

New developments in the PROSA PDF fit

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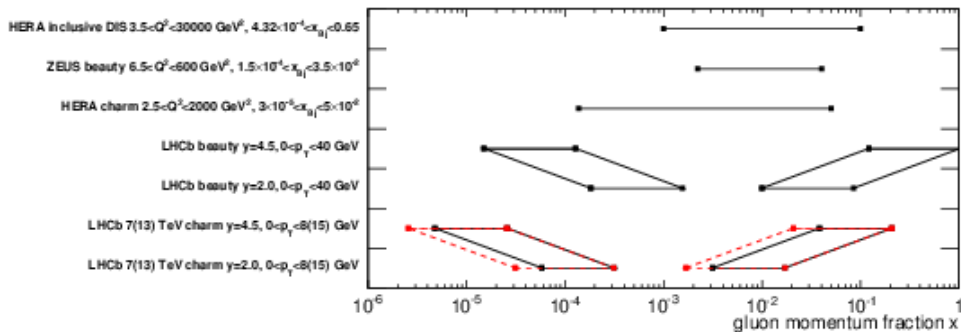
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on the basis of
O. Zenaiev, M.V. Garzelli, K. Lipka et al., DESY-19-211
arXiv:1912.XXXX

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x coverage of HERA and LHCb experiments

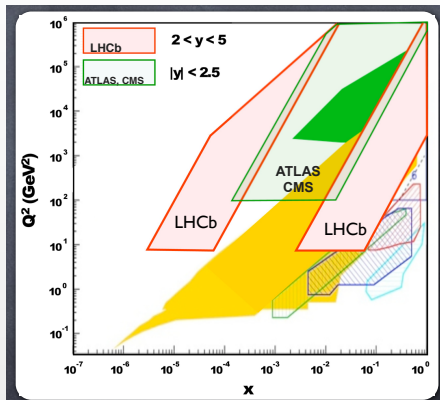


LHCb data allows to cover x regions uncovered by HERA data, both at low x 's (especially open charm data) and at large x 's (especially open bottom data).

Larger rapidities of the emitted quark and/or larger collision energies correspond to more extreme x 's

Open heavy-flavour data from further experiments

- * LHCb open-charm data
($2 < y < 4.5$)
- * ATLAS (and CMS)
open-charm data
($|y| < 2.5$)
- * CDF open-charm data ($|y| < 1$)
- * ALICE open-charm data
($|y| < 0.5$)
- + further open-bottom data



Different experiments span (Q^2 , x) regions partially overlapping:
good for verifying their compatibility and for cross-checking their
theoretical description.

The PROSA 2015 PDF fit

The PROSA PDF fit [EPJC 75 (2015) 471] is the first one appeared in the literature which has proposed the following

basic idea: use the data on D -meson and B -meson hadroproduction at LHCb to constrain PDFs (especially gluon PDFs) at low x 's.

Data sets:

Open charm data at 7 TeV: D -meson p_T distributions in the range $[0, 8]$ GeV, in five equal-size rapidity bins between $2 < y < 4.5$. [arXiv:1302.2864]

Open bottom data at 7 TeV: B -meson p_T distributions in the range $[0, 40]$ GeV, in five equal-size rapidity bins between $2 < y < 4.5$ [arXiv:1306.3663]

These data are considered together with all HERA data used for the HERAPDF1.0 PDF fit:

- NC and CC inclusive DIS combined HERA-I data,
- $c\bar{c}$ DIS combined HERA data and $b\bar{b}$ DIS ZEUS data.

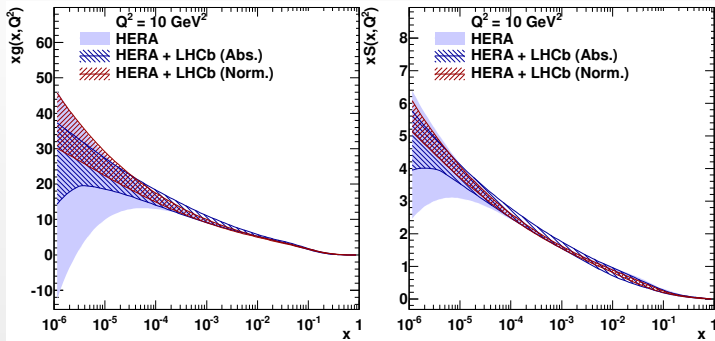
Follow-up fits (made by reweighting recent NNPDF PDF fits):

- R. Gauld, J. Rojo, L. Rottoli, J. Talbert, JHEP 1511 (2015) 009
- R. Gauld, J. Rojo, PRL 118 (2017) 072001
- V. Bertone, R. Gauld and J. Rojo, arXiv:1808.02034

The last two use even LHCb data at $\sqrt{s} = 5$ and 13 TeV.

PROSA 2015 PDF fit: comparison between three variants

from PROSA collab., EPJC 75 (2015) 471



Three variants of the PDF fit:

- 1) one only with HERA data;
- 2) one also including LHCb absolute differential cross-sections;
- 3) another one with reduced uncertainties: for each fixed LHCb p_T bin, use the ratios of distributions $(d\sigma/dy)/(d\sigma/dy)_0$ considering different rapidity intervals (i.e. normalized to the central bin $3 < y_0 < 3.5$):

in the ratios theoretical uncertainties partly cancel.

Main differences of the PROSA 2019 PDF fit

(w.r.t. PROSA 2015)

- * We used the HERA I + HERA II combined inclusive DIS data [arXiv:1506.06042] (instead of the HERA I ones)
- * We used the HERA I + HERA II combined charm and bottom DIS data [arXiv:1804.01019]
- * We used additional LHCb data:
 - open charm data at $\sqrt{s} = 5 \text{ TeV}$ [arXiv:1610.02230],
 - open charm data at $\sqrt{s} = 13 \text{ TeV}$ [arXiv:1510.01707].
- * We included recent ALICE data:
 - open charm data at $\sqrt{s} = 5 \text{ TeV}$ [arXiv:1702.00766],
 - open charm data at $\sqrt{s} = 7 \text{ TeV}$ [arXiv:1901.07979].

Main differences of the PROSA 2019 PDF fit

(w.r.t. PROSA 2015)

- * (μ_R, μ_F) scale choices
- * Together with the PDF dependence on x , we fit the values of $m_c(m_c)$ and $m_b(m_b)$ in the MSbar scheme, consistently used for all theoretical predictions at NLO in the FFNS.
- * PDF parameterization modified/extended with additional terms.
- * FFNS and VFNS versions: the latter exploits the possibility now present in xFitter to select $\mu_c, \mu_b > m_c, m_b$.

PROSA 2019 PDF parameterization

- * Most general parameterization considered:

$$xf(x) = Ax^B(1-x)^C(1 + Dx + Ex^2 + F \log x), \quad f = g$$

$$xf(x) = Ax^B(1-x)^C(1 + Dx + Ex^2), \quad f = u_v, d_v, \bar{U}, \bar{D}$$

- D , E , F parameters initially set to zero and then included one at a time, monitoring the improvement of the χ^2 .
- F from [1902.11125] fitted value small (0.068 ± 0.024),
 F variation affects the fit uncertainties.

- * Final parameterization:

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} (1 + F_g \log x),$$

$$xu_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2),$$

$$xd_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = x\bar{u}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = x\bar{d}(x) + x\bar{s}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- * Constraints reduce the number of free parameters

Alternative gluon PDF parameterizations

PROSA19:

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} (1 + F_g \log x),$$

ABMP16:

$$xg(x) = A(1-x)^b x^{a(1+\gamma_1 x)},$$

CT14:

$$xg(x) = Ax^{a_1}(1-x)^{a_2}(e_0(1-y)^2 + e_1(2y(1-y)) + y^2), y = 2\sqrt{x} - x,$$

HERAPDF2.0 flex. g :

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{25},$$

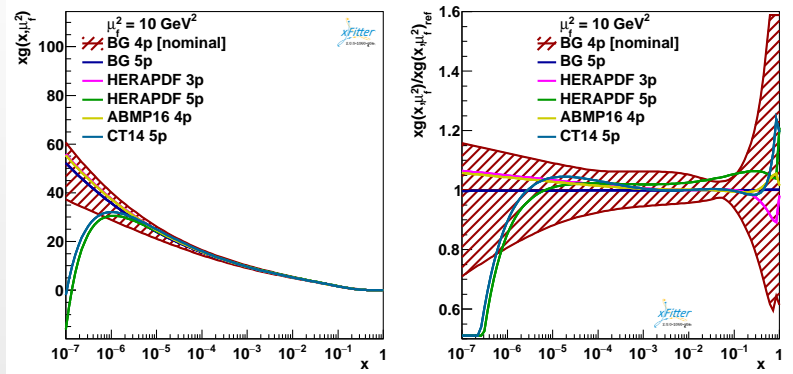
HERAPDF2.0 no flex. g :

$$xg(x) = A_g x^{B_g} (1-x)^{C_g},$$

BG:

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} (1 + F_g \log x + G_g \log^2 x)$$

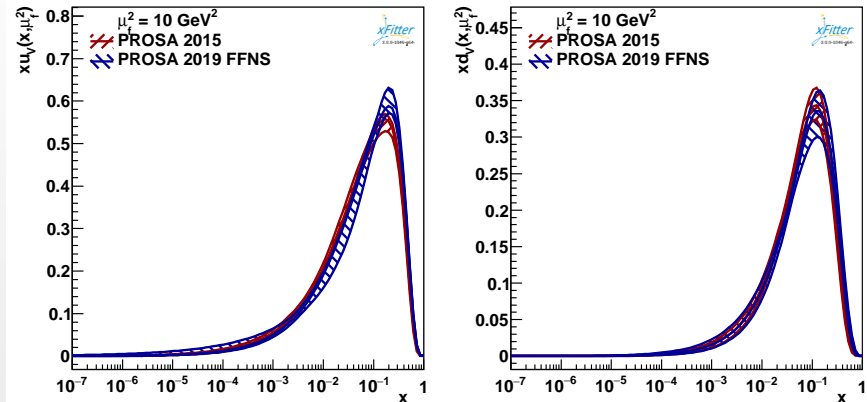
Sensitivity of the low- x gluon to the PDF parameterization employed



* CT14 and HERAPDF flex gluon yield a gluon distribution with a sharp turnover to negative values at the edge of the kinematic reach of the measurements used in the fit ($x \sim 10^{-6}$)

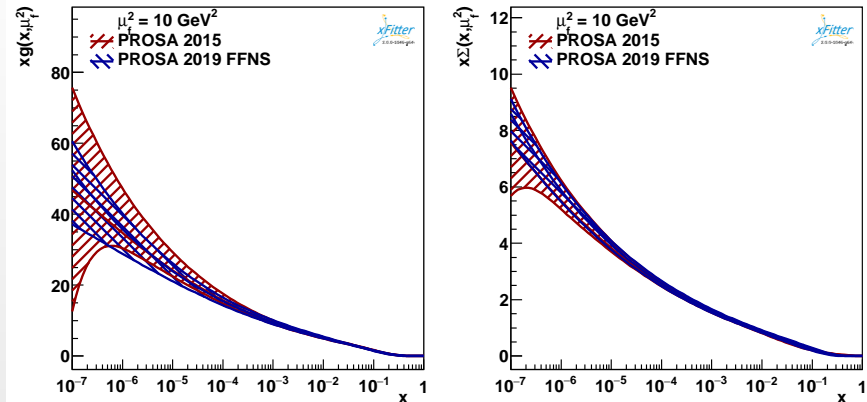
* They provide a slightly better χ^2 but negative $\sigma_{c\bar{c}}$ for $\sqrt{s} > 20 \text{ TeV}$

PROSA 2019 vs PROSA 2015: valence quarks



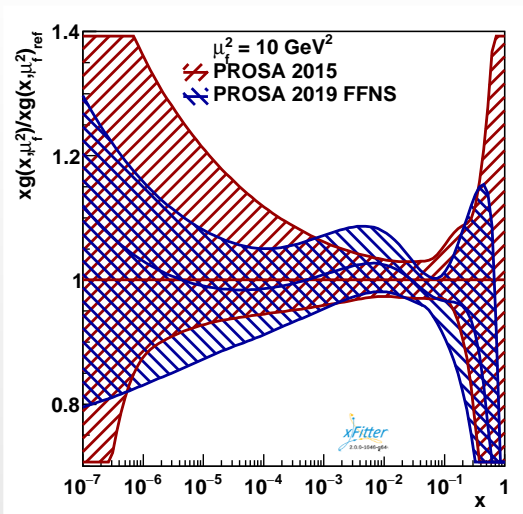
- * approximatively consistent results,
- * differences mainly driven by the use of different sets of inclusive DIS data.

PROSA 2019 vs PROSA 2015: gluons & sea quarks



- * new gluon and sea quark PDFs consistent with the old ones
- * reduced uncertainties for $x < 10^{-4}$

PROSA 2019 vs PROSA 2015: gluons



- * new gluon PDFs consistent with the old one
- * reduced uncertainties for $x < 10^{-4}$

PROSA 2019 PDF fit uncertainties

* **fit** uncertainties: uncertainties in the measurements, estimated by Hessian method with tolerance criterion $\Delta\chi^2 = 1$ (68% C.L.)

* **model** uncertainties:

strangeness fraction $f_s = x\bar{s}/(x\bar{d} + x\bar{s})$ with $0.3 < f_s < 0.5$

$2.5 < Q_{min}^2 < 5.0 \text{ GeV}^2$ cut on HERA I+II data

$0.105 < \alpha_S^{nf=3}(M_Z) < 0.107$ ($0.117 < \alpha_S^{nf=5}(M_Z) < 0.119$)

$\alpha_k^c = 4.4 \pm 1.7$, $\alpha_k^b = 11 \pm 3$

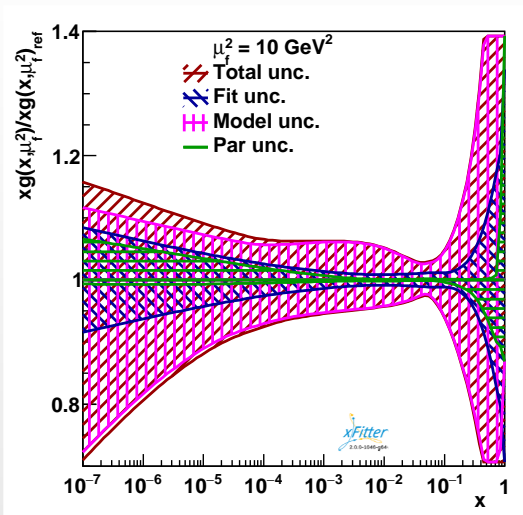
(μ_R, μ_F) 7-point scale variation

* **parameterization** uncertainties:

$1.6 < \mu_{f0}^2 < 2.2 \text{ GeV}^2$

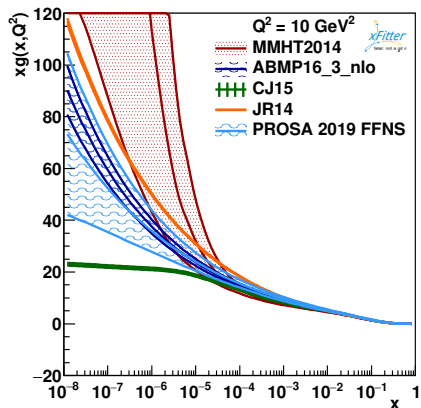
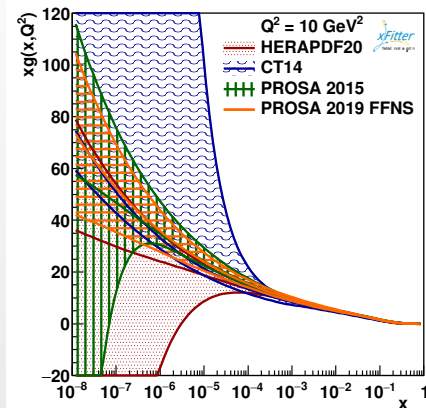
D , E parameters and $G_g \log^2 x$ term

PROSA 2019 vs PROSA 2015: gluon uncertainties

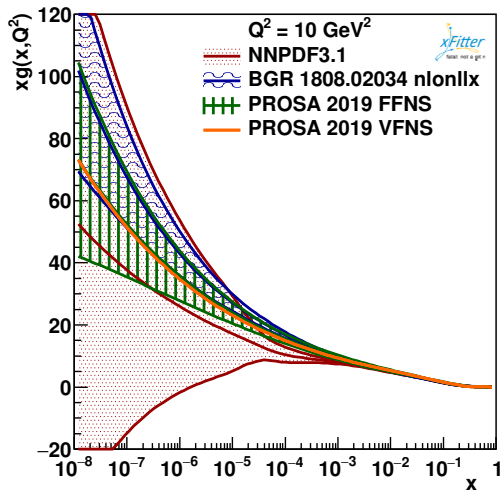


- * Model uncertainties dominating over the others.
They are mostly driven by (μ_R, μ_F) variation.

gluon PDF: comparison between different PDF fits



gluon PDF: comparison between different PDF fits



* Differences between different gluon PDF fits at relatively large x values

* Compatibility of the PDF fits including D -meson data.

Why improving the description of heavy-flavour hadroproduction matter ?

- * Constraints of PDFs at low x 's, which in turns is relevant for
 - **forward physics and multiple parton interactions**, already in the LHC era:
with increasing precision of the LHC data,
improving the description of these aspects matters!
 - **future high-energy colliders**: FCC-hh, etc.....
(see the study in the FCC-hh SM report [arXiv:1607.01831]).
- * **high-energy astroparticle physics** applications:
 - High Energy Cosmic Ray physics and prompt neutrino fluxes
- * disentangling cold and hot **nuclear matter** effects
(in pA and AA collisions).

How to get atmospheric fluxes? From cascade equations to Z -moments [review in Gaisser, 1990; Lipari, 1993]

Solve a system of **coupled differential equations** regulating particle evolution in the atmosphere (interaction/decay/(re)generation):

$$\frac{d\phi_j(E_j, X)}{dX} = -\frac{\phi_j(E_j, X)}{\lambda_{j,int}(E_j)} - \frac{\phi_j(E_j, X)}{\lambda_{j,dec}(E_j)} + \sum_{k \neq j} S_{prod}^{k \rightarrow j}(E_j, X) + \sum_{k \neq j} S_{decay}^{k \rightarrow j}(E_j, X) + S_{reg}^{j \rightarrow j}(E_j, X)$$

Under assumption that X dependence of fluxes factorizes from E dependence, analytical approximated solutions in terms of Z -moments:

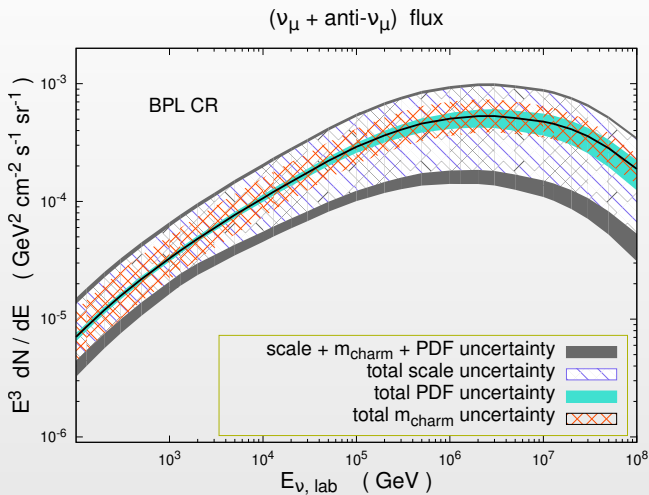
– **Particle Production:**

$$S_{prod}^{k \rightarrow j}(E_j, X) = \int_{E_j}^{\infty} dE_k \frac{\phi_k(E_k, X)}{\lambda_k(E_k)} \frac{1}{\sigma_k} \frac{d\sigma_{k \rightarrow j}(E_k, E_j)}{dE_j} \sim \frac{\phi_k(E_j, X)}{\lambda_k(E_j)} Z_{kj}(E_j)$$

– **Particle Decay:**

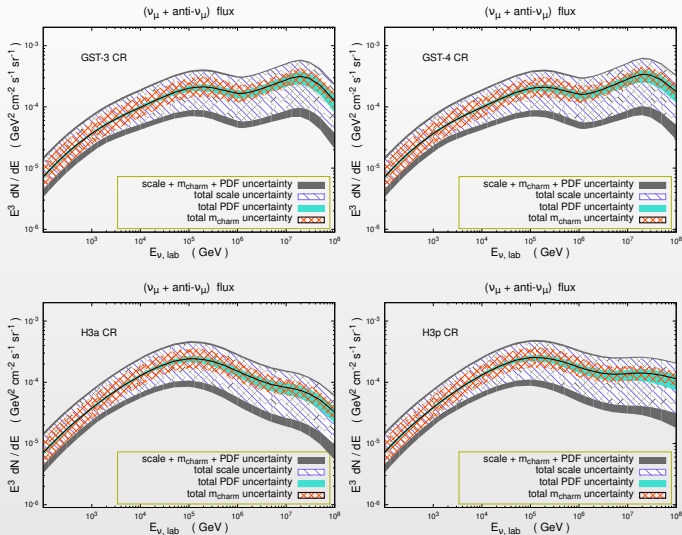
$$S_{decay}^{j \rightarrow l}(E_l, X) = \int_{E_l}^{\infty} dE_j \frac{\phi_j(E_j, X)}{\lambda_j(E_j)} \frac{1}{\Gamma_j} \frac{d\Gamma_{j \rightarrow l}(E_j, E_l)}{dE_l} \sim \frac{\phi_j(E_l, X)}{\lambda_j(E_l)} Z_{jl}(E_l)$$

PROSA 2019 atmospheric prompt ($\nu_\mu + \bar{\nu}_\mu$) flux: QCD scale, mass and PDF uncertainties



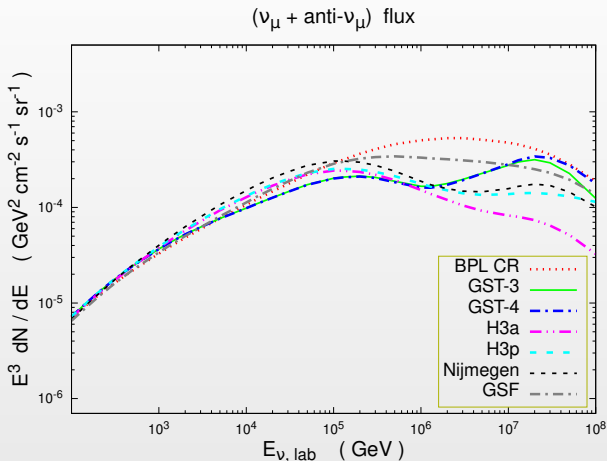
PDF uncertainty subdominant, assuming extrapolation at $x < 10^{-6}$ works.

Prompt neutrino flux uncertainties:



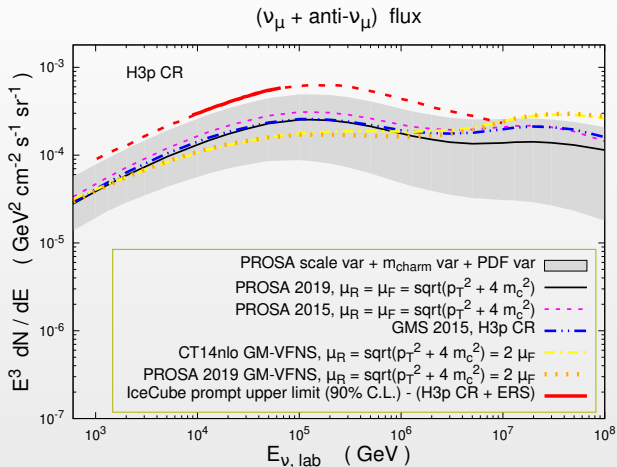
* Panels differ for different assumptions in CR composition.

PROSA prompt ($\nu_\mu + \bar{\nu}_\mu$) fluxes with different CR primary all-nucleon fluxes



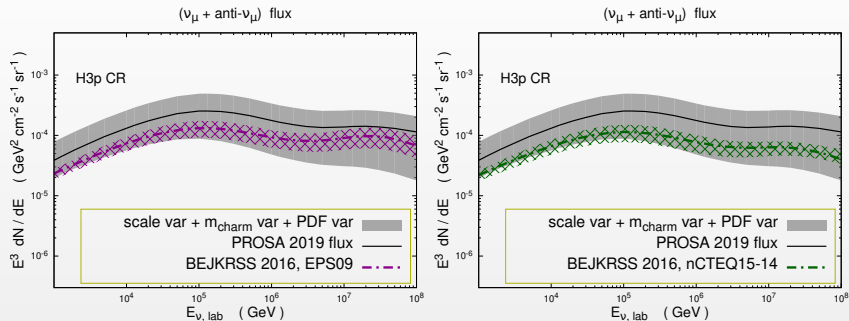
* Uncertainty in CR composition turns out to be smaller than QCD scale uncertainties.

Prompt neutrino fluxes: theoretical predictions vs. IceCube upper limits



IceCube upper limit on prompt fluxes from the 6-year analysis of thoroughgoing μ tracks from the Northeast Hemisphere [arXiv:1607.08006] assumed the ERS flux as a basis for modelling prompt neutrinos (reweighted to the H3p CR flux).

Nuclear PDFs and prompt neutrino fluxes



- * Bhattacharya et al. 2016, produce predictions by using nuclear PDFs, instead of nucleon PDFs + superposition model
→ their prompt fluxes look suppressed with respect to their older ones.
- * However, still compatible with our predictions on the basis of nucleon PDFs + superposition model.
- * Uncertainty on these nuclear PDF fits are probably underestimated.

Conclusions

- * Open charm and bottom data have the potentiality to constrain gluon and sea quark PDF at various x values.
- * At present experimental uncertainties smaller than theoretical ones.
- * Theory predictions (and PDF fits) plagued by large scale uncertainty.
- * Incorporation in PDF fits so far limited to very few cases (PROSA 15, recent NNPDF variants, PROSA 19, ABMP preliminary, nCTEQ15).
- * In order to use open charm and bottom data in PDF fits: information on bin-to-bin correlations for each separate measurement as well as between different measurements (charm and beauty, and different center of mass energies) is necessary. Information of correlations between integrated cross-sections is not enough.
- * Notwithstanding the uncertainties, the compatibility of the gluon distribution from the fits including these data is remarkable.