

The proton radius puzzle – 9 years later

Jan C. Bernauer

FCCP, August 2019



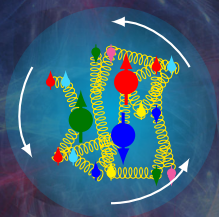
RBRC
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**Stony Brook
University**

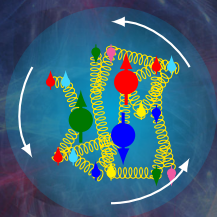
What is "stuff"?

The matter around us is described by non-perturbative quantum chromodynamics. npQCD is hard.
Simplest QCD system to study: Protons



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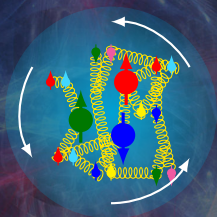
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Simplest QCD system to study: Protons



100 years of protons!

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The matter around us is described by non-perturbative quantum chromodynamics. npQCD is hard.
Simplest QCD system to study: Protons

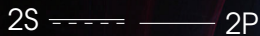
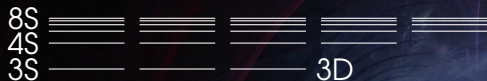


100 years of protons!

Proton is a composite system. It must have a size!

How big is it?

Motivation: "Normal" Hydrogen Spectroscopy

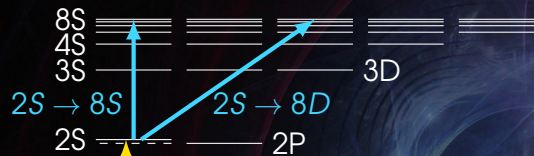


$$\gg E_{nS} \approx -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$

Energy level diagram for hydrogen showing the 1S level splitting into 1S and 1S states. The 1S level is split into two sub-levels: 1S (top) and 1S (bottom).

$$L_{1S} = 8171.626(4) + 1.5645 \langle r_p^2 \rangle \text{ MHz}$$

Motivation: "Normal" Hydrogen Spectroscopy



» $E_{nS} \approx -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$

» **Two transitions** for two unknowns:

» Rydberg constant R_∞

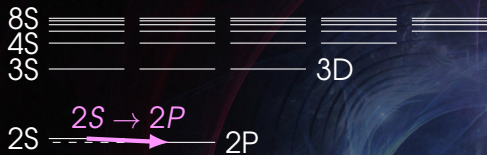
» 1S Lamb shift \Rightarrow radius

$1S \rightarrow 2S$

1S

$$L_{1S} = 8171.626(4) + 1.5645 \langle r_p^2 \rangle \text{ MHz}$$

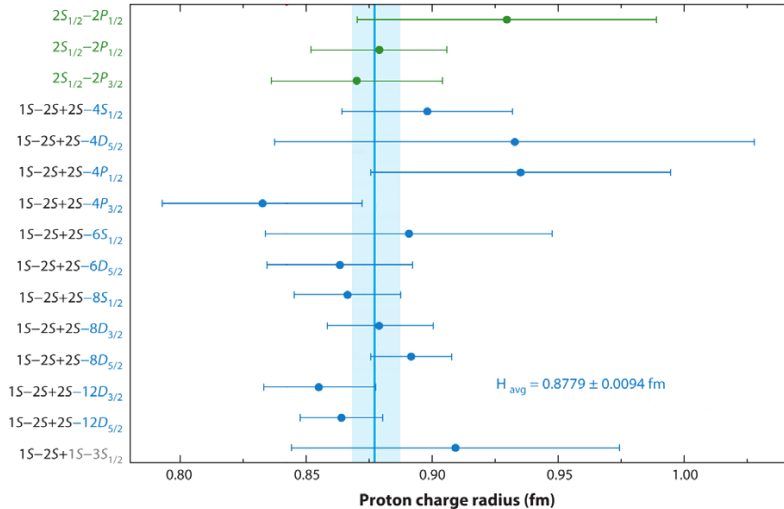
Motivation: "Normal" Hydrogen Spectroscopy



- » $E_{nS} \approx -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$
- » **Two transitions** for two unknowns:
 - » Rydberg constant R_∞
 - » 1S Lamb shift \Rightarrow radius
- » **Direct Lamb shift** $2S \rightarrow 2P$

1S ——— $L_{1S} = 8171.626(4) + 1.5645 \langle r_p^2 \rangle$ MHz

"Normal" Hydrogen Spectroscopy Results



Elastic lepton-proton scattering

Method of choice: Lepton-proton scattering

- » Point-like probe
- » No strong force
- » Lepton interaction "straight-forward"

Measure **cross sections** and reconstruct **form factors**.

Cross section for elastic scattering

$$\frac{\left(\frac{d\sigma}{d\Omega}\right)}{\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}}} = \frac{1}{\varepsilon(1+\tau)} \left[\varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2) \right]$$

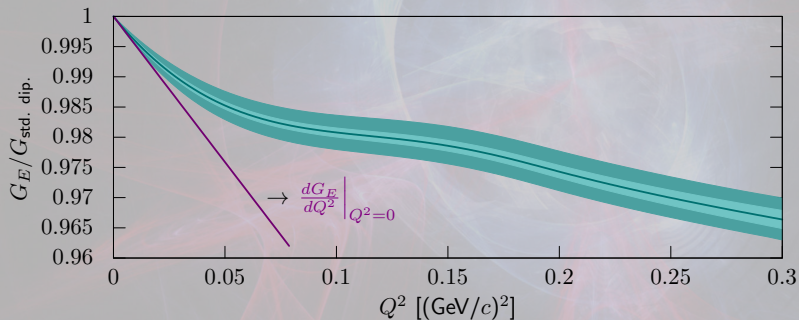
with:

$$\tau = \frac{Q^2}{4m_p^2}, \quad \varepsilon = \left(1 + 2(1+\tau) \tan^2 \frac{\theta_e}{2} \right)^{-1}$$

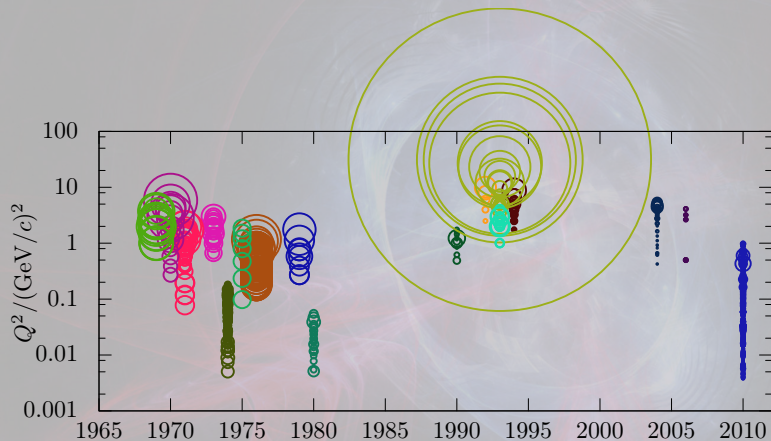
- » Rosenbluth formula
- » Electric and magnetic form factor encode the shape of the proton
- » Fourier transform (almost) gives the spatial distribution, in the Breit frame

How to measure the proton radius

$$\langle r_E^2 \rangle = -6\hbar^2 \left. \frac{dG_E}{dQ^2} \right|_{Q^2=0} \quad \langle r_M^2 \rangle = -6\hbar^2 \left. \frac{d(G_M/\mu_p)}{dQ^2} \right|_{Q^2=0}$$



History of unpolarized electron-proton scattering



- | | | | | |
|-------------|-------------|------------|---------|----------|
| ○ Andivahis | ○ Borkowski | ○ Janssens | ○ Rock | ○ Walker |
| ○ Bartel | ○ Bosted | ○ Litt | ○ Sill | |
| ○ Berger | ○ Christy | ○ Price | ○ Simon | |
| ○ Bernauer | ○ Goitein | ○ Qattan | ○ Stein | |

High-precision $p(e, e')$ measurement at MAMI



Imagery Date: 7/31/2013 50°00'20.12" N 8°19'50.19" E elev 352 ft eye alt 17.20 mi

High-precision $p(e,e')p$ measurement at MAMI

Mainz Microtron

- » cw electron beam
- » $10 \mu\text{A}$ polarized,
 $100 \mu\text{A}$ unpolarized
- » MAMI A+B: 180-855 MeV
- » MAMI C: 1.6 GeV

Johannes Gutenberg University of Mainz

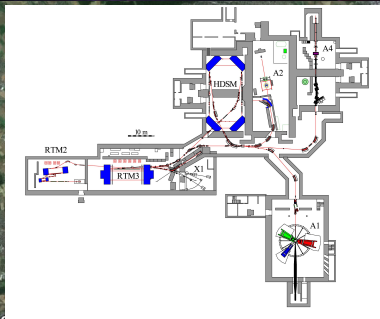


Image © 2015 GeoBasis
Image © 2015 Digital
Image © 2015 Aero

3.97 mi

Imagery Date: 7/31/2013 50°00'20.12" N 8°19'50.19" E elev 352 ft eye alt 17.20 mi

High-precision $p(e,e')p$ measurement at MAMI

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Johannes Gutenberg Uni

A1 3-spectrometer facility

- » 28 msr acceptance
- » angle resolution: 3 mrad
- » momentum res.: 10^{-4}



Image © 2015 GeoBasis - DE/BKG

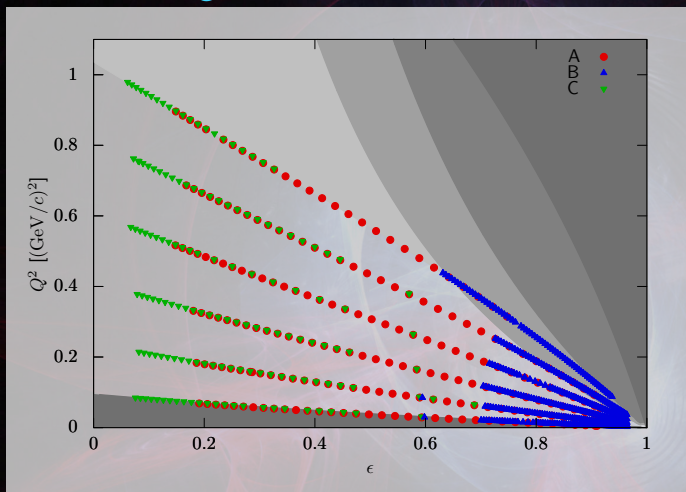
Image © 2015 DigitalGlobe

Image © 2015 AeroWest

Google earth

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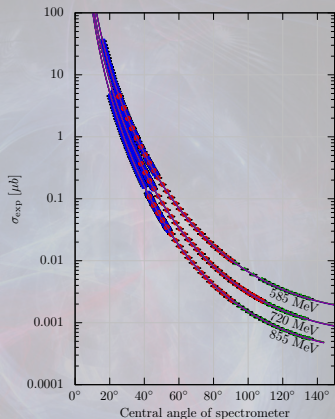
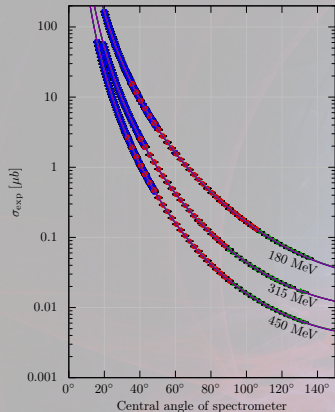
Measured settings



1422 settings

JCB et al., Phys. Rev. Lett. 105 (2010) 242001,
M. O. Distler, JCB, Th. Walcher, Phys. Lett. B 696, 343 (2011)
JCB et al., Phys. Rev. C90 (2014) 015206

Cross sections



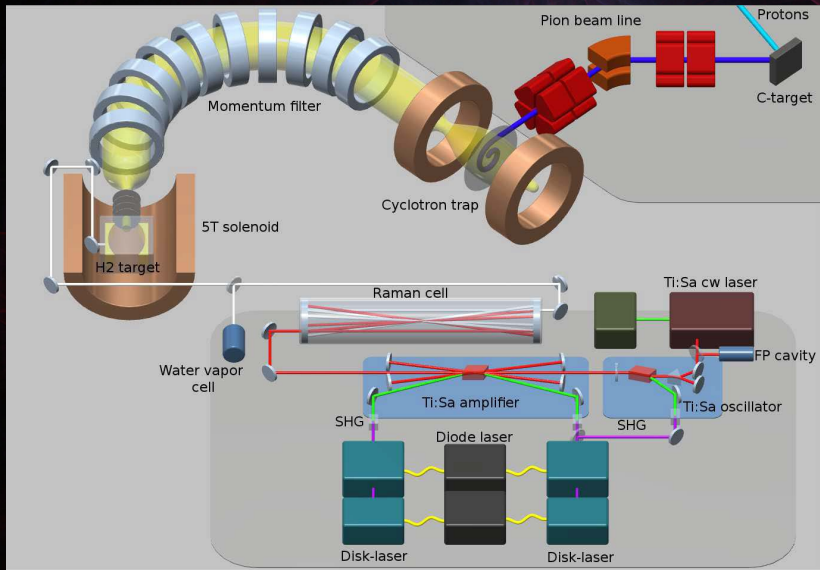
Polynomial	—	Inv. poly.	—	Friedrich-Walcher	—
Poly. + dip	—	Spline	—	Double dipole	—
Poly. \times dip	—	Spline \times dip	—	Extended G.K.	—

Muonic Hydrogen Spectroscopy

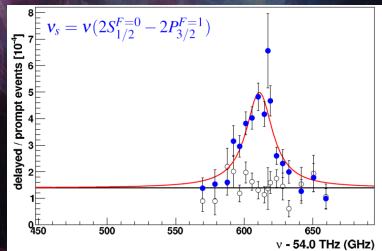
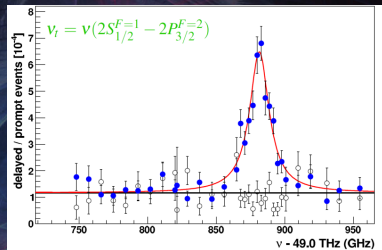
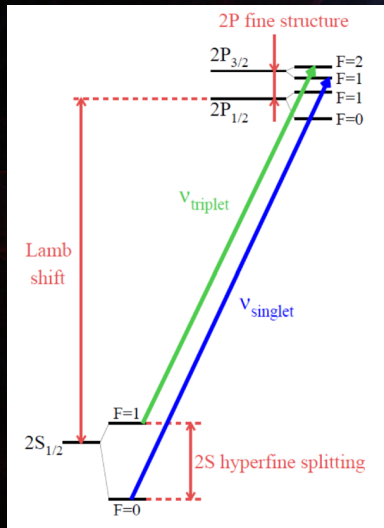


- » Replace **electron** with **muon**
- » 200 times heavier \implies 200 times smaller orbit
- » Probability to be “inside” 200^3 higher!

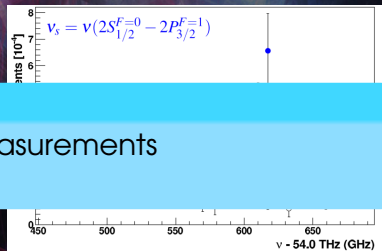
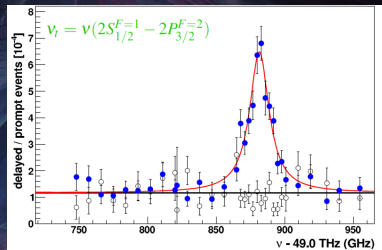
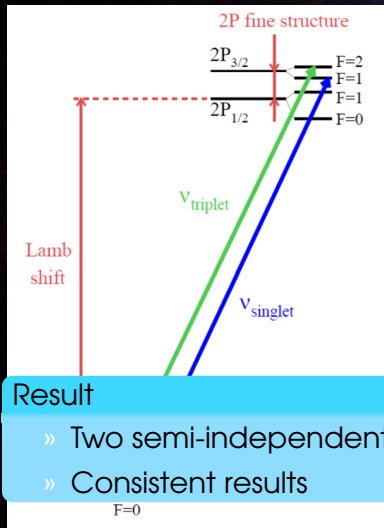
PSI setup (CREMA)



Muonic Hydrogen Spectroscopy Results



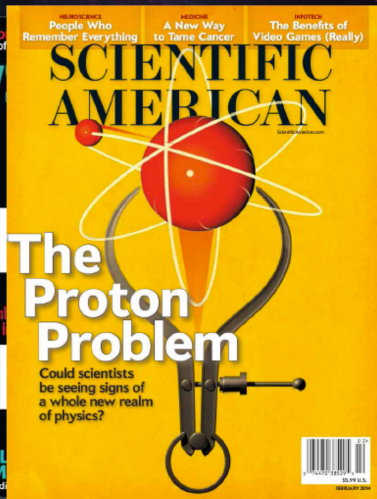
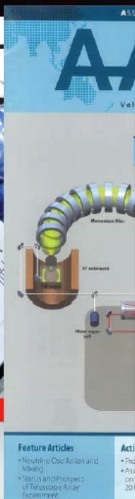
Muonic Hydrogen Spectroscopy Results



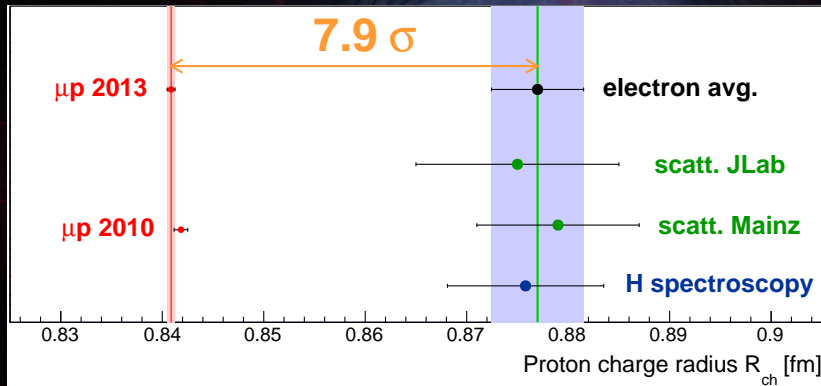
Result

- » Two semi-independent measurements
- » Consistent results

The Proton Radius puzzle



The Proton Radius puzzle



Theory / Fitting

- » Many people have checked spectroscopy theory
 - » generally seems robust, but few papers pop up with criticism
- » We are sure we are measuring the same thing: G. Miller, Phys. Rev. C 99, 035202
- » For scattering, radiative corrections might be problematic
- » Fitting: Many people fit data and get different results.

Theory / Fitting

- » Many people have checked spectroscopy theory
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- » For scattering, radiative corrections might be problematic
- » Fitting: Many people fit data and get different results.
- » **BSM physics?** Still alive and kicking, E.g.: Liu, Cloet, Miller Nucl. Phys. B 944 114638 (also explains $g_{\mu} - 2$)

The face puzzle that launched a thousand ships experiments



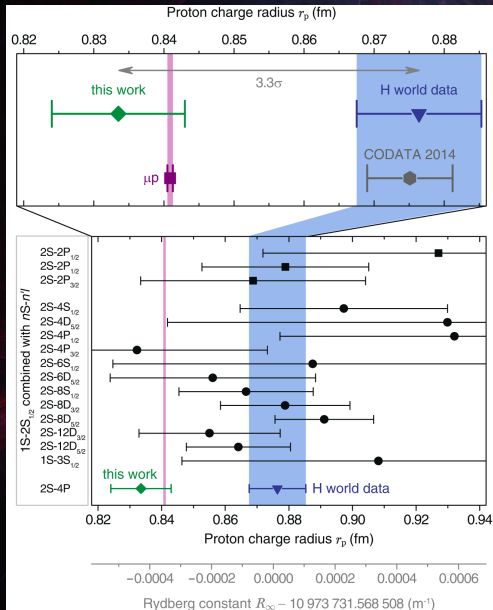
Spectroscopy:

- » MPQ
- » York University
- » Paris
- » + measurements on d , ^3He , ^4He , ...

Scattering:

- » PRad (Jefferson Lab)
- » Mainz: ISR, H-TPC, Next-gen FF
- » Muon Hydrogen-TPC, CERN
- » PRAE Paris
- » ELPH Japan
- » MUSE

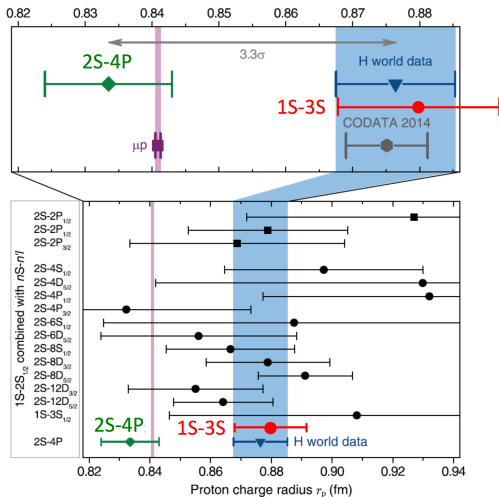
New hydrogen results: MPQ (A. Beyer et al., Science 358, 79 (2017))



New results: Paris (Fleurbaey et al., Phys. Rev. Lett. 120, 183001 (2018))



Overview



More spectroscopy

There are more spectroscopy results coming.

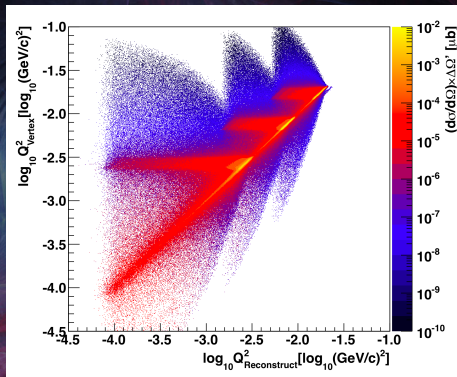
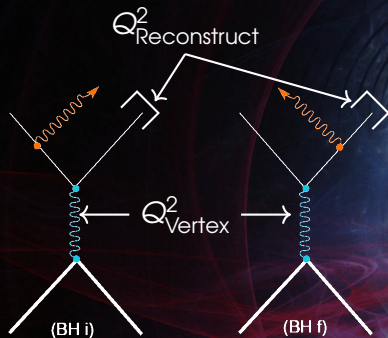
- » AFAIK, all give something in agreement with small radius!

More spectroscopy

There are more spectroscopy results coming.

- » AFAIK, all give something in agreement with small radius!
- » Some ready to declare victory.
- » I think it's too early. We should at least understand what has gone wrong in Paris!

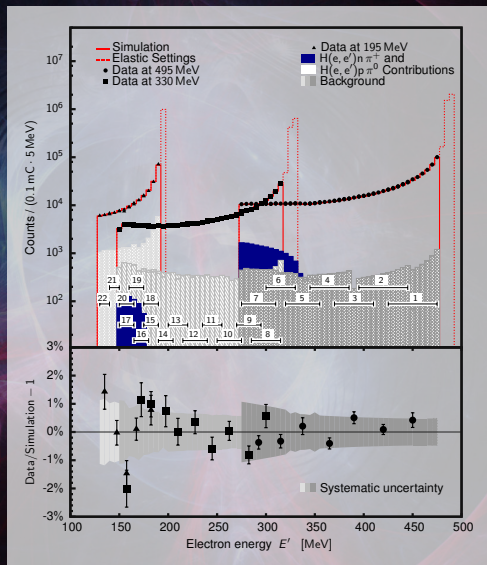
ISR method



- » Use initial state radiation to reduce effective beam energy
- » Have to subtract FSR

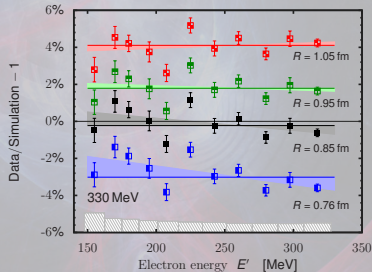
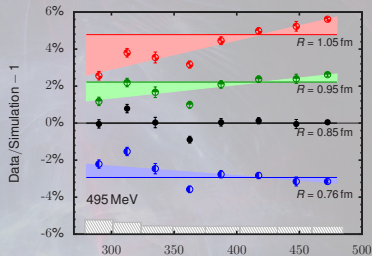
ISR at MAMI

- » Published: PLB 771:194-198
- » Radiative correction correct on the 1% level deep in the tail!
- » Radius extraction not competitive in precision
- » In principle: Larger scattering angle for G_M



Updated analysis of ISR

- » arXiv:1905.11182
- » Focuses on cs instead of FF
- » $r_p = 0.870 \pm 0.014_{stat} \pm 0.024_{sys} \pm 0.003_{mod} \text{ fm}$
- » Slightly prefers large radius



Slides provided by E. Pasyuk, presented at MENU
2019

PRAD slides removed on request of PRAD collaboration.

The missing piece

r_E (fm)	ep	μp
Spectroscopy	0.8758 ± 0.077	0.84087 ± 0.00039
Scattering	0.8770 ± 0.060 or not?	????

Measure radius with muon-proton scattering!

MUSE - Muon Scattering Experiment at PSI

PAUL SCHERRER INSTITUT

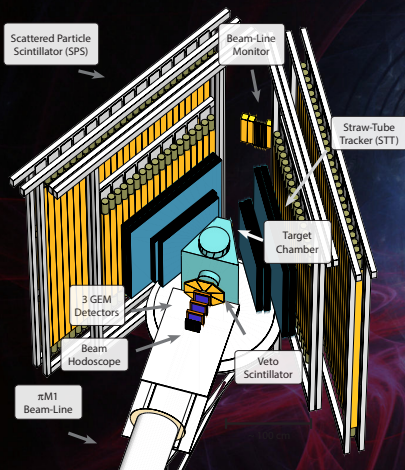
PSI

World's most powerful low-energy $e/\pi/\mu$ -beam:

Direct comparison of ep and μp !

- » Beam of $e^+/\pi^+/\mu^+$ or $e^-/\pi^-/\mu^-$ on liquid H_2 target
 - » Species separated by ToF, charge by magnet
- » Absolute cross sections for ep and μp
- » Ratio to cancel systematics
- » Charge reversal: test TPE
- » Momenta 115-210 MeV/c \Rightarrow Rosenbluth G_E, G_M

Experiment layout



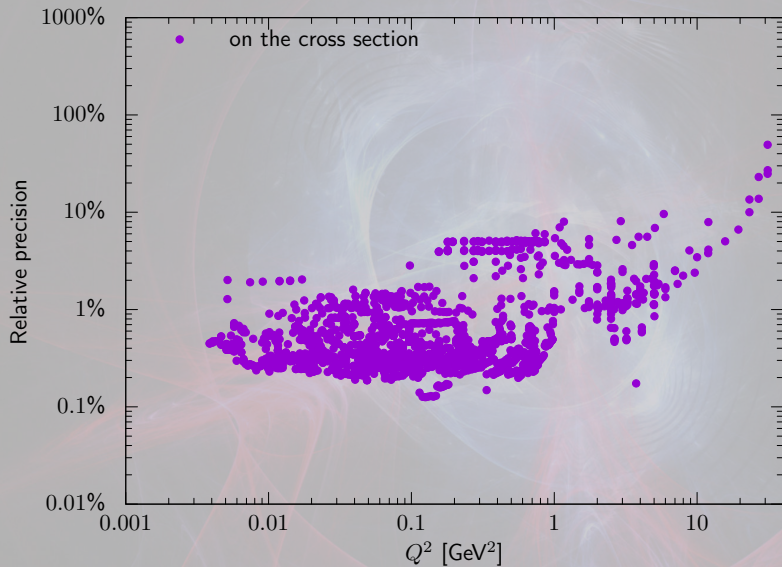
- » Secondary beam \implies track beam particles
- » Low flux (5 MHz) \implies large acceptance
- » Mixed beam \implies PID in trigger

R. Gilman et al., arXiv:1303.2160 (nucl-ex)

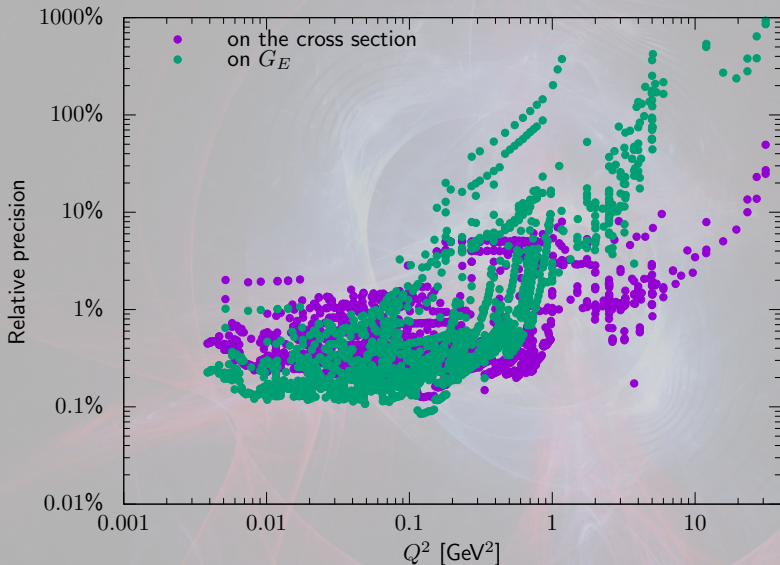
MUSE in the air



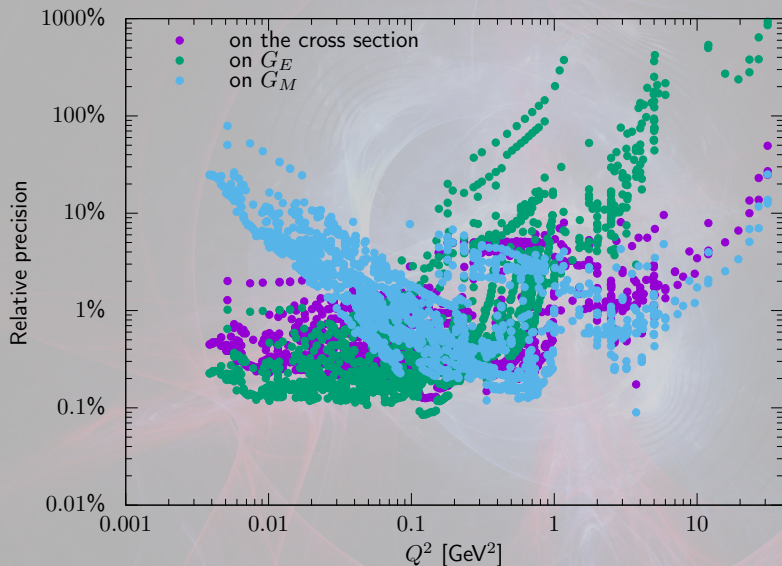
What do we know about G_M



What do we know about G_M



What do we know about G_M

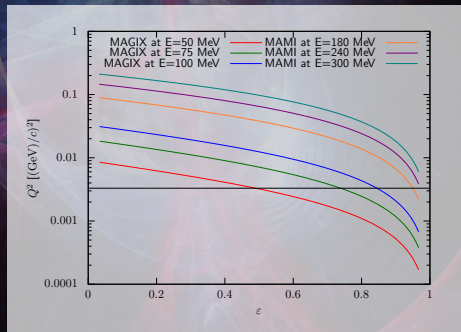
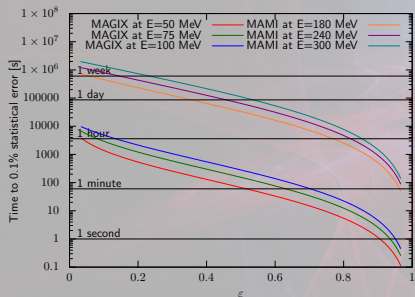


Next generation experiments at Mainz

- » **Initial State Radiation**
- » Next-gen Rosenbluth-type with improved systematics at MAMI and MESA
- » Active target: high pressure Hydrogen TPC

Mainz future plans

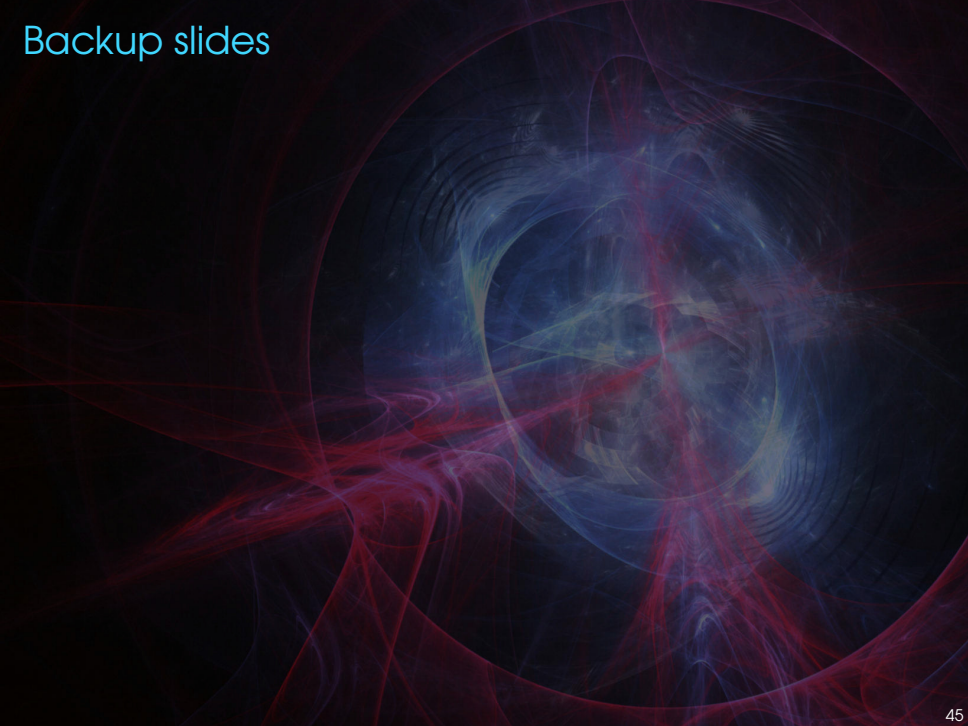
- » Cluster jet target to kill major contributions to systematic errors
- » Repeat ISR with new target (mainly G_E)
- » Use new target also for classical approach
- » Already had test beam. Construct active veto and collimator for further background reduction



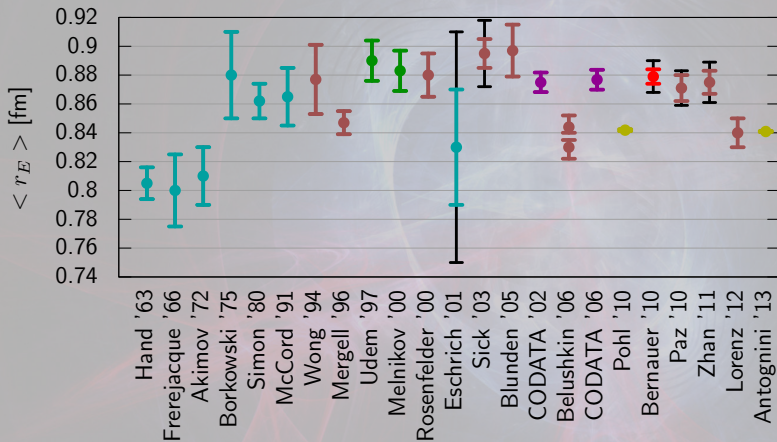
Summary

- » After 9 years, the **puzzle still stands**
- » **Spectroscopy** has many new results, mixed, but with weight behind the **smaller radius**
 - » unknown what causes difference in spectroscopy results
- » **Scattering**; First values released / about to be released. **Situation still unclear**
- » More scattering data in the pipeline
- » **Don't forget about magnetic radius!**

Backup slides



Timeline of proton radius results



Comments on some newer fitting results

2010: >0.870 Hill, Paz: old data, z expansion with disp. bounds

» Bounds on infinite exp. \rightarrow bounds for truncated exp.?

2012: $0.840(10)$ Lorenz, Hammer, Meissner: Disp. relation fit.

» Same value but a lot more data. Probably model dominated.

2014: 0.84 Lorenz, Meissner: z expansion without bounds

» Fit did not converge. In real minimum, large radius is found.

2014: $0.8989(1)$ Gracyk/Juszczak: Bayesian estimation

» Interesting technique, unbelievable? small errors

2016: $0.84?$ Higinbotham: F-Test to select max. order

» Misunderstood F-test. Absence of proof \neq proof of absence.

2016: $0.84?$ Horbatsch/Hessels/Griffioen/Carlson/Maddox... Low-Q

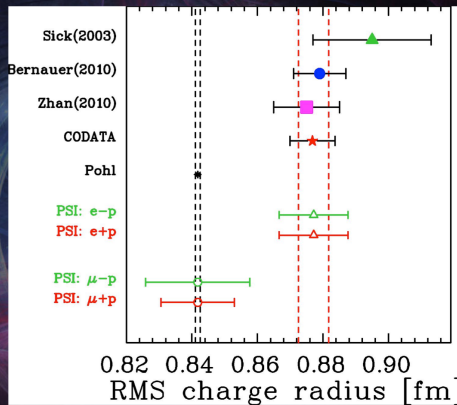
» Low-Q fits with low order don't work.

2018: XXX Yan/Higinbotham/...

» Small radius fraction finally does bias testing

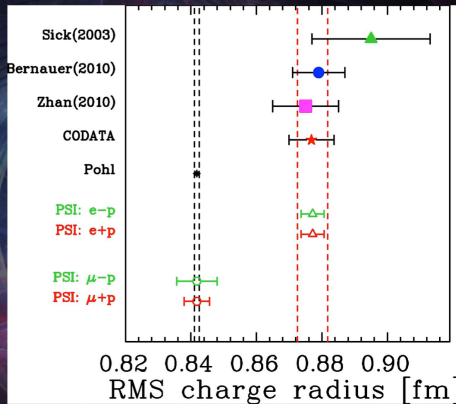
MUSE: Predicted performance

- » Absolute radius extraction uncertainties similar to current exp's.



MUSE: Predicted performance

- » Absolute radius extraction uncertainties similar to current exp's.
- » **Difference:** Common uncertainties cancel!
- » \rightarrow **factor two more sensitivity**



MUSE can verify 7σ effect with similar significance!

Mainz: Volume of Data

