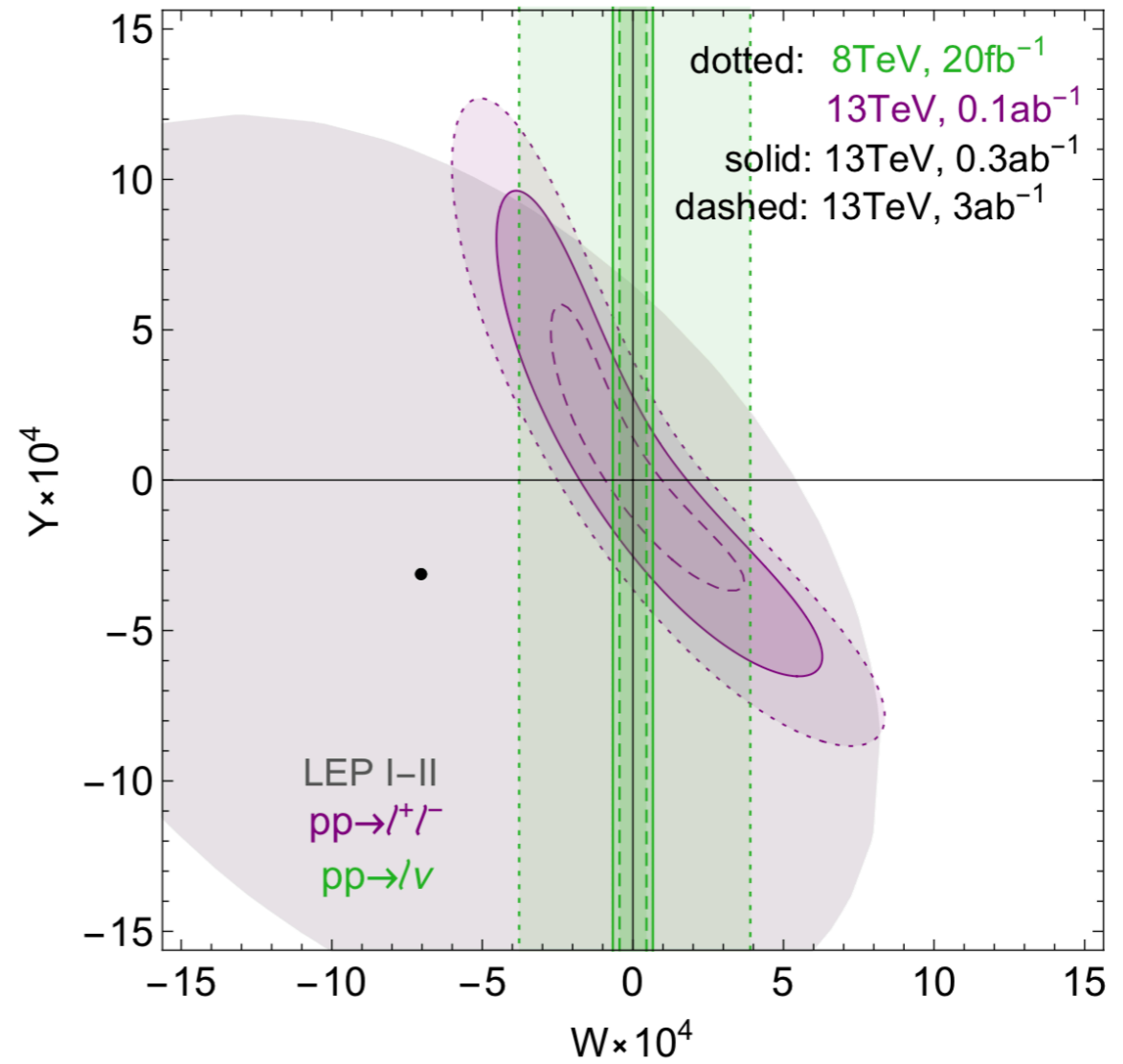


today



LHC \sim LEP

tomorrow (zoomed in)



LHC $>$ LEP!



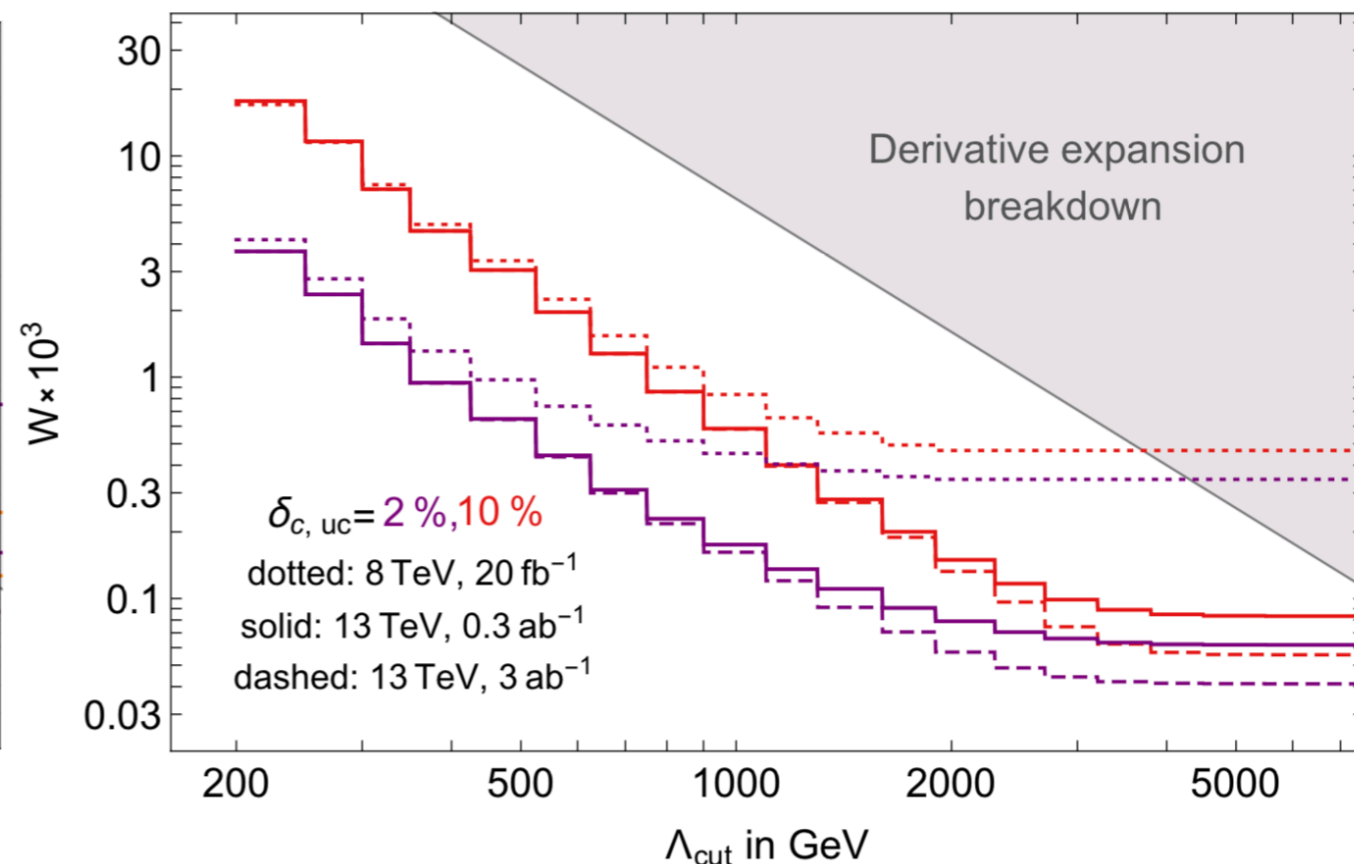
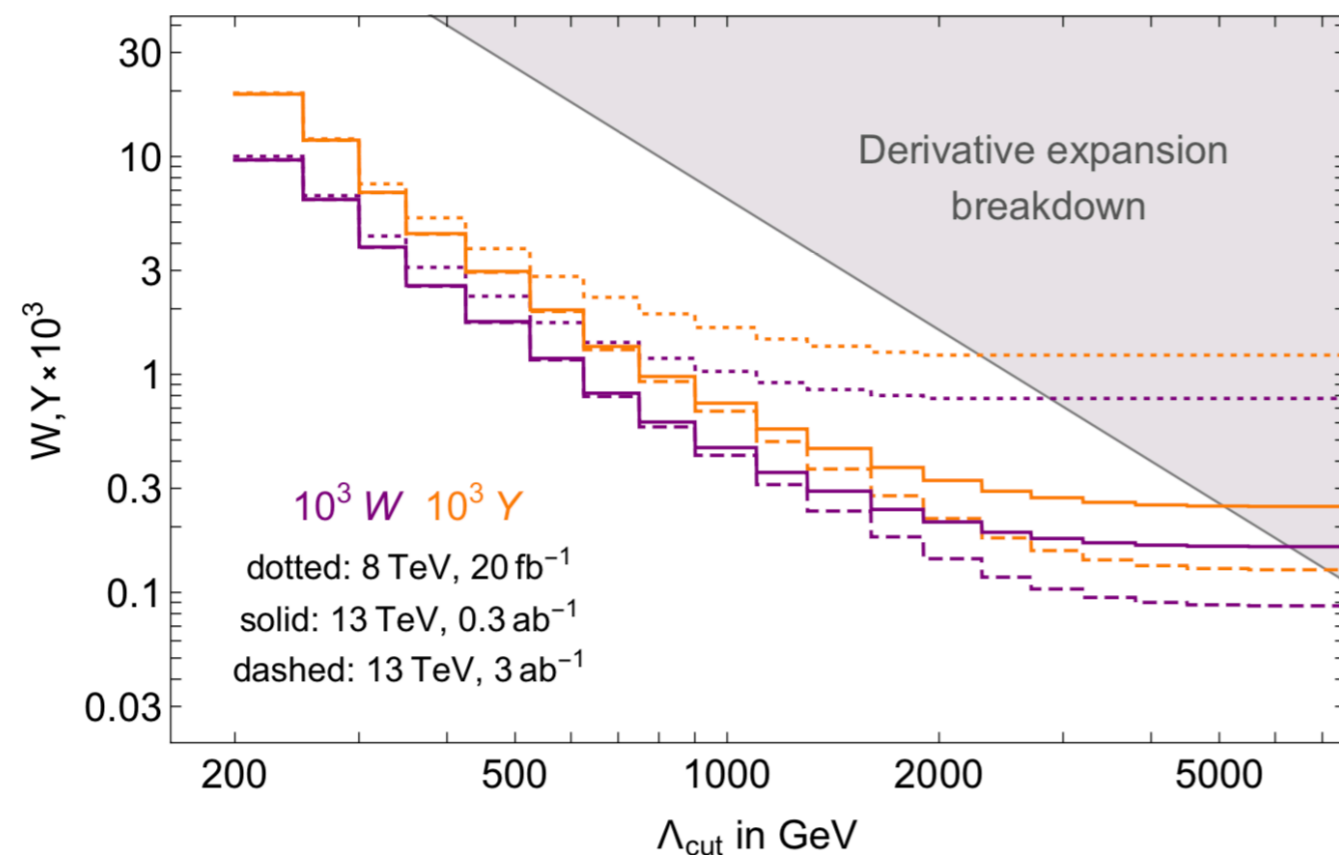
neutral DY

$$pp \rightarrow l^+l^-$$

charged DY

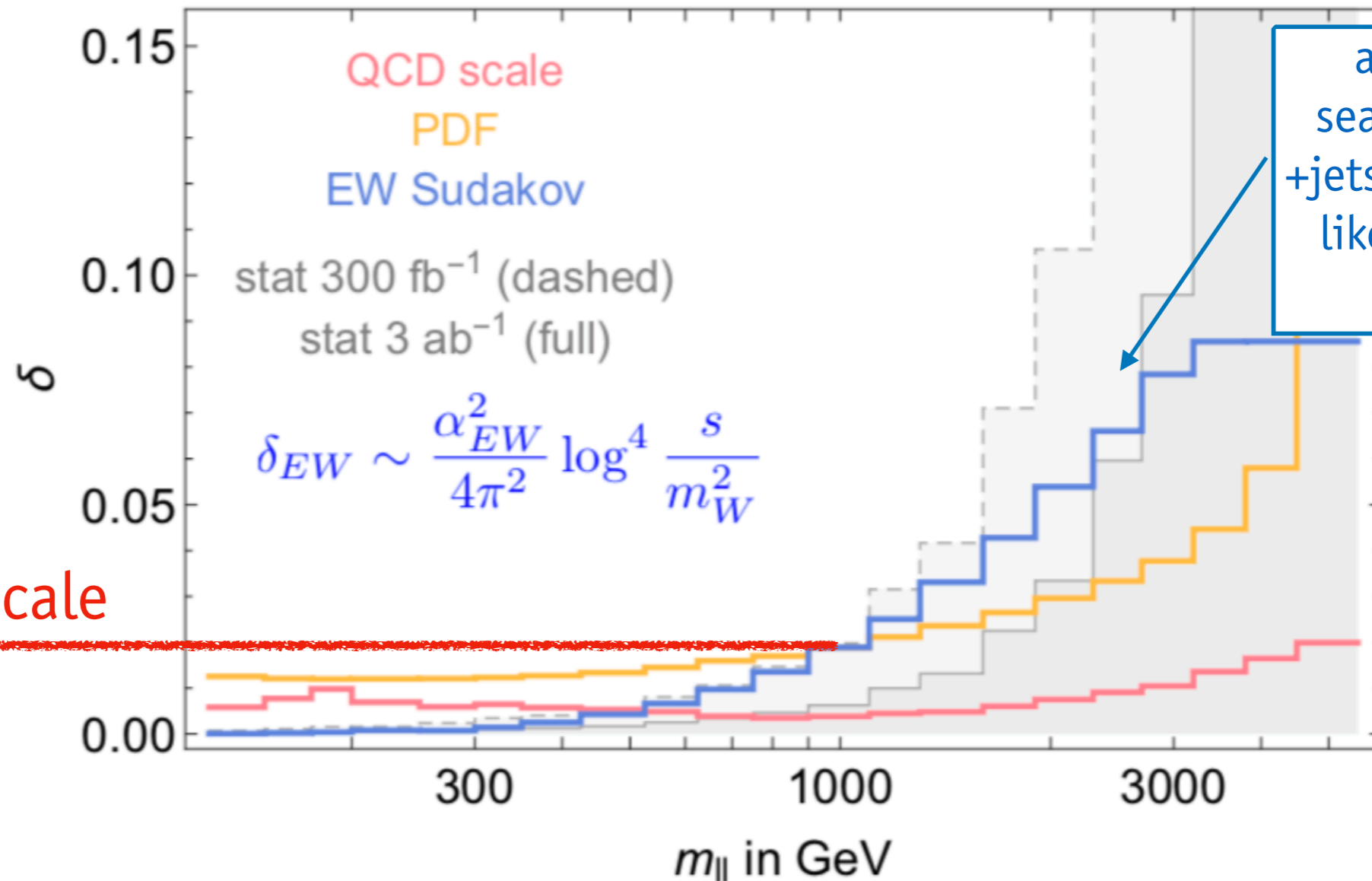
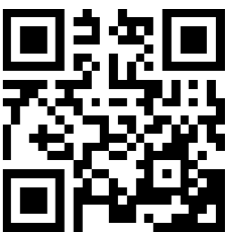
varying uncertainties from the assumed 5%

$$pp \rightarrow l\nu$$



- tails matter!
 - 13 TeV: region up to mass ~ 2 TeV
- statistically dominated (next: lepton energy scale and EW uncertainties)
- can do the same with dijet

WHAT REALLY MATTERS: UNCERTAINTIES



a nightmare for searches with Z(vv)+jets as a background, like WIMP searches with MET!

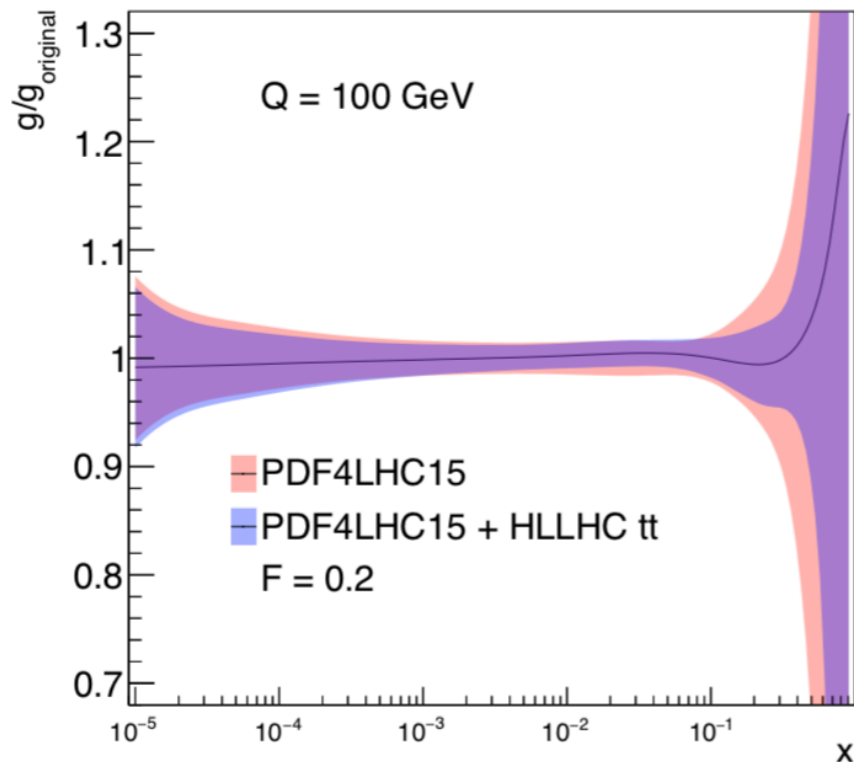
~~~ energy scale~~

- tails matter!
  - 13 TeV: region up to mass ~ 2 TeV
- statistically dominated (next: lepton energy scale and EW uncertainties)
- can do the same with dijet

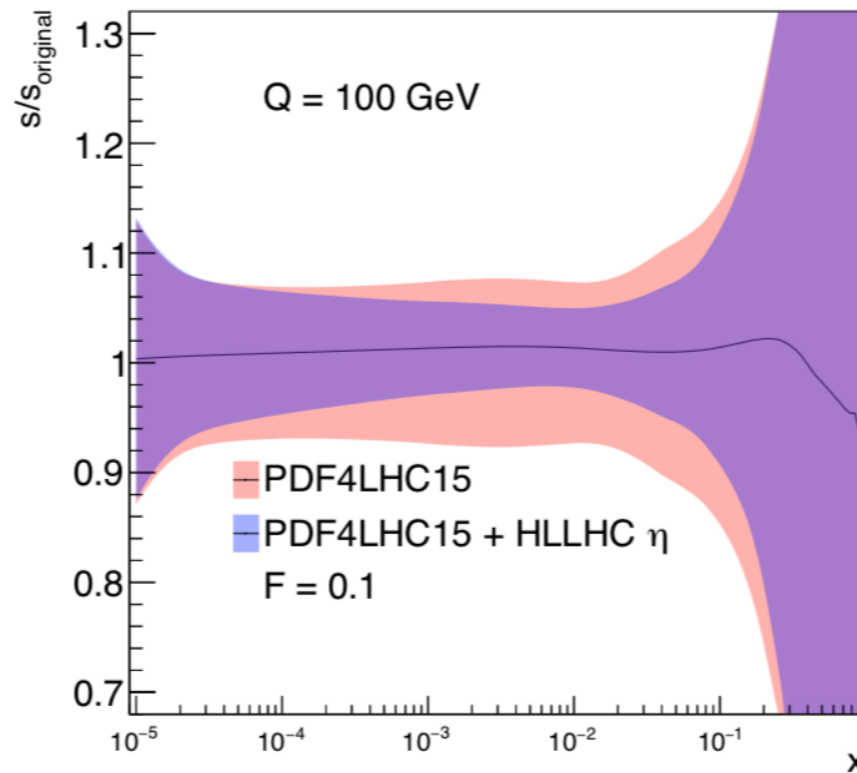
# PDF UNCERTAINTIES

- significant reduction in PDF uncertainties due to large HL-LHC statistics foreseen
  - crucial for all EW observables!

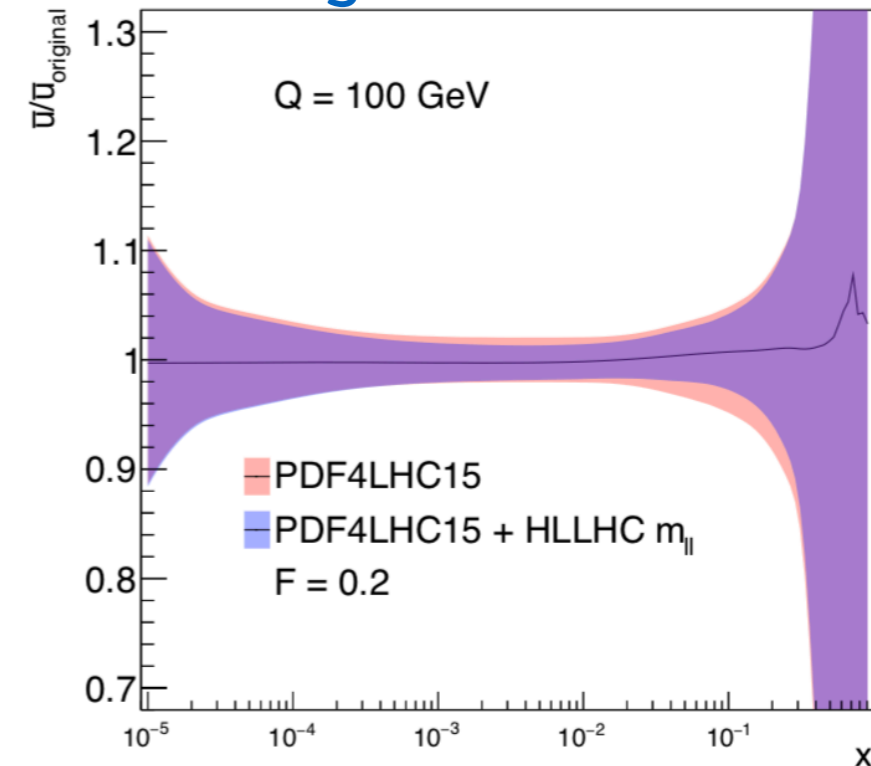
## ttbar



## W+c



## high-mass DY



what

where

mid-x gluon

isolated photons

large-x gluon

ttbar differential

large-x gluon  
valence quarks

inclusive jets

s

W+c

large-x sea quarks  
(flavour separation)

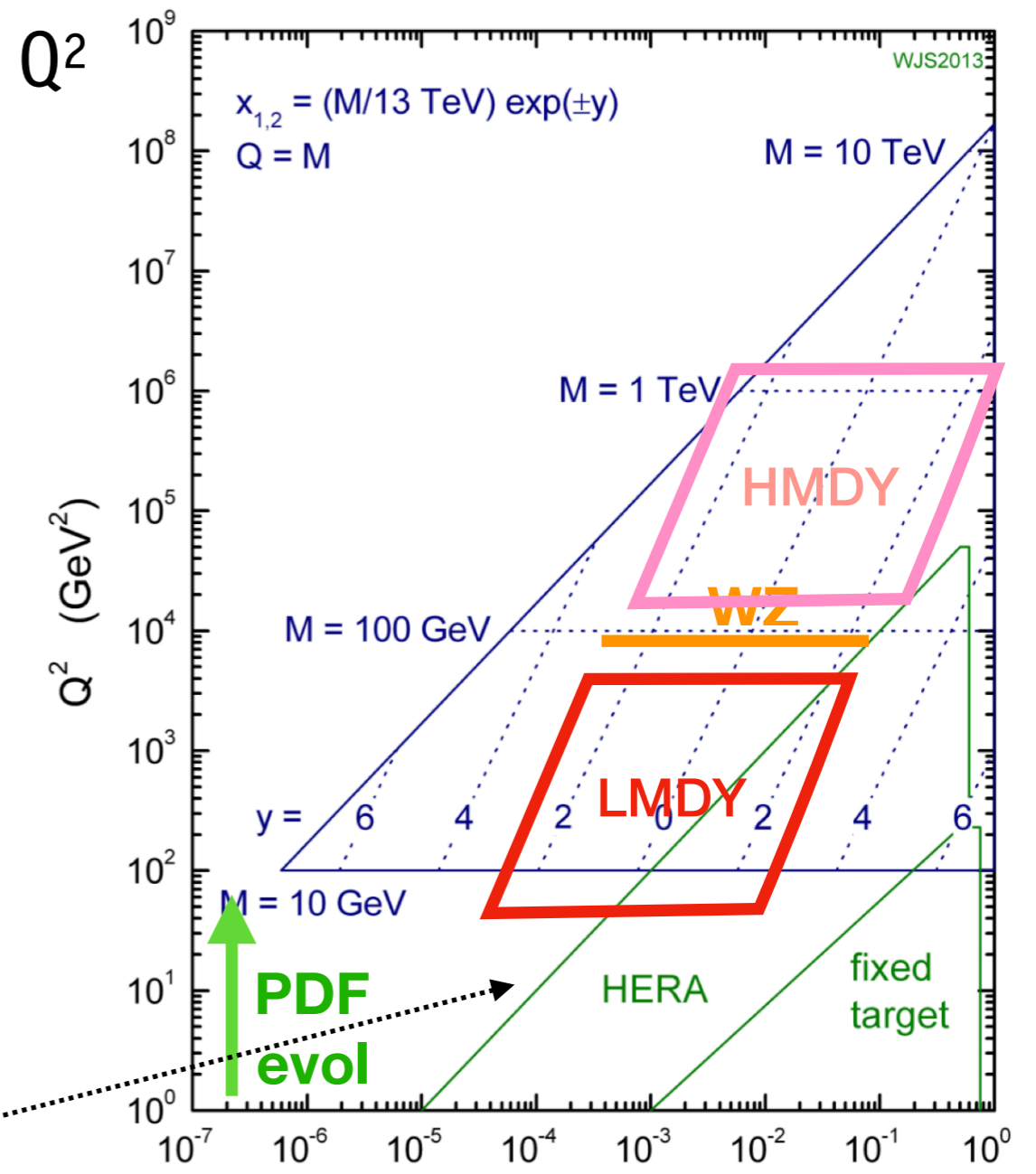
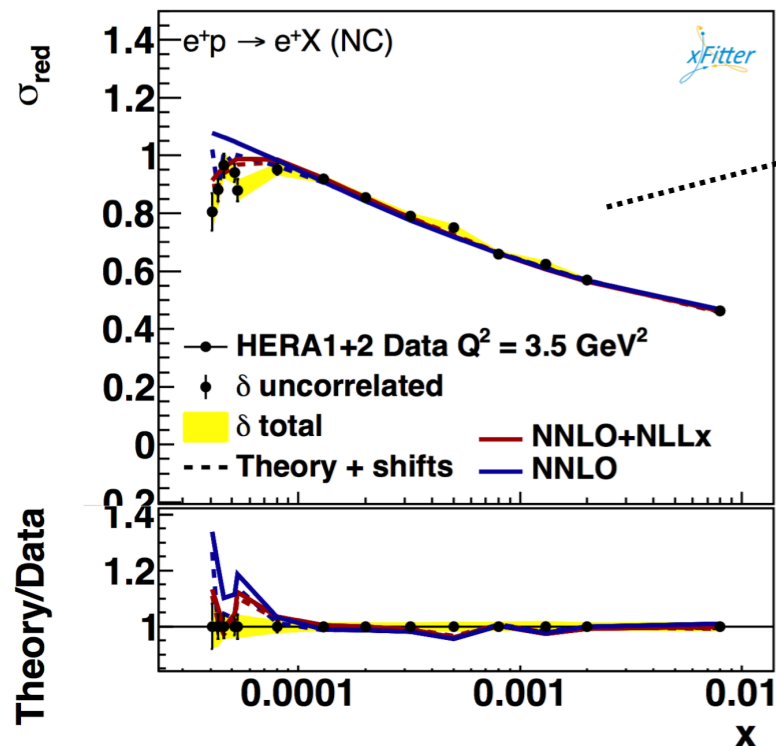
high-mass DY



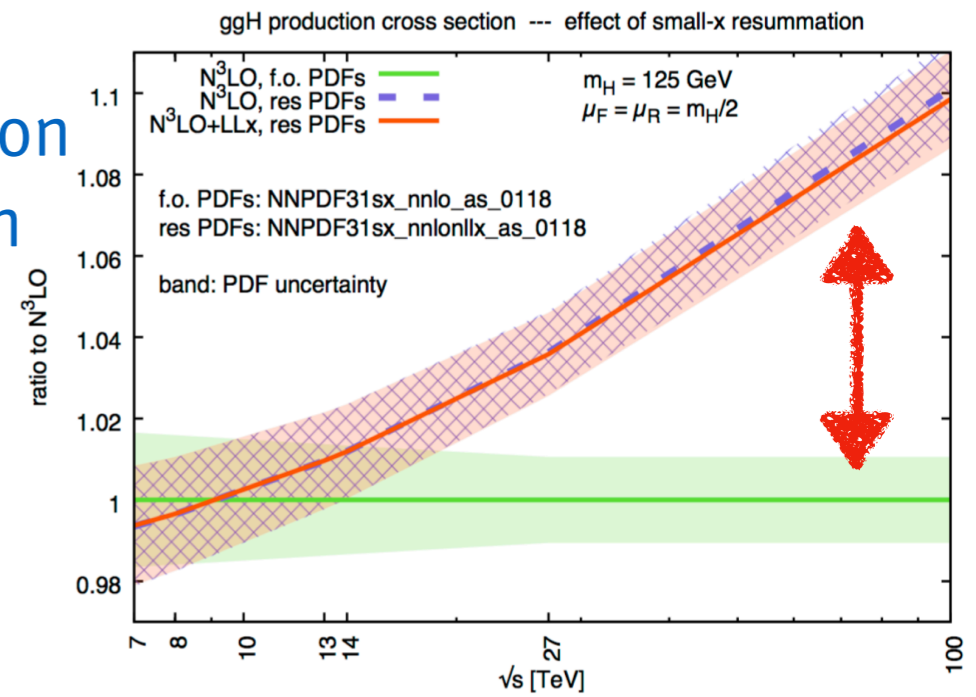
# PDFs: EXPERIMENTAL CHALLENGES

- PDFs don't reproduce low-x data from HERA
  - affects Higgs at FCC!
- due to low-x resummation?
  - answer with low-mass DY (at higher  $Q^2$ )
  - lepton trigger is a challenge!

## HERA vs prediction



effect of resummation on H production (vs  $\sqrt{s}$ )

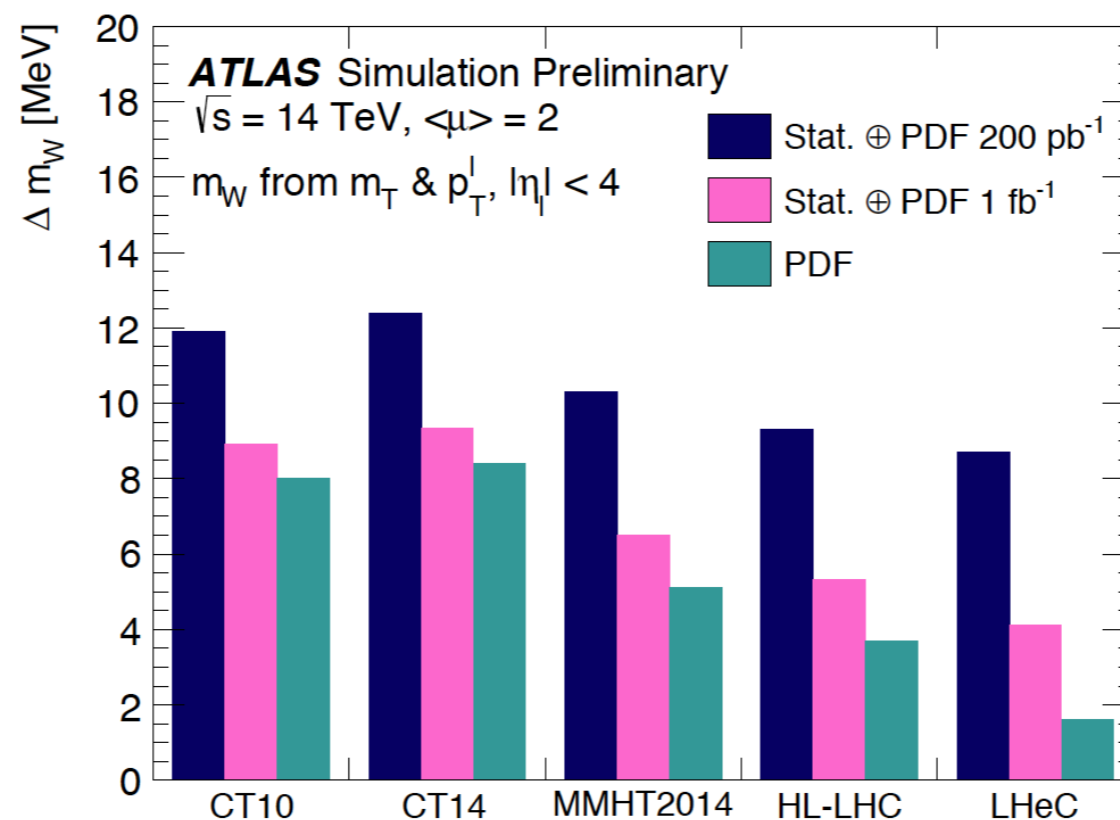


# W mass at HL LHC

- Special **low pile-up collision data** at the HL-LHC (and HE-LHC) of large interest for W boson physics.

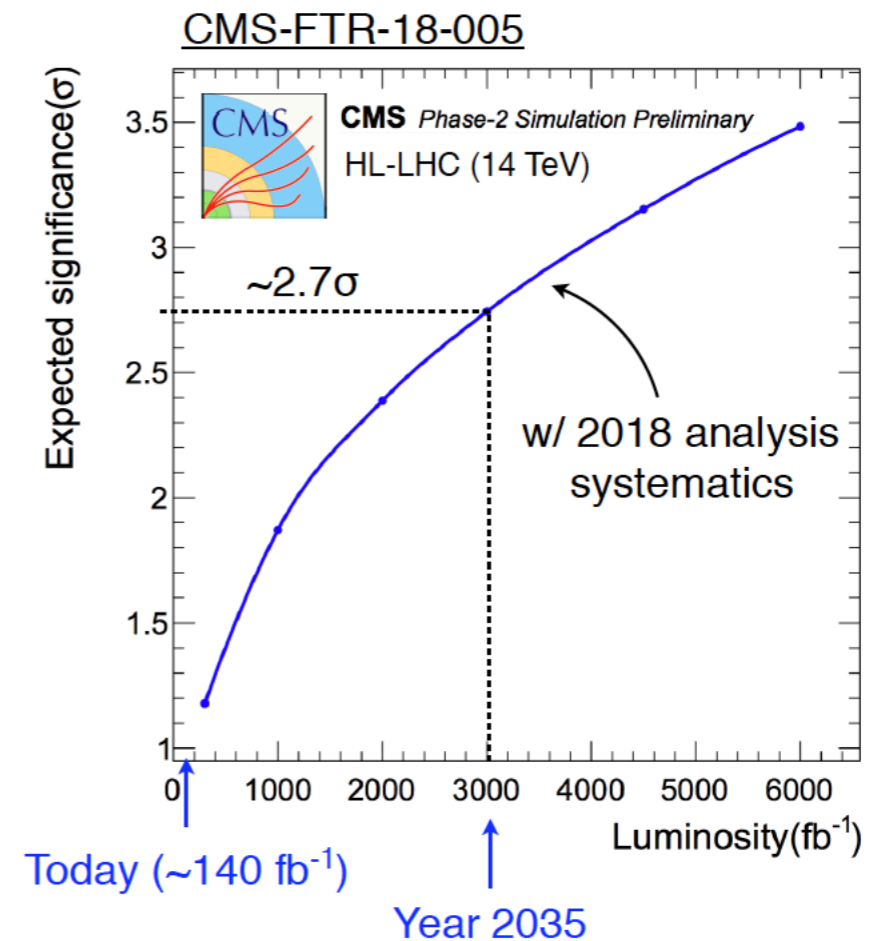
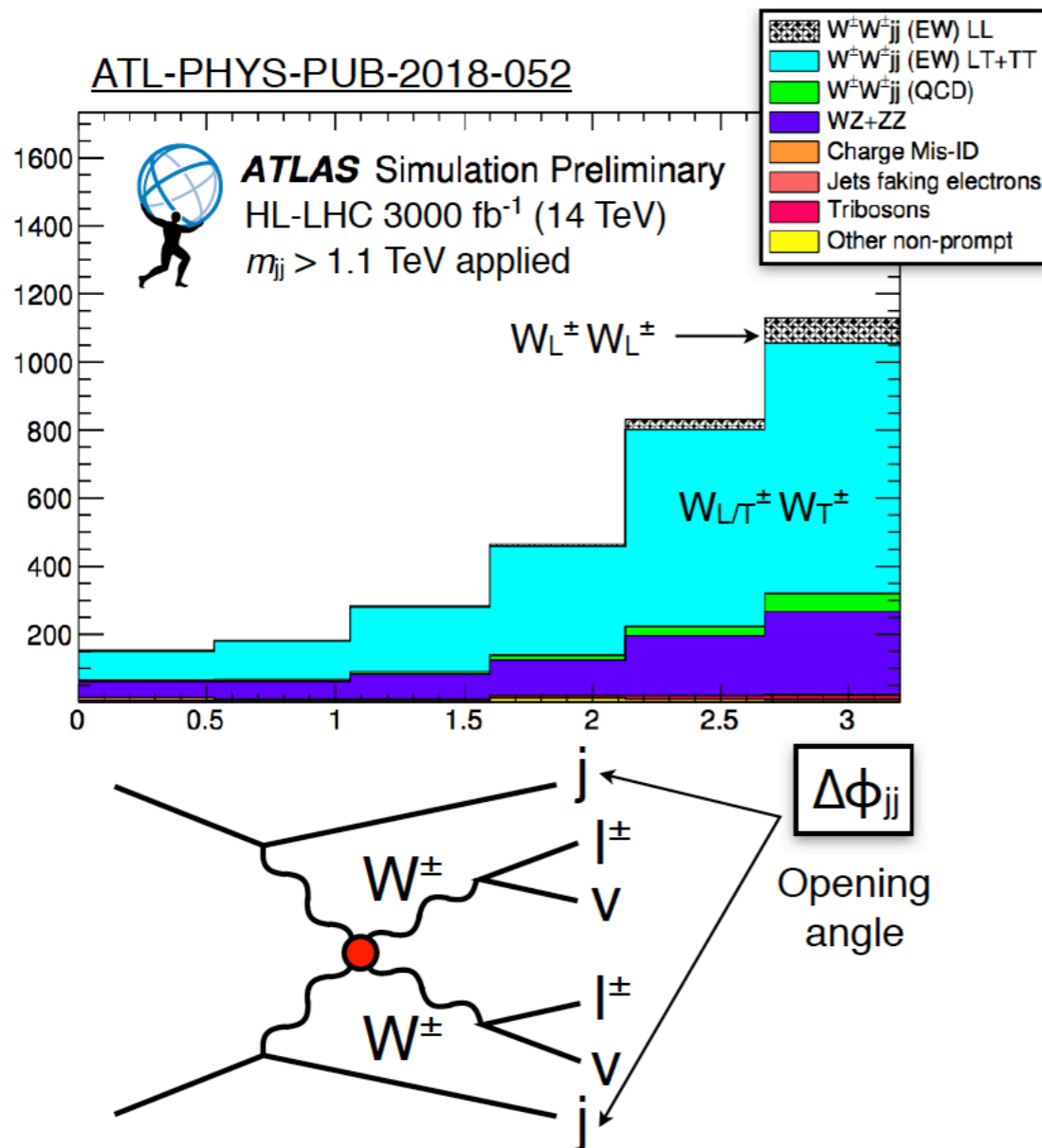
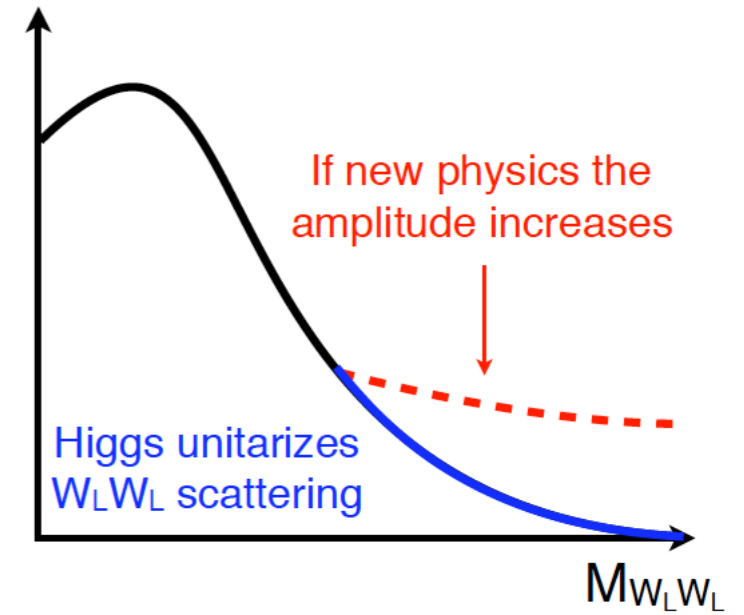
|         |                                                       |                           |                                     |                   |
|---------|-------------------------------------------------------|---------------------------|-------------------------------------|-------------------|
| @14 TeV | $L = 5 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ | $\langle \mu \rangle = 2$ | $2 \times 10^6 \text{ events/week}$ | 10 MeV stat. unc. |
|---------|-------------------------------------------------------|---------------------------|-------------------------------------|-------------------|

- First **quantitative study** of the potential improvement in the W-boson mass considering **only statistical and PDF uncertainties**.
- Experimental uncertainties maintained at a level similar to the statistical uncertainty
- Events are selected by applying Run2 cuts to the object kinematics



# HL LHC Longitudinal VBS

- **LL component** indirect probe of the unitarization mechanism of the VBS amplitude through **Higgs and NP**
- Exploit **kinematic information to disentangle polarization**



- Polarized **WZ and ZZ** can be measured in similar way w/ 2D fit to  $m_{jj}$  and opening angle

# Conclusions

- **Both theory and LHC experiments are moving into an high precision era**

LHC can improve precision observables and global SM fit

- **PDF uncertainties are often a limitation**

overcome with differential cross-section measurements (e.g.  $\sin^2(\theta_{\text{eff}})$ )

- **SM-EFT highlights complementarity with LEP**

examples in Drell-Yan and di-jet production

- **Detector acceptance upgrade and advanced experimental techniques for HL-LHC is crucial**

forward region is the only hope for a pp collider

- **Improved measurements may further confirm the validity of the SM or indicate deviations which could point to new physics**

# Backup





Z(ll) / gamma+jets

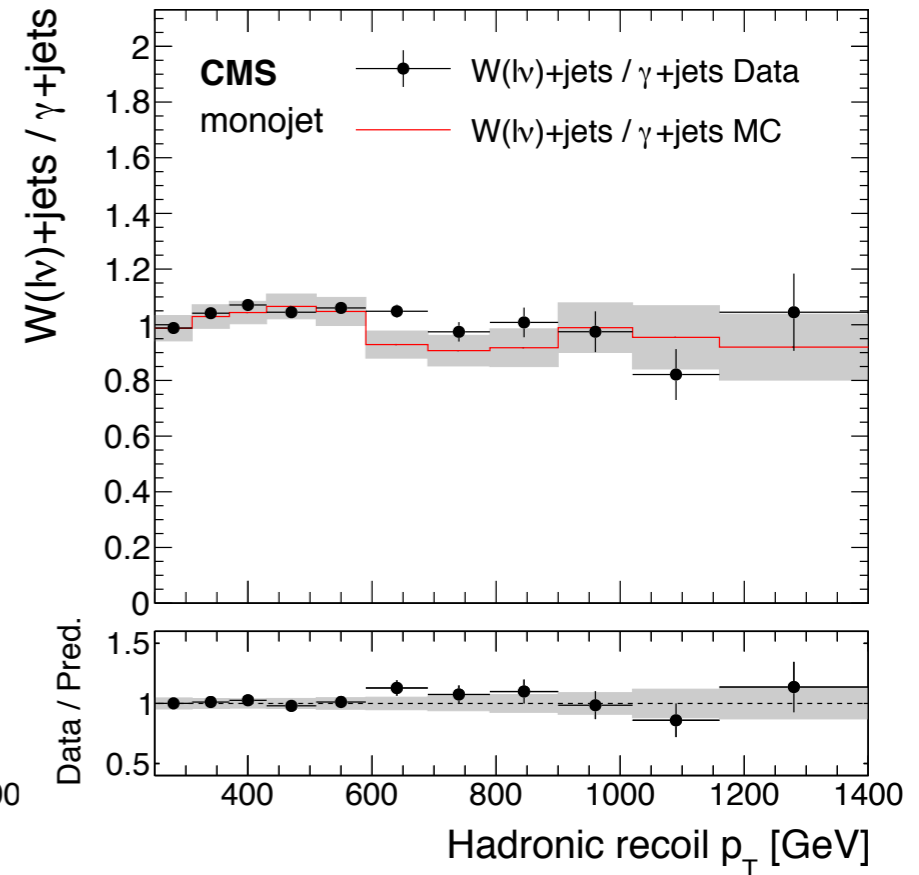
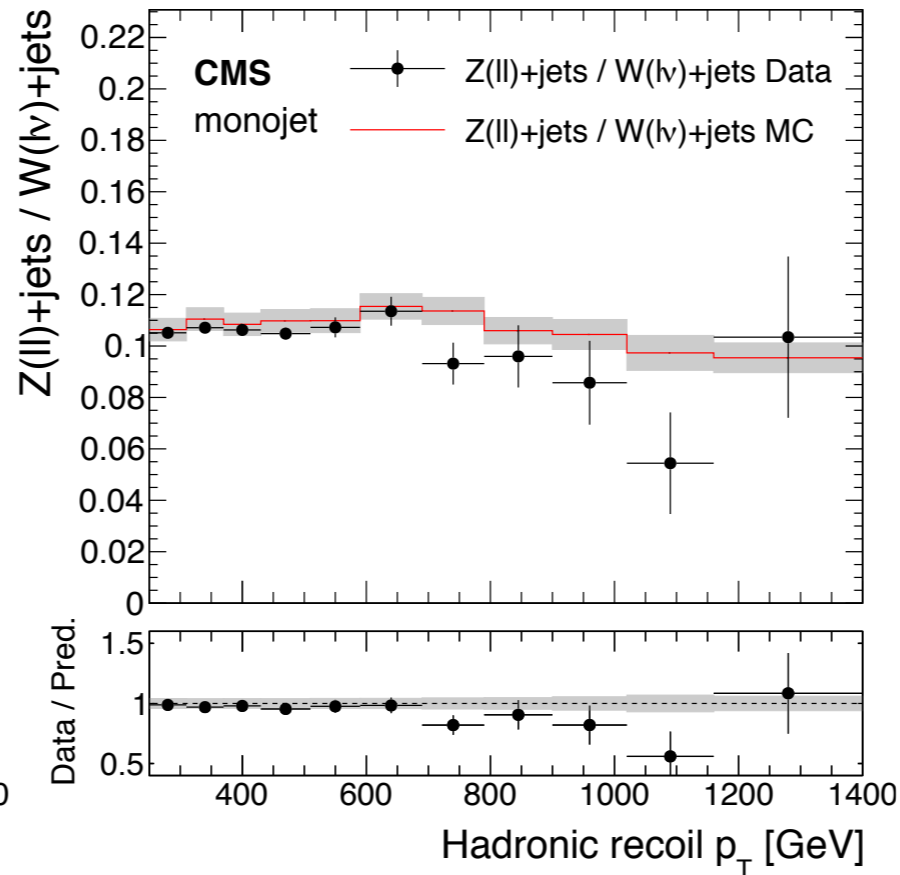
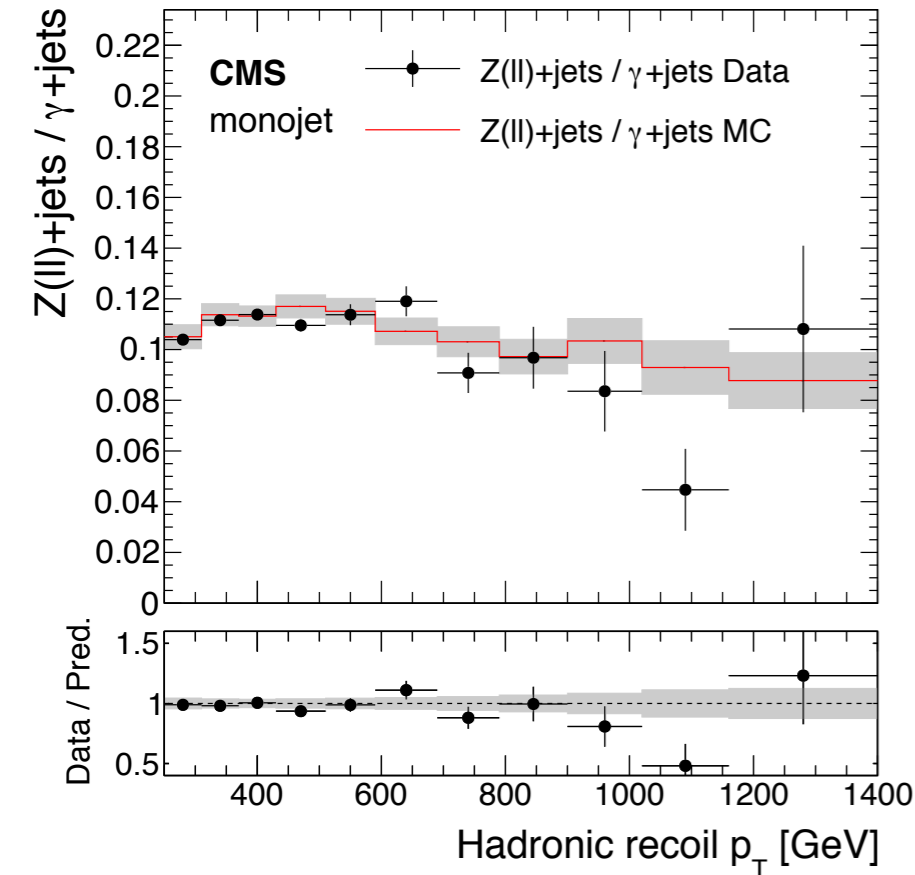
Z(ll) / W(lv)+jets

W(lv) / gamma+jets

35.9 fb<sup>-1</sup> (13 TeV)

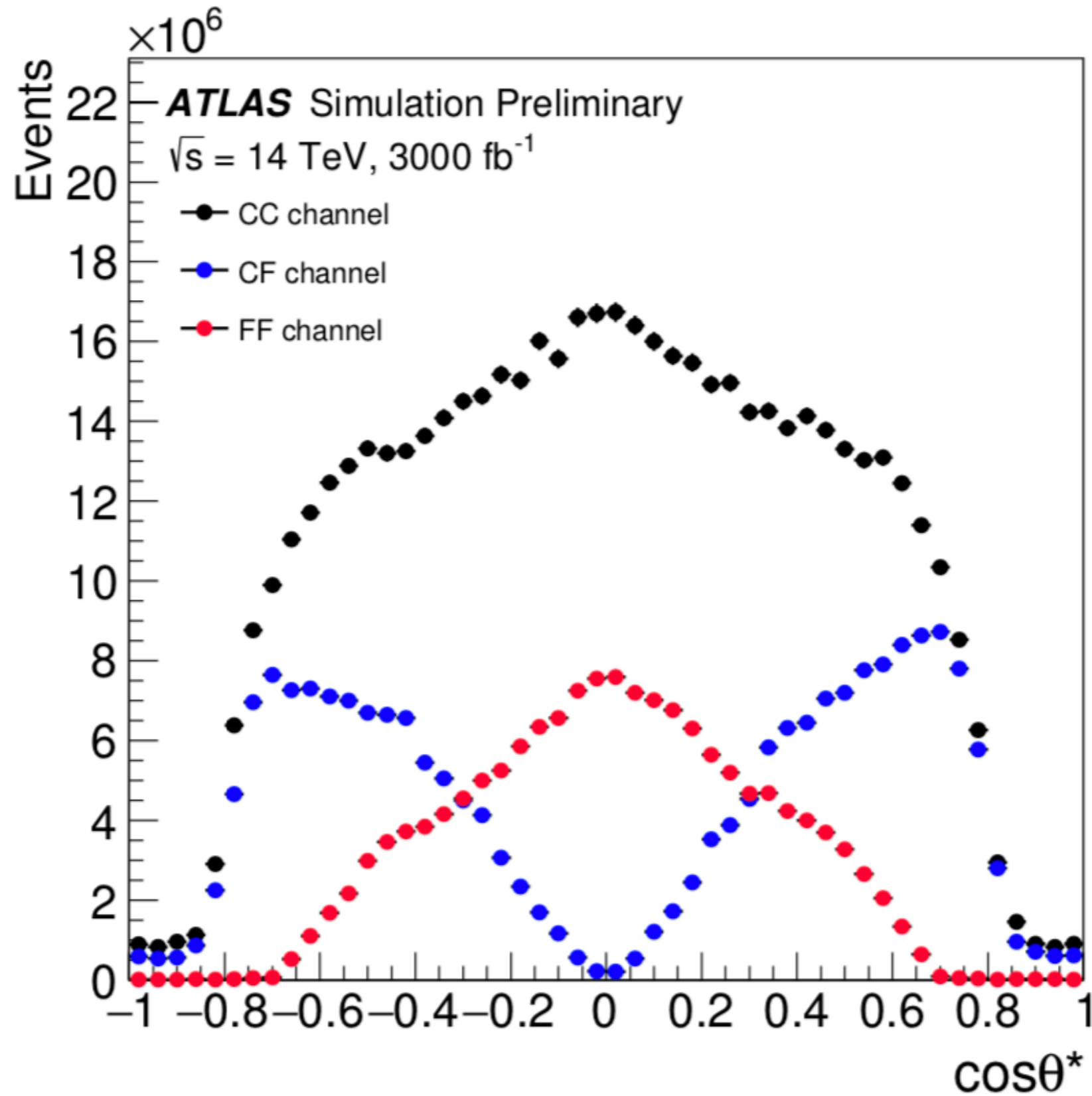
35.9 fb<sup>-1</sup> (13 TeV)

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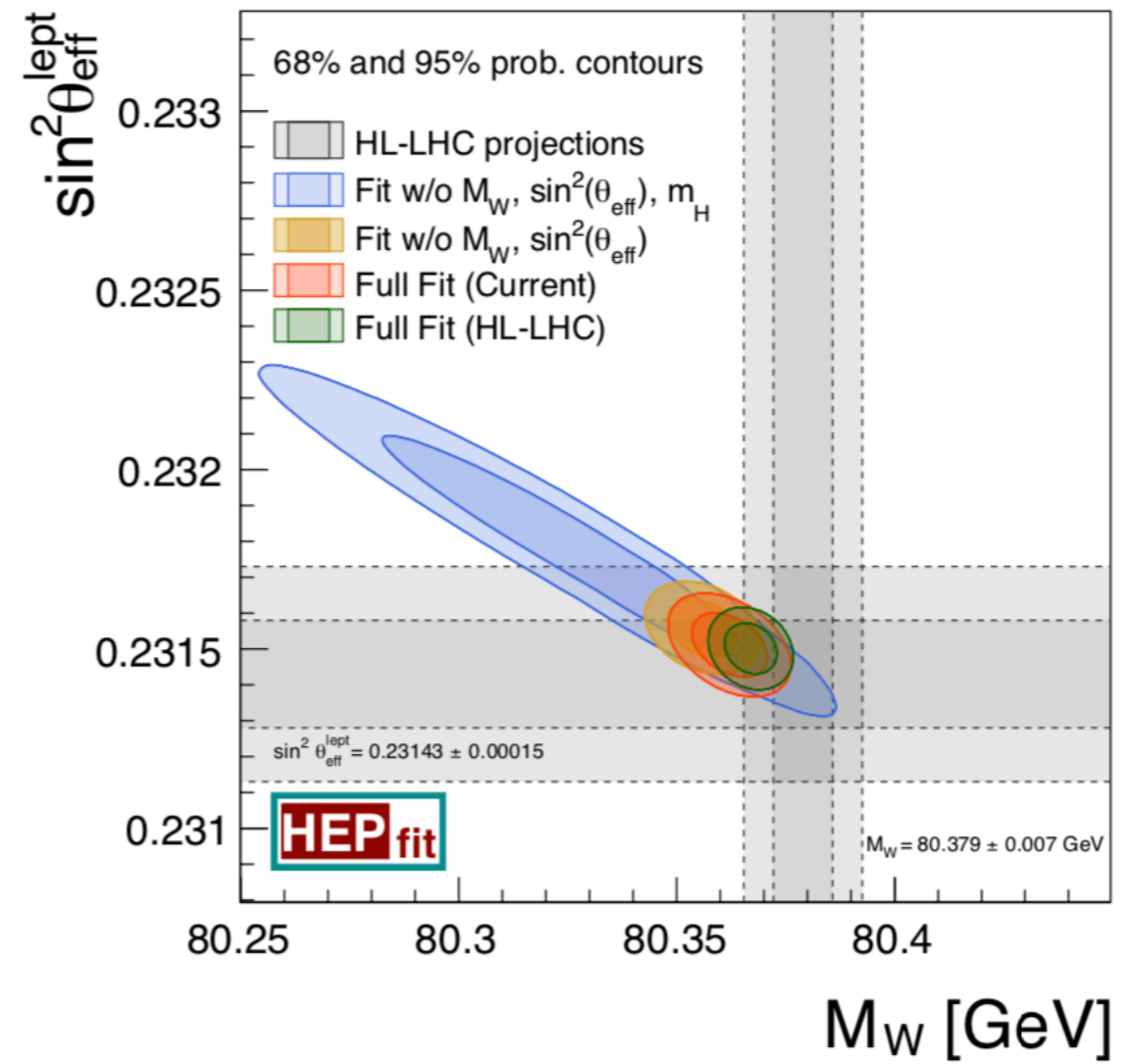
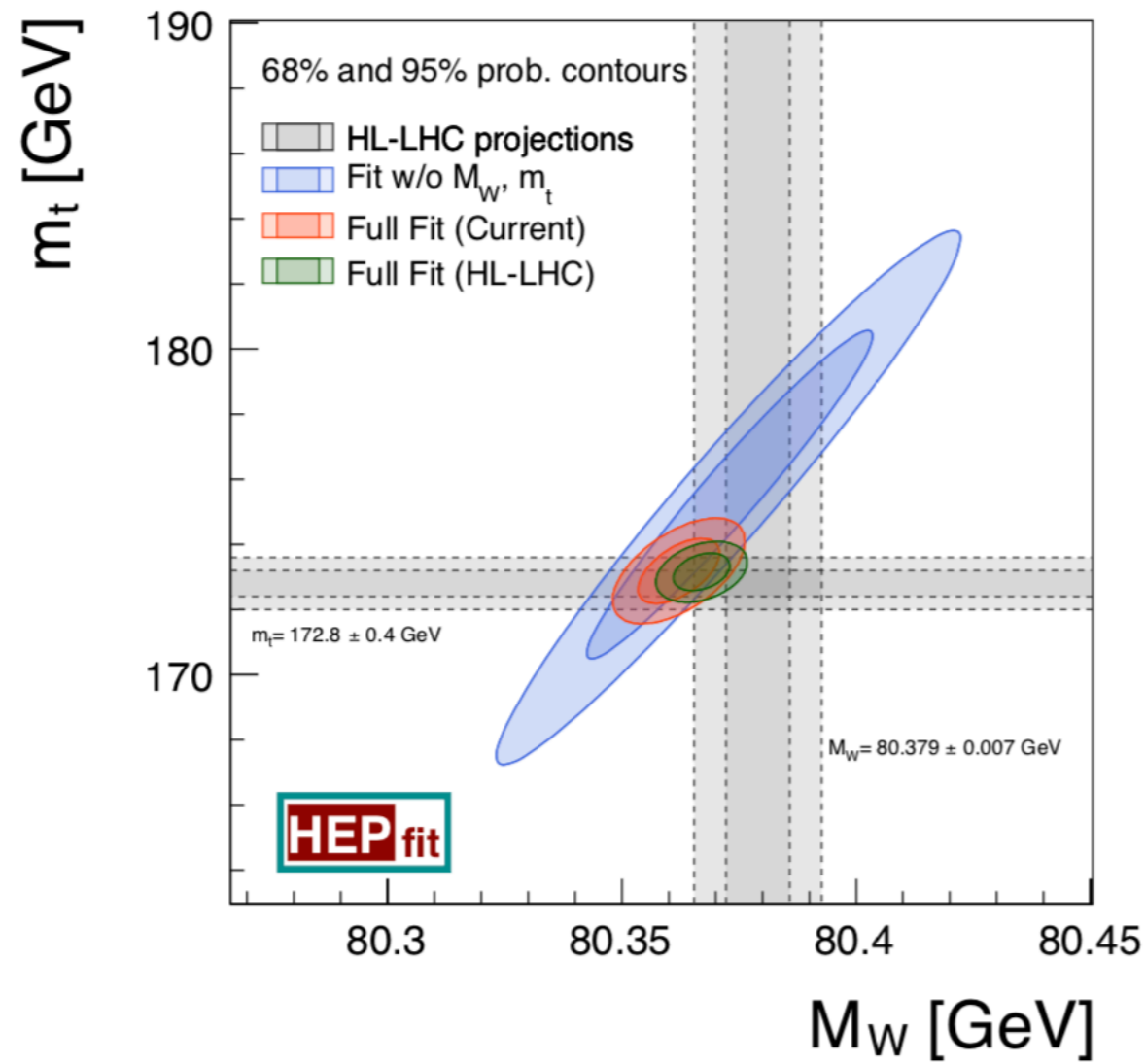


- new physics searches often in invisible final states
  - e.g.: WIMP pair in association with jets ("mono-jet")
- obvious background: Z( $\nu\nu$ )+jets
  - estimated from leptonic Z, W decays and gamma+jets (high stats!)
- search sensitivity limited by EW (and QCD) uncertainties!

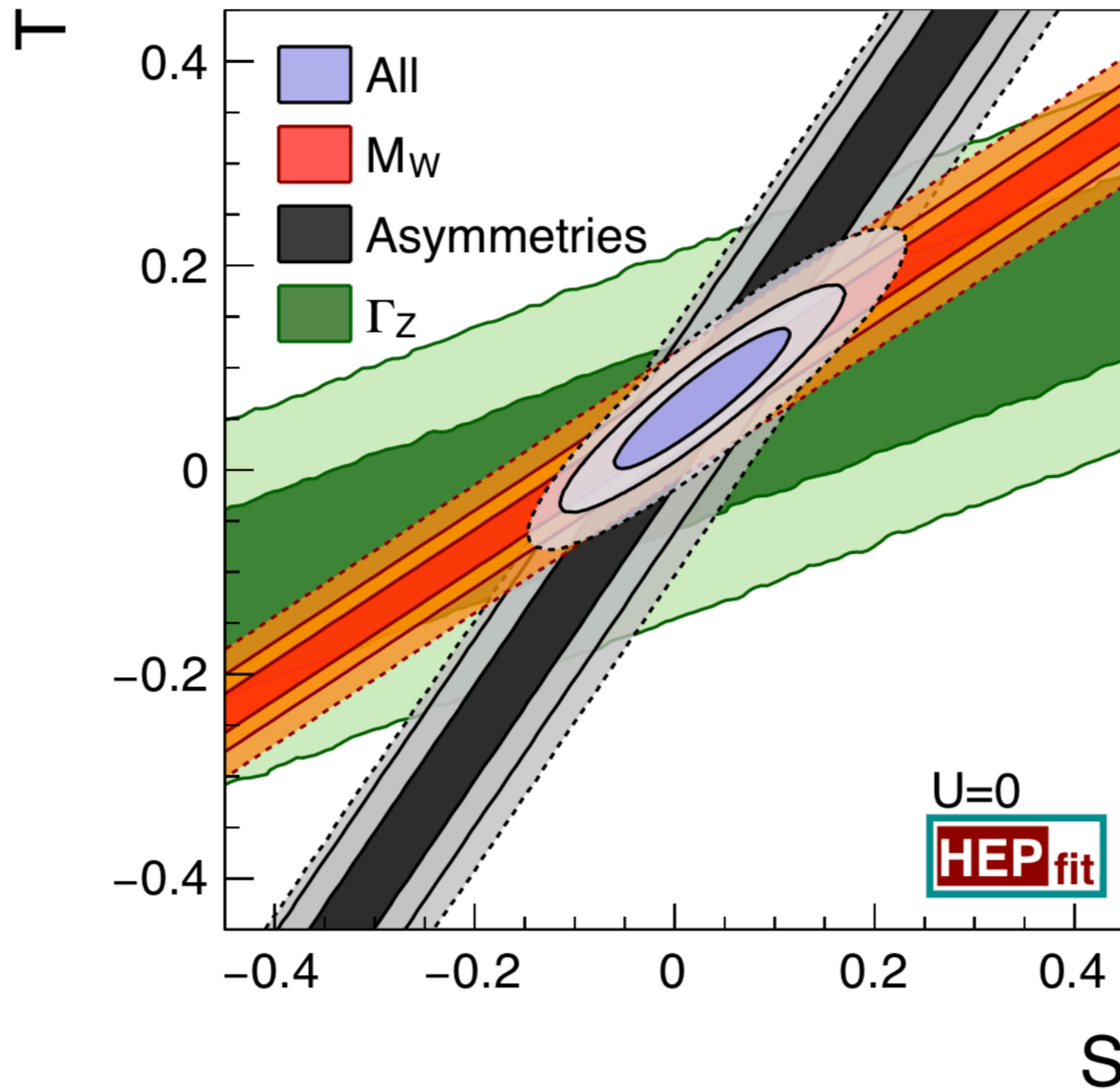
# THE IMPORTANCE OF BEING FORWARD



# ELECTROWEAK FIT

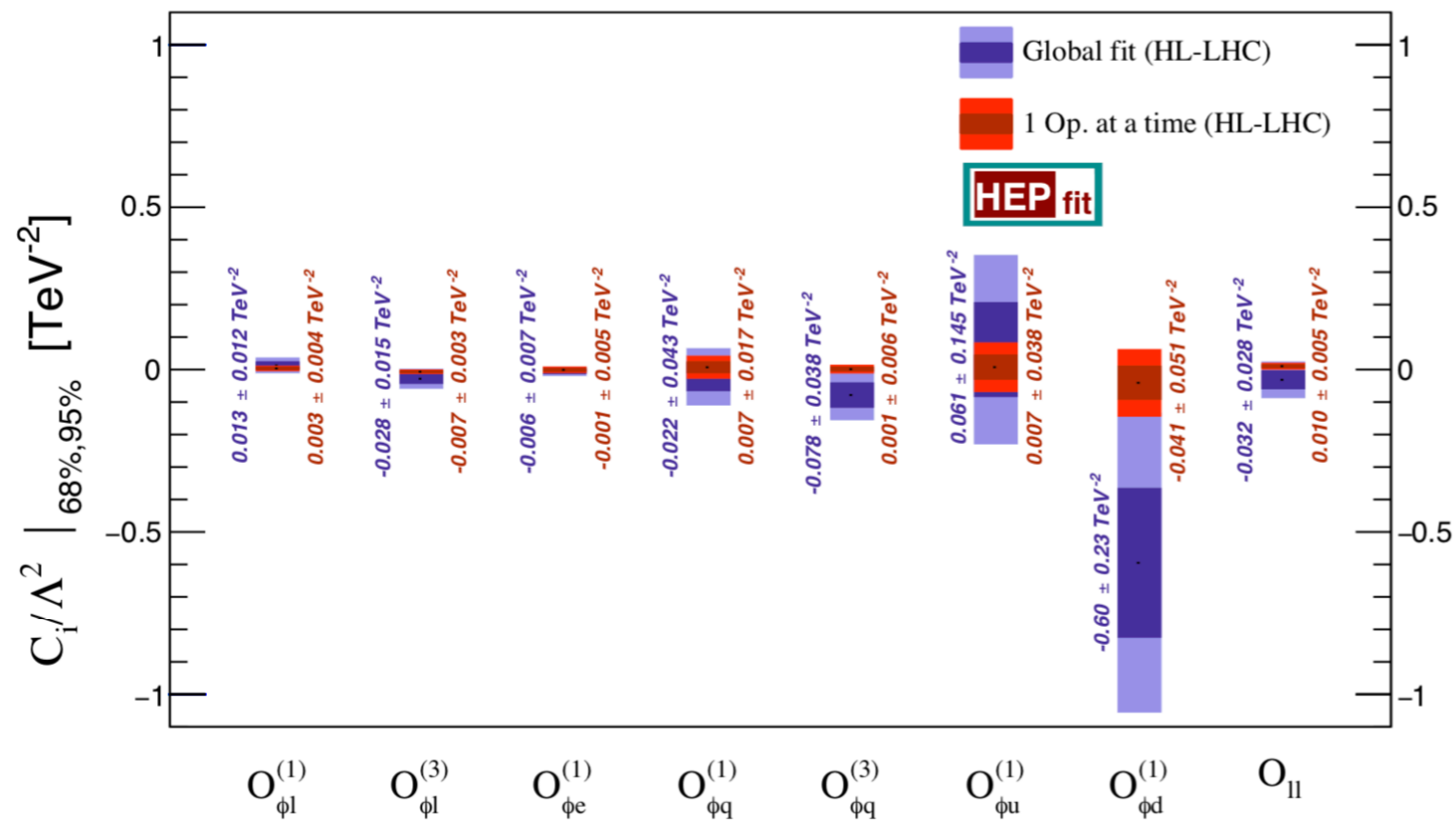


# OBLIQUE PARAMETERS



# ELECTROWEAK FIT

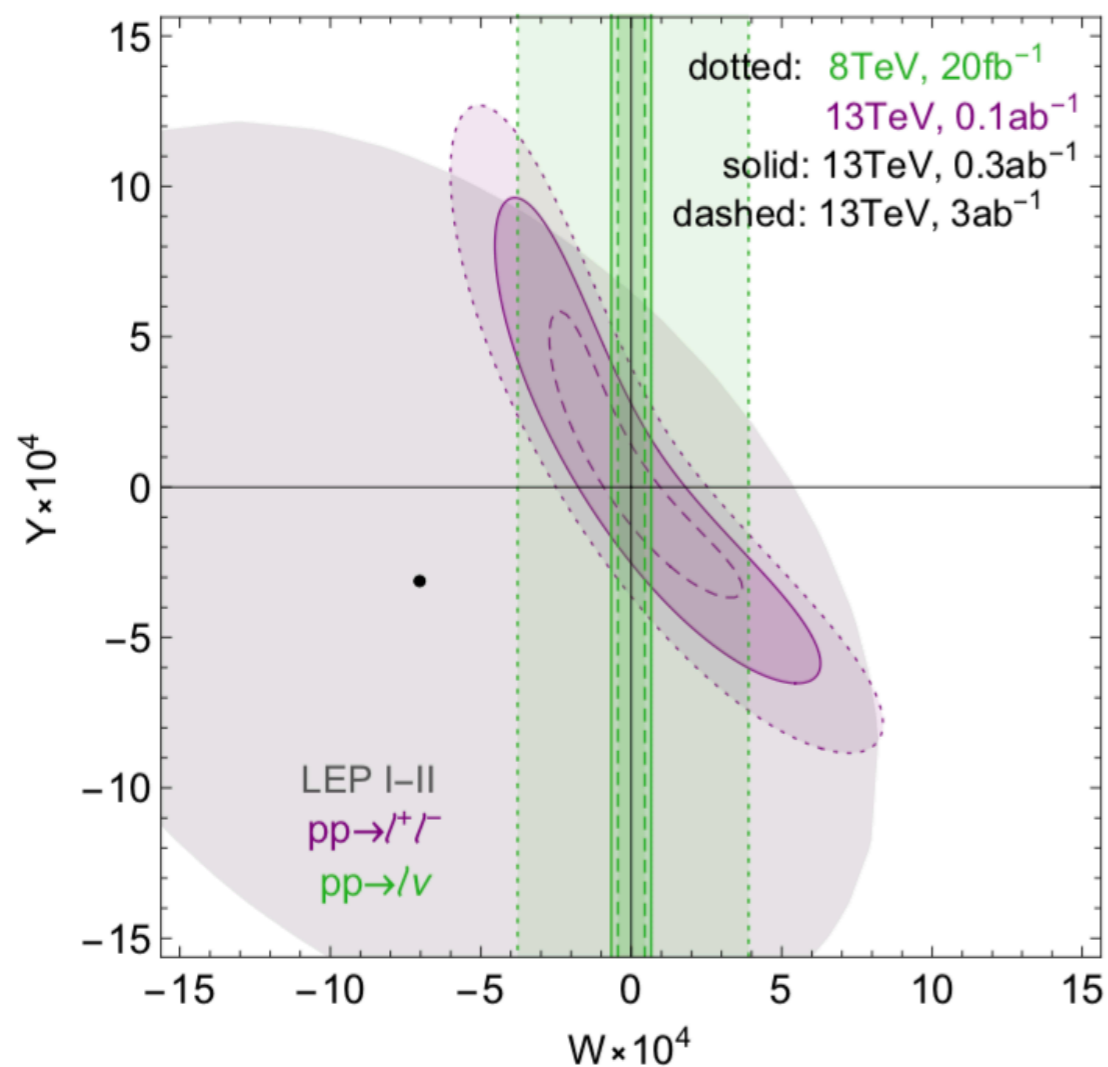
$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \frac{1}{\Lambda^{d-4}} \mathcal{L}_d, \quad \text{with } \mathcal{L}_d = \sum_i C_i \mathcal{O}_i^{(d)}, \quad [\mathcal{O}_i^{(d)}] = d$$



| Operator<br>Coefficient       | Current uncertainty<br>[TeV <sup>-2</sup> ] |               | Precision at HL-LHC<br>[TeV <sup>-2</sup> ] |               |
|-------------------------------|---------------------------------------------|---------------|---------------------------------------------|---------------|
|                               | 1 op. at<br>a time                          | Global<br>fit | 1 op. at<br>a time                          | Global<br>fit |
| $\overline{C}_{\phi l}^{(1)}$ | 0.004                                       | 0.012         | 0.004                                       | 0.012         |
| $\overline{C}_{\phi q}^{(1)}$ | 0.018                                       | 0.044         | 0.017                                       | 0.043         |
| $\overline{C}_{\phi e}$       | 0.005                                       | 0.009         | 0.005                                       | 0.007         |
| $\overline{C}_{\phi u}$       | 0.040                                       | 0.146         | 0.038                                       | 0.145         |
| $\overline{C}_{\phi d}$       | 0.054                                       | 0.237         | 0.051                                       | 0.230         |
| $\overline{C}_{\phi l}^{(3)}$ | 0.004                                       | 0.017         | 0.003                                       | 0.015         |
| $\overline{C}_{\phi q}^{(3)}$ | 0.007                                       | 0.040         | 0.006                                       | 0.038         |
| $\overline{C}_{ll}$           | 0.007                                       | 0.028         | 0.005                                       | 0.028         |
| $\overline{C}_{\phi WB}$      | 0.003                                       | —             | 0.002                                       | —             |
| $\overline{C}_{\phi D}$       | 0.007                                       | —             | 0.005                                       | —             |

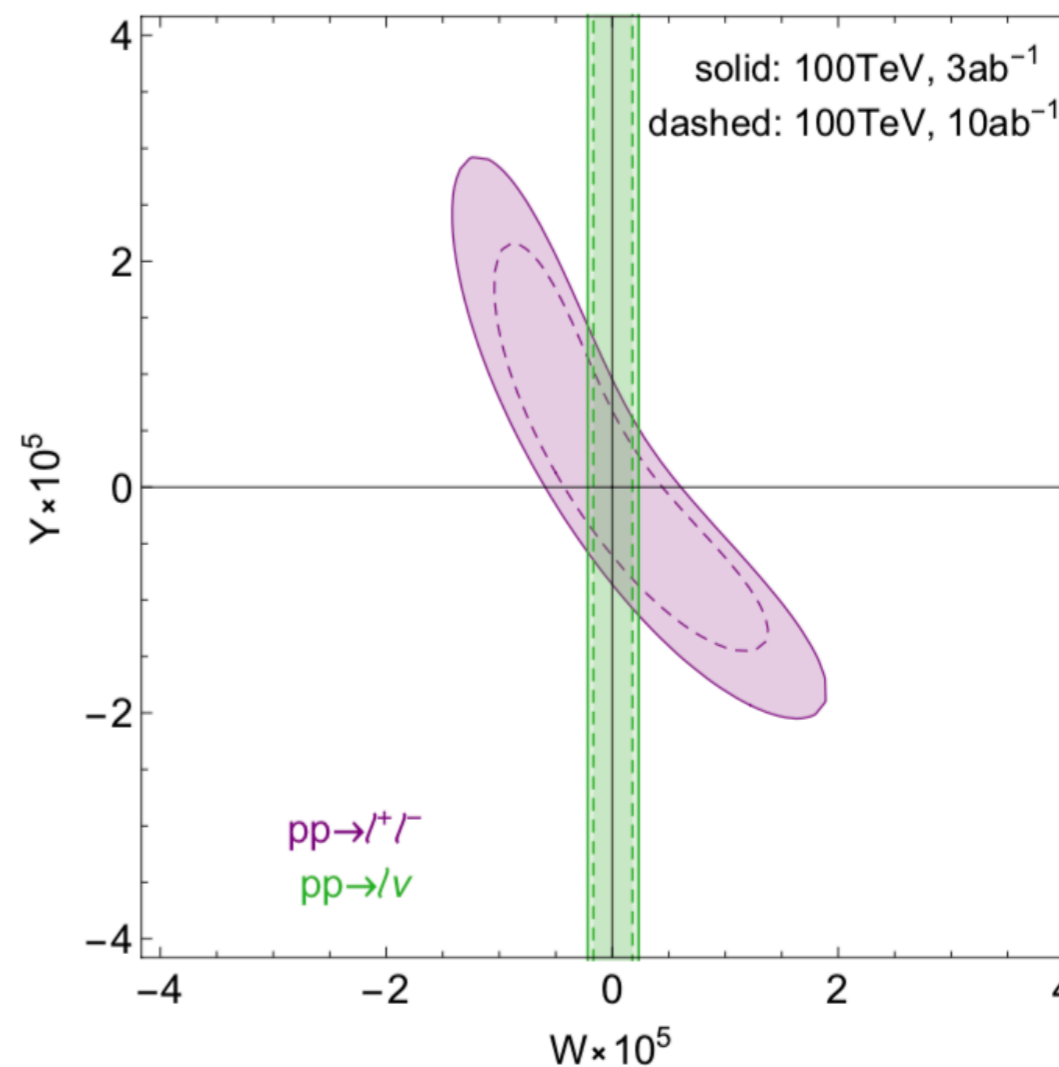


"quota 1"



< 2 TeV region important

"quota 100" zoomed in



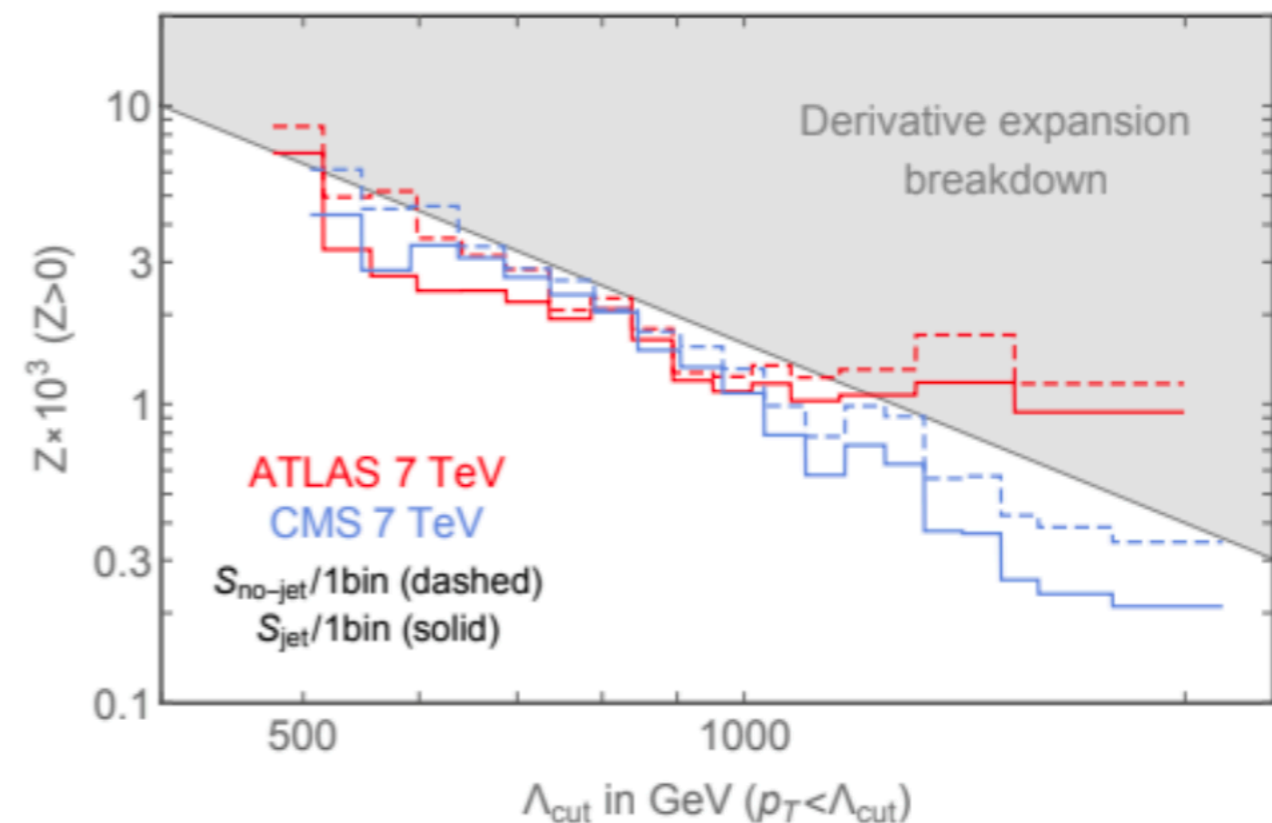
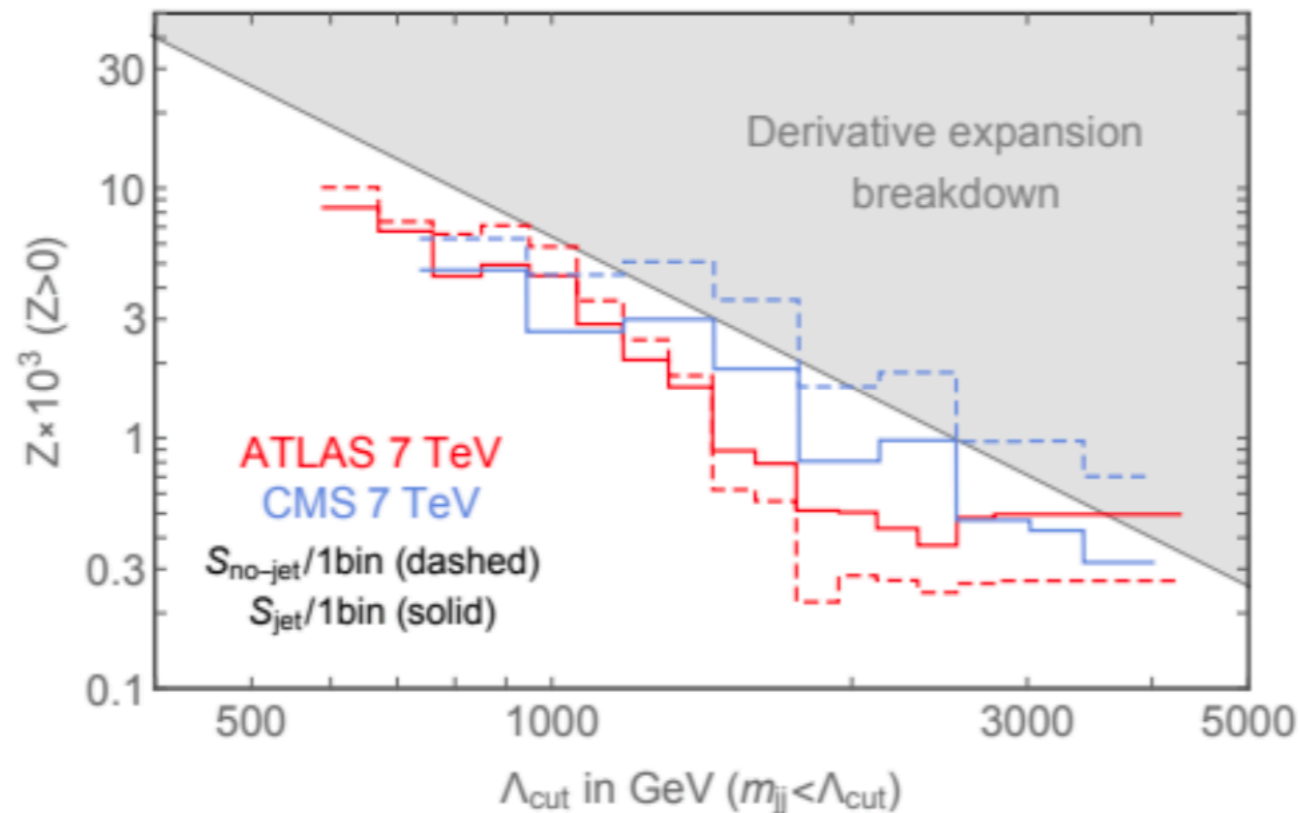
< 10 TeV region important

# THE IMPORTANCE OF BEING DIJET



dijet mass

inclusive jet  $p_T$



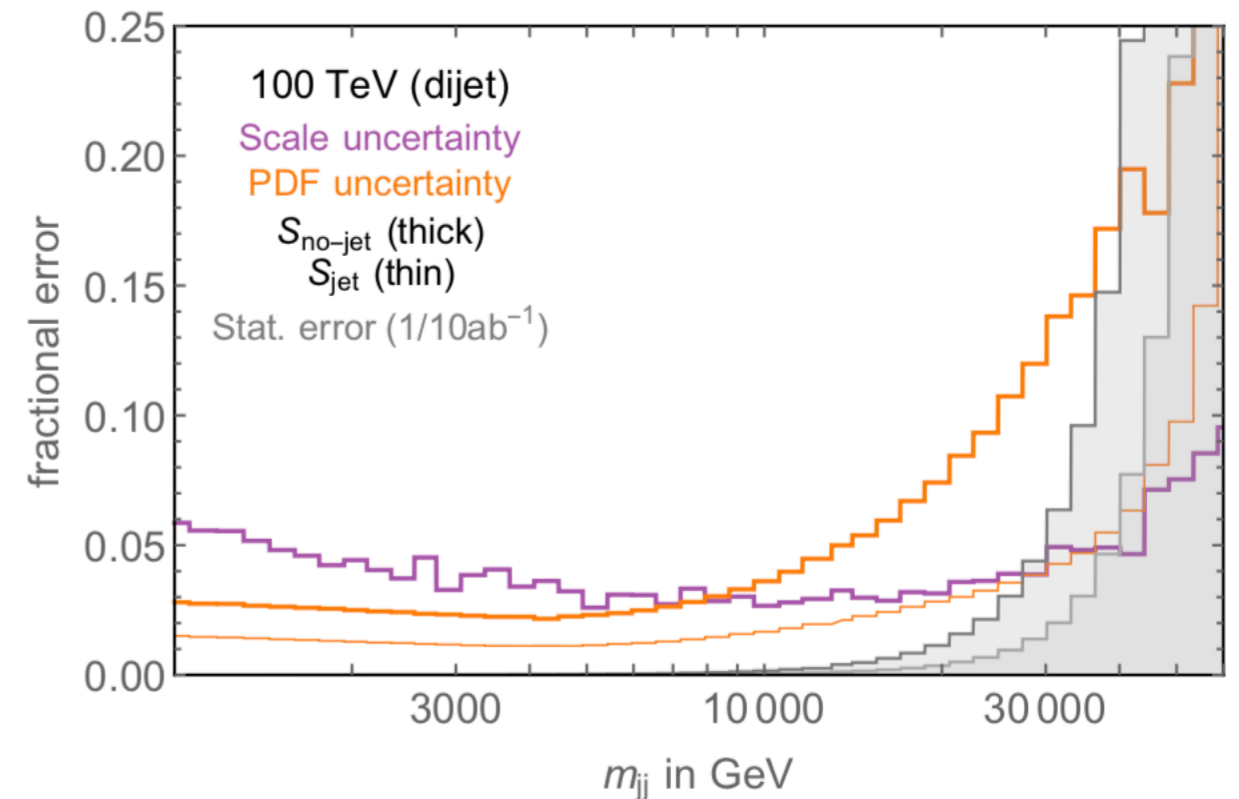
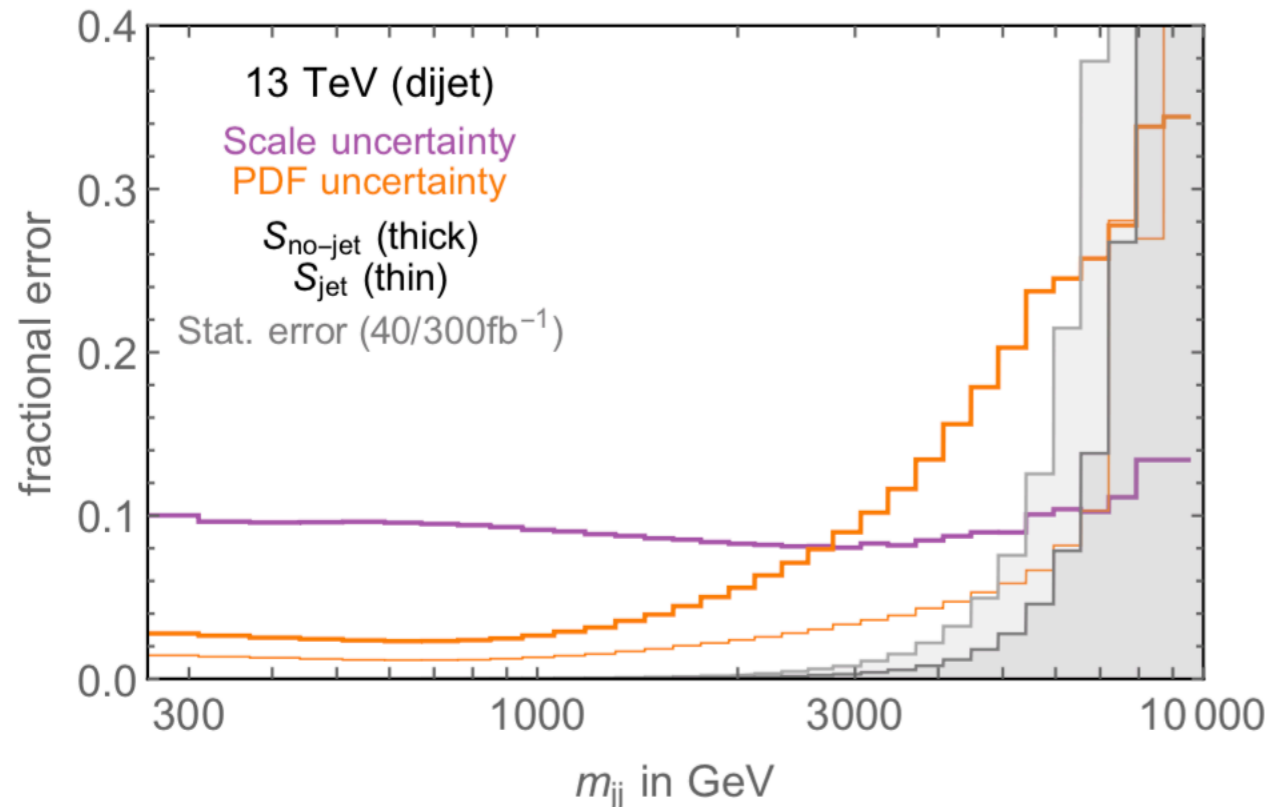
- sensitive to gluon propagator modifications:  $-\frac{Z}{4m_W^2} \left( D_\rho G_{\mu\nu}^A \right)^2$
- obvious caveat: use LHC data for PDFs?
- 0(1) new physics effects
- PDF uncertainties limit sensitivity...





13 TeV

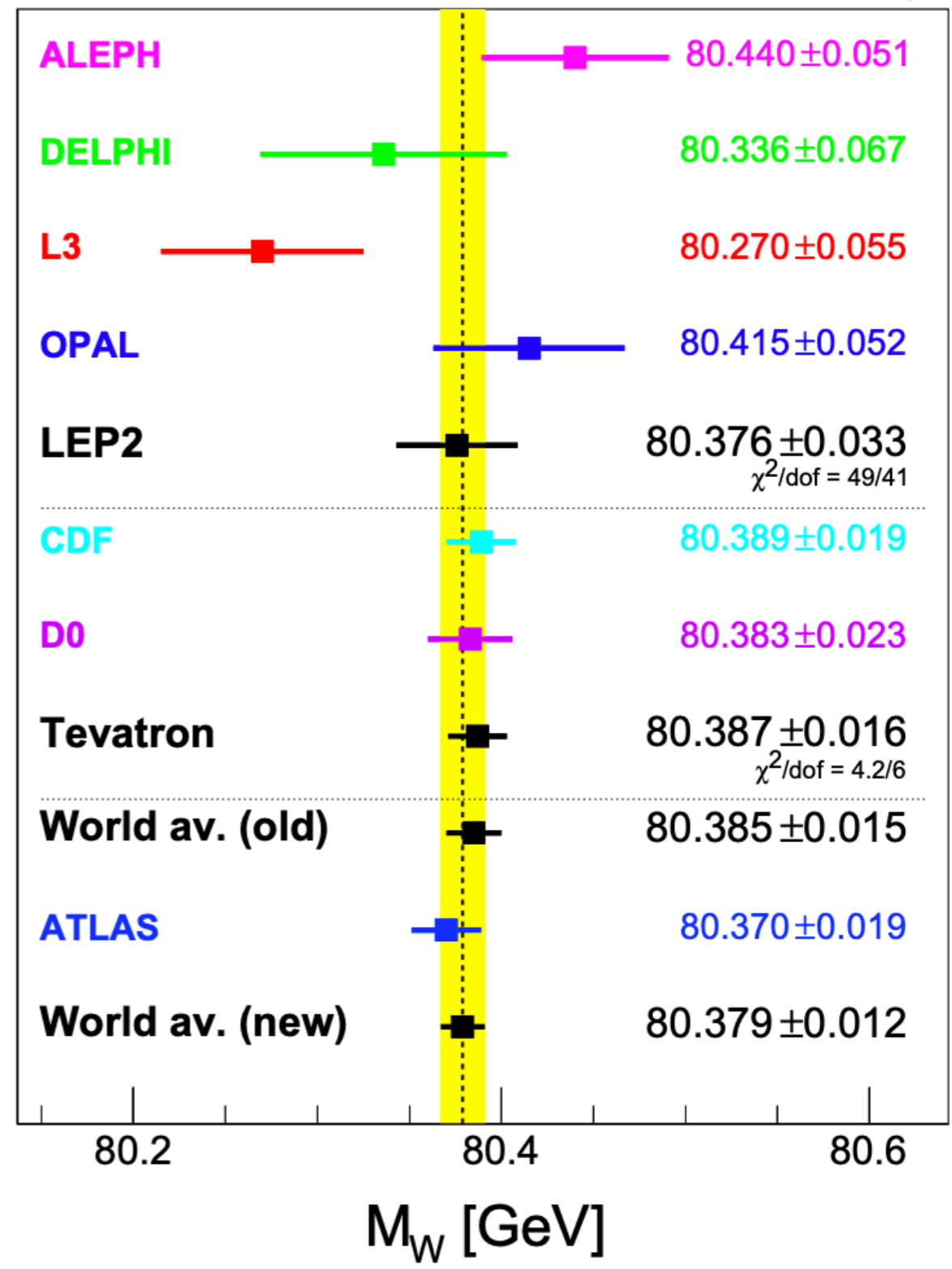
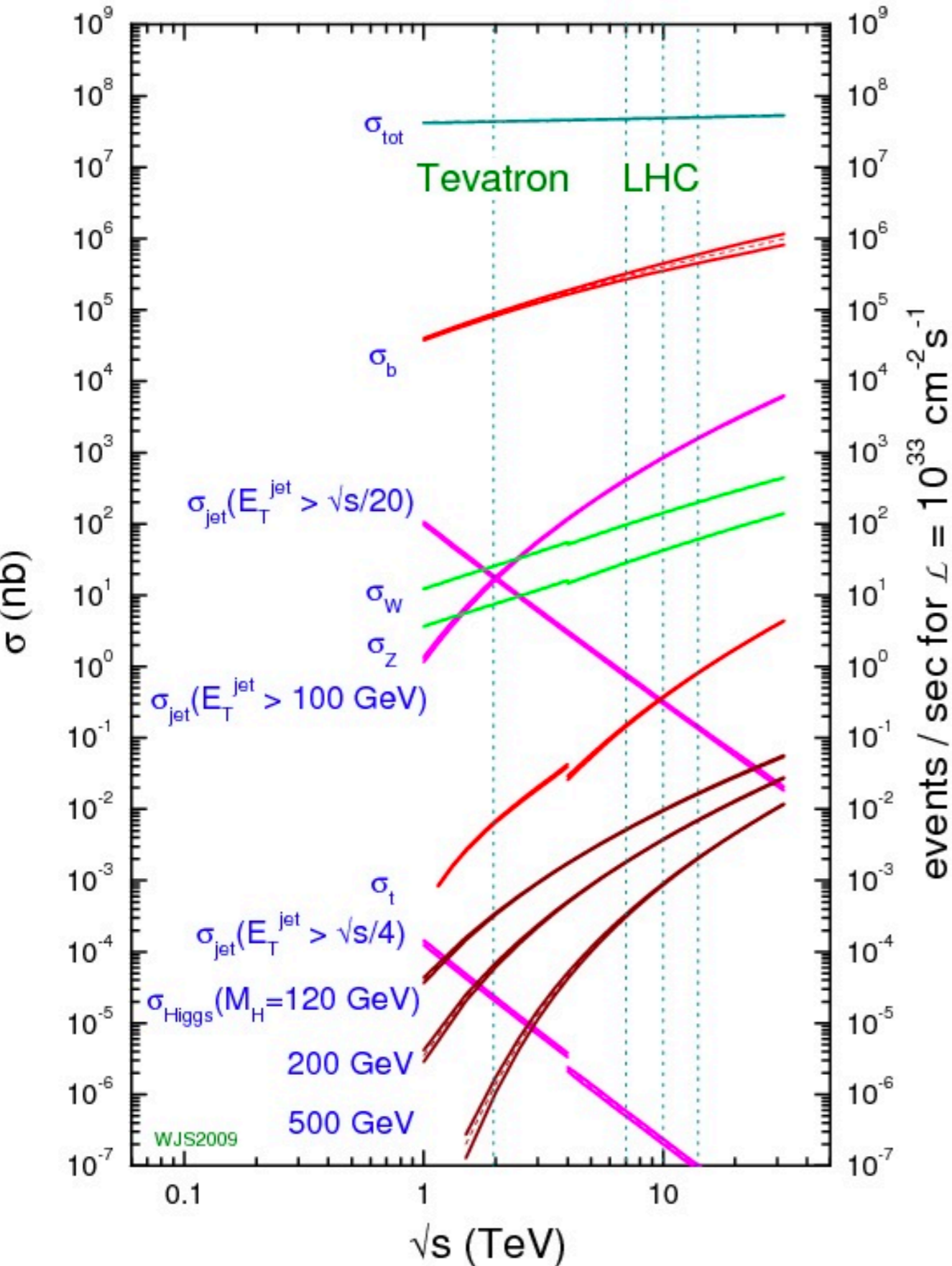
100 TeV



- sensitive to gluon propagator modifications:  $-\frac{Z}{4m_W^2} \left( D_\rho G_{\mu\nu}^A \right)^2$
- obvious caveat: use LHC data for PDFs?
- 0(1) new physics effects
- PDF uncertainties limit sensitivity...

# LHC vs Tevatron

proton - (anti)proton cross sections



# Tevatron results

## CDF experiment:

[Phys. Rev. Lett.108 \(2012\) 151803](#)

electron/muon channels  
2.2 fb<sup>-1</sup> integrated luminosity

$$m_W = 80387 \pm 12(\text{stat}) \pm 15(\text{syst}) \text{ MeV}$$

| Source                             | Uncertainty (MeV) |
|------------------------------------|-------------------|
| Lepton energy scale and resolution | 7                 |
| Recoil energy scale and resolution | 6                 |
| Lepton removal                     | 2                 |
| Backgrounds                        | 3                 |
| $p_T(W)$ model                     | 5                 |
| Parton distributions               | 10                |
| QED radiation                      | 4                 |
| $W$ -boson statistics              | 12                |
| Total                              | 19                |

## D0 experiment:

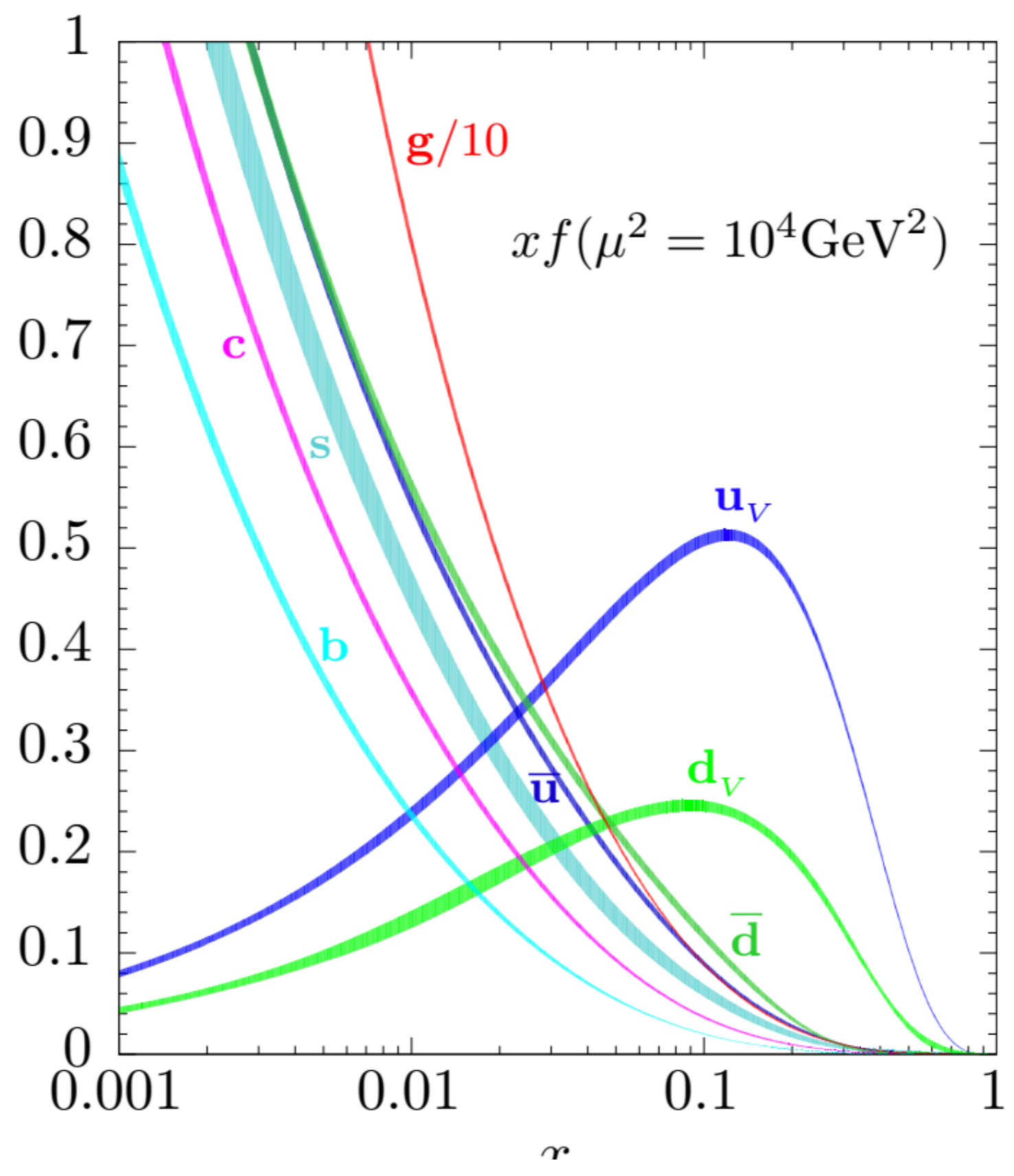
[Phys. Rev. Lett. 108 \(2012\) 151804](#)

electron channel  
~5.3 fb<sup>-1</sup> integrated luminosity

$$m_W = 80375 \pm 11(\text{stat}) \pm 20(\text{syst}) \text{ MeV}$$

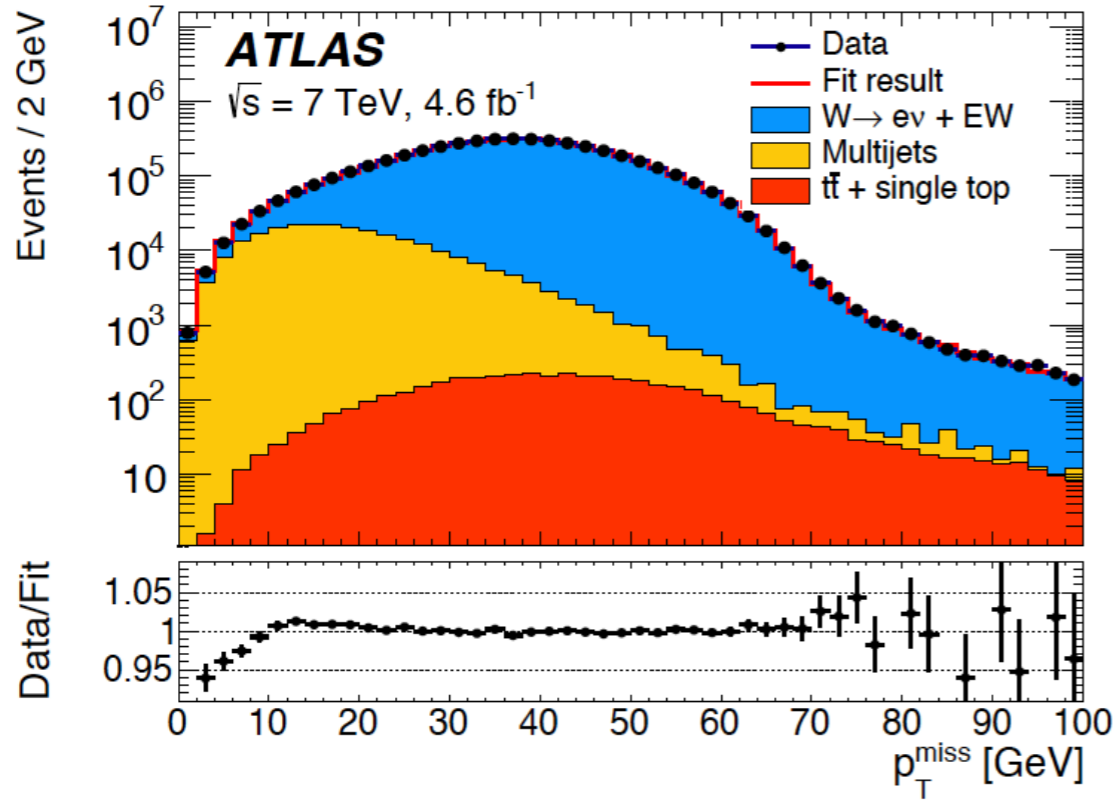
| Source                      | $\Delta M_W$ (MeV) |         |       |
|-----------------------------|--------------------|---------|-------|
|                             | $m_T$              | $p_T^e$ | $E_T$ |
| Electron energy calibration | 16                 | 17      | 16    |
| Electron resolution model   | 2                  | 2       | 3     |
| Electron shower modeling    | 4                  | 6       | 7     |
| Electron energy loss model  | 4                  | 4       | 4     |
| Hadronic recoil model       | 5                  | 6       | 14    |
| Electron efficiencies       | 1                  | 3       | 5     |
| Backgrounds                 | 2                  | 2       | 2     |
| Experimental subtotal       | 18                 | 20      | 24    |
| PDF                         | 11                 | 11      | 14    |
| QED                         | 7                  | 7       | 9     |
| Boson $p_T$                 | 2                  | 5       | 2     |
| Production subtotal         | 13                 | 14      | 17    |
| Total                       | 22                 | 24      | 29    |

$$M_W = 80387 \pm 16 \text{ MeV}$$

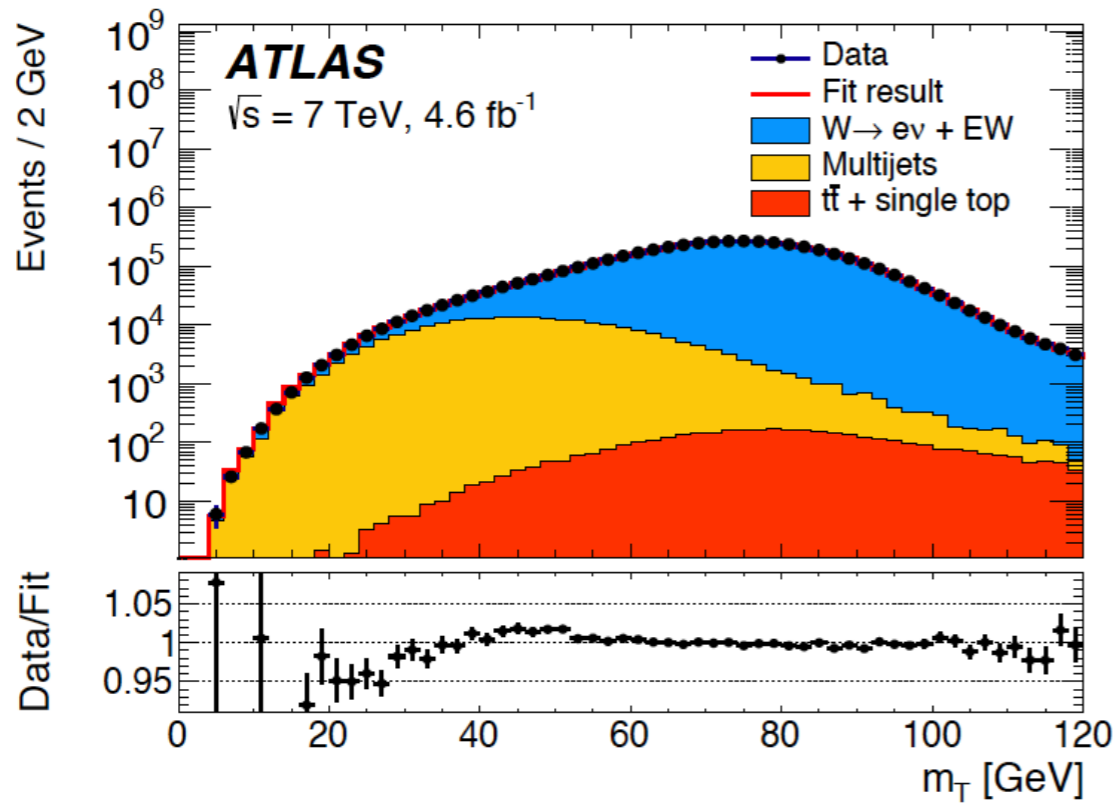




# W mass ATLAS - Background Summary



(a)

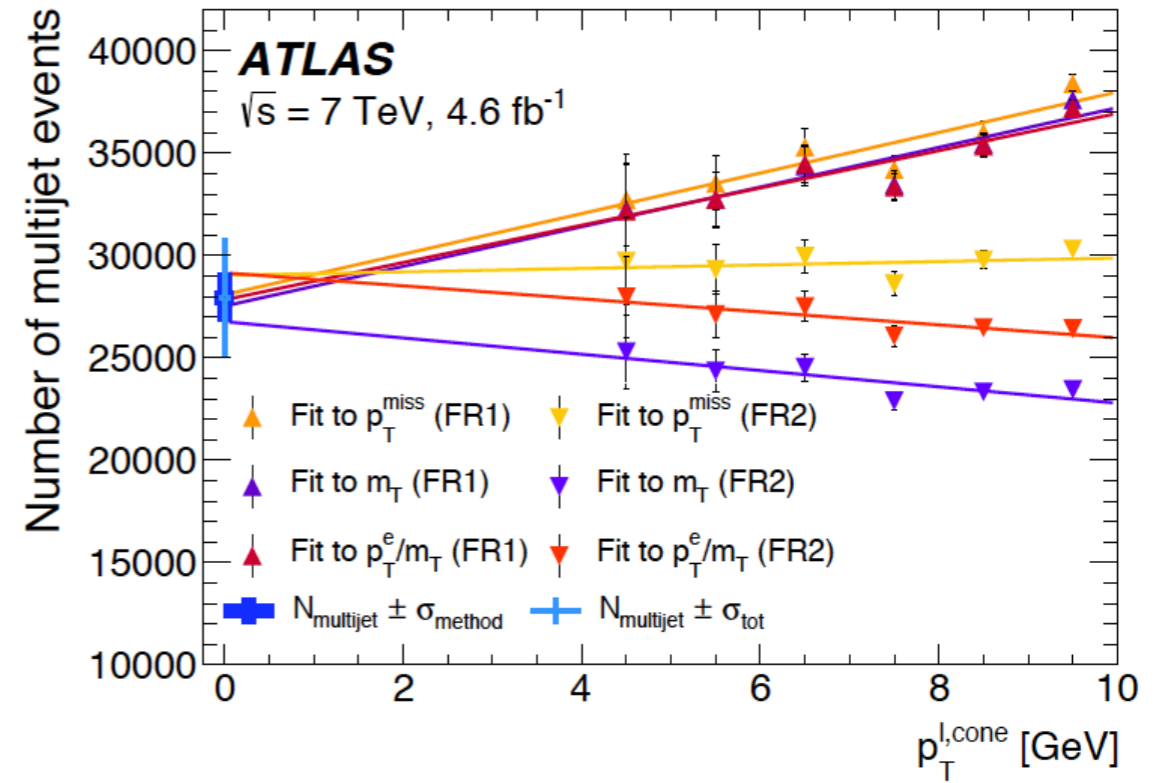


Events / 2 GeV

Data/Fit

Events / 2 GeV

Data/Fit



# W mass ATLAS - Uncertainties Summary

| W-boson charge<br>Kinematic distribution               | $W^+$      |       | $W^-$      |       | Combined   |       |
|--------------------------------------------------------|------------|-------|------------|-------|------------|-------|
|                                                        | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ |
| $\delta m_W$ [MeV]                                     |            |       |            |       |            |       |
| Fixed-order PDF uncertainty                            | 13.1       | 14.9  | 12.0       | 14.2  | 8.0        | 8.7   |
| AZ tune                                                | 3.0        | 3.4   | 3.0        | 3.4   | 3.0        | 3.4   |
| Charm-quark mass                                       | 1.2        | 1.5   | 1.2        | 1.5   | 1.2        | 1.5   |
| Parton shower $\mu_F$ with heavy-flavour decorrelation | 5.0        | 6.9   | 5.0        | 6.9   | 5.0        | 6.9   |
| Parton shower PDF uncertainty                          | 3.6        | 4.0   | 2.6        | 2.4   | 1.0        | 1.6   |
| Angular coefficients                                   | 5.8        | 5.3   | 5.8        | 5.3   | 5.8        | 5.3   |
| Total                                                  | 15.9       | 18.1  | 14.8       | 17.2  | 11.6       | 12.9  |

| $ \eta_\ell $ range<br>Kinematic distribution | [0.0, 0.8] |       | [0.8, 1.4] |       | [1.4, 2.0] |       | [2.0, 2.4] |       | Combined   |       |
|-----------------------------------------------|------------|-------|------------|-------|------------|-------|------------|-------|------------|-------|
|                                               | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ |
| $\delta m_W$ [MeV]                            |            |       |            |       |            |       |            |       |            |       |
| Momentum scale                                | 8.9        | 9.3   | 14.2       | 15.6  | 27.4       | 29.2  | 111.0      | 115.4 | 8.4        | 8.8   |
| Momentum resolution                           | 1.8        | 2.0   | 1.9        | 1.7   | 1.5        | 2.2   | 3.4        | 3.8   | 1.0        | 1.2   |
| Sagitta bias                                  | 0.7        | 0.8   | 1.7        | 1.7   | 3.1        | 3.1   | 4.5        | 4.3   | 0.6        | 0.6   |
| Reconstruction and<br>isolation efficiencies  | 4.0        | 3.6   | 5.1        | 3.7   | 4.7        | 3.5   | 6.4        | 5.5   | 2.7        | 2.2   |
| Trigger efficiency                            | 5.6        | 5.0   | 7.1        | 5.0   | 11.8       | 9.1   | 12.1       | 9.9   | 4.1        | 3.2   |
| Total                                         | 11.4       | 11.4  | 16.9       | 17.0  | 30.4       | 31.0  | 112.0      | 116.1 | 9.8        | 9.7   |

# W mass ATLAS - Uncertainties Summary

| $ \eta_\ell $ range                | [0.0, 0.6] |       | [0.6, 1.2] |       | [1.82, 2.4] |       | Combined   |       |
|------------------------------------|------------|-------|------------|-------|-------------|-------|------------|-------|
| Kinematic distribution             | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$  | $m_T$ | $p_T^\ell$ | $m_T$ |
| $\delta m_W$ [MeV]                 |            |       |            |       |             |       |            |       |
| Energy scale                       | 10.4       | 10.3  | 10.8       | 10.1  | 16.1        | 17.1  | 8.1        | 8.0   |
| Energy resolution                  | 5.0        | 6.0   | 7.3        | 6.7   | 10.4        | 15.5  | 3.5        | 5.5   |
| Energy linearity                   | 2.2        | 4.2   | 5.8        | 8.9   | 8.6         | 10.6  | 3.4        | 5.5   |
| Energy tails                       | 2.3        | 3.3   | 2.3        | 3.3   | 2.3         | 3.3   | 2.3        | 3.3   |
| Reconstruction efficiency          | 10.5       | 8.8   | 9.9        | 7.8   | 14.5        | 11.0  | 7.2        | 6.0   |
| Identification efficiency          | 10.4       | 7.7   | 11.7       | 8.8   | 16.7        | 12.1  | 7.3        | 5.6   |
| Trigger and isolation efficiencies | 0.2        | 0.5   | 0.3        | 0.5   | 2.0         | 2.2   | 0.8        | 0.9   |
| Charge mismeasurement              | 0.2        | 0.2   | 0.2        | 0.2   | 1.5         | 1.5   | 0.1        | 0.1   |
| Total                              | 19.0       | 17.5  | 21.1       | 19.4  | 30.7        | 30.5  | 14.2       | 14.3  |

| $W$ -boson charge                                       | $W^+$      |       | $W^-$      |       | Combined   |       |      |
|---------------------------------------------------------|------------|-------|------------|-------|------------|-------|------|
| Kinematic distribution                                  | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ | $p_T^\ell$ | $m_T$ |      |
| $\delta m_W$ [MeV]                                      |            |       |            |       |            |       |      |
| $\langle\mu\rangle$ scale factor                        |            | 0.2   | 1.0        | 0.2   | 1.0        | 0.2   | 1.0  |
| $\Sigma E_T^*$ correction                               |            | 0.9   | 12.2       | 1.1   | 10.2       | 1.0   | 11.2 |
| Residual corrections (statistics)                       |            | 2.0   | 2.7        | 2.0   | 2.7        | 2.0   | 2.7  |
| Residual corrections (interpolation)                    |            | 1.4   | 3.1        | 1.4   | 3.1        | 1.4   | 3.1  |
| Residual corrections ( $Z \rightarrow W$ extrapolation) |            | 0.2   | 5.8        | 0.2   | 4.3        | 0.2   | 5.1  |
| Total                                                   |            | 2.6   | 14.2       | 2.7   | 11.8       | 2.6   | 13.0 |





# THEORY ERRORS: WHAT CAN WE ASSUME?

| Quantity                            | Current theory error    | Leading missing terms                                                | Est. future theory error     |
|-------------------------------------|-------------------------|----------------------------------------------------------------------|------------------------------|
| $\sin^2 \theta_{\text{eff}}^{\ell}$ | $4.5 \times 10^{-5}$    | $\mathcal{O}(\alpha^2 \alpha_s), \mathcal{O}(N_f^{\geq 2} \alpha^3)$ | $1 \dots 1.5 \times 10^{-5}$ |
| $R_b$                               | $\sim 2 \times 10^{-4}$ | $\mathcal{O}(\alpha^2), \mathcal{O}(N_f^{\geq 2} \alpha^3)$          | $\sim 1 \times 10^{-4}$      |
| $\Gamma_Z$                          | few MeV                 | $\mathcal{O}(\alpha^2), \mathcal{O}(N_f^{\geq 2} \alpha^3)$          | $< 1$ MeV                    |
| $M_W$                               | 4 MeV                   | $\mathcal{O}(\alpha^2 \alpha_s), \mathcal{O}(N_f^{\geq 2} \alpha^3)$ | $\lesssim 1$ MeV             |

**Table 1-1.** Some of the most important precision observables for  $Z$ -boson production and decay and the  $W$  mass (first column), their present-day estimated theory error (second column), the dominant missing higher-order corrections (third column), and the estimated improvement when these corrections are available (fourth column). In many cases, the leading parts in a large-mass expansion are already known, in which case the third column refers to the remaining pieces at the given order. The numbers in the last column are rough order-of-magnitude guesses.

# EXPERIMENTAL ERRORS: WHAT CAN WE ASSUME?



| $\Delta \sin^2 \theta_{\text{eff}}^l [10^{-5}]$ | ATLAS | CMS | LHC/per experiment |     |      |
|-------------------------------------------------|-------|-----|--------------------|-----|------|
| $\sqrt{s}$ [TeV]                                | 7     | 7   | 8                  | 14  | 14   |
| $\mathcal{L} [\text{fb}^{-1}]$                  | 4.8   | 1.1 | 20                 | 300 | 3000 |
| PDF                                             | 70    | 130 | 35                 | 25  | 10   |
| higher order corr.                              | 20    | 110 | 20                 | 15  | 10   |
| other systematics                               | 70    | 181 | 60 (35)            | 20  | 15   |
| statistical                                     | 40    | 200 | 20                 | 5   | 2    |
| Total                                           | 108   | 319 | 75 (57)            | 36  | 21   |