

$$\Omega(\ell-1)(p,k) \equiv \text{Id}(\ell-2)(p,k)$$