

$$F(z) = \mathcal{L}_{10101}(z) + 2\zeta_2 \left(\mathcal{L}_{1000}(z) + \mathcal{L}_{0001}(z) \right)$$