

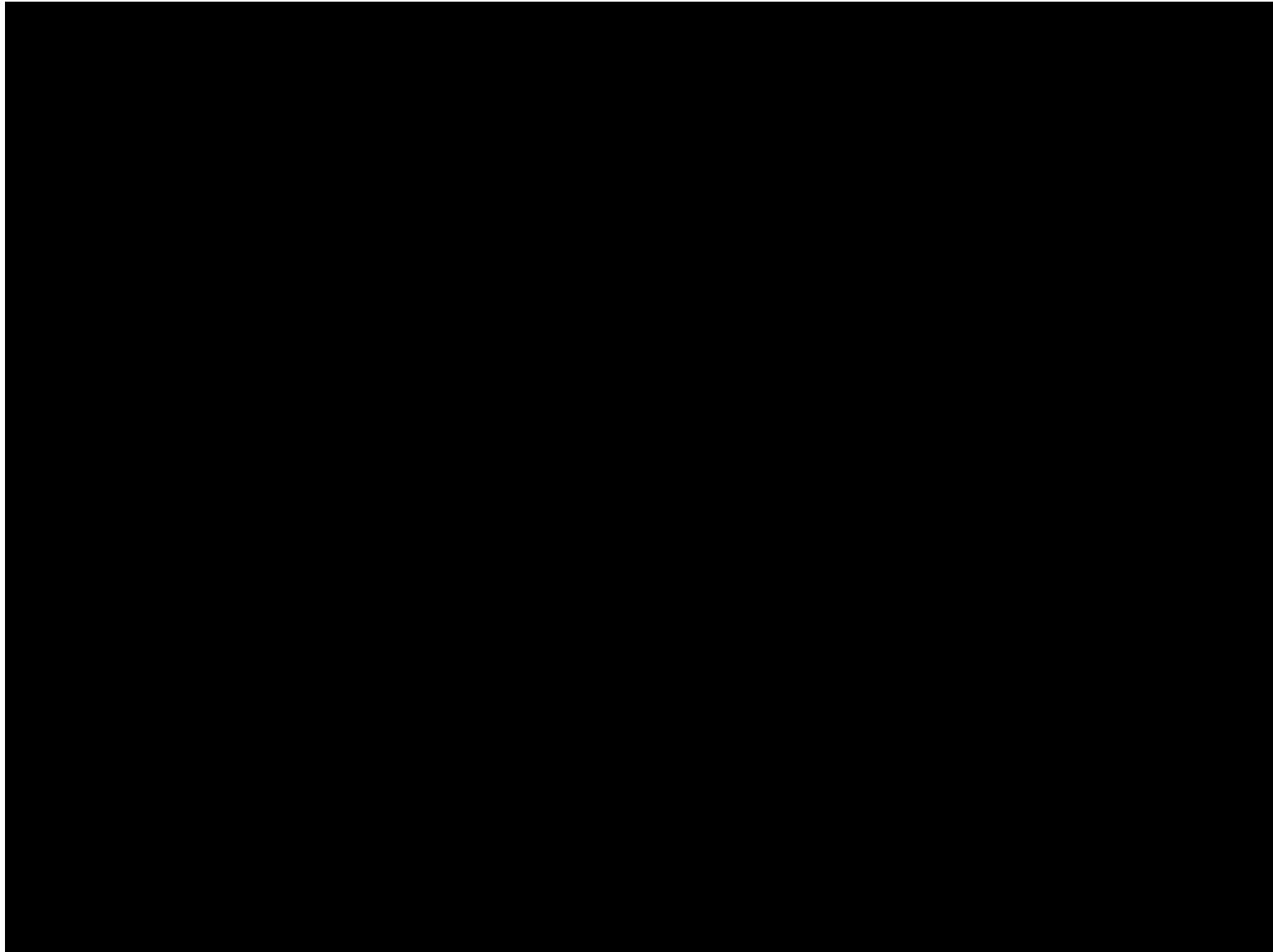
Collective excitations in nuclei: The isoscalar and isovector electric giant resonances and spin-isospin charge- exchange modes

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Vibrations of a liquid drop in weightlessness



In the following:

IS = Iso-Scalar

IV = Iso-Vector

S = Spin

G = Giant

M = Monopole

D = Dipole

Q = Quadrupole

O = Octupole

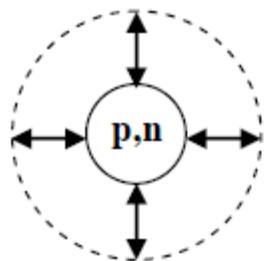
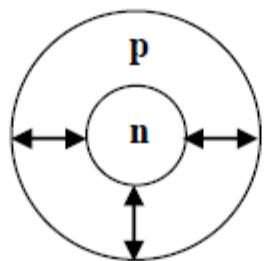
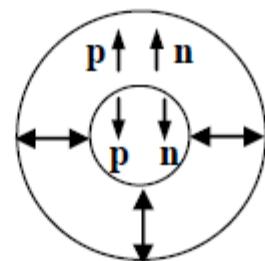
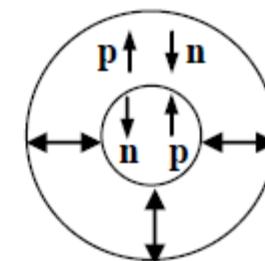
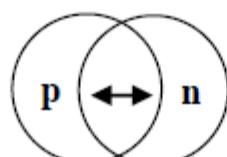
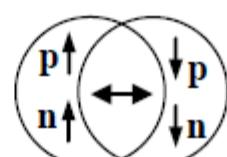
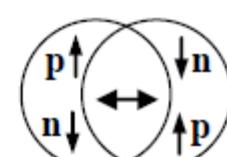
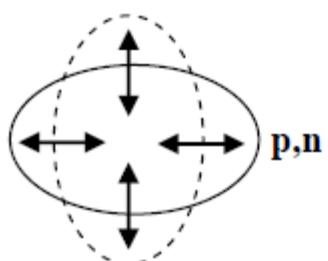
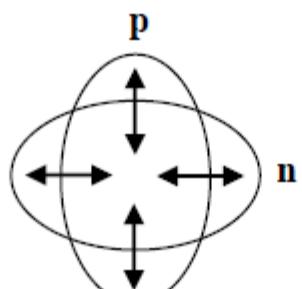
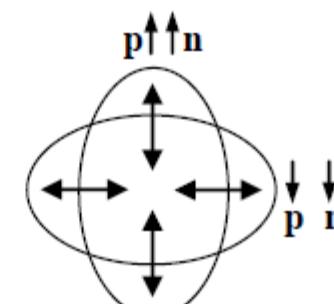
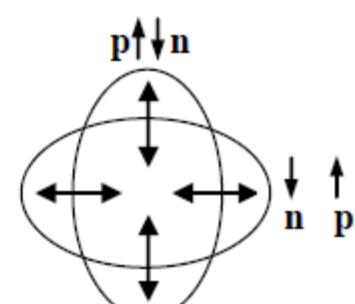
e.g., **ISGMR = Isoscalar giant monopole resonance**

ISGDR = Isoscalar giant dipole resonance

IVGDR = Isovector giant dipole resonance

IVSGMR = Isovector spin giant monopole resonance

IVSGDR = Isovector spin giant dipole resonance

$\Delta L = 0$ **ISGMR****IVGMR****ISSGMR****IVSGMR** $\Delta L = 1$ **ISGDR**
??**IVGDR****ISSGDR****IVSGDR** $\Delta L = 2$ **ISGQR****IVGQR****ISSGQR****IVSGQR** $\Delta T = 0$ $\Delta T = 1$ $\Delta T = 0$ $\Delta T = 1$ $\Delta S = 0$ $\Delta S = 0$ $\Delta S = 1$ $\Delta S = 1$

The Collective Response of the Nucleus: Giant Resonances

Compression modes

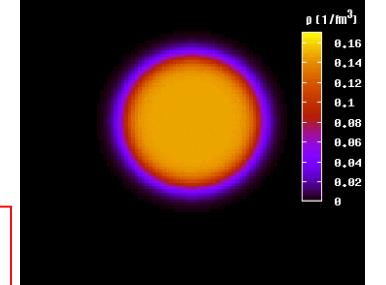
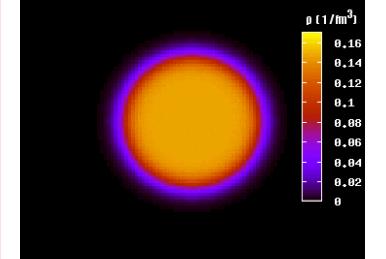
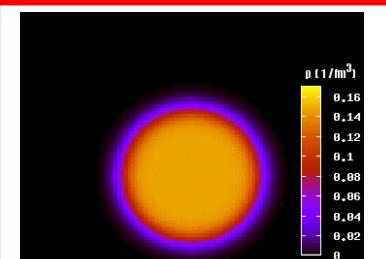
Monopole
 $\Delta L = 0$
(GMR)

Dipole
 $\Delta L = 1$
(GDR)

Quadrupole
 $\Delta L = 2$
(GQR)

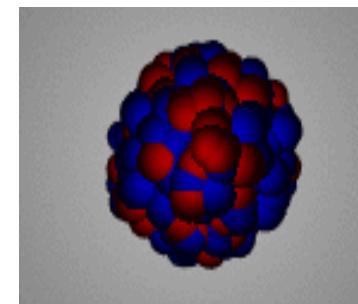
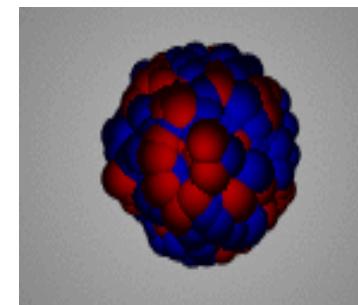
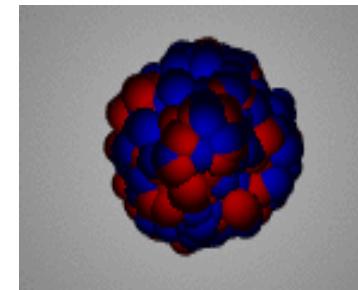
Isoscalar (In phase)

$$\Delta T = 0$$



Isovector (Out of phase)

$$\Delta T = 1$$



M. Itoh

Operators and Microscopic Structure

Microscopic picture: GRs are coherent (1p-1h) excitations induced by single-particle operators.

- Excitation energy depends on
 - i) multipole L ($L\hbar\omega$, since radial operator $\propto r^L$; except for ISGMR and ISGDR, $2\hbar\omega$ & $3\hbar\omega$, respectively),
 - ii) strength of effective interaction and
 - iii) collectivity.
- Exhaust appreciable % of EWSR
- Acquire a width due to coupling to continuum and to underlying 2p-2h configurations.

Microscopic structure of ISGMR & ISGDR

Transition operators:

$$O^{L=0} = \sum_i \cancel{r_i^0 Y_0^0} + \frac{1}{2} \sum_i r_i^2 Y_0^0 + \dots$$

Constant Overtone

$2\hbar\omega$ excitation

$$O^{L=1} = \sum_i \cancel{r_i^1 Y_0^1} + \frac{1}{2} \sum_i r_i^3 Y_0^1 + \dots$$

Spurious c.o.m. Overtone
motion

$3\hbar\omega$ excitation (overtone of c.o.m. motion)

Nucleus \longrightarrow Many-body system with a finite size

Vibrations \longrightarrow Multipole expansion with r, Y_{lm}, τ, σ

$\Delta S=0, \Delta T=0$ $\Delta S=0, \Delta T=1$ $\Delta S=0, \Delta T=1$ $\Delta S=1, \Delta T=1$ $\Delta S=1, \Delta T=1$

$L=0$: Monopole	ISGMR $r^2 Y_0$	IAS τY_0	IVGMR $\tau r^2 Y_0$	GTR $\tau \sigma Y_0$	IVSGMR $\tau \sigma r^2 Y_0$
$L=1$: Dipole	ISGDR $(r^3 - 5/3 \langle r^2 \rangle r) Y_1$		IVGDR $\tau r Y_1$		IVSGDR $\tau \sigma r Y_1$
$L=2$: Quadrupole	ISGQR $r^2 Y_2$		IVGQR $\tau r^2 Y_2$		IVSGQR $\tau \sigma r^2 Y_2$
$L=3$: Octupole	LEOR, HEOR $r^3 Y_3$			Dropped $\Delta S=1, \Delta T=0$ operators because excitations are very weak	

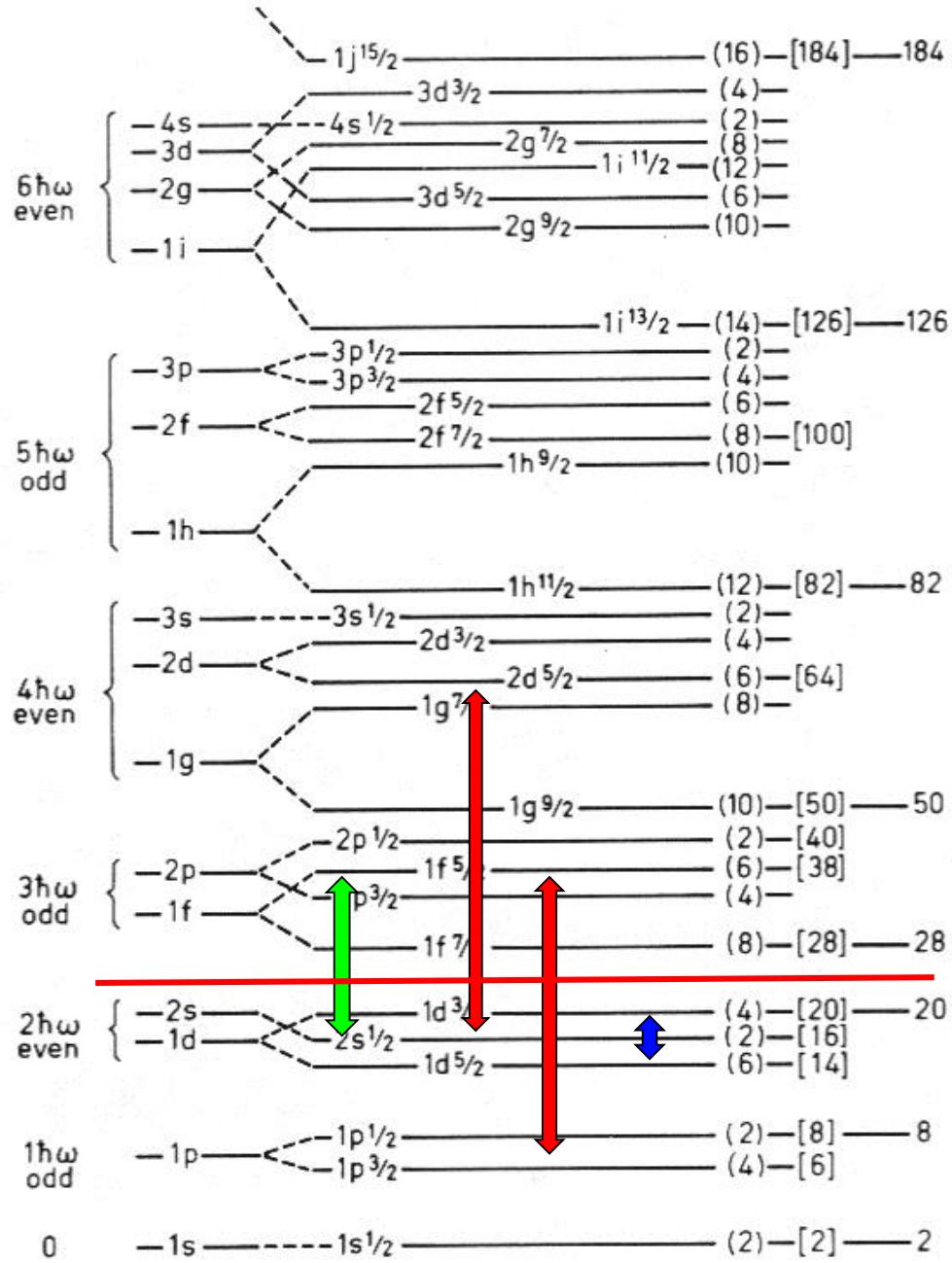
IVGDR
 τrY_1

↔ **$\Delta N = 1$ E1 (IVGDR)**

↔ **$\Delta N = 2$ E2 (ISGQR)**
↔ **$\Delta N = 0$ E0 (ISGMR)**

ISGMR
 r^2Y_0

ISGQR
 r^2Y_2



Decay of giant resonances

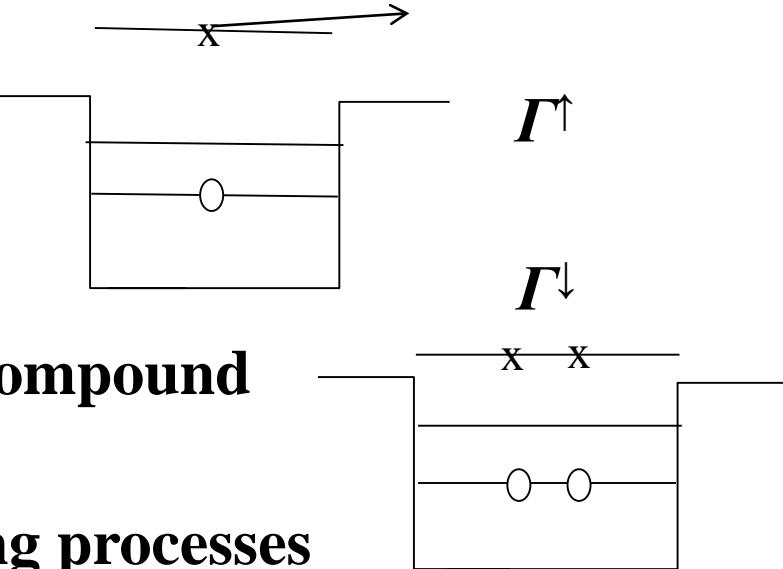
■ Width of resonance

$$\Gamma, \Gamma^\uparrow, \Gamma^\downarrow (\Gamma^{\downarrow\uparrow}, \Gamma^{\downarrow\downarrow})$$

■ Γ^\uparrow : direct or escape width

■ Γ^\downarrow : spreading width

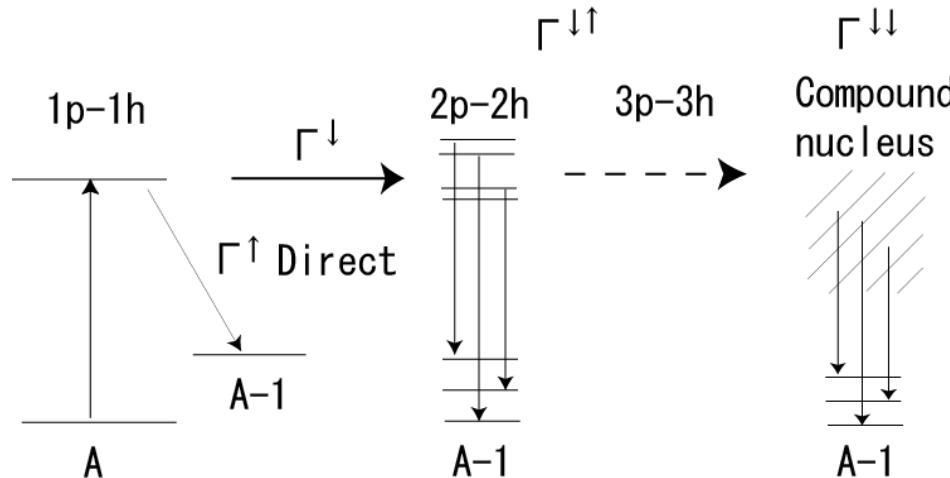
$\Gamma^{\downarrow\uparrow}$: pre-equilibrium, $\Gamma^{\downarrow\downarrow}$: compound



■ Decay measurements

⇒ Direct reflection of damping processes

Allows detailed comparison with theoretical calculations



Energy-Weighted Sum Rules

Intermezzo: Sum rules

Consider the most general electric multipole operator (Bohr & Mottelson 69), neglecting the current term:

$$\mathcal{M}(E\lambda, \mu) = \frac{(2\lambda + 1)!!}{q^\lambda(\lambda + 1)} \int \rho(\vec{r}) \frac{\partial}{\partial r} (r j_\lambda(qr)) Y_{\lambda\mu}(\hat{r}) d\tau$$

$$j_\lambda(qr) = \frac{(qr)^\lambda}{(2\lambda + 1)!!} \left(1 - \frac{1}{2} \frac{(qr)^2}{(2\lambda + 3)} + \dots \right)$$

Bessel function

This leads in 1st order (long-wave length limit, i.e. $qr \ll 1$):

$$\mathcal{M}(E\lambda, \mu) = \frac{(2\lambda + 1)!!}{q^\lambda(\lambda + 1)} \int \rho(\vec{r}) \frac{\partial}{\partial r} \left(\frac{r(qr)^\lambda}{(2\lambda + 1)!!} \right) Y_{\lambda\mu}(\hat{r}) d\tau$$

$$\mathcal{M}(E\lambda, \mu) = \int \rho(\vec{r}) r^\lambda Y_{\lambda\mu}(\hat{r}) d\tau$$

Using $\rho(\vec{r}) = \sum_k e \left(\frac{1}{2} - t_{zk} \right) \delta(\vec{r} - \vec{r}_k)$

we get:

$$\mathcal{M}(E\lambda, \mu) = \sum_k e \left(\frac{1}{2} - t_{zk} \right) r_k^\lambda Y_{\lambda\mu}(\Omega_k)$$

$$\mathcal{M}(E\lambda, \mu) = \frac{1}{2} e \sum_k r_k^\lambda Y_{\lambda\mu}(\Omega_k) - e \sum_k t_{zk} r_k^\lambda Y_{\lambda\mu}(\Omega_k)$$

For the isoscalar $E0$ and $E1$, 1st order leads to a constant and c.o.m. coordinate, respectively. Expanding to 2nd order (taking only dependence on r) we get:

$$\mathcal{M}(E0) = \frac{1}{4} e \sum_k r_k^2 - \frac{1}{2} e \sum_k t_{zk} r_k^2$$

Isoscalar Isovector

$$\mathcal{M}(E1, \mu) = \frac{1}{4} e \sum_k r_k^3 Y_{1\mu}(\Omega_k)$$

Isovector term
neglected

Thomas Reiche Kuhn (TRK) sum rule is originally obtained for an atomic system assuming an electric field directed along z-axis:

$$S_e(E1) = \sum_f (E_f - E_i) |\langle f | \sum_k z_k | i \rangle|^2$$

The total absorption cross section is in the long-wave length limit:

$$\int_0^\infty \sigma(E_\gamma) dE_\gamma = \frac{4\pi^2 e^2}{\hbar c} \sum_f (E_f - E_i) |\langle f | \sum_k z_k | i \rangle|^2$$

For a Hermitian operator and using closure relation

$(\sum_f |f \rangle \langle f| = 1)$, we obtain:

$$\int_0^\infty \sigma(E_\gamma) dE_\gamma = \frac{4\pi^2 e^2}{\hbar c} \frac{1}{2} \langle i | [\sum_k z_k, [H, \sum_k z_k]] | i \rangle$$

Consider only kinetic term of Hamiltonian:

$$\int_0^\infty \sigma(E_\gamma) dE_\gamma = \frac{4\pi^2 e^2}{\hbar c} \frac{1}{2} \left\langle i \left| \left[\sum_k z_k, \left[\frac{p_z^2}{2m_e}, \sum_k z_k \right] \right] \right| i \right\rangle$$

$$\int_0^\infty \sigma(E_\gamma) dE_\gamma = \frac{4\pi^2 e^2}{\hbar c} \frac{\hbar^2 I}{2m_e}$$

I is number of electrons. For a nucleus (see later):

$$e_{eff}^2 I = Z e_{peff}^2 + N e_{neff}^2 = \frac{NZ}{A} e^2$$

Therefore:

$$\int_0^\infty \sigma(E_\gamma) dE_\gamma = \frac{2\pi^2 e^2 \hbar}{mc} \frac{NZ}{A} = 60 \frac{NZ}{A} \text{ MeV mb}$$

This is the TRK sum rule for a nucleus.

$$B(E\lambda, J_i \rightarrow J_f) = \sum_{\mu M_f} |\langle \Psi_f | \mathcal{M}(E\lambda, \mu) | \Psi_i \rangle|^2$$

$$B(E\lambda, J_i \rightarrow J_f) = \sum_{\mu M_f} \langle J_i M_i \lambda \mu | J_f M_f \rangle^2 |\langle \Psi_f | \mathcal{M}(E\lambda) | \Psi_i \rangle|^2$$

$$B(E\lambda, J_i \rightarrow J_f) = \frac{2J_f + 1}{2J_i + 1} |\langle \Psi_f | \mathcal{M}(E\lambda) | \Psi_i \rangle|^2$$

$$S_\lambda(E\lambda) = \sum_f (E_f - E_i) |\langle f | \mathcal{M}(E\lambda, \mu) | i \rangle|^2$$

$$\Rightarrow S_\lambda(E\lambda) = \frac{1}{2} |\langle i | [\mathcal{M}(E\lambda, \mu), [H, \mathcal{M}(E\lambda, \mu)]] | i \rangle|$$

Introducing for $\mathcal{M}(E\lambda, \mu)$ the isoscalar $E0$, $E1$ and $E\lambda$ operators, and using a similar procedure as for TRK sum rule (using Hermitian property and closure relation), we obtain the isoscalar $E0$, $E1$ and $E\lambda$ energy-weighted sum rules (EWSR).

$$P_{0\mu} = \frac{1}{2} \sum_i r_i^2$$

$$\sum_n (E_n - E_0) B(E0, 0 \rightarrow n) = S_0 = \frac{\hbar^2}{2m} A \langle r^2 \rangle$$

$$P_{1\mu} = \frac{1}{2} \sum_i r_i^3 Y_{1\mu}(r_i)$$

$$\sum_n (E_n - E_0) B(E1, 0 \rightarrow n) = S_1 = \frac{\hbar^2}{8\pi m} \frac{3}{4} A [11 \langle r^4 \rangle - \frac{25}{3} \langle r^2 \rangle^2 - 10\varepsilon \langle r^2 \rangle]$$

$$\varepsilon = \left(\frac{4}{E_2} + \frac{5}{E_0} \right) \frac{\hbar^2}{3mA}$$

$$Q_{\lambda\mu} = \sum_i r_i^\lambda Y_{\lambda\mu}(r_i)$$

$$\sum_n (E_n - E_0) B(E\lambda, 0 \rightarrow n) = S_\lambda = \frac{\hbar^2}{8\pi m} \lambda (2\lambda + 1)^2 A \langle r^{2\lambda - 2} \rangle$$

Isovector E1 operator

$$\mathcal{M}(E1) = \sum_{k=1}^A e \left(\frac{1}{2} - t_{zk} \right) \vec{r}_k^{int}$$

$$\vec{r}_k = \vec{R} + \vec{r}_k^{int} \quad \text{where } \vec{R} = \sum_k \vec{r}_k / A$$

$$\mathcal{M}(E1) = e \sum_{k=1}^A \left(\frac{1}{2} - t_{zk} \right) (\vec{r}_k - \vec{R})$$

$$\mathcal{M}(E1) = -e \sum_{k=1}^A t_{zk} (\vec{r}_k - \vec{R})$$

$$\mathcal{M}(E1) = e \sum_{k=1}^A \left(\frac{N-Z}{2A} - t_{zk} \right) \vec{r}_k$$

⇒ Effective charges for neutrons and protons

$$e_D = e \left(\frac{N-Z}{2A} - t_{zk} \right) = \begin{cases} \frac{N}{A} e & \text{for proton} \\ -\frac{Z}{A} e & \text{for neutron} \end{cases}$$

$$\sum_n (E_n - E_0) B(E\lambda, 0 \rightarrow n) = S_\lambda = \frac{\hbar^2}{8\pi m} \lambda (2\lambda + 1)^2 A \langle r^{2\lambda-2} \rangle$$

For isovector $E1$, $\lambda=1$ and A becomes $Ze_{peff}^2 + Ne_{neff}^2$, which leads to:

$$\sum_n (E_n - E_0) B(E1, 0 \rightarrow n) = \frac{\hbar^2}{8\pi m} 9 \left[Z \left(\frac{N}{A} \right)^2 e^2 \right]$$

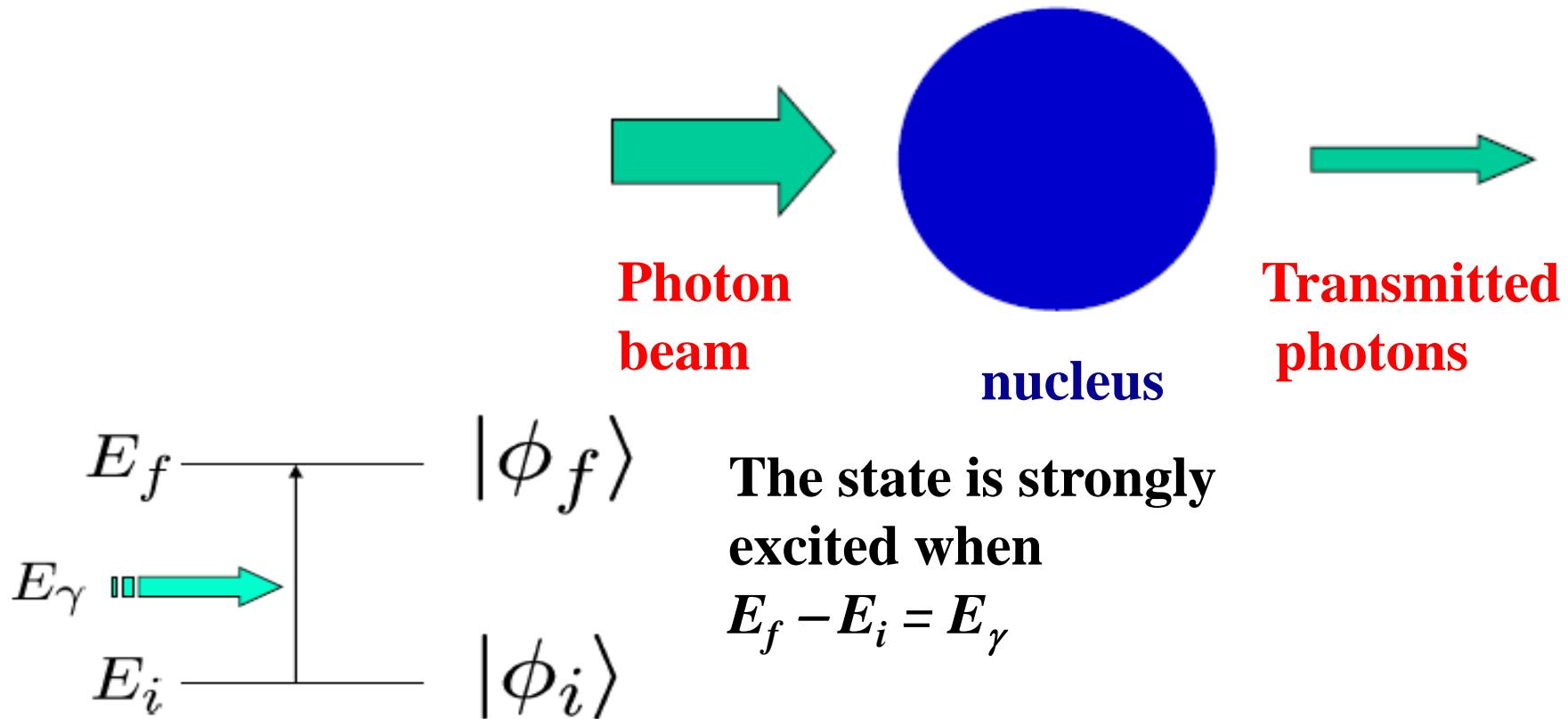
IVGDR

Consider isovector electric dipole excitations.

How does a nucleus respond to an external perturbation,
e.g., real photons?

⇒ Photo-absorption cross section

γ-rays from bremsstrahlung or positron capture in flight

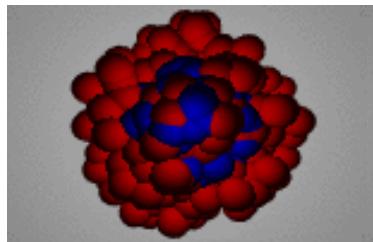


Nuclear Collective response

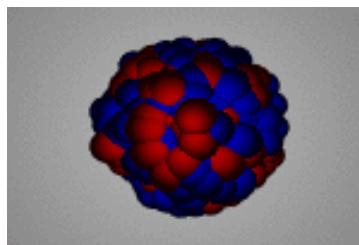
Giant Resonances

Isovector Electric
Giant Resonances

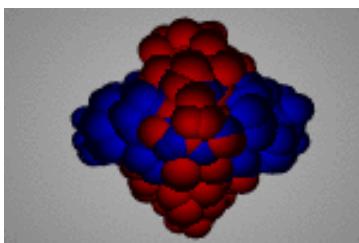
Isovector



Monopole
(IVGMR)

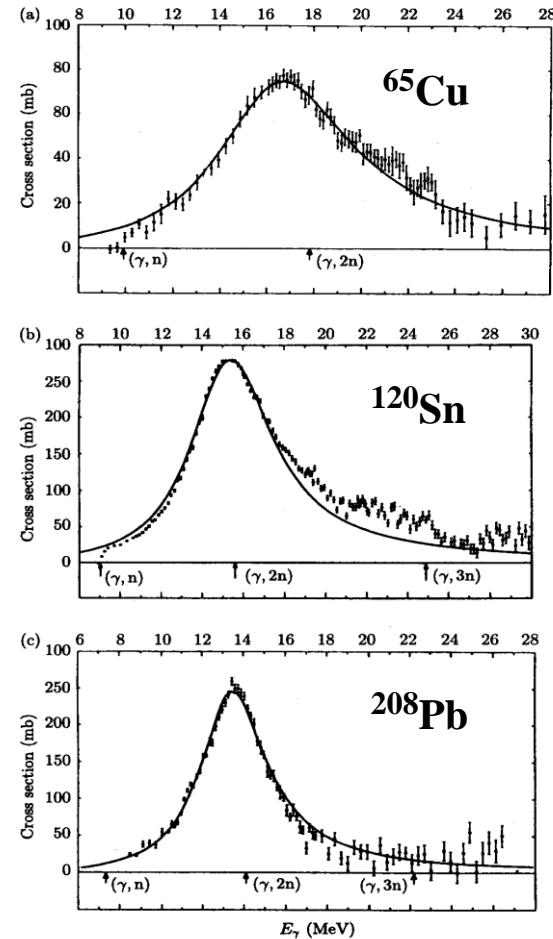


Dipole
(IVGDR)



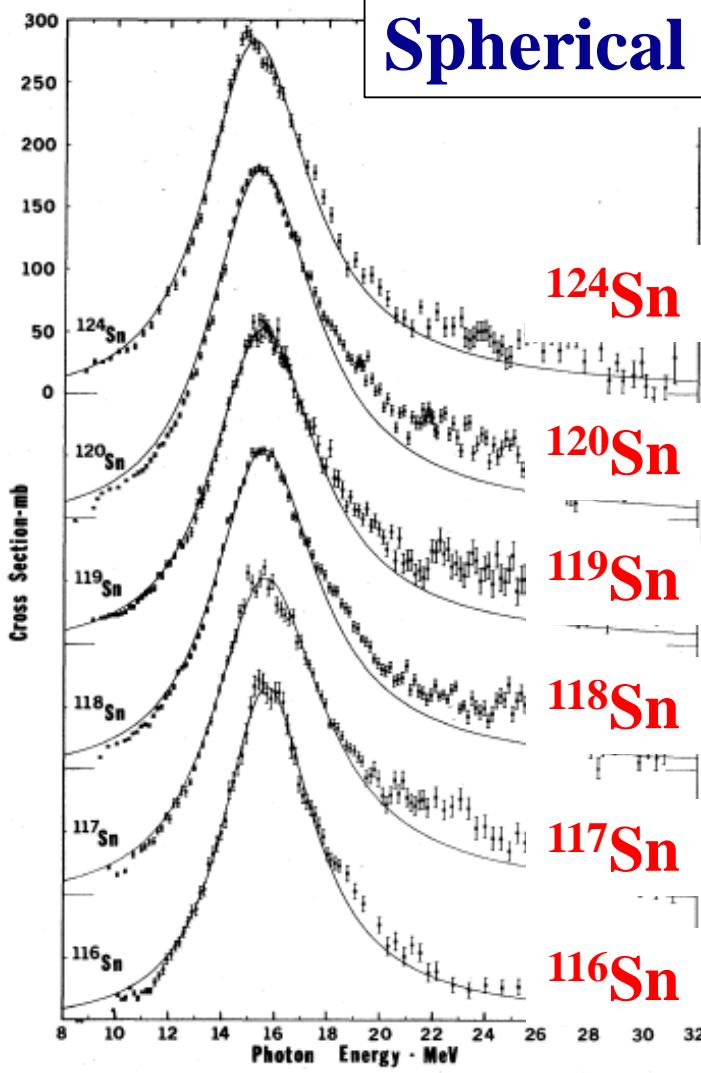
Quadrupole
(IVGQR)

Photo-neutron
cross sections

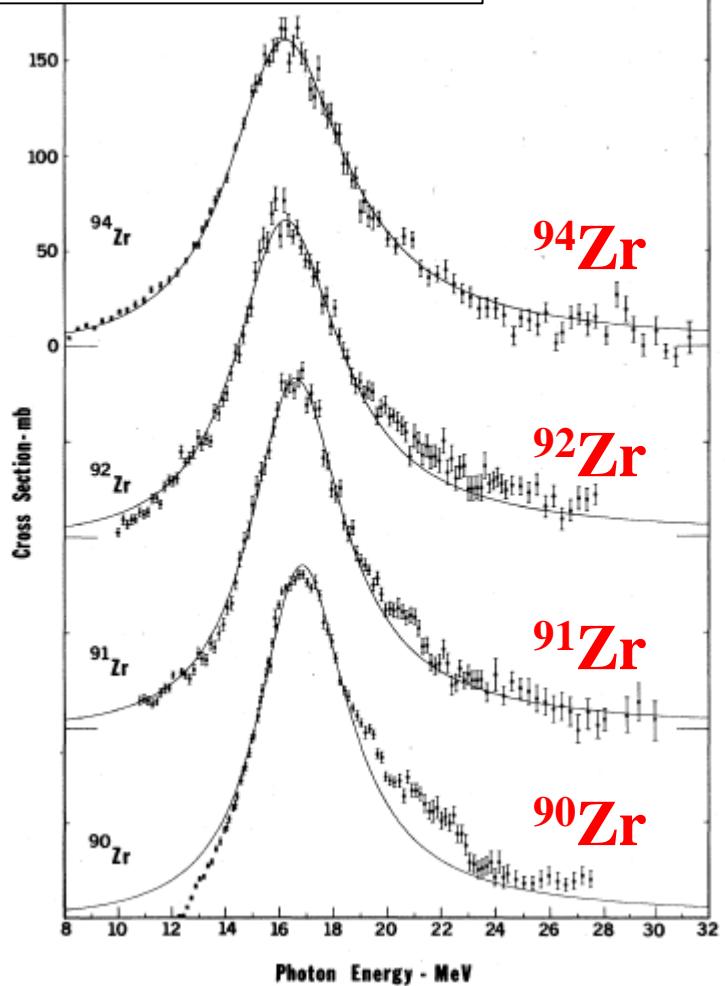
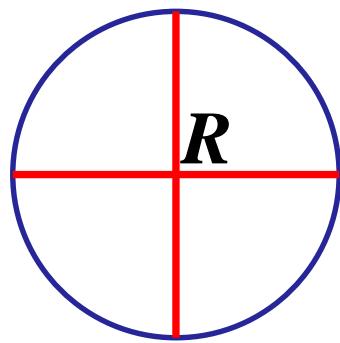


Isovector Giant Dipole Resonances: Photo-neutron cross section

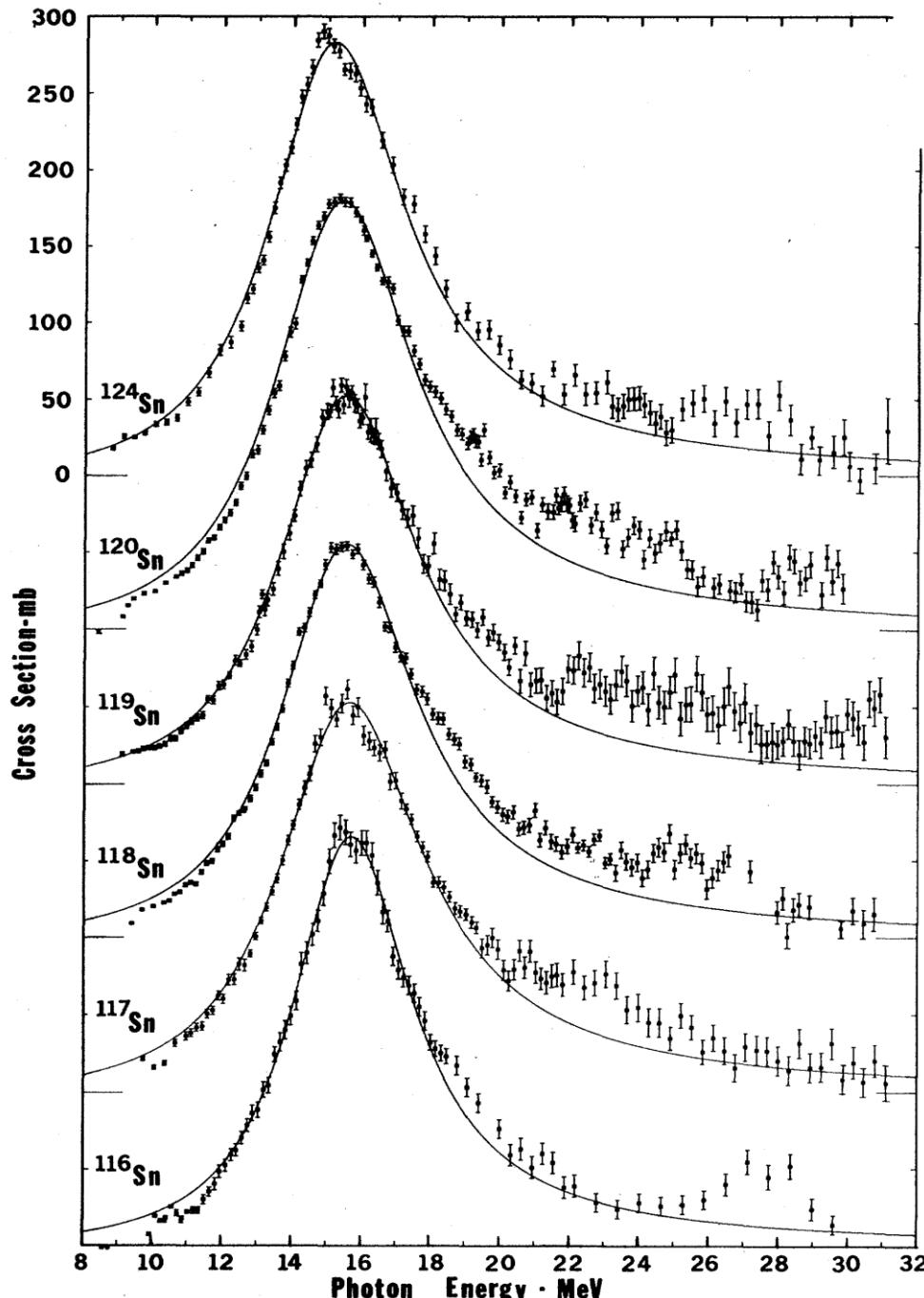
Spherical and nearly spherical nuclei



$$\omega \propto \frac{1}{R} \propto A^{-\frac{1}{3}}$$



B. L. Berman and S. C. Fultz, Rev. Mod. Phys. 47 (1975) 713



Measurement of the giant dipole resonance with mono-energetic photons

B.L. Berman and S.C. Fultz
Rev. Mod. Phys. 47 (1975) 713

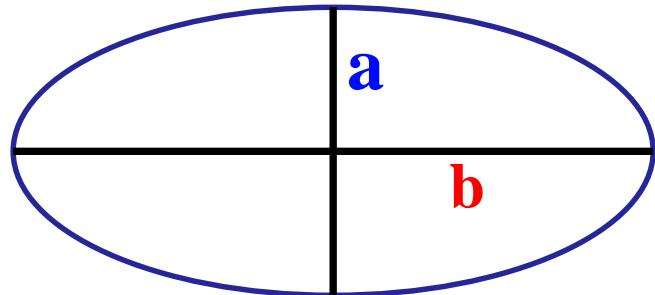
Nucleus	Centroid (MeV)	Width (MeV)
116Sn	15.68	4.19
117Sn	15.66	5.02
118Sn	15.59	4.77
119Sn	15.53	4.81
120Sn	15.40	4.89
124Sn	15.19	4.81

Photo-neutron cross section in deformed nuclei:

Deformed Nucleus

$$R(\theta, \phi) = R_0(1 + \beta_2 Y_{20}(\theta, \phi))$$

$$\beta_2(^{150}\text{Nd}) = 0.285(3)$$



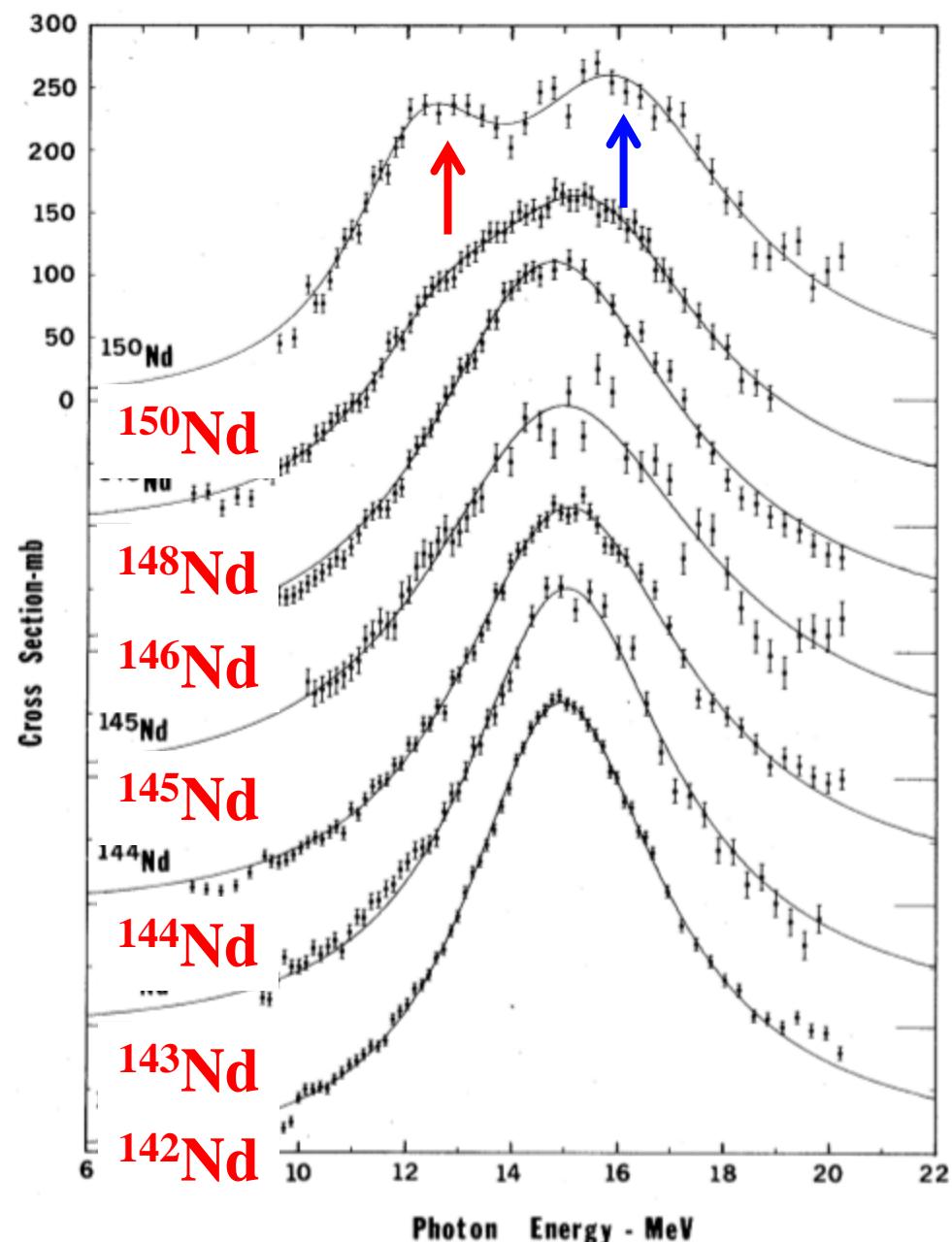
Excitation energies:

$$E_2/E_1 = 0.911\eta + 0.089$$

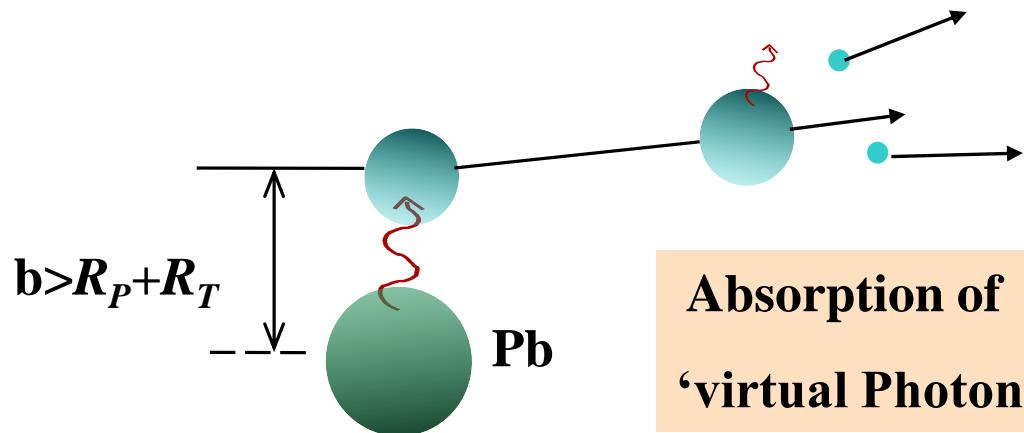
Where $\eta = b/a$

$$S_1/S_2 = 1/2$$

B. L. Berman and S. C. Fultz,
Rev. Mod. Phys. 47, 713 (1975)



Experimental Tool: Electromagnetic excitation at high energies

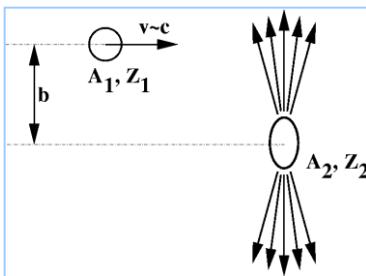


Absorption of
'virtual Photons'

$$\sigma_{e.m.} \sim Z^2$$

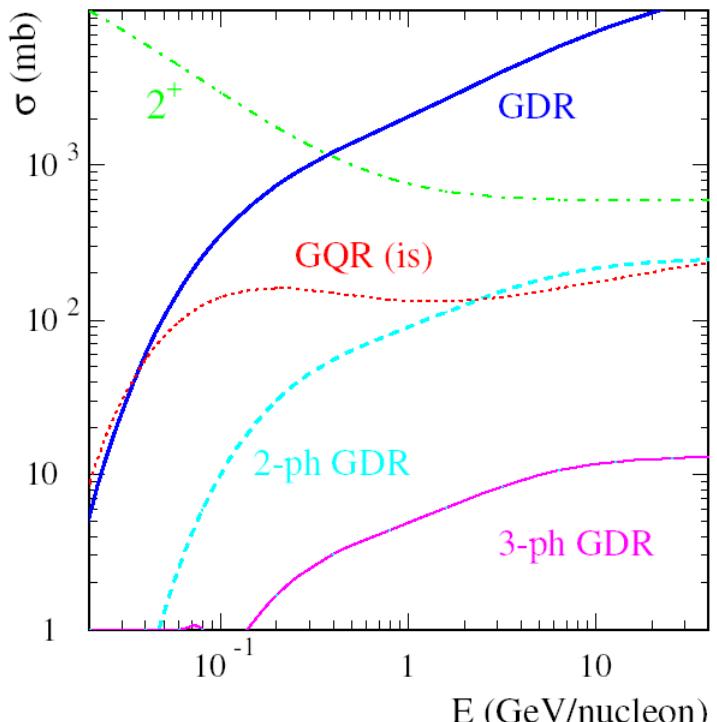
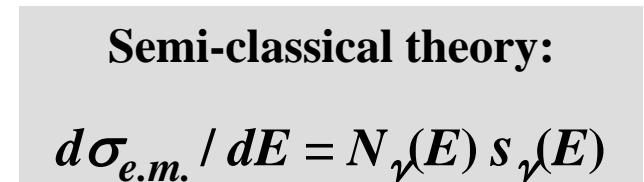
adiabatic cut-off:

$$E_{\max} = \frac{\hbar}{\tau} = \frac{\hbar c \gamma \beta}{b}$$



High velocities $v/c \approx 0.6-0.9$
 \Rightarrow High-frequency Fourier components

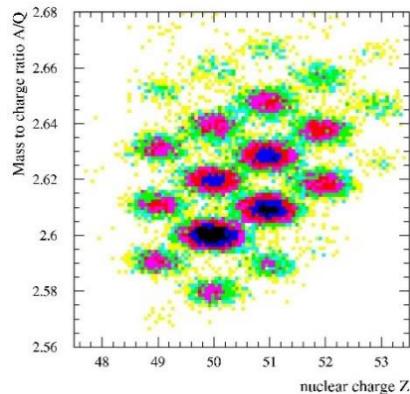
$$E_{\gamma, \max} \approx 25 \text{ MeV} (@ 1 \text{ GeV/u})$$



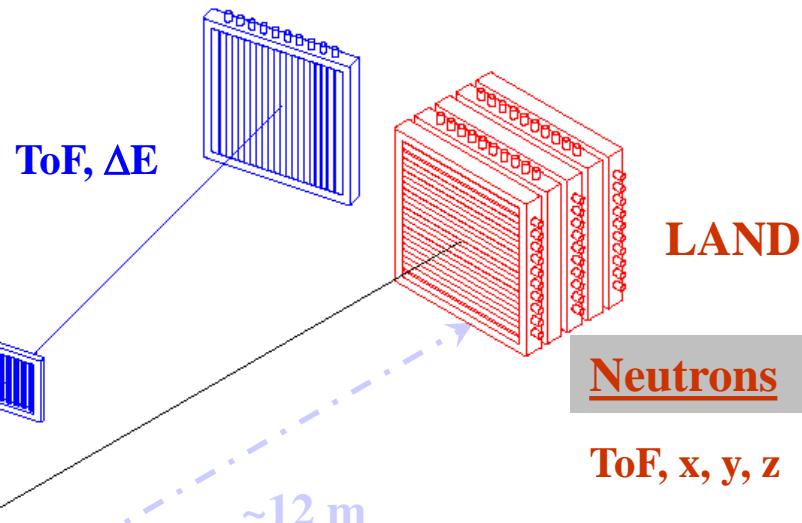
Determination of 'photon energy' (excitation energy) via a kinematically complete measurement of the momenta of all outgoing particles (invariant mass)

Experimental Scheme: The LAND reaction setup @GSI

Mixed beam

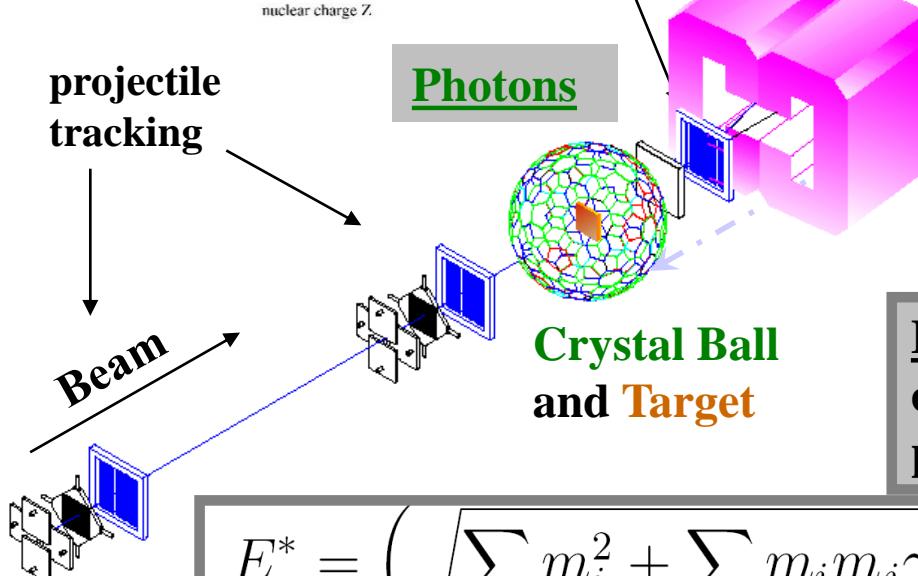


Charged fragments



projectile tracking

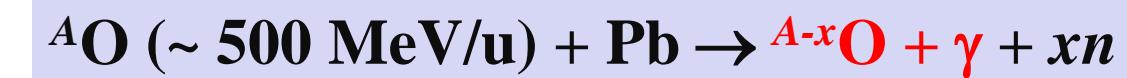
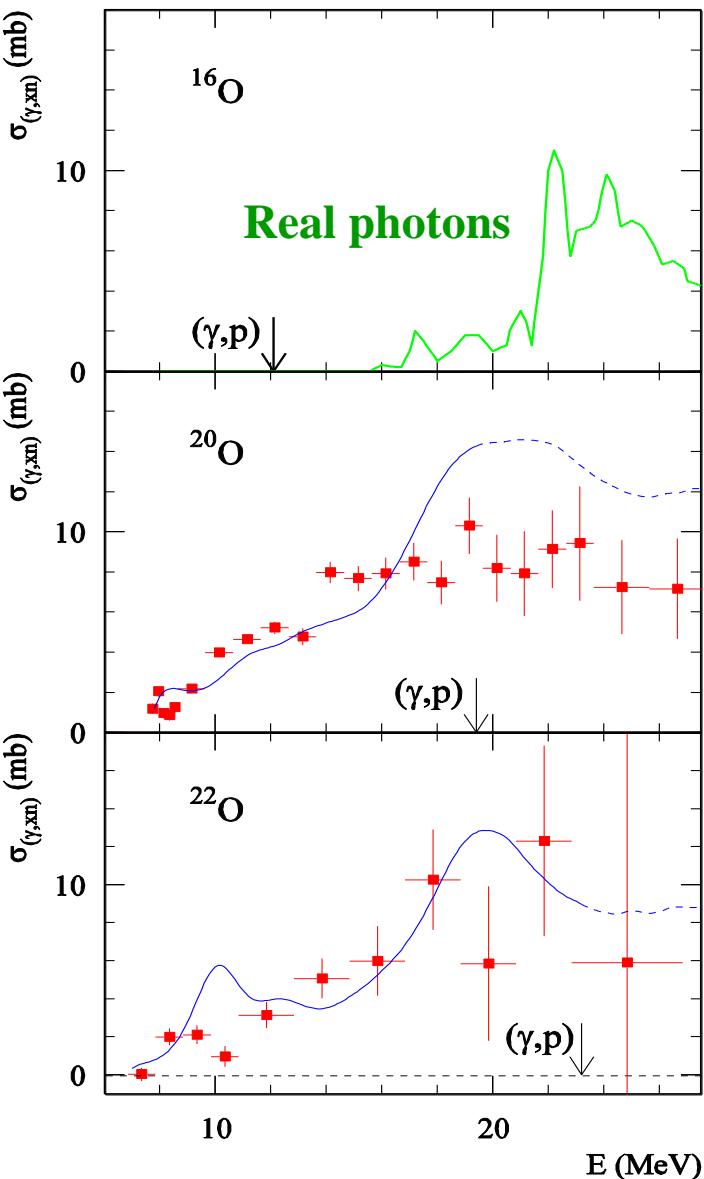
Photons



Excitation energy E^* from kinematically complete measurement of all outgoing particles:

$$E^* = \left(\sqrt{\sum_i m_i^2 + \sum_{i \neq j} m_i m_j \gamma_i \gamma_j (1 - \beta_i \beta_j \cos \theta_{ij})} - m_{proj} \right) c^2 + E_\gamma$$

Dipole Strength Distribution of n-Rich Nuclei



$N-Z=0$

\Rightarrow Photo-neutron cross sections from virtual photons

$N-Z=4$

\Rightarrow Low-lying dipole strength

\Rightarrow Fragmentation of GDR strength

? Collective soft mode ?

$N-Z=6$

— Large-scale shell model calculation

H. Sagawa, T. Suzuki,

Phys. Rev. C 59 (1999) 3116

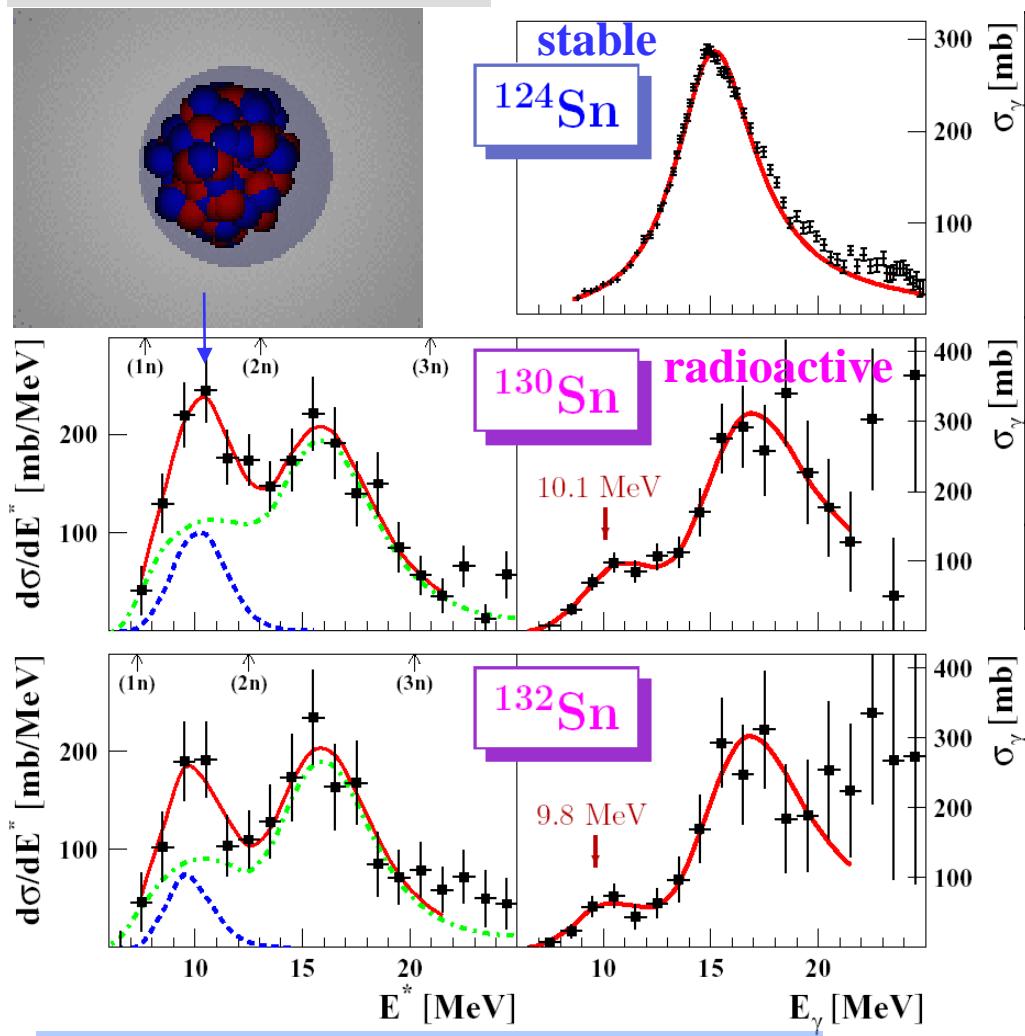
Data: LAND-FRS@GSI

A. Leistenschneider *et al.*, Phys. Rev. Lett. 86 (2001) 5442

Dipole strength distributions in neutron-rich Sn isotopes

Electromagnetic-excitation
cross section

Photo-neutron cross section



P. Adrich *et al.*, PRL 95 (2005) 132501

A	PDR		GDR		
	E_{centr} [MeV]	sum-rule fraction [%]	E_{centr} [MeV]	Γ [MeV]	sum-rule fraction [%]
^{124}Sn	-	-	15.3	4.8	116
^{130}Sn	10.1 (0.7)	7.0 (3.0)	15.9 (0.5)	4.8 (1.8)	145 (19)
^{132}Sn	9.8 (0.7)	4.0 (3.1)	16.1 (0.8)	4.7 (2.2)	125 (32)

PDR

- located at 10 MeV
- exhausts a few % TRK sum rule
- in agreement with theory

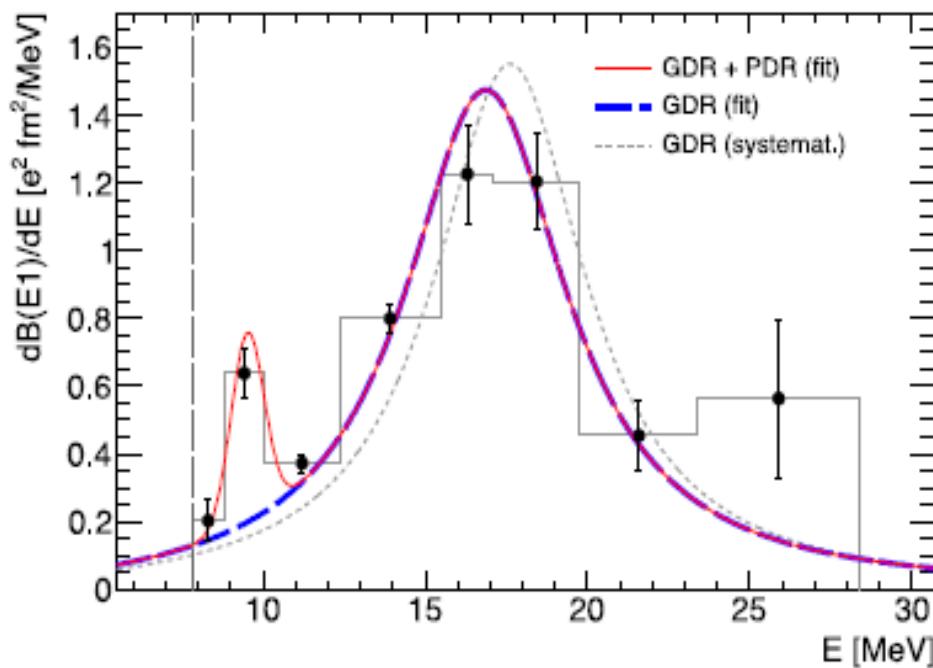
GDR

- no deviation from systematics

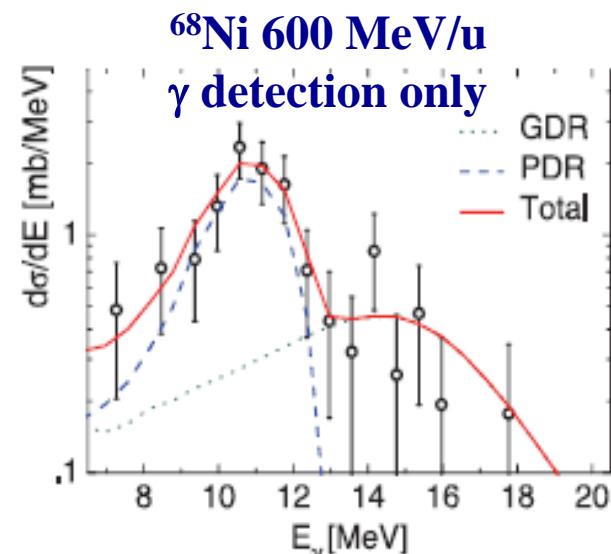
Dipole strength distributions in ^{68}Ni

Simultaneous fit of spectra with 8 individual energy bins as free fit parameters:

„deconvolution“



	This work		Lit.	Ref.
GDR	E_m [MeV]	17.1(2)	17.84	[30]
	Γ [MeV]	6.1(5)	5.69	
	S_{EWSR} [%]	98(7)	100	
PDR	E_m [MeV]	9.55(17)	11	[13, 25]
	σ [MeV]	0.51(13)	< 1	
	S_{EWSR} [%]	2.8(5)	5.0(1.5)	

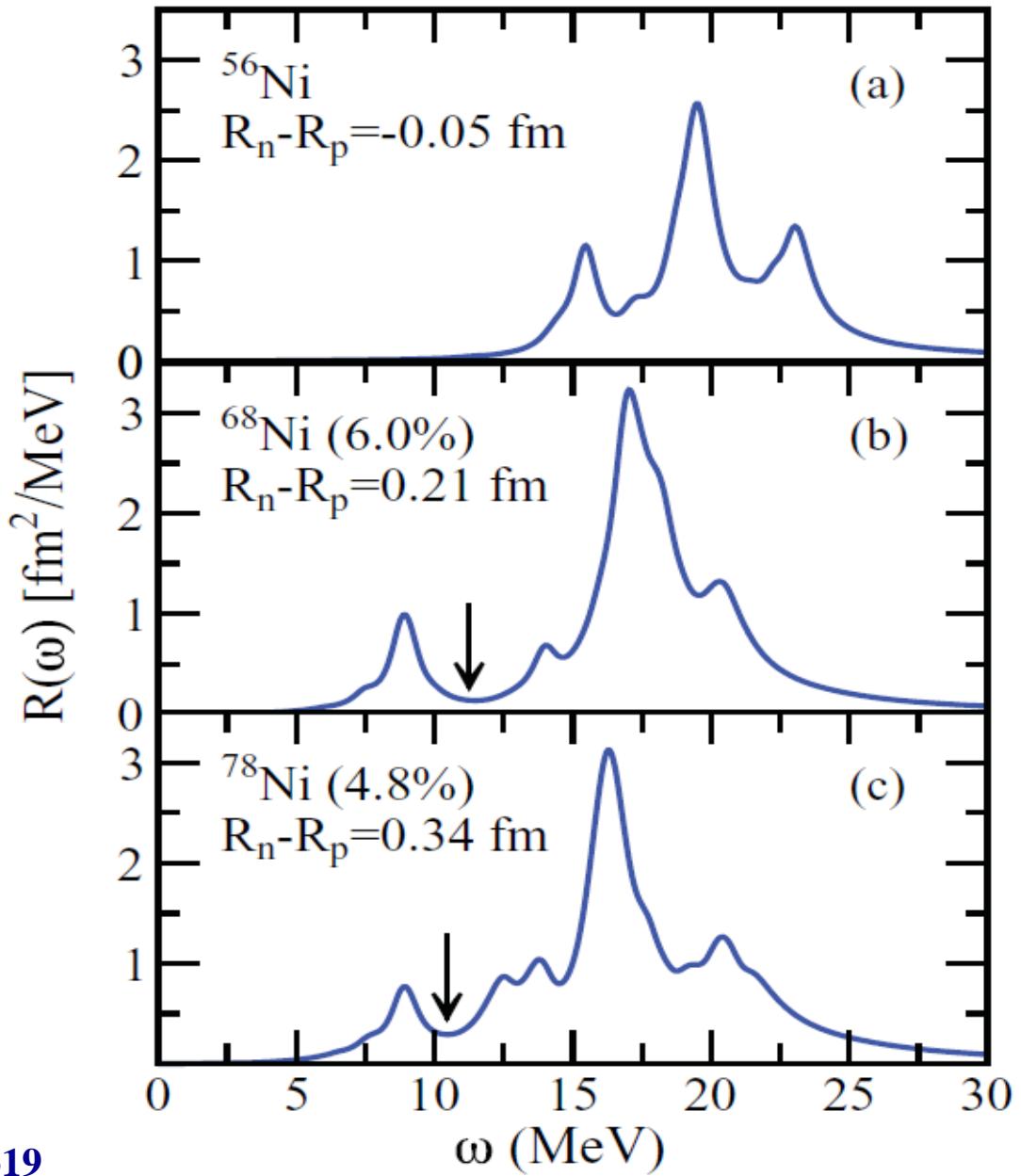


O. Wieland et al., PRL 102, 092502 (2009)

Direct gamma-decay branching ratio
 $\Gamma_0/\Gamma = 7(2)\%$

D. Rossi et al., Phys. Rev. Lett. 111 (2013) 242503

Distribution of isovector dipole strength for the three closed-(sub)shell nickel isotopes ^{56}Ni , ^{68}Ni , and ^{78}Ni calculated in HF-plus-RPA using the FSUGold interaction parameter set.

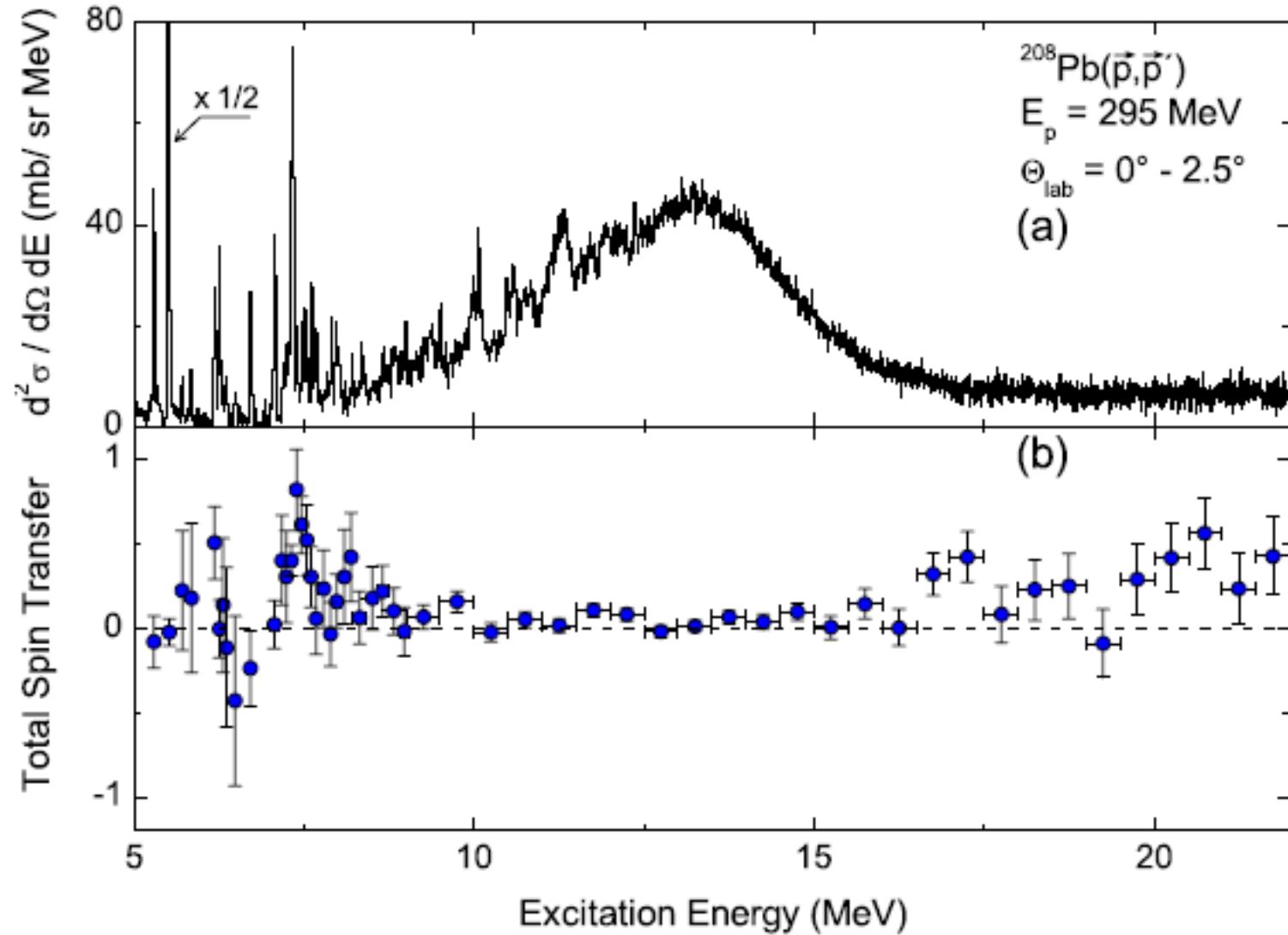


J. Piekarewicz, PRC 83 (2011) 034319

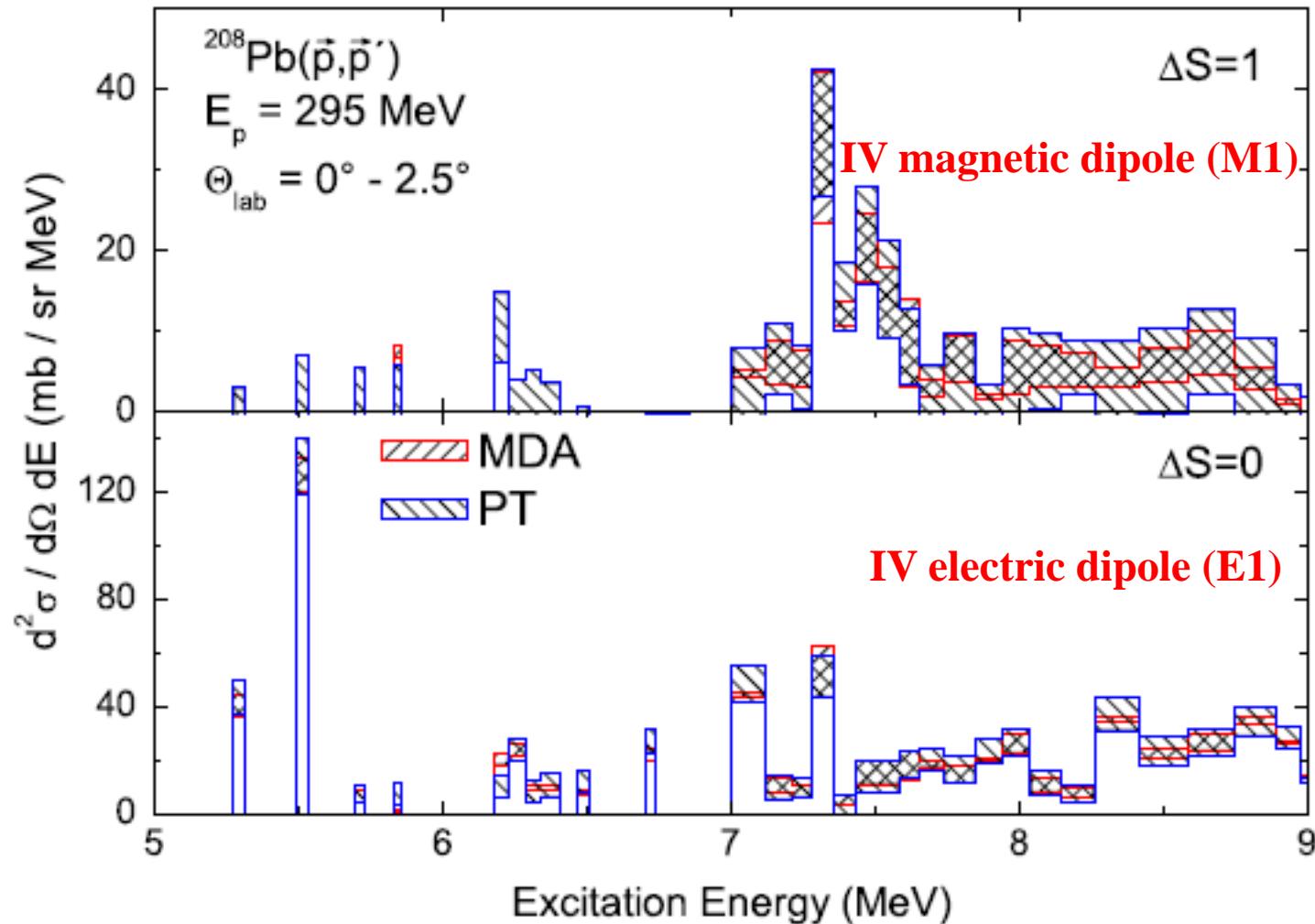
Experiments at RCNP, Osaka University

- (p,p') reaction at 295 MeV
 - High-resolution spectrometer “Grand Raiden”





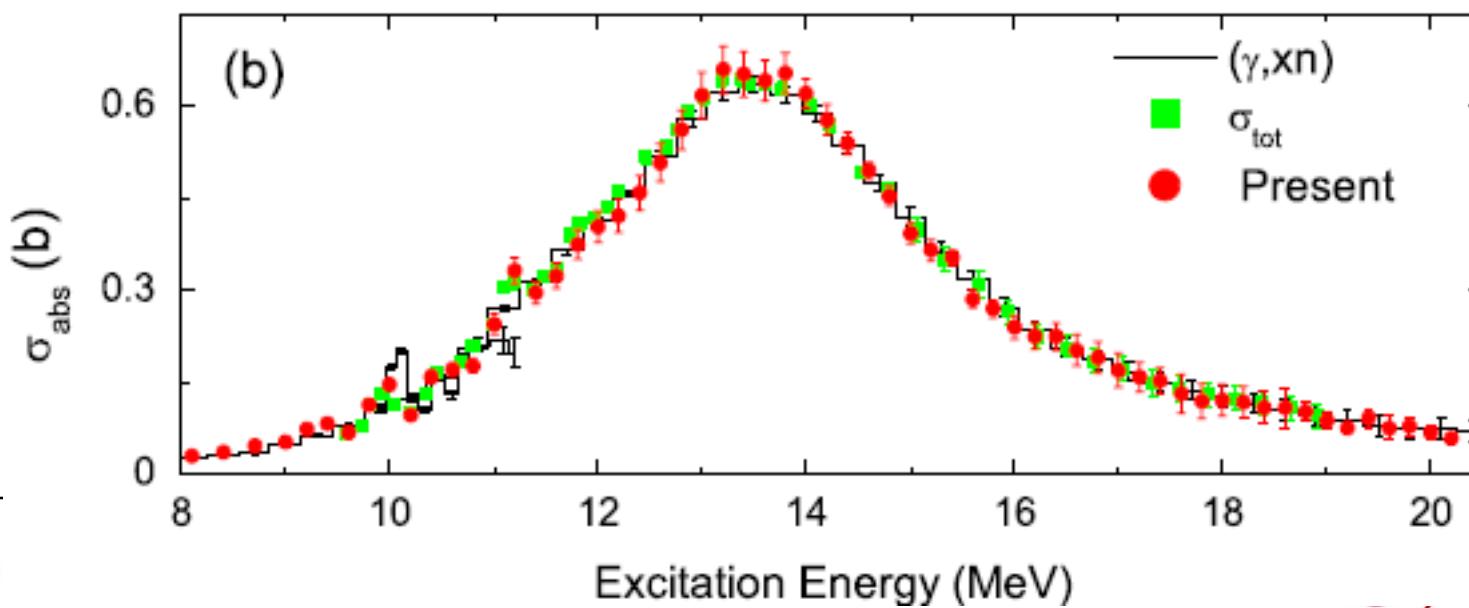
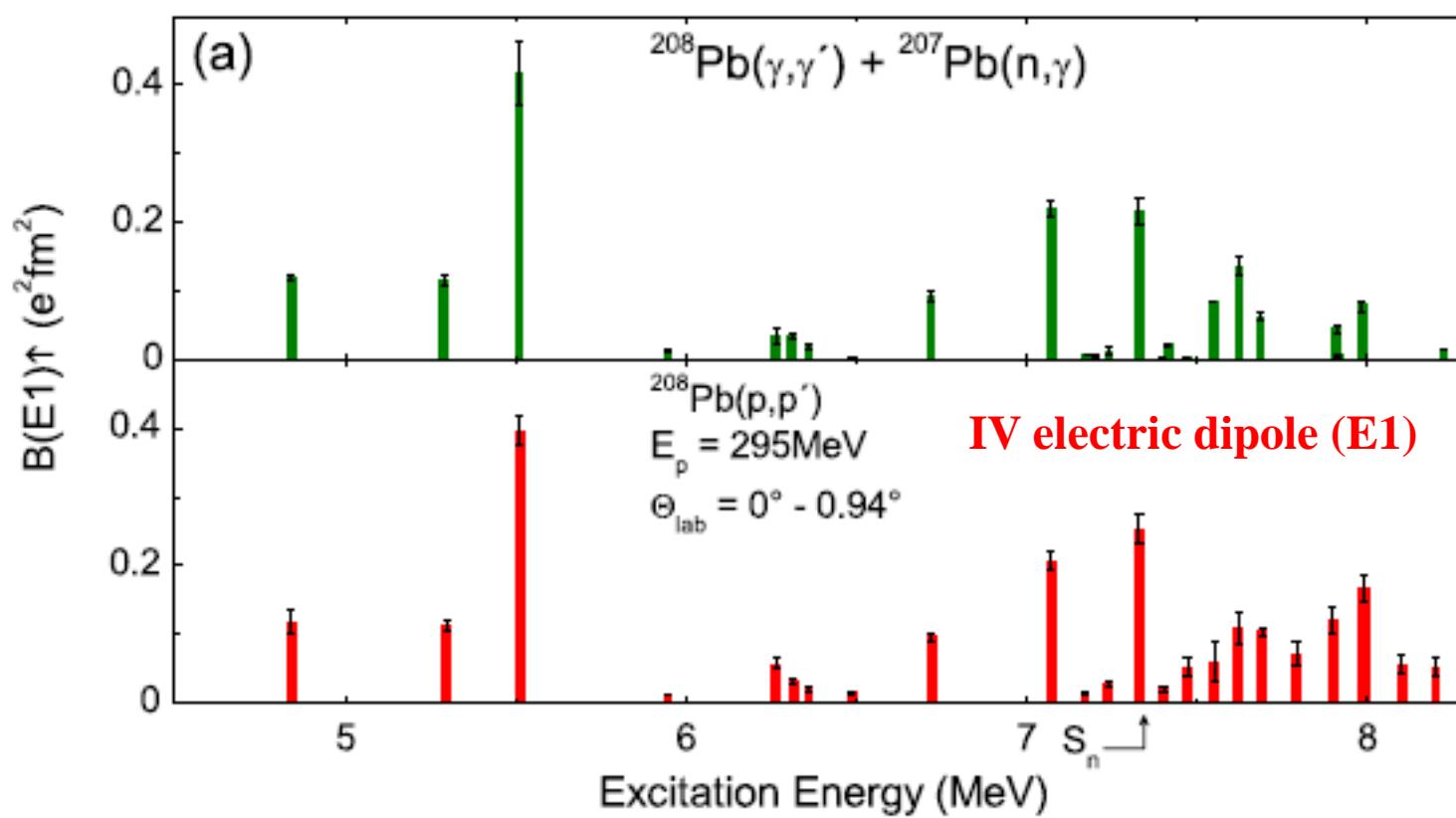
A. Tamii *et al.*, Phys. Rev. Lett. 107 (2011) 062502



MDA = Multipole-Decomposition Analysis

PT = Polarisation Transfer

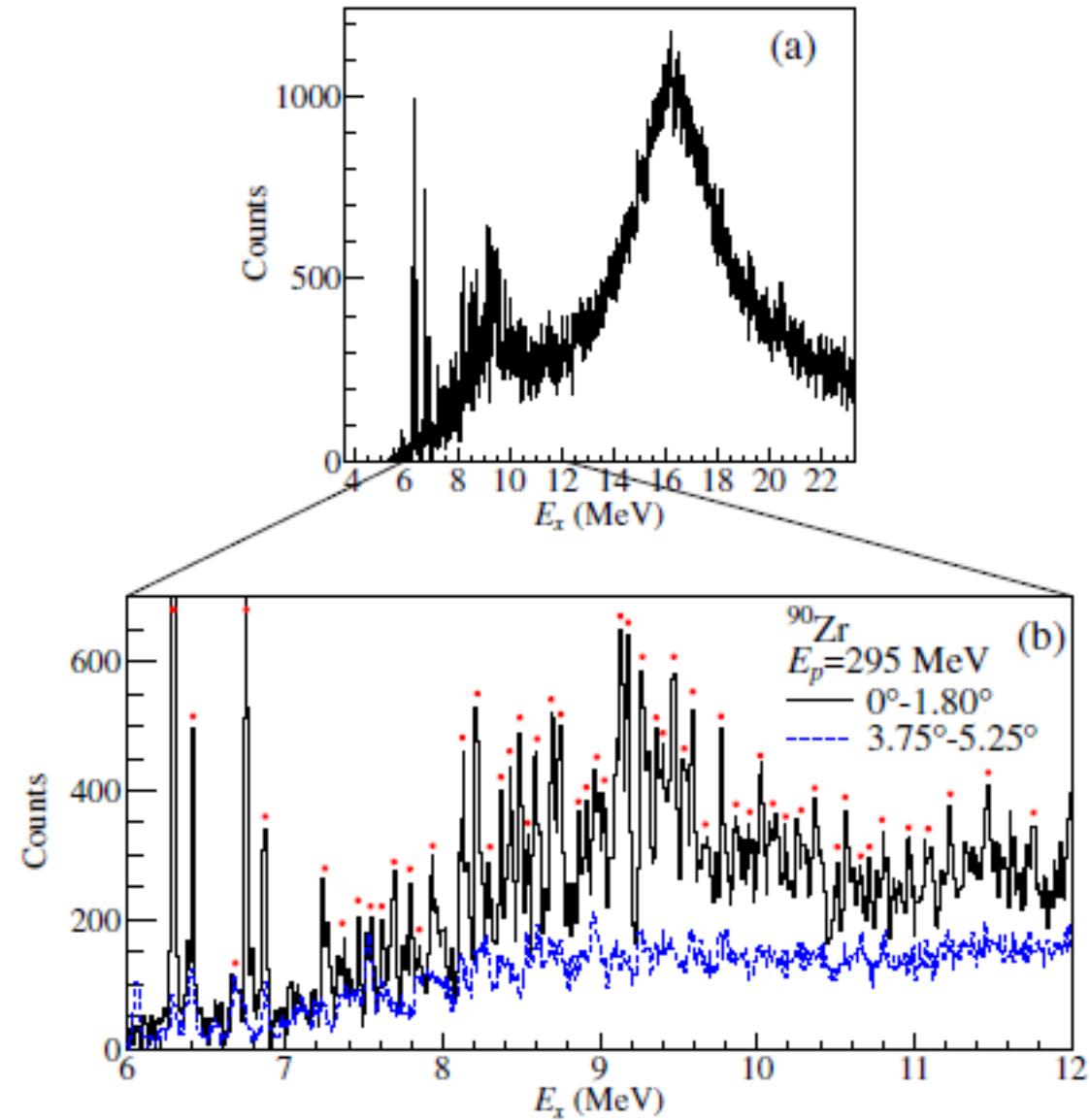
A. Tamii *et al.*, Phys. Rev. Lett. 107 (2011) 062502



0° - 1.8° inelastic proton scattering spectrum shows in addition to IVGDR low-lying E1 and M1 structures.

Peaks with (*) have been selected for multipole-decomposition analysis.

3.75° - 5.25° inelastic proton scattering spectrum is almost structure-less.

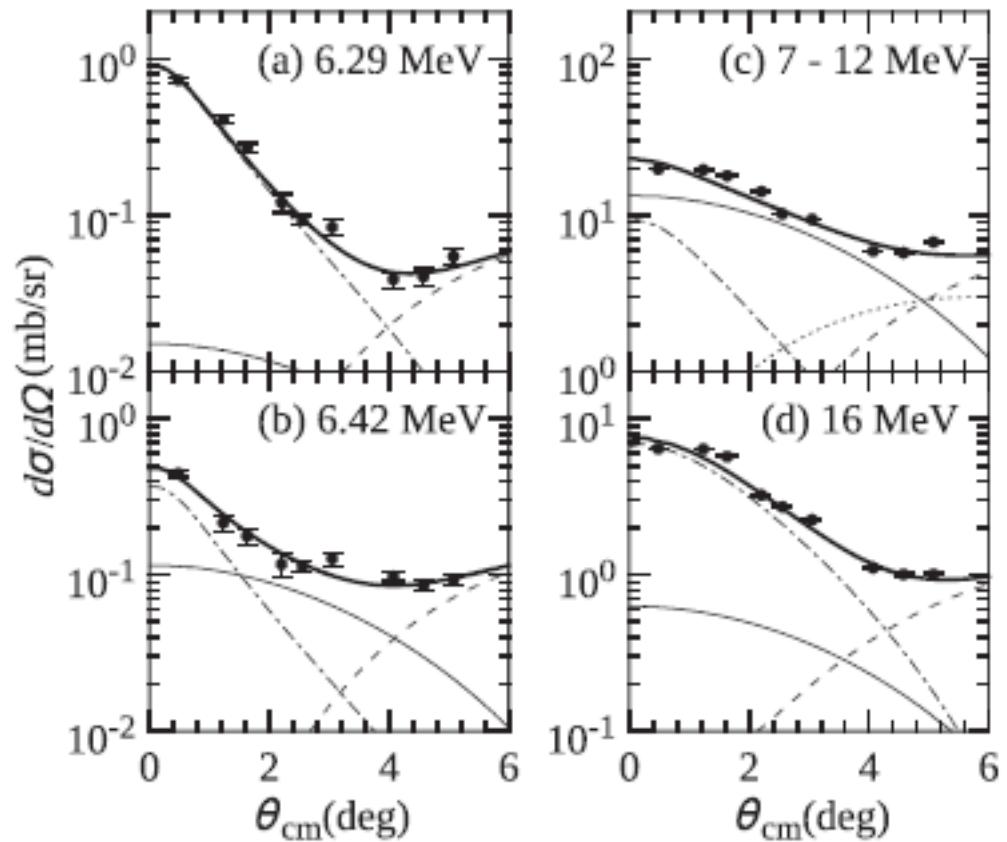


C. Iwamoto *et al.*, Phys. Rev. Lett. 108 (2012) 262501

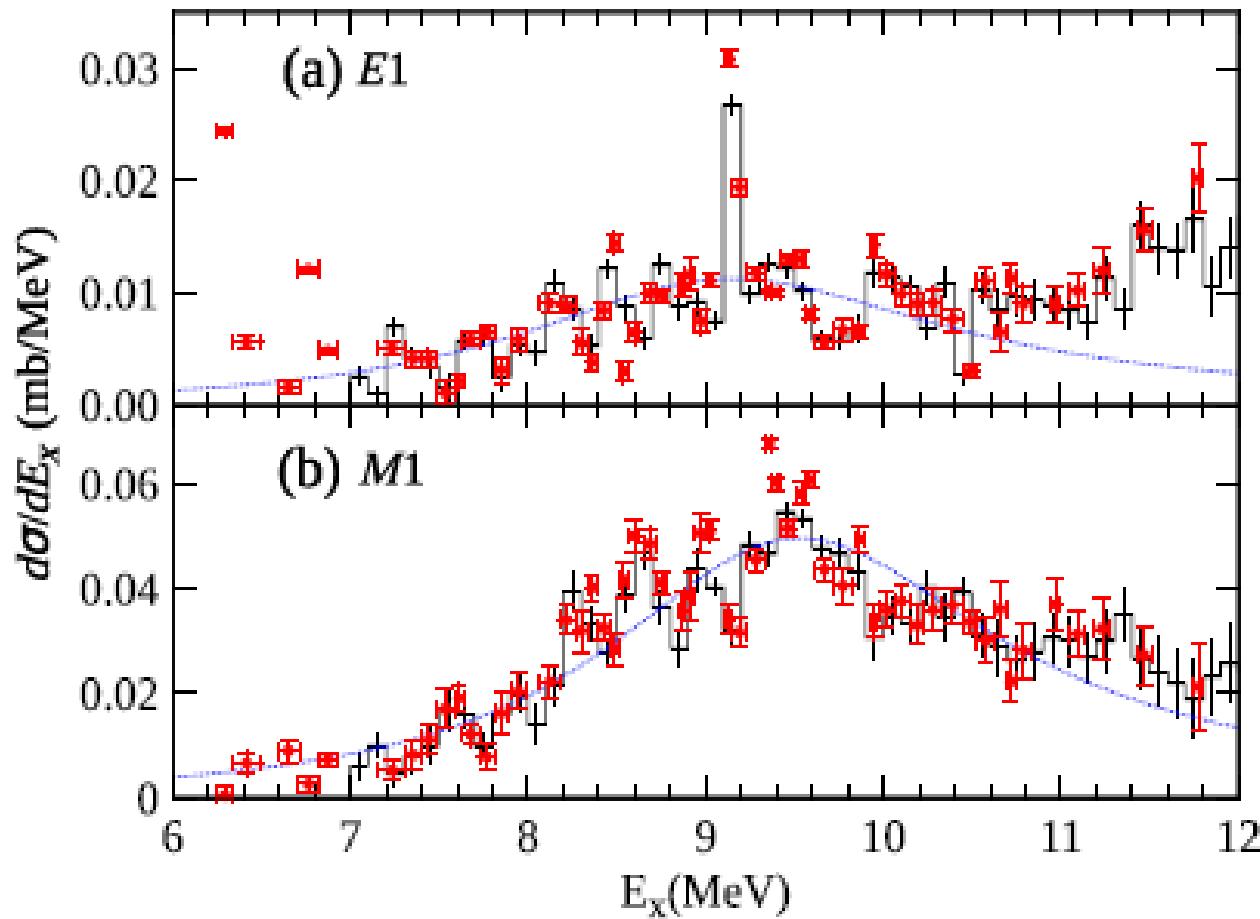
E1 (dash-dotted line)

M1 (solid line)

E2 (dashed line)



C. Iwamoto *et al.*, Phys. Rev. Lett. 108 (2012) 262501

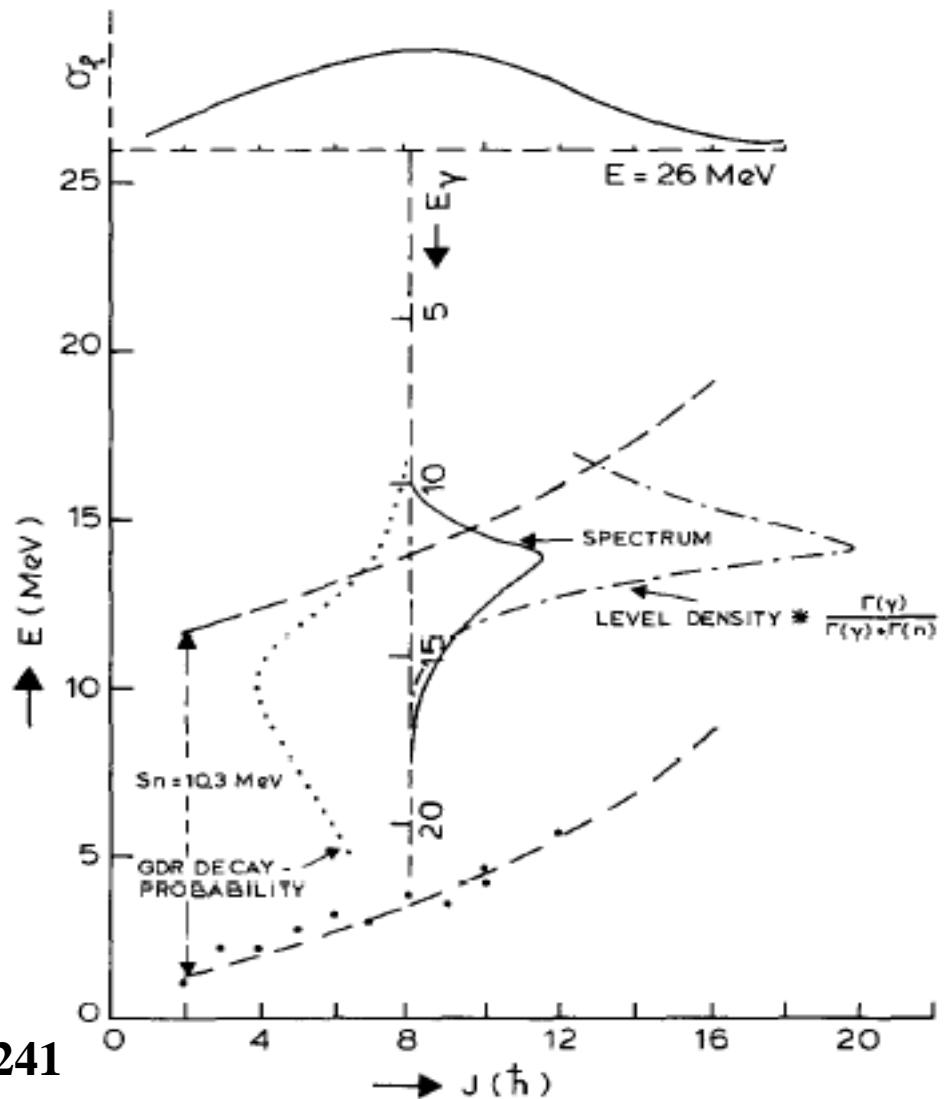


Histograms MDA of 100 keV bins and red circles with errors are of selected peaks.

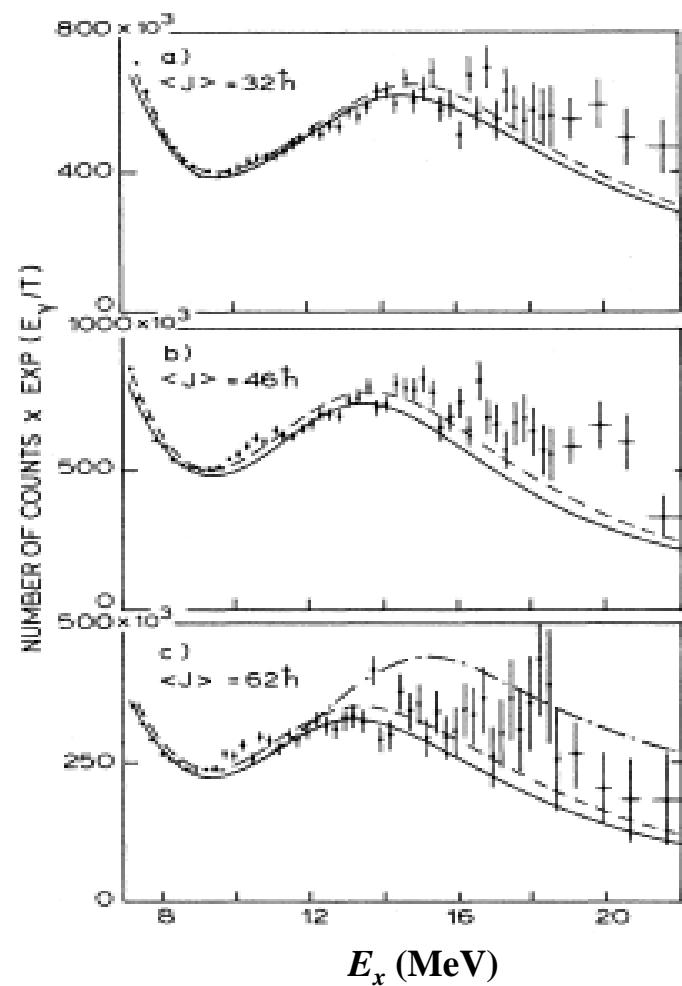
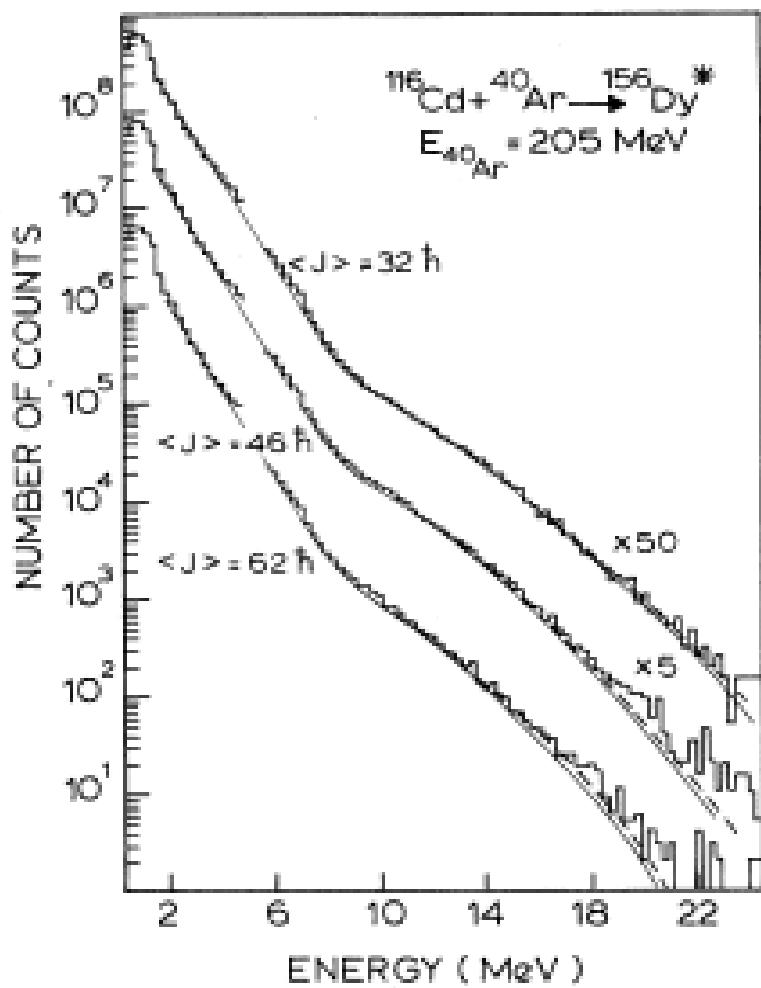
C. Iwamoto *et al.*, Phys. Rev. Lett. 108 (2012) 262501

Decay of IVGDR built on excited states

Schematic picture of
statistical decay of IVGDR
built on excited states in ^{114}Sn

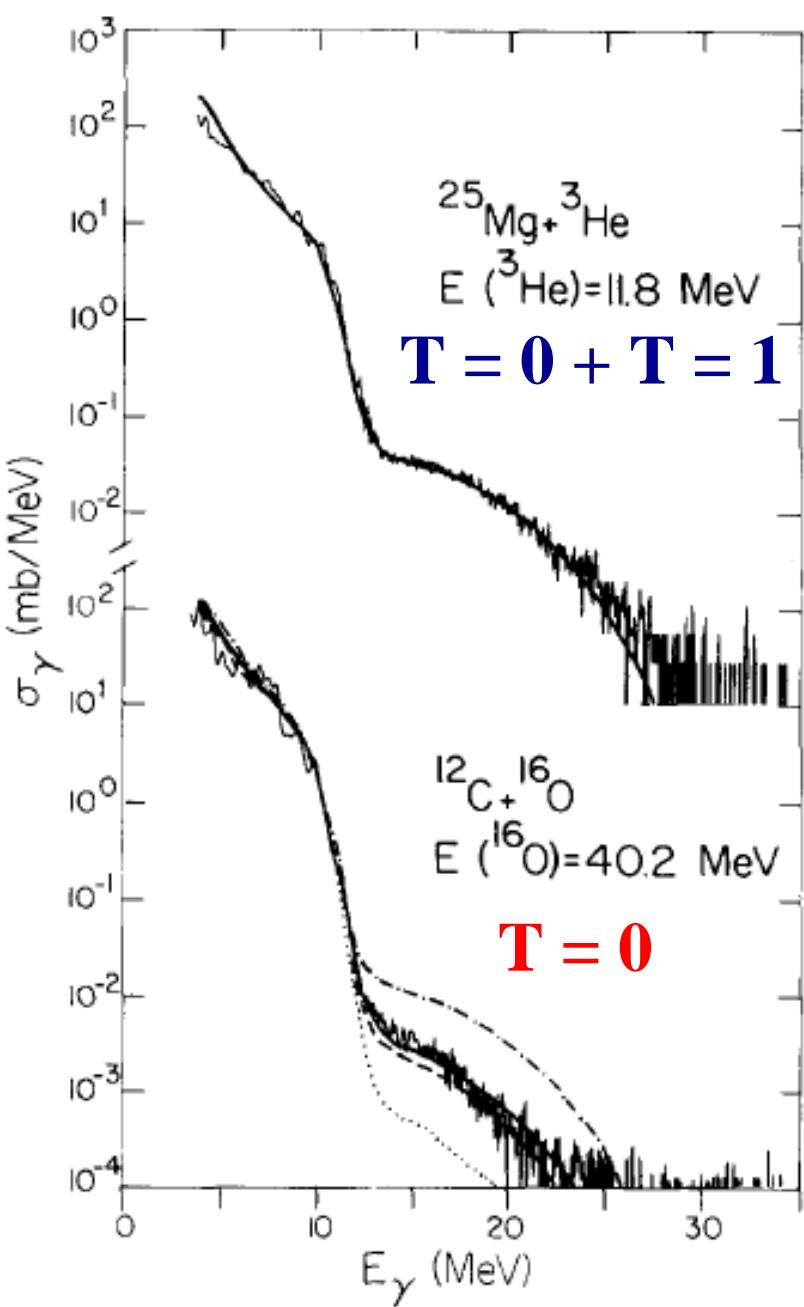


A. Stolk *et al.*, Nucl. Phys. A505 (1989) 241



Left: Statistical decay of IVGDR in ^{156}Dy selected on different angular momentum bins. Curves fits CASCADE calculations with dashed curve increased by 5%. **Right:** Same as left linearized by multiplying with $e^{E\gamma/\text{Teff}}$

A. Stolk *et al.*, Phys. Rev. C40 (1989) R2454



*Role of isospin in the statistical decay
of the IVGDR built on excited states*

Clebsch-Gordon coefficient for
isospin coupling
 $\langle 0010|00\rangle = 0$

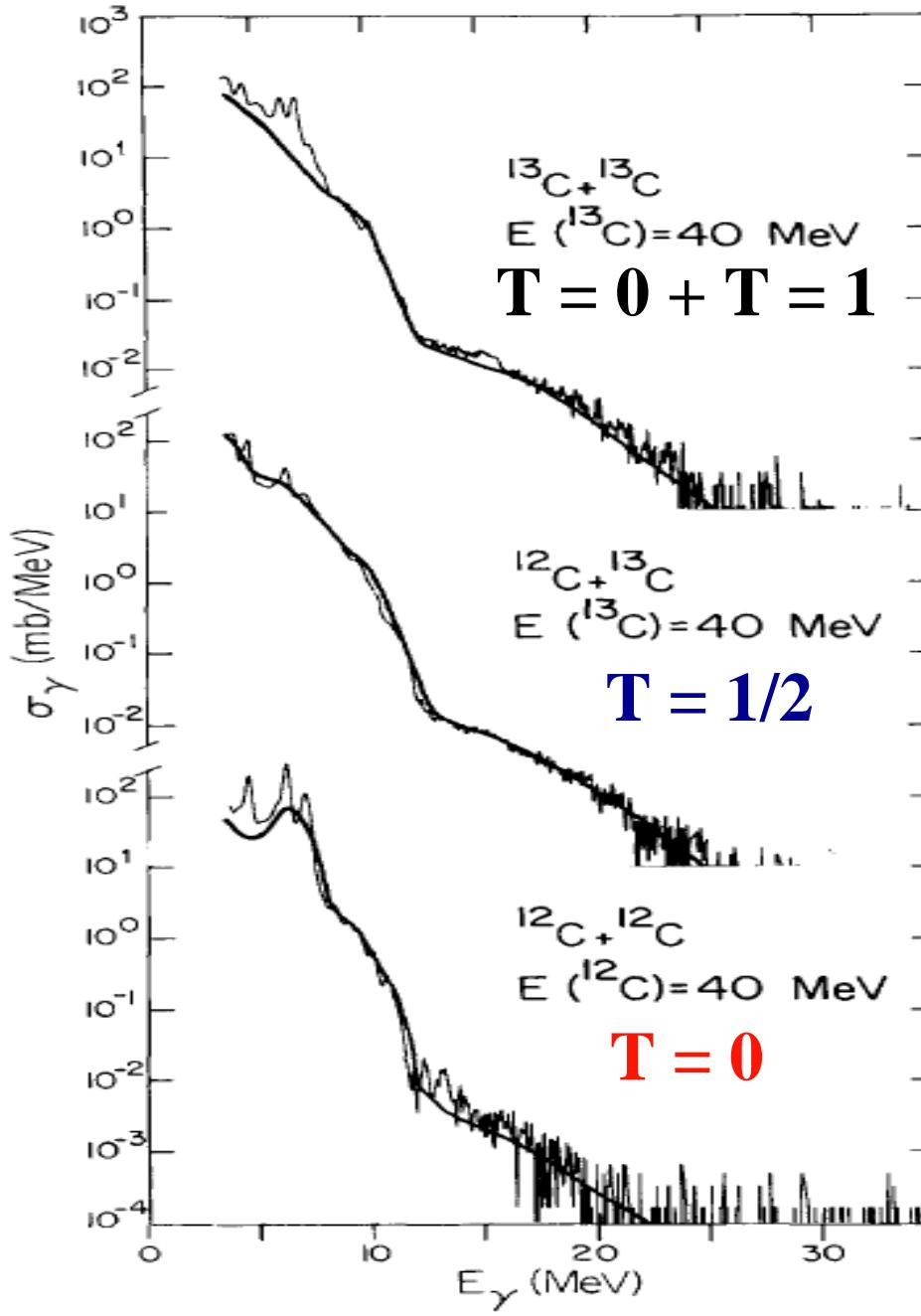
Dotted: pure ISGQR

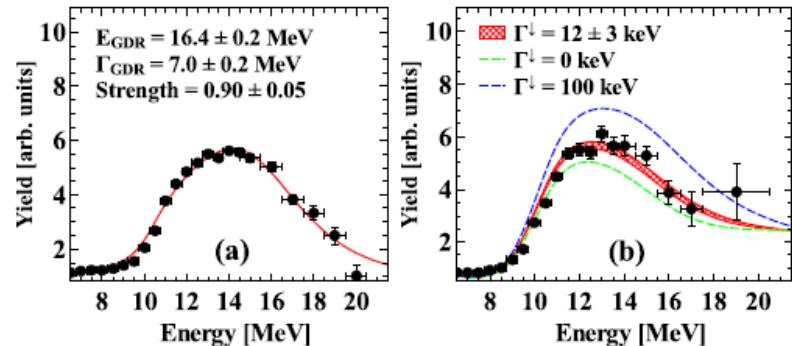
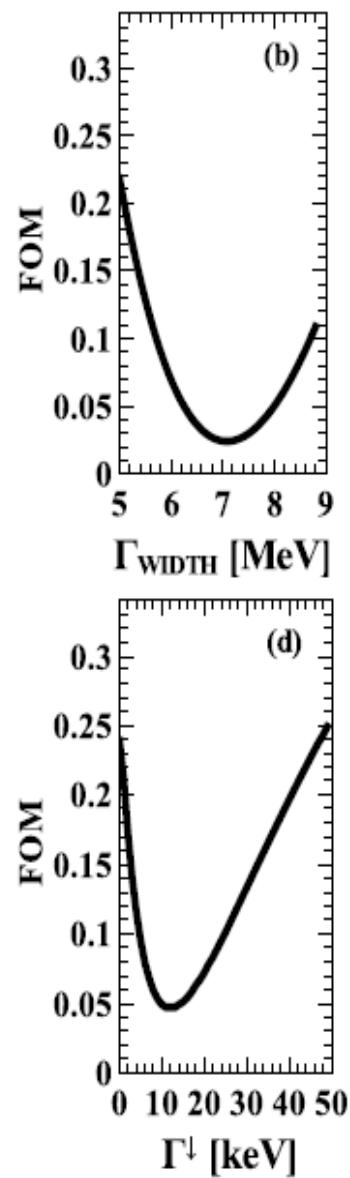
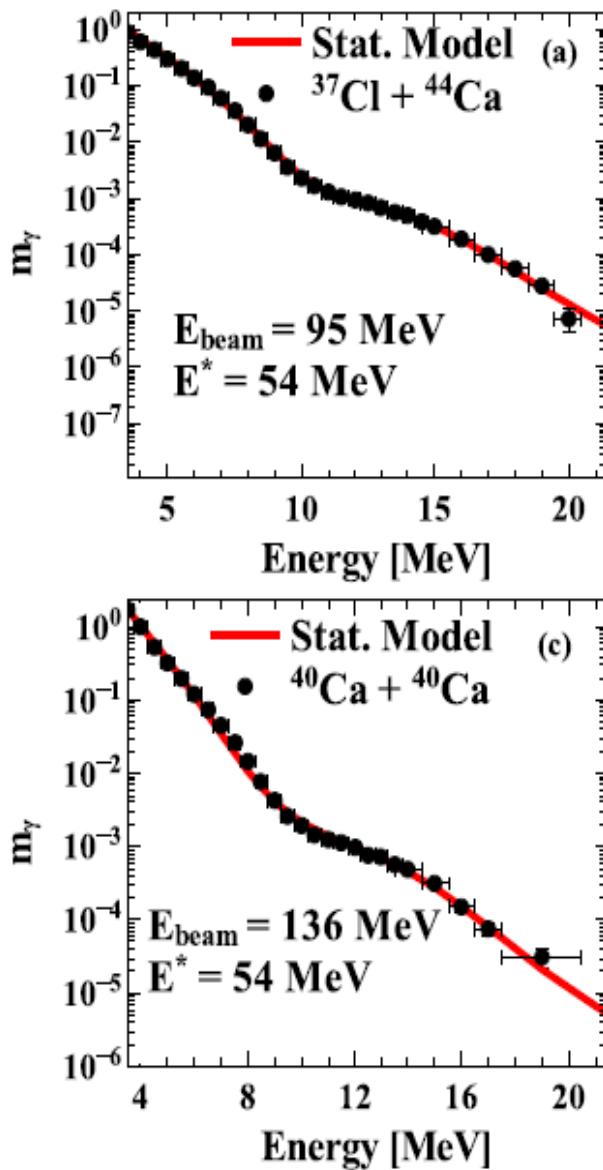
Dashed: pure isospin

Red: Dash-dotted: complete isospin
mixing

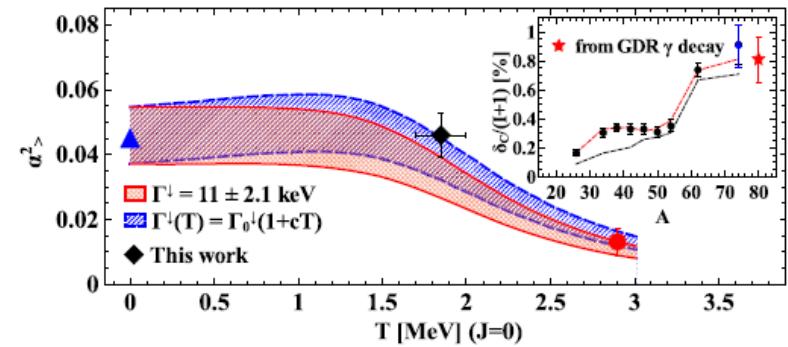
Blue: Solid: isospin mixing ($\sim 5\%$)

M.N. Harakeh *et al.*, Phys. Lett. B176 (1986) 297





$$T = \sqrt{(E^* - E_{\text{GDR}} - E_{\text{rot}})/a}$$



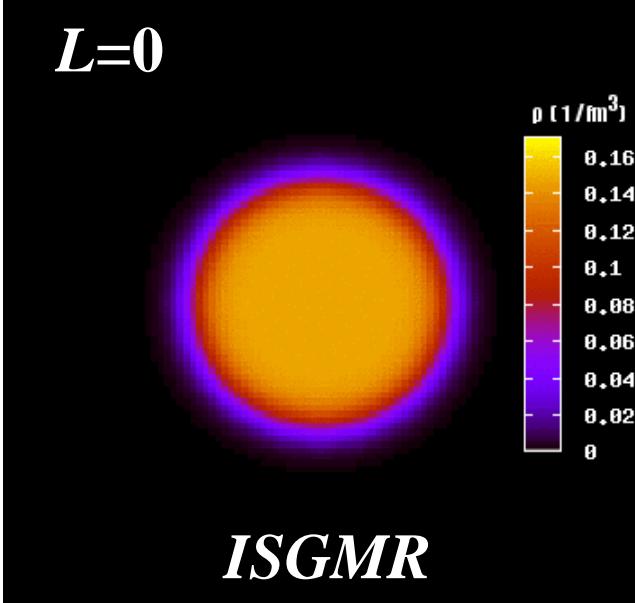
Role of isospin in the statistical decay of the IVGDR built on excited states

- S. Ceruti *et al.*, PRL 115 (2015) 222502
- A. Corsi *et al.*, PRC 84 (2011) 041304 (R)

Compression Modes

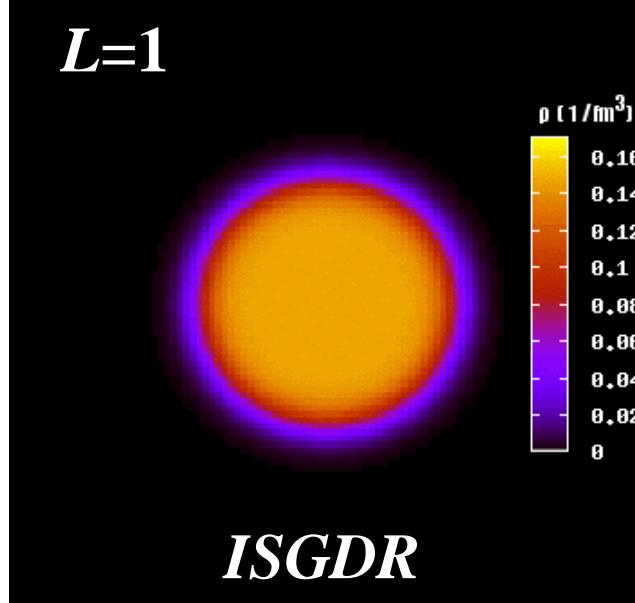
ISGMR & ISGDR

$L=0$



ISGMR

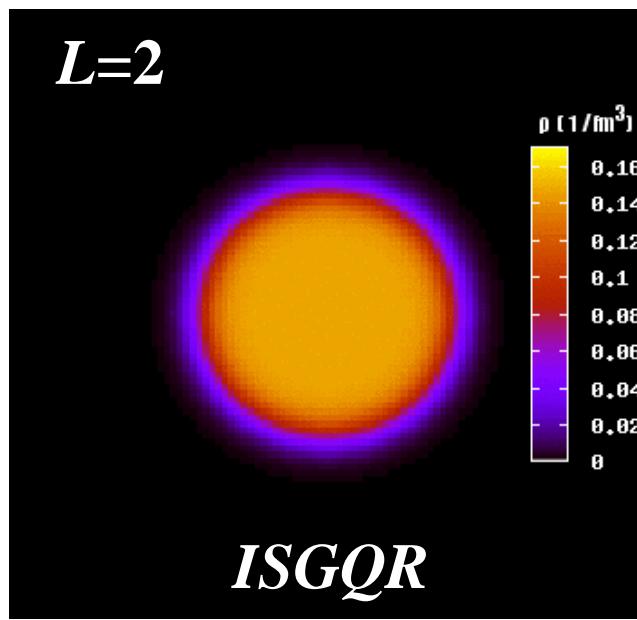
$L=1$



ISGDR

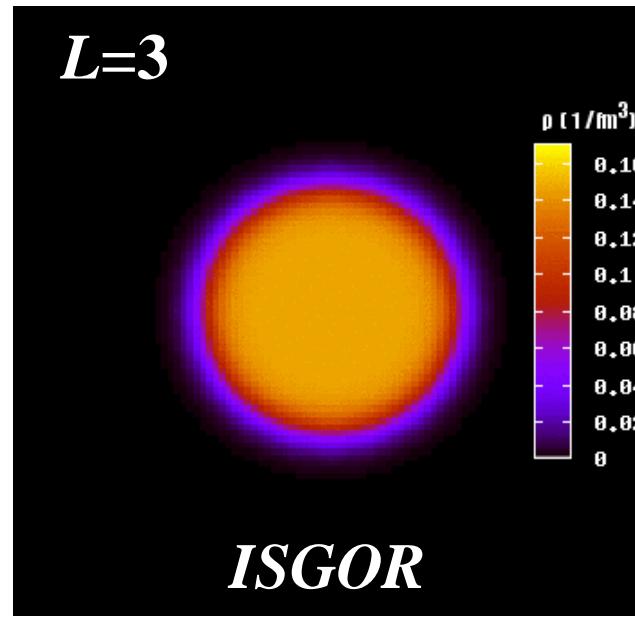
M. Itoh

$L=2$



ISGQR

$L=3$



ISGOR

In fluid mechanics, **compressibility** is a measure of the relative volume change of a fluid as a response to a pressure change.

$$\beta = -\frac{1}{V} \frac{\partial V}{\partial P}$$

where **P** is pressure, **V** is volume.

Incompressibility or **bulk modulus** (**K**) is a measure of a substance's resistance to uniform compression and can be formally defined:

$$K = -V \frac{\partial P}{\partial V}$$

For the equation of state of symmetric nuclear matter at saturation nuclear density:

$$\left[\frac{d(E/A)}{d\rho} \right]_{\rho=\rho_0} = 0$$

and one can derive the incompressibility of nuclear matter:

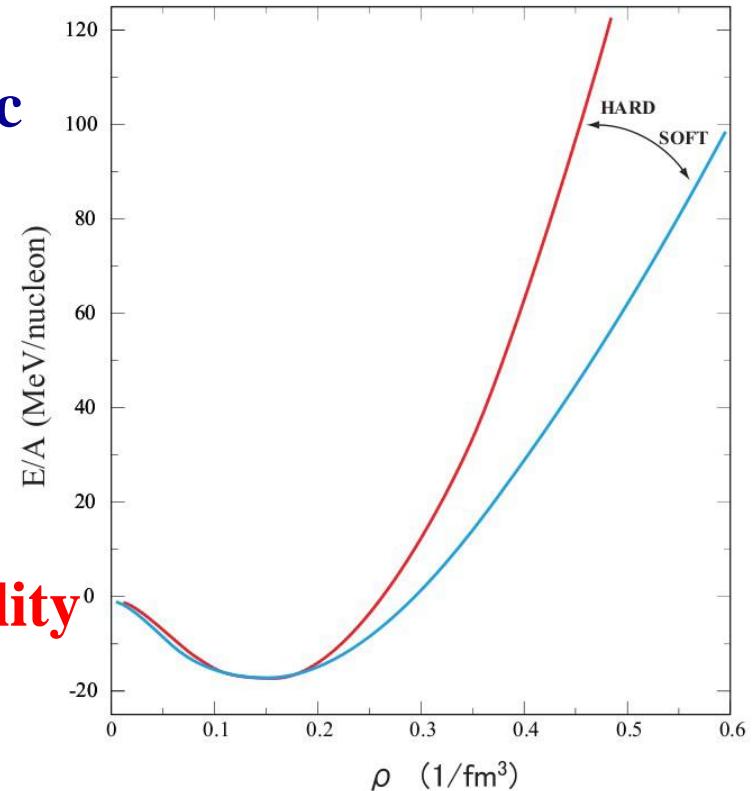
$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho=\rho_0}$$

E/A: binding energy per nucleon

ρ : nuclear density

J.P. Blaizot, Phys. Rep. 64 (1980) 171

ρ_0 : nuclear density at saturation



Equation of state (EOS) of nuclear matter

More complex than for infinite neutral liquids

Neutrons and protons with different interactions

Coulomb interaction of protons

1. **Governs the collapse and explosion of giant stars (supernovae)**
2. **Governs formation of neutron stars (mass, radius, crust)**
3. **Governs collisions of heavy ions.**
4. **Important ingredient in the study of nuclear properties.**

Isoscalar Excitation Modes of Nuclei

Hydrodynamic models/Giant Resonances

Coherent vibrations of nucleonic fluids in a nucleus.

Compression modes: **ISGMR, ISGDR**

In Constrained and Scaling Models:

$$E_{ISGMR} = \hbar \sqrt{\frac{K_A}{m \langle r^2 \rangle}}$$

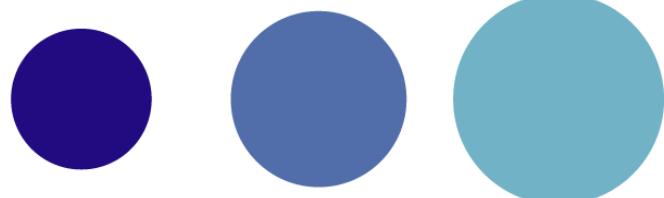
$$E_{ISGDR} = \hbar \sqrt{\frac{7}{3} \frac{K_A + \frac{27}{25} \varepsilon_F}{m \langle r^2 \rangle}}$$

ε_F is the Fermi energy and the nucleus incompressibility:

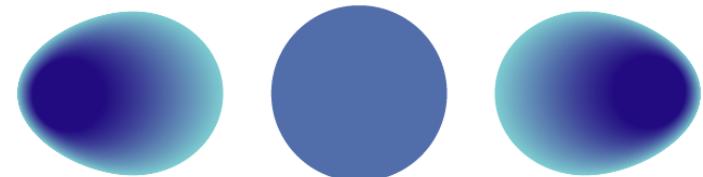
$$\rightarrow K_A = \left[r^2 (d^2(E/A)/dr^2) \right]_{r=R_0}$$

J.P. Blaizot, Phys. Rep. 64 (1980) 171

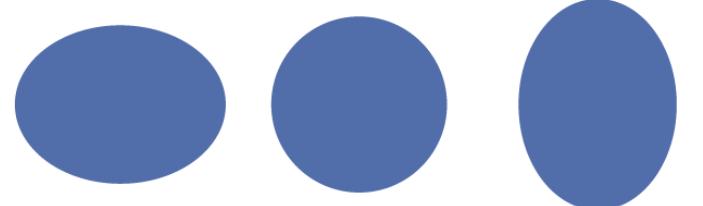
ISGMR (T=0, L=0)



ISGDR (T=0, L=1)



ISGQR (T=0, L=2)

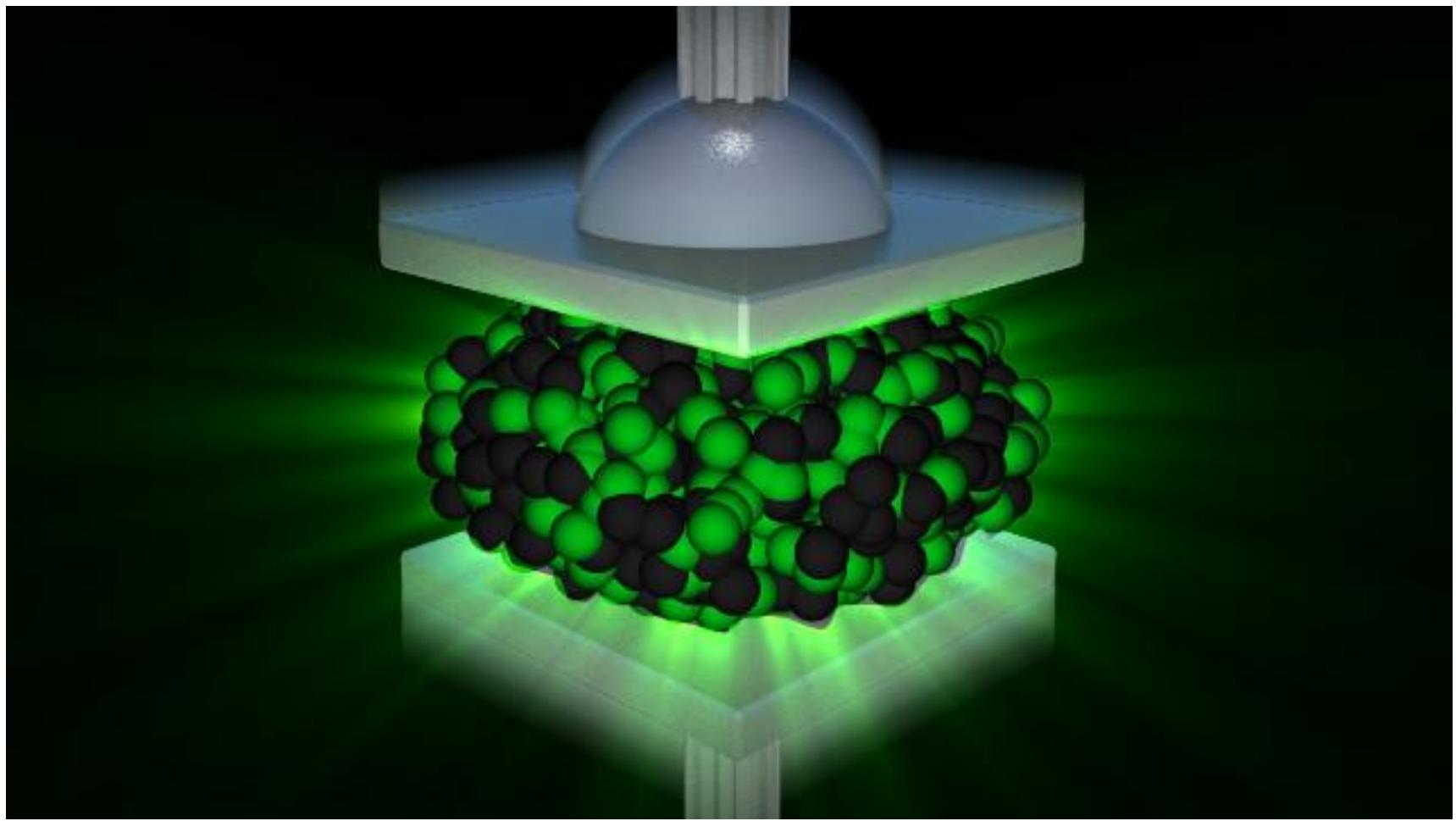


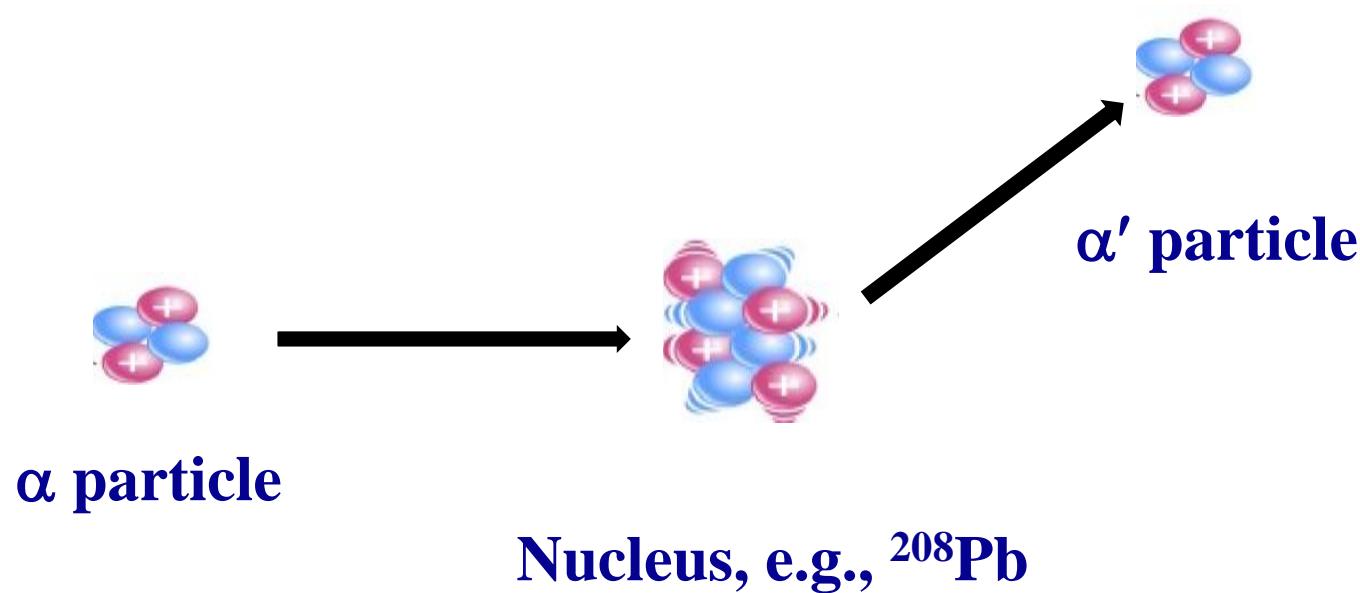
Giant resonances

- Macroscopic properties: E_x , Γ , %EWSR
- Isoscalar giant resonances; compression modes

ISGMR, ISGDR \Rightarrow Incompressibility, symmetry energy

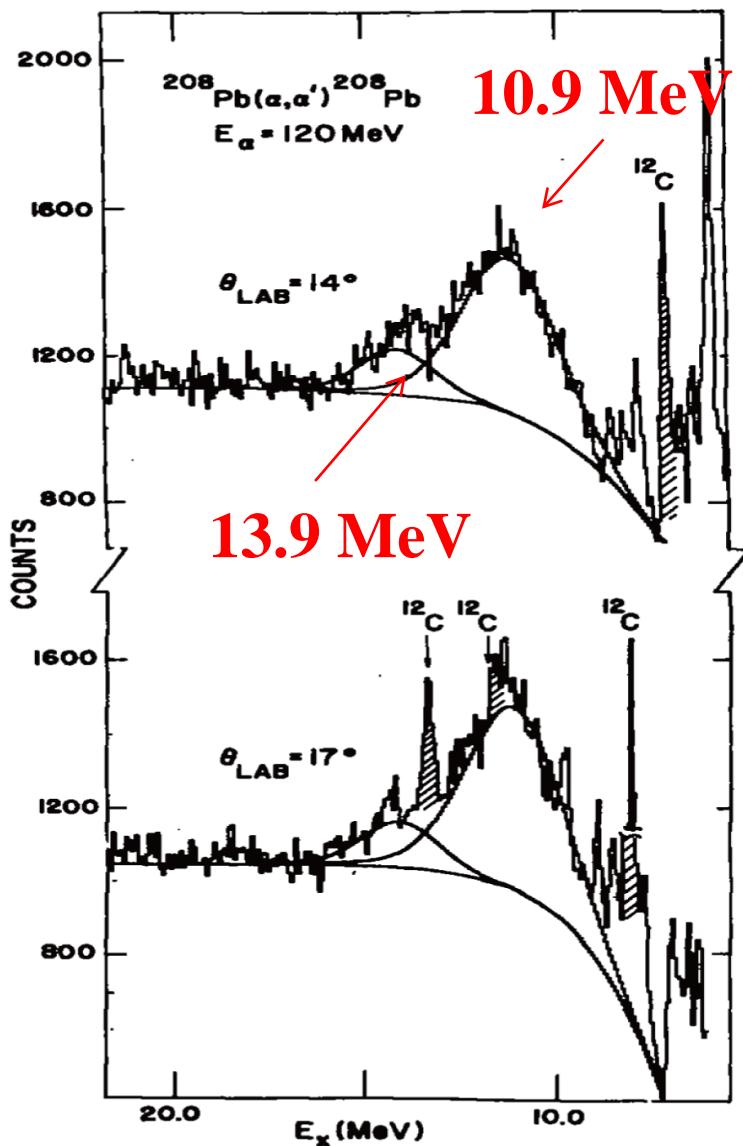
$$K_A = K_{vol} + K_{surf} A^{-1/3} + K_{sym} ((N-Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$





Inelastic α scattering

ISGQR, ISGMR



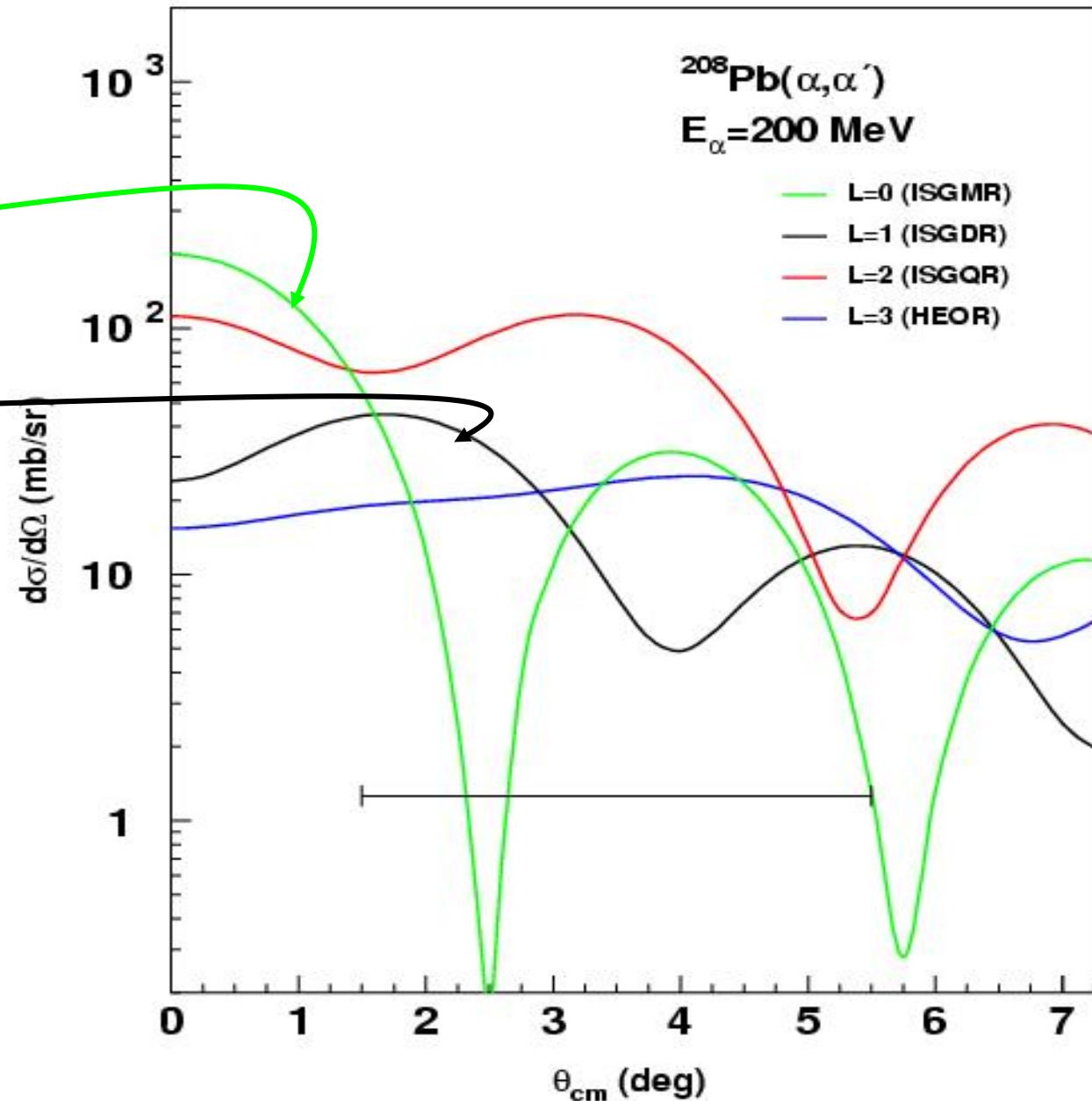
$\Leftarrow ^{208}\text{Pb}(\alpha, \alpha')$ at $E_\alpha = 120$ MeV

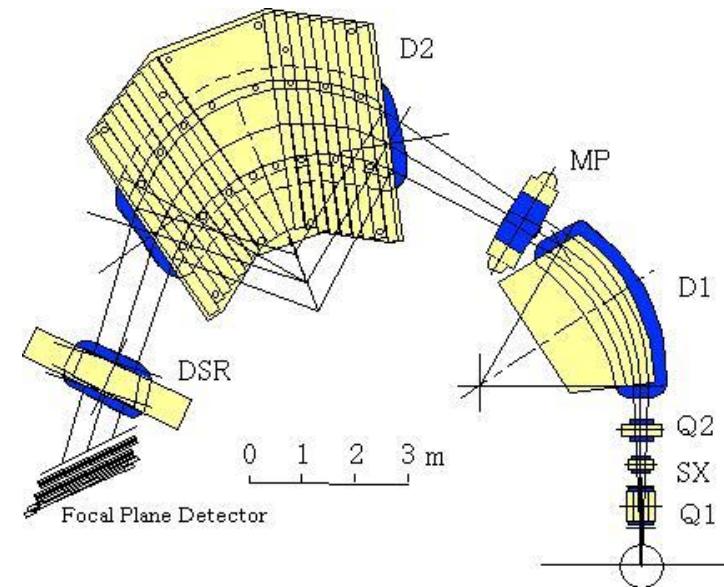
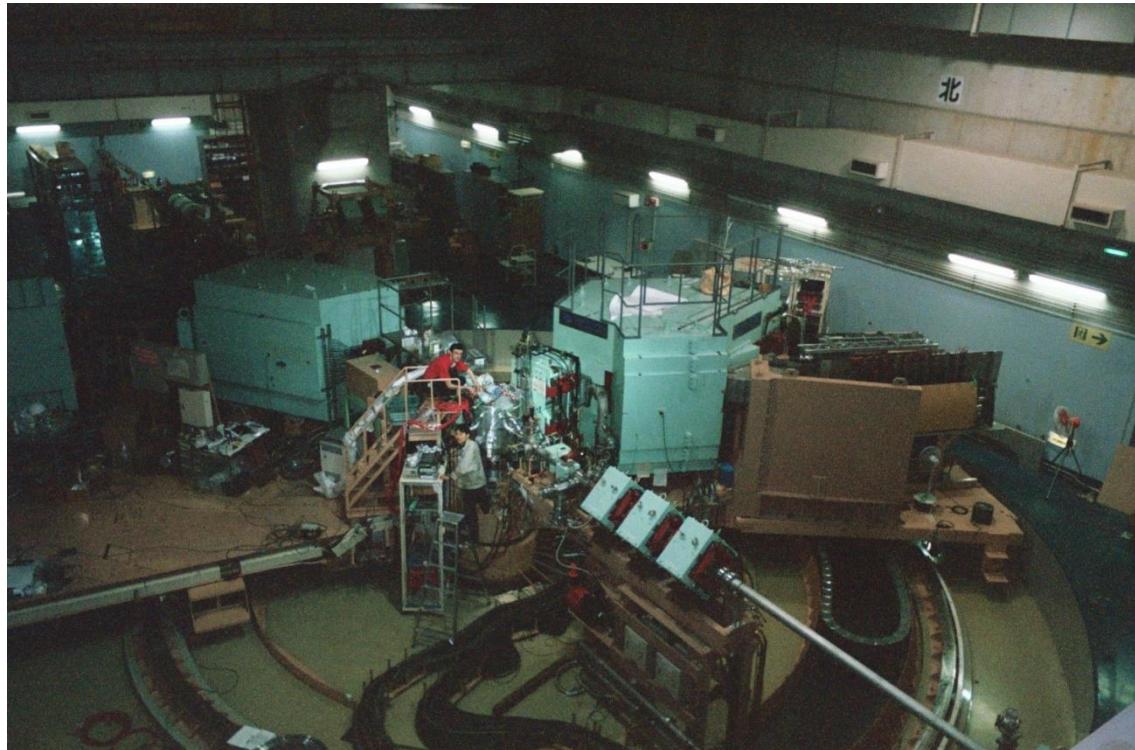
Large instrumental background
and nuclear continuum!

M. N. Harakeh *et al.*, Phys. Rev. Lett. 38 (1977) 676

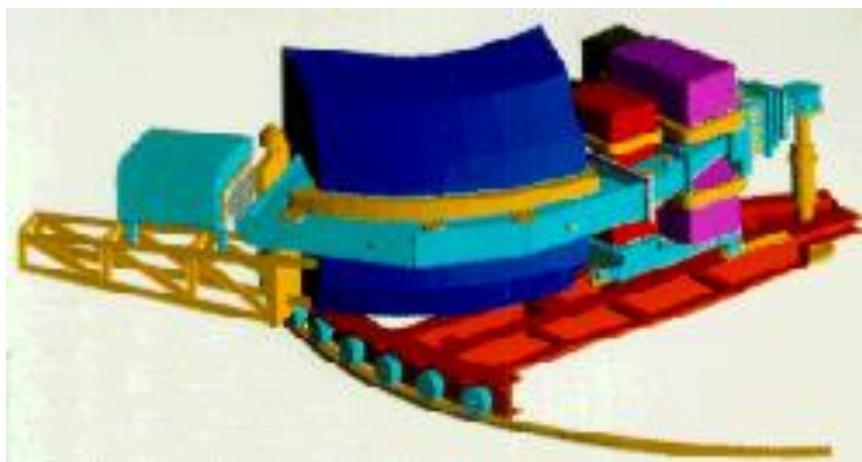
ISGMR $L = 0$

ISGDR $L = 1$



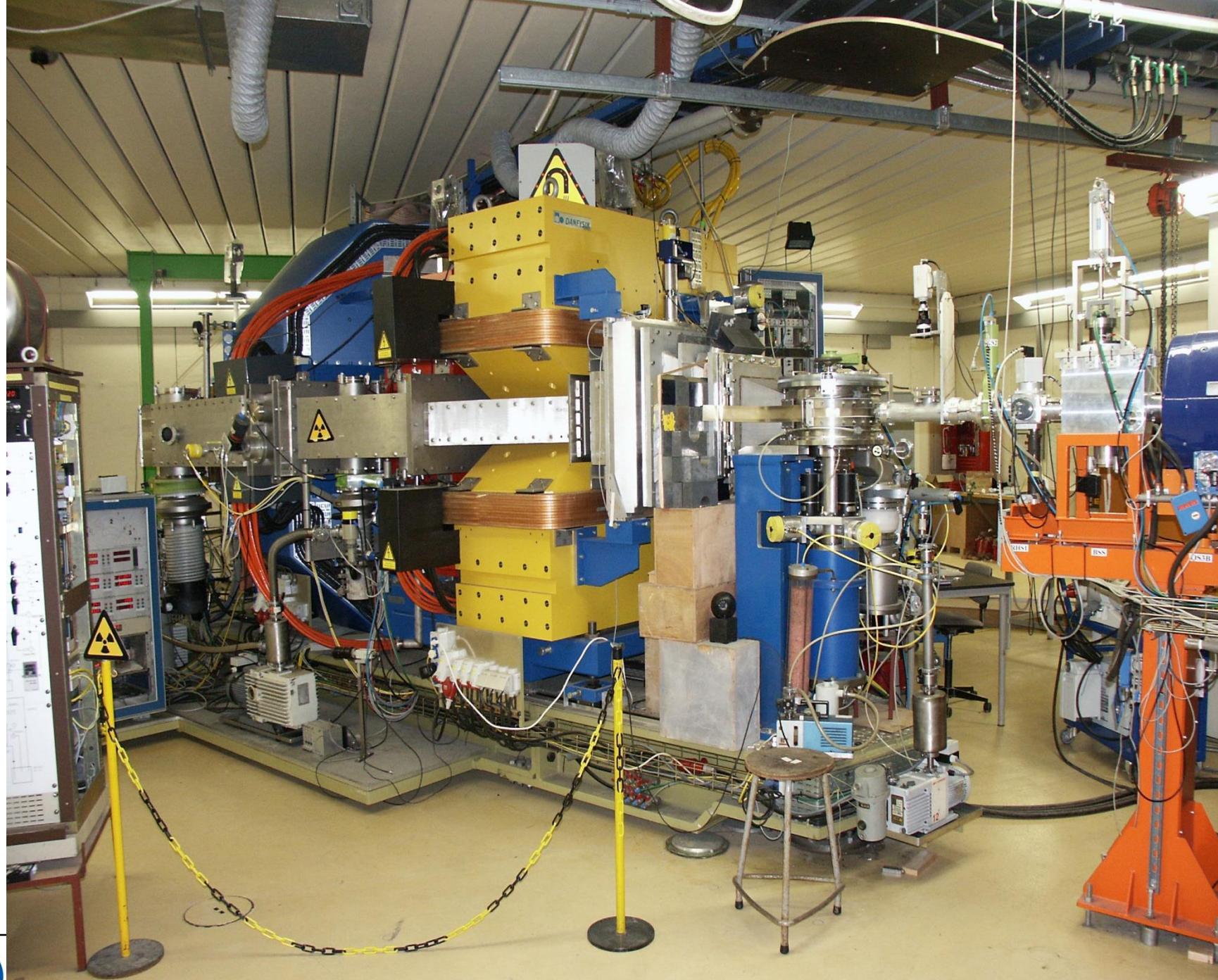


Grand Raiden@ RCNP

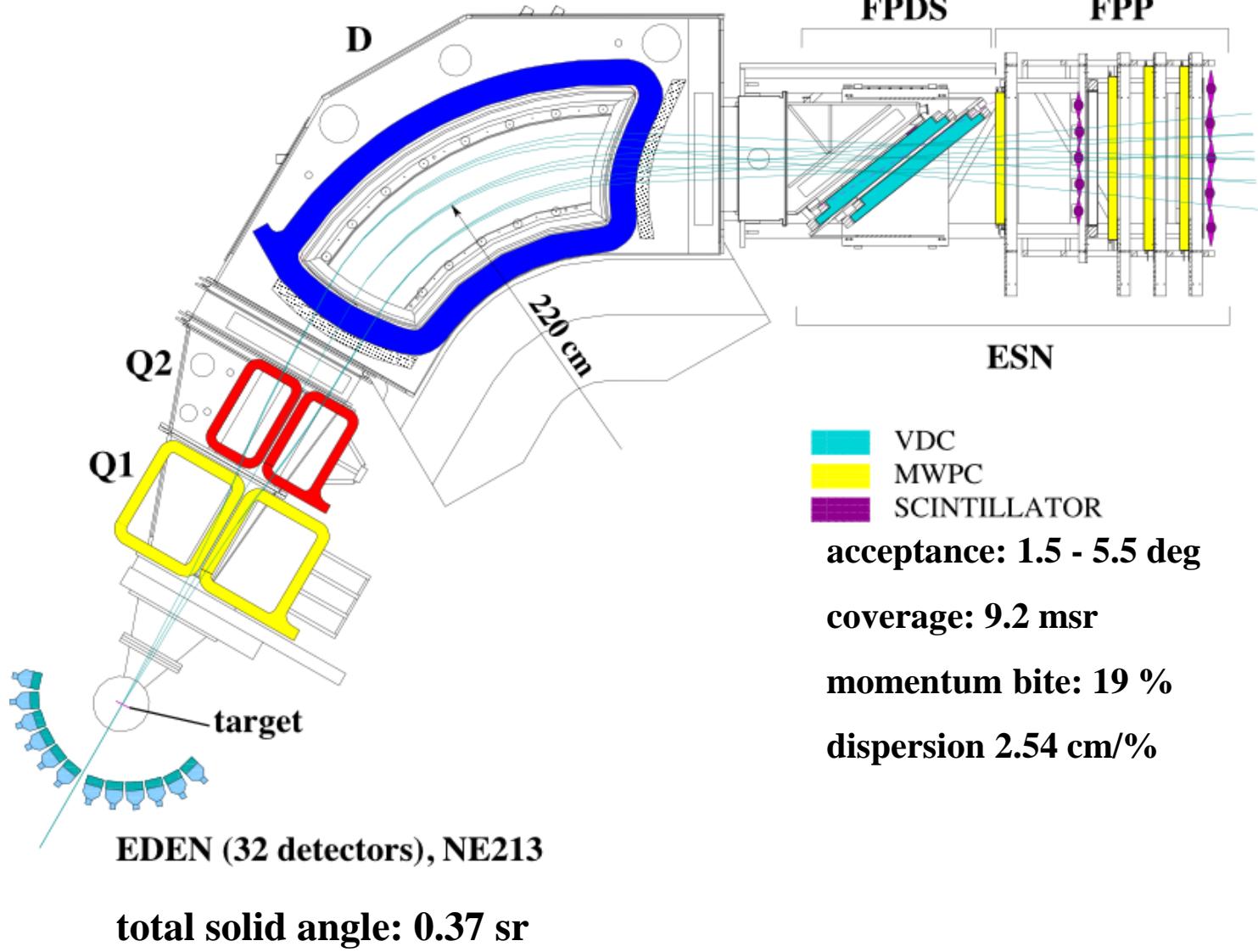


BBS@KVI

(p, p') at $E_p \sim 300$
 (α, α') at $E_\alpha \sim 400$
& 200 MeV at
RCNP & KVI,
respectively



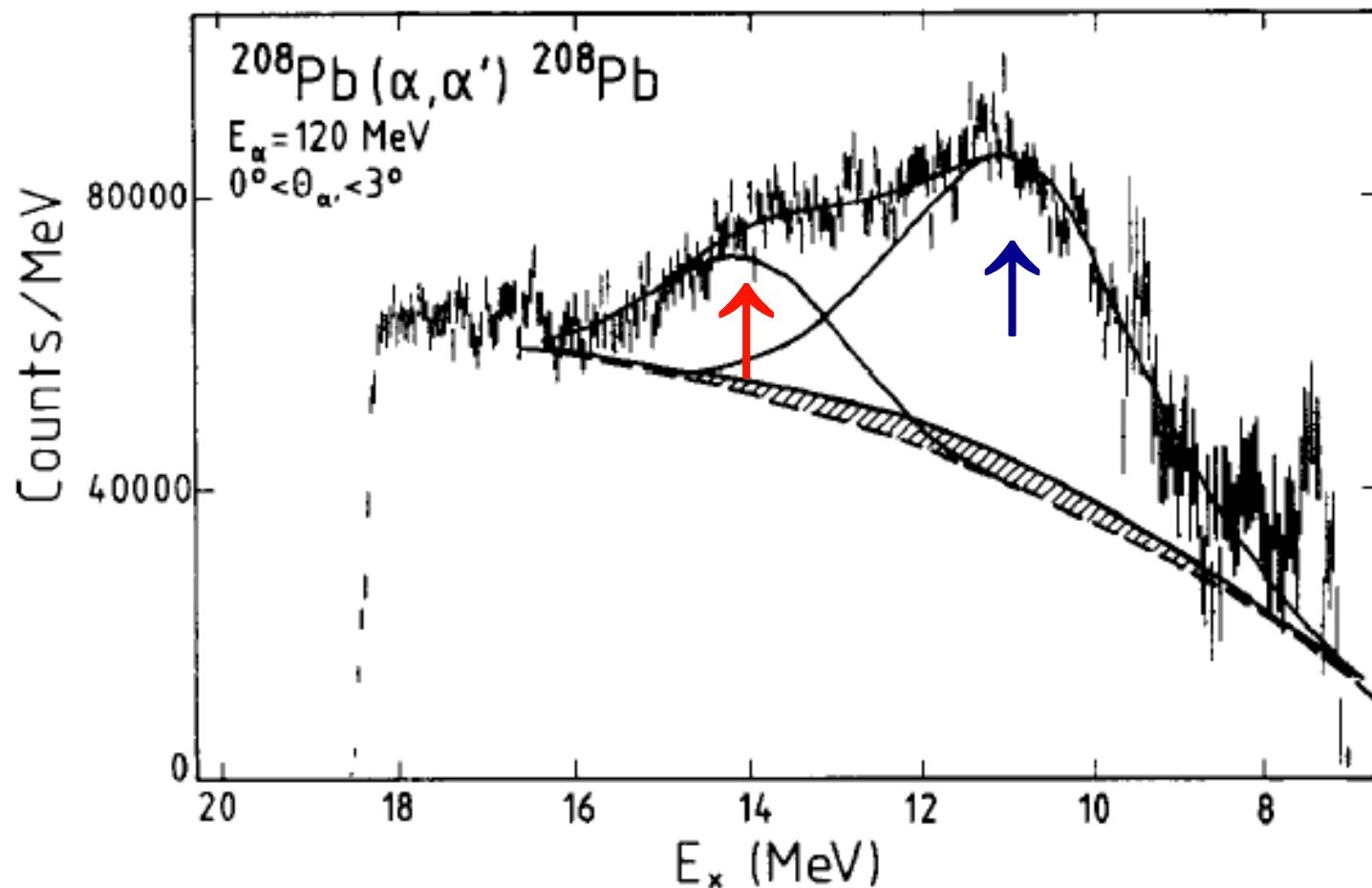
Si-ball
**16 Si-detectors at
10 cm from the target**
total solid angle: 1 sr



KVI Big-Bite Spectrometer (BBS)

ISGQR at 10.9 MeV

ISGMR at 13.9 MeV



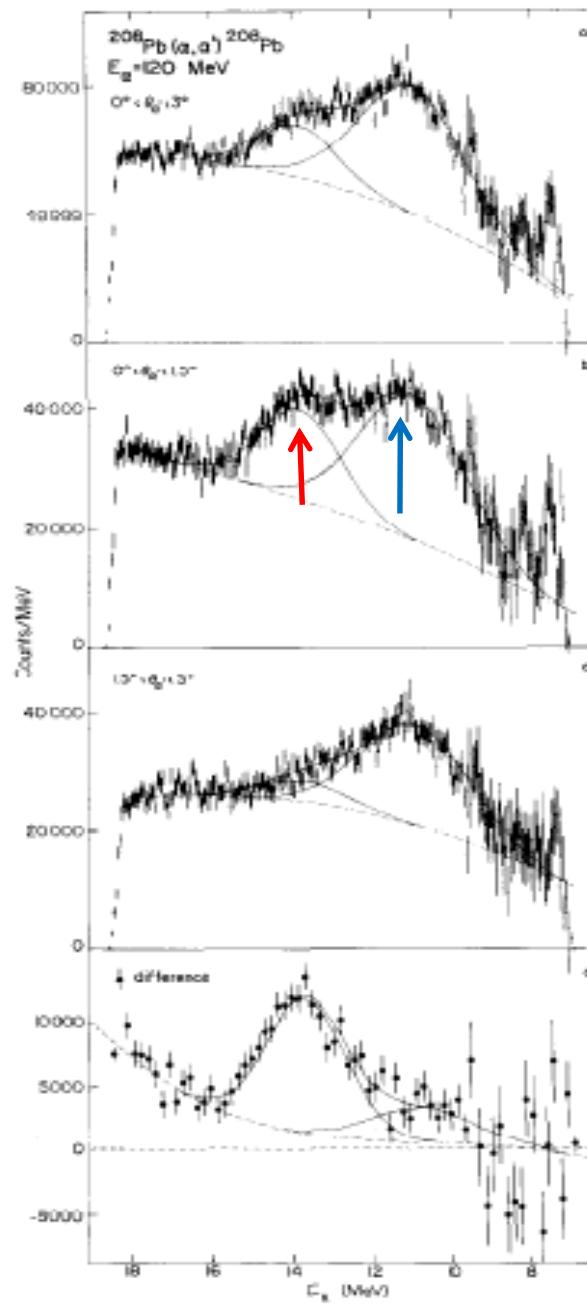
Difference of spectra

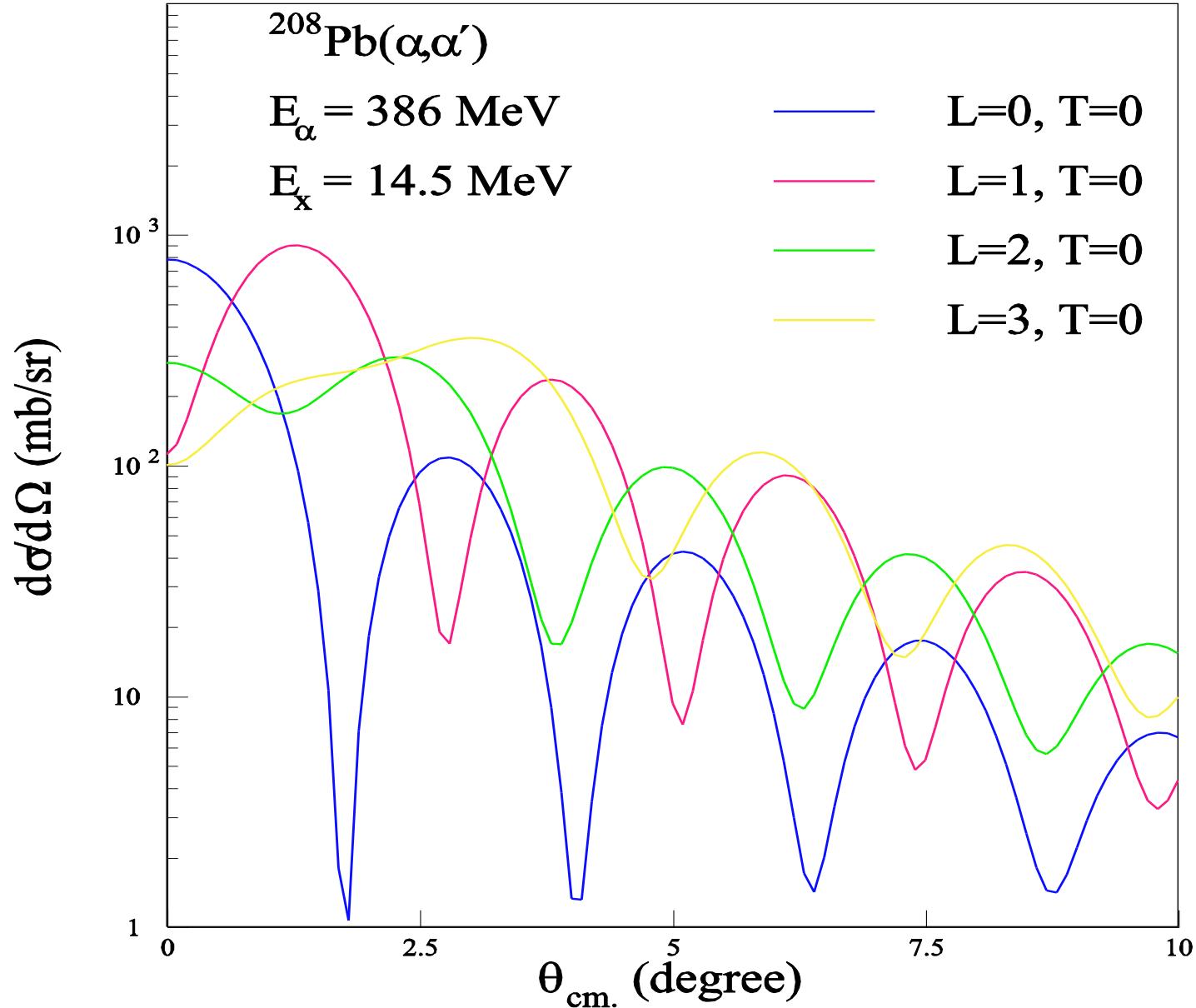
$0^\circ < \theta_{\alpha'} < 3^\circ$

$0^\circ < \theta_{\alpha'} < 1.5^\circ$

$1.5^\circ < \theta_{\alpha'} < 3^\circ$

Difference



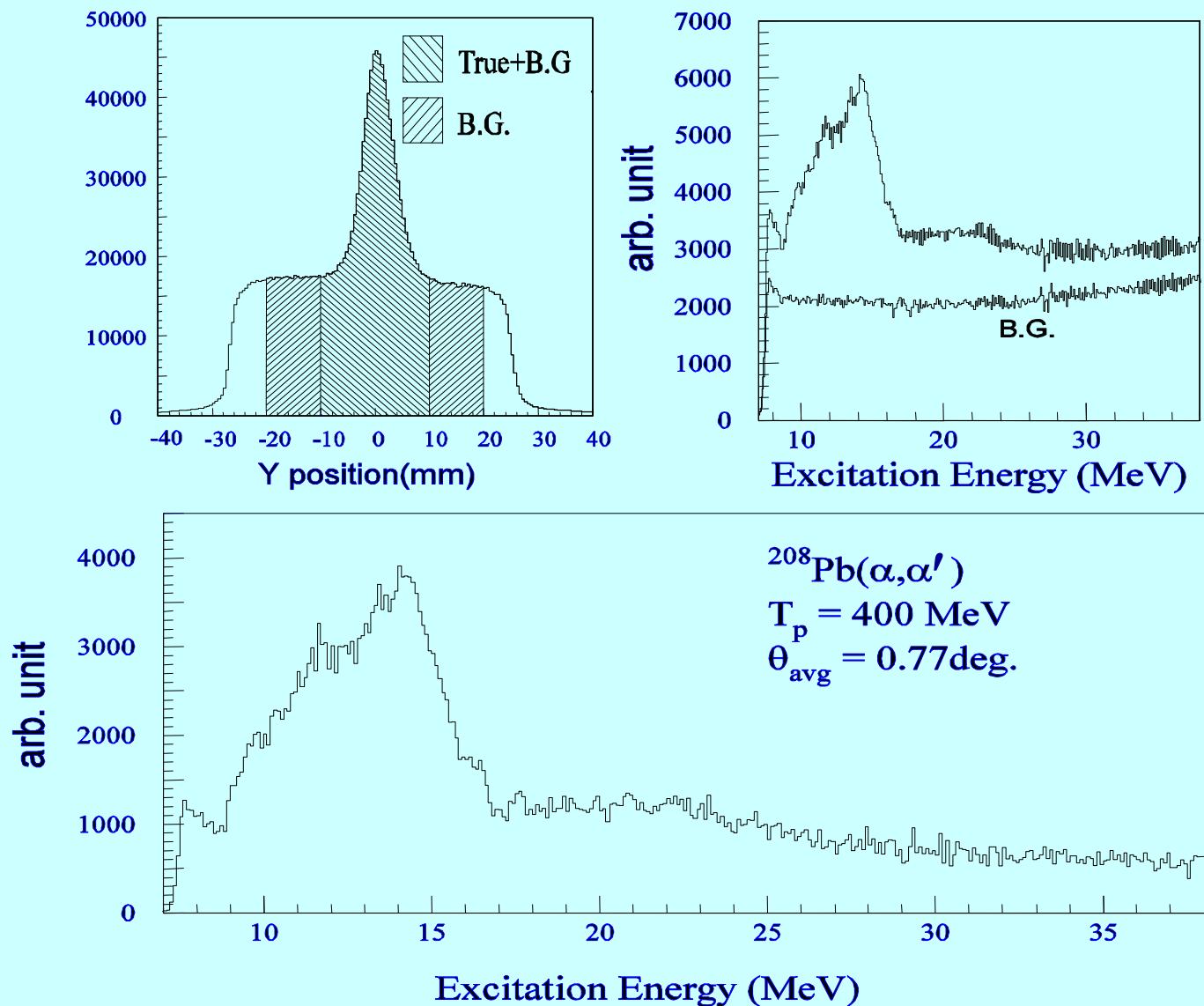


ISGMR, ISGDR

ISGQR, HEOR

100 % EWSR

At $E_x = 14.5$
MeV



Multipole decomposition analysis (MDA)

$$\left(\frac{d^2\sigma}{d\Omega dE}(\vartheta_{c.m.}, E) \right)^{\text{exp.}} = \sum_L a_L(E) \left(\frac{d^2\sigma}{d\Omega dE}(\vartheta_{c.m.}, E) \right)_L^{\text{calc.}}$$

$\left(\frac{d^2\sigma}{d\Omega dE}(\vartheta_{c.m.}, E) \right)^{\text{exp.}}$: Experimental cross section

$\left(\frac{d^2\sigma}{d\Omega dE}(\vartheta_{c.m.}, E) \right)_L^{\text{calc.}}$: DWBA cross section (unit cross section)

$a_L(E)$: EWSR fraction

- a. ISGR (L<15)+ IVGDR (through Coulomb excitation)
- b. DWBA formalism; single folding \Rightarrow transition potential

$$\delta U_L(r, E) = \int d\vec{r}' \delta\rho_L(\vec{r}', E) [V(|\vec{r} - \vec{r}'|, \rho_0(r')) + \rho_0(r') \frac{\partial V(|\vec{r} - \vec{r}'|, \rho(r'))}{\partial \rho_0(r')}]$$

$$U(r) = \int d\vec{r}' V(|\vec{r} - \vec{r}'|, \rho_0(r')) \rho_0(r')$$

Transition density

- ISGMR Satchler, Nucl. Phys. A472 (1987) 215

$$\delta\rho_0(r, E) = -\alpha_0 [3 + r \frac{d}{dr}] \rho_0(r)$$

$$\alpha_0^2 = \frac{2\pi\hbar^2}{mA \langle r^2 \rangle E}$$

- ISGDR Harakeh & Dieperink, Phys. Rev. C23 (1981) 2329

$$\delta\rho_1(r, E) = -\frac{\beta_1}{R\sqrt{3}} [3r^2 \frac{d}{dr} + 10r - \frac{5}{3} \langle r^2 \rangle \frac{d}{dr} + \varepsilon(r \frac{d^2}{dr^2} + 4 \frac{d}{dr})] \rho_0(r)$$

$$\beta_1^2 = \frac{6\pi\hbar^2}{mAE} \frac{R^2}{(11 \langle r^4 \rangle - (25/3) \langle r^2 \rangle^2 - 10\varepsilon \langle r^2 \rangle)}$$

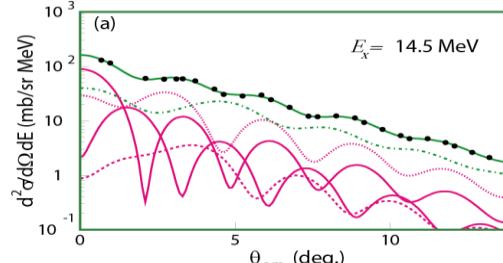
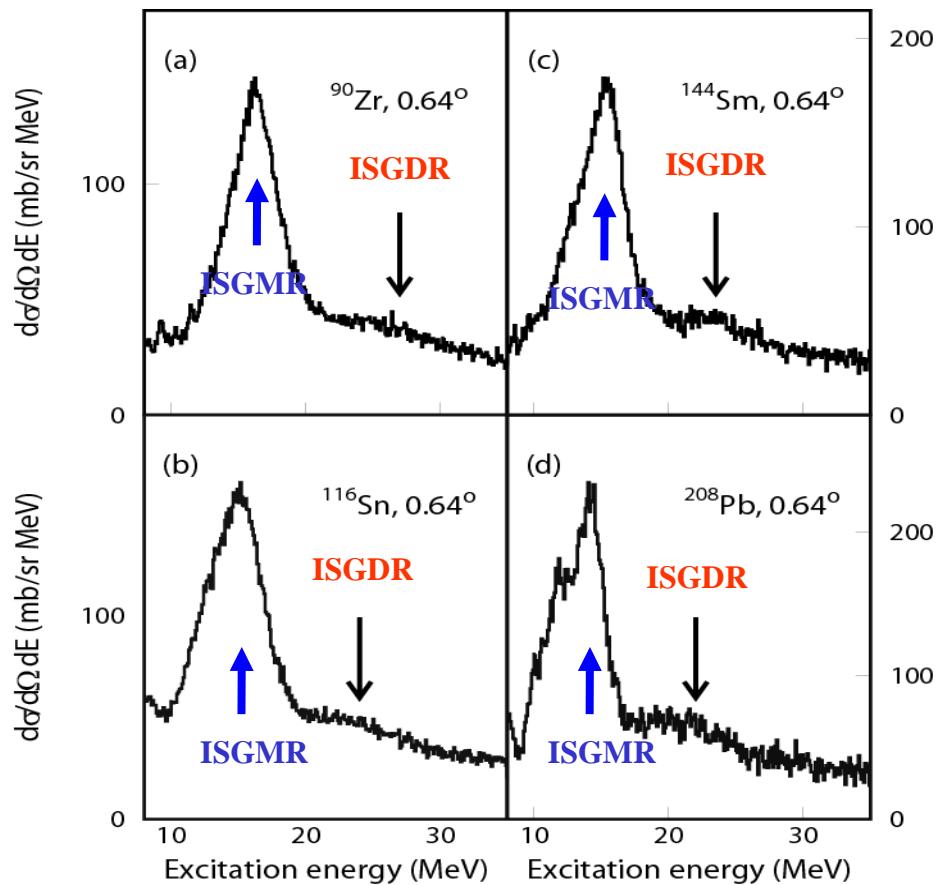
- Other modes Bohr-Mottelson (BM) model

$$\delta\rho_L(r, E) = -\delta_L \frac{d}{dr} \rho_0(r)$$

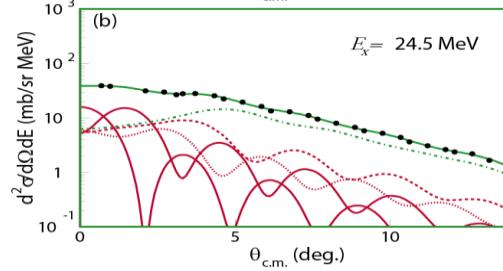
$$\delta_L^2 = (\beta_L c)^2 = \frac{L(2L+1)^2}{(L+2)^2} \frac{2\pi\hbar^2}{mAE} \frac{\langle r^{2L-2} \rangle}{\langle r^{L-1} \rangle^2}$$

Uchida *et al.*,
 Phys. Lett. B557 (2003) 12
 Phys. Rev. C69 (2004) 051301

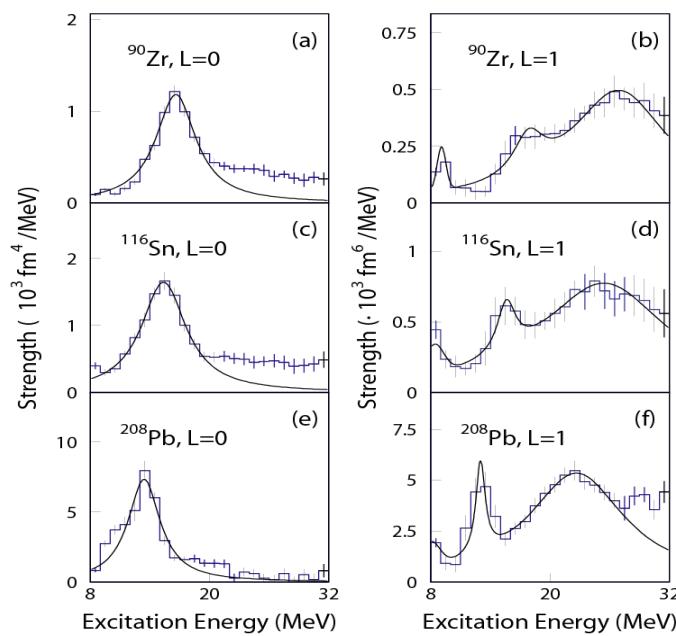
(α, α') spectra at 386 MeV

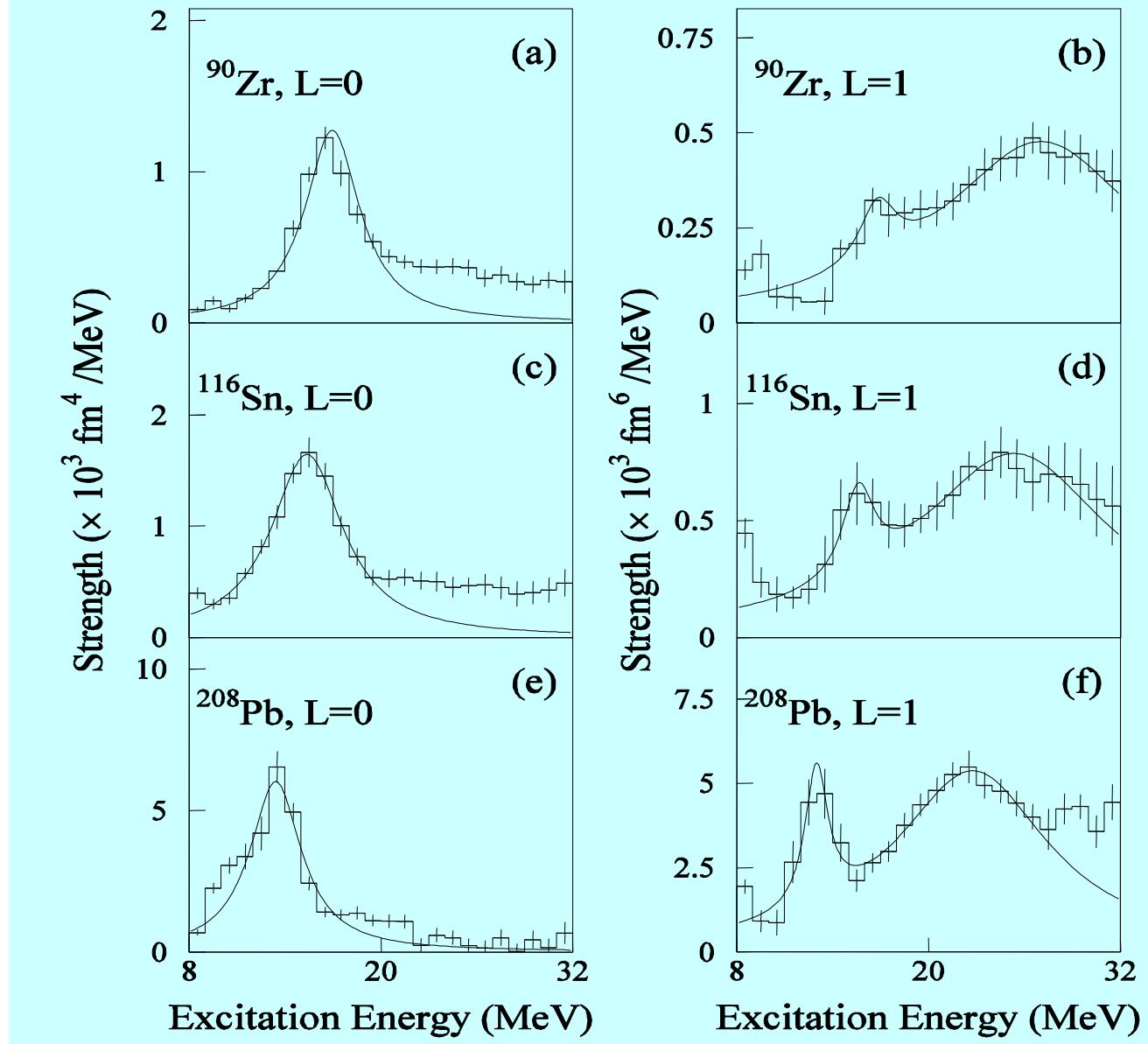


^{116}Sn



MDA results for $L=0$ and $L=1$





In HF+RPA calculations,

$$K_{nm} = \left[9\rho^2 \frac{d^2(E/A)}{d\rho^2} \right]_{\rho=\rho_0}$$

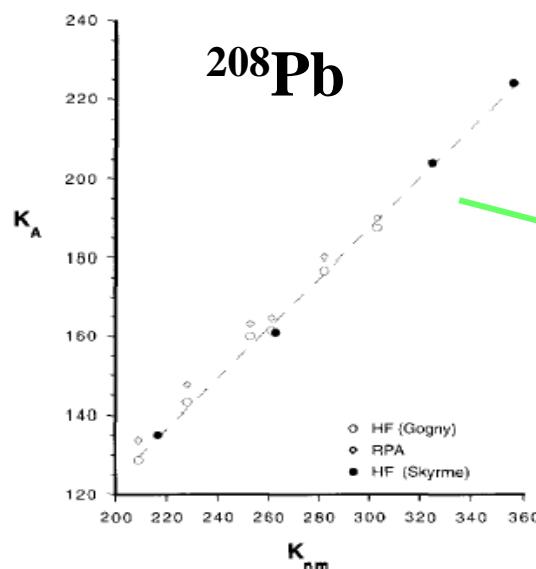
Nuclear matter

E/A: binding energy per nucleon

ρ : nuclear density

ρ_0 : nuclear density at saturation

K_A : incompressibility



K_A is obtained from excitation energy of ISGMR & ISGDR

$$K_A = 0.64K_{nm} - 3.5$$

J.P. Blaizot, Nucl. Phys. A591 (1995) 435

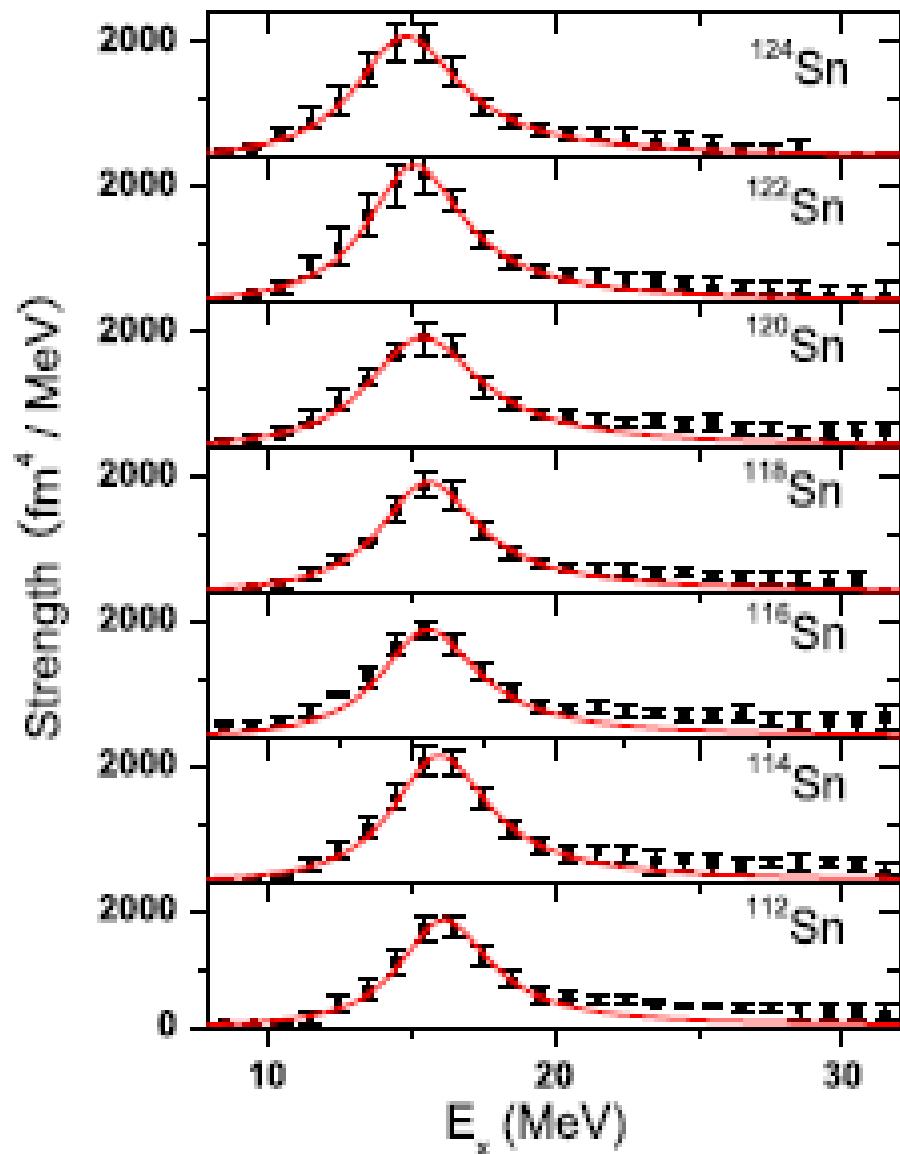
From GMR data on ^{208}Pb and ^{90}Zr ,

$$K_\infty = 240 \pm 10 \text{ MeV}$$

[See, e.g., G. Colò *et al.*, Phys. Rev. C 70 (2004) 024307]

This number is consistent
with both ISGMR and ISGDR Data
and
with non-relativistic and relativistic calculations

Isoscalar GMR strength distribution in Sn-isotopes obtained by Multipole Decomposition Analysis of singles spectra obtained in $^A\text{Sn}(\alpha, \alpha')$ measurements at incident energy 400 MeV and angles from 0° to 9°



$$K_A \sim K_{vol} (1 + cA^{-1/3}) + K_\tau ((N - Z)/A)^2 + K_{Coul} Z^2 A^{-4/3}$$

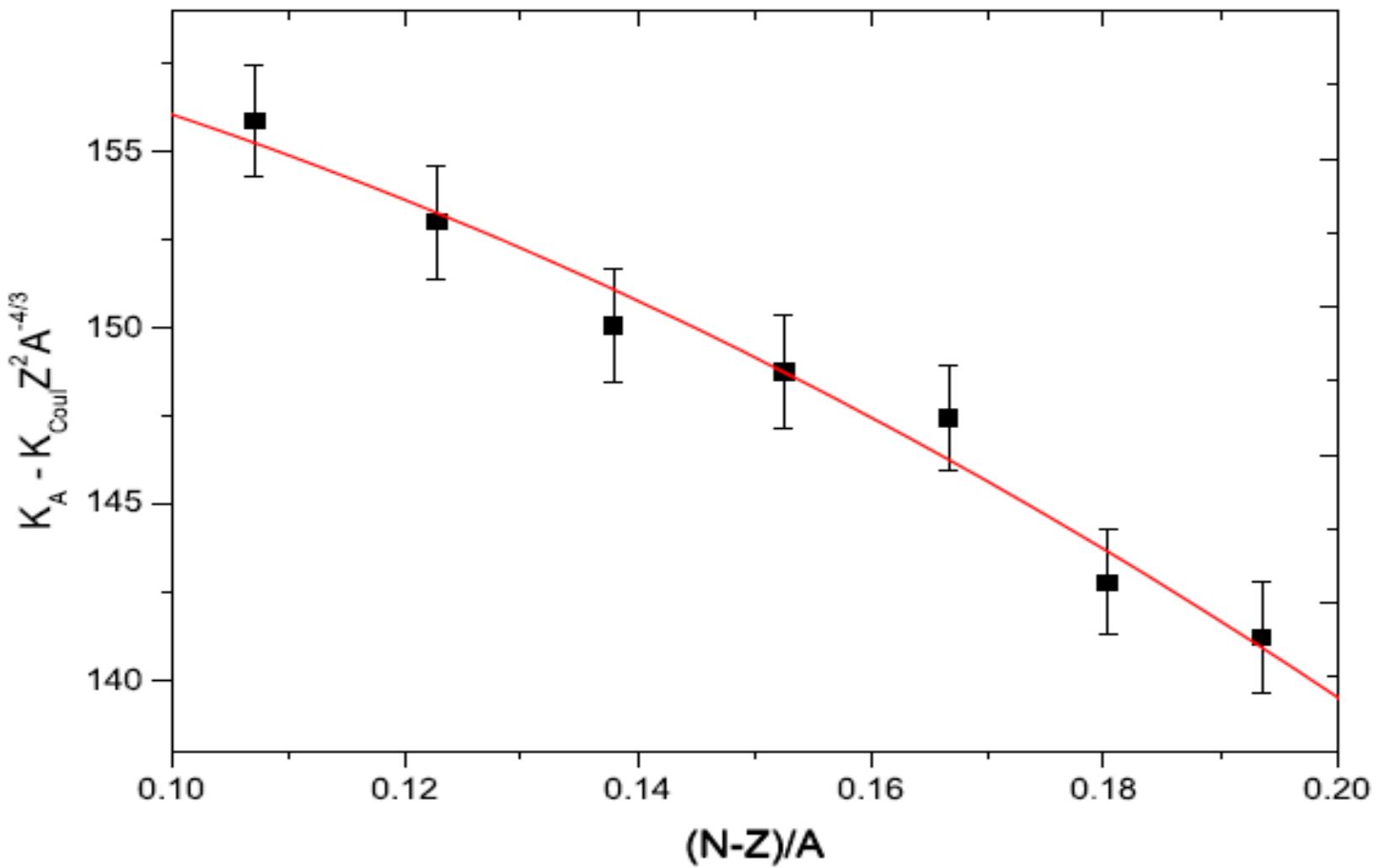
$$K_A - K_{Coul} Z^2 A^{-4/3} \sim K_{vol} (1 + cA^{-1/3}) + K_\tau ((N - Z)/A)^2$$

$$\sim \text{Constant} + K_\tau ((N - Z)/A)^2$$

We use $K_{Coul} = -5.2$ MeV (from Sagawa)

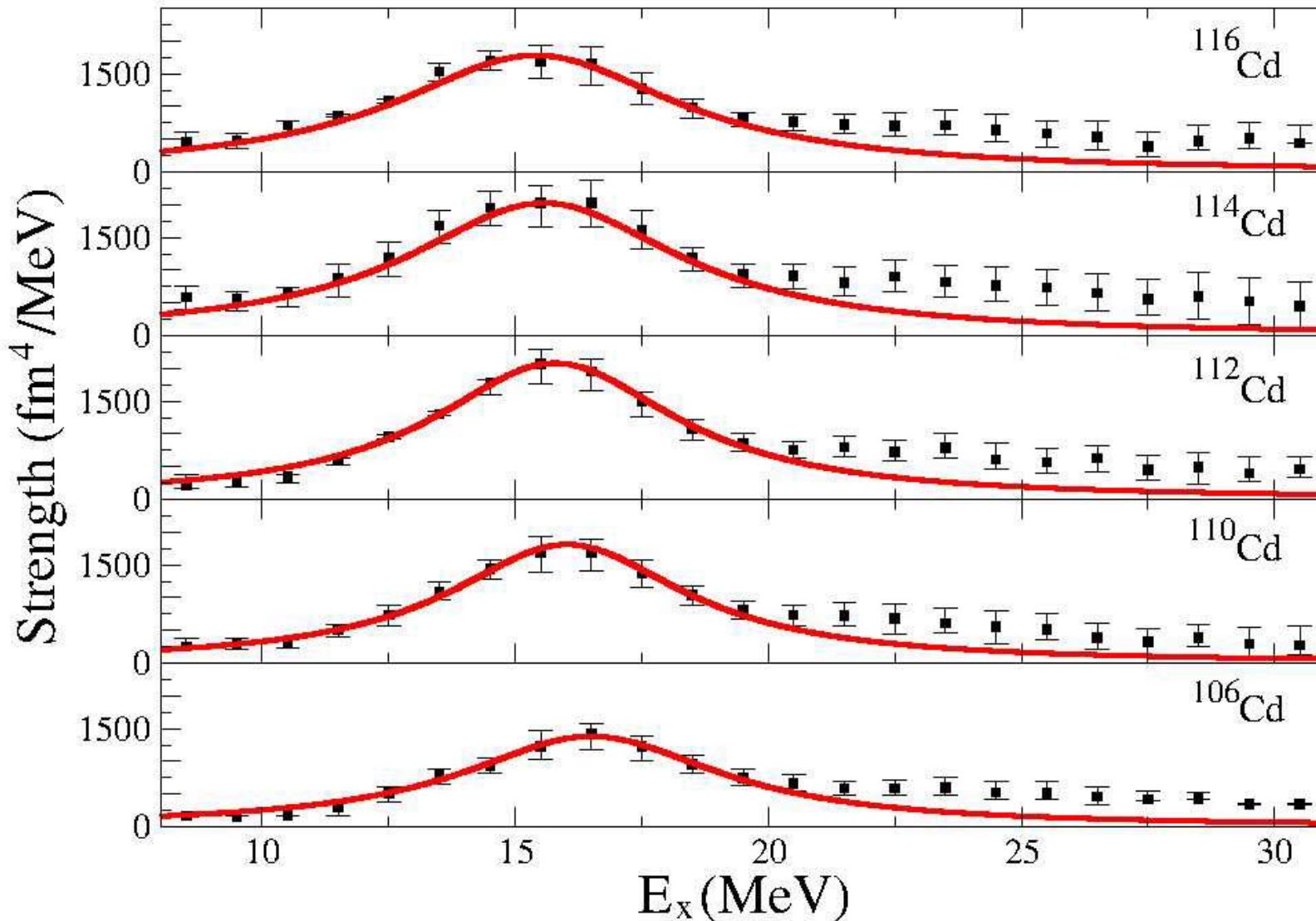
$$(N - Z)/A$$

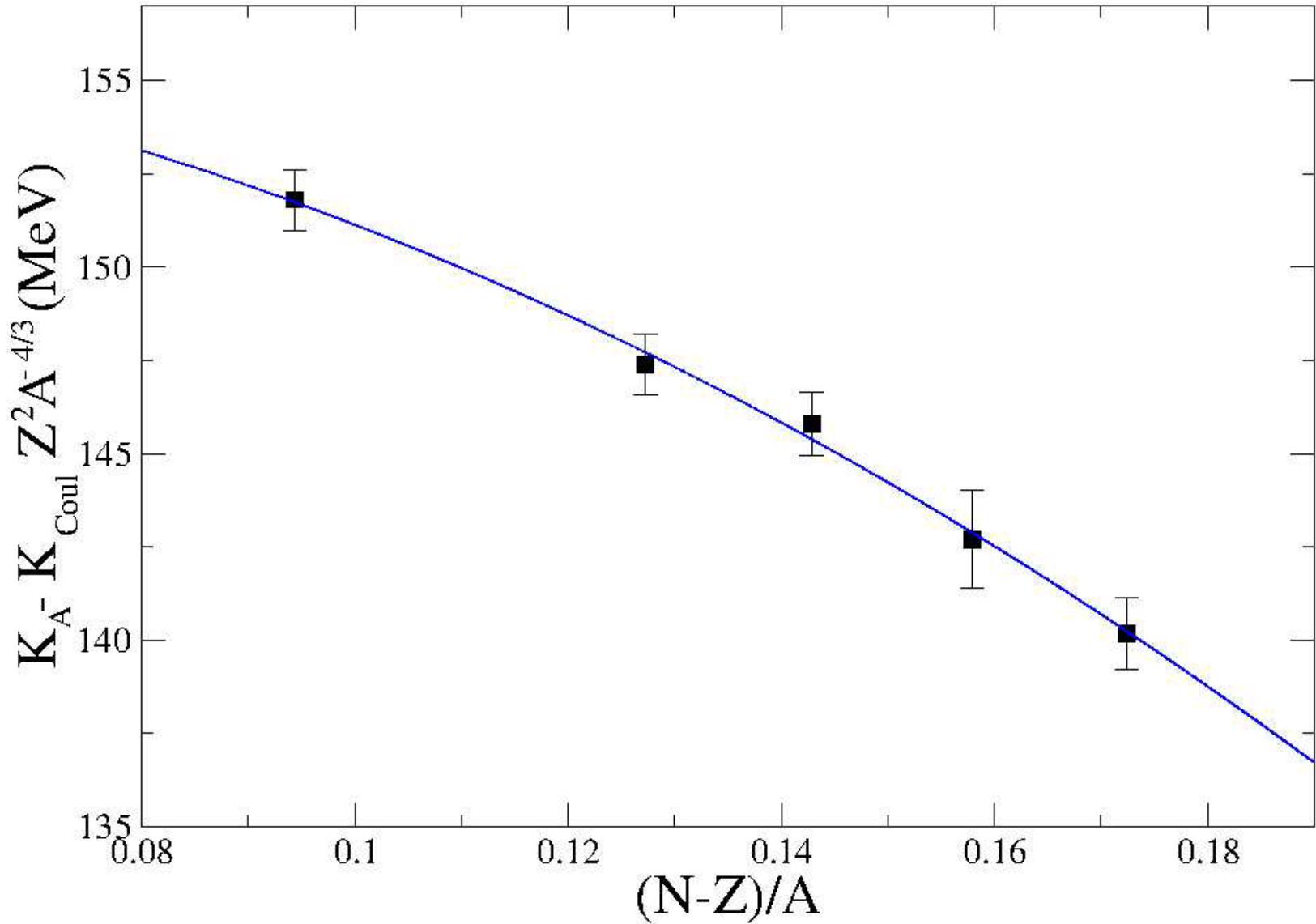
$$^{112}\text{Sn} - ^{124}\text{Sn}: \textcolor{red}{0.107 - 0.194}$$



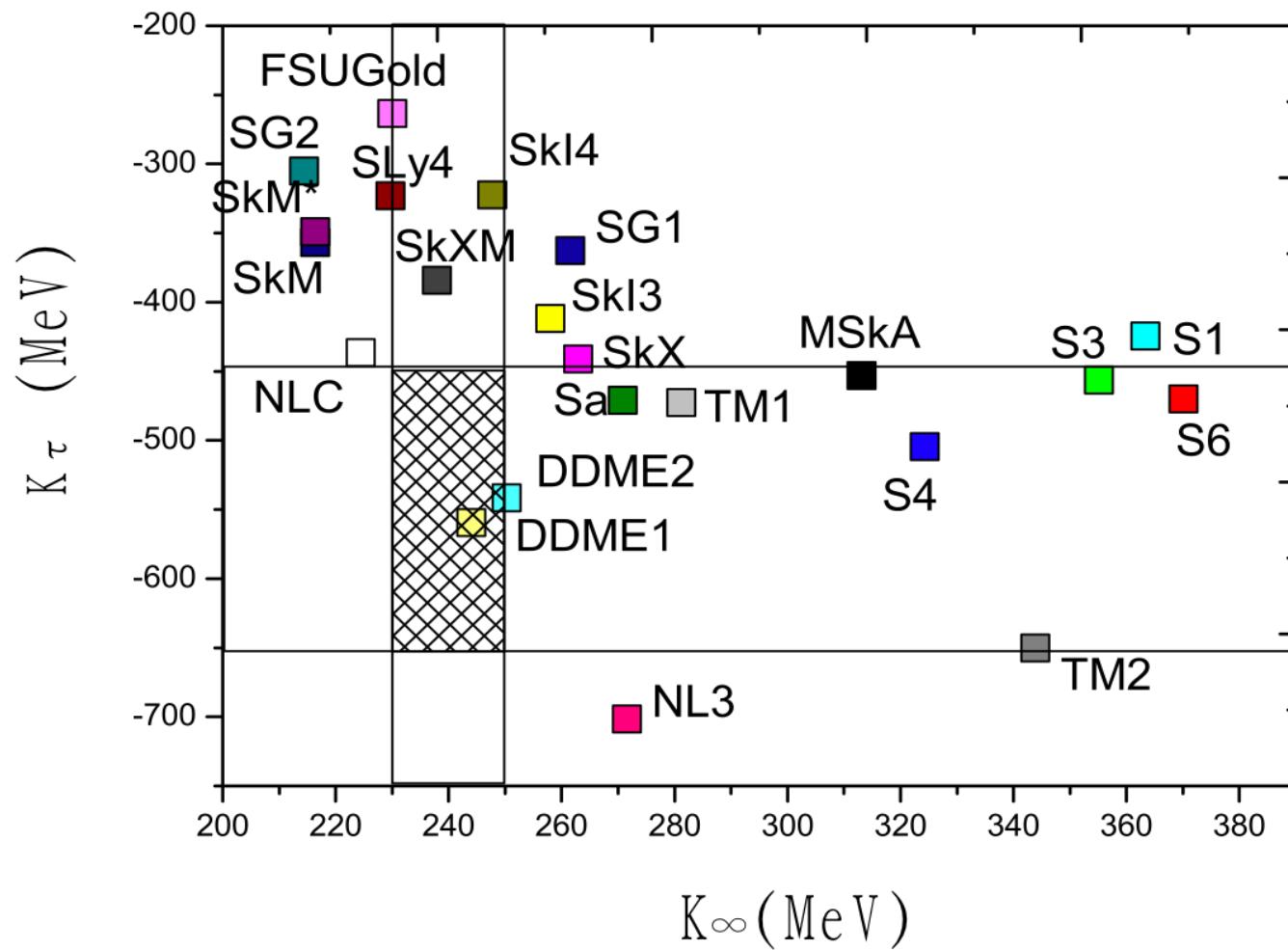
Sn isotopes $\Rightarrow K_\tau = -550 \pm 100$ MeV

Monopole strength Distribution

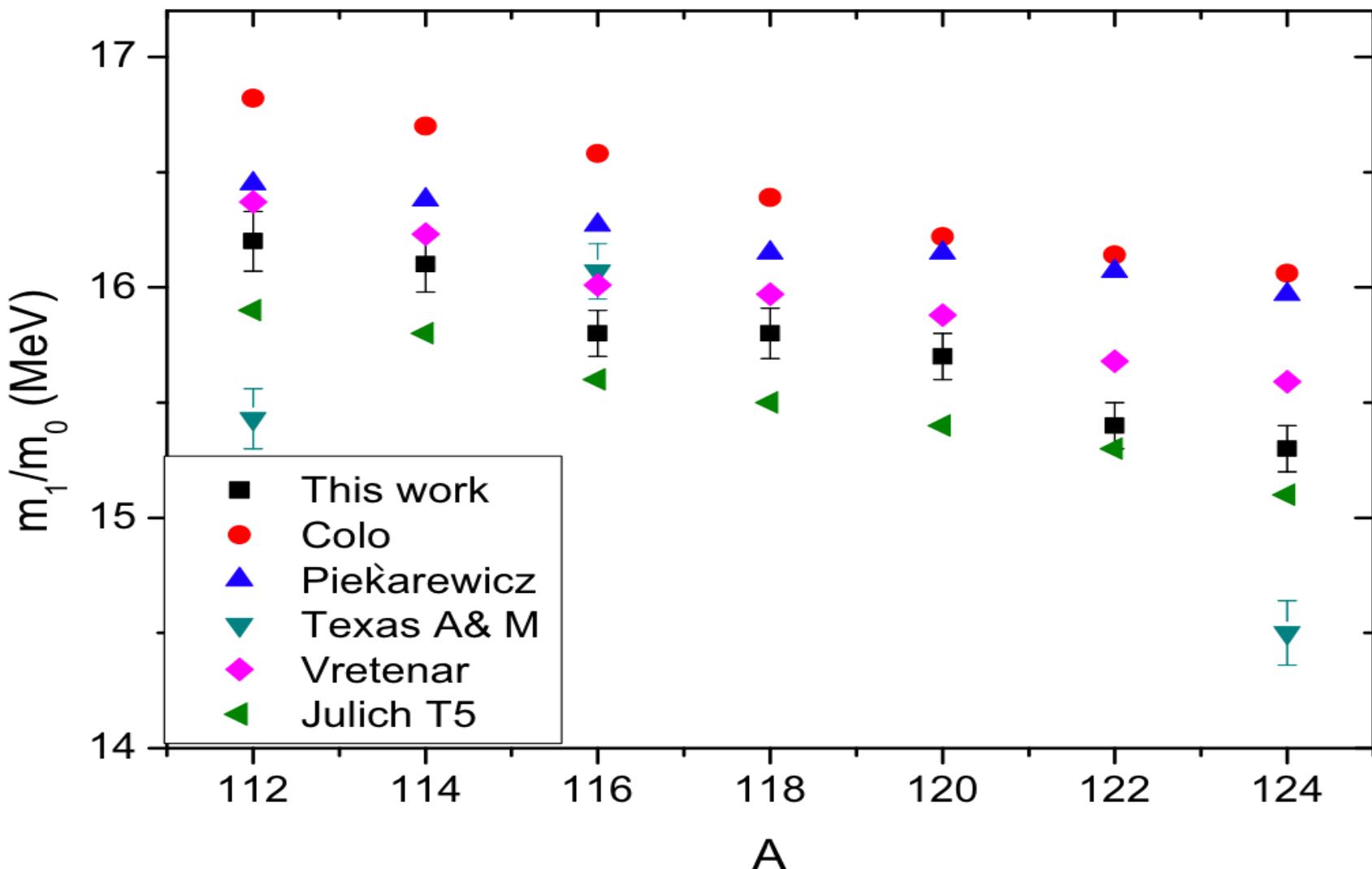




Cd isotopes $\Rightarrow K_\tau = -555 \pm 75 \text{ MeV}$



Data from H. Sagawa *et al.*, Phys. Rev. C **76** (2007) 034327



Colò *et al.*: Non-relativistic RPA (without pairing) reproduces ISGMR in ^{208}Pb and ^{90}Zr .

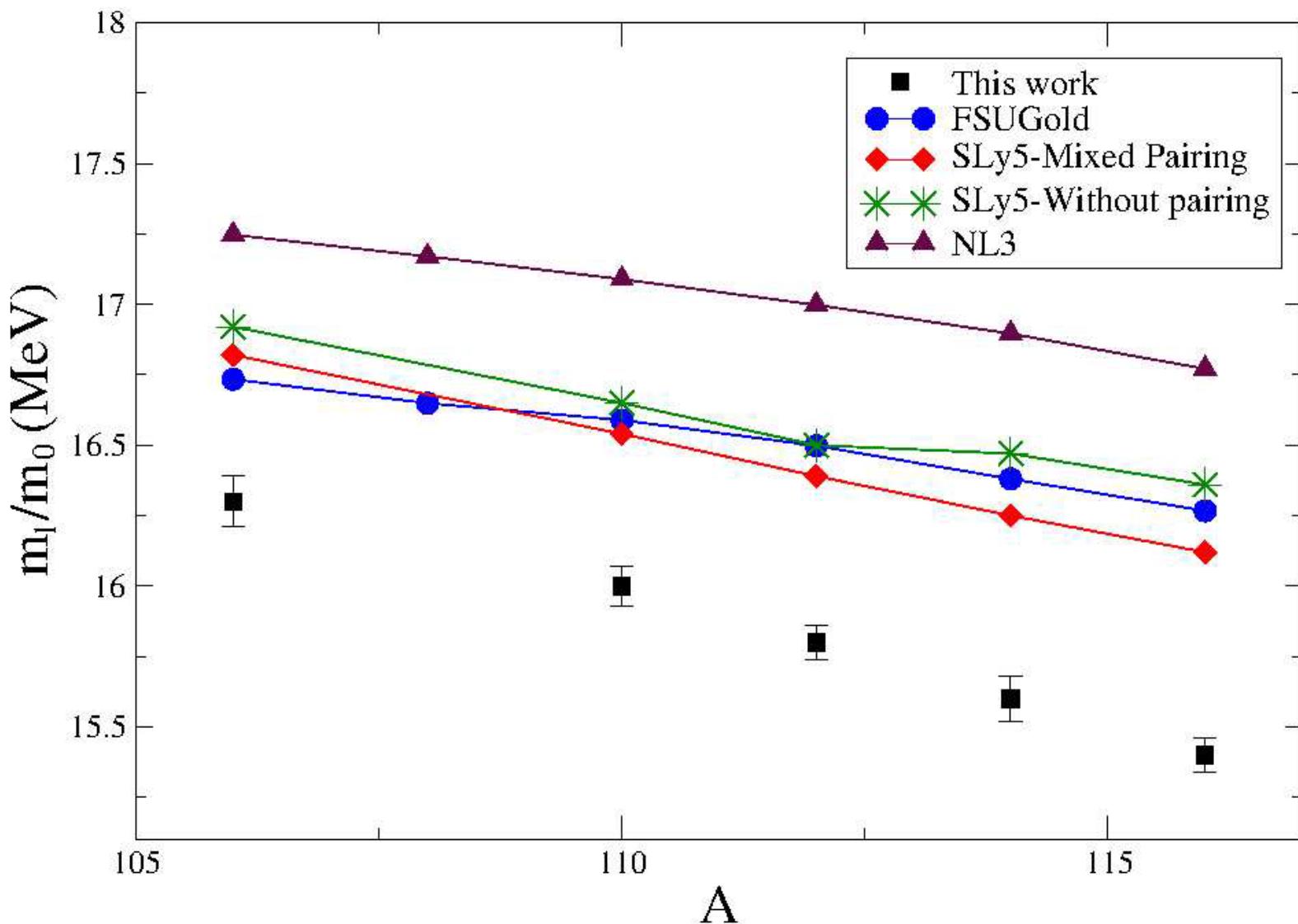
Piekarewicz: Relativistic RPA (FSUGold model) reproduces g.s. observables and ISGMR in ^{208}Pb , ^{144}Sm and ^{90}Zr [$K_\infty = 230$ MeV]

Vretenar: Relativistic mean field (DD-ME2: density-dependent mean-field effective interaction).

[$K_\infty = 240$ MeV]. Possibly agreement is fortuitous since strength distributions are not much different from those by Colò *et al.* and Piekarewicz.

Tselyaev *et al.*: Quasi-particle time-blocking approximation (QTBA) (T5 Skyrme interaction)
[$K_\infty = 202$ MeV?!!]

Softness of Sn-nuclei is still unresolved

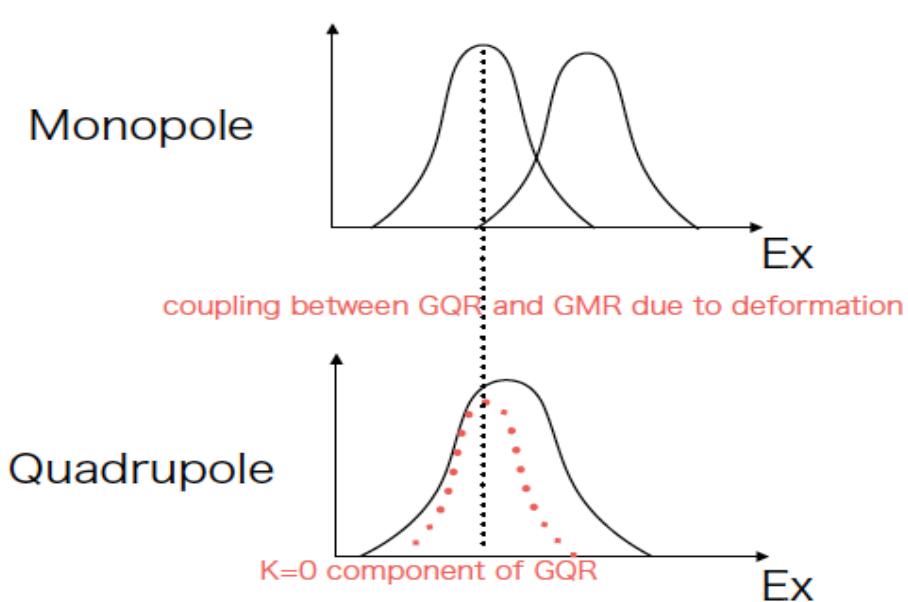
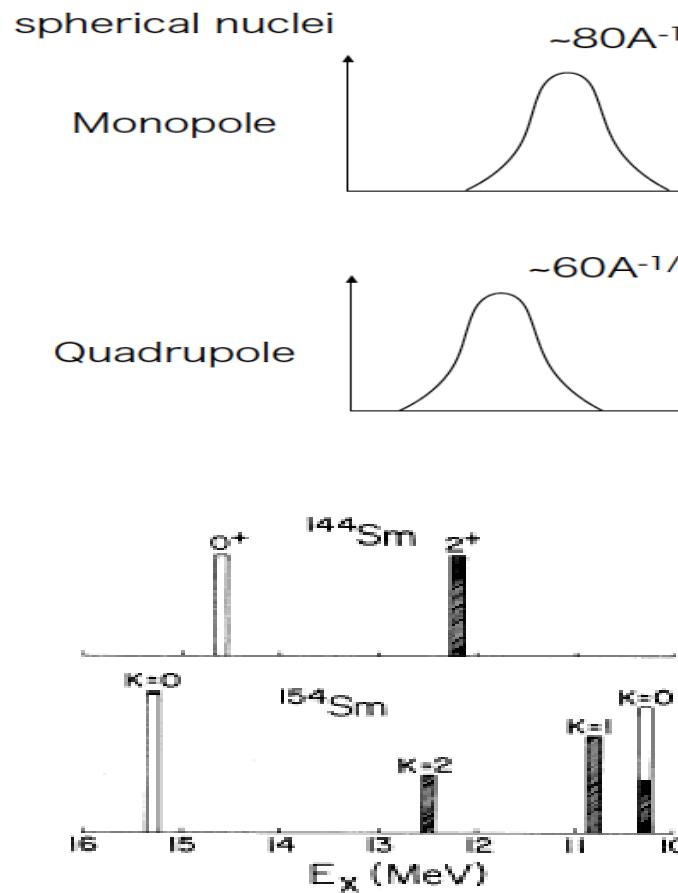


**RRPA: FSUGold [$K_\infty = 230$ MeV]; SLy5 [$K_\infty = 230$ MeV];
NL3 [$K_\infty = 271$ MeV]**

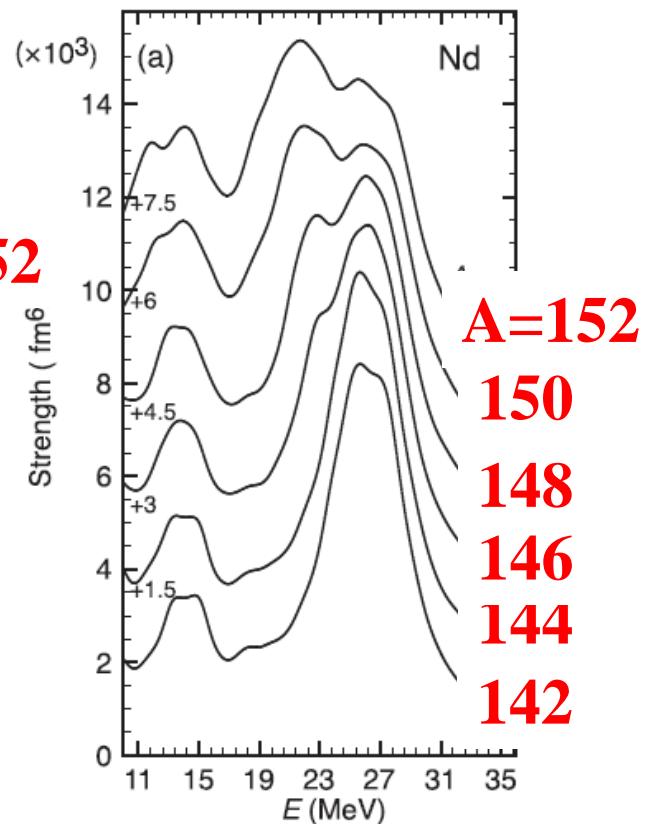
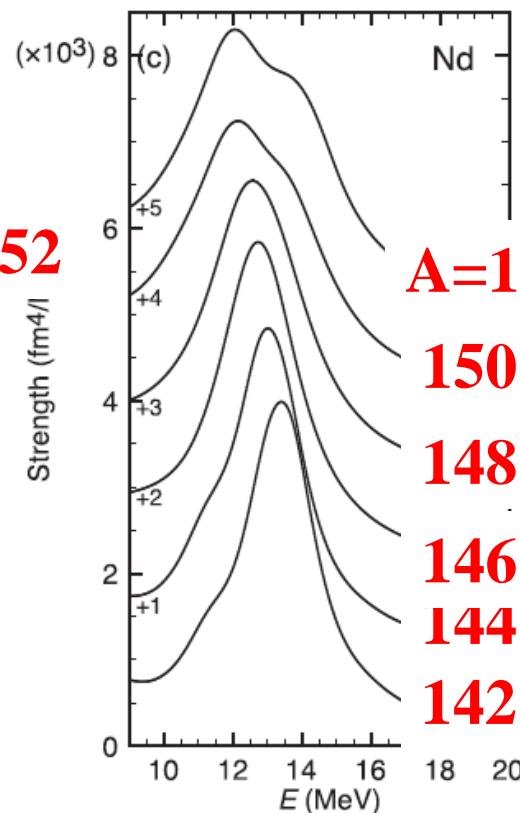
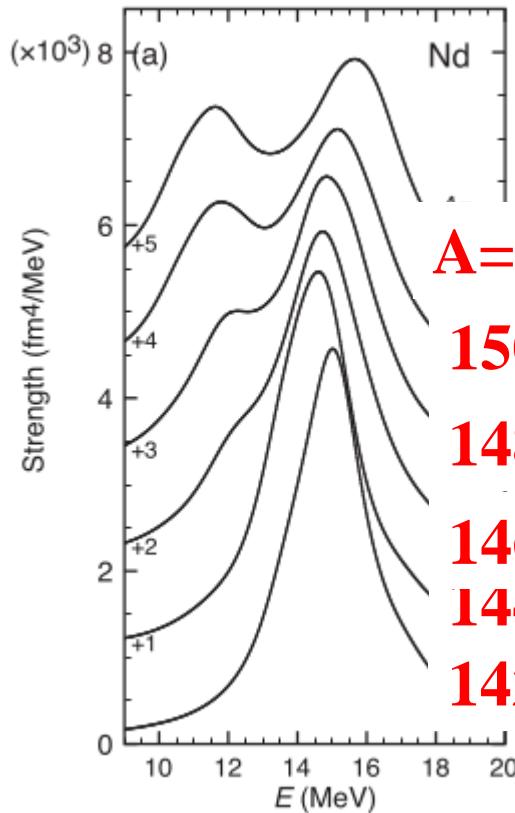
Splitting of the ISGMR under deformation

K projection of J on symmetry axis is good quantum number in deformed nuclei

Coupling of ISGMR with K=0 component of ISGQR



Isoscalar Giant Resonances in Nd isotopes: QRPA calculations



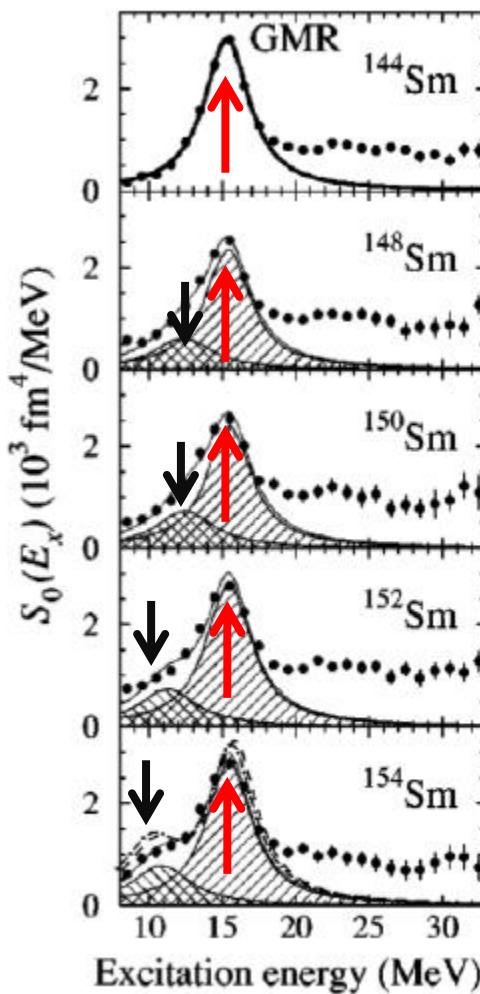
$\Delta L = 0$; ISGMR

$\Delta L = 2$; ISGQR

$\Delta L = 1$; ISGDR

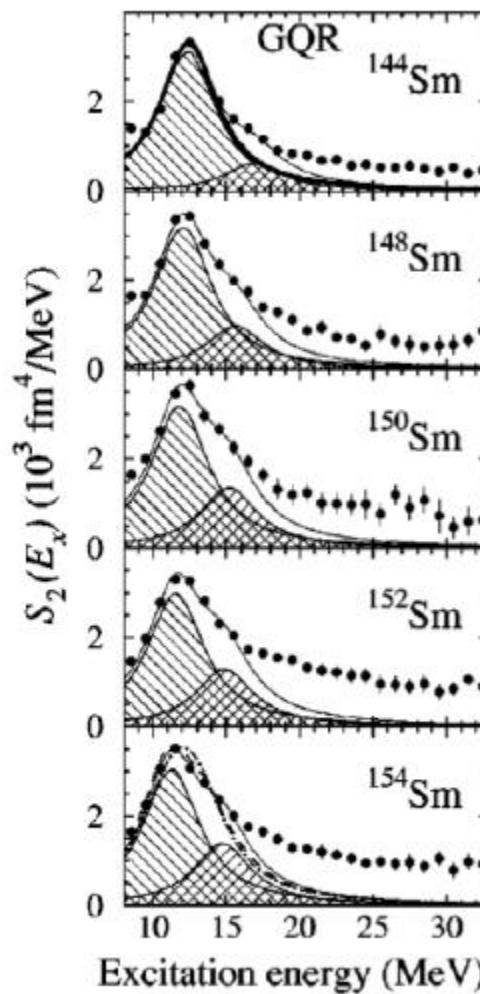
K. Yoshida and T. Nakatsukasa, Phys. Rev. C 88 (2013) 034309

Effect of deformation on Isoscalar Giant Resonances: Sm isotopes

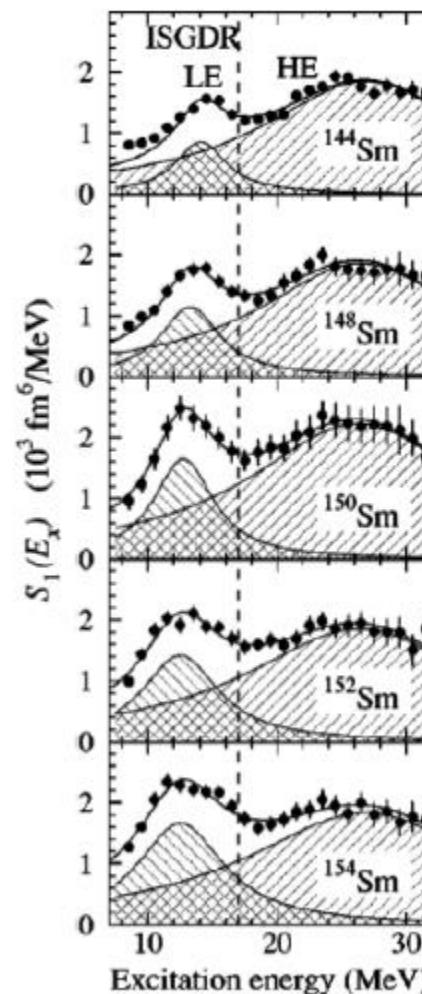


$\Delta L = 0$; ISGMR

M. Itoh *et al.*, Phys. Rev. C 68 (2003) 064602



$\Delta L = 2$; ISGQR



$\Delta L = 1$; ISGDR

^{144}Sm
 $\beta_2 = 0.0881 (13)$

^{148}Sm

^{150}Sm

^{152}Sm

^{154}Sm
 $\beta_2 = 0.339 (3)$

Decay of Giant Resonances

Decay of giant resonances

■ Width of resonance

$$\Gamma, \Gamma^\uparrow, \Gamma^\downarrow (\Gamma^{\downarrow\uparrow}, \Gamma^{\downarrow\downarrow})$$

■ Γ^\uparrow : direct or escape width

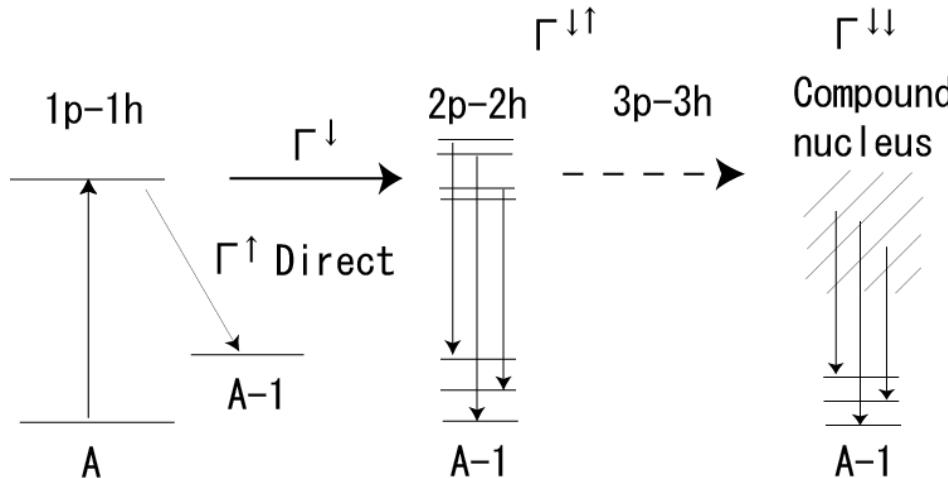
■ Γ^\downarrow : spreading width

$\Gamma^{\downarrow\uparrow}$: pre-equilibrium, $\Gamma^{\downarrow\downarrow}$: compound

■ Decay measurements

⇒ Direct reflection of damping processes

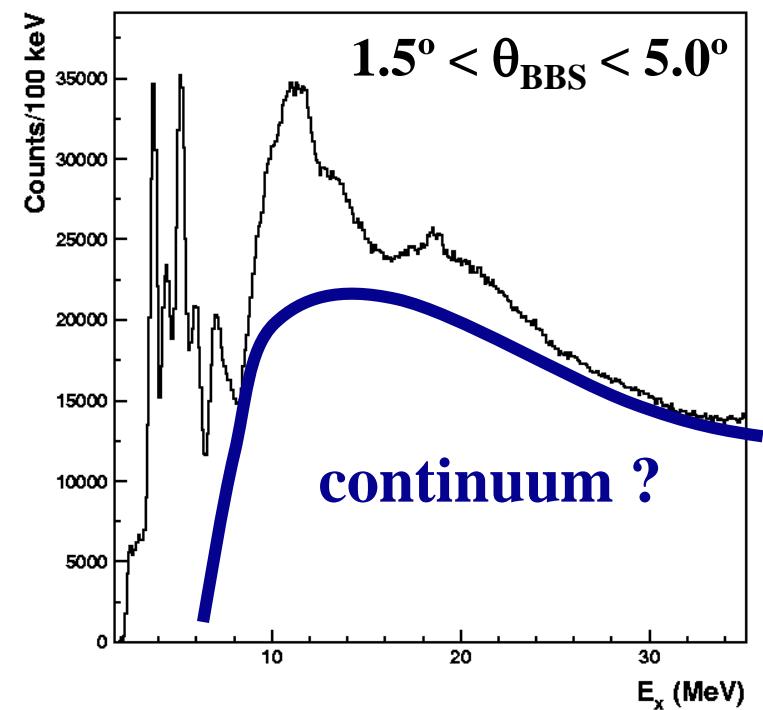
Allows detailed comparison with theoretical calculations



Excitation of ISGDR in ^{208}Pb

- In ^{208}Pb located around 22 MeV and width of 4 MeV
- $L=1$ angular distribution peaks close to a scattering angle of 3°
- Difficult to identify in nuclear continuum and rides on instrumental background

Singles $^{208}\text{Pb}(\alpha, \alpha')$
At $E_\alpha = 200 \text{ MeV}$ \Rightarrow



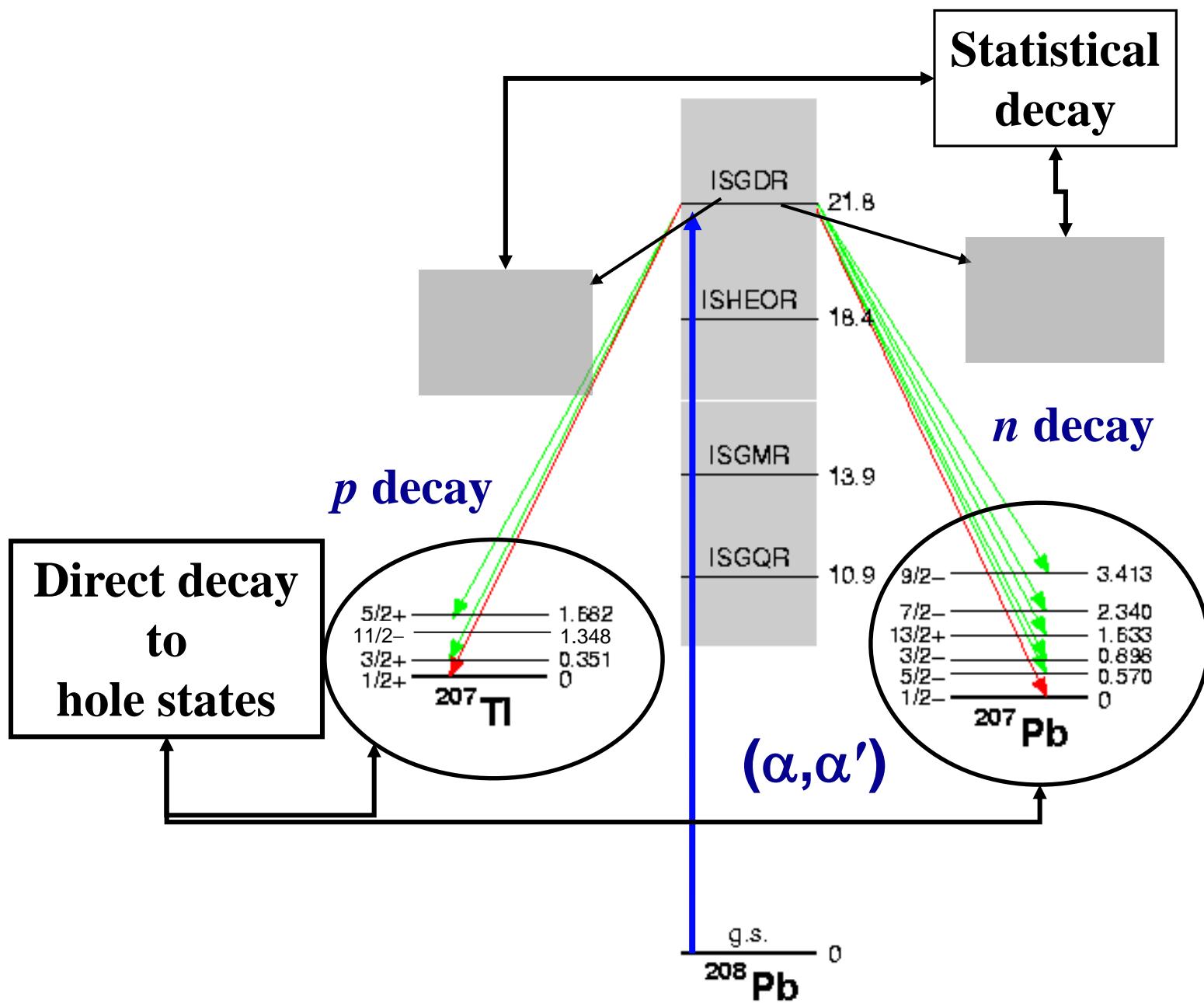
Microscopic structure of ISGDR

Transition operator

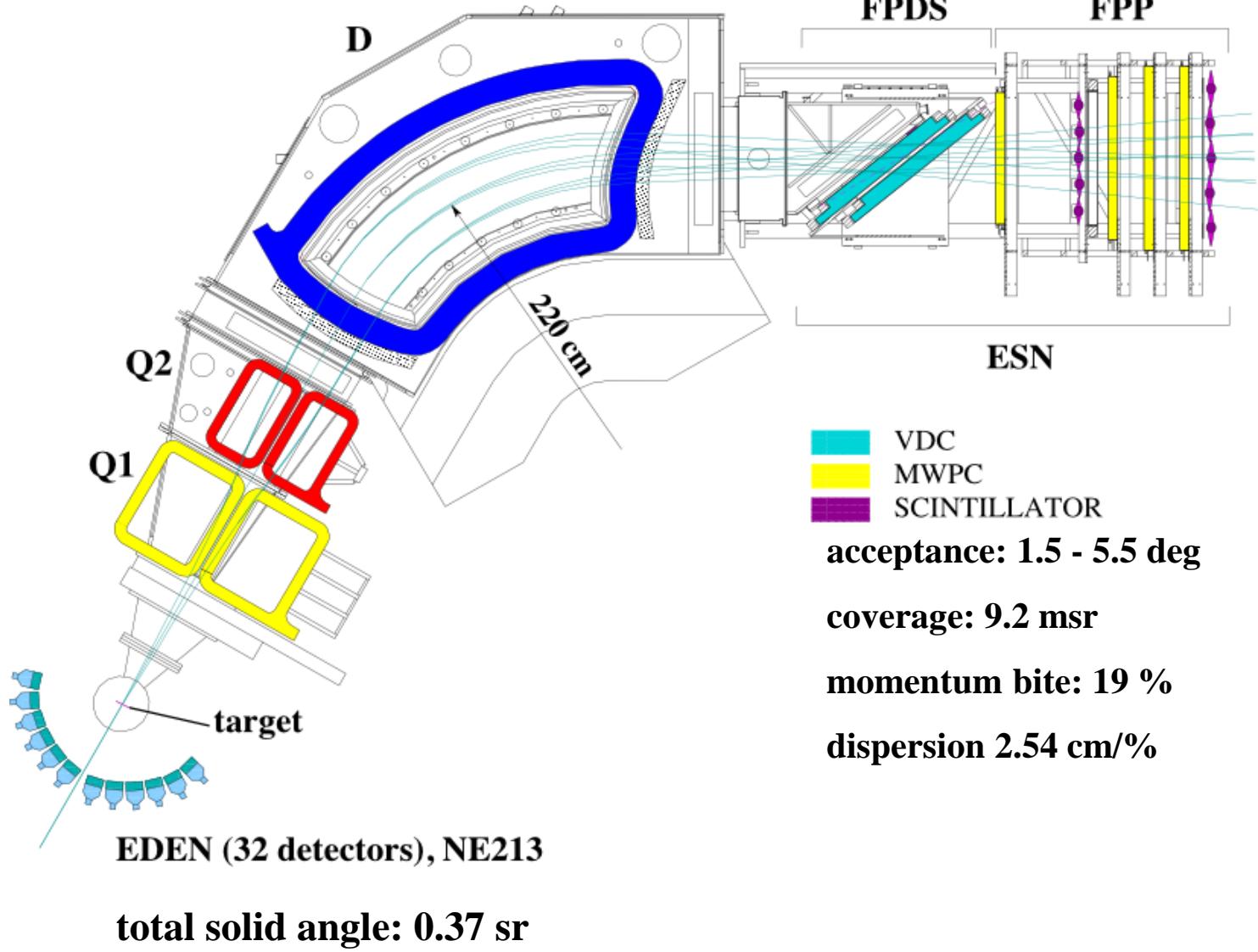
$$O^{L=1} = \sum_i r_i^1 Y_0^1 + \frac{1}{2} \sum_i r_i^3 Y_0^1 + \dots$$

Spurious center Overtone
of mass motion

$3\hbar\omega$ excitation (overtone of c.o.m. motion)

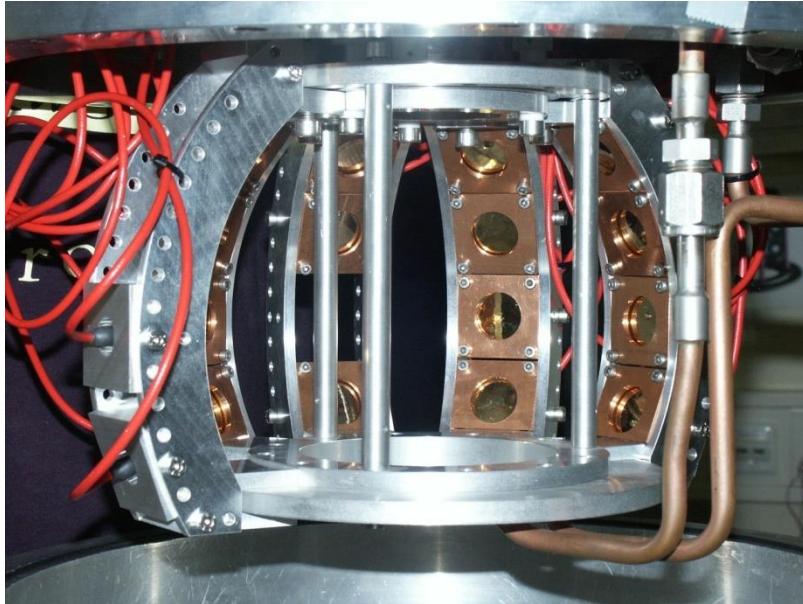


Si-ball
**16 Si-detectors at
10 cm from the target**
total solid angle: 1 sr

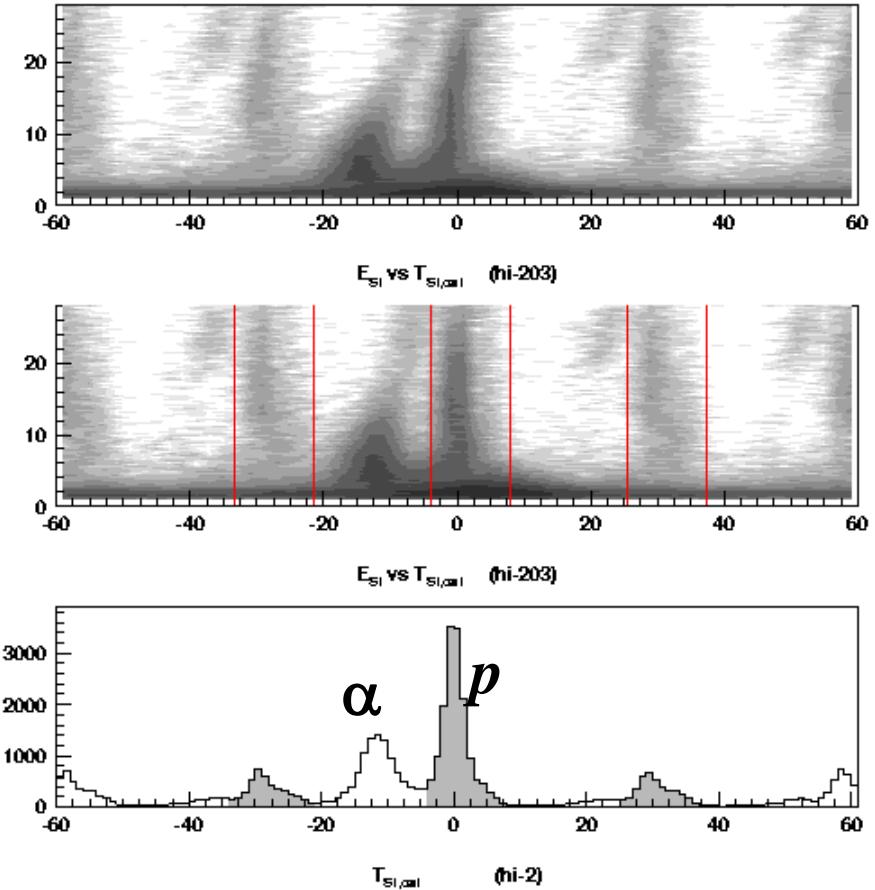


KVI Big-Bite Spectrometer (BBS)

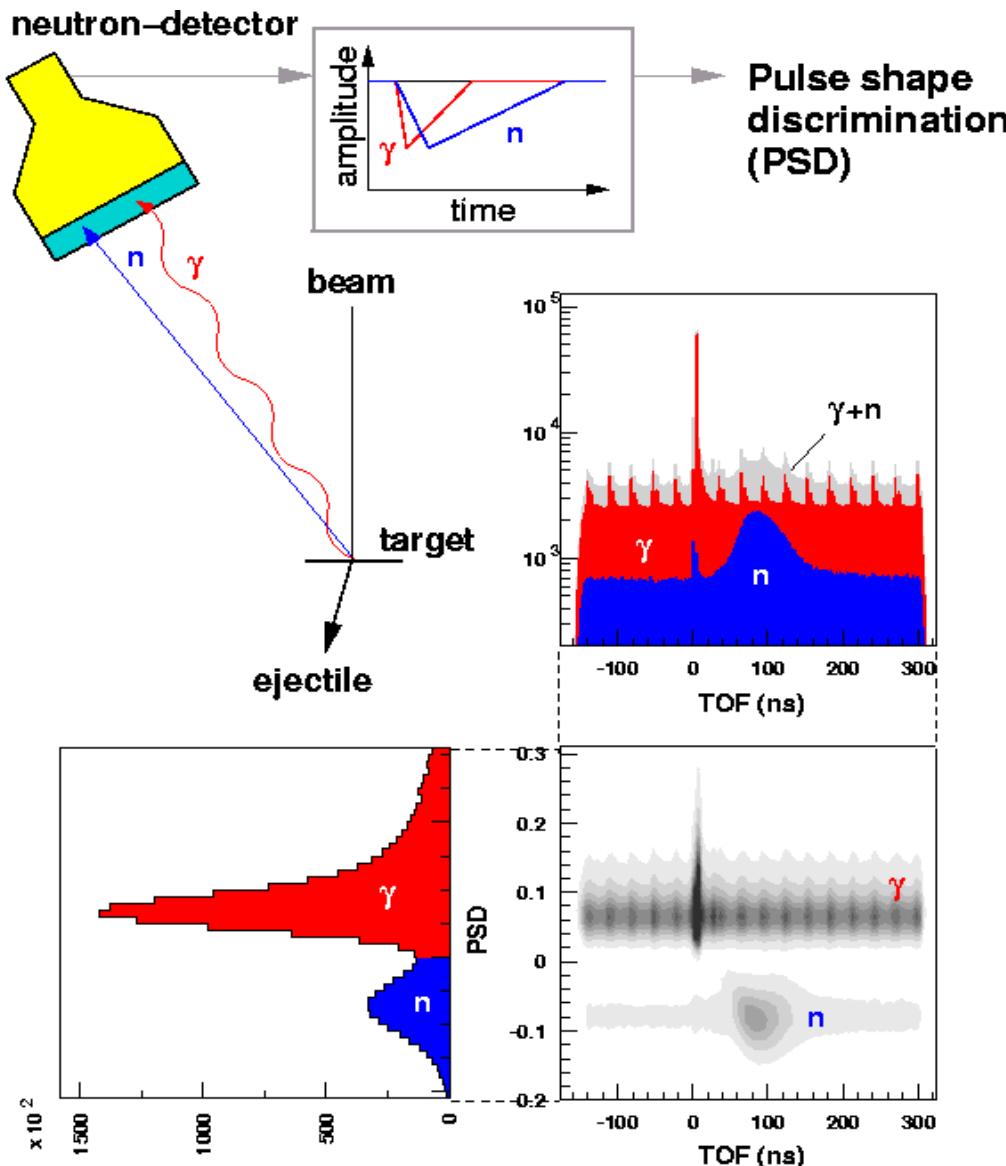
Proton-decay detection



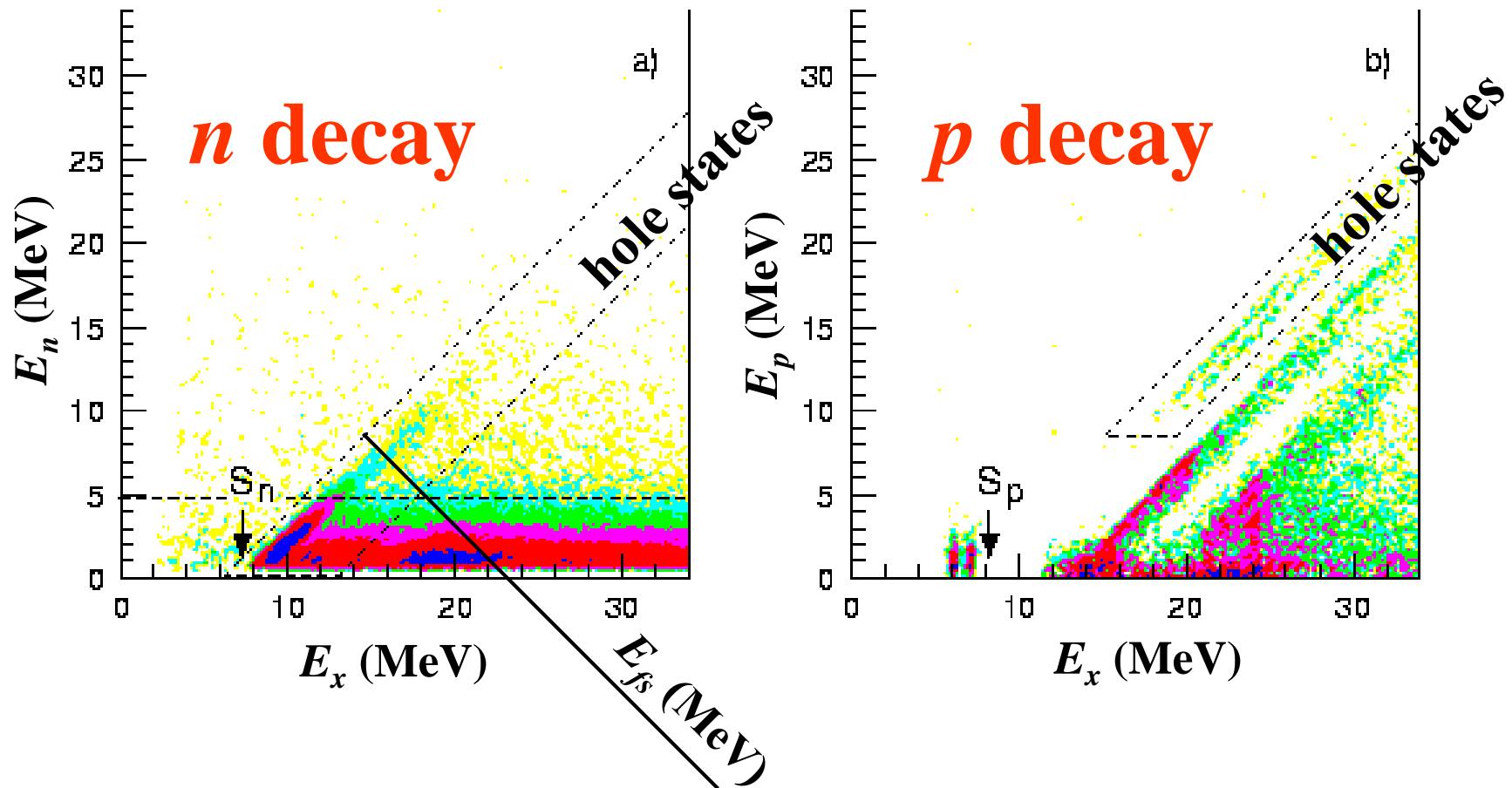
α - p separation using
rise time of signal Si(Li)



Neutron-decay detection

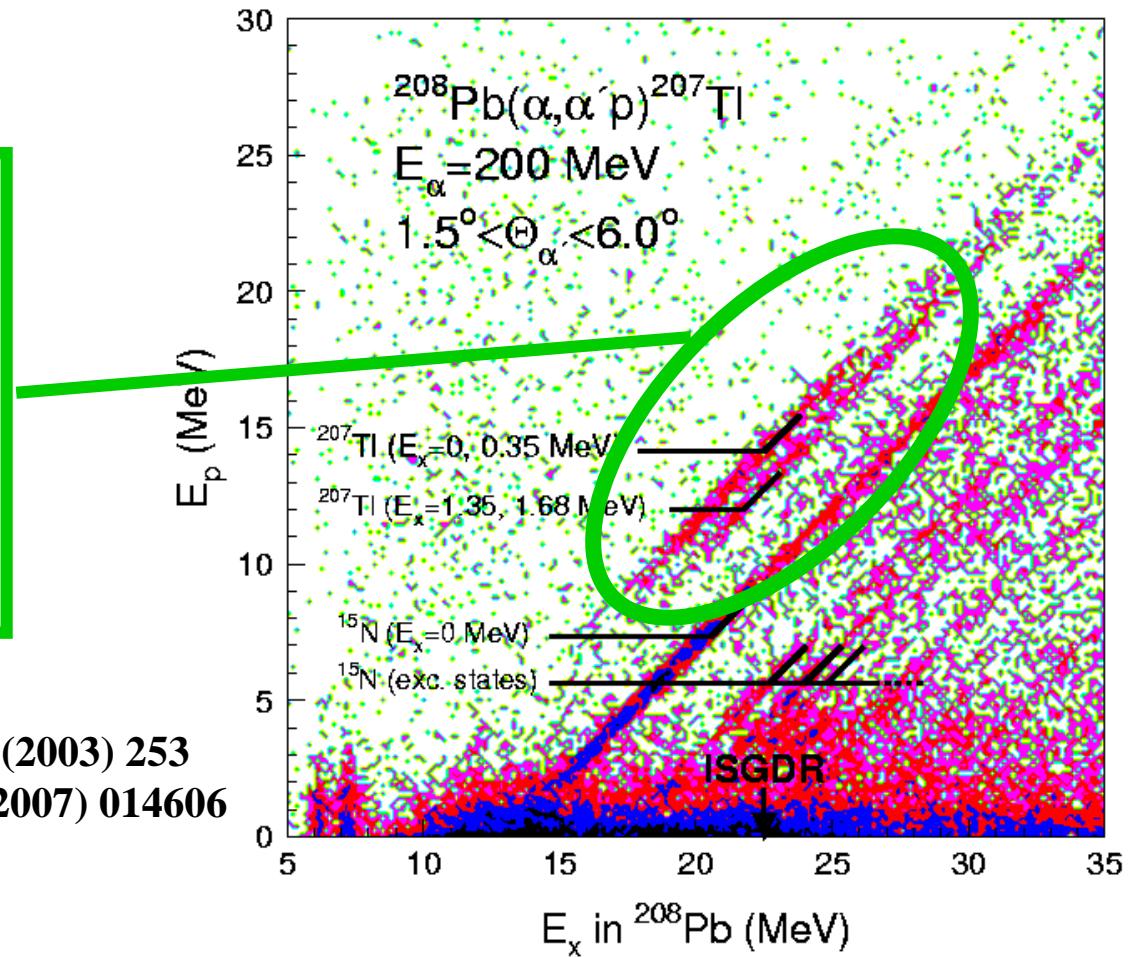


$^{208}\text{Pb}(\alpha, \alpha' p \text{ or } n)$



$^{208}\text{Pb}(\alpha, \alpha')$ followed by p decay

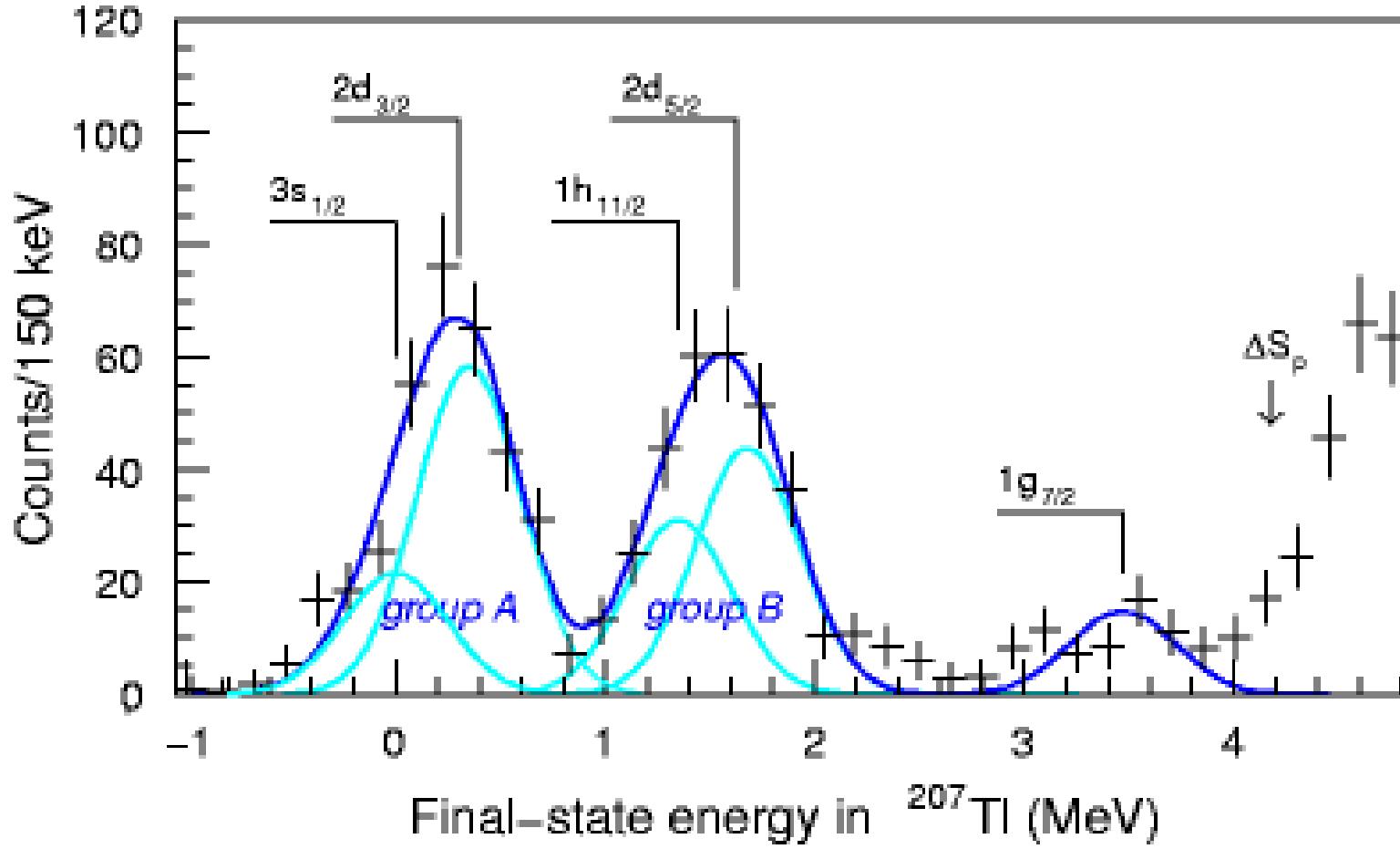
Decay to hole states in ^{207}Tl ;
branching ratios predicted by
Gorelik *et al.*



M. Hunyadi *et al.*, Phys. Lett. B576 (2003) 253

M. Hunyadi *et al.*, Phys. Rev. C75 (2007) 014606

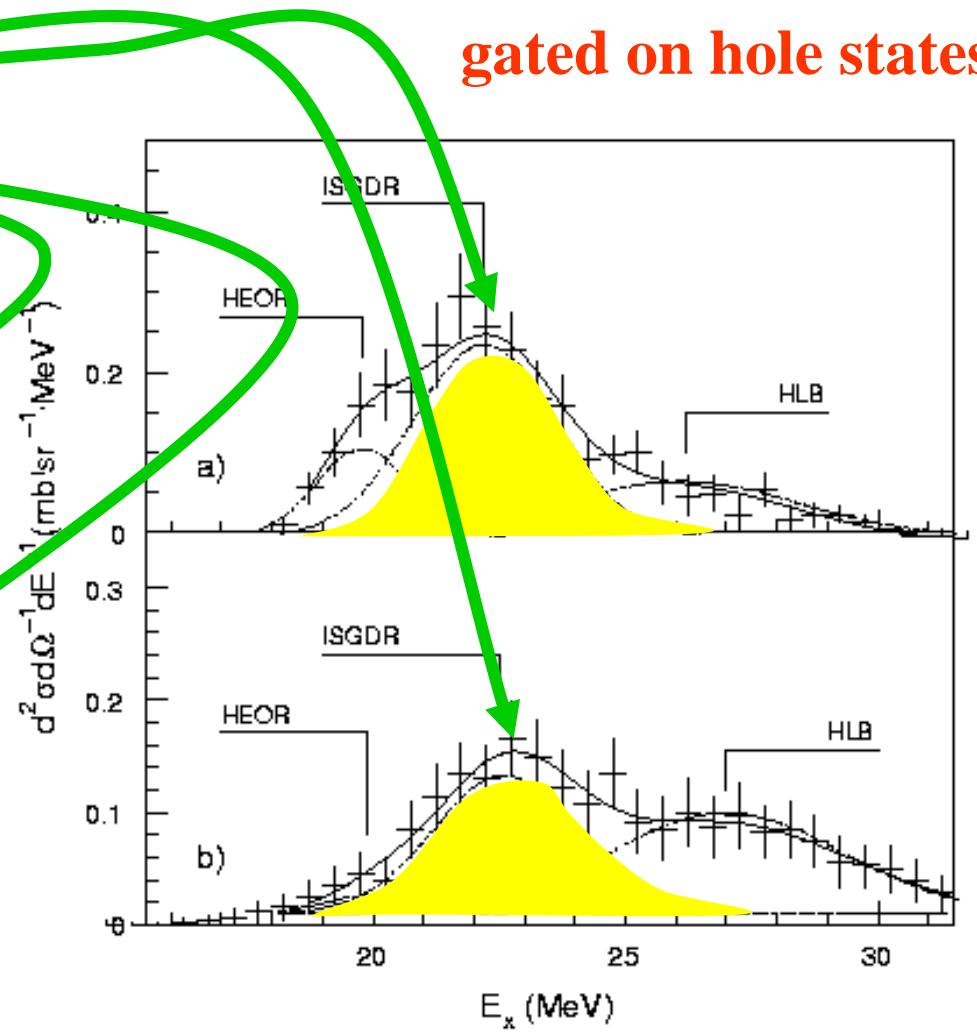
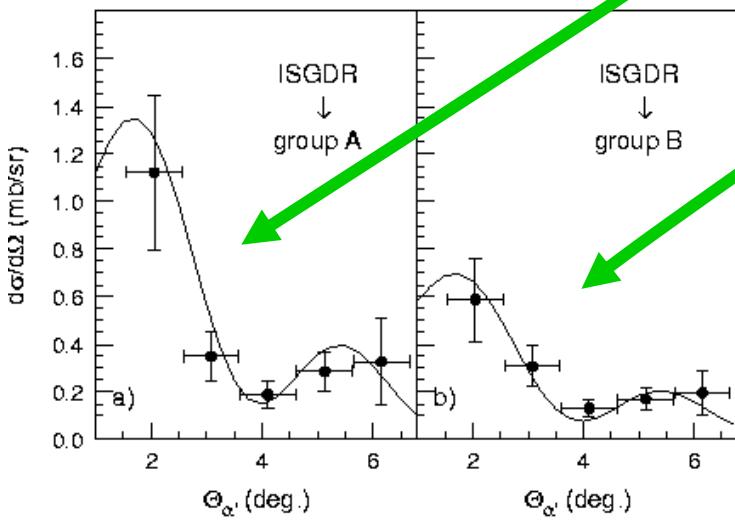
Branching ratios for decay



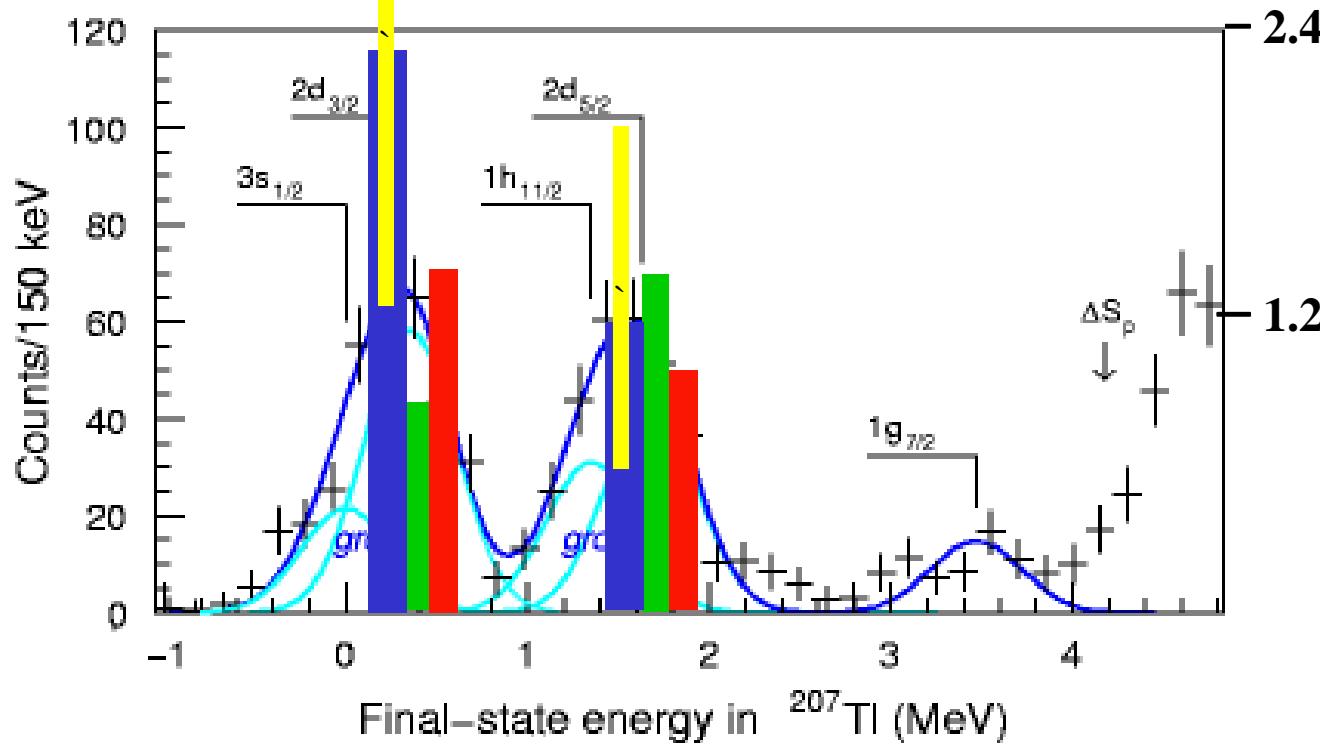
ISGDR in ^{208}Pb in p decay

$E_x = 22.1 \pm 0.3 \text{ MeV}$
 $L = 1$ transition

gated on hole states



Branching ratios for decay



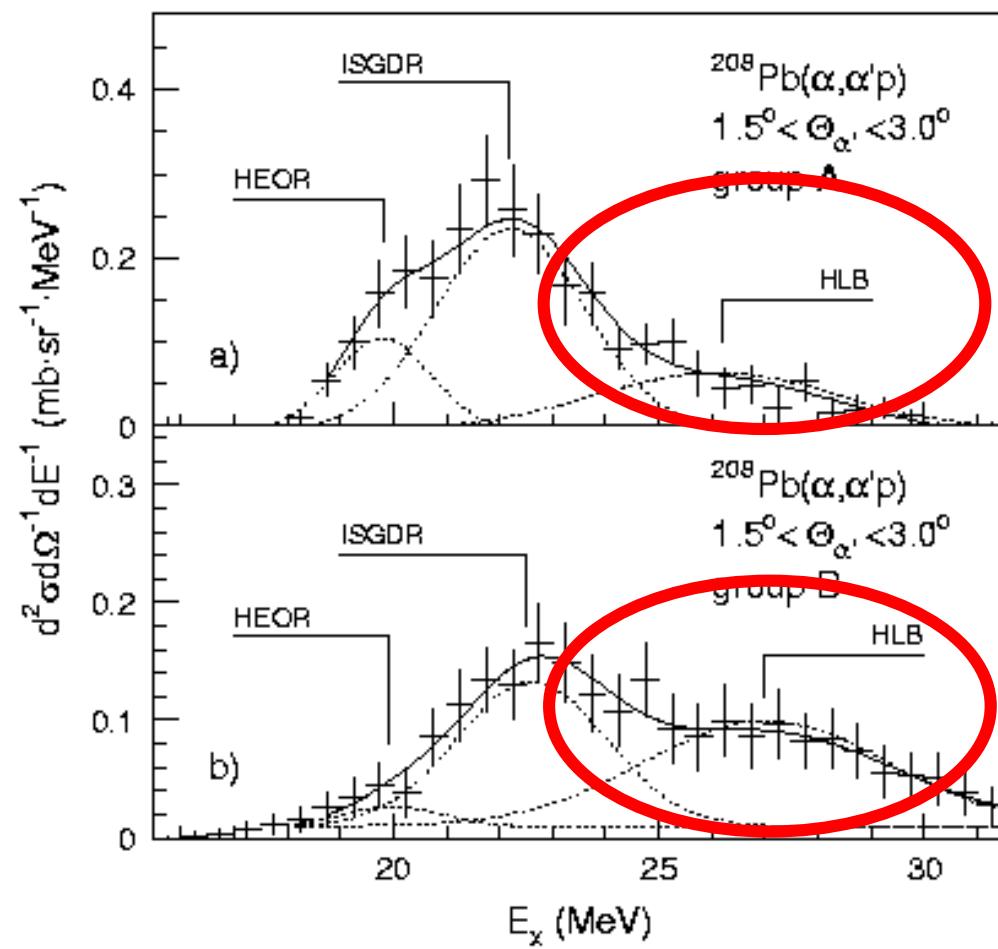
This work

M.L. Gorelik *et al.*,
PRC 62 (2000) 047301;
Continuum RPA;
Landau-Migdal
Parameters: f^{ex}, f' ;
Smearing parameter
Δ energy-dependent

M.L. Gorelik *et al.*, PRC 69 (2004) 054322

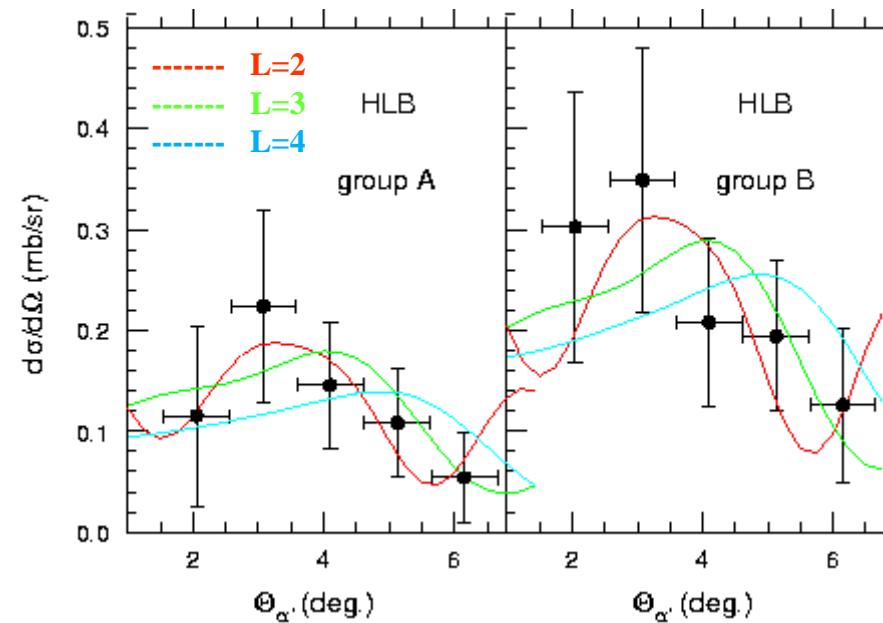
$1/2^+ + 3/2^+$	2.6%	(S~0.56) 1.45%	2.3 ± 1.1
$1/2^- + 5/2^+$	1.9%	(S~0.56) 1.04%	1.2 ± 0.7

Overtone of the ISGQR? [r^4Y_2]

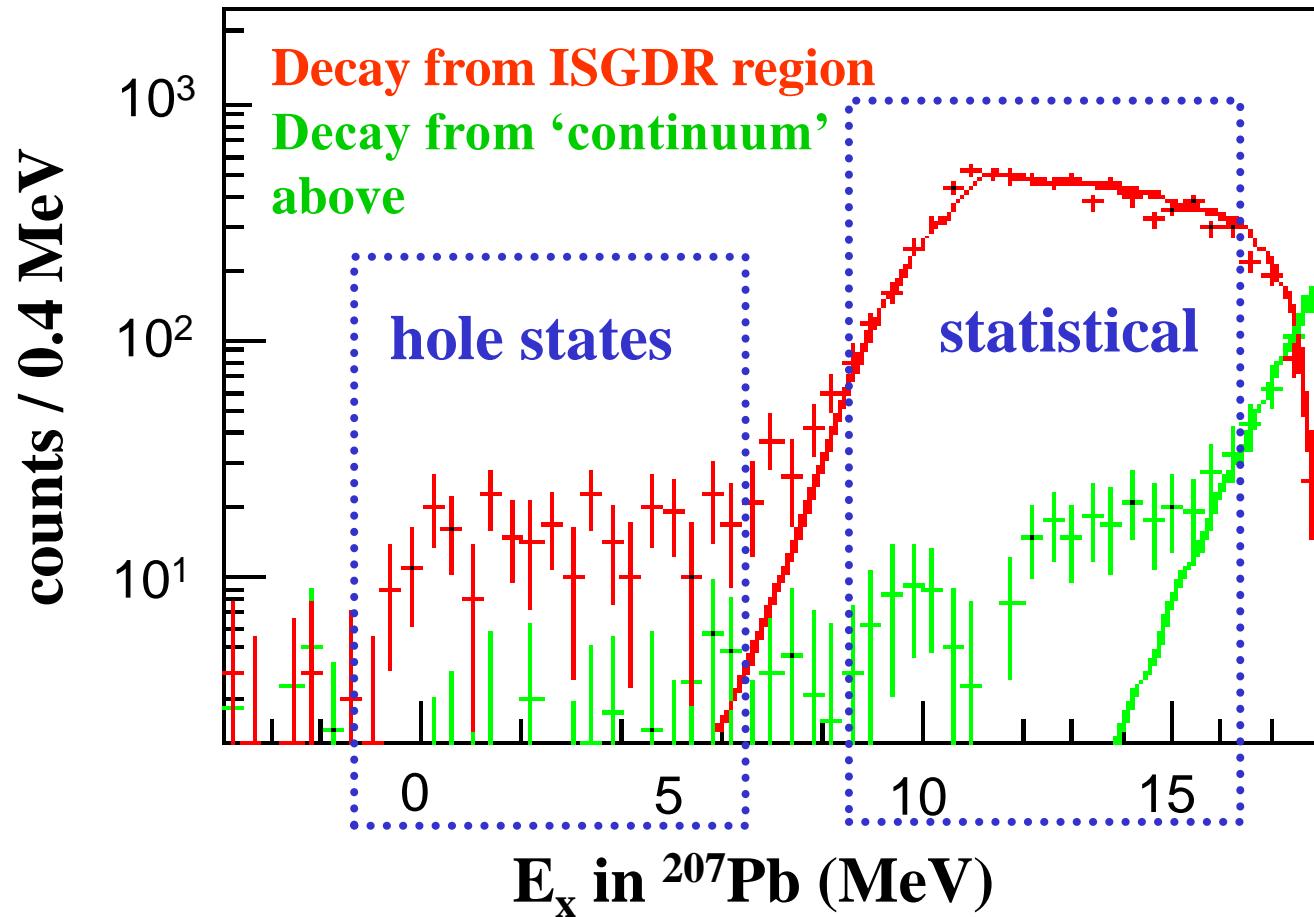


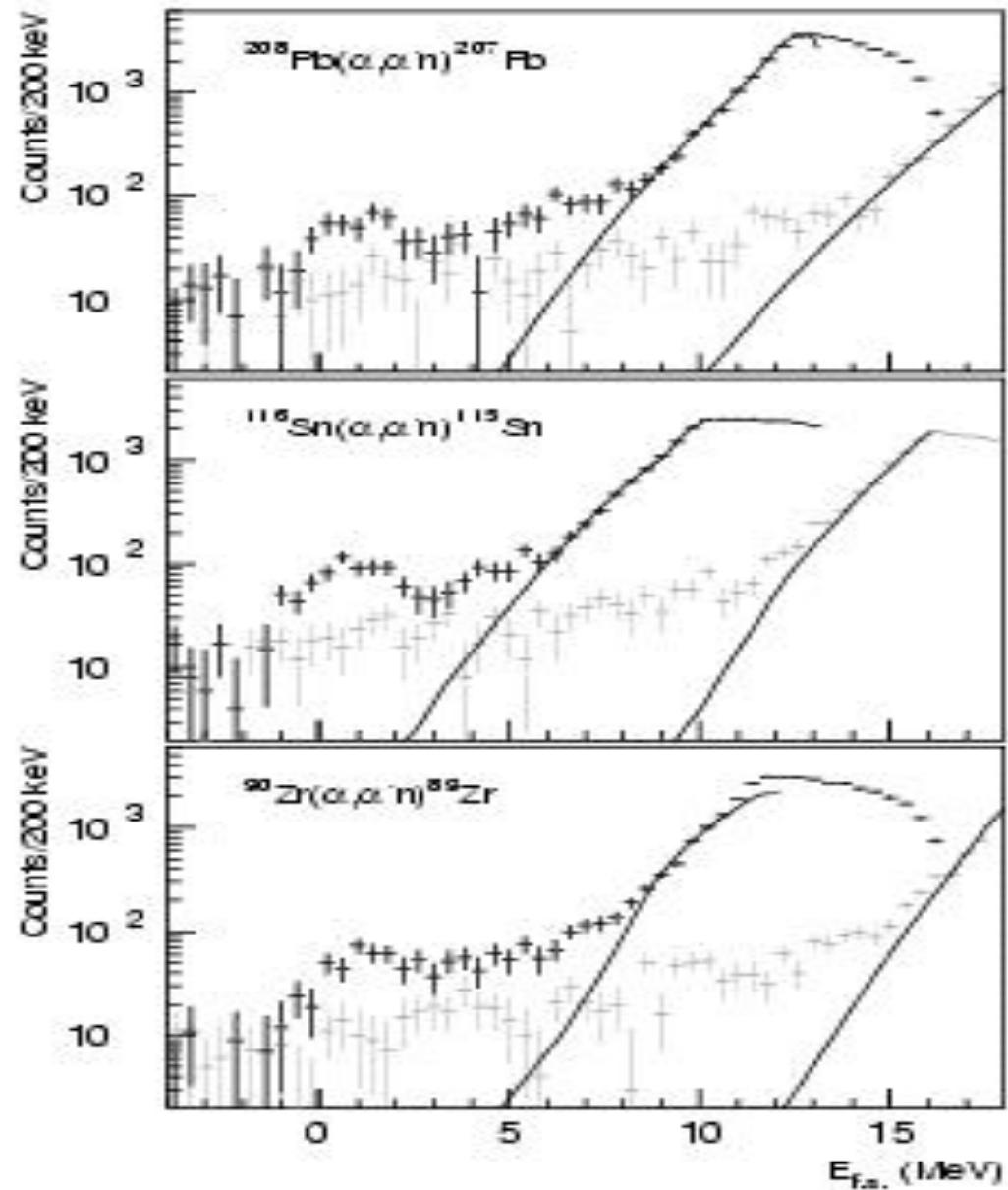
$$E_x = 26.9 \pm 0.7 \text{ MeV}$$

Muraviev and Urin
Bull. Acad. Sci. USSR
Phys. Ser. 52 (1988) 123
 $E_x = 28.3 \text{ MeV}$



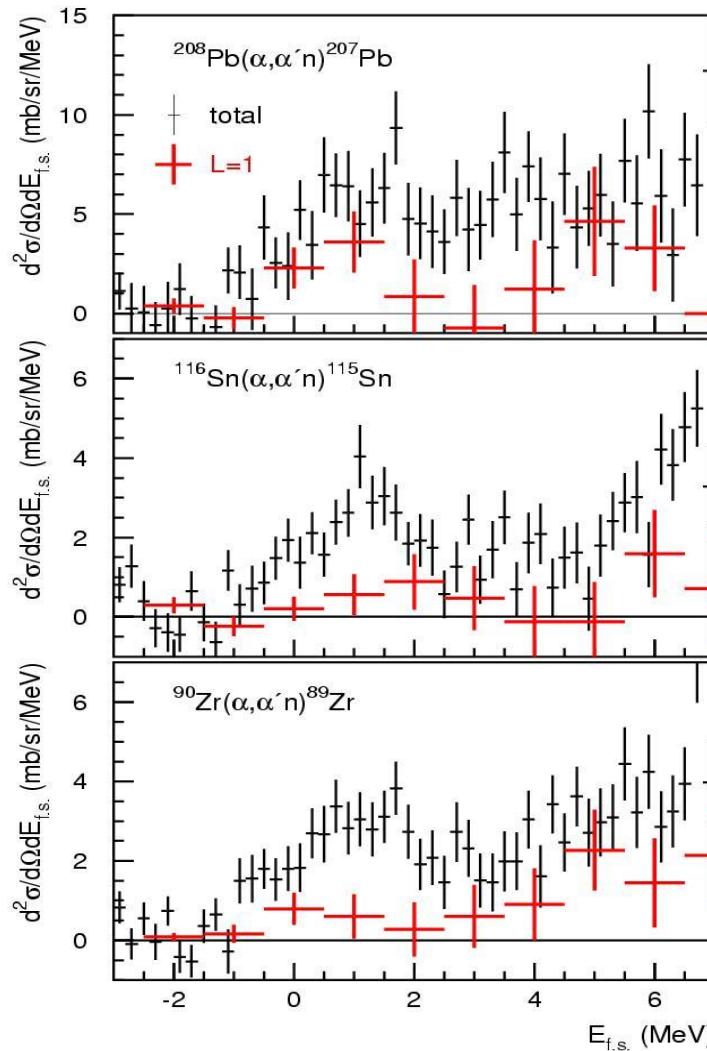
$^{208}\text{Pb}(\alpha, \alpha')$ followed by n decay





Branching ratios for the direct neutron-decay channel

From the simplified
MDA of angular
distributions



Br (Exp.)

Br (CRPA)

$10.5 \pm 5.6 \%$
 11.46%

$5.1 \pm 0.7 \%$
 10.85%

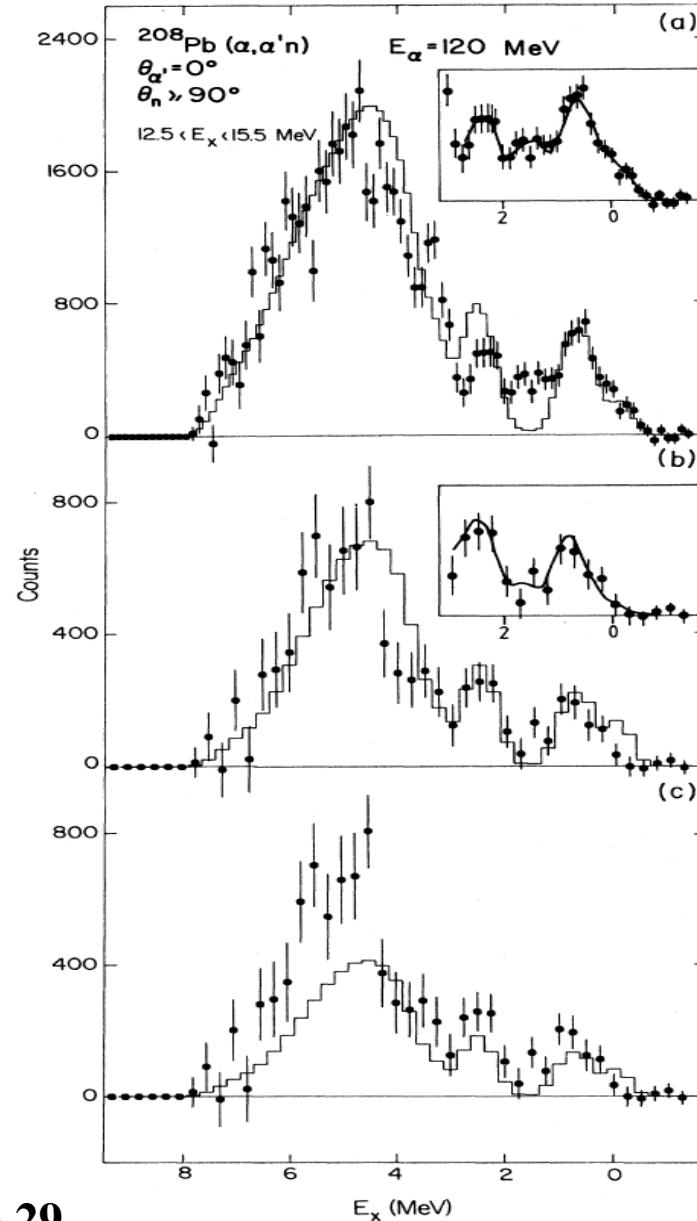
$4.8 \pm 0.9 \%$
 16.8%

Final-state spectra in ^{207}Pb obtained from neutron decay of

- (a) continuum underlying ISGMR in ^{208}Pb and
- (b and c) ISGMR proper.
- (b) Fit with 100% statistical
- (c) Fit with 60% statistical

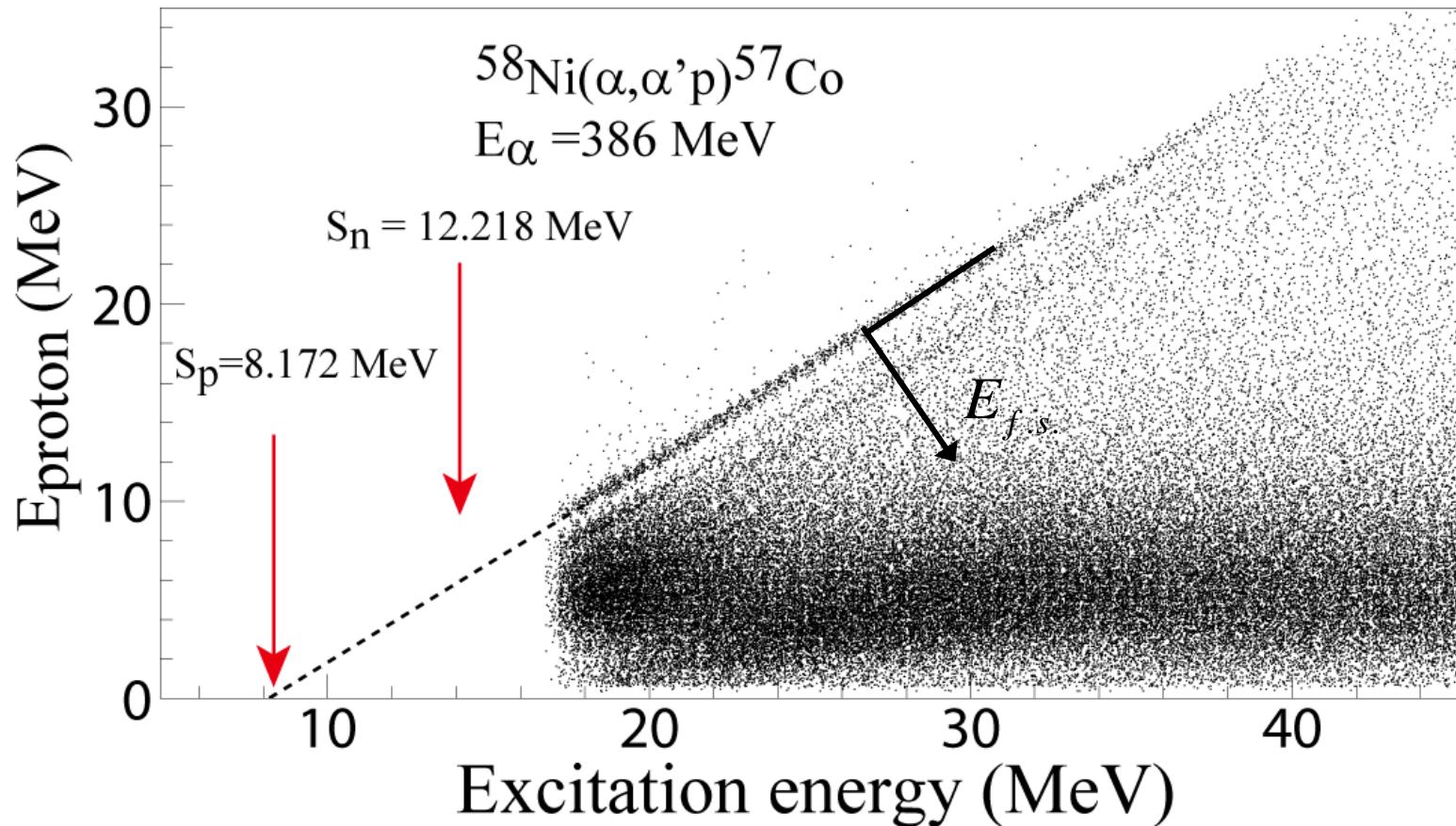
l_j	E_x (MeV)	Γ_j^{\dagger} (keV), expt.	Γ_j^{\dagger} (keV), theory
$p_{1/2}$	0	140 ± 35	5
$t_{1/2}$	1.630		6
$f_{3/2}$	0.570	70 ± 15	92
$p_{3/2}$	0.890	50 ± 10	8
$f_{7/2}$	2.340	165 ± 40	174

$\Gamma_{tot} = 2.9 \text{ MeV}; \Gamma^{\dagger} = 425 \text{ keV}$
 $\approx 15\% \text{ Direct decay}$



S. Brandenburg *et al.*, Nucl. Phys. A466 (1987) 29

Data analysis: Proton decay



Final-state energy

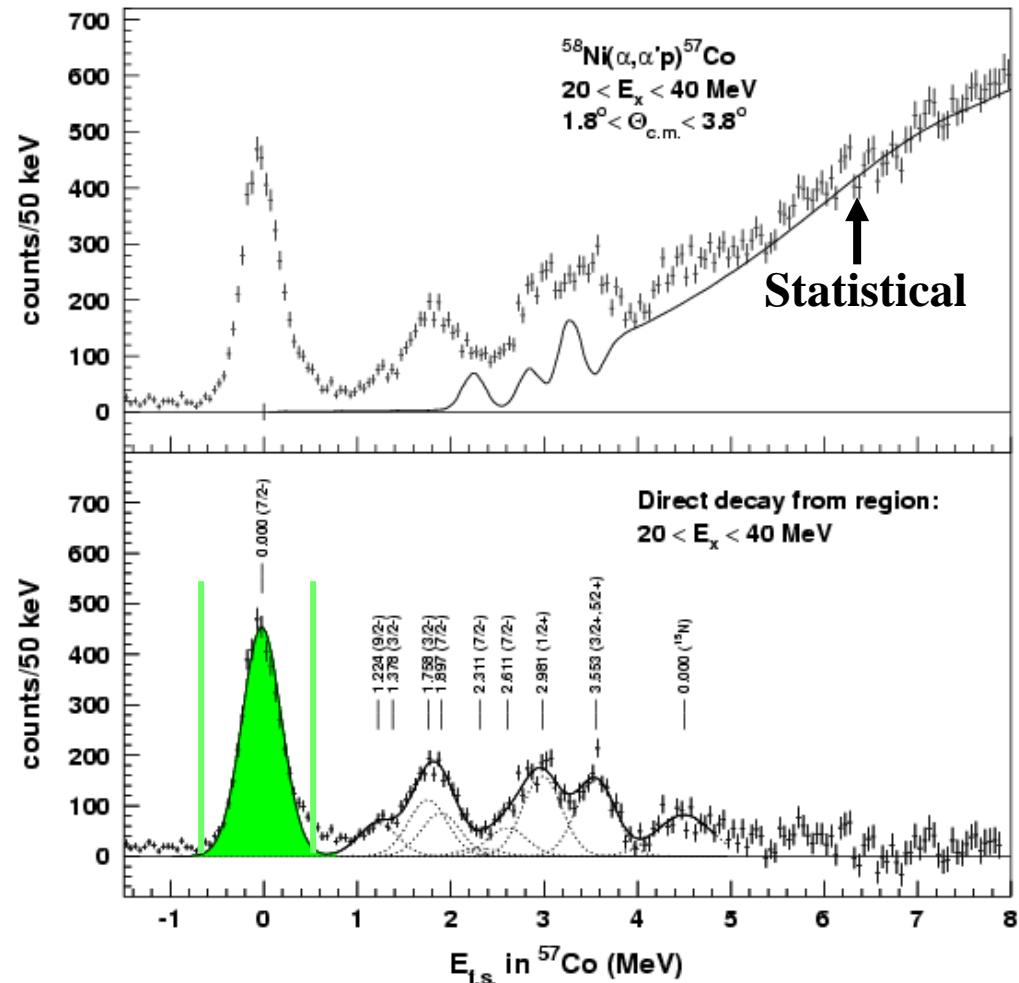
$$E_{f.s.} = E_X - E_p - S_p$$

Experimental results

M. Hunyadi *et al.*, Phys. Rev. C 80 (2009) 044317

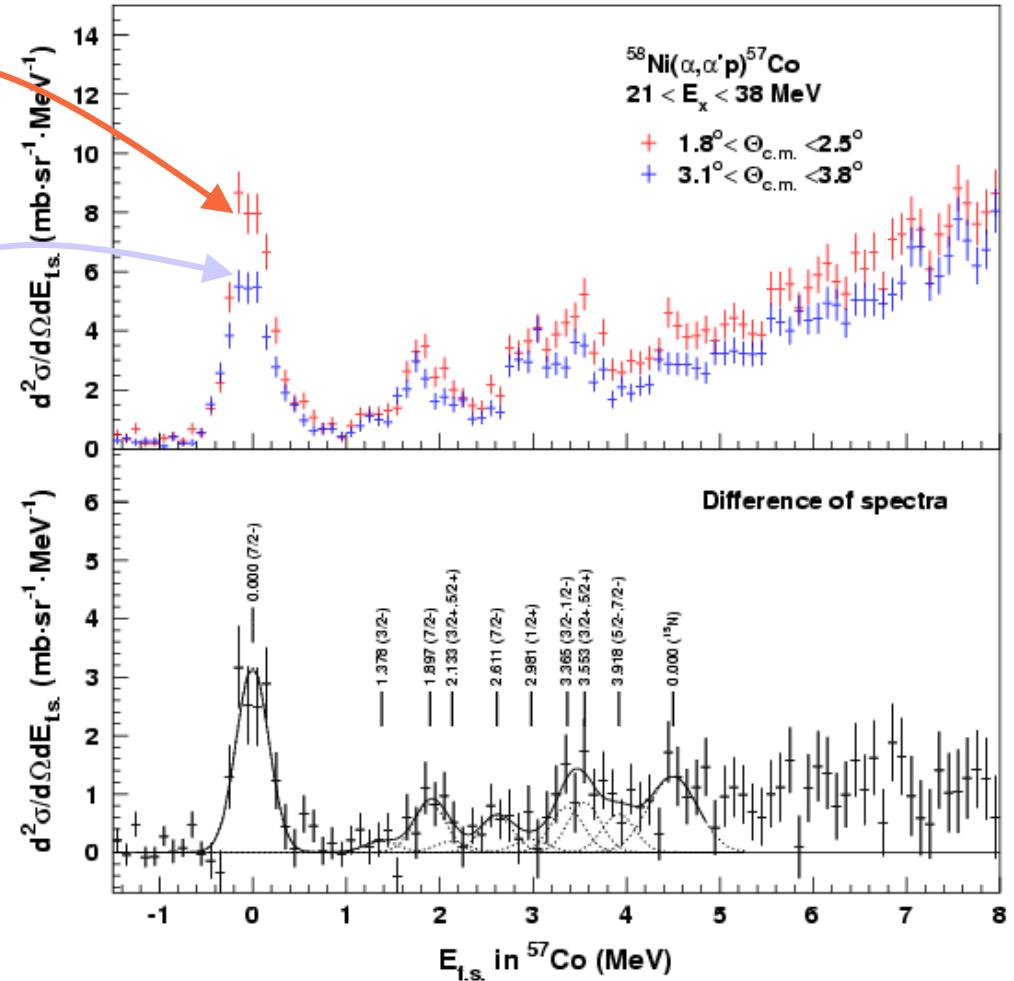
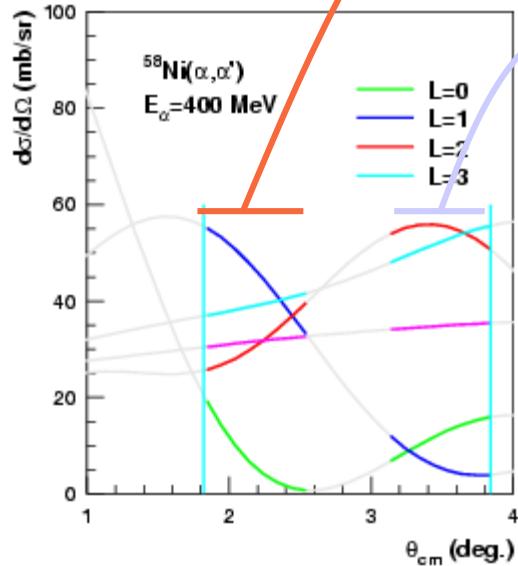
Final-state energy spectra

Final-state energy spectra after subtracting statistical contribution

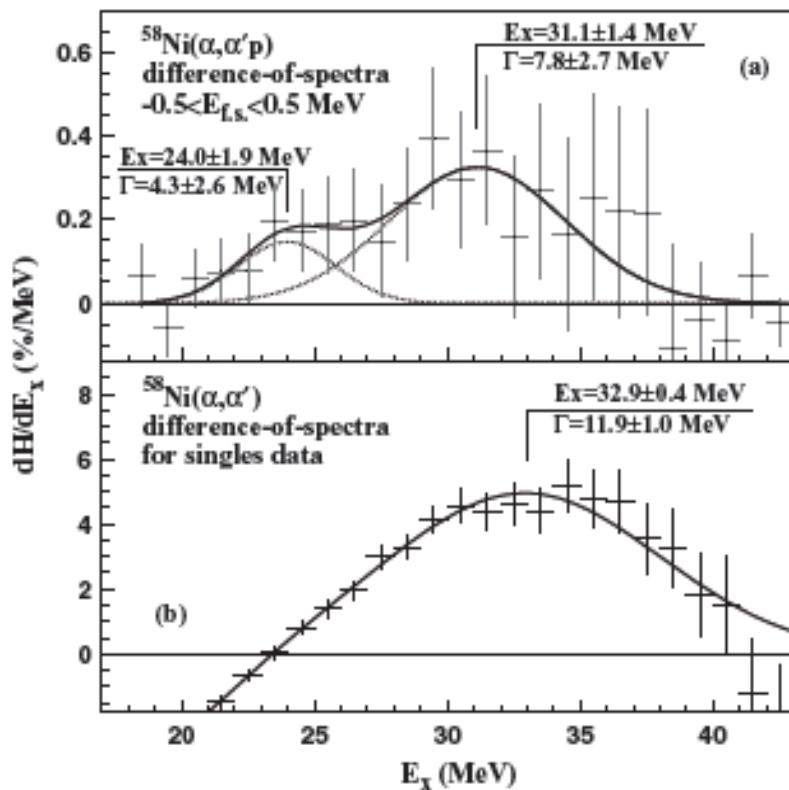


Experimental results

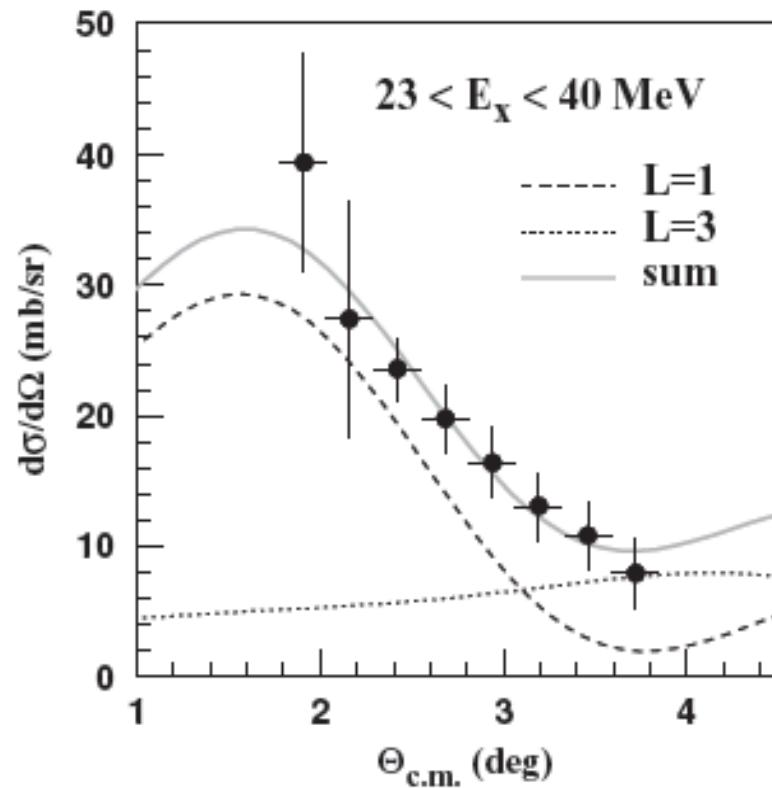
Difference of $E_{f.s.}$ -spectra



Strength distribution of ISGDR in ^{58}Ni



Spectra of $L = 1$ strengths obtained with DOS method in percentage of isoscalar EWSR; a) coincidence data gated on g.s. decay and b) singles data.



Differential cross section of resonance structure fitted with $L = 1$ and $L = 3$ DWBA calculations.

Proton-decay branching ratios Normalized to 100%

	Exp. (%) (24-38 MeV)	Cal. (%) (15-40 MeV)
$7/2^-$	61.3 (with $5/2^-$)	47
$3/2^-$	7.9	3.1
$3/2^-, 1/2^-$	9.9	2.2 (only for $1/2^-$)
$5/2^-$	3.2 ± 3.4	-
$1/2^+$	2.0 ± 4.2	13.4
$3/2^+, 5/2^+$	15.9	34.3
Σ	100 %	100%

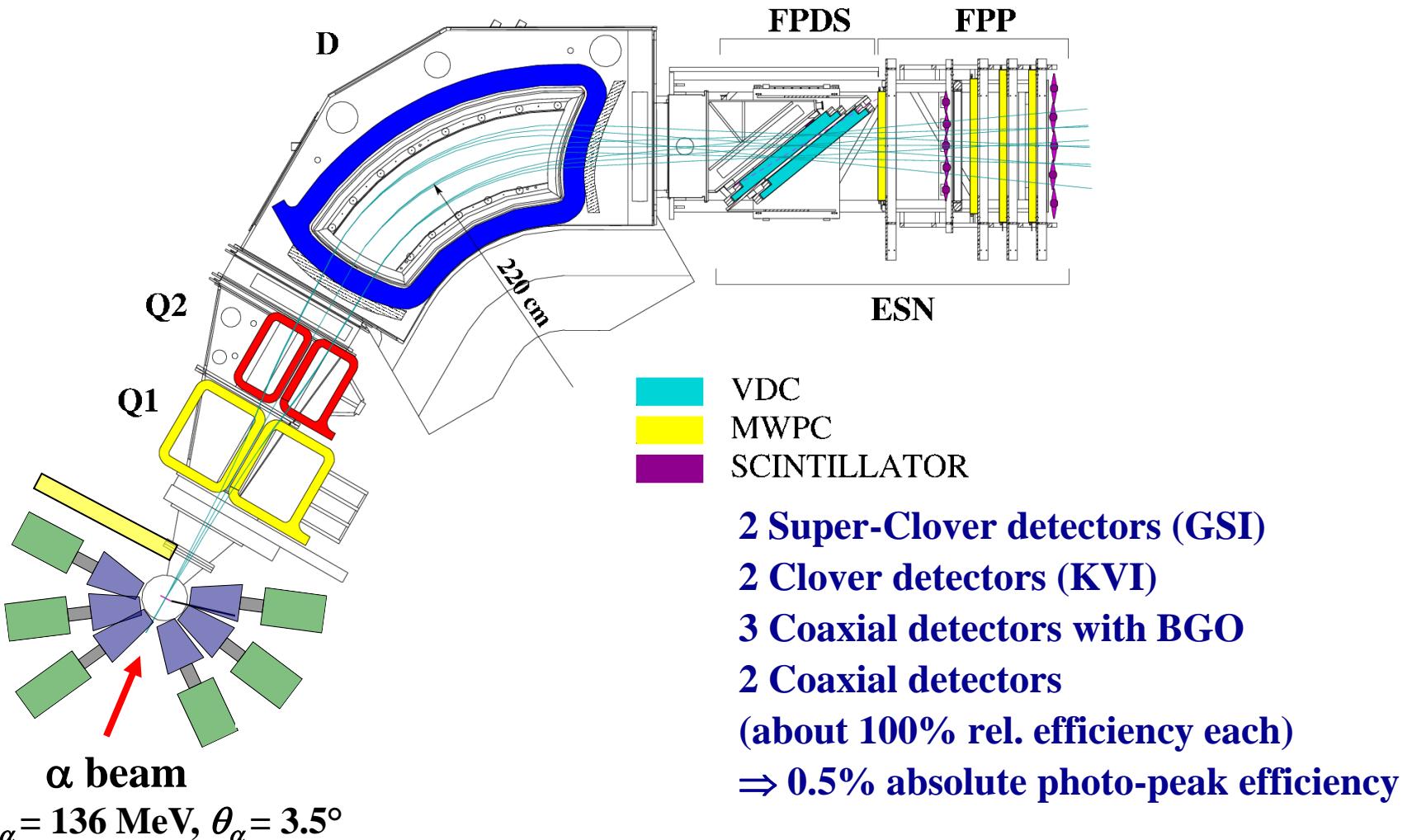
**Calculations: M.L. Goerlik, I.V. Safonov, and M.H. Urin,
Phys. Rev. C69 (2004) 054322**

Conclusions!

- There has been much progress in understanding ISGMR & ISGDR macroscopic properties
 - **Systematics:** E_x , Γ , %EWSR
 - ⇒ $K_{\text{nm}} \approx 240$ MeV
 - ⇒ $K_\tau \approx -500$ MeV
- Sn nuclei are softer than ^{208}Pb and ^{90}Zr .
- Recently, Microscopic Structure for a few nuclei
 - CRPA has some success in ^{208}Pb & ^{58}Ni but fails badly in ^{116}Sn & ^{90}Zr .
- Possible observation quadrupole compression mode, i.e. overtone of ISGQR

Gamma-Decay Neutron-Skin Thickness Pygmy Dipole Resonance

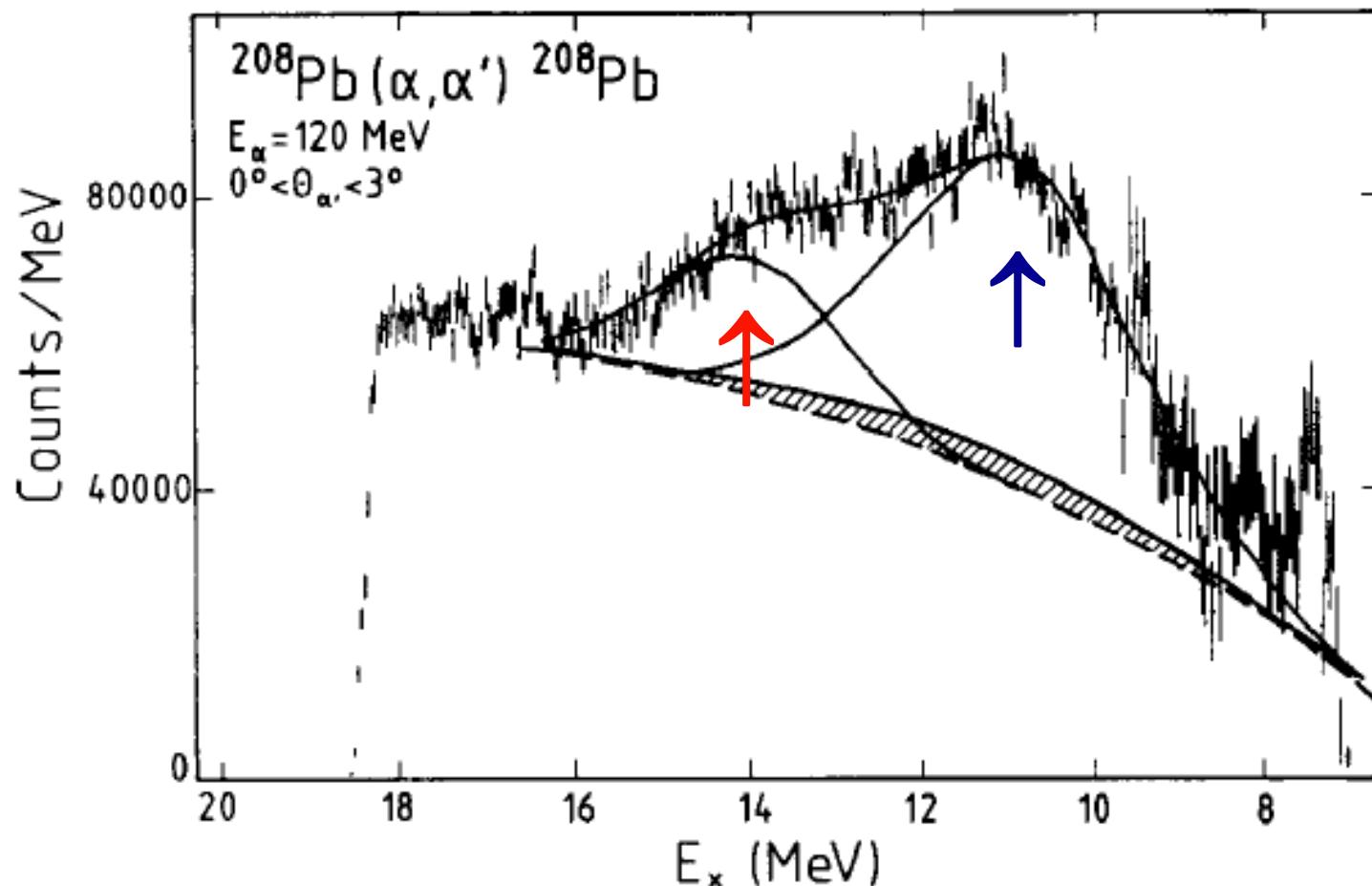
Setup at KVI

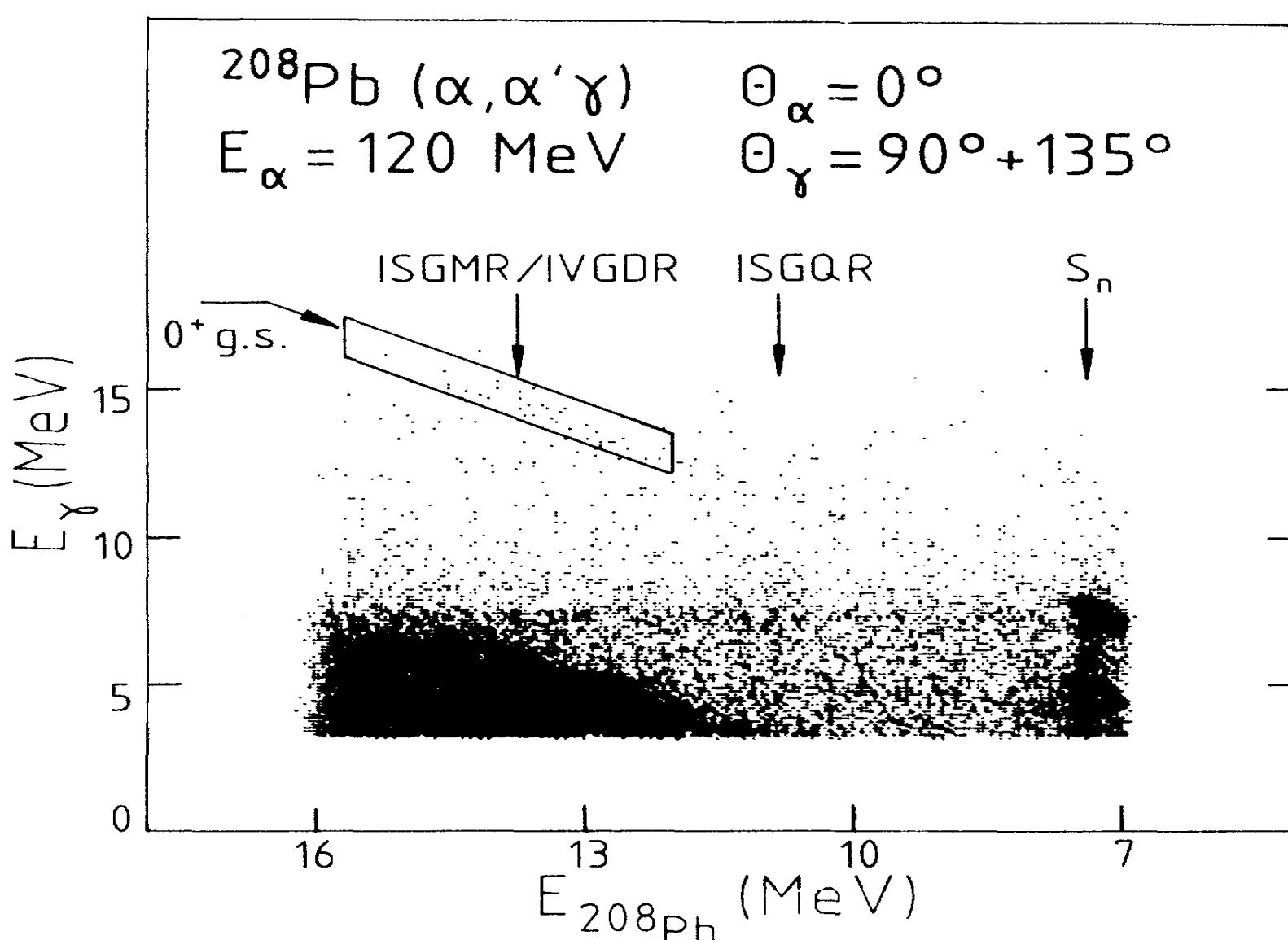


D. Savran *et al.*, Nucl. Inst. and Meth. Phys. Res. A 564 (2006) 267

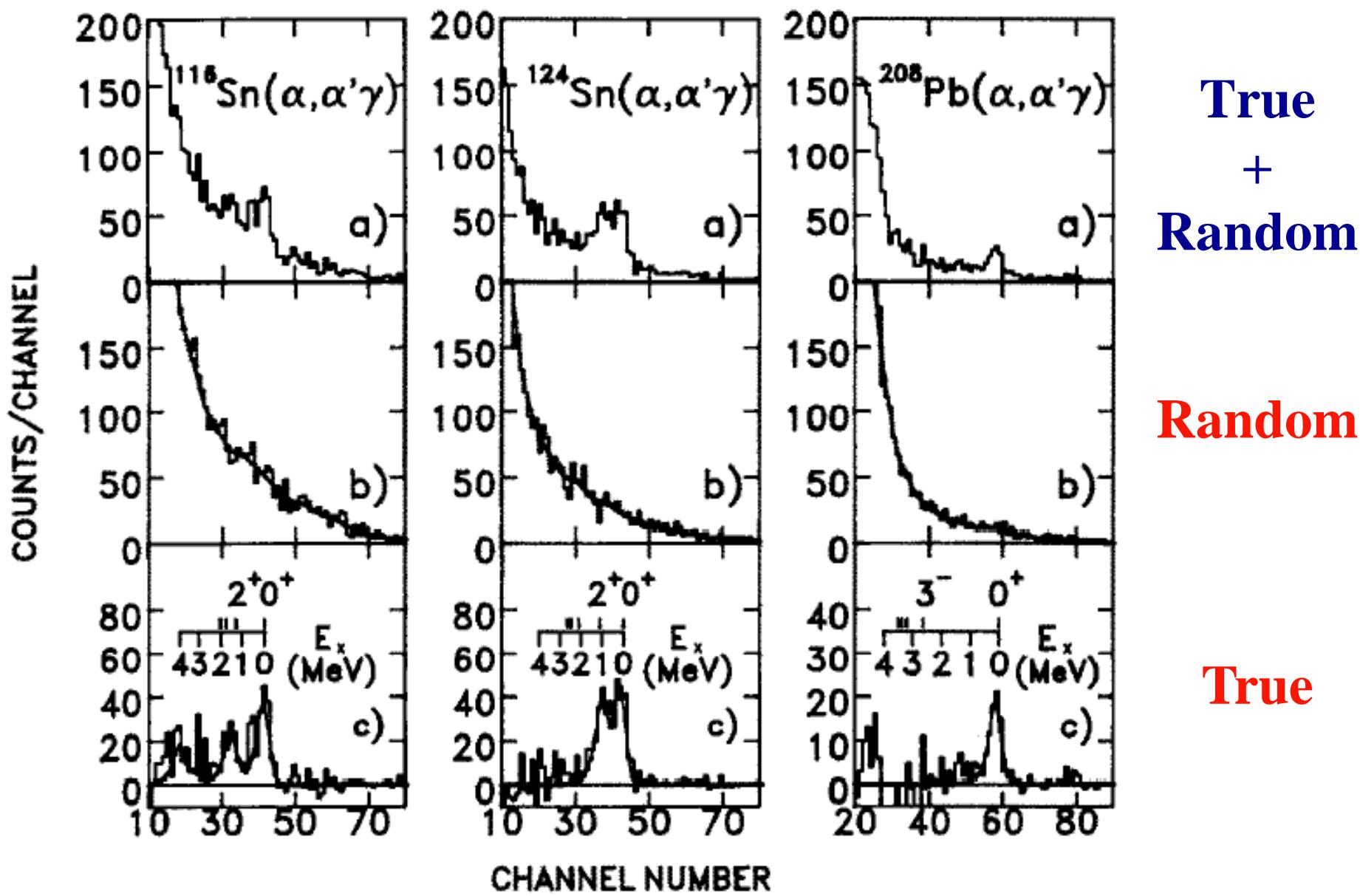
ISGQR at 10.8 MeV
ISGMR at 13.8 MeV

Hatched area \Rightarrow IVGDR contribution (Coulomb + nuclear)





Two-dimensional spectrum showing inelastic α -scattering in coincidence with γ -decay



A. Krasznahorkay et al., Phys. Rev. Lett. 66 (1991) 1287

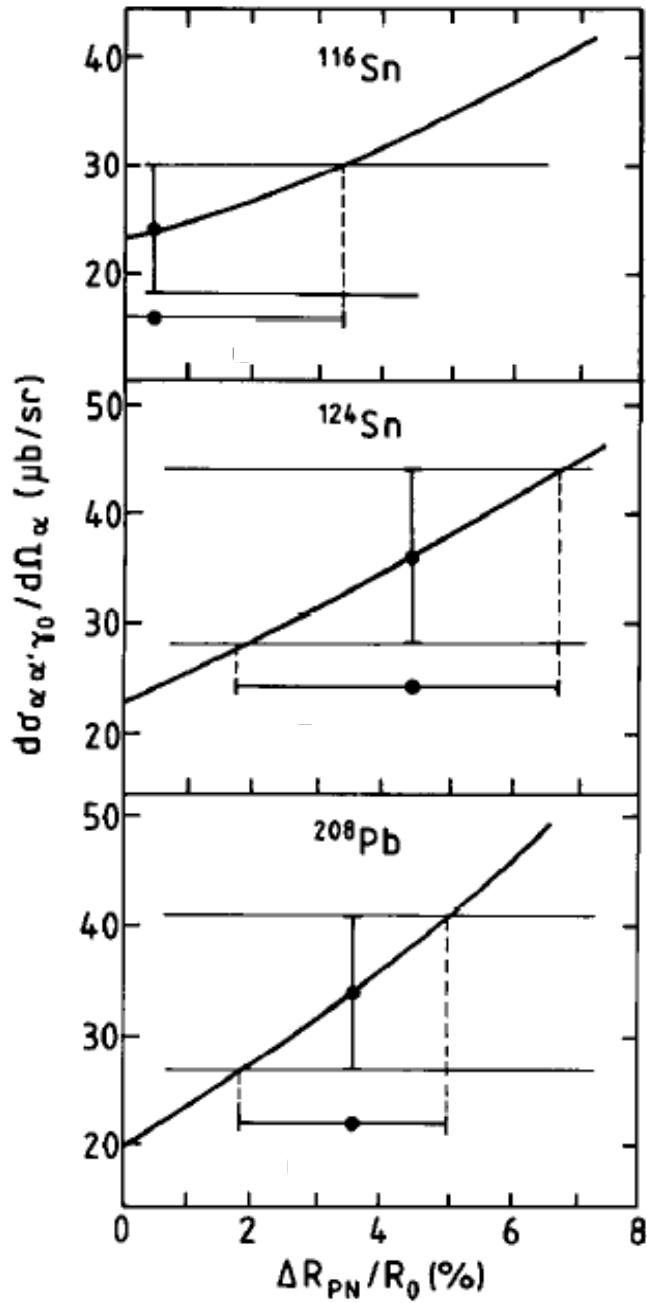
Isoscalar transition density in the Goldhaber-Teller model for excitation of IVGDR in inelastic α -scattering.

$$g_1^{10}(r) = g_1^n(r) - g_1^p(r) = \alpha_1 \gamma \left(\frac{N - Z}{A} \right) \left(\frac{d\rho(r)}{dr} + \frac{1}{3} c \frac{d^2\rho(r)}{dr^2} \right).$$

$$\frac{\Delta R_{\text{PN}}}{R_0} = \frac{R_n - R_p}{\frac{1}{2}(R_n + R_p)} = \gamma \frac{2(N - Z)}{3A}.$$

Here, γ is related to the proton and neutron central density distributions and thus to ΔR_{pn} . α_1 is deformation length obtained from TRK sum rule. Therefore, DWBA cross sections can be calculated as function of $\Delta R_{pn}/R_0$ for the Goldhaber-Teller model and similarly for the Steinwedel-Jensen model.

γ -decay branching ratios are known from photo-absorption experiments.

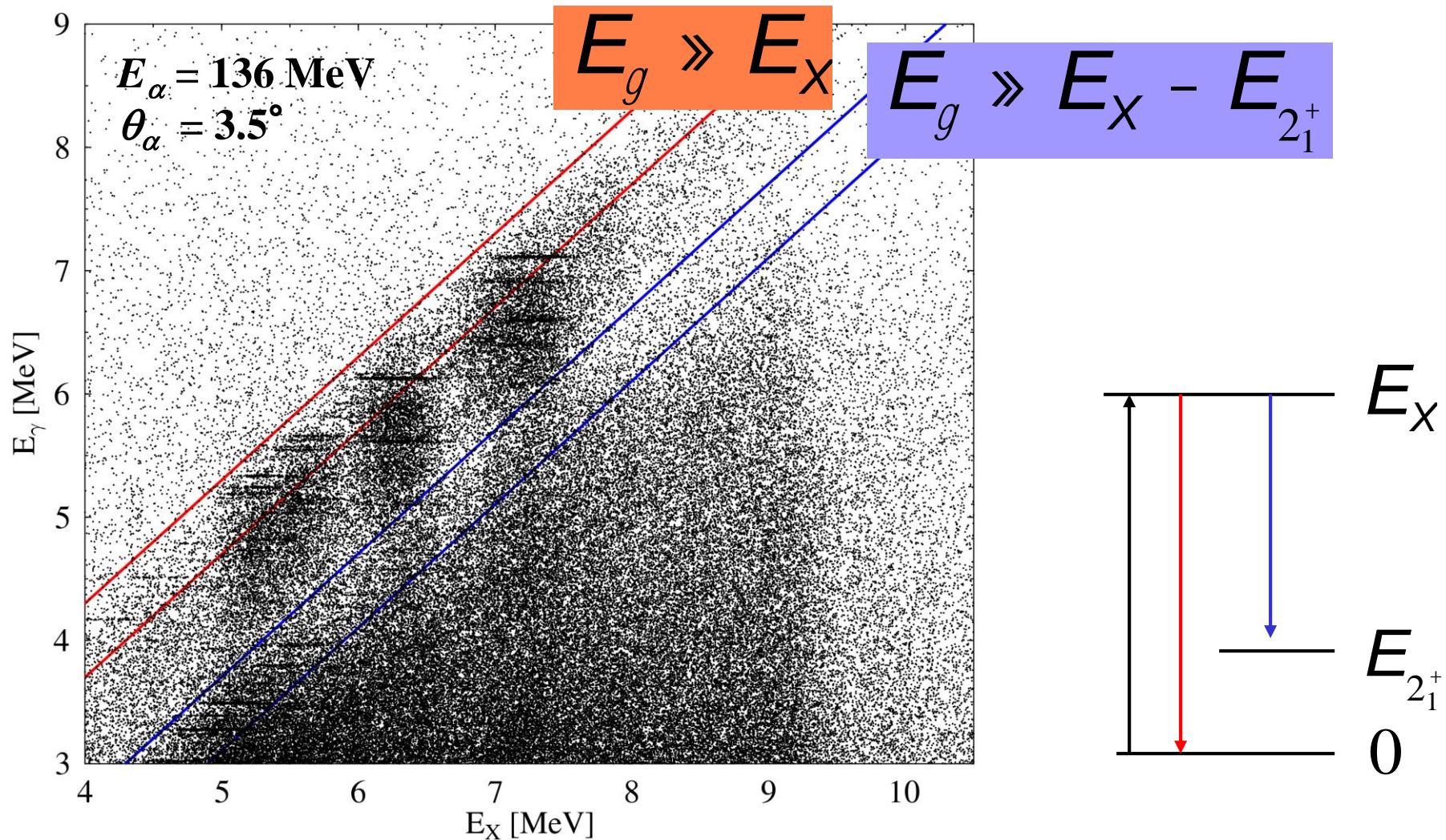


Full line is the calculated $\alpha\gamma_0$ coincidence cross section, averaged over the solid angle of the α -particle and integrated over the full γ -ray solid angle (4π) and over the ΔE energy range as function of $\Delta R_{pn}/R$.

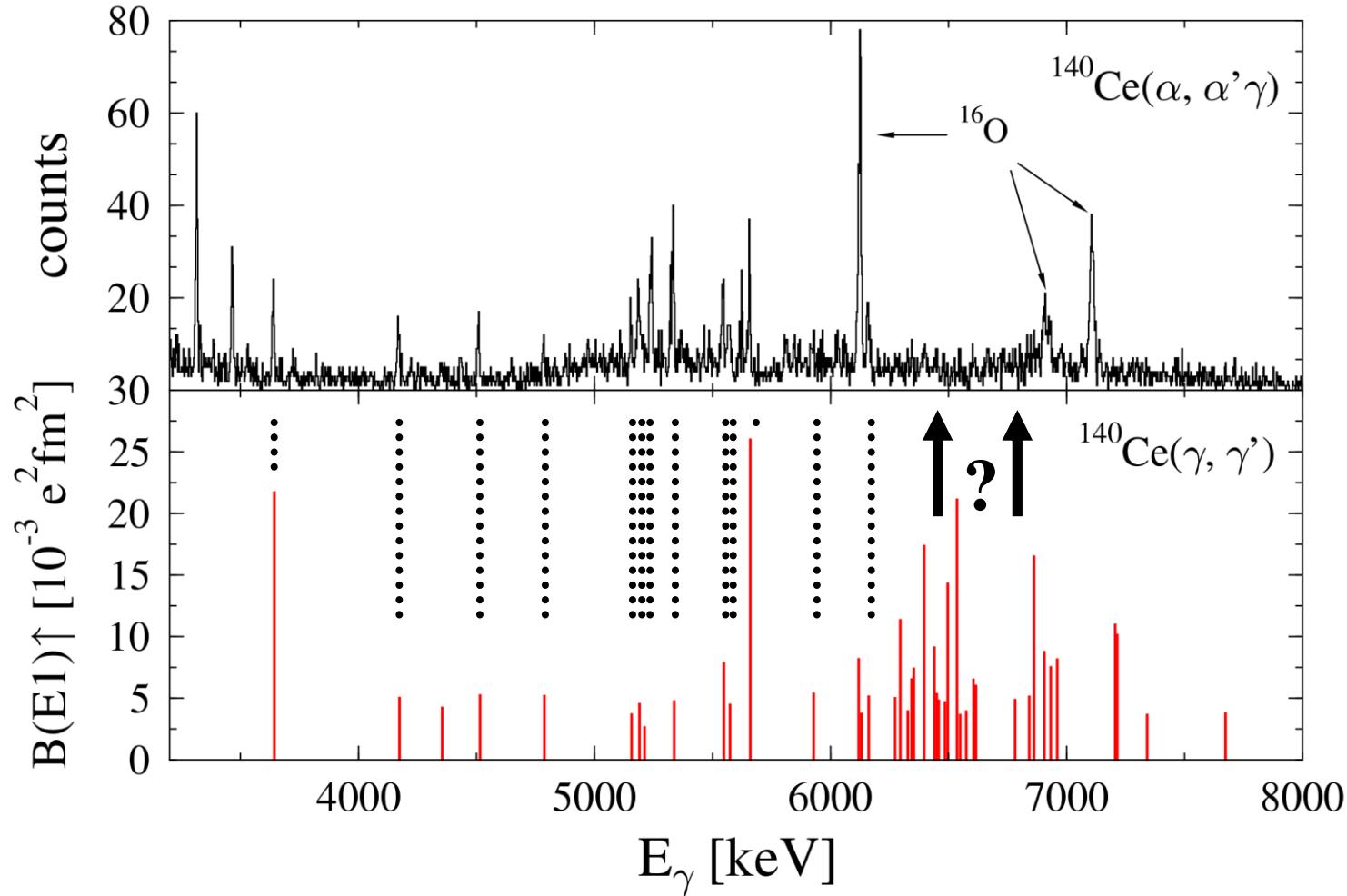
The experimental $\alpha\gamma_0$ cross sections for the IVGDR are shown as full circles with vertical error bars. The deduced values for $\Delta R_{pn}/R$ with the associated uncertainty (full circles with horizontal error bars) are also indicated.

Isotope	Present work $\Delta R_{PN}/R_0$ (%)	Present work ΔR_{PN} (fm)	Batty et al. [2] ΔR_{PN} (fm)	Angeli et al. [6] ΔR_{PN} (fm)
^{116}Sn	0.5 ± 2.7	0.02 ± 0.12	0.15 ± 0.05	0.13
^{124}Sn	4.4 ± 2.4	0.21 ± 0.11	0.25 ± 0.05	0.22
^{208}Pb	$3.5^{+1.5}_{-1.6}$	0.19 ± 0.09	0.14 ± 0.04	0.22

$^{140}\text{Ce}(\alpha, \alpha'\gamma)$ - coincidence matrix

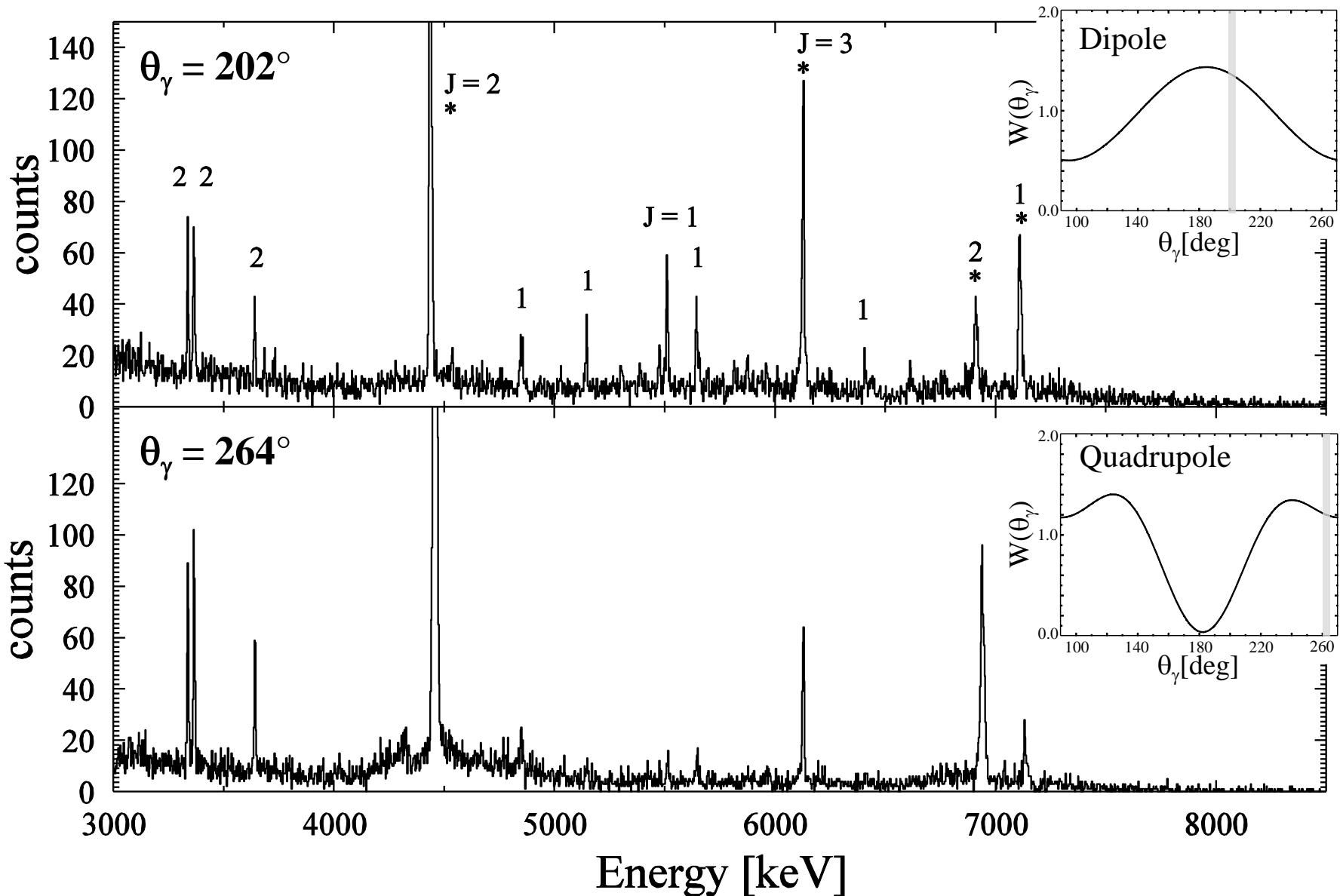


$^{140}\text{Ce}(\alpha, \alpha'\gamma)$ vs. $^{140}\text{Ce}(\gamma, \gamma')$

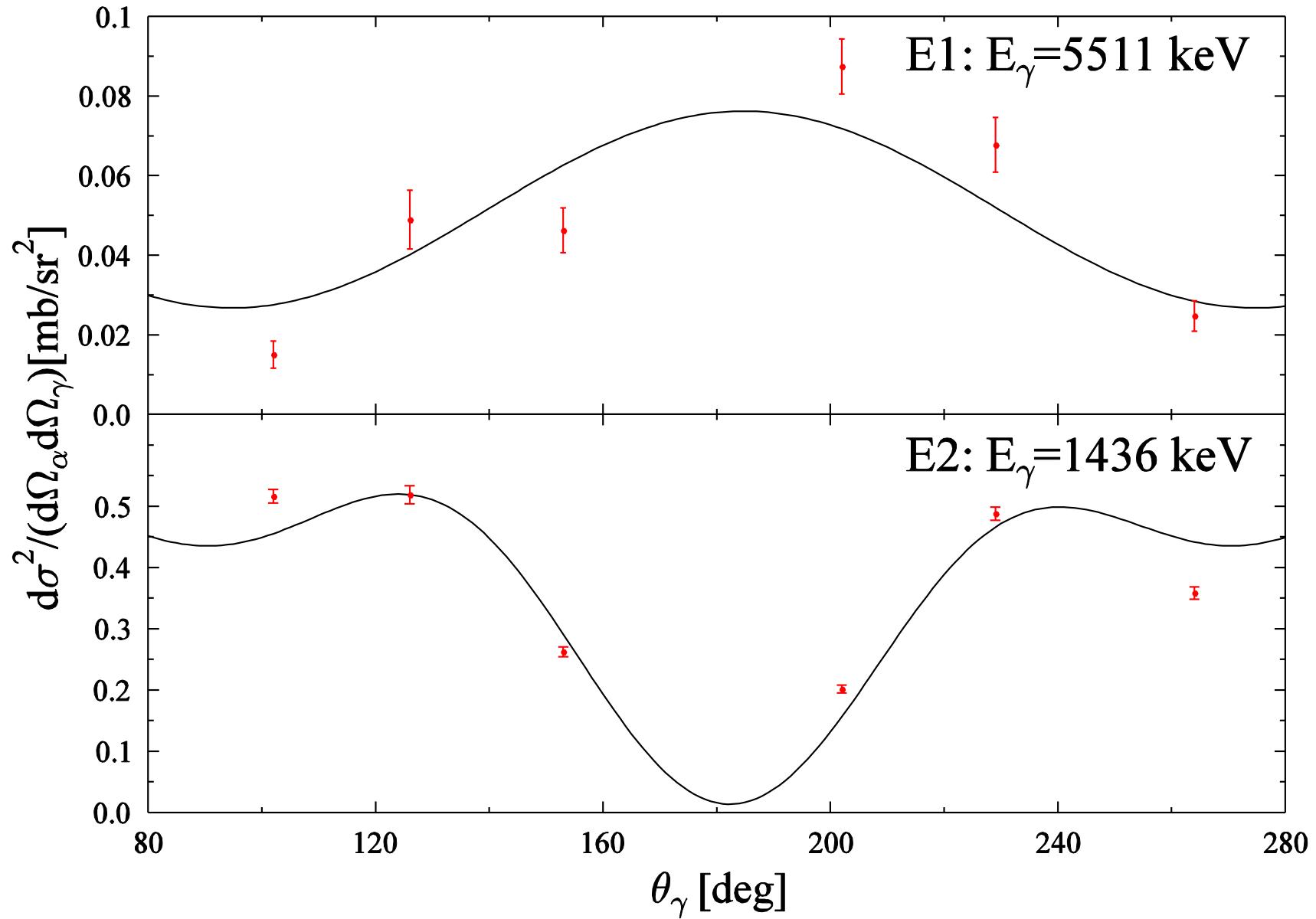


D. Savran *et al.*, Phys. Rev. Lett. 97 (2006) 172502

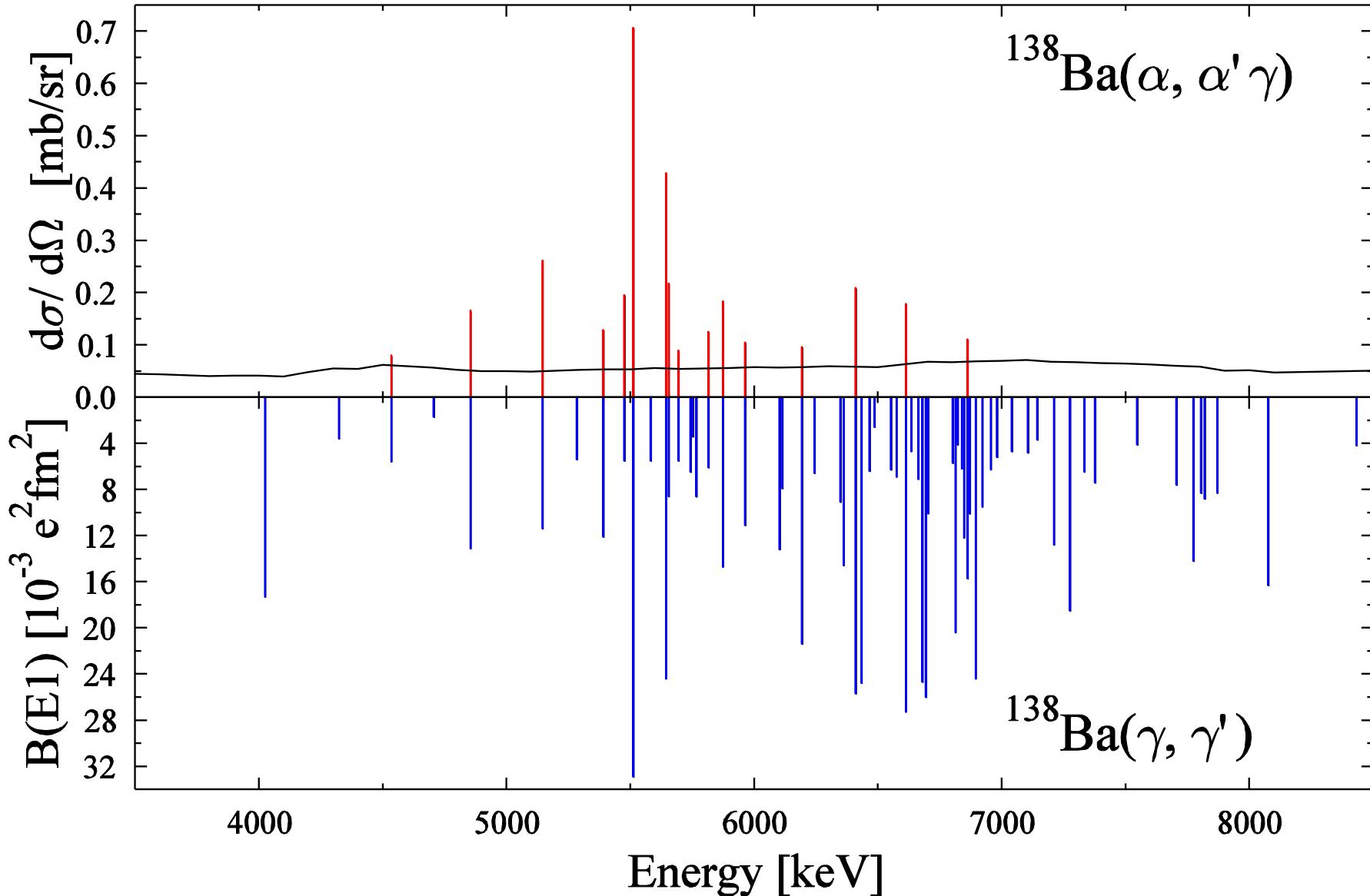
Multipole assignment with α - γ angular correlation



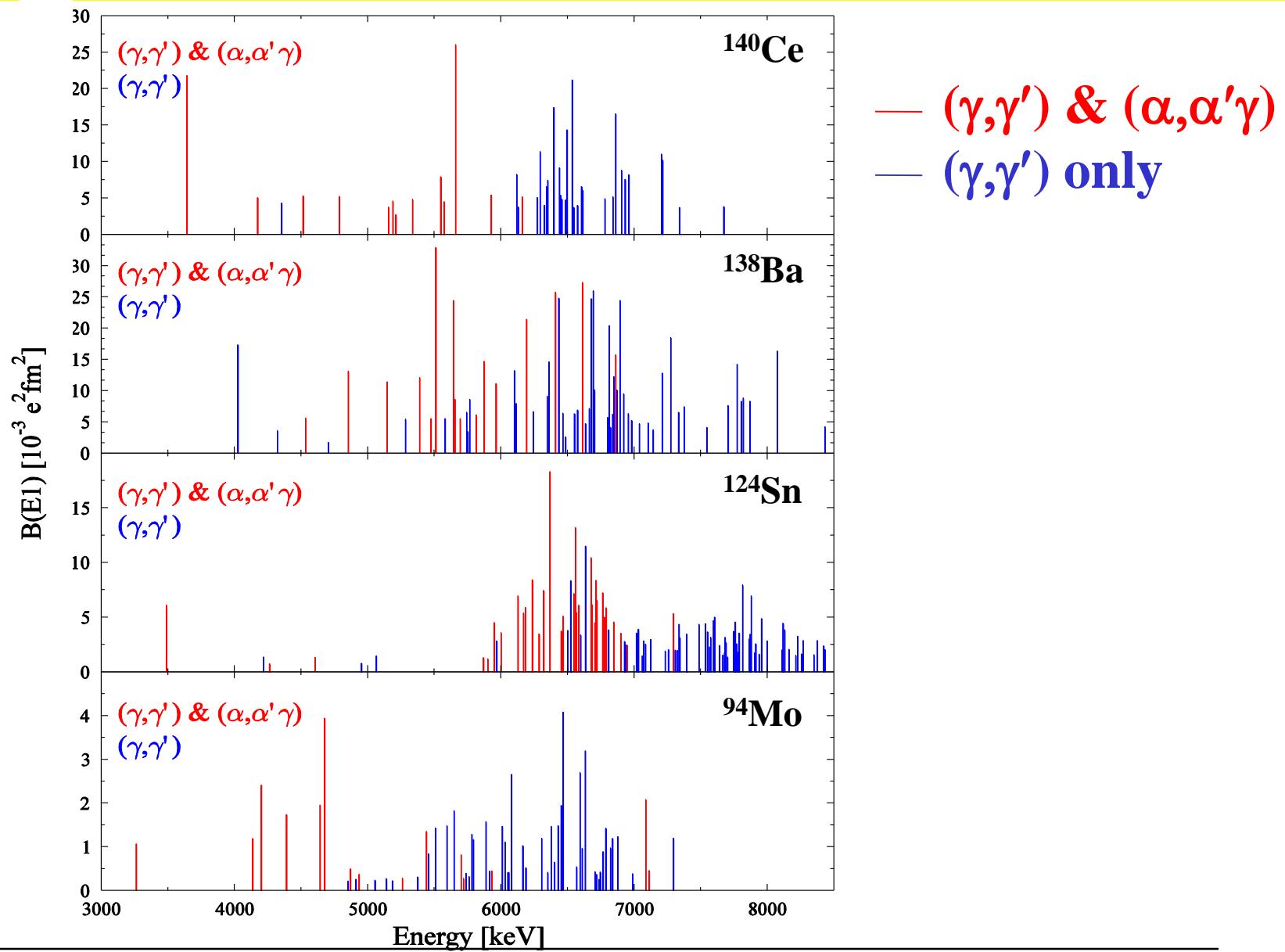
Multipole assignment with α - γ angular correlation



Comparison of $(\alpha, \alpha'\gamma)$ with (γ, γ') on ^{138}Ba

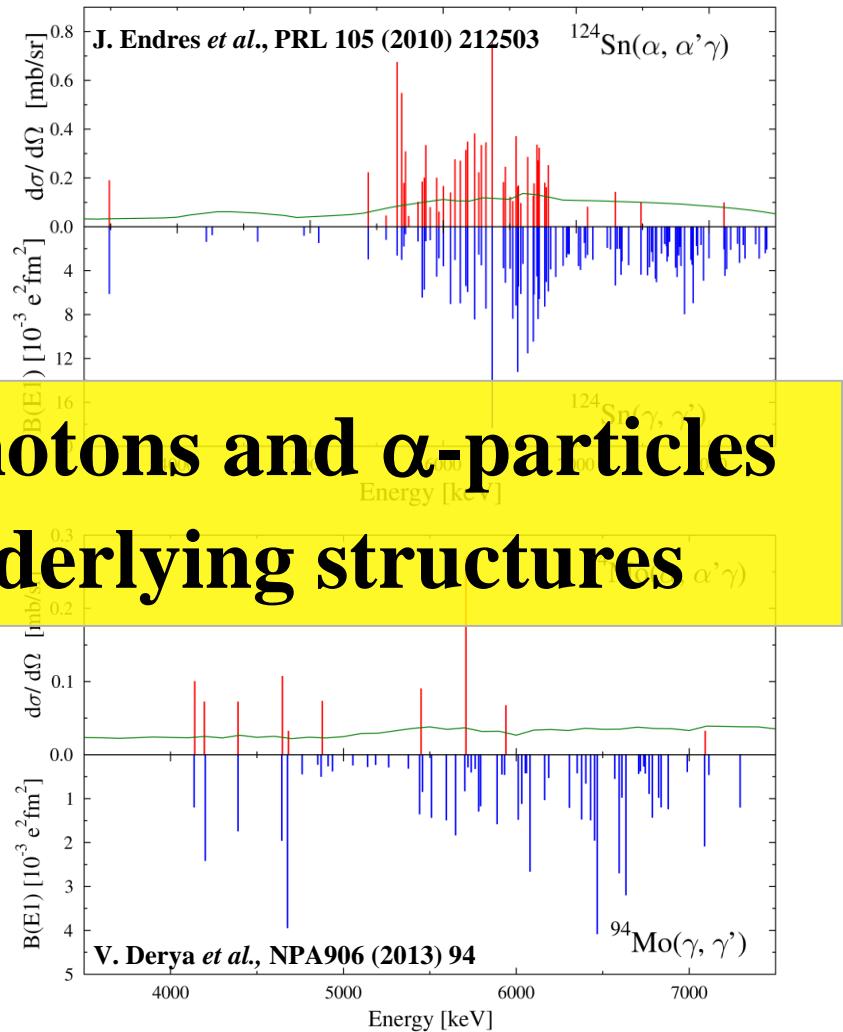
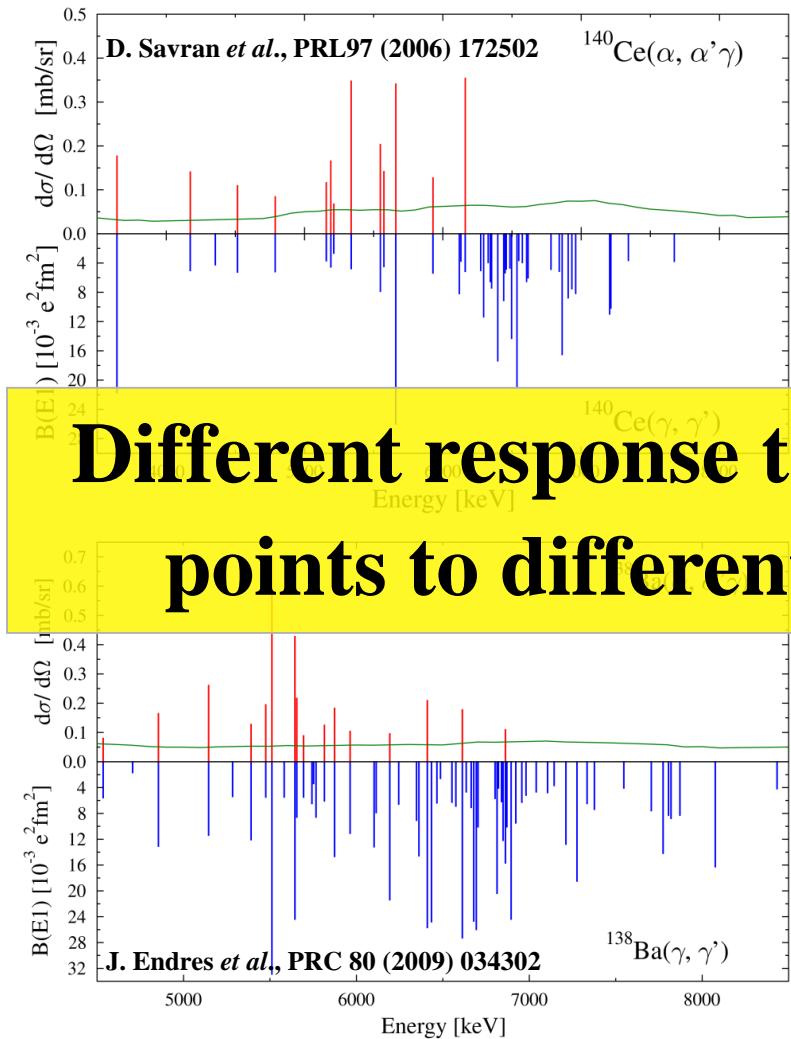


E1 strength distribution in ^{140}Ce , ^{138}Ba , ^{124}Sn , and ^{94}Mo



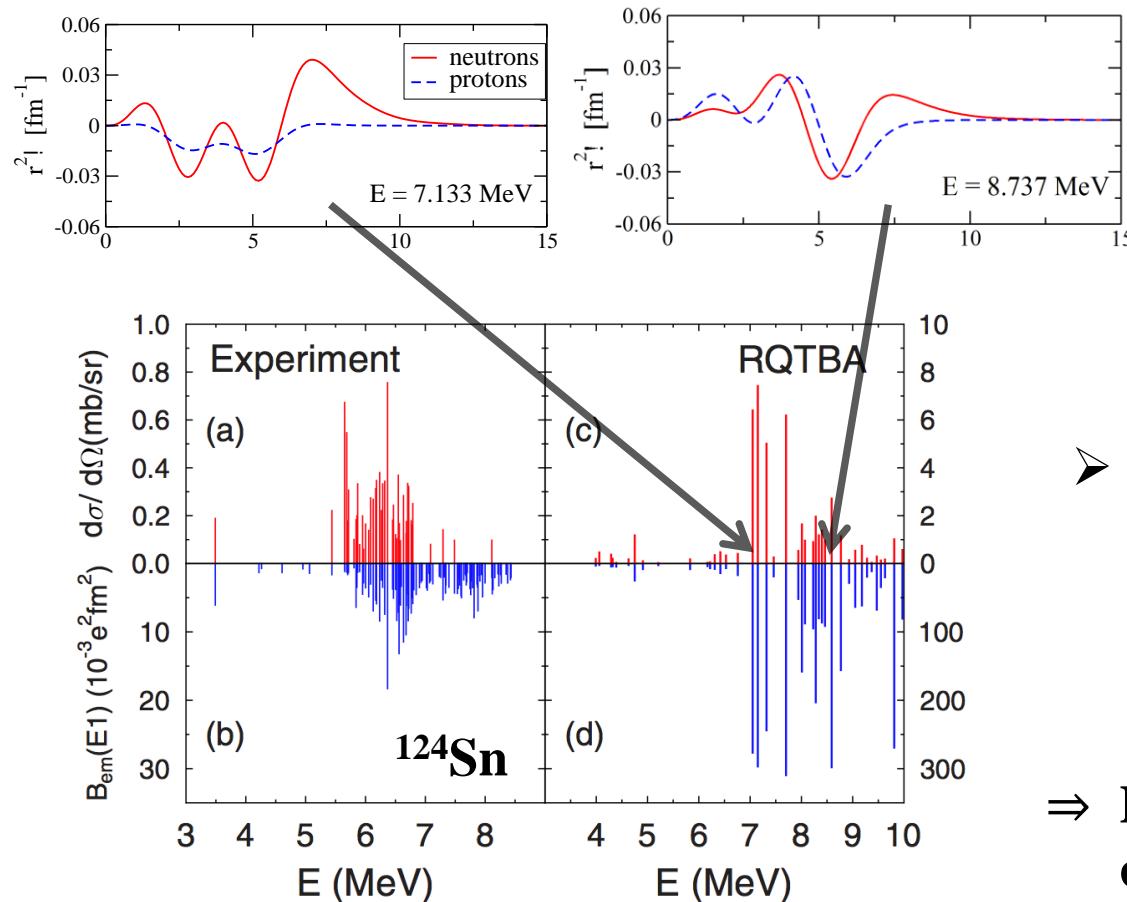
Nantes; 19-20 January 2015

Systematics



Different response to photons and α -particles
points to different underlying structures

Identification of PDR structure in $(\alpha, \alpha'\gamma)$



- Good reproduction of experimental results using RQTBA transition densities + semi-classical reaction model
- ⇒ Different response to complementary probes allows identification of PDR structure

J. Endres *et al.*, PRL 105 (2010) 212503
E. Lanza *et al.*, PRC 89 (2014) 041601(R)

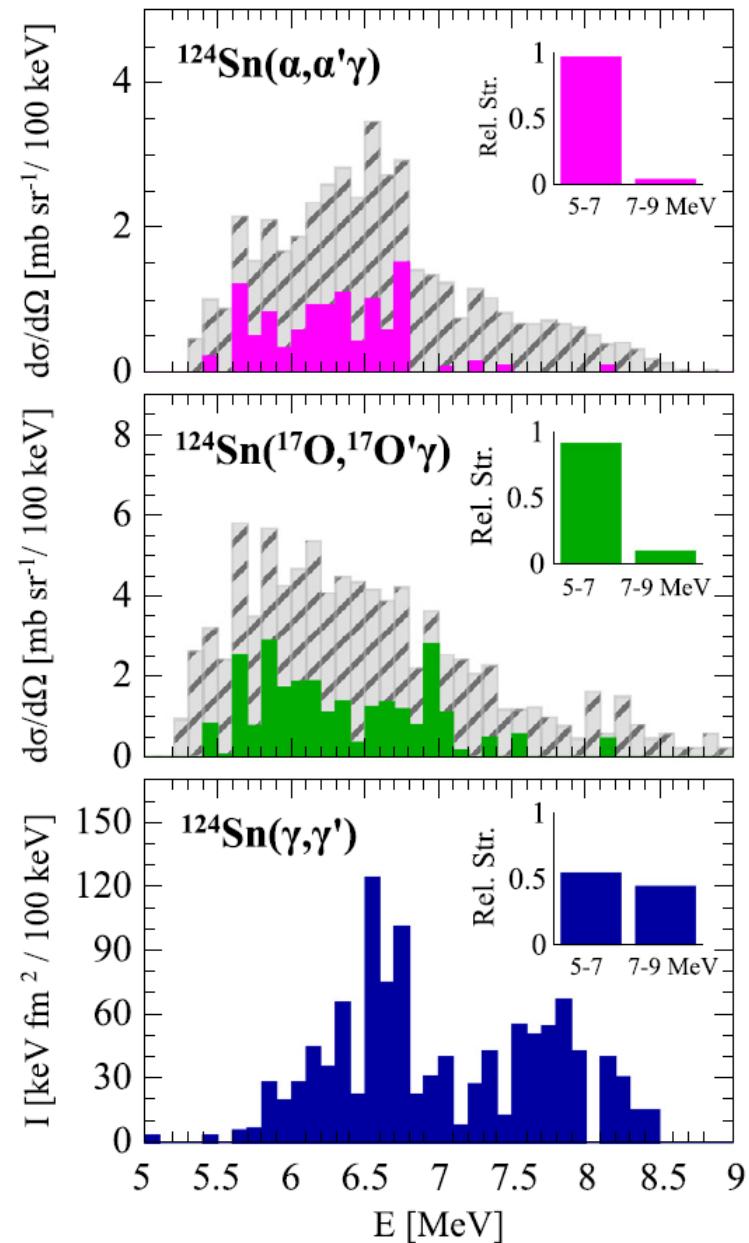
The grey histogram corresponds to the total unresolved strength.

Top panel: Discrete level in α scattering

Centre panel: Discrete levels in ^{17}O scattering

Bottom panel: photon scattering

L. Pellegrini *et al.*, Phys. Lett. B738 (2014) 519



Future Prospects

Outlook

**Radioactive ion beams will be available at energies
where it will be possible to study excitation of
ISGMR and ISGDR**

RIKEN, FAIR, SPIRAL2, NSCL, EURISOL

Determine ISGMR and ISGDR in unstable Sn nuclei.

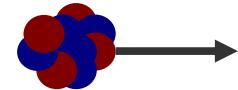
$A = 106$ to 134 possible

\Rightarrow A more precise determination of K_τ

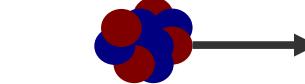
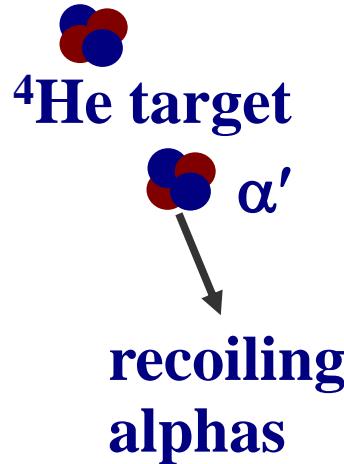
Nuclear structure studies with reactions in inverse kinematics

- Possible at GSI/FAIR, RIKEN, GANIL
(beam energies of 50-100 MeV/u are needed!)

(α, α')



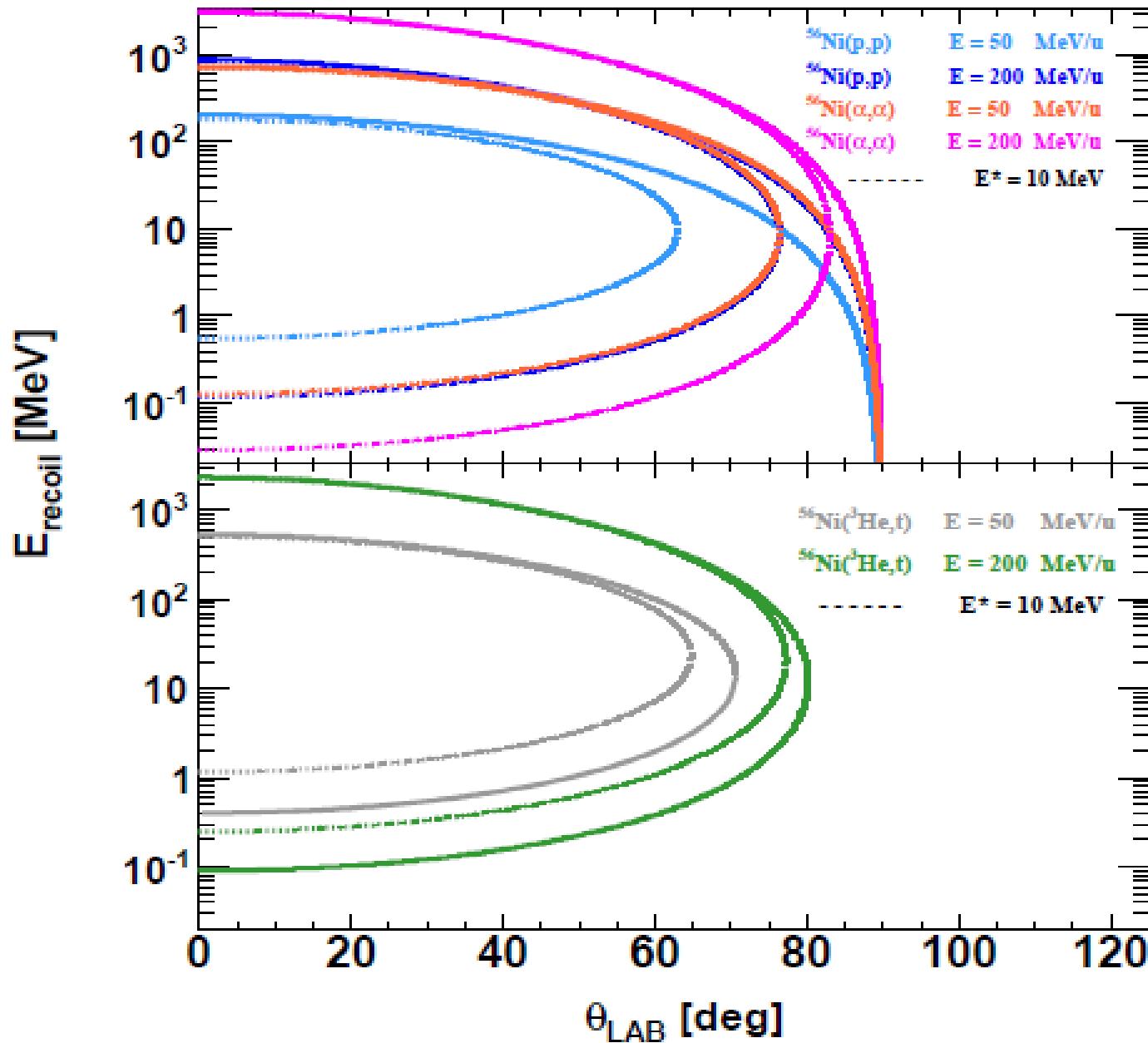
heavy projectile



heavy ejectile

Approach
measure the recoiling alphas

Inconvenience:
difficulty to detect the low-energy alphas

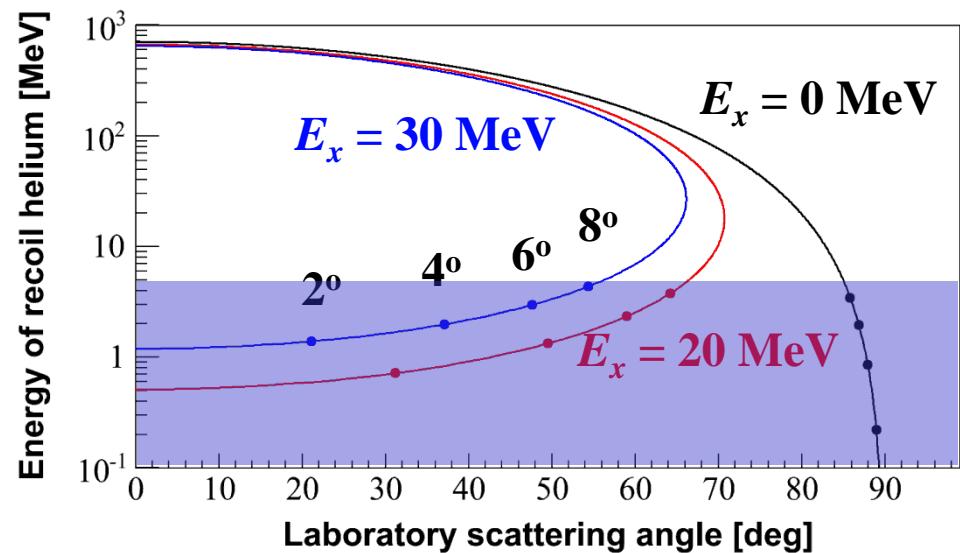


Nuclear structure studies with reactions in inverse kinematics

Challenges with exotic beams

- Inverse kinematics

$^{56}\text{Ni}(\alpha, \alpha')^{56}\text{Ni}^*$
 α = Target
 ^{56}Ni = Projectile
at 50 MeV/u



- Intensity of exotic beams is very low ($\sim 10^4 - 10^5$ pps)
- To get reasonable yields thick target is needed
- Very low energy (\sim sub MeV) recoil particle will not come out of the thick target

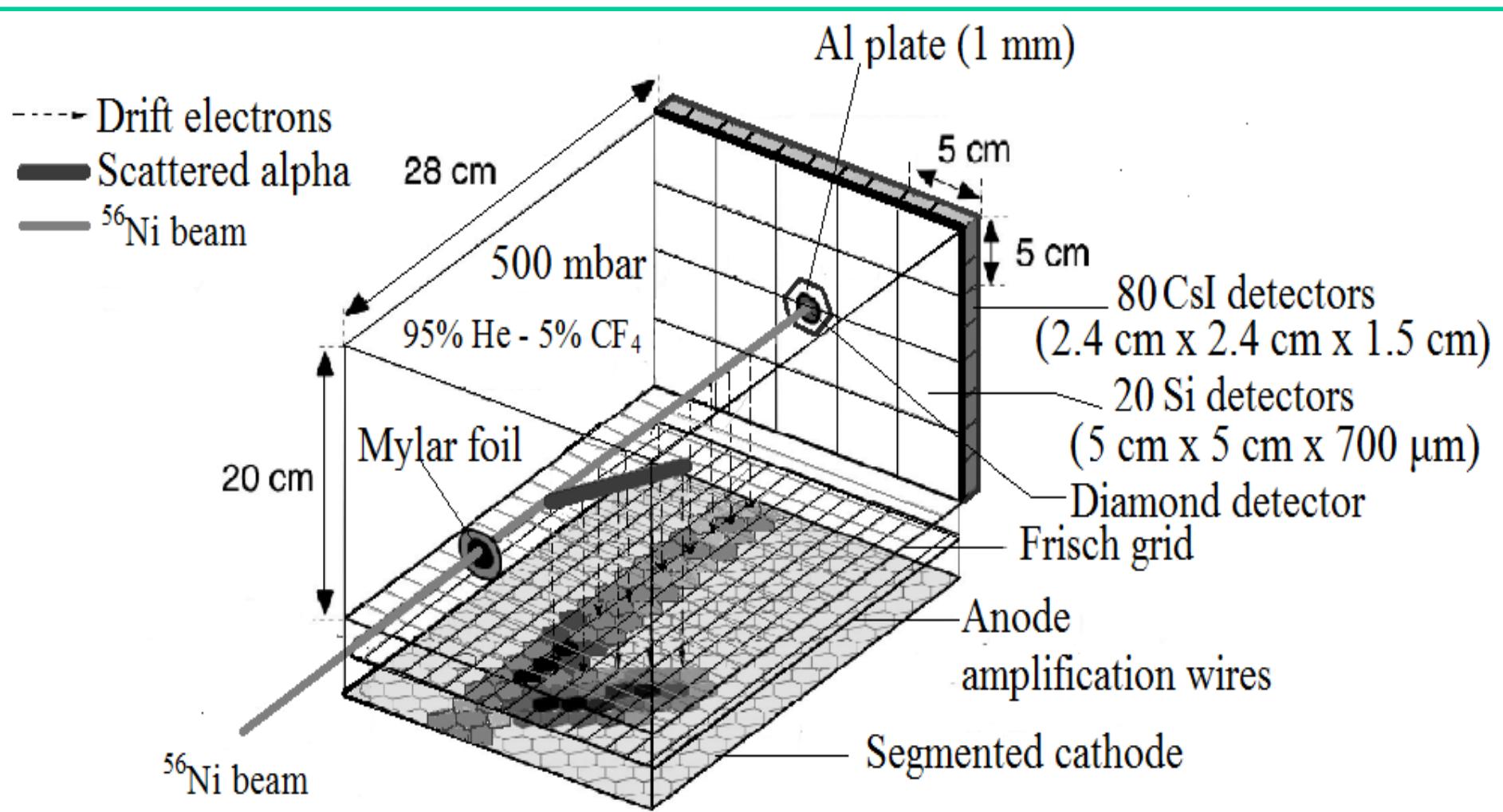
Active target

A gas detector where the target gas also acts as a detector

- Good angular coverage
- Effective target thickness can be increased without much loss of resolution
- Detection of very low energy recoil particle is possible

MAYA active-target detector at GANIL

Schematic view of MAYA active target detector

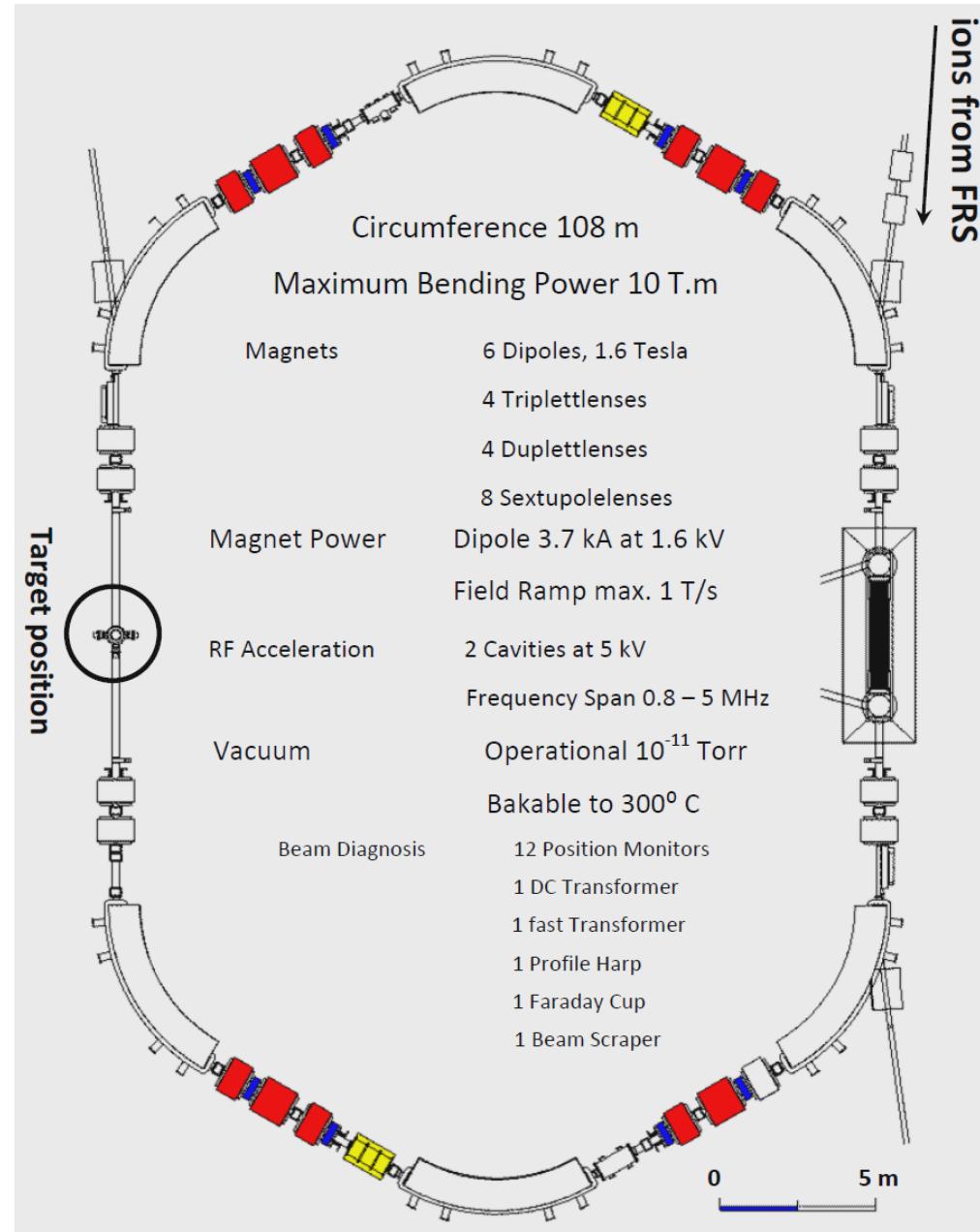


GSI Storage Ring

Experimental Storage Ring

Luminosity:
 $10^{26} - 10^{27} \text{ cm}^{-2}\text{s}^{-1}$

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Advantages and disadvantages of storage-ring experiments

Advantages:

Large intensities in the ring

Little energy loss in the target

No target window (no background)

High resolution of the beam (cooling)

Forward focusing for high-energy particles

Low-energy threshold

Disadvantages:

Ultra high vacuum

Very small recoil energies for low q

Thin targets

Detection system @ FAIR

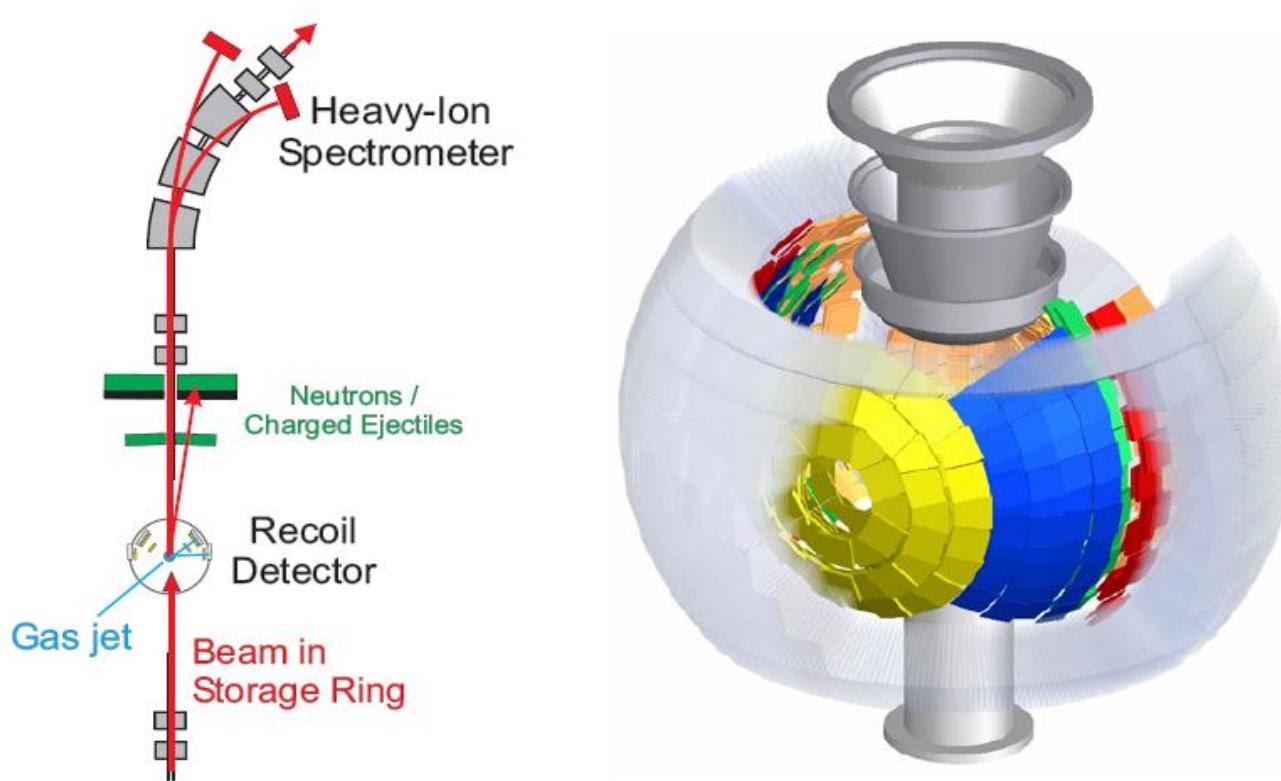


Figure 1: Schematic view of the EXL detection systems. Left: Set-up built into the NESR storage ring. Right: Target-recoil detector surrounding the gas-jet target.

Use of EXL recoil detector has been under evaluation

Thank you for your attention