



Istituto Nazionale di Fisica Nucleare
Laboratori Nazionali del Sud

PID

Programma Infn per Docenti

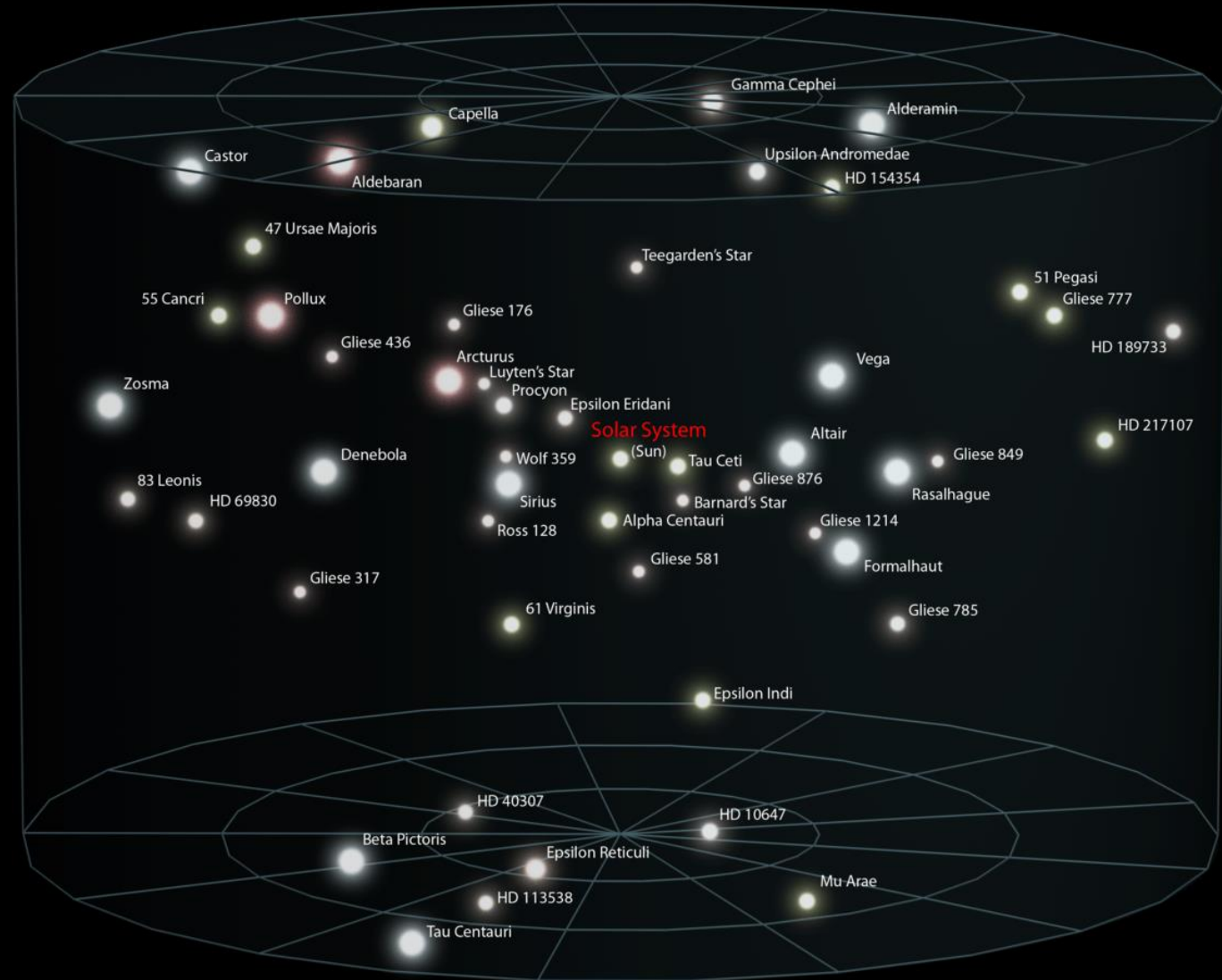
LNS – 18-22 febbraio 2019

Astrofisica Nucleare

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INTERSTELLAR NEIGHBORHOOD



What is Nuclear Astrophysics?

Starts from the marriage between



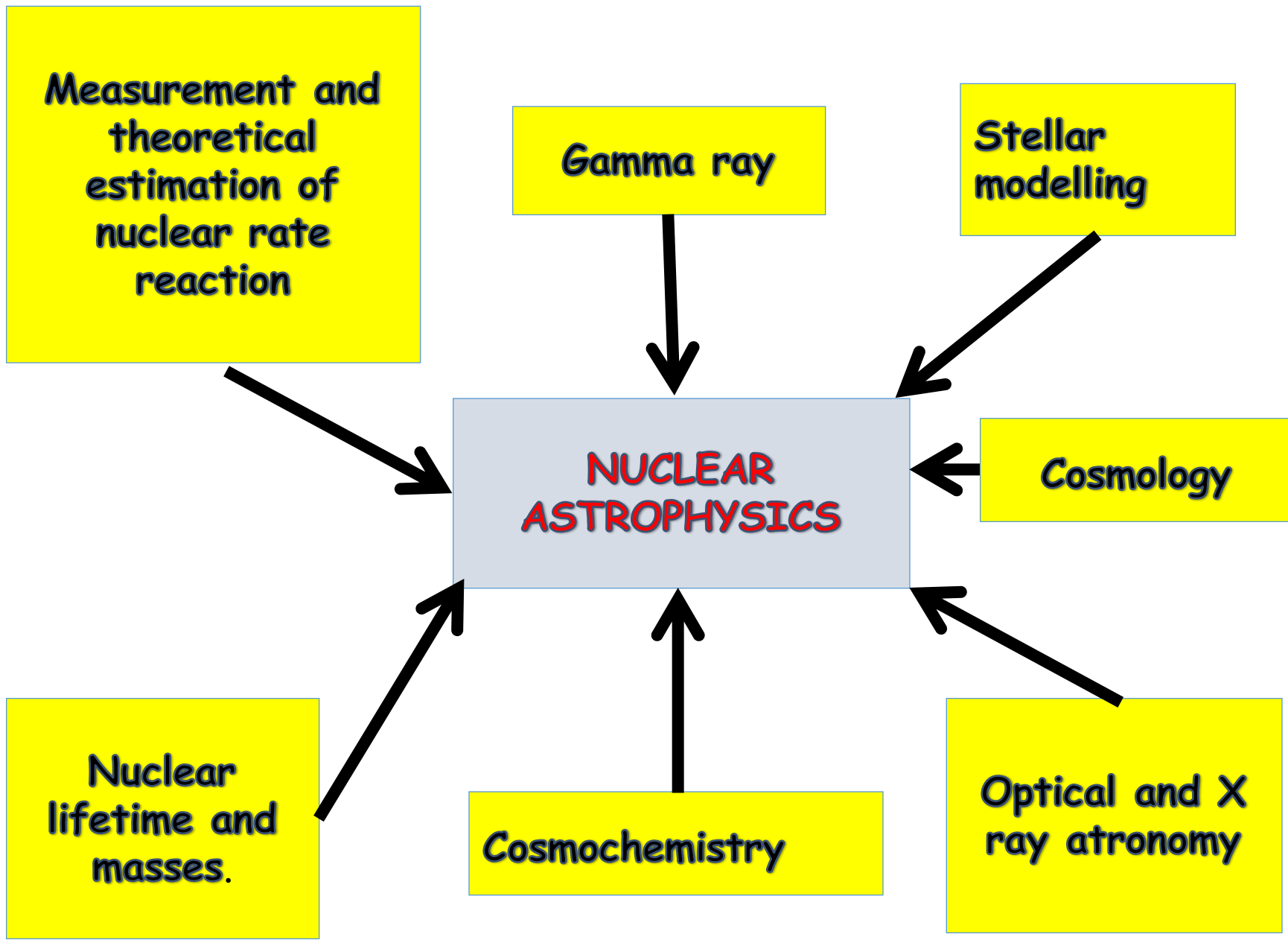
ASTROPHYSICS

NUCLEAR PHYSICS



William A. Fowler
Nobel Price Physics
(1983)

Premio Nobel per la Fisica nel 1983 per i suoi studi teorici e sperimentali sulle reazioni nucleari che danno origine agli elementi chimici nell'universo.



Argomenti

- Introduzione all'Astrofisica Nucleare

osservazioni astronomiche e aspetti astrofisici

aspetti nucleari

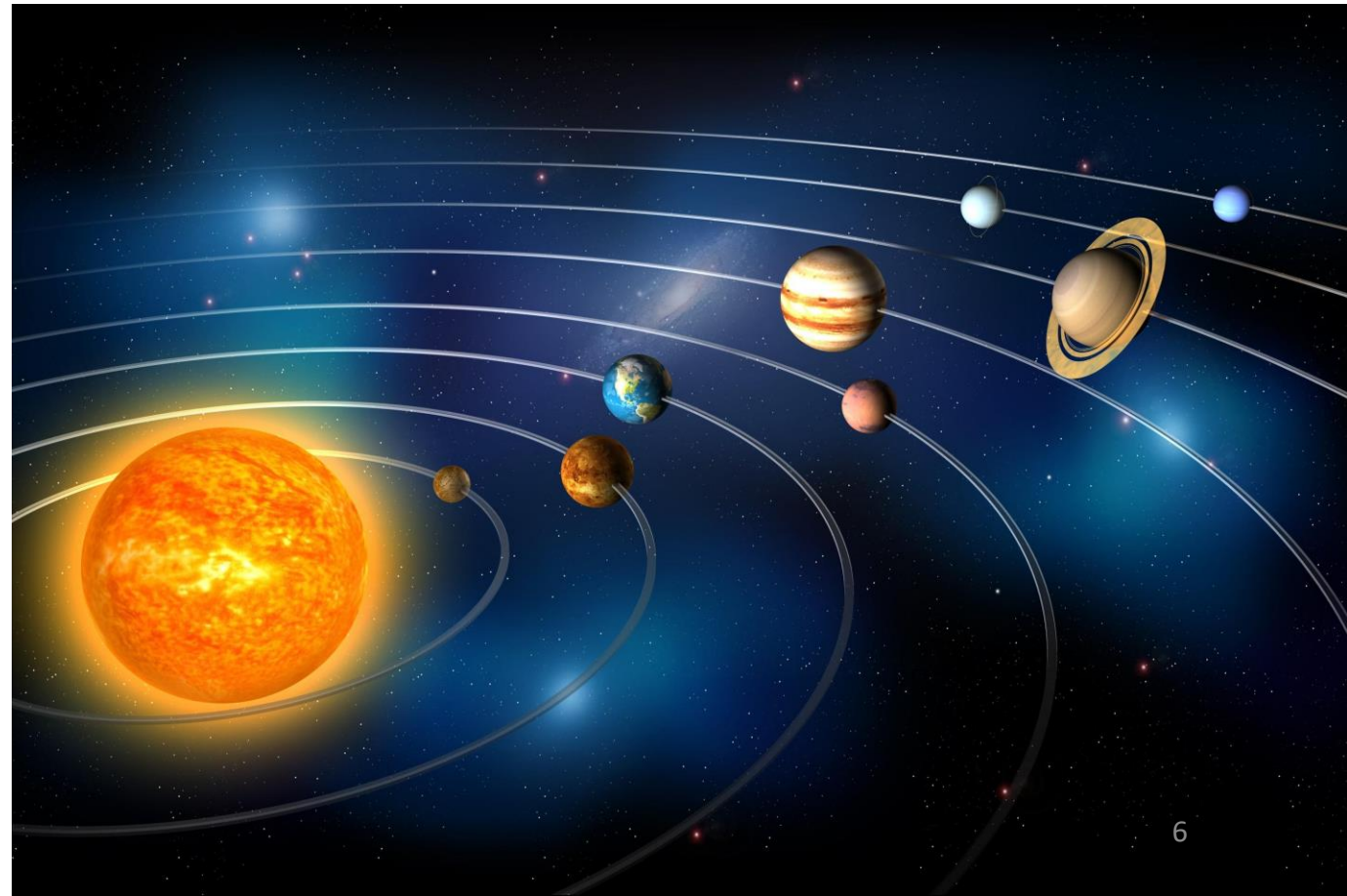
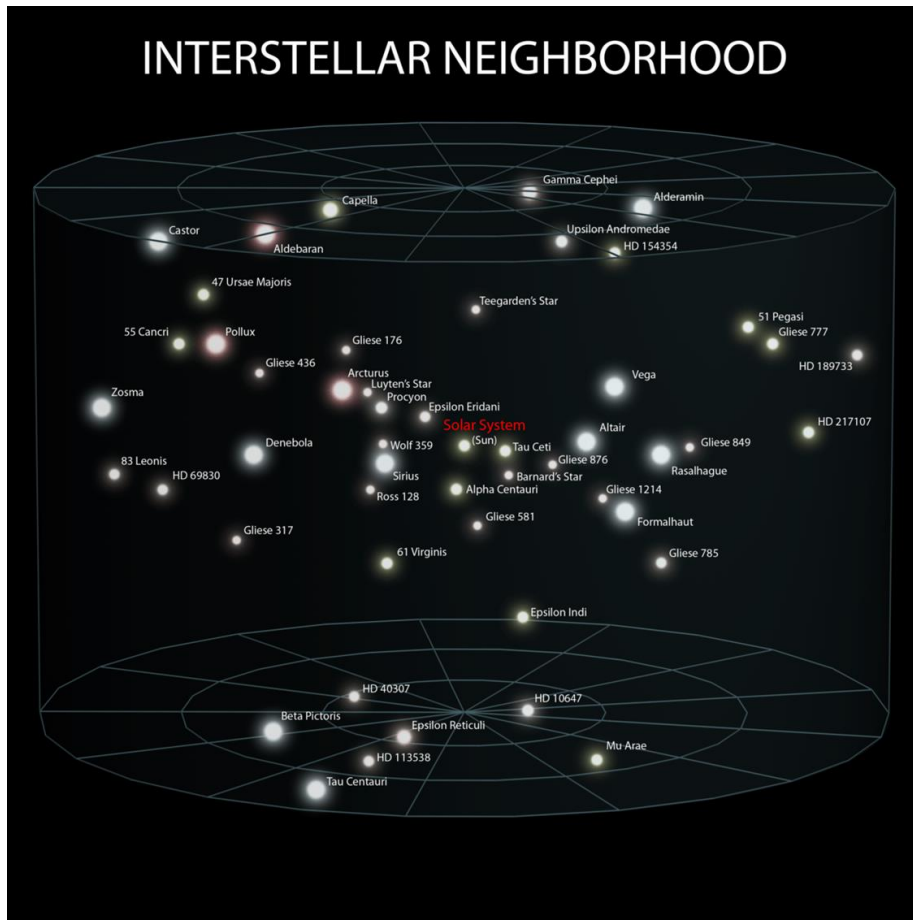
- reazioni termonucleari
- Parametri nucleari di interesse astrofisico: rate di reazione
- misure di sezione d'urto di interesse astrofisico
- Astrofisica nucleare ai LNS: tecniche e apparati sperimentali in Astrofisica Nucleare

Osservazioni astronomiche

- Oggetti di «lunga vita» nel cielo

Astro... aspects

The study of stars is central to astronomy and astrophysics since stars are long-lived objects that are responsible for most of the visible light we observe from normal galaxies.



Osservazioni astronomiche

- Oggetti di «lunga vita» nel cielo
- luminosità

Stellar Magnitude --- Luminosity

- Greek astronomer Hipparchus was one of the first skywatchers to systematically catalogue the ~850 stars he observed
- He assigned a magnitude index to each star ranging from $m=1$, for the brightest stars, to $m=6$ for the dimmest (opposite ordering of what one would expect)
- Human eye has a nearly logarithmic subjective response to radiant energy flux
- Modern astronomy defines: a 5 magnitude difference corresponds to a factor 100 in brightness (flux)
- [Apparent magnitude](#), the brightness of an object as it appears in the night sky.
- [Absolute magnitude](#), which measures the [luminosity](#) of an object (or reflected light for non-luminous objects like [asteroids](#)); it is the object's apparent magnitude as seen from a specific distance, conventionally 10 [parsecs](#) (32.6 [light years](#)).



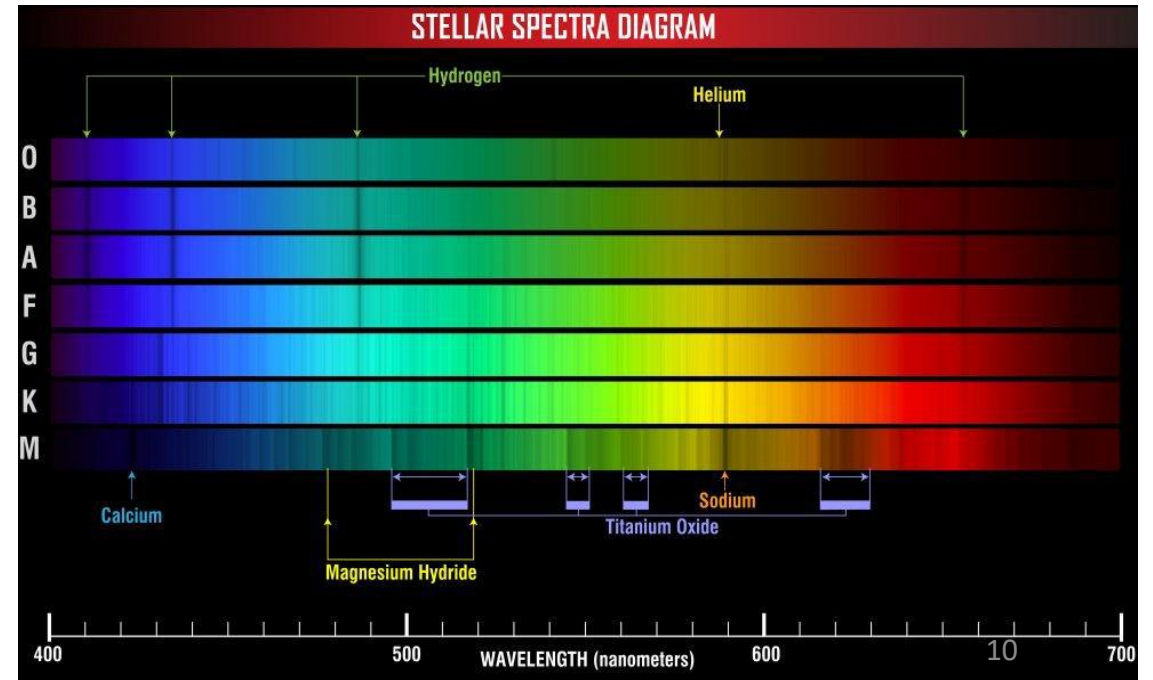
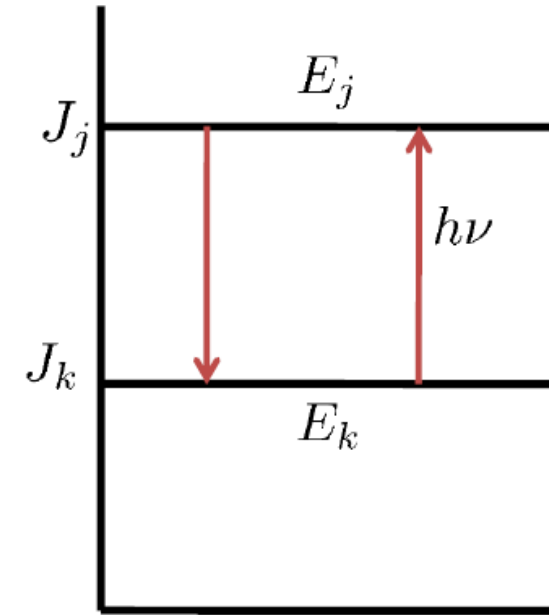
Osservazioni astrofisiche

- Oggetti di «lunga vita» nel cielo
- Luminosità
- temperatura

Stellar Temperatures

- Astronomers measure the spectra of atomic transitions
- The spectral source is line absorption of continuum light in the stellar atmosphere
- Photo-absorption and scattering can cause atomic transitions
- Population ratio between two atomic states in thermal equilibrium given by Boltzmann's formula:

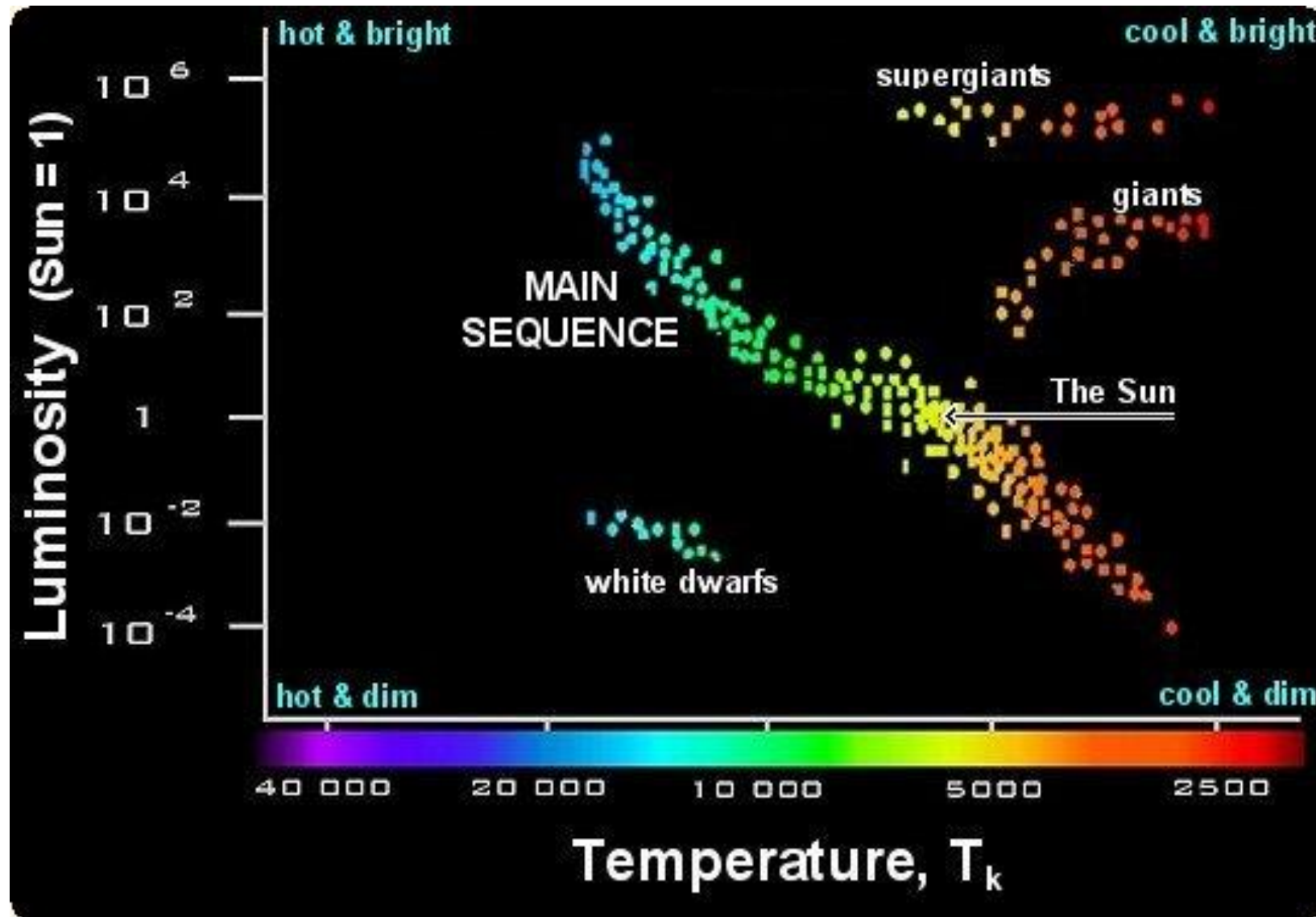
$$\frac{n_j}{n_k} = \frac{g_j}{g_k} \exp\left(-\frac{E_j - E_k}{kT}\right)$$



Osservazioni astrofisiche

- Oggetti di «lunga vita» nel cielo
- Luminosità
- Temperatura
- Evoluzione delle stelle e dell'universo

Hertzsprung-Russel Diagram – stellar evolution



Stellar birth

1. Stars are born of “seed” gas undergoing localized gravitational collapse
2. 1st generation stars: primordial gas: H and He
3. Later generations formed of processed gas
4. Points 2 & 3 suggest possibility of 2 populations of stars: very old and young
5. Point 4 suggests populations should have different abundance distributions

Virial Theorem

$$2T + \Omega = \frac{d^2I}{dt^2}$$

T = total kinetic energy Ω = gravitational energy
I = momentum of inertia

Static configuration $2T + \Omega = 0 \rightarrow dT = -d\Omega/2$



Stellar Populations

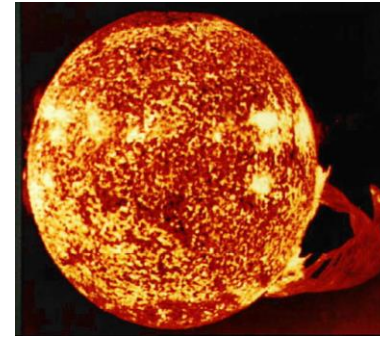
- Population I (Pop I): Stars that are “metal-rich” (the Sun is included). They are young stars, having formed within the past few billion years, and can be found in the disk of the Galaxy.
- Population II (Pop II): Stars that are “metal-poor”. *Ancient* relics of the initial star formation periods of Galaxies and first generation of primordial stars. Their metal abundance, relative to hydrogen, is smaller by a factor of 100 or more compared to population I stars.
- Metals: any element $A > 4$; that is, any element with $Z > 2$

STELLAR LIFE CYCLE

BIRTH
gravitational contraction

mixing of
interstellar gas

INCREASE THE mixing of
interstellar gas



Stars

thermonuclear
reactions

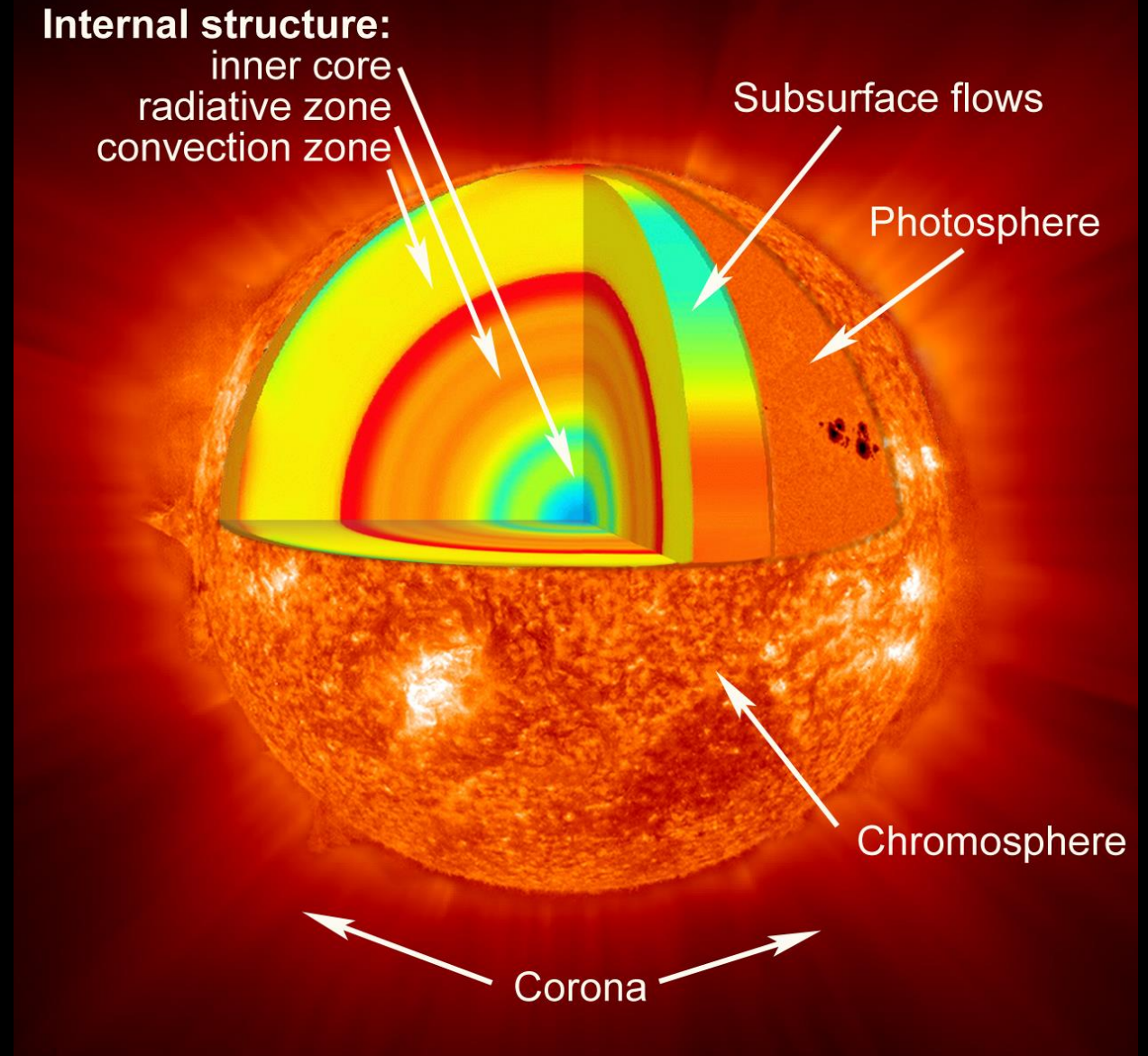
explosion
DEATH

- energy production
- stability against collapse
- synthesis of "metals"

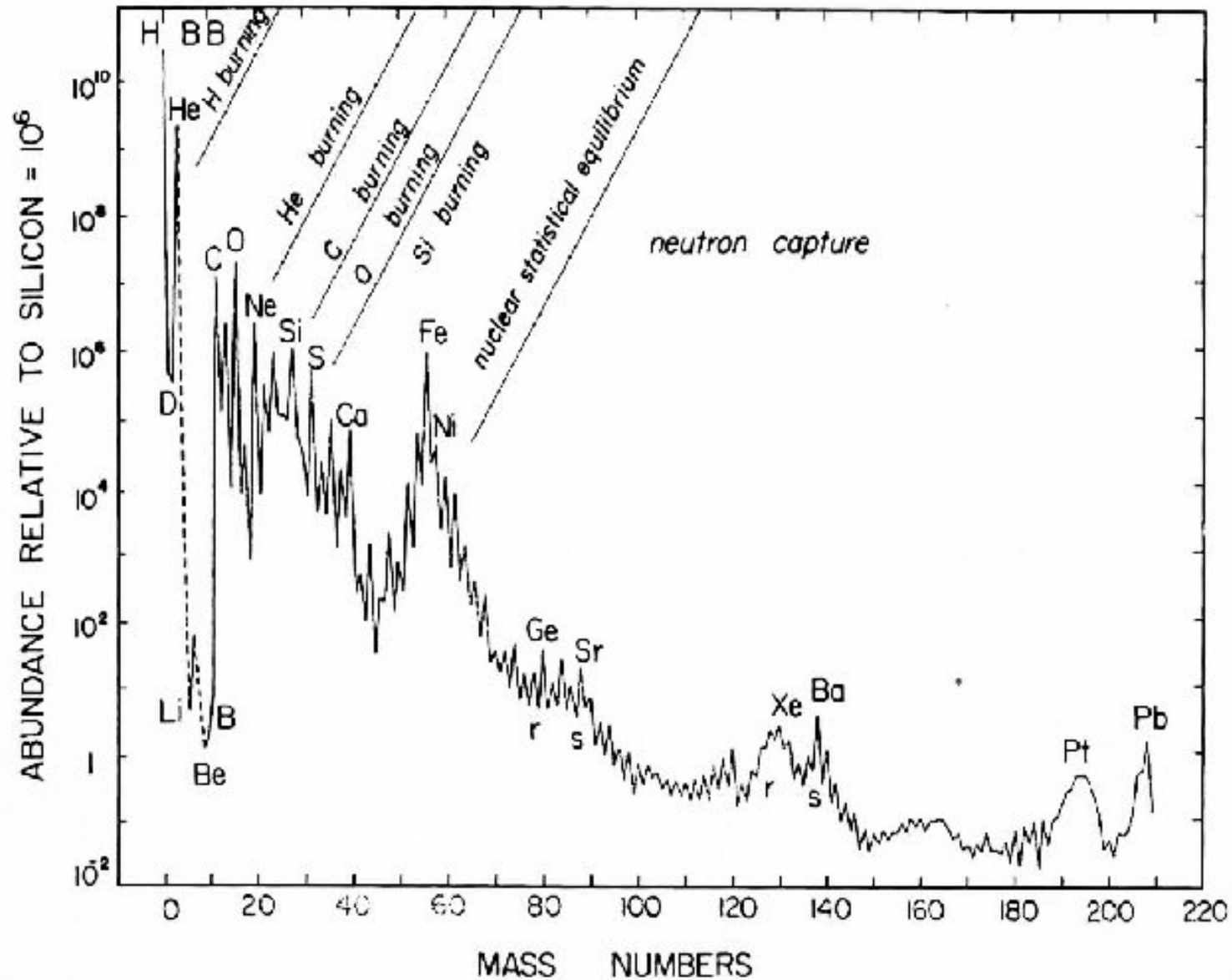


Our star: the most known

- $M_{\odot} = (1.98855 \pm 0.00025) \times 10^{30}$ kg
about 332946 times the mass of Earth (M_{\oplus})
- mean density = 1.408×10^3 kg/m³
- radius = 695.700 km
about 110 times the radius of the Earth)
- volume = 1.4122×10^{27} m³
about 1.3×10^6 the volume of the Earth
- age = 4.6 Gyr
- luminosity = 3.827×10^{26} W
- surface temperature = 6000 K
- core temperature = 16 MK
- distance from Earth = 15×10^7 km = 1 AU



Solar system abundances



Argomenti

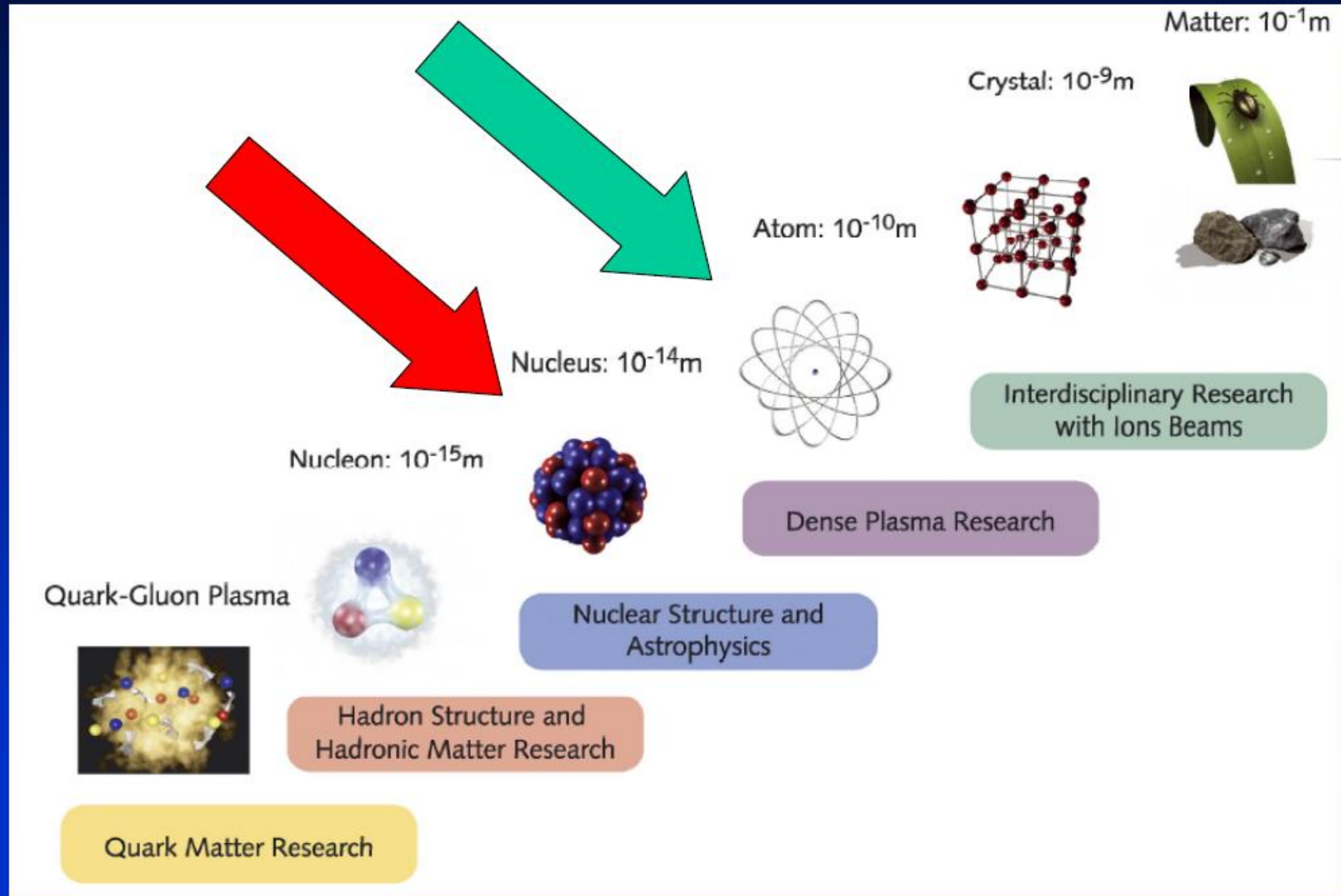
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 - osservazioni astronomiche e aspetti astrofisici

 - aspetti nucleari

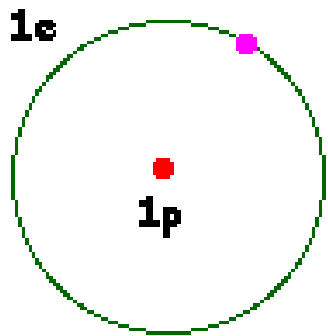
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Di cosa ci occupiamo....

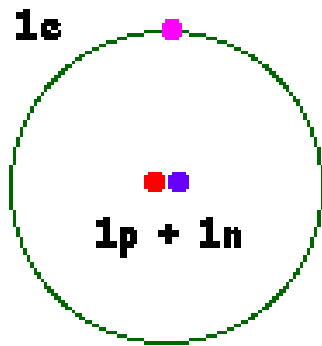


Nuclear aspects

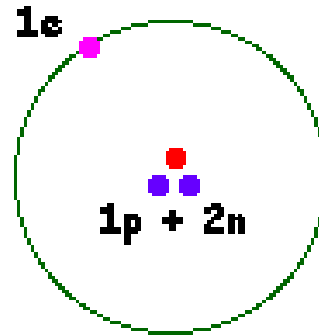
- Nuclear mass = the most fundamental property of the atomic nucleus
- According to the Einstein relationship the mass m is equivalent to an energy of $E = m \cdot c^2$



Hydrogen



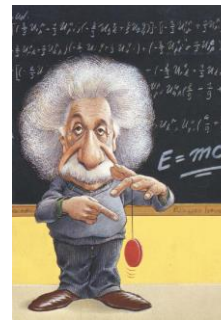
Deuterium



Tritium



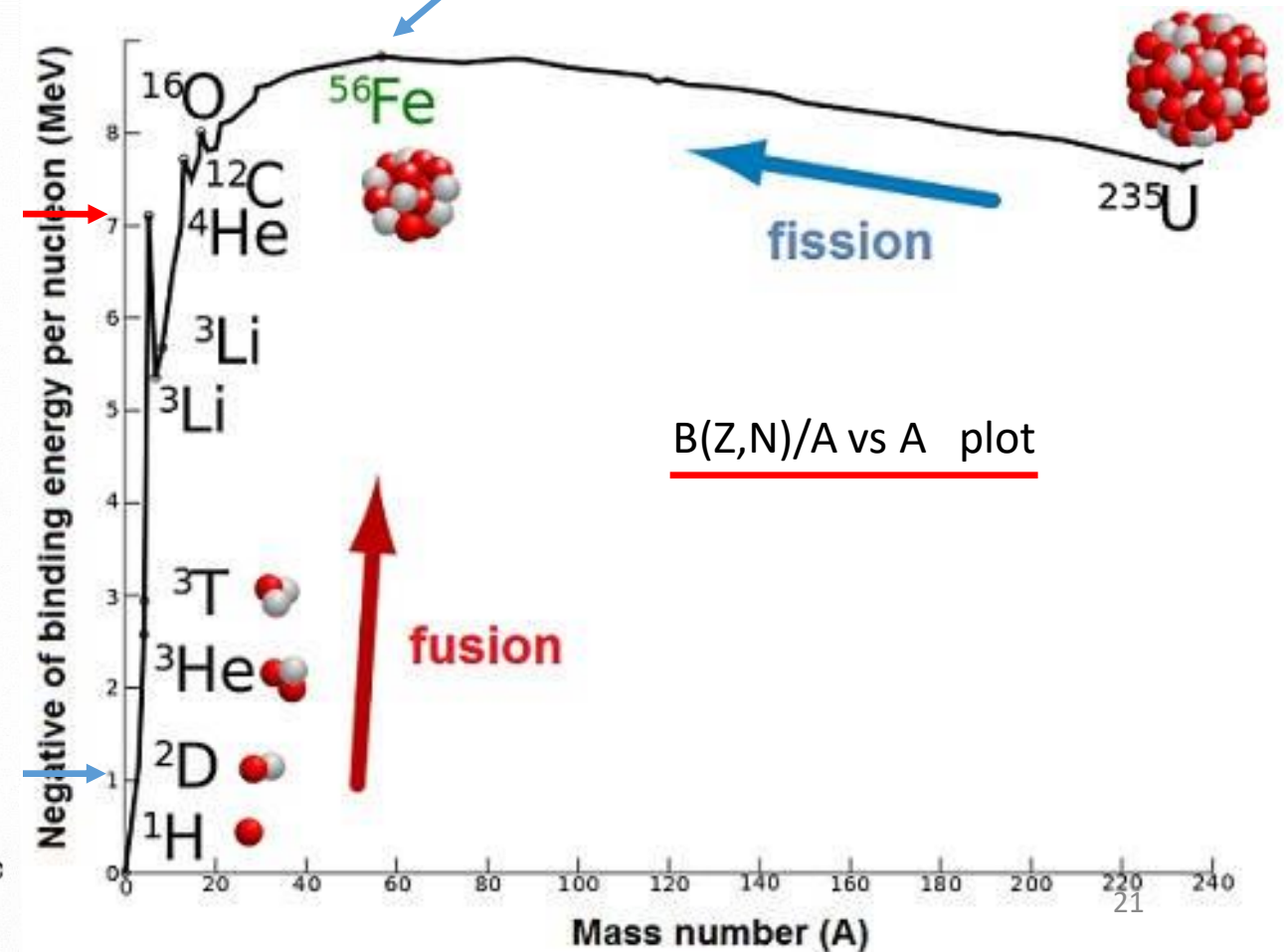
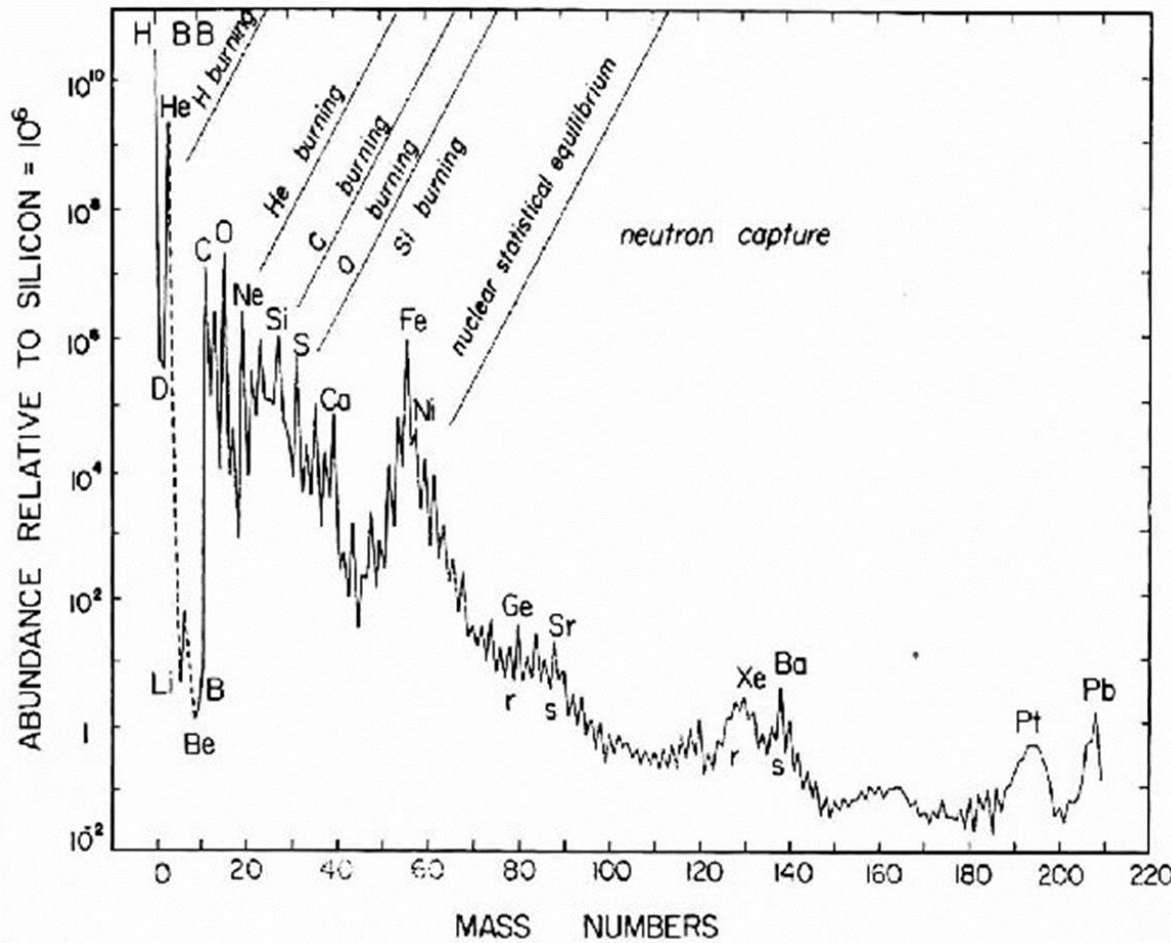
Nuclear aspects



- measurements showed that the total nuclear mass, m_{nuc} , is less than the sum of masses of the constituent nucleons.

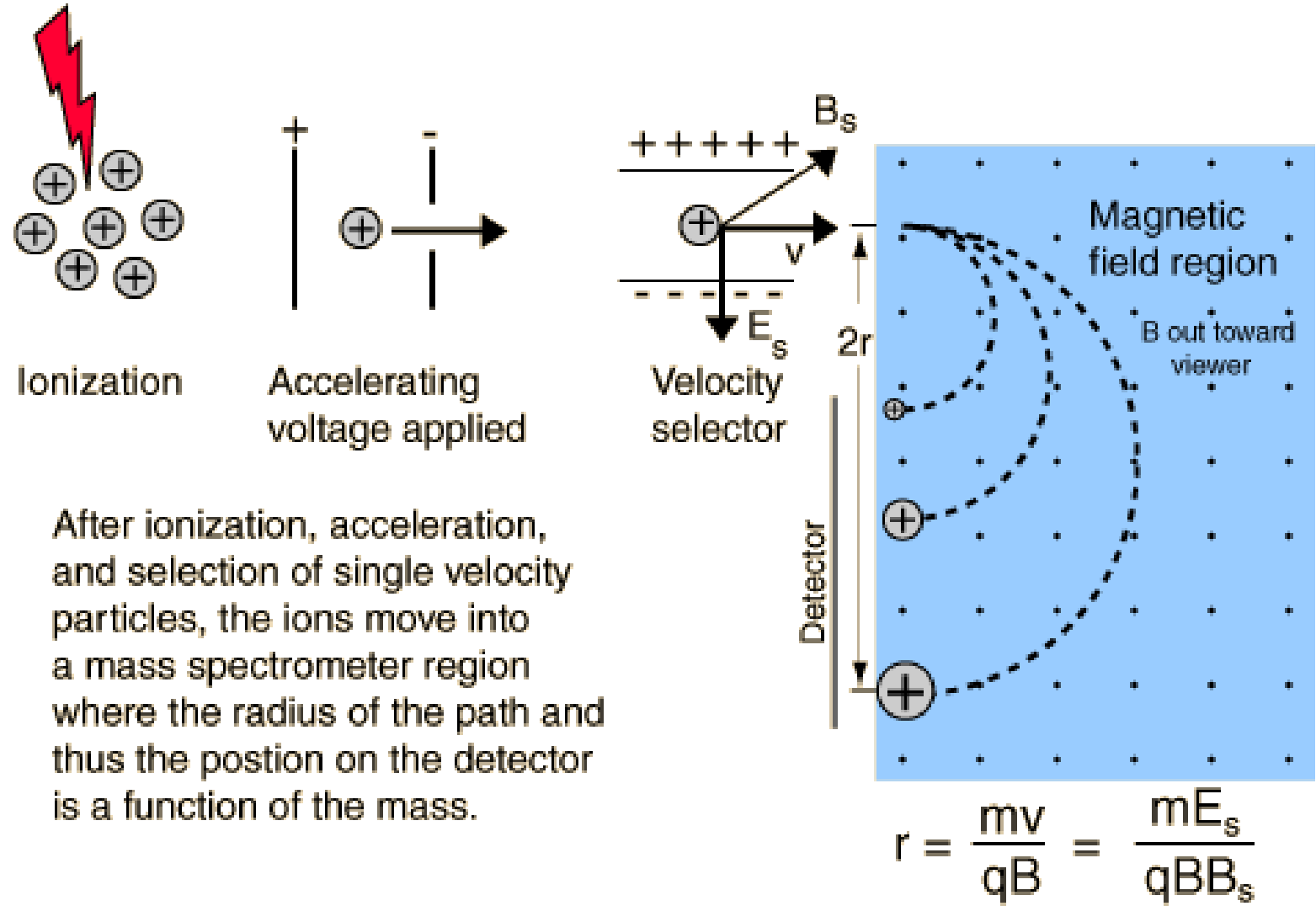


Iron peak in the solar system abundances



Cosa conosciamo dei nuclei?

Nuclear mass measurement



Quantum behaviour

It is known (experimentally) that the kinetic energies of nucleons in a nucleus is of the order of 10 MeV.

10 MeV \ll nucleon rest energy (about 1000 MeV) \rightarrow nonrelativistic quantum mechanics.

Quantum mechanic fundamental concepts:

- The size of a classical particle is the same in every experiment we may do; the “size” of a quantum particle varies with the experiment we perform.

Dimension Δx of an electron:

- electrical conduction in solids $\rightarrow \Delta x =$ dimension of the material block
- atomic physics $\rightarrow \Delta x =$ dimension of a single atom
- β decay $\rightarrow \Delta x =$ nucleus

Heisenberg uncertainty relationships:

$$\Delta x \cdot \Delta p \geq \frac{\hbar}{2}; \quad \Delta E \cdot \Delta t \geq \frac{\hbar}{2}; \quad \Delta l_z \cdot \Delta \phi \geq \frac{\hbar}{2}$$

Mathematical aspects \rightarrow Schrödinger equation: $-\frac{\hbar^2}{2m} \frac{d^2\Psi}{dx^2} + V(x) \Psi(x) = E \Psi(x)$ $\Psi(x) =$ Schr. wave function

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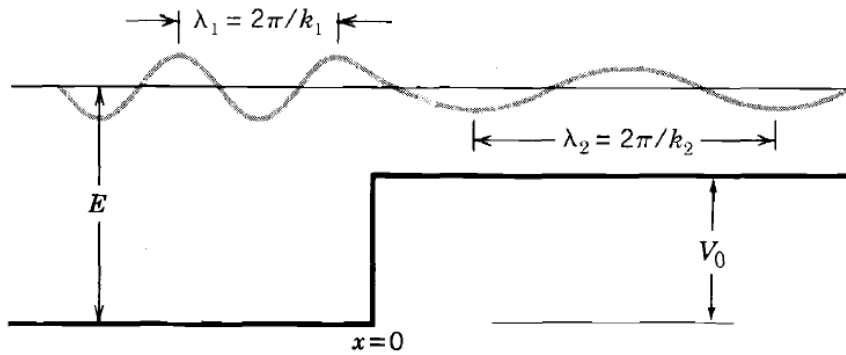
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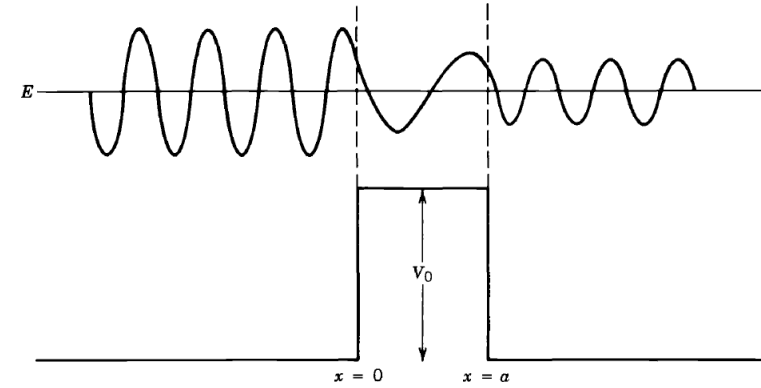
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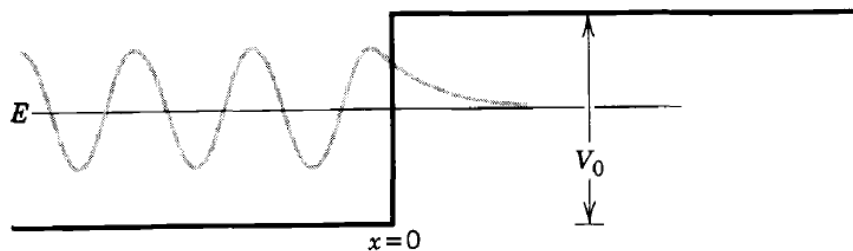
Problem in one dimension – free particle



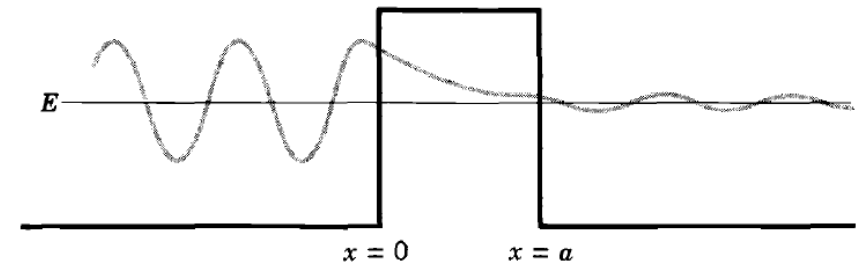
Step potential $E > V_0$



Barrier potential $E > V_0$



Step potential $E < V_0$

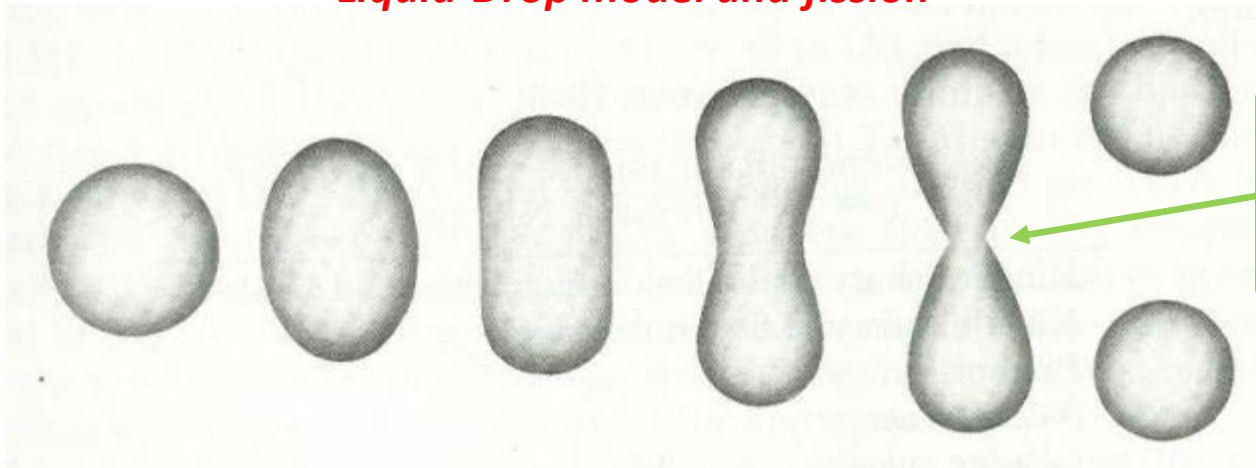


Barrier potential $E < V_0$ (tunneling)

Liquid-Drop model

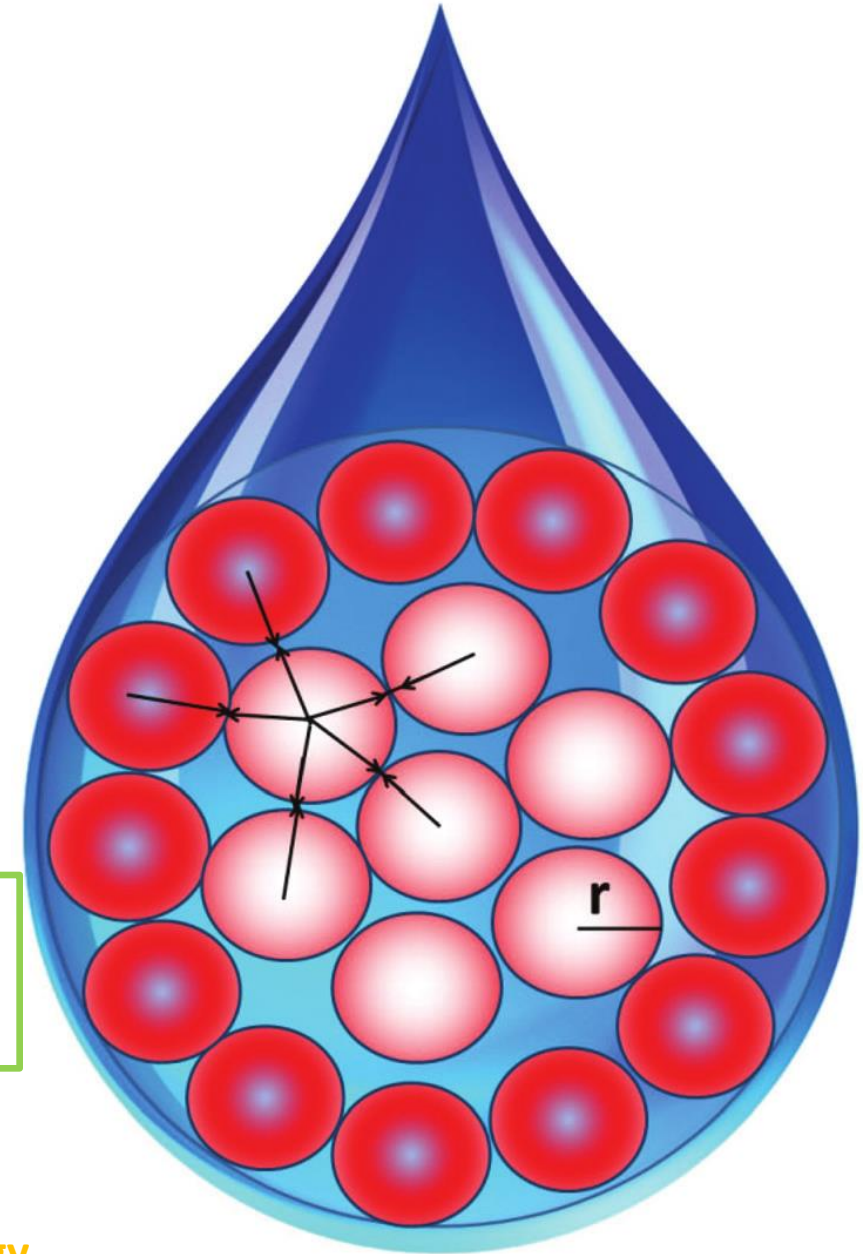
- is based on: short range of nuclear forces, additivity of volumes and binding energies
- The nearest nucleons interact so strongly as the molecules in a drop of water
- The nuclear properties can be described (as an approximation) with the analog quantities, i. e., radius, density, surface tension, volume energy

Liquid-Drop model and fission



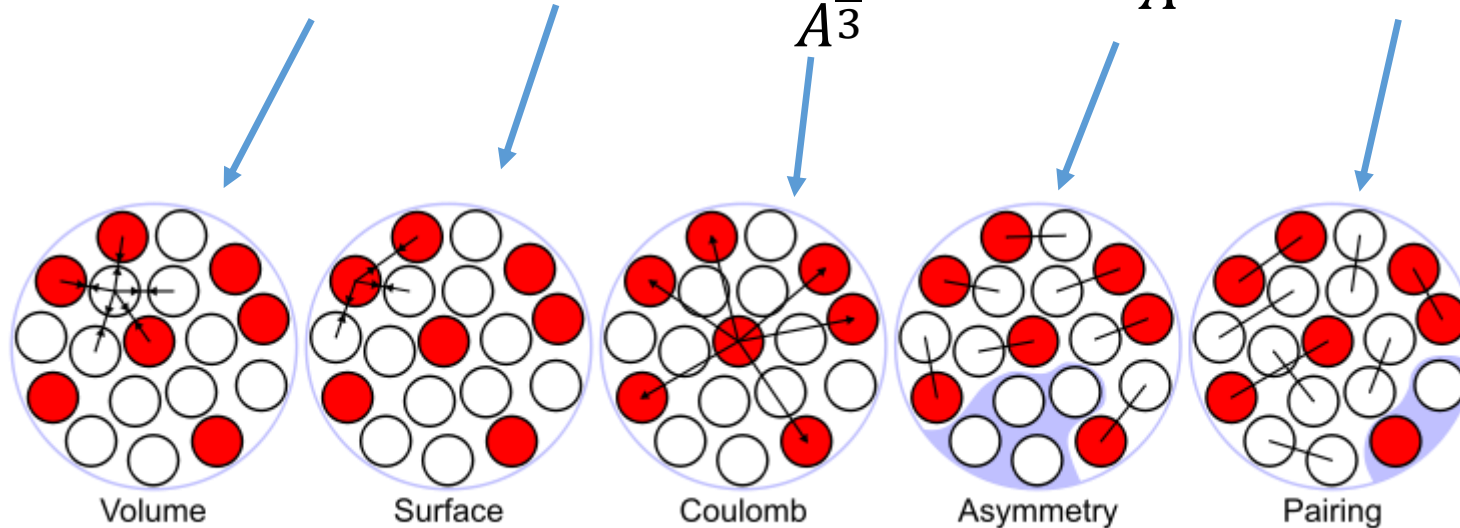
Coulomb energy
wins over
surface energy

← Coulomb energy
→ Surface energy



Bethe–Weizsäcker mass formula

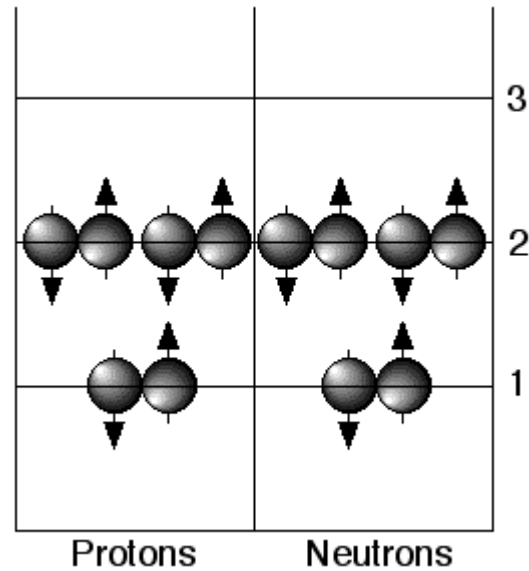
$$B(A, Z) = a_v A - a_s A^{\frac{2}{3}} - a_c \frac{Z^2}{A^{\frac{1}{3}}} - a_a \frac{(N - Z)^2}{A} + \delta(A)$$



$$\begin{aligned} a_v &= 15.7 \text{ MeV} \\ a_s &= 17.8 \text{ MeV} \\ a_c &= 0.7 \text{ MeV} \\ a_a &= 23.7 \text{ MeV} \end{aligned}$$

$$\delta(A) = \begin{cases} 33.6 A^{-\frac{3}{4}} & (\text{even} - \text{even}) \\ -36.6 A^{-\frac{3}{4}} & (\text{odd} - \text{odd}) \\ 0 & (eo, oe) \end{cases}$$

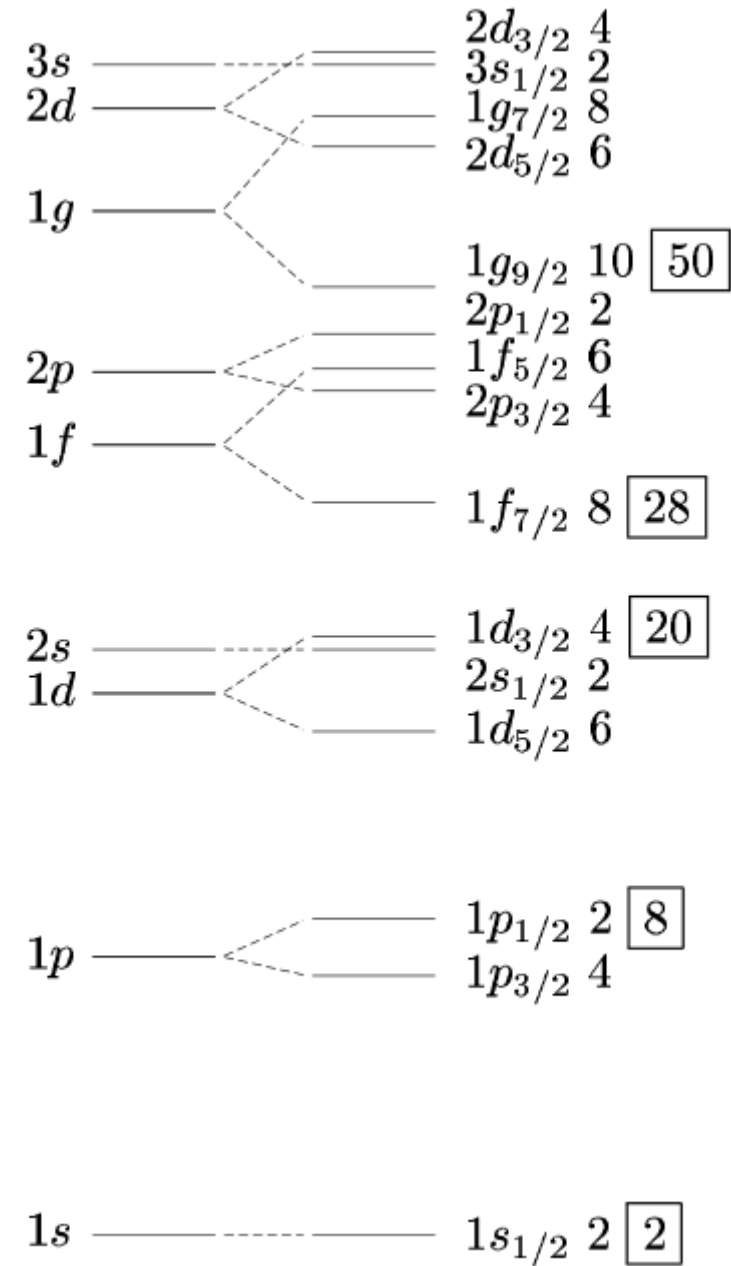
Shell model



- Analogy with atomic case: the atomic electron configuration follow the Pauli exclusion principle and the shells are filled in order of increasing energy → configuration with filled shells and some valence electrons
- Nuclear case: different kind of interaction (even not well know); two different particles (proton and neutrons); there is not a clear centre of the interaction field → BUT high performance in the description of many nuclear proprieties
- average potential $V(r)$ plus strong spin-orbit coupling → three quantum numbers n, l, j in the S.E. solutions

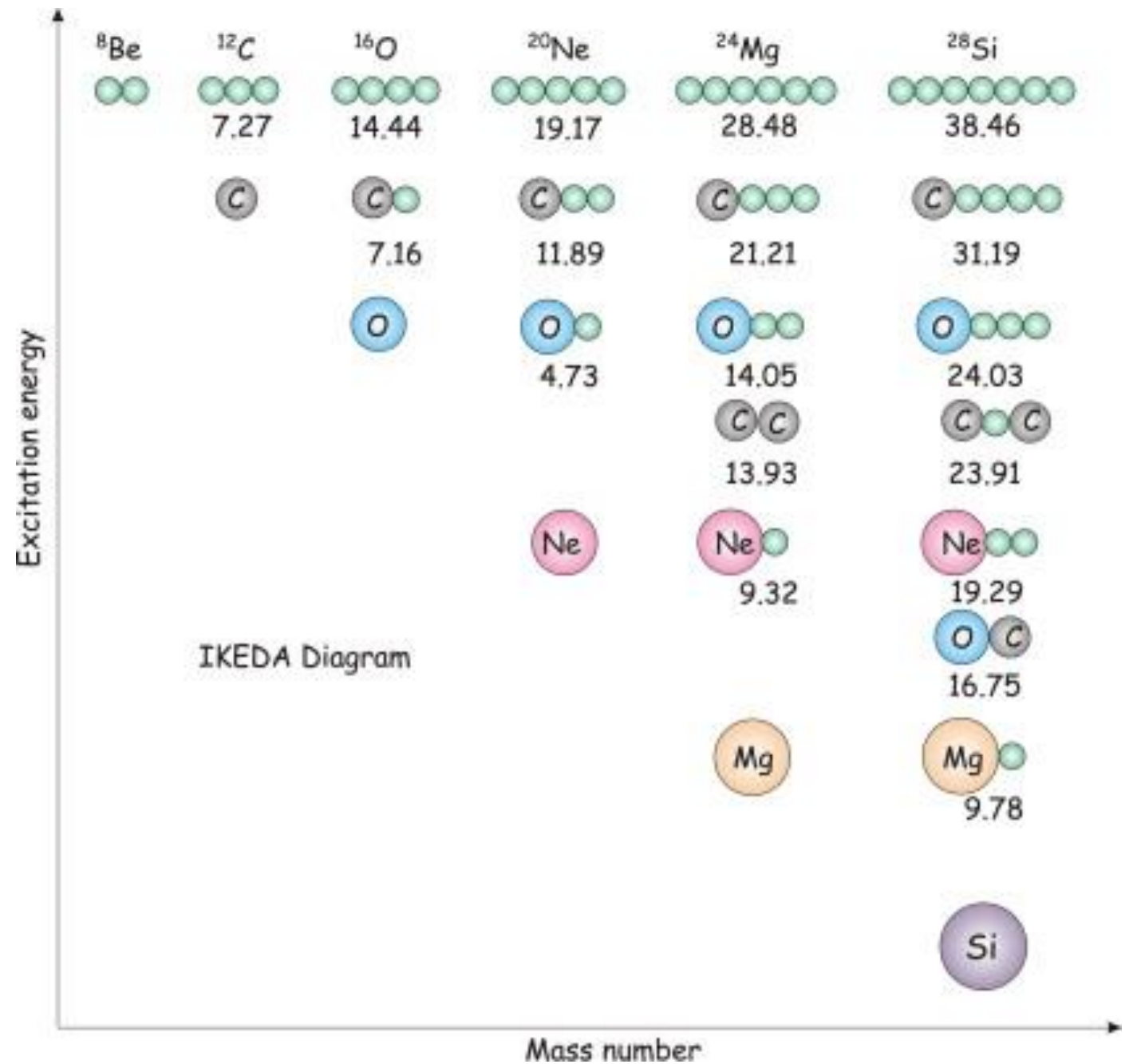
Magic numbers

- 2
- $8 = 2 + 6$
- $20 = 2 + 6 + 12$
- $28 = 2 + 6 + 12 + 8$
- $50 = 2 + 6 + 12 + 8 + 22$
- $82 = 2 + 6 + 12 + 8 + 22 + 32$
- $126 = 2 + 6 + 12 + 8 + 22 + 32 + 44$
- $184 = 2 + 6 + 12 + 8 + 22 + 32 + 44 + 58$

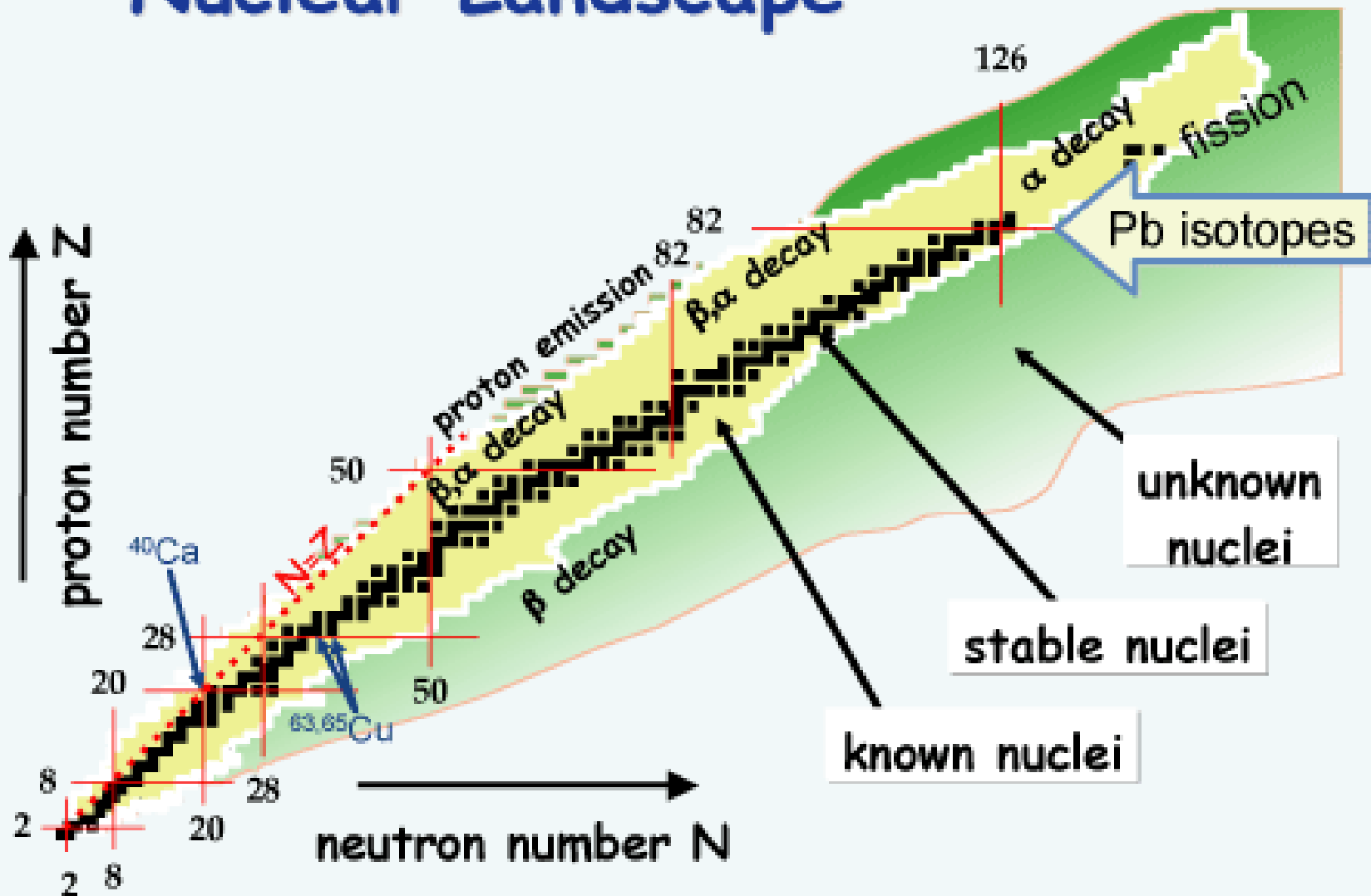


Cluster α configurations

Ikeda diagram



Nuclear Landscape



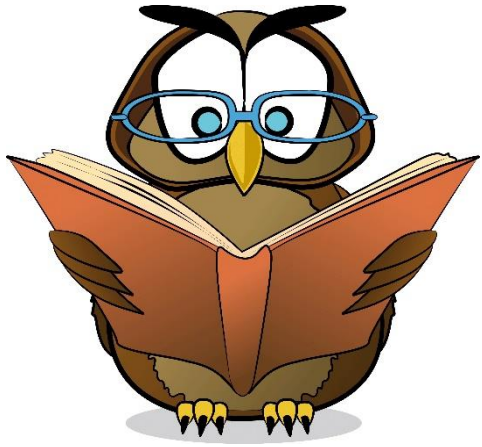
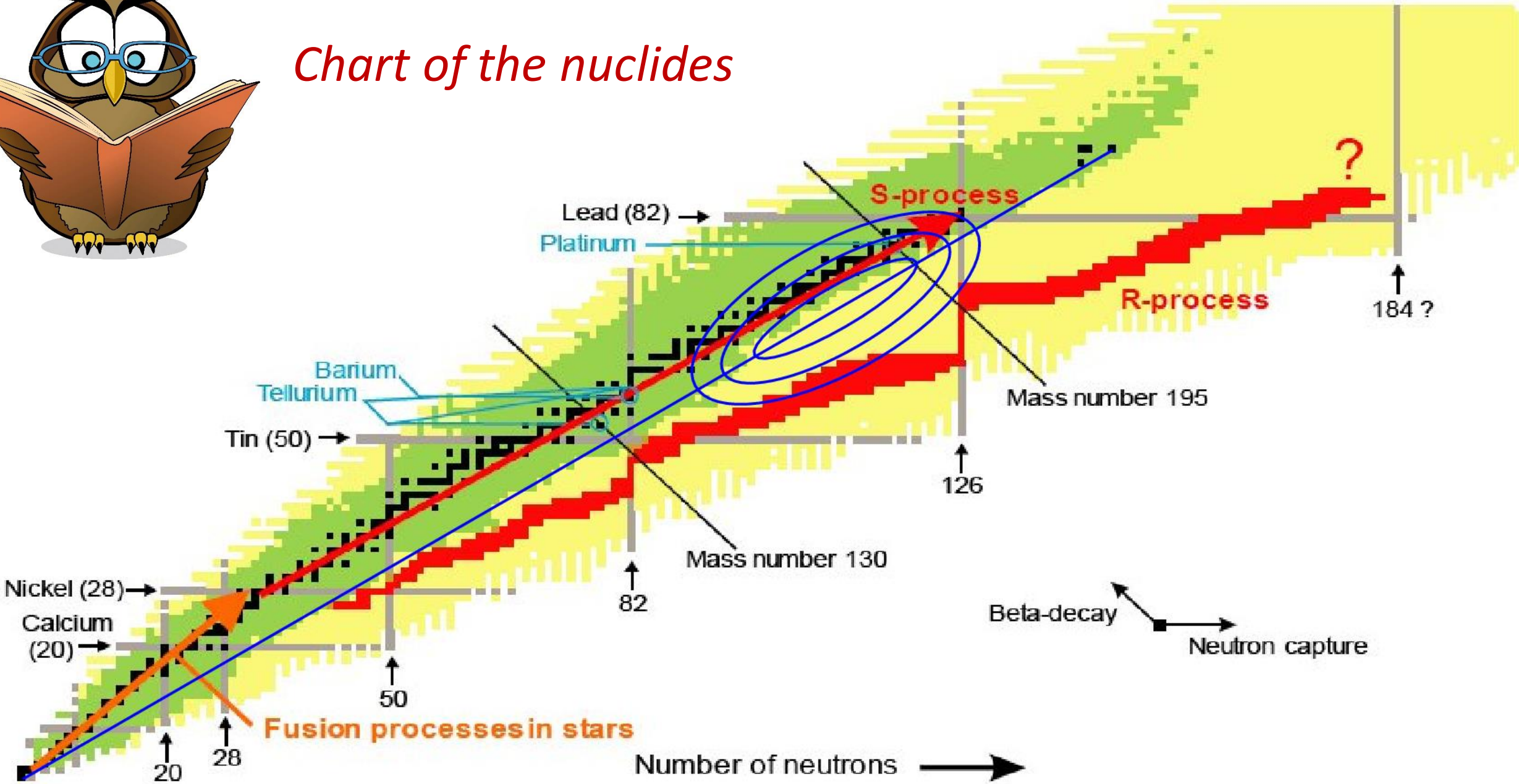


Chart of the nuclides

Number of protons ↑



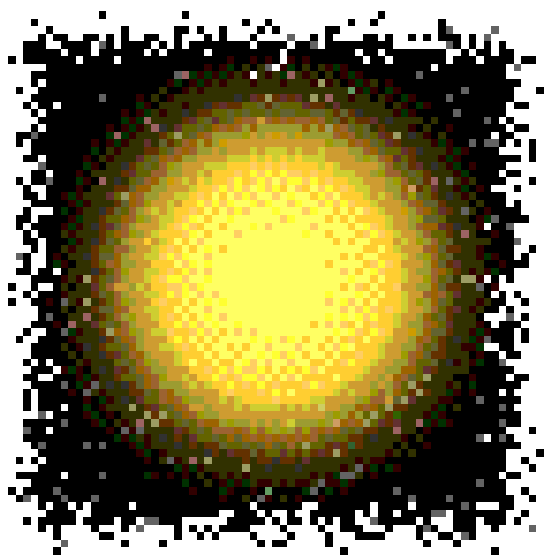
... qual è la provenienza degli elementi?



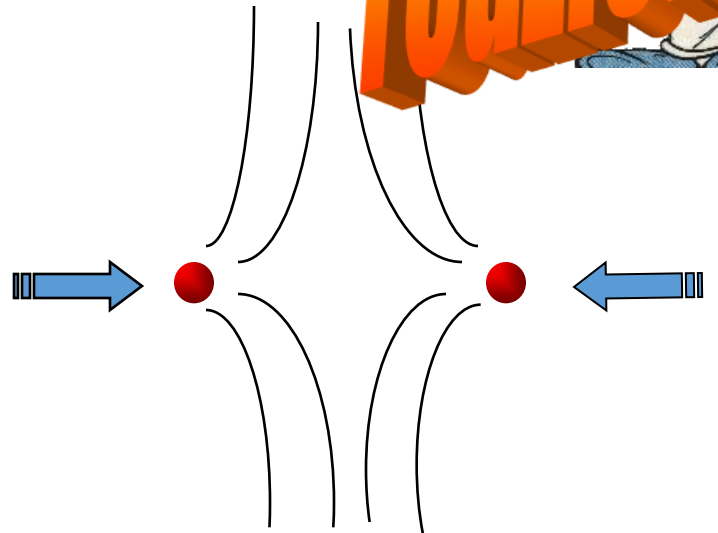
Per scoprirlo ...



... ritorniamo nelle stelle.



reazioni nucleari



● carica positiva
● carica positiva

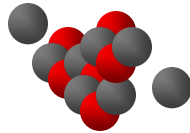
Esempi



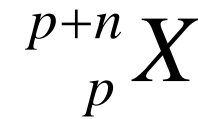
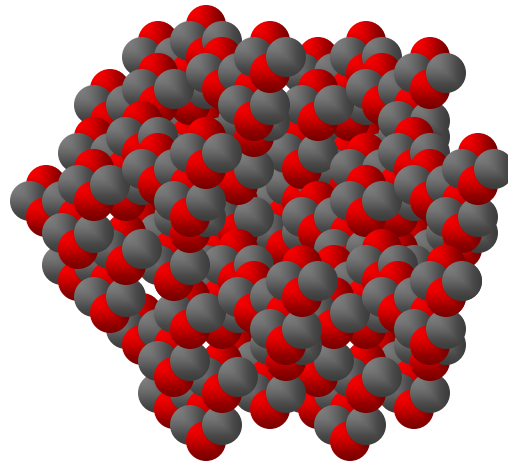
nucleo di He – particella α – $2p + 2n$



nucleo di ^{12}C – $6p + 6n$



nucleo di ^{14}C – $6p + 8n$ (isotopo del ^{12}C)



Catena p-p

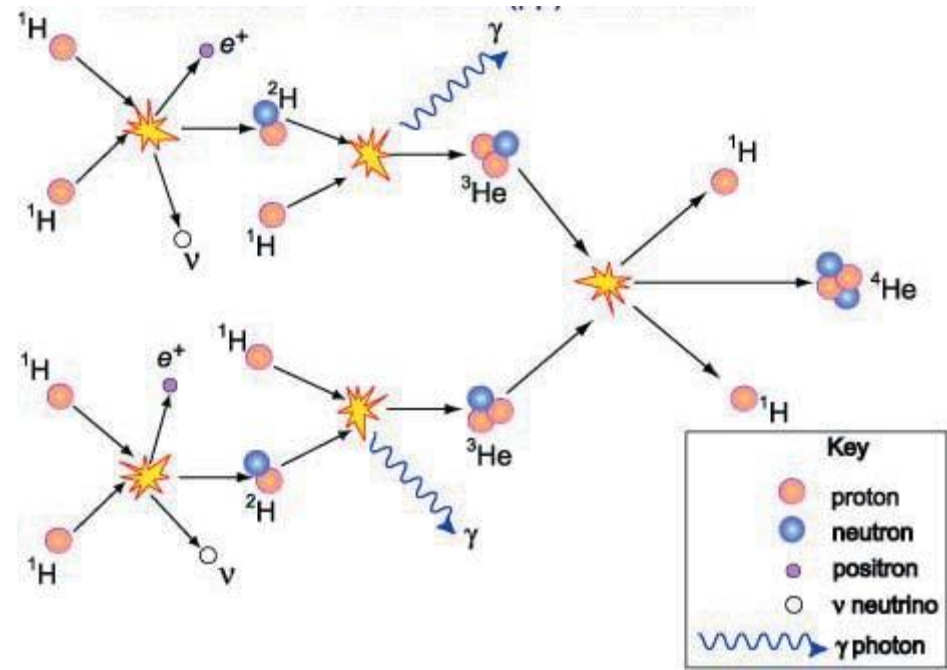


Tavola Periodica degli Elementi

1 1A 1 H Idrogeno 1.00794	2 IIA 4 Be Berillio 9.01218	13 IIIA 14 IVA 15 VA 16 VIA 17 VIIA 18 VIIIA 2 2 He Elio 4.002602
3 2 Li Litio 6.941	11 3 Na Sodio 22.989770	12 3 Mg Magnesio 24.3050
19 4 K Potassio 39.0983	20 4 Ca Calcio 40.078	36 4 Kr Kriptone 83.798
37 5 Rb Rubidio 85.4678	38 5 Sr Stronzio 87.62	54 5 Xe Xenone 131.293
55 6 Cs Cesio 132.90545	56 6 Ba Bario 137.327	86 6 Rn Radone (222)
87 7 Fr Francio (223)	88 7 Ra Radio (226)	118 7 Uuo Ununottium

Fin dai primi istanti dopo il big bang, le reazioni nucleari hanno governato l'evoluzione e la morte delle stelle, hanno determinato l'evoluzione chimica delle galassie e la produzione di tutti gli elementi dai quali dipende la nostra stessa composizione.

89 to 103	Rf Rutherfordio (261)	Db Dubnio (262)	Sg Seaborgio (266)	Bh Bohrio (264)	Hs Hassio (269)	Mt Meitnerio (268)	Ds Darmstadtio (271)	Rg Roentgenio (272)	Uub Ununbio (285)	Uut Ununtrio (284)	Uuq Ununquadio (289)	Uup Ununpentio (288)	Uuh Ununhexio (292)	Uus Ununseptium	Uuo Ununottium
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Le masse atomiche tra sono quelle degli isotopi più stabili o più comuni.

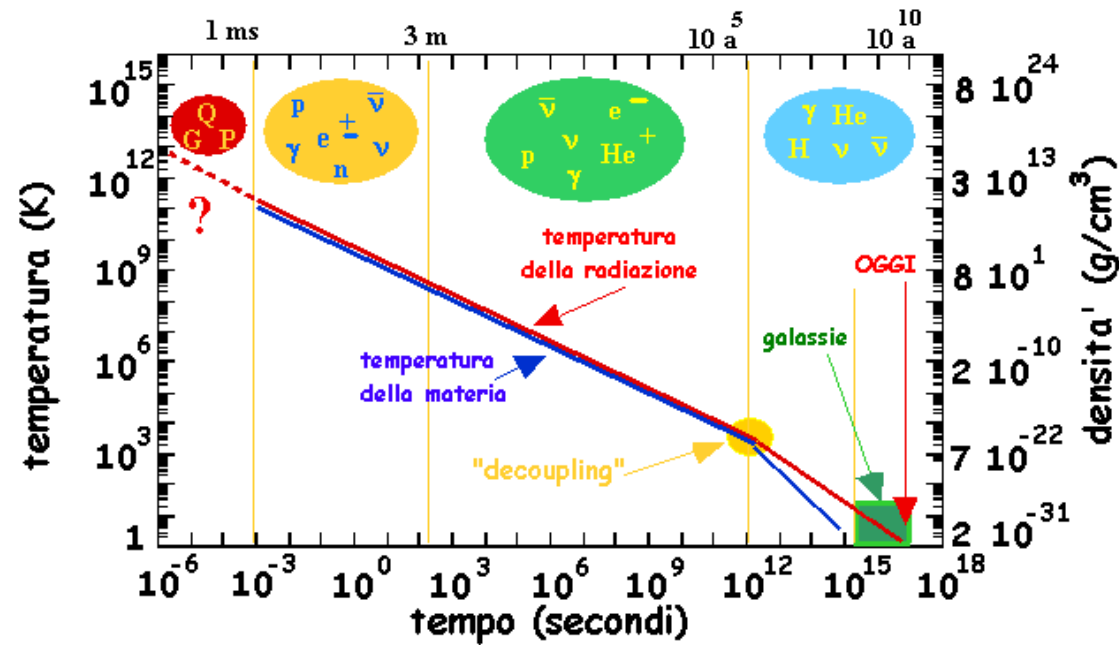
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57 La Lantanio 138.9055	58 Ce Cerio 140.116	59 Pr Praseodimio 140.90765	60 Nd Neodimio 144.24	61 Pm Promezio (145)	62 Sm Samario 150.36	63 Eu Europio 151.964	64 Gd Gadolinio 157.25	65 Tb Terbio 158.92534	66 Dy Disprosio 162.500	67 Ho Olmio 164.93032	68 Er Erbio 167.259	69 Tm Tulio 168.93421	70 Yb Itterbio 173.04	71 Lu Lutezio 174.967
89 Ac Attinio (227)	90 Th Torio 232.0381	91 Pa Protoattinio 231.03588	92 U Uranio 238.02891	93 Np Nettunio (237)	94 Pu Plutonio (244)	95 Am Americio (243)	96 Cm Curio (247)	97 Bk Berkelio (247)	98 Cf Californio (251)	99 Es Einsteinio (252)	100 Fm Fermio (257)	101 Md Mendelevio (258)	102 No Nobelio (259)	103 Lr Laurenzio (262)

Nota: il sotto gruppo dei numeri 1-18 è stato adottato nel 1984 dalla International Union of Pure and Applied Chemistry (IUPAC). I nomi degli elementi 112-118 sono gli equivalenti latini di quei nomi.

Astrofisica ↔ fisica nucleare

La fisica nucleare e l'origine dell'Universo



nei ... "primi tre minuti"
creazione p, n, d, He

$$m_p > kT \text{ per } T < 10^{12} \text{ K}$$

negli ultimi 10 miliardi di anni formazione di stelle e galassie
nascita, vita e morte delle stelle nucleosintesi degli elementi

Argomenti

- Introduzione all'Astrofisica Nucleare

 - osservazioni astronomiche e aspetti astrofisici

 - aspetti nucleari

- reazioni termonucleari

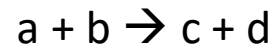
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Nuclear reactions

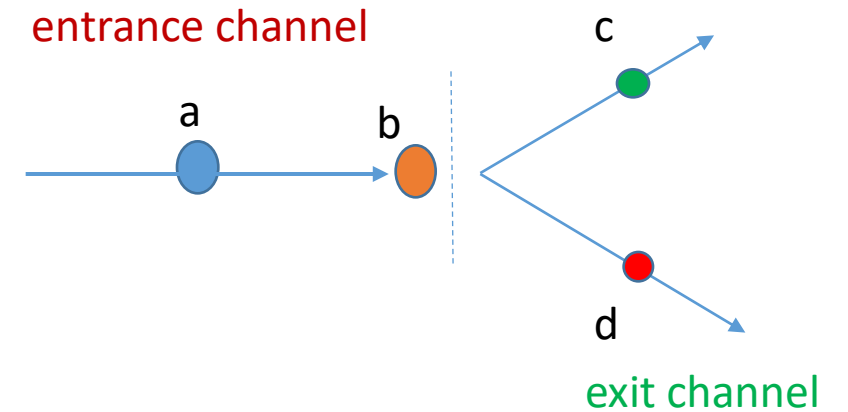
A nuclear reaction may be indicated by the following symbolic relationship



Where a and b are the colliding nuclei before the interaction, while c and d denote the products after the interaction.

Different types of reactions:

- | | |
|--|--|
| 1) $a + b \rightarrow a + b$ | <i>elastic or inelastic</i> scattering (identical species in the two channels) |
| 2) $a + b \rightarrow c + d$ | two body transfer reaction |
| 3) $a + b \rightarrow c + d + e$ | three body transfer reaction |
| 4) $a + b \rightarrow c + \gamma$ | radiative capture reaction |
| 5) $a + \gamma \rightarrow b + c$ | photodisintegration reaction |
| 6) $(a + b) + c \rightarrow a + b + c$ | breakup reaction |



Most nuclear interactions of astrophysical interest involve just two species before and after the interaction.

Energetics of Nuclear reactions

The total relativistic energy in a nuclear reaction must be conserved:

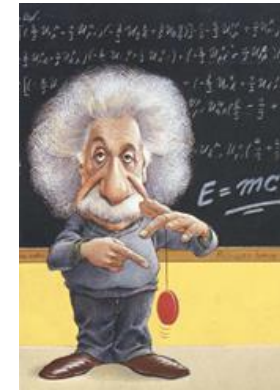
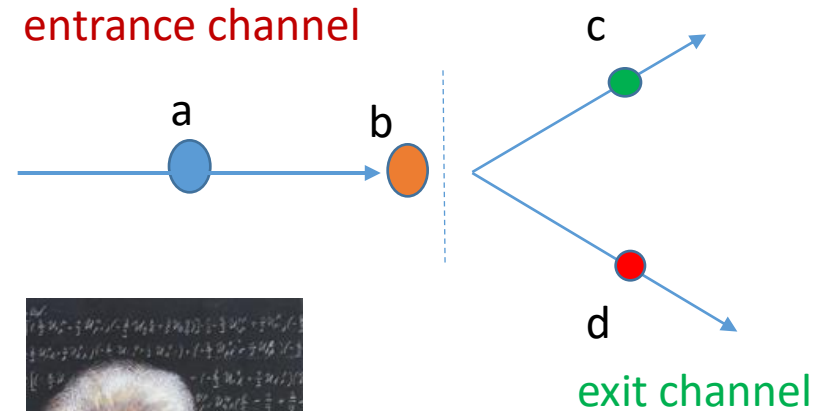
Bilancio energetico

$$a + b \rightarrow c + d$$

$$m_a c^2 + m_b c^2 + E_a + E_b = m_c c^2 + m_d c^2 + E_c + E_d$$

or

$$Q_{(a+b \rightarrow c+d)} = \underbrace{m_a c^2 + m_b c^2}_{\text{in}} - \underbrace{m_c c^2 - m_d c^2}_{\text{out}} = \underbrace{E_c + E_d}_{\text{out}} - \underbrace{E_a - E_b}_{\text{in}}$$

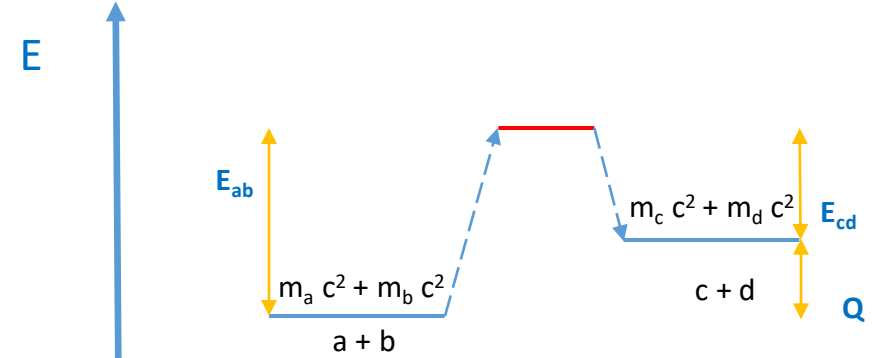


where E_i are kinetic energies, m_i are rest masses and $Q_{(a+b \rightarrow c+d)}$ is the reaction Q-value

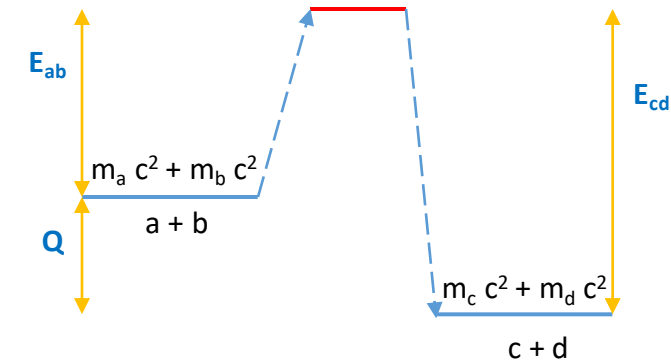
The *reaction Q-value* is the difference in masses before and after the reaction, or the difference in kinetic energies after and before the reaction. It is equal to the reaction energy release.

Energetics of Nuclear reactions

- If **Q is positive**, the reaction releases energy and is called **exothermic**.
- Otherwise the reaction consumes energy and is called **endothermic**.
- **Apart from a few exceptions, the most important nuclear reactions in stars are exothermic ($Q > 0$).**
- The quantities E_{ab} and E_{cd} represent the total kinetic energies in the center-of-mass system before and after the reaction, respectively.



$$Q = (m_a + m_b - m_c - m_d)c^2 = E_{cd} - E_{ab}$$



$$Q = (m_a + m_b - m_c - m_d)c^2 = E_{cd} - E_{ab}$$

Esempio: energia scambiata nella formazione di un nucleo di elio

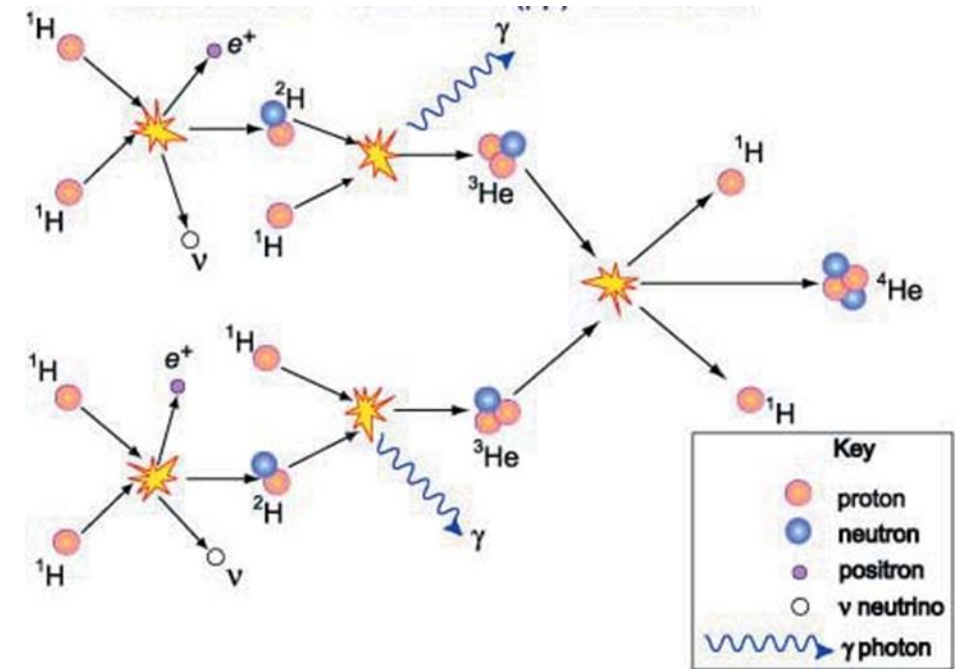
$$\alpha = 2p + 2n$$

$$2p + 2n \rightarrow 2 * 938 + 2 * 939.5 = 3755 \text{ MeV}$$

$$\alpha \rightarrow 3727 \text{ MeV}$$

$$(m_i - m_f)c^2 = Q_{\text{value}} = 3755 - 3727 = 28 \text{ MeV}$$

$$2p + 2n \rightarrow \alpha + 28 \text{ MeV} \quad !!!$$

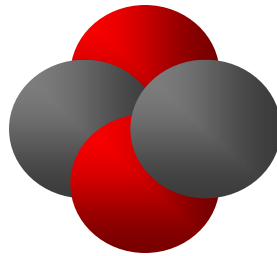


nuclei stabili

reazioni nucleari

energia corrispondente a

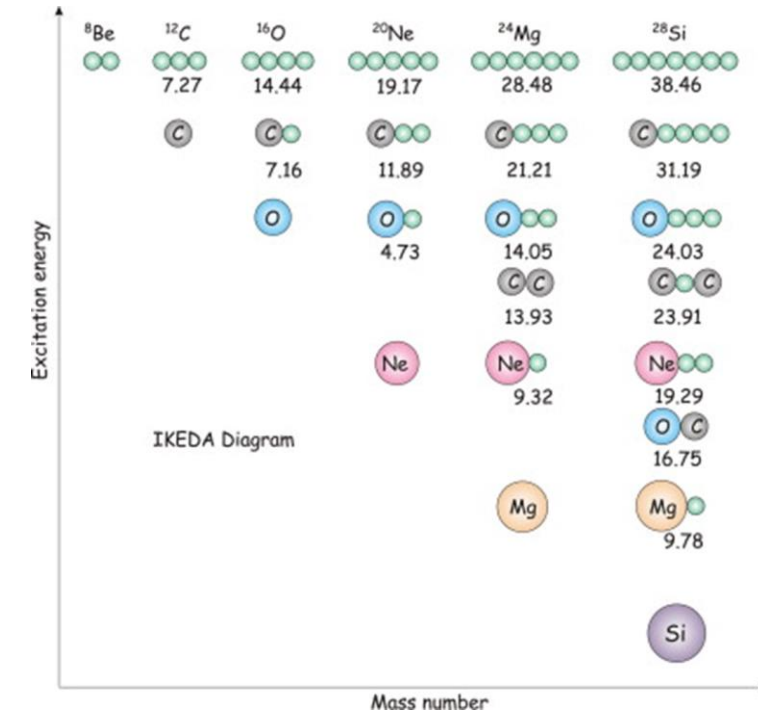
10 milioni di gradi $\rightarrow \sim \text{keV}$ ($1 \text{ eV} = 1.6 \cdot 10^{-19} \text{ J}$)



particella α

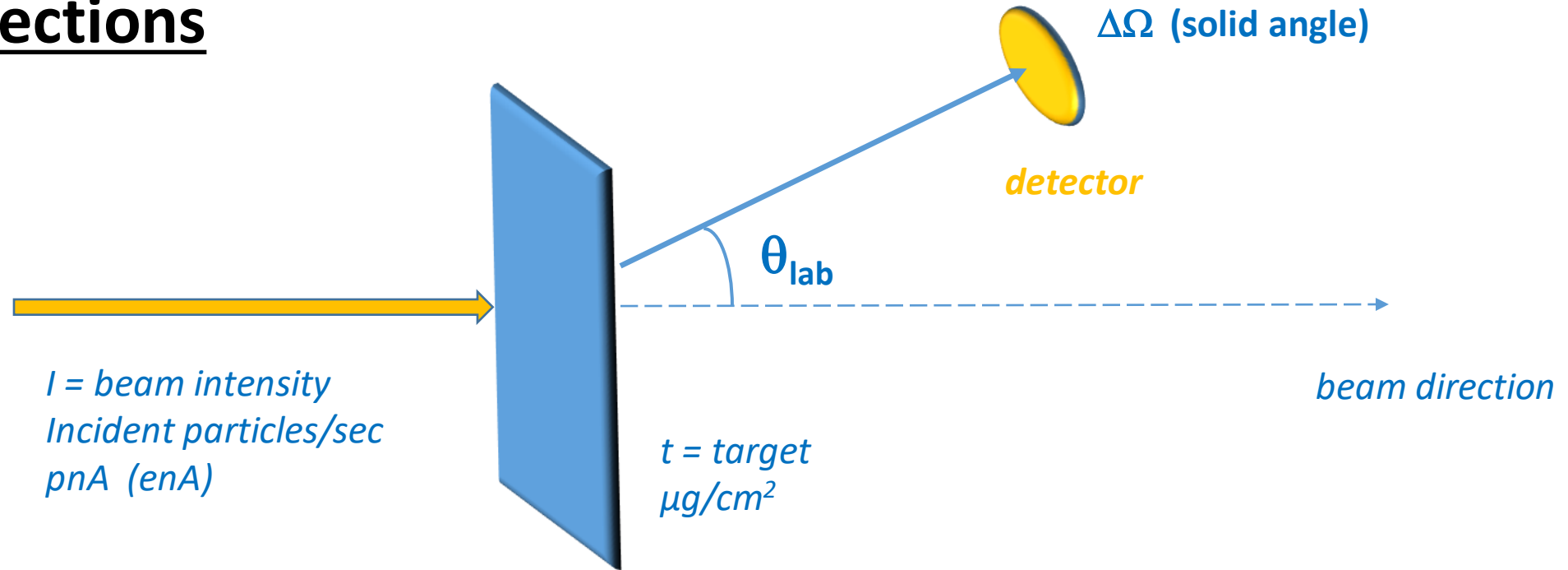
energia di legame $28 \text{ MeV} \rightarrow$

100 miliardi di gradi !!!



Come posso descrivere la probabilità che una reazione nucleare avvenga? ... sezione d'urto (cross section)

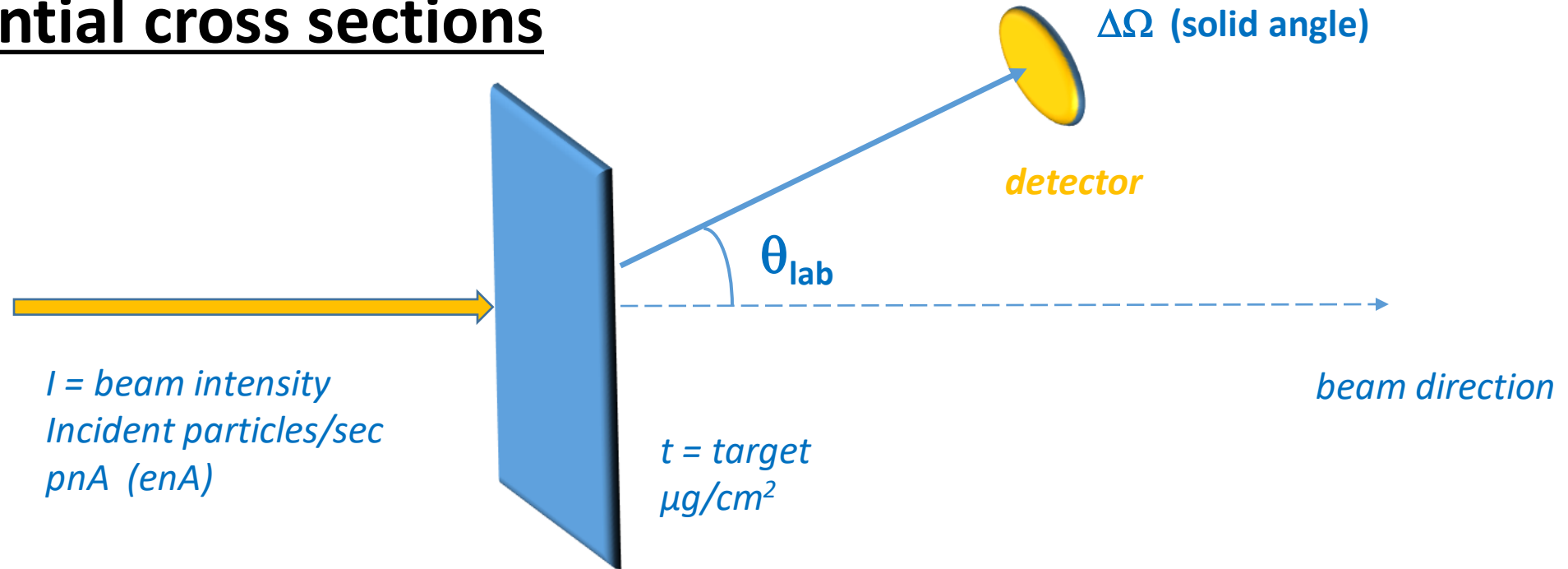
Cross sections



$$\sigma \equiv \frac{\text{(number of interactions per time)}}{\text{(number of incident particles per area per time)} \text{(number of target nuclei within the beam)}} = \frac{N_R/t}{(N_b/tA)N_t}$$

The *cross section* is a quantitative measure of an interaction probability \rightarrow **1 barn = 10^{-24} cm^2**

Differential cross sections



$$\frac{d\sigma}{d\Omega} = \frac{N_d/t}{(N_b/t)(N_t/A)} \frac{1}{d\Omega}$$

$N_d = \text{number of products detected}$

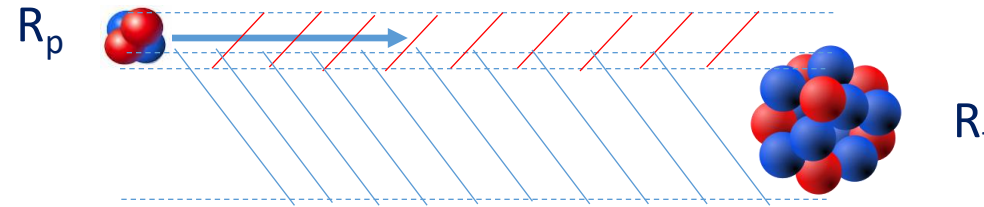
$$\frac{d\sigma}{d\Omega} \rightarrow \text{mbarn/sr}$$

(geometrical efficiency)

Classically

$$1 \text{ b} = 10^{-24} \text{ cm}^2 = 10^{-28} \text{ m}^2$$

$$1 \text{ fm}^2 = (10^{-15})^2 \text{ m}^2 = 10^{-2} \text{ b}$$



$$\sigma = \pi (R_p + R_t)^2$$

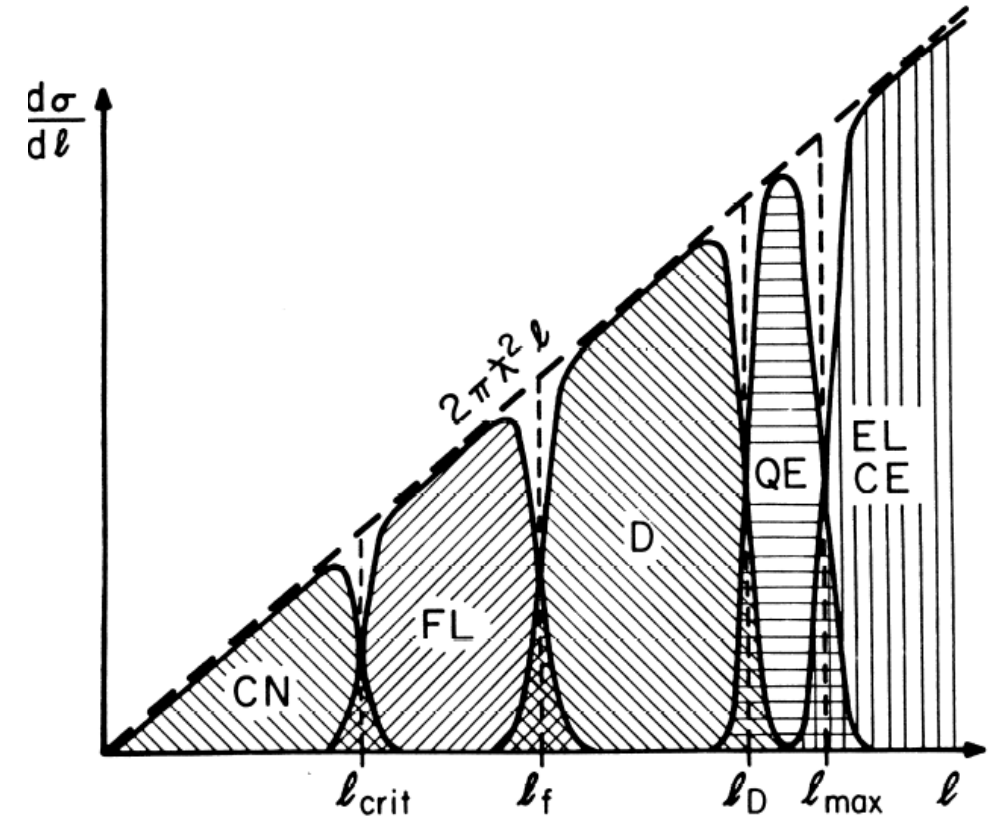
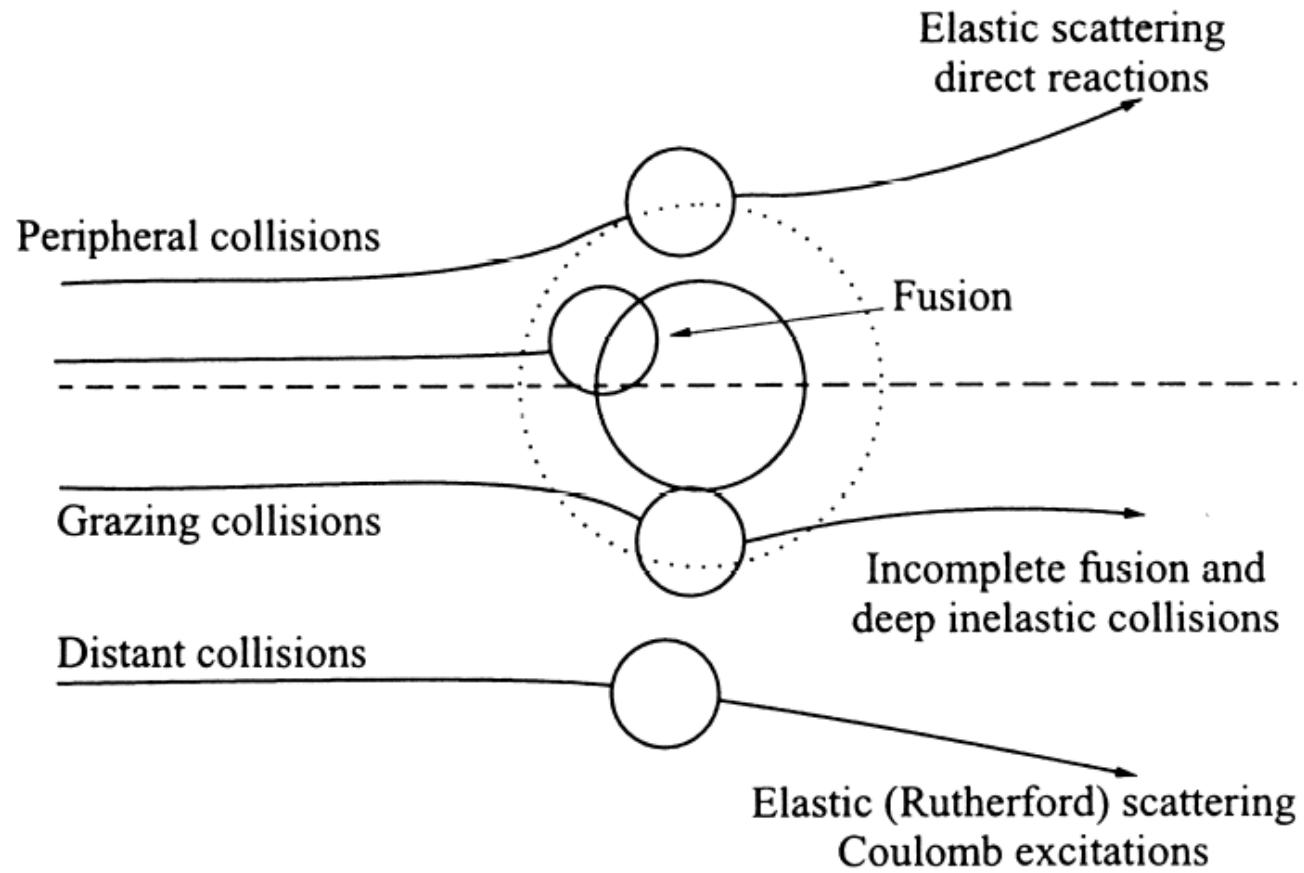
$$R = R_0 A^{\frac{1}{3}}$$

$$R_0 \cong 1.2 \text{ fm} = 1.2^{-13} \text{ cm}$$

collision	$\sigma \text{ (cm}^2\text{)}$
$^1\text{H} + ^1\text{H}$	0.2×10^{-24}
$^1\text{H} + ^{238}\text{U}$	2.8×10^{-24}
$^{238}\text{U} + ^{238}\text{U}$	4.8×10^{-24}

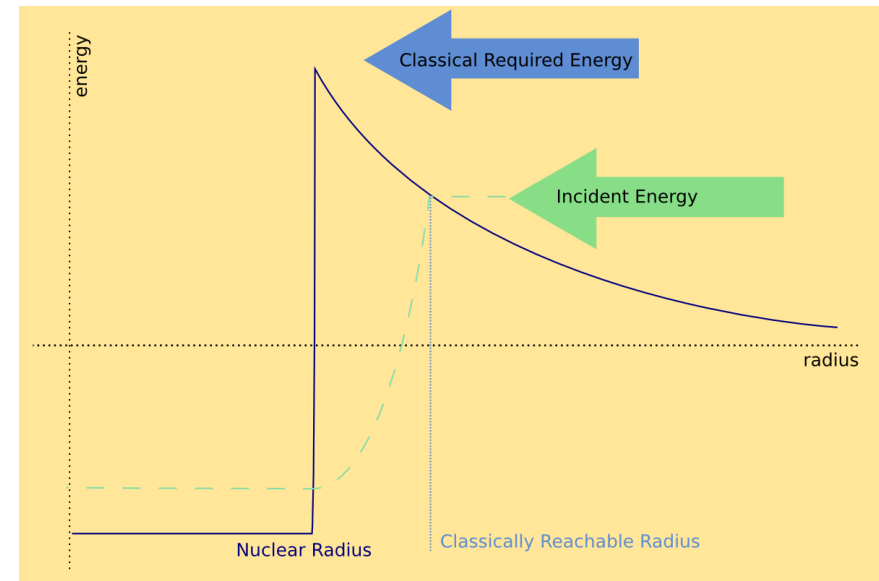
Strong force $^{15}\text{N}(p,\alpha)^{12}\text{C}$	$\sigma = 0.5 \text{ b}$	$E_p = 2.0 \text{ MeV}$
Electromagnetic force $^3\text{He}(\alpha,\gamma)^7\text{Be}$	$\sigma = 10^{-6} \text{ b}$	$E_p = 2.0 \text{ MeV}$
Weak force $p(p,e+\nu)d$	$\sigma = 10^{-20} \text{ b}$	$E_p = 2.0 \text{ MeV}$

Heavy ion reactions

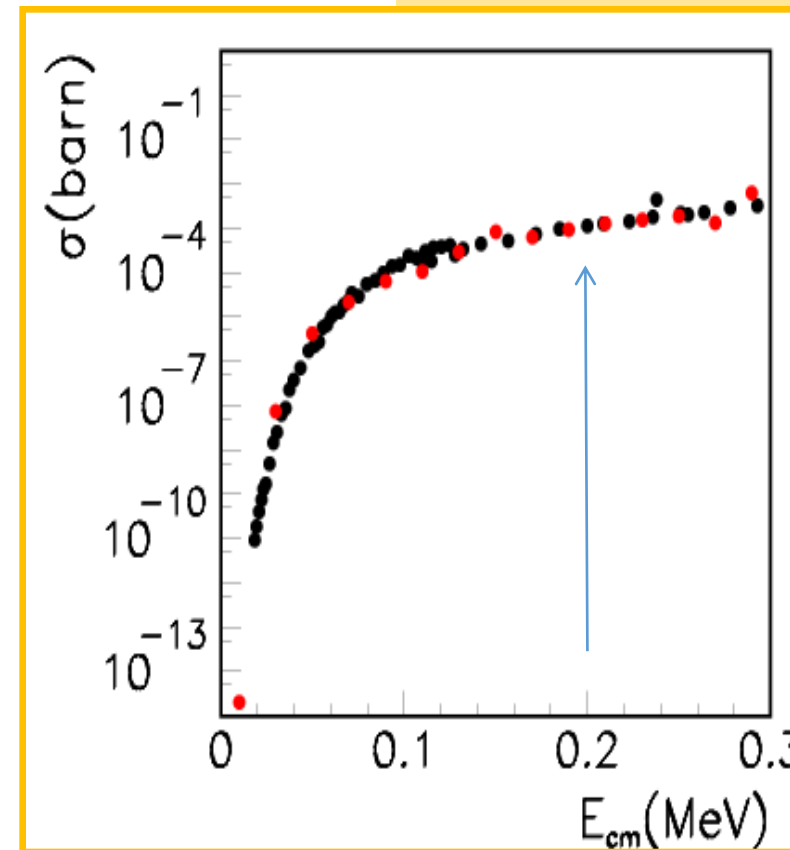


Cross section and coulomb barrier

$$E_c = \frac{1}{4\pi\epsilon_0} \frac{Z_1 Z_2 e^2}{(R_1 + R_2)} \approx 1.2 \frac{Z_1 Z_2}{\left(A_1^{\frac{1}{3}} + A_2^{\frac{1}{3}}\right)} \text{ MeV}$$



Examples:



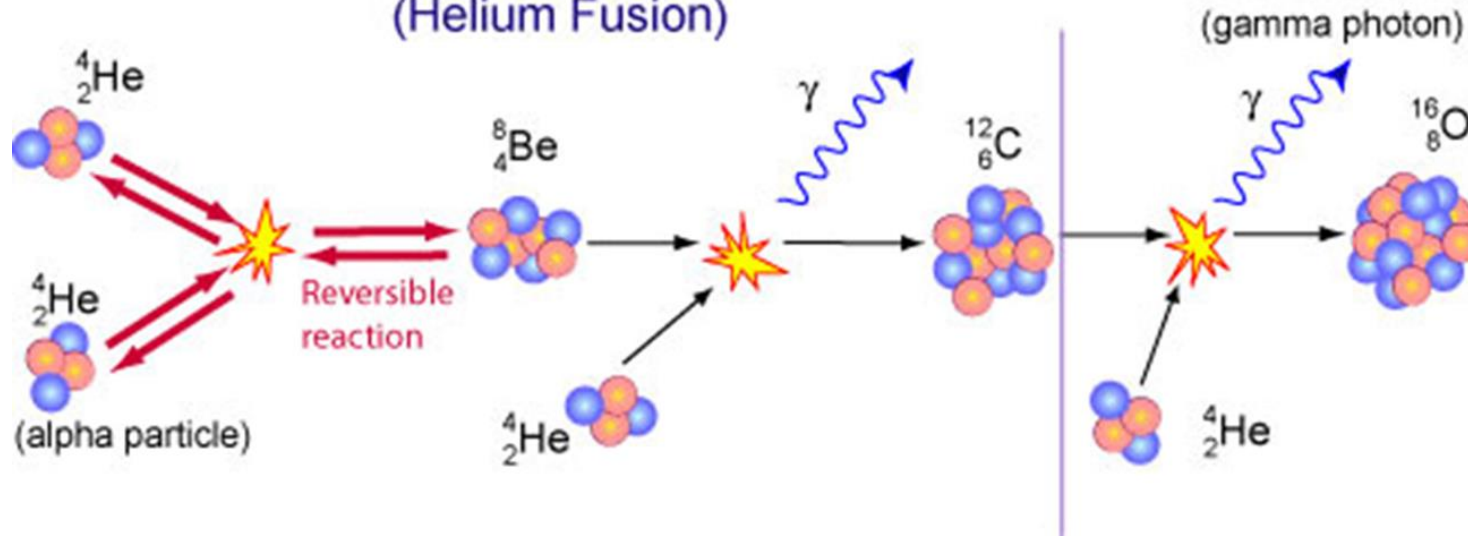
$^{10}\text{B} + \text{p}$

$E_c = 1.9 \text{ MeV}$

$E_{cm} = 0.2 \text{ MeV}$

Esempio

The Triple Alpha Process (Helium Fusion)



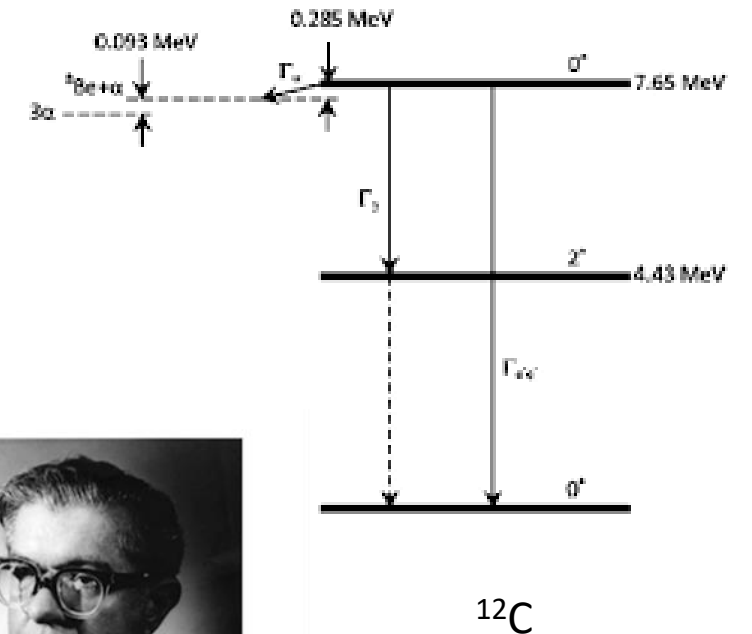
$T = 100 \text{ MK} !!!$

Alto numero di reazioni (rate) fortemente improbabili



Fred Hoyle

1915-2001



Argomenti

- Introduzione all'Astrofisica Nucleare

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Energy production in stars: Thermonuclear Reactions

The *reaction Q-value* is the difference in masses before and after the reaction, or the difference in kinetic energies after and before the reaction. It is equal to the reaction energy release.

$$\sigma \equiv \frac{\text{(number of interactions per time)}}{\text{(number of incident particles per area per time)} \text{(number of target nuclei within the beam)}} = \frac{N_R/t}{(N_b/tA)N_t}$$

Reaction rate: number of reactions per time t and unit volume V

Nuclear reaction rate – particle-induced reactions

Consider the reaction



Where both the projectile 1 and the target 2 are particles with rest mass.
This means that neither 1 nor 2 represents a photon.

$$r_{12} = N_1 N_2 v \sigma(v)$$

Where $N_1 = N_b/V$ $N_2 = N_t/V$

Nuclear reaction rate – particle-induced reactions

In a stellar plasma the relative velocity of the interacting 1 – 2 nuclei is not constant, but it is described by a distribution of relative velocities with a probability function $P(v)$.

$P(v)dv$ represents the probability that v is within the $v - v + dv$ range

with $\int_0^\infty P(v)dv = 1$

Therefore

$$r_{12} = N_1 N_2 \int_0^\infty v P(v) \sigma(v) dv = N_1 N_2 \langle \sigma v \rangle_{12}$$

Where $\langle \sigma v \rangle_{12} = \int_0^\infty v P(v) \sigma(v) dv$ is the reaction rate per particle pair

$N_1 N_2$ represents pair density of nonidentical 1 and 2 nuclei

Nuclear reaction rate – particle-induced reactions

In stellar plasma the relative velocity is generated by the thermal motion and the nuclear reactions are called *thermonuclear reactions*.

In most cases the velocities of nuclei can be described by a *Maxwell-Boltzmann* distribution

$$P(v)dv = \left(\frac{m_{12}}{2\pi kT} \right)^{3/2} e^{-m_{12}v^2/(2kT)} 4\pi v^2 dv$$

Where $m_{12} = \frac{m_1 m_2}{(m_1 + m_2)}$ is the reduced mass

$k = 8.6173 \times 10^{-5}$ eV/K is the Boltzmann constant

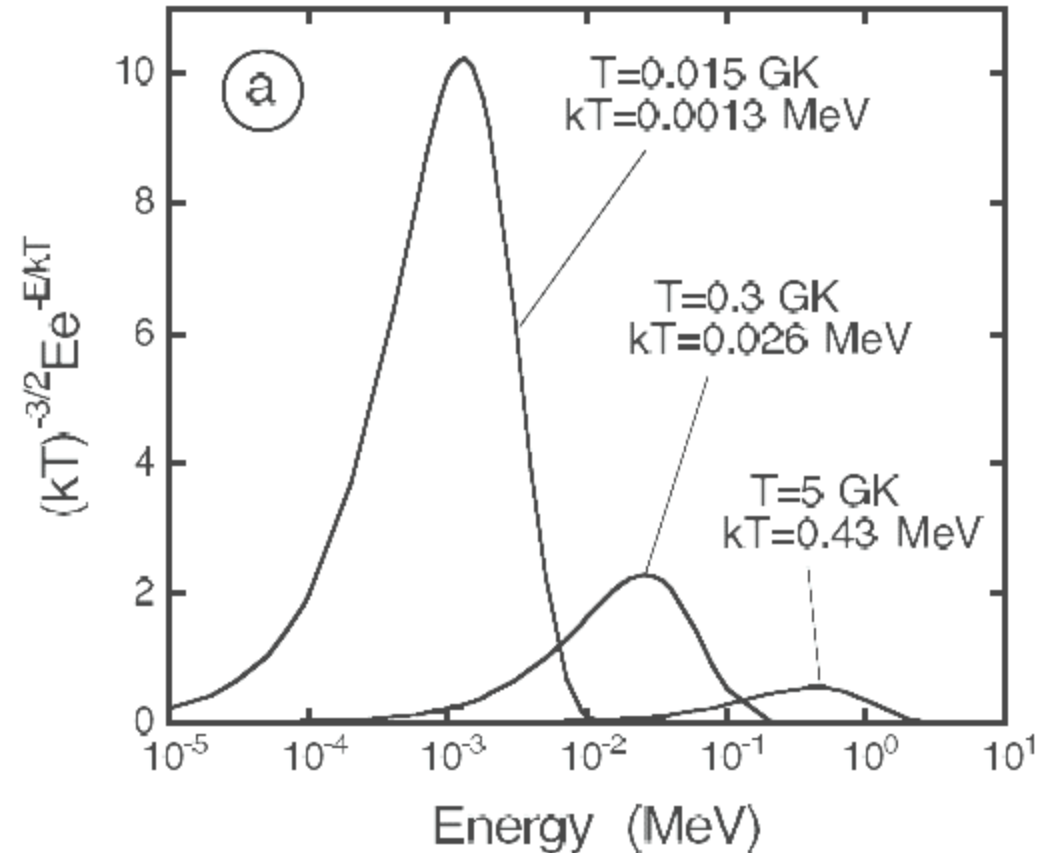
Nuclear reaction rate – particle-induced reactions

Maximum at $E = kT$

$T = 15 \text{ MK} \rightarrow$ Sun core

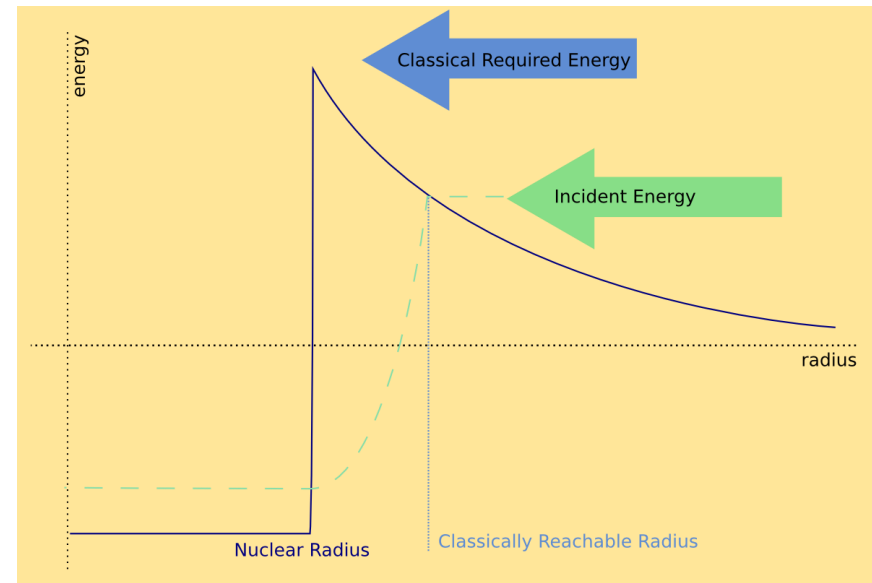
$T = 300 \text{ MK} \rightarrow$ nova

$T = 5 \text{ GK} \rightarrow$ supernova



Cross section and coulomb barrier

$$E_c = \frac{1}{4\pi\epsilon_0} \frac{Z_1 Z_2 e^2}{(R_1 + R_2)} \approx 1.2 \frac{Z_1 Z_2}{(A_1^{1/3} + A_2^{1/3})} \text{ MeV}$$



Examples:



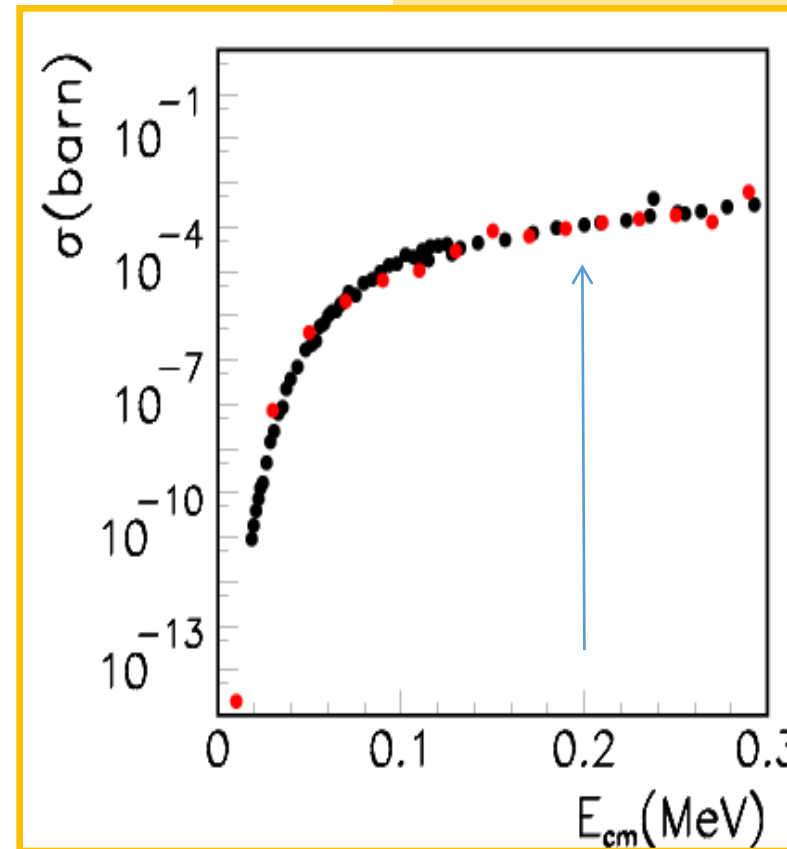
$$E_c = 0.60 \text{ MeV}$$



$$E_c = 0.48 \text{ MeV}$$



$$E_c = 1.51 \text{ MeV}$$



$^{10}\text{B} + \text{p}$

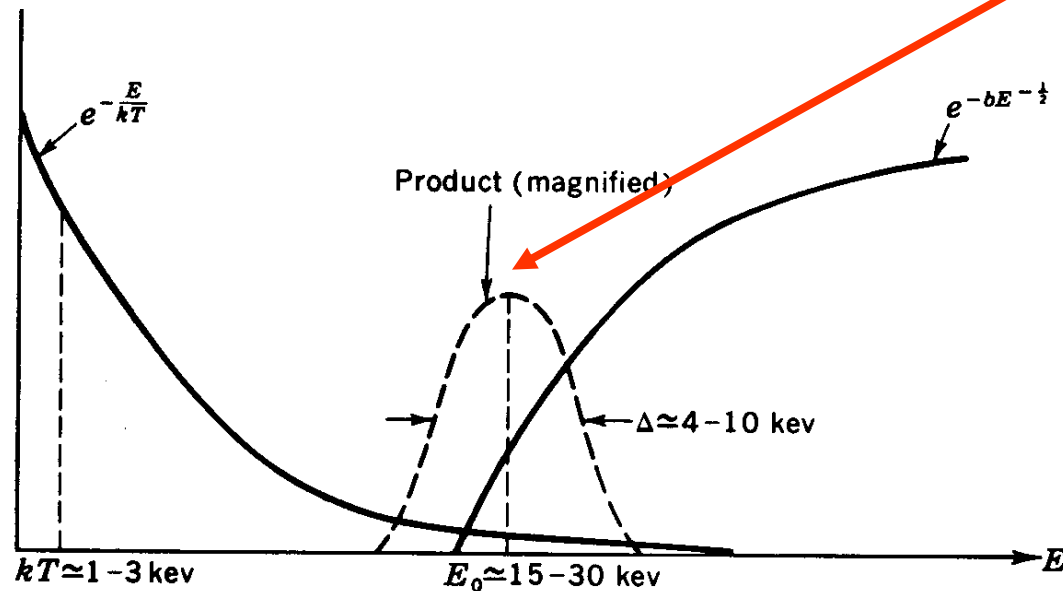
$E_c = 1.9 \text{ MeV}$

$E_{cm} = 0.2 \text{ MeV}$

Charged particle-induced reactions (non-resonant)

$$\langle \sigma v \rangle = \left(\frac{8}{\pi m_{ab}} \right) \frac{1}{2} \frac{1}{(kT)^{\frac{3}{2}}} \int_0^{\infty} S(E) e^{-\left(\frac{b}{\sqrt{E}} + \frac{E}{kT} \right)} dE$$


Gamov Peak



Note: relevant cross section in tail of M.B. distribution, much larger than kT (very different from n-capture !)

For astrophysical purposes the **reaction rates** are needed.

The nuclear physicist have been asked to measure the nuclear reaction **cross sections** in the astrophysical relevant energy region.

If the nuclear reactions are induced by **charged particles**, two coulomb effects represent a limitation in direct measurements:

- 1) Coulomb barrier
- 2) Electron screening

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Stellar environments

nuclear processes



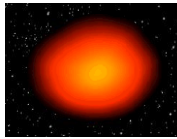
Big Bang
(primordial nucleosynthesis)

Reaction light elements
p, d, He, Be, Li, B



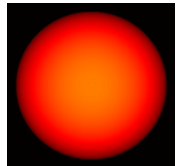
Main sequenza
(es. Sun)

H burning
proton - proton chain , cicle
CNO, cicle Ne-Na, cicle Mg-Al



Red Gigant, asymptotic branch

'He burning
 3α -process, $^{12}\text{C}(\alpha,\gamma)^{16}\text{O}$
(α,γ) and (α,n) reazioni



Super gigant
Wolf-Rayet e
Pre-supernovae

advanced stages of burning
Reaction C, O, N, Ne, Si...



Novae, supernovae,
X-ray bursts

explosive burning
Cicle HCNO
Process rp



AGB stars,
supernovae II,
Neutrons stars

nucleosynthesis beyond iron
s-process
r-process
Photodisintegration and p-process

STELLAR LIFE CYCLE

BIRTH

gravitational contraction

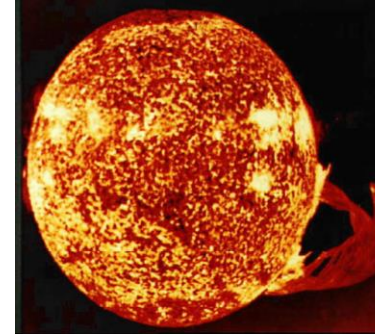
mixing of
interstellar gas

INCREASE THE mixing of
interstellar gas



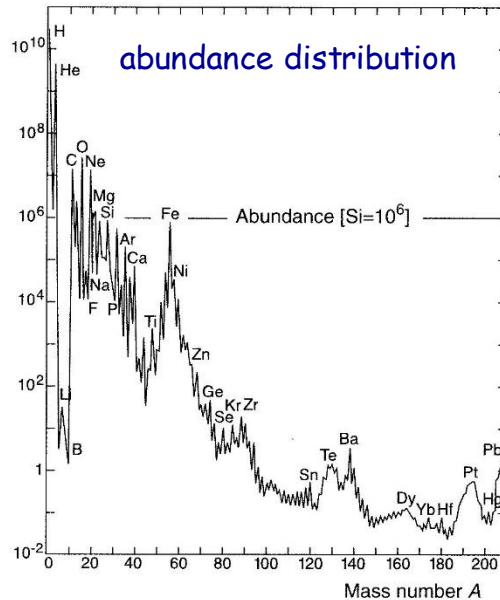
Stars

thermonuclear
reactions

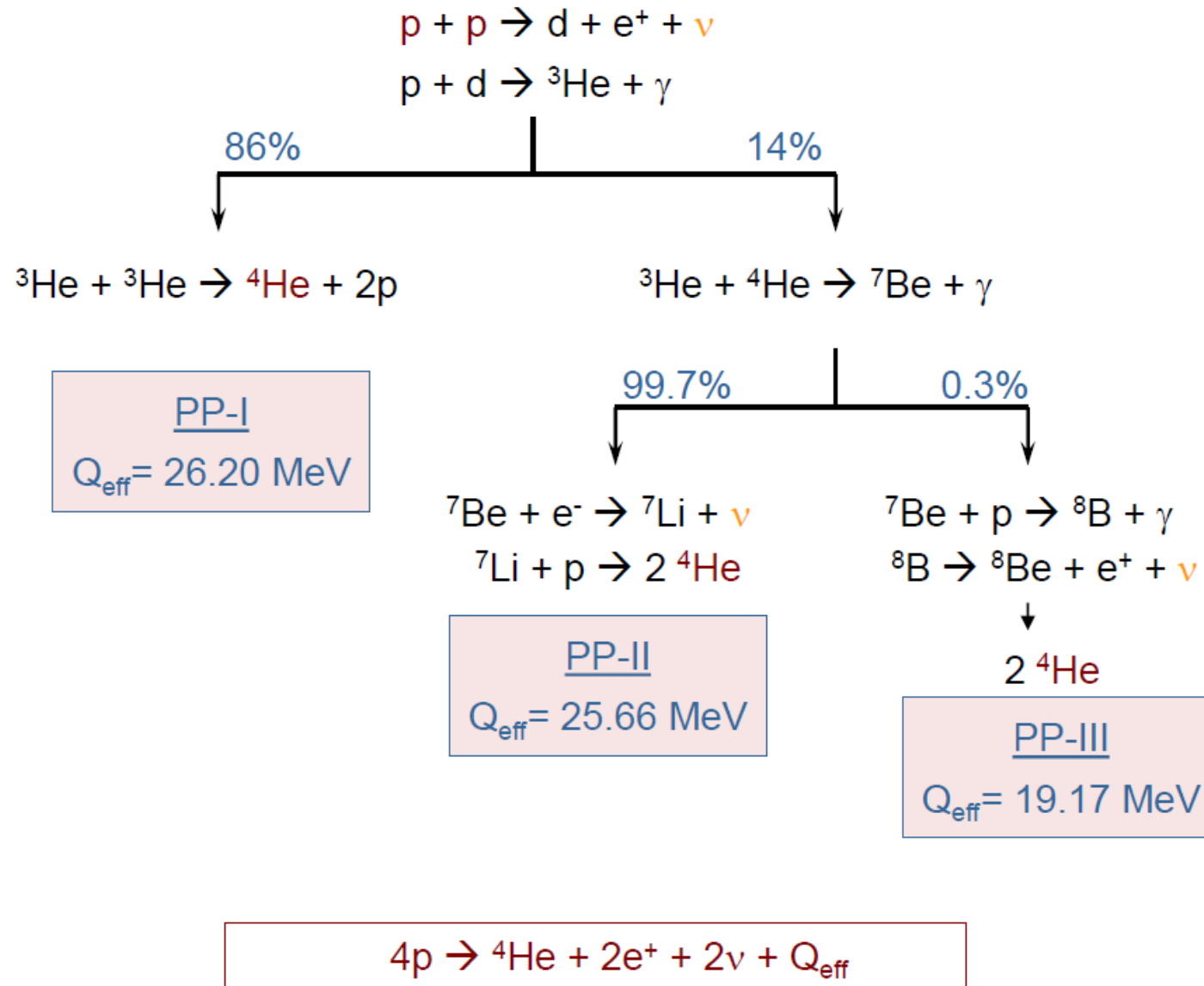


explosion
DEATH

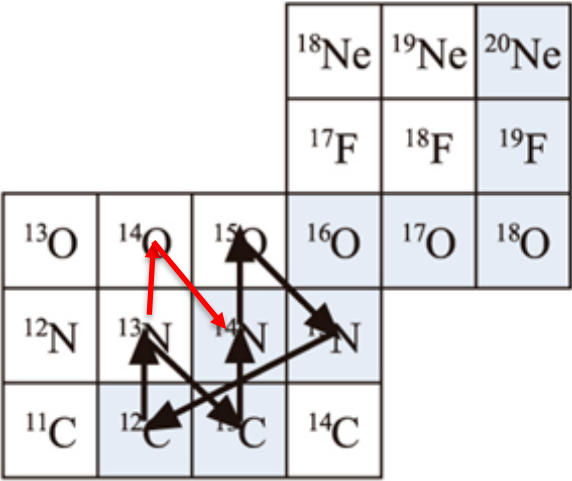
- energy production
- stability against collapse
- synthesis of "metals"



Proton-Proton-Chain

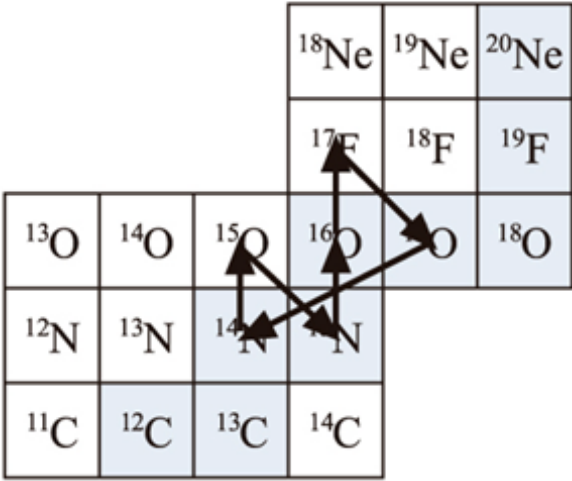


Hydrogen burning: CNO cycles

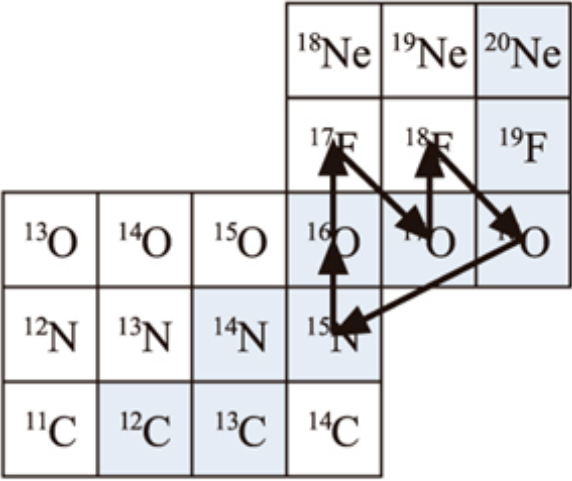


CNO1

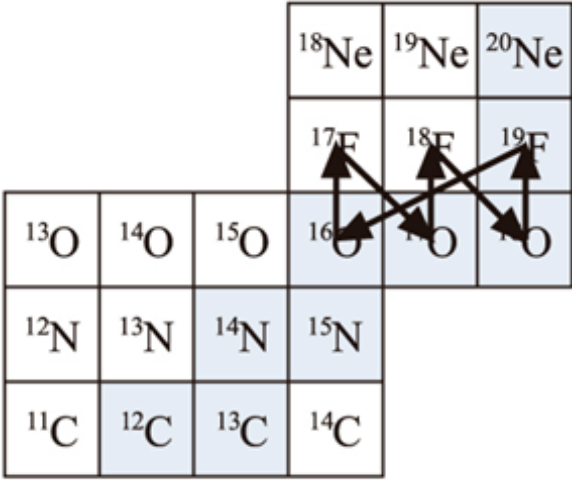
^{13}N : $T_{1/2} = 9.965 \text{ min}$



CNO2



CNO3



CNO4

CNO1

- $^{12}\text{C}(p,\gamma)^{13}\text{N}$
- $^{13}\text{N}(\beta^+ \nu)^{13}\text{C}$
- $^{13}\text{C}(p,\gamma)^{14}\text{N}$
- $^{14}\text{N}(p,\gamma)^{15}\text{O}$
- $^{15}\text{O}(\beta^+ \nu)^{15}\text{N}$
- $^{15}\text{N}(p,\alpha)^{12}\text{C}$

CNO2

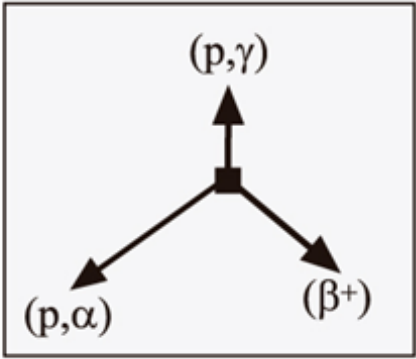
- $^{14}\text{N}(p,\gamma)^{15}\text{O}$
- $^{15}\text{O}(\beta^+ \nu)^{15}\text{N}$
- $^{15}\text{N}(p,\gamma)^{16}\text{O}$
- $^{16}\text{O}(p,\gamma)^{17}\text{F}$
- $^{17}\text{F}(\beta^+ \nu)^{17}\text{O}$
- $^{17}\text{O}(p,\alpha)^{14}\text{N}$

CNO3

- $^{15}\text{N}(p,\gamma)^{16}\text{O}$
- $^{16}\text{O}(p,\gamma)^{17}\text{F}$
- $^{17}\text{F}(\beta^+ \nu)^{17}\text{O}$
- $^{17}\text{O}(p,\gamma)^{18}\text{F}$
- $^{18}\text{F}(\beta^+ \nu)^{18}\text{O}$
- $^{18}\text{O}(p,\alpha)^{15}\text{N}$

CNO4

- $^{16}\text{O}(p,\gamma)^{17}\text{F}$
- $^{17}\text{F}(\beta^+ \nu)^{17}\text{O}$
- $^{17}\text{O}(p,\gamma)^{18}\text{F}$
- $^{18}\text{F}(\beta^+ \nu)^{18}\text{O}$
- $^{18}\text{O}(p,\gamma)^{19}\text{F}$
- $^{19}\text{F}(p,\alpha)^{16}\text{O}$



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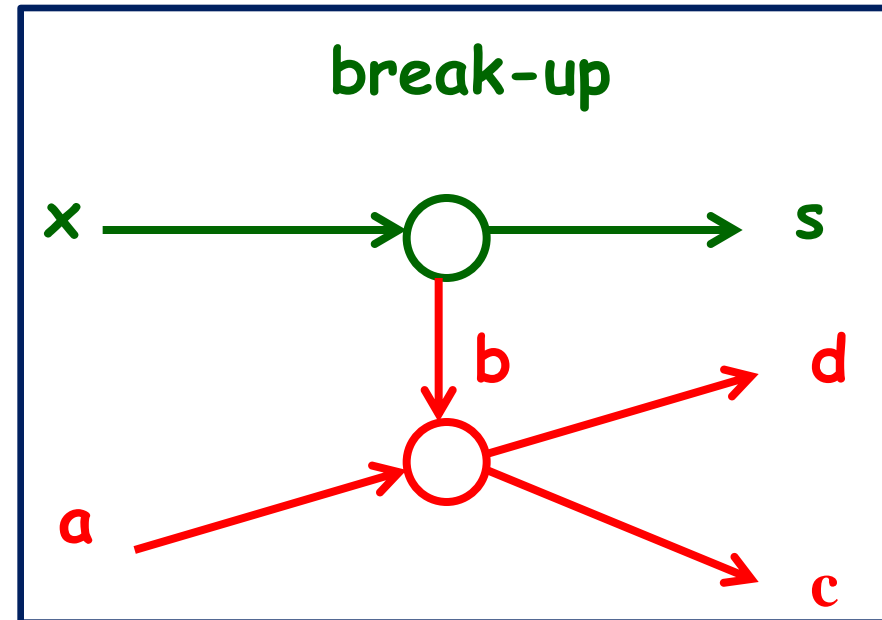
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Trojan Horse Method

If the incoming energy of the incident particle is larger than the Coulomb barrier energy

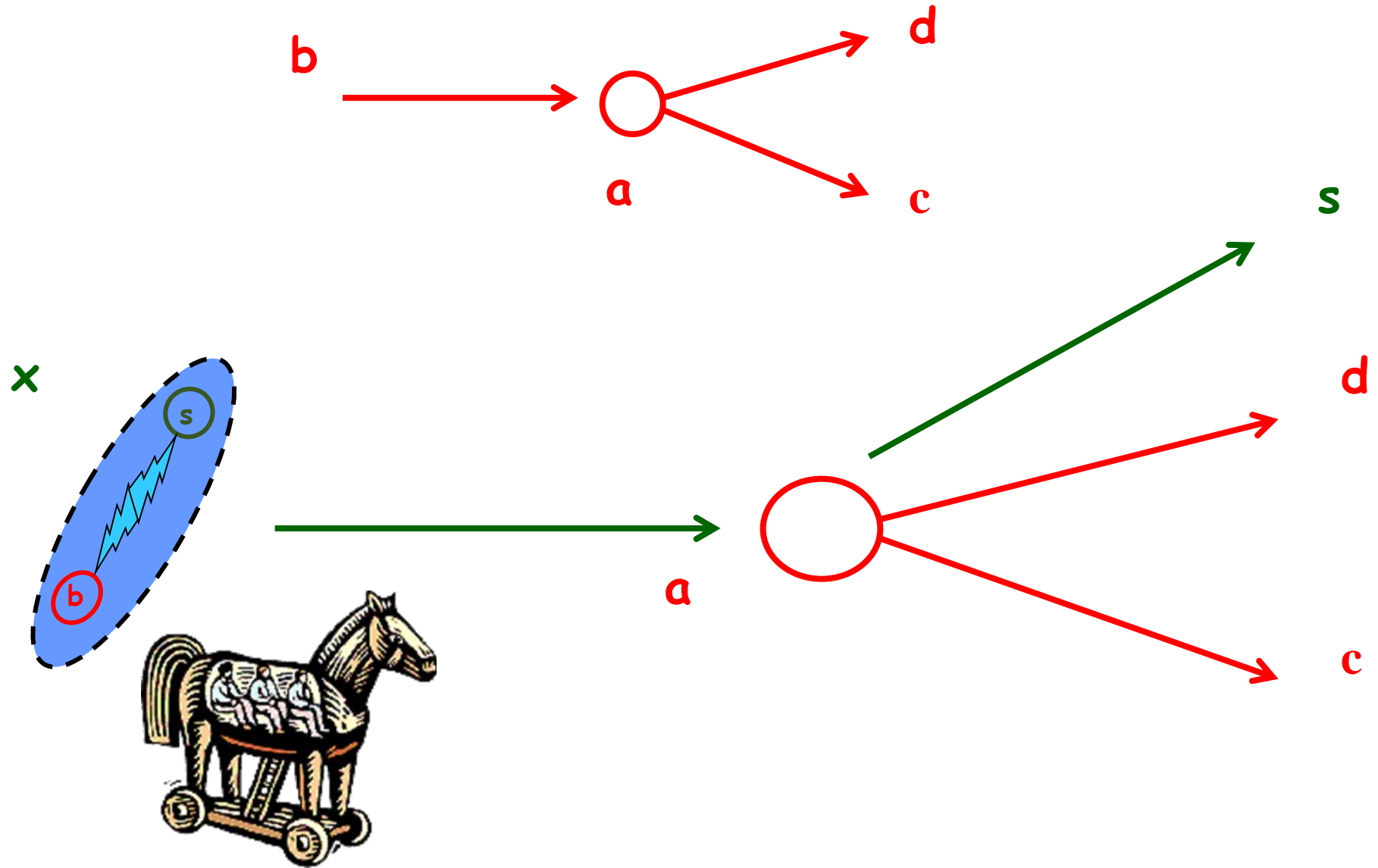
the TH nucleus **x** can be brought into nuclear field of nucleus **a** and the cluster **b** induces the virtual reaction



NO Coulomb-suppression
NO Screening effects

virtual two body reaction
 $a + b \rightarrow c + d$

C. Spitaleri et al., PRC 64(2001)068801
C. Spitaleri et al., PRC 69(2004)055806





... on NATURE (May – 2018)

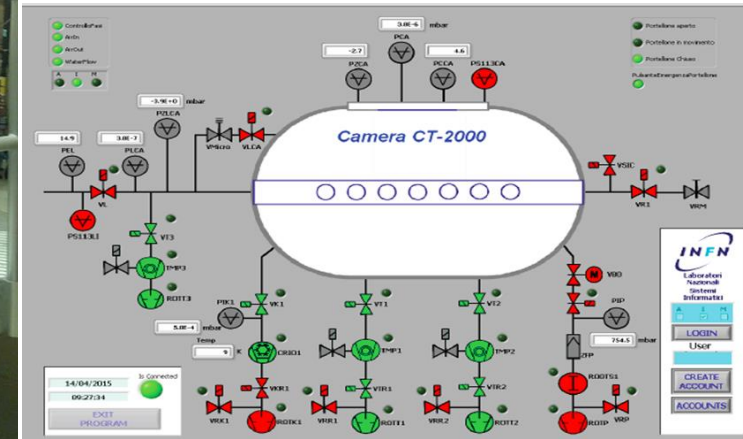
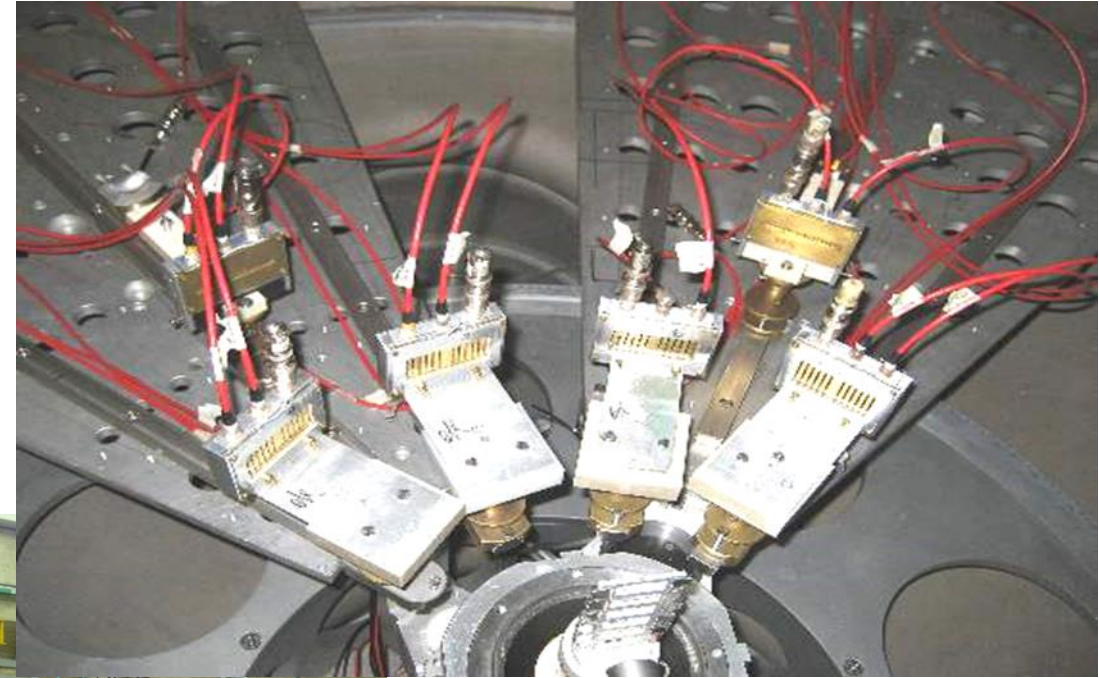
LETTER

<https://doi.org/10.1038/s41586-018-0149-4>

An increase in the $^{12}\text{C} + ^{12}\text{C}$ fusion rate from resonances at astrophysical energies

A. Tumino^{1,2*}, C. Spitaleri^{2,3}, M. La Cognata², S. Cherubini^{2,3}, G. L. Guardo^{2,4}, M. Gulino^{1,2}, S. Hayakawa^{2,5}, I. Indelicato², L. Lamia^{2,3}, H. Petrascu⁴, R. G. Pizzone², S. M. R. Puglia², G. G. Rapisarda², S. Romano^{2,3}, M. L. Sergi², R. Spartá² & L. Trache⁴

experimental facilities

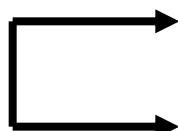
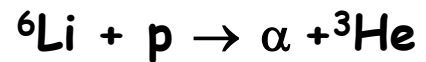
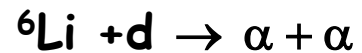
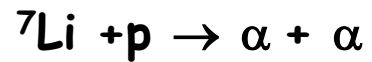


Astrophysical Application

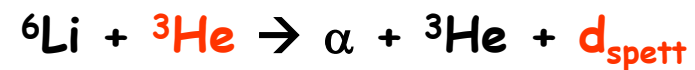
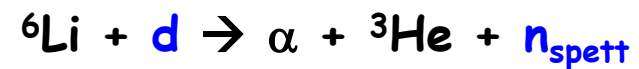
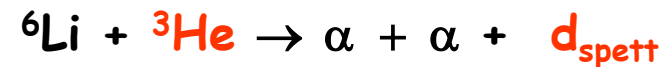
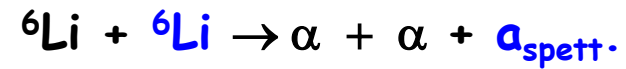
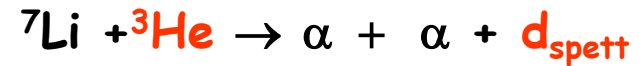
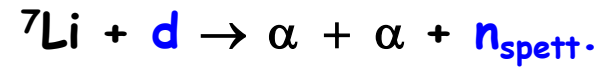
Light nuclei depletion:
Li, B, Be: **Li reactions**



DIRECT REACTIONS



INDIRECT REACTIONS



Astrophysical Application

Light nuclei depletion:
Li, B, Be

Be reactions



INDIRECT REACTION



Astrophysical Application

Depletion lights nuclei:
Li, B, Be

B reactions



INDIRECT REACTIONS



Astrophysical Application

The Fluorine problem in the AGB



INDIRECT REACTIONS



Summary

What is Nuclear Astrophysics?

Starts from the marriage between



ASTROPHYSICS

NUCLEAR PHYSICS

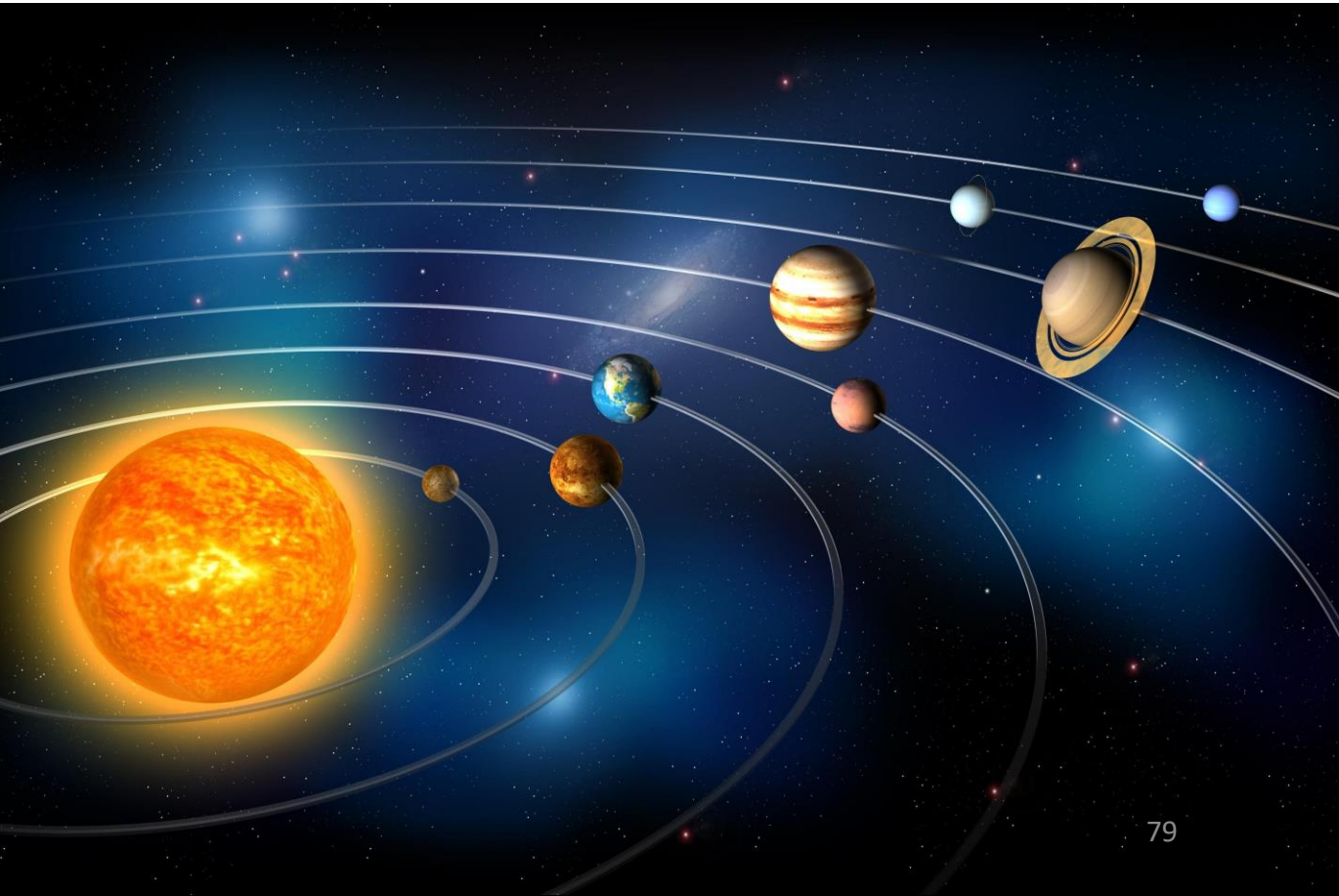
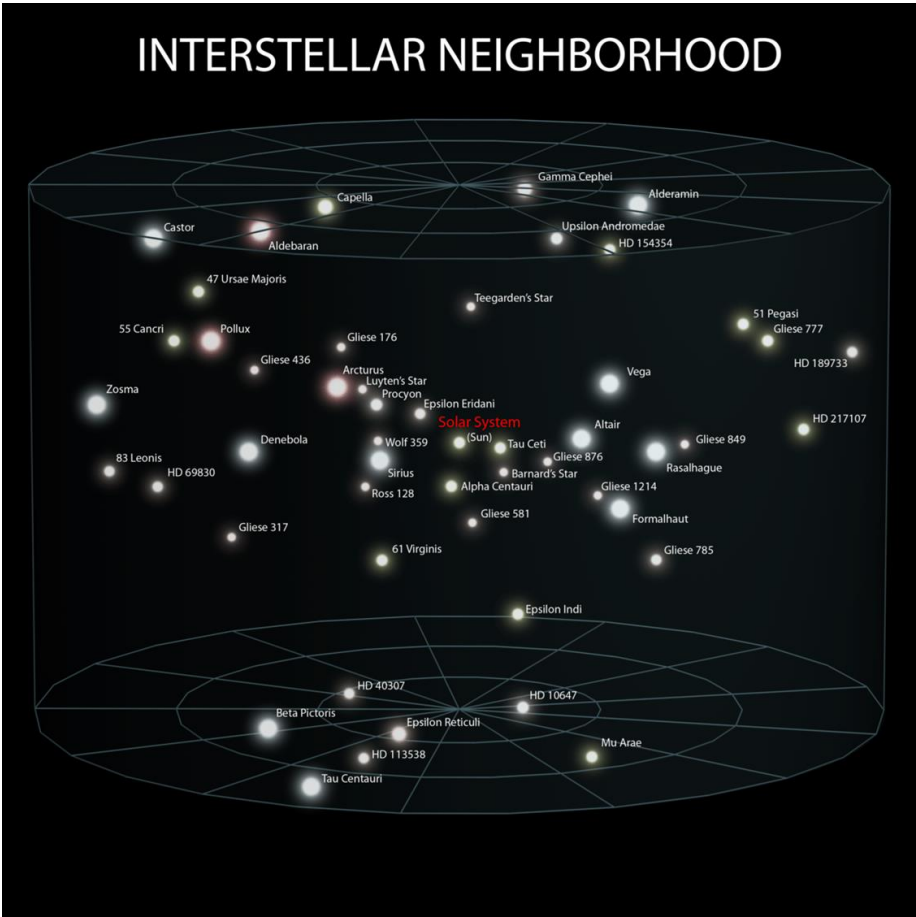


William A. Fowler
Nobel Price Physics
(1983)

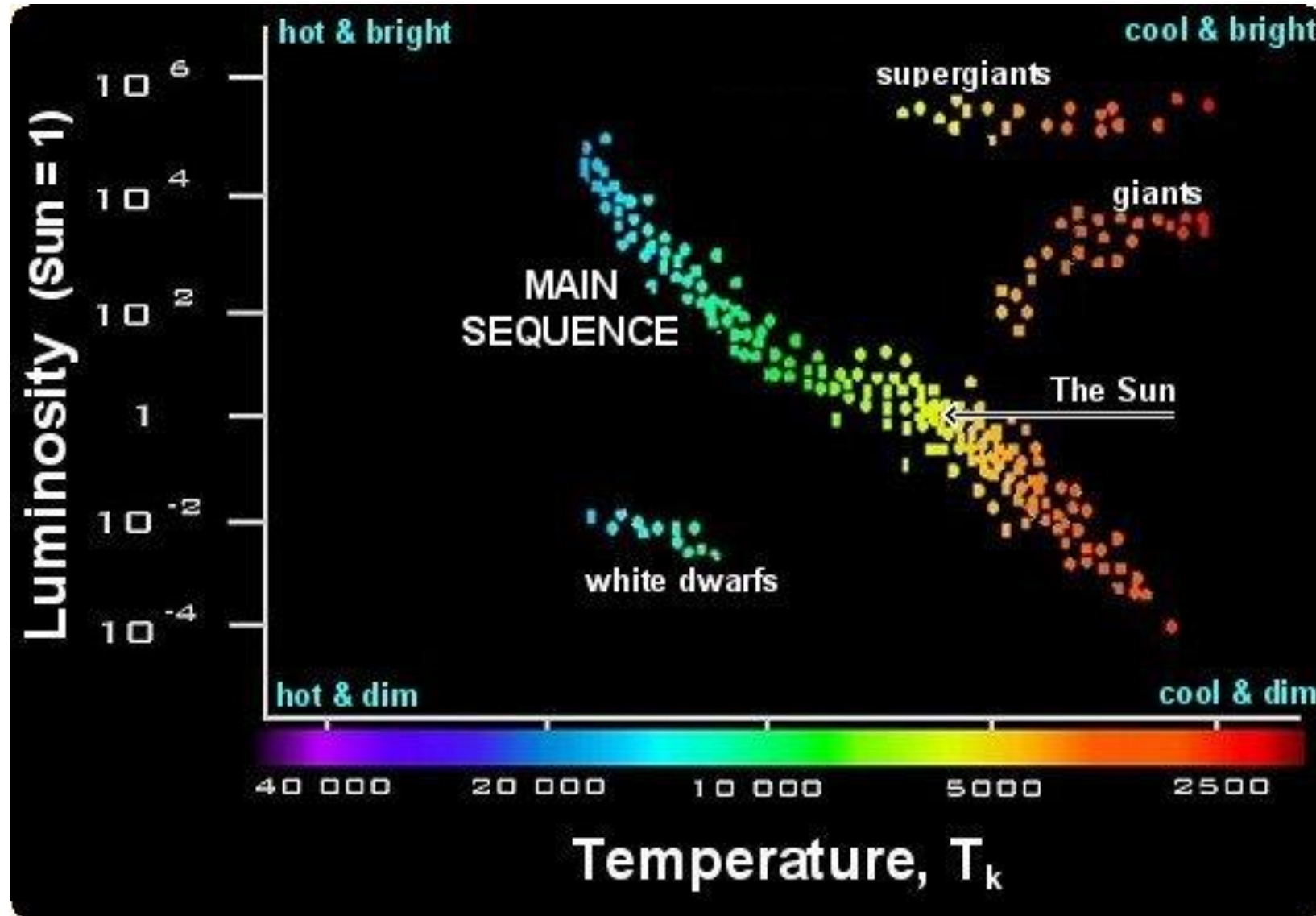
FROM

Astrophysical aspects

The study of stars is central to astronomy and astrophysics since stars are long-lived objects that are responsible for most of the visible light we observe from normal galaxies.



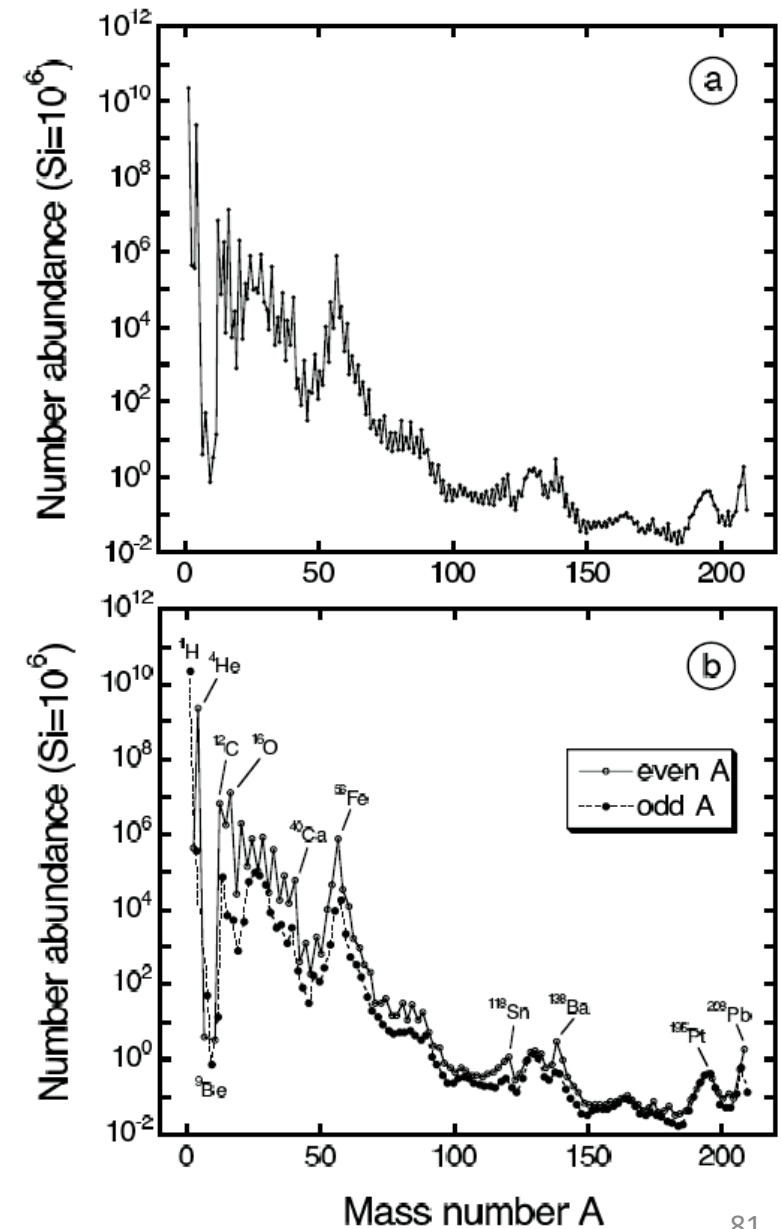
Hertzsprung-Russel Diagram – stellar evolution



Solar system abundances

- Solar system abundances of the nuclides versus mass number A
- The abundances are normalized to the number of silicon atoms
- Figure (a): sum of nuclide abundances at a given A
- Figure (b): abundances separately for even- A and odd- A nuclides
- Almost all the mass is contained in ^1H (71.1%) and ^4He (27.4%)
- There is an abundance minimum in the $A = 5\text{--}11$ region, corresponding to the elements Li , Be , and B
- More than half of the remaining mass (1.5%) is in the form of ^{12}C and ^{16}O
- The abundances drop slowly with increasing mass number (charge!)
- Another minimum occurs in the $A = 41\text{--}49$ region, around the element Sc
- The abundance curve exhibits a maximum in the $A = 50\text{--}65$ region, near the element Fe (iron peak)

Data from Lodders (2003)



Nuclear aspects

TO ...

- measurements showed that the total nuclear mass, m_{nuc} , is less than the sum of masses of the constituent nucleons.
- We may write

$$m_{nuc} = Zm_p + Nm_n - \Delta m$$

The quantity

$$B(Z,N) = \Delta m \cdot c^2 = (Zm_p + Nm_n - m_{nuc}) \cdot c^2$$

represents the nuclear binding energy

Example

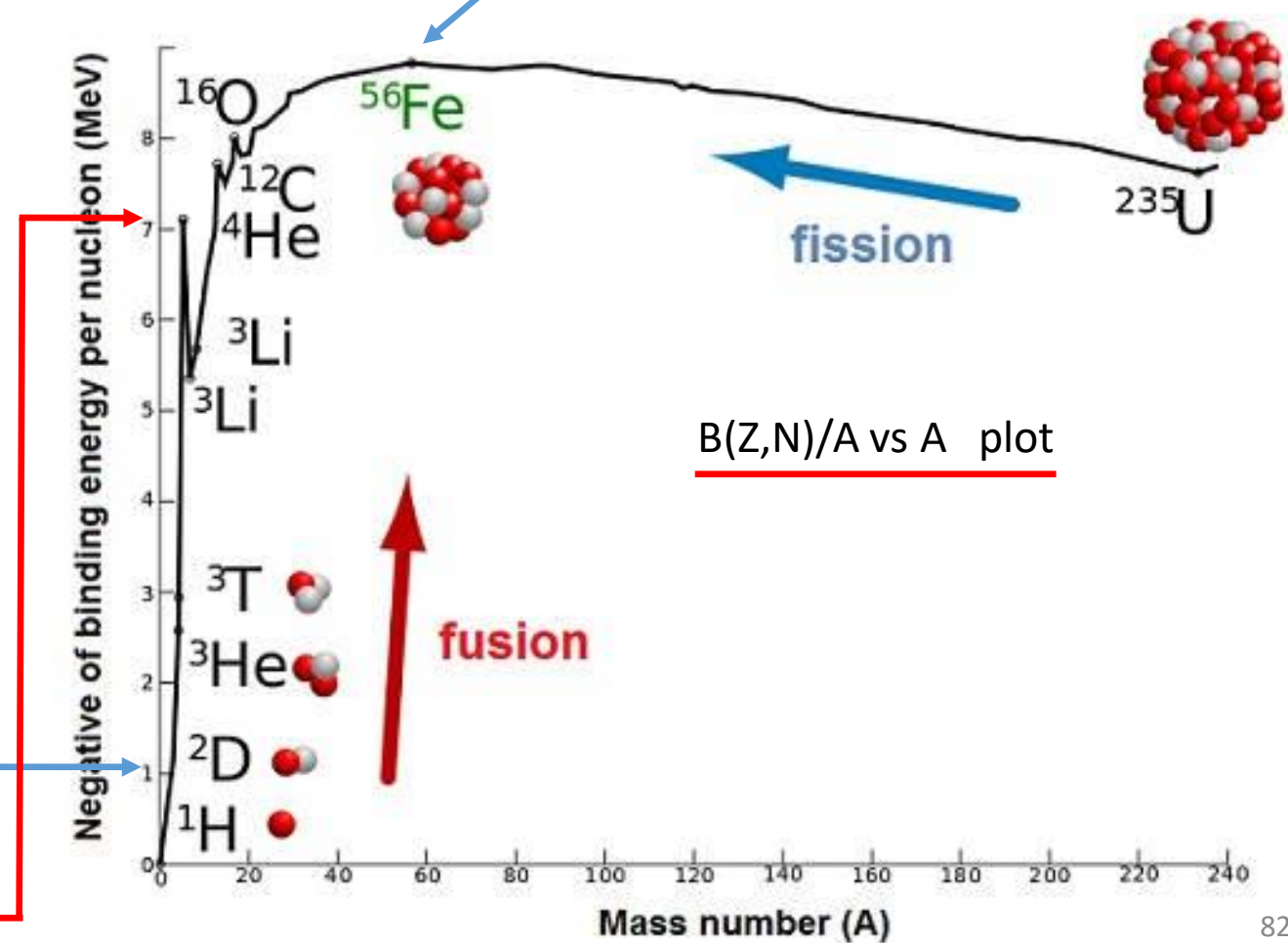
binding energies of deuterium and ^4He :

$$B(d) = B(d)/A \cdot A = (1.112 \text{ MeV}) \cdot 2 = 2.224 \text{ MeV}$$

$$B(\alpha) = B(\alpha)/A \cdot A = (7.074 \text{ MeV}) \cdot 4 = 28.296 \text{ MeV}$$



Iron peak in the solar system abundances



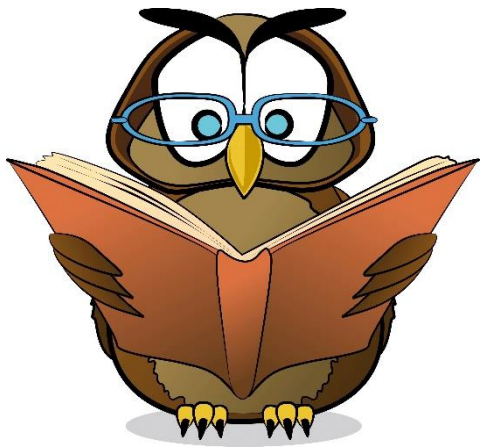
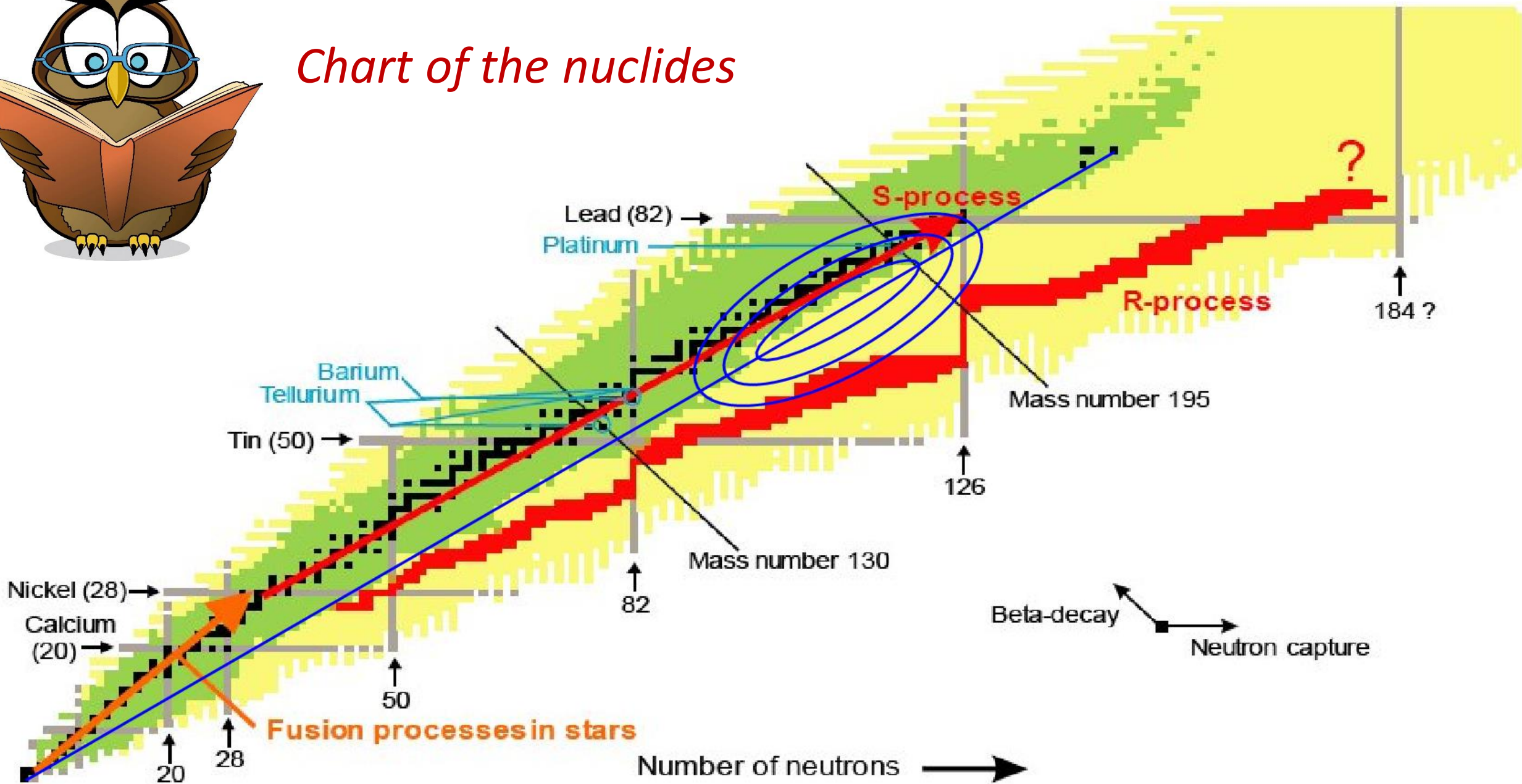
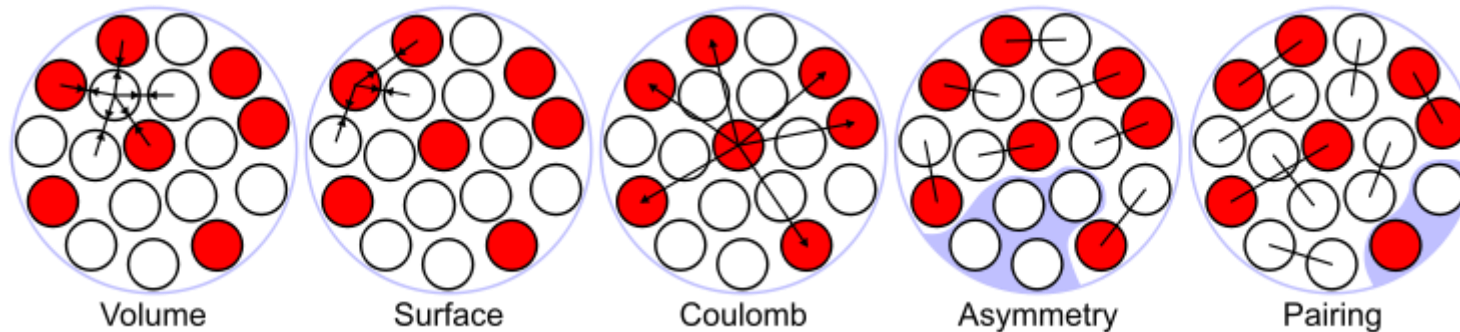


Chart of the nuclides

Number of protons ↑



$$B(A, Z) = a_v A - a_s A^{\frac{2}{3}} - a_c \frac{Z^2}{A} - a_a \frac{(N - Z)^2}{A} + \delta(A)$$



$$\begin{aligned} a_v &= 15.7 \text{ MeV} \\ a_s &= 17.8 \text{ MeV} \\ a_c &= 0.7 \text{ MeV} \\ a_a &= 23.7 \text{ MeV} \end{aligned}$$

$$\delta(A) = \begin{cases} 33.6 A^{-\frac{3}{4}} & (\text{even} - \text{even}) \\ -36.6 A^{-\frac{3}{4}} & (\text{odd} - \text{odd}) \\ 0 & (eo, oe) \end{cases}$$

... FROM

Nuclear reactions

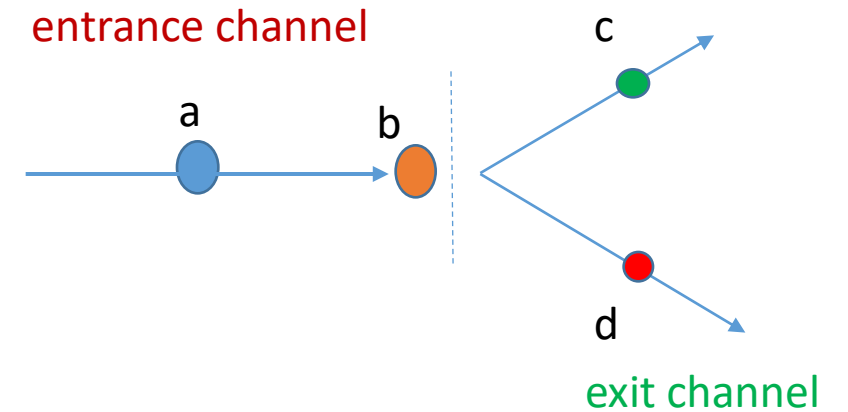
A nuclear reaction may be indicated by the following symbolic relationship



Where a and b are the colliding nuclei before the interaction, while c and d denote the products after the interaction.

Different types of reactions:

- | | |
|--|--|
| 1) $a + b \rightarrow a + b$ | <i>elastic or inelastic</i> scattering (identical species in the two channels) |
| 2) $a + b \rightarrow c + d$ | two body transfer reaction |
| 3) $a + b \rightarrow c + d + e$ | three body transfer reaction |
| 4) $a + b \rightarrow c + \gamma$ | radiative capture reaction |
| 5) $a + \gamma \rightarrow b + c$ | photodisintegration reaction |
| 6) $(a + b) + c \rightarrow a + b + c$ | breakup reaction |

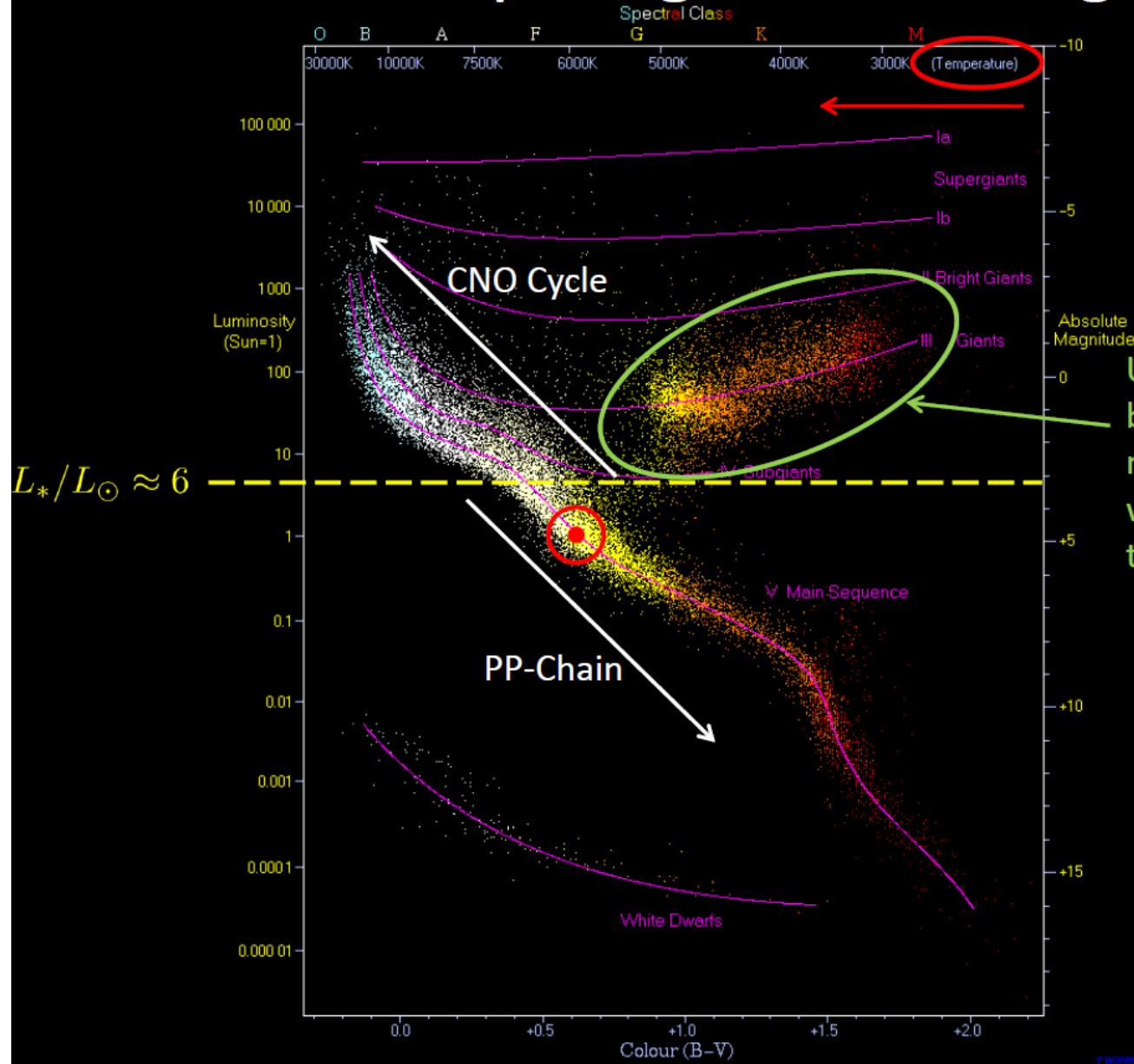


Most nuclear interactions of astrophysical interest involve just two species before and after the interaction.

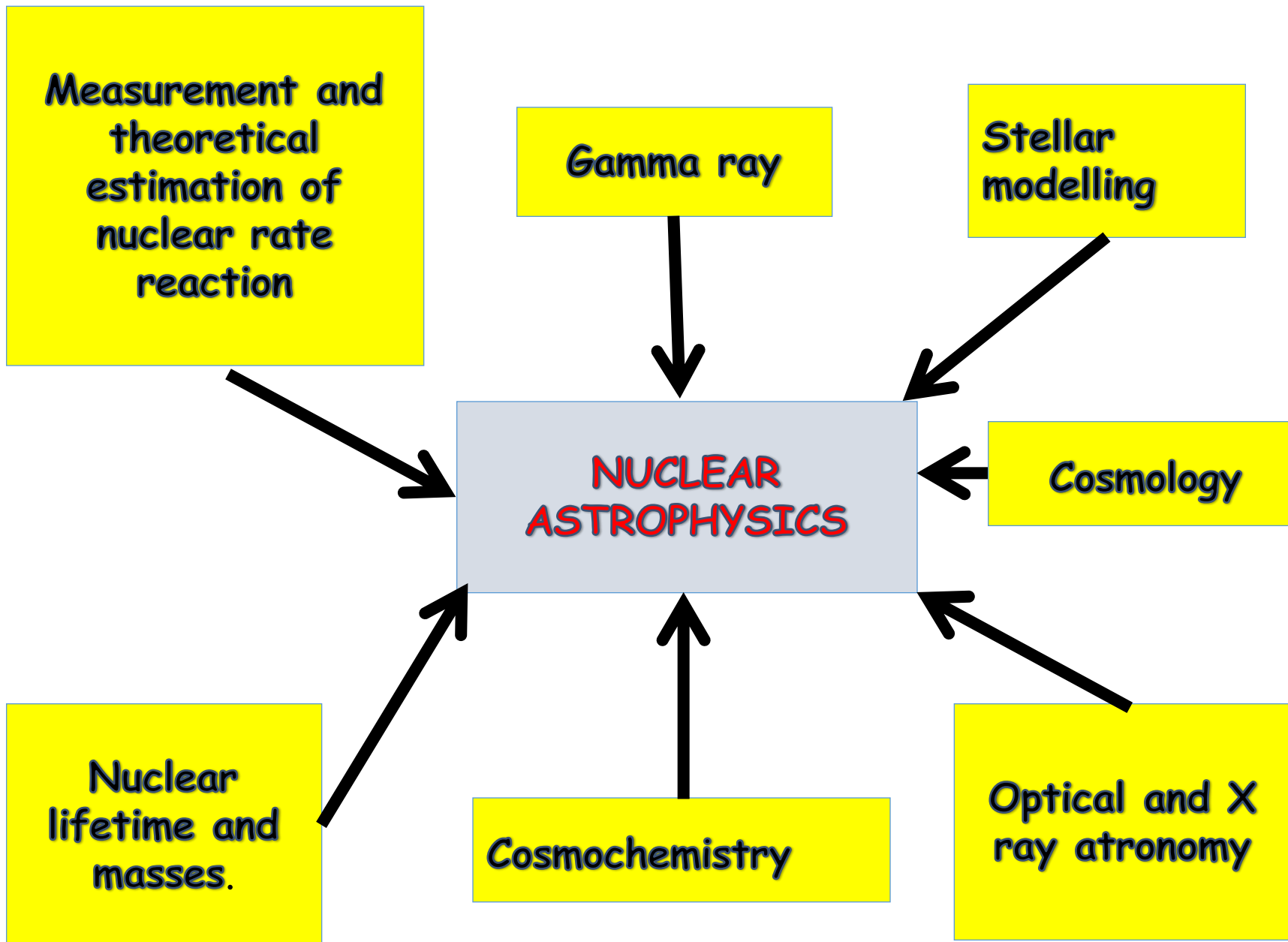
... FROM

- Theory
- Observations
- Models
- ...

Hertzprung-Russel Diagram



Understanding how stars become Giants, and the nuclear processes within, will be our next step in the New Year.



A che serve la ricerca fondamentale?

Questa domanda è stata posta diverse volte nella storia...



**Sir Michael
Faraday (1791-
1867)**

Caro Sir Faraday, ma a cosa servirà mai questa elettricità che lei sta studiando?

Caro Primo Ministro, ancora non lo so, ma sono sicuro che il governò ci metterà una tassa sopra



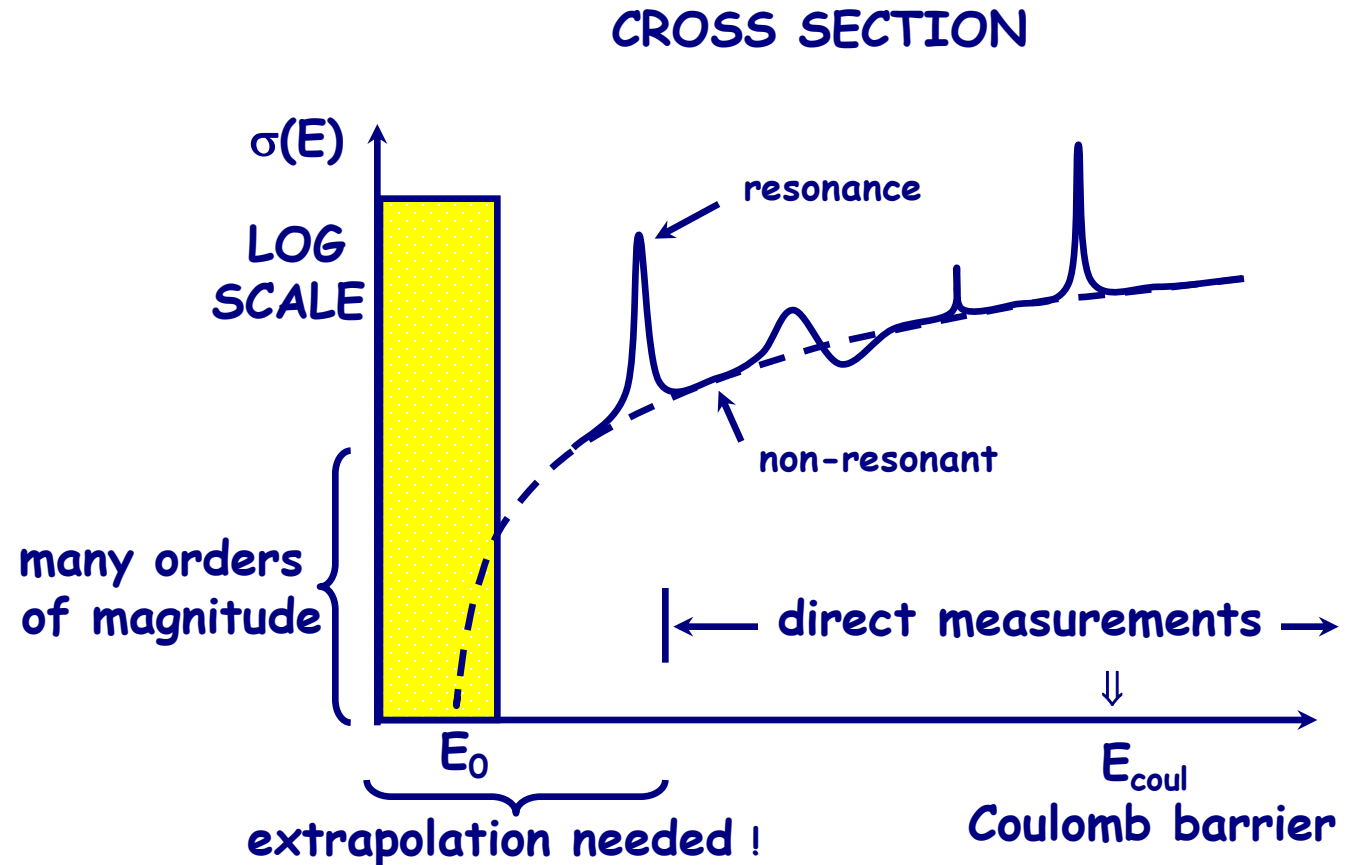
**Sir Robert
Peel (1788-
1850)**

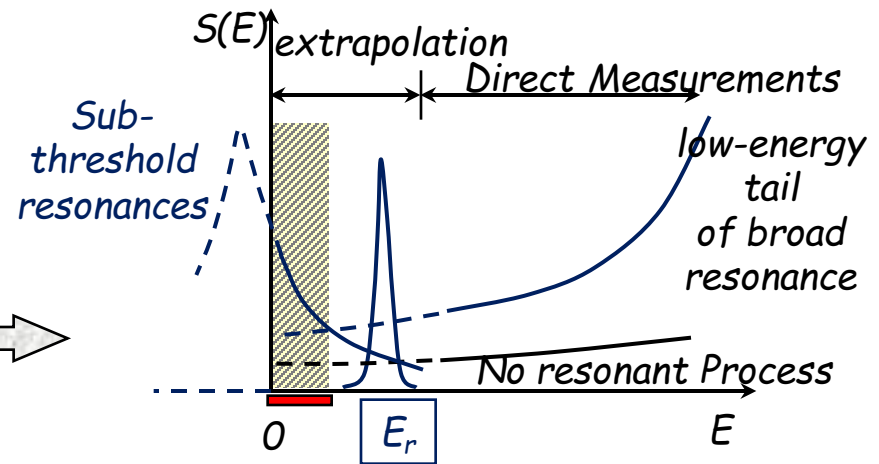
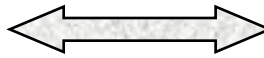
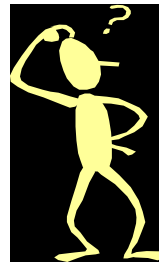
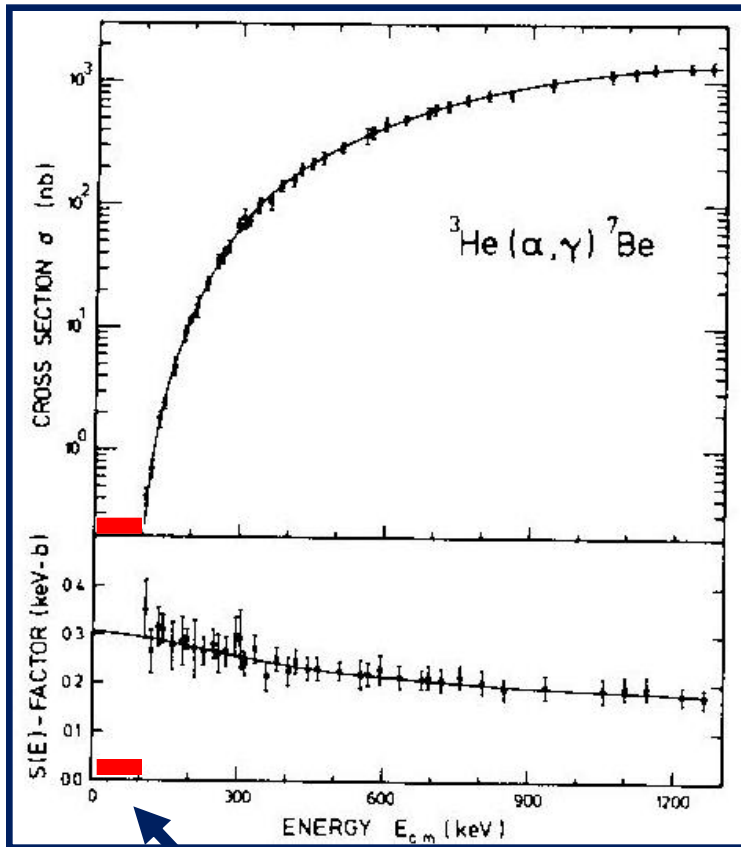
THE END

Since the cross-section varies of several orders of magnitude, the extrapolation procedure can be quite complicated



Astrophysical $S(E)$ -factor is introduced.





Astrophysical
energies
(Gamow region)

$$S(E) = E\sigma(E)\exp(2\pi\eta)$$

Possible solutions to improve the signal/noise ratio:

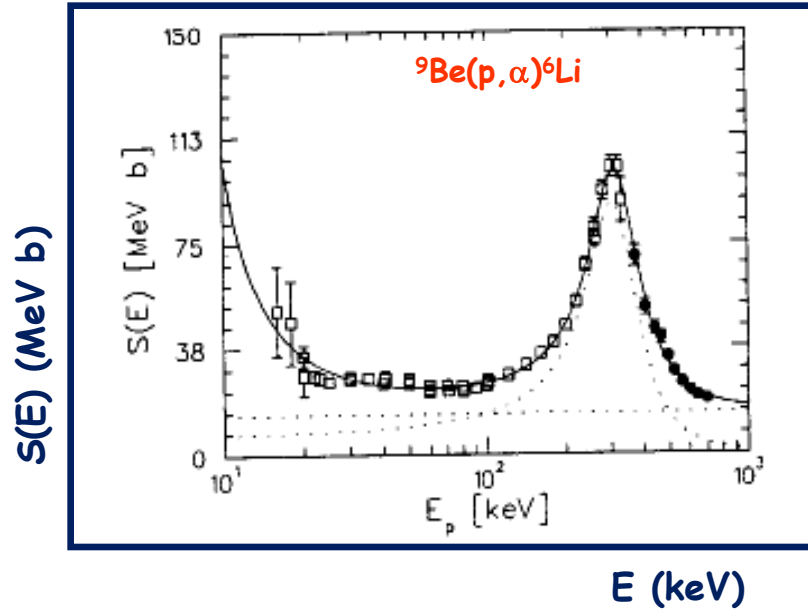
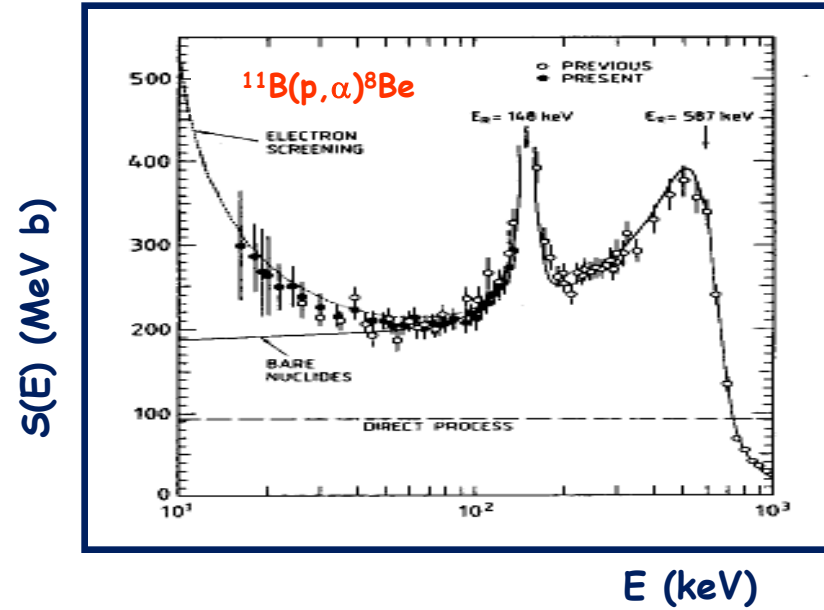
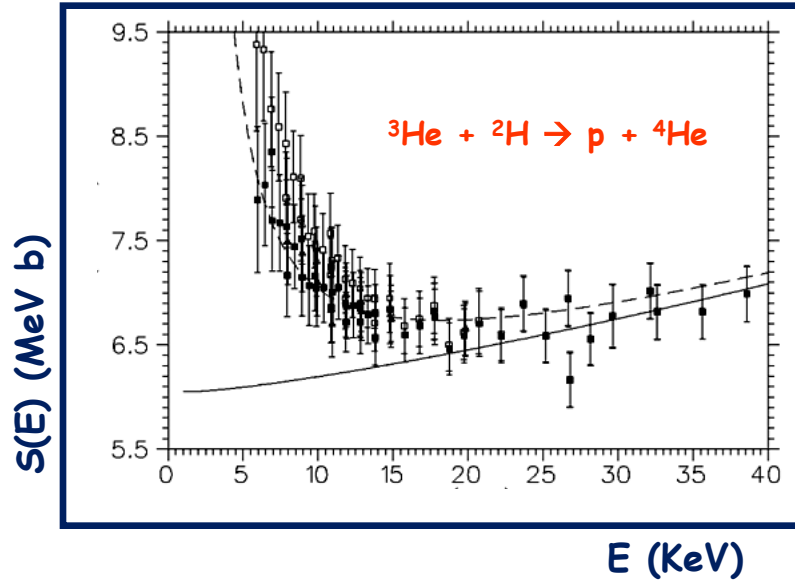
Increase the number of detected particle Reduce the background

4π detectors

High beam intensity

Underground laboratories





Evidences of electron screening

COULOMB POTENTIAL

E_c

E

BARE NUCLEUS

SHIELDED NUCLEUS

ELECTRON CLOUD

PROJECTILE

DISTANCE r

0 R_n R_a R_c

electron screening

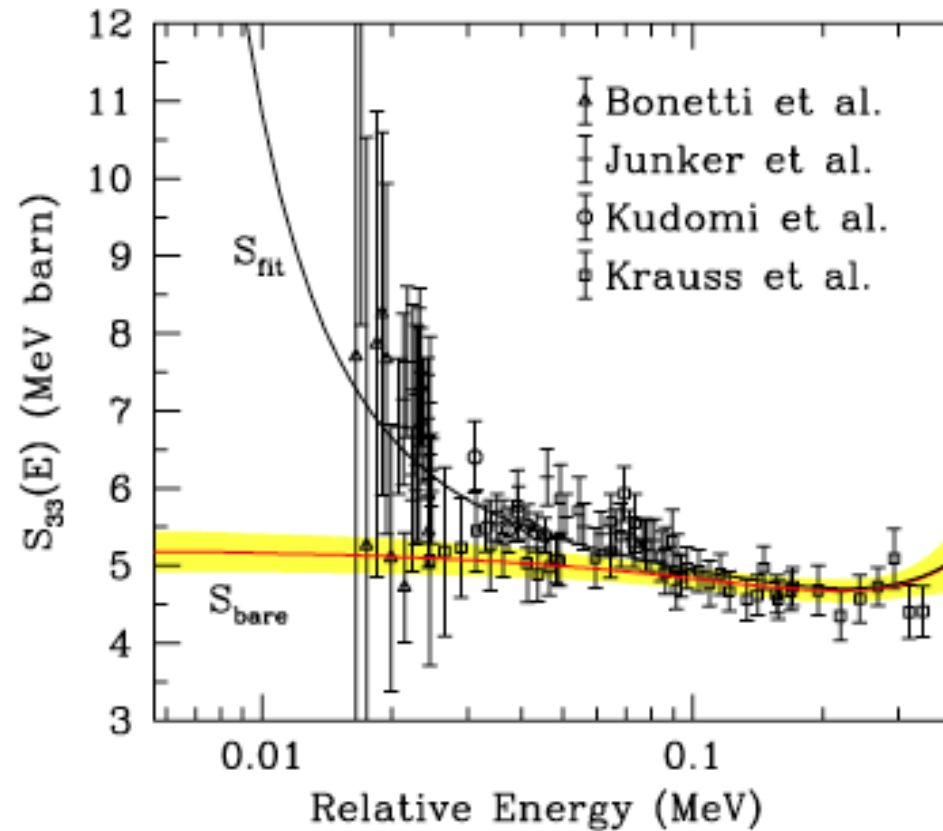
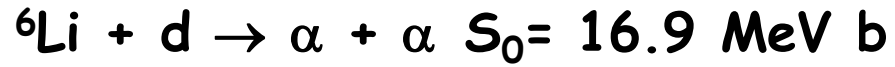
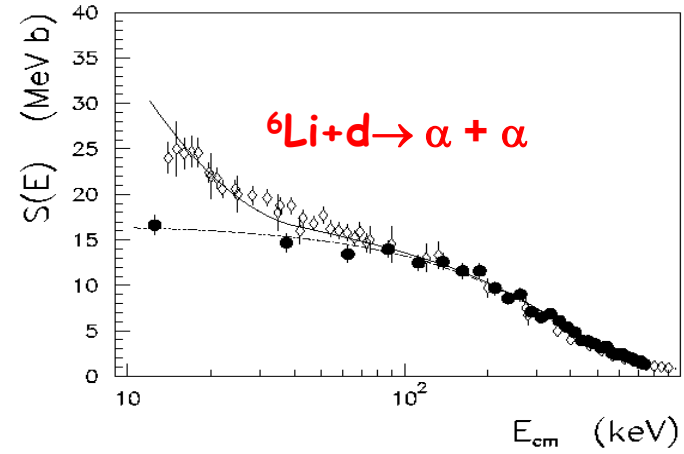


FIG. 4 (color online). The data, the best quadratic + screening result for $S_{33}(E)$, and the deduced best quadratic fit (line) and allowed range (band) for S_{33}^{bare} . See text for references.

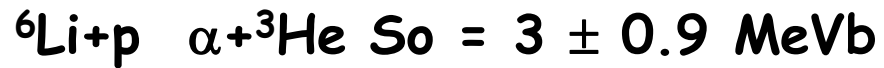
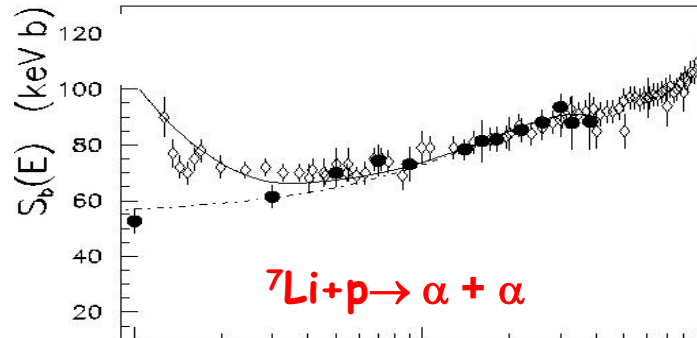
E.G. Adelberger , C.S. et al. . Review of Modern Physics 83, 195 (2011)



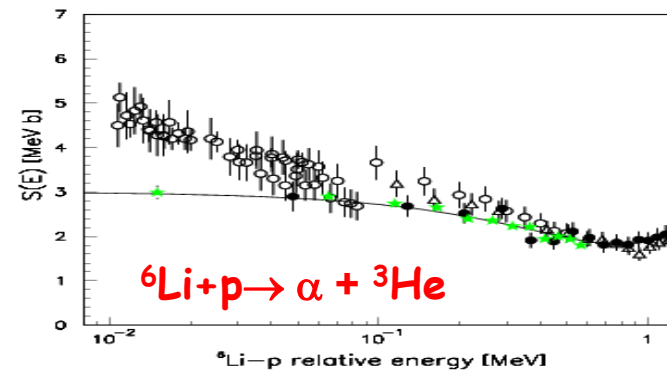
U_e (ad)	U_e (Dir) ${}^6\text{Li}+d$
186 eV	$330 \pm 120 \text{ eV}$



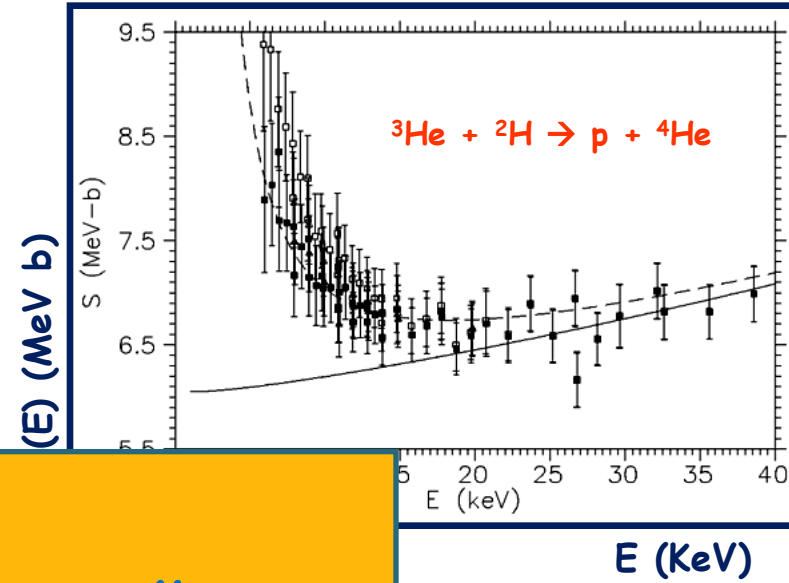
U_e (ad)	U_e (Dir) ${}^7\text{Li}+p$
186 eV	$300 \pm 160 \text{ eV}$



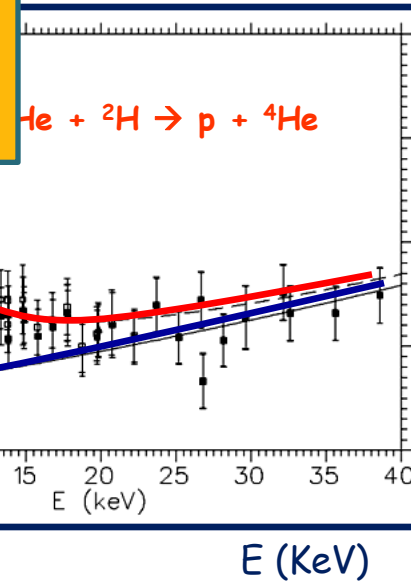
U_e (ad)	U_e (Dir) ${}^6\text{Li}+p$
186 eV	$440 \pm 80 \text{ eV}$



$$f_{lab}(E) = \frac{S_s(E)}{S_b(E)} \approx \exp\left(\pi\eta \frac{U_e}{E}\right) \geq 1$$



The extrapolation is still needed!



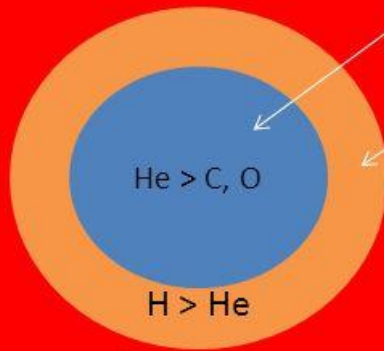
$$U_e = \frac{E}{\pi\eta} \ln \frac{S_b(E)}{S_s(E)}$$

Directly measured

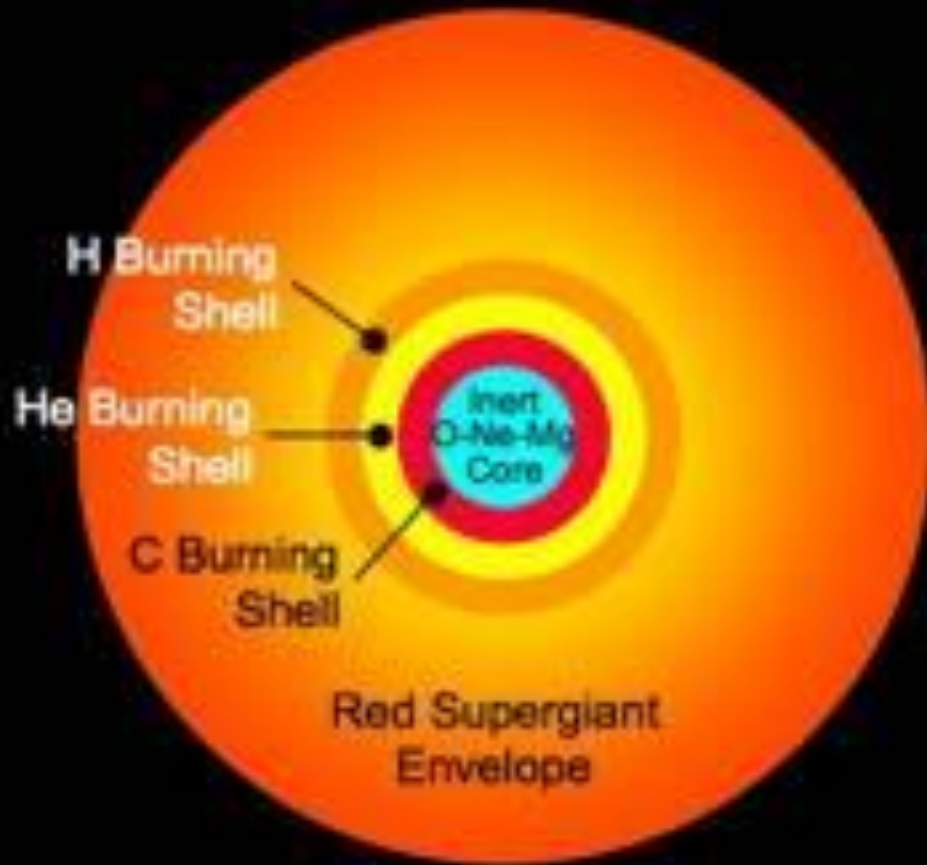
End of He-burning

Helium Burning

- Extra energy from He Fusion causes core to Expand
- This forces H burning shell to expand.



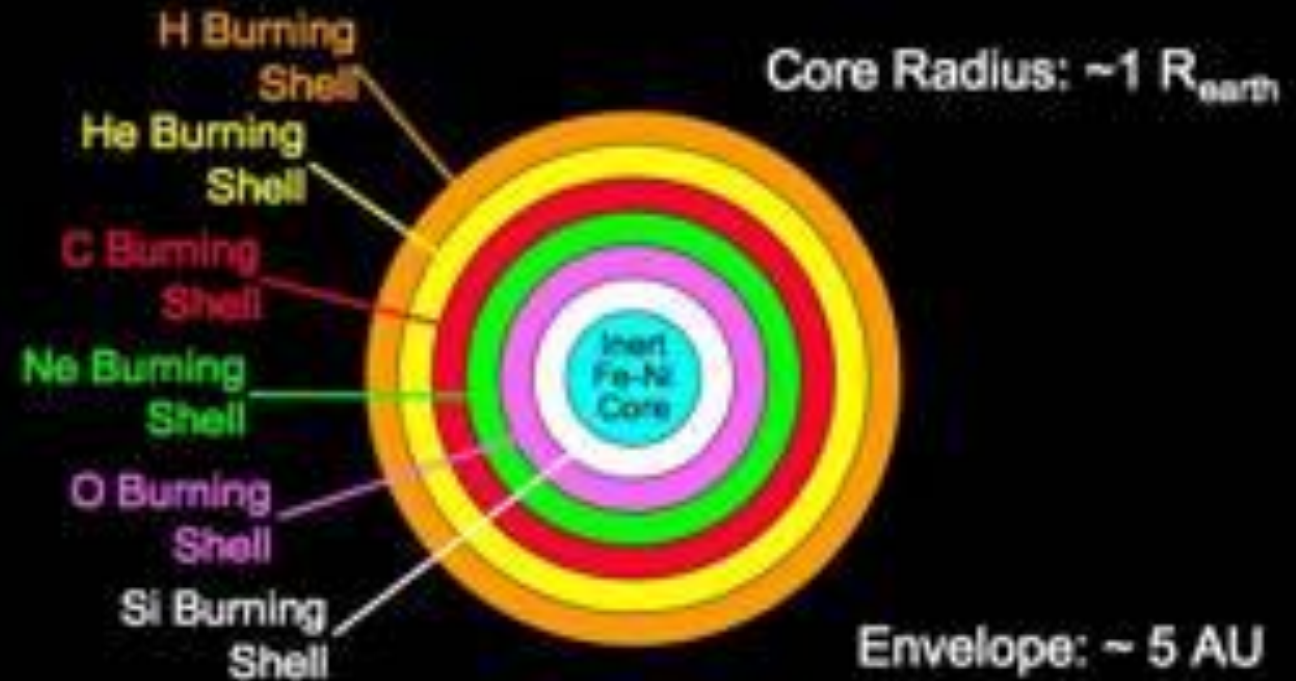
End of Carbon Burning Phase:

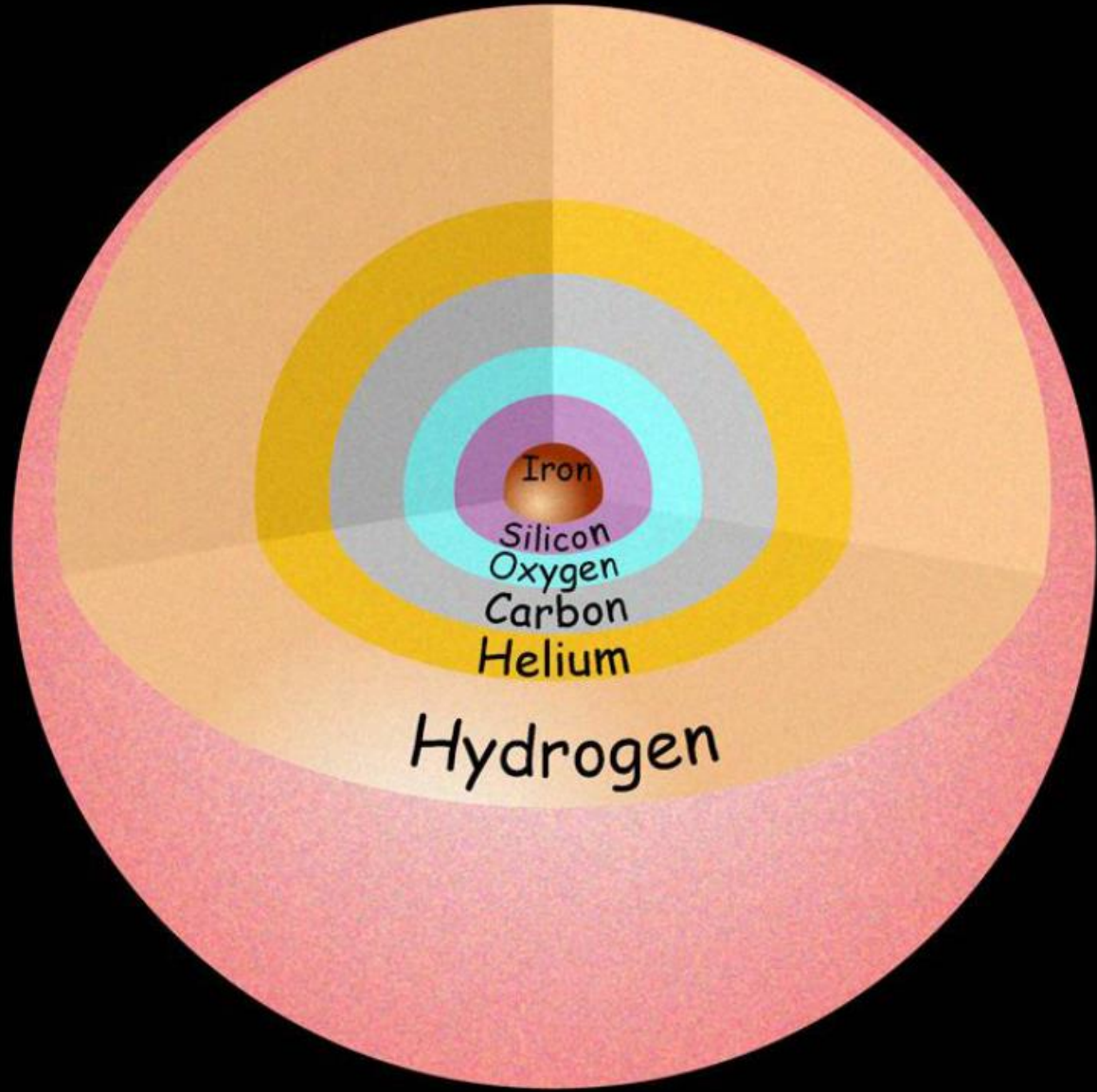


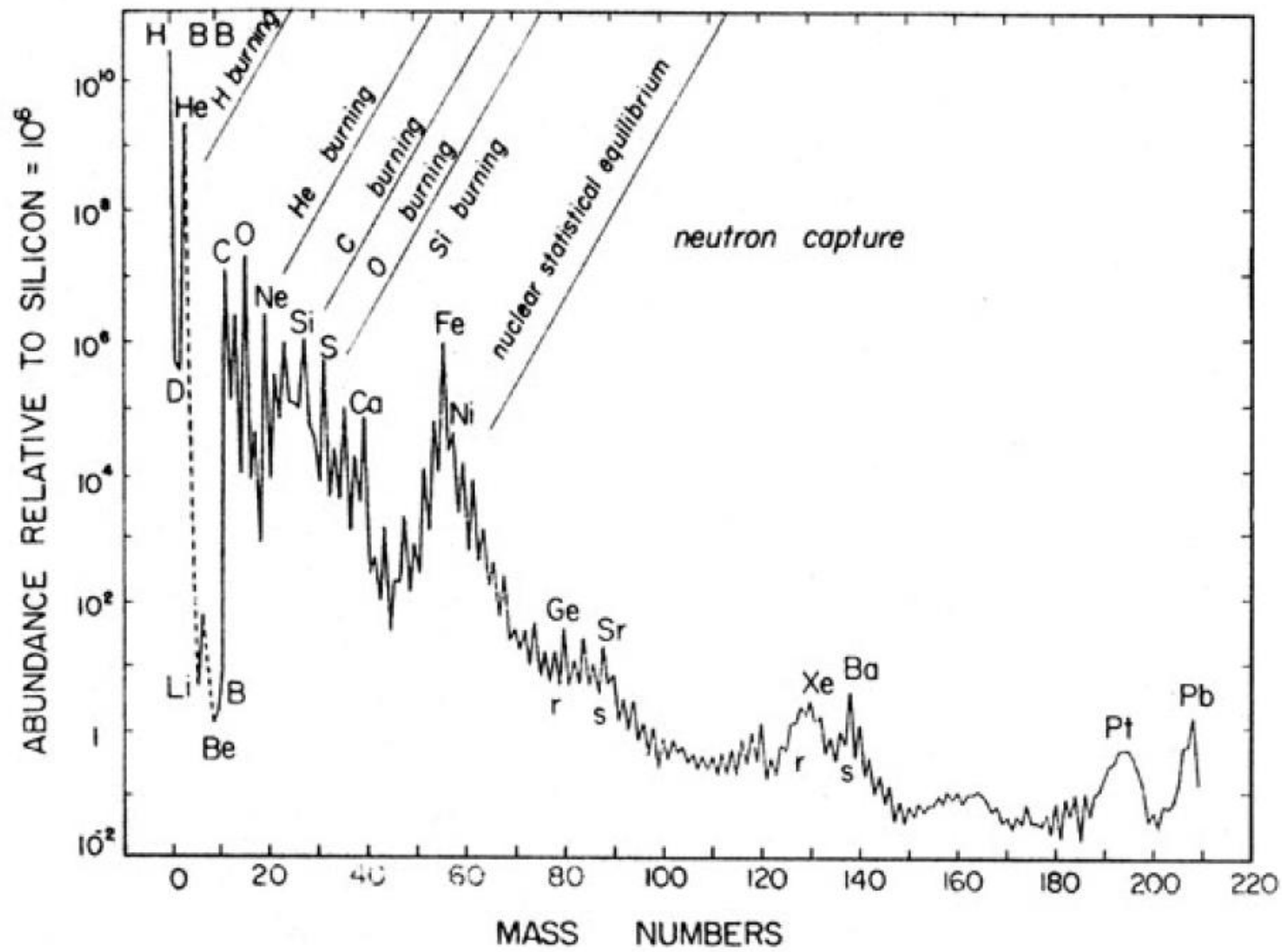
Start: $M > 8 M_{\odot}$

Start: 2.7-3.5 billion Kelvin (GK)

End of Silicon Burning Phase:







Going beyond the Iron Peak

BUILDING THE HEAVY ELEMENTS