

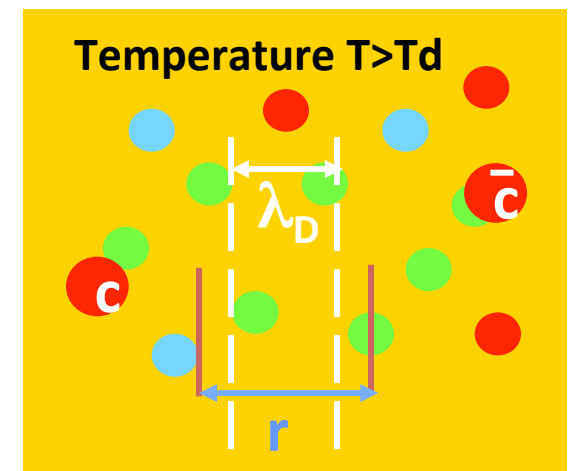
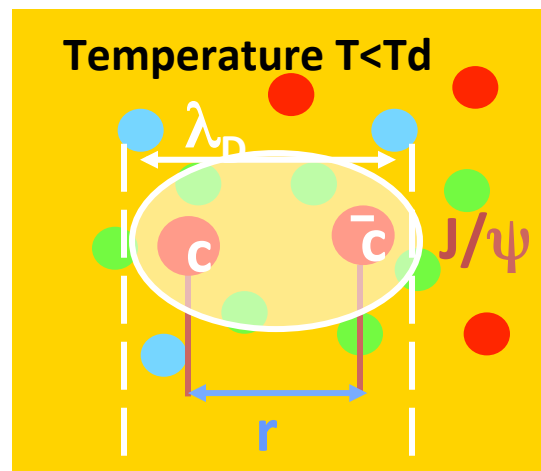
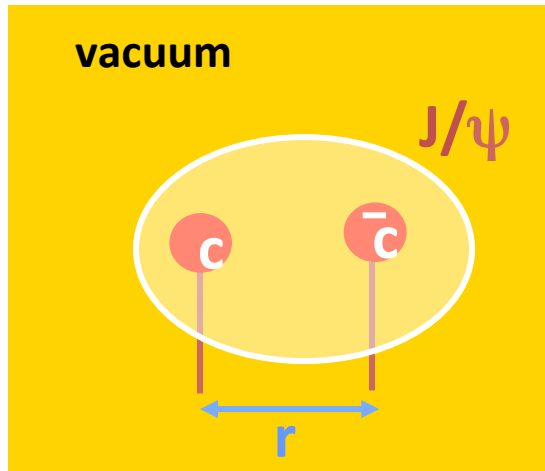
## Quarkonium theory

Elena G. Ferreira

*IGFAE, Universidade de Santiago de Compostela, Spain*

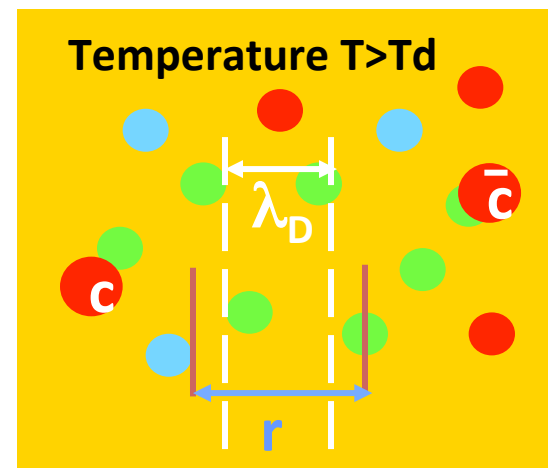
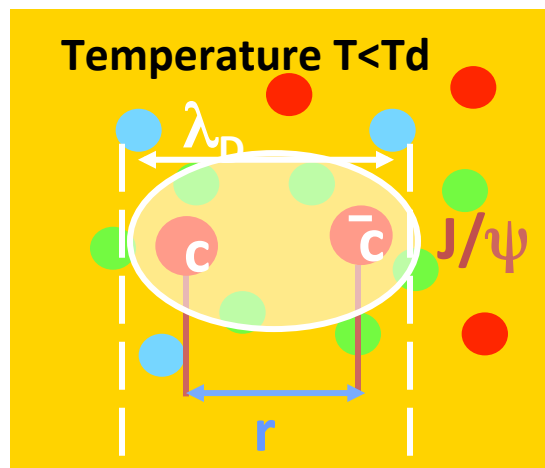
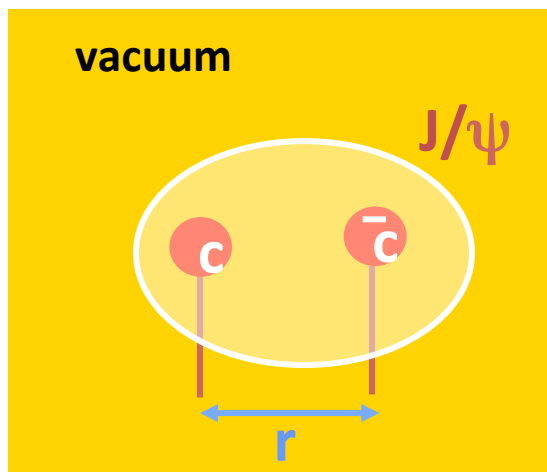
# Why quarkonium?

The usual introduction: Debye screening  $\lambda_D(T)$

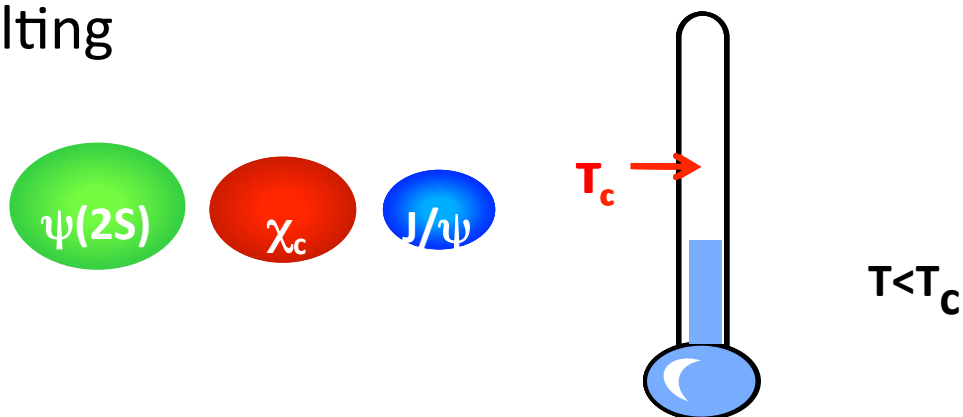


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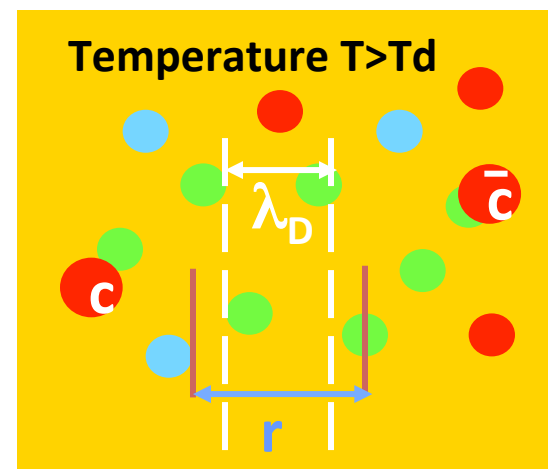
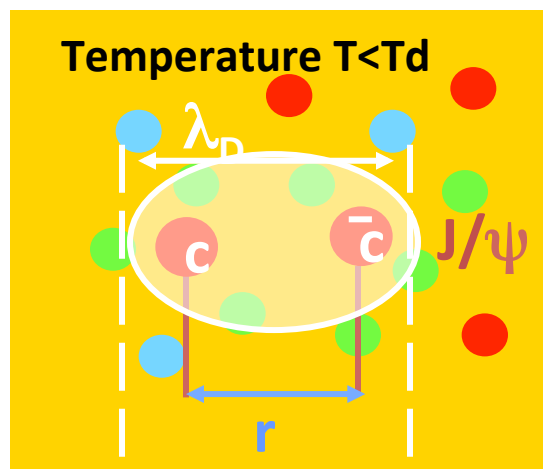
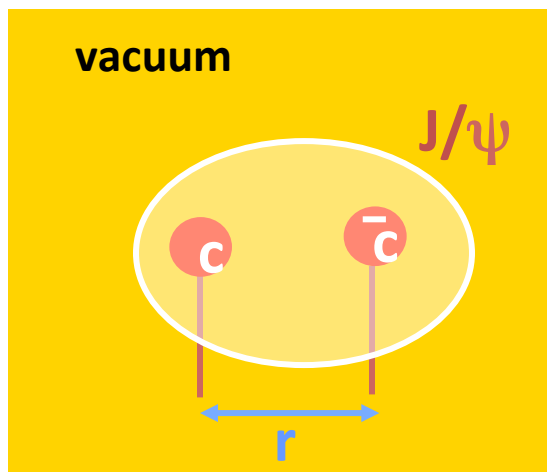


Sequential melting

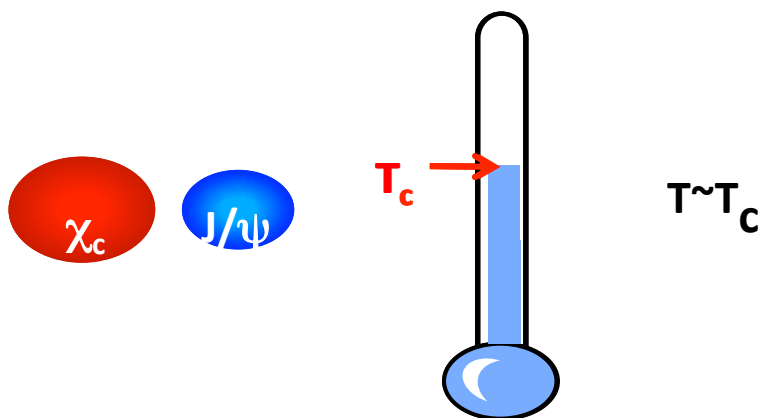


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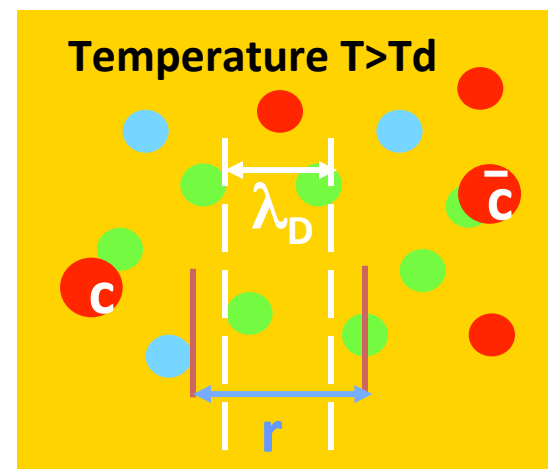
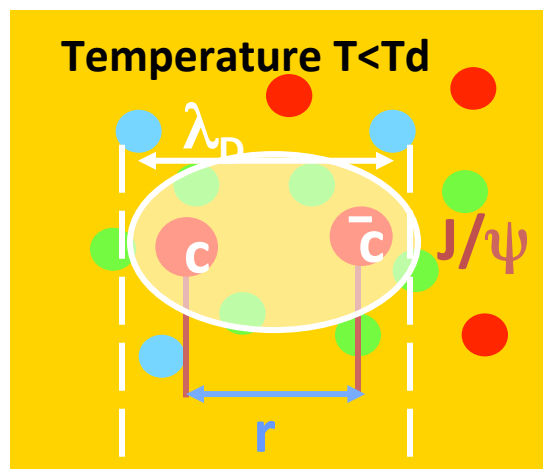
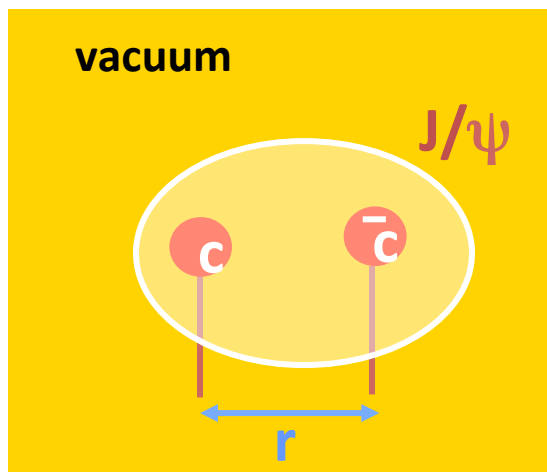


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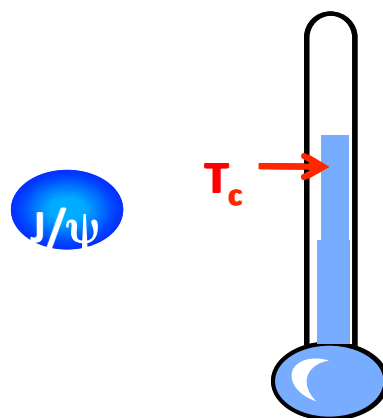


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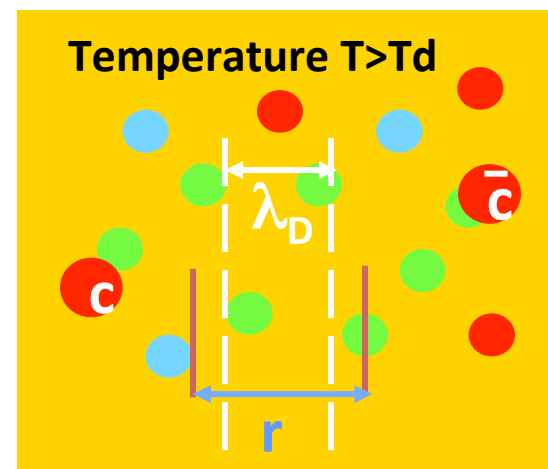
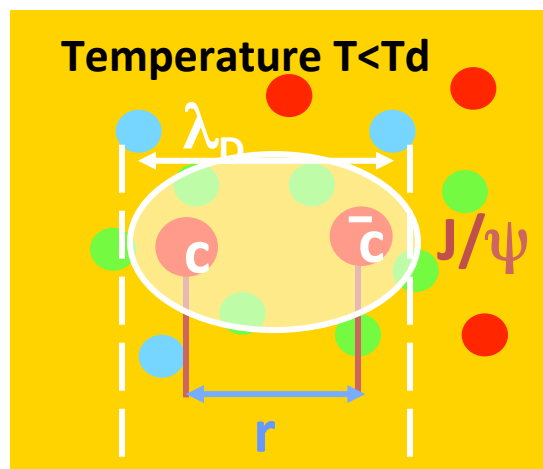
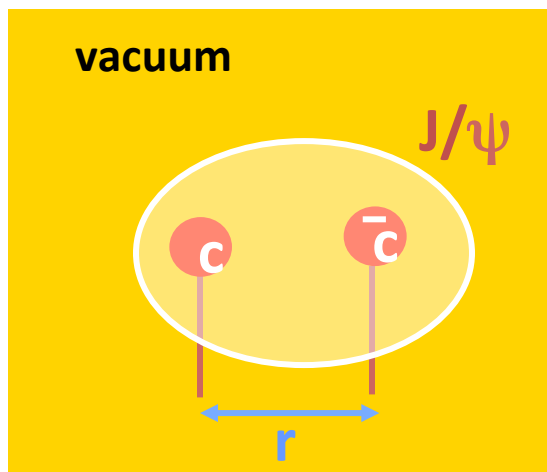
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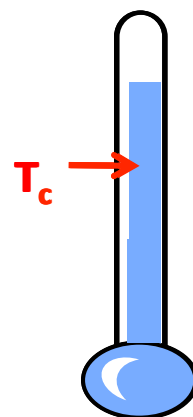
$$T \sim 1.1 T_c$$

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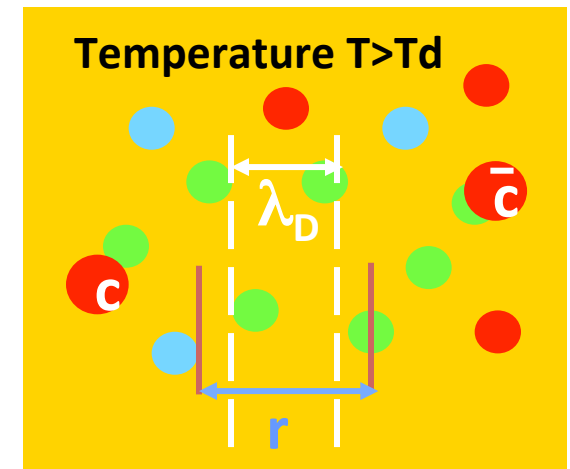
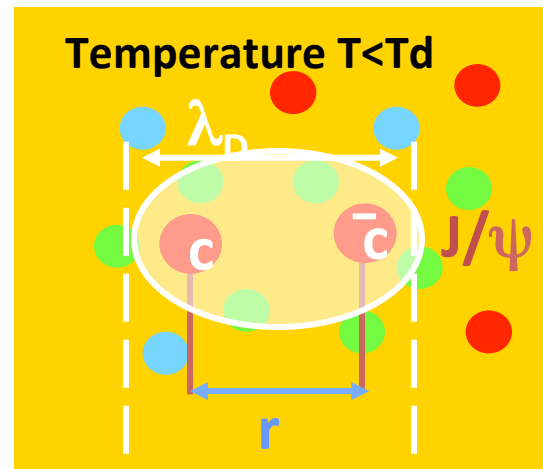
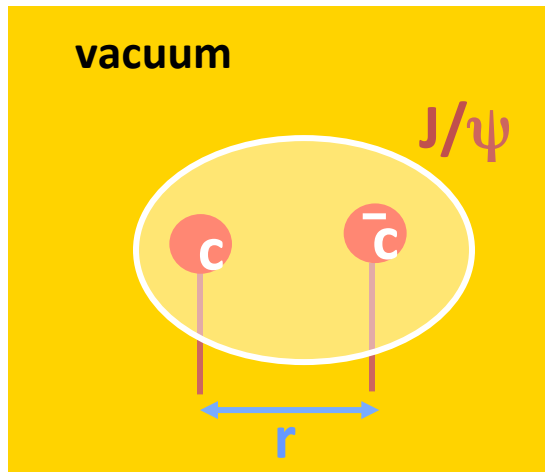
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$T \gg T_c$

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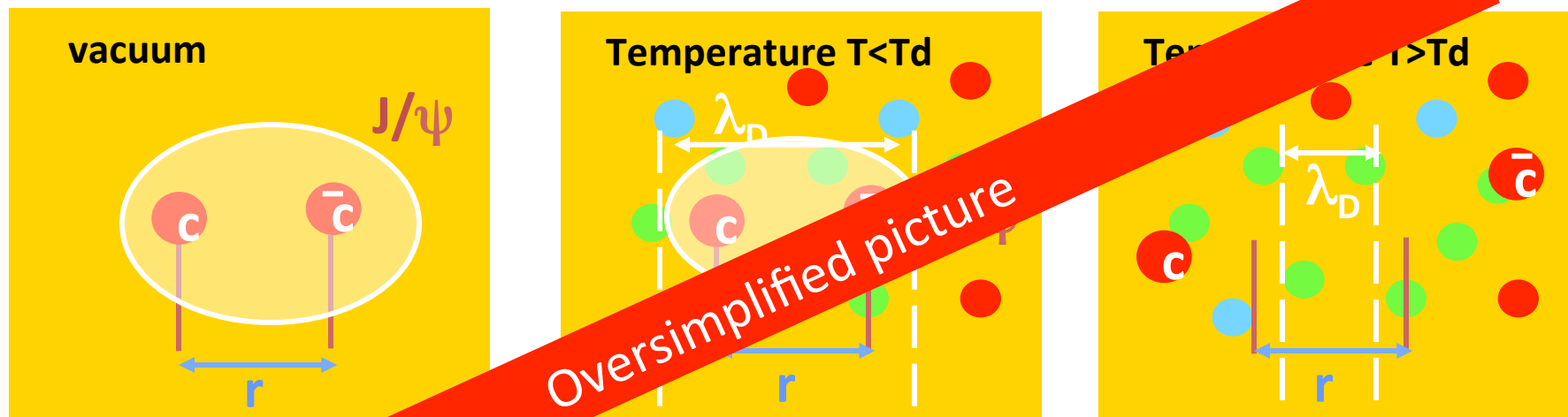


Sequential melting

Quarkonia suppression  $\Rightarrow$  QGP signature

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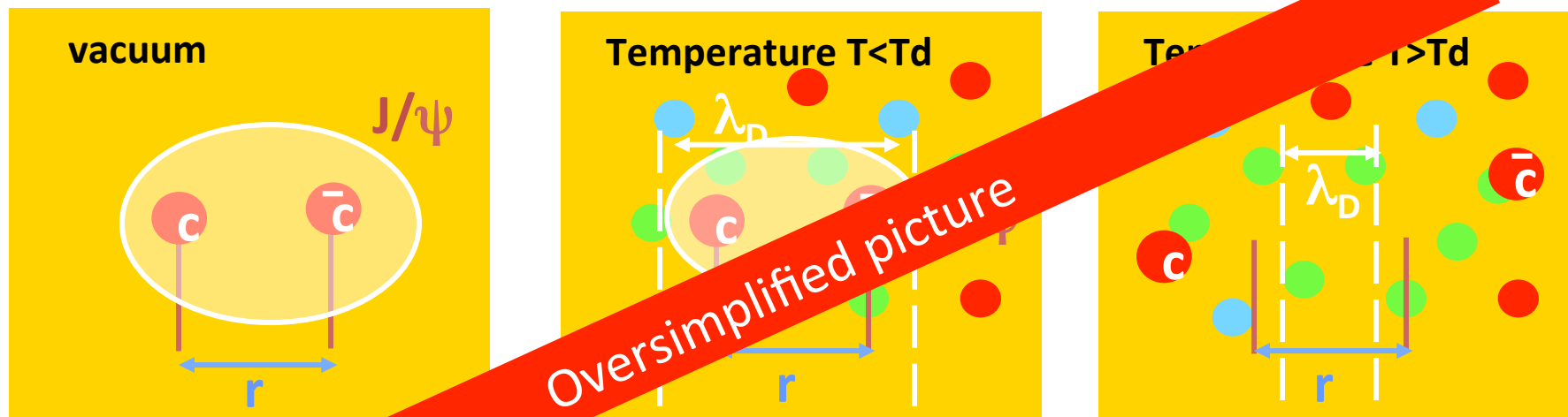


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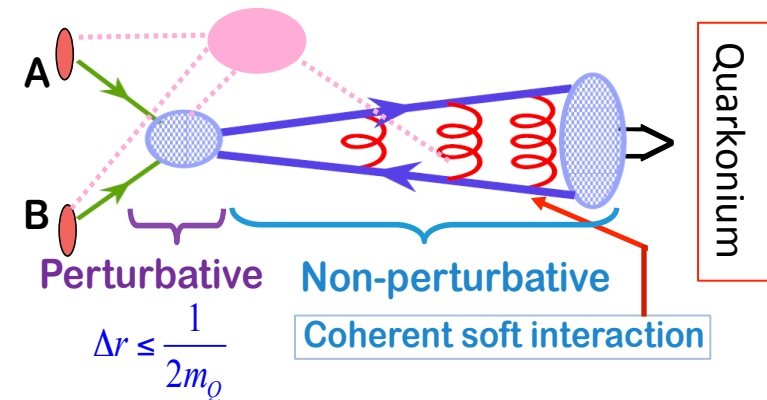
Quarkonia suppression  $\Rightarrow$  QGP signature

We need a global picture including from the production mechanism (pp) to the medium effects (AA) covering different system sizes (pA) and energies

# Quarkonium production schemes in pp: A long history

Quarkonium production involves perturbative and non perturbative QCD

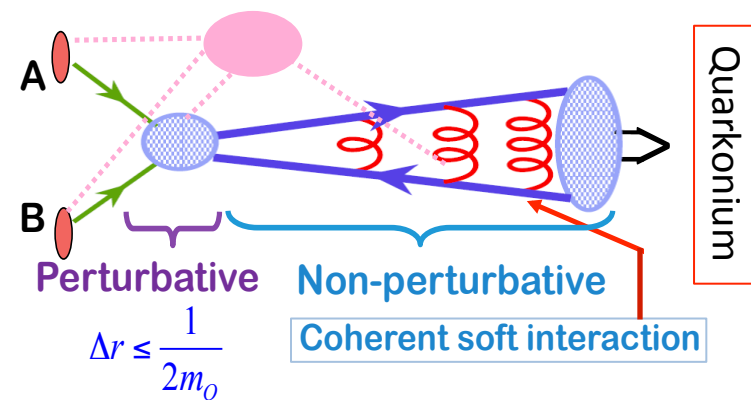
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## Different approaches to hadronization:

### Color singlet model (CSM): 1975 -

Einhorn, Ellis (1975), Chang (1980), Berger & Jone (1981), ...

- Assume physical color singlet state, quantum numbers are conserved
- Only the pair with right quantum numbers

**Effectively no free parameter**

### Color evaporation model (CEM): 1977 -

Fritsch (1977), Halzen (1977), ...

- Does not distinguish states with respect to their color and spin
- All pairs with mass less than open heavy flavor threshold

**One parameter per quarkonium state**

### Nonrelativistic QCD (NRQCD): 1986 -

Caswell, Lapage (1986) Bodwin, Braaten, Lepage (1995), ...

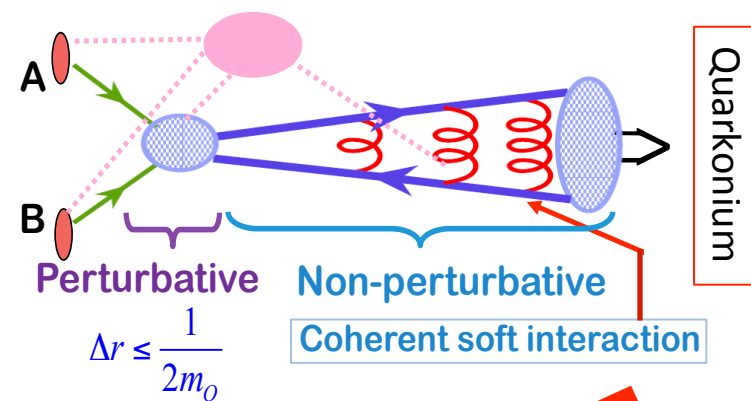
- Rigorous effective field theory based on factorization of soft and hard scales
- All pairs with various probabilities – NRQCD matrix elements

**Infinite parameters – organized in powers of  $v$  and  $\alpha_s$**

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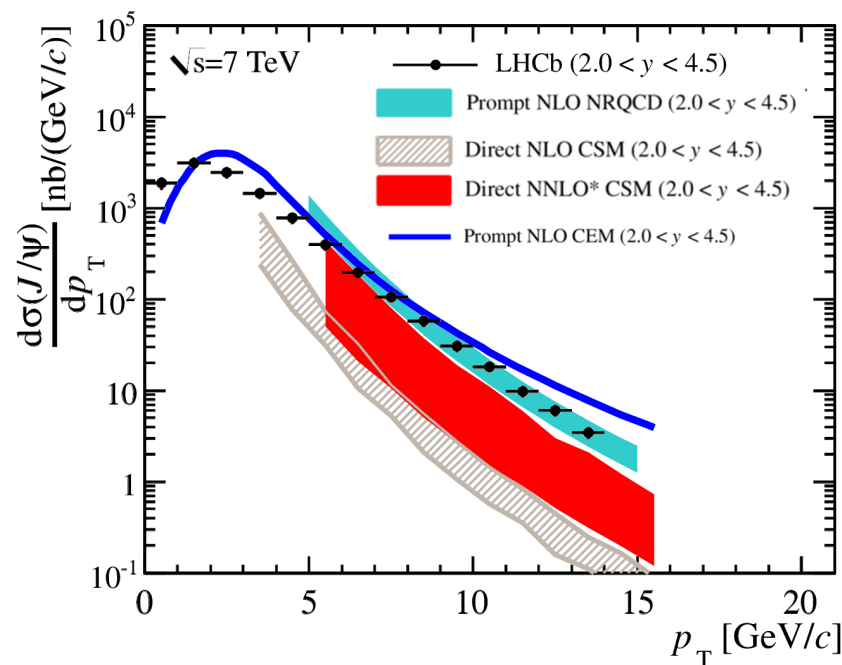
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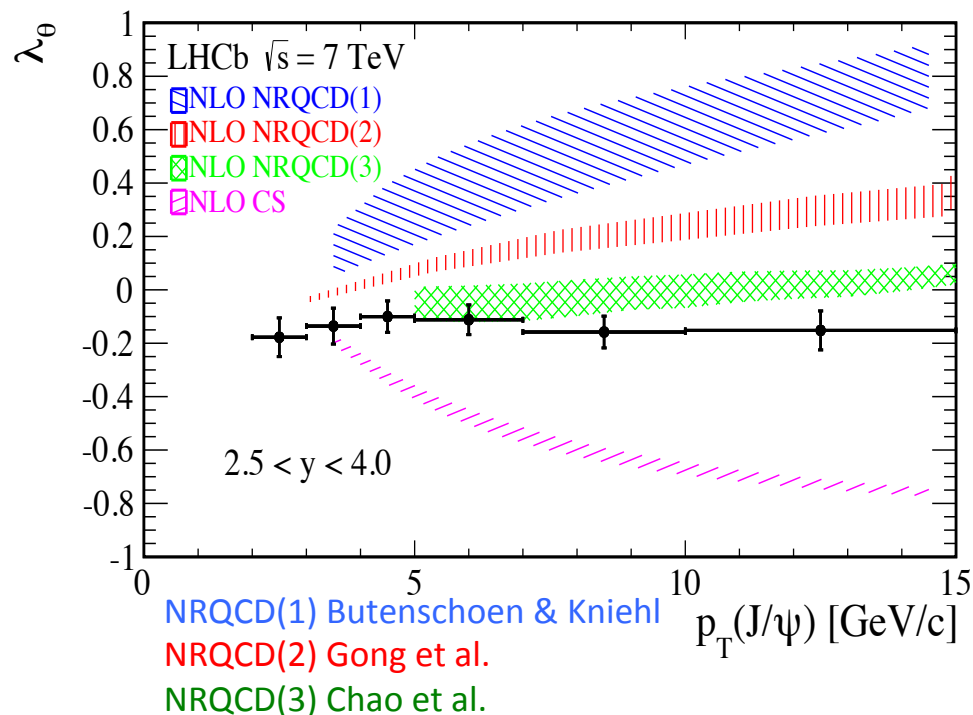
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# Production models: state of the art for the $J/\psi$



Sapores Gravis Review arXiv:1506.03981



- **CSM** still in the game: Large NLO and NNLO\* corrections in  $p_T$ ; need a full NNLO
  - **NRQCD**: COM helps in describing the  $p_T$  spectrum
- Yet, fits differ in their conclusions owing to their assumptions  
(data set,  $p_T$  cut, polarization fitted or not)

At low and mid  $p_T$  –region where quarkonium heavy-ion studies are mainly carried out– none of the models can simply be ruled out due to theoretical uncertainties

Recent developments may be helpful:

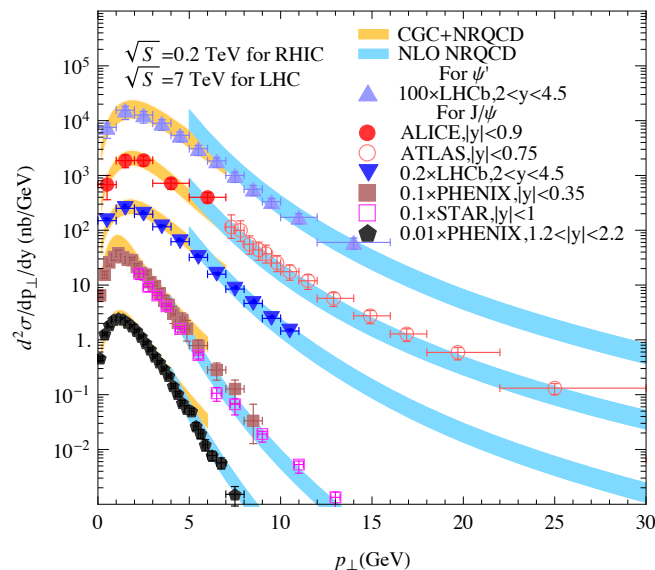
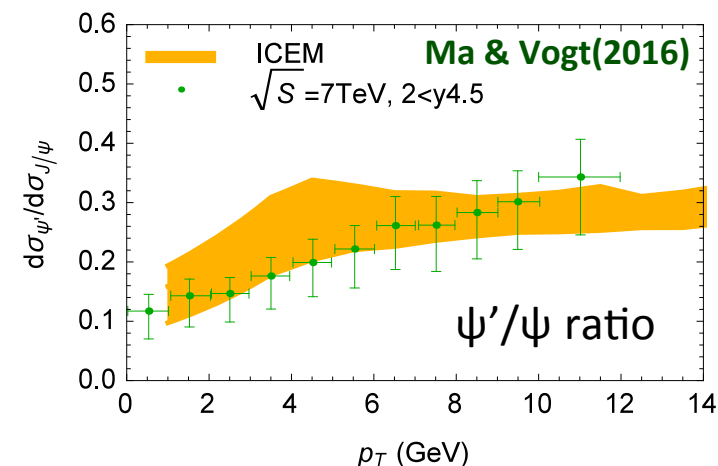
- **CEM** improved
- **CGC** meets **NRQCD**

# Recent developments on production

- **Color Evaporation Model (CEM) Improved**
- Explicit charmonium mass dependence  
=>  $\psi'/\psi$  ratio no longer  $p_T$  independent
- Relates  $\langle p_\psi \rangle$  to the  $c\bar{c}$  pair momentum  
=> explain the high  $p_T$  data better
- LO calculation of quarkonium polarization in the CEM, longitudinal polarized @ LHC  
**Cheung & Vogt(2017)**
- **Saturation meets NRQCD**

$$\sigma_Q^{(N)LO} = F_Q \int_{2m_Q}^{2m_H} \frac{d\sigma_{Q\bar{Q}}^{(N)LO}}{dm_{Q\bar{Q}}} dm_{Q\bar{Q}}$$

changes to  $M_\psi$



- Uses **Color Glass Condensate** saturation model of gluon distributions in the proton with NLO NRQCD matrix elements
- Saturation physics at low  $p_T$ ,  
normal collinear factorization at high  $p_T$ ,  
matching at intermediate  $p_T$

**Ma, Venugopalan & Zhang (2015)**

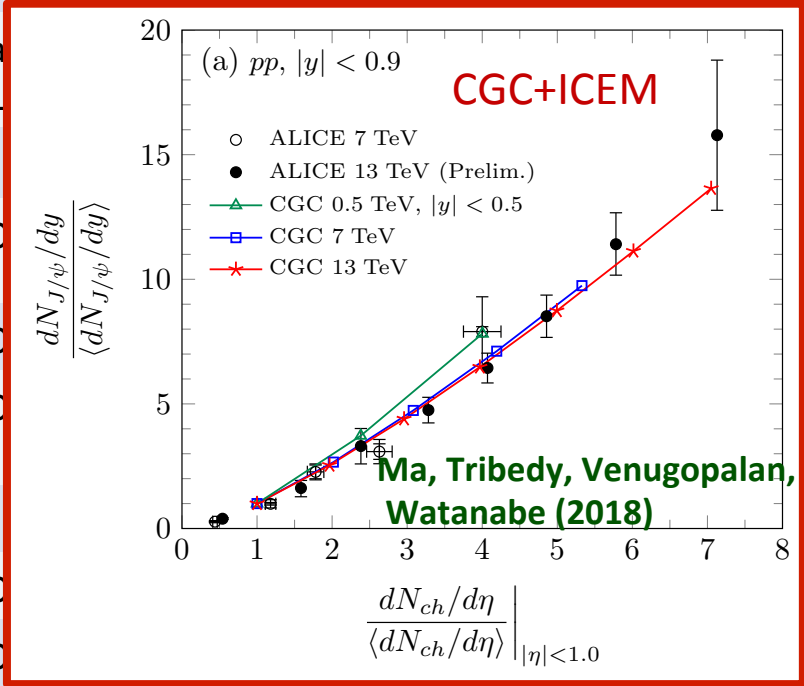
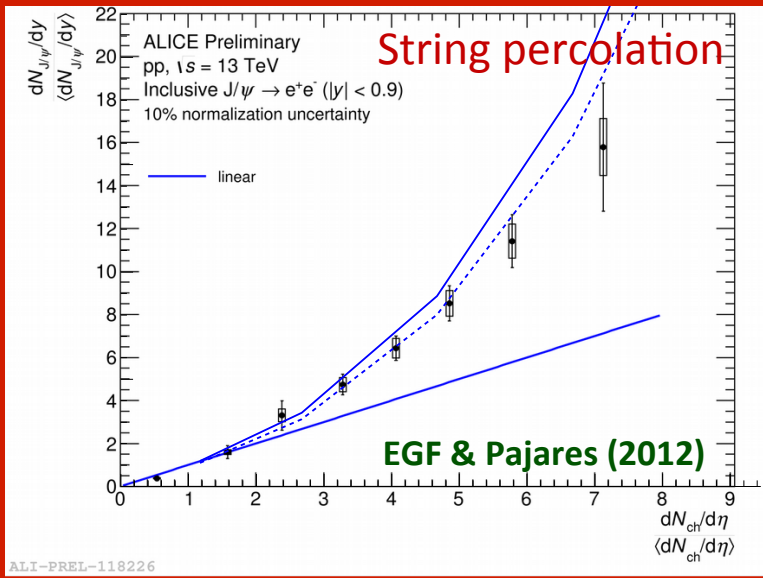
# New observables can help

Observables	Experiments	CSM	CEM	NRQCD	Interest
$J/\psi + J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CS dominant) + DPS + gluon TMD
$J/\psi + D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to J/psi fragmentation) + DPS
$J/\psi + \Upsilon$	D0	(N)LO	LO ?	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi + \text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi + Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi + W$	ATLAS	LO	LO ?	Partial NLO	Prod. Mechanism (CO dominant) + DPS
$J/\psi$ vs mult.	ALICE, CMS (+UA1)	--	--	--	Density effects (Saturation/Hydro)
$J/\psi + b$	-- (LHCb, D0, CMS ?)	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$\Upsilon + D$	LHCb	LO	LO ?	LO	DPS
$\Upsilon + \gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
$\Upsilon$ vs mult.	CMS	--	--	--	Density effects (Saturation/Hydro)
$\Upsilon + Z$	--	NLO	LO ?	LO	Prod. Mechanism + DPS
$\Upsilon + \Upsilon$	CMS	NLO?	LO?	LO?	Prod. Mechanism + DPS + gluon TMD

Lansberg (2018)

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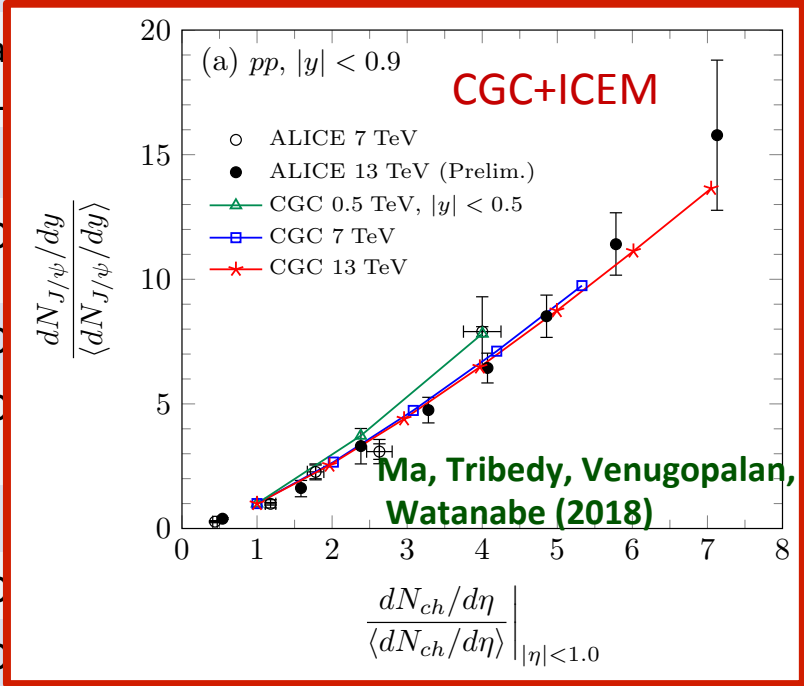
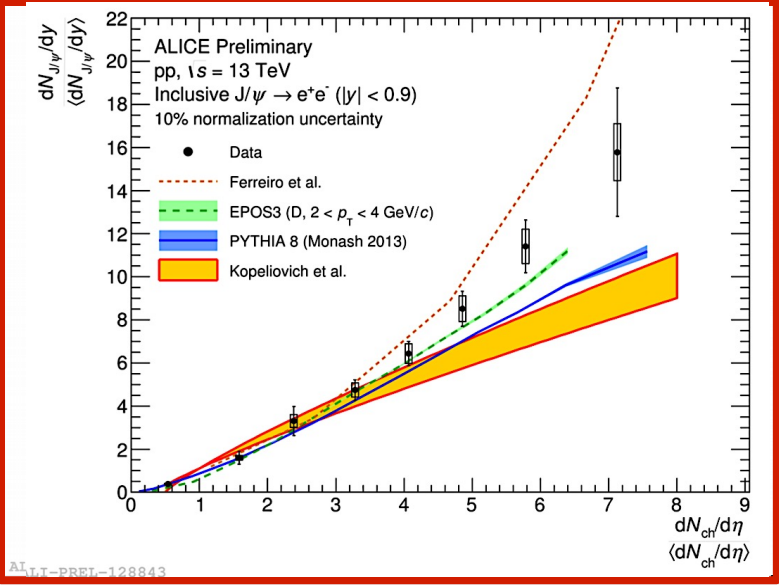
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<div>Events at different energies with the same <math>\rho_{\text{strings}}</math> or <math>Q_s</math> are identical</div> <div>Saturation in high multiplicity pp?</div>					
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Lansberg (2018)

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Lansberg (2018)

# Quarkonium in proton-nucleus: Motivations and expected effects

In such reactions, many physics effects of specific interest are involved:

- **Modification of the gluon flux** *initial-state effect*
  - ◆ Modification of **PDF in nuclei** nPDF shadowing
  - ◆ Gluon **saturation** at low x CGC
- **Parton propagation in medium** *initial/final effect* Coherent energy loss
- **Quarkonium-hadron interaction** *final-state effect*
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In addition of quantifying nuclear effects, quarkonium production in pA may be able to:

- Test **QCD factorization** in media
- Test the **quarkonium production mechanisms**: octet vs. singlet
- Test the dynamics of **hadronization** and time evolution of the  $Q\bar{Q}$  pair

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- **QGP-like** effects?

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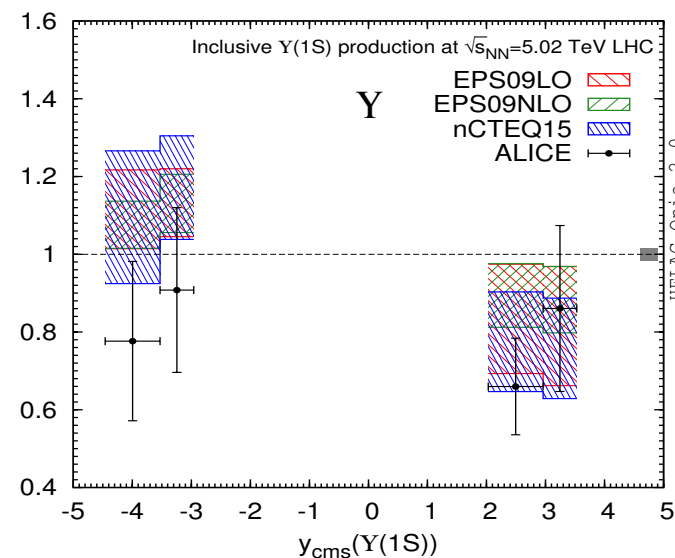
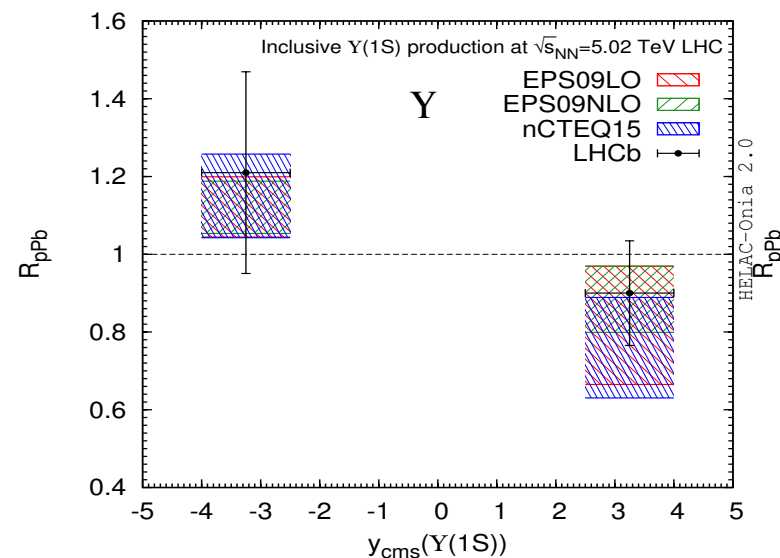
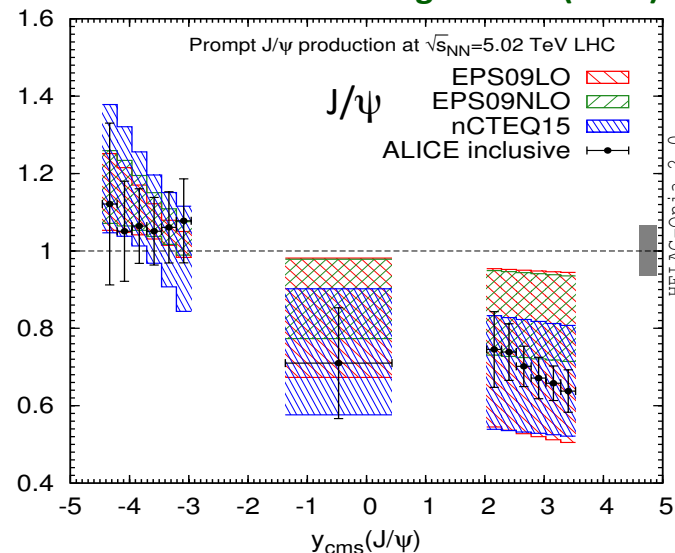
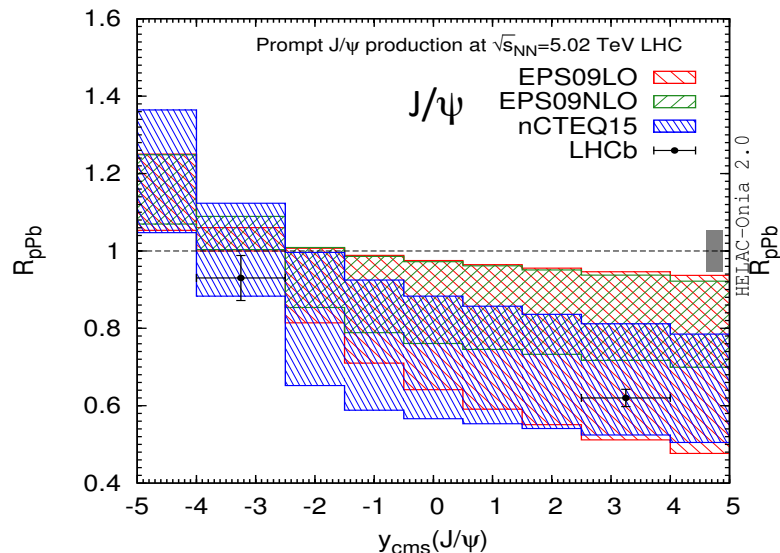
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Obviously relevant if one wishes to use quarkonia  
as probes of the QGP => baseline

# Comparison of nPDFs with LHC data

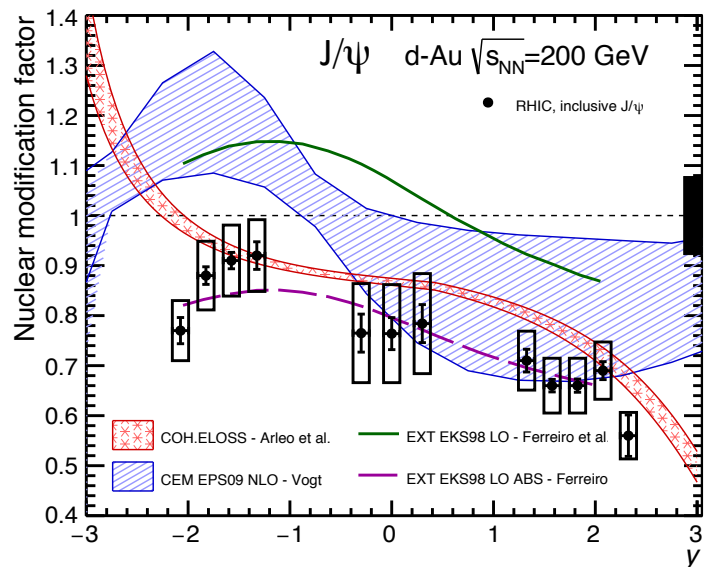
- Several nPDF sets available (using various data, LO/NLO, etc)
- Nuclear break-up neglected at LHC energies

Lansberg & Shao (2016)



- Data is compatible with strong shadowing
- The precision of the current data is already much better than the nPDF uncertainties
- It may offer hints for constraining the gluon density in Pb

# Comparison of nPDFs & $E_{\text{loss}}$ with RHIC & LHC d/p+A data

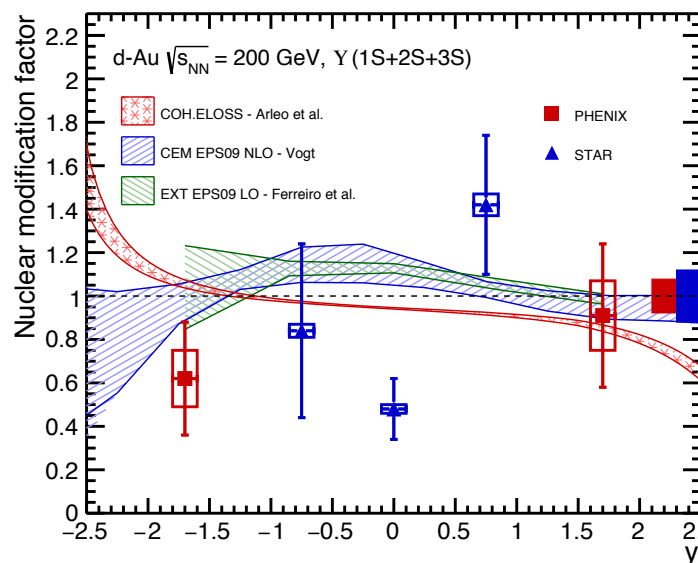


Coherent  $E_{\text{loss}}$

$$\Delta E \propto E$$

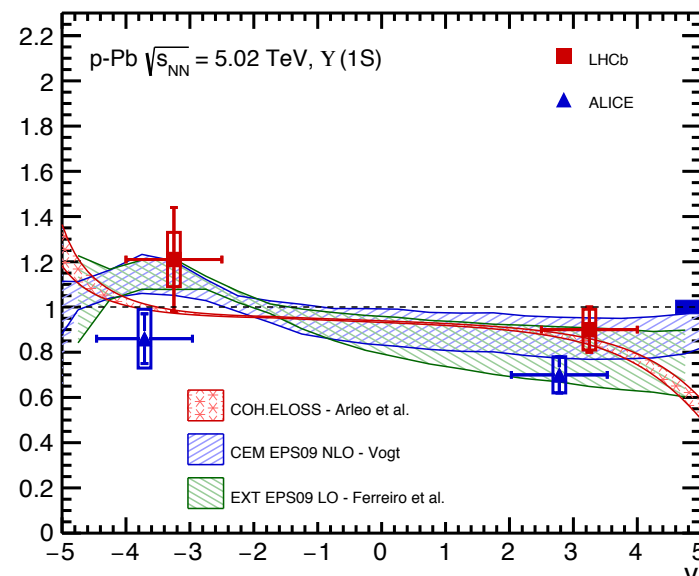
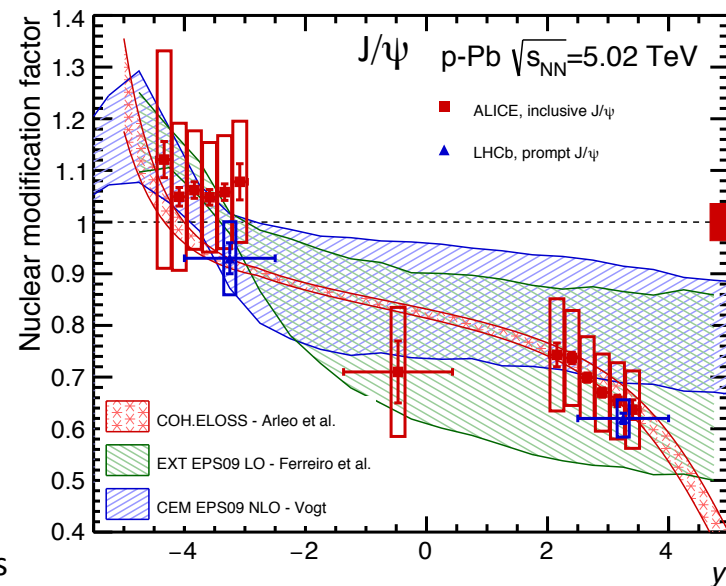
Interference  
terms initial/final  
state for  $t_f \gg R$   
Arleo *et al.* (2014)

nPDF modifi-  
cation &/or  $E_{\text{loss}}$   
fairly agree  
with data



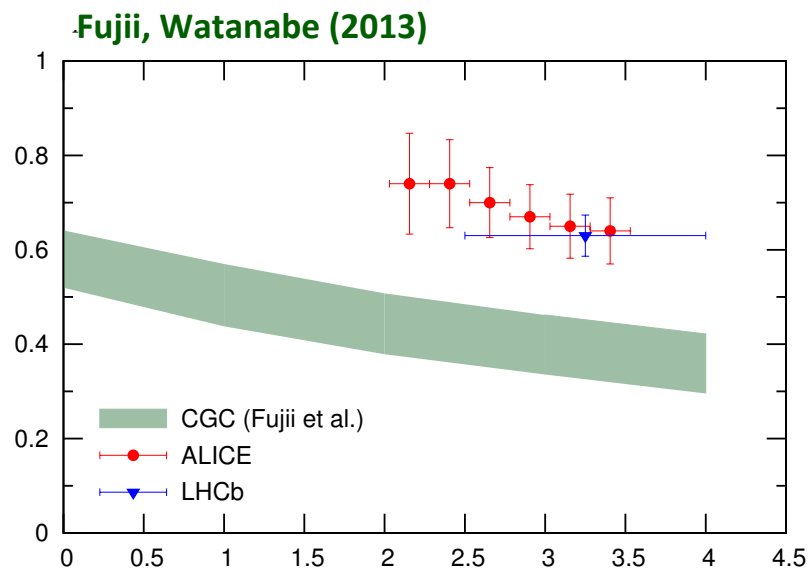
Do data show  
energy increase  
of suppression?

More precise  
data needed



# CGC computations: not just gluon saturation

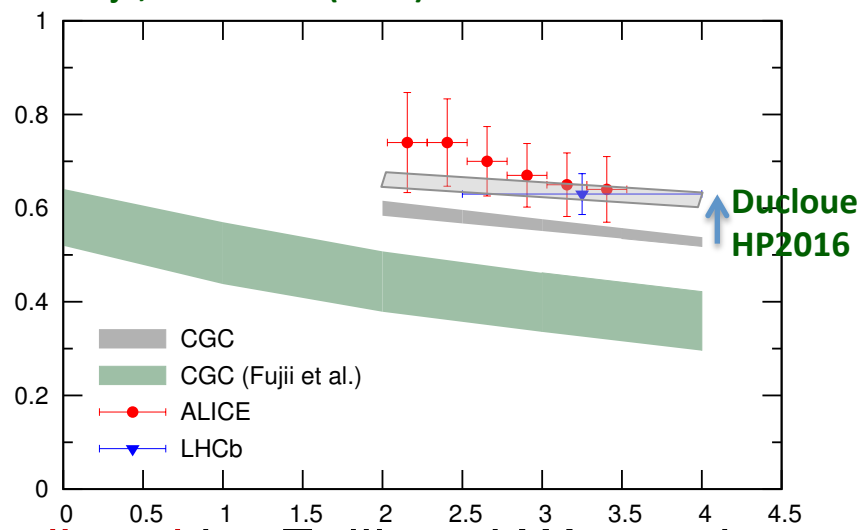
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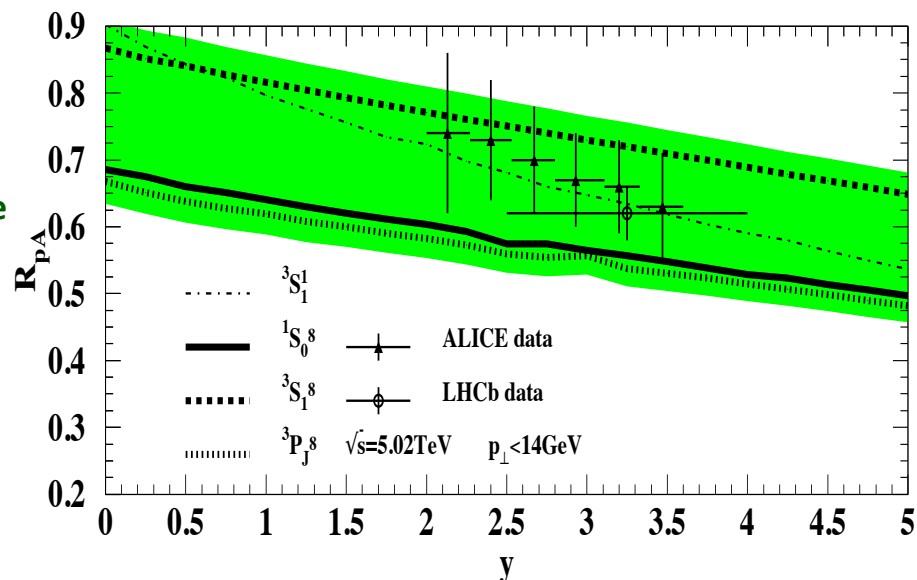
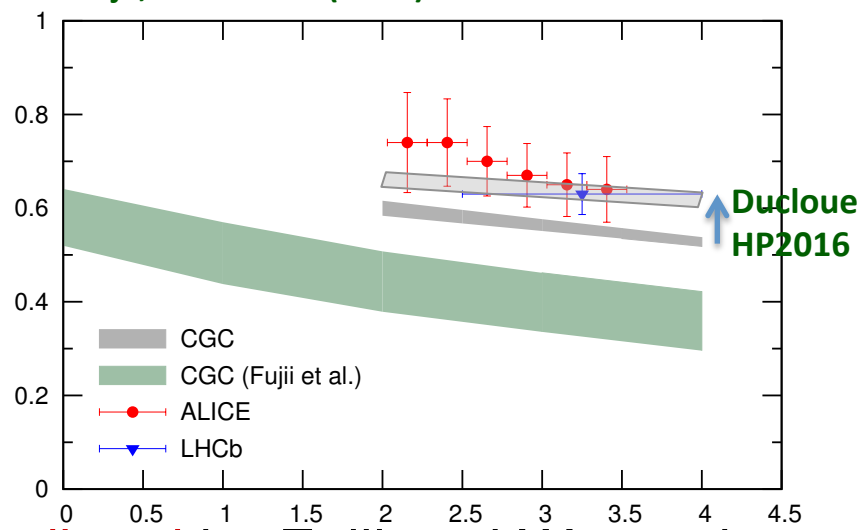


- Improved **postdictions**:
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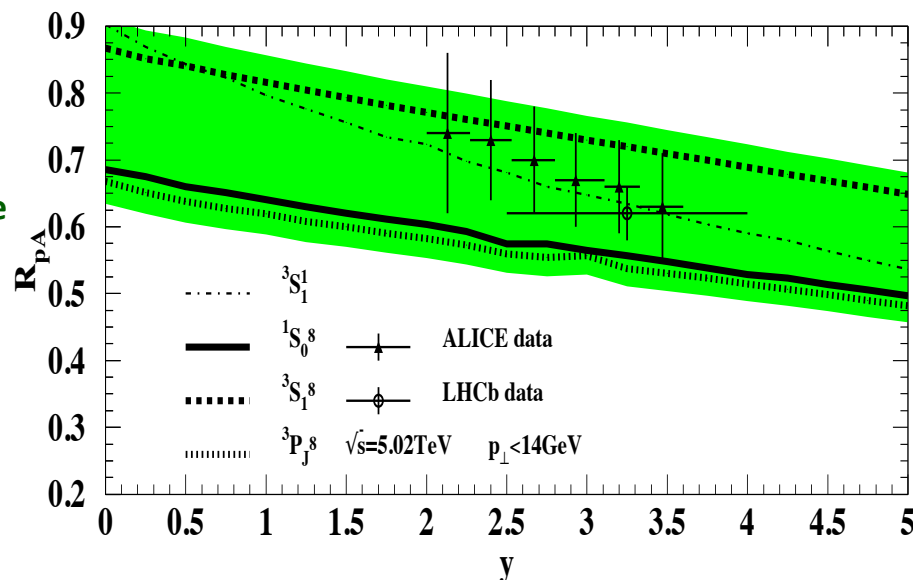
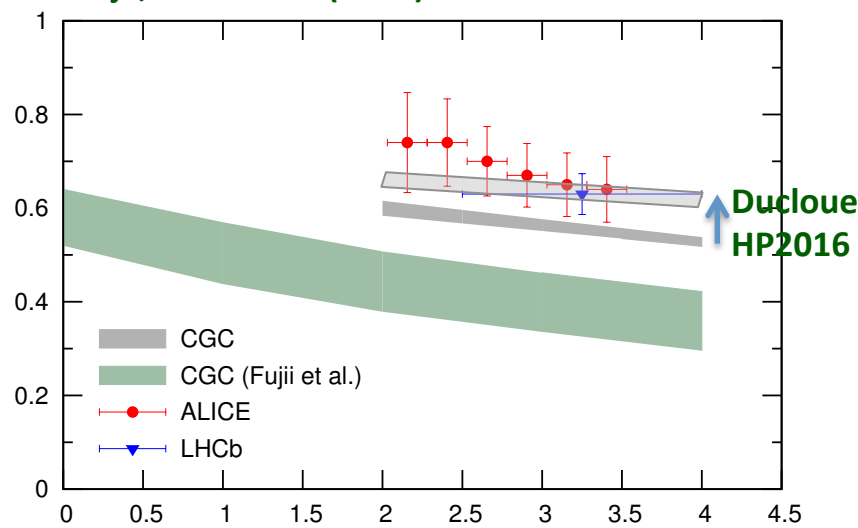


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contribution of CS channel relatively small 10% in pp, 15-20% in pA at low  $p_T$

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contribution of CS channel relatively small 10% in pp, 15-20% in pA at low  $p_T$
- Issue**: CGC results very much widespread (as those from nPDFs)
- Note**: CGC on J/ $\psi$  suppression applies at forward y (not backward)

# Excited states: An intriguing relative suppression in pA

## The facts: **data from RHIC & LHC**

- PHENIX: **relative  $\psi(2S)/J/\psi$  suppression** in **dAu** collisions @ 200 GeV
- ALICE & LHCb: **relative  $\psi(2S)/J/\psi$  suppression** in **pPb** collisions @ 5 & 8 TeV
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# Excited states: An intriguing relative suppression in pA

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  - At low E: the relative suppression can be explained by nuclear absorption
- $\sigma_{\text{breakup}} \propto r_{\text{meson}}^2$
- At high E: too long formation times  $t_f = \gamma \tau_f \gg R \Rightarrow$   
the quantum state does not matter!

# Excited states: An intriguing relative suppression in pA

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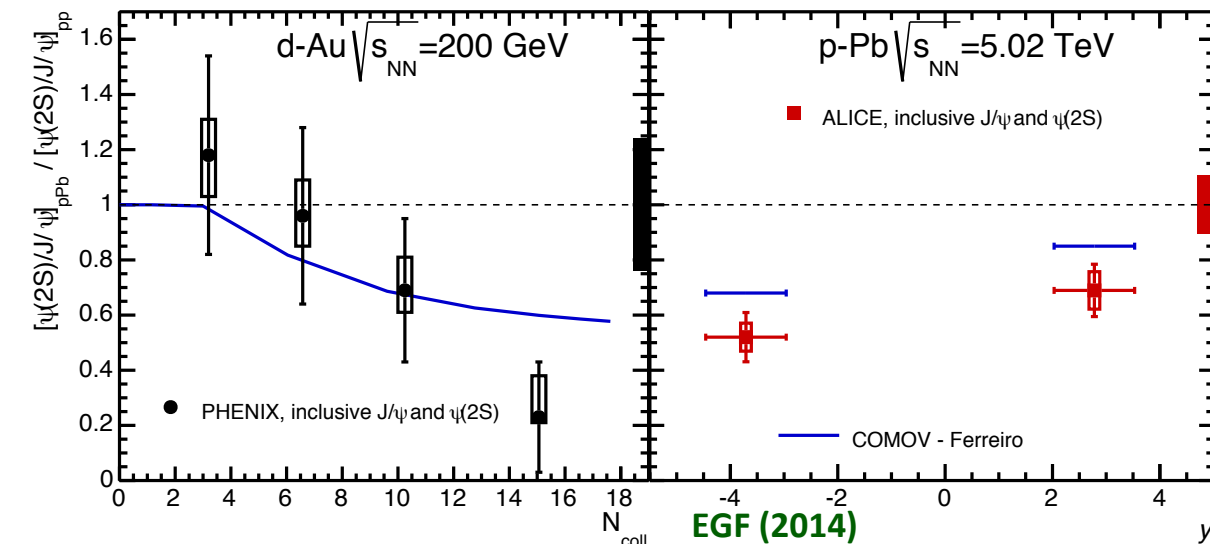
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the quantum state does not matter!

A natural explanation would be a **final-state effect** acting over sufficiently long time  
 $\Rightarrow$  **interaction with a comoving medium?**

# Excited states: Comover interaction

- In a comover model: suppression from scatterings of the nascent  $\psi$  with comoving medium of partonic/hadronic origin Gavin, Vogt, Capella, Armesto, EGF, Tywoniuk...
- Stronger comover suppression where the comover densities are larger. For asymmetric collisions as proton-nucleus, **stronger in the nucleus-going direction**
- Rate equation governing the charmonium density:
 
$$\tau \frac{d\rho^\psi}{d\tau}(b, s, y) = -\sigma^{co-\psi} \rho^{co}(b, s, y) \rho^\psi(b, s, y)$$

$\sigma^{co-\psi}$  originally fitted from SPS data



EGF (2014)

# Excited states: Comover interaction

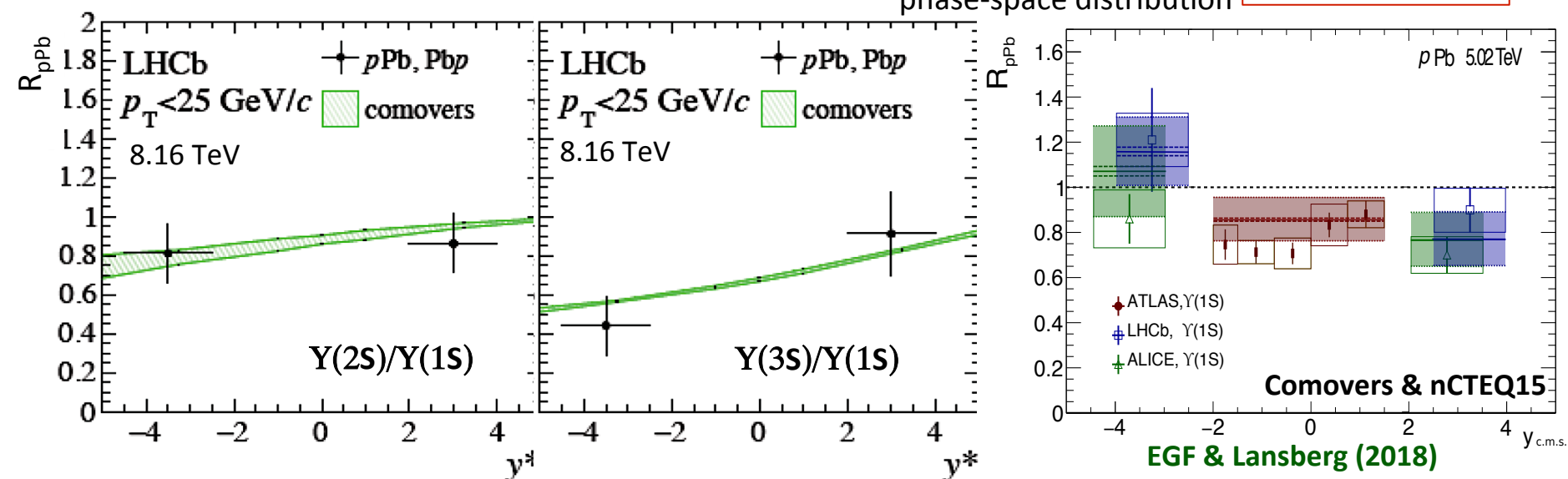
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- $\sigma^{co-\psi}$

originally fitted from SPS data

$$\sigma^{co-Q_{b\bar{b}}} = \sigma_{\text{geom}} \left(1 - \frac{E_{\text{Binding}}}{\langle E_{co} \rangle}\right)^n$$
- New:**  $\sigma^{co-\psi}$  can be parametrized:  $n$  &  $T_{\text{eff}}$  averaged over comover phase-space distribution 

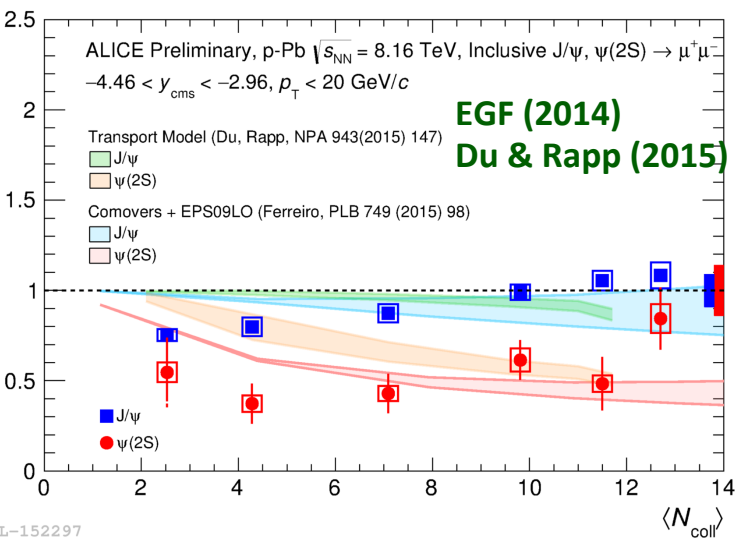
$$1/(e^{E_{co}/T_{\text{eff}}} - 1)$$



# Excited states: Comover interaction

Transport model with final interactions  
“similar in spirit to *comover* suppression”

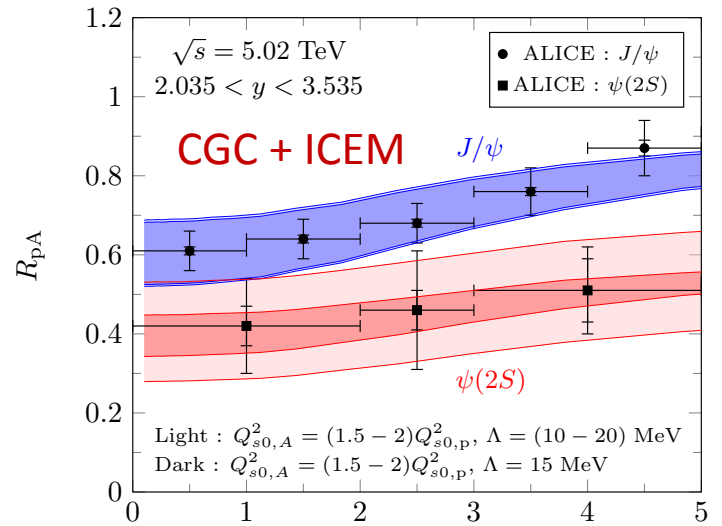
Soft color exchanges between cc & *co-movers* at later stage => effect on  $\psi(2S)$



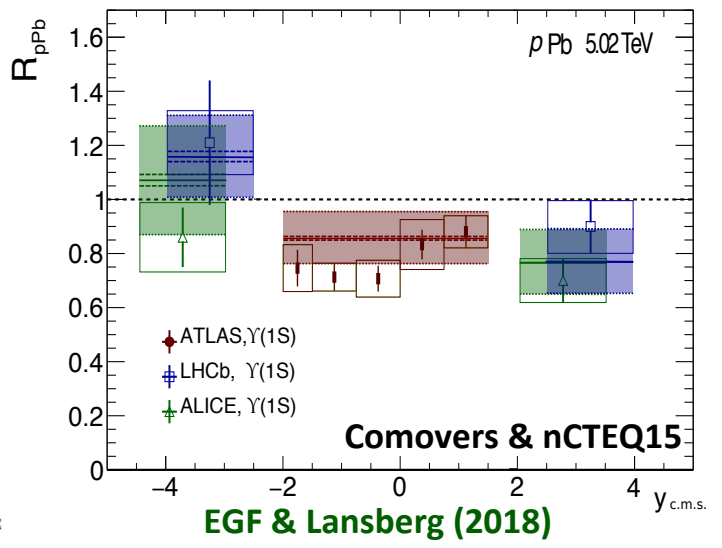
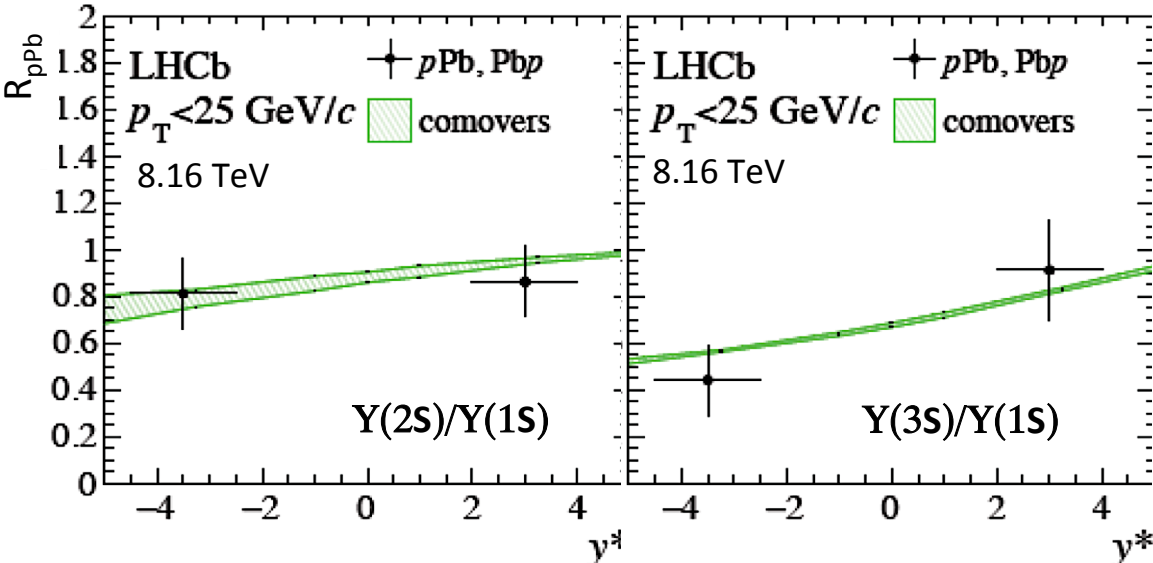
→ New results on  $\psi(2S)$  confirm stronger suppression w.r.t. to  $J/\psi$  in the Pb-going direction.

→ Final state effects are needed to reproduce the  $\psi(2S)$  suppression.

→ Still problems for a quantitative description of the data.



Ma, Venugopalan, Zhang, Watanabe (2018)

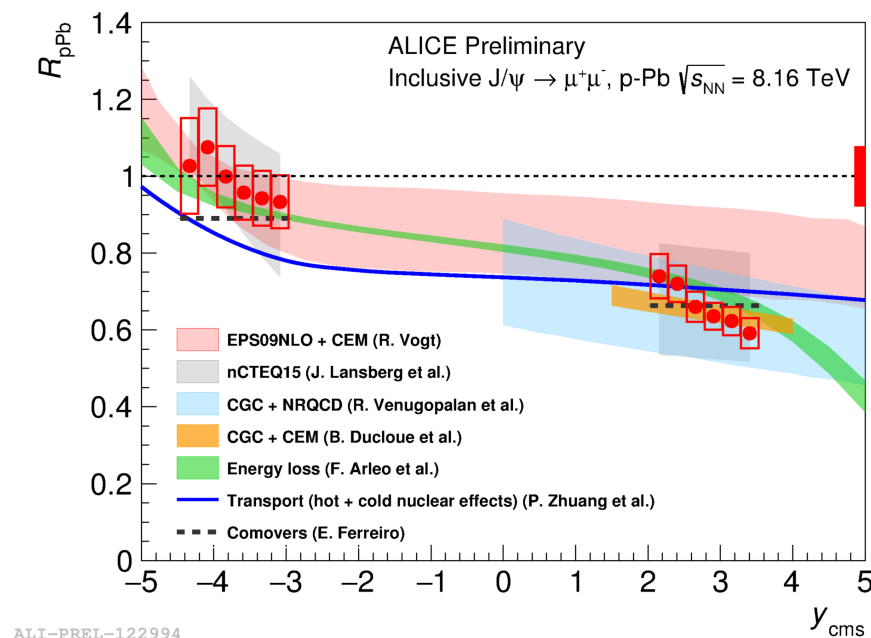


# Some comments on proton-nucleus collisions

- Initial-state effects are required to explain pA data from RHIC and LHC  
=> Modification of the gluon flux, either by modified nPDF or CGC, needs to be taken into account

## Issues:

- Huge uncertainty of nPDFs
- Widespread CGC results
- Coherent Eloss mechanism can also reproduce ground state data

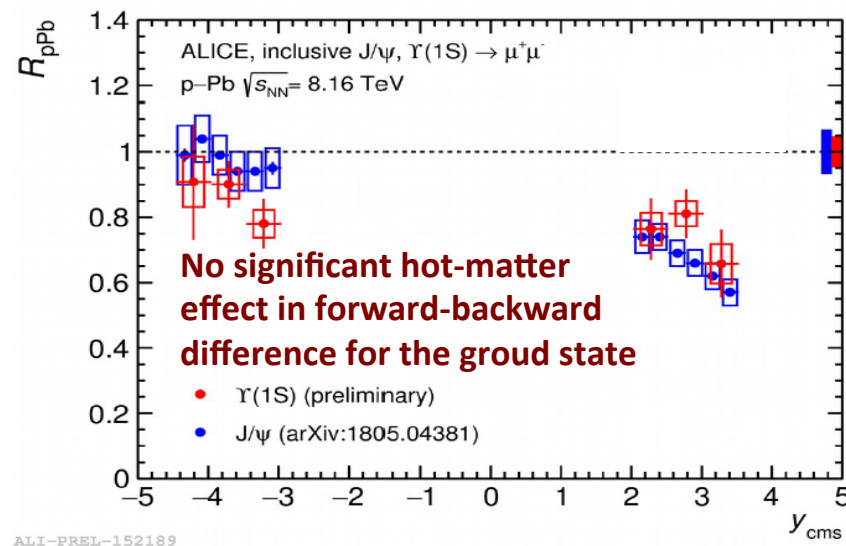


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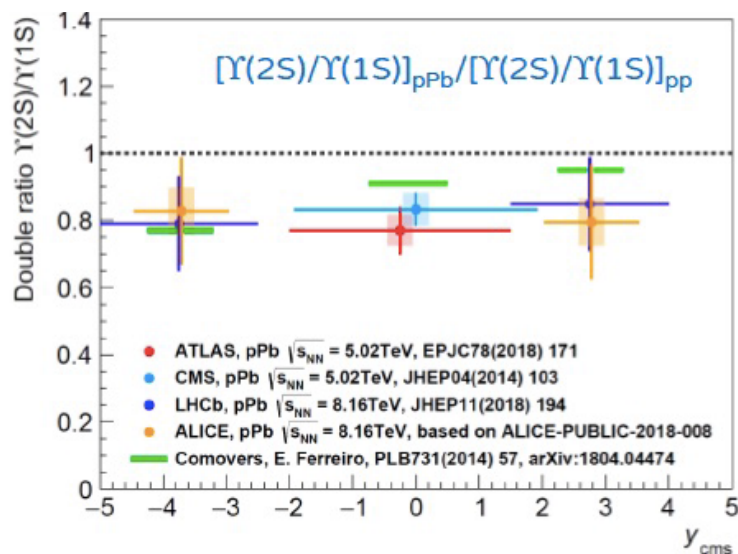
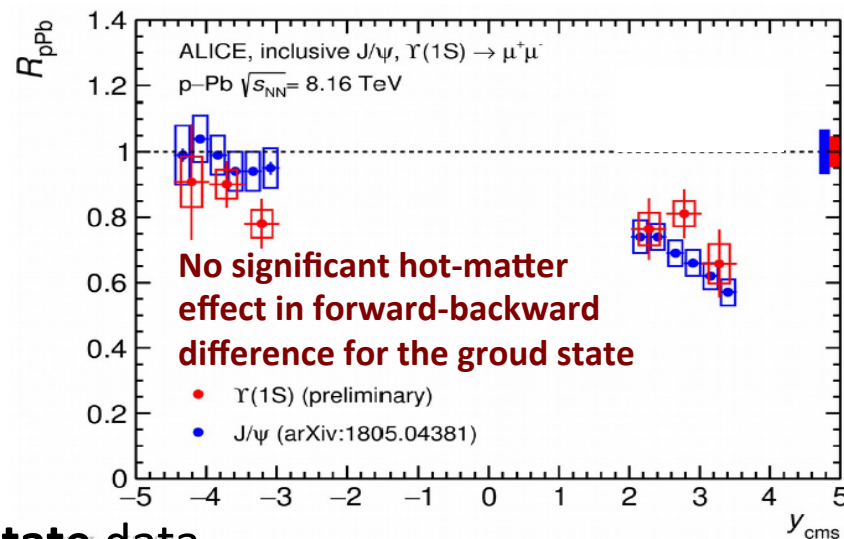


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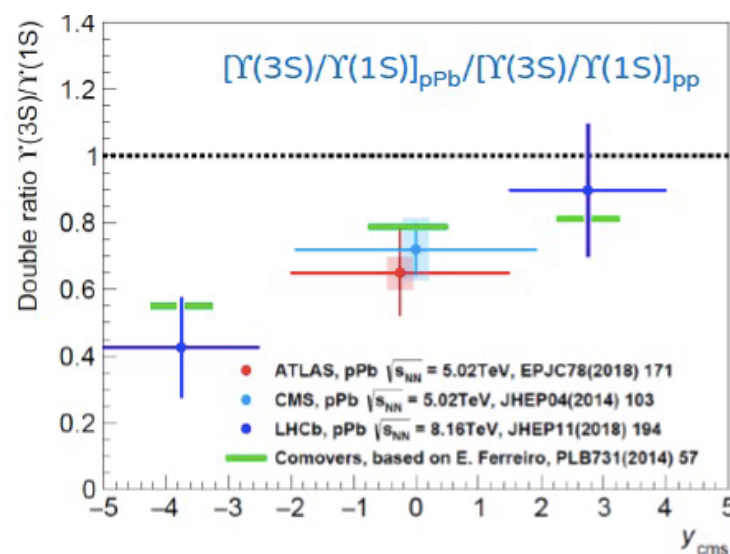
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- Final-state effects as comover interaction needed to reproduce excited to ground state data



Arnaldi  
SQM2019

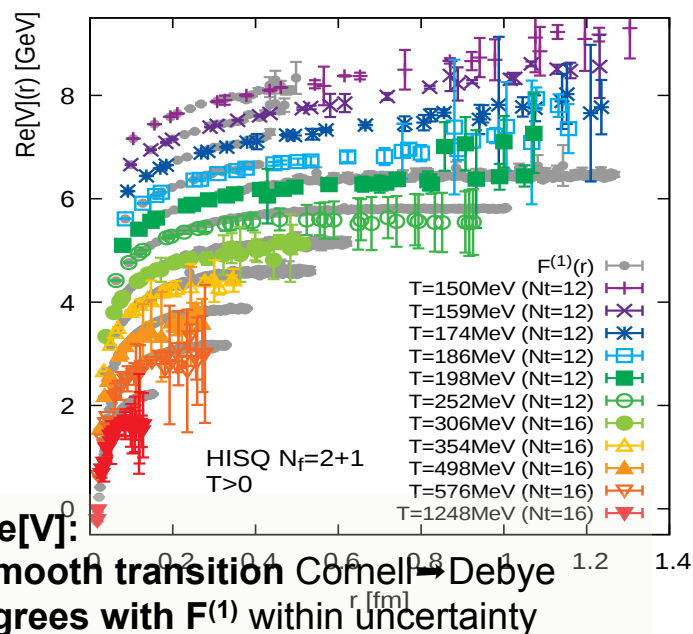


# Think bigger: quarkonium in nucleus-nucleus collisions

- Matsui and Satz: suppression of quarkonium as a signature of the QGP  
Debye screened potential above the deconfinement temperature
- Time-independent notion of the melting process, **purely real model potentials**  
Popular candidates: free energies  $F^1(r)$  &/or internal energies  $U^1(r)$  **Static**
- An essential step: heavy quark potential not only shows Debye screening but also features an **imaginary part** **Laine et al. (2007)**  
Intuitive idea: **Re[V]** captures the screened  $Q\bar{Q}$  interaction **Dynamic**  
**Im[V]** captures dissociation by Landau damping & singlet  $\Leftrightarrow$  octet

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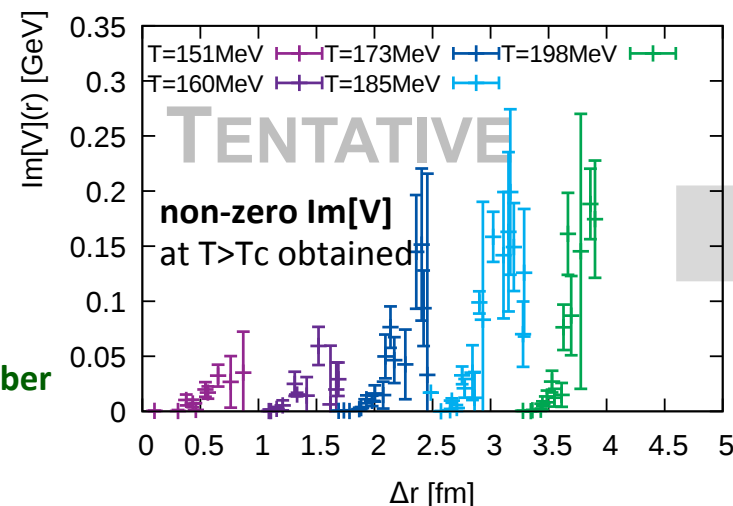


## Current efforts:

- lattice QCD calculation of complex in-medium HQ potential

Petreczky, Rothkopf, Weber  
[TUM-QCD] 2019

- understand the origin and physics implications of  $\text{Im}[V]$

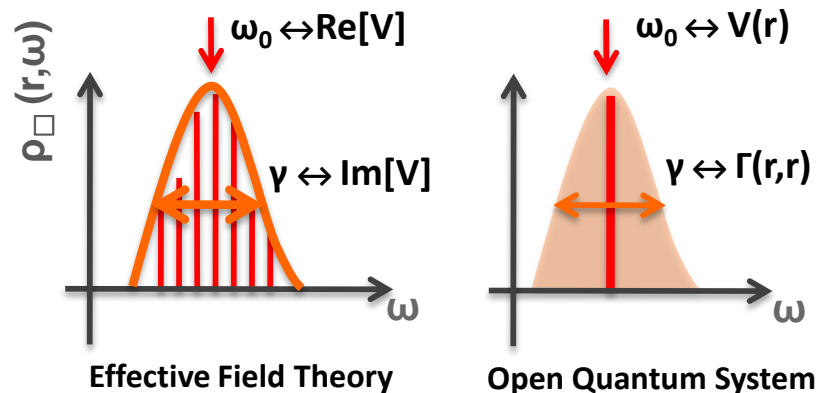
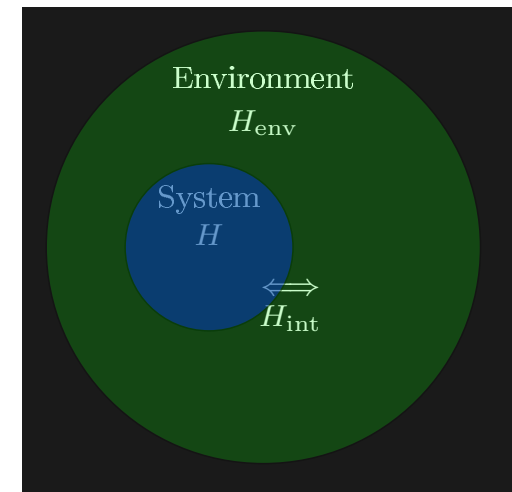


# Thinking big: quarkonium in nucleus-nucleus collisions

- To formalize the idea of decoherence in the language of QM and to see how the imaginary part arises from the thermal fluctuations in the medium:

## Theory of open quantum systems:

- solution of a stochastic Schrodinger equation  
Asakawa& Rothkopf; Katz & Gossiaux,  
Kajimoto, Akamatsu, Asakawa, Rothkopf
- computation of the evolution of the density matrix  
Borghini, Dutta, Gombeaud;  
Brambilla, Escobedo, Soto, Vairo;  
Blaizot; De Boni



The real and imaginary parts of the in-medium HQ potential can be related to the stochastic evolution of the in-medium wave function which is perturbed by the thermal medium:

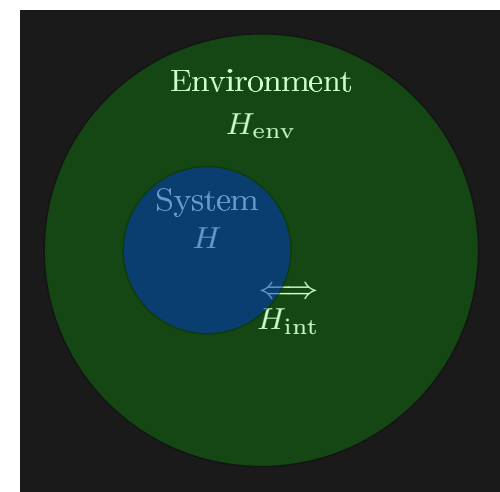
- Stochastic term = thermal noise
- $\text{Im}[V]$  related to the strength of the thermal noise

# Thinking big: quarkonium in nucleus-nucleus collisions

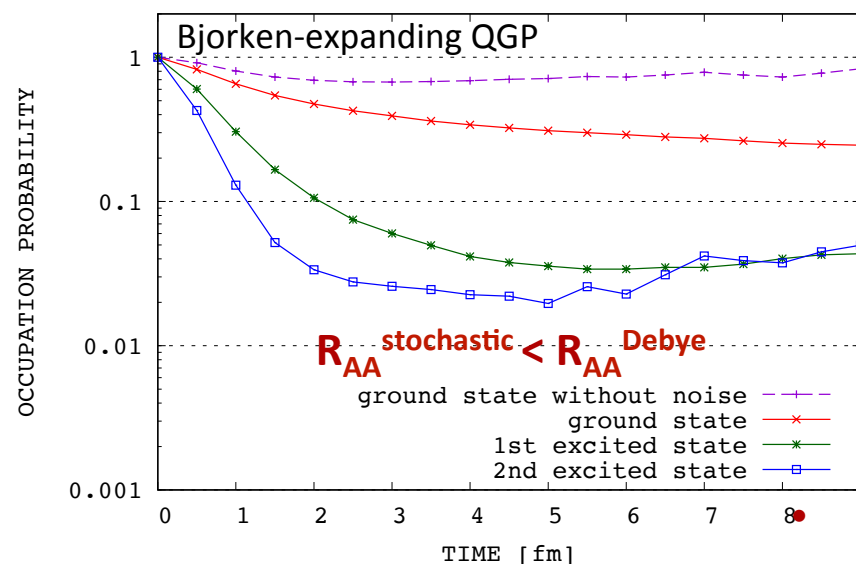
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CHARMONIUM



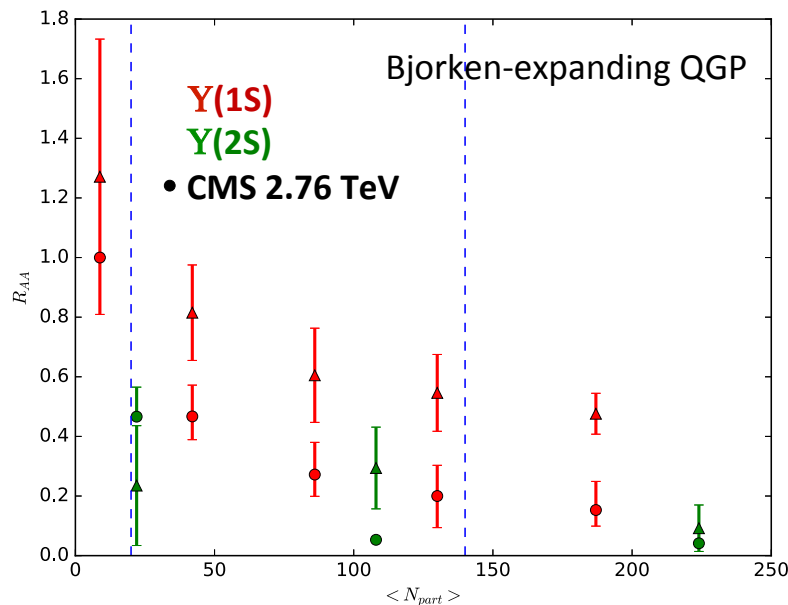
**Kajimoto, Akamatsu, Asakawa, Rothkopf (2018)**

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Noise provides a dynamical dissociation mechanism

# Recent developments on open quantum systems for quarkonia



Time evolution of HQ states in an expanding hot QCD medium by implementing EFT –pNRQCD- in the framework of open quantum systems

=> Lindblad equation

- non-Abelian nature of QCD: color transitions

Brambilla, Escobedo, Soto & Vairo (2017)

In the same line: equations for the time evolution of the HQ reduced-density matrix in a non-Abelian QGP

Blaizot & Escobedo (2017)

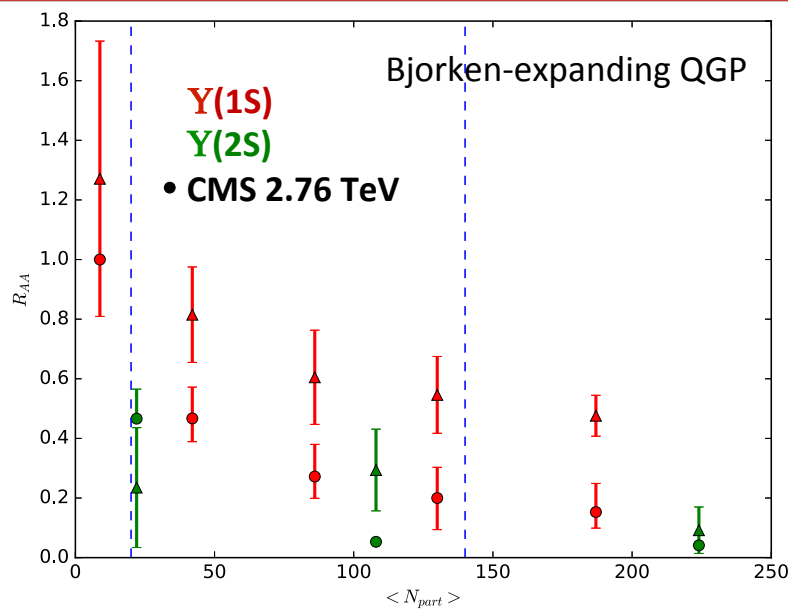
- take into account the color transitions within 2 strategies:
  - perturbation theory => Langevin equation, analogous to QED
  - as collisions => Boltzmann equation

Also: Schrödinger-Langevin equation

Gossiaux & Katz (2016)

- interesting framework but not derived from first QCD principles
- QCD features enter in the parameters (similarly to Langevin dynamics in HF physics)

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Master equation with time evolution of the HQ states

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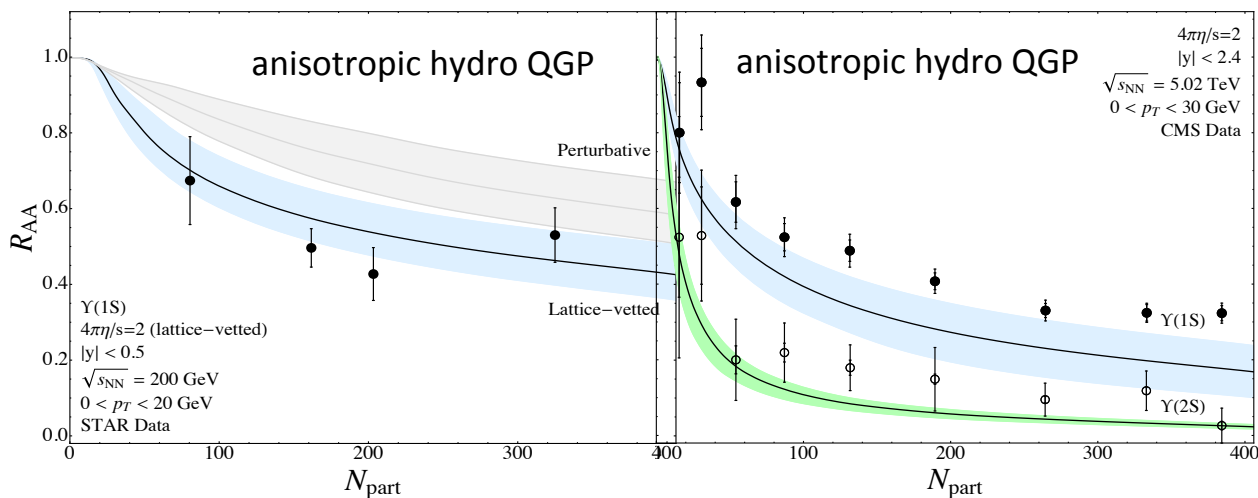
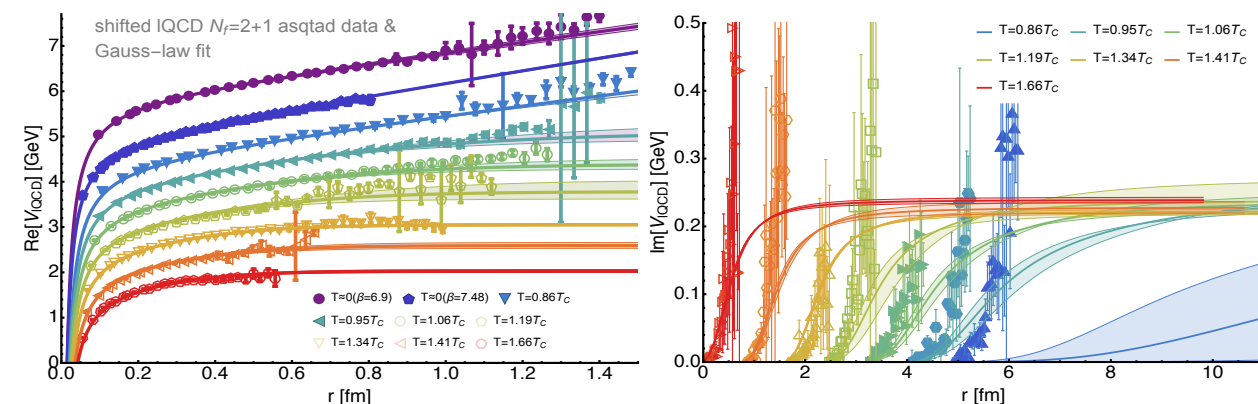
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# Recent developments on phenomenology for quarkonia

## Anisotropic QGP with lattice potential

- lattice QCD vetted in-medium heavy-quark potential with anisotropic hydro QGP
- in-medium potential: complex values at high temperatures
- discrete values of the potential obtained from lattice QCD

Kroupa, Strickland, Rothkopf (2018)



- stronger imaginary part present in the lattice-vetted potential

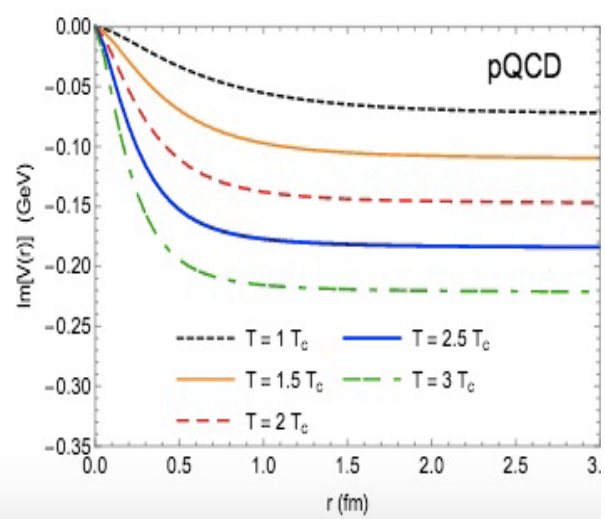
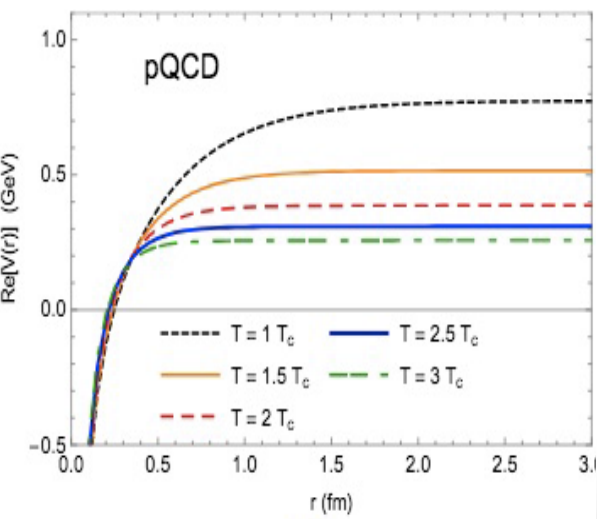
⇒ Y states more easily dissociated

# Recent developments on phenomenology for quarkonia

## AdS/CFT techniques

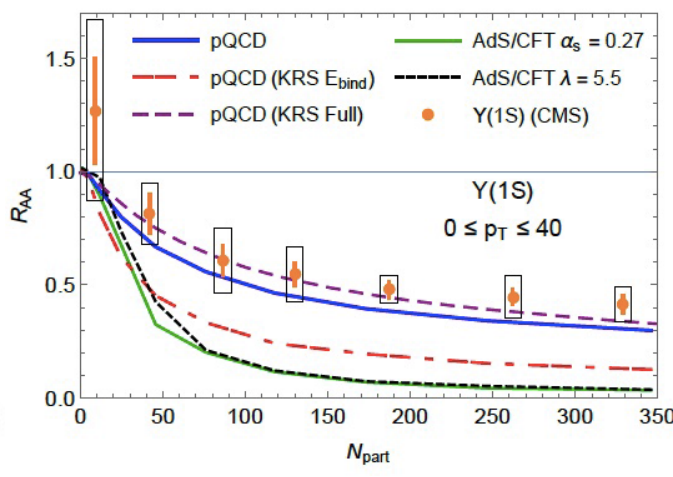
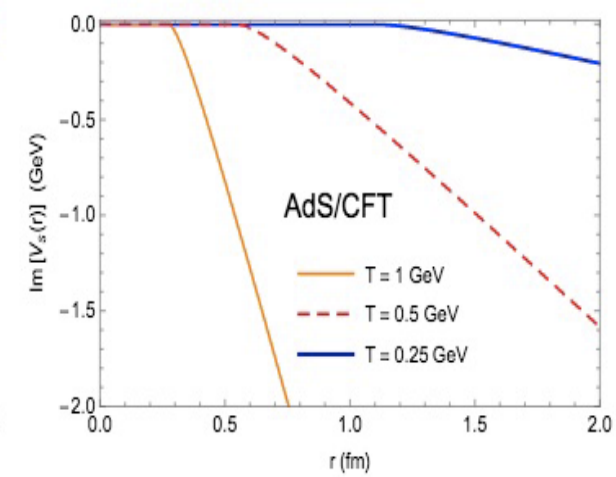
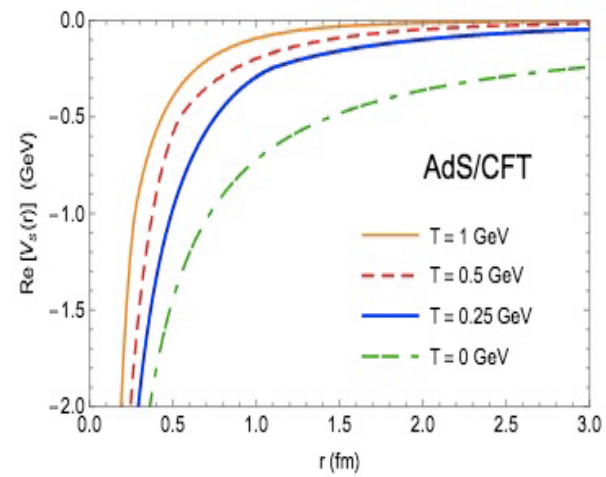
Barnard & Horowitz (2017)

- Strong coupling techniques of AdS/CFT vs weak coupling techniques from pQCD



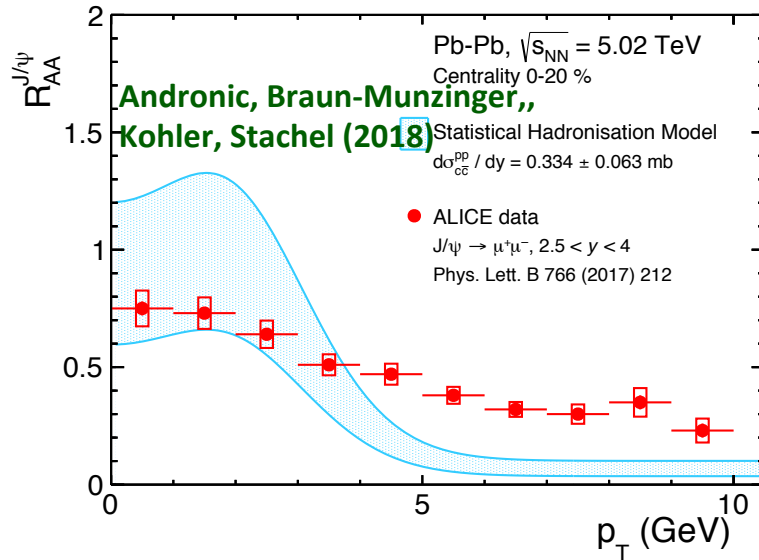
- AdS/CFT potential has a divergent imaginary part, compared to the saturation of the imaginary part of the pQCD potential

⇒ overpredicts the suppression of Y states

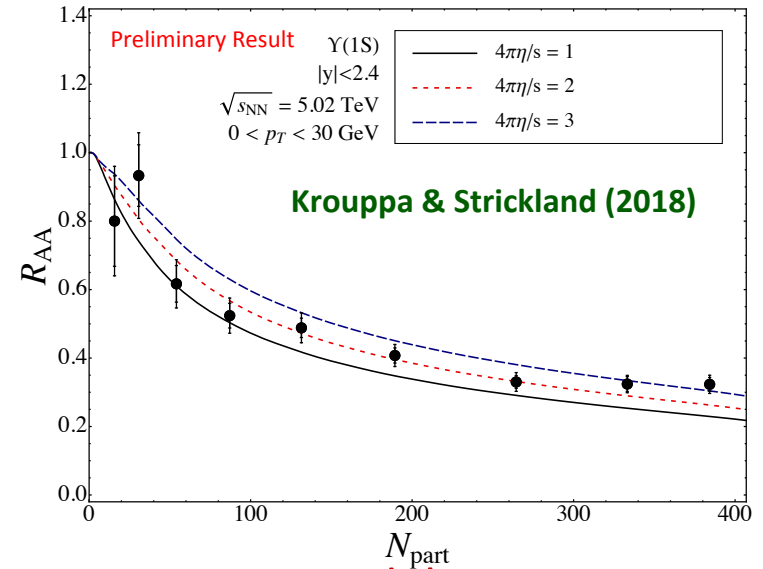


# Recent results from some long-lasting phenomenology models

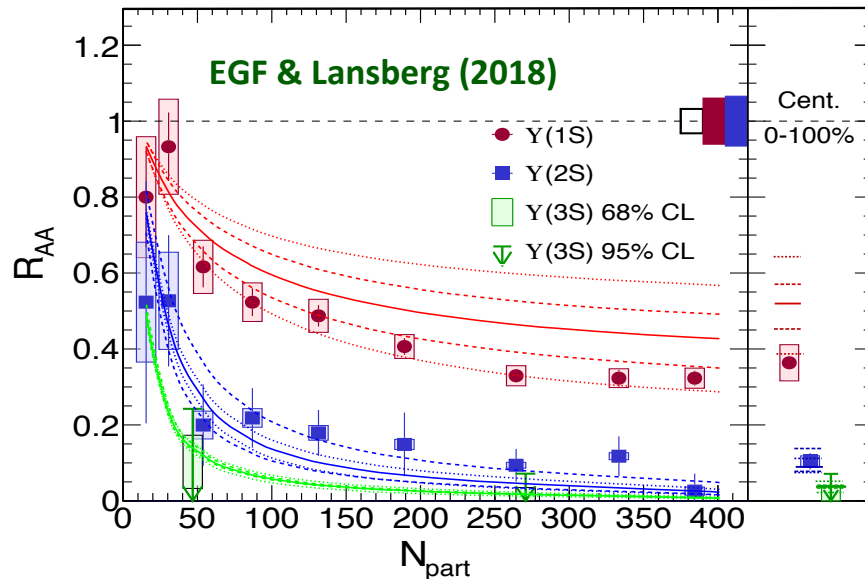
## Statistical hadronization model



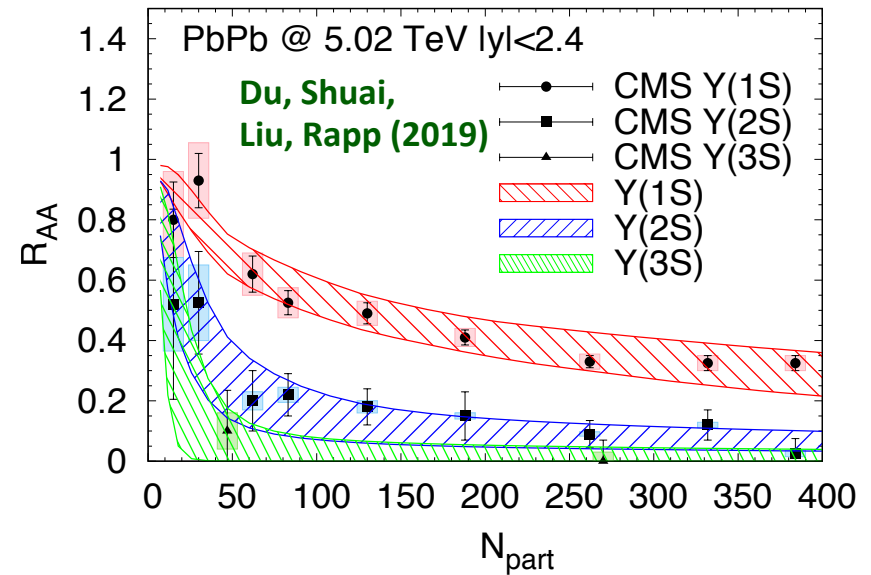
## a-hydro model



## Comover model

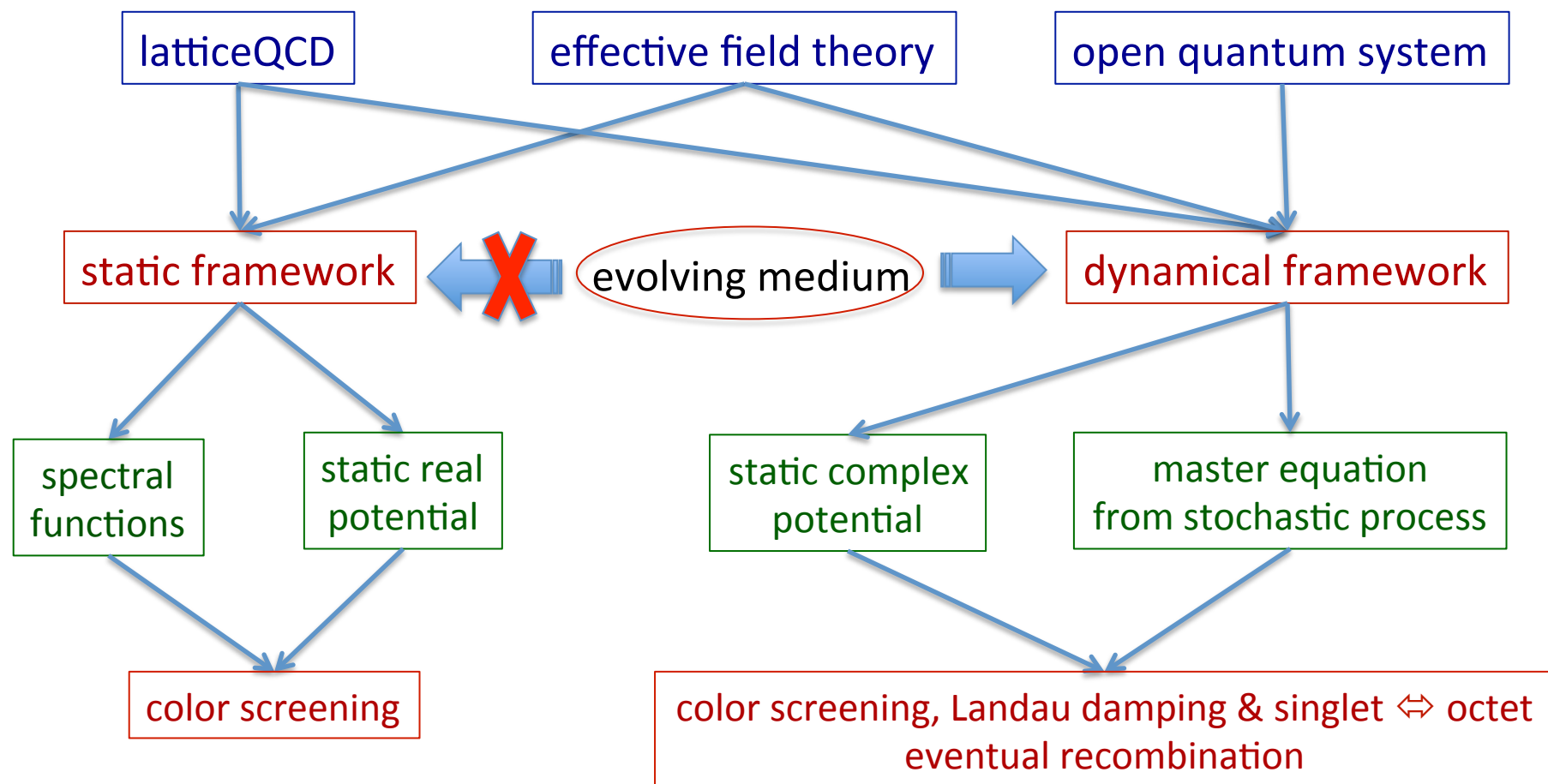


## Transport model



# Summarizing: theory elements on quarkonia in a QGP

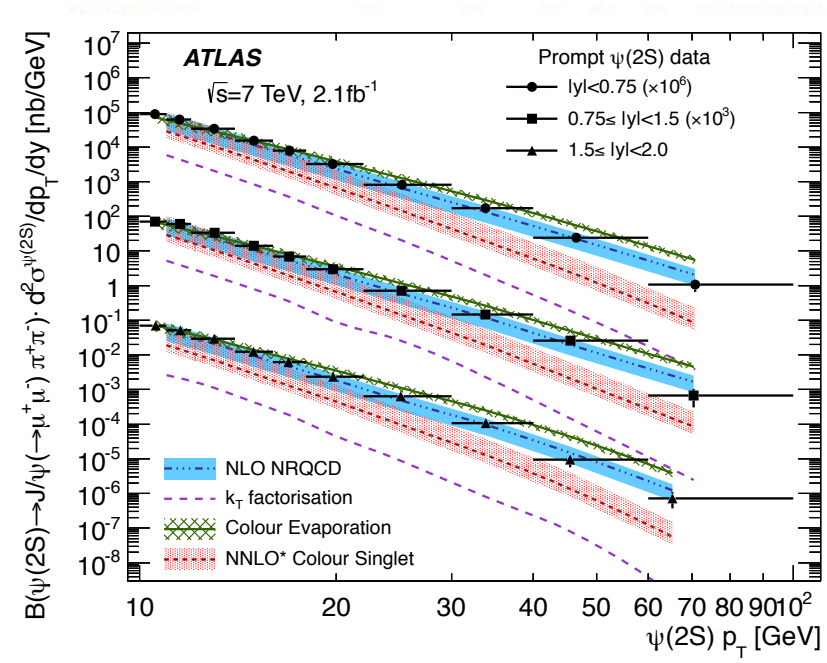
**Caveat I:** we need firm theoretical understanding of quarkonium production in pp collisions



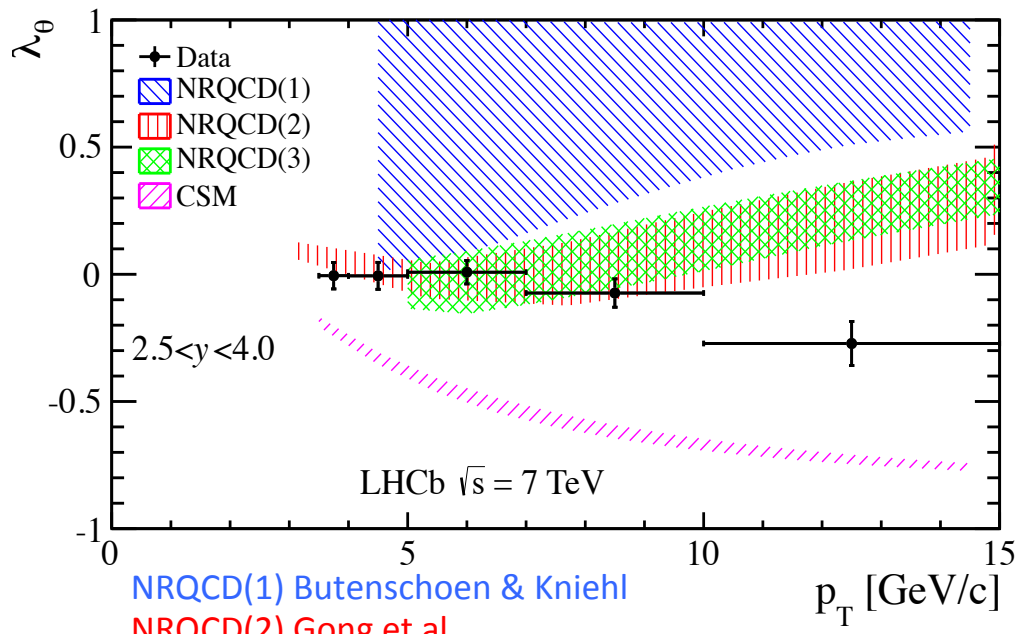
**Caveat II:** how to extrapolate **pA** effects –initial & **final**- to AA? Factorization?  
If yes... nature of the medium in pA?

BACKUP PROTON-PROTON

# Production model: state of the art for the $\psi(2S)$



Sapore Gravis Review arXiv:1506.03981



NRQCD(1) Butenschoen & Kniehl  
NRQCD(2) Gong et al.  
NRQCD(3) Chao et al.

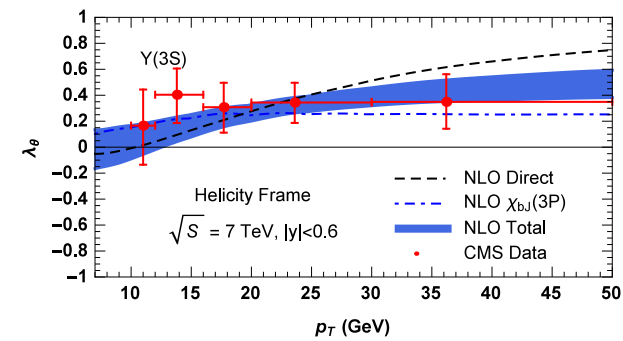
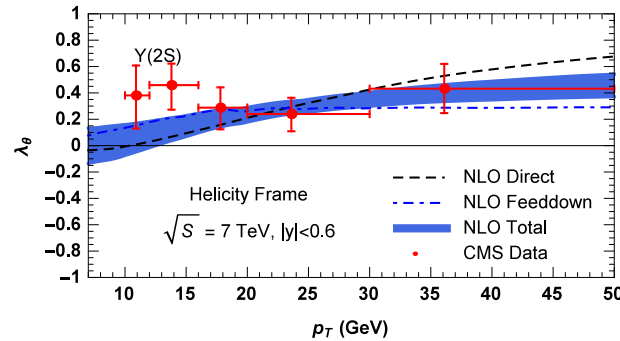
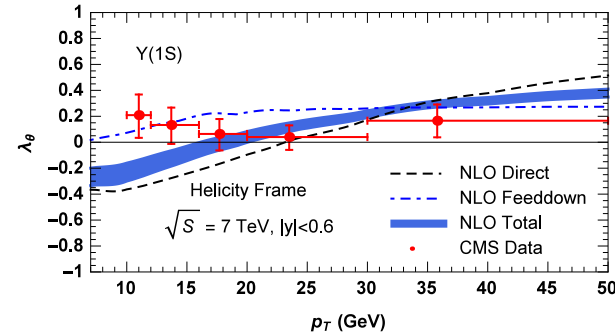
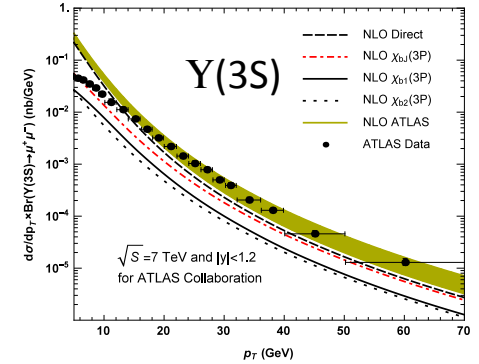
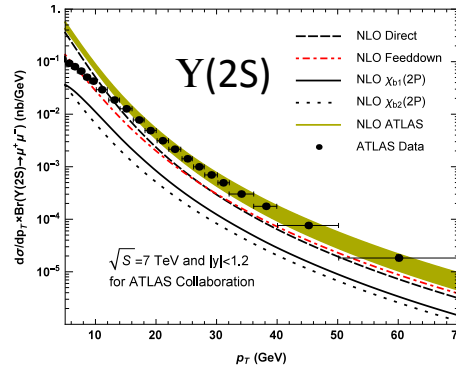
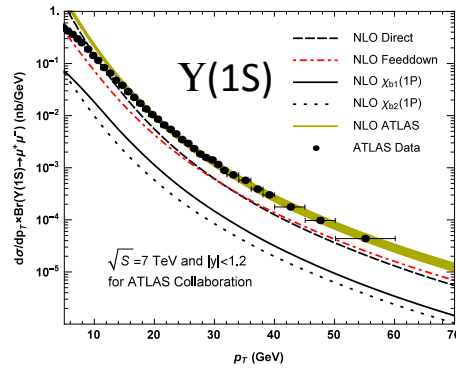
At low and mid  $p_T$  –region where quarkonium heavy-ion studies are mainly carried out– none of the models can simply be ruled out due to theoretical uncertainties (heavy-quark mass, scales, non-perturbative parameters, unknown QCD and relativistic corrections, ...)

- New recent developments on may be helpful:
- CEM improved
  - CGC meets NRQCD

# Production model: state of the art for the $Y$

- Larger mass, higher scale and slower velocity could make  $Y$  a better candidate for NRQCD

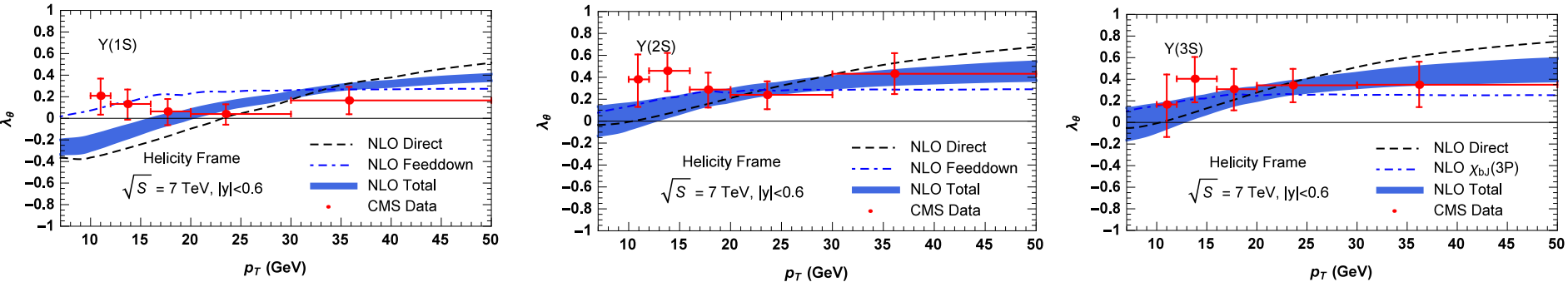
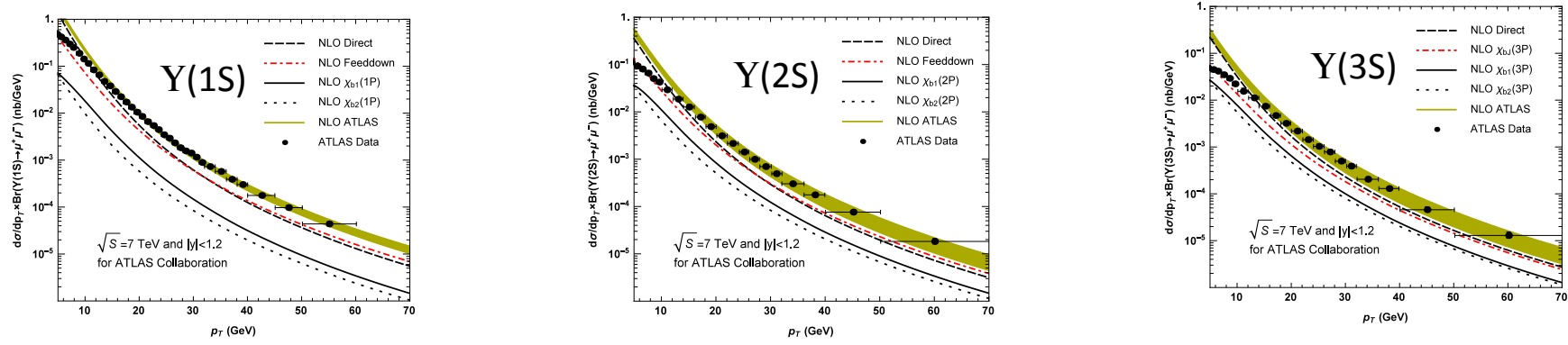
Hang et al.



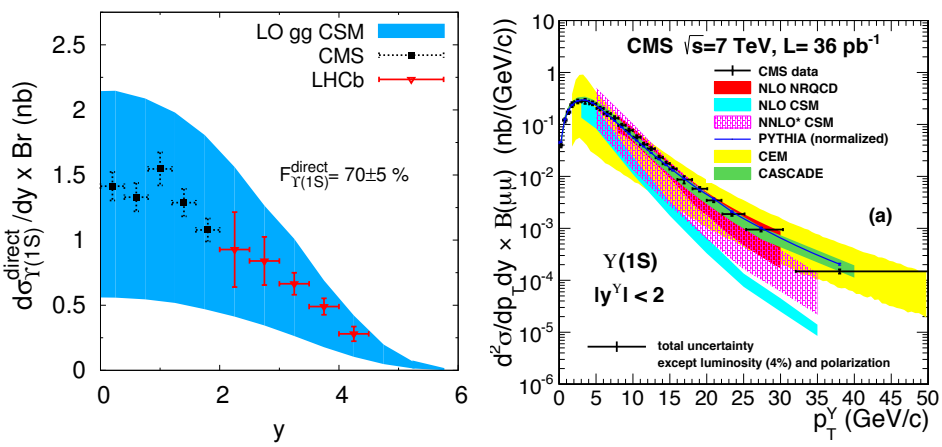
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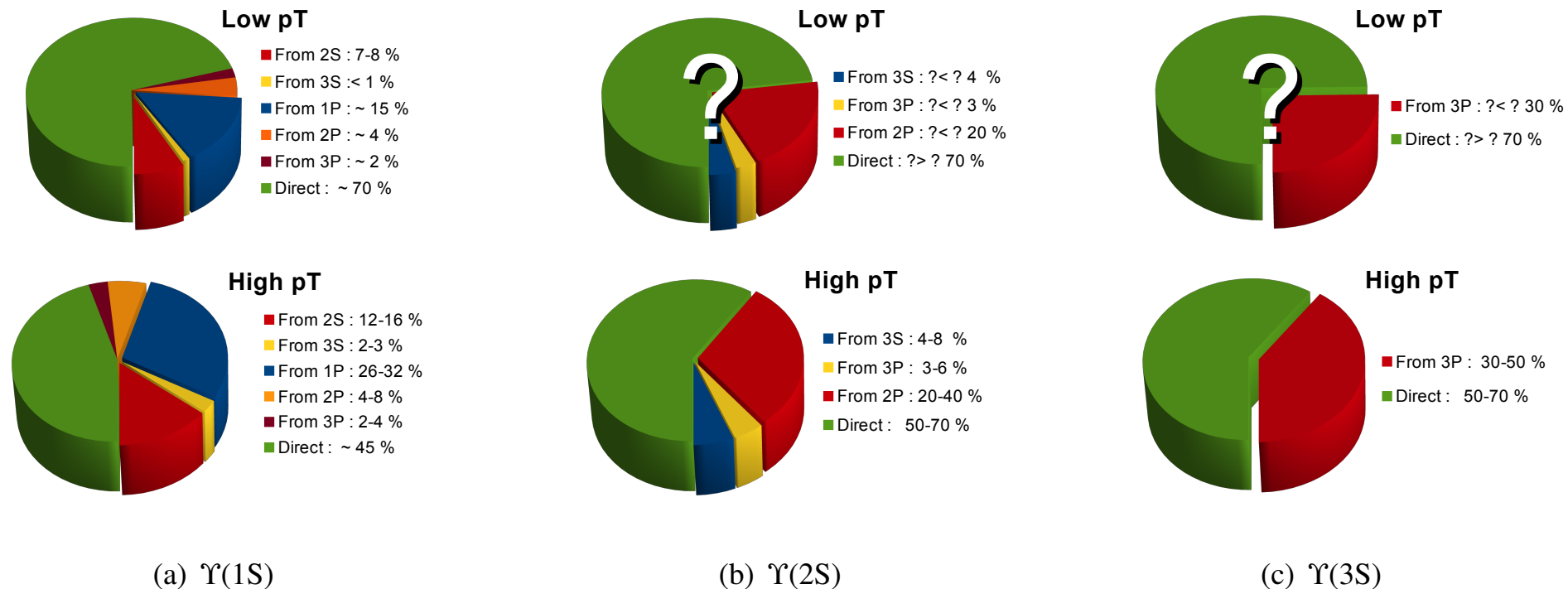
Lansberg



- None of the models can simply be ruled out due to their theoretical uncertainties
- In general, LHC data are much more precise than theory
- **Caveat:** Important feeddown contributions -6 states- to be taken into account for interpretations of their possible sequential suppression

# News from feed-down

Feed-down structure at low  $p_T$  -where quarkonium heavy-ion measurements are mostly carried out- is quite different than that commonly accepted ten years ago based on the CDF measurement, with a  $p_T > 8$  GeV



Sapore Gravis Review arXiv:1506.03981 from LHCb data

This information is fundamental to use bottomonia as probes of QGP, especially for the interpretation of their possible sequential suppression

BACKUP PROTON-NUCLEUS

# Baseline: nPDFs & nuclear absorption in a collinear pQCD framework

- Parton densities in nuclei are modified

Nuclear PDF assumed to be factorizable in terms of the nucleon PDFs :

$$\mathcal{F}_g^A(x_1, \mu_f) = g(x_1; \mu_f) \times R_g^A(x, \mu_f)$$

In presence of nuclear effects:  $R_g^A(x, \mu_f) \neq 1$

- Mesons may scatter inelastically with nucleons in the nuclear matter  
Survival probability for a  $Q\bar{Q}$  to pass through the target unscathed:

$$S_A(\vec{r}_A, z_A) = \exp \left( -A \sigma_{\text{break-up}} \int_{z_A}^{\infty} d\tilde{z} \rho_A(\vec{r}_A, \tilde{z}) \right)$$

- Any differential cross section can then be obtained from the partonic one:

$$\frac{d\sigma_{pA \rightarrow QX}}{dy dP_T d\vec{b}} = \int dx_1 dx_2 g(x_1, \mu_f) \int dz_A \mathcal{F}_g^A(x_2, \vec{b}, z_B, \mu_f) \mathcal{J} \frac{d\sigma_{gg \rightarrow Q+g}}{d\hat{t}} S_A(\vec{b}, z_A)$$

From any model (CSM, COM, CEM)

# Nuclear absorption: Generalities on the break-up cross section

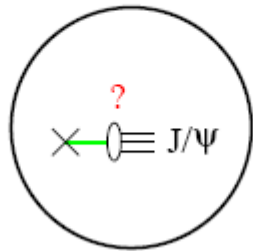
The **bound states** may be destroyed by inelastic scatterings with nucleons if they are formed in the nuclear medium. One expects

$$\sigma_{\text{break-up}} \propto r_{\text{meson}}^2$$

- In order to interact with nuclear matter =>  $t_f \leq R$
- In the meson rest frame:  $\tau_f = \frac{2M_{c\bar{c}}}{(M_{2S}^2 - M_{1S}^2)} \approx 0.3 \div 0.4 \text{ fm}$
- $t_f$  has to be considered in the rest frame of the target nucleus =>  $t_f = \gamma \tau_f$

Low energy:  $t_f = \gamma(x_2) \tau_f \ll R$

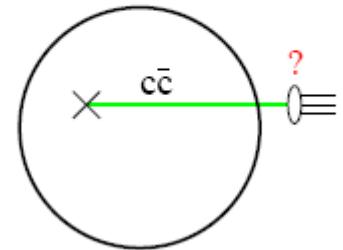
High energy:  $t_f = \gamma(x_2) \tau_f \gg R$



**Formation time depends on the boost**

$$\gamma = \cosh(y - y_{\text{beam}}^A) \Rightarrow \text{At } y=0:$$

$$\gamma_{\text{RHIC}}=107 \text{ and } \gamma_{\text{LHC}}=2660$$



It takes  $t_f=30 \text{ fm/c}$  at RHIC and  $t_f=800-1000 \text{ fm/c}$  at LHC for a quarkonium to form and to become distinguishable from its excited states

$$t_f \gg R$$

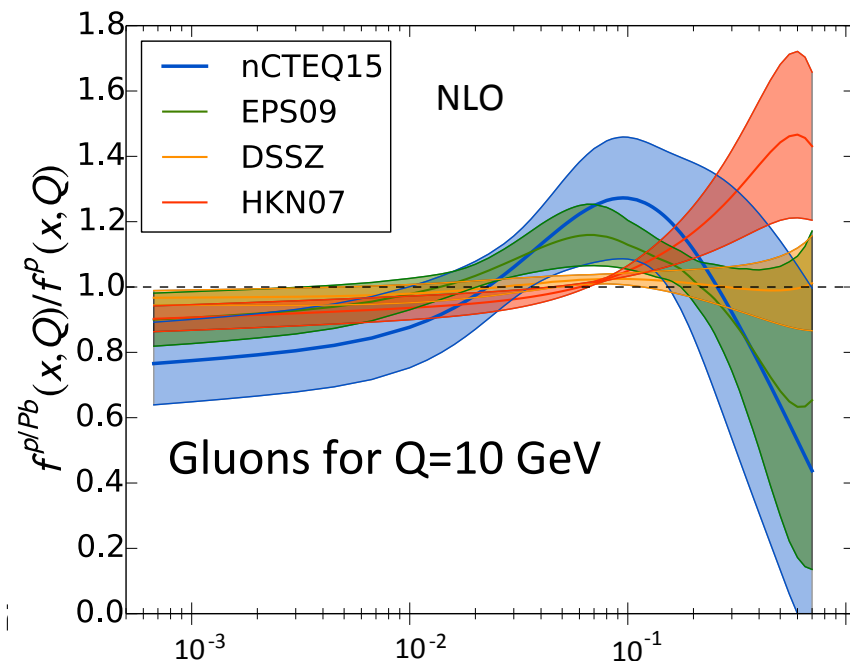
**Consensus:**  $\sigma_{\text{break-up}}$  is getting small at high energies and may be the same for ground and excited states

# Typical gluon nuclear PDFs

There are several nPDF sets available (using various data, LO/NLO, etc)

Typical gluon nPDFs: 4 regions

- $x \leq 10^{-2}$ : shadowing
- $x \approx 10^{-1}$ : anti-shadowing
- $0.3 \leq x \leq 0.7$ : EMC effect
- $x \geq 0.7$ : Fermi motion

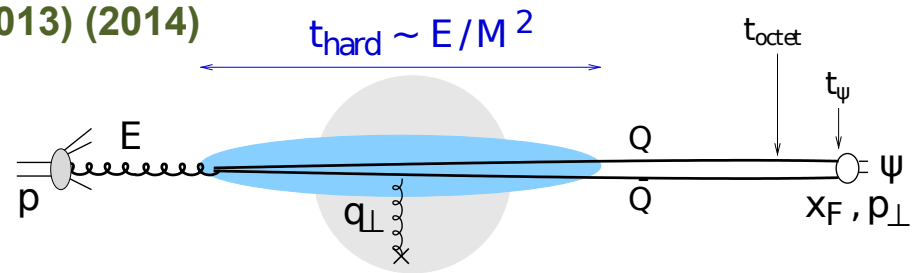


- For the gluons, only the **shadowing** depletion is established although its magnitude is still discussed
- The gluon **antishadowing** not yet observed although used in many studies; absent in some nPDF fits
- The gluon **EMC effect** is even less known, hence the uncertainty there

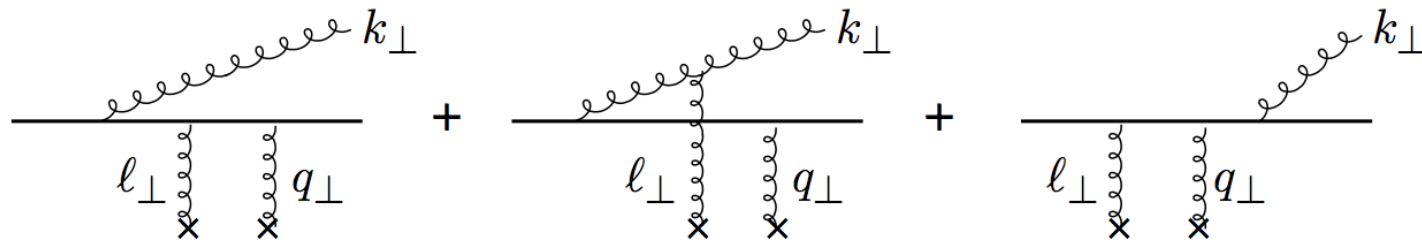
# Going further: Coherent energy loss

Arleo, Kolevatov, Peigné, Rustamova (2012) (2013) (2014)

This approach is based on the fact that **for large formation times** all scattering centers in the medium act **coherently**.



- Coherent radiation** (interference) in the initial/final state crucial for  $t_f \gg R$



IS and FS radiation cancels out in the **induced spectrum**

**Interference terms** does not cancel in the **induced spectrum**!

- Leads to a **behaviour**  $\Delta E \propto E$

$$\Delta E = \int d\omega \omega \left. \frac{dI}{d\omega} \right|_{\text{ind}} = N_c \alpha_s \frac{\sqrt{\Delta q_{\perp}^2}}{m_T} E$$

- $\sqrt{\Delta q_{\perp}^2}$  related to the **transport coefficient**  $\hat{q}$

- $\hat{q}$  related to the **saturation scale** by  $Q_s^2(x, L) = \hat{q}(x) L$

$$\hat{q}(x) \simeq \hat{q}_0 \left( \frac{10^{-2}}{x} \right)^{0.3}$$

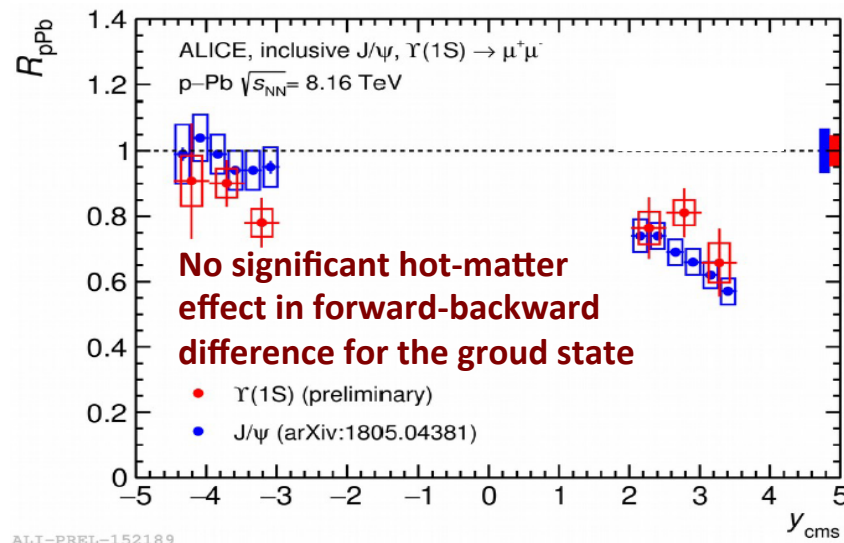
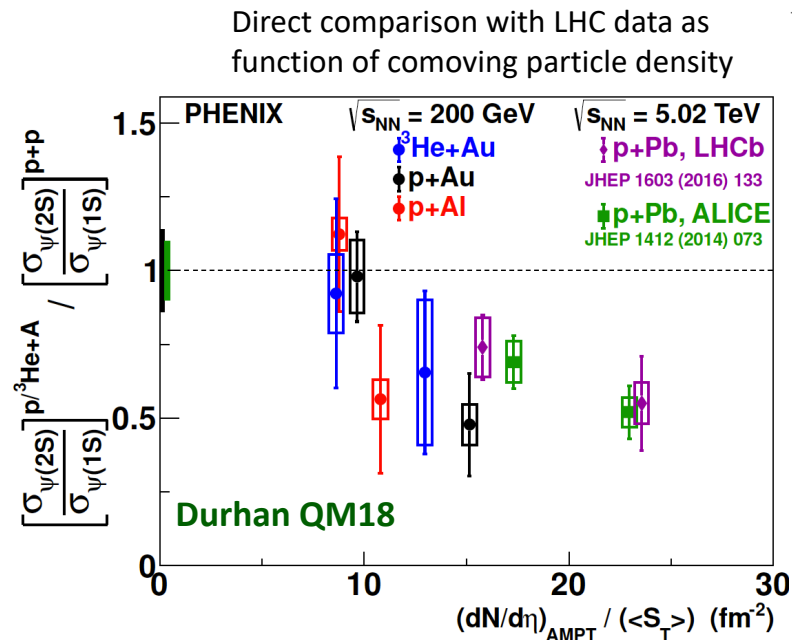
$\hat{q}_0$  is the only fitted parameter of the approach+the option to switch on/off the shadowing

# Some comments on proton-nucleus collisions

- Initial-state effects are required to explain pA data from RHIC and LHC  
=> **Modification of the gluon flux**, either by modified **nPDF** or **CGC**, needs to be taken into account

## Issues:

- Huge uncertainty of nPDFs
- Widespread CGC results
- Coherent Eloss mechanism** can also reproduce **ground state** data

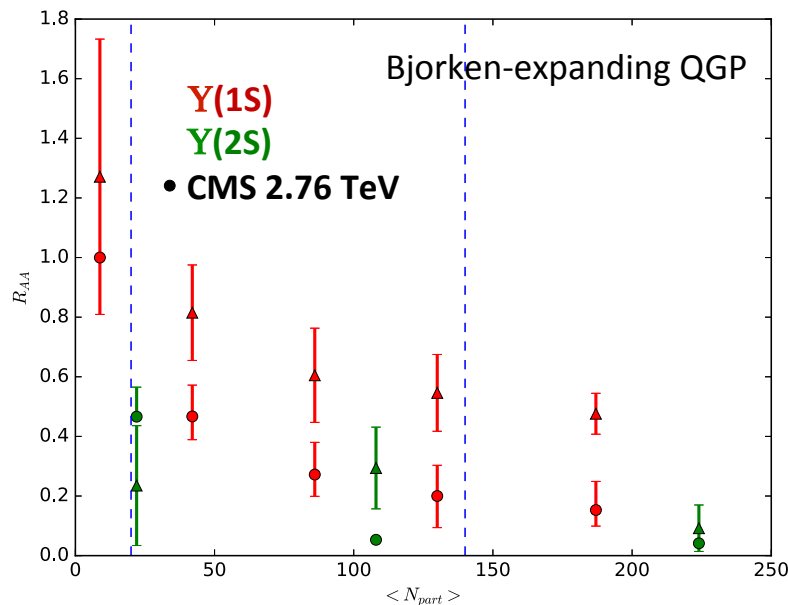


- Final-state effects as **comover interaction**, are good candidates to reproduce **excited to ground state** data **EGF & Lansberg (2018)**

pPb 5.02 TeV	Comover model	CMS data $-1.93 < y < 1.93$
	$-1.93 < y < 1.93$	CMS data
$\Upsilon(2S)/\Upsilon(1S)$	$0.91 \pm 0.03$	$0.83 \pm 0.05$ (stat.) $\pm 0.05$ (syst.)
$\Upsilon(3S)/\Upsilon(1S)$	$0.72 \pm 0.02$	$0.71 \pm 0.08$ (stat.) $\pm 0.09$ (syst.)

BACKUP NUCLEUS-NUCLEUS

# Recent developments on open quantum systems for quarkonia



Time evolution of HQ states in an expanding hot QCD medium by implementing EFT –pNRQCD- in the framework of open quantum systems

=> Lindblad equation

- non-Abelian nature of QCD: color transitions
- conserves the total number of heavy quarks
- avoids classical approximations

Brambilla, Escobedo, Soto & Vairo (2017)

In the same line: equations for the time evolution of the HQ reduced-density matrix in a non-Abelian QGP

Blaizot & Escobedo (2017)

- treat the relative motion of the heavy quarks semi-classically
- take into account the color transitions within 2 strategies:
  - instantaneously, perturbation theory => Langevin equation, analogous to QED
  - as collisions => Boltzmann equation

De Boni (2017)

Also: Schrödinger-Langevin equation

Gossiaux & Katz (2016)

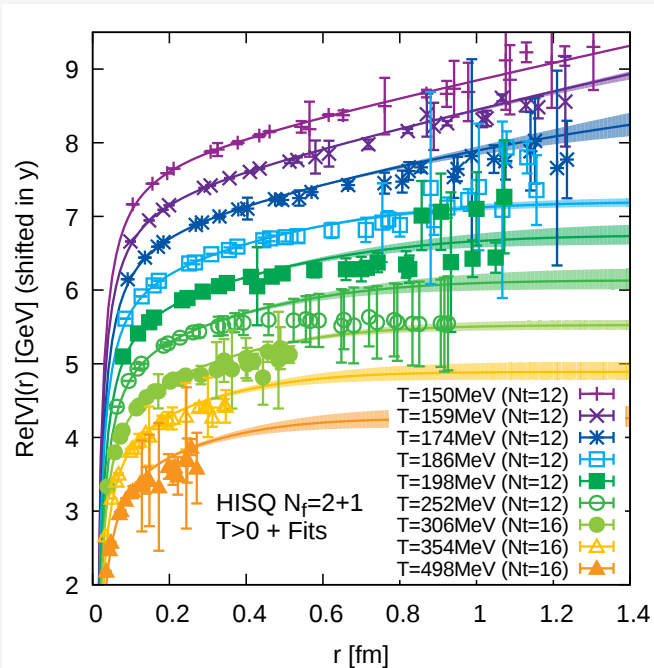
- interesting framework but not derived from first QCD principles
- QCD features enter in the parameters (similarly to Langevin dynamics in HF physics)

# In-medium Quarkonium properties from first principles

Realistic **lattice QCD**  
calculation of the complex in-  
medium **heavy quark potential**

P. Petreczky, A. Rothkopf, J. Weber  
[TUM-QCD] in preparation

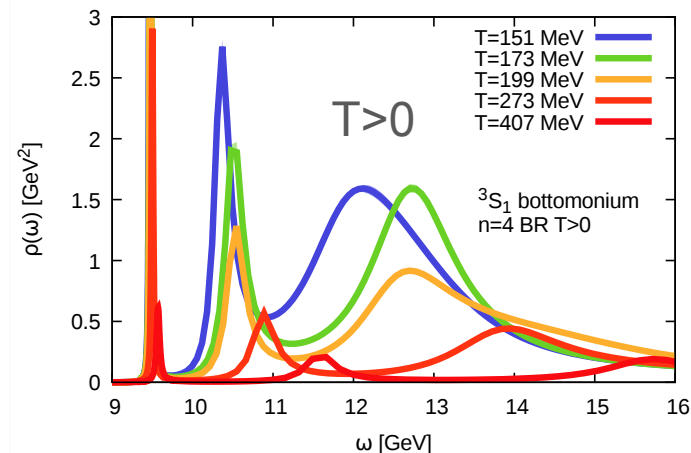
**Re[V]:**  
smooth transition Cornell  $\rightarrow$  Debye  
agrees with  $F^{(1)}$  within uncertainty



**non-zero Im[V] at  $T > T_c$  obtained**

In-medium quarkonium **spectral properties** from  
a lattice **effective field theory (NRQCD)**

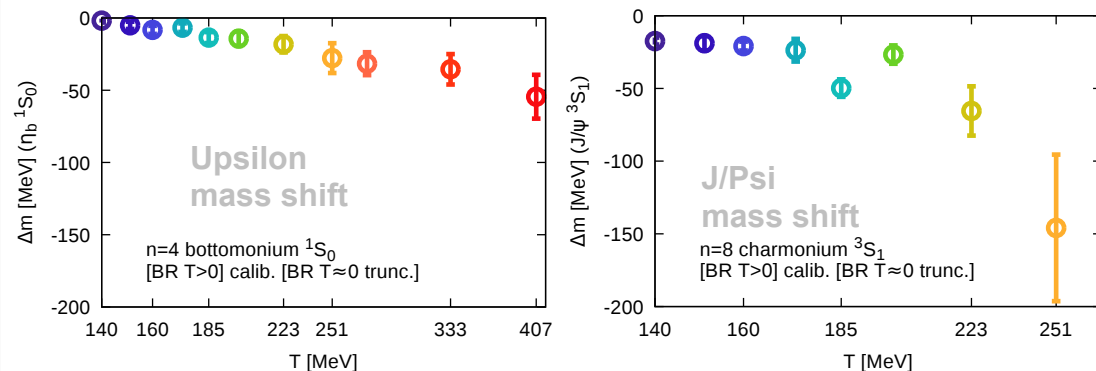
**Improved** spectral function extraction **algorithm**,  
**higher statistics**, **larger temperature range**



S. Kim, P. Petreczky,  
A. Rothkopf,  
in preparation

more accurate  
**melting  
temperatures**

Heavy  $Q\bar{Q}$  becomes **lighter** before melting

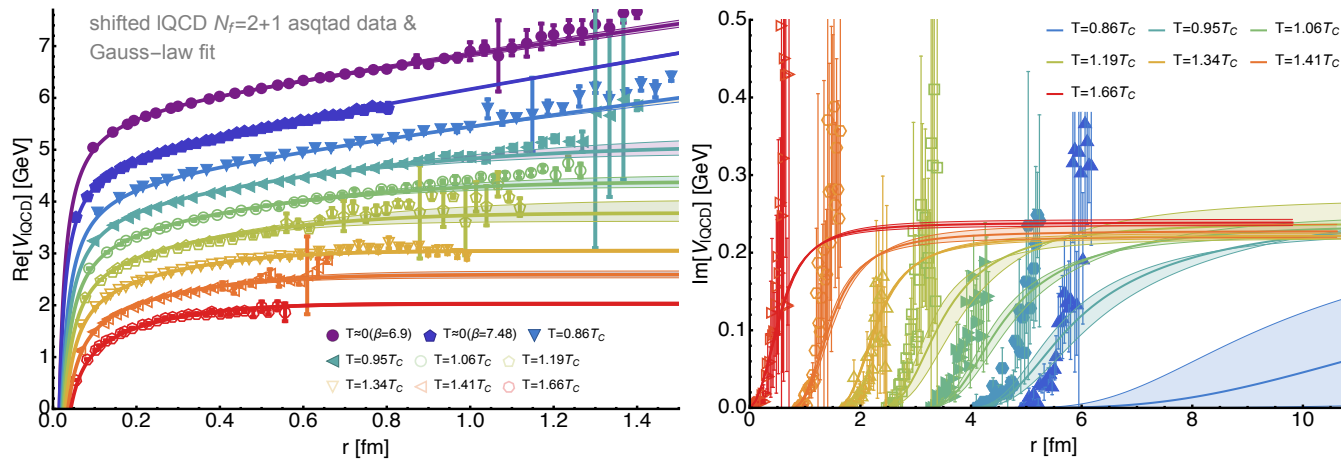


$\Delta m < 0$  consistent with potential based results

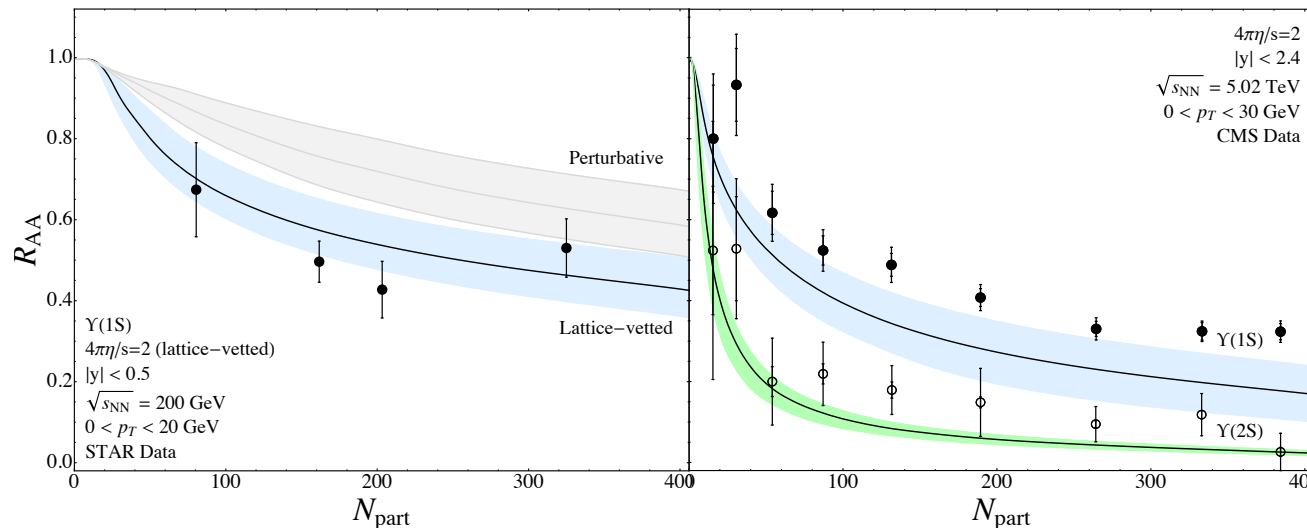
# Pheno: $\Upsilon$ suppression in anisotropic QGP with lattice potential

- lattice QCD vetted in-medium heavy-quark potential with anisotropic hydro QGP
- in-medium potential: complex values at high temperatures
- discrete values of the potential obtained from lattice QCD

Krouppa, Strickland, Rothkopf (2018)



- a single  $T$ -dependent parameter remains, the Debye mass  $m_D$

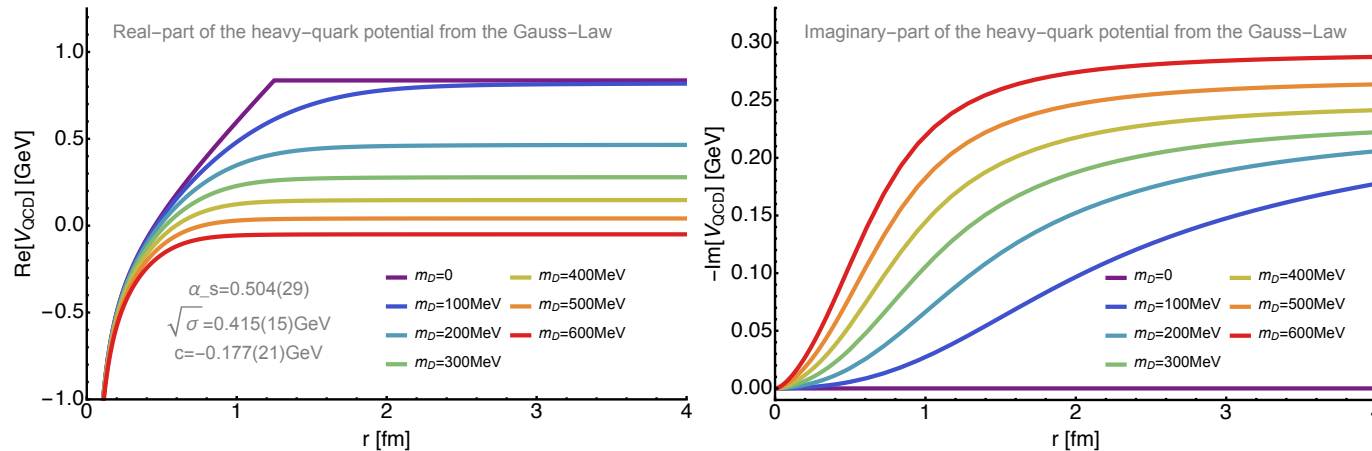


- feed down taken into account
- stronger imaginary part present in the lattice-vetted potential  $\Rightarrow \Upsilon$  states more easily dissociated
- space for recombination?

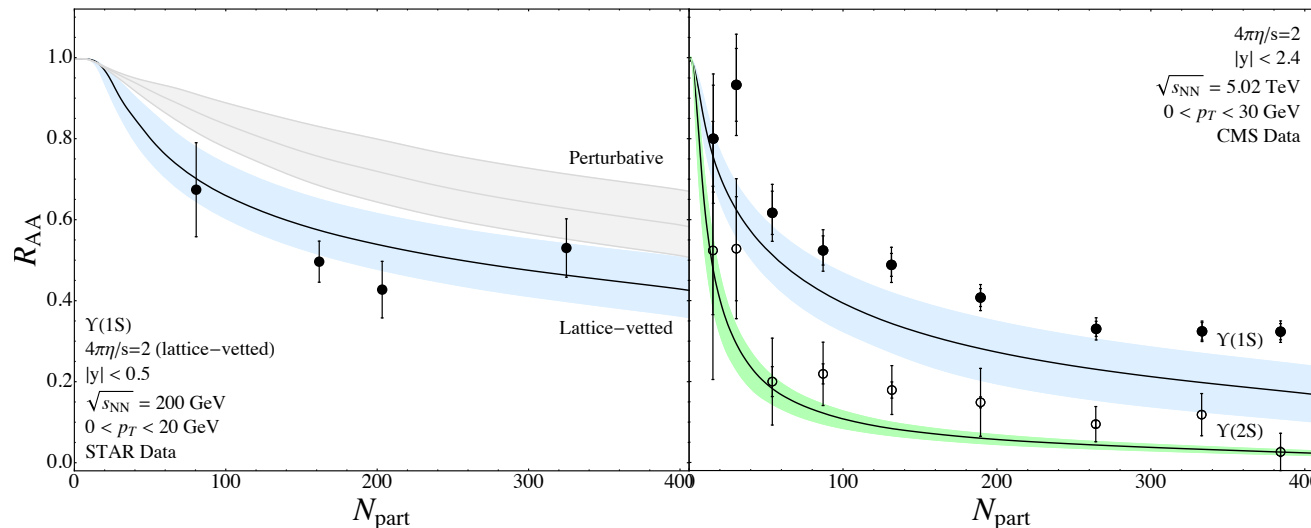
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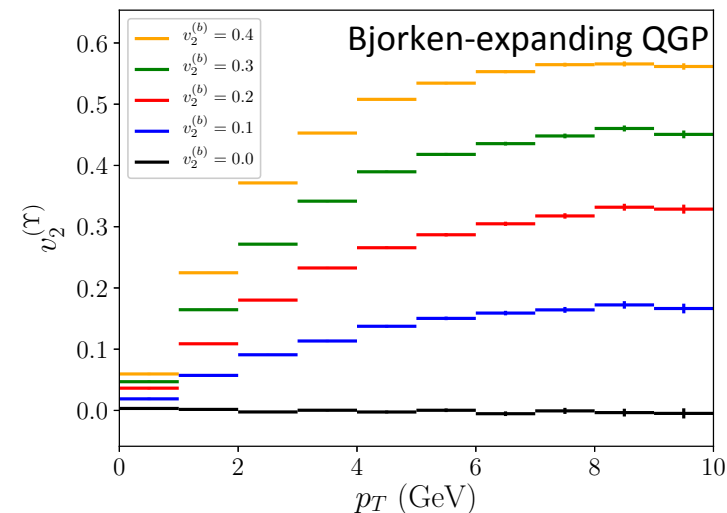


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# Phenomenology: recent developments

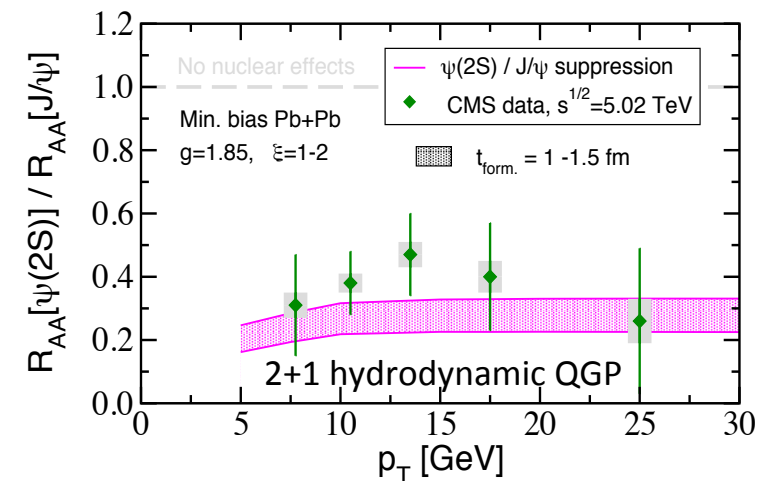
## Dynamical in-medium transport model:

- pNRQCD in a thermal QGP
- Stochastic Boltzmann equations
- HQ diffusion in the medium: necessary for the system to reach equilibrium
- Predicts  $v_2$  from recombination **Yao & Muller (2018)**



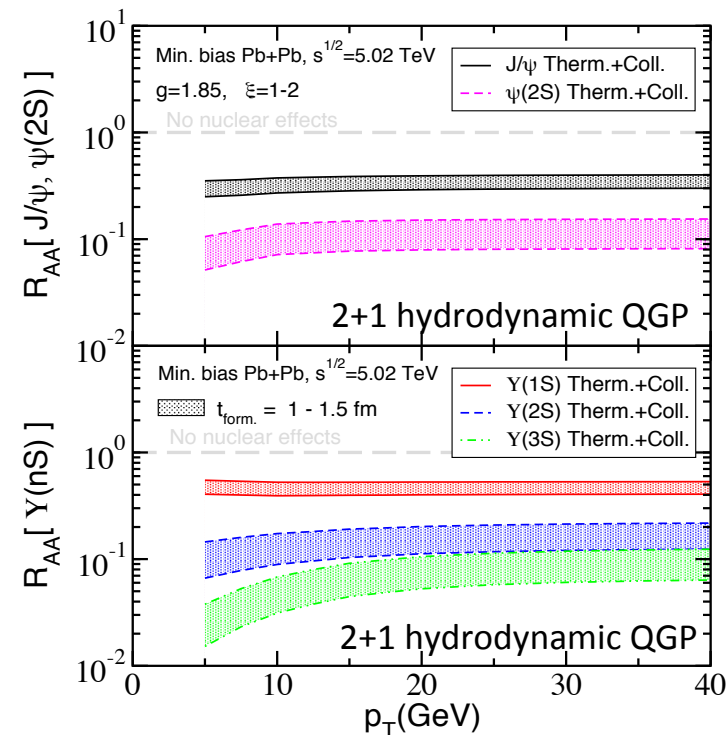
## Collisional and thermal dissociation at high $p_T$ :

- Collisional dissociation by  $p_T$  broadening
- Debye screening, no  $\text{Im}[V]$  **Vitev & Sharma (2017)**



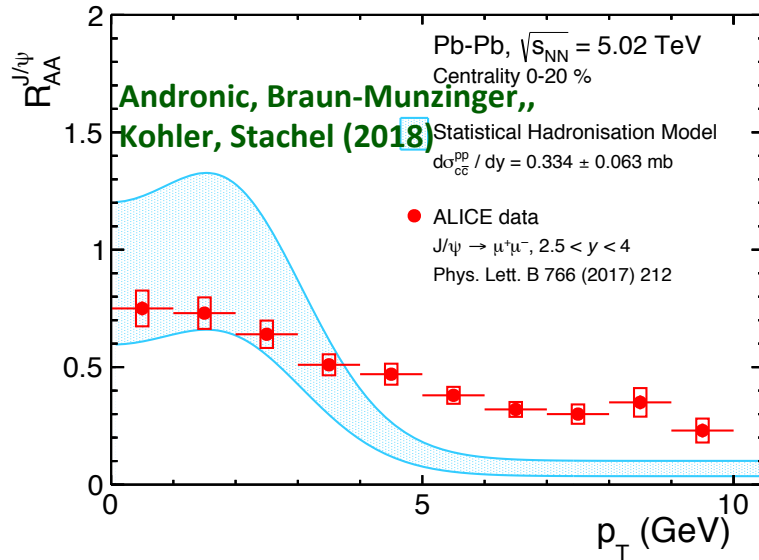
Quarkonium  
formation time  
 $\sim 1$  fm

NRQCD for  
nucleon-nucleon  
baseline

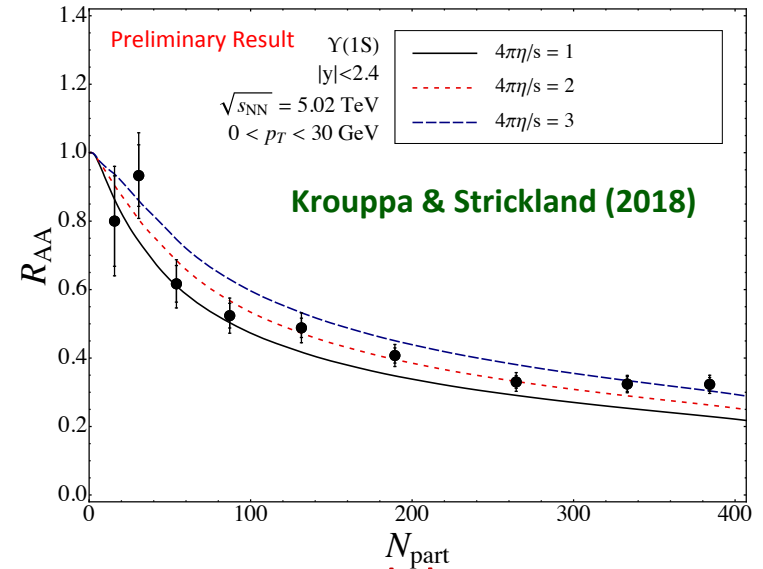


# Recent results from some long-lasting phenomenology models

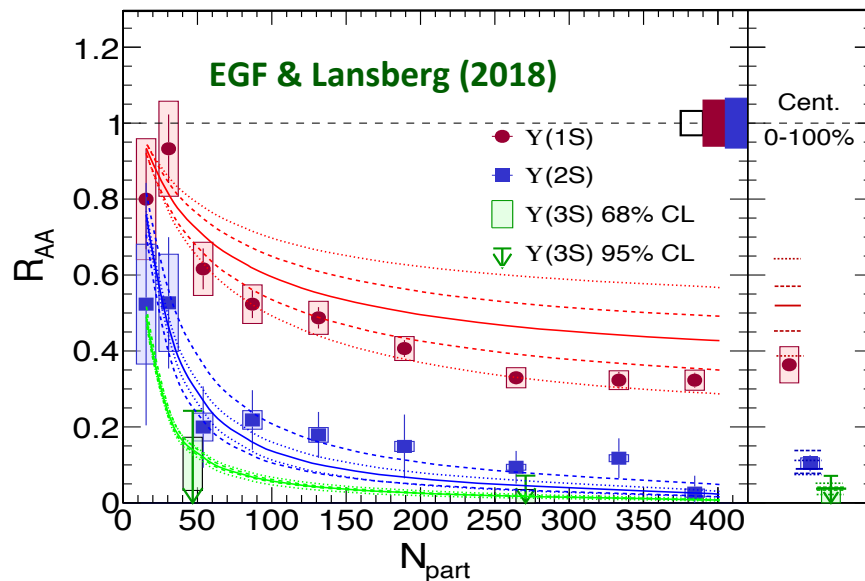
## Statistical hadronisation model



## a-hydro model



## Comover model



## Transport model

