

The effect of rotation and non-canonical mixing on CEMP stars surface distributions

Sergio Cristallo, Luciano Piersanti

INAF - Osservatorio Astronomico di Teramo

INFN - Sezione di Perugia



Summary

- An overview on the mechanisms at the origin of the ^{13}C pocket (major neutron source in low-mass AGBs);
- Models vs. Observations at low metallicities;
- The effects induced by rotation at low metallicities;
- The occurrence of the i-process at low metallicities;
- Alternative solutions

F.R.U.I.T.Y.

FULL-Network Repository of Updated Isotopic Tables & Yields

F.R.U.I.T.Y.
(FULL-Network Repository of Updated Isotopic Tables & Yields)

Select Data:

MODEL SELECTION	OUTPUT SELECTION	OUTPUT FORMAT	
Mass (M_{\odot}) ---	Nuclides Properties <input type="radio"/> Elements ^(3,4) Z: All <input type="radio"/> Isotopes ⁽⁵⁾ A: All Z: All <input type="radio"/> s-process ⁽⁶⁾ : [hs/ls], [Pb/hs], ... <input type="radio"/> Net ⁽⁸⁾ Yields ⁽⁷⁾ A: All Z: All <input type="radio"/> Total	Multiple Table format ⁽¹⁰⁾	Single Table format ⁽¹¹⁾
Metallicity (Z) ⁽¹⁾ ---		<input checked="" type="radio"/> All Dredge Up Episodes ⁽¹²⁾	<input type="radio"/> Final Composition
Initial Rotational Velocity (IRV) ⁽²⁾ 0		<input type="radio"/> Final	<input type="radio"/> Final
¹³ C Pocket ⁽⁹⁾ Standard			

[NOTES ON THE MODELS \(pdf file\)](#)

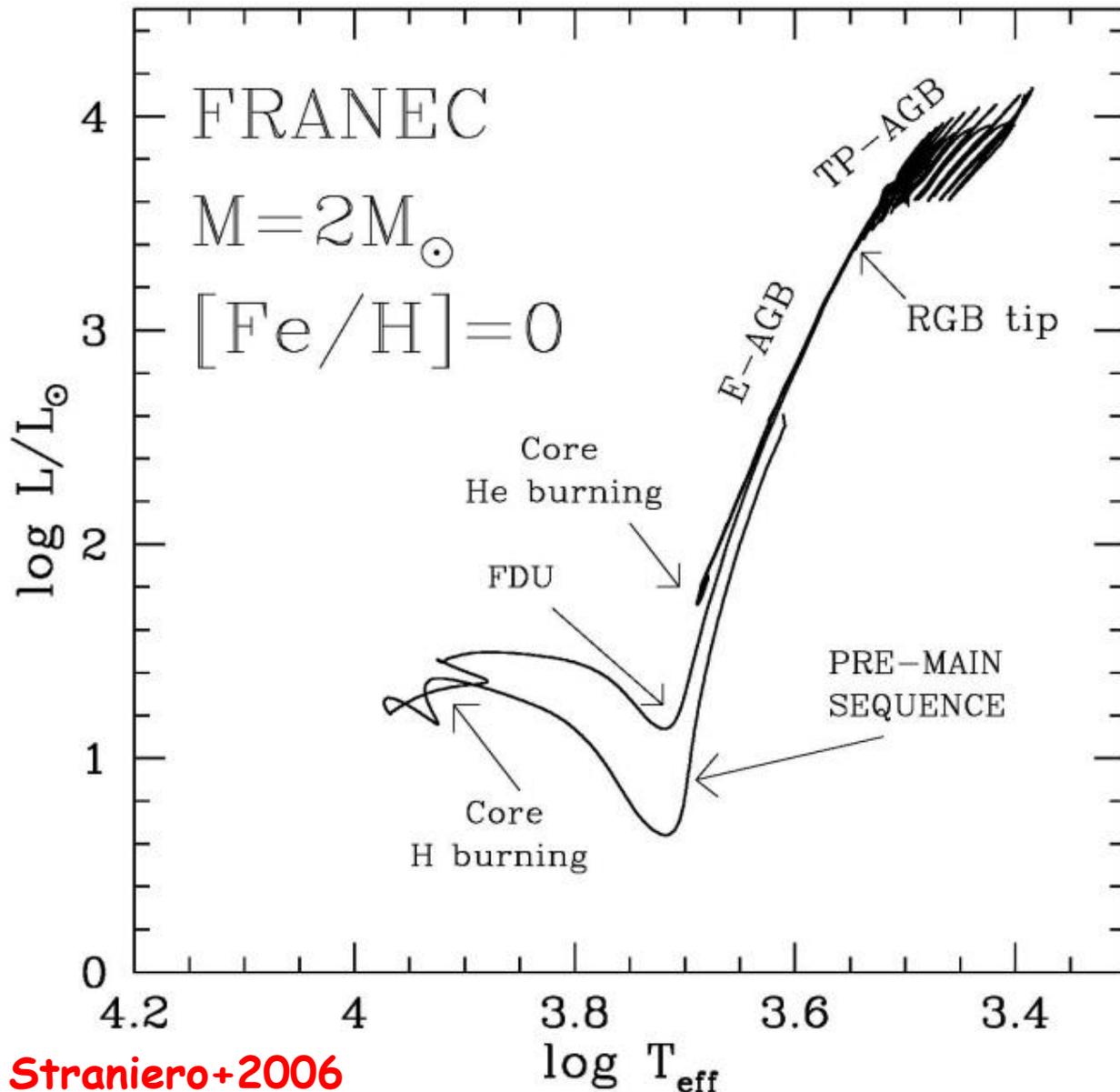
SC+ 2011, 2015

fruity.oa-abruzzo.inaf.it

$-2.85 \leq [\text{Fe}/\text{H}] \leq +0.15$

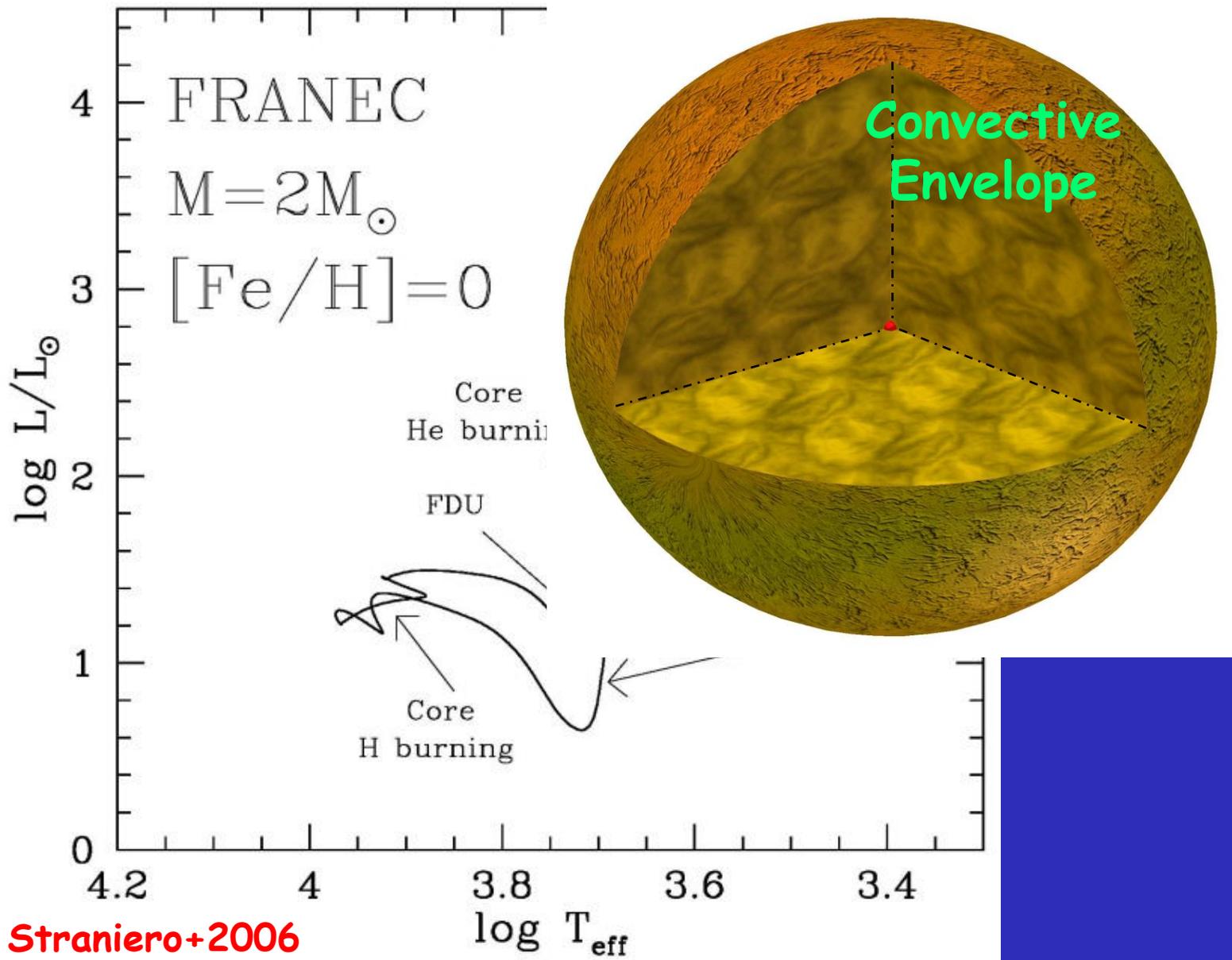
$1.3 \leq M/M_{\text{sun}} \leq 6.0$

Theoretical HR diagram



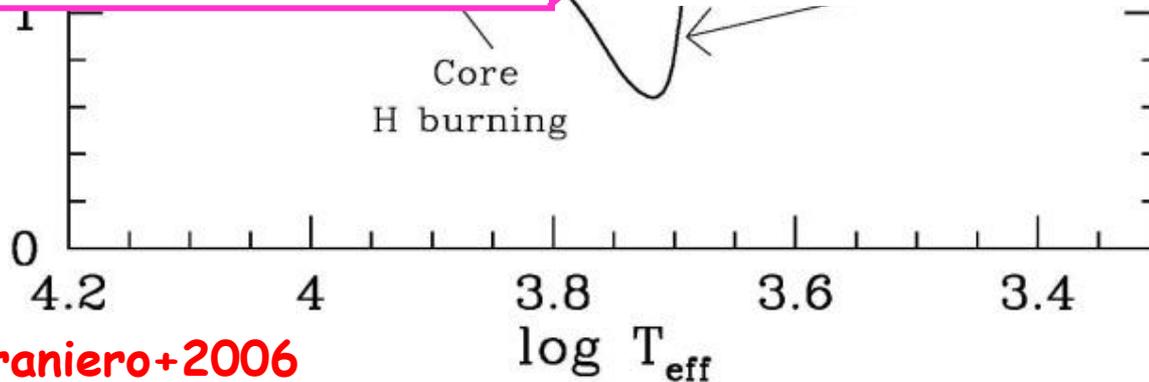
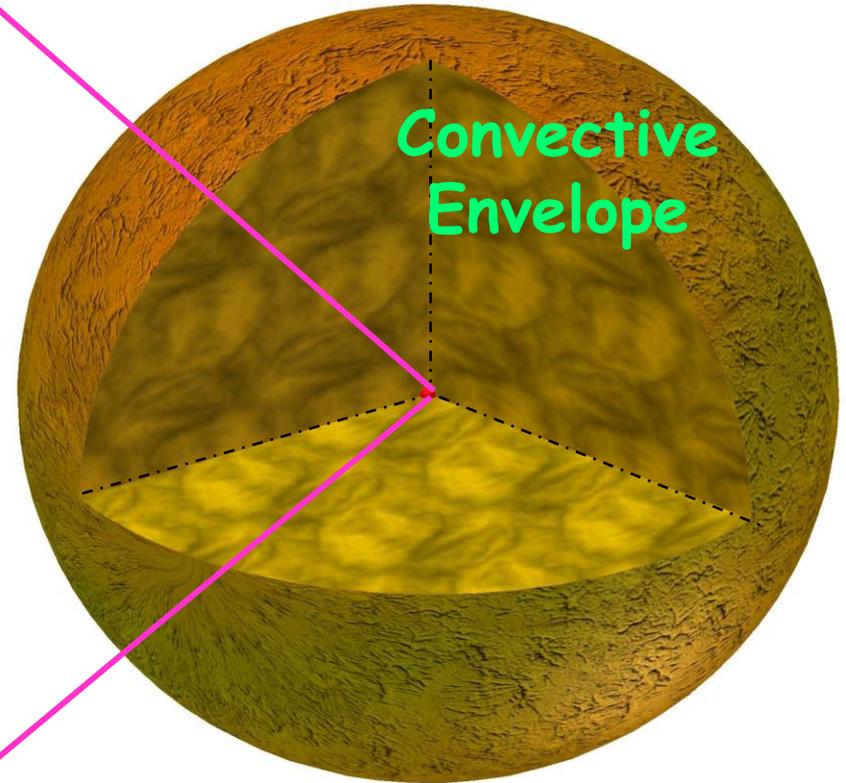
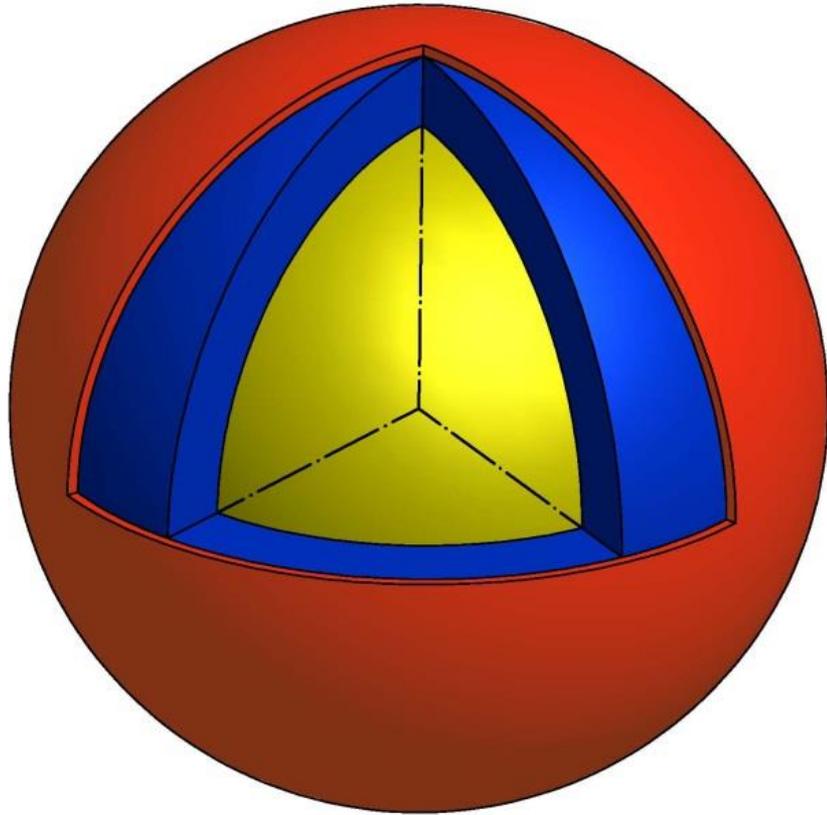
Straniero+2006

Theoretical HR diagram



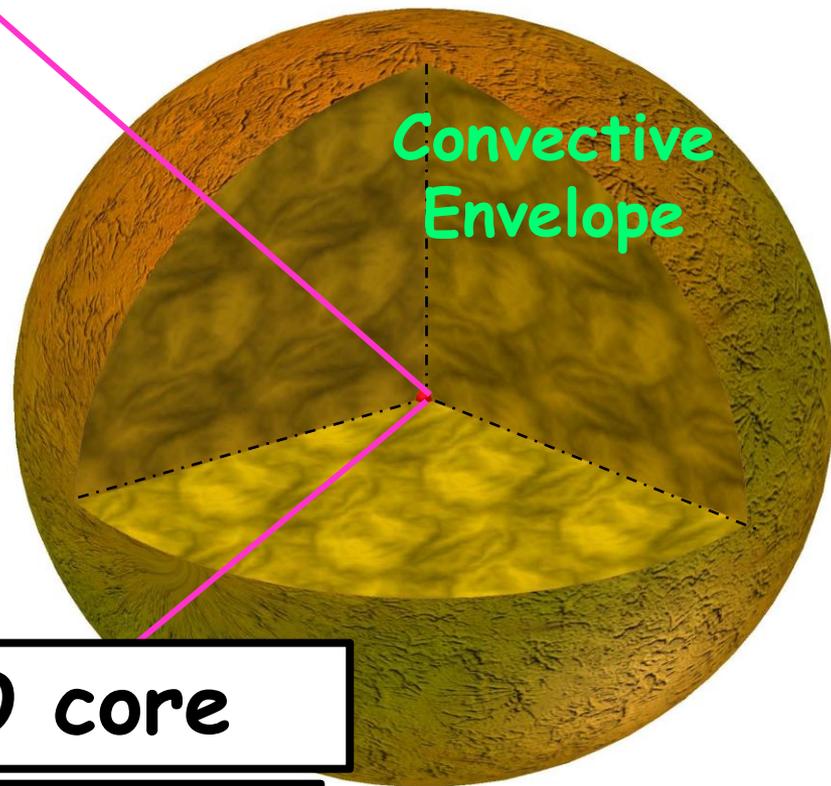
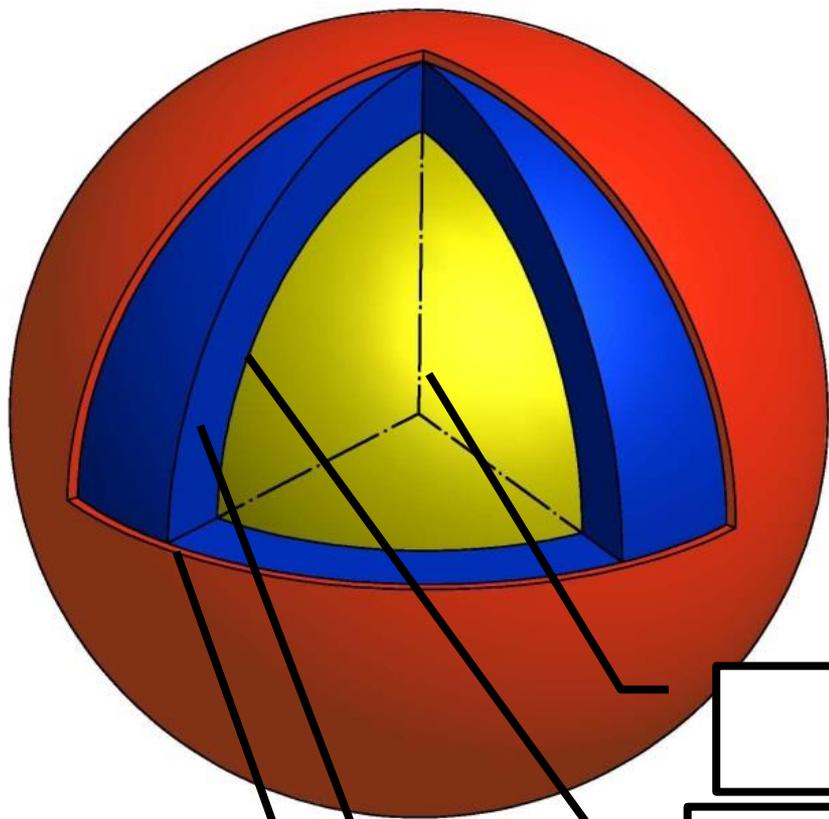
Straniero+2006

Theoretical HR diagram



Straniero+2006

Theoretical HR diagram

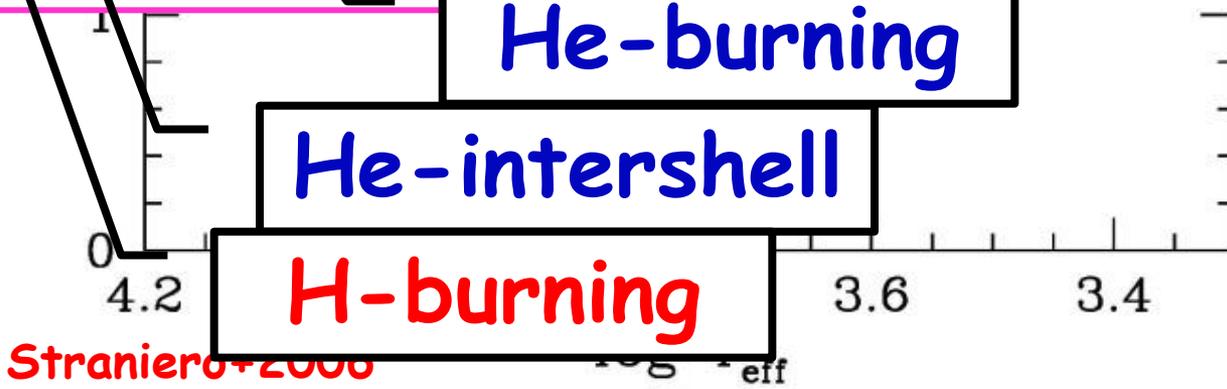


CO core

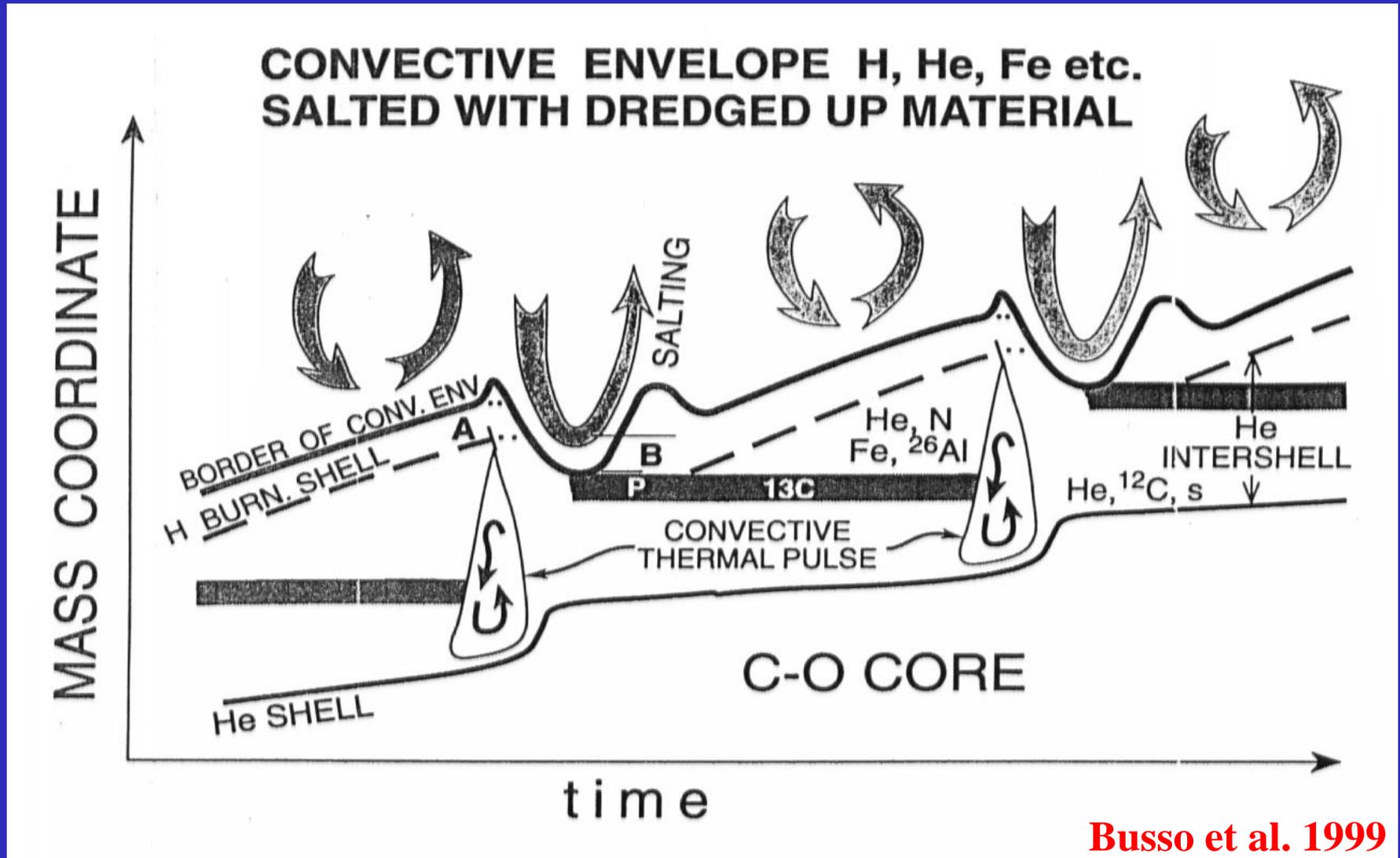
He-burning

He-intershell

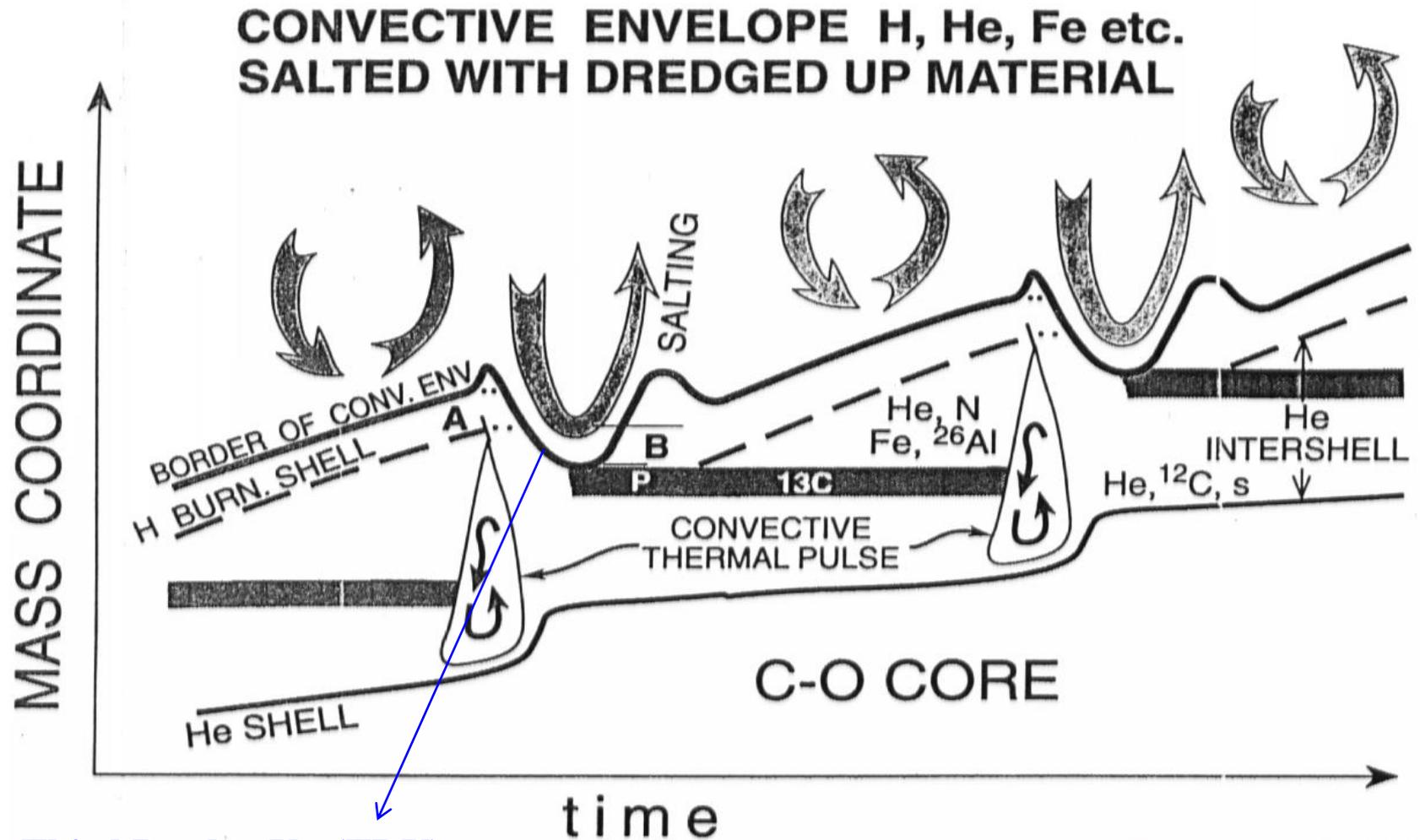
H-burning



The s-process in AGB stars



The s-process in AGB stars



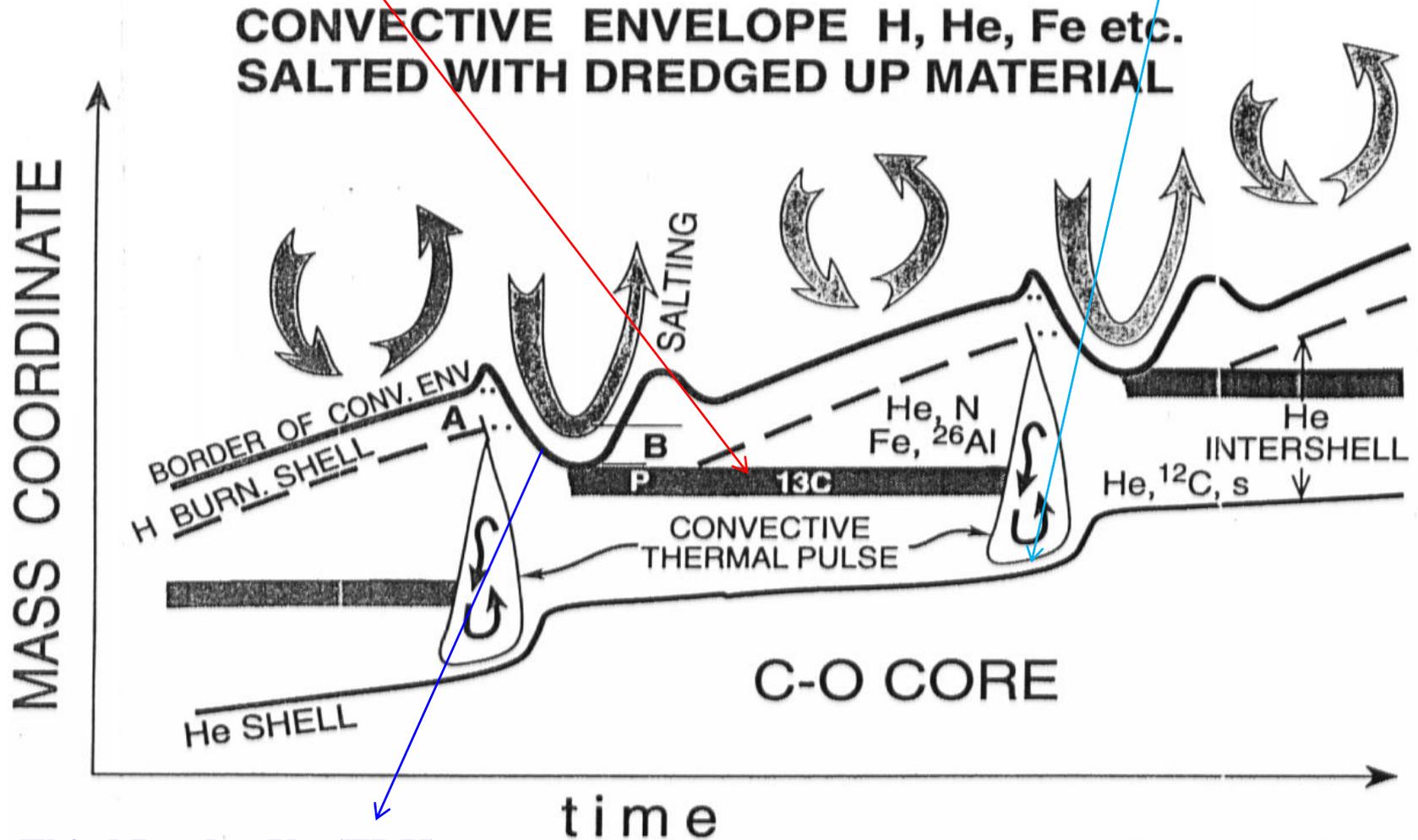
Third Dredge Up (TDU)

Busso et al. 1999

The s-process in AGB stars

$^{13}\text{C}(\alpha, n)^{16}\text{O}$ reaction

$^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$ reaction



Third Dredge Up (TDU)

Busso et al. 1999

The ^{13}C pocket in stellar evolutionary models

- ✓ **Opacity induced overshoot (SC+...)**
- ✓ **Convective Boundary Mixing + Gravity Waves (Battino+ 2017)**

The ^{13}C pockets in post-process calculations:

- ✓ **n-zones profile (Gallino+...)**
- ✓ **Exponential hydrogen profile (Lugaro+...)**
- ✓ **Magnetic-induced mixing (Trippella+ 2014)**

How does the ^{13}C pocket change?

- ✓ **Rotation-induced mixing (Herwig+ 2003; Siess+ 2004; Piersanti+ 2013)**

Opacity induced overshoot: a ballistic approach

Let's assume that the deceleration is proportional to the square of the velocity, as it happens to a body moving in a sufficiently dense fluid:

Viscosity

$$\dot{v} \propto -kv^{-2}$$

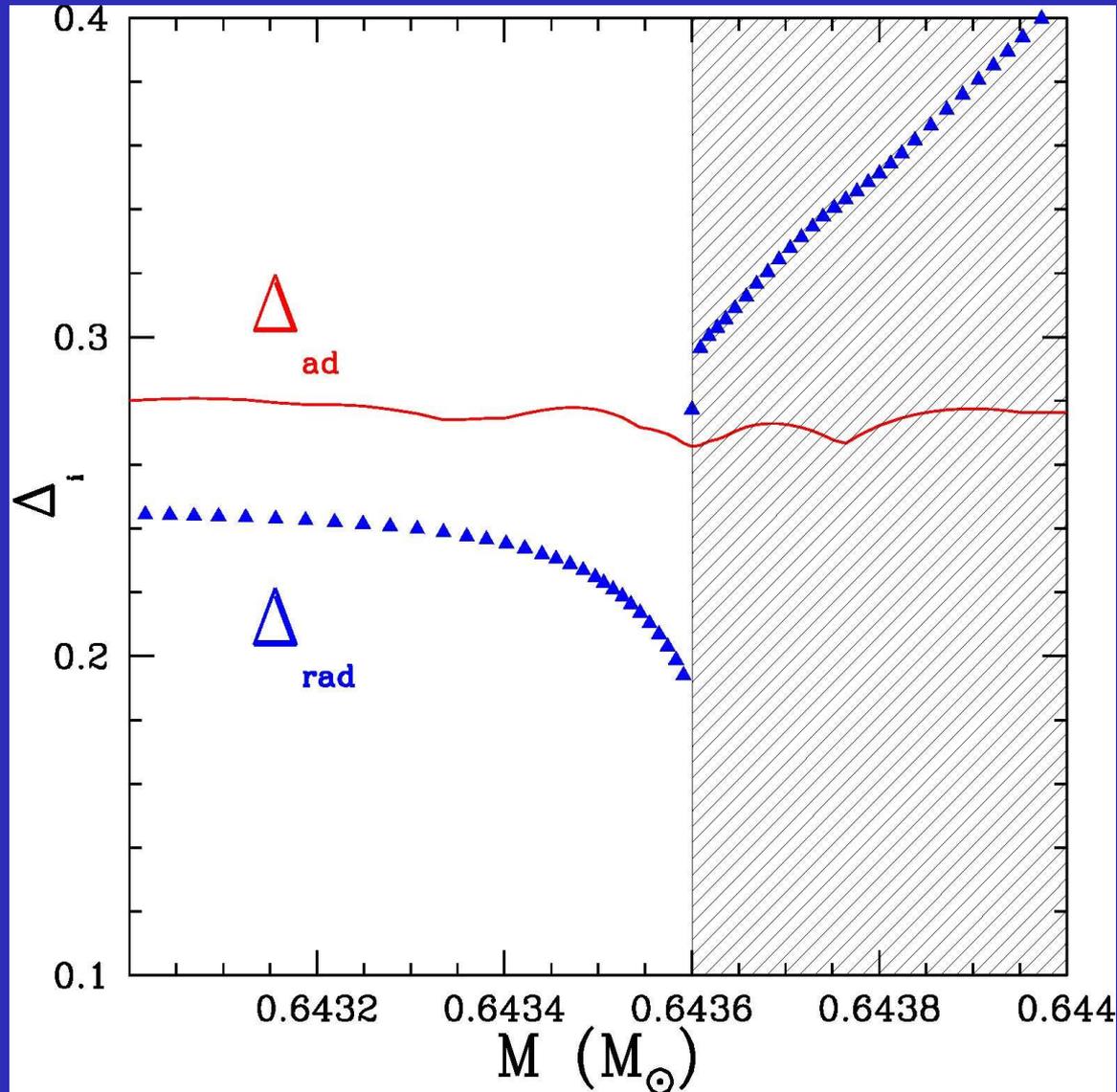
$$v = v_0 \exp[-k(r-r_0)]$$

$$v = v_{\text{bce}} \cdot \exp(-d/\beta H_p)$$

- v_{bce} is the convective velocity at the inner border of the convective envelope (*CE*)
- d is the distance from the *CE*
- H_p is the scale pressure height
- $\beta = 0.1$

The formation of the ^{13}C pocket

Opacity
induced
overshoot

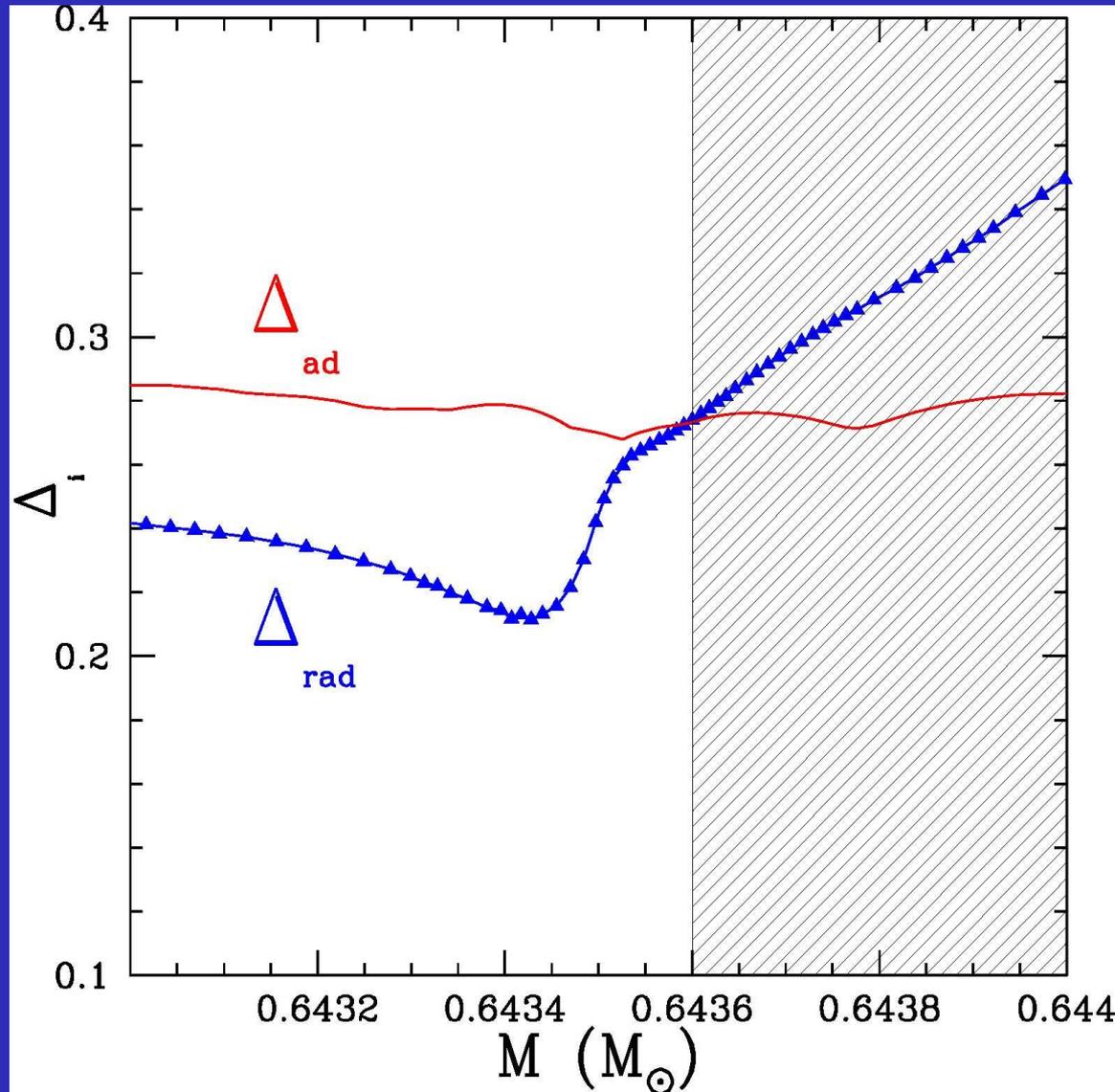


v=0 beyond SC

SC+2009

The formation of the ^{13}C pocket

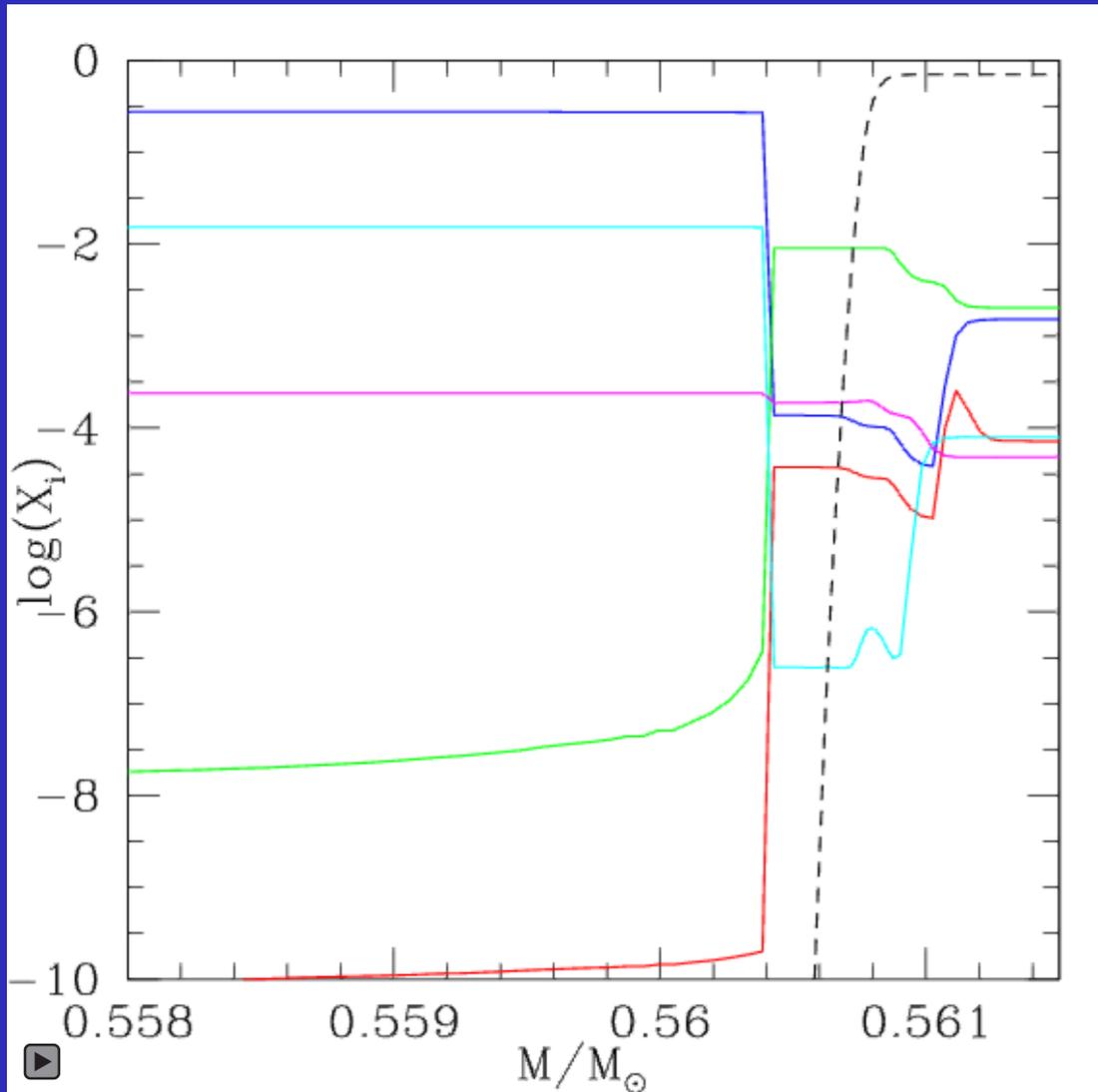
Opacity
induced
overshoot



$$v = v_{BCE} e^{-\frac{d}{\beta H_P}}$$

SC+2009

The formation of the ^{13}C pocket



^{12}C

^{13}C

^{14}N

^{22}Ne

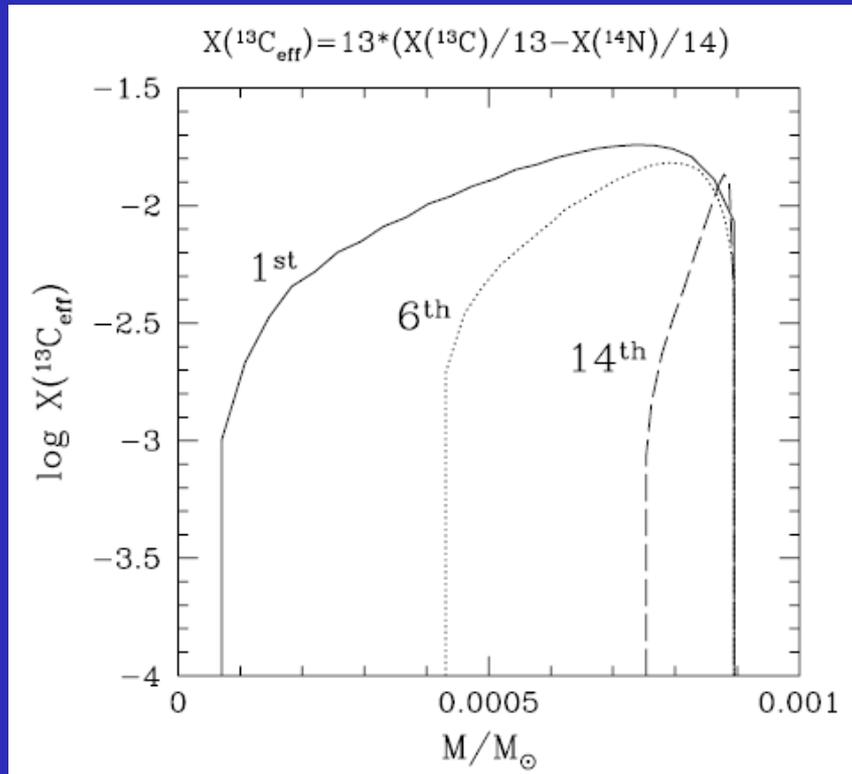
^{23}Na

H

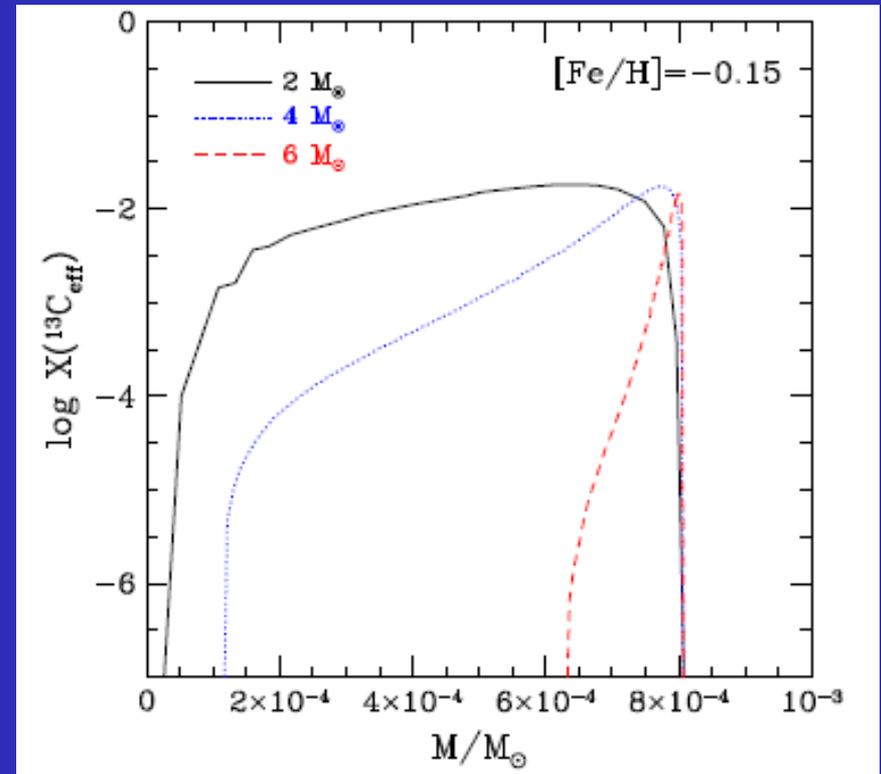
$M=2M_\odot$

$Z=Z_\odot$

Stellar model vs. post-process



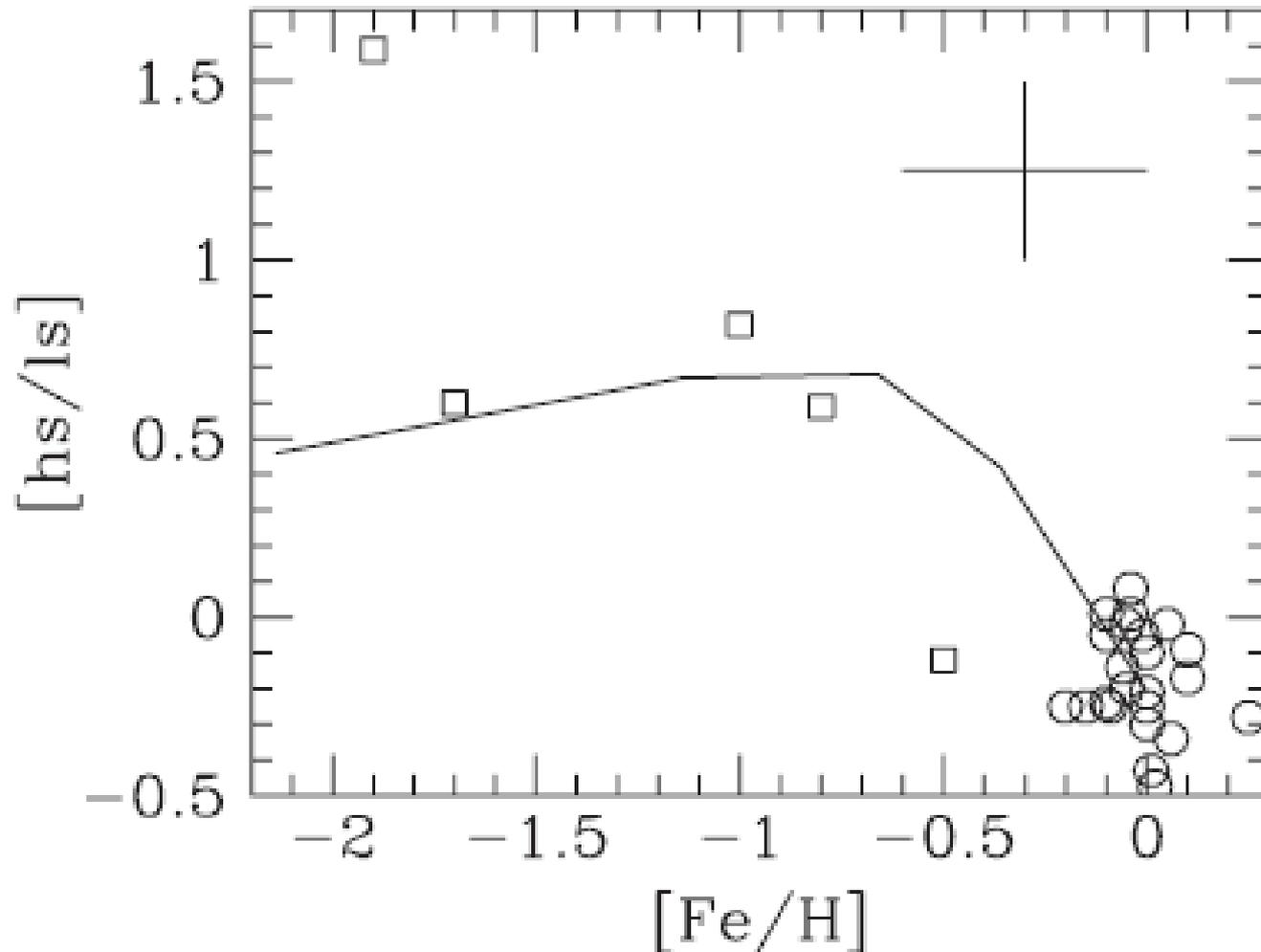
SC+2011



SC+2015

The pocket mass extension scales as the inverse of the core mass

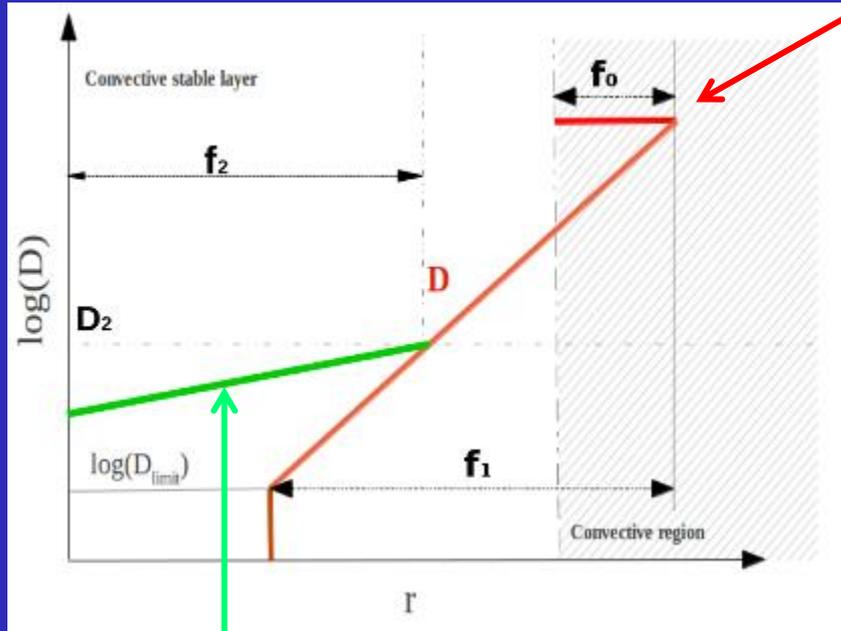
Comparison with observations



SC+2009

Convective Boundary Mixing + Gravity Waves

Battino+ 2016



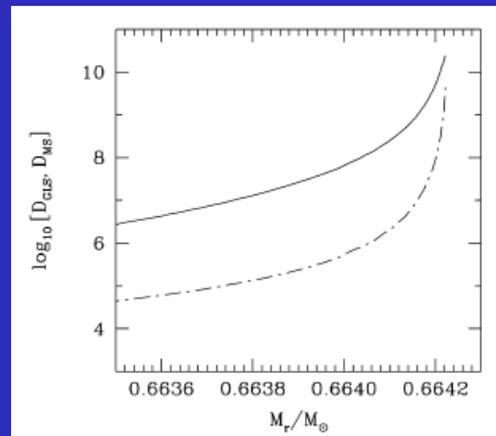
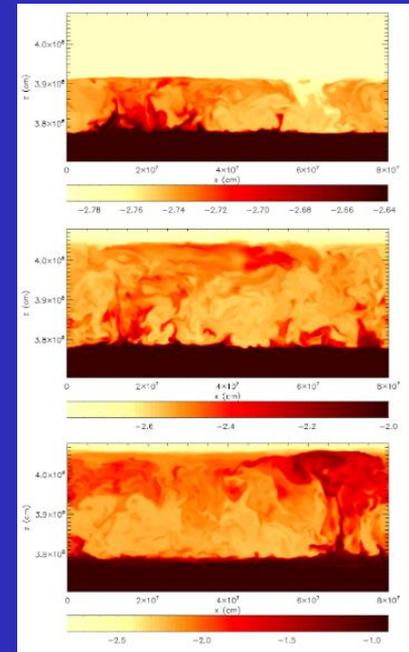
Gravity waves

Kelvin-Helmholtz (shear) instability

Casanova+ 2016

Depending on the velocity difference across the interface, K-H instability may induce mixing if:

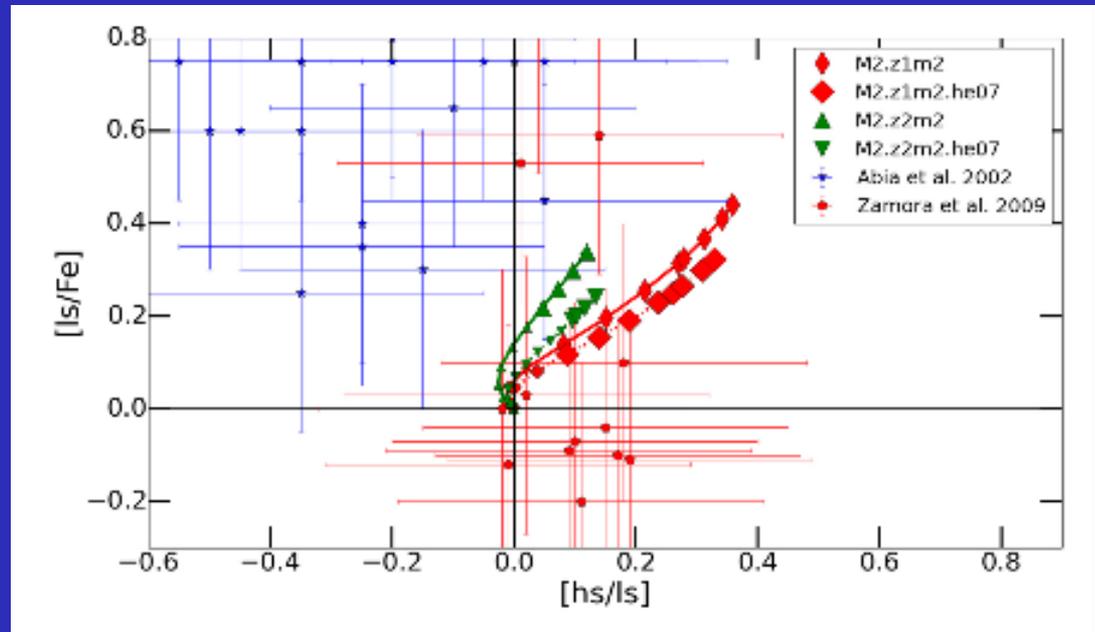
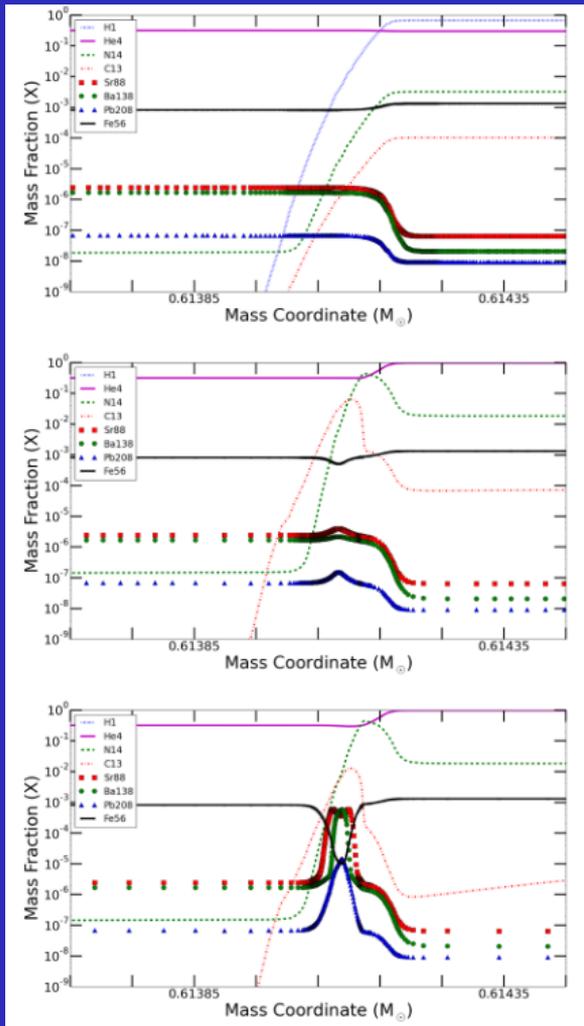
$$N^2 / (dv/dr)^2 < 0.25$$



Denissenkov & Tout 2003

Comparison with observations

Battino+ 2016



In agreement with observations, but pockets are very small

Post-processes

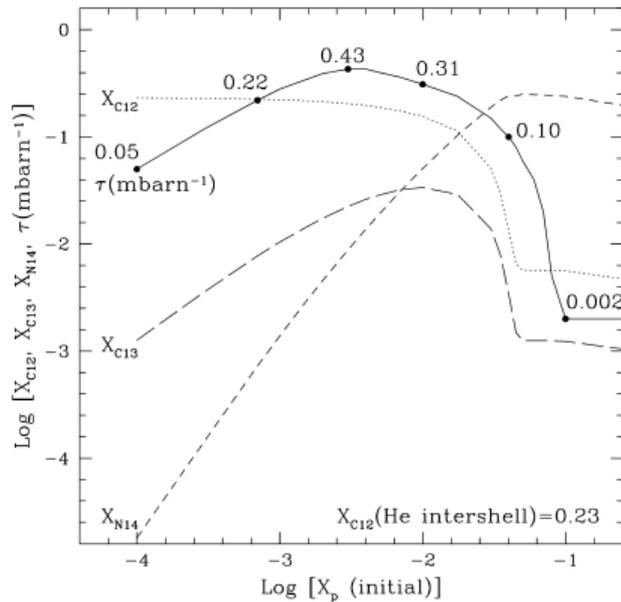


FIG. 4.—Resulting mass fractions of ^{12}C , ^{13}C , and ^{14}N as functions of the initial mass fraction of protons introduced below the H/He discontinuity during the simulations performed with the Monash nucleosynthesis code. The protons are introduced after the 10th TDU episode of the $3 M_{\odot}$ star of solar metallicity computed with the MSSSP code. Also plotted is the corresponding neutron exposure at the end of the interpulse period after all the ^{13}C has burnt.

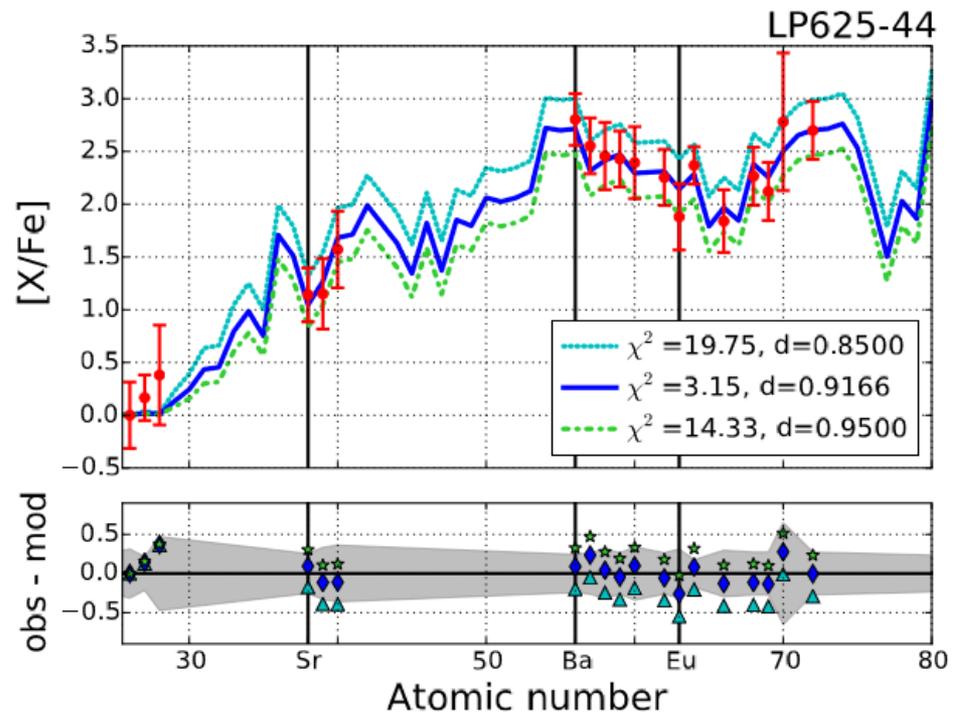
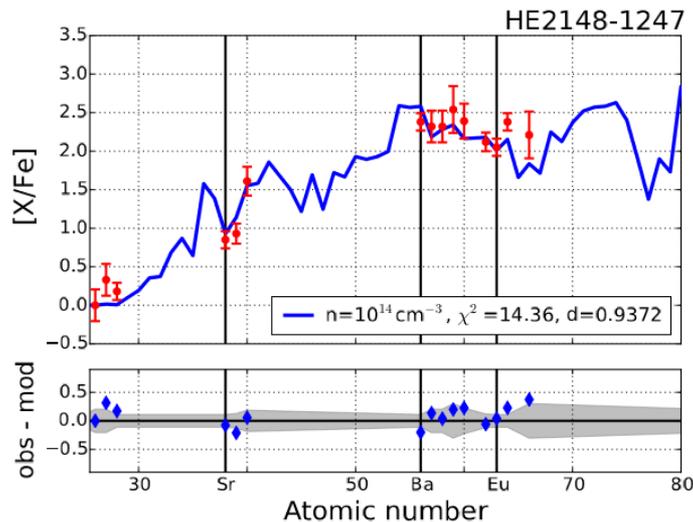
Artificially introduced an exponentially decaying profile of protons in Monash models (Karakas+...)

Similar to SC+2009, but they do not feed the change of physics quantities along the AGB.

Lugaro+ 2003

Post-processes

For CEMP stars analysis (i-process): Hempel+2016



See also Abate & Stancliffe 2016

Post-processes

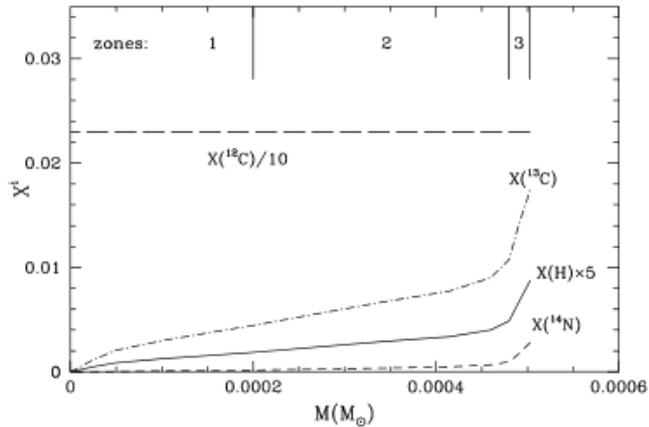
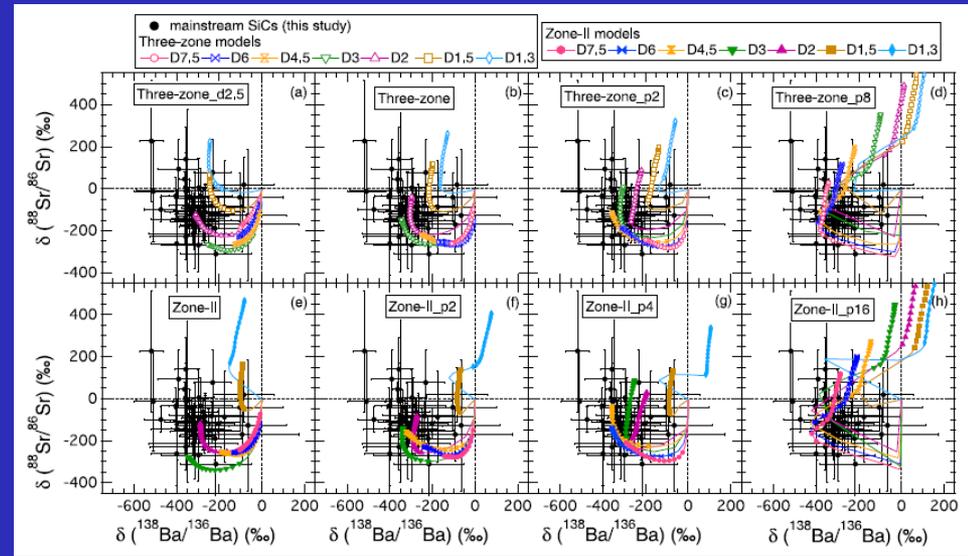


FIG. 1.—The adopted distribution in the mass of hydrogen introduced in the ^{12}C -rich intershell, and of the resulting ^{13}C and ^{14}N profiles at H-shell reignition, as discussed in the text.

Gallino+ 1998



Liu+ 2015

Strong points: versatility and speed

Torino Post-process

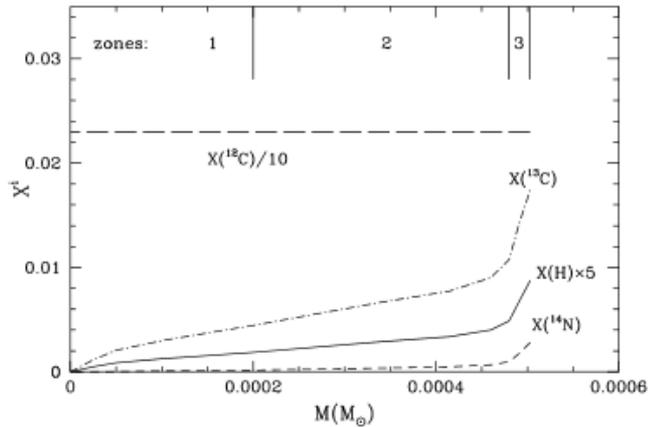
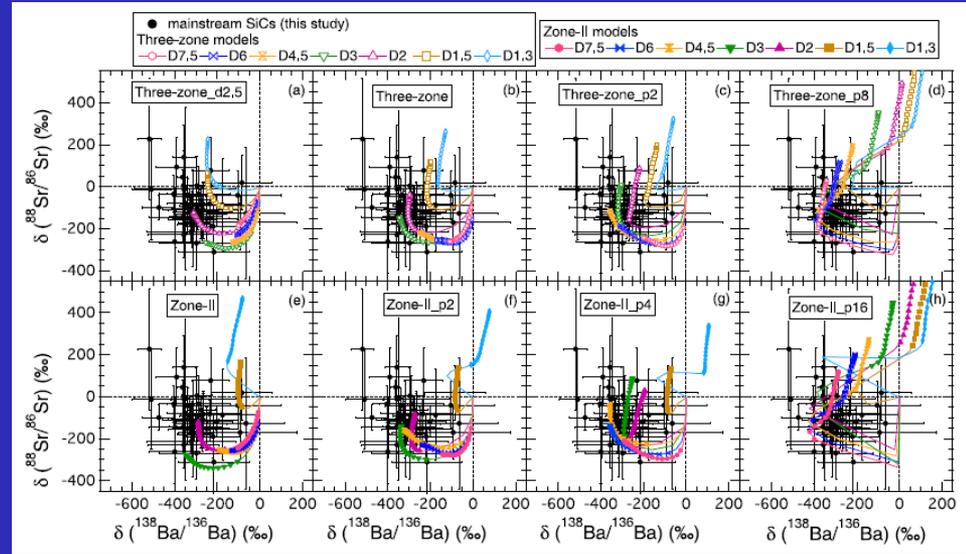


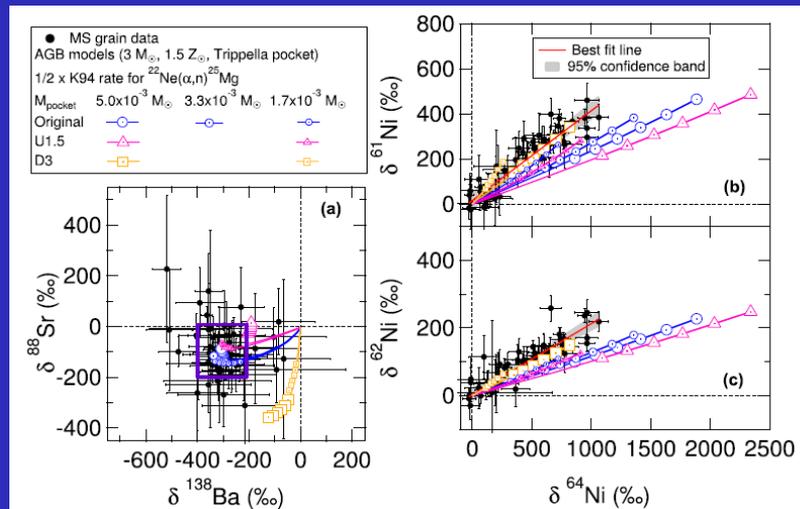
FIG. 1.—The adopted distribution in the mass of hydrogen introduced in the ^{12}C -rich intershell, and of the resulting ^{13}C and ^{14}N profiles at H-shell reignition, as discussed in the text.



Liu+ 2015

Gallino+ 1998

However, ...



Liu+ 2018

Magnetic induced mixing

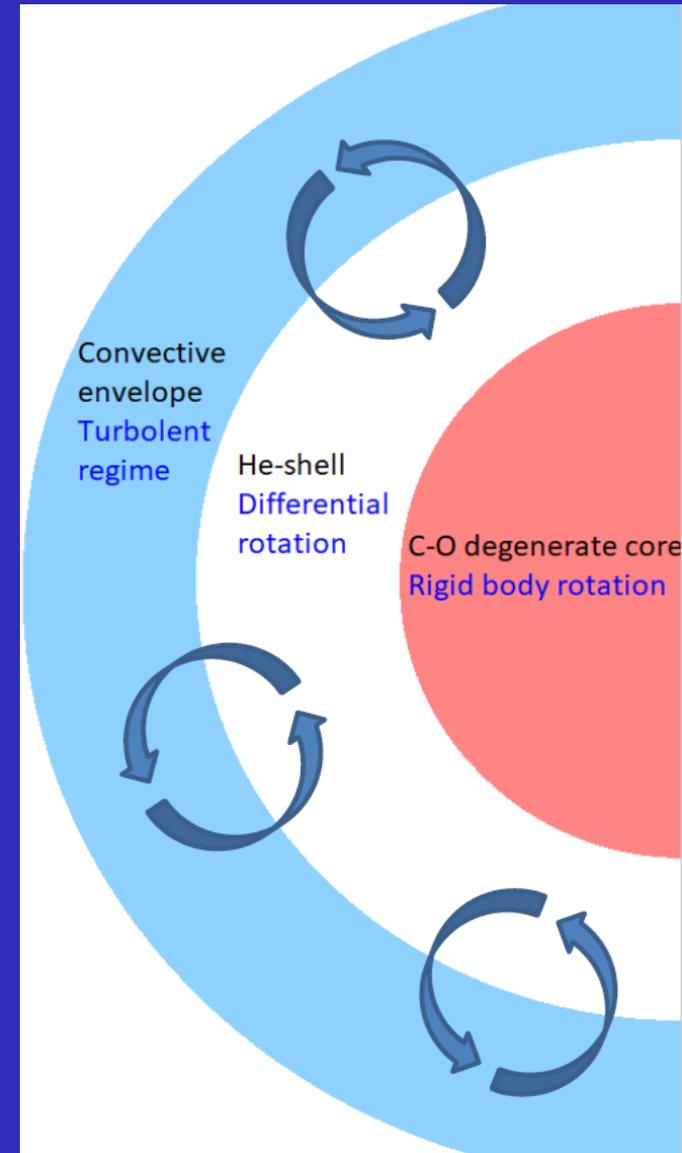
Nucci & Busso 2014

$$v_r = \frac{dw(t)}{dt} r^{-(k+1)}$$

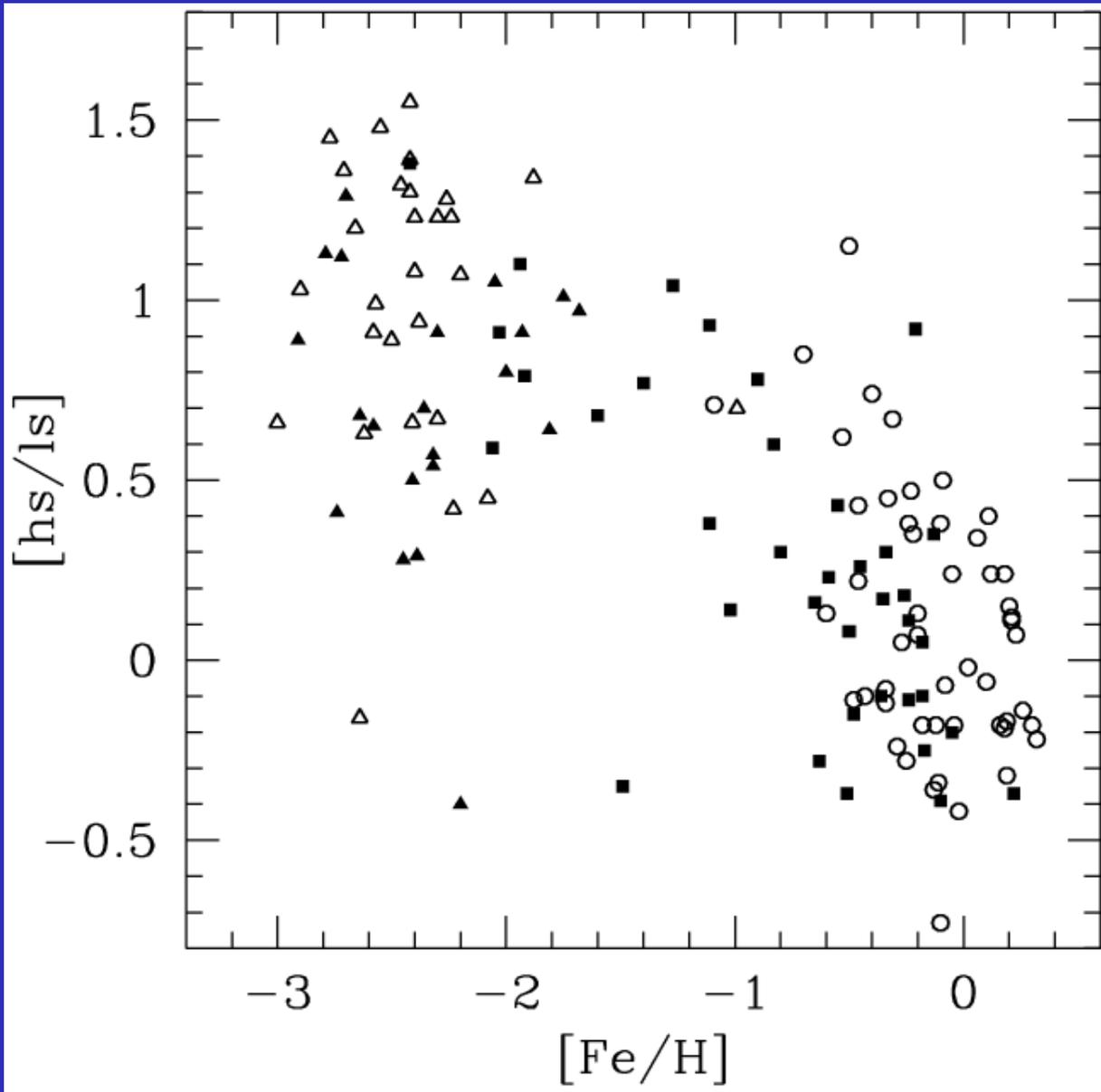
$$B_\varphi = \Phi(\xi)r^{k+1}, \quad [\xi = -(k+2)w(t) + r^{k+2}].$$

This morning: talk by D. Vescovi

$$v_{down}(r) = v(r_p) \frac{\rho(r_p)}{\rho(r_{h+1})} \left(\frac{r_h}{r_p}\right)^{k+2} \left(\frac{r_h}{r}\right)^{k+1}$$



The s-process at low metallicities



- Ba stars
- CH stars
- ▲ CEMP-s stars
- △ CEMP-sr stars

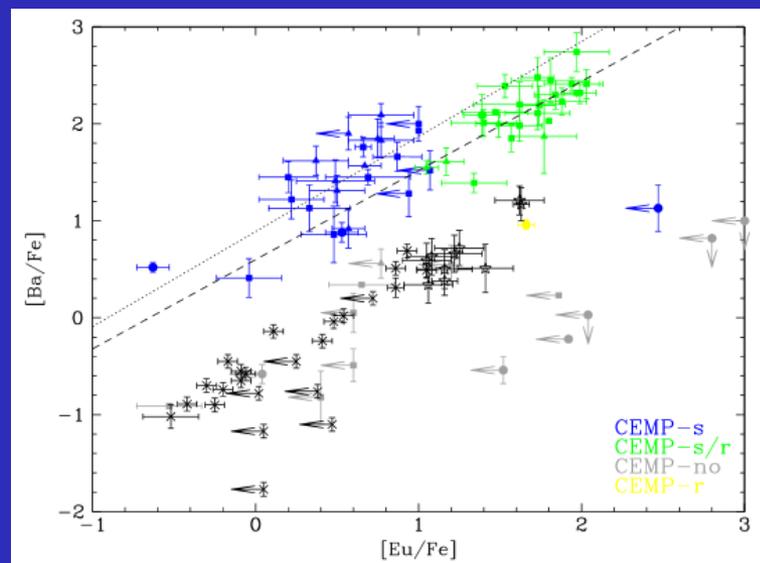
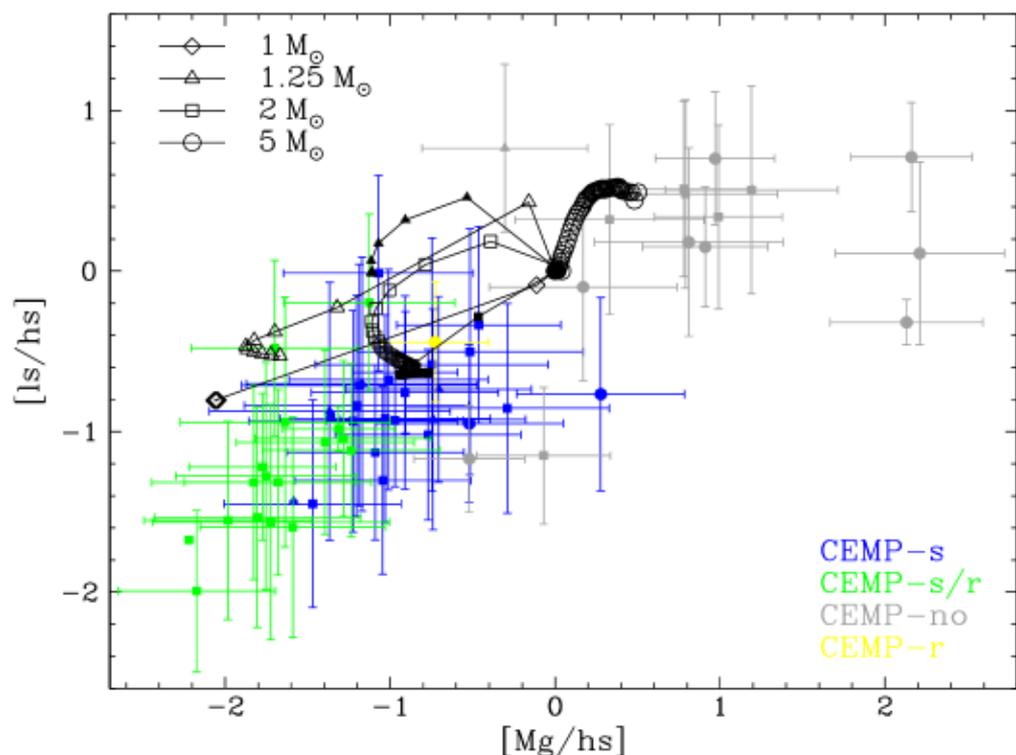
CEMP stars: nucleosynthesis features

CEMP: Carbon Enhanced Metal poor stars

CEMP-s: CEMP stars enriched in s-process only

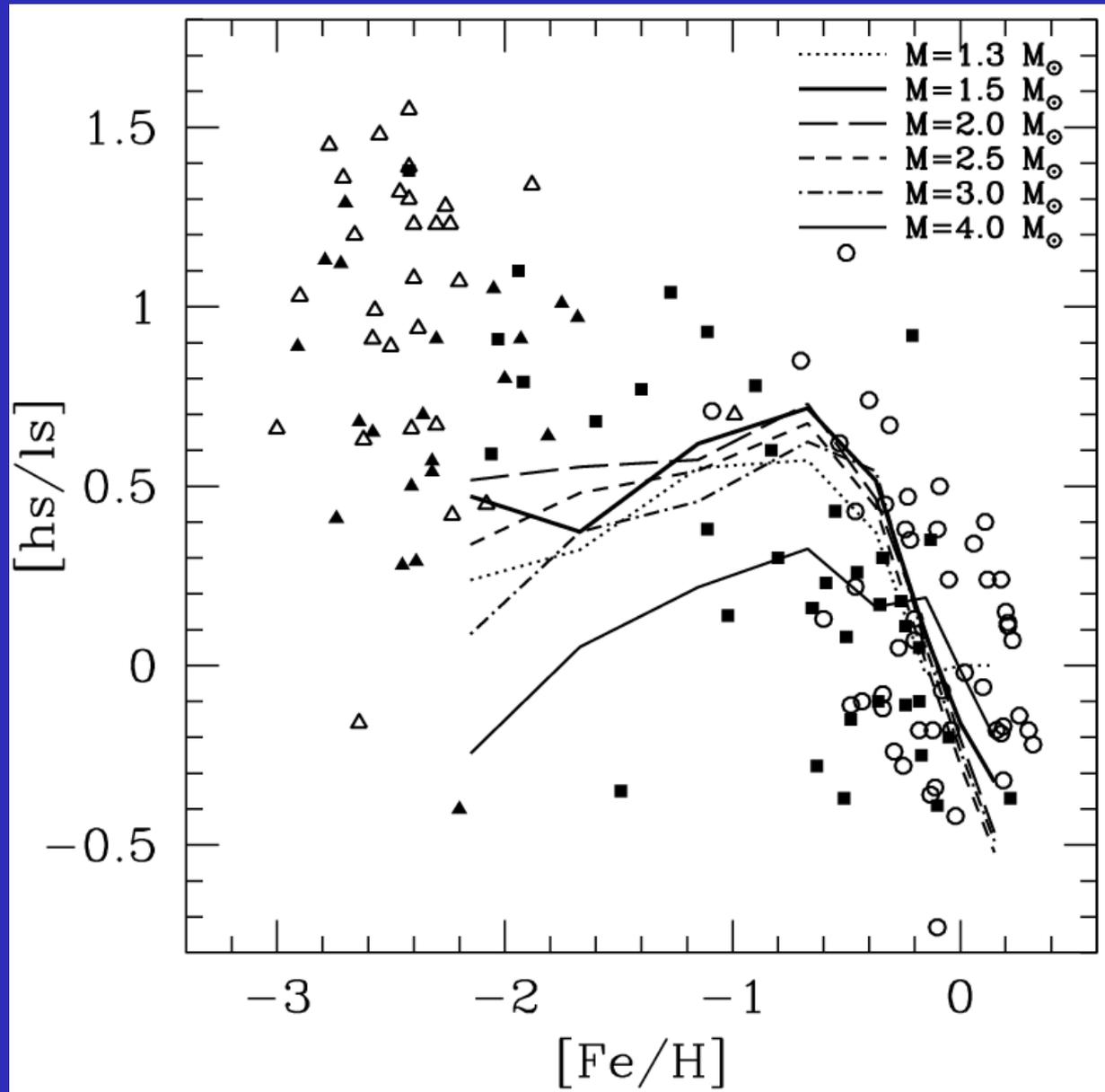
CEMP-r: CEMP stars enriched in r-process only

CEMP-s/r: CEMP stars enriched in both s- and r-processes



Lugaro+ 2012

Problems at low metallicities: the effect of initial mass



The effects of rotation: I

Lifting + cylindrical symmetry

$$\frac{dm}{dr} = 4\pi r^2 \rho$$

$$\frac{dL}{dm} = \varepsilon_{nuc} - \varepsilon_v + \varepsilon_g$$

$$\frac{dP}{dm} = -\frac{Gm_r}{4\pi r^4} \cdot f_P$$

$$\frac{d \ln T}{d \ln P} = \min \left[\nabla_{ad}, \nabla_{rad} \cdot \frac{f_T}{f_P} \right]$$

$$f_P = \frac{4\pi r_\psi^4}{m_\psi S_\psi} \langle g^{-1} \rangle^{-1}$$

$$f_T = \left(\frac{4\pi r_\psi^2}{S_\psi} \right)^2 (\langle g \rangle \langle g^{-1} \rangle)^{-1}$$

The effects of rotation: II

Transport of angular momentum & mixing

$$\frac{\partial \omega}{\partial t} = \frac{1}{i} \frac{\partial}{\partial m} \left[(4\pi r^2 \rho)^2 i D_J \left(\frac{\partial \omega}{\partial m} \right) \right]$$

$$D_J = D_{conv} + f_\omega (D_{ES} + D_{GSF} + D_{SS} + D_{DS} + D_{SH})$$

$$\frac{\partial X_k}{\partial t} = \frac{\partial}{\partial m} \left[(4\pi r^2 \rho)^2 i D_C \left(\frac{\partial X_k}{\partial m} \right) \right]$$

$$D_J = D_{conv} + f_\omega f_c (D_{ES} + D_{GSF} + D_{SS} + D_{DS} + D_{SH})$$

The ES circulation velocity

$$v_{ES} = \frac{\nabla_{ad}}{\delta(\nabla_{ad} - \nabla_{rad})} \frac{\omega^2 r^3 L}{(Gm)^2} \left[\frac{2\epsilon r^2}{L} - \frac{2r^2}{m} - \frac{3}{4\pi\rho r} \right]$$

$$v_{ES} \sim - \frac{\nabla_{ad}}{\delta(\nabla_{ad} - \nabla_{rad})} \frac{\omega^2 r^3 L}{(Gm)^2} \frac{3}{4\pi\rho r} = \text{const.} \frac{j(r)^2}{\rho}$$

μ -gradient barrier

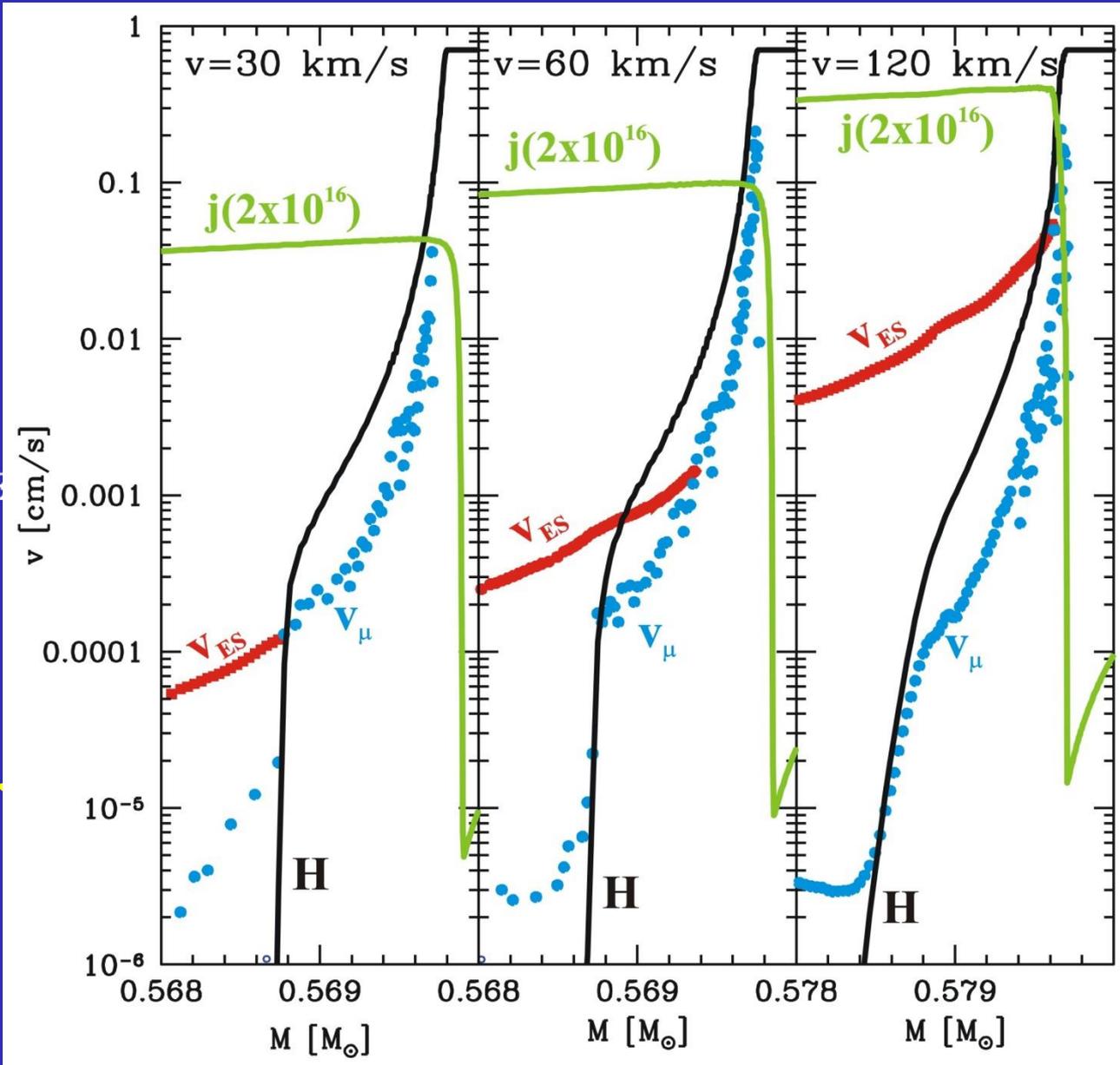
$$v_{\mu} = f_{\mu} \frac{H_p}{\tau_{th}} \frac{\varphi \nabla_{\mu}}{\nabla - \nabla_{ad}}$$

The ES circulation velocity

$v_{ES} =$

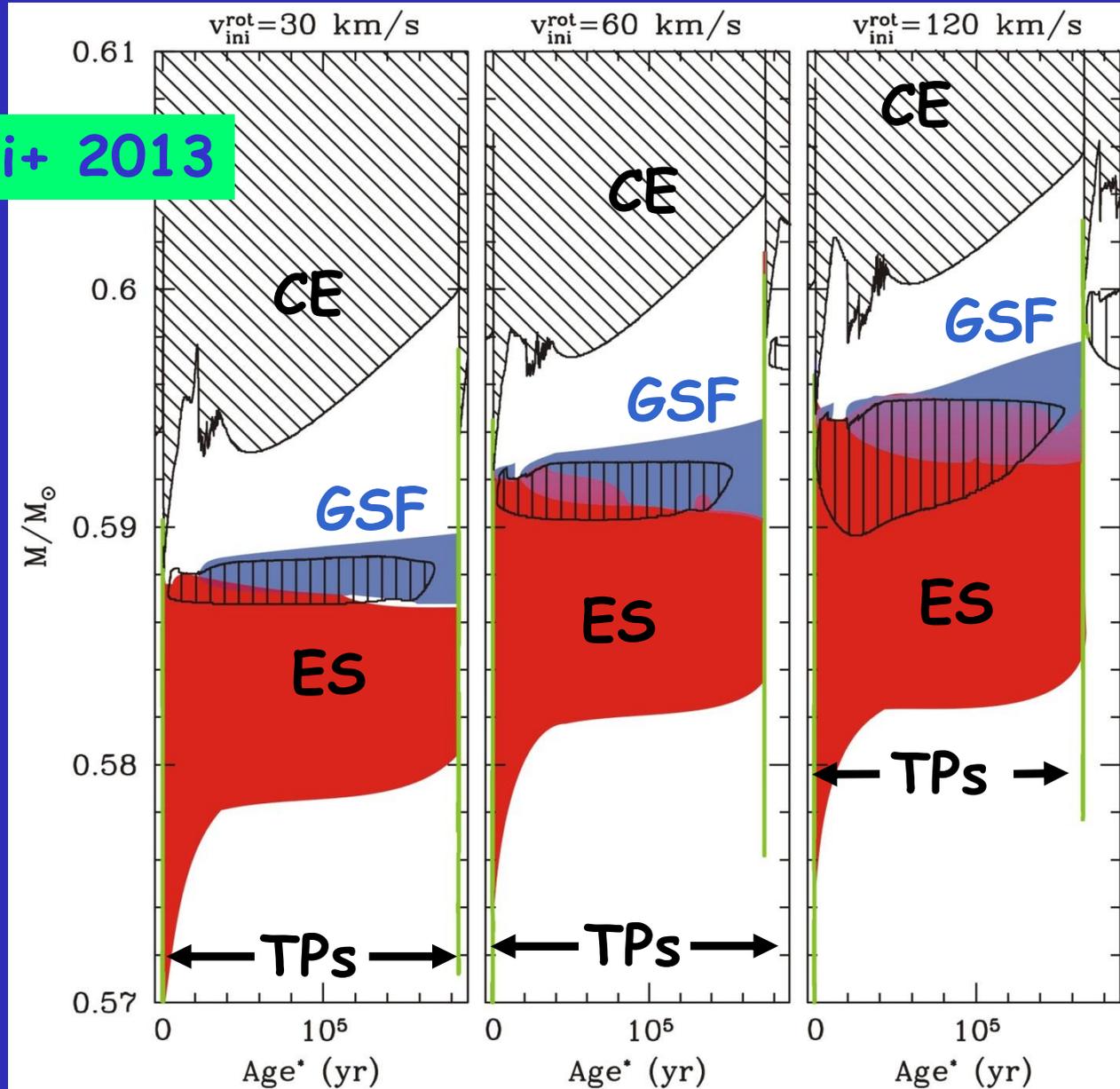
v_E

μ -gr



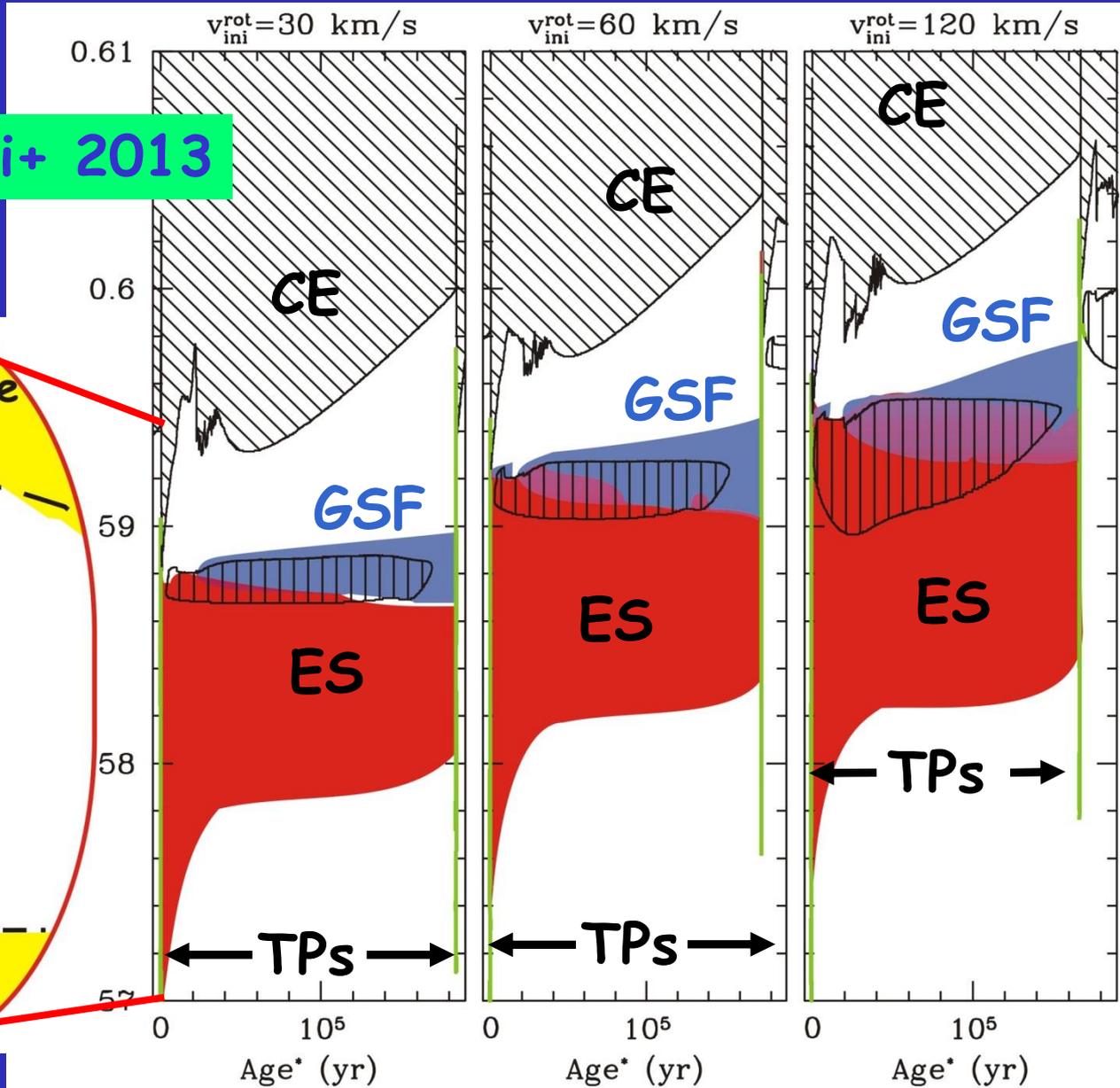
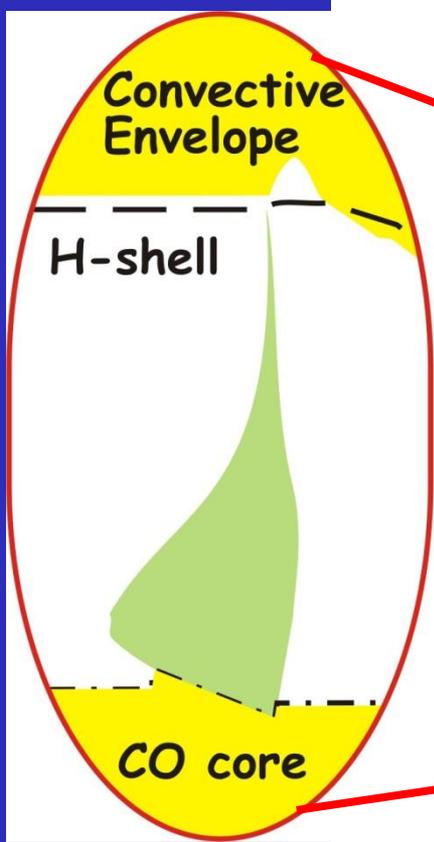
The AGB phase: the $[Fe/H] = -1.7$ case

Piersanti+ 2013



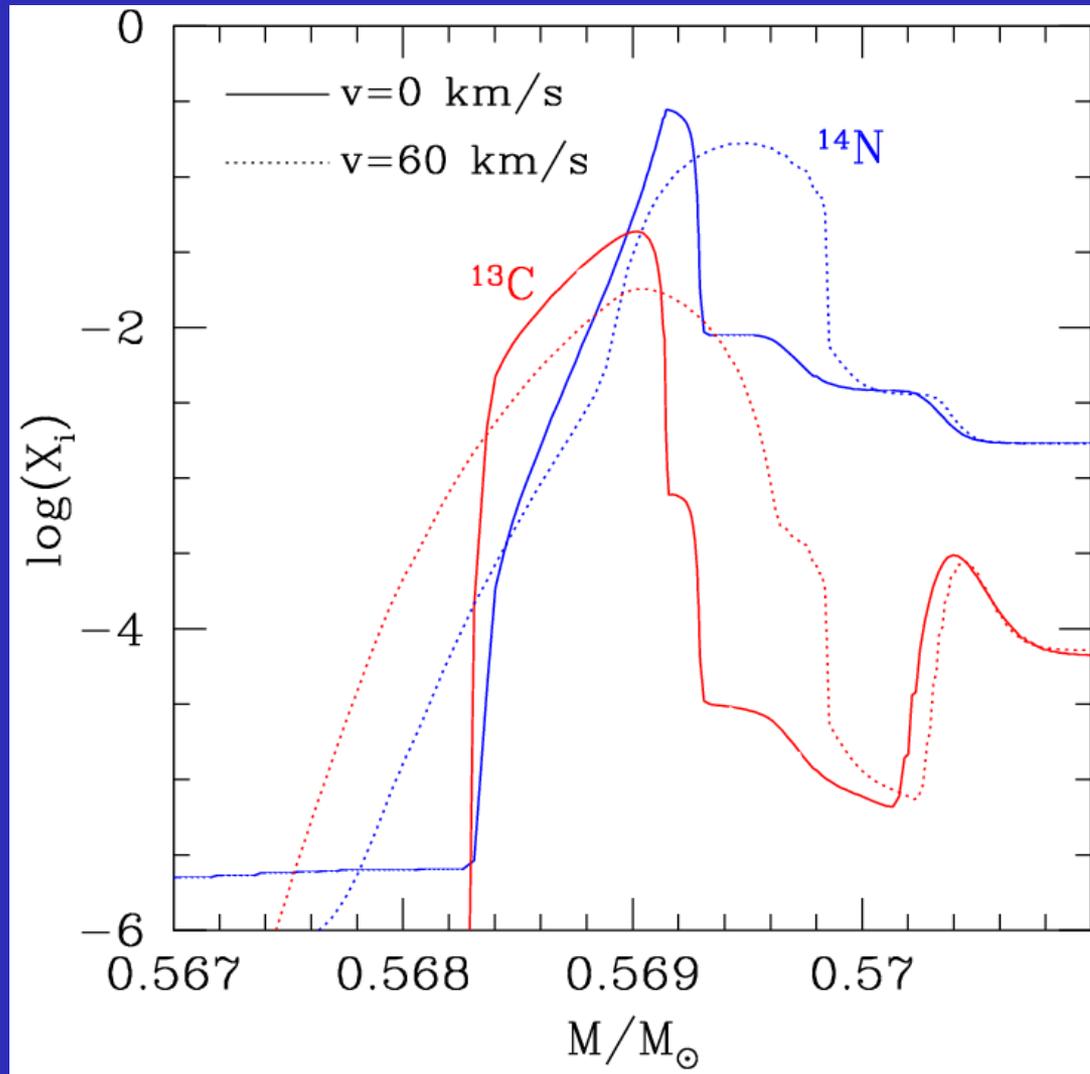
The AGB phase: the $[Fe/H] = -1.7$ case

Piersanti+ 2013



NET EFFECT:

It mixes ^{14}N in ^{13}C -rich layers (and viceversa), thus implying a decrease of the local neutron density and an increase of the iron seeds. As a consequence, the surface s-process distributions change.



The AGB phase: the $[Fe/H]=-1.7$ case

Without rotation ...

The Fe abundance is low

The neutrons-to-seeds ratio is very high

The s-process produces large amount a Pb

Rotation reduces neutrons-to-seeds ratio

The Pb production is reduced

The abundances of hs and ls increase!!!

The AGB phase: the $[Fe/Al] = 1.7$ case

Without

The Fe c

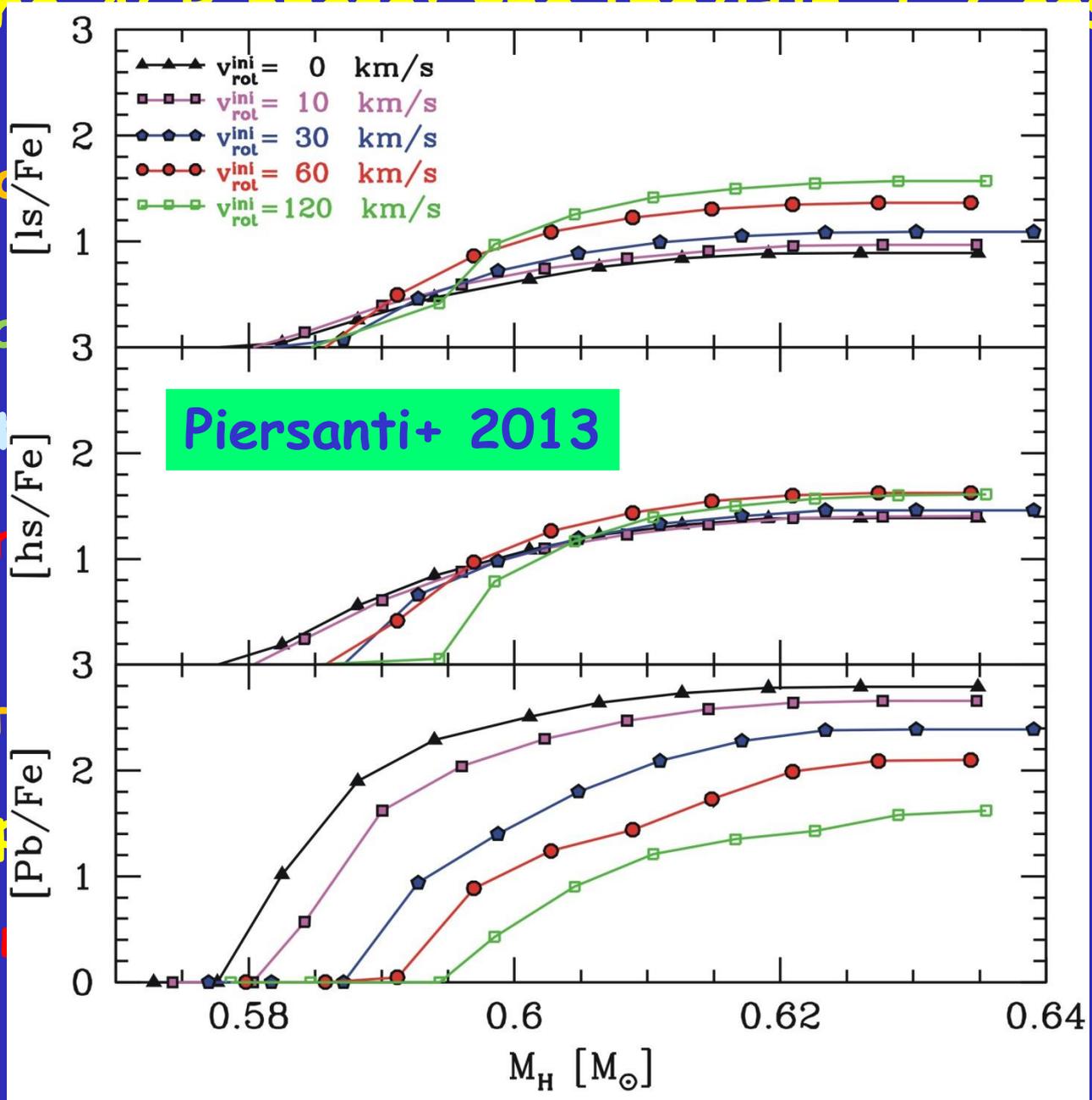
The neut

The s-pr

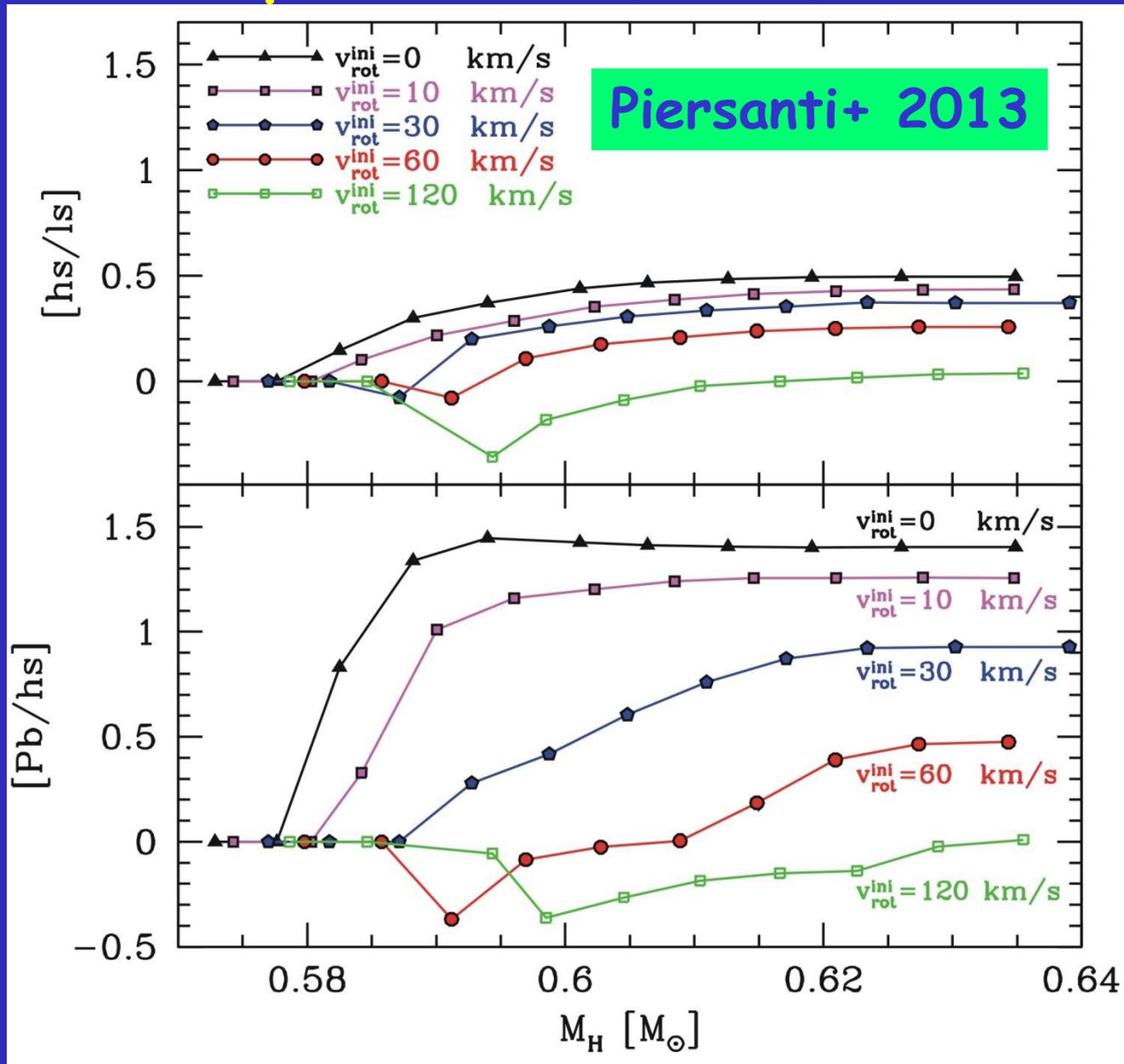
Rotat

The Pb p

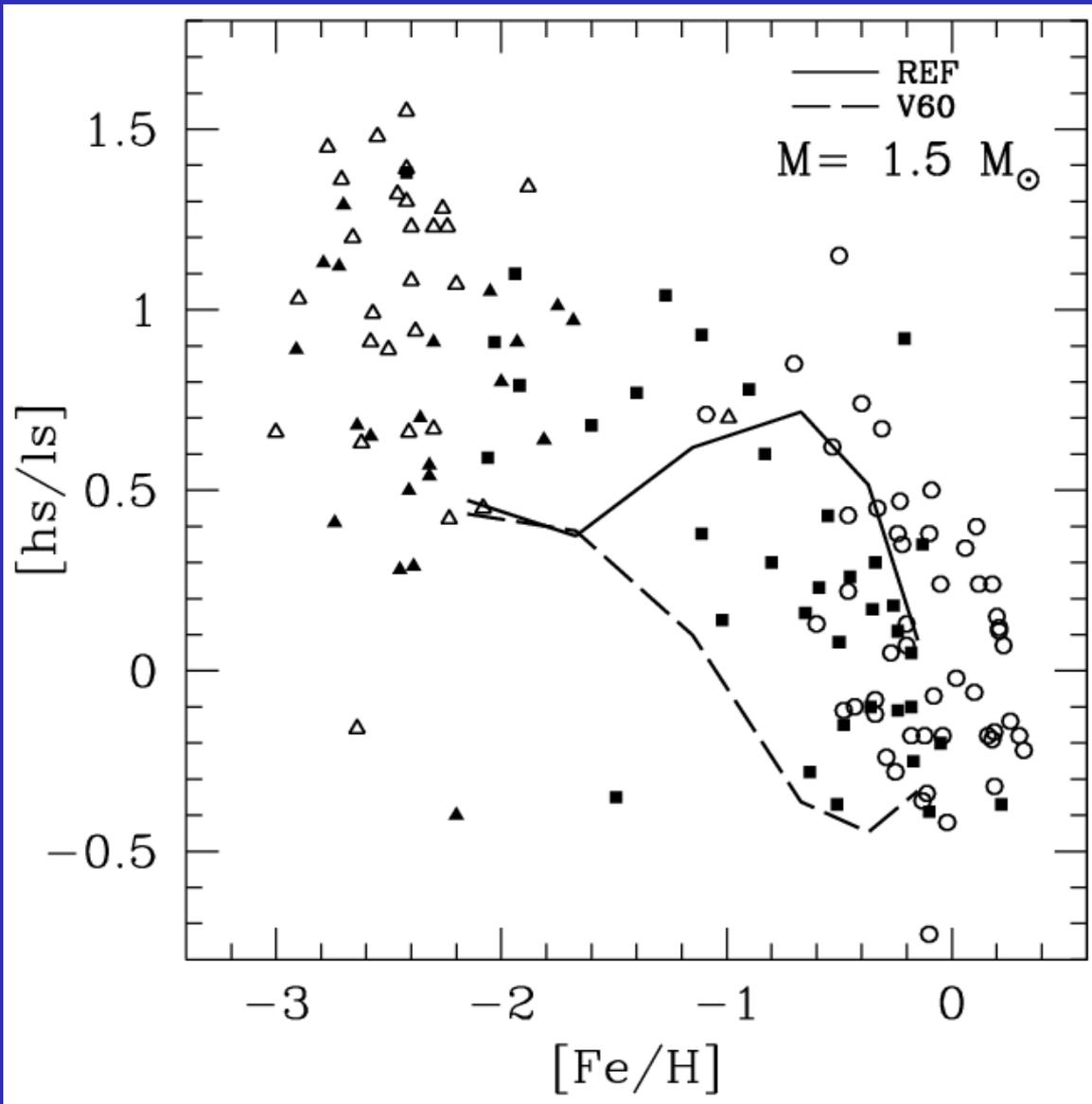
The abu



The AGB phase: the $[Fe/H] = -1.7$ case



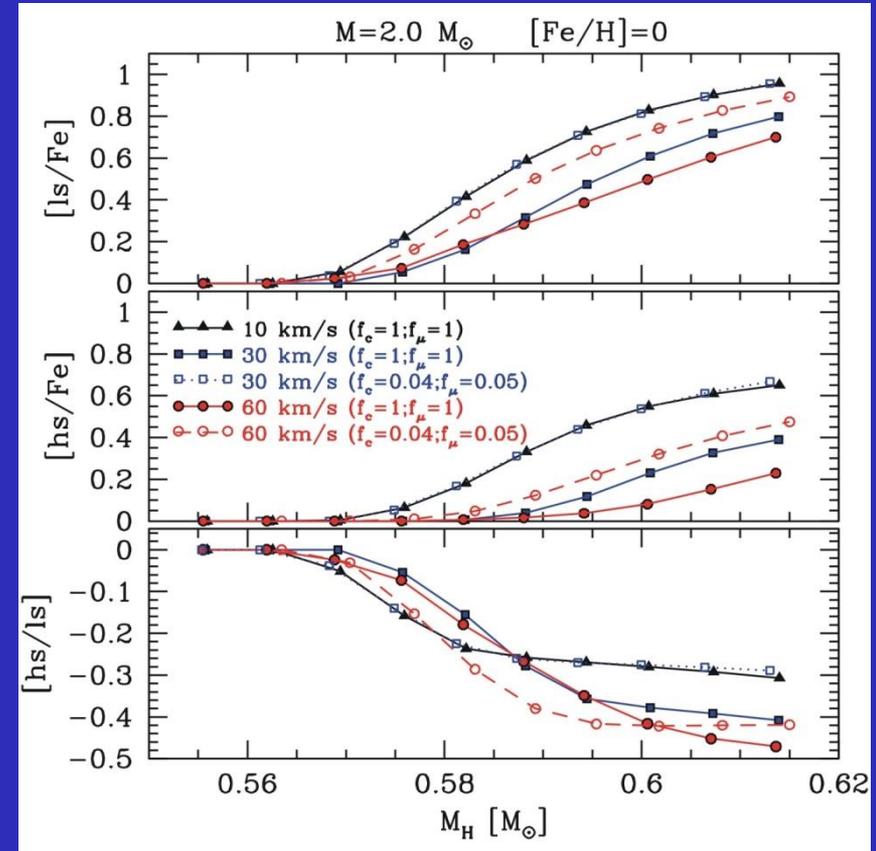
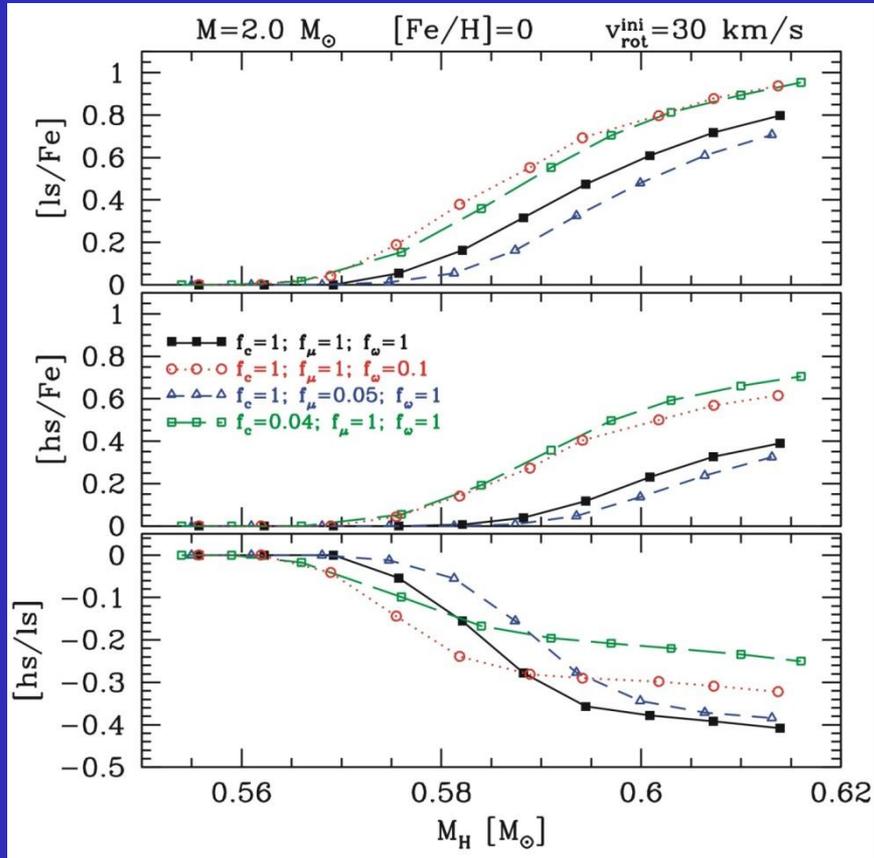
Problems at low metallicities: the effect of rotation



- Ba stars
- CH stars
- ▲ CEMP-s stars
- △ CEMP-sr stars

SC+ 2016

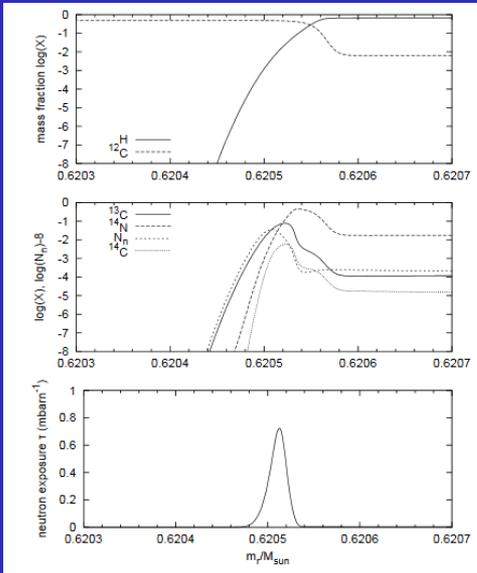
Uncertainties: efficiency of mixing



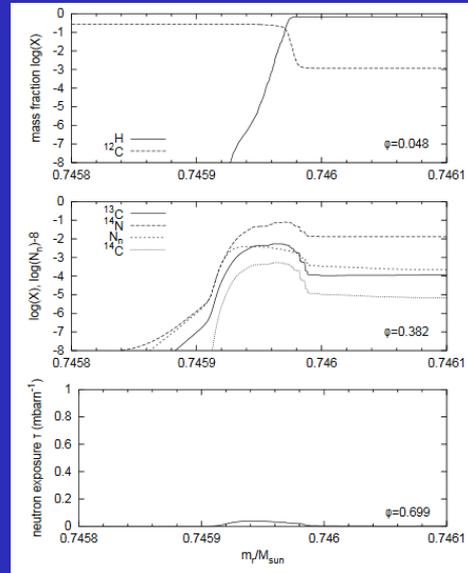
Piersanti+ 2013

Rotation-induced mixing: other studies

Overshoot



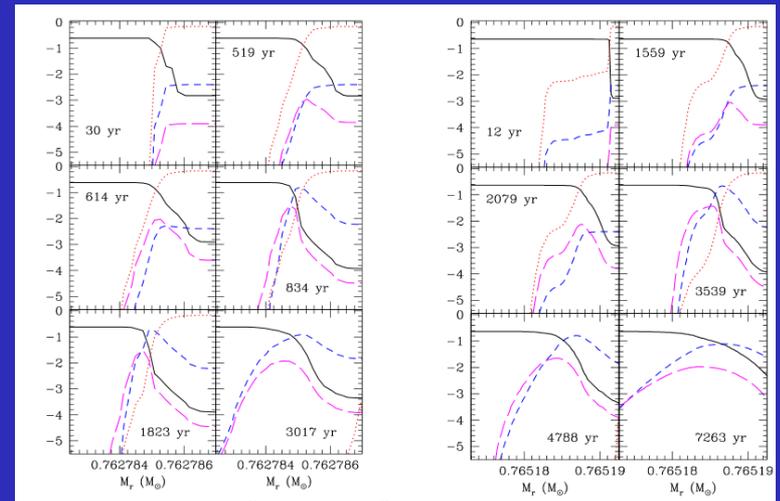
Overshoot+rotation



Herwig+ 2003

See also Langer+1999

Siess+ 2004



Without μ barrier

With μ barrier

Asteroseismology constraints

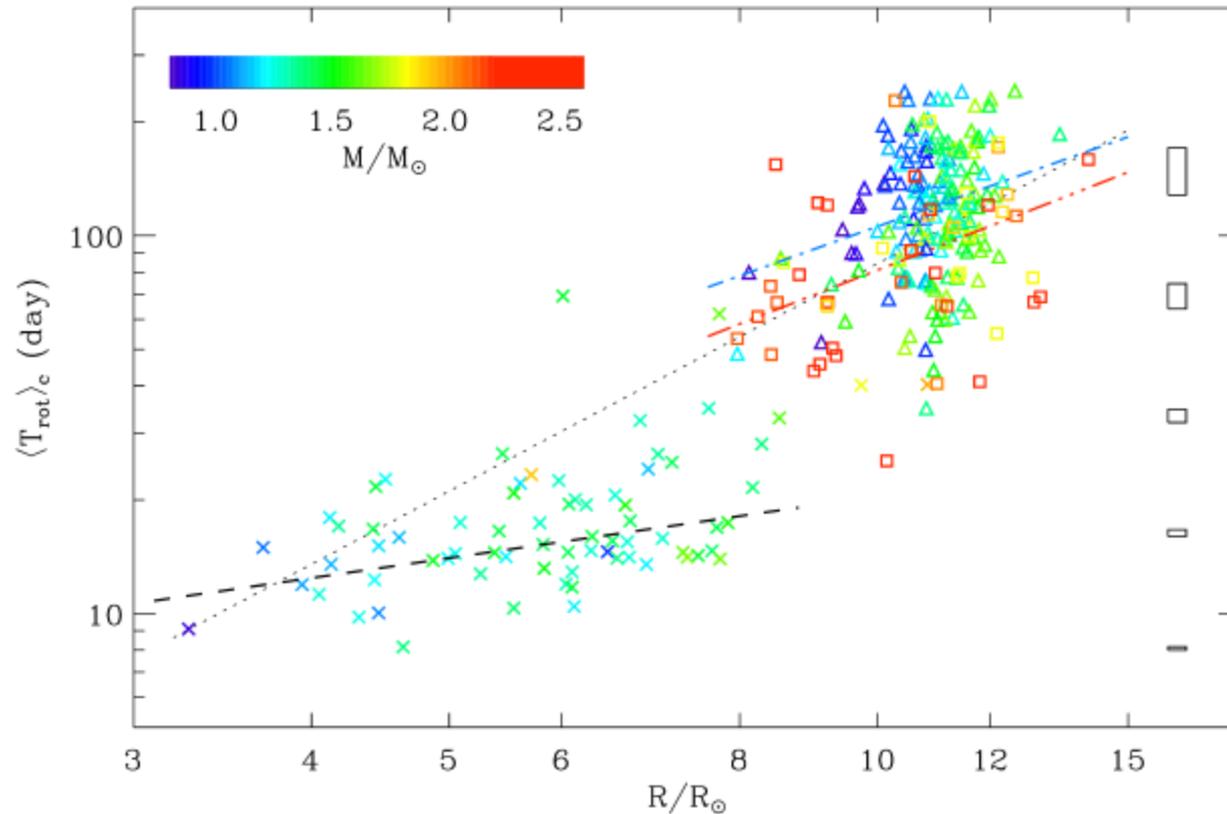
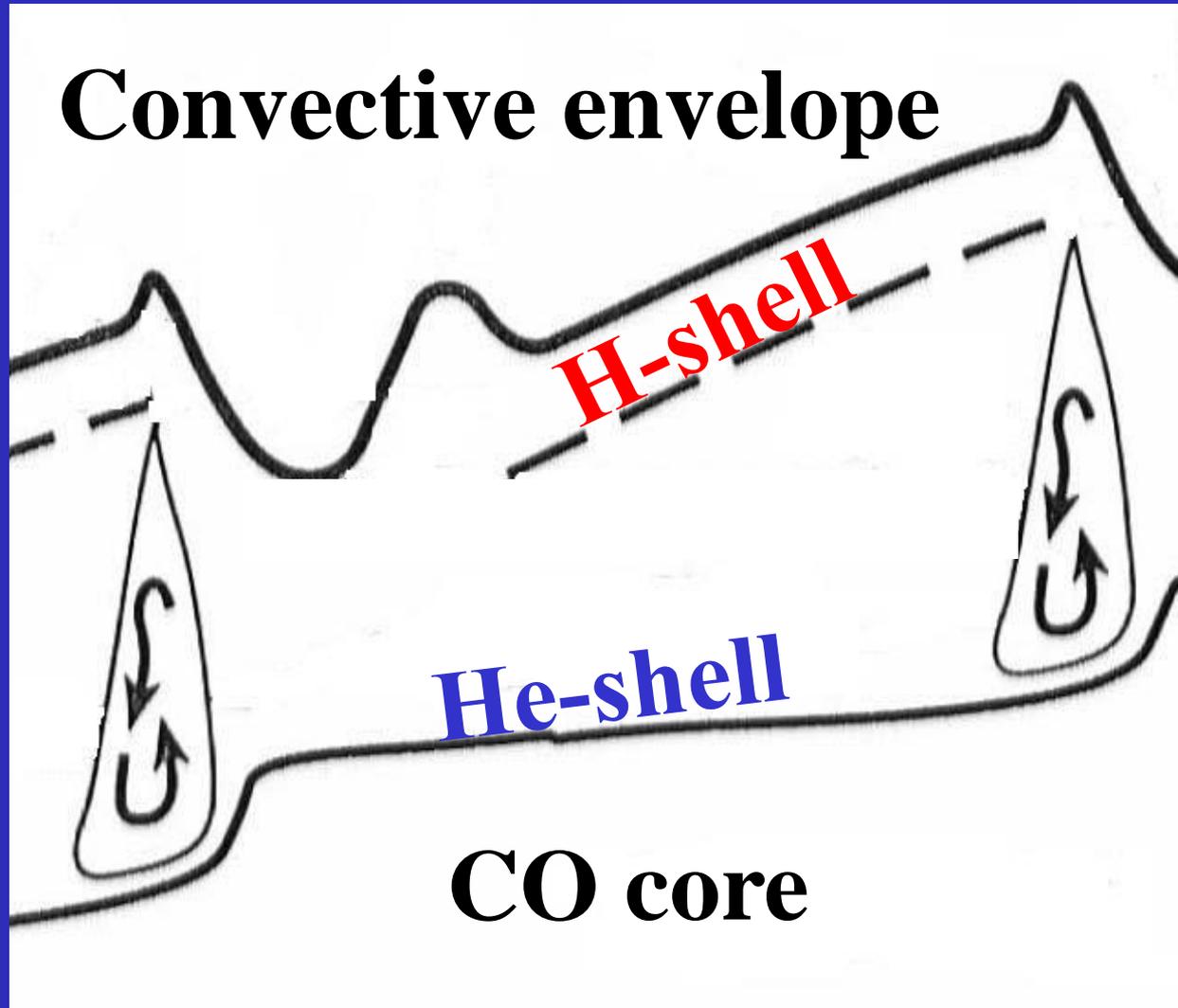


Fig. 9. Mean period of core rotation as a function of the asteroseismic stellar radius, in log-log scale. Same symbols and color code as in Fig. 6. The dotted line indicates a rotation period varying as R^2 . The dashed (dot-dashed, triple-dot-dashed) line indicates the fit of RGB (clump, secondary clump) core rotation period. The rectangles in the right side indicate the typical error boxes, as a function of the rotation period.

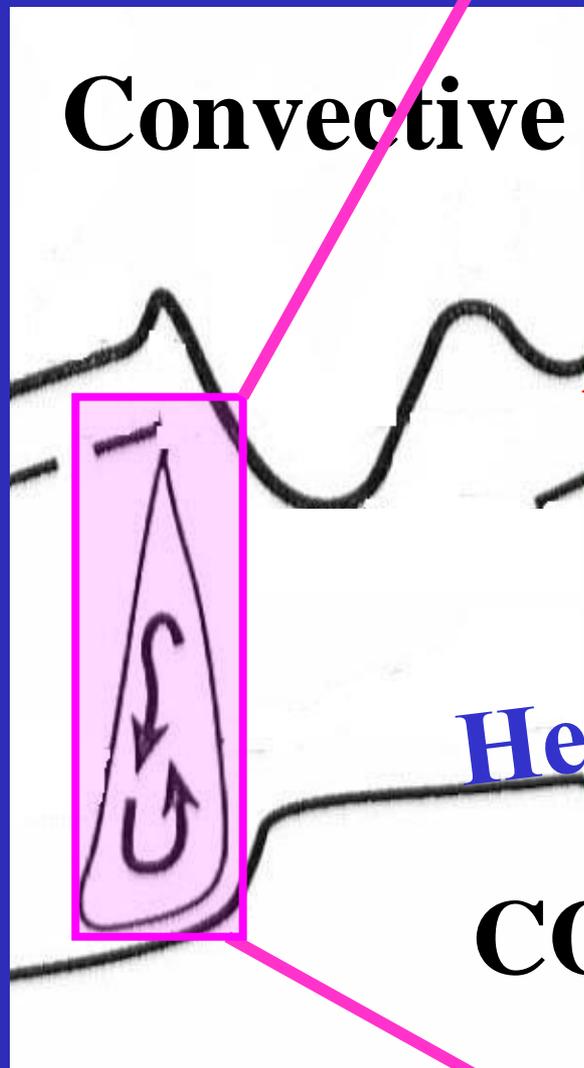
Mosser+ 2012

Low metallicity low mass AGBs

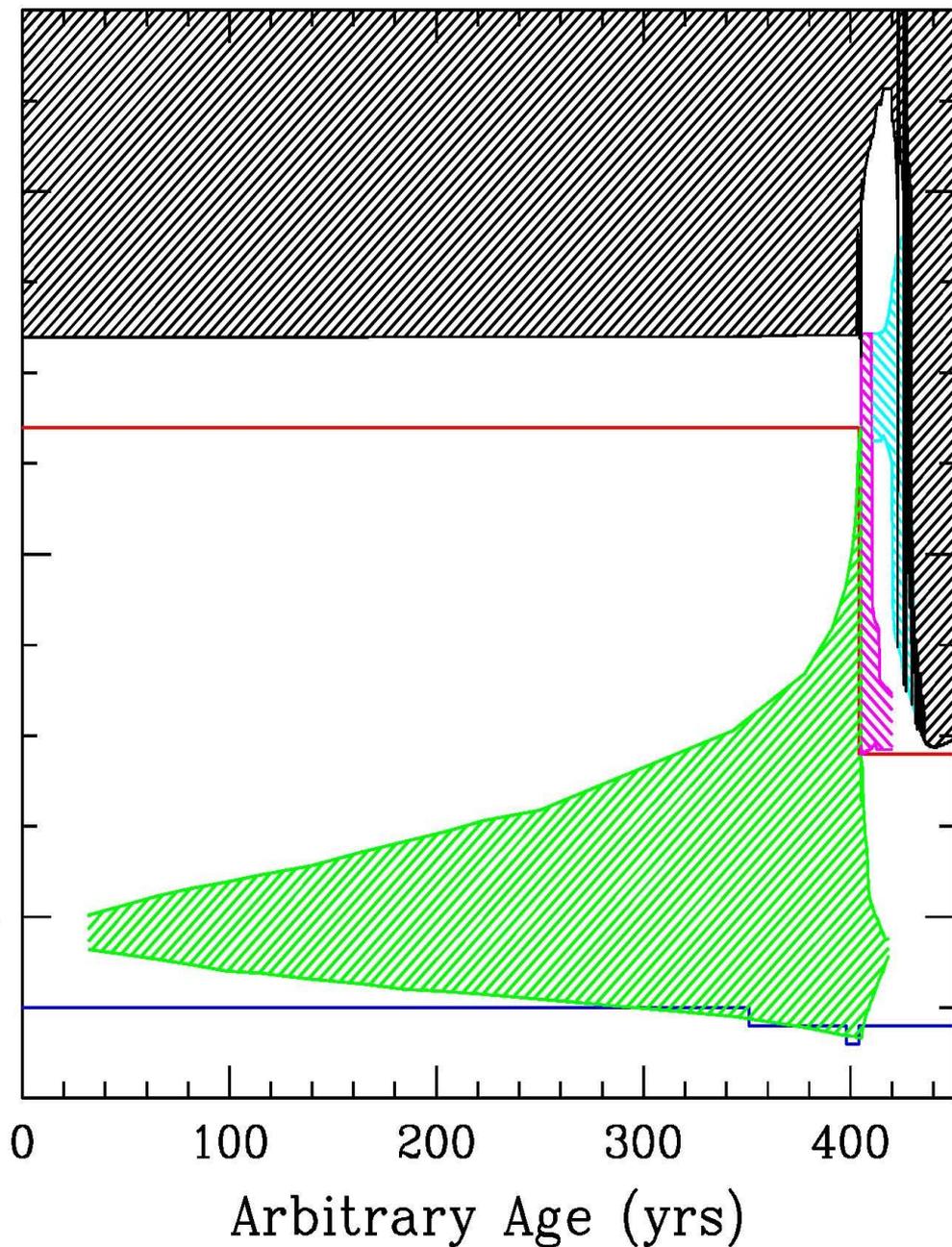


Low metallicity

Convective



$M (M_{\odot})$

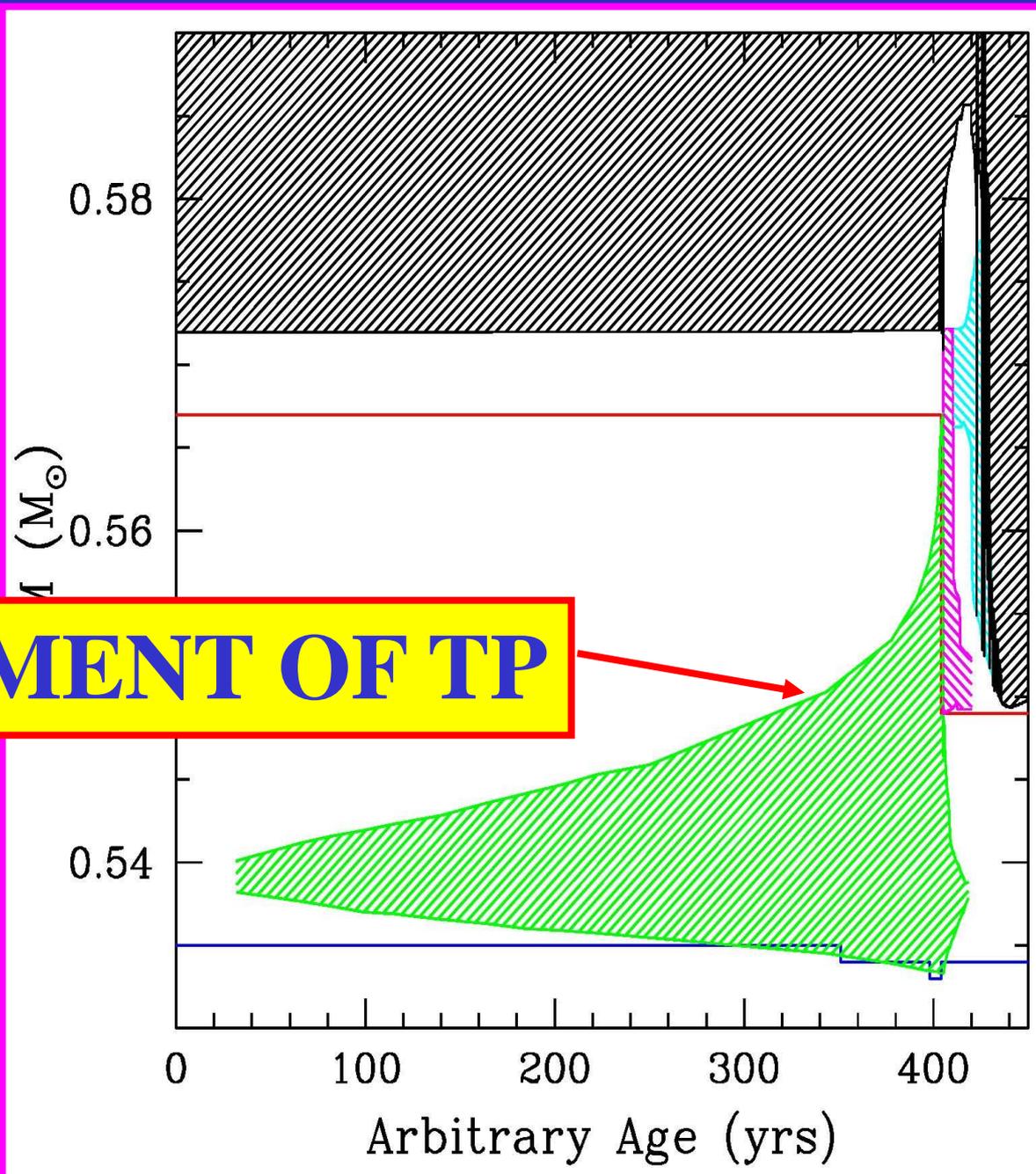


Low metal

Convective



DEVELOPMENT OF TP



Low metal

Convective

PROTONS INGESTION

He

CO

M

0.58

0.54

0

100

200

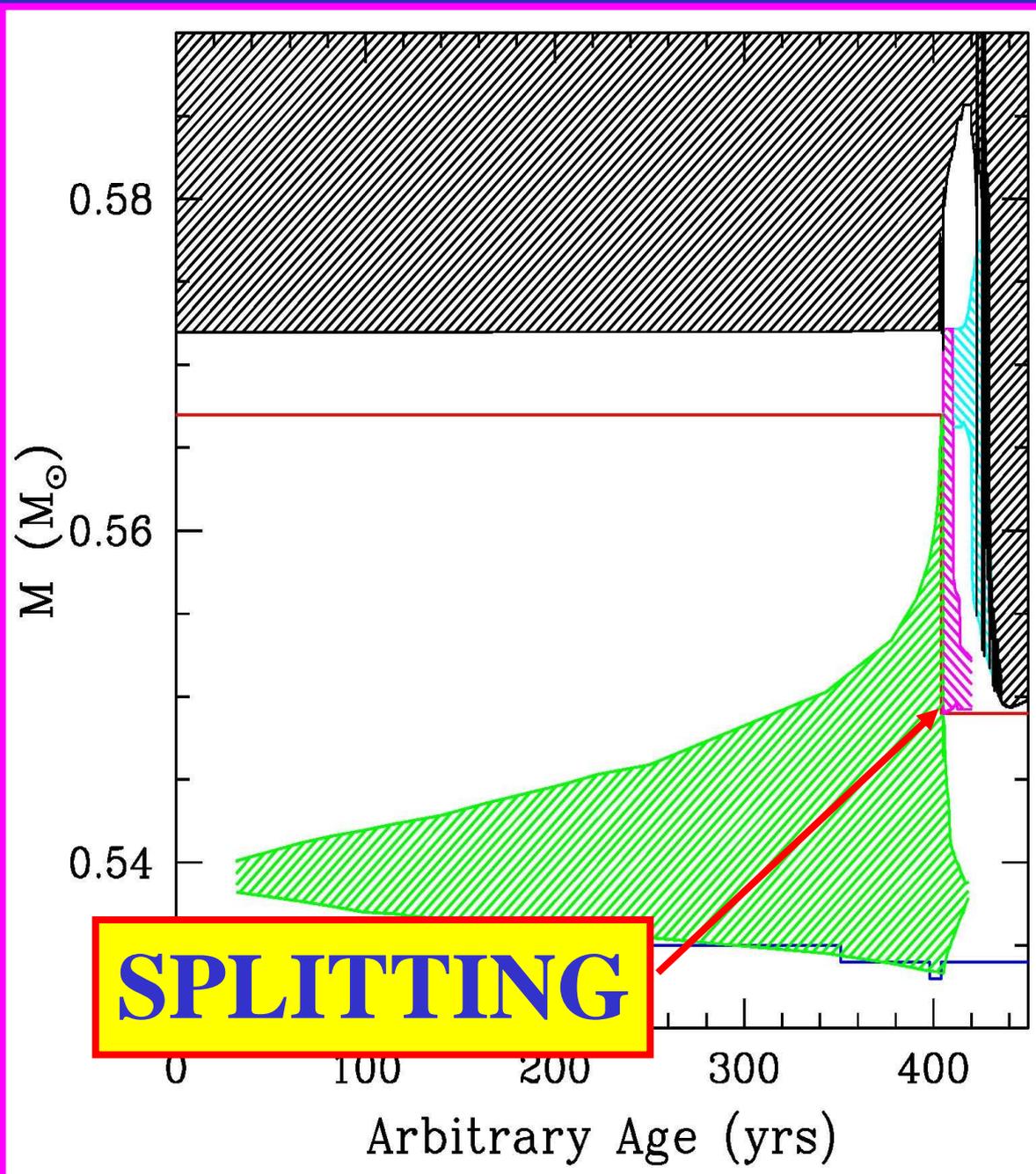
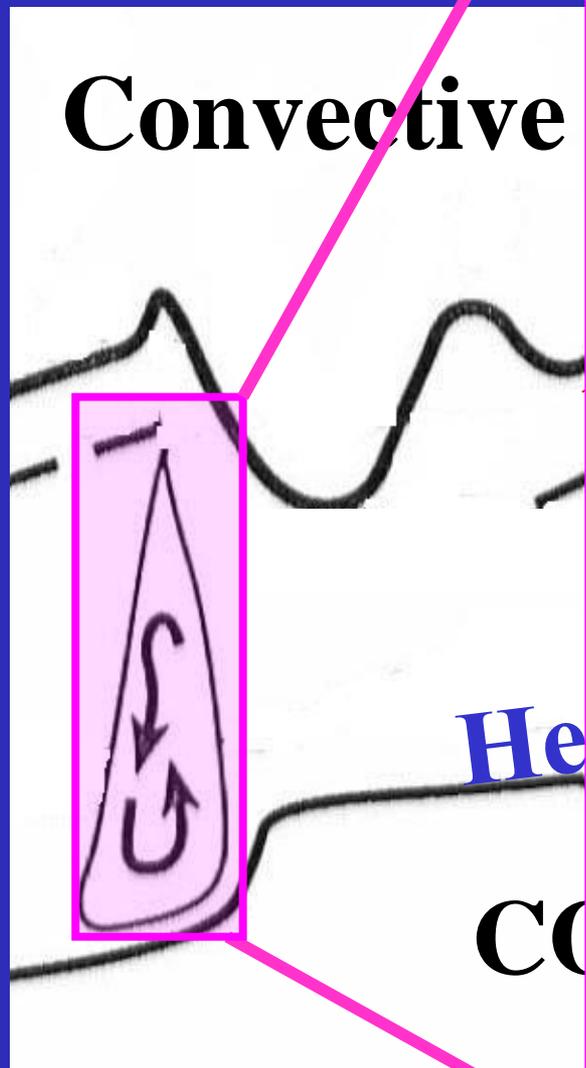
300

400

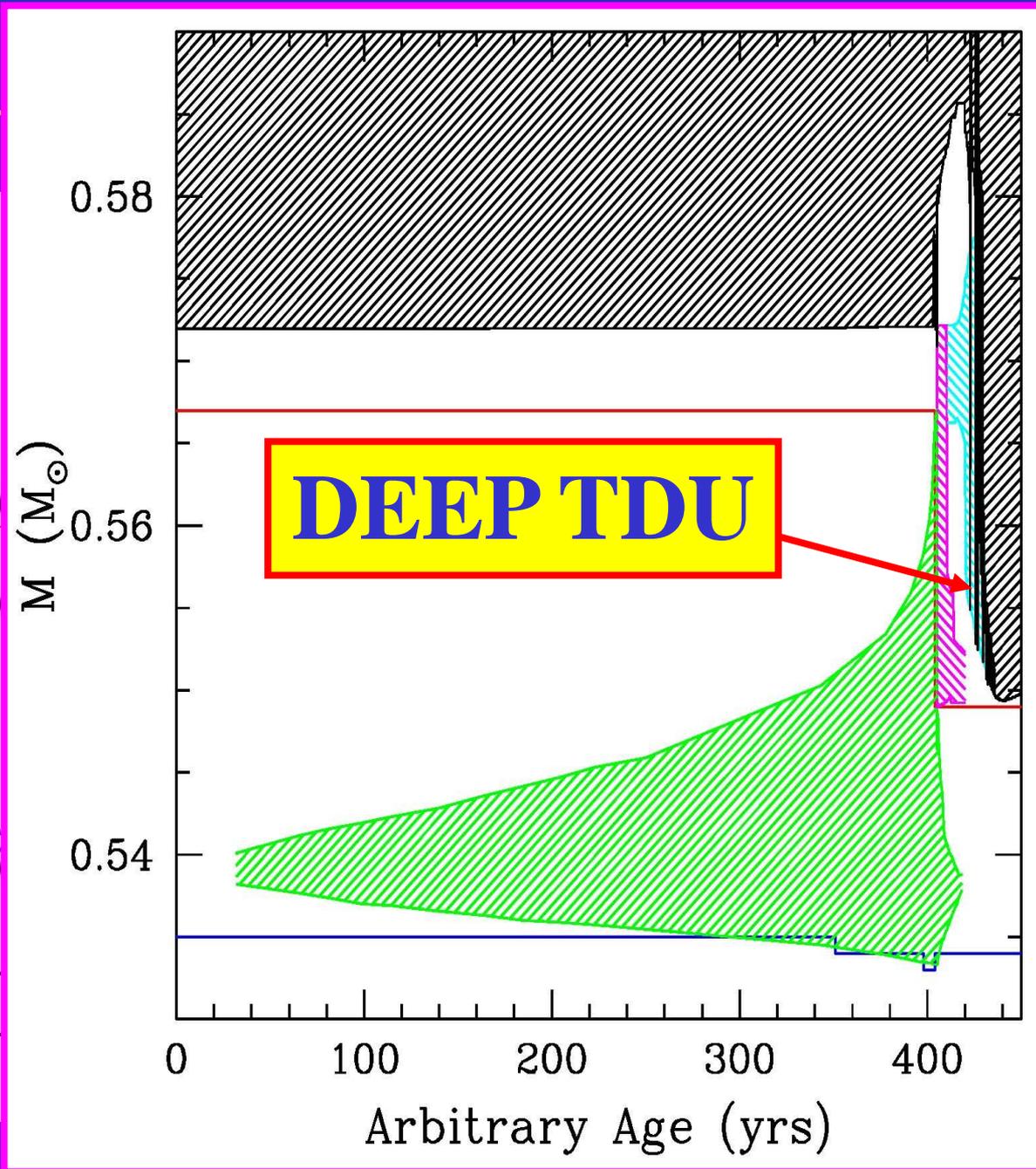
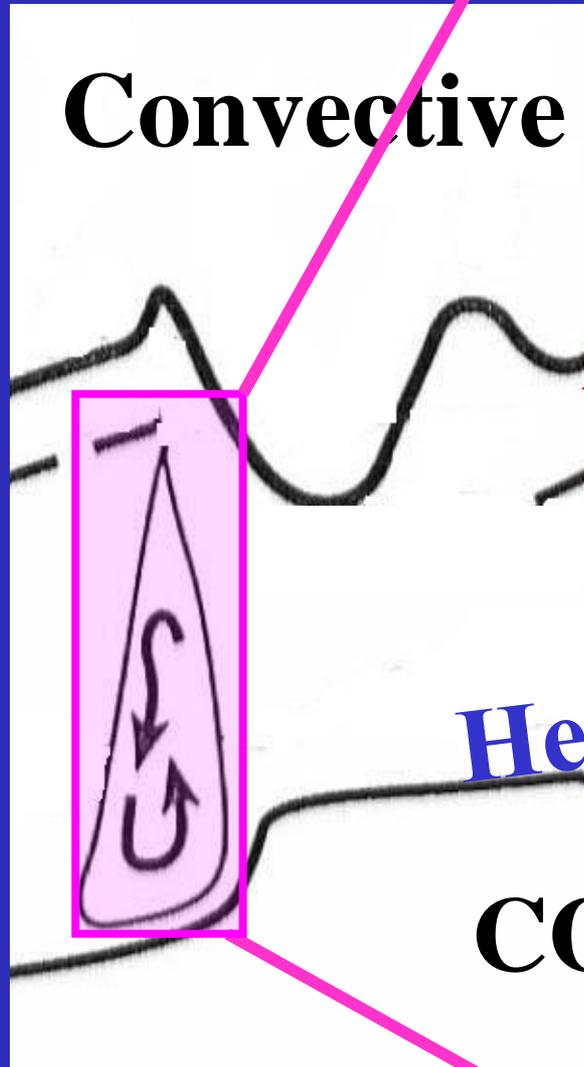
Arbitrary Age (yrs)

Low metallicity

Convective

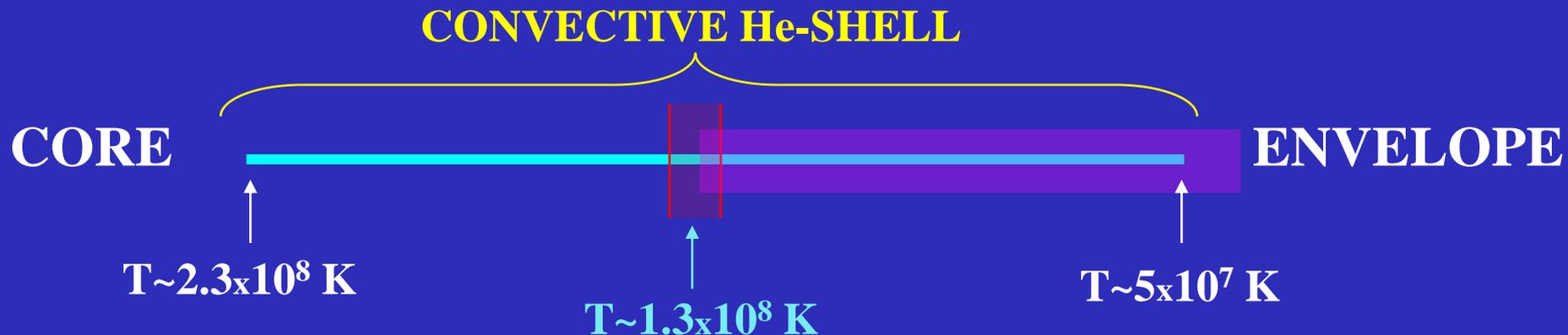


Low metallicity



Proton Ingestion Episode (PIE)

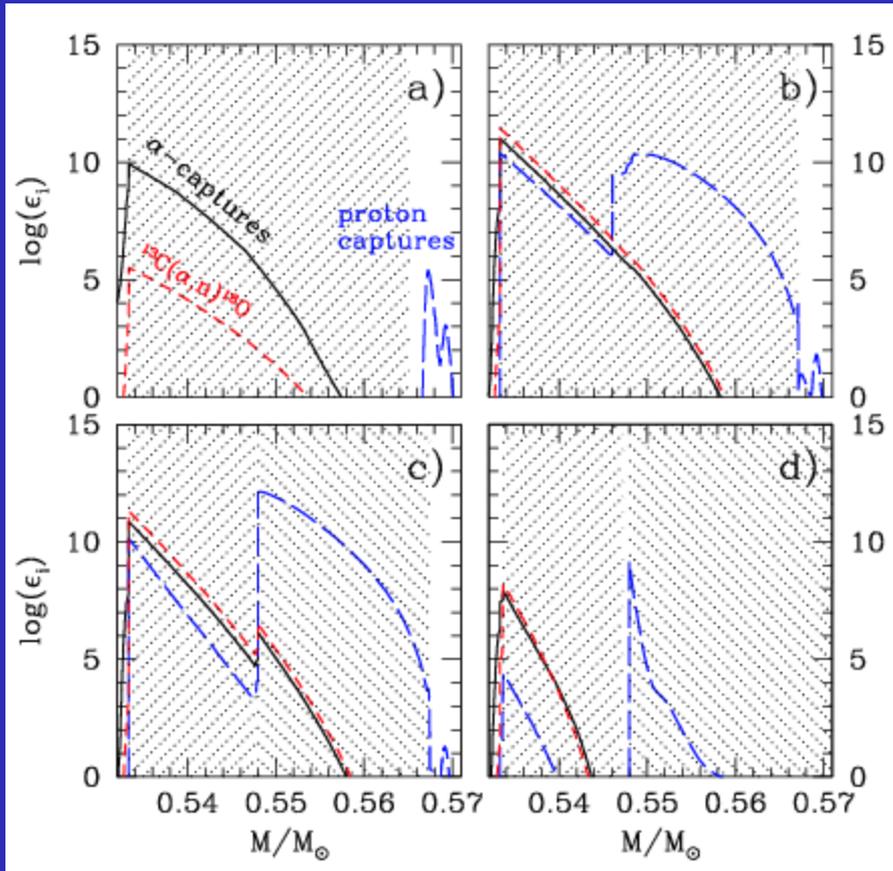
- Low time steps \rightarrow Time dependent mixing
- Rapid structure reaction \rightarrow Coupling between physical and chemical evolution
- Large neutron densities ($n_n > 10^{15} \text{ cm}^{-3}$) \rightarrow 700 isotopes & 1000 reactions



We limit proton ingestion up to the mesh where $\tau_{\text{CNO}} = 1/3 \Delta t$

Temporal step of the model (Δt) is limited to $1/2 \tau_{\text{mix}}$

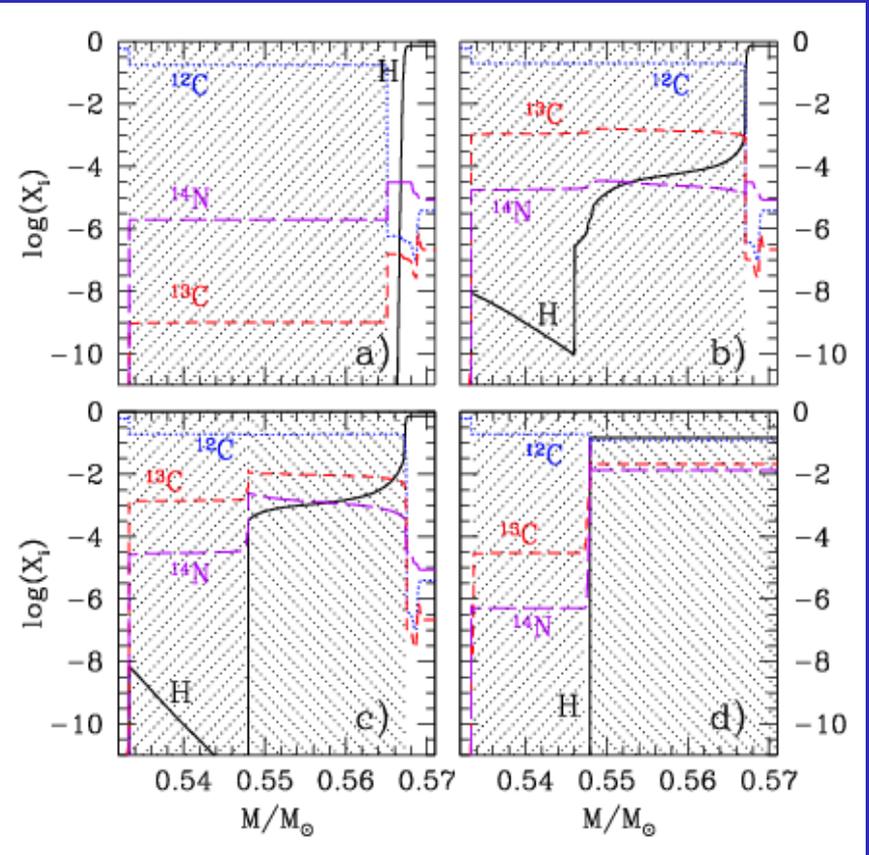
Energy



SC+ 2009b

$M = 1.5 M_\odot$, $[\text{Fe}/\text{H}] = -2.45$

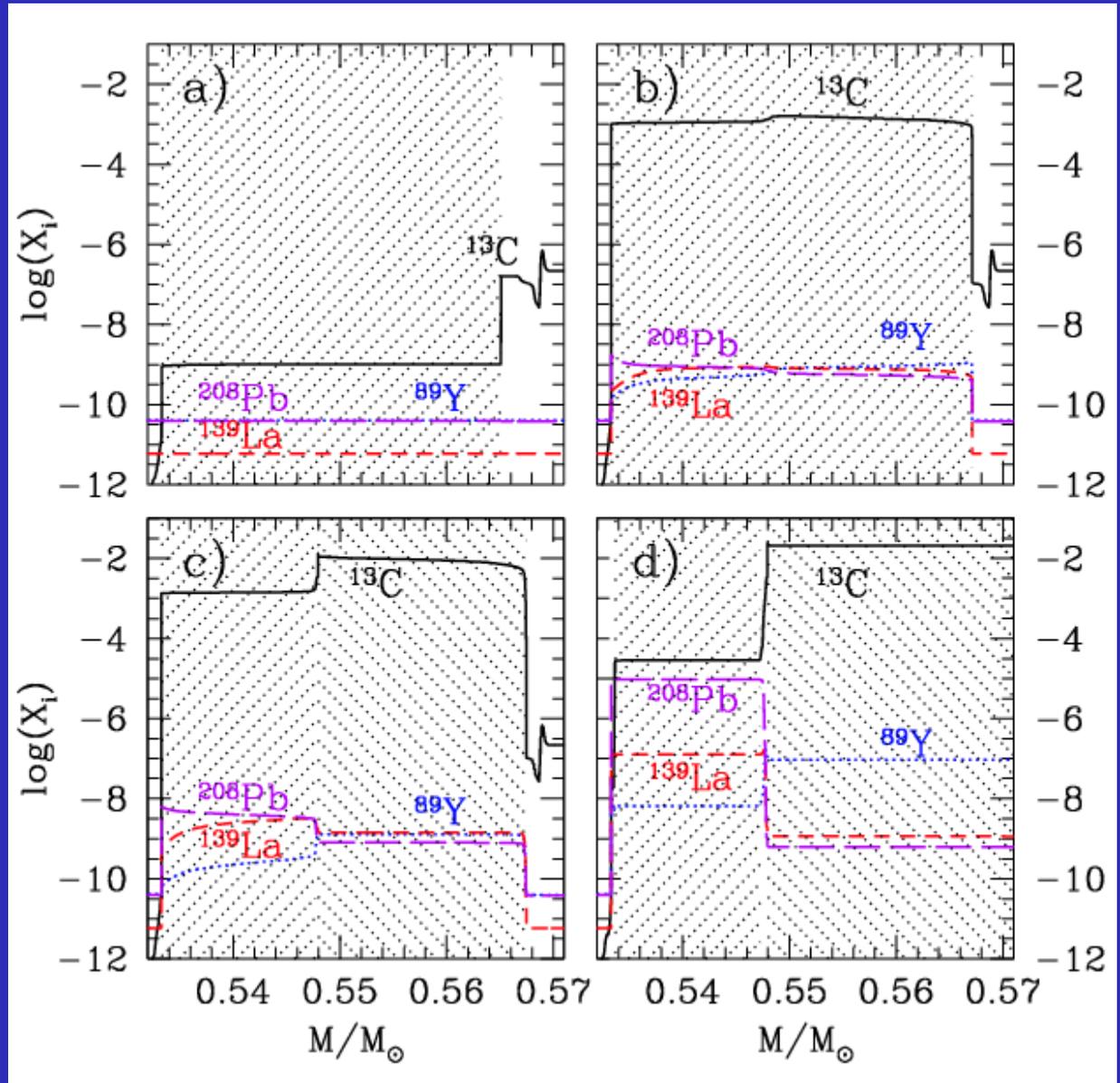
- a) $\Delta t = 0$
- b) $\Delta t = 1.6457$ yrs
- c) $\Delta t = 1.6468$ yrs
- d) $\Delta t = 2.1843$ yrs



Light elements

Heavy elements

SC+ 2009b



$M = 1.5 M_\odot$
 $[\text{Fe}/\text{H}] = -2.45$

Nuclear Network
of 700 isotopes
coupled with the
physics

The importance of nuclear cross sections



— Normal s-process (main path)

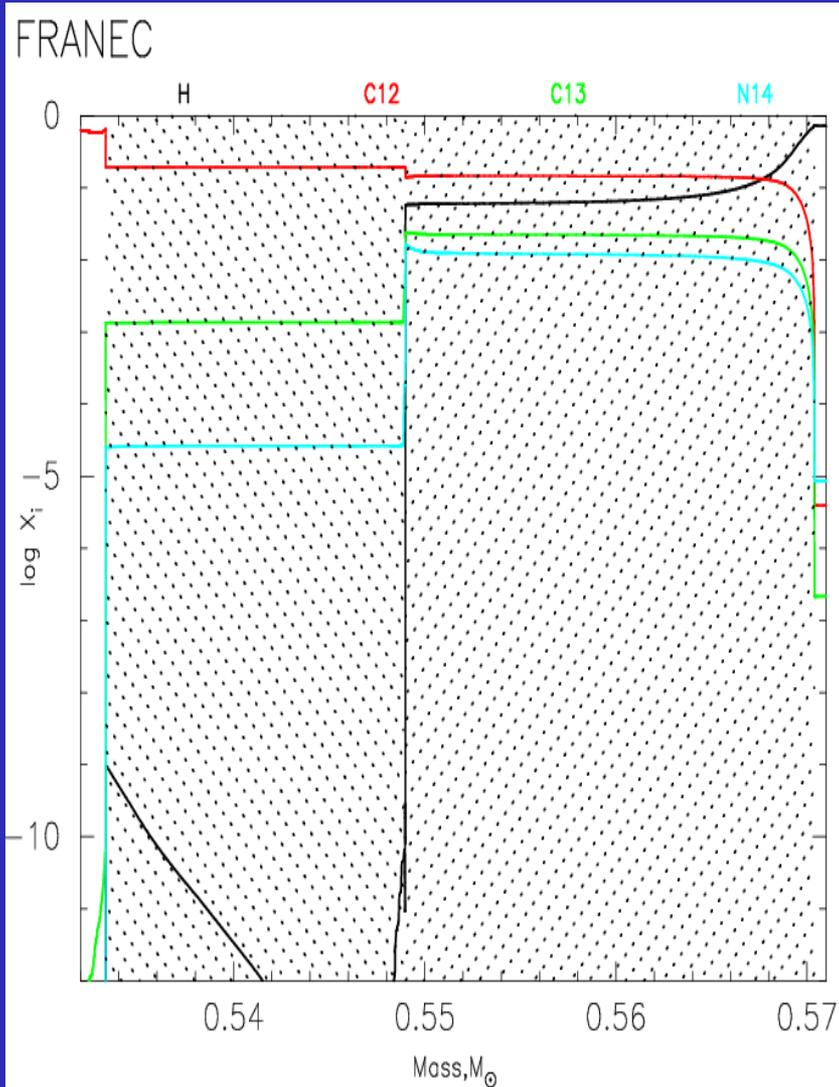
— Proton ingestion

$$n_n > 10^{14} \text{ cm}^{-3}$$

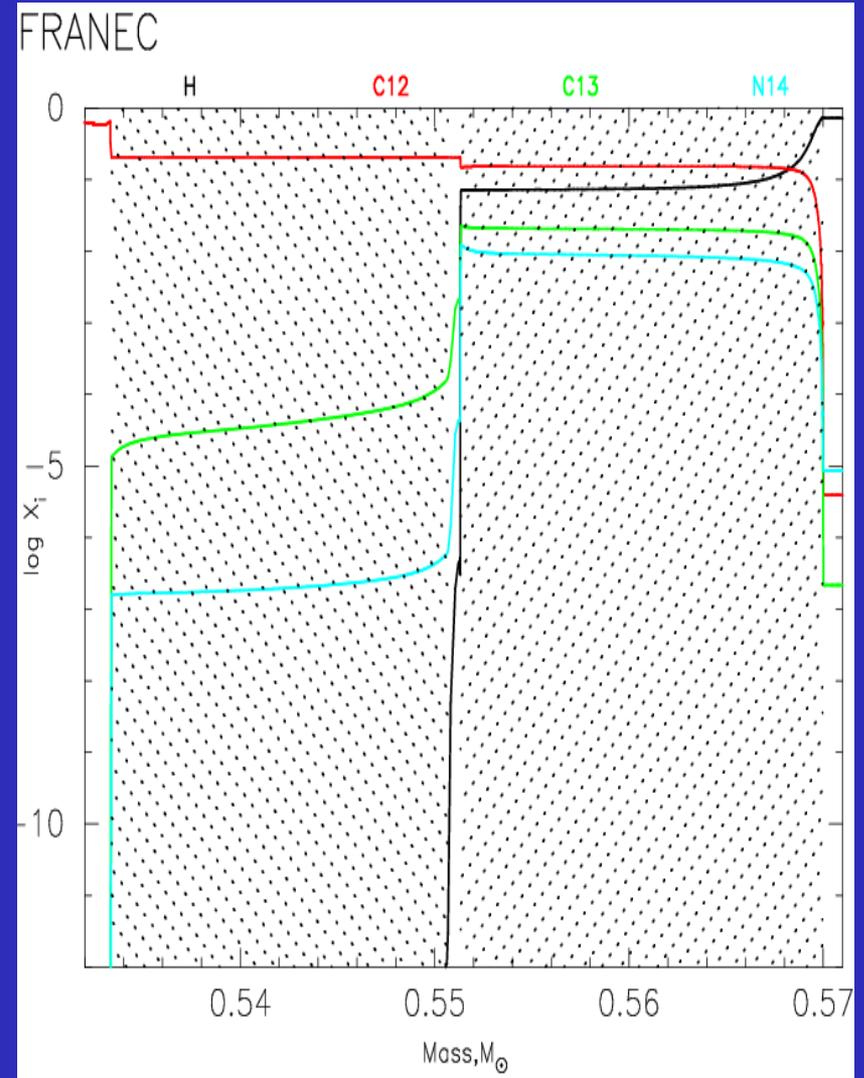
$$\sigma(^{135}\text{I})_{30 \text{ KeV}} \sim 1/20 \sigma(^{138}\text{Ba})_{30 \text{ KeV}}$$

from Rauscher & Thielemann 2000

The importance of the network

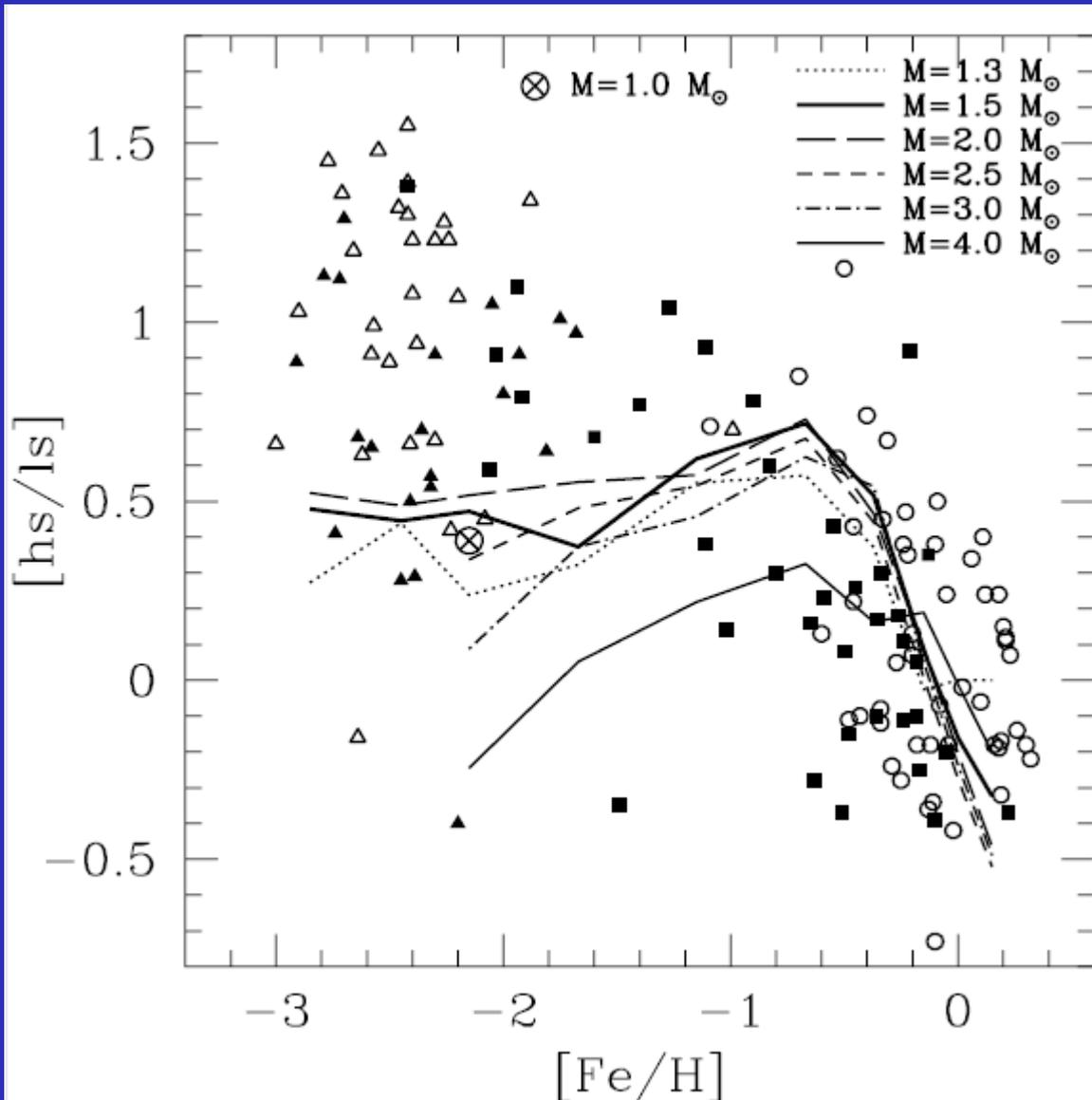


Complete network



Reduced network

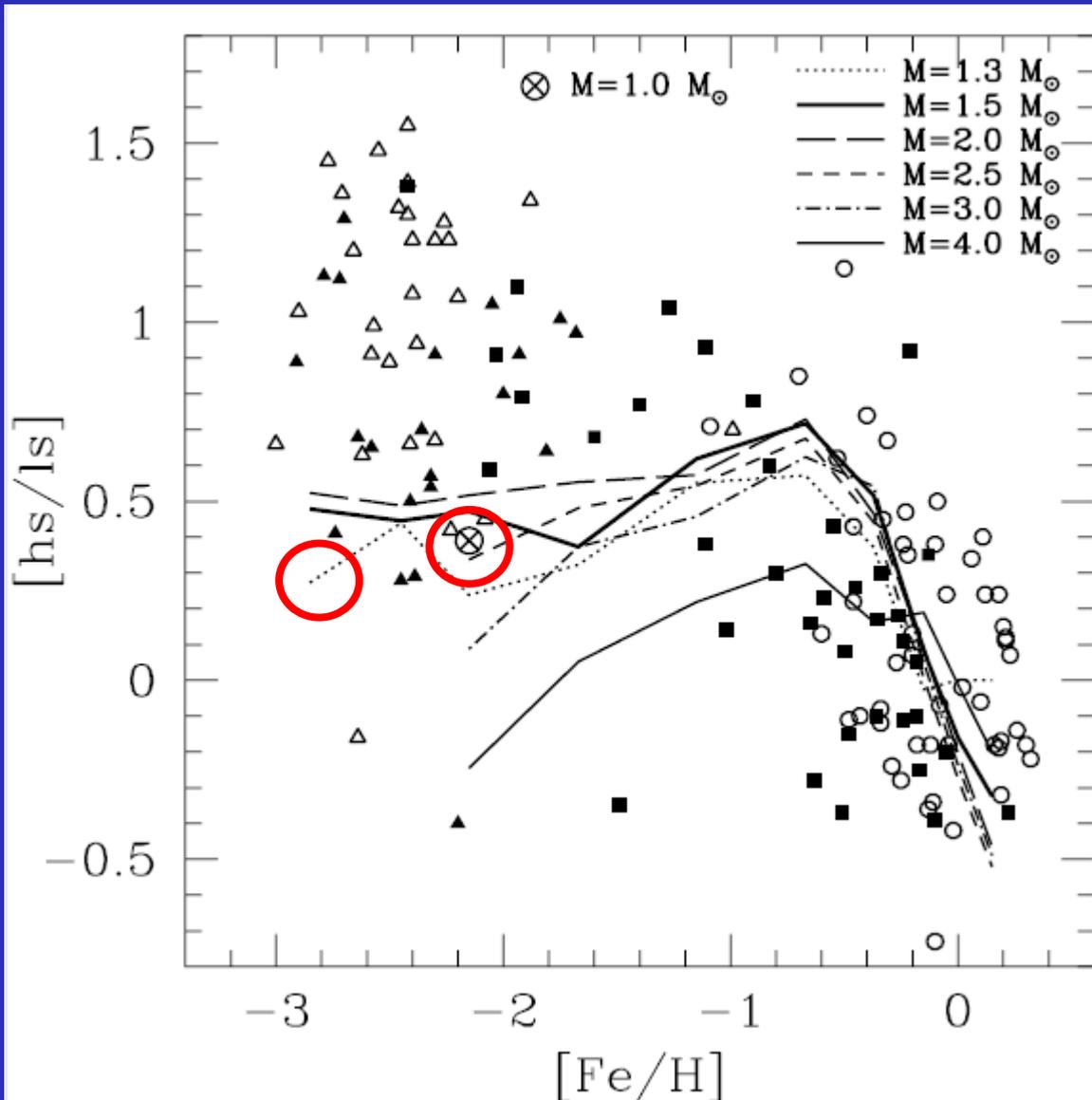
Problems at low metallicities: the effect of PIEs



- Ba stars
- CH stars
- ▲ CEMP-s stars
- △ CEMP-sr stars

SC+ 2016

Problems at low metallicities: the effect of PIEs



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- CH stars
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SC+ 2016

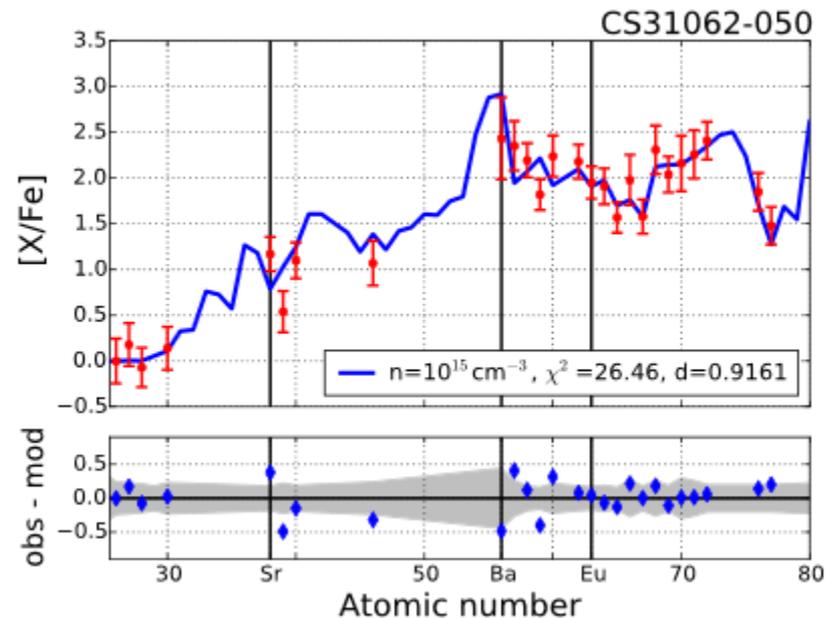
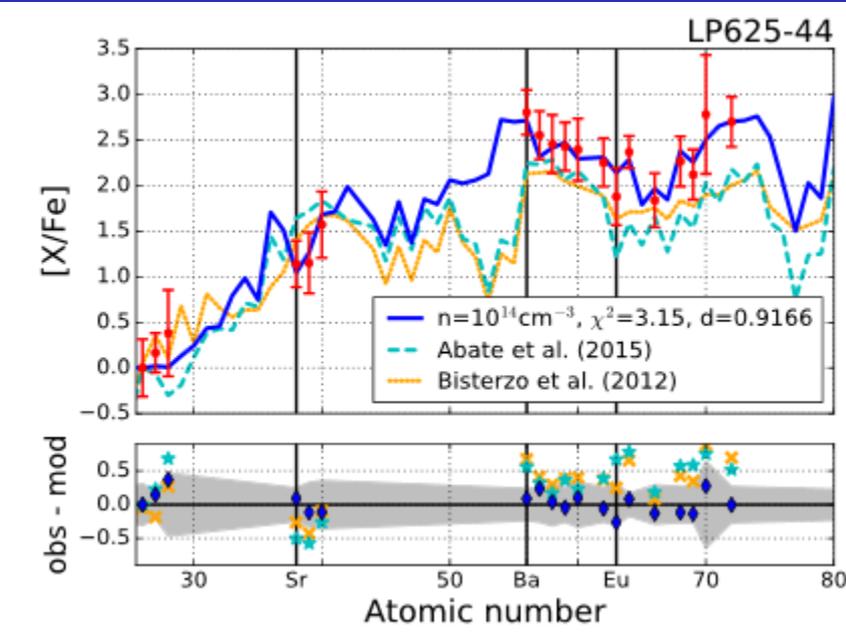
PIEs:

transient phase or destructive episode?

Dardelet+ 2015

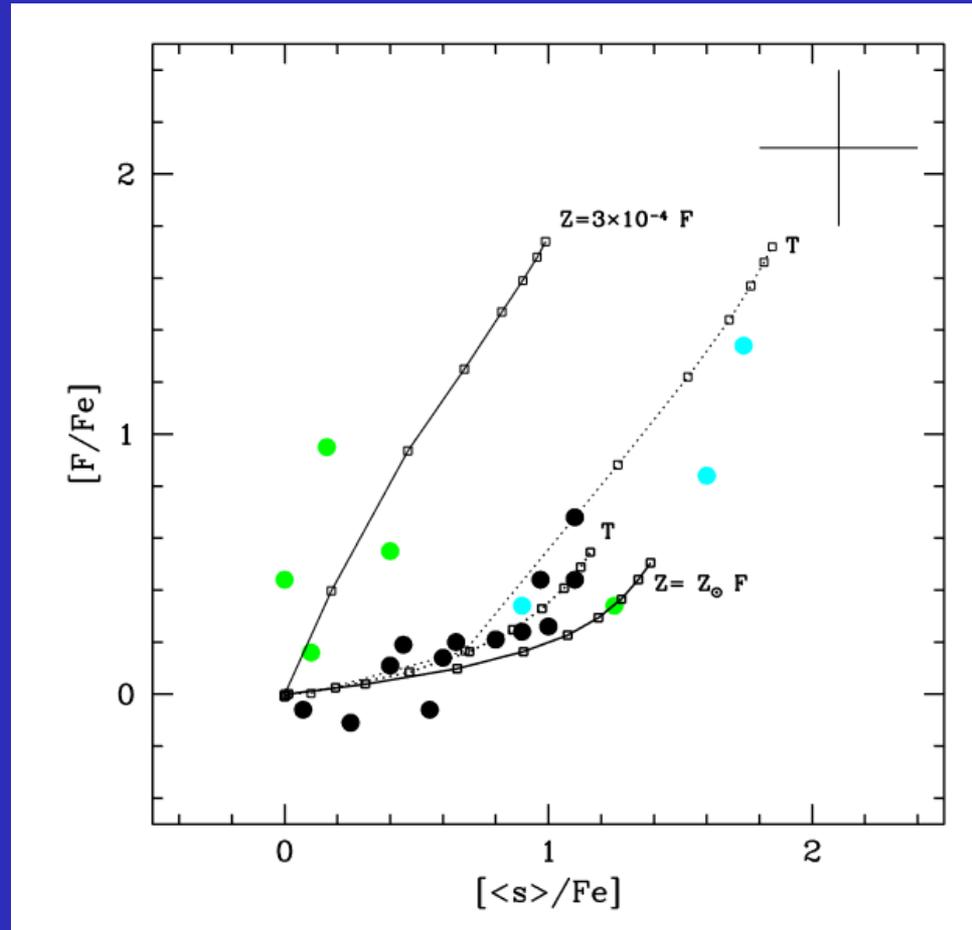
Observed [hs/lr] ratios can be matched with very high neutron densities ($n_n > 10^{15} \text{ cm}^{-3}$) lasting for about 0.1 yr.

Hampel+ 2016



Fluorine production at low metallicity

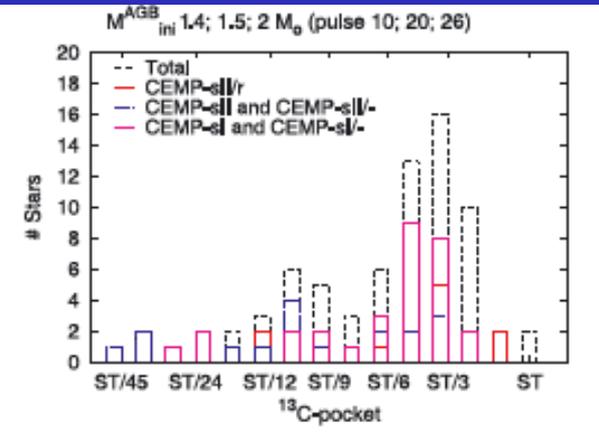
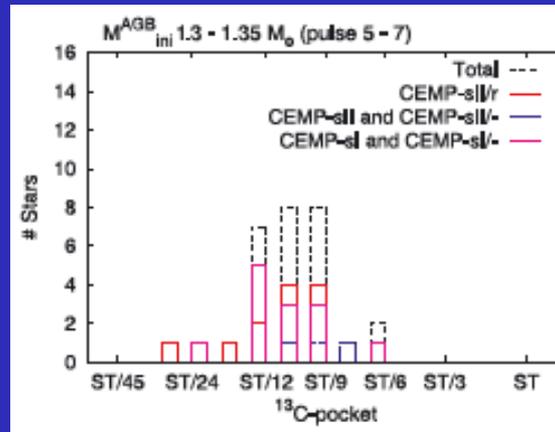
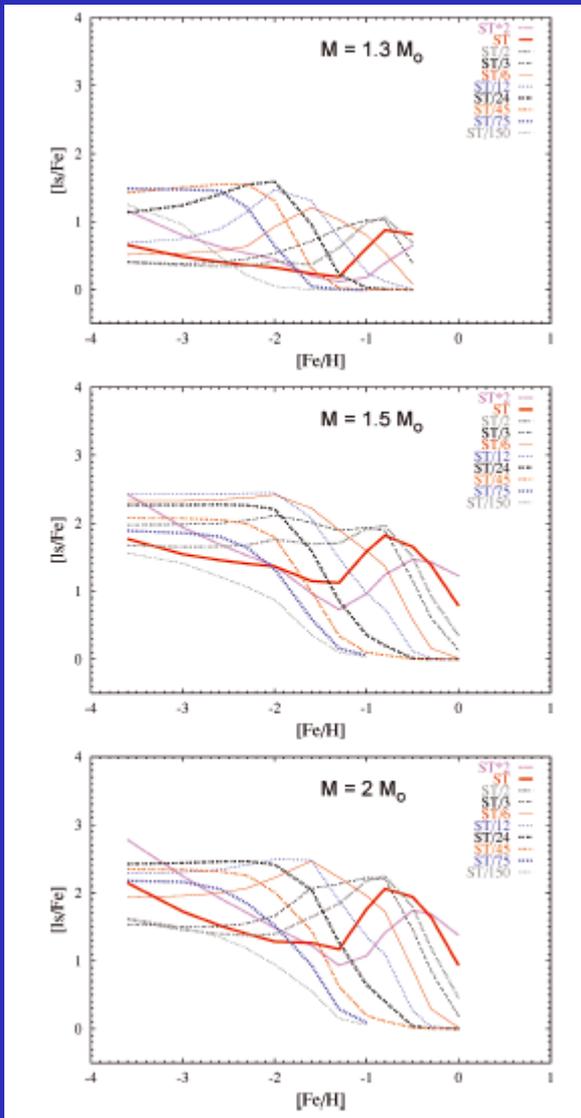
Abia+2015



It's not just a problem of relative values, but also of absolute ones!



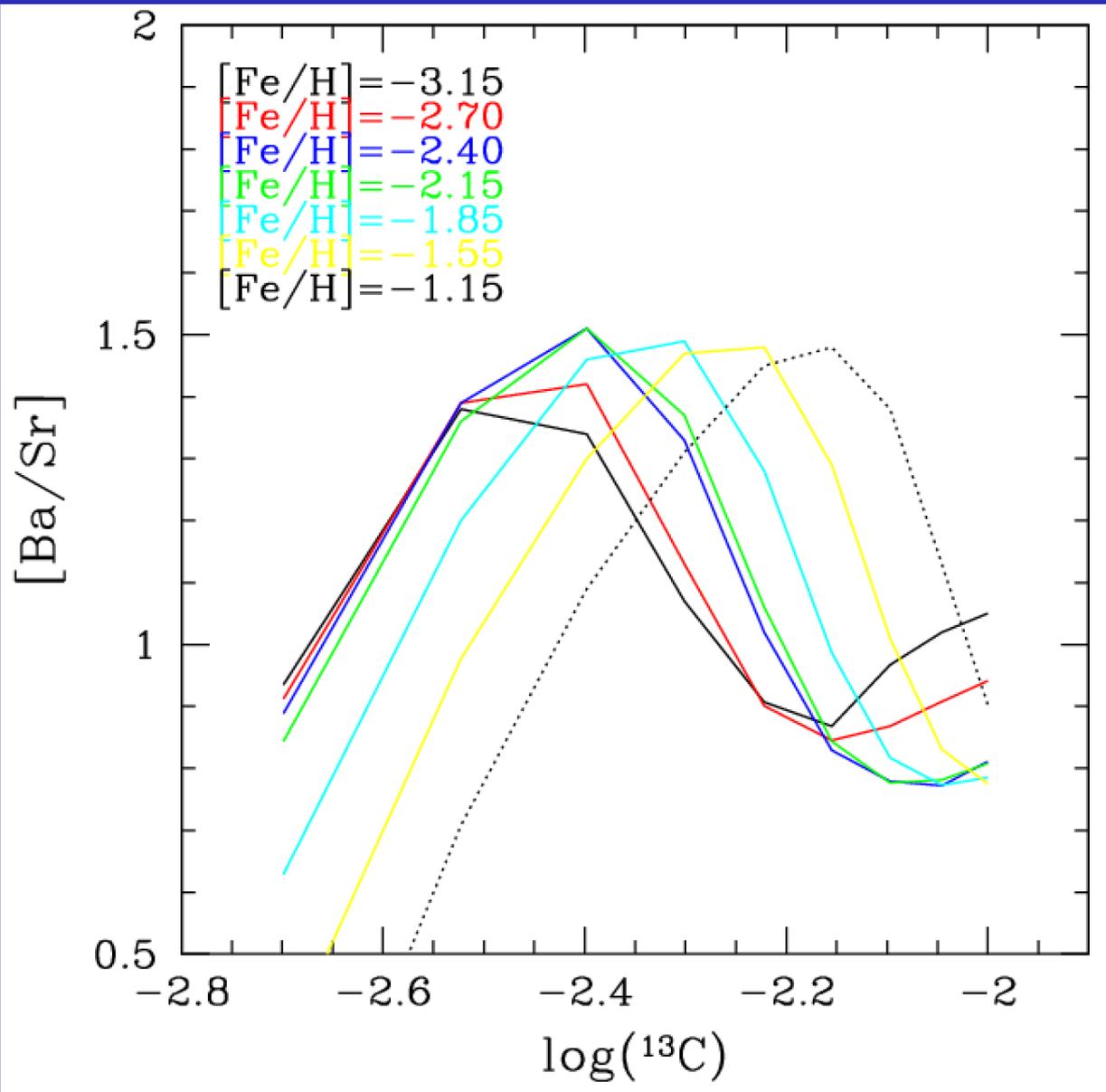
HINTS from POST_PROCESSES



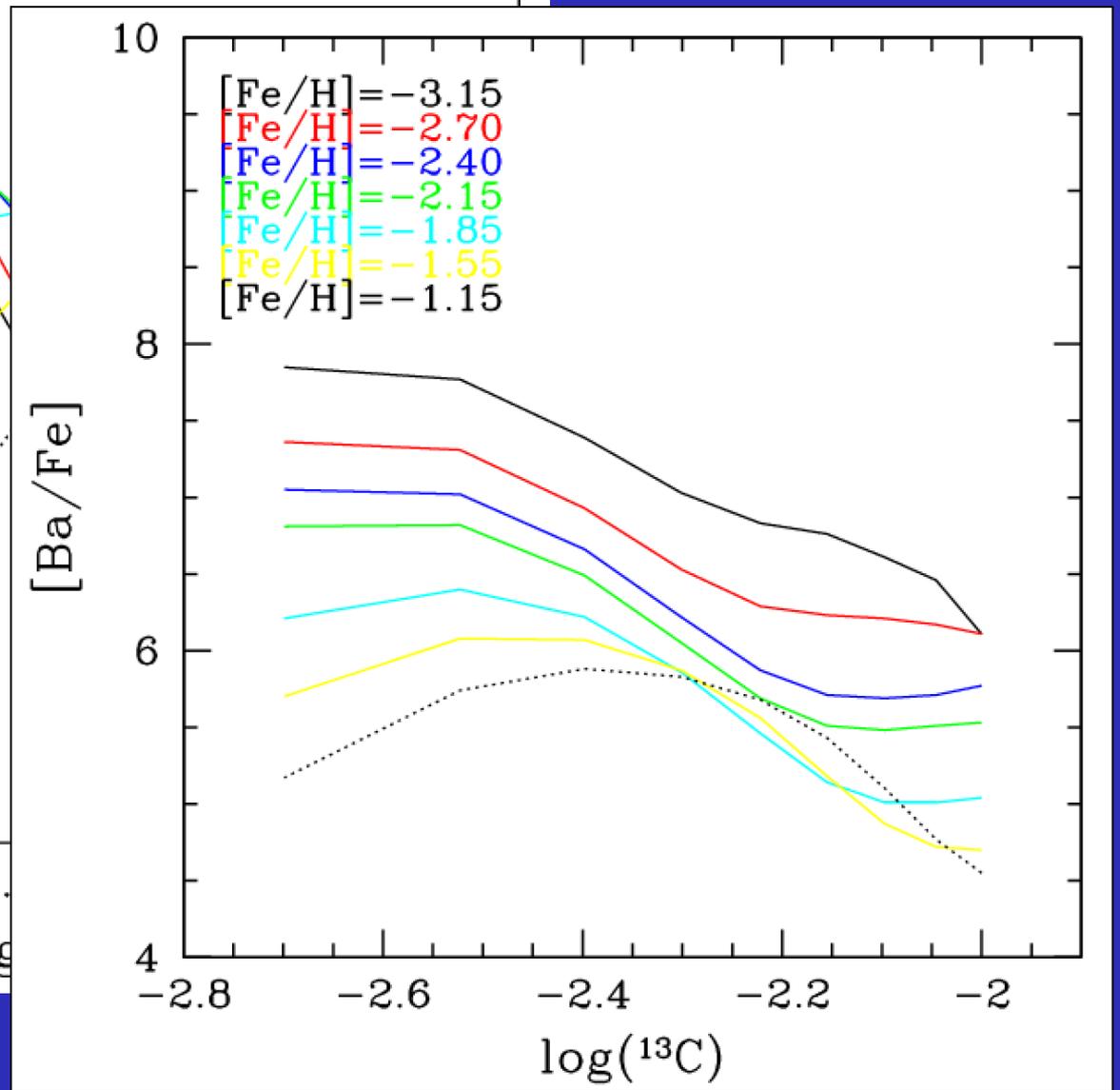
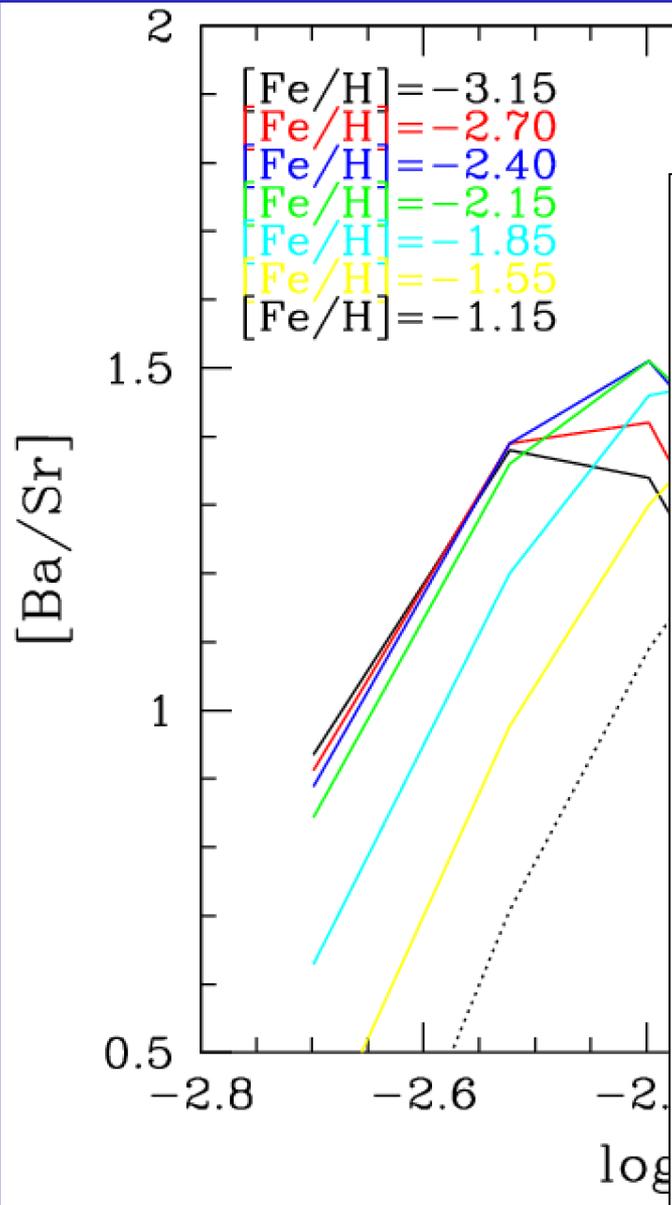
Bisterzo+ 2011

Bisterzo+ 2010

TOY MODEL



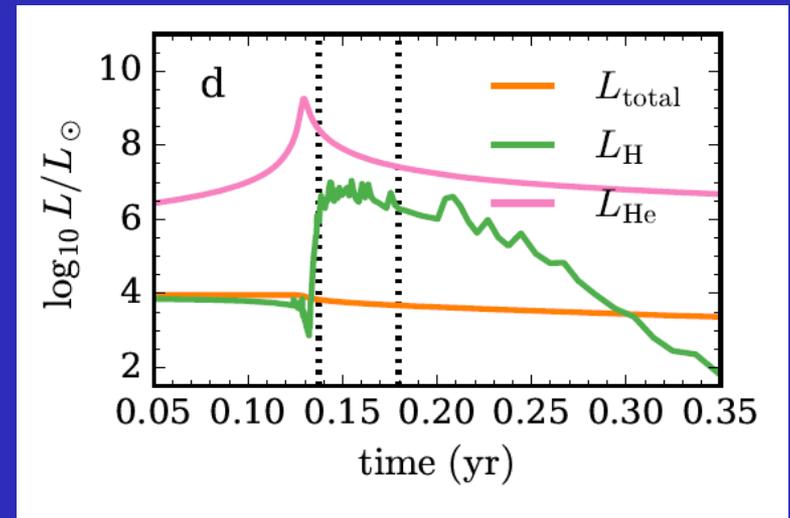
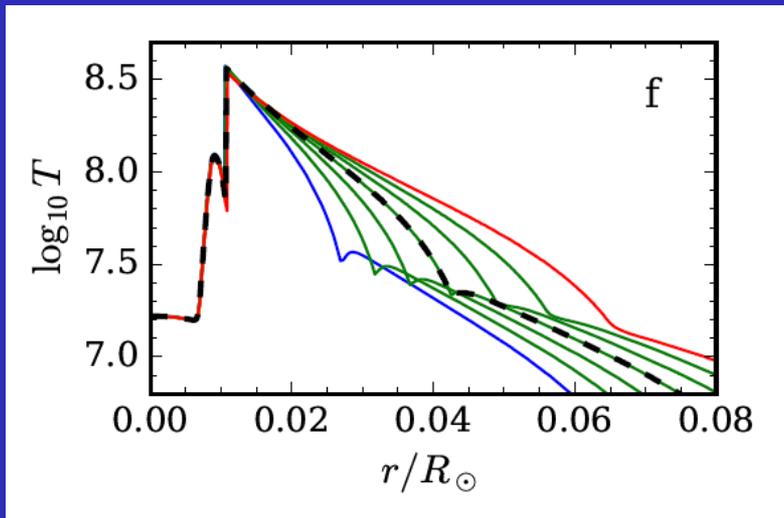
TOY MODEL



ALTERNATIVE SOLUTIONS?

H-ingestion in rapidly accreting WDs (talk by F. Herwig)

Activation of the intermediate neutron-capture process (i process), as the dominant process for the production of heavy elements beyond Fe.



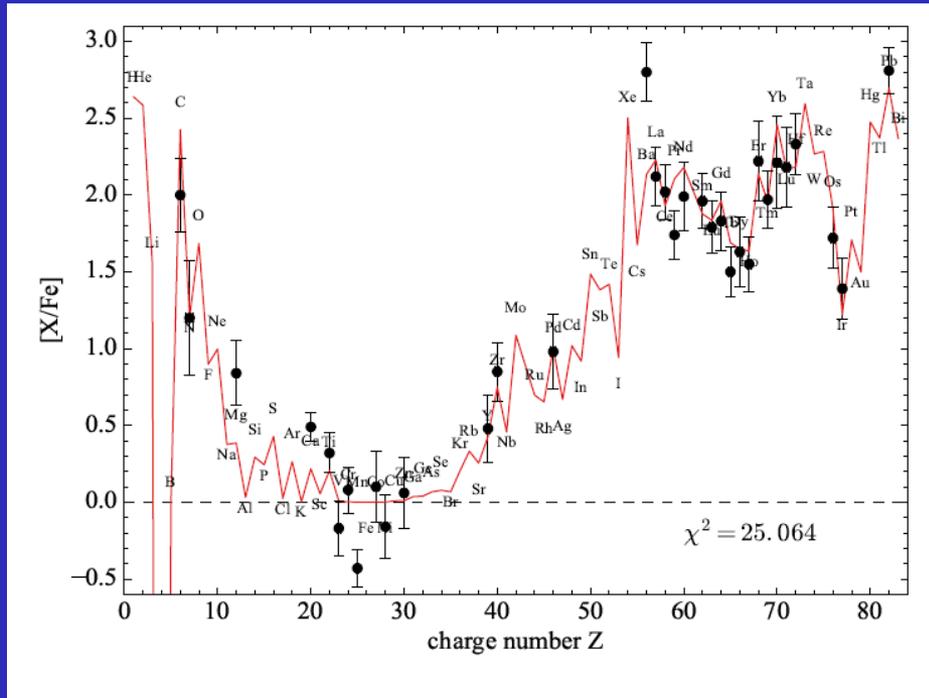
Denissenkov+ 2018

Higher temperature at the base of the convective shell

NO SPLITTING of the shell

ALTERNATIVE SOLUTIONS?

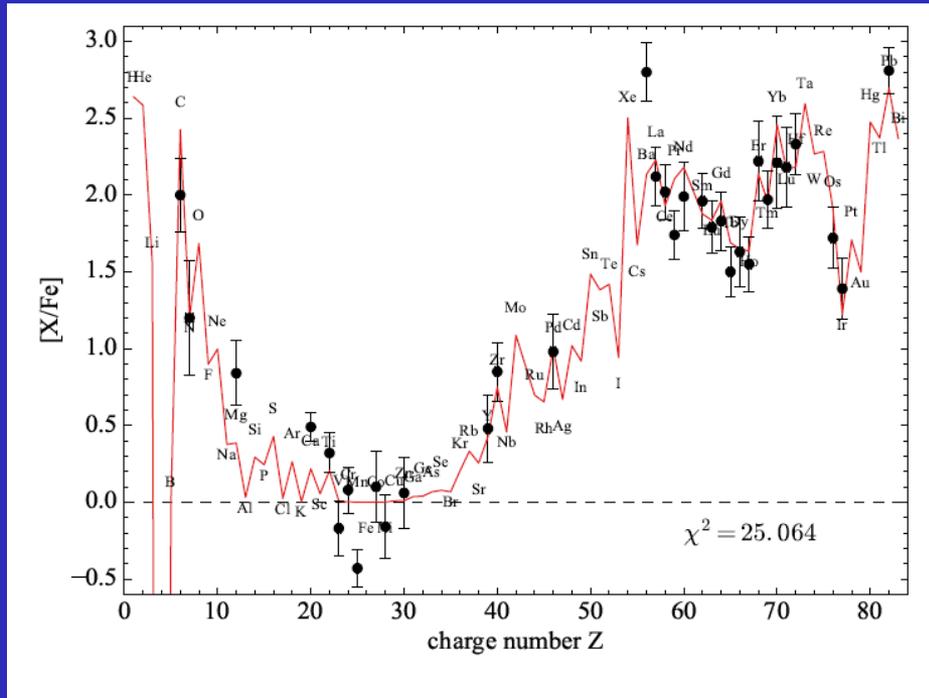
H-ingestion in rapidly accreting WDs (RAWD)



Denissenkov+ 2018

ALTERNATIVE SOLUTIONS?

H-ingestion in rapidly accreting WDs (RAWD)



Denissenkov+ 2018

PROBLEMS

- Statistics: how many triple systems in the halo? Binarity of CEMP s/r stars? (talk by Abate & Stancliffe)

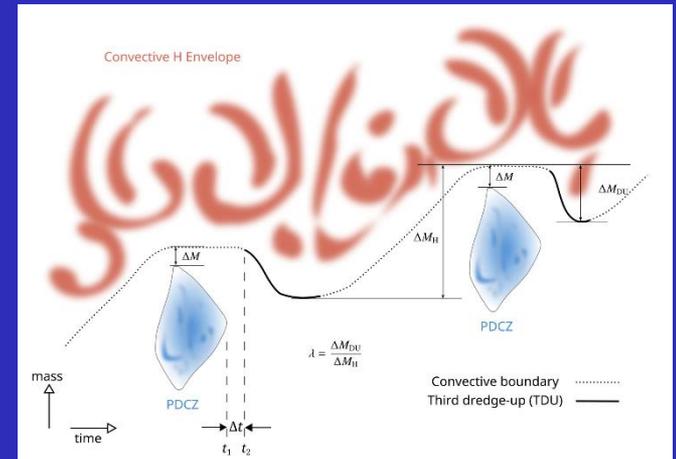
ALTERNATIVE SOLUTIONS?

Massive AGBs stars at low Z

Jones+ 2016 suggest that PIEs occurring in massive AGBs could lead to the observed [hs/lr] ratios. However, no s-process calculation has been performed yet (?)

Complex interaction between dredge-up and dredge-out events.

Next talk by C. Doherty



Jones+ 2016

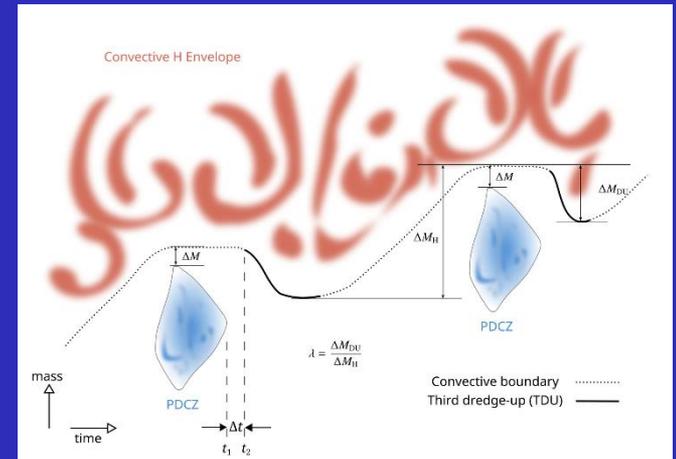
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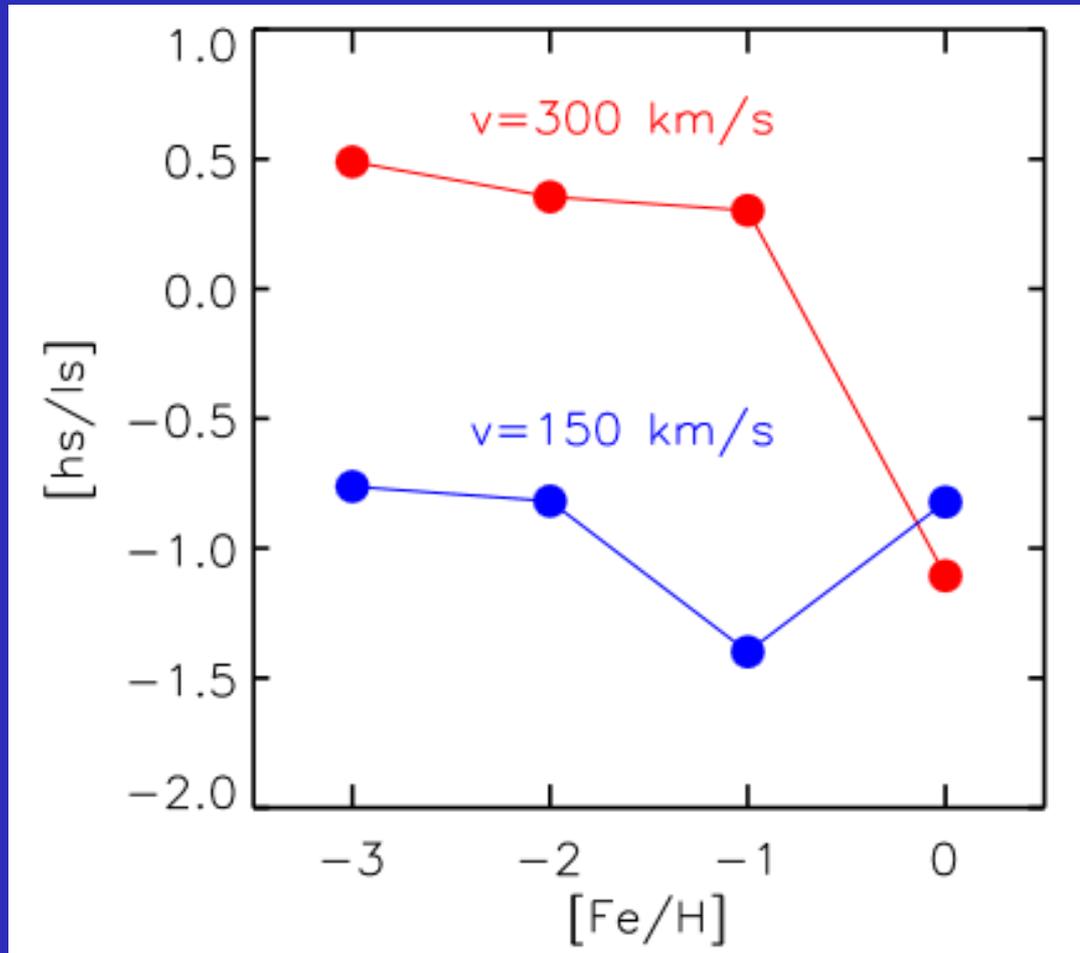
Jones+ 2016

PROBLEMS

- Statistics
- Very high temperature (see Goriely & Siess 2004)

ALTERNATIVE SOLUTIONS?

Rotating massive stars at low Z



See also
Frischknecht+ 2016

Talk by G. Meynet

Limongi & Chieffi 2018

Take home message

1. Mechanism at the origin of the ^{13}C pocket still not unequivocally identified;
2. Only post-processes are able to fit observed distributions;
3. Rotation cannot help improving the situation;
4. PIEs (i-process) could be a viable solution, but AGB stellar models are not yet able to reproduce observed distributions
5. Magnetic induced mixing: to be studied yet!
6. Alternative solutions (RAWD)? To be verified!