

CLAS Collaboration

Moments of nucleon
structure function F_2
part III - complex nuclei
part II - deuteron: PRC73
part I - proton: PRD67

M. Osipenko, October 19,
JLab12 meeting,
Rome 2009

Moments

QCD $\xrightarrow{\text{OPE}}$ Structure Function Moments

$$M_n(Q^2) \equiv \int_0^1 dx x^{n-2} F_2(x, Q^2) = \sum_{\tau=2k}^{\infty} E_{n\tau}(\mu^2, Q^2) O_{n\tau}(\mu^2) \left(\frac{\mu^2}{Q^2}\right)^{\frac{1}{2}(\tau-2)}$$

n - operator spin
 τ - operator twist
 = dimension-spin
 μ - arbitrary scale

evolution

static

Perturbative QCD

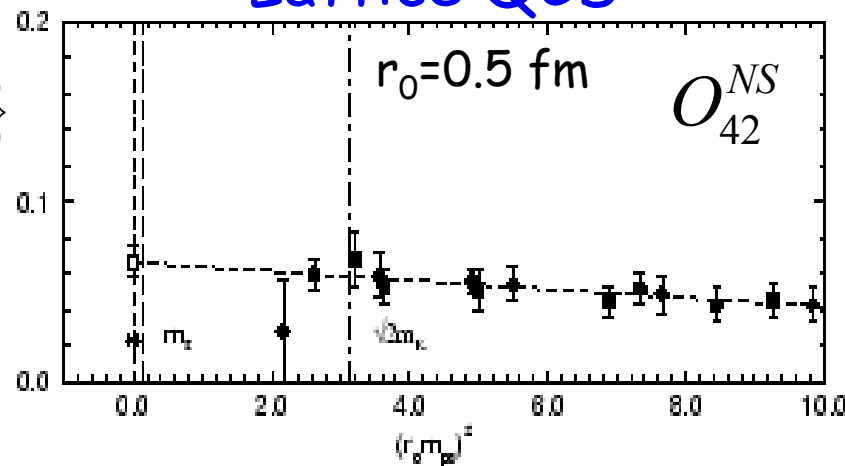
Lattice QCD

R. Horsley,
[hep-lat/0412007](https://arxiv.org/abs/hep-lat/0412007)

$$E_{n\tau}(\mu, Q^2) \sim \left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu^2)}\right)^{\gamma_n^\tau} \left\{1 + B_n^\tau \alpha_s(Q^2) + \dots\right\}$$

γ_n^2 - anomalous dimension

B_n^2 - coefficient functions

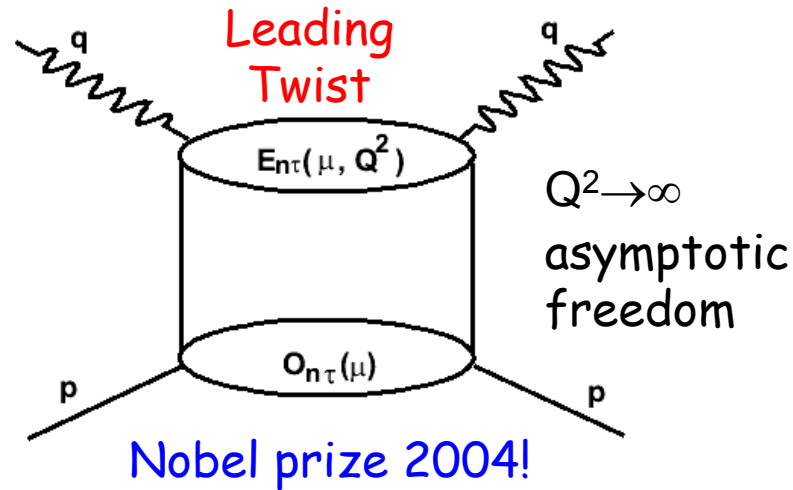


*Present technique of Lattice QCD can handle flavor Non-Singlet operators only
 (noisy disconnected diagrams cancel in such combination)

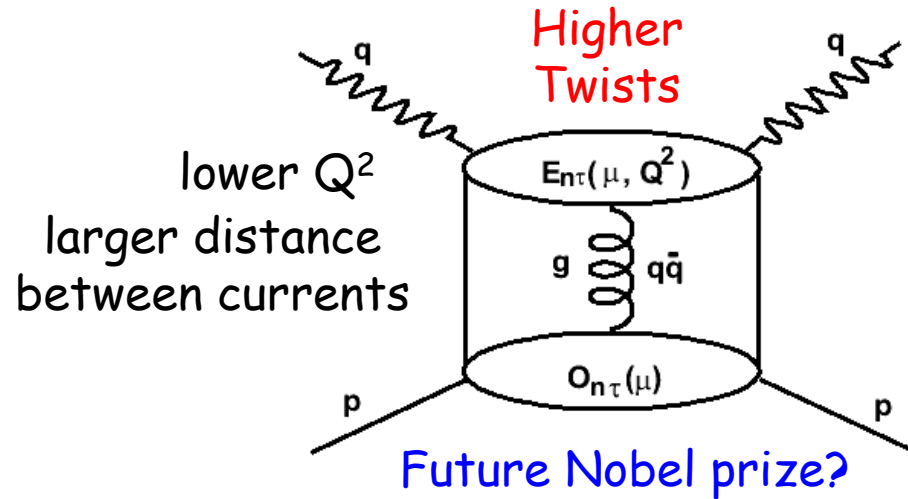
→ necessary to measure moments of both the proton and neutron.

Twists

Higher Twists represent the virtual photon scattering off interacting (correlated) partons: e.g. diquarks, entire nucleon etc.



+



- Twist separation through Q^2 -evolution study of the moments in a large Q^2 interval
- X. Ji and Unrau, PRD52

Leading twist

Higher twists
suppressed in DIS by $1/Q^\tau$

$$M_n(Q^2) = LT_n(\alpha_S) + \sum_{\tau=2k} a_n^\tau(\mu) \left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu^2)} \right)^{\gamma_n^\tau} \left(\frac{\mu^2}{Q^2} \right)^{\frac{\tau-2}{2}}$$

* a_n^τ and γ_n^τ are known only in few cases:

E. Shuryak and A. Vainstein, NPB201

H. Kawamura, MPLA12

M. Osipenko

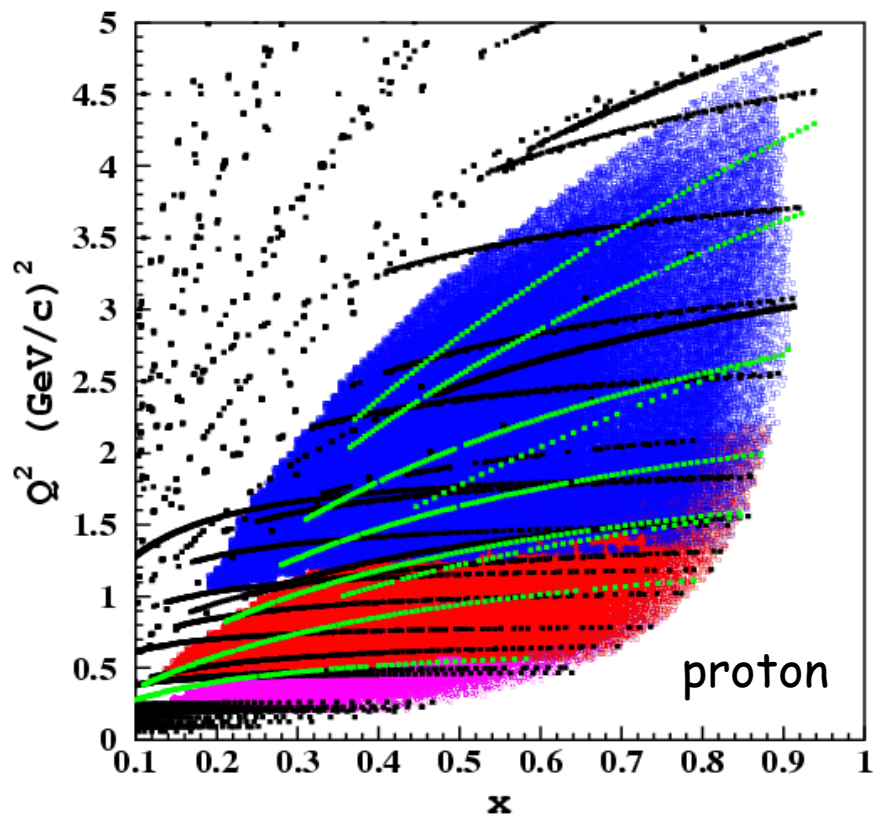
Operator
matrix
element

LO
Coefficient
function

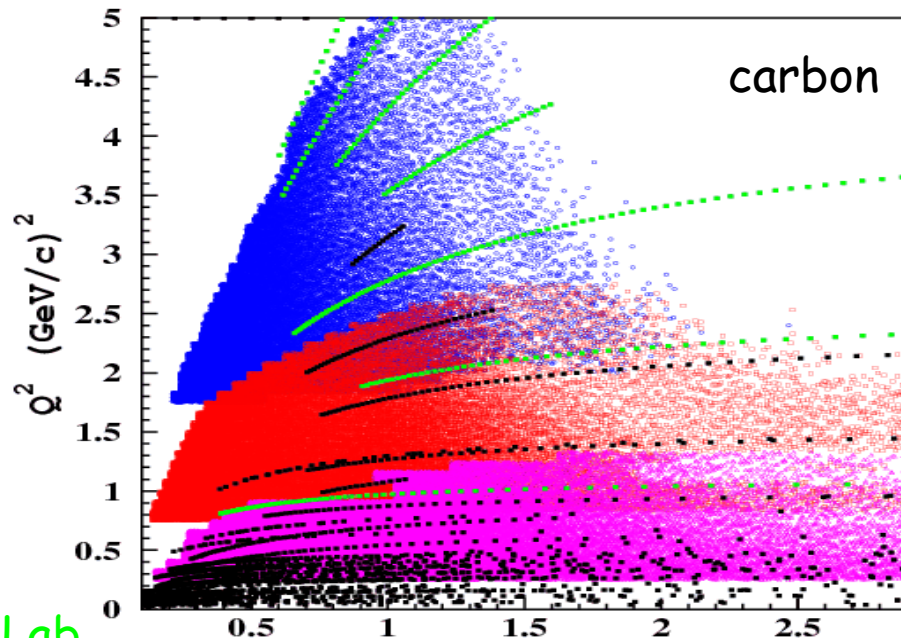
CLAS F₂ Data

- Continuous two-dimensional kinematics
- Wide x-coverage at each fixed Q²
- Very detailed large-x region
- $R = \sigma_L / \sigma_T$ is known from Hall-C experiment: C. Keppel E94-110

CLAS 1.5 GeV + 2.5 GeV + 4 GeV

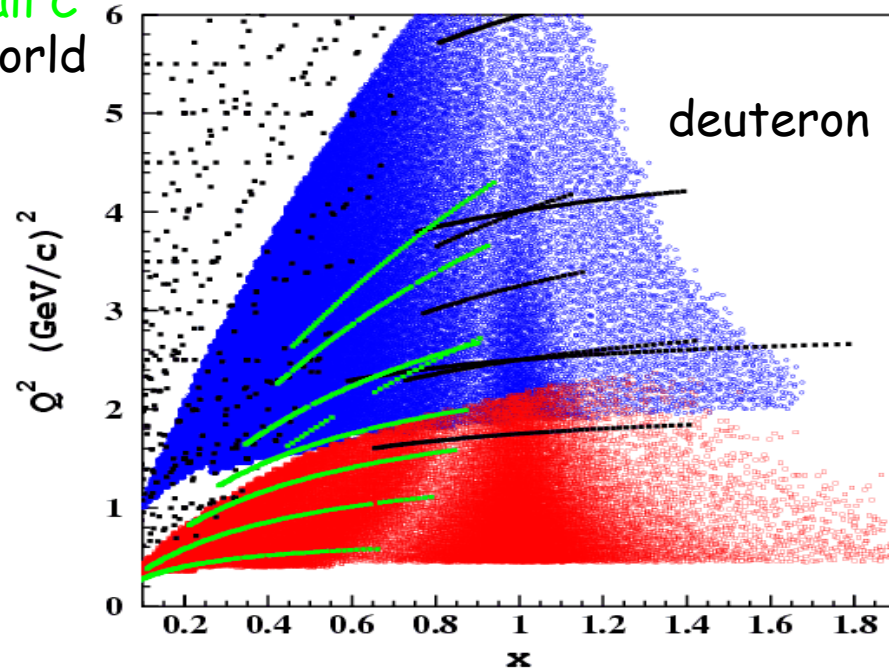


CLAS 1 GeV + 2 GeV + 4.4 GeV



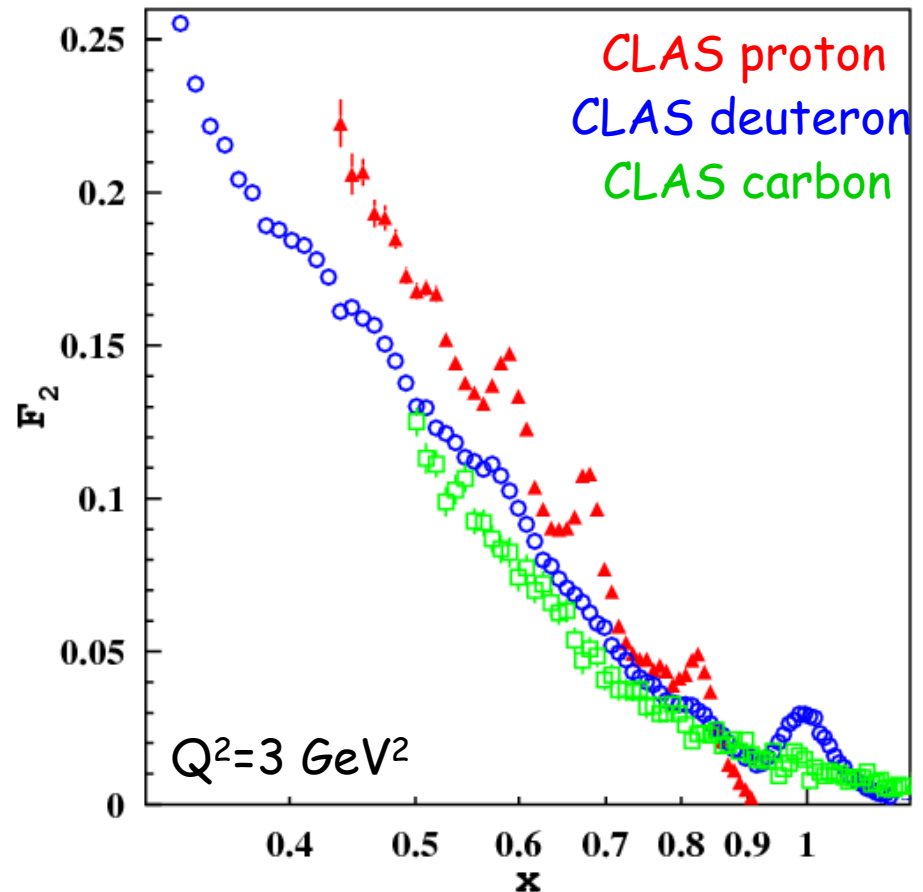
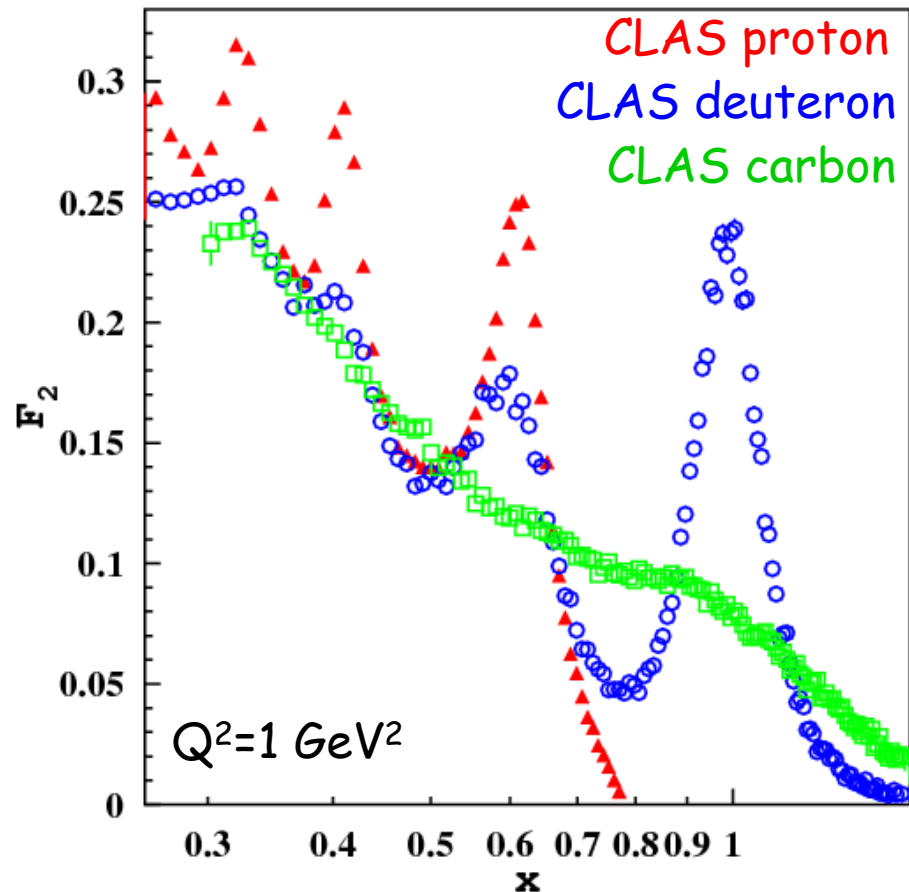
JLab
Hall C
World

CLAS 2.5 GeV* + 5.8 GeV



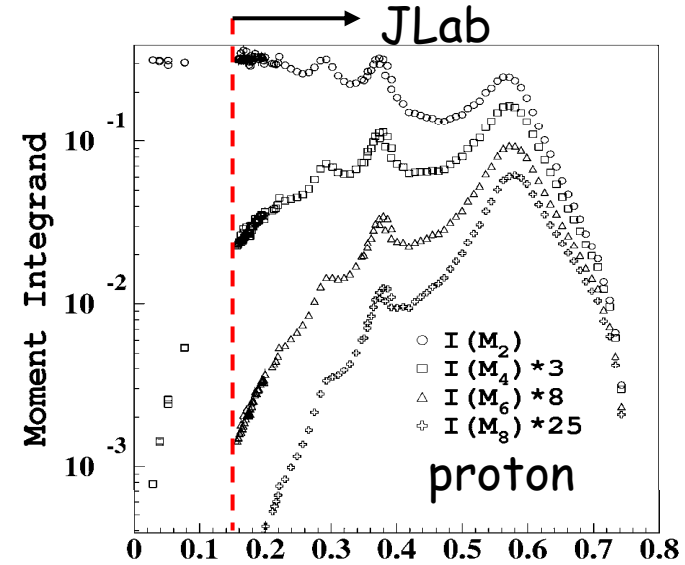
F_2 Nuclei vs. Proton

- The measurements of the nuclear structure functions were performed in the same bins as for proton F_2 .
- Resonance peaks seem to be smaller in the deuteron and completely disappeared in carbon even at low Q^2 . But, mostly it is the effect of the Fermi motion.



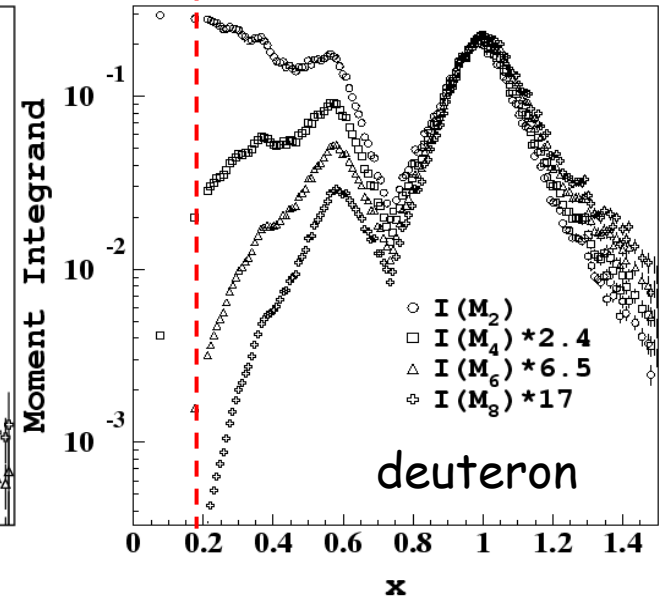
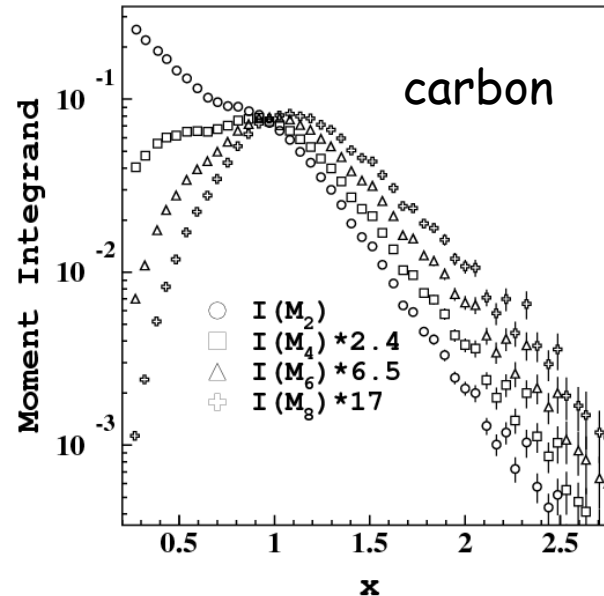
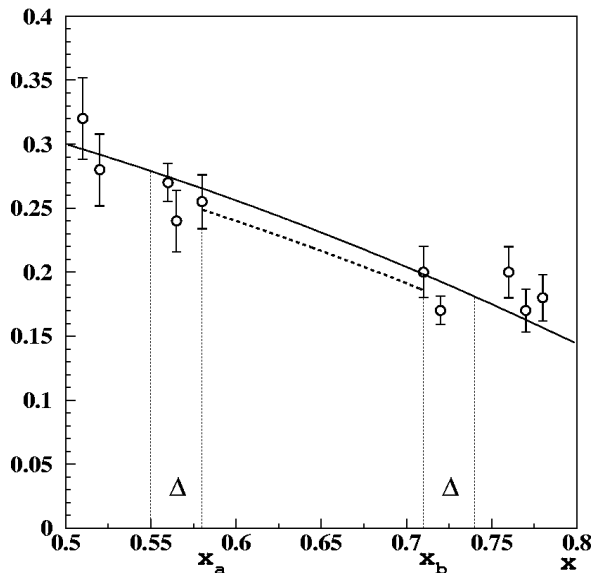
Extraction of moments

- CLAS data cover most significant region for higher moments ($n > 2$)
- For nuclei we also measured the quasi-elastic peak at each Q^2 value
- Extraction method is essentially independent of x -behavior of the structure function
- Reliable evaluation of the Q^2 -evolution of structure function moments.



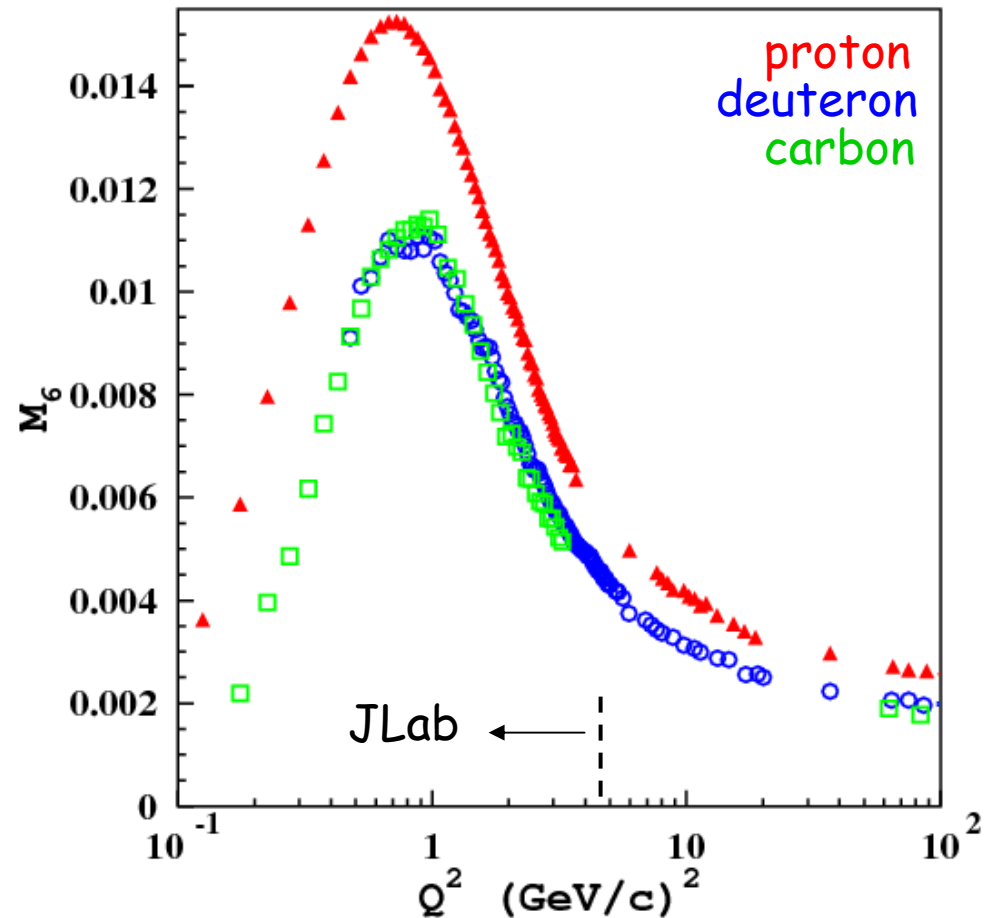
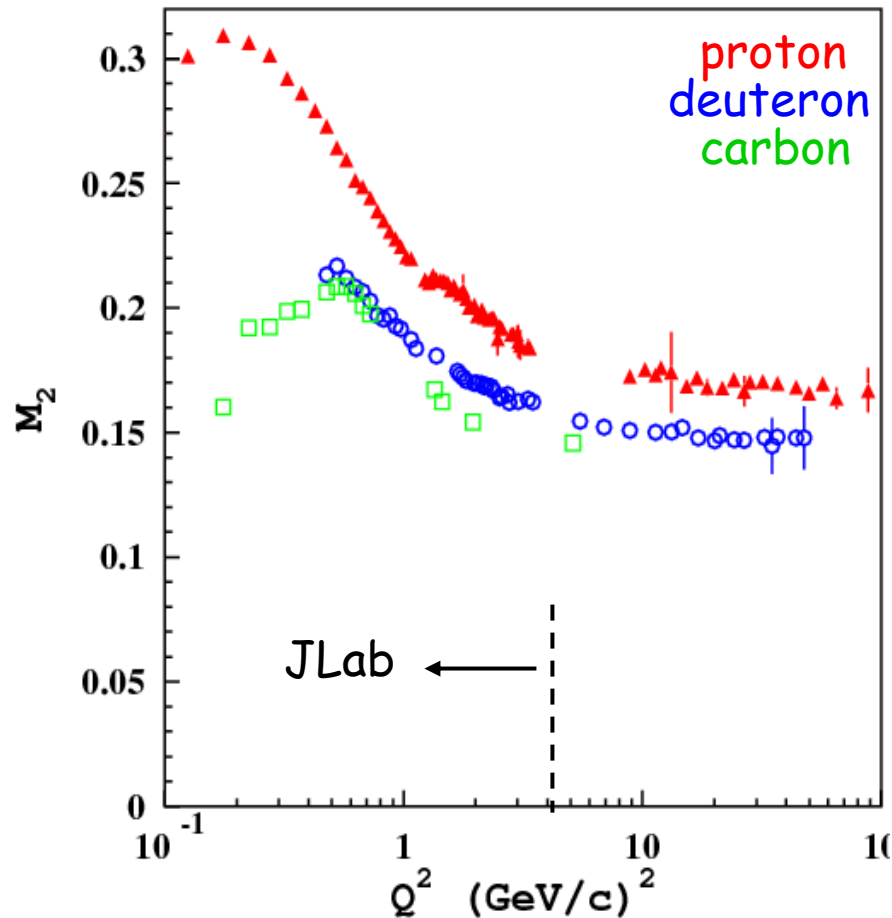
$$Q^2 = 0.825 \text{ GeV}^2$$

Moment Integrand



Moments

- Leading Twist Q^2 -evolution is the same for the proton, deuteron and carbon.
- Higher Twist contribution in nuclei contains additional nuclear HT terms
- Proton and nuclear moments have similar Q^2 -behavior suggesting a small contribution of nuclear Higher Twists.
- Carbon moments are very similar to the deuteron ones.

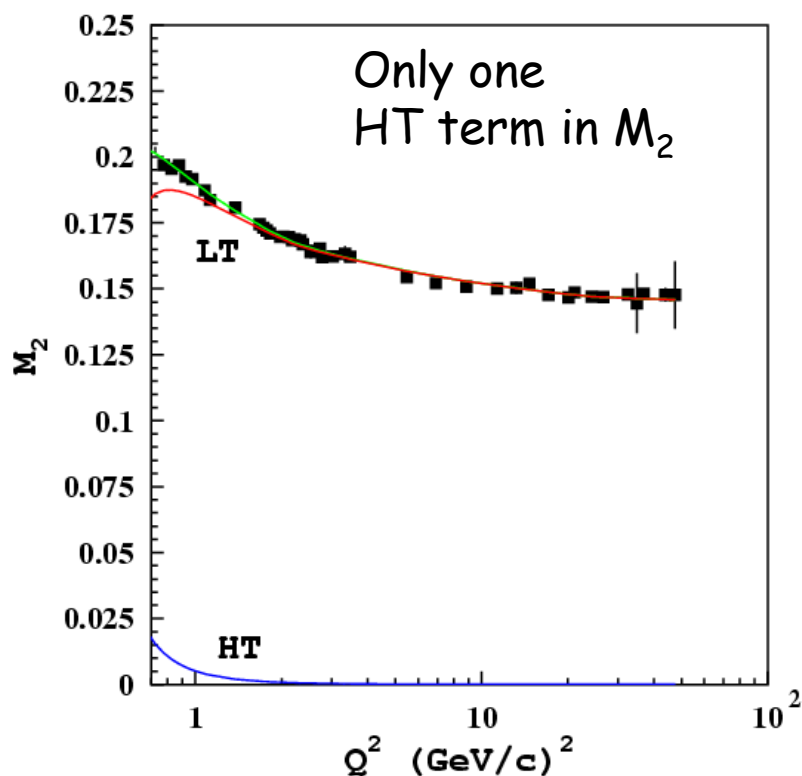


Twist Expansion

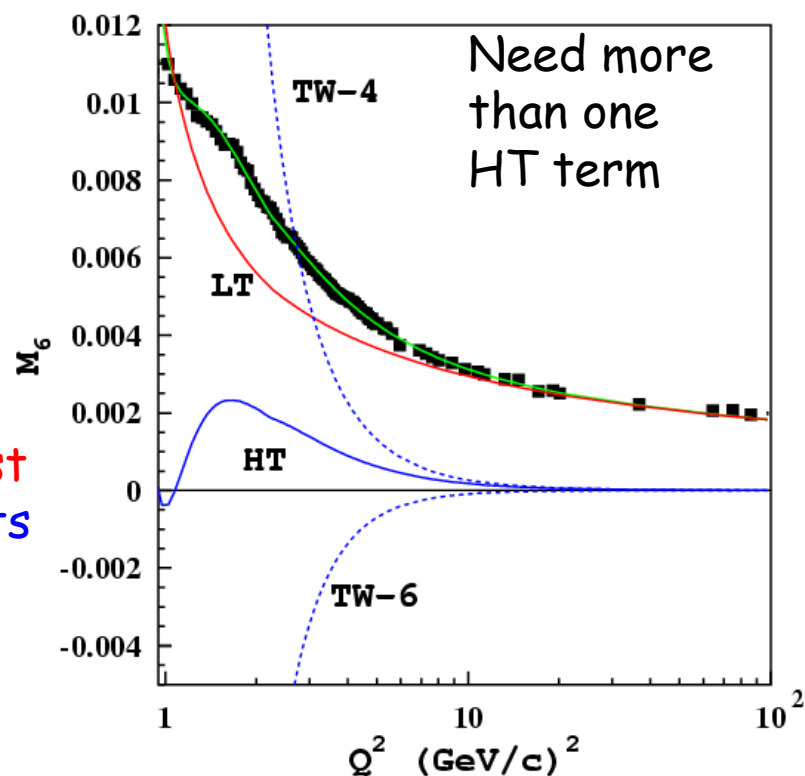
Leading and Higher Twists were separated by fitting the data with the following expression:

$$M_n(Q^2) = LT_n(\alpha_s) + \sum_{\tau=4,6} a_n^\tau \left(\frac{\alpha_s(Q^2)}{\alpha_s(\mu^2)} \right)^{\gamma_n^\tau} \left(\frac{\mu^2}{Q^2} \right)^{\frac{\tau-2}{2}}$$

- Leading Twist is determined by one free parameter $LT_n(\mu^2)$
- Higher Twist contribution is described by four free parameters $a_n^4, \gamma_n^4, a_n^6, \gamma_n^6$



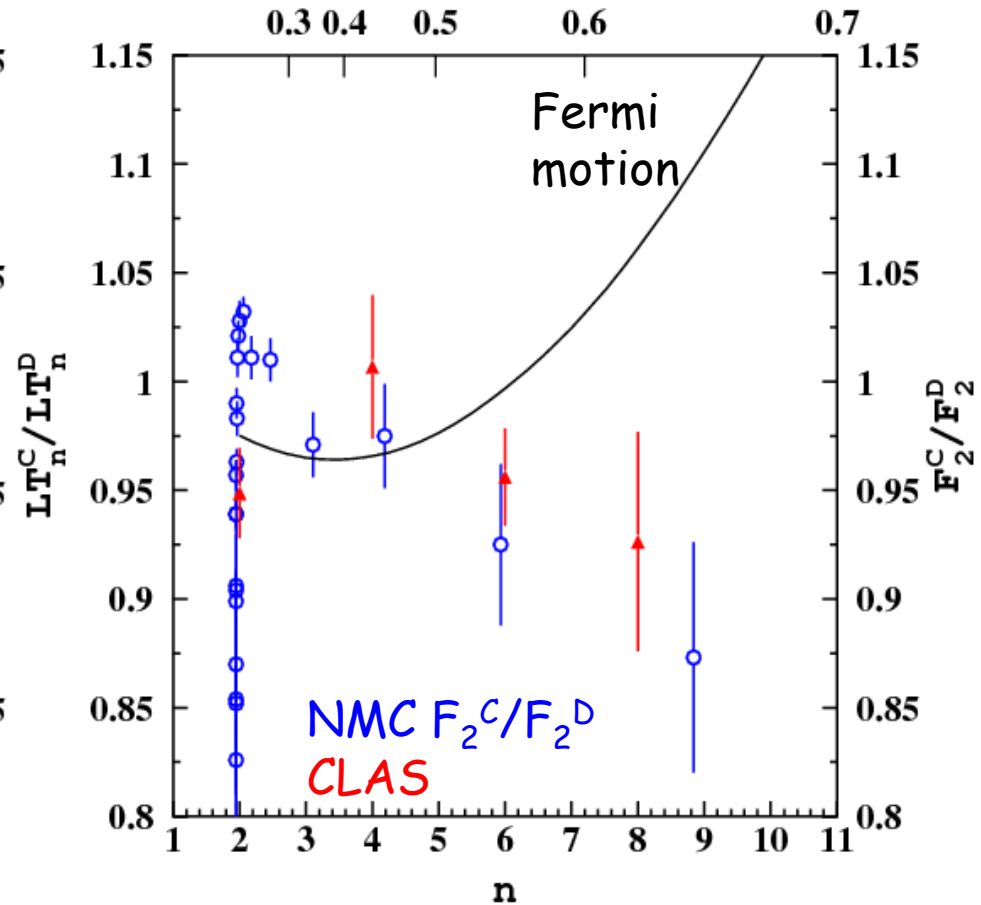
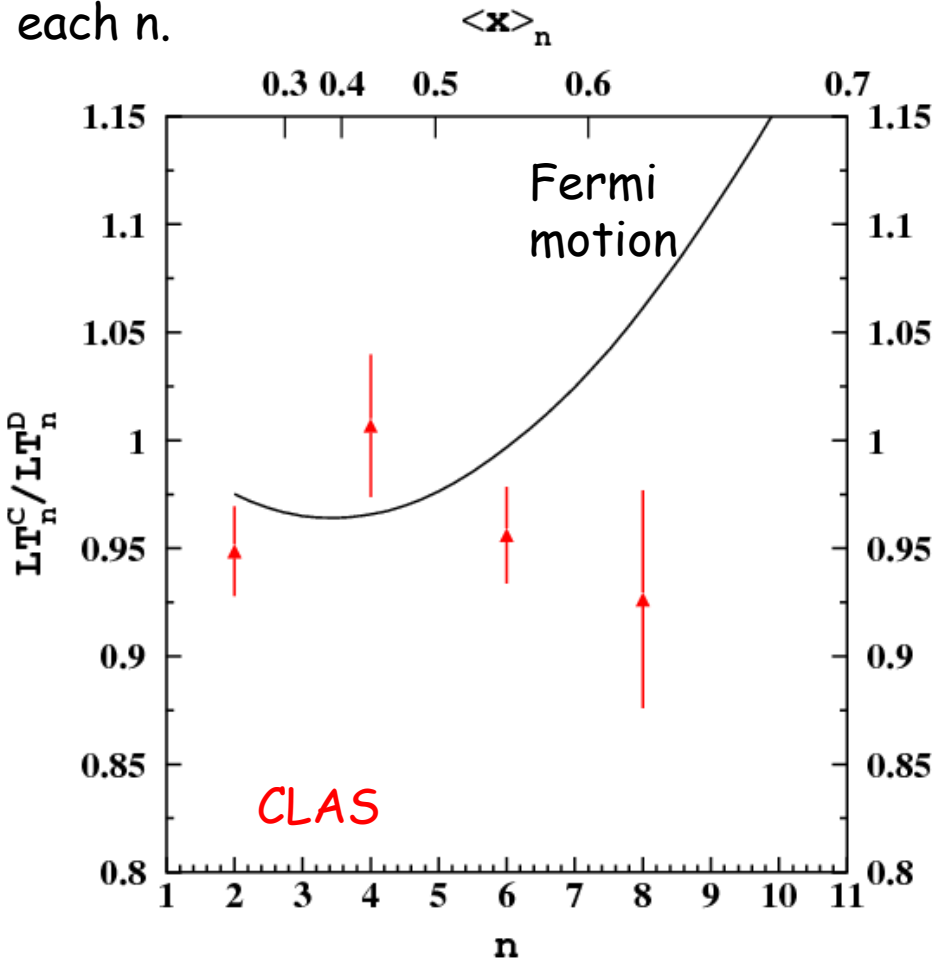
Fit
 Leading Twist
 Higher Twists



EMC effect: Leading Twist

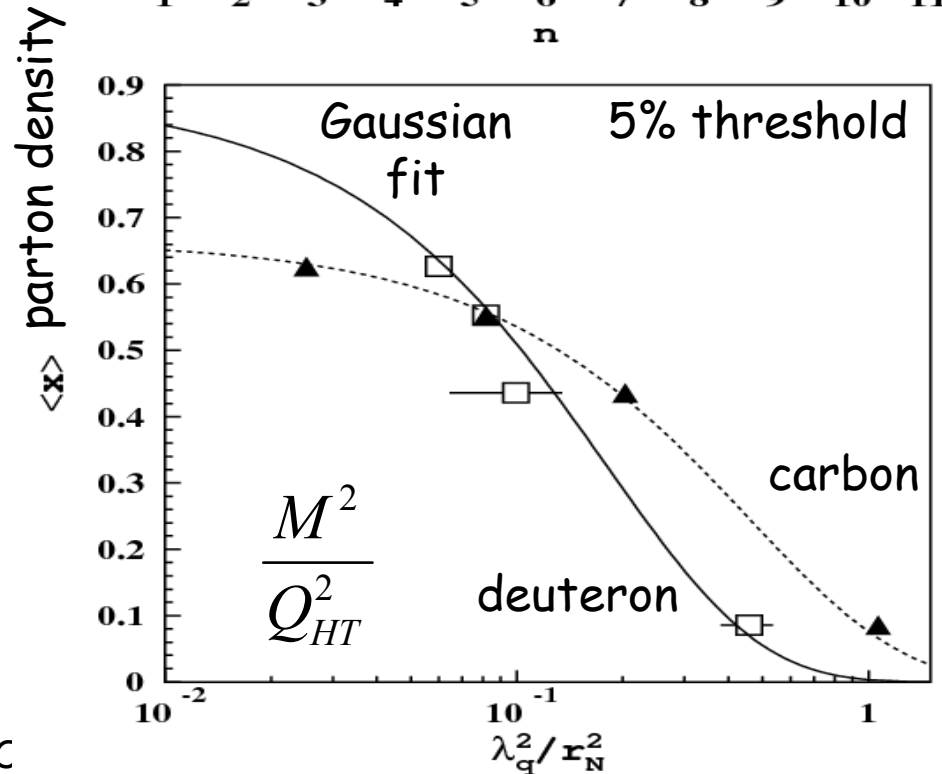
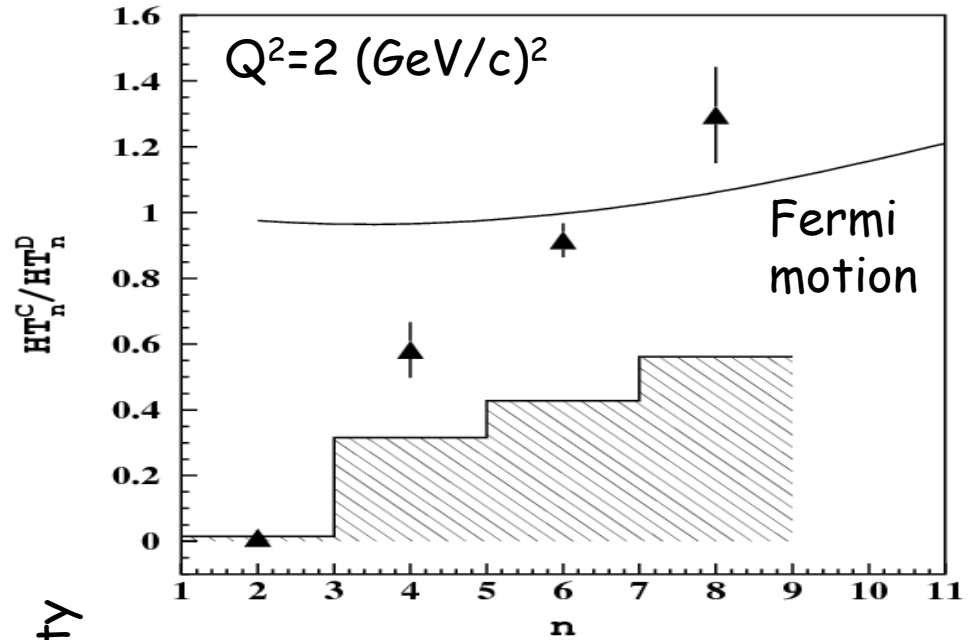
- Ratio of C/D moments exhibits deviation from IA Fermi motion prediction, demonstrating EMC effect discovered in x-space.
- The ratio of moments is in good agreement with the ratio of the structure functions taken at average value of x for each n.

$$\frac{LT_n^C}{LT_n^D} = \frac{\int_0^1 dz f^C(z) z^{n-1}}{\int_0^1 dz f^D(z) z^{n-1}}$$



HTs in Nuclei

- Ratio of Higher Twists in carbon and deuteron, taken at fixed Q^2 , demonstrates linear rise with n ;
- At small $n < 8$ the Higher Twist contribution in carbon is smaller than in the deuteron;
- For $n=2$ the Higher Twist contribution in carbon is compatible with zero;
- The suppression of Higher Twists in complex nuclei can be related to a partial quark deconfinement;
- For higher moments $n \geq 8$ the contribution of Short Range Correlations, found in the region $x > 1$, becomes important. This contribution, not related to internal nucleon structure, may be responsible for the rise of nuclear Higher Twists with n .



Summary

- Carbon structure functions F_2 were measured in continuous two-dimensional kinematical range of x and Q^2 ;
- These data combined with all previous measurements were used to obtain experimental moments of the structure function F_2 ;
- Extracted moments were analyzed in terms of Operator Product Expansion;
- The ratio of Leading Twists of carbon to deuteron reveals EMC effect compatible with that in the x -space.
- The ratio of Higher Twist contributions in carbon and deuteron is found to be suppressed for low n and increasing rapidly with n .
- The draft of the paper is in AdHoc review of CLAS Collaboration.
WG review (Nuclear): Michael Dugger (chair), Tony Forest, Rakhsha Nasseripour
Started - September 27, 2007,
Approved - February 12, 2009, \rightarrow 1 year and 4 months
AdHoc review: Tony Forest (chair), Stepan Stepanian, Chaden Djalali
Started - April 10, 2009
Today - October 19, 2009 \rightarrow 7 months