

# Full 1-loop EW corrections to $e^+e^- \rightarrow 3$ jets at linear colliders with flavour identification and event orientation

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$e^+e^-$  Physics at TeV scale and the Dark Matter Connection  
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in collaboration with S. Moretti, F. Piccinini and D.A. Ross

JHEP 0903:047 (2009), EPJC 62, 355 (2009) and arXiv:0903.0490 [hep-ph]

## ★ Motivations for

- ILC:  $e^+e^- \rightarrow 3 \text{ jets}$ 
  - $e^+e^- \rightarrow \gamma/Z \rightarrow q\bar{q}g$
- LHC:  $pp \rightarrow Z/\gamma \rightarrow \ell^+\ell^- + \text{jet}$  (in short  $Z + \text{jet}$ )
  - $q\bar{q} \rightarrow \ell^+\ell^-g + qg \rightarrow \ell^+\ell^-q + \bar{q}g \rightarrow \ell^+\ell^-\bar{q}$

## ★ Existing literature

## ★ The complete EW one-loop calculation

- calculation details
- implementation in a Monte Carlo event generator

## ★ Results

- unflavored sample
- $b$ -tagged sample
- polarised initial state

## ★ Conclusions

# Motivations

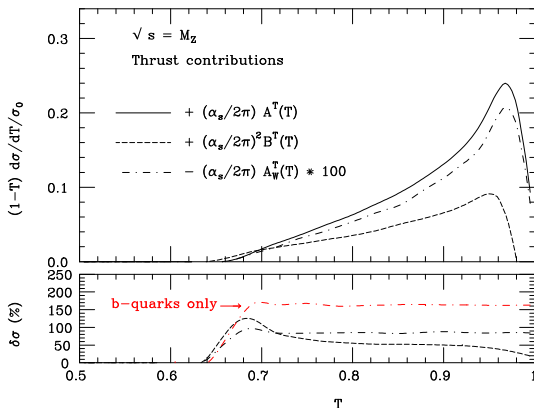
- ★ at  $e^+e^-$  colliders ( $e^+e^- \rightarrow \gamma^*/Z \rightarrow 3$  jets)
  - $e^+e^- \rightarrow 3$  jets was the “golden” process for QCD measurements and tests at LEP
  - precise measurement of  $\alpha_s$  ( $\mathcal{O}(1\%)$  at LEP/SLC,  $\mathcal{O}(0.1\%)$  at GigaZ)
  - $\mathcal{O}(\alpha)$  EW RC roughly expected as large as NNLO QCD and, at high energies (Sudakov double-logs), as NLO QCD
  - EW effects can induce asymmetries in 3 jets observables
- ★ at hadron colliders ( $pp \rightarrow \gamma^*/Z \rightarrow \ell^+\ell^- + \text{jet}$ )
  - measurement of PDFs via  $p_{\perp}^{\gamma/Z}$  spectrum, in particular the gluon PDF
  - large effects of EW Sudakov double-logs in  $Z$ +jet observables, e.g. at high  $p_{\perp}^Z$  where BSM physics can show up
  - detector calibration for jets measurements
- SM effects must be well under control to match the experimental accuracy and to test the SM and disentangle it from BSM physics

# Literature for $e^+e^- \rightarrow 3 \text{ jets and } Z+\text{jet}$

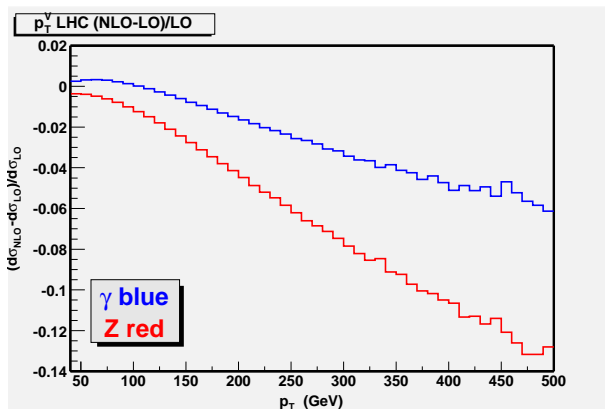
- Restricting to EW corrections

- ★ E. Maina, S. Moretti, D.A. Ross, JHEP 0304:056 (2003)
  - factorizable weak corrections to  $e^+e^- \rightarrow 3 \text{ jets}$  (no real & virtual QED, no RC connecting initial and final state) at  $M_Z$
- ★ E. Maina, S. Moretti, D.A. Ross, PLB 593 (2004), Erratum PLB 614 (2005)
  - weak corrections to  $pp \rightarrow Z, \gamma + \text{jet}$  at high  $p_T^{\gamma/Z}$ . on-shell  $\gamma, Z$
- ★ Kuhn, Kulesza, Pozzorini, Schulze, 1. PLB 609 (2005) and 2. NPB 727 (2005) 368
  - 1. logarithmic weak corrections to  $pp \rightarrow Z + \text{jet}$  (high  $p_{\perp}^Z$ ) at one and two loop order with LL and NLL accuracy ([Sudakov expansion](#))
  - 2. Exact one-loop corrections to  $pp \rightarrow Z + \text{jet}$
- ★ Denner, Dittmaier, Gehrmann, Kurz, arXiv:0906.0372 [hep-ph]
  - 1-loop EW corrections to  $e^+e^- \rightarrow 3 \text{ jets}$

- QCD corrections to  $e^+e^- \rightarrow 3 \text{ jets}$  are known up to **NNLO order** (work by Gehrmann-De Ridder, Gehrmann, Glover, Heinrich)



- weak corrections have a  $\mathcal{O}(1\%)$  effect, which could be **not negligible** for  $\alpha_s$  determination at GigaZ at the 0.1% level
- larger effect for the  $b\bar{b}$  sub-sample (due to top in the loops)



- $\gamma$  and  $Z$  are on-shell here
- large corrections ( $\mathcal{O}(10\%)$ ) in the high boson  $p_\perp$  tail, where SM is a background to new physics signatures

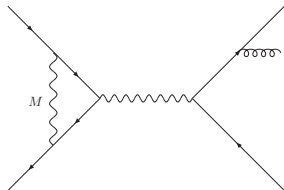
# Complete 1-loop EW RC to $e^+e^- \rightarrow 3$ jets

- we calculated the **full 1-loop EW corrections to  $e^+e^- \rightarrow 3$  jets**
  - QED can give a sizeable effect if realistic event selection criteria are considered
  - non-factorizable RC are not negligible far from  $M_Z$
  - non-factorizable RC can have a not trivial impact on asymmetries
- **by crossing symmetry**, EW RC to  $pp \rightarrow \ell^+\ell^- + \text{jet}$  are (in principle) straightforwardly obtained
- the precise control of SM effects is mandatory for precision tests of SM and new physics searches

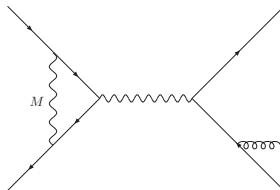
# Prototype diagrams

The 1-loop diagrams to be evaluated are:

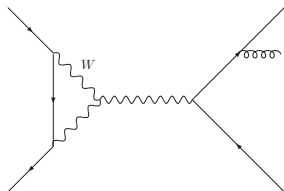
- $e^+e^-$  vertices



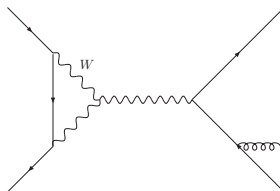
(a)



(b)



(c)

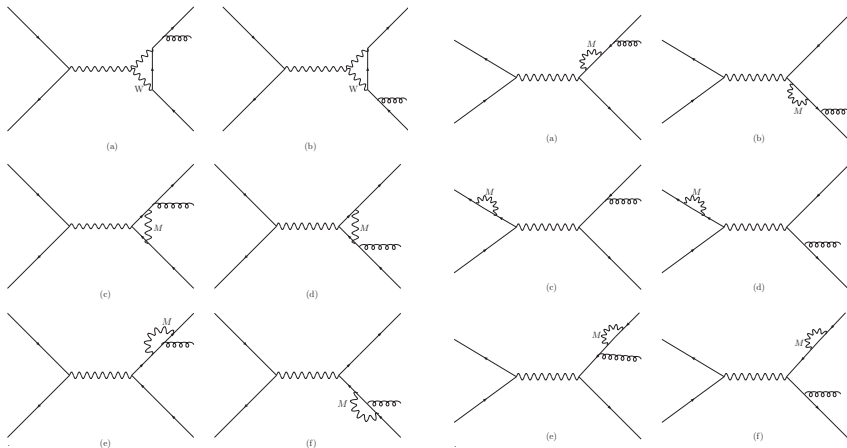


(d)



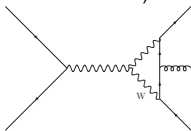
# Prototype diagrams

- $q\bar{q}$  and gluon vertices and fermion self-energies

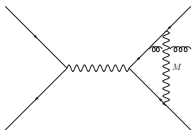


# Prototype diagrams

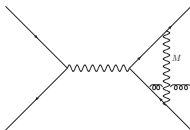
- box diagrams (factorizable and not factorizable)



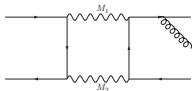
(a)



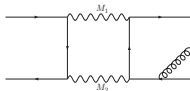
(b)



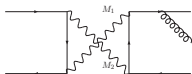
(c)



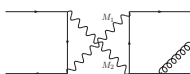
(d)



(e)



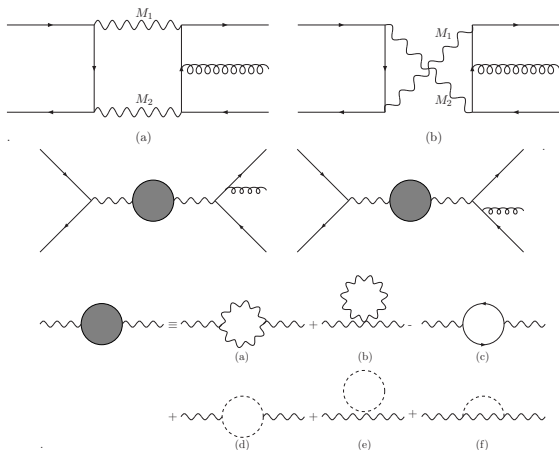
(f)



(g)

# Prototype diagrams

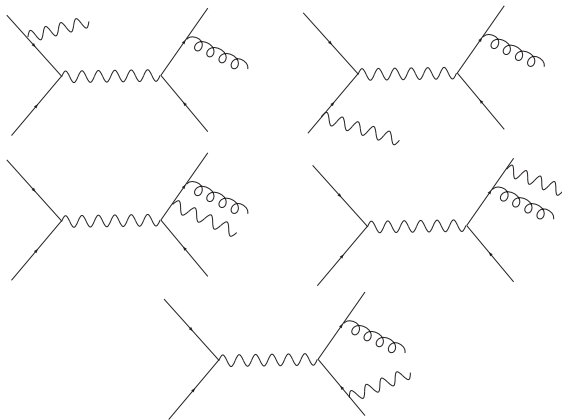
- pentagons and gauge-bosons self-energies



# Calculation details

- the calculation has been performed in the limit  $m_{ext}^2/s \rightarrow 0$
- collinear singularities cured with **a small fermion & quark mass**
- infrared divergencies regularized with **a finite photon mass  $\lambda$**
- virtual corrections
  - ★ amplitudes evaluated with helicity techniques and manipulated with **FORM**
  - ★ two independent calculations
  - ★ up to 4-point functions: reduction of tensor integrals with Passarino-Veltman reduction
  - ★ 5-point functions, reduction according to PV or to Denner-Dittmaier (as coded in a our own library or in **LoopTools**)
  - ★ **good agreement** among different implementations
  - ★ IR/collinear divergent scalar integrals calculated also in dimensional regularisation and cross-checked with mass regularisation up to high numerical accuracy

# Real corrections



- the squared amplitude for the real emission process  $e^+e^- \rightarrow q\bar{q}\gamma$  has been calculated
  - ★ with **ALPHA** (Moretti & Caravaglios)
  - ★ with **MADGRAPH** (Maltoni, Stelzer et al.)

# Gauge boson width

- in the real part of the calculation we have the  $Z$  propagator with fixed width switched on, in order to avoid the  $Z$  pole in the phase space integration
- the same propagator has to be retained in the virtual corrections (complex masses) (e.g., in order to ensure the cancellation of IR singularities between virtual and real corrections)
- in **LoopTools** only scalar functions up to 3-points are available with finite width
- we implemented **a 4-point scalar function with complex masses**, according to 't Hooft-Veltman (Nucl. Phys. **B** 153,1979) and to Denner-Beenakker (Nucl. Phys. **B** 338,1990) for IR configurations
- **all the calculation can then be performed with complex  $Z$  (and  $W$ ) mass**

# Cross section calculation

As usual, the cross section is split into two parts

- $e^+e^- \rightarrow q\bar{q}g$

$$\sigma_{2\rightarrow 3} = \int d\Phi_3 ( |\mathcal{M}_0|^2 + 2\Re[\mathcal{M}_0^*\mathcal{M}_\alpha^{virt}(\lambda)] )$$

- $e^+e^- \rightarrow q\bar{q}g\gamma$

$$\sigma_{2\rightarrow 4} = \int_{\lambda < \omega} d\Phi_4 |\mathcal{M}_\alpha^{real}|^2 =$$

$$\int_{\lambda < \omega < k_0} d\Phi_4 |\mathcal{M}_\alpha^{real}|^2 + \int_{k_0 < \omega} d\Phi_4 |\mathcal{M}_\alpha^{real}|^2 = \delta_s(\lambda, k_0)\sigma_0 + \sigma_{2\rightarrow 4}^{hard}(k_0)$$

- $\sigma_{2\rightarrow 3} + \sigma_{2\rightarrow 4} \equiv \sigma^{SV}(k_0) + \sigma^{hard}(k_0)$  has to be independent from the unphysical parameters  $\lambda$  and  $k_0$
- the integral over  $2 \rightarrow 3$  and  $2 \rightarrow 4$  phase space is performed with a Monte Carlo generator

# Initial state higher-order QED effects

- Large collinear logs  $\ln(s/m_e^2)$  associated with ISR
- for reliable predictions they need to be resummed, in order to take into account leading-log higher order QED corrections ( $\alpha^n, n \geq 2$ )
- we use the SF formalism avoiding double counting

G. Montagna, O. Nicrosini and F. Piccinini, Phys. Lett. **B385** (1996) 348

$$d\sigma_{\text{LL}}^{\infty} = \int dx_1 dx_2 D(x_1, s) D(x_2, s) d\sigma_0(x_1 x_2 s)$$

$$d\sigma_{\text{LL}}^{\alpha} = \int dx_1 dx_2 [D(x_1, s) D(x_2, s)]_{\alpha} d\sigma_0(x_1 x_2 s)$$

$$d\sigma_{\text{exact}} \mathcal{O}(\alpha)+h.o. = d\sigma_{\text{LL}}^{\infty} - d\sigma_{\text{LL}}^{\alpha} + d\sigma_{\text{exact}}^{\alpha}$$



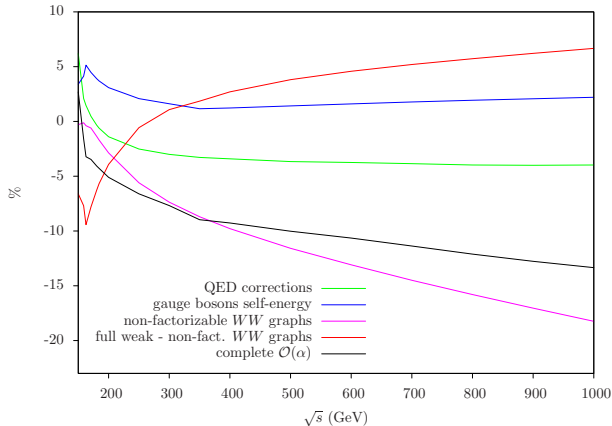
# Results

- numerical results for  $\sqrt{s} = M_Z$  and 1 TeV (and 350 GeV in the papers)
- cuts & parameters:
  - ★ momenta clustered into jets according to the Cambridge algorithm, i.e. if  $y_{ij} < y_{min}$ , where

$$y_{ij} = 2 \frac{\min(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{s}$$

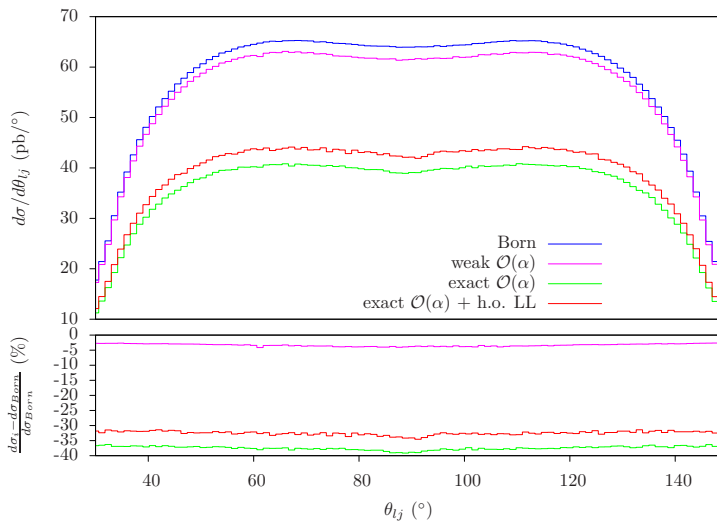
- ★ photon (in  $2 \rightarrow 4$ ) recombined according to the same algorithm
- ★ at least 3 “hadronic” jets requested
- ★  $y_{min} = 0.001$ ,  $30^\circ < \theta_{jets} < 150^\circ$ ,  $M_{3 jets} > 0.75 \sqrt{s}$
- ★  $\alpha_s = 0.118$ ,  $\alpha_{em} = 1/127.7$ ,  $M_Z = 91.18$  GeV,  $M_W = 80.4$  GeV
- for the inclusive case, summed over final state quarks ( $q\bar{q} = u\bar{u}, d\bar{d}, c\bar{c}, s\bar{s}, b\bar{b}$ ) and over initial- and final-state helicities
- the final state  $b\bar{b}$  has been treated retaining the full  $m_{top}$  dependence

# Energy scan

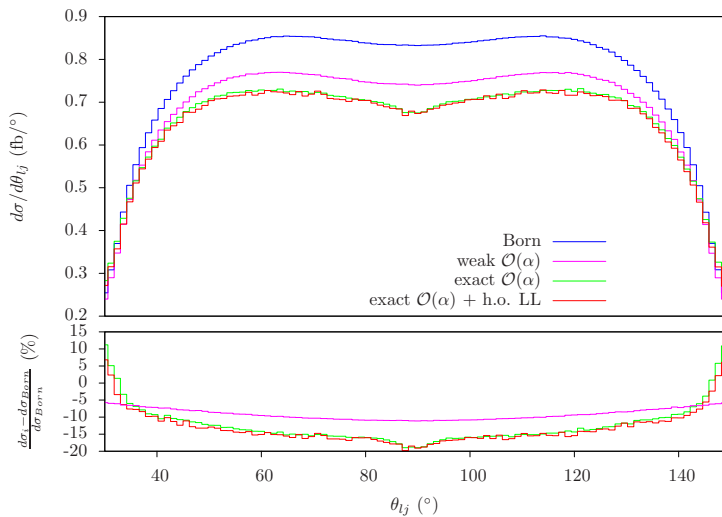


- for  $d, s, b$  ( $u, c$ ) only “direct” (“crossed”)  $WW$  virtual non-fact. diagrams survive (the ones giving negative correction)
- large negative corrections induced by **lack of cancellation of  $WW$  direct and crossed diagrams**, as it happens at LL level for  $ZZ$  diagrams

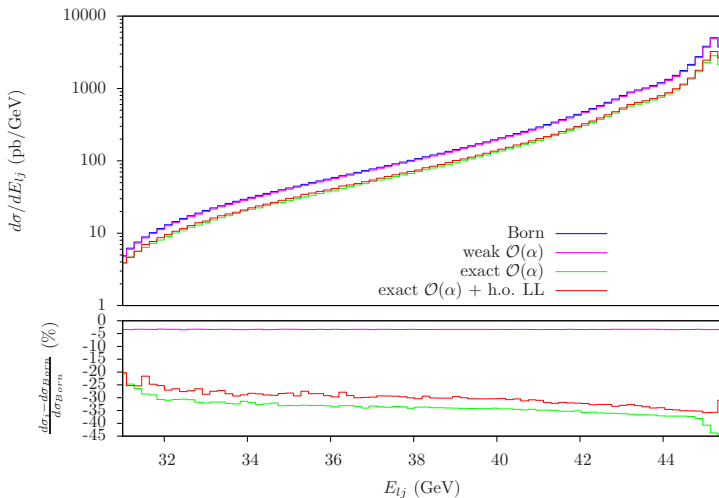
# Leading jet angle at $Z$ peak



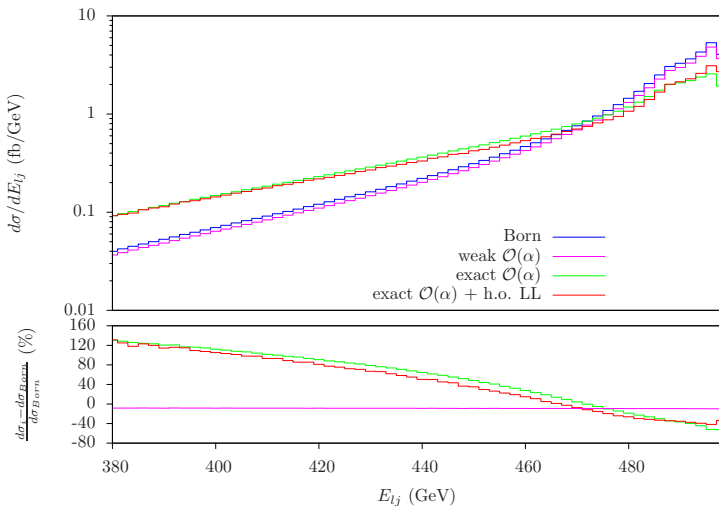
# Leading jet angle at $\sqrt{s} = 1$ TeV



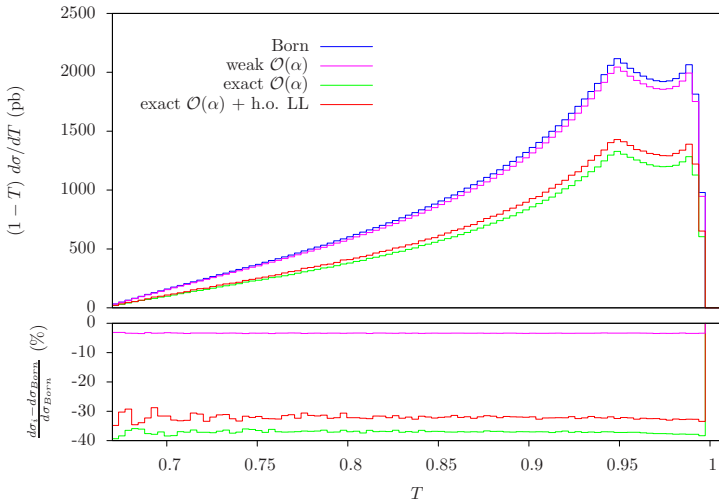
# Leading jet energy at $Z$ peak



# Leading jet energy at $\sqrt{s} = 1$ TeV

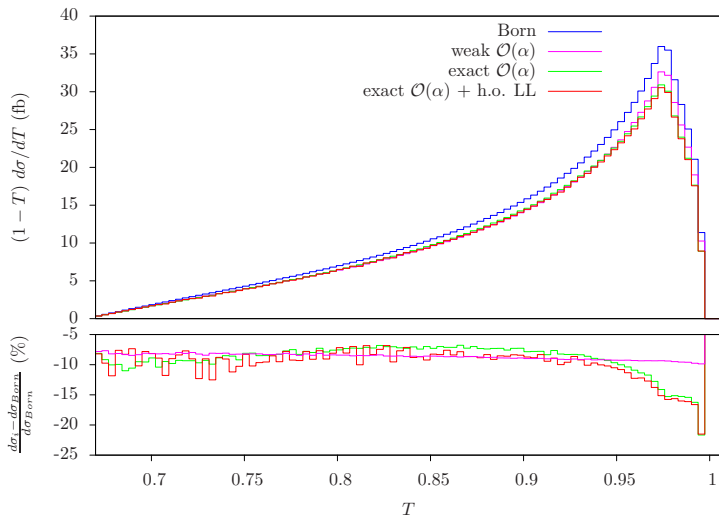


# Thrust at $Z$ peak



$$T = \max \frac{\sum_i |\vec{p}_i \cdot \vec{n}_T|}{\sum_i |\vec{p}_i|}$$

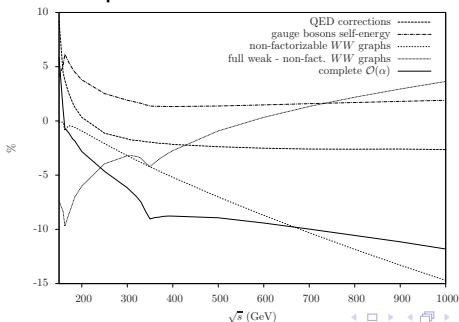
# Thrust at $\sqrt{s} = 1$ TeV



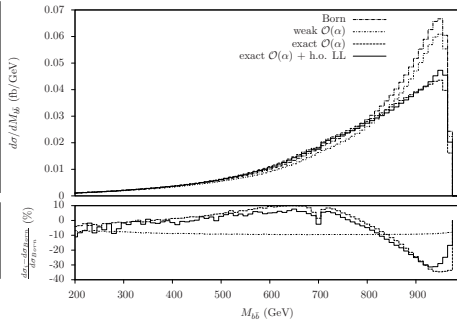
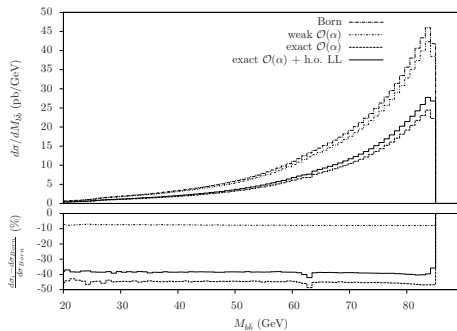


$$e^+e^- \rightarrow b\bar{b}g$$

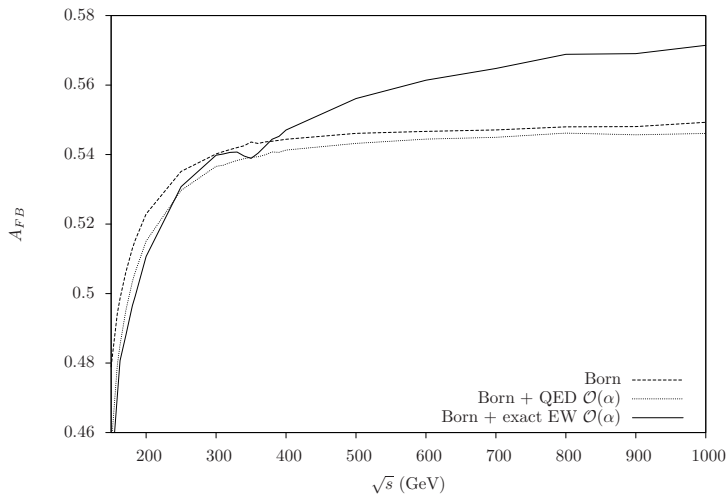
- thanks to  $b$ -flavour tagging techniques, quark and gluons can be distinguished, e.g. allowing for:
  1. verifying flavour independence of  $\alpha_S$
  2. studying the properties of the gluon
  3. measuring the  $b$  mass
- all of them can be studied in  $e^+e^- \rightarrow b\bar{b}g$   
(for the sake of simplicity we assume 100%  $b$ -tag efficiency)
- Energy scan for  $b\bar{b}$  sample



# $b\bar{b}$ invariant mass at the $Z$ peak and 1 TeV



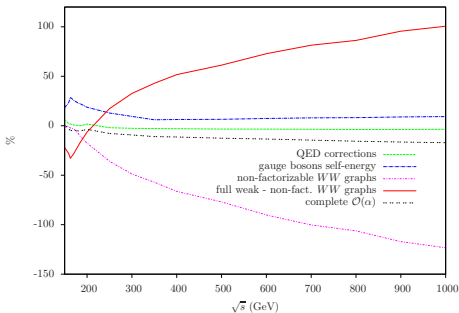
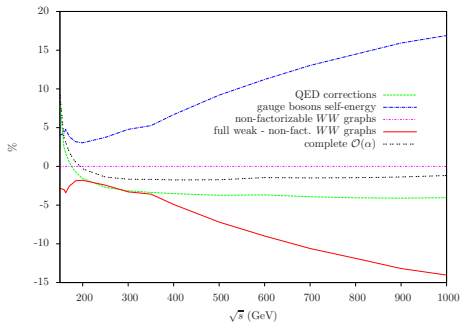
# Forward-Backward asymmetry



$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

# Polarised beams

- Polarisation is a search-ground for anomalous contribution to asymmetries
- EW corrections affect in a different way left- and right-polarised beams
- e.g. EW corrections for  $e_R^-$  and  $e_L^-$  (assuming 100% polarisation)

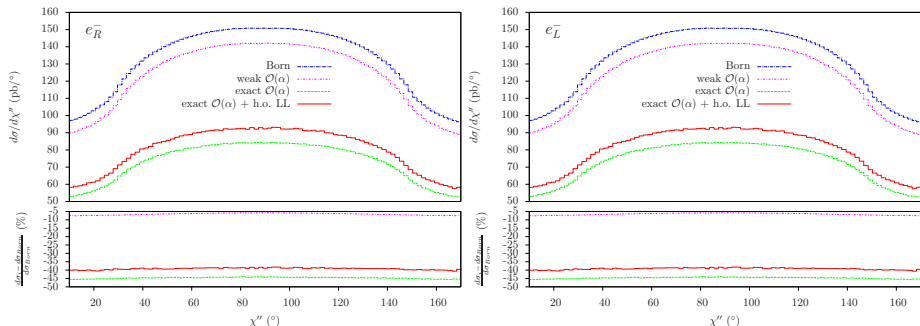


# EW corrections on azimuthal angle

- Energy-ordered jets:  $E_1 > E_2 > E_3$

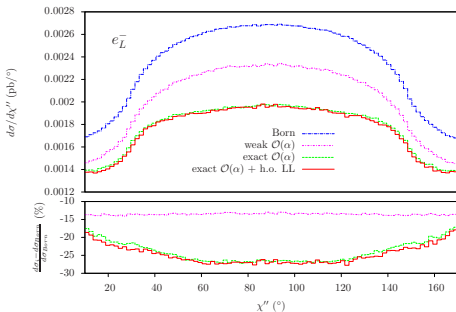
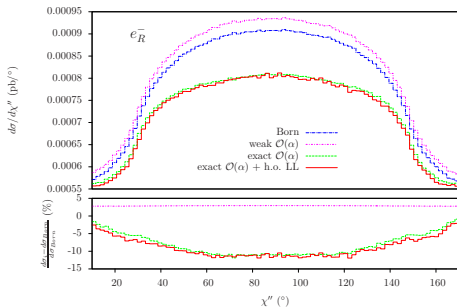
$$\cos \chi'' = \frac{\vec{1} \times \vec{3}}{|\vec{1} \times \vec{3}|} \cdot \frac{\vec{1} \times \vec{e}^-}{|\vec{1} \times \vec{e}^-|}$$

- at peak (70% polarization)



# EW corrections on azimuthal angle

- at 1 TeV (100% polarization)



# Conclusions

- ★ the complete one-loop EW corrections to  $e^+e^- \rightarrow 3$  jets have been calculated
  - each contribution calculated independently twice
  - good agreement between different implementations
- ★ the effects of EW RC are important for future precision studies at ILC (e.g.  $\alpha_s$  determination), test of SM and BSM searches
- ★ the phenomenology of EW RC is even richer in presence of polarised beams, unlike QCD RC
- ★ work in progress:
  - crossing the process to study EW RC to  $Z$ +jet at hadron colliders

# Preliminary: $p_{\perp}^{jet}$ at LHC in $Z+jet$

