Z' Explanations of Neutral Current B Anomalies

by

Ben Allanach

(University of Cambridge)

- Can we directly discover the Z's responsible
- Third Family Hypercharge Model
- General SM$\times U(1)$ model

BCA, Gripaios, You, arXiv:1710.06363; BCA, Davighi, arXiv:1809.01158; BCA, Corbett, Dolan, You, arXiv:1810.02166; BCA, Davighi, Melville, arXiv:1812.04602

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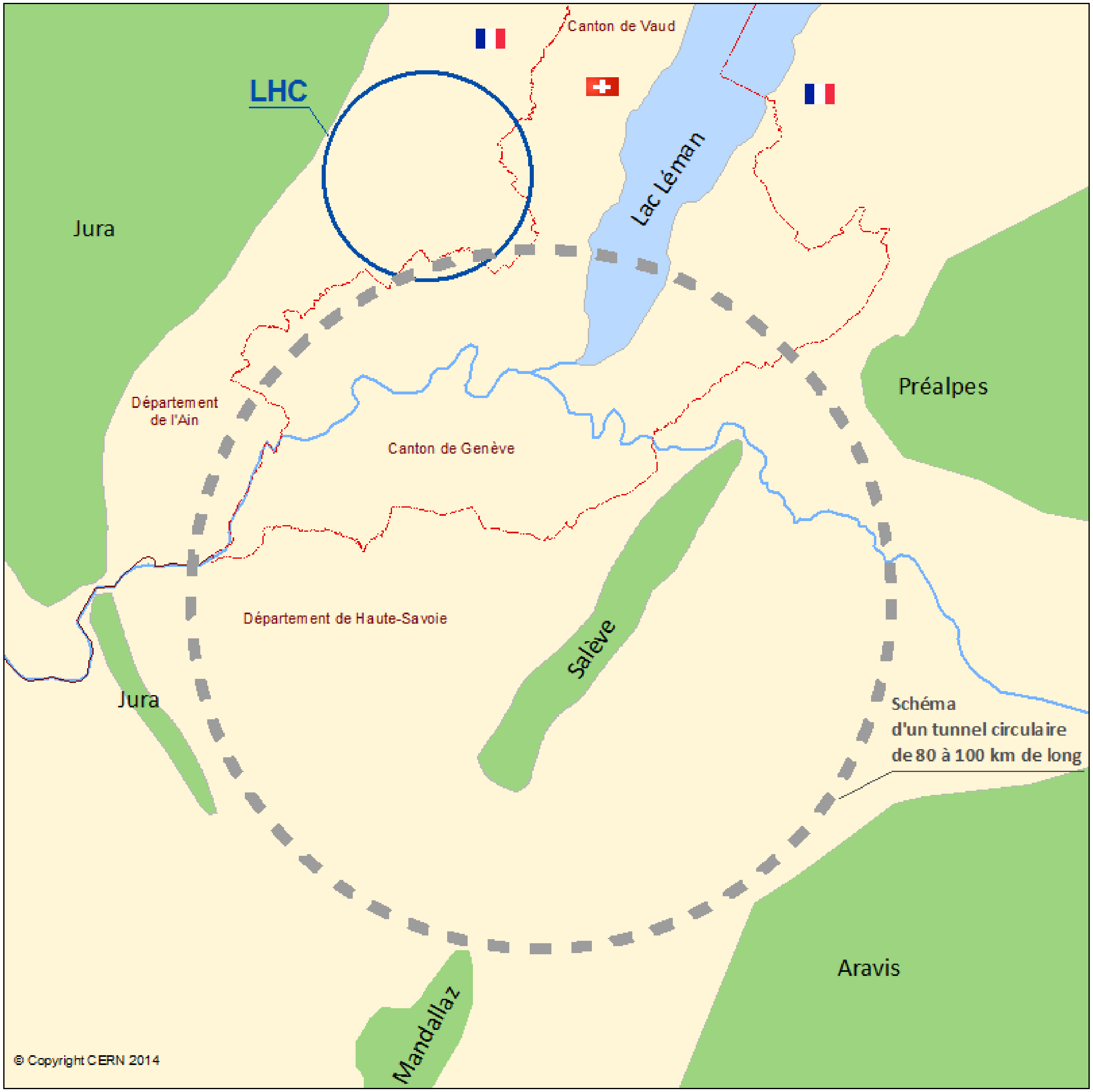
Cern

Cern draws up plans for collider four times the size of Large Hadron

The Future Circular Collider would smash particles together in a tunnel 100km long


LHC
Canton de Vaud
Lac Léman
Jura
Département
de l'Ain
Canton de Genève
Préalpes
Département de Haute-Savoie
Salève
Jura
Schéma
d'un tunnel circulaire
de 80 à 100 km de long
Aravis
Mandallaz
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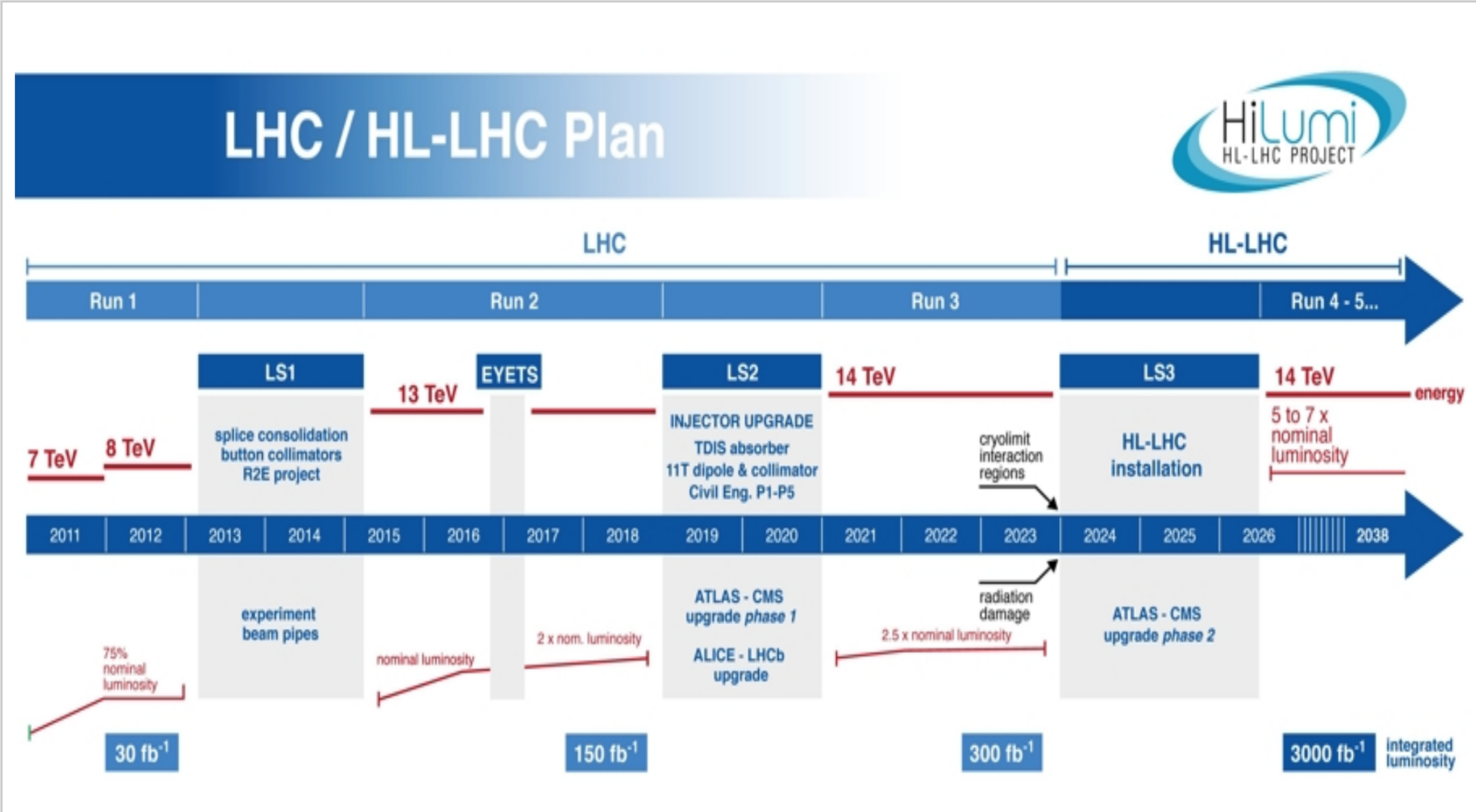
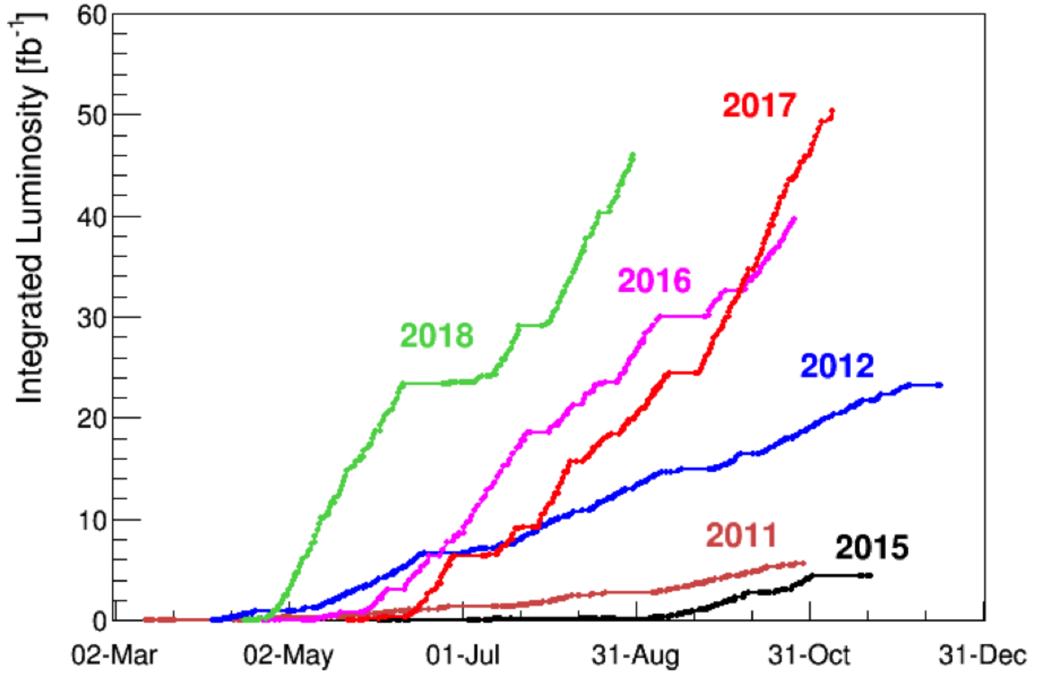

LHC / HL-LHC Plan
HiLumi
HL-LHC PROJECT
LHC
HL-LHC
Run 1
Run 2
Run 3
Run 4 - 5...
LS1
EYETS
LS2
LS3
7 TeV
8 TeV
13 TeV
14 TeV
14 TeV
energy
splice consolidation
button collimators
R2E project
INJECTOR UPGRADE
TDIS absorber
11T dipole & collimator
Civil Eng. P1-P5
cryolimit
interaction
regions
HL-LHC
installation
5 to 7 x
nominal
luminosity
2011
2012
2013
2014
2015
2016
2017
2018
2019
2020
2021
2022
2023
2024
2025
2026
2038
experiment
beam pipes
ATLAS - CMS
upgrade phase 1
ALICE - LHCb
upgrade
radiation
damage
ATLAS - CMS
upgrade phase 2
75%
nominal
luminosity
nominal luminosity
2 x nom. luminosity
2.5 x nominal luminosity
30 fb-1
150 fb-1
300 fb-1
3000 fb-1
integrated
luminosity

LHC Upgrades



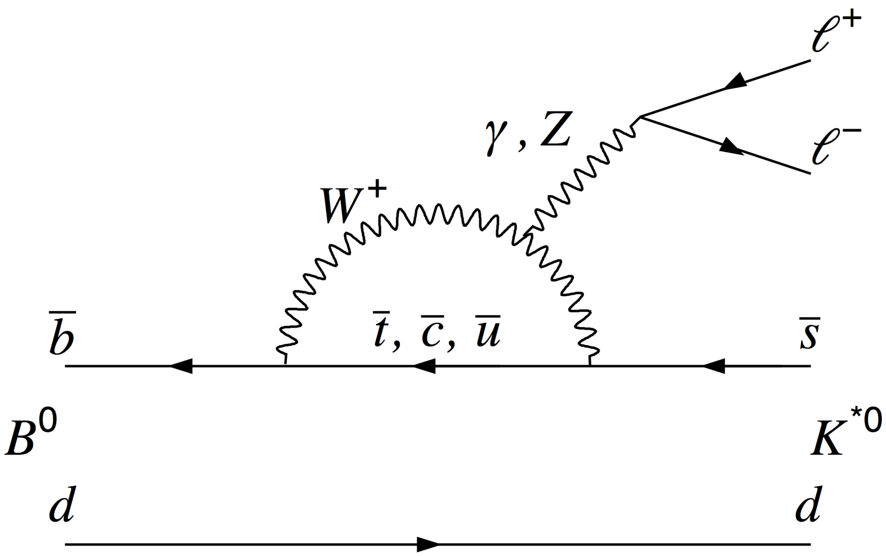
High Luminosity (HL) LHC: go to 3000 fb^{-1} (3 ab^{-1}).

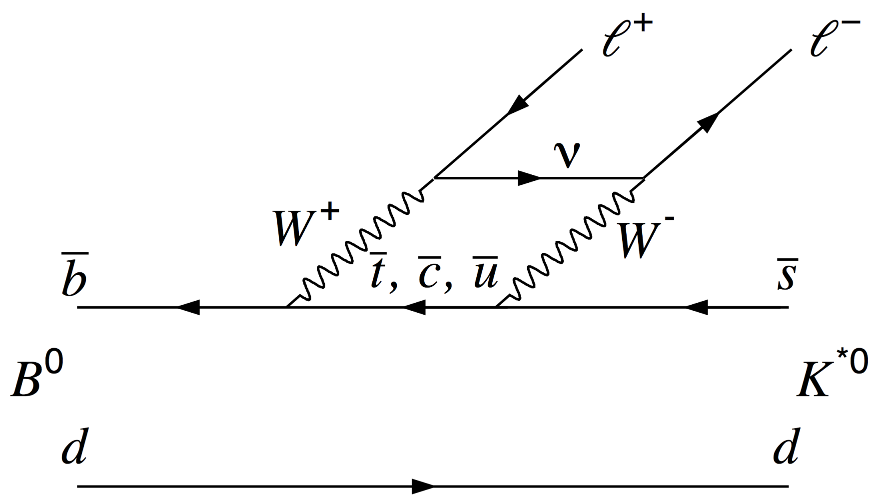
High Energy (HE) LHC: Put FCC magnets (16 Tesla rather than 8.33 Tesla) into LHC ring: roughly *twice* collision energy: 27 TeV.

$R_K^{(*)}$ in Standard Model

$$R_K = \frac{BR(B \to K\mu^+\mu^-)}{BR(B \to Ke^+e^-)}, \qquad R_{K^*} = \frac{BR(B \to K^*\mu^+\mu^-)}{BR(B \to K^*e^+e^-)}.$$

These are rare decays (each BR$\sim \mathcal{O}(10^{-7})$) because they are absent at tree level in SM.

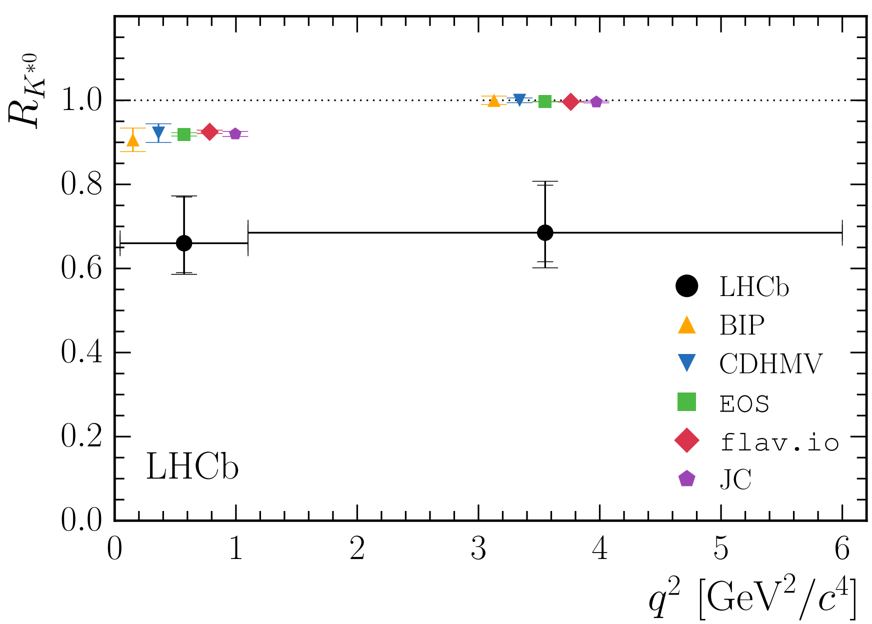


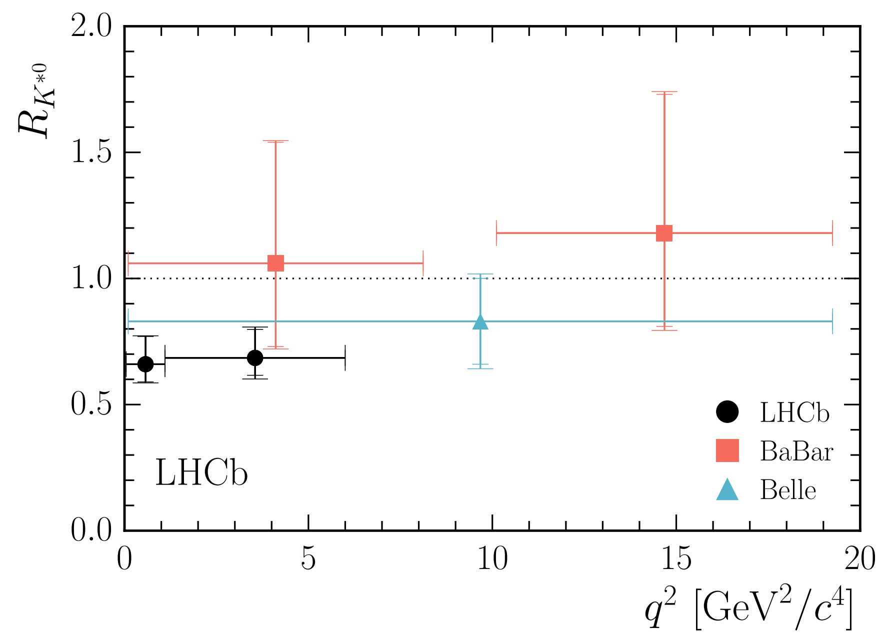


$R_{K^{(*)}}$ Measurements

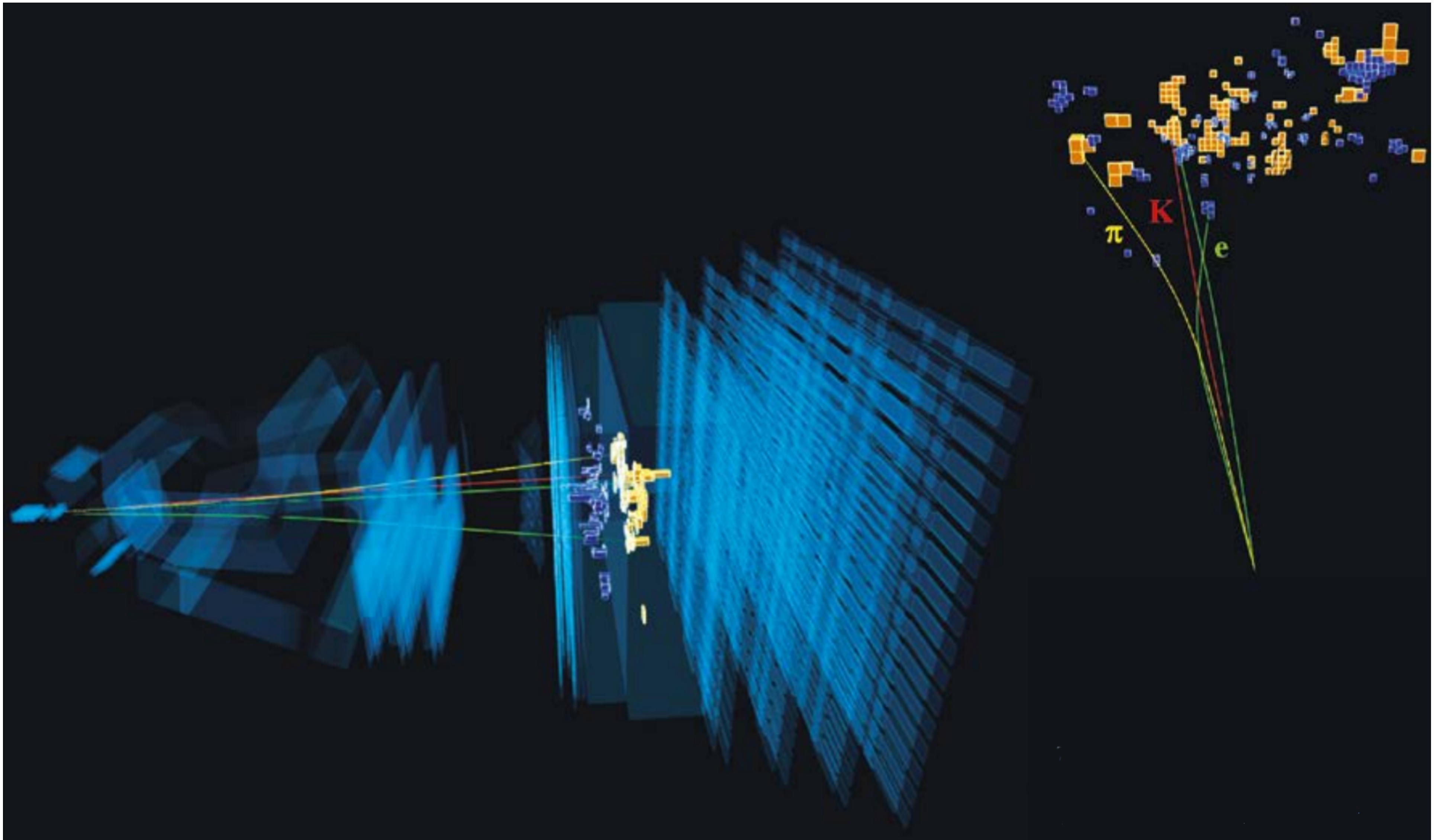
LHCb results from 7 and 8 TeV: $q^2 = m_{ll}^2$.

	q^2/GeV^2	SM	LHCb 3 fb^{-1}	σ
R_K	$[1, 6]$	1.00 ± 0.01	$0.745^{+0.090}_{-0.074}$	2.6
R_{K^*}	$[0.045, 1.1]$	0.91 ± 0.03	$0.66^{+0.11}_{-0.07}$	2.2
R_{K^*}	$[1.1, 6]$	1.00 ± 0.01	$0.69^{+0.11}_{-0.07}$	2.5



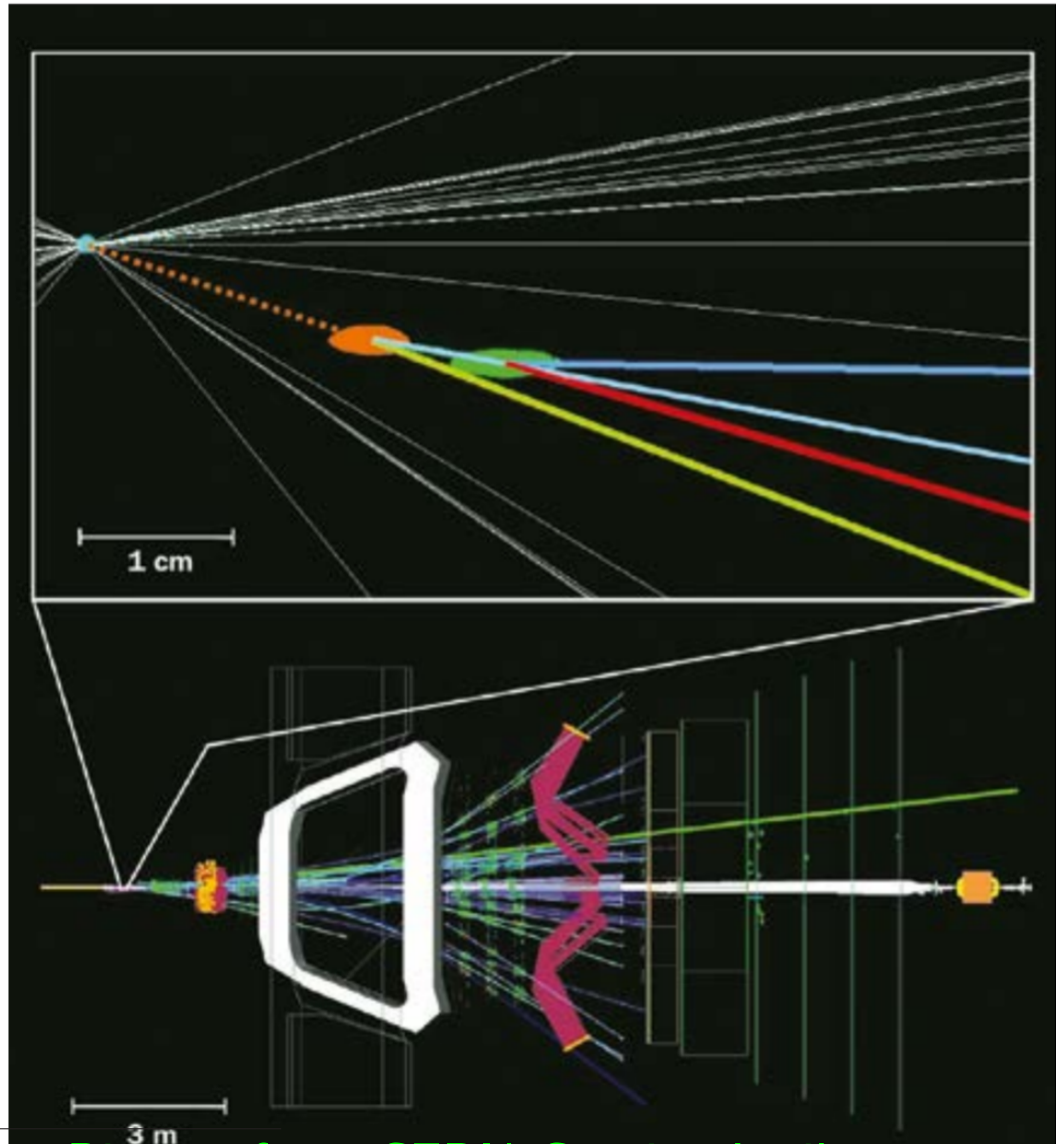


LHCb $B^0 \to K^{0*}e^+e^-$ Event[1]



[1] Picture from CERN Courier April 2018

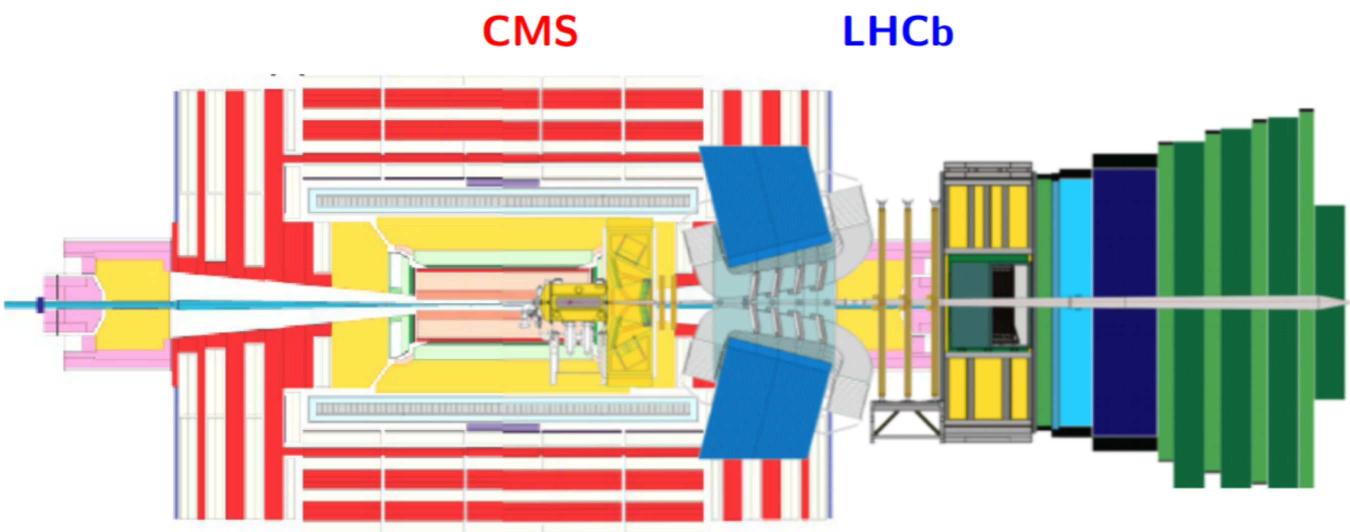
LHCb Detector II[2]



Picture from CERN Courier April 2018

2

LHCb Detector[3]

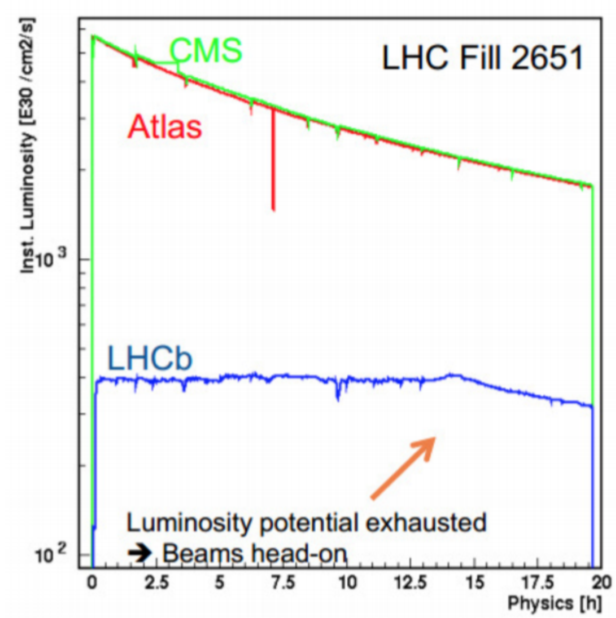


Optimised to study beauty and charm hadrons

→ provides complementary η coverage compared with a GPD.

LHCb as a **forward GPD**:

- ✓ Precise integrated luminosity computation
- ✓ **Stable** data-taking conditions due to **luminosity levelling**
- ✓ Average pile-up ∼2 (twice design)
- ✓ Excellent **vertexing**, particle ID, momentum resolution...
- × Lower luminosity than to ATLAS/CMS
- × Lower acceptance
- × Not hermetic! (can't use E_T^{miss} variable)



[3] Diaz talk 53rd EW Rencontres de Moriond 2018

Wilson Coefficients $\bar{c}^l_{ij}$

In SM, can form an EFT since $m_B \ll M_W$:

$$\begin{aligned}
\mathcal{O}^l_{ij} &= (\bar{s}\gamma^\mu P_i b)(\bar{l}\gamma_\mu P_j l)\,. \\
\mathcal{L}_{\rm eff} &\supset \sum_{l=e,\mu,\tau}\sum_{i=L,R}\sum_{j=L,R}\frac{c^l_{ij}}{\Lambda^2_{l,ij}}\mathcal{O}^l_{ij}\,, \\
&= \sum_{l=e,\mu,\tau} V_{tb}V^*_{ts}\frac{\alpha}{4\pi v^2}\left(\bar{c}^l_{LL}\mathcal{O}^l_{LL}+\bar{c}^l_{LR}\mathcal{O}^l_{LR}\right. \\
&\quad \left.+\bar{c}^l_{RL}\mathcal{O}^l_{RL}+\bar{c}^l_{RR}\mathcal{O}^l_{RR}\right) \\
\Rightarrow \bar{c}^l_{ij} &= (36\ \mathrm{TeV}/\Lambda)^2 c^l_{ij}.
\end{aligned}$$

$c^l_{ij} \sim \pm\mathcal{O}(1)$ all predicted by weak interactions in SM.

Which Ones Work?

Options *for a single* *BSM* *operator*:

- $\bar{c}^{e}_{ij}$ operators fine for $R_{K^{(*)}}$ but are disfavoured by global fits including other observables.
- $\bar{c}^{\mu}_{LR}$ disfavoured: predicts *enhancement* in both R_K and R_{K^*}
- $\bar{c}^{\mu}_{RR}$, $\bar{c}^{\mu}_{RL}$ disfavoured: they pull R_K and R_{K^*} in *opposite directions*.
- $\bar{c}^{\mu}_{LL} = -1.33 \pm 0.34$ fits well globally[4].

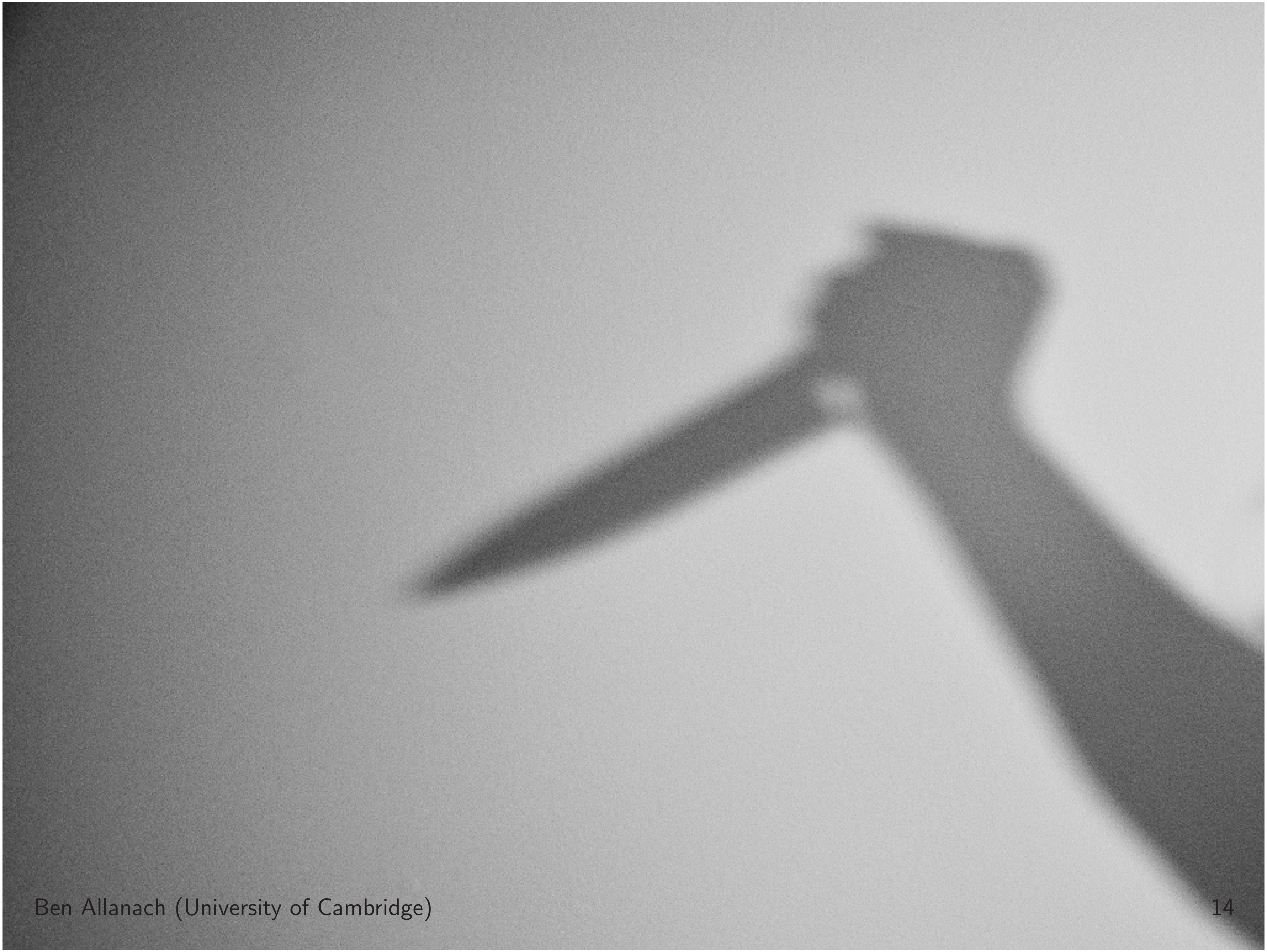
[4] D'Amico et al, 1704.05438.

Statistics[5]

	$\bar{c}^{\mu}_{LL}$	$\sqrt{\chi^2_{SM} - \chi^2_{best}}$
clean	-1.33 ± 0.34	4.1
dirty	-1.33 ± 0.32	4.6
all	-1.33 ± 0.23	6.2
	$C^{\mu}_9 = (\bar{c}^{\mu}_{LL} + \bar{c}^{\mu}_{LR})/2$	$\sqrt{\chi^2_{SM} - \chi^2_{best}}$
clean	-1.51 ± 0.46	3.9
dirty	-1.15 ± 0.17	5.5
all	-1.19 ± 0.15	6.7

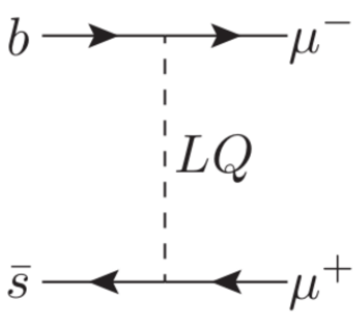
Table 1: A fit to flavour anomalies for ‘clean’ (R_K, R_{K^*}, $B_s \to \mu\mu$) and ‘dirty’ (100 others) observables

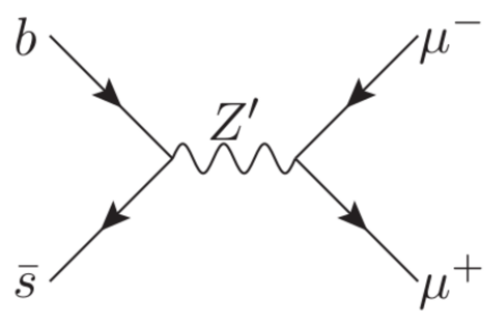
[5] D’Amico, Nardecchia, Panci, Sannino, Strumia, Torre, Urbano 1704.05438

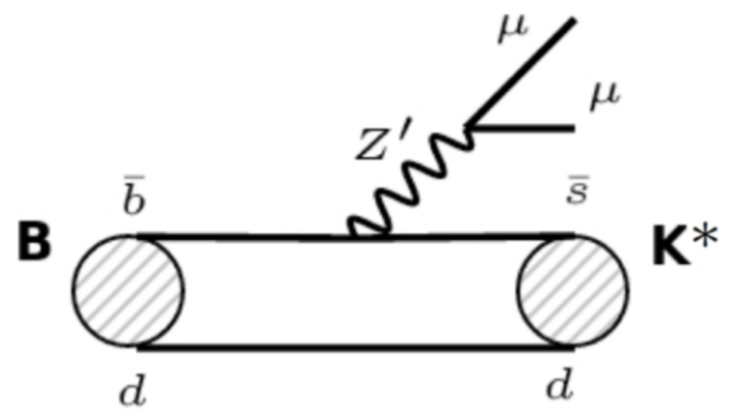


Simplified Models for c^{μ}_{LL}

At tree-level, we have:



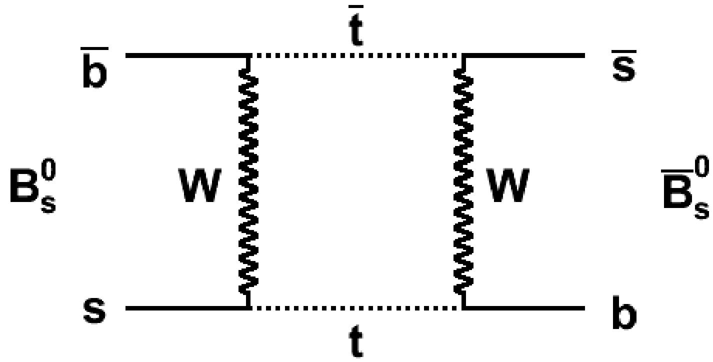


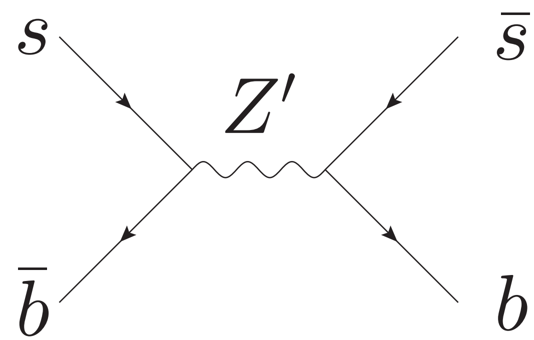


At loop-level, there are many more possibilities but the particles are 4π lighter: they are much easier to detect.

Principle of Maximal Pessimism

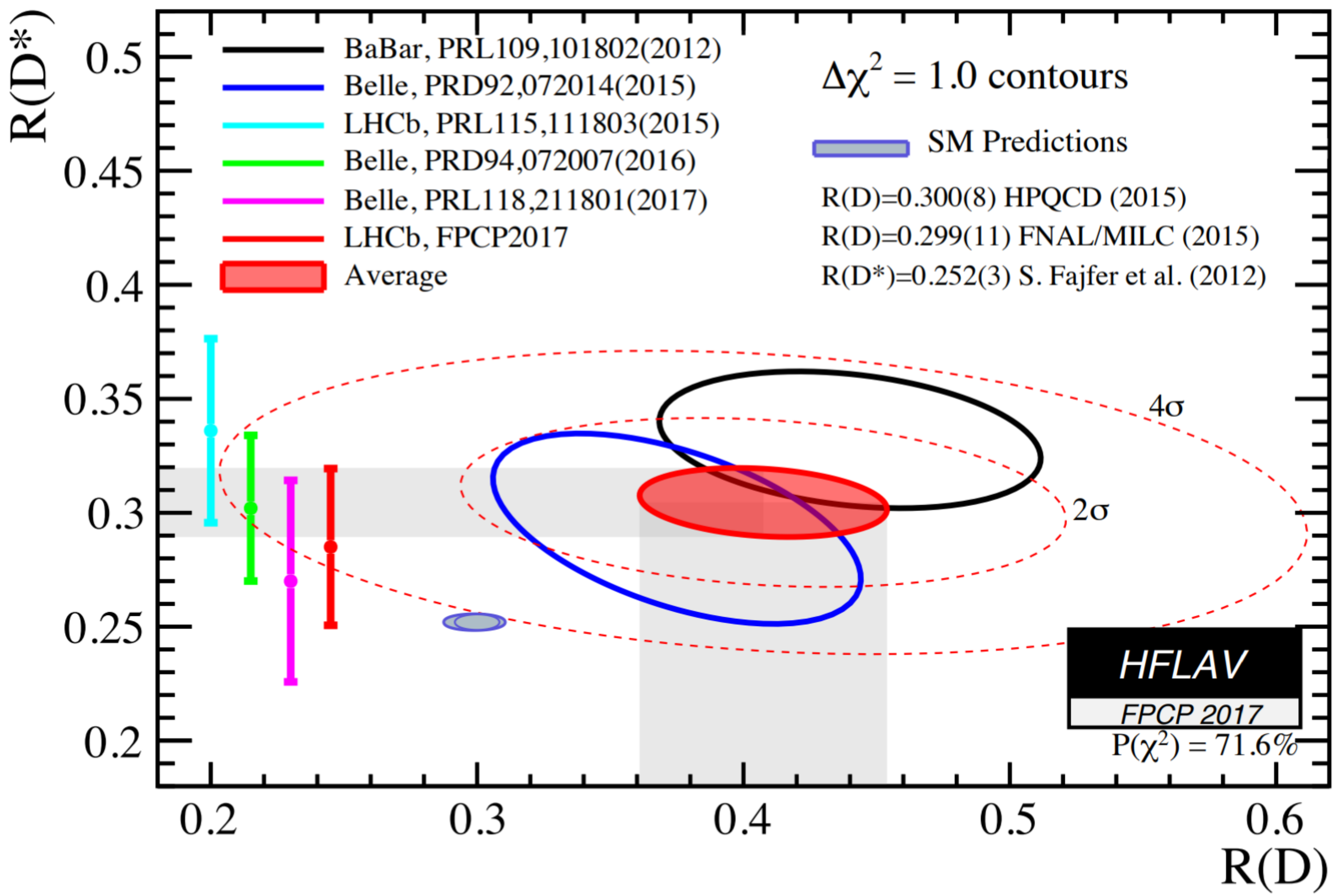
$B_s - \bar{B}_s$ Mixing





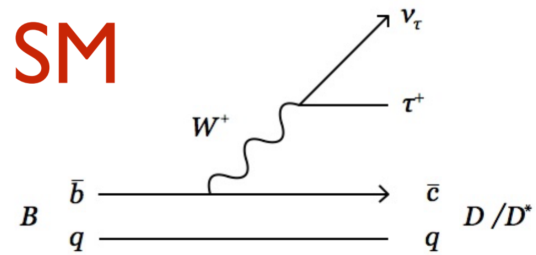
$$\bar{g}_L^{sb} \lesssim \frac{M_{Z'}}{148\ \text{TeV}}.$$

$$R_{D^{(*)}} = BR(B^- \to D^{(*)}\tau\nu)/BR(B^- \to D^{(*)}\mu\nu)$$



$R_{D^{(*)}}$: BSM Explanation

SM



. . . has to compete with

$$\mathcal{L}_{eff} = -\frac{2}{\Lambda^2}\left(\bar{c}_L \gamma^\mu b_L\right)\left(\bar{\tau}_L \gamma_\mu \nu_{\tau L}\right) + H.c.$$

$$\Lambda = 3.4\ \mathrm{TeV}$$

A factor 10 lower than required for $R_{K^{(*)}} \Rightarrow$ *different explanation?*

PMP$\Rightarrow$we ignore $R_{D^{(*)}}$.

Z' $\mu\mu$ ATLAS 13 TeV 36 fb^{-1}

ATLAS analysis: look for two track-based isolated μ, $p_T > 30$ GeV. One reconstructed primary vertex. Keep only highest scalar sum p_T pair[6].

$$m^2_{\mu_1\mu_2} = (p_1^\mu + p_2^\mu)\left(p_{1\mu} + p_{2\mu}\right)$$

CMS also have released[7] a similar 36 fb^{-1} analysis.

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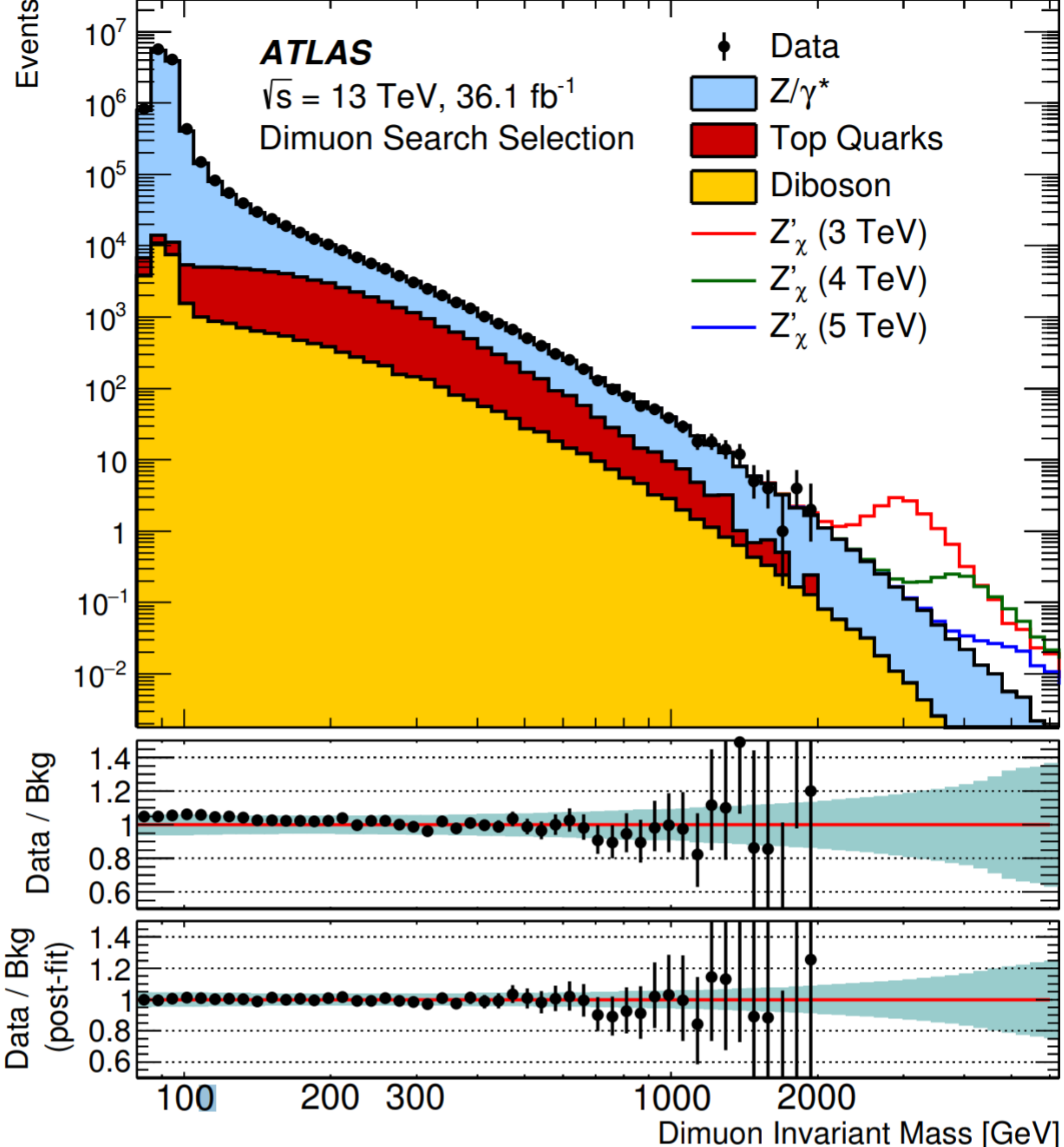
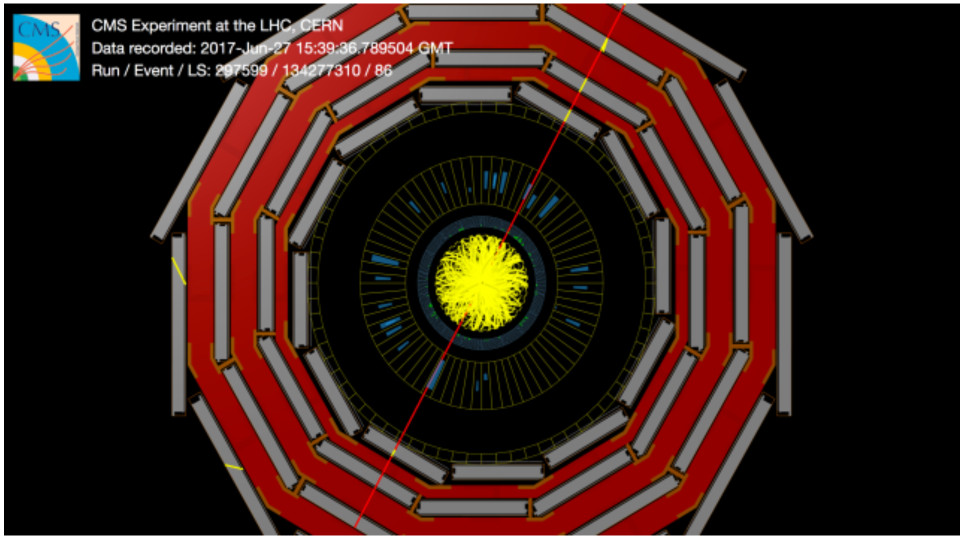
[6] 1707.02424

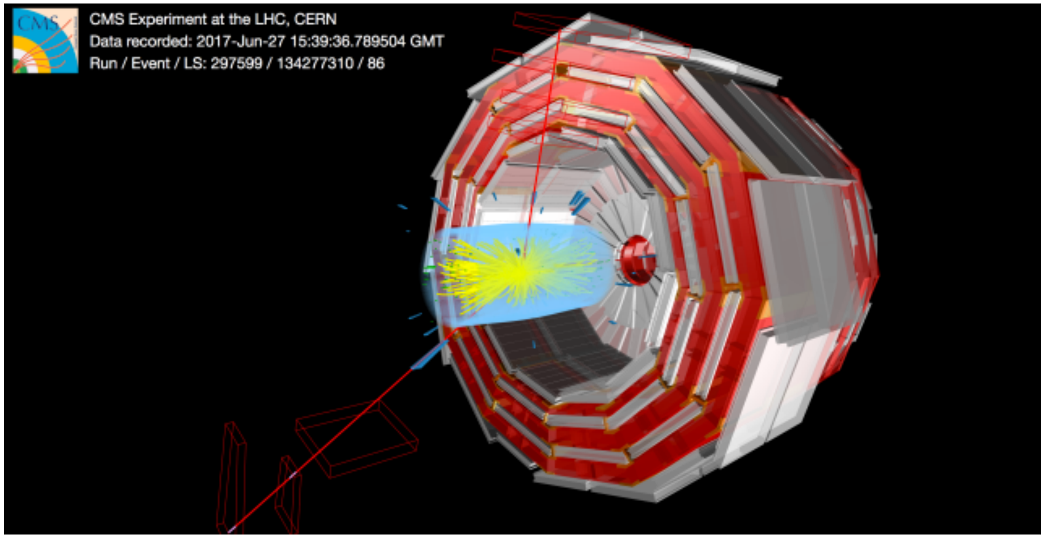
[7] 1803.06292

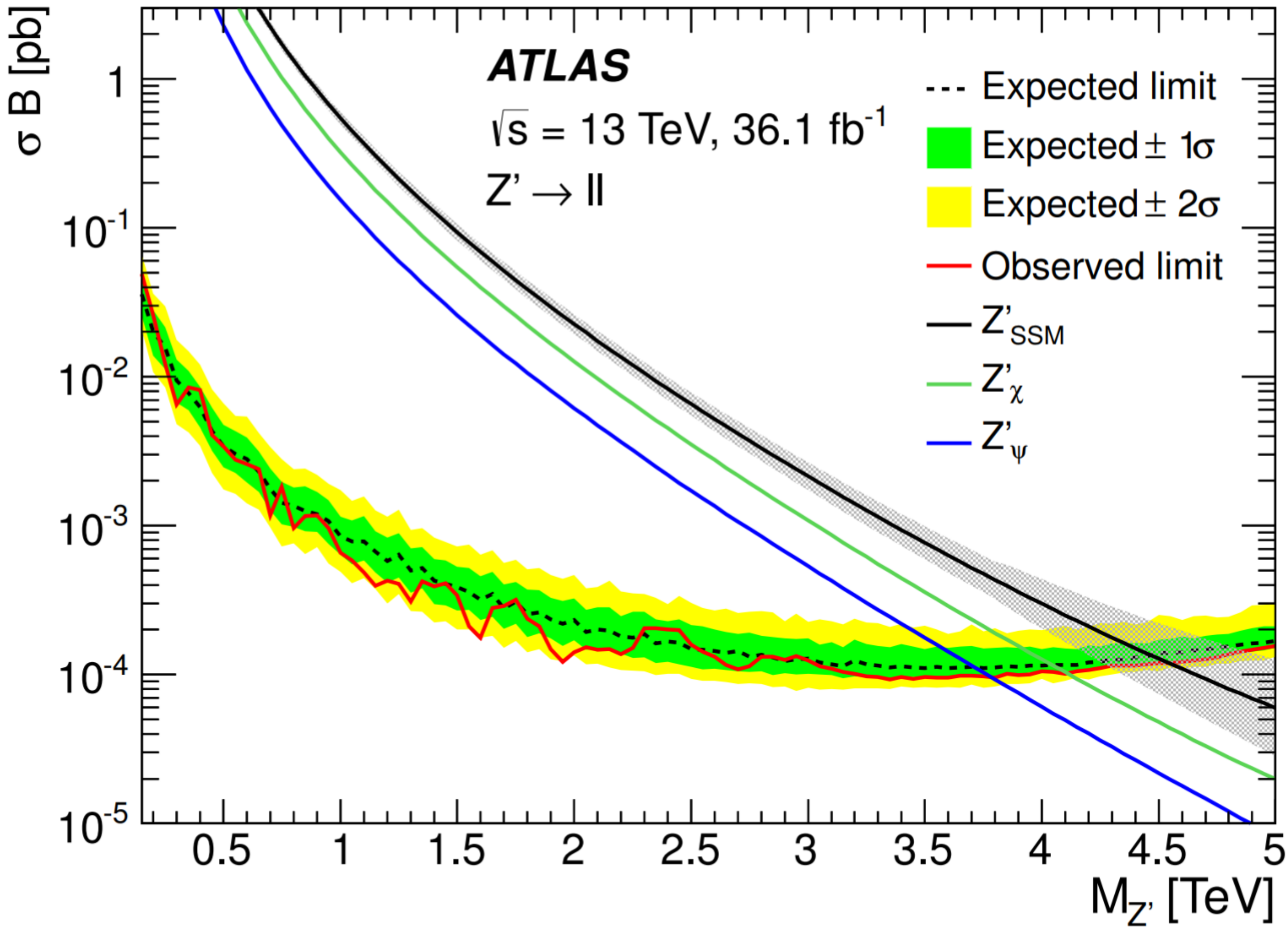


ATLAS
$\sqrt{s}$ = 13 TeV, 36.1 fb^{-1}
Dimuon Search Selection
Data
Z/γ*
Top Quarks
Diboson
Z'$_\chi$ (3 TeV)
Z'$_\chi$ (4 TeV)
Z'$_\chi$ (5 TeV)
Events
Data / Bkg
Data / Bkg (post-fit)
Dimuon Invariant Mass [GeV]

High $m_{\mu\mu} = 2.4$ TeV Event






σ B [pb]
ATLAS
√s = 13 TeV, 36.1 fb^-1
Z' → ll
Expected limit
Expected ± 1σ
Expected ± 2σ
Observed limit
Z'_SSM
Z'_χ
Z'_ψ
M_Z' [TeV]
1
10^-1
10^-2
10^-3
10^-4
10^-5
0.5
1
1.5
2
2.5
3
3.5
4
4.5
5

1607.03669

Simplified Z' Models[8]

Naïve model: only include couplings to $\bar{b}s/b\bar{s}$ and $\mu^+\mu^-$ (*less model dependent*).

$$\mathcal{L}_{Z'}^{\text{min.}} \supset \left(g_L^{sb} Z'_\rho \bar{s} \gamma^\rho P_L b + \text{h.c.} \right) + g_L^{\mu\mu} Z'_\rho \bar{\mu} \gamma^\rho P_L \mu \,,$$

which contributes to the $\mathcal{O}_{LL}^{\mu}$ coefficient with

$$\bar{c}_{LL}^{\mu} = -\frac{4\pi v^2}{\alpha_{\text{EM}} V_{tb} V_{ts}^*} \frac{g_L^{sb} g_L^{\mu\mu}}{M_{Z'}^2},$$

$$\Rightarrow g_L^{sb} g_L^{\mu\mu} \left(\frac{36 \text{ TeV}}{M_{Z'}} \right)^2 = -1.33 \pm 0.34 \text{ (clean)}.$$

[8] BCA, Queiroz, Strumia, Sun arXiv:1511.07447

Simplified Z' Models[9]

$$\mathcal{L}_{Z'f} = \left(\overline{\mathbf{Q'_L}}_i \lambda_{ij}^{(Q)} \gamma^\rho \mathbf{Q'_L}_j + \overline{\mathbf{L'_L}}_i \lambda_{ij}^{(L)} \gamma^\rho \mathbf{L'_L}_j\right) Z'_\rho,$$

After CKM mixing of $V = V_{u_L^\dagger} V_{d_L}$ and PMNS $U = V_{\nu_L}^\dagger V_{e_L}$,

$$\begin{aligned}\mathcal{L} \;=\; & \Big(\overline{\mathbf{u_L}} V \Lambda^{(Q)} V^\dagger \gamma^\rho \mathbf{u_L} + \overline{\mathbf{d_L}} \Lambda^{(Q)} \gamma^\rho \mathbf{d_L} + \\ & \overline{\mathbf{n_L}} U \Lambda^{(L)} U^\dagger \gamma^\rho \mathbf{n_L} + \overline{\mathbf{e_L}} \Lambda^{(L)} \gamma^\rho \mathbf{e_L}\Big) Z'_\rho,\end{aligned}$$

where

$$\Lambda^{(Q)} \equiv V_{d_L}^\dagger \lambda^{(Q)} V_{d_L}, \qquad \Lambda^{(L)} \equiv V_{e_L}^\dagger \lambda^{(L)} V_{e_L}.$$

[9] BCA, Corbett, Dolan, You, arXiv:1810.02166

Limiting Cases

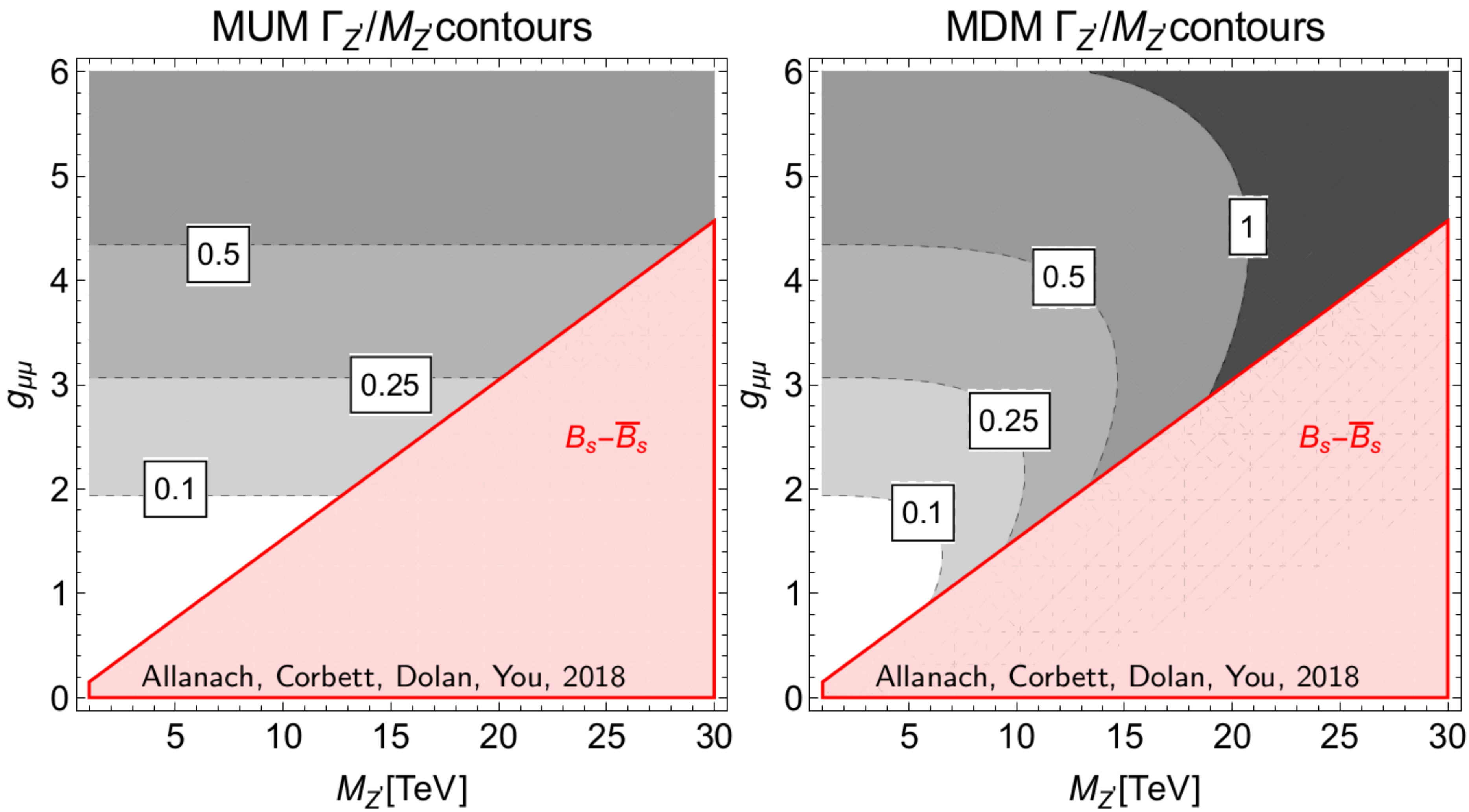
Mixed Up Model: all quark mixing is in left-handed ups

$$\Lambda^{(Q)} = g_{bs} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \qquad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

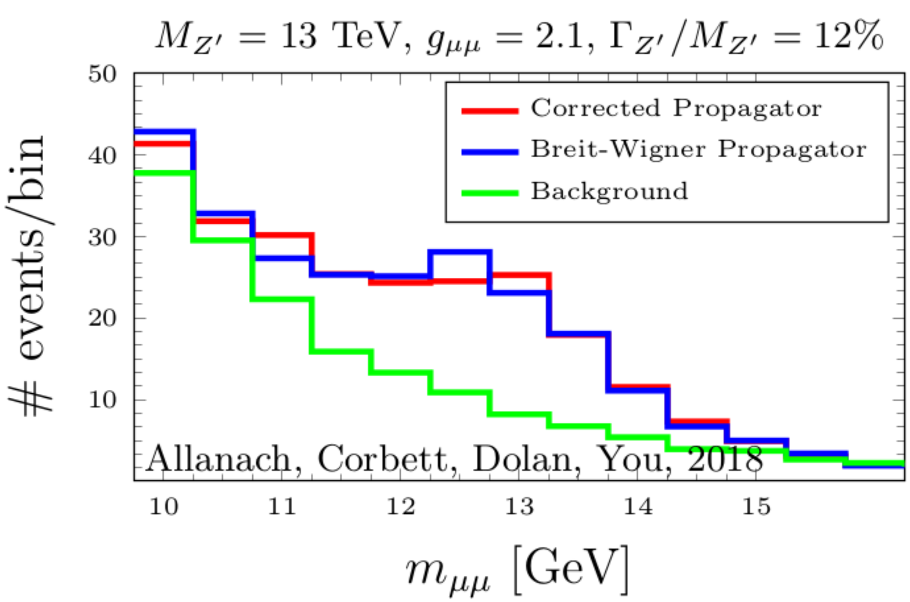
Mixed Down Model: all quark mixing is in left-handed downs

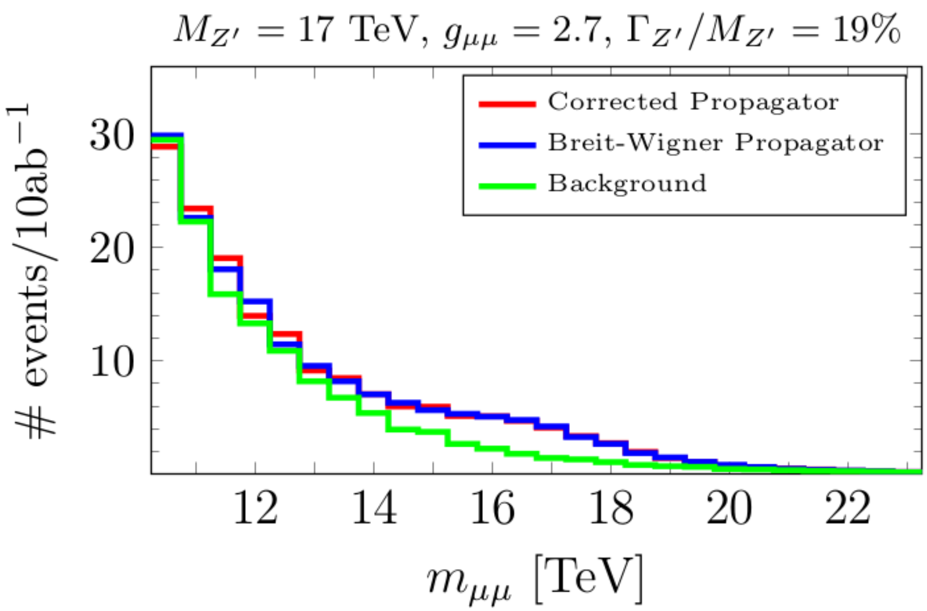
$$\Lambda^{(Q)} = g_{tt} V^\dagger \cdot \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot V, \qquad \Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

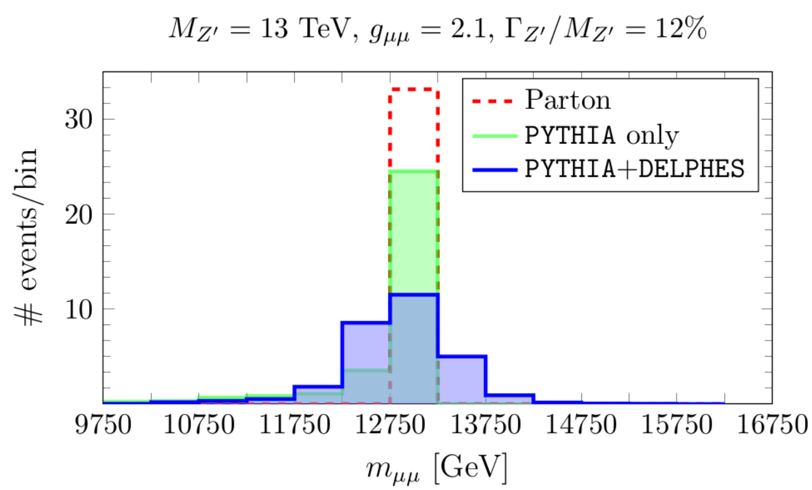
$\Rightarrow g_{bs} = V_{ts}^* V_{tb} g_{tt} = 0.04 g_{tt}$: the quark couplings are weaker than the leptonic ones

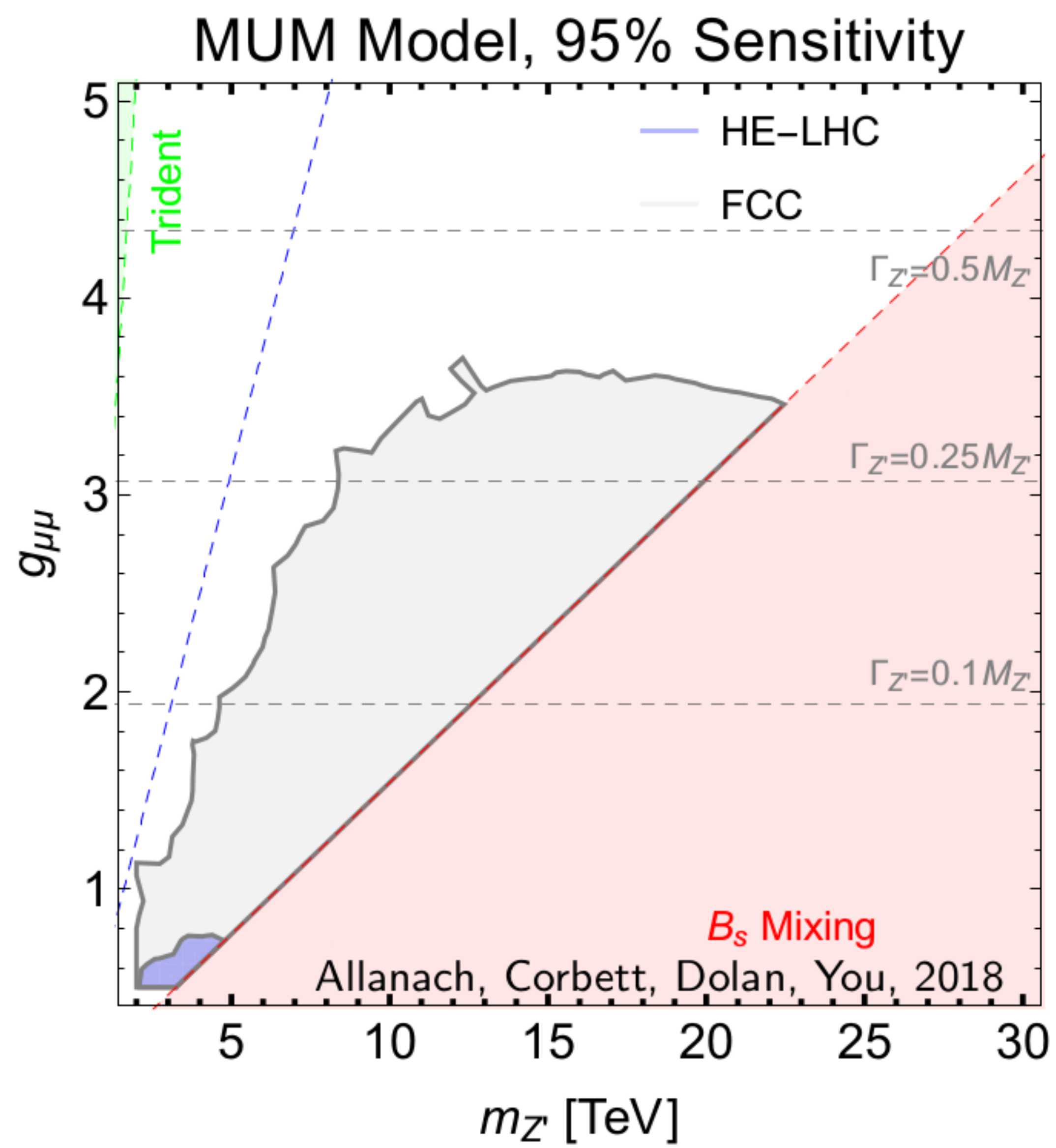


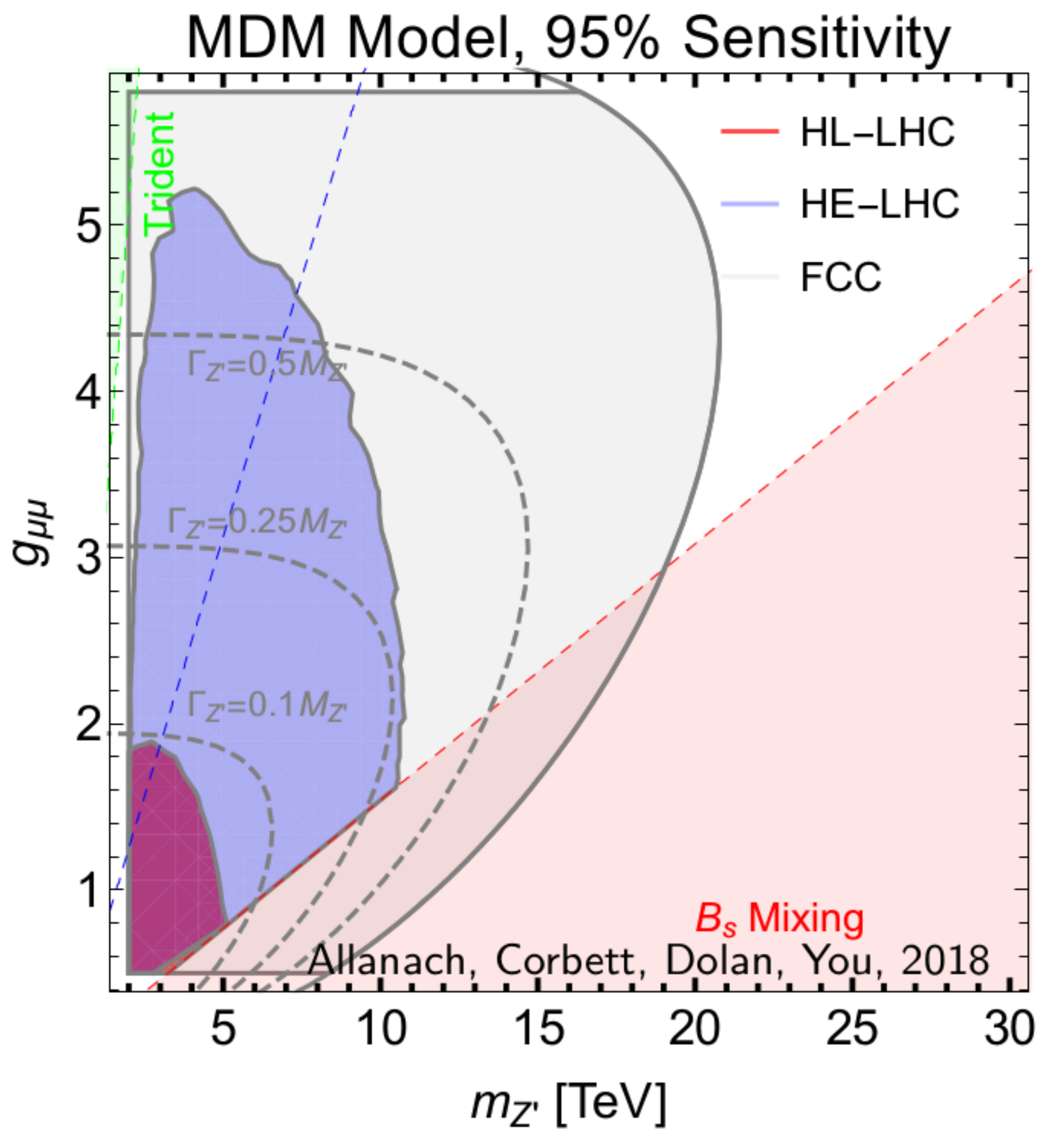
Widths: pick g_{bs} to fit anomalies at each point.


$M_{Z'} = 13$ TeV, $g_{\mu\mu} = 2.1$, $\Gamma_{Z'}/M_{Z'} = 12\%$
Corrected Propagator
Breit-Wigner Propagator
Background
Allanach, Corbett, Dolan, You, 2018
events/bin
$m_{\mu\mu}$ [GeV]


$M_{Z'} = 17$ TeV, $g_{\mu\mu} = 2.7$, $\Gamma_{Z'}/M_{Z'} = 19\%$
Corrected Propagator
Breit-Wigner Propagator
Background
events/10ab^{-1}
$m_{\mu\mu}$ [TeV]


$M_{Z'} = 13$ TeV, $g_{\mu\mu} = 2.1$, $\Gamma_{Z'}/M_{Z'} = 12\%$
Parton
PYTHIA only
PYTHIA+DELPHES
events/bin
$m_{\mu\mu}$ [GeV]


MUM Model, 95% Sensitivity
HE–LHC
FCC
Trident
$\Gamma_{Z'}$=0.5$M_{Z'}$
$\Gamma_{Z'}$=0.25$M_{Z'}$
$\Gamma_{Z'}$=0.1$M_{Z'}$
B_s Mixing
Allanach, Corbett, Dolan, You, 2018
$g_{\mu\mu}$
$m_{Z'}$ [TeV]
1
2
3
4
5
5
10
15
20
25
30


MDM Model, 95% Sensitivity
HL−LHC
HE−LHC
FCC
Trident
$\Gamma_{Z'}=0.5M_{Z'}$
$\Gamma_{Z'}=0.25M_{Z'}$
$\Gamma_{Z'}=0.1M_{Z'}$
B_s Mixing
Allanach, Corbett, Dolan, You, 2018
$g_{\mu\mu}$
$m_{Z'}$ [TeV]
1
2
3
4
5
5
10
15
20
25
30

During the 1990s

We wanted to be the Grand Architects, searching for **the** string model to rule them all

During the 2010s

We are happy with **any** beyond the Standard Model roof

Third Family Hypercharge Model

Add complex SM singlet scalar θ and gauged $U(1)_F$:

$$\begin{array}{c} SU(3) \times SU(2)_L \times U(1)_Y \times U(1)_F \\ \Big\downarrow \langle\theta\rangle \sim \text{Several TeV} \\ SU(3) \times SU(2)_L \times U(1)_Y \\ \Big\downarrow \langle H\rangle \sim 246 \text{ GeV} \\ SU(3) \times U(1)_{em} \end{array}$$

- SM fermion content
- anomaly cancellation
- 0 F charges for first two generations

Unique Solution

$$\boxed{\begin{array}{cccc} F_{Q'_i}=0 & F_{u_{R_i}'}=0 & F_{d_{R_i}'}=0 & F_{L'_i}=0 \\ F_{e_{R_i}'}=0 & F_H=-1/2 & F_{Q'_3}=1/6 & F_{u'_{R3}}=2/3 \\ F_{d'_{R3}}=-1/3 & F_{L'_3}=-1/2 & F_{e'_{R3}}=-1 & F_\theta\neq 0 \end{array}}$$

$$\mathcal{L}=Y_t\overline{Q_3{}'_L}Ht'_R+Y_b\overline{Q'_{3L}}H^cb'_R+Y_\tau\overline{L_3{}'_L}H^c\tau'_R+H.c.,$$

- First two families massless at renormalisable level
- Their masses and fermion mixings generated by small non-renormalisable operators

This explains the hierarchical heaviness of the third family and small CKM angles

$Z - X$ mixing

Because $F_H = -1/2$, $Z - X$ mix:

$$\mathcal{M}_N^2 = \frac{v^2}{4} \begin{pmatrix} g'^2 & -gg' & g'g_F \\ -gg' & g^2 & -gg_F \\ g'g_F & -gg_F & g_F^2(1+4F_\theta^2 r^2) \end{pmatrix} \begin{array}{c} -B_\mu \\ -W_\mu^3 \\ -X_\mu \end{array}$$

- $v \approx 246$ GeV is SM Higgs VEV
- $g_F = U(1)_F$ gauge coupling
- $r \equiv v_F/v \gg 1$, where $v_F = \langle\theta\rangle$
- F_θ is F *charge* of θ field

$Z - X$ mixing angle

$$\sin\alpha_z \approx \frac{g_F}{\sqrt{g^2+g'^2}}\left(\frac{M_Z}{M'_Z}\right)^2 \ll 1.$$

This gives small non-flavour universal couplings to the Z boson propotional to g_F and:

$$Z_\mu = \cos\alpha_z\left(-\sin\theta_w B_\mu + \cos\theta_w W^3_\mu\right) + \sin\alpha_z X_\mu,$$

$$
\begin{aligned}
\mathcal{L}_{X\psi} \;=\; g_F \;& \left(\frac{1}{6}\overline{\mathbf{u_L}}\Lambda^{(u_L)}\gamma^\rho \mathbf{u_L} + \frac{1}{6}\overline{\mathbf{d_L}}\Lambda^{(d_L)}\gamma^\rho \mathbf{d_L} - \right. \\
& \frac{1}{2}\overline{\mathbf{n_L}}\Lambda^{(n_L)}\gamma^\rho \mathbf{n_L} - \frac{1}{2}\overline{\mathbf{e_L}}\Lambda^{(e_L)}\gamma^\rho \mathbf{e_L} + \\
& \frac{2}{3}\overline{\mathbf{u_R}}\Lambda^{(u_R)}\gamma^\rho \mathbf{u_R} - \\
& \left. \frac{1}{3}\overline{\mathbf{d_R}}\Lambda^{(d_R)}\gamma^\rho \mathbf{d_R} - \overline{\mathbf{e_R}}\Lambda^{(e_R)}\gamma^\rho \mathbf{e_R}\right) Z'_\rho,
\end{aligned}
$$

$$
\Lambda^{(I)} \equiv V_I^\dagger \xi V_I, \qquad \xi = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}
$$

Z' couplings, $I \in \{u_L, d_L, e_L, \nu_L, u_R, d_R, e_R\}$

Example Case

Take a simple limiting case:
$V_{u_L} = 1 \Rightarrow V_{d_L} = V$, the CKM matrix. $V_{u_R} = V_{d_R} = V_{e_R} = 1$ for simplicity and the ease of passing bounds.

$$V_{d_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{sb} & -\sin\theta_{sb} \\ 0 & \sin\theta_{sb} & \cos\theta_{sb} \end{pmatrix}, \qquad V_{e_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix},$$

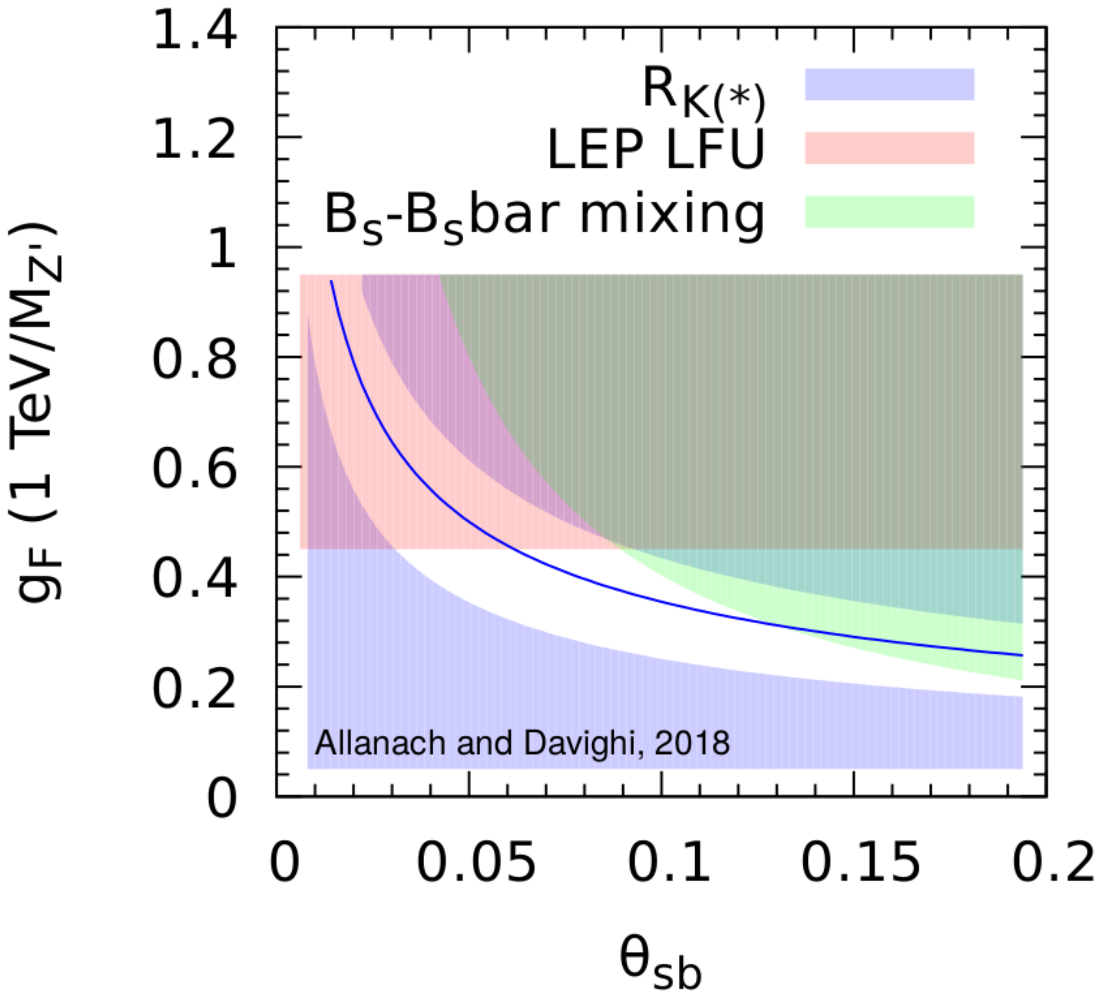
$V_{e_R} = 1 \Rightarrow V_{\nu_L} = V_{e_L} U^\dagger$, where U is the PMNS matrix.

Important Z' Couplings

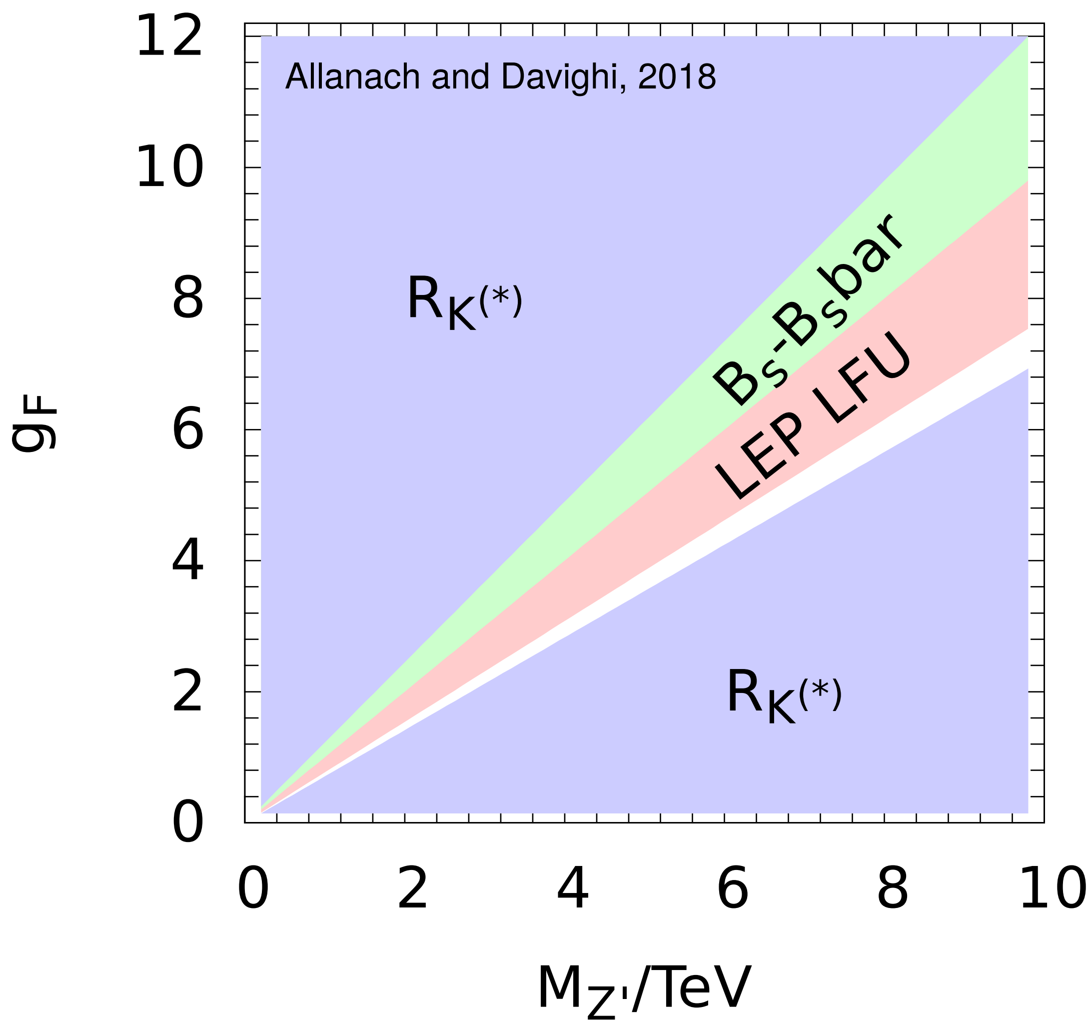
$$g_F \left(\frac{1}{6}\overline{\mathbf{d_L}} \begin{pmatrix} 0 & 0 & 0 \\ 0 & \sin^2\theta_{sb} & \frac{1}{2}\sin 2\theta_{sb} \\ 0 & \frac{1}{2}\sin 2\theta_{sb} & \cos^2\theta_{sb} \end{pmatrix} \not{Z}' \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} + \right.$$

$$\left. -\frac{1}{2}\overline{\mathbf{e_L}} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \not{Z}' \begin{pmatrix} e_L \\ \mu_L \\ \tau_L \end{pmatrix} \right)$$

Put $|\sin\theta_{sb}| = |V_{ts}| = 0.04$, so $g_{\mu\mu} \gg g_{bs}$, which helps us survive $B_s - \overline{B_s}$ constraint



$R_{K(*)}$
LEP LFU
B_s-$B_s$bar mixing
Allanach and Davighi, 2018
g_F (1 TeV/$M_{Z'}$)
θ_{sb}
0
0.2
0.4
0.6
0.8
1
1.2
1.4
0
0.05
0.1
0.15
0.2


Allanach and Davighi, 2018
$R_{K^{(*)}}$
B_s-$B_s$bar
LEP LFU
$R_{K^{(*)}}$
g_F
0
2
4
6
8
10
12
0
2
4
6
8
10
$M_{Z'}$/TeV

Example Case Predictions

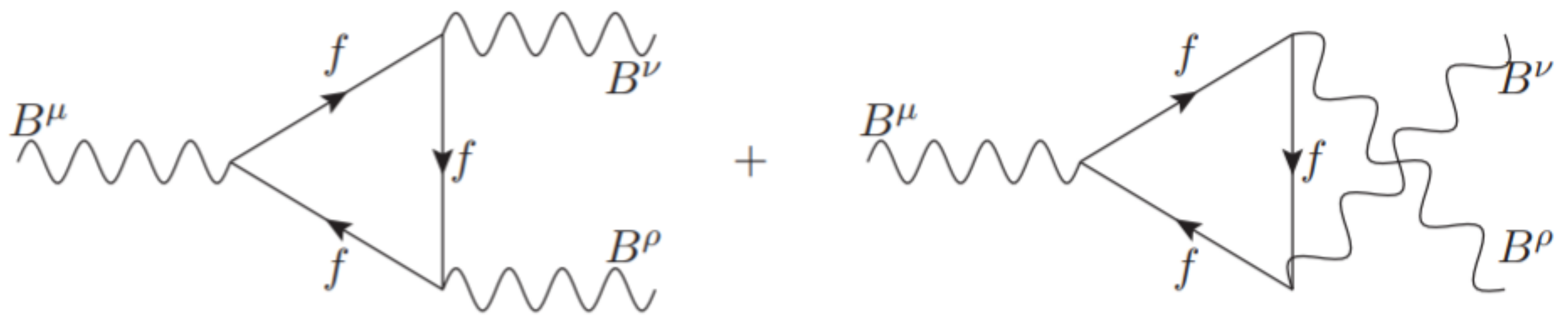
Mode	BR	Mode	BR	Mode	BR
$t\bar{t}$	0.42	$b\bar{b}$	0.12	$\nu\bar{\nu}'$	0.08
$\mu^+\mu^-$	0.08	$\tau^+\tau^-$	0.30	other $f_i f_j$	$\sim \mathcal{O}(10^{-4})$

LEP LFU

$$g_F^2 \left(\frac{M_Z}{M_{Z'}}\right)^2 \leq 0.004 \Rightarrow g_F \leq \frac{M_{Z'}}{1.3\text{ TeV}}.$$

It's worth LHCb, BELLE II chasing $BR(B \to K^{(*)}\tau^\pm\tau^\mp)$.

Quantum Field Theory Anomalies



$$A \equiv \sum_{LH\ \ f_i} Y_i^3 - \sum_{RH\ \ f_i} Y_i^3$$

Anomaly equations

4 linear ones, and

$$\sum_{i=1}^{3}(F_{Q_i}^2 - F_{L_i}^2 - 2F_{u_i}^2 + F_{d_i}^2 + F_{e_i}^2) = 0,$$

, ACC is the cubic

$$\sum_{i=1}^{3}(6F_{Q_i}^3 + 2F_{L_i}^3 - 3F_{u_i}^3 - 3F_{d_i}^3 - F_{e_i}^3 - F_{\nu_i}^3) = 0,$$

Look for solutions in rational numbers. Also, re-scaling invariance means that can re-scale to integers.

Solve case for 1 or 2 families of charges *analytically*, using old Diophantine methods. For 3 families, wrote a efficient computer program to search through $(2Q_{max}+1)^{18}$ sets of charges for SM and SM$+3\nu_R$, find all those that solve the anomaly equations.

Q	Q	Q	ν	ν	ν	e	e	e	u	u	u	L	L	L	d	d	d
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	-1	0	1	-1	0	1
0	0	0	0	0	0	-1	0	1	0	0	0	-1	0	1	0	0	0
0	0	0	0	0	0	-1	0	1	-1	0	1	0	0	0	-1	0	1
-1	0	1	0	0	0	0	0	0	0	0	0	-1	0	1	0	0	0
-1	0	1	0	0	0	0	0	0	-1	0	1	0	0	0	-1	0	1
-1	0	1	0	0	0	-1	0	1	-1	0	1	0	0	0	0	0	0
-1	0	1	0	0	0	-1	0	1	-1	0	1	-1	0	1	-1	0	1

eg: $Q_{max} = 1.$ Charges within a species are listed in *increasing order*.

$Q_{\max}$	**Solutions**	Symmetry	Quadratics	Cubics	Time/sec
1	**8**	8	32	8	0.0
2	**22**	14	1861	161	0.0
3	**82**	32	23288	1061	0.0
4	**251**	56	303949	7757	0.0
5	**626**	114	1966248	35430	0.0
6	**1983**	144	11470333	143171	0.2
7	**3902**	252	46471312	454767	0.6
8	**7068**	336	176496916	1311965	2.2
9	**14354**	492	539687692	3310802	6.7
10	**23800**	582	1580566538	7795283	20

SM solutions

An Anomaly-Free Atlas

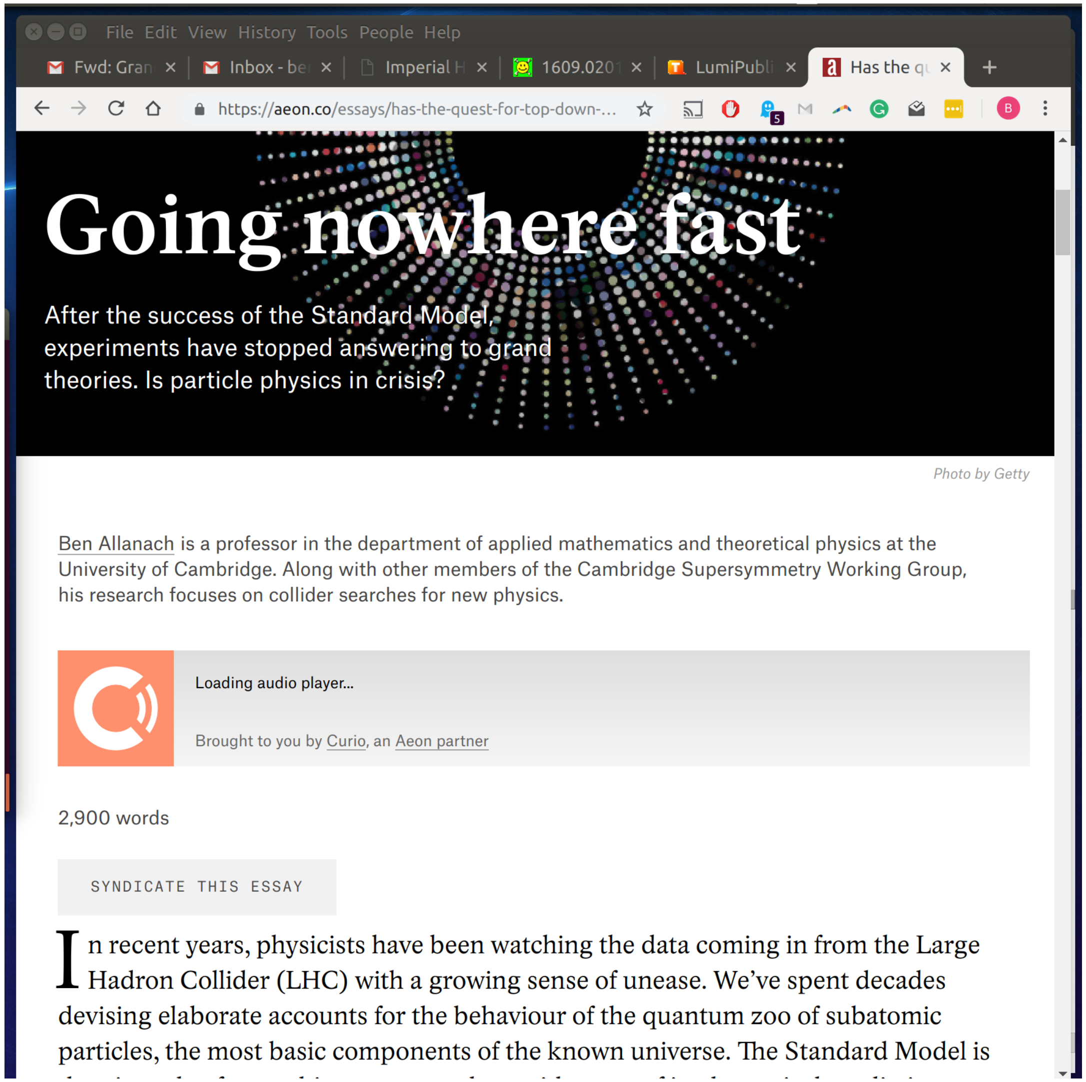
The atlas is available for public use:
`http://doi.org/10.5281/zenodo.1478085`

We did various checks (are solutions that were found in the literature before present, and are classes that have been banned not present?)

BCA, Davighi, Melville, `arXiv:1812.04602`

Conclusions

The answers to the questions raised by $R_{K^{(*)}}$ may provide a direct experimental probe into the flavour problem.



Going nowhere fast

After the success of the Standard Model, experiments have stopped answering to grand theories. Is particle physics in crisis?

Photo by Getty

Ben Allanach is a professor in the department of applied mathematics and theoretical physics at the University of Cambridge. Along with other members of the Cambridge Supersymmetry Working Group, his research focuses on collider searches for new physics.

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2,900 words

SYNDICATE THIS ESSAY

In recent years, physicists have been watching the data coming in from the Large Hadron Collider (LHC) with a growing sense of unease. We've spent decades devising elaborate accounts for the behaviour of the quantum zoo of subatomic particles, the most basic components of the known universe. The Standard Model is

Other conclusions

- The answers to the questions raise by $R_{K^{(*)}}$ may provide a direct experimental probe into the flavour problem.
- Focused on *tree-level* explanations of $R_{K^{(*)}}$ as they are usually harder to discover: Z' and leptoquarks.
- News on $R_K^{(*)}$ expected *in 2019*. At the current central value, Belle II can reach 5σ by mid 2021. LHCb's R_{K^*} would be close to[10] 5σ by 2020.
- $R_{K^{(*)}} \Rightarrow$ *HL-LHC, HE-LHC and FCC-hh*

[10] Albrecht *et al*, 1709.10308

Backup

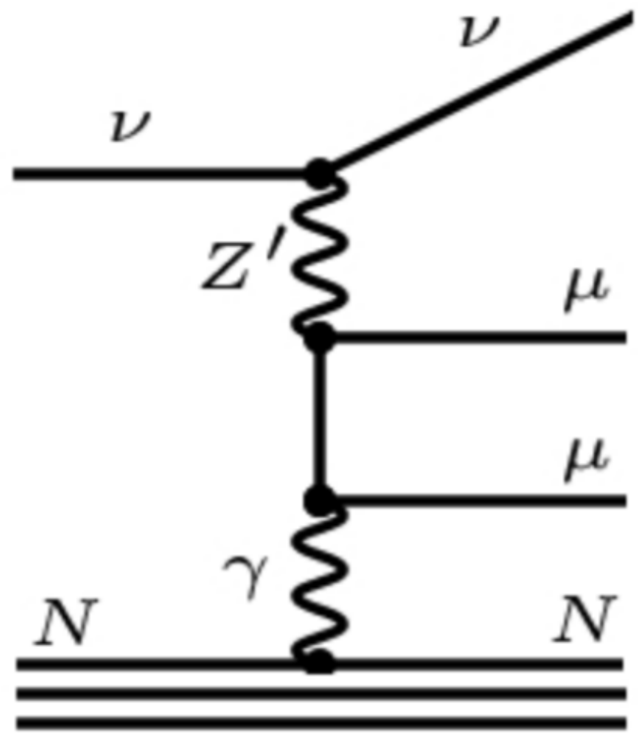
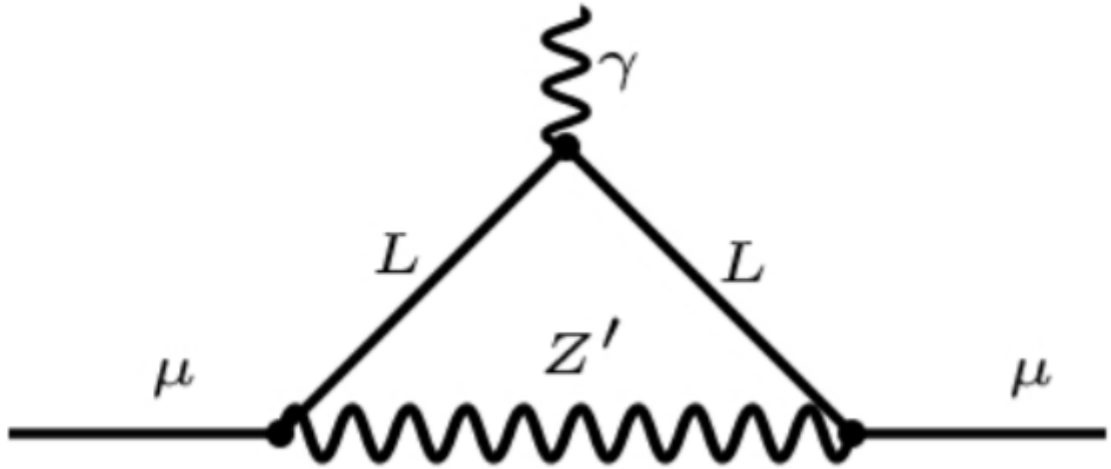
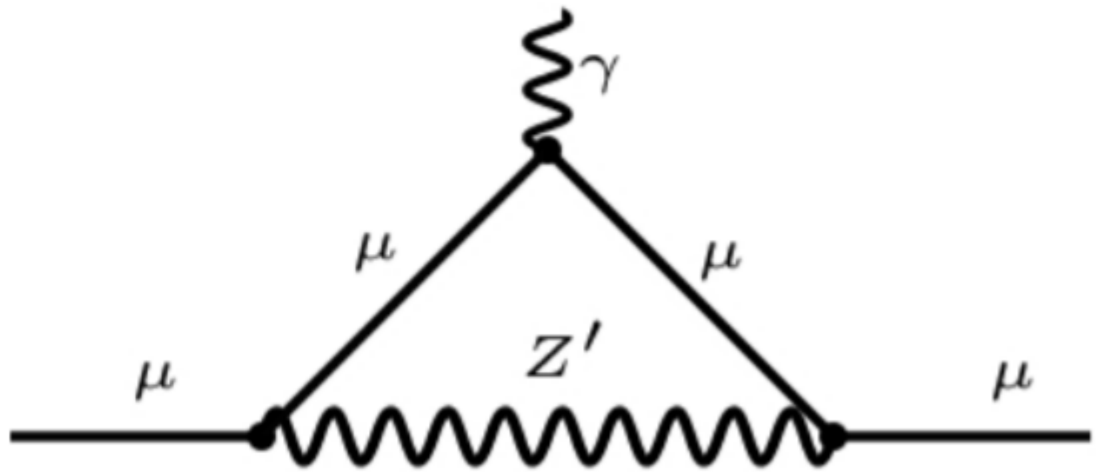


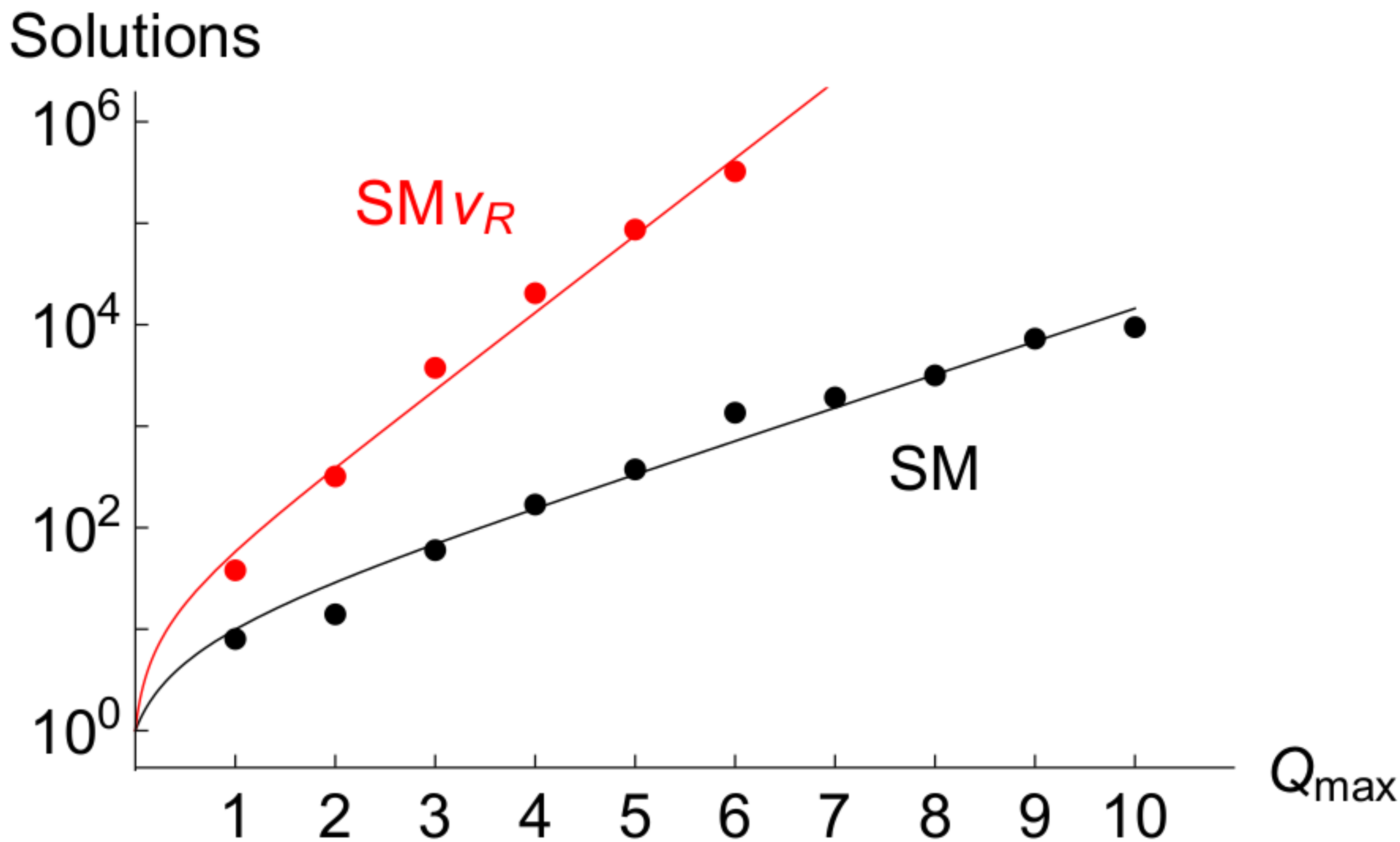
FIG. 10. Neutrino trident process that leads to constraints on the Z^{μ} coupling strength to neutrinos-muons, namely $M_{Z'}/g_{v\mu} \gtrsim 750$ GeV.


γ
L
L
Z′
μ
μ

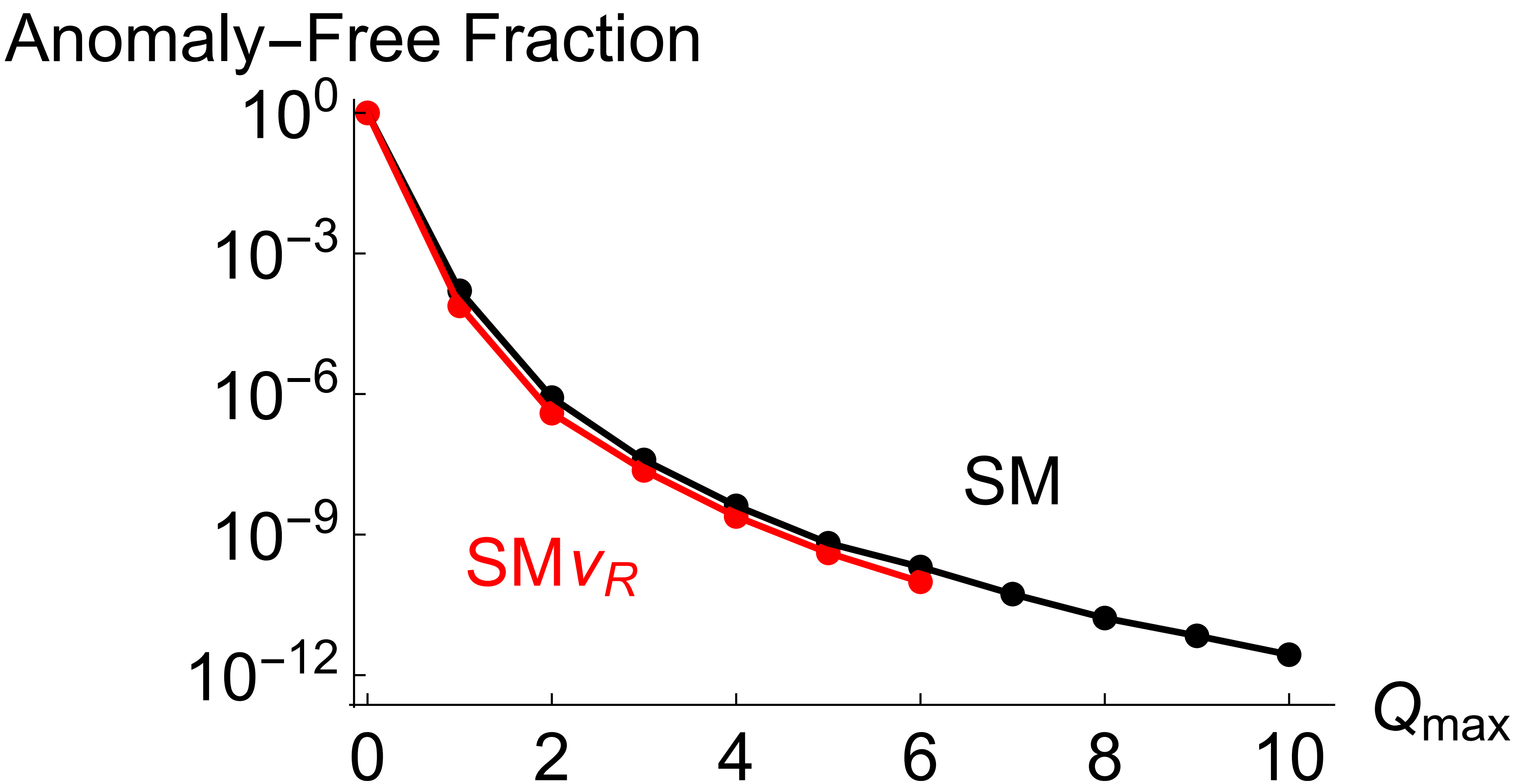

γ
μ
μ
Z′
μ
μ

$Q_{\max}$	**Solutions**	Symmetry	Quadratics	Cubics	Time/sec
1	**38**	16	144	38	0.0
2	**358**	48	31439	2829	0.0
3	**4116**	154	1571716	69421	0.1
4	**24552**	338	34761022	932736	0.6
5	**111152**	796	442549238	7993169	6.8
6	**435305**	1218	3813718154	49541883	56

SM $+$ 3 ν_R: number of solutions etc



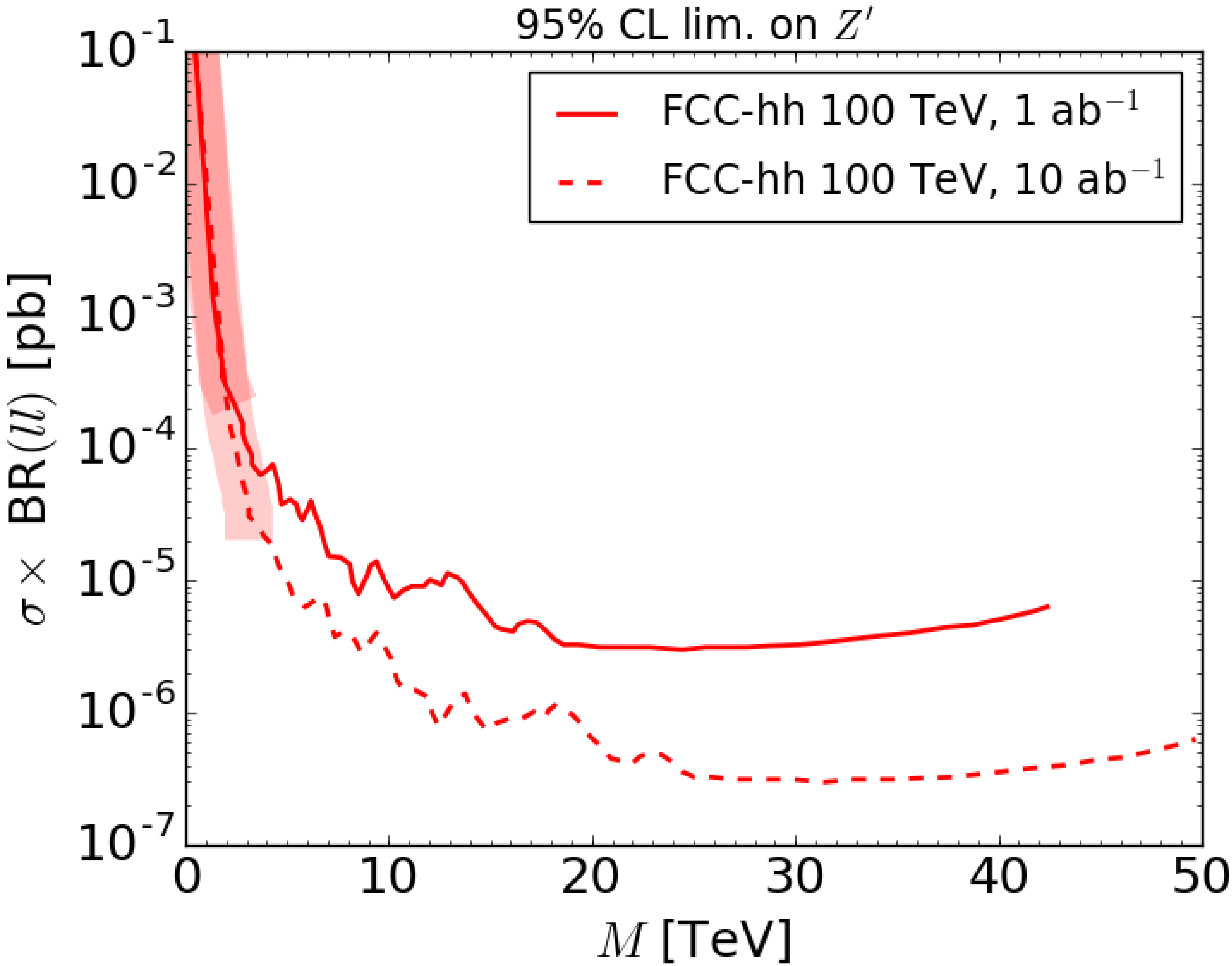
Solutions
10^6
10^4
10^2
10^0
SMν_R
SM
1
2
3
4
5
6
7
8
9
10
Q_max


Anomaly−Free Fraction
10^{0}
10^{-3}
10^{-6}
10^{-9}
10^{-12}
SM
SMν_R
0
2
4
6
8
10
Q_{max}

Known Solutions

Model	Q	Q	Q	ν	ν	ν	e	e	e	u	u	u	L	L	L	d	d	d
$L_\mu - L_\tau$	0	0	0	-1	0	1	-1	0	1	0	0	0	-1	0	1	0	0	0
TFHM	-1	0	0	0	0	0	0	0	6	-4	0	0	0	0	3	0	0	2
$B_3 - L_3$	-1	0	0	0	0	3	0	0	3	-1	0	0	0	0	3	-1	0	0

13 TeV ATLAS 3.2 fb^{-1} $\mu\mu$



Neutrino Masses

At dimension 5:

$$\mathcal{L}_{SS} = \frac{1}{2M}({L'_3}^T H^c)(L'_3 H^c),$$

but if we add RH neutrinos, then integrate them out

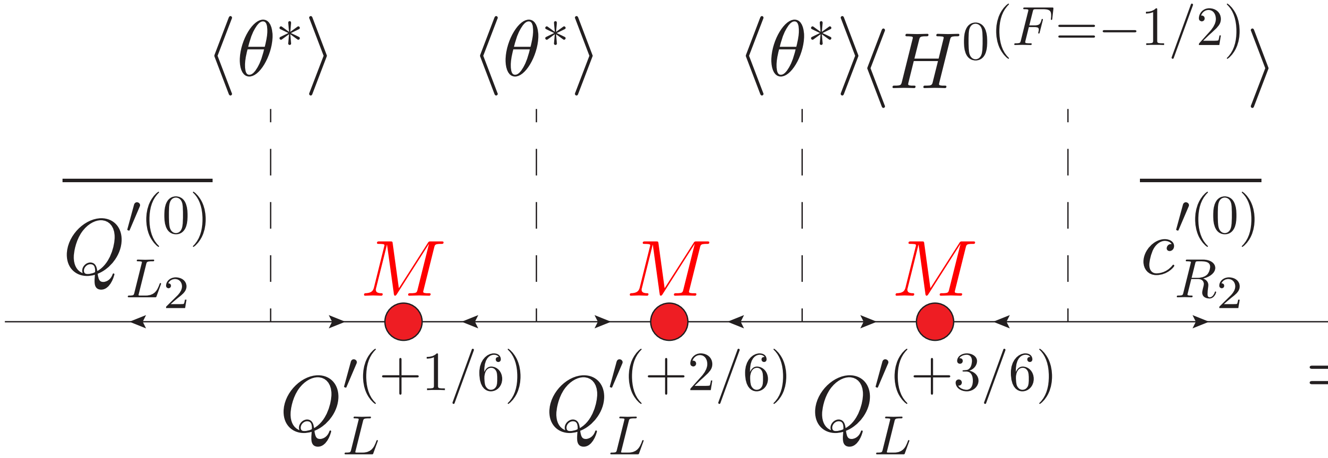
$$\mathcal{L}_{SS} = 1/2 \sum_{ij} (L'_i H^c)(M^{-1})_{ij}(L'_j H^c),$$

where now $(M^{-1})_{ij}$ may well have a non-trivial structure. If $(M^{-1})_{ij}$ are of same order, large PMNS mixing results.

Froggatt Neilsen Mechanism[11]

A means of generating the non-renormalisable Yukawa terms, e.g. $F_\theta = 1/6$:

$$Y_c \overline{Q'_{L2}}^{(F=0)} H^{(F=-1/2)} {c'_R}^{(F=0)} \sim \mathcal{O}\left[\left(\frac{\langle\theta\rangle}{M} \right)^3 \overline{Q'_{L2}} H c'_R \right]$$

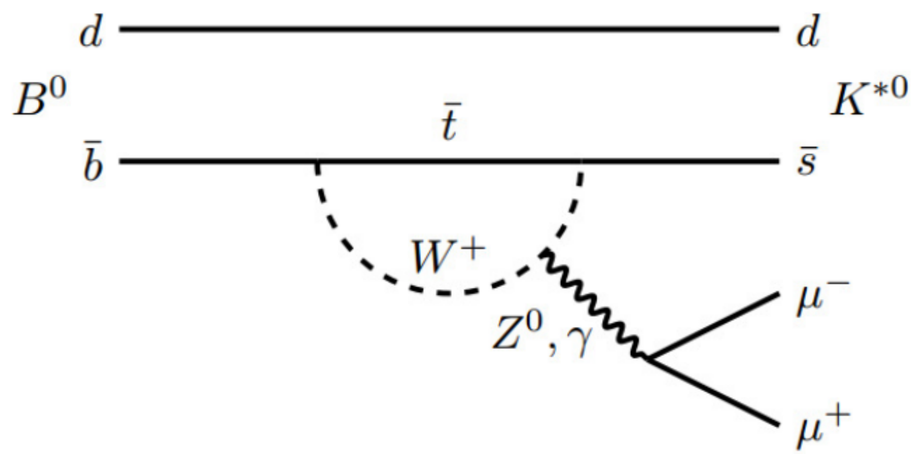


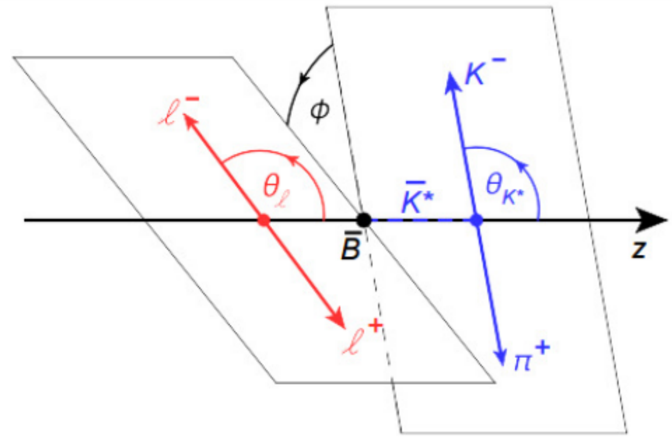
eg $\left(\frac{\langle\theta\rangle}{M} \right) \sim 0.2$

$\Rightarrow Y_c/Y_t \sim 1/100$

[11] C Froggatt and H Neilsen, NPB **147** (1979) 277

$B^0 \to K^{*0}(\to K^+\pi^-)\mu^+\mu^-$

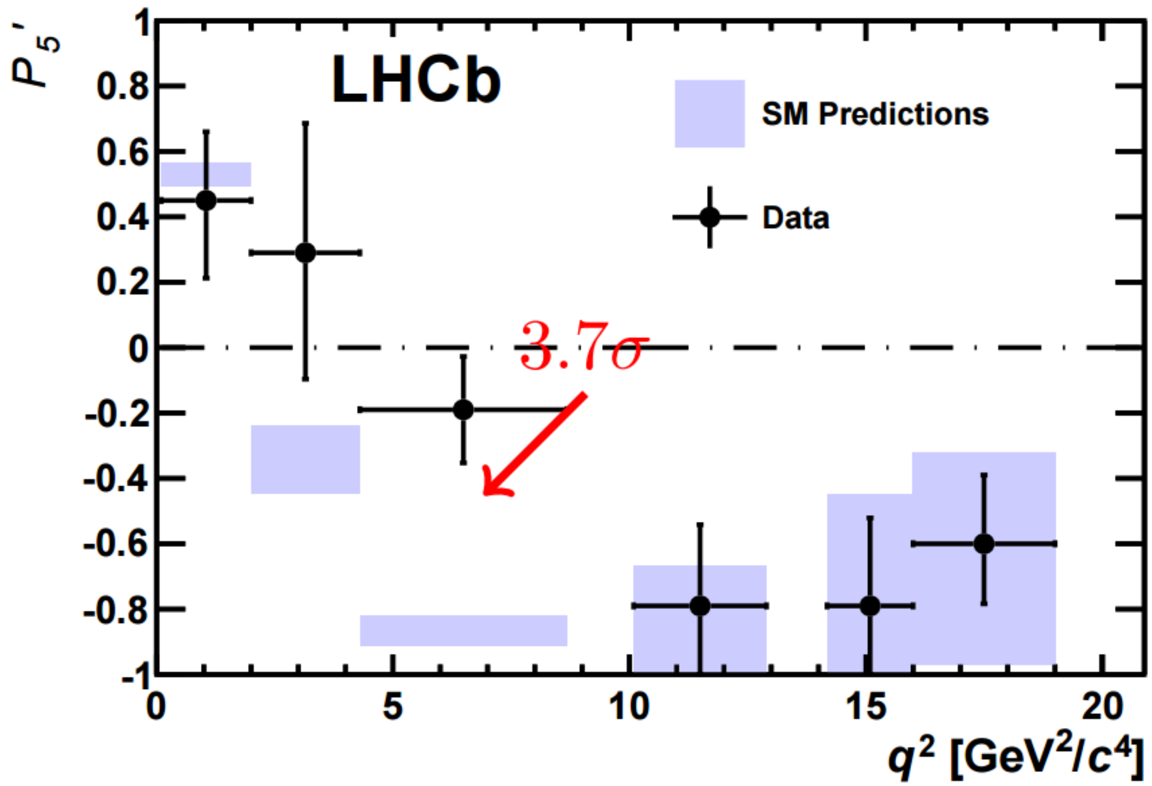




Decay fully described by three helicity angles $\vec{\Omega} = (\theta_\ell, \theta_K, \phi)$ and $q^2 = m^2_{\mu\mu}$

$$
\begin{aligned}
\frac{1}{\mathrm{d}(\Gamma+\bar{\Gamma})/\mathrm{d}q^2}\frac{\mathrm{d}^3(\Gamma+\bar{\Gamma})}{\mathrm{d}\vec{\Omega}} = \frac{9}{32\pi}\Big[&\tfrac{3}{4}(1-F_{\mathrm{L}})\sin^2\theta_K + F_{\mathrm{L}}\cos^2\theta_K + \tfrac{1}{4}(1-F_{\mathrm{L}})\sin^2\theta_K\cos 2\theta_\ell \\
&- F_{\mathrm{L}}\cos^2\theta_K\cos 2\theta_\ell + S_3\sin^2\theta_K\sin^2\theta_\ell\cos 2\phi \\
&+ S_4\sin 2\theta_K\sin 2\theta_\ell\cos\phi + S_5\sin 2\theta_K\sin\theta_\ell\cos\phi \\
&+ \tfrac{4}{3}A_{\mathrm{FB}}\sin^2\theta_K\cos\theta_\ell + S_7\sin 2\theta_K\sin\theta_\ell\sin\phi \\
&+ S_8\sin 2\theta_K\sin 2\theta_\ell\sin\phi + S_9\sin^2\theta_K\sin^2\theta_\ell\sin 2\phi\Big]
\end{aligned}
$$

P_5'

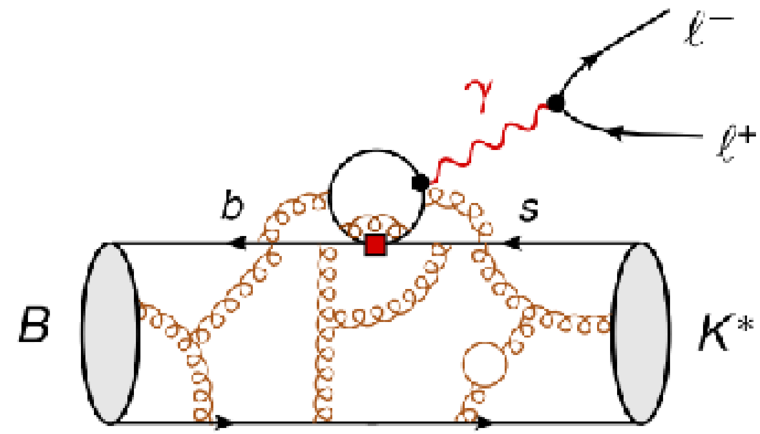


$P_5' = S_5/\sqrt{F_L(1-F_L)}$, leading form factor uncertainties cancel. Tension already in 1 fb^{-1} and confirmed in 3 fb^{-1}

LHCb-CONF-2015-002

Hadronic Uncertainties

- Hadronic effects like charm loop are photon-mediated $\Rightarrow$ vector-like coupling to leptons just like C_9



- How to disentangle NP $\leftrightarrow$ QCD?
  - Hadronic effect can have different q^2 dependence
  - Hadronic effect is lepton flavour universal ($\rightarrow R_K$!)

LQ Models

Scalar[12] $S_3 = (\bar{3},\ 3,\ 1/3)$ of $SU(2) \times SU(2)_L \times U(1)_Y$:

$$\mathcal{L} = \ldots + y_3 QLS_3 + y_q QQS_3^\dagger + \text{h.c.}$$

Vector $V_1 = (\bar{3}, 1, 2/3)$ or $V_3 = (3, 3, 2/3)$

$$\mathcal{L} = \ldots + y_3' V_3^\mu \bar{Q}\gamma_\mu L + y_1 V_1^\mu \bar{Q}\gamma_\mu L + y_1' V_1^\mu \bar{d}\gamma_\mu l + \text{h.c.}$$

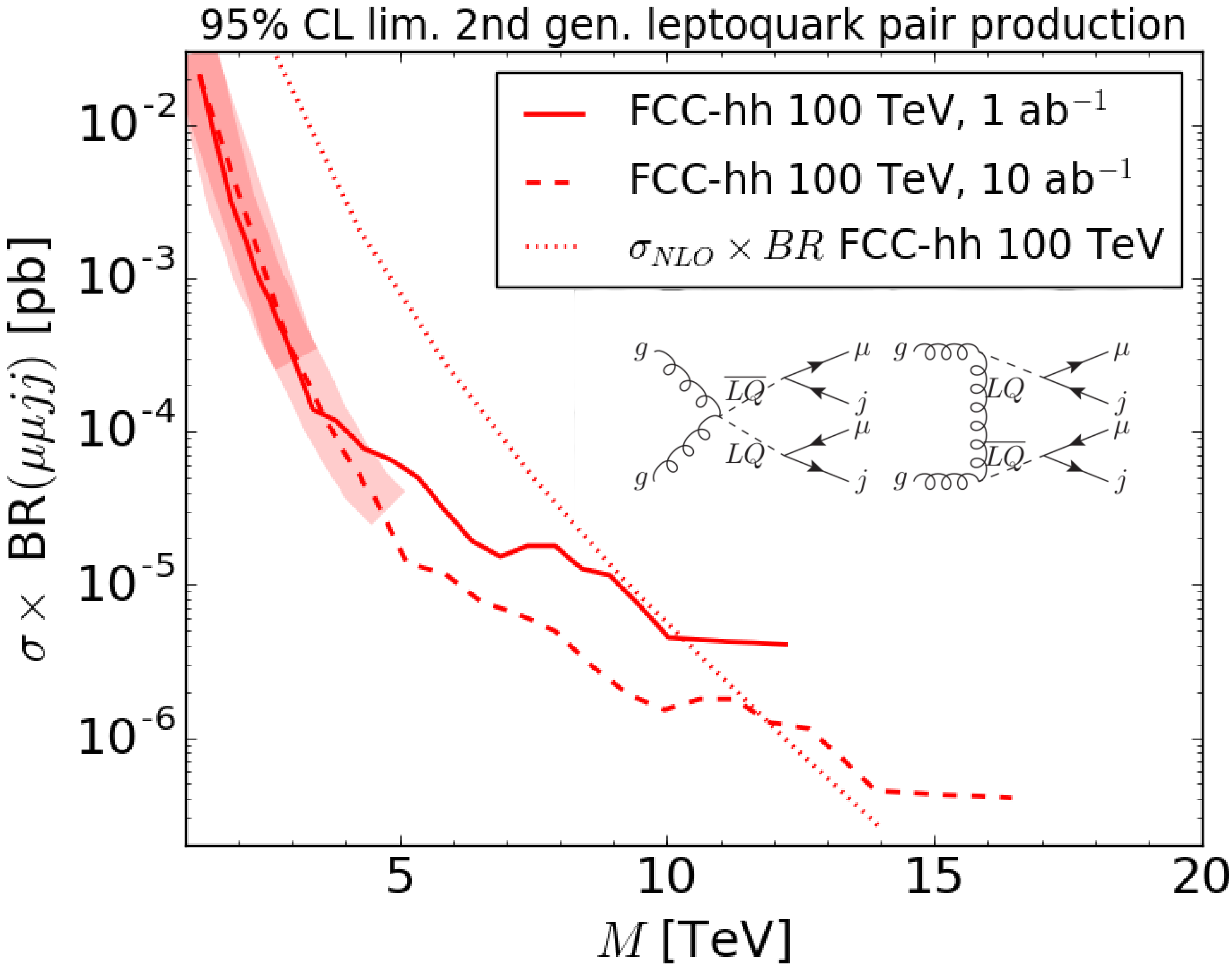
$$\Rightarrow \bar{c}_{LL}^\mu = \kappa \frac{4\pi v^2}{\alpha_{\text{EM}} V_{tb} V_{ts}^*} \frac{|y_i|^2}{M^2}.$$

$\kappa = 1, -1, -1$ and $y = y_3, y_1, y_3'$ for S_3, V_1, V_3.

[12] Capdevila *et al* 1704.05340, Hiller and Hisandzic 1704.05444, D'Amico *et al* 1704.05438.

CMS 8 TeV 20fb^{-1} 2nd gen

CMS-PAS-EXO-12-042: $M > 1.07$ TeV.



Other Constraints On LQs

Note that the extrapolation is very rough for pair production. Fix $M = 2M_{LQ}$, assuming they are produced close to threshold: $\Delta = 0.1$.

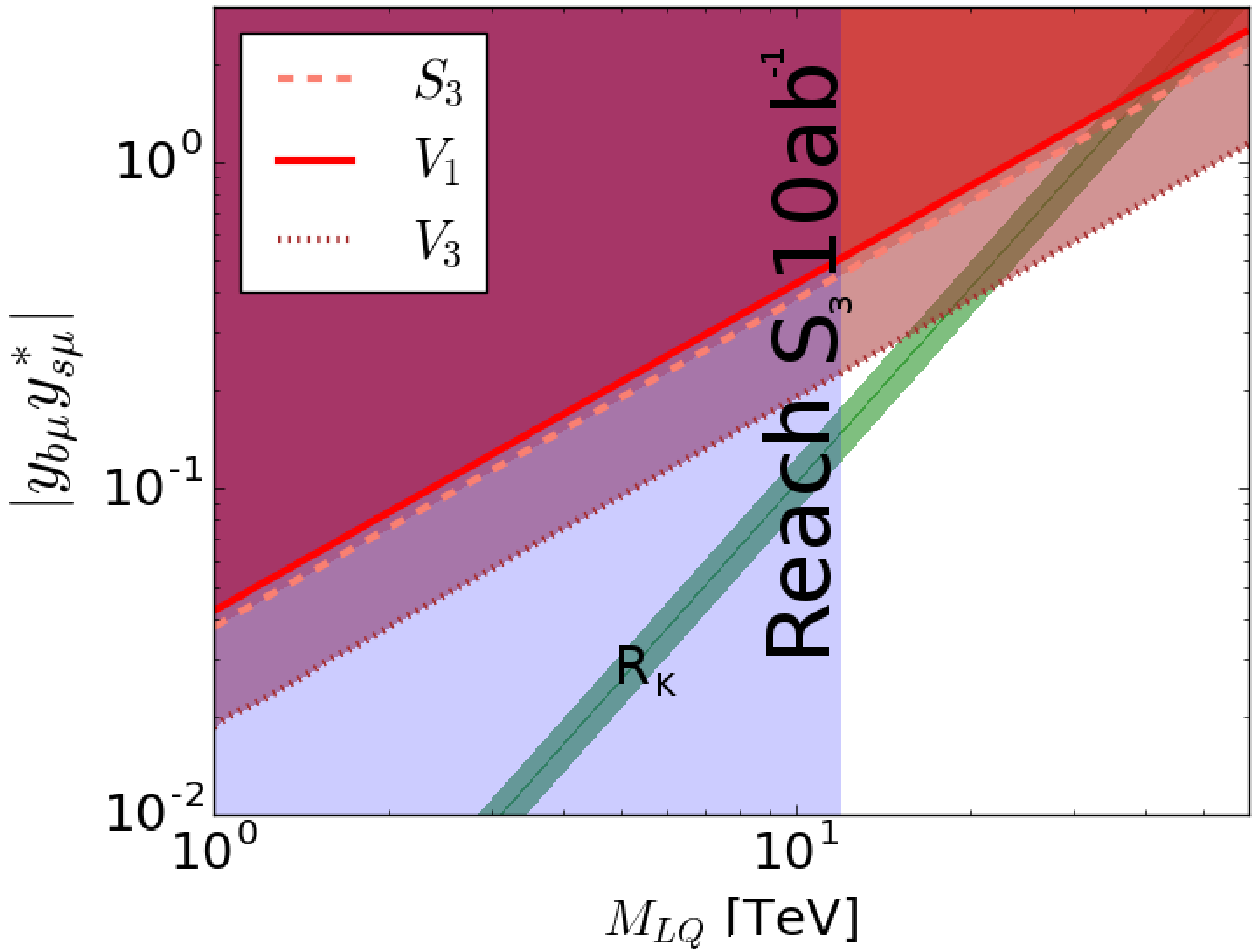
$B_s - \bar{B}_s$ mixing is at one-loop:

$$\mathcal{L}_{\bar{b}s\bar{b}s} = k\frac{|y_{b\mu}y^*_{s\mu}|^2}{32\pi^2 M_{LQ}^2}\left(\bar{b}\gamma_\mu P_L s\right)\left(\bar{s}\gamma^\mu P_L b\right) + \text{h.c.}$$

$y = y_3, y_1, y_3'$ and $k = 5, 4, 20$ for S_3, V_1, V_3.
Data $\Rightarrow c_{LL}^{bb} < 1/(210\text{TeV})^2$. Recently, some[13] used a Fermilab MILC lattice determination of f_B which makes the SM differ from experiment at the 2σ level.

[13] Lenz *et al*, 1712.06572

8 TeV CMS 20fb^{-1} 2nd gen



Up to 14 TeV LQs with 100 TeV 10 ab^{-1} FCC-hh. $M_{LQ} < 41$ TeV.

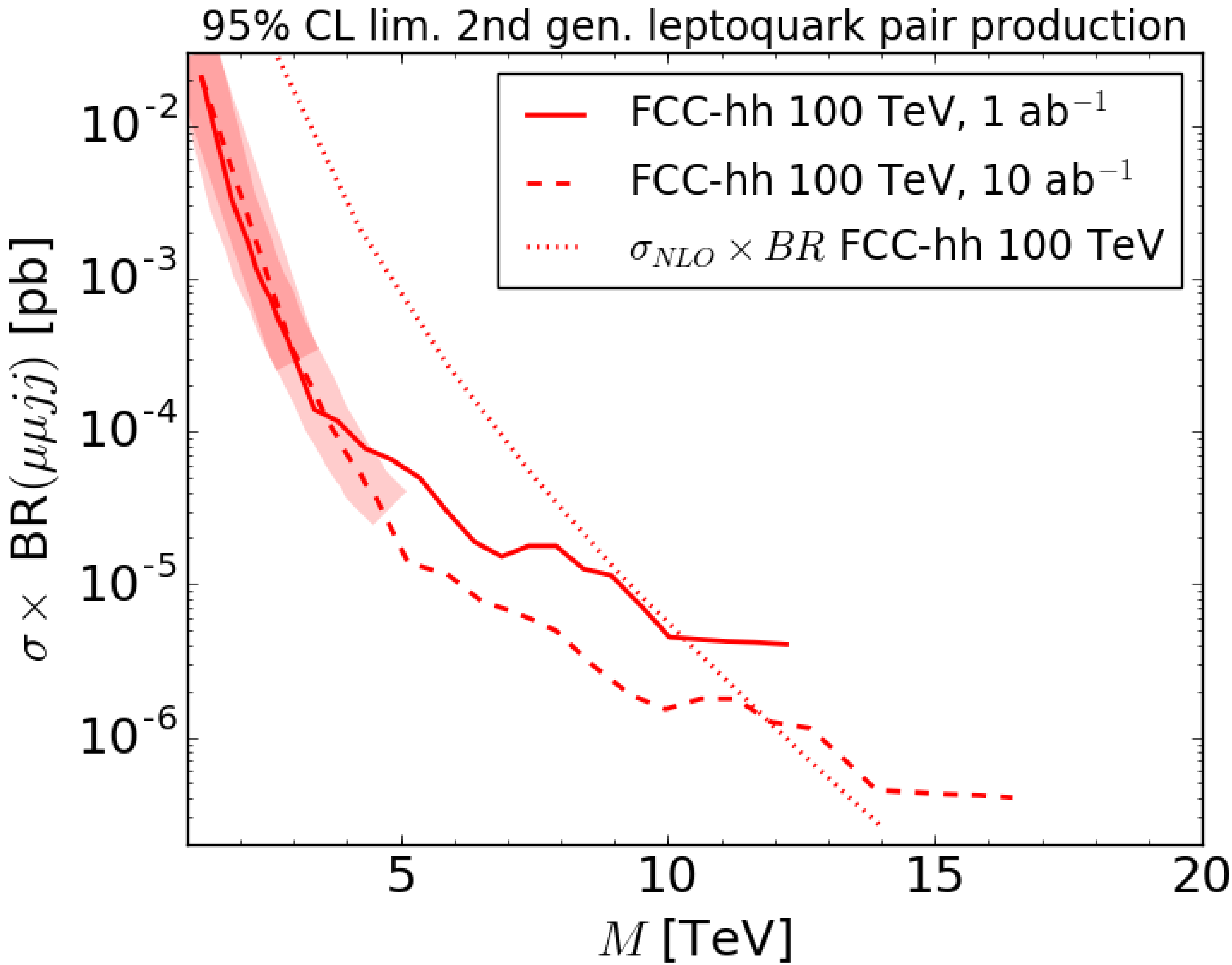
LQ Mass Limits

S_3	41 TeV
V_1	41 TeV
V_3	18 TeV

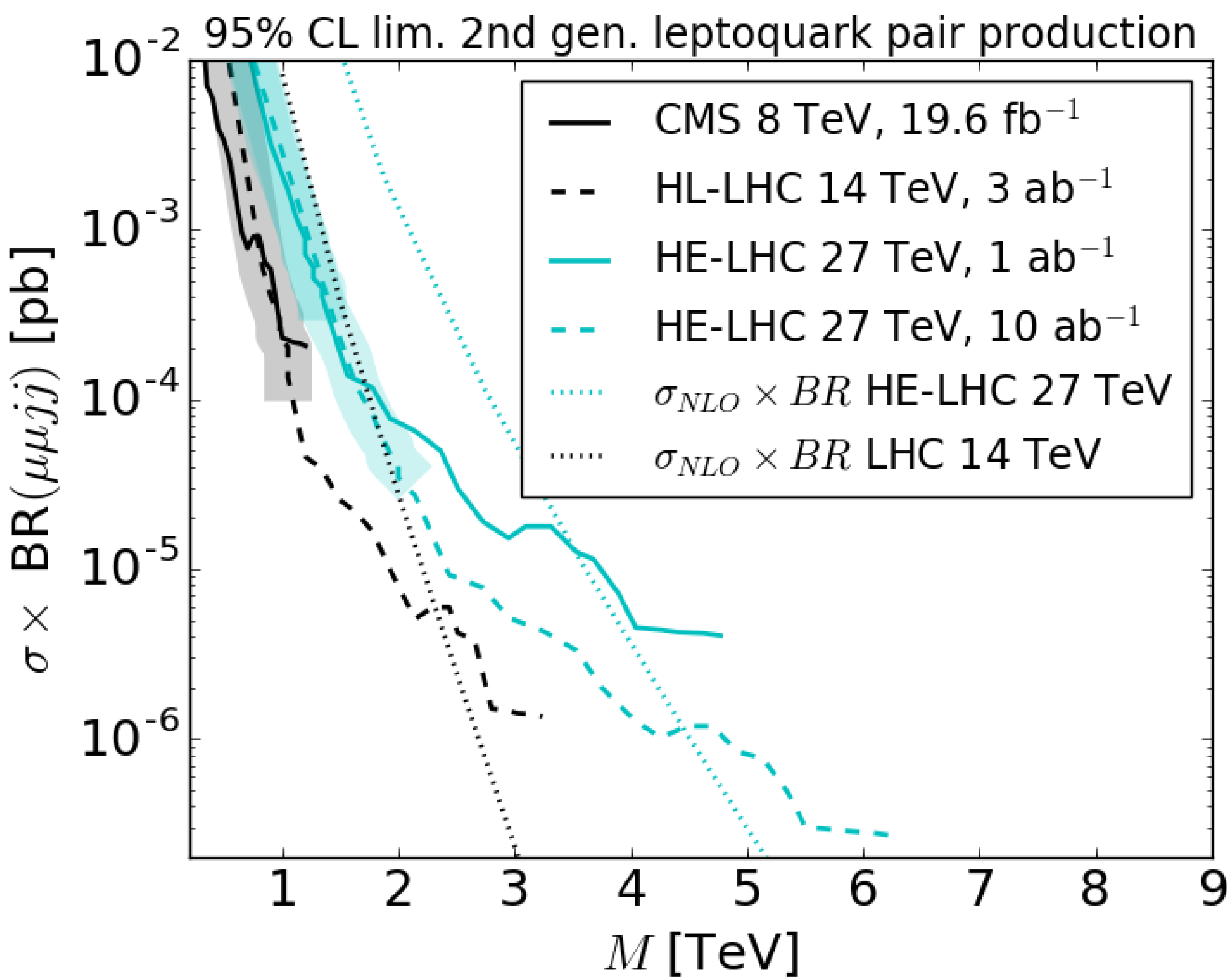
From $B_s - \bar{B}_s$ mixing and fitting $b-$anomalies.

Pair production has a reach up to 12 TeV.

The pair production cross-section is insensitive to the representation of $SU(2)$ in this case.


95% CL lim. 2nd gen. leptoquark pair production
FCC-hh 100 TeV, 1 ab^{-1}
FCC-hh 100 TeV, 10 ab^{-1}
$\sigma_{NLO} \times BR$ FCC-hh 100 TeV
$\sigma \times$ BR$(\mu\mu jj)$ [pb]
10^{-2}
10^{-3}
10^{-4}
10^{-5}
10^{-6}
5
10
15
20
M [TeV]

HL-LHC/HE-LHC LQs



$B_s \to \mu^+\mu^-$

Lattice QCD provides important input to

$$BR(B_s \to \mu\mu)_{SM} = (3.65 \pm 0.23) \times 10^{-9},$$

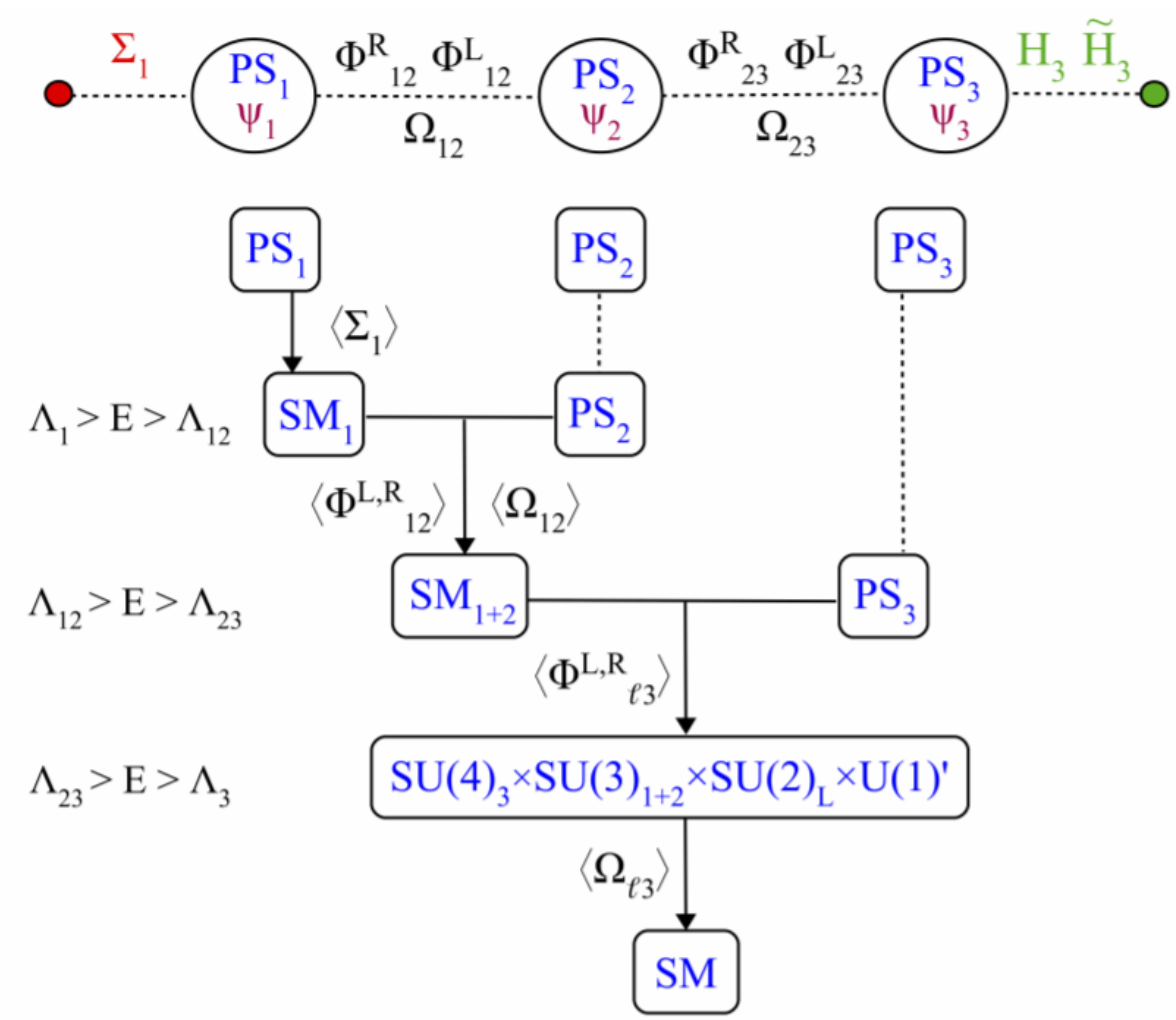
$$BR(B_s \to \mu\mu)_{exp}) = (3.0 \pm 0.6) \times 10^{-9}.$$

$$\frac{BR(B_s \to \mu\mu)}{BR(B_s \to \mu\mu)_{SM}} = \left| \frac{(\bar{c}^{\mu}_{LL} + \bar{c}^{\mu}_{RR} - \bar{c}^{\mu}_{LR} - \bar{c}^{\mu}_{RL})^{tot}}{(\bar{c}^{\mu}_{LL} + \bar{c}^{\mu}_{RR} - \bar{c}^{\mu}_{LR} - \bar{c}^{\mu}_{RL})^{SM}} \right|^2 .$$

Other Flavour Models

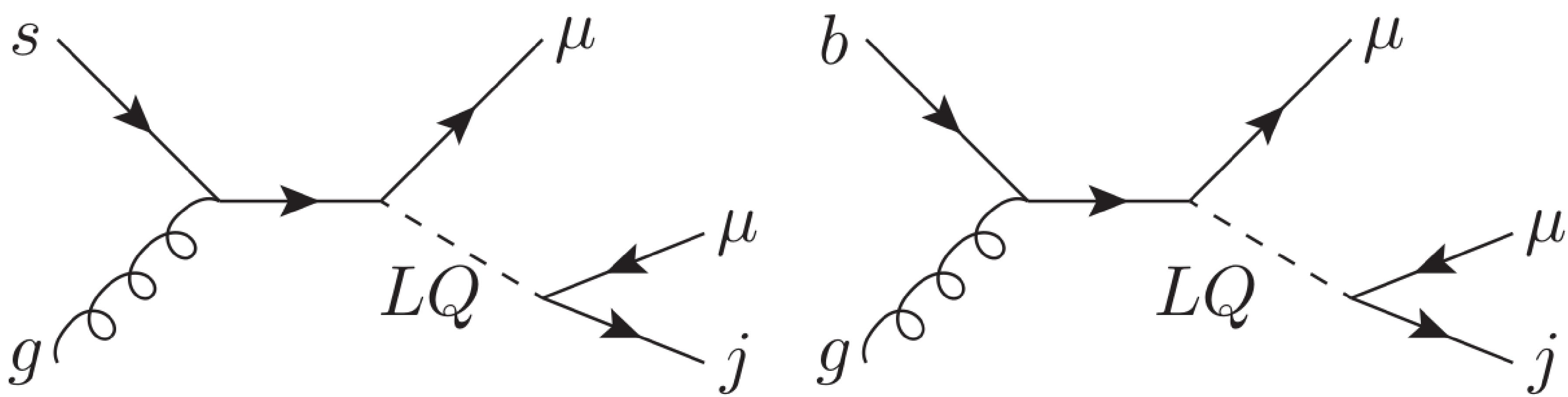
Realising[14] the vector LQ solution based on $PS = [SU(4) \times SU(2)_L \times SU(2)_R]^3$. SM-like Higgs lies in third generation PS group, explaining large Yukawas (others come from VEV hierarchies). Get $U(2)_Q \times U(2)_L$ approximate global flavour symmetry.

[14] Di Luzio Greljo, Nardecchia arXiv:1708.08450, Bordone, Cornella, Fuentes-Martin, Isidori, arXiv:1712.01368

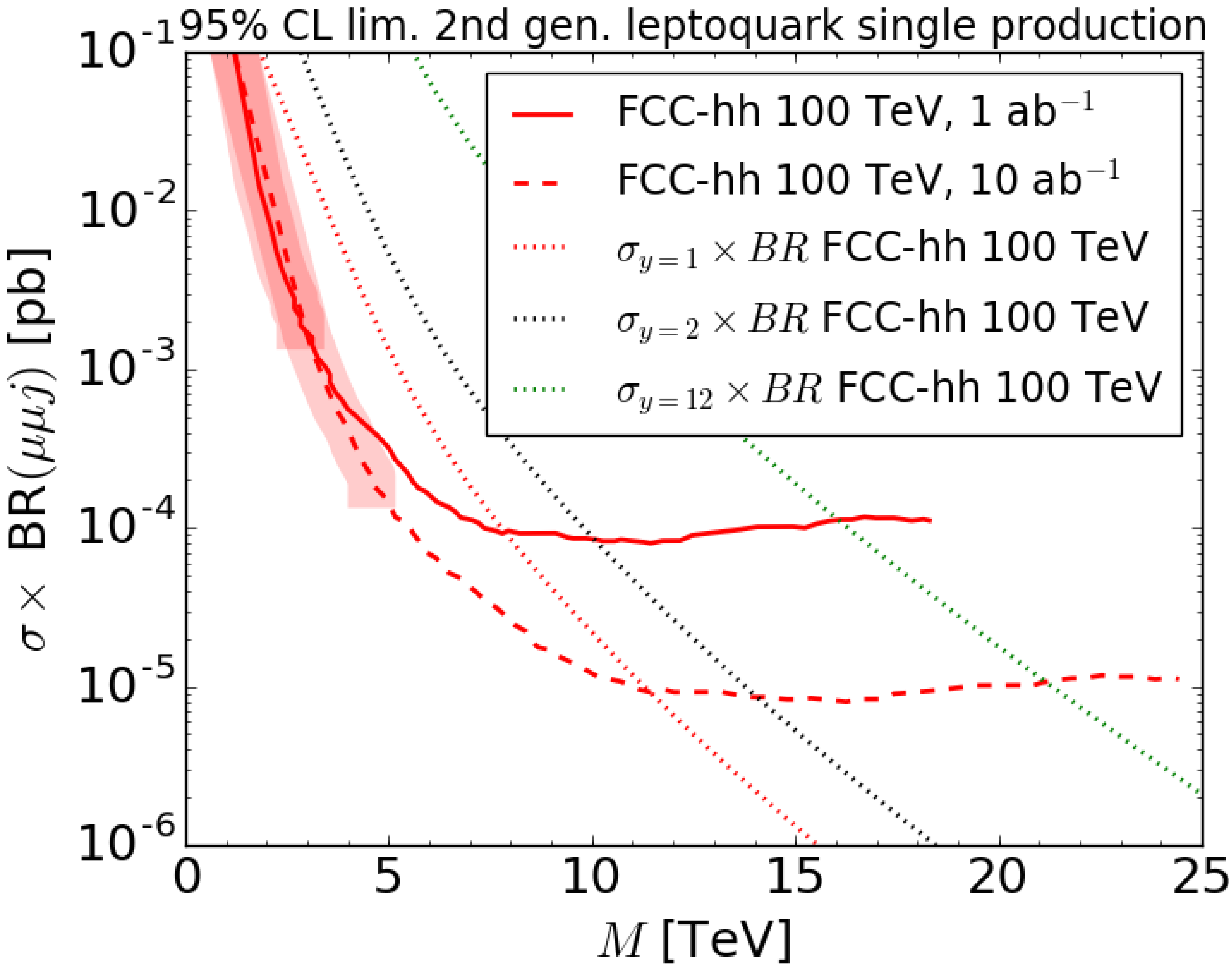

Σ_1
PS_1 ψ_1
$\Phi^R{}_{12}$ $\Phi^L{}_{12}$
Ω_{12}
PS_2 ψ_2
$\Phi^R{}_{23}$ $\Phi^L{}_{23}$
Ω_{23}
PS_3 ψ_3
H_3 $\widetilde{H}_3$
PS_1
PS_2
PS_3
$\langle \Sigma_1 \rangle$
$\Lambda_1 > E > \Lambda_{12}$
SM_1
PS_2
$\langle \Phi^{L,R}{}_{12} \rangle$ $\langle \Omega_{12} \rangle$
$\Lambda_{12} > E > \Lambda_{23}$
SM_{1+2}
PS_3
$\langle \Phi^{L,R}{}_{\ell 3} \rangle$
$\Lambda_{23} > E > \Lambda_3$
$SU(4)_3 \times SU(3)_{1+2} \times SU(2)_L \times U(1)'$
$\langle \Omega_{\ell 3} \rangle$
SM

Single Production of LQ

Depends upon LQ coupling as well as LQ mass



Current bound by CMS from 8 TeV 20 fb^{-1}: $M_{LQ} > 660$ GeV for $s\mu$ coupling of 1. We include b as well from `NNPDF2.3LO` ($\alpha_s(M_Z) = 0.119$), re-summing large logs from initial state b. Integrate $\hat{\sigma}$ with `LHAPDF`.



σs for S_3 with $y_{s\mu} = y_{b\mu} = y$.

Single LQ Production σ

$$\hat{\sigma}(qg \to \phi l) = \frac{y^2 \alpha_S}{96 \hat{s}} \left(1 + 6r - 7r^2 + 4r(r+1)\ln r\right) \ ,$$

where[15] $r = M_{LQ}^2/\hat{s}$ and we set $y_{s\mu} = y_{b\mu} = y$.

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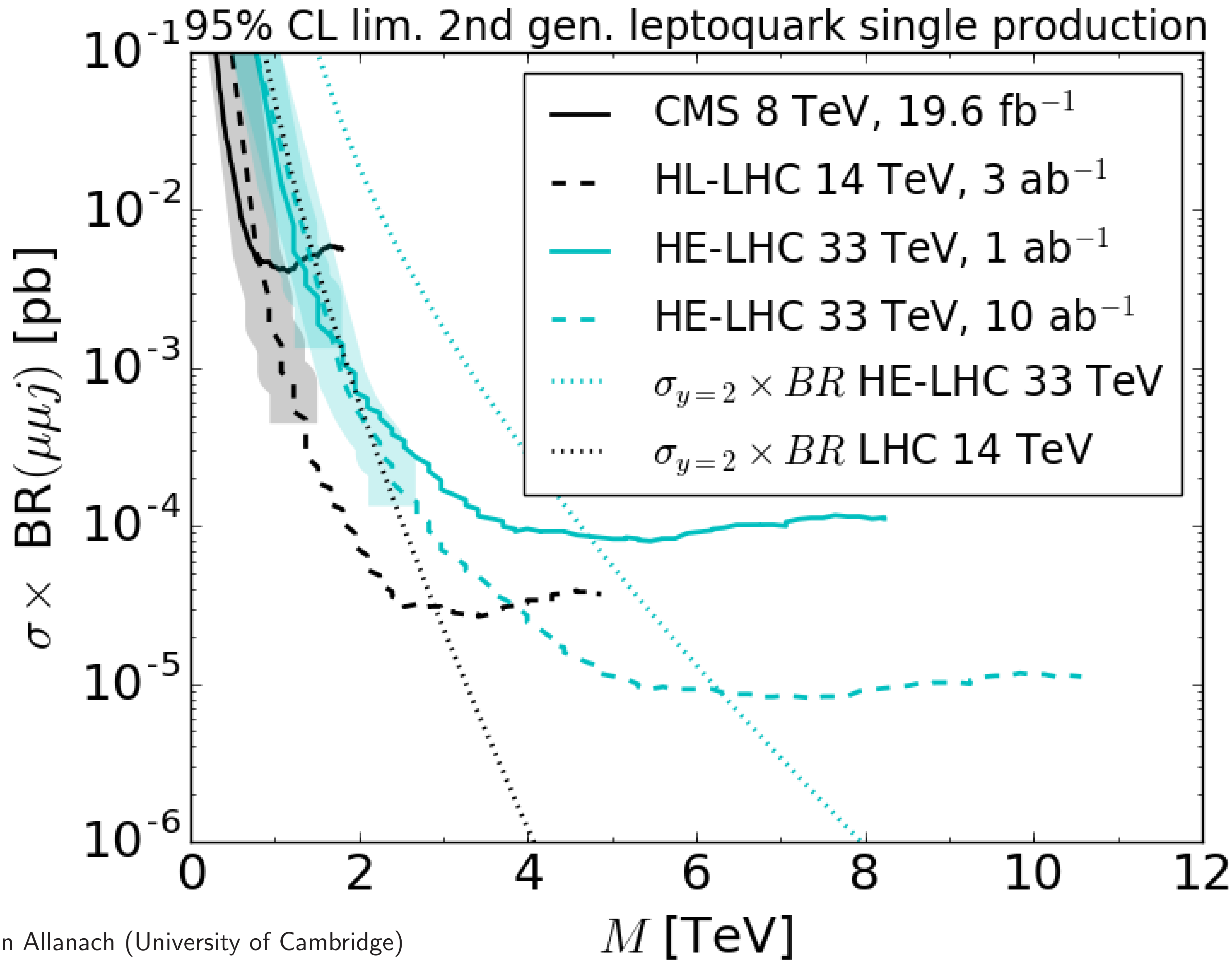
[15] Hewett and Pakvasa, PRD **57** (1988) 3165.

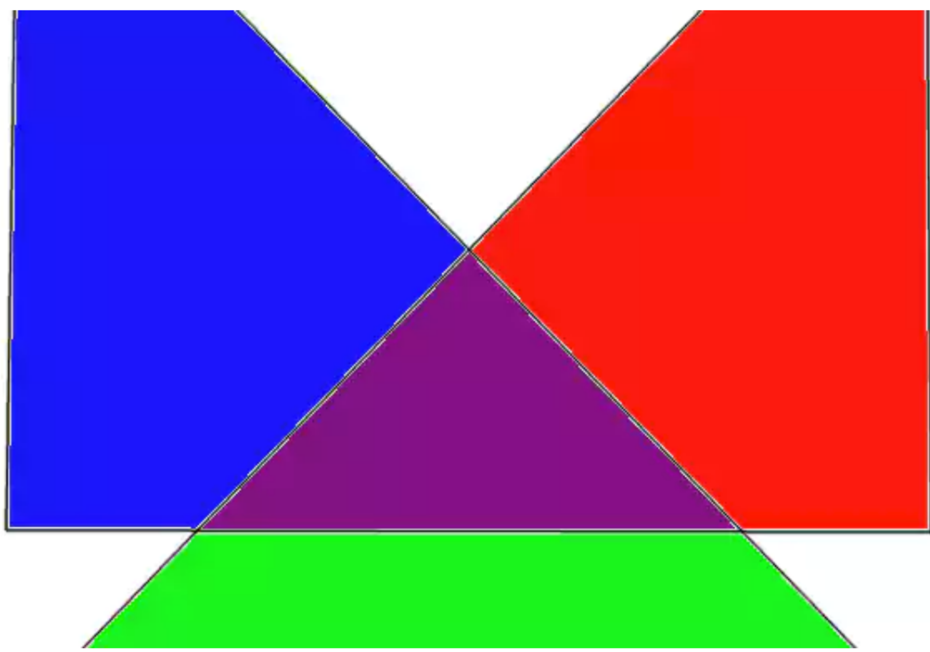


95% CL lim. 2nd gen. leptoquark single production
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
10^{-6}
$\sigma \times$ BR$(\mu\mu j)$ [pb]
CMS 8 TeV, 19.6 fb^{-1}
HL-LHC 14 TeV, 3 ab^{-1}
HE-LHC 33 TeV, 1 ab^{-1}
HE-LHC 33 TeV, 10 ab^{-1}
$\sigma_{y=2} \times BR$ HE-LHC 33 TeV
$\sigma_{y=2} \times BR$ LHC 14 TeV
0
2
4
6
8
10
12
M [TeV]

Science Life and Physics

Modelling the fourth colour: dispatch from de Moriond

At the particle physics conference, it's clear inconclusive LHCb data are stimulating strange new ideas

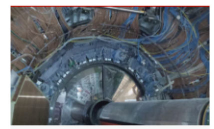


Four colours (or colors?) Photograph: Ben Allanach

Ben Allanach
Sat 17 Mar 2018 10.15 GMT

In the middle of the Rencontres de Moriond particle physics conference in Italy, the scientific talks stopped to allow a standing ovation dedicated to the memory and achievements of my inspirational colleague Stephen Hawking, who we heard had died earlier that day.

The talks quickly resumed, which I think Stephen would have approved of. The most striking thing about the scientific content of the conference this year was that a whole day was dedicated to the weirdness in bottom particles that Tevong You and I wrote about last November. As Marco Nardecchia reviewed in his talk (PDF), bottom particles produced in the LHCb detector in proton collisions are decaying too often in certain particular ways, compared to predictions from the Standard Model of particle physics. Their decay products are coming out with the wrong angles too often compared with predictions, too.



Anomalous bottoms at Cern and the case for a new collider
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We were hoping for an update on the data at the conference: the amount of data has roughly doubled since they were last released, and we need to see the new data to be convinced that something really new is happening in the collisions. I strongly suspect that if the effect is seen in the new data, the theoretical physics community will "go nuts" and we will quickly see the resulting avalanche of papers. If the new data look ordinary, the effect will be forgotten and everyone will move on. Taking such measurements correctly takes care and time, however, and the LHCb experiment didn't release them. We shall have to wait until other conferences later this year for the LHCb to present its analyses of the new data.

There were interesting theory talks on how new forces could explain the strange properties of the bottom particle decays. The full mathematical models look quite baroque: they need a lot of "bells and whistles" in order to pass other experimental tests. But these models prove that it can be done, and they are quite different to what has been proposed before.

One of them even unifies different classes of particle (leptons and quarks), describing the lepton as the "fourth colour" of a quark. We are used to the idea that quarks come in three (otherwise identical) copies: physicists label them red, green and blue to distinguish them. As Javier Fuentes-Martin describe (PDF), once you design the mathematics to make leptons the fourth colour, the existence of a new force-carrying particle with just the correct properties to break up the