

# P1.1037 The Ideal Evolution Equation and Fast Magnetic Reconnection

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See the full abstract here:

<http://ocs.ciemat.es/EPS2019ABS/pdf/P1.1037.pdf>

The ideal evolution equation,  $\partial B/\partial t = \text{curl} \times (\mathbf{u} \times \mathbf{B})$ , implies magnetic field lines move with a velocity  $\mathbf{u} \perp$  and cannot change their connections. Nevertheless, for an electric field that is arbitrarily close to the ideal form,  $\mathbf{E} + \mathbf{u} \perp \times \mathbf{B} = -\text{grad} \Phi$ , magnetic connections will in general break on a time scale  $\tau$ , where  $1/\tau \approx |\text{grad} \mathbf{u} \perp|$ , times the logarithm of the magnetic Reynolds number  $\mathfrak{R}_m$ , which is  $|\mathbf{u} \perp \times \mathbf{B}|$  divided by the deviation of the parallel electric field from the ideal form. The connections breaking part of the magnetic field is proportional to  $\exp(t/\tau)/\mathfrak{R}_m$ . This mathematical theorem is proven [1] using Lagrangian coordinates,  $\partial \mathbf{x}(x_0, t)/\partial t = \mathbf{u} \perp(x, t)$ , which provide an explicit solution for an ideally evolving magnetic field  $\mathbf{B}(\mathbf{x}, t)$ . The exact electric field defines the evolution of the Clebsch potential  $\sin \mathbf{B} = \text{grad} \alpha \times \text{grad} \beta$ . This evolution can be solved analytically for the deviation of a magnetic field from its ideal form,  $\mathbf{B} - \mathbf{B}_I$ , while that deviation is small. The generic behavior of a near-ideal evolution provides answers to four fundamental questions on magnetic reconnection: (1) Why does the near-ideal evolution of natural and laboratory magnetic fields robustly lead to states of fast magnetic reconnection independent of the drive and of the initial state? (2) What is the characteristic time required to reach a state of fast magnetic reconnection? (3) What is the explanation of the effects produced by fast magnetic reconnection, which are primarily associated with magnetic helicity conservation and an energy transfer from the magnetic field to the plasma? (4) Why does the Alfvén speed define the time scale during which the effects produced by fast magnetic reconnection occur? A middle singular value of the Singular Value Decomposition of the Jacobian matrix  $\partial \mathbf{x}/\partial \mathbf{x}_0$  of Lagrangian coordinates is required for an exponential growth of the connections-breaking field while having a small, non-exponential, change in the magnetic field strength. The two-dimensional assumption of traditional reconnection theories effectively excludes exponentiation. Traditional theories are inapplicable to the fast reconnection that occurs during tokamak disruptions and of problematic applicability to the astrophysical problems for which they were developed.

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[1] A. H. Boozer, Phys. Plasmas 26, 042104 (2019).

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