

$$\Omega_{2d}^{(\ell-1)}(z, \bar{z}) = \hat{H}_{2d} \Omega_{2d}^{(\ell-2)}(z, \bar{z})$$