

# Binary Neutron Star Mergers: Numerical Simulations and Observations

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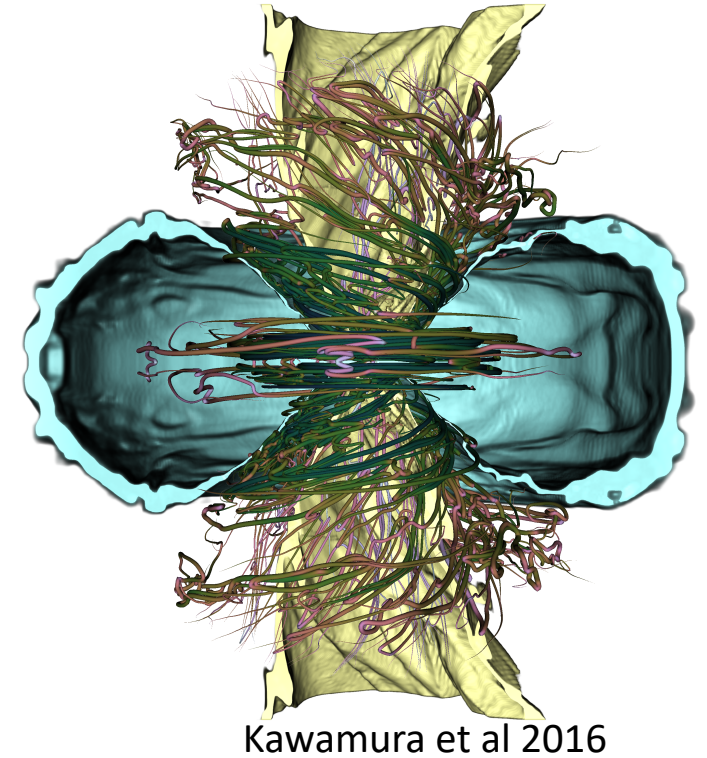
[www.brunogiacomazzo.org](http://www.brunogiacomazzo.org)



Trento Institute for  
Fundamental Physics  
and Applications

# General Relativity and Astrophysics

- Binary Black Hole Mergers
- Binary Neutron Star Mergers
- Neutron Star – Black Hole Mergers
- Supernovae
- Accretion Disks
- Cosmology



In all these scenarios general relativity plays a fundamental role.

Developing a code that solves the full set of GR and (Magneto)Hydrodynamic equations is not an easy task.

# (a brief) History of Numerical Relativity

(see <https://link.springer.com/article/10.1007/lrr-2015-1>)

- 1962 Arnowitt, Deser and Misner (ADM) 3+1 formulation
- 1966 May and White first 1D GR simulation of collapse to BH
- 1985 Stark and Piran extract GWs from a simulation of rotating collapse to a BH in NR.
- 1993 Anninos et al. first simulation of head-on collision of two BHs
- 1995-1998 BSSN formulation
- 1996 Brüggmann mesh refinement simulation of BHs
- 1997 Cactus 1.0 is released
- 1997 Brandt & Brüggmann “puncture” initial data
- 2000 Brandt et al. simulate the first grazing collisions of BHs
- 2000 Shibata and Uryū first NS-NS merger simulation in GR
- 2003 Schnetter et al. “Carpet” driver for Cactus
- 2005 Pretorius first simulation of BH-BH inspiral and merger

# Equations

Einstein Equations

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu}$$

Hydro Equations

$$\nabla_{\mu} T^{\mu\nu} = 0$$

$$\nabla_{\mu} J^{\mu} = 0 \qquad P = P(\rho, \epsilon)$$

$$J^{\mu} = \rho u^{\mu}$$

$$T^{\mu\nu} = (\rho h + b^2)u^{\mu}u^{\nu} + \left(p + \frac{b^2}{2}\right)g^{\mu\nu} - b^{\mu}b^{\nu}$$

Maxwell Equations

$$\nabla_{\nu} {}^*F^{\mu\nu} = 0$$



einstein  
toolkit

# Einstein Toolkit

## einsteintoolkit.org

- Set of publicly available tools for relativistic astrophysics
- Latest release on March 29 2019 (codename “Proca”)
- More than 150 users on 6 continents
- Tested on several HPC infrastructures around the world
- Includes over 100 Cactus thorns, including:
  - McLachlan (space-time evolution)
  - GRHydro and IllinoisGRMHD (GRMHD equations)
  - Several initial data and analysis routines
- Data can be read and visualized by open source codes (e.g., Visit, PostCactus, yt)

# References

- Einstein Toolkit Webpage: <http://einsteintoolkit.org>
- Main Publications presenting the toolkit:
  - Loeffler et al 2012: <http://arxiv.org/abs/1111.3344>
  - Moesta et al 2013: <http://arxiv.org/abs/1304.5544>
  - Zilhao and Loeffler 2013: <http://arxiv.org/abs/1305.5299>
- Visualization Tools:
  - PostCactus & SimRep: <https://bitbucket.org/DrWhat/pycactuset>
  - Visit: <https://visit.llnl.gov/>
  - YT: <http://yt-project.org/>
- Every year workshops and (sometimes) schools are organized in EU and USA:
  - Rochester, NY, USA, June 2019: <https://ccrg.rit.edu/content/events/2019-06-17/north-american-einstein-toolkit-workshop-2019>
  - **London, UK, September 2019:** <https://sites.google.com/view/eetm2019/home>



# Binary Neutron Star Mergers

# NEUTRON STARS

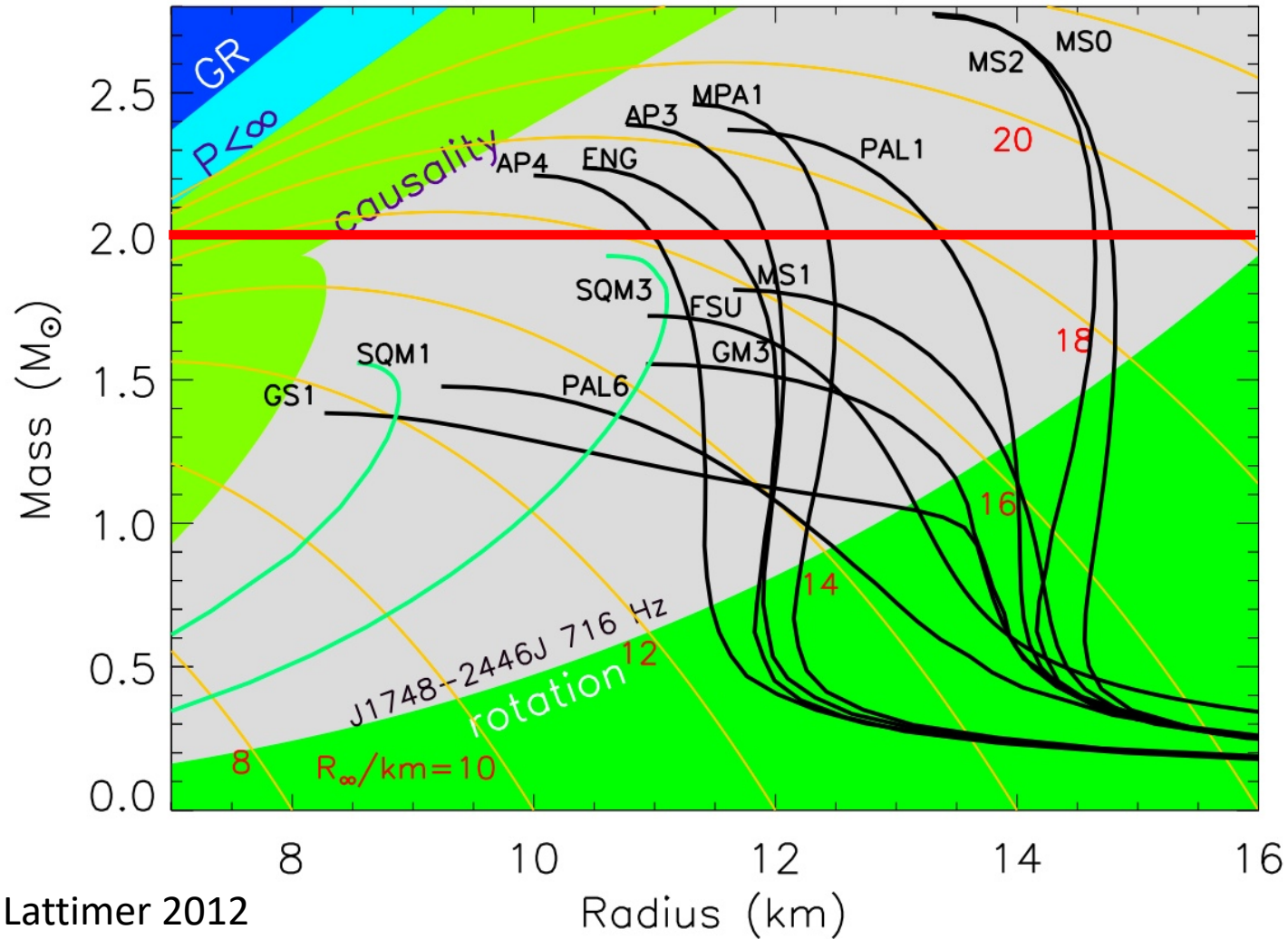
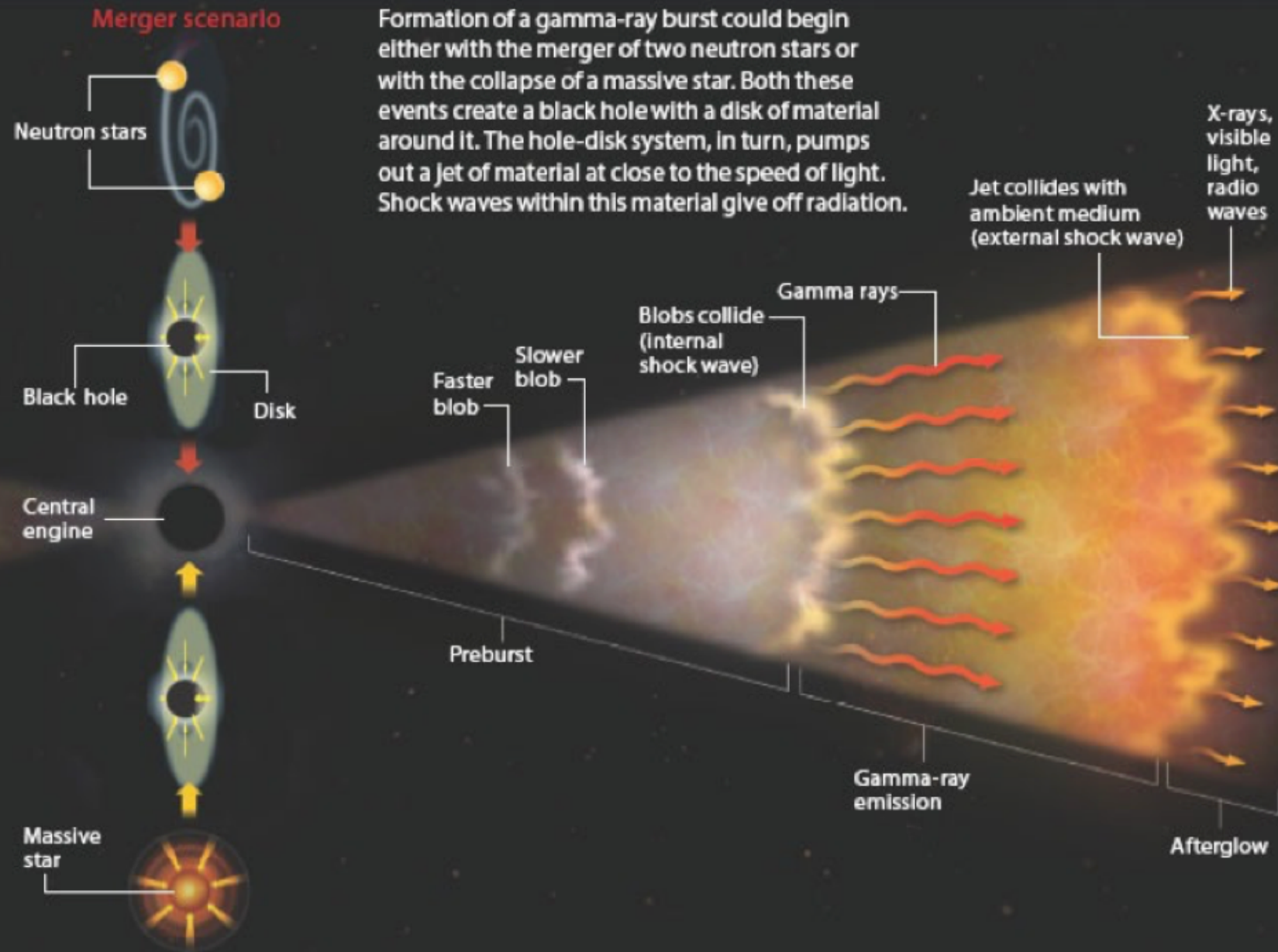


Photo by Daily Herald Archive/SSPL/Getty Images  
(23/02/1968)

First NS discovered as a “pulsar” (radio frequencies) in 1967 by PhD student Jocelyn Bell and her supervisor Antony Hewish



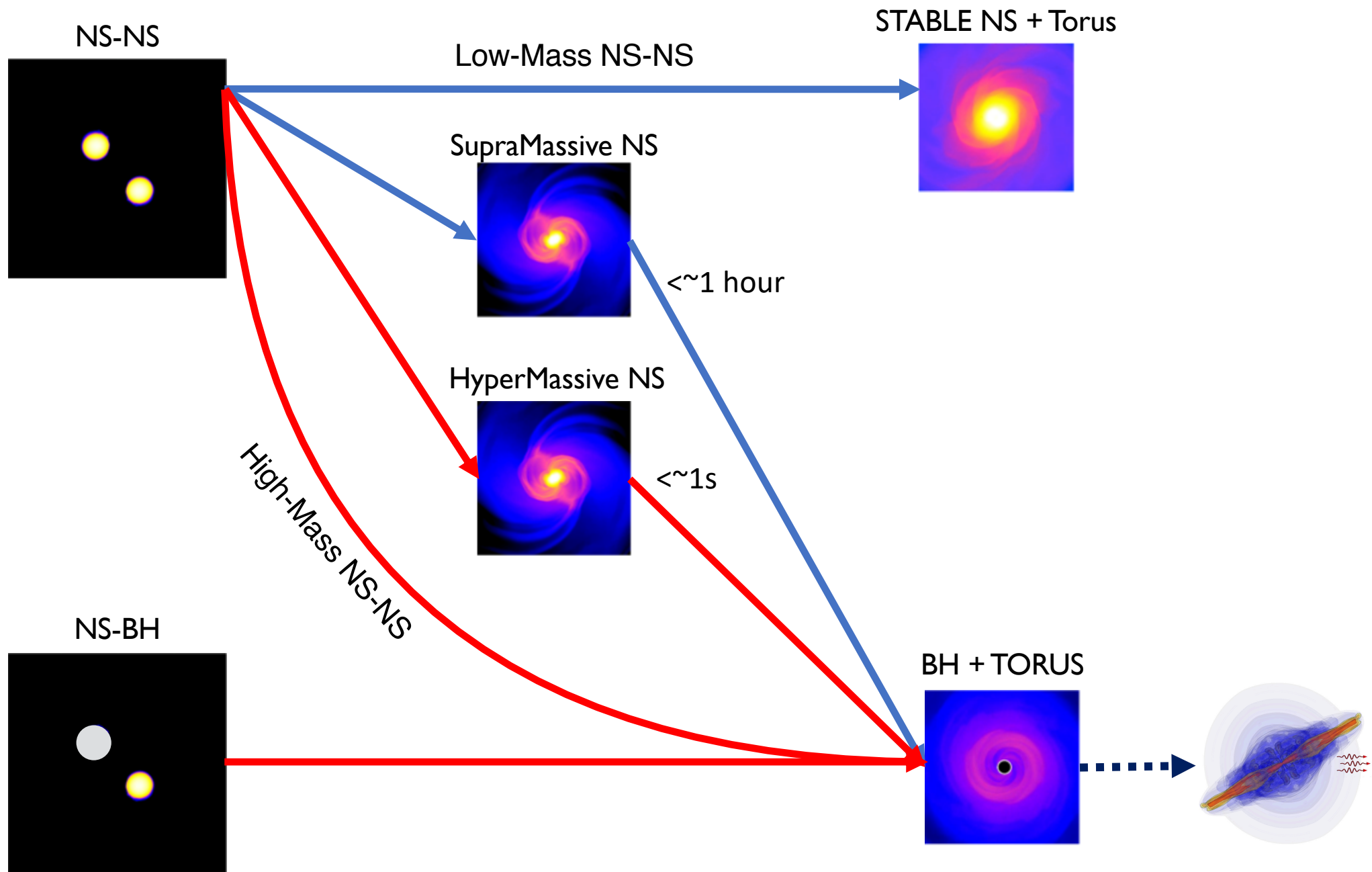
# Bursting Out



## Gamma-Ray Bursts

- Discovered in 1967
- Two types:
  - Short (<2 s)
  - Long (>2 s)
- Long GRBs are due to Supernovae explosions (discovered in 1998)
- Short GRBs have been quite a mystery

# Neutron Star Binary Mergers

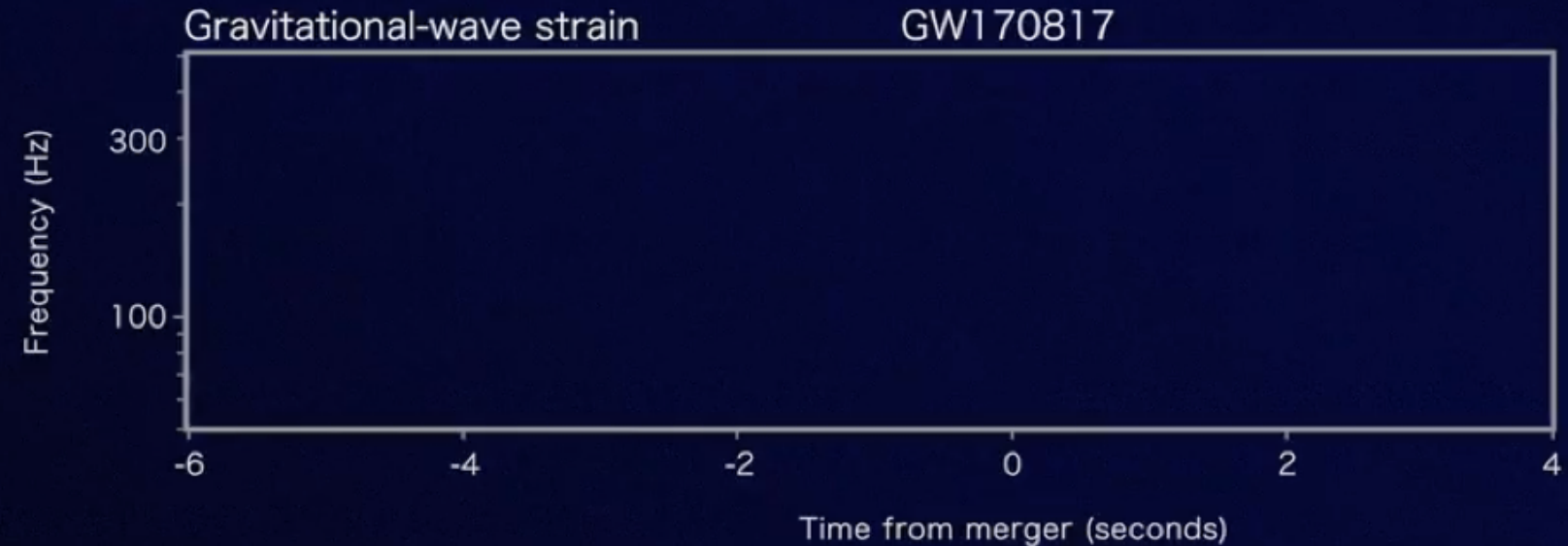


# GW170817: the first NS-NS detection

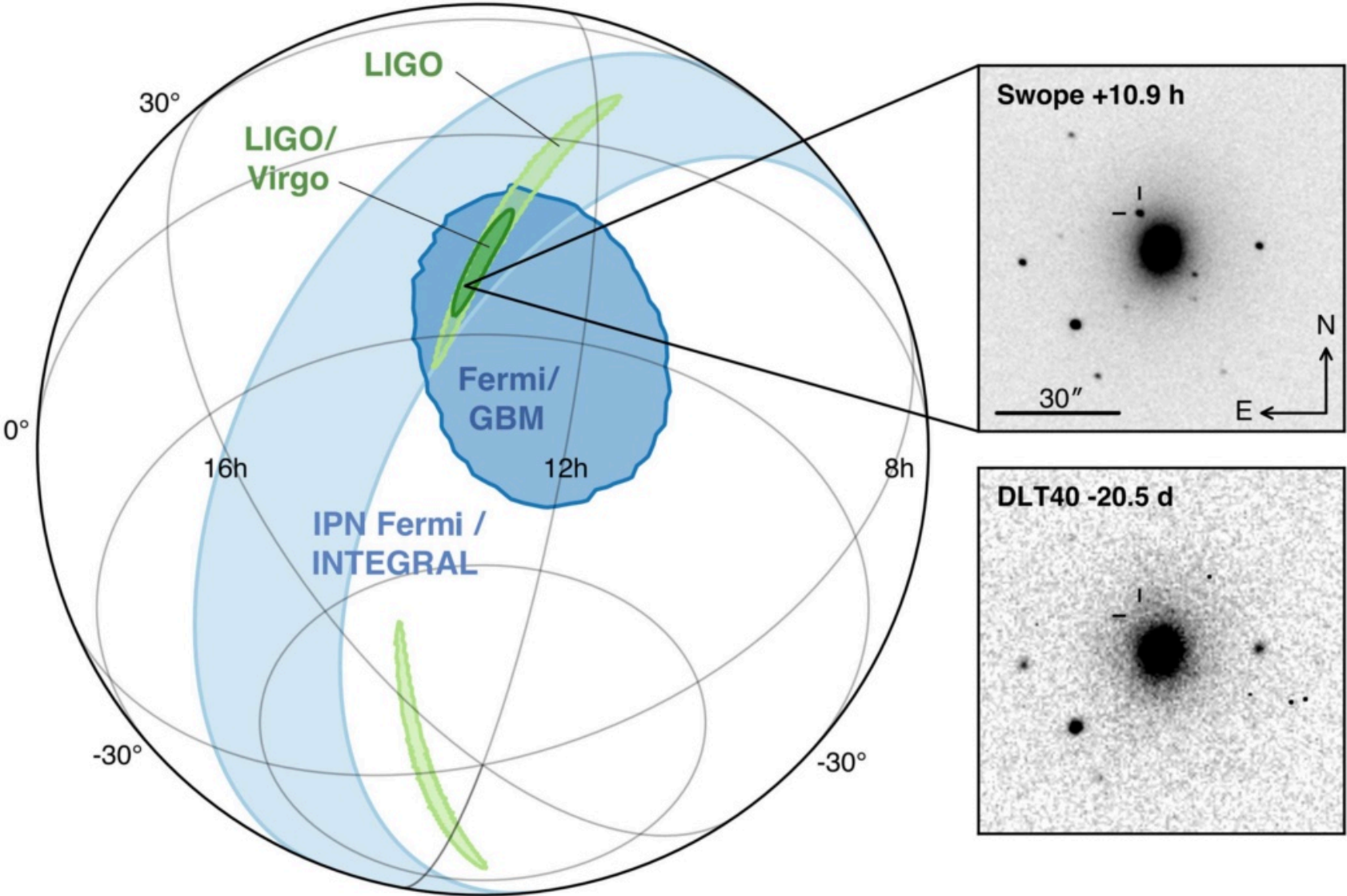
Fermi

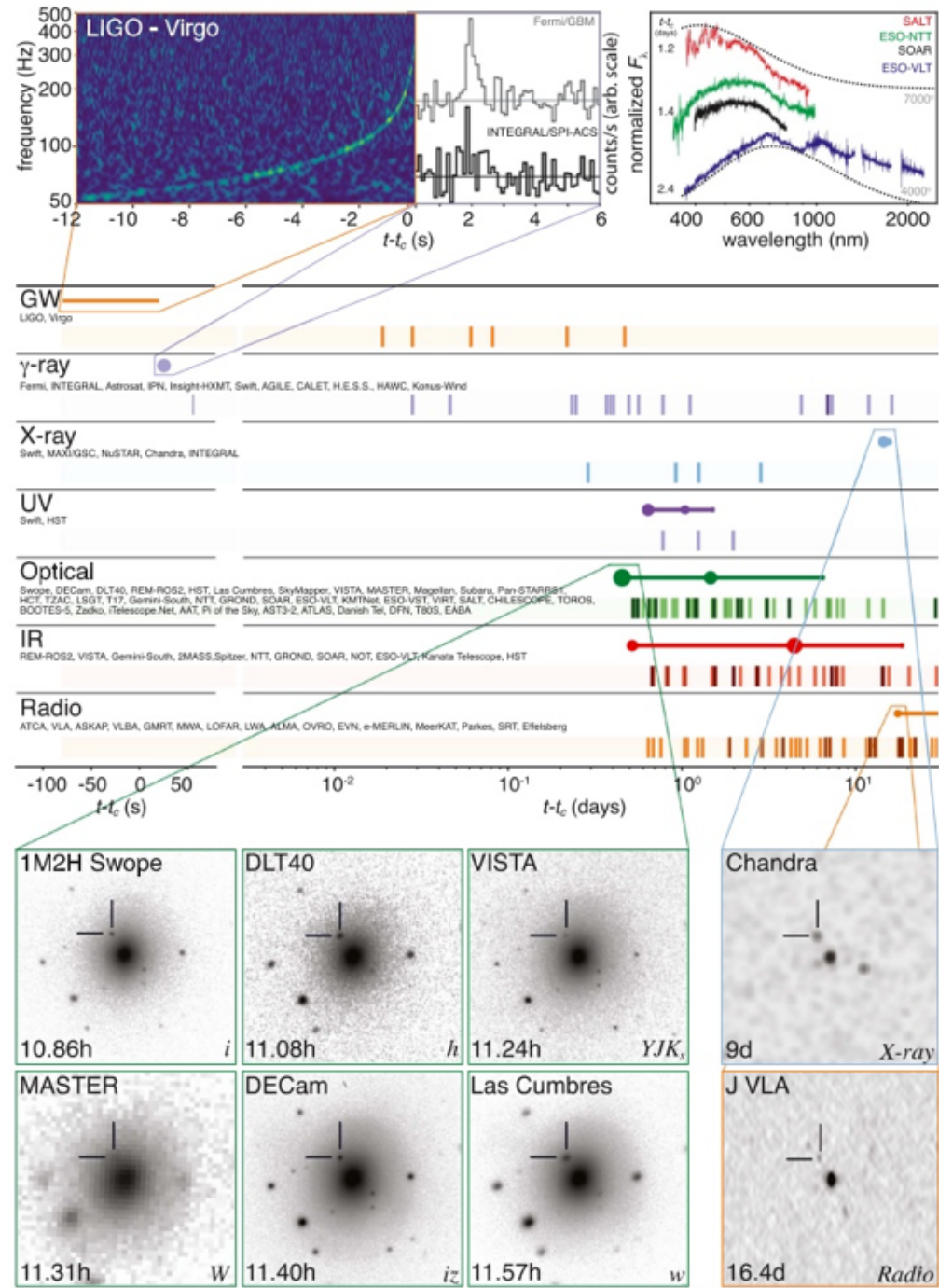


LIGO





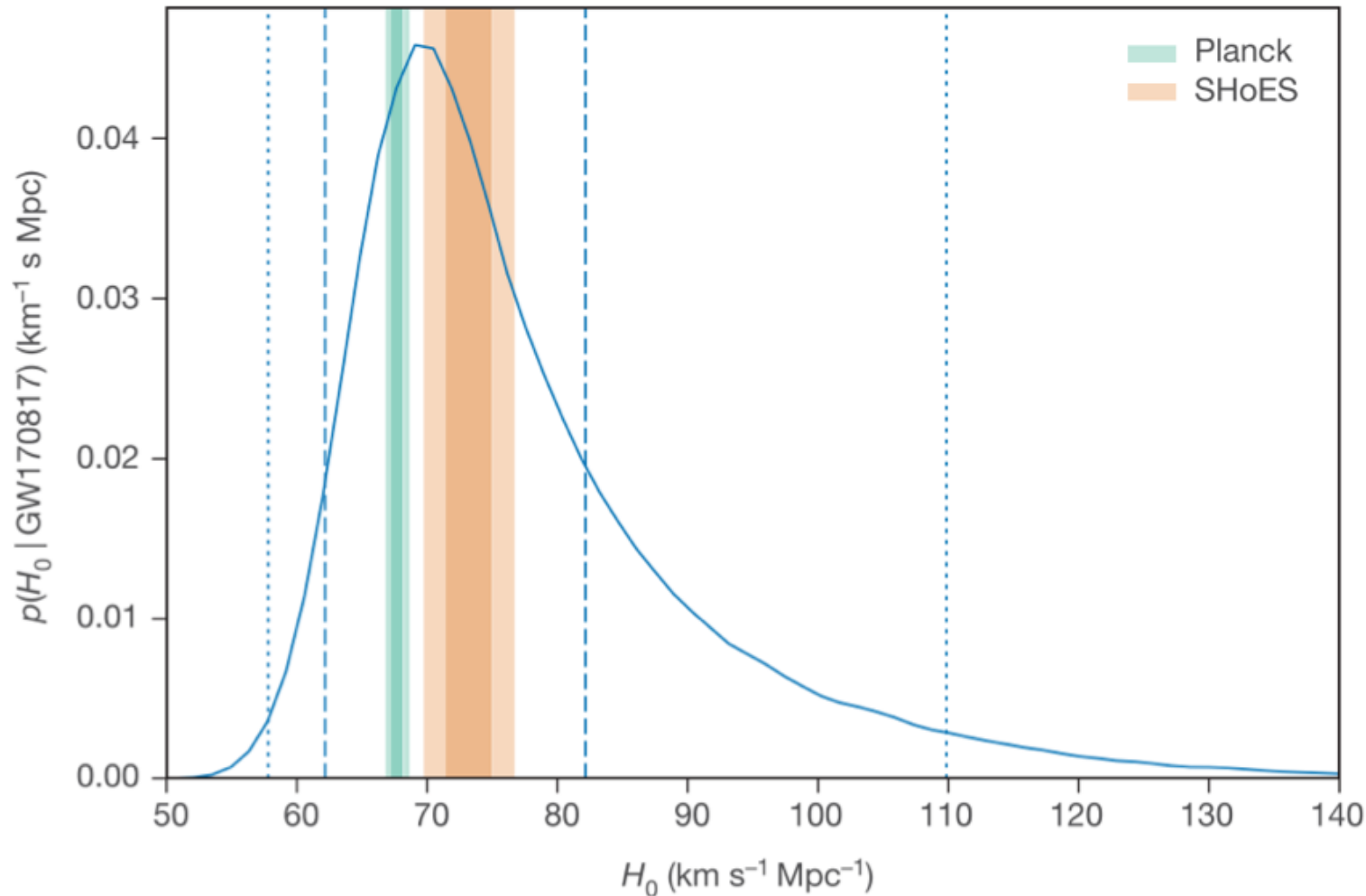




The event has been detected in the full EM spectrum from gamma-ray to radio.

GW and EM emission allowed also to put constraints on NS equation of state and SGRB models.

# Hubble Constant Measure

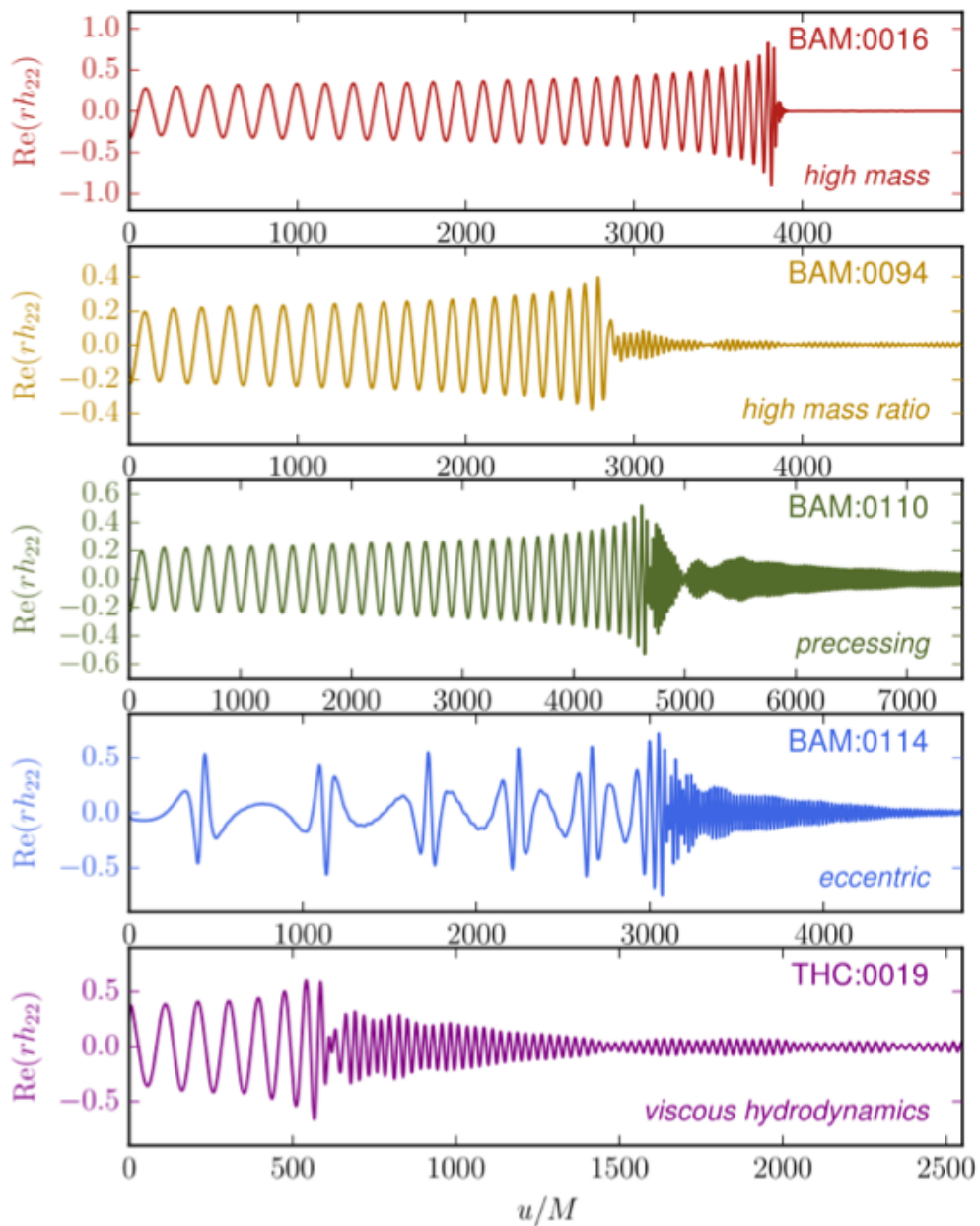


Combination of GW and EM emission allowed for a new measure of the Hubble constant.

The comparison of time of arrival also constrained the speed of gravitational waves to be equal to the speed of light:

$$\frac{\Delta v}{v_{EM}} \approx 10^{-15}$$

# Equation of State Effects



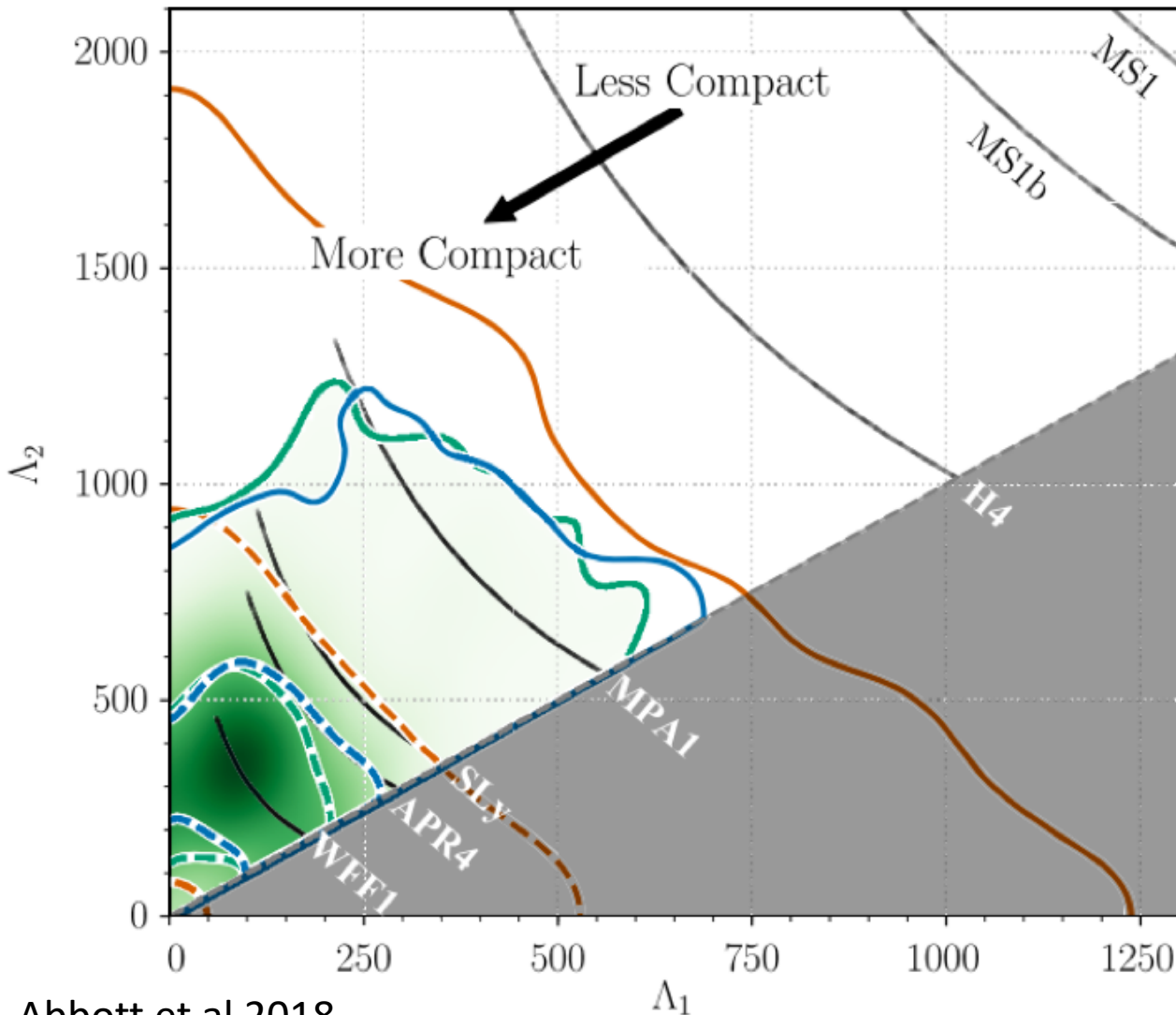
General relativistic simulations of BNS mergers from different groups now include quite a range of parameters:

- Total mass
- Mass ratio
- Spins (few)
- Cold and (a few) hot EOSs
- Eccentricity (few)
- Viscosity (few)
- Neutrinos (few)
- Magnetic fields (few)

Dietrich et al 2018

<http://www.computational-relativity.org/index.html>

An important quantity that can be measured is the dimensionless tidal deformability  $\Lambda = \frac{2}{3} k_2 \left[ \left( \frac{c^2}{G} \right) \left( \frac{R}{m} \right) \right]^5$  where  $k_2$  is the (dimensionless) Love number. One can more easily extract a combination of the tidal deformabilities of the two NSs:

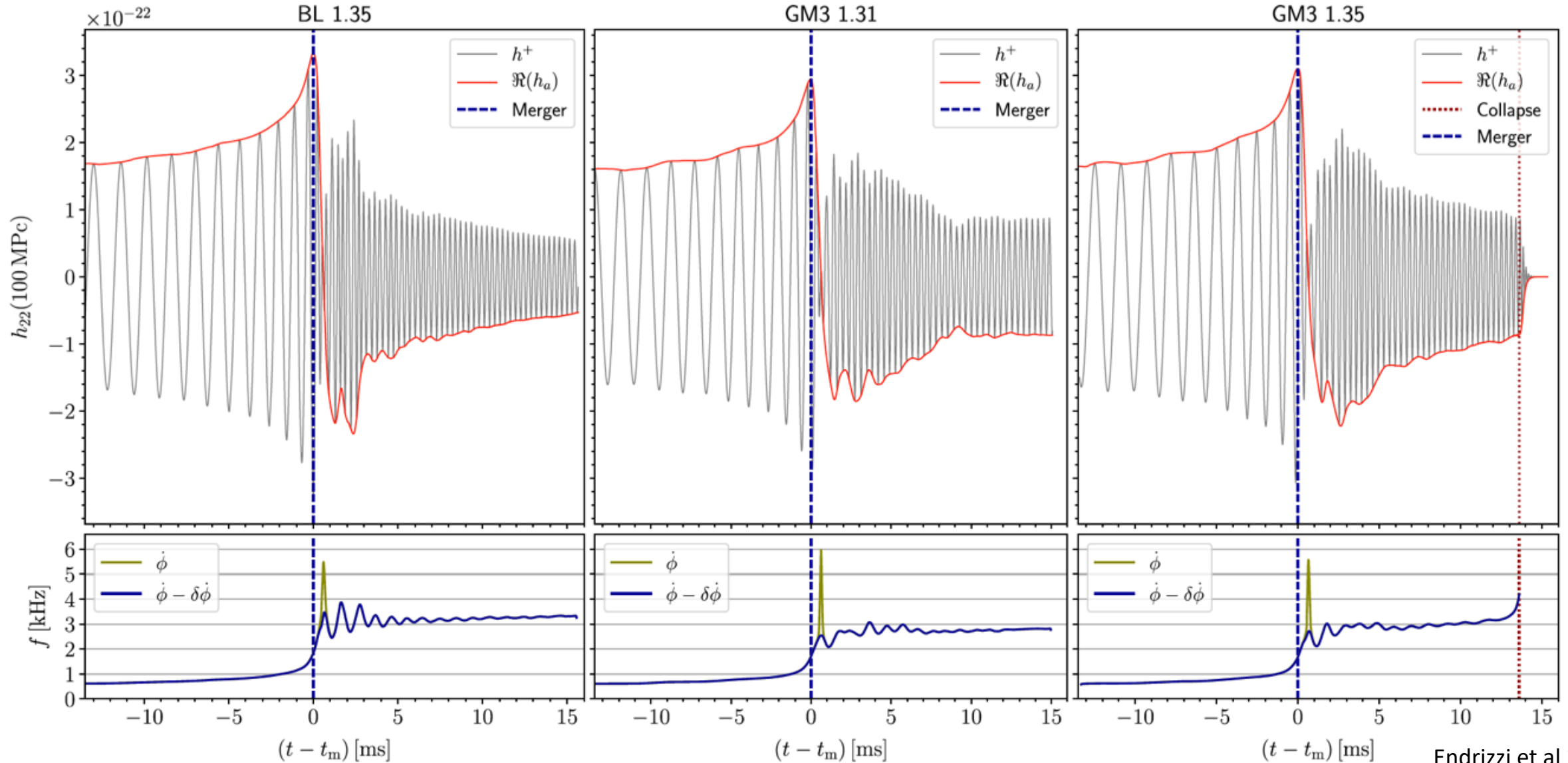


$$\tilde{\Lambda} = \frac{16 (m_1 + 12m_2)m_1^4\Lambda_1 + (m_2 + 12m_1)m_2^4\Lambda_2}{13 (m_1 + m_2)^5}$$

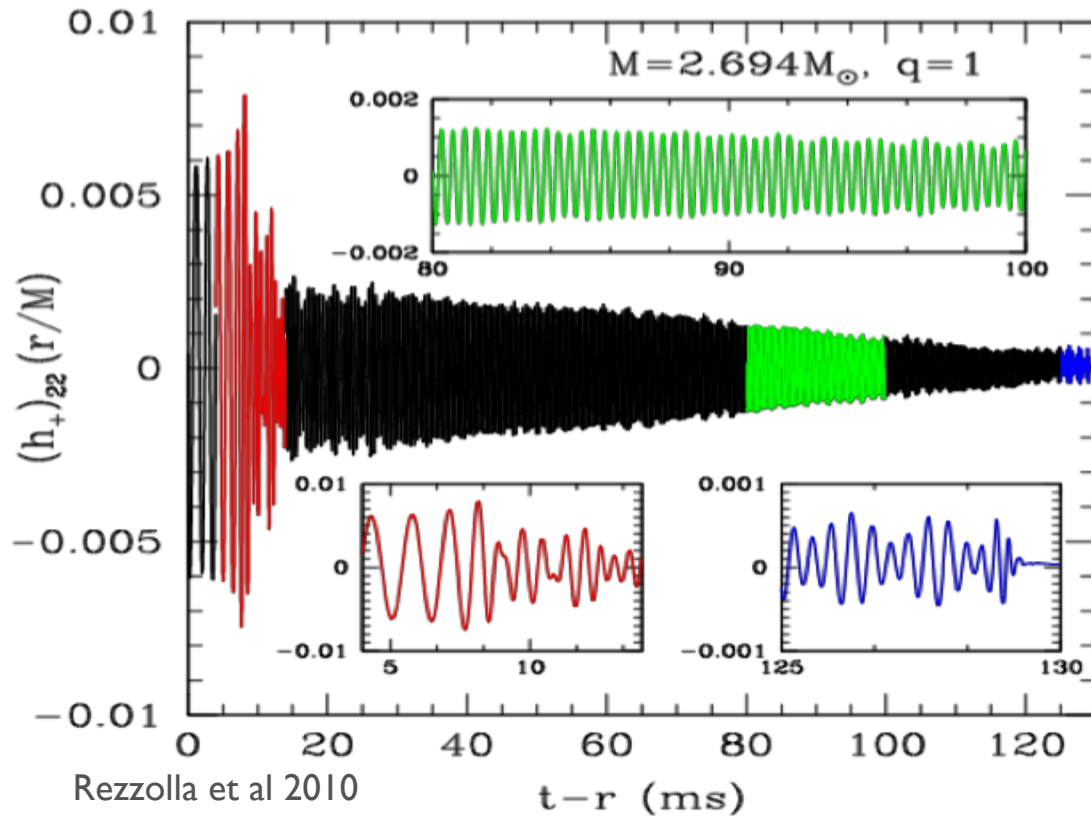
$\tilde{\Lambda} = 300^{+500}_{-190}$  for low spin ( $<0.05$ )  
 $\tilde{\Lambda} = (0, 630)$  for high spin ( $<0.89$ )  
 (see Abbott et al 2019)



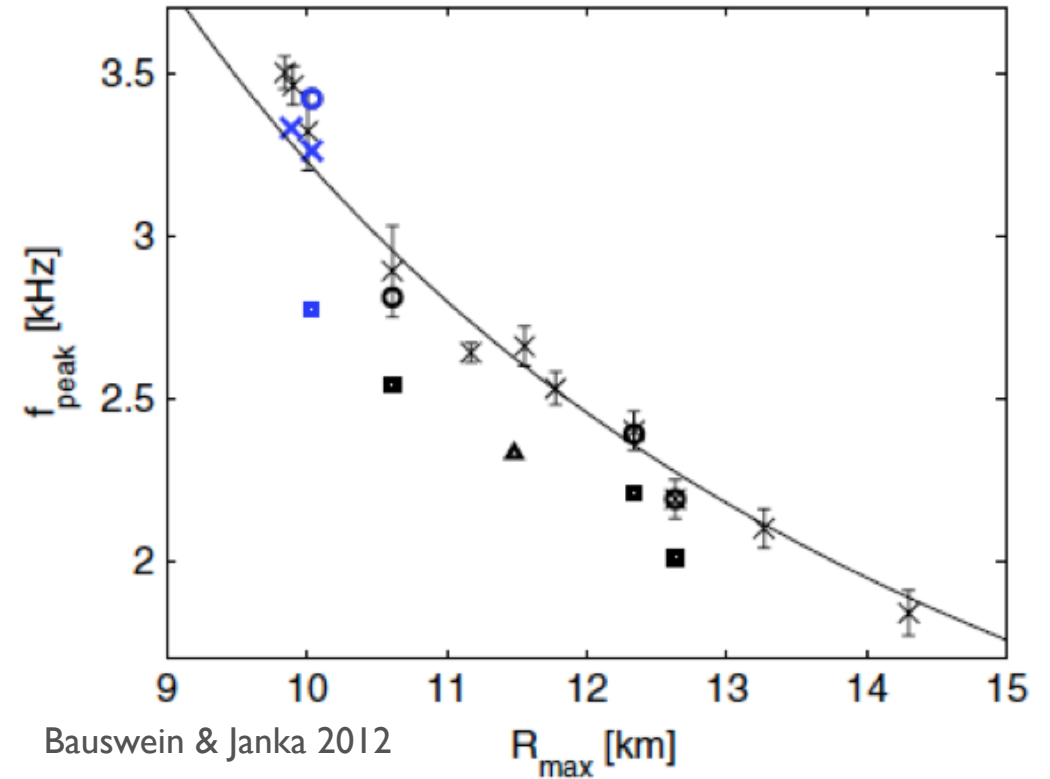
# Post-Merger Effects



# EOS EFFECTS IN THE POSTMERGER



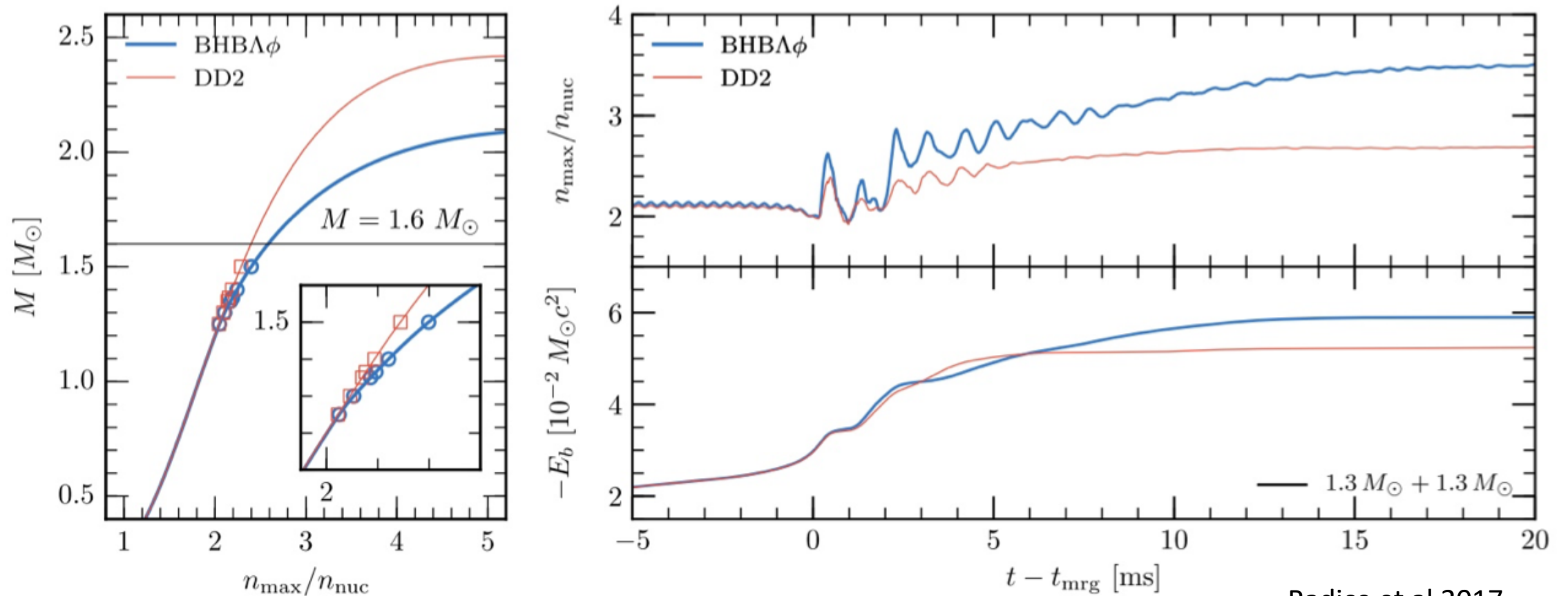
A significant fraction of NS-NS mergers can produce long-lived NSs (e.g., Piro, Giacomazzo, Perna 2017)



Frequency peak in GWs emitted after merger can constrain EOS at high densities and temperature (and maybe magnetic fields).



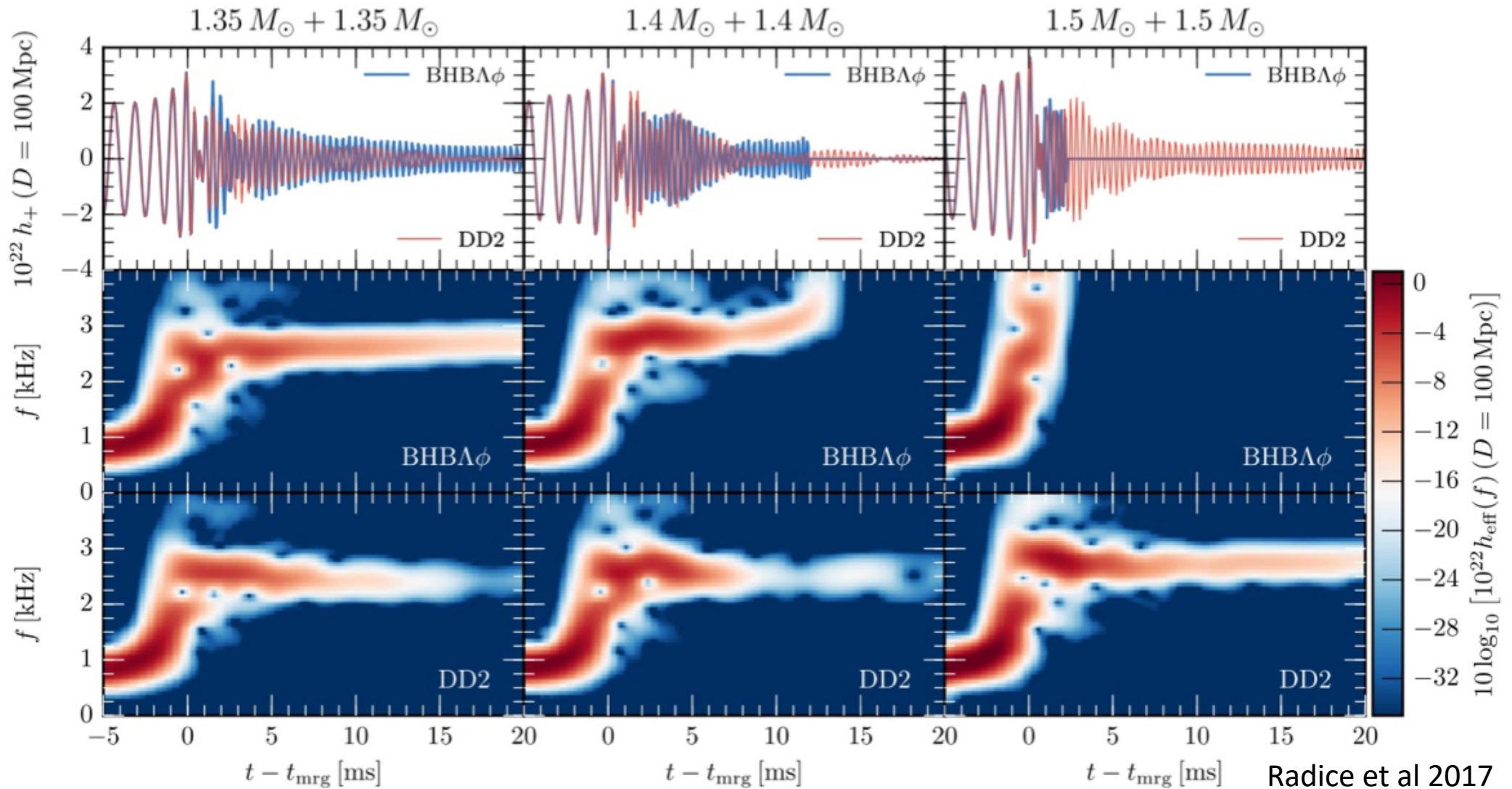
# EOS EFFECTS IN THE POSTMERGER



Radice et al 2017

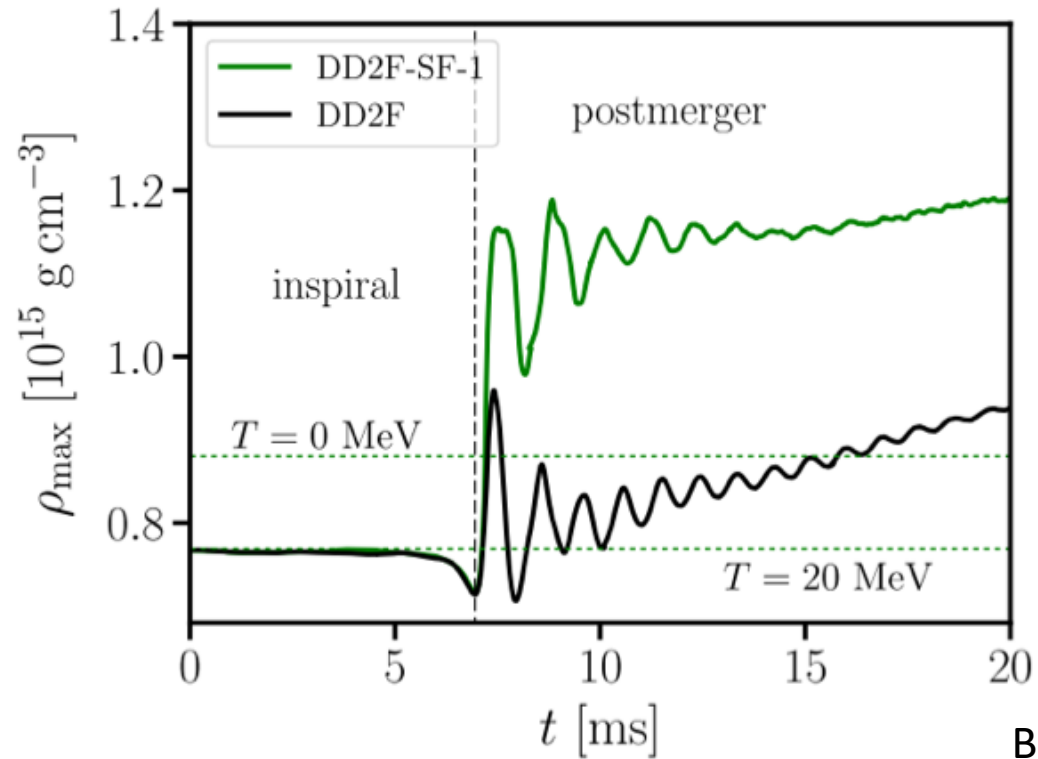
EOS identical at “low” (inspiral) densities, but different at post-merger densities (due to appearance of hyperons).

# EOS EFFECTS IN THE POSTMERGER

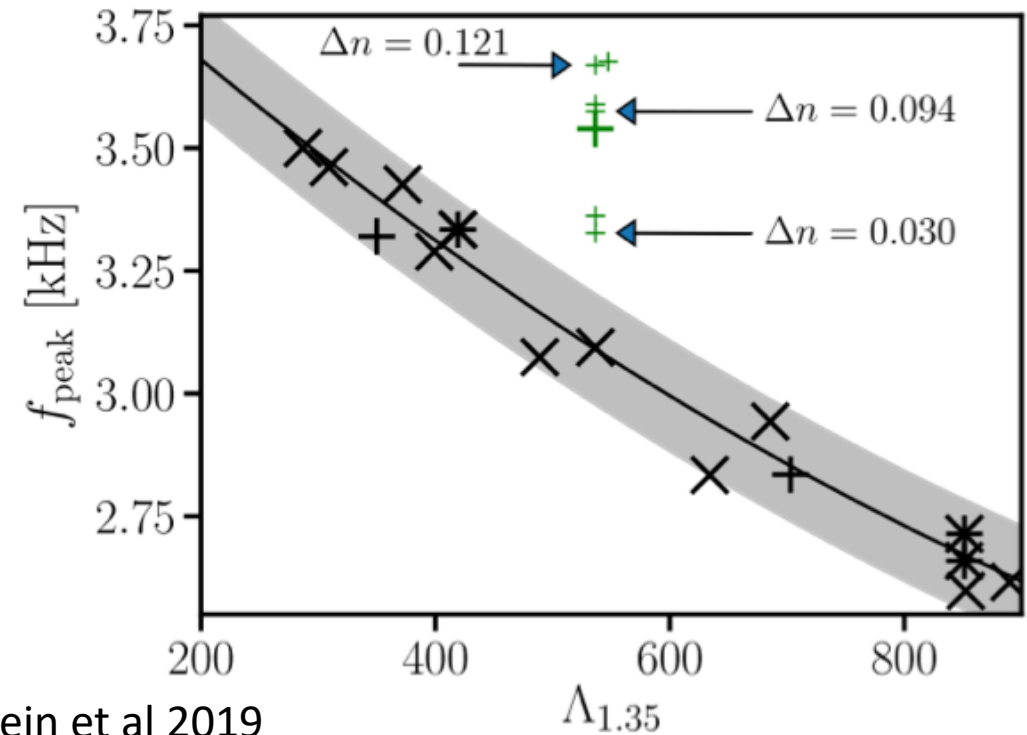


Effects are more evident in post-merger luminosities and phase evolution (see also Bernuzzi et al 2016).

# PHASE TRANSITIONS IN THE POST-MERGER

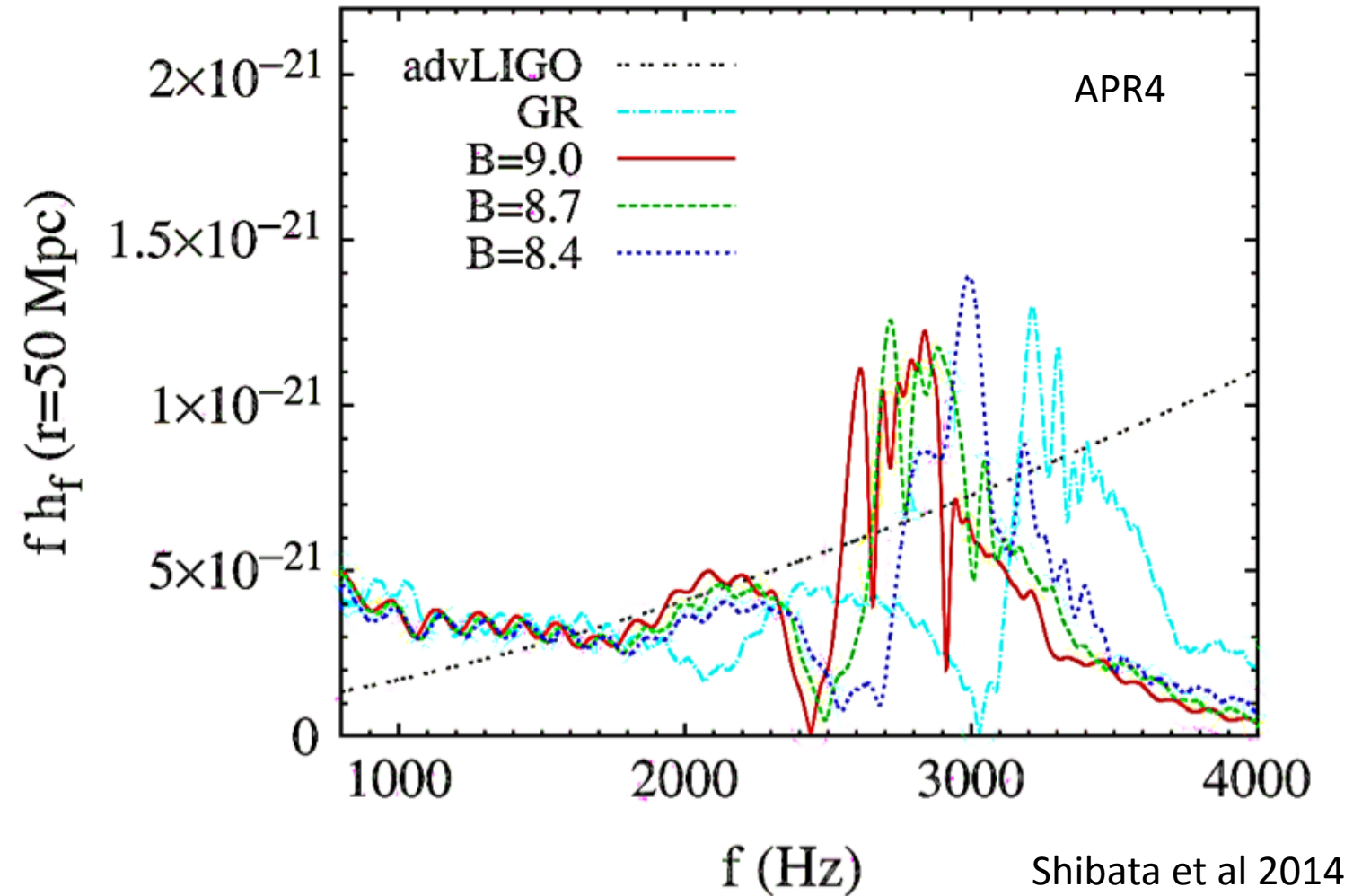
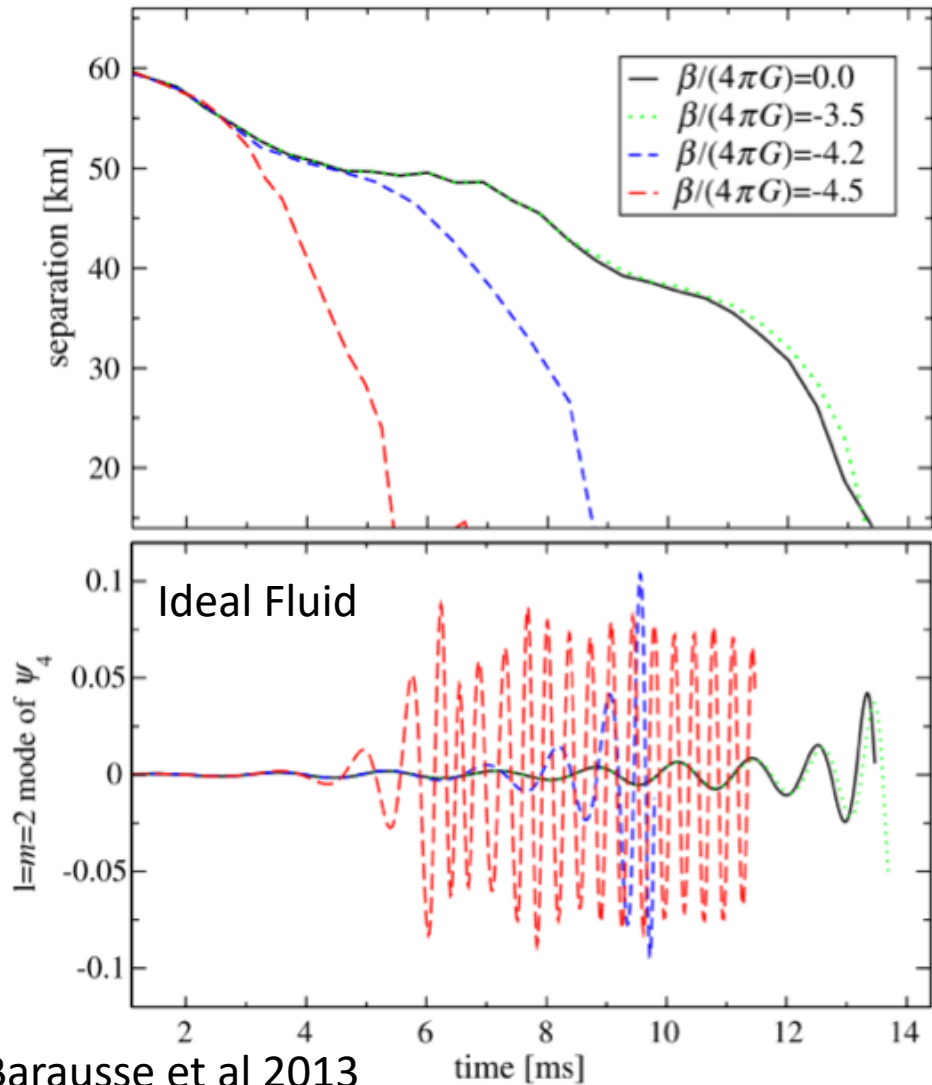


Bauswein et al 2019



A phase transition to a deconfined-quark-matter core affects significantly the post-merger GW peak.

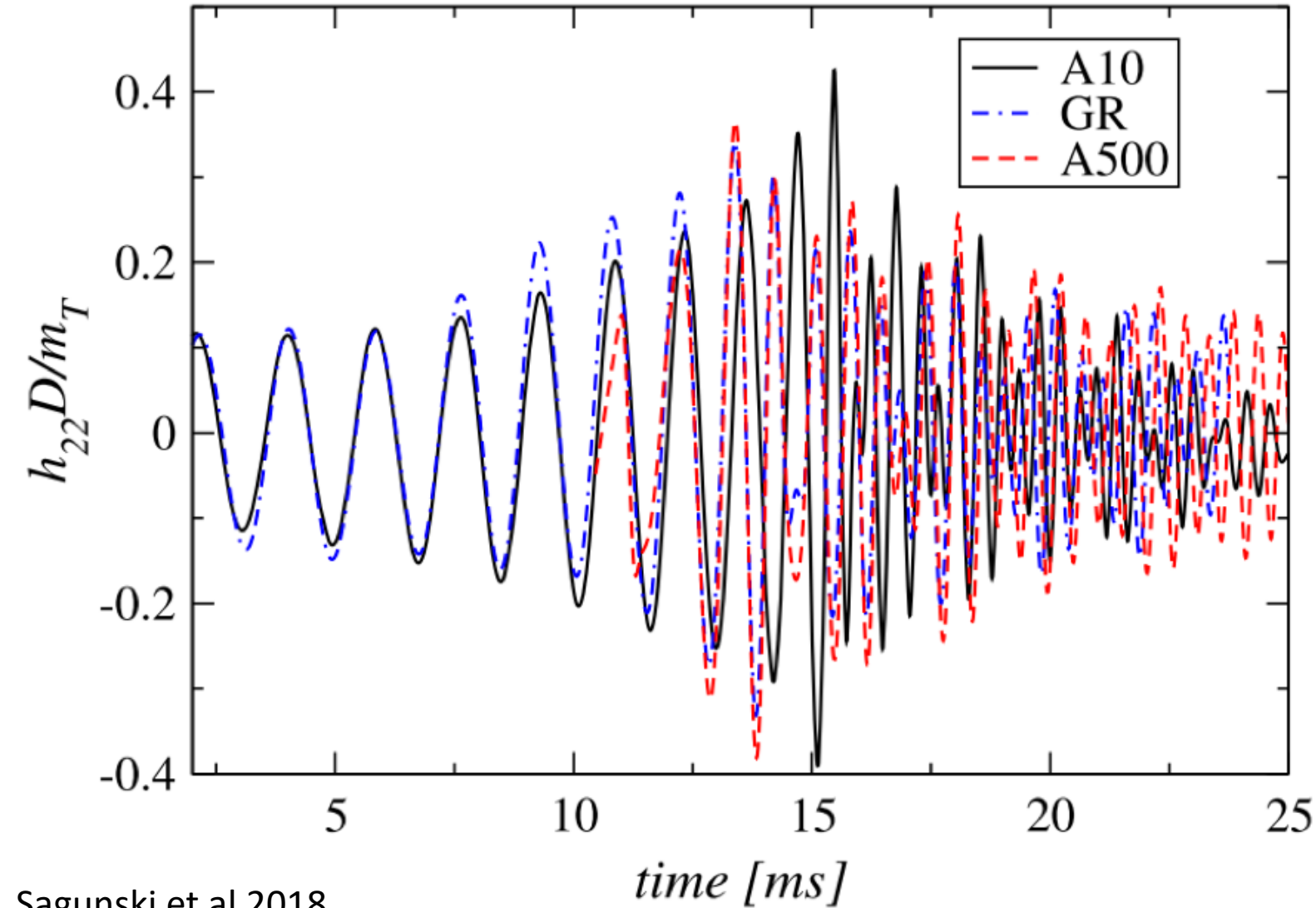
# BNS Mergers in Scalar-Tensor Theories



Spontaneous scalarization may happen during the inspiral or merger and may affect the GW signal.

# BNS Mergers in $f(R)$ Theories

Considered  $f(R) = R + a_2 R^2$  with  $a_2 = 1090.3 \text{ km}^2$  (model A500) and  $a_2 = 21.8 \text{ km}^2$  (A10)



The long-range scalar force (A500) produce an earlier merger while the short-range one is similar to GR.

Effects of short-range scalar force are more evident in the post-merger phase, but they may be confused with EOS effects.

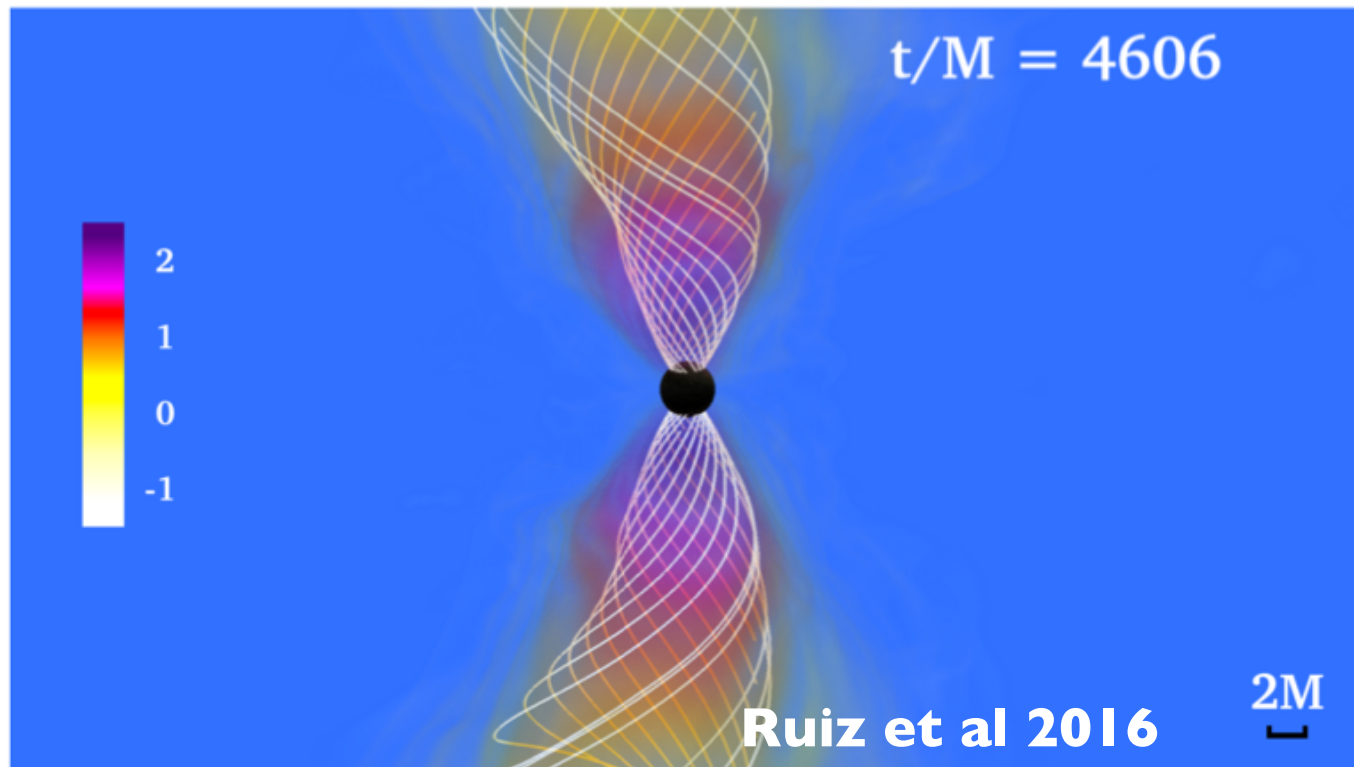
Combining EM and GW signals (e.g., Ponce et al 2015) may help (perhaps).

# The Role of Magnetic Fields



# JETS FROM NS BINARY MERGERS

NS-NS



NS-BH



Jet formation observed in Ideal-Fluid simulations with the IllinoisGRMHD code starting with very large ( $10^{16}\text{G}$ ) fields

# WHISKYMHD SIMULATIONS OF BNS MERGERS

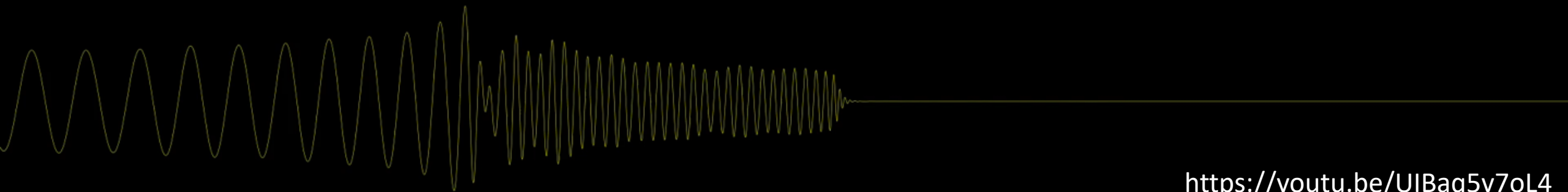
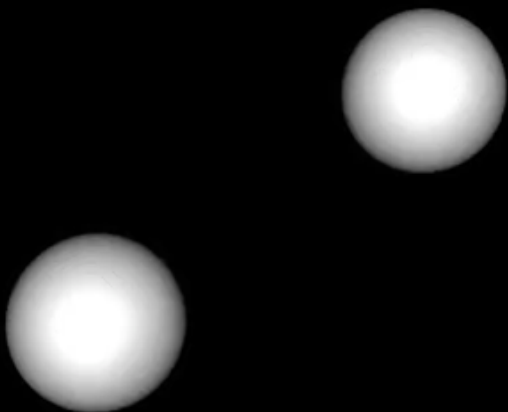
- T. Kawamura, **B. Giacomazzo**, W. Kastaun, R. Ciolfi, A. Endrizzi, L. Baiotti, R. Perna 2016, PRD 94, 064012
  - First study of different “high-mass” models (two EOSs, two mass ratios, different magnetic field orientations)
  - All models started with  $B \sim 10^{12} \text{G}$  (vs  $\sim 10^{16} \text{G}$  of Ruiz et al 2016)
- R. Ciolfi, W. Kastaun, **B. Giacomazzo**, A. Endrizzi, D. M. Siegel, R. Perna 2017, PRD 95, 063016
  - Studied 6 different models with 3 EOSs and 2 mass ratios
  - All models had the same total gravitational mass at infinity (2.7 solar masses) and the same magnetic energy (initial magnetic field  $\sim 10^{15} \text{G}$ )

All simulations performed with **WhiskyMHD + EinsteinToolkit**.



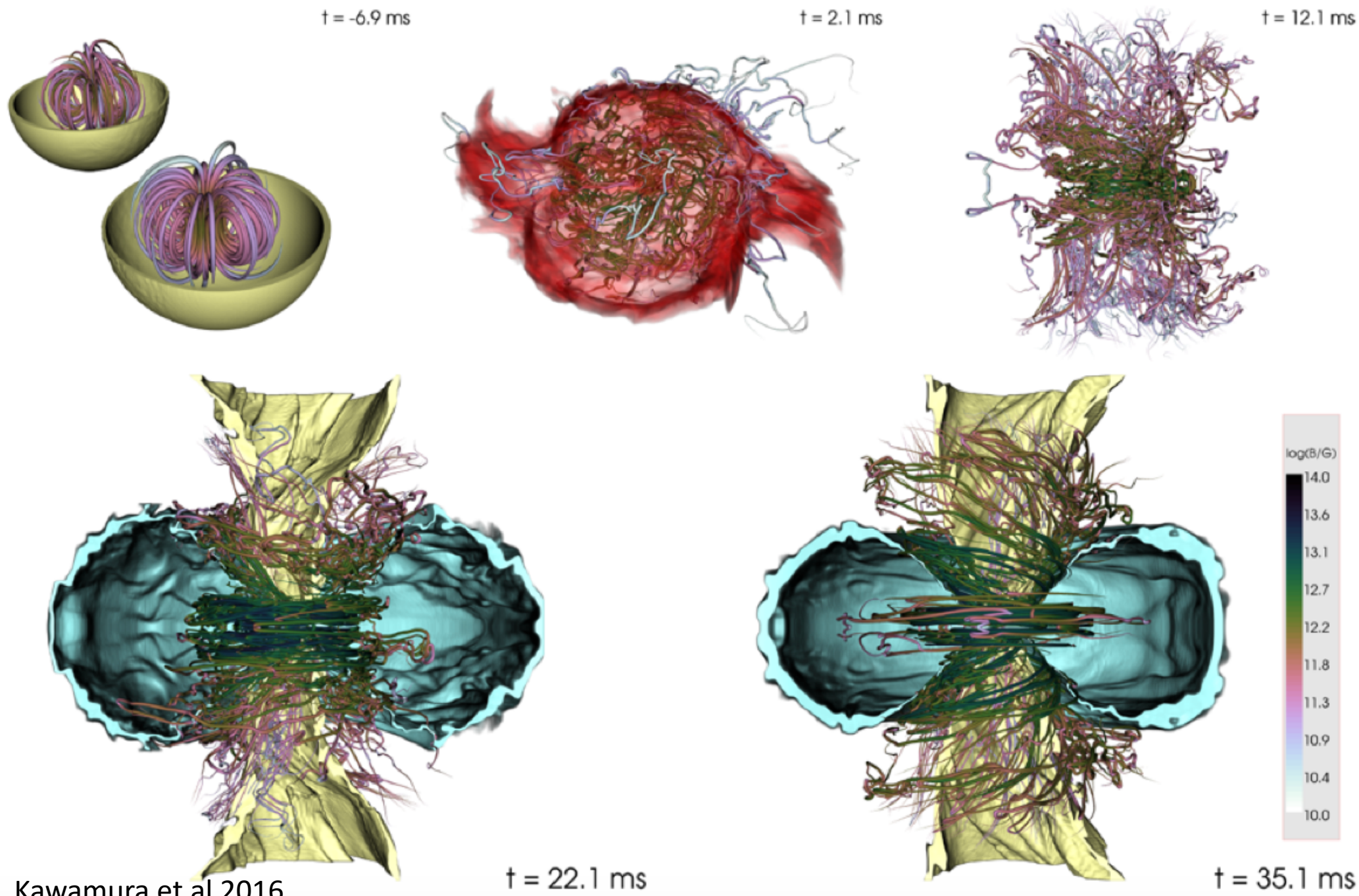


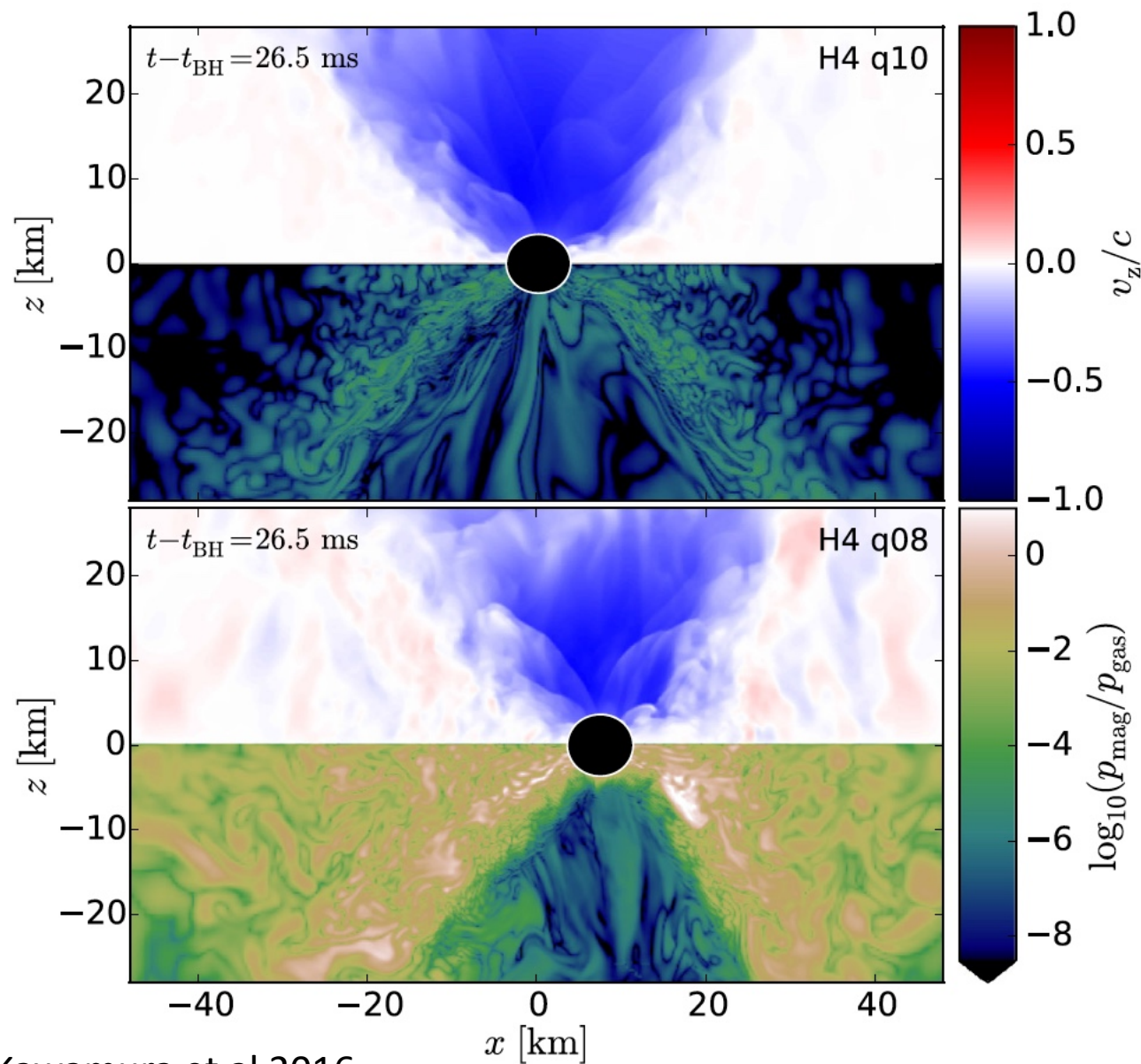
$t = 0.0 \text{ ms}$



<https://youtu.be/UIBaq5v7oL4>

# Magnetic Field Structure Evolution



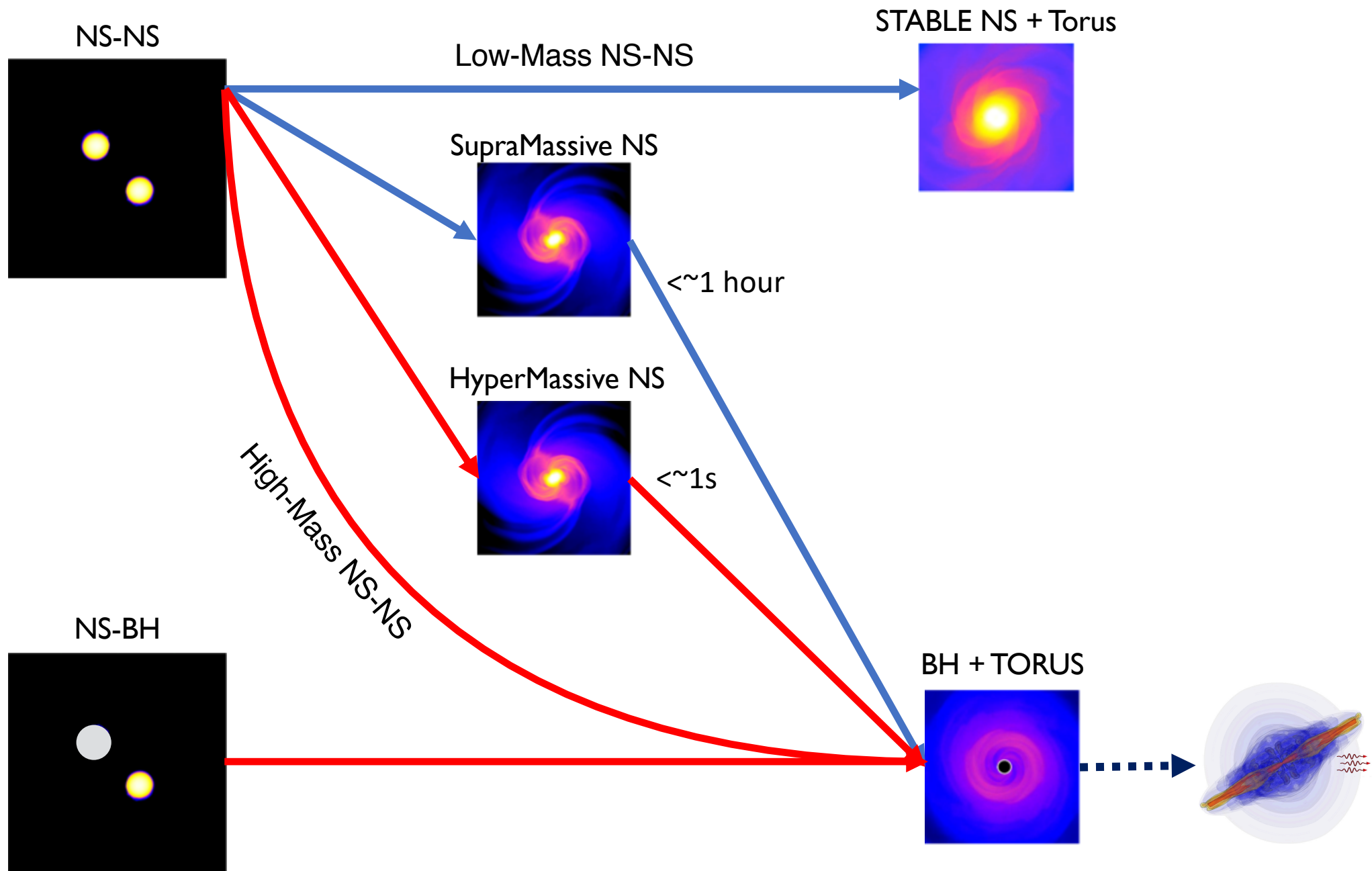


Kawamura et al 2016

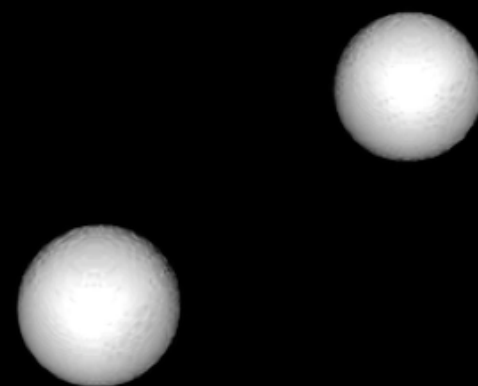
No Jet observed, but it may change with longer evolutions and much **higher resolutions** (e.g., Kiuchi et al 2015) or by using a **subgrid model** (e.g., Giacomazzo et al 2015).

Necessary to have a magnetically dominated funnel to launch a jet (Ruiz et al 2016 starts sims with  $\sim 10^{16} \text{G}$ ).

# Neutron Star Binary Mergers

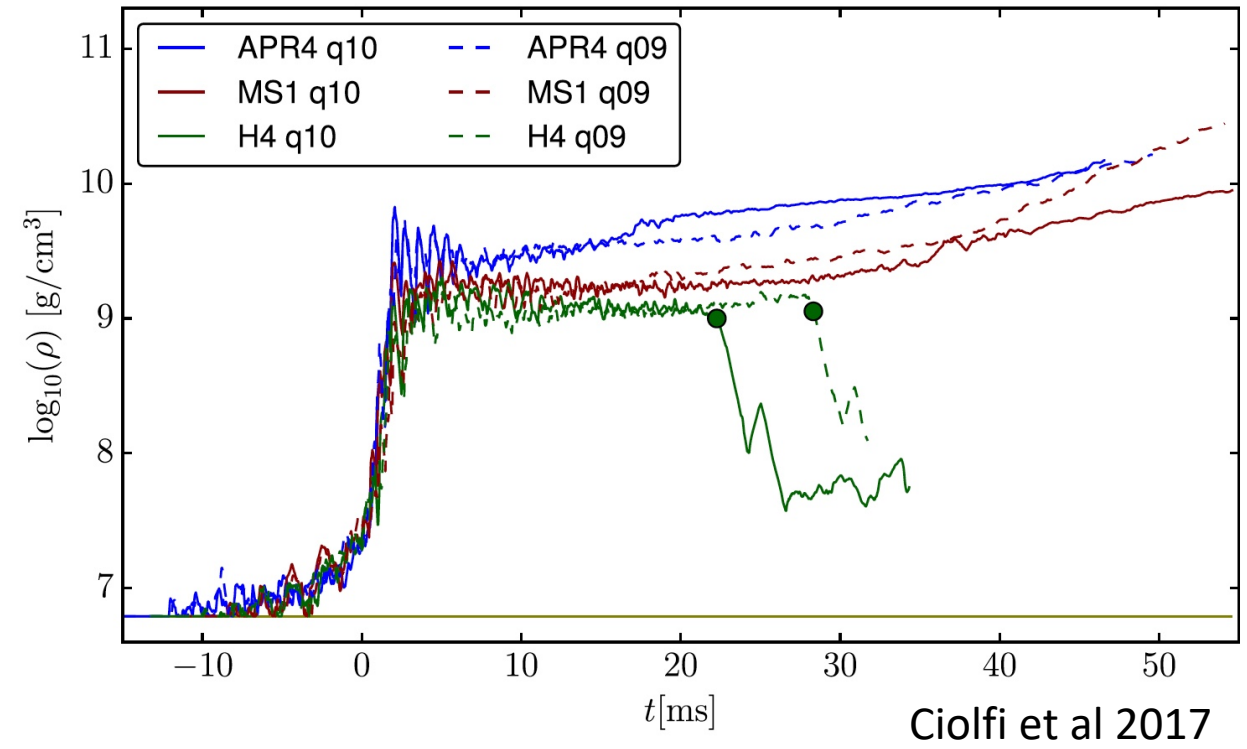
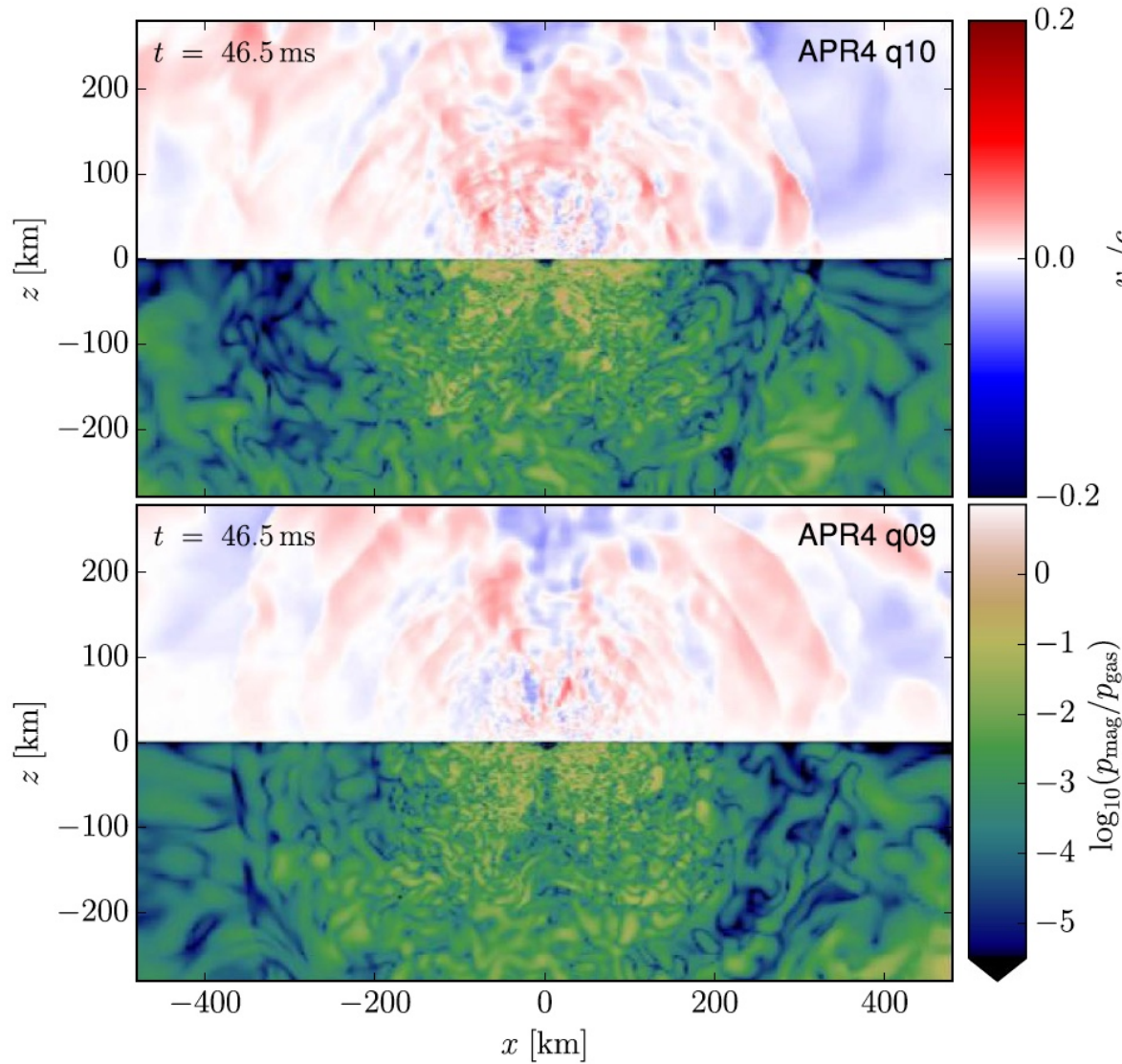


$t = 0.0$  ms



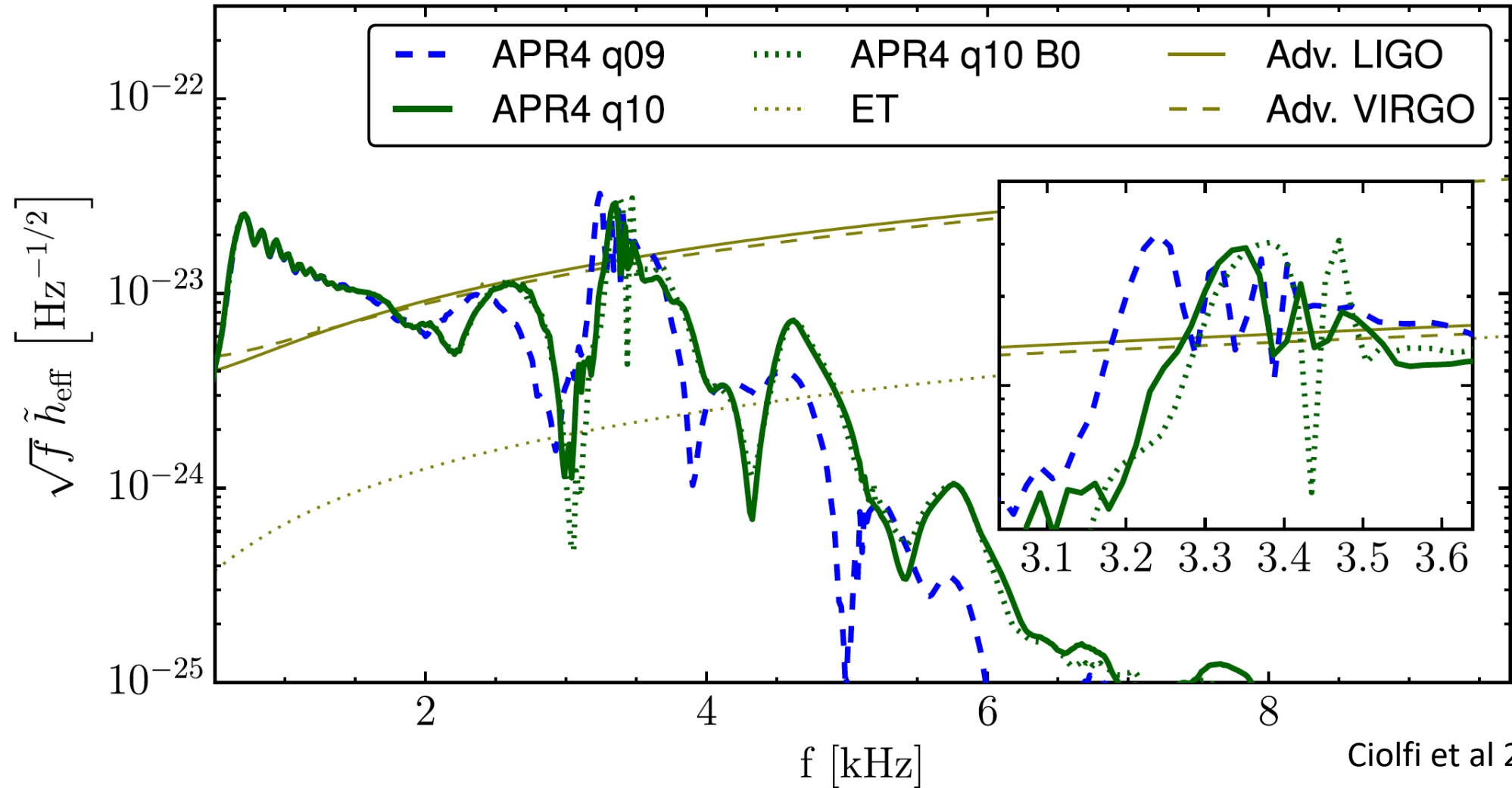


# SHORT- OR LONG-LIVED REMNANT?



No magnetically dominated funnel.  
Baryon pollution problem when a (long-lived) NS is formed instead of a BH.

# Magnetic Field Effects on Post-Merger GW Emission



Evolved “low-mass” BNS with high magnetic fields ( $\sim 10^{15}$  G during inspiral,  $\sim 10^{16}$  G after merger). Difference in the post-merger peak of less than  $\sim 100$  Hz.

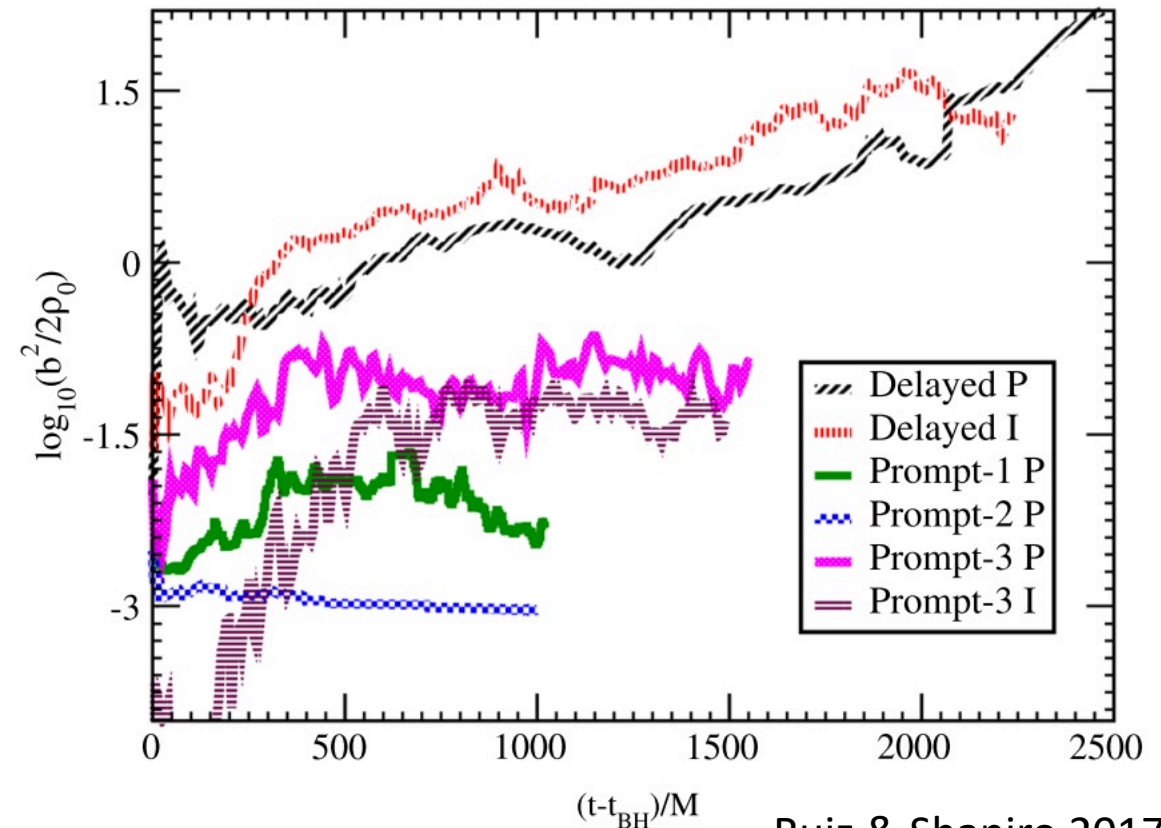
# Open Problem: Do all “High-Mass” BNS launch jets?

Ruiz & Shapiro 2017 run a set of 2 equal and 1 unequal-mass BNS mergers with ideal-fluid EOS and large initial magnetic field ( $B \sim 10^{16} \text{G}$ ).

Considered models that result in prompt collapse to BH after merger (no HMNS phase).

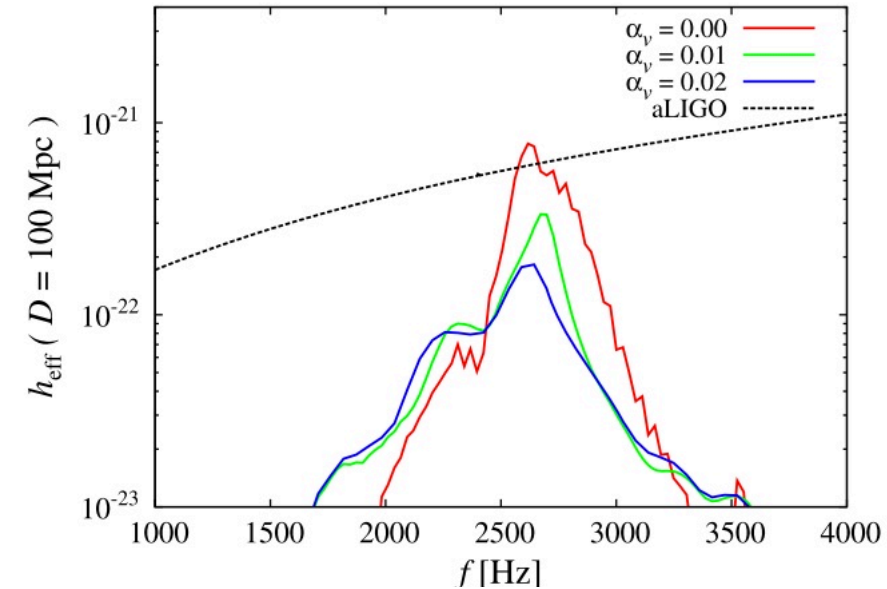
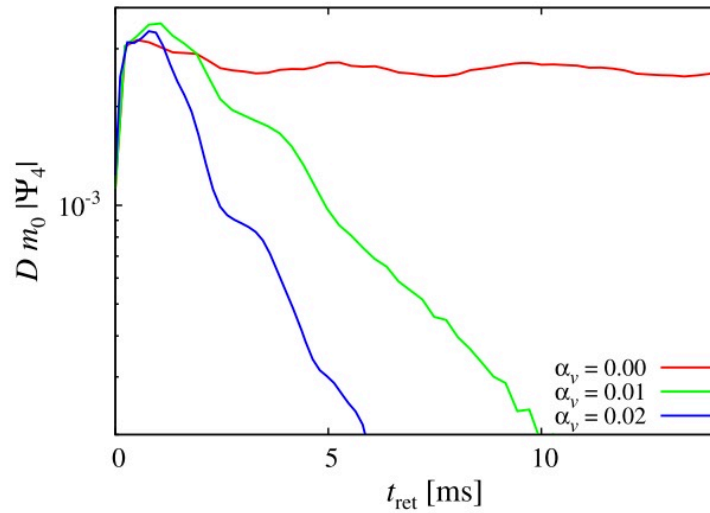
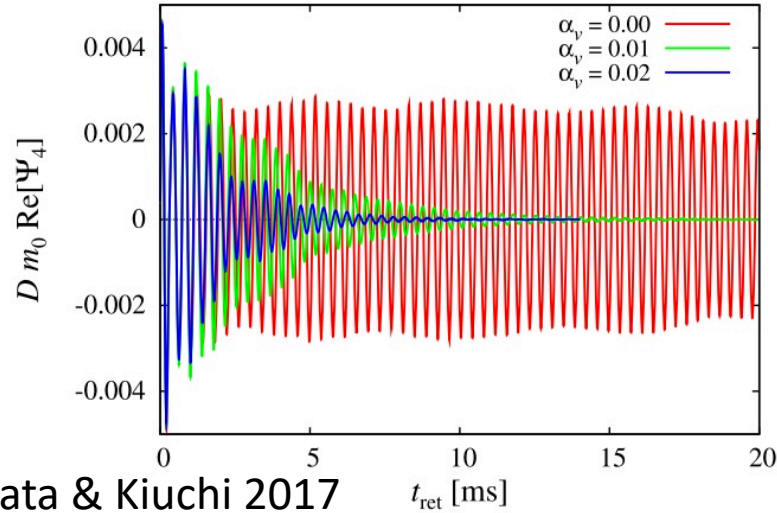
All prompt collapse models do not launch a jet and do not produce a magnetically dominated region.

Delayed collapse necessary to produce SGRB?





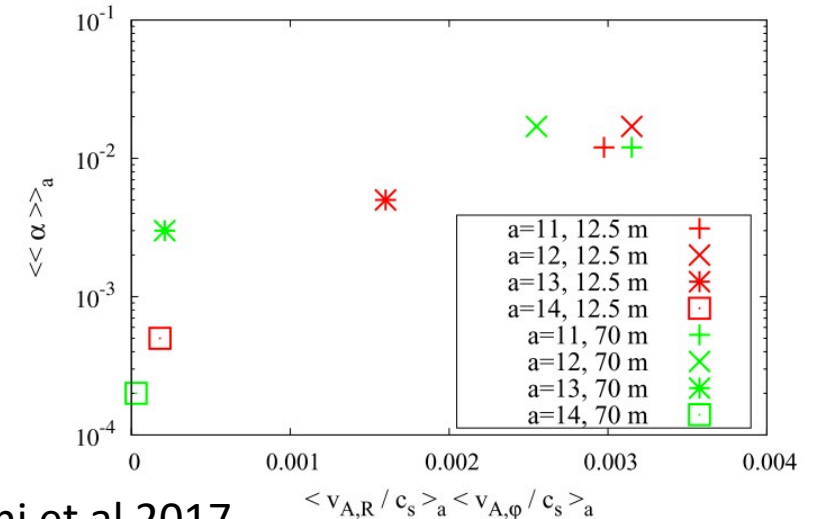
# Open Problem: Magnetic Field Effects in the PostMerger



Shibata & Kiuchi 2017 state that strong magnetic fields can damp quickly the GW signal (result obtained using viscosity as a model for magnetic field effects).

Kiuchi et al 2017 performed ultra high resolution ( $dx=12.5$  m) simulation of BNS post-merger remnant with magnetic fields.

Magnetic field amplified via KH up to 1% of thermal energy and may act as viscosity with  $\alpha_{\text{max}} \sim 0.001-0.02$ .

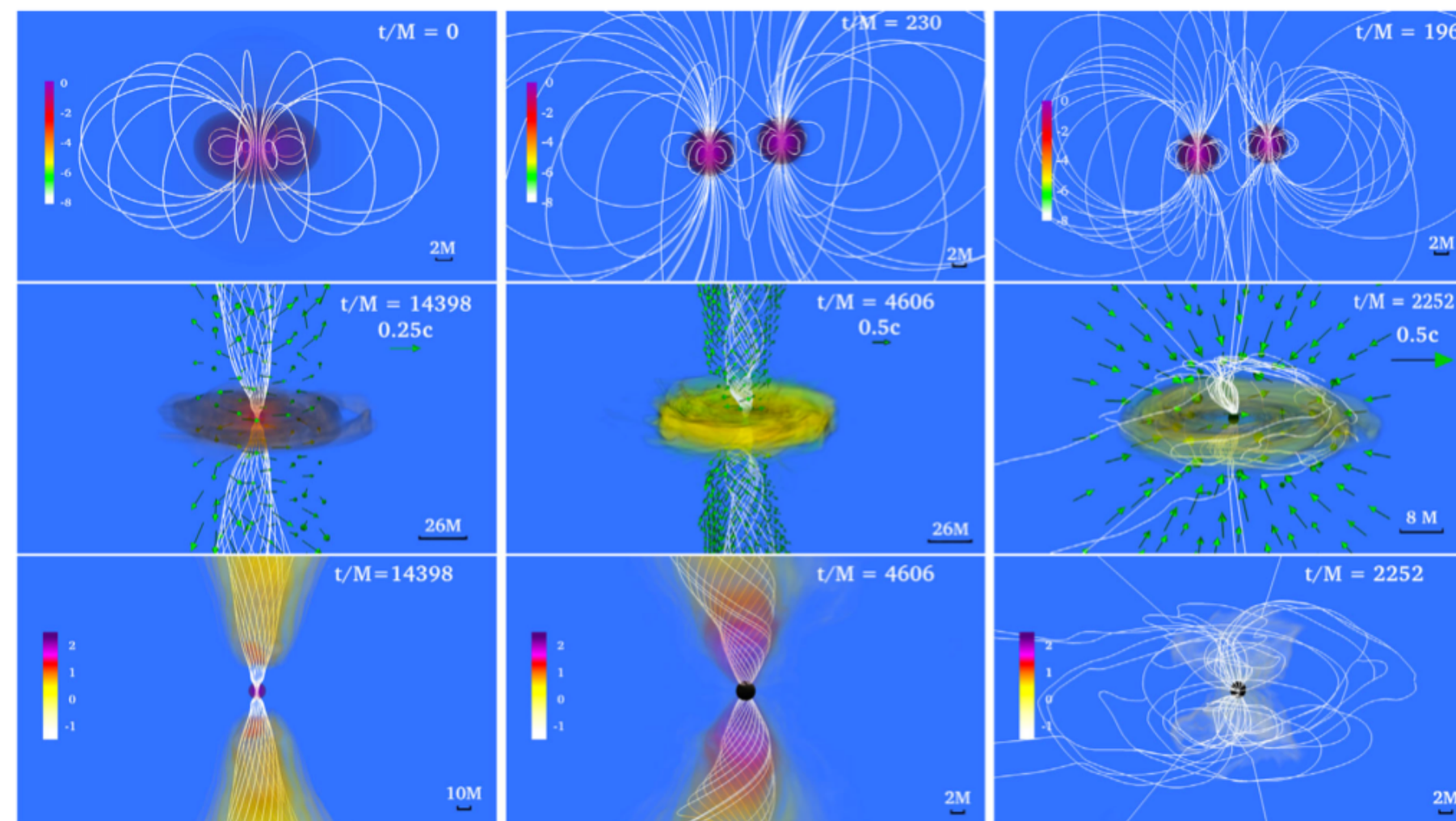


# Using GW and GRB to Infer Maximum NS Mass

SMNS

HMNS

BH



In order to produce a jet it seems necessary to have an HMNS phase followed by BH collapse.

This would constrain the maximum mass to  $M_{\text{max}} \sim 2.15-2.28$  in order to explain GW170817 and GRB 170817A

# CONCLUSIONS

- Open source codes can be used now to study binary neutron star mergers (Einstein Toolkit)
- Several BNS sims now with piecewise polytropes, cold tabulated EOSs, and a few finite temperature EOSs
- Neutrino effects still poorly studied (very few simulations include absorption by ejecta)
- Magnetic fields are crucial to explain GRBs, but only one code reported jet formation and with a simple Ideal Fluid EOS
- Magnetic field effects on GWs seem minimal, but discussion still going on in the community
- Simulations of BNS mergers in alternative theories of gravity are still limited (due to well-posedness problem)