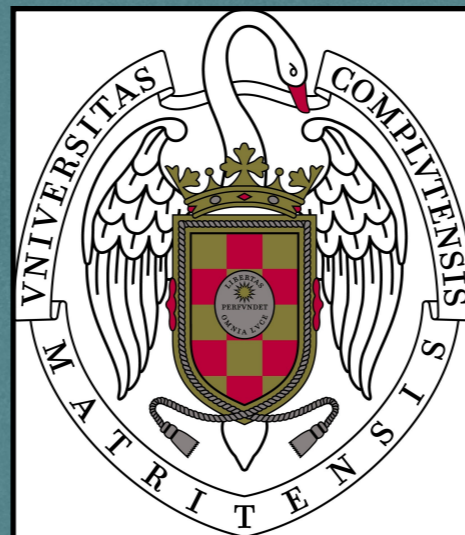


REF2019-PAVIA 25-29/11/2019

USING JETS FOR TMD SEARCH

IGNAZIO SCIMEMI

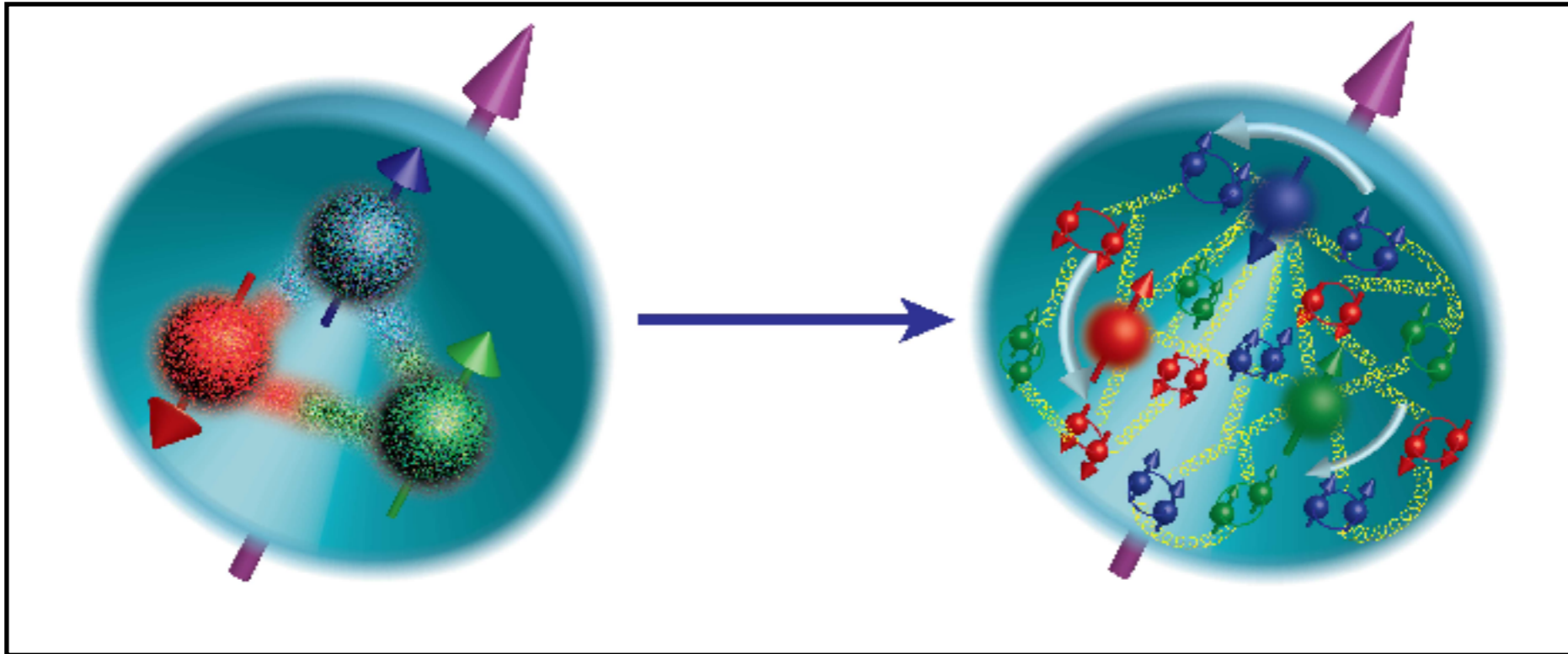
UNIVERSIDAD COMPLUTENSE DE MADRID
(UCM AND IPARCOS)



Based on :

- D. Gutierrez-Reyes, I.S., W. Waalewijn, L. Zoppi PRL 121, 162001(2018)
- D. Gutierrez-Reyes, I.S., W. Waalewijn, L. Zoppi JHEP 1910 (2019) 031
- D. Gutierrez-Reyes, Y. Makris, I.S., V. Vaidya, L. Zoppi JHEP 1908 (2019) 161

The study of the hadron structure is (again) a hot topic

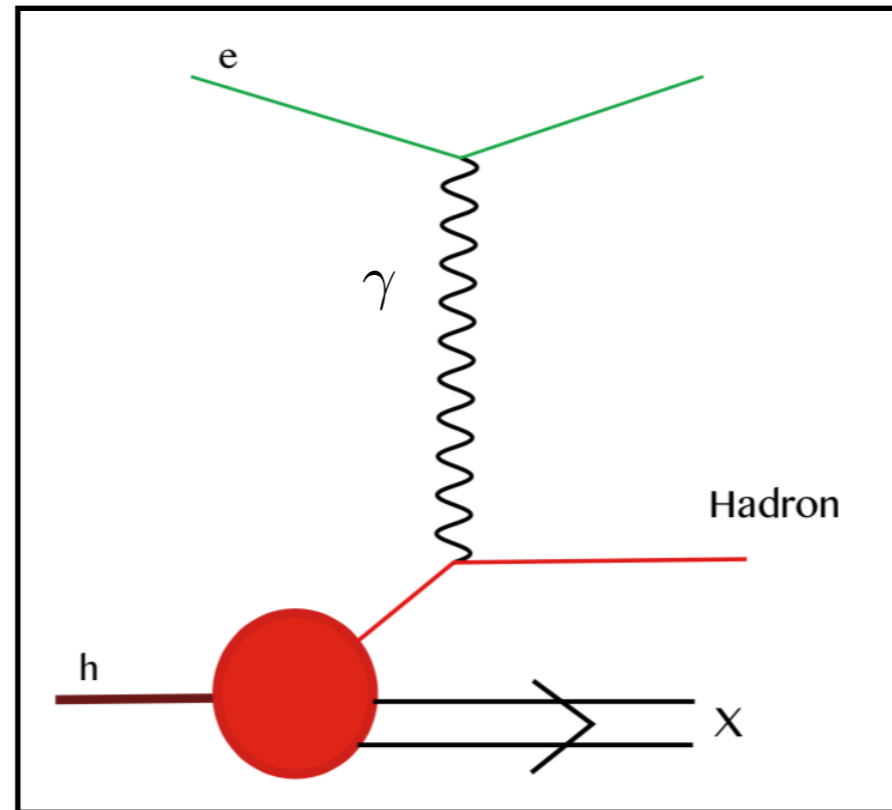


The 3D mapping of hadrons is still challenging...



Let us use **jets** to investigate hadron structure!

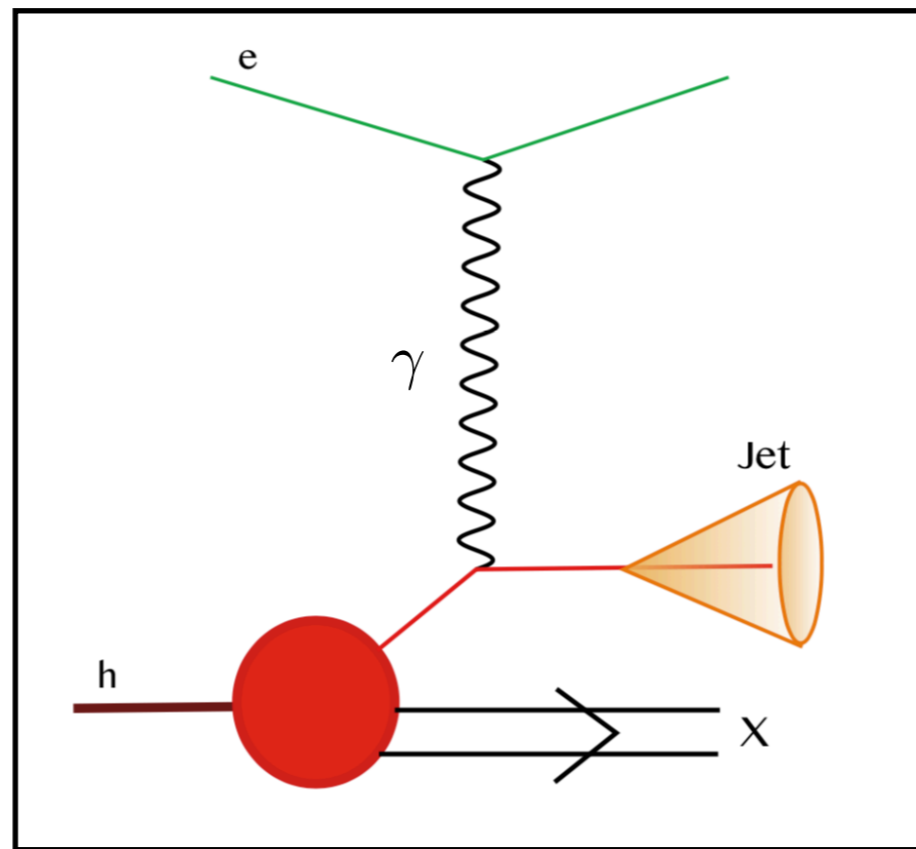
TMDS WITHOUT JETS



Factorization theorem for **SIDIS**

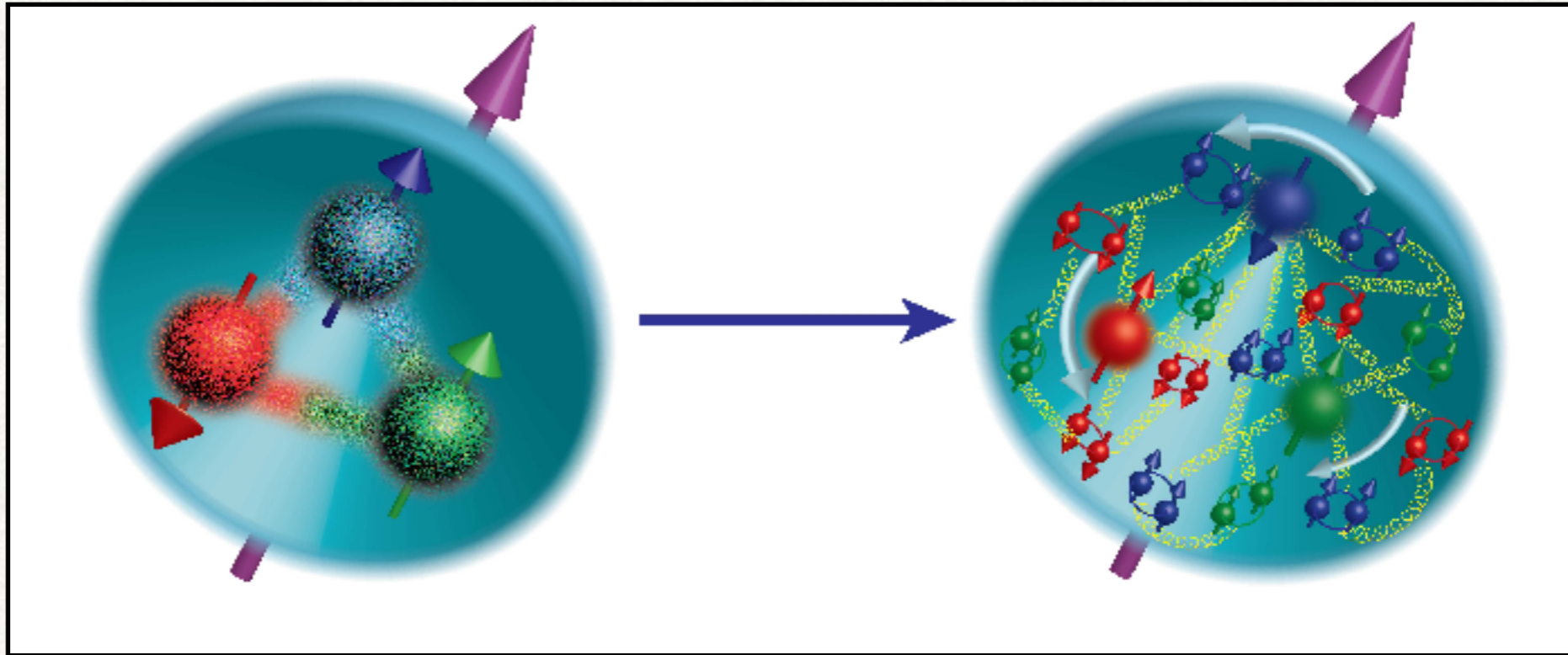
$$\frac{d\sigma_{eN \rightarrow eN'X}}{dQ^2 dx dz d\mathbf{q}} = \sum_a \mathcal{H}_a(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} \underbrace{f_{a/N}(x, \mathbf{b}, \mu, \zeta)}_{\text{TMDPDF}} \underbrace{d_{a/N'}(z, \mathbf{b}, \mu, \zeta)}_{\text{TMDFF}}$$

TMDS WITH JETS



Factorization theorem for **SIDIS**

$$\frac{d\sigma_{eN \rightarrow eJX}}{dQ^2 dx dz d\mathbf{q}} = \sum_a \mathcal{H}_a(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} \underbrace{f_{a/N}(x, \mathbf{b}, \mu, \zeta)}_{\text{TMDPDF}} \underbrace{J_q^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta)}_{\text{TMD jet function}}$$



We want to study the non-perturbative part of the evolution kernel:
 We consider the possibility to reduce non-perturbative effects in final states using jets.

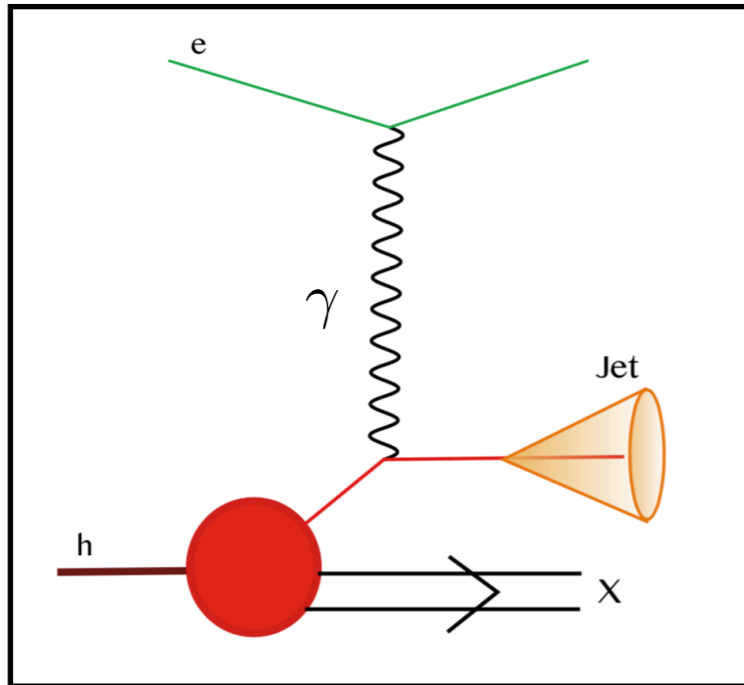
In SIDIS
 With a jet:

$$\frac{d\sigma}{dQ^2 dx dz dq_T^2} = \sigma_0 \sum_{f_1, f_2} \int \frac{d^2\mathbf{b}}{4\pi} e^{i\mathbf{b}\cdot\mathbf{q}_T} \{R[\mathbf{b}; (Q, Q^2)]\}^2 F_{f_1 \leftarrow h}(x, \mathbf{b}) J_{f_2 \rightarrow J}(z, \mathbf{b})$$

In DY:

$$\frac{d\sigma}{dQ^2 dy dq_T^2} = \sigma_0 \sum_{f_1, f_2} \int \frac{d^2\mathbf{b}}{4\pi} e^{i(\mathbf{b}\cdot\mathbf{q}_T)} H_{f_1 f_2}(Q, Q) \{R[\mathbf{b}; (Q, Q^2)]\}^2 F_{f_1 \leftarrow h_1}(x_1, \mathbf{b}) F_{f_2 \leftarrow h_2}(x_2, \mathbf{b}).$$

TMDs WITH JETS



Questions:

Can we write TMD factorization theorems for processes with jets?

Can we write factorization theorems for jets regardless of the size of the jet?

Non-perturbative effects for jets are in principle more suppressed than for nuclear TMDs!

This would be a clean channel to measure non-perturbative effects in the initial nucleon

Hadronization effects should be considered (ungroomed/groomed jets)

OUTLINE

- **Building** a jet
 - Radius and jet algorithms
 - Jet axis
- TMD factorization
- Factorization: **ungroomed/groomed jets**. Phenomenology
 - **Ungroomed jets**: Factorization for dijet decorrelation and SIDIS processes
 - **Groomed jets**: Factorization for dijet decorrelation and SIDIS processes
- Conclusions

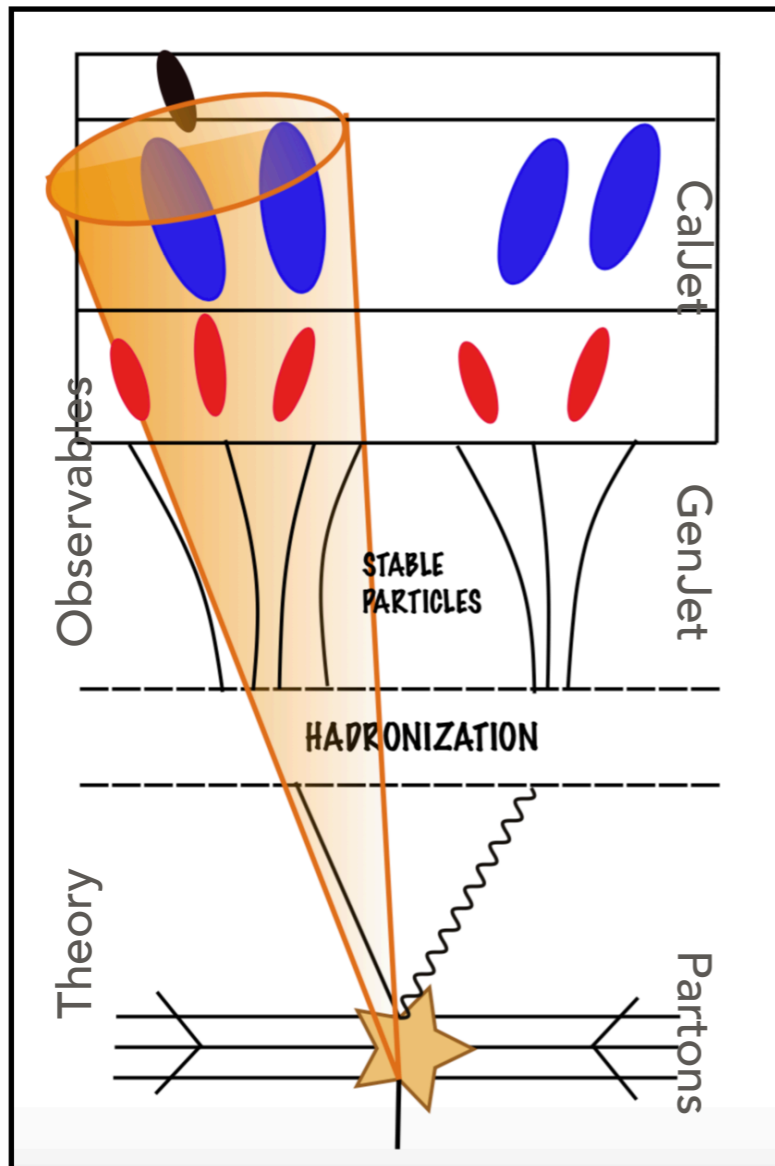
JETS

RADIUS AND JET ALGORITHMS

Standard kt-type algorithms

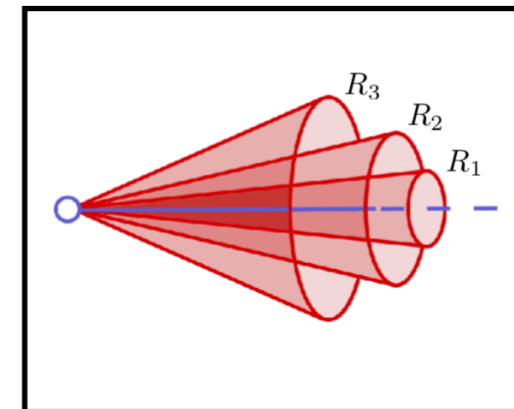
$$d_{ij} = \min(k_{T,1}^{2w}, k_{T,2}^{2w}) \frac{\Delta R_{ij}}{R}$$

$$w \in \{-1, 0, 1\}$$

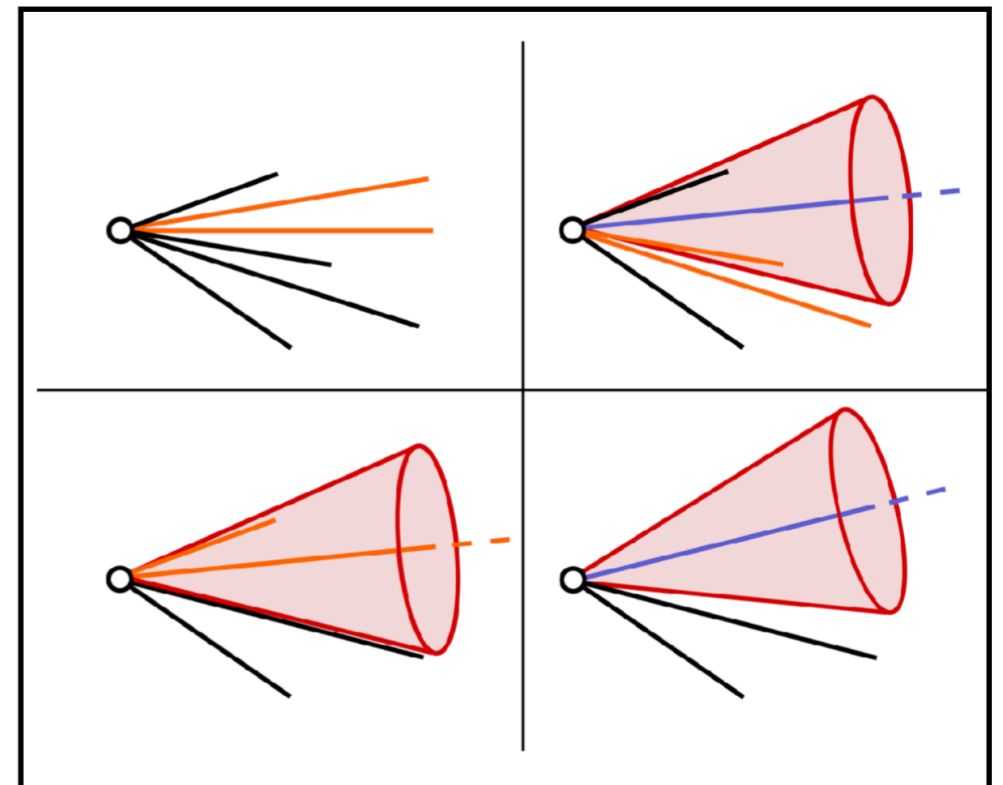


Building a jet...

Step 1:
Set a size
(Radius)



Step 2:
Run a jet
algorithm



JET AXIS

Larkoski, Neill, Thaler '14
arXiv: 1401.2158

Standard jet axis (SJA)

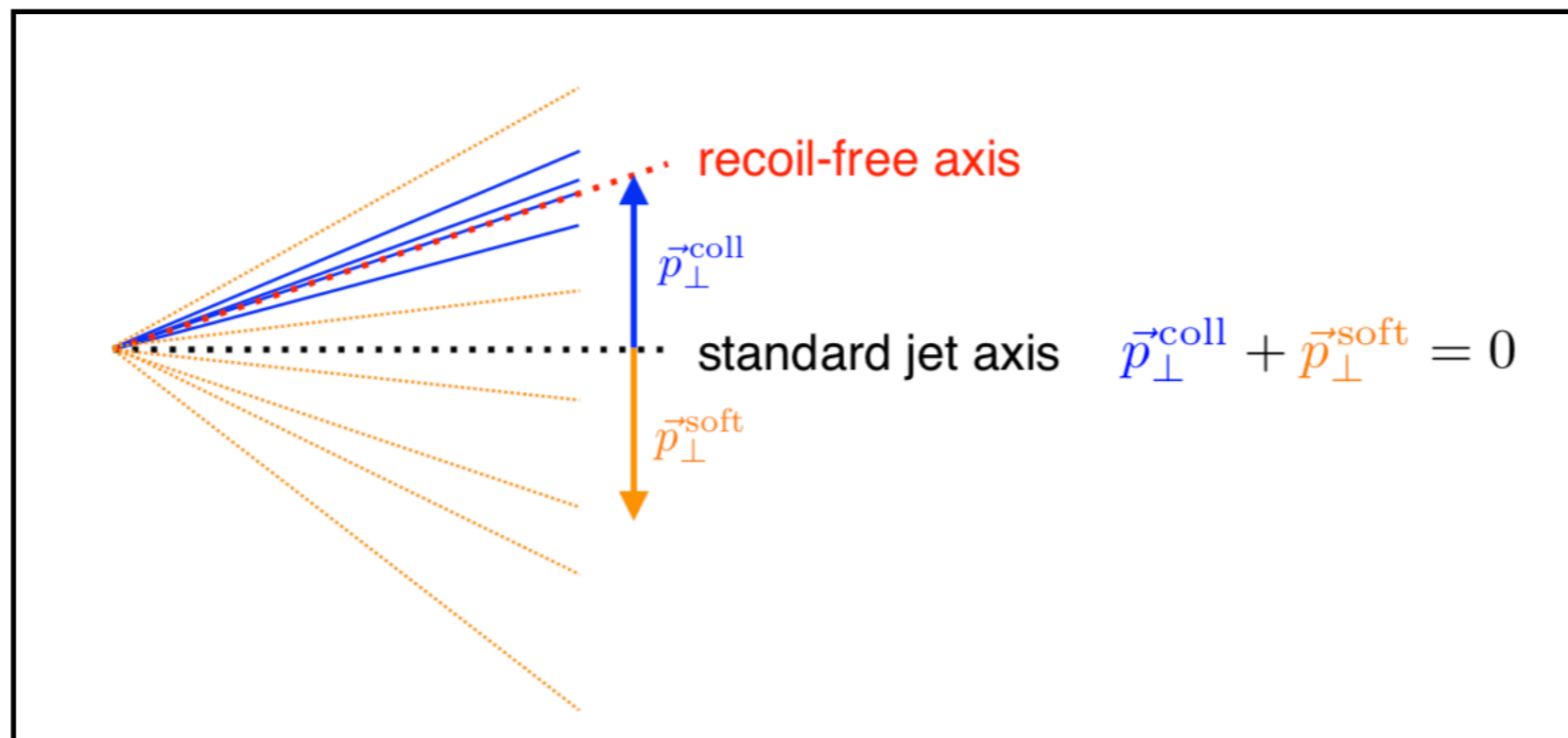
The sum of the momentum of collinear and soft particles is zero

Introduces soft-sensitivity to the axis definition. Important with unintegrated transverse momentum

Winner-take-all (WTA)

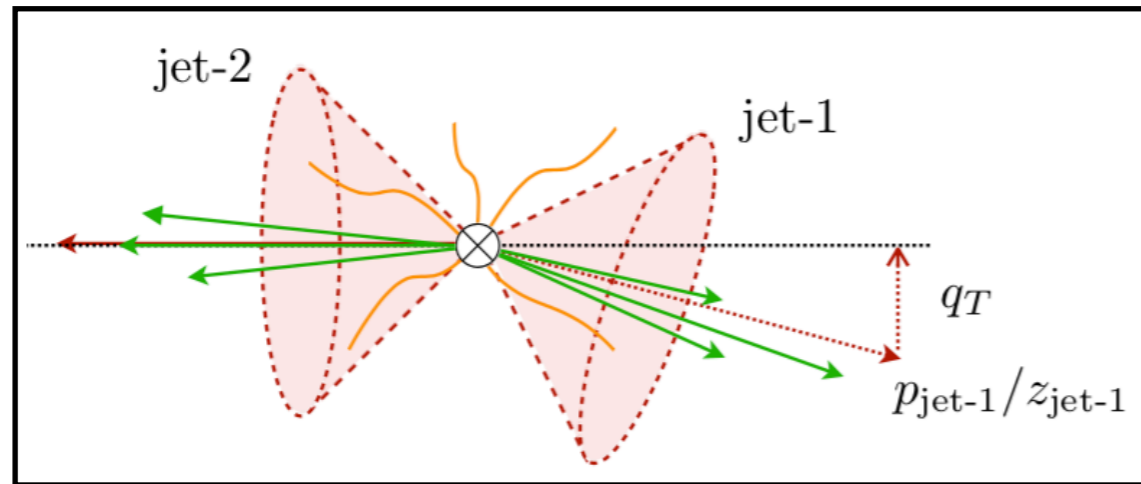
It always follows the direction of the most energetic particle

Recoil invariant. It is not sensitive to soft radiation

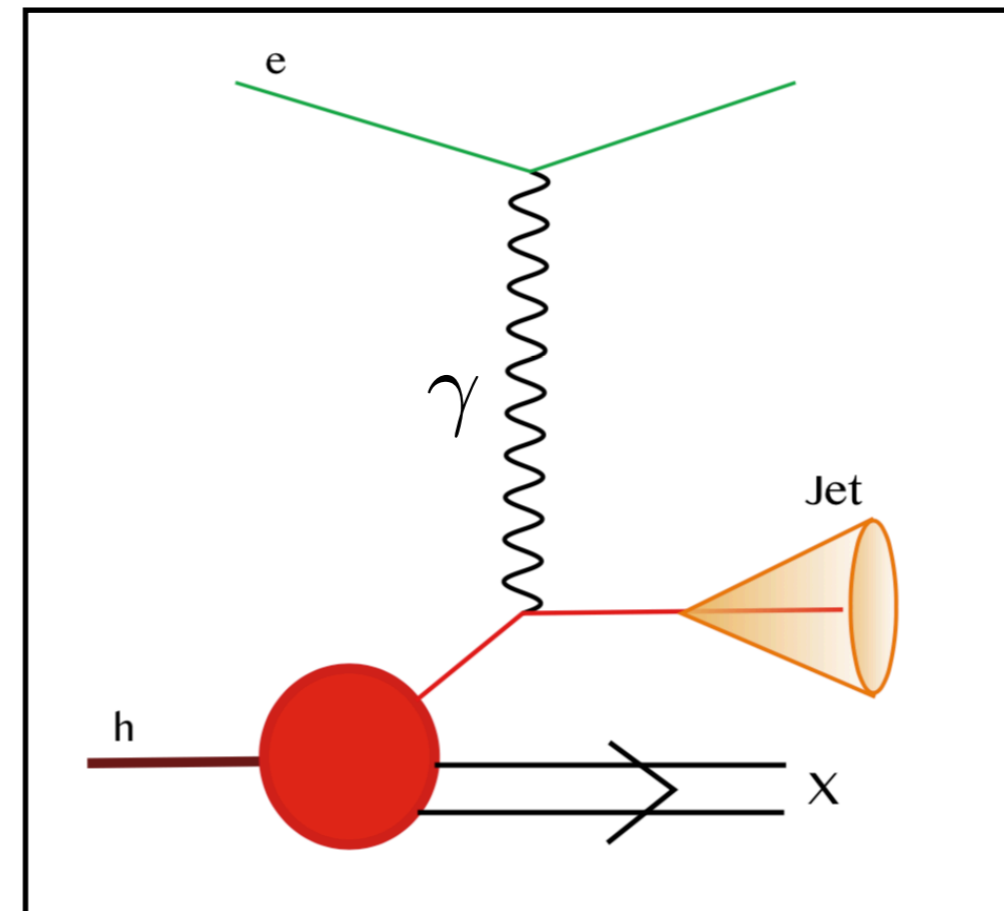


INTERESTING PROCESSES TO FACTORIZE

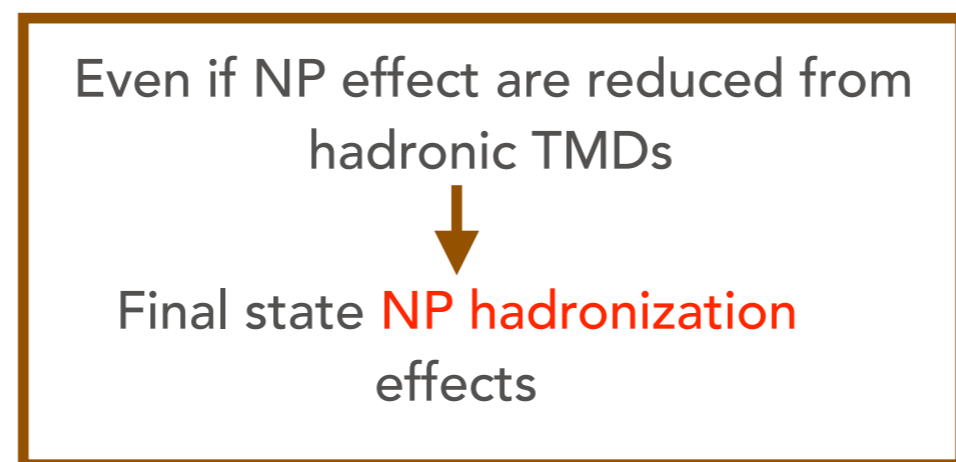
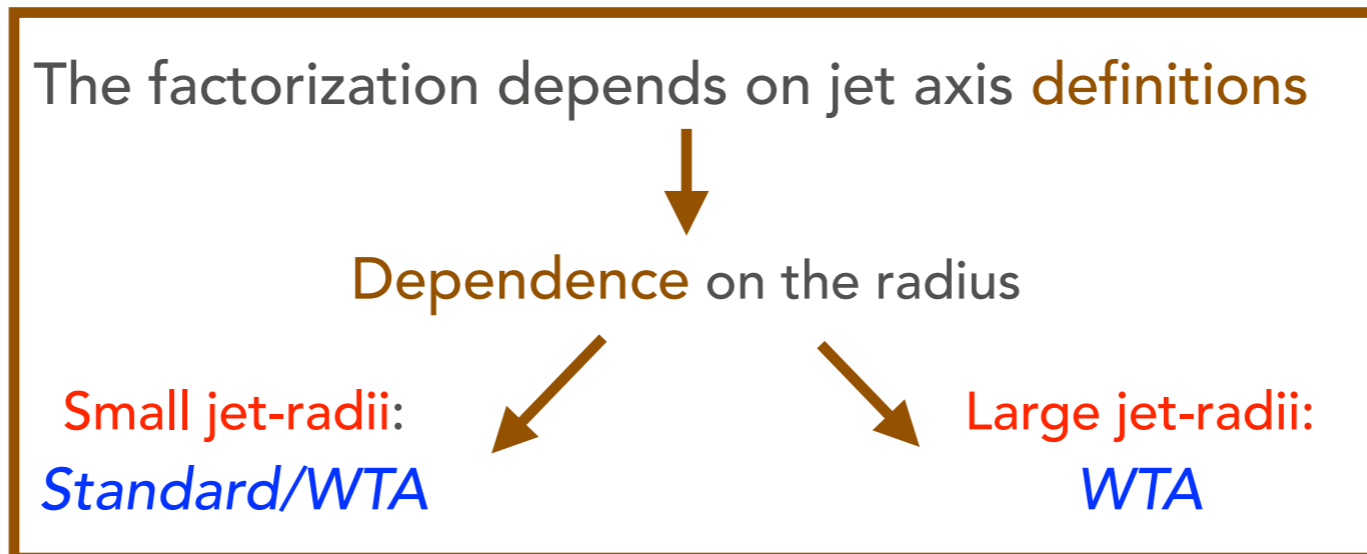
$$e^+ e^- \rightarrow \text{dijet} + X$$



SIDIS with jet



UNGROOMED JETS



GROOMED JETS

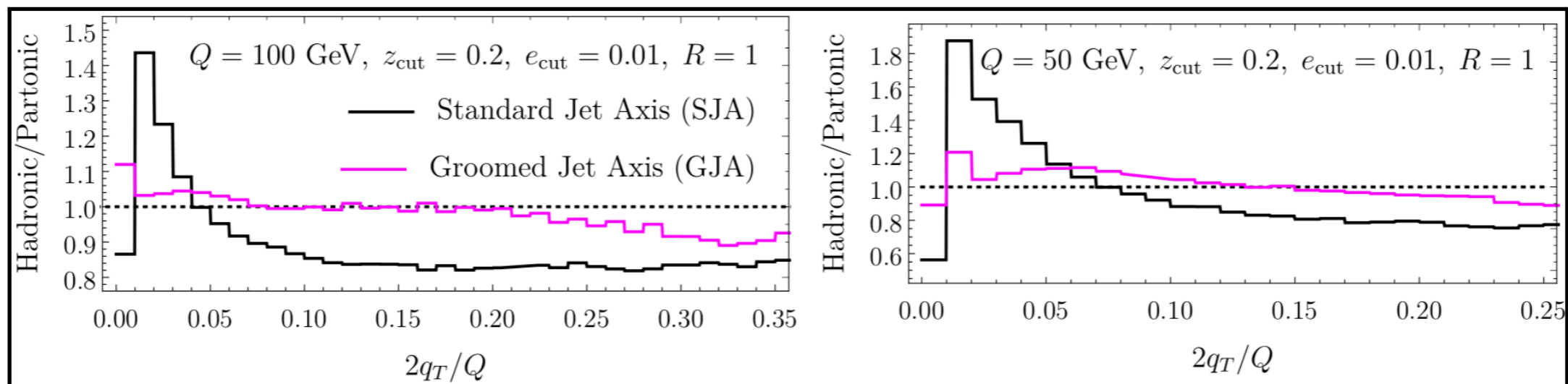
SOFT-DROP : Removes large angle (soft) radiation

1. **Construction** an angular tree of the jet
2. **Removal** of branches that fail an energy requirement

Only narrow energetic **core remains** from the original jet



NP hadronization effects are highly reduced!



FACTORIZATION: UNGROOMED JETS

FACTORIZATION: UNGROOMED JETS

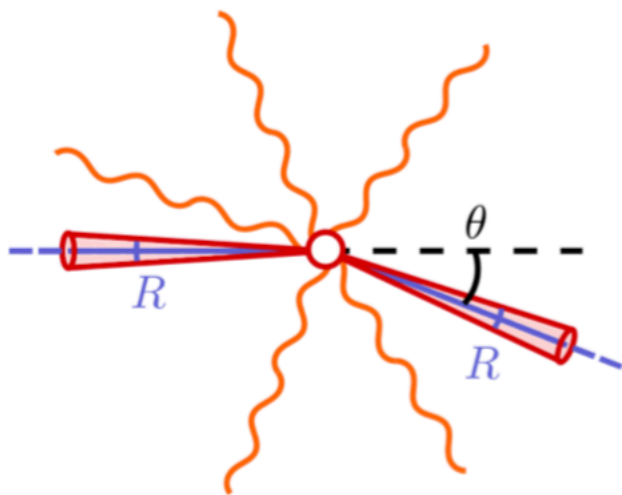
Dijet decorrelation

$$e^+e^- \rightarrow \text{dijet} + X$$

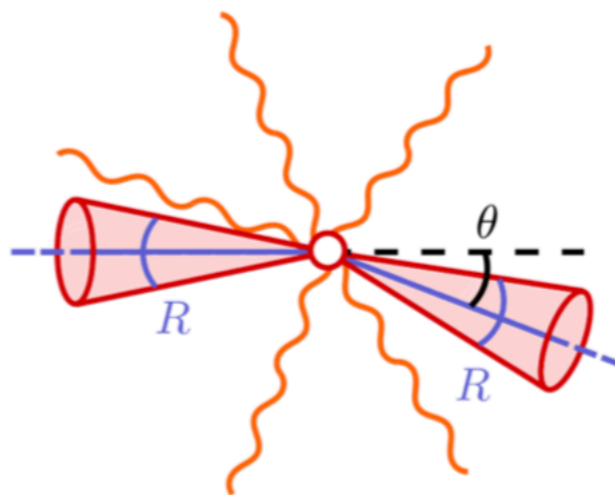
$$\mathbf{q} = \frac{\mathbf{p}_1}{z_1} + \frac{\mathbf{p}_2}{z_2} \quad \text{competes with } R$$
$$\theta \approx \tan \theta = 2|\mathbf{q}|/Q$$

In all cases

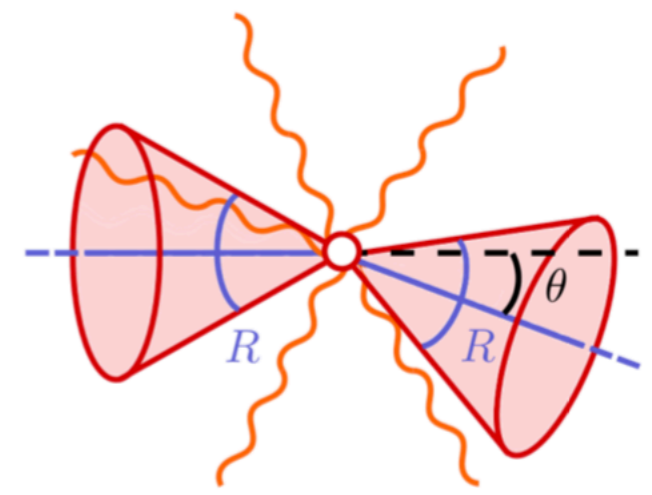
$$\theta \ll 1$$



$$\theta \gg R$$



$$\theta \sim R$$



$$\theta \ll R$$

FACTORIZATION: UNGROOMED JETS

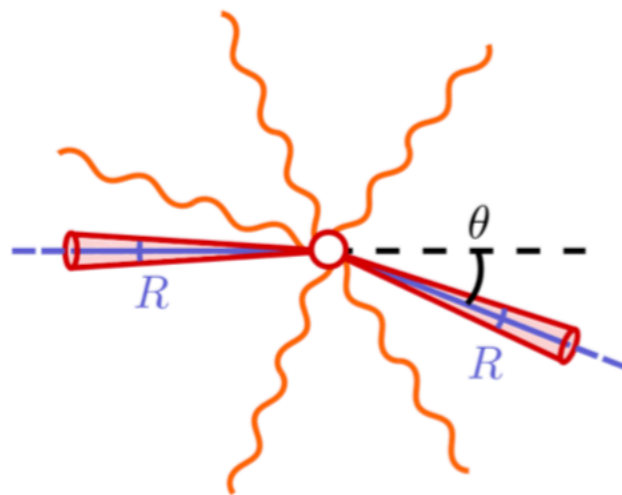
Dijet decorrelation

$$e^+e^- \rightarrow \text{dijet} + X$$

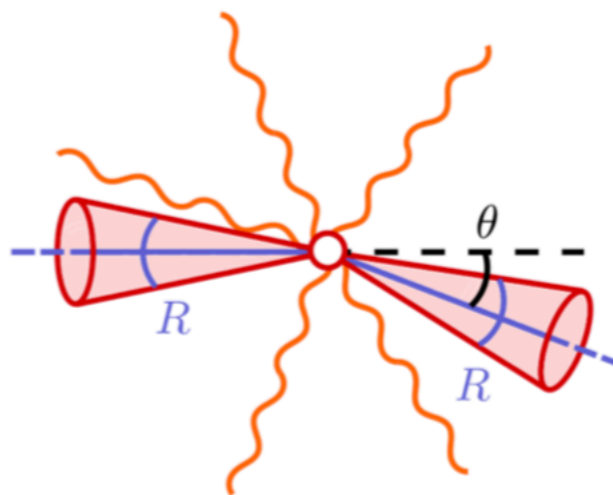
$$q = \frac{p_1}{z_1} + \frac{p_2}{z_2} \text{ competes with } R$$
$$\theta \approx \tan \theta = 2|q|/Q$$

In all cases

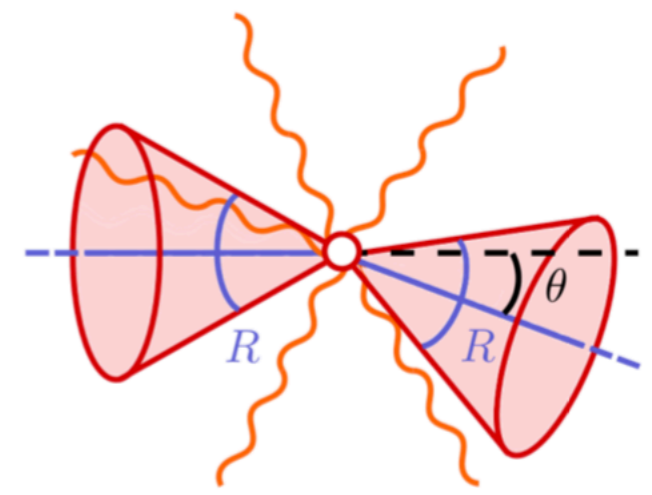
$$\theta \ll 1$$



$$\theta \gg R$$



$$\theta \sim R$$

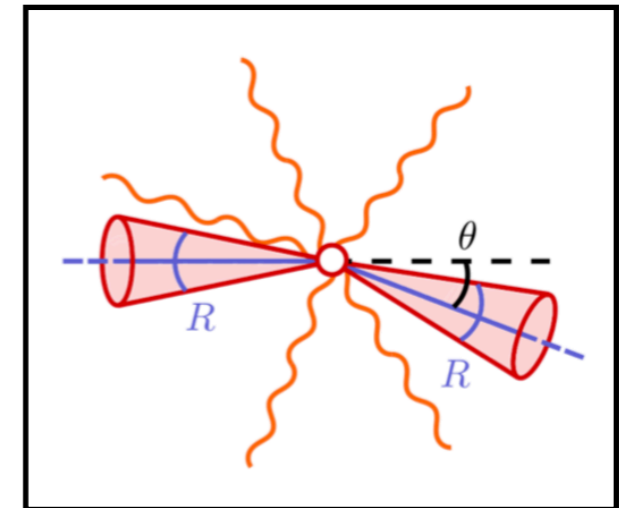


$$\theta \ll R$$

Most interesting case for
current and future experiments!

FACTORIZATION: UNGROOMED JETS

$$\theta \sim R \ll 1$$



$$\frac{d\sigma_{ee \rightarrow JJX}}{dz_1 dz_2 d\mathbf{q}} = H(s, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} J_q^{\text{axis}} \left(z_1, \mathbf{b}, \frac{\sqrt{s}}{2} R, \mu, \zeta_1 \right) J_q^{\text{axis}} \left(z_2, \mathbf{b}, \frac{\sqrt{s}}{2} R, \mu, \zeta_2 \right) \left[1 + \mathcal{O} \left(\frac{q^2}{s} \right) \right]$$



$$J_q^{\text{axis}} = \frac{z}{2N_c} \sum_X \text{Tr} \left\{ \frac{\not{n}}{2} \langle 0 | \delta(\bar{n} \cdot p_J / z - \bar{n} \cdot P) e^{-i\mathbf{b}\mathbf{P}_\perp} \chi_n(0) | J_{\text{alg}, R}^{\text{axis}} X \rangle \langle J_{\text{alg}, R}^{\text{axis}} X | \bar{\chi}_n(0) | 0 \rangle \right\}$$

TMD semi-inclusive
Jet function



$$J_i^{\text{axis}} = \sum_j \int \frac{dz'}{z'} [(z')^2 \mathbb{C}(z', \mathbf{b}, \mu, \zeta)] \mathcal{J}_i \left(\frac{z}{z'}, \frac{\sqrt{s}}{2} R, \mu \right) \left[1 + \mathcal{O}(b^2 s^2 R^2 / 4) \right]$$

Refactorized!
 $R \ll \theta \ll 1$

NNLO TMDFFs Coefficients
Echevarría, Scimemi, Vladimirov `16



Coll. jet Function
Kang, Ringer, Vitev `16
arXiv:1606.06732

The wide angle soft radiation does not resolve individual collinear emissions in the jet

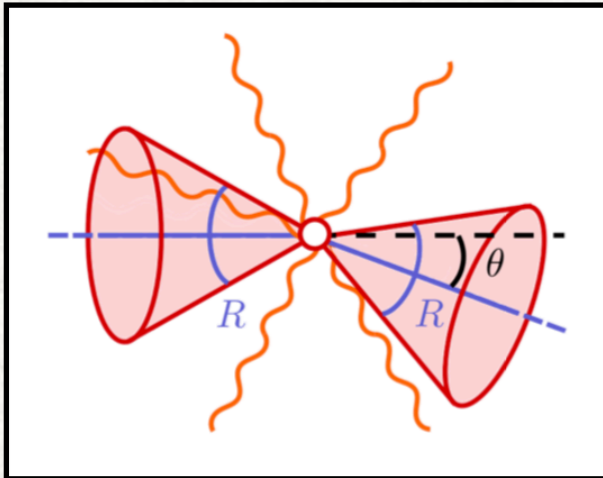


The soft function is the same
Than that for TMD fragmentation

FACTORIZATION: UNGROOMED JETS

$$\theta \ll 1 \quad \theta \ll R$$

WTA axis



The soft radiation does resolve the jet boundary, but this fact does not affect to the position of the axis



No distinction between soft radiation inside and outside the jet!



TMD Soft function is conserved!
And factorization holds!

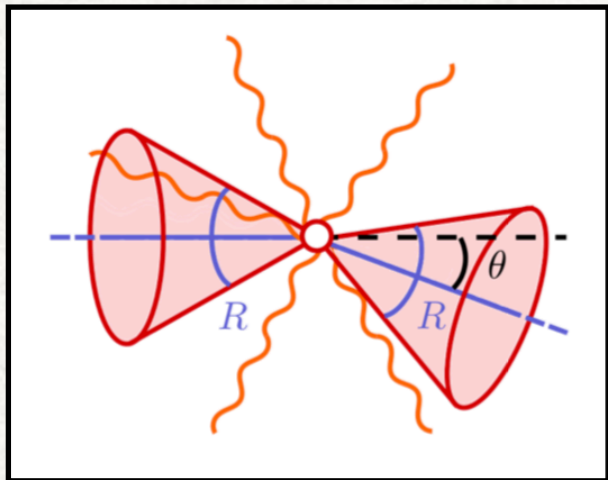
**The factorization with WTA
Works for every R!**

$$\frac{d\sigma_{(ee \rightarrow JJX)}^{\text{WTA}}}{dz_1 dz_2 dq} = H \int \frac{d\mathbf{b}}{(2\pi)^2} J_q^{\text{WTA}}(z_1, \mathbf{b}) J_q^{\text{WTA}}(z_2, \mathbf{b})$$

FACTORIZATION: UNGROOMED JETS

$$\theta \ll 1 \quad \theta \ll R$$

Standard Jet Axis



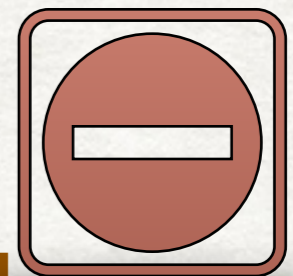
The SJA is aligned with the total momentum of the jet



Hard splittings with typical angle R are allowed inside the jet, generating additional soft radiation

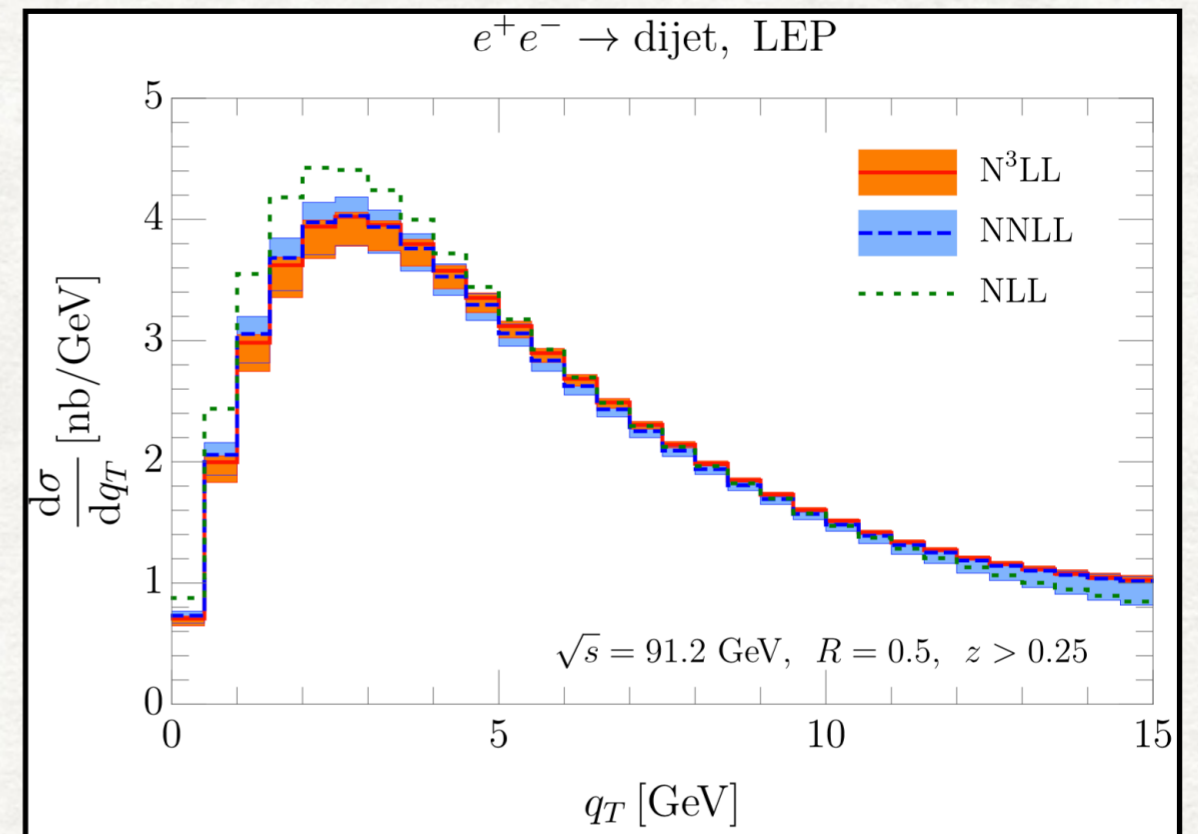
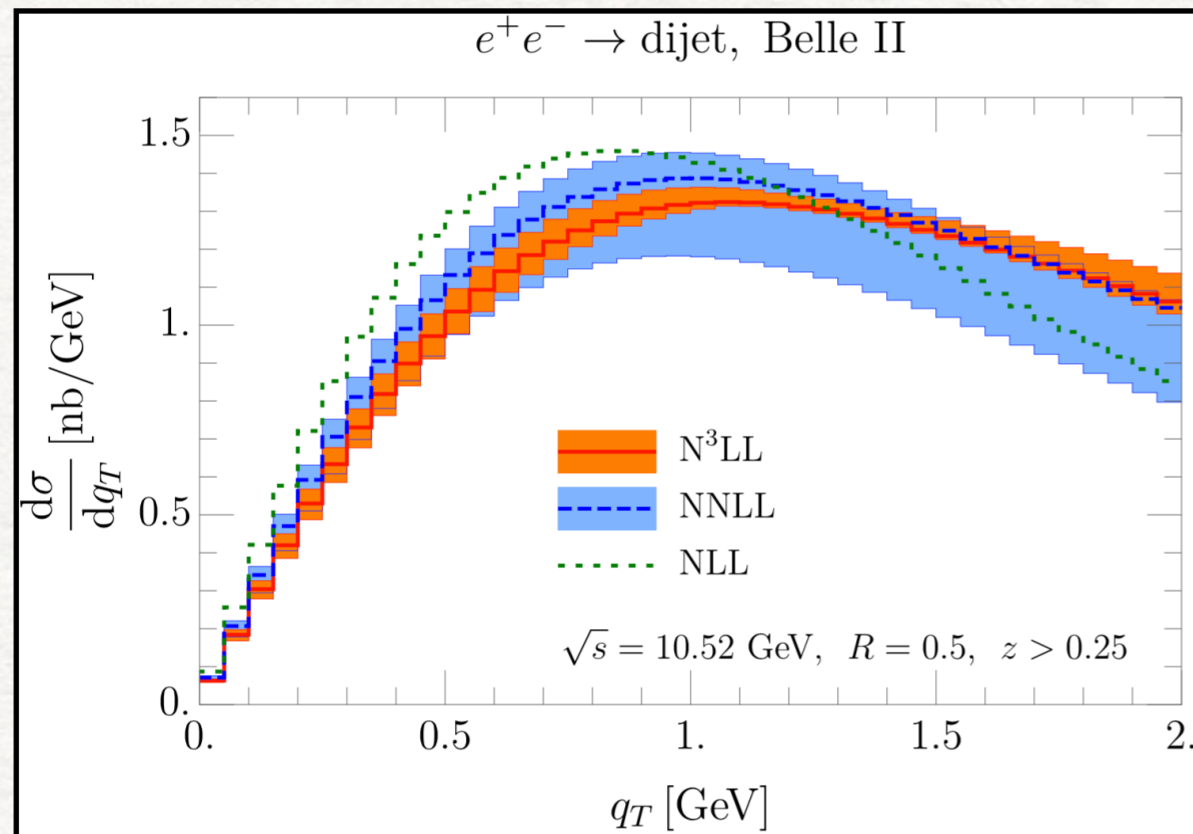


Factorization broken!



$$\frac{d\sigma_{(ee \rightarrow JJX)}^{\text{SJA}}}{dq} = \sum_{m=2}^{\infty} \text{Tr}_c [\mathcal{H}_m(\{n_i\}) \otimes \mathcal{S}_m(\mathbf{q}, \{n_i\})]$$

PERTURBATIVE CONVERGENCE: LARGE RADIUS



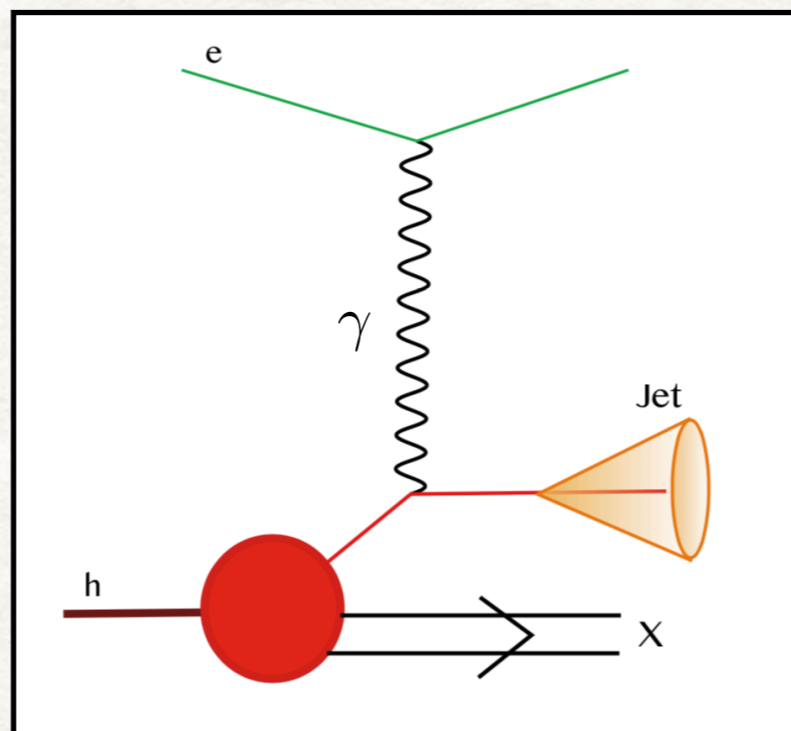
As the large- R jet function does not depend on radius or z , we can predict the two loop jet function by **RG + Numerical constant (Event2)**

We use an improved NLO + NNLO large- R jet functions
Resummation up to **N3LL!**

Theoretical errors are **reduced** when the perturbative order is increased!

FACTORIZATION: UNGROOMED JETS SIDIS

Factorization in **SIDIS with a jet** is analogous to the one already studied!

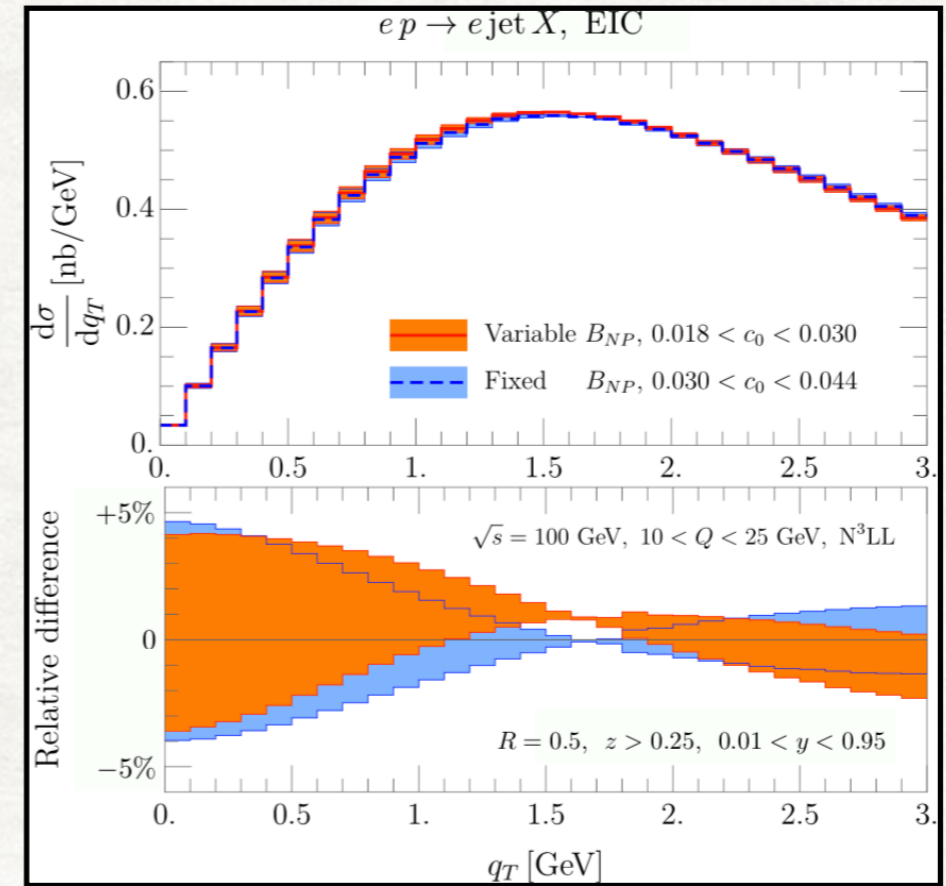
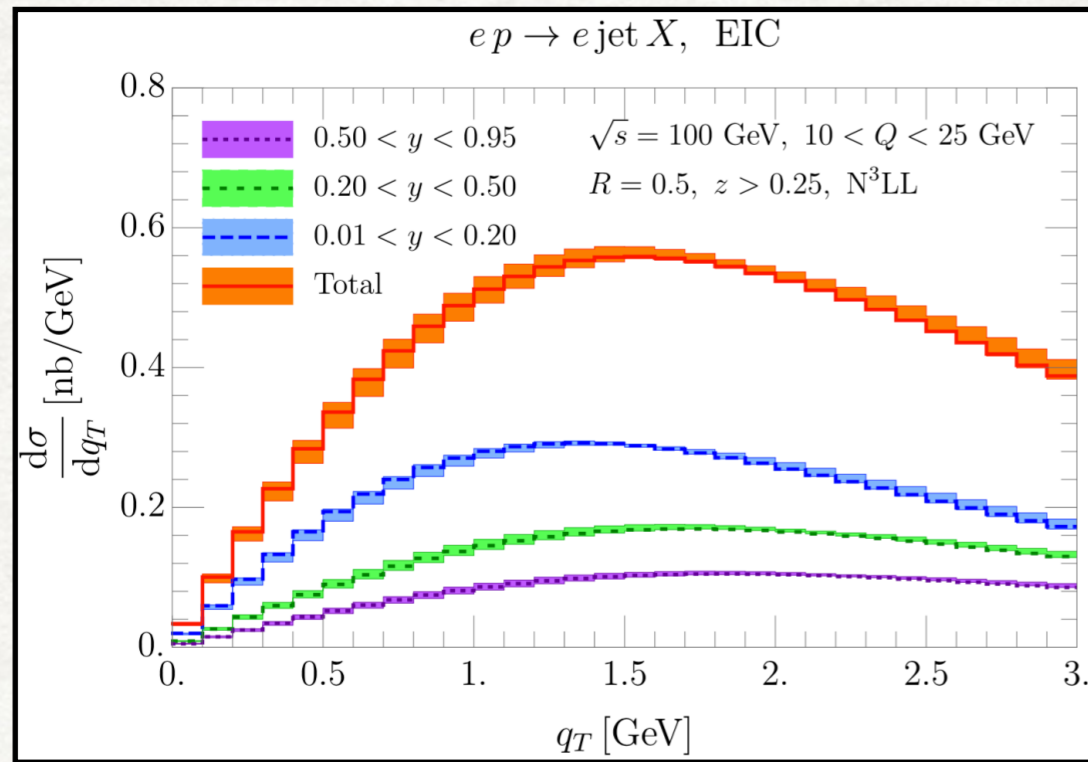


Factorization for **SIDIS with jet** in hadron/jet Breit frame

$$\frac{d\sigma_{eN \rightarrow eJX}}{dQ^2 dx dz d\mathbf{q}} = \sum_a \mathcal{H}_a(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} \underbrace{f_{a/N}(x, \mathbf{b}, \mu, \zeta)}_{\text{TMDPDF}} \underbrace{J_q^{\text{axis}}(z, \mathbf{b}, QR/2, \mu, \zeta)}_{\text{TMD jet function}}$$

It has **dependence on the jet radius**. For all R we use WTA axis

PHENO RESULTS FOR SIDIS WITH UNGROOMED JET



We include an effect of the two-loop jet function

Most of the cross section comes from low elasticity region

Theoretical errors from the Hard scale and the OPE scale are shown and are small

Non perturbative model for the TMDPDF taken from Bertone, Scimemi, Vladimirov `19
arXiv:1902.08474

$$f_{NP}(x, \mathbf{b}) = \exp \left(- \frac{(\lambda_1(1-x) + \lambda_2 x + \lambda_3 x(1-x)) \mathbf{b}^2}{\sqrt{1 + \lambda_4 x^{\lambda_5} \mathbf{b}^2}} \right)$$

But the cross section is dominated by non-perturbative parameters of evolution (BNP, c_0)

FACTORIZATION: GROOMED JETS

FACTORIZATION: GROOMED JETS

Two extra scales
for groomed jets

Grooming parameter $\rightarrow \frac{\min\{E_i, E_j\}}{E_i + E_j} > z_{\text{cut}} \left(\frac{\theta_{ij}}{R}\right)^\beta$

Jet mass $\rightarrow e \equiv \left(\frac{m_J}{2E_J}\right)^2$

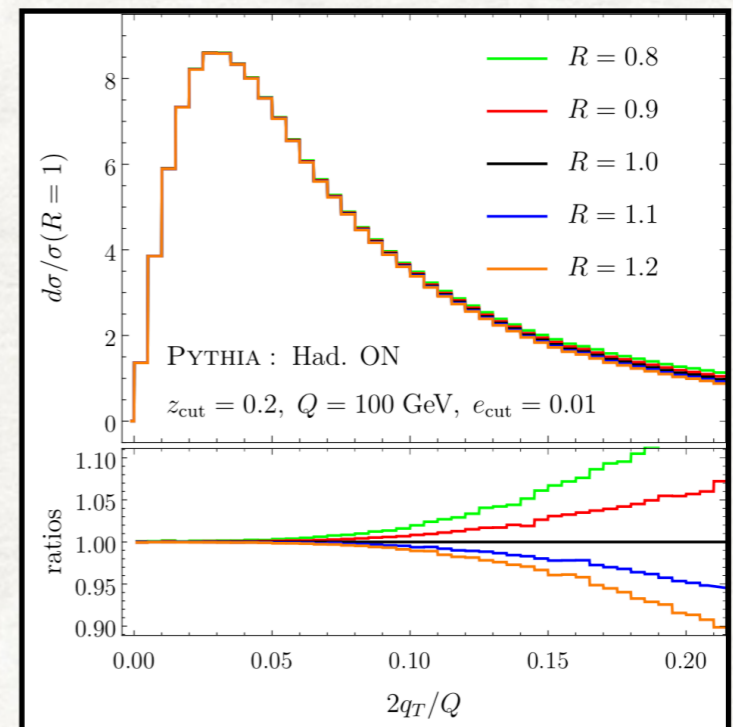
Hierarchy

$$Q \gg Qz_{\text{cut}} \gg q_T \geq Q\sqrt{e} \gg Q\sqrt{ez_{\text{cut}}}$$

Remove
contaminating
Soft radiation

Independence on
the radius

Pythia
check



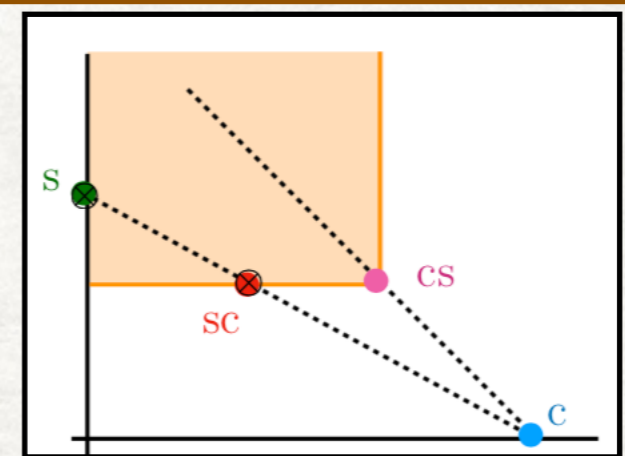
New modes in factorization!

Soft: $p_s^\mu \sim q_T(1, 1, 1)$

Collinear: $p_c^\mu \sim Q(\lambda_c^2, 1, \lambda_c), \lambda_c = \sqrt{e}$

Soft-collinear: $p_{sc}^\mu \sim Qz_{\text{cut}}(\lambda_{sc}^2, 1, \lambda_{sc}), \lambda_{sc} = q_T/(Qz_{\text{cut}})$

Collinear-soft: $p_{cs}^\mu \sim Qz_{\text{cut}}(\lambda_{cs}^2, 1, \lambda_{cs}), \lambda_{cs} = \sqrt{e/z_{\text{cut}}}$



FACTORIZATION: GROOMED JETS

The cross-section is factorized as

$$\frac{d\sigma}{de_1 de_2 d^2\mathbf{q}_T} = H^{ij}(Q; \mu) \times \mathcal{J}_i^\perp(e_1, Q, z_{\text{cut}}, \mathbf{q}_T; \mu, \zeta_A) \otimes \mathcal{J}_j^\perp(e_2, Q, z_{\text{cut}}, \mathbf{q}_T; \mu, \zeta_B)$$

Groomed jet function

$$\mathcal{J}_i^\perp(e, Q, z_{\text{cut}}, \mathbf{b}; \mu, \zeta) = \sqrt{S(\mathbf{b})} \mathcal{J}_i^\perp(e, Q, z_{\text{cut}}, \mathbf{b})$$

Soft radiation absorbed
same as TMDs

$$\zeta_A \zeta_B = Q^4 z_{\text{cut}}^4$$

Energy needed is higher!

FACTORIZATION: GROOMED JETS

The cross-section is factorized as

$$\frac{d\sigma}{de_1 de_2 d^2 \mathbf{q}_T} = H^{ij}(Q; \mu) \times \mathcal{J}_i^\perp(e_1, Q, z_{\text{cut}}, \mathbf{q}_T; \mu, \zeta_A) \otimes \mathcal{J}_j^\perp(e_2, Q, z_{\text{cut}}, \mathbf{q}_T; \mu, \zeta_B)$$

Groomed jet function

$$\mathcal{J}_i^\perp(e, Q, z_{\text{cut}}, \mathbf{b}; \mu, \zeta) = \sqrt{S(\mathbf{b})} \mathcal{J}_i^\perp(e, Q, z_{\text{cut}}, \mathbf{b})$$

Soft radiation absorbed
same as TMDs

$$\zeta_A \zeta_B = Q^4 z_{\text{cut}}^4$$

Energy needed is higher!

New modes → Refactorization!

$$\mathcal{J}_i^\perp(e, Q, z_{\text{cut}}, \mathbf{b}) = \underbrace{S_{sc,i}^\perp(Q z_{\text{cut}}, \mathbf{b})}_{\text{Soft-collinear}} \times \int de' \underbrace{S_{cs,i}(e - e', Q z_{\text{cut}})}_{\text{Collinear-soft}} \underbrace{J_i(e', Q)}_{\text{Jet}}$$

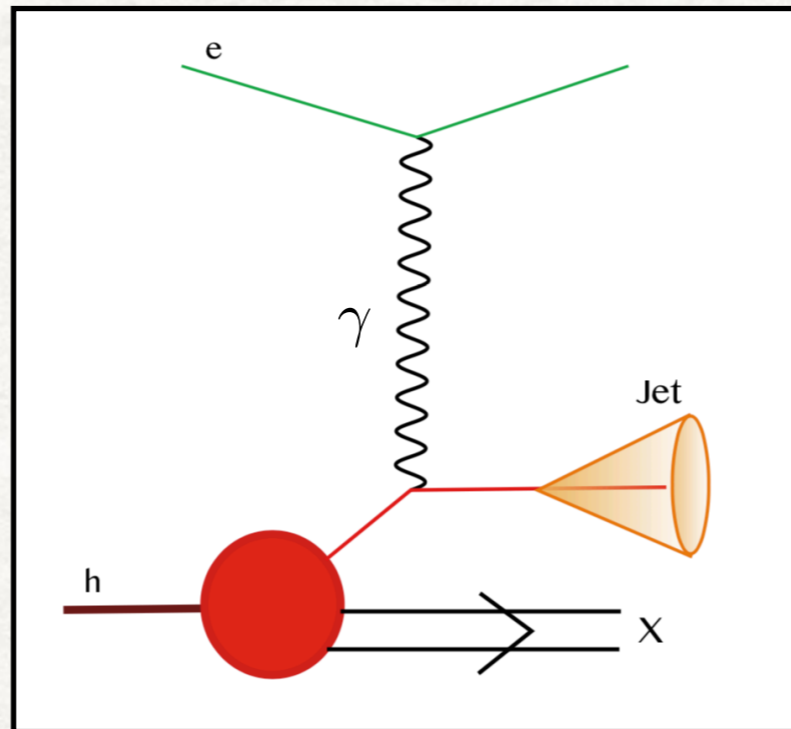
All at NLO!

Integrate parameters
as in experiments

$$\frac{d\sigma}{d^2 \mathbf{q}_T}(e_{\text{cut}}) = H^{ij}(Q; \mu) \int \frac{d^2 \mathbf{b}}{4\pi} e^{i(\mathbf{b}\mathbf{q})_T} \mathcal{J}_i^\perp(e_{\text{cut}}, Q, z_{\text{cut}}, \mathbf{b}; \mu, \zeta) \mathcal{J}_j^\perp(e_{\text{cut}}, Q, z_{\text{cut}}, \mathbf{b}; \mu, \zeta)$$

FACTORIZATION: GROOMED JETS SIDIS

Factorization in **SIDIS with a groomed jet** introduces now the groomed jet function



Factorization for **SIDIS with jet** in Breit frame

$$\frac{d\sigma_{eN \rightarrow eJX}}{dQ^2 dx dy d\mathbf{q}} = \sum_a \mathcal{H}_a(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} \underbrace{f_{a/N}(x, \mathbf{b}, \mu, \zeta)}_{\text{TMDPDF}} \underbrace{\mathcal{J}^\perp(e_{\text{cut}}, Q, z_{\text{cut}}, \mathbf{b}; \mu, \zeta)}_{\text{Groomed TMD jet function}}$$

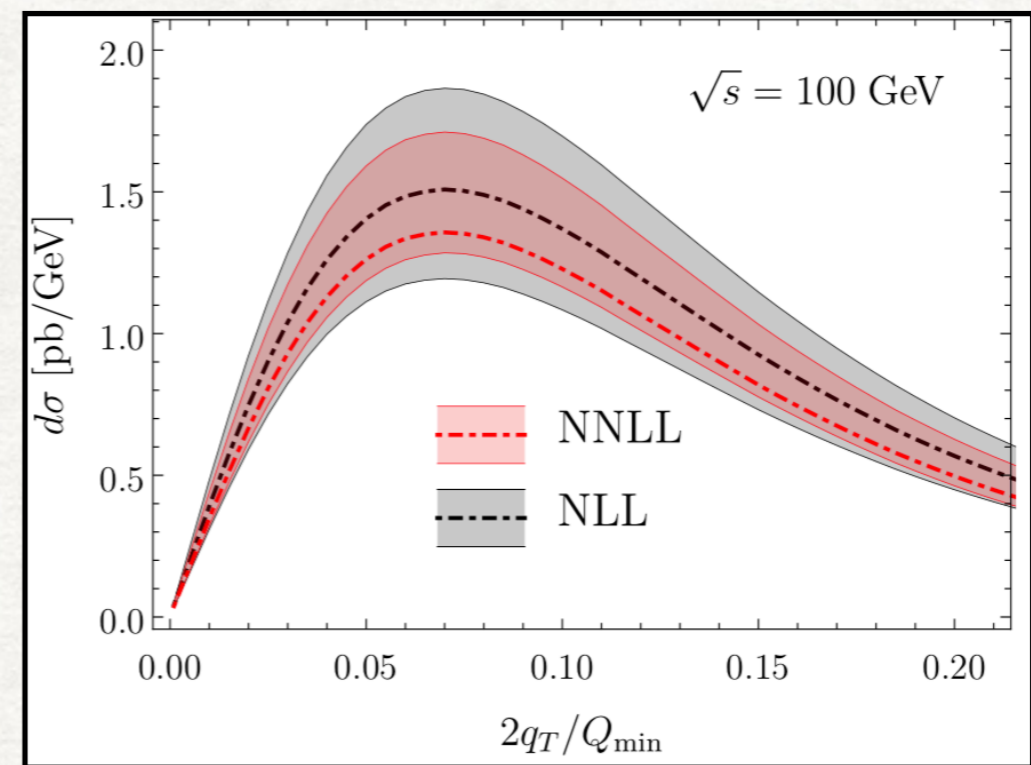
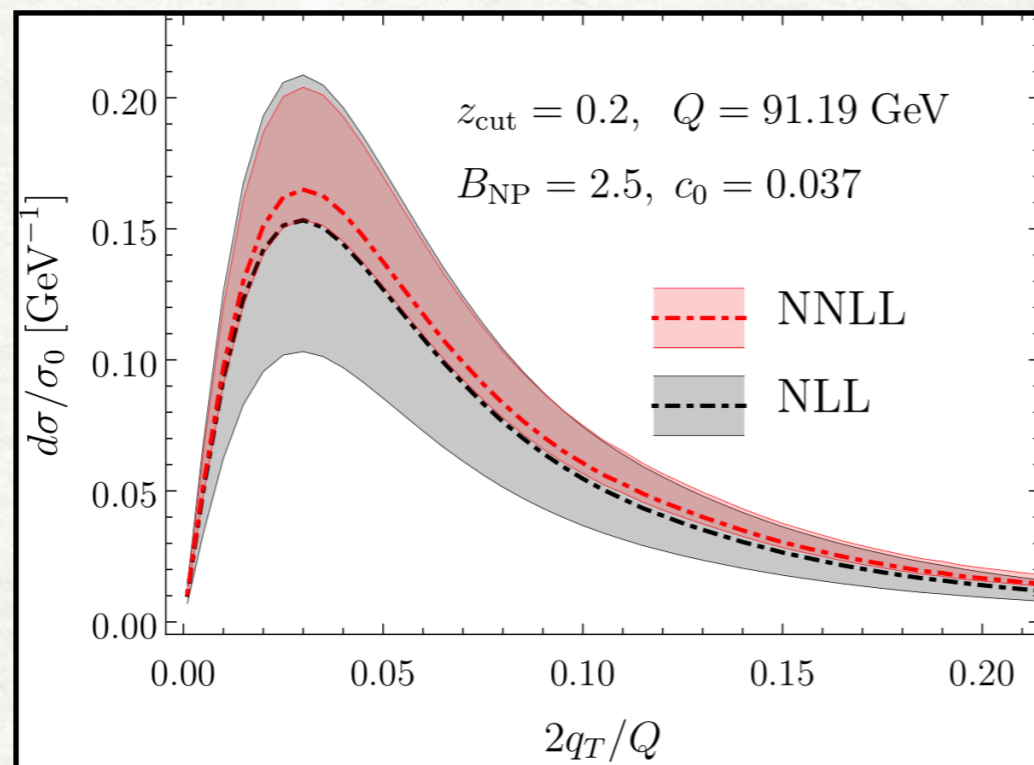
TMDPDF

Groomed
TMD jet function

PHENO: GROOMED JETS. PERTURBATIVE CONVERGENCE

$$e^+e^- \rightarrow \text{dijet} + X$$

SIDIS with jet



Scale variations are reduced when we go to NNLL calculation

But they are somewhat larger for a NNLL calculation

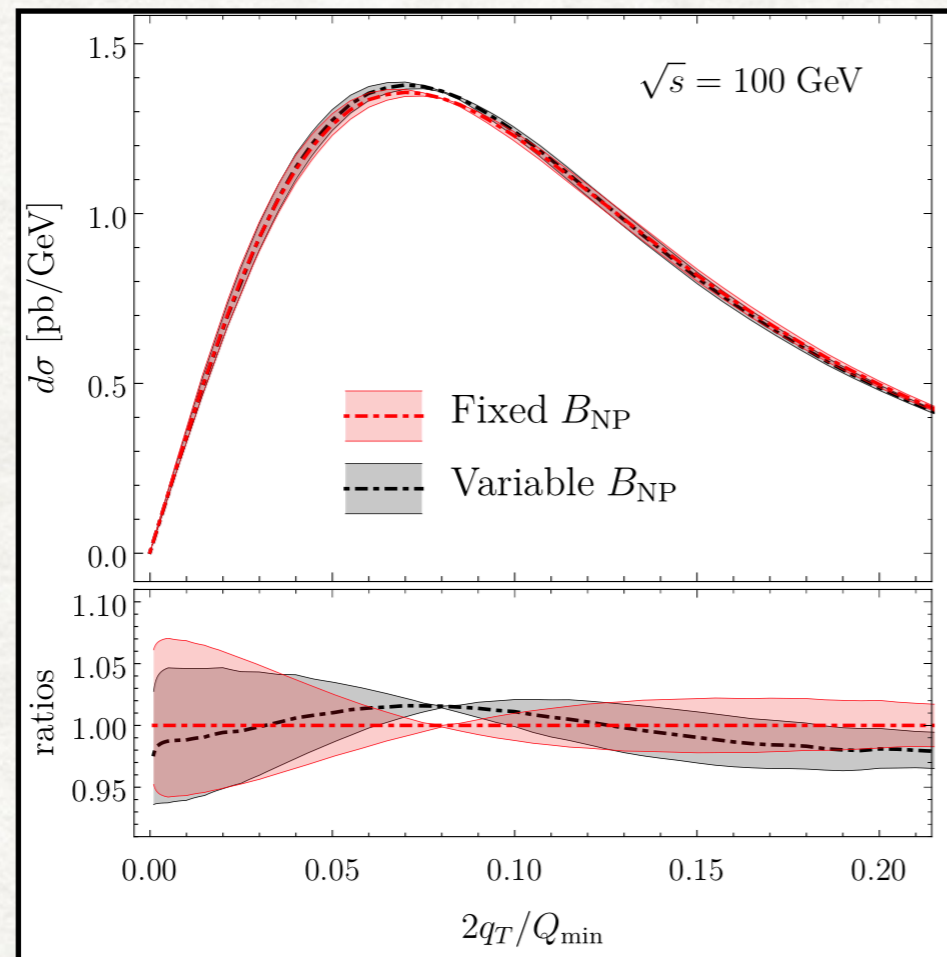


$\mu_{cs} \sim Q\sqrt{e_{\text{cut}}z_{\text{cut}}}$
approaches to NP-regime



Profiles
Increase Pert. order

PHENO: GROOMED JETS. SIZE OF NP EFFECTS



Non perturbative model for the TMDPDF taken from
Bertone, Scimemi, Vladimirov `19
arXiv:1902.08474

$$f_{NP}(x, \mathbf{b}) = \exp\left(-\frac{(\lambda_1(1-x) + \lambda_2x + \lambda_3x(1-x))\mathbf{b}^2}{\sqrt{1 + \lambda_4x\lambda_5\mathbf{b}^2}}\right)$$

But the cross section is dominated by
 nonperturbative parameter of evolution

$$\mathcal{D}(\mu, \mathbf{b}) = \int_{\mu_0}^{\mu} \frac{d\mu'}{\mu'} \Gamma + \mathcal{D}_{\text{pert}}(\mu_0, \mathbf{b}) + c_0 \mathbf{b} \mathbf{b}^*$$

NP effects are smaller for groomed-jets than for ungroomed-jets!

CONCLUSIONS

CONCLUSIONS

Our aim is to **extract information about NP contributions** to hadronic TMDs



We use **jets**, in order to **reduce NP effects** in final state with hadrons (TMDFFs)

TWO APPROACHES

UNGROOMED JETS (N³LL)

Factorization depends on the **radius** of the jet

WTA axis election the **Soft function** is the same that for hadronic TMD



We find a way to study big radius jets

GROOMED JETS (NNLL)

Factorization does **not** depend on the **radius** of the jet

New modes

Contaminating soft radiation is out!

Due to grooming parameter **energy** needed is **higher**

Hadronic TMDs and TMD jet functions share the same **double-scale RG evolution**

arTeMiDe



Pheno



Needs future comparison with **data!**

<https://teorica.fis.ucm.es/artemide/>

BACKUP SLIDES

DOUBLE-SCALE RENORMALIZATION GROUP EVOLUTION

Same RG evolution for **hadronic TMDs** and for **TMD jet functions**!

TMDs

$$\mu^2 \frac{d}{d\mu^2} D_i(z, \mathbf{b}, \mu, \zeta) = \frac{1}{2} \gamma_F^i(\mu, \zeta) D_i(z, \mathbf{b}, \mu, \zeta)$$

$$\zeta \frac{d}{d\zeta} D_i(z, \mathbf{b}, \mu, \zeta) = -\mathcal{D}^i(\mu, \mathbf{b}) D_i(z, \mathbf{b}, \mu, \zeta)$$

Jets

$$\mu^2 \frac{d}{d\mu^2} J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = \frac{1}{2} \gamma_F^i(\mu, \zeta) J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta)$$

$$\zeta \frac{d}{d\zeta} J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = -\mathcal{D}^i(\mu, \mathbf{b}) J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta)$$

DOUBLE-SCALE RENORMALIZATION GROUP EVOLUTION

They have a common **evolution factor**

TMDs

$$D_i(z, \mathbf{b}, \mu_f, \zeta_f) = \exp \left[\int_{(\mu_i, \zeta_i)}^{(\mu_f, \zeta_f)} \left(\gamma_F^i(\mu, \zeta) \frac{d\mu}{\mu} - \mathcal{D}^i(\mu, \mathbf{b}) \frac{d\zeta}{\zeta} \right) \right] D_i(z, \mathbf{b}, \mu_i, \zeta_i)$$

Jets

$$J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu_f, \zeta_f) = \exp \left[\int_{(\mu_i, \zeta_i)}^{(\mu_f, \zeta_f)} \left(\gamma_F^i(\mu, \zeta) \frac{d\mu}{\mu} - \mathcal{D}^i(\mu, \mathbf{b}) \frac{d\zeta}{\zeta} \right) \right] J_i^{\text{axis}}(z, \mathbf{b}, QR, \mu_i, \zeta_i)$$

This fact makes phenomenological analysis simpler!

arTeMiD.e

Scimemi, Vladimirov `17

<https://teorica.fis.ucm.es/artemide/>

TMD SEMI-INCLUSIVE JET FUNCTION AT NLO

$$\theta \ll 1$$

$$\theta \ll R$$

Collinear radiation of typical angle θ sees the jet boundary infinitely far away

The collinear radiation is mostly inside the jet



Independence of the radius of the jet!



The dependence on z is power suppressed!

$$J_i^{\text{WTA}}(z, \mathbf{b}, ER, \mu, \zeta) = \delta(1 - z) \mathcal{J}_i^{\text{WTA}}(\mathbf{b}, \mu, \zeta) \left[1 + \mathcal{O}\left(\frac{1}{\mathbf{b}^2 E^2 R^2}\right) \right]$$

where

$$\mathcal{J}_i^{\text{WTA}}(\mathbf{b}, \mu, \zeta) = \frac{1}{2N_c(\bar{\mathbf{n}} \cdot p_J)} \text{Tr} \left\{ \frac{\not{\bar{\mathbf{n}}}}{2} \langle 0 | e^{-i\mathbf{b} \mathbf{P}_\perp} \chi_n(0) | J_{\text{alg}}^{\text{WTA}} \rangle \langle J_{\text{alg}}^{\text{WTA}} | \bar{\chi}_n(0) | 0 \rangle \right\}$$

$$\mathcal{J}_i^{[0]\text{WTA}}(\mathbf{b}, \mu, \zeta) = 1$$

$$\mathcal{J}_i^{[1]\text{WTA}}(\mathbf{b}, \mu, \zeta) = 2 \left\{ N_i + L_\mu \left[C'_i + C_i \left(1_\zeta - \frac{1}{2} L_\mu \right) \right] \right\}$$

$$N_q = C_F \left(\frac{7}{2} - \frac{5\pi^2}{12} - 3 \ln 2 \right)$$

$$N_g = C_A \left(\frac{131}{36} - \frac{5\pi^2}{12} \right) - \frac{17}{18} n_f T_R - \beta_0 \ln 2$$

TMD SEMI-INCLUSIVE JET FUNCTION AT NNLO

We know the evolution of the TMD jet function and in this limit it does not depend on radius or z



We can predict the **log behavior** of the two-loop jet function solving renormalization group equations and the **constant can be numerically calculated** (EVENT2)

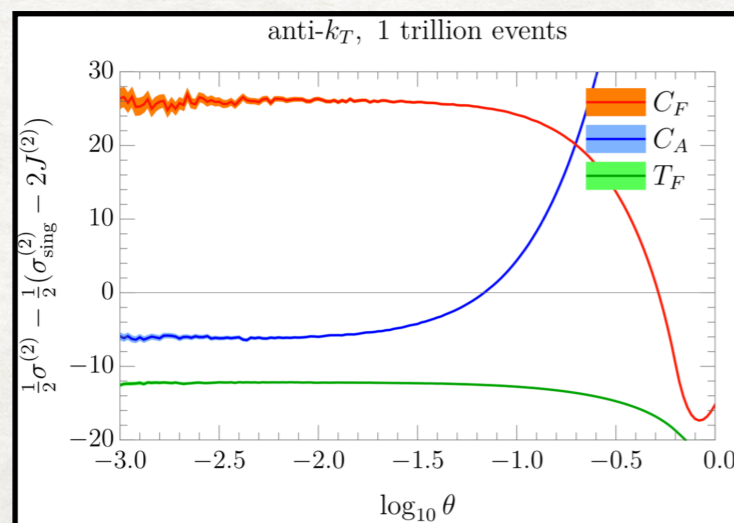
$$\theta \ll 1$$

$$\theta \ll R$$

Predicted by RG equations

Predicted by EVENT2

$$\mathcal{J}^{[2]WTA}(\mathbf{b}, \mu, \zeta) = \sum_{k=1}^4 \sum_{l=0}^k C_{kl} L_{\mu}^k \mathbf{1}_{\zeta}^l + C_0$$



$$C_0 = j_{C_F} + j_{C_A} + n_f j_{T_F}$$

TMD SEMI-INCLUSIVE JET FUNCTION AT NLO

The **Soft function** is the same that for TMDs in **some cases for SJA** and
in **ALL cases for WTA**

The Semi-inclusive jet function is renormalized as a TMD

$$J_q^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = Z_{UV}(\mu, \epsilon) R_q(\delta, \zeta, \epsilon) J_q^{\text{axis}, B}(z, \mathbf{b}, QR, \mu, \delta)$$

$$\theta \ll 1$$

$$\theta \ll R$$

We have a new definition of the operator only valid for WTA axis!

Collinear radiation of typical angle θ
sees the jet boundary infinitely far away

The collinear radiation is mostly inside the jet

Independence of the radius of the jet!

The dependence on z is power suppressed!

$$J_i^{\text{WTA}}(z, \mathbf{b}, QR, \mu, \zeta) = \delta(1 - z) \mathcal{J}_i^{\text{WTA}}(\mathbf{b}, \mu, \zeta) \left[1 + \mathcal{O}\left(\frac{1}{b^2 Q^2 R^2}\right) \right]$$

where

$$\mathcal{J}_i^{\text{WTA}}(\mathbf{b}, \mu, \zeta) = \frac{1}{2N_c(\bar{\mathbf{n}} \cdot p_J)} \text{Tr} \left\{ \frac{\not{\bar{\mathbf{n}}}}{2} \langle 0 | e^{-i\mathbf{b} \cdot \mathbf{P}_\perp} \chi_n(0) | J_{\text{alg}}^{\text{WTA}} \rangle \langle J_{\text{alg}}^{\text{WTA}} | \bar{\chi}_n(0) | 0 \rangle \right\}$$

TMD SEMI-INCLUSIVE JET FUNCTION AT NLO

The **Soft function** is the same that for TMDs in **some cases for SJA** and
in **ALL cases for WTA**

The Semi-inclusive jet function is renormalized as a TMD

$$J_q^{\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = Z_{UV}(\mu, \epsilon) R_q(\delta, \zeta, \epsilon) J_q^{\text{axis}, B}(z, \mathbf{b}, QR, \mu, \delta)$$

$$\theta \ll 1$$

$$\theta \sim R$$

The definition of the operator is
the usual one

$$J_i^{\text{axis}} = \sum_{n=0}^{\infty} a_s^n J_i^{[n]\text{axis}}$$

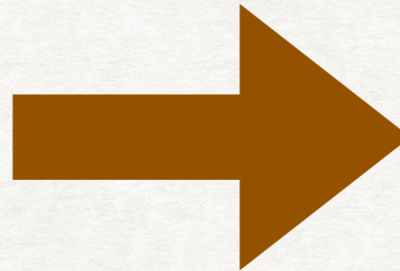
$$J_i^{[0]\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = \delta(1 - z)$$

$$J_i^{[1]\text{axis}}(z, \mathbf{b}, QR, \mu, \zeta) = 2 \left(\sum_j c_{ji} p_{ji} \right) \left[L_R - L_\mu - 2 \ln(1 - z) + \frac{1}{4} |\mathbf{b}|^2 Q^2 R^2 (1 - z)^2 \right. \\ \left. \times {}_2F_3 \left(\{1, 1\}, \{2, 2, 2\}; -\frac{1}{4} |\mathbf{b}|^2 Q^2 R^2 (1 - z)^2 \right) \right] + \delta(1 - z) \left[2C'_i L_R - C_i L_\mu^2 + 2C_i L_\mu \mathbf{1}_\zeta + 2\tilde{d}_i^{\text{axis}}(\mathbf{b}QR) \right]$$

The dependence on the axis
is only here!

NUMERICAL RESULTS: LARGE RADIUS

The cross-section is simplified!



The jet functions do not depend on the radius size

The dependence in z is power suppressed (cross-section is less differential)

In the case of big radius factorization is only held for WTA axis!

$$\frac{d\sigma_{ee \rightarrow JJX}}{dq} = H(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} \mathcal{J}_q^{\text{WTA}}(\mathbf{b}, \mu, \zeta) \mathcal{J}_q^{\text{WTA}}(\mathbf{b}, \mu, \zeta) R^2[\mathbf{b}; (\mu_i, \zeta_i) \rightarrow (\mu_f, \zeta_f)]$$

NUMERICAL RESULTS

Ingredients to build cross-section

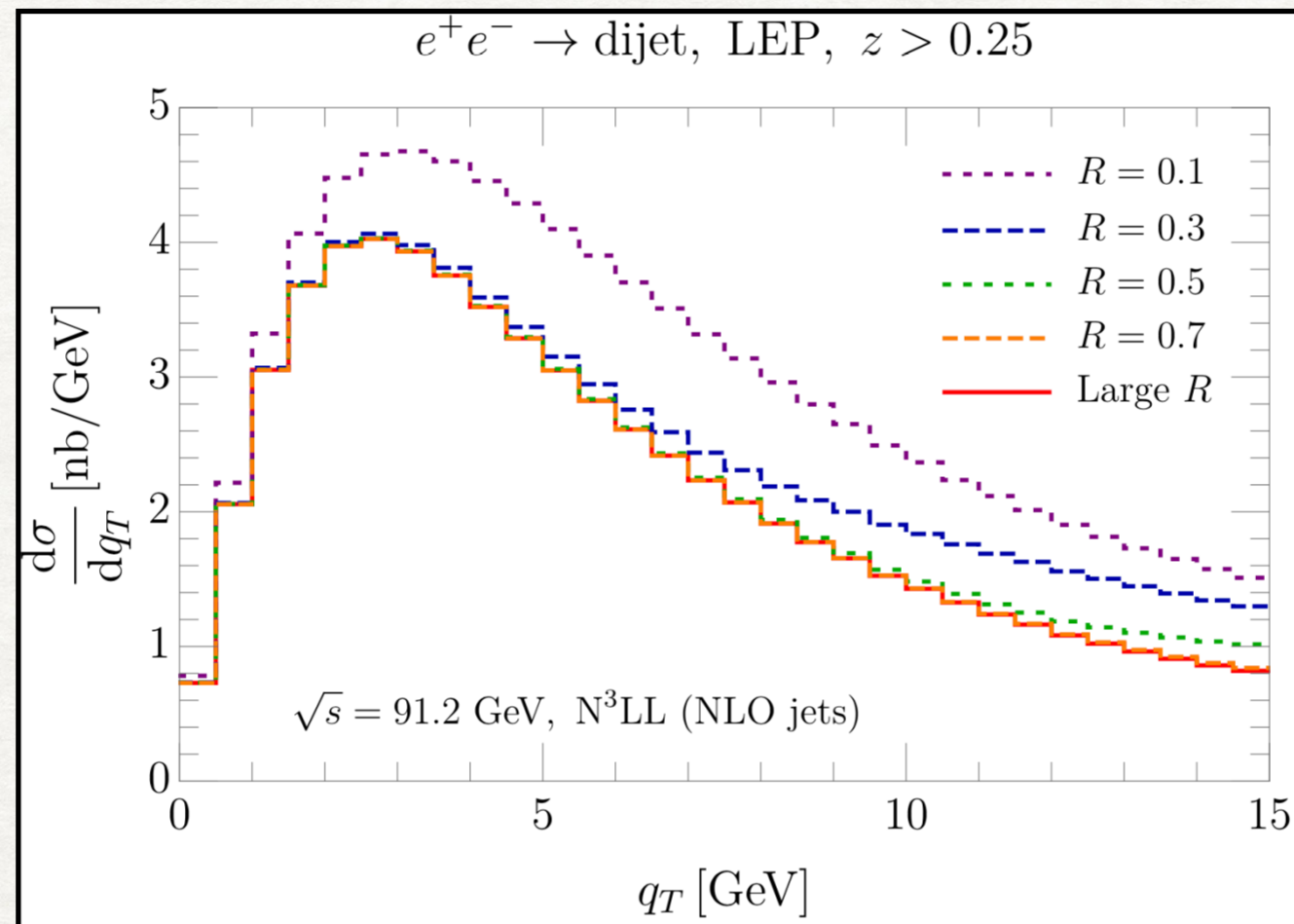
$$\frac{d\sigma_{ee \rightarrow JJX}}{dz_1 dz_2 d\mathbf{q}} = H(Q^2, \mu) \int \frac{d\mathbf{b}}{(2\pi)^2} e^{-i\mathbf{b}\mathbf{q}} J_q^{\text{axis}}(z_1, \mathbf{b}, QR, \mu, \zeta) J_q^{\text{axis}}(z_2, \mathbf{b}, QR, \mu, \zeta) R^2[\mathbf{b}; (\mu_i, \zeta_i) \rightarrow (\mu_f, \zeta_f)]$$

Hard factor: Same that for DY. Known and introduced in arTeMiDe up to 2-loops.

Evolution kernel: Same that for TMDs. Known and introduced in arTeMiDe up to 3-loops.

TMD jet functions: Calculated at 1-loop. New arTeMiDe module built.

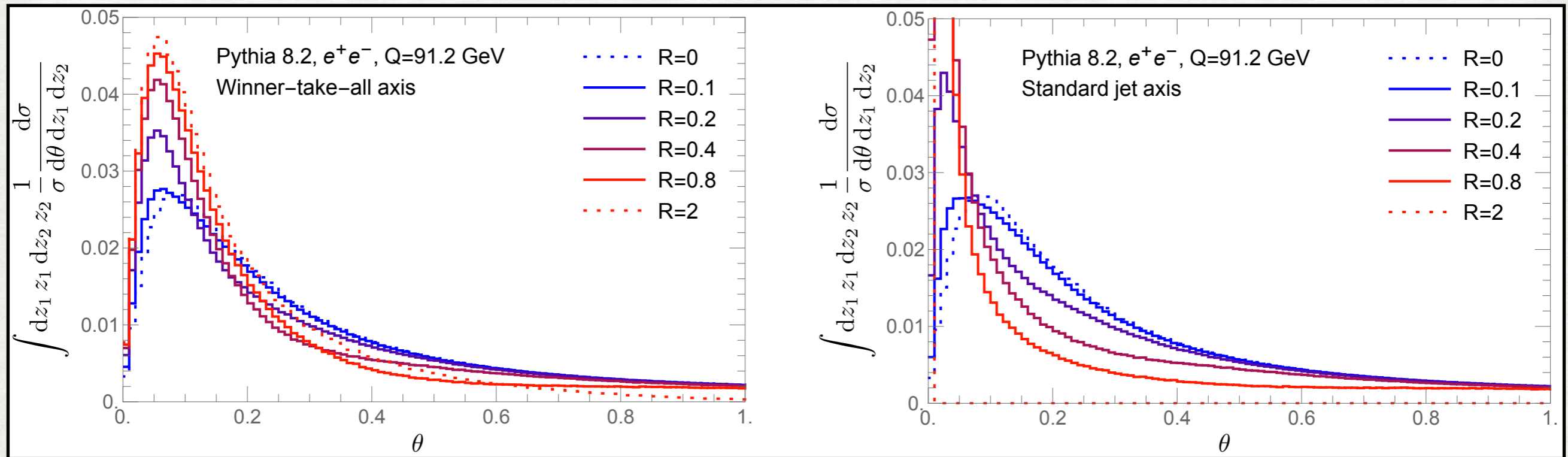
VARY RADIUS: LARGE-R VS FINITE R



The large radius approximation is a **very accurate approximation** for jet functions with finite radius (but not so small)

This fact allow us to **skip some of the technical complications** of the finite radius jet function

CHECKING WITH PYTHIA 8.2.



Cross-section of angular decorrelation for different values of the radii of the jets

For **small values of R** the cross-section for both axis elections agrees!

For **big values of R** the cross section in **SJA** is inconsistent!

Factorization is broken

WTA axis **solves the problems!**